

# NUISANCE

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# Luke Pickering

NuSTEC board meeting 2019







# Who are we?

- T2K, MINERvA, DUNE collaborators
- A breadth of experience using GENIE, NuWro, NEUT, GiBUU
- Have worked on neutrino cross-sections measurements, generators dev. and oscillation analyses on T2K and DUNE
- Stared at, thought about, and discussed a lot of neutrino interaction measurements (at NuSTEC and elsewhere)
- Developed interaction systematics for T2K and DUNE analyses
- Started as PhD project, now junior postdocs

#### L. Pickering MICHIGAN STATE







C. Wilkinson  $u^{^{b}}$ 





#### This Talk

- What is NUISANCE?
- What have we done with NUISANCE?
- What do we plan to do with NUISANCE?
- How can NUISANCE be used in conjunction with NuSTEC?



#### What a NUISANCE

- Converts generator output from GENIE, NuWro, NEUT, GiBUU and NUANCE
- Uses a common event format with common functions (e.g. GetLepton(), GetQ2(),
   GetFinalState())

With all generators in the same format, it's easy to produce

- Generator-to-generator comparisons
- Model to model comparisons
- Comparison to data
- If event reweighting is available (GENIE, NEUT, NuWro):
  - Fit parameters to data
  - Evaluate uncertainty bands against data
  - Evaluate uncertainties against each other

JINST 12 (2017) no. 01, P01016

#### What a NUISANCE

Compare effect of systematics on distributions from the same generator



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Compare different generators and their models in a "flat-tree" format



Compare your favourite generators and models, which does best/worst?



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#### Tutorials, how-to's

- Hosted tutorials at FNAL, J-PARC, NuSTEC, NuInt, and to interested experiments at collaboration meetings (MINERvA, MicroBooNE, T2K)
- <u>https://nuisance.hepforge.org/nuisancetalks.html</u>,
   <u>https://nuisance.hepforge.org/tutorials/general.html</u> and
   <u>https://nuisance.hepforge.org/trac/wiki</u> contains information on how to **run generators**,
   how to **run NUISANCE**, how to **include new data**, and so on
- Users range from Master's students to senior lecturers, accessibility was key goal

Example

able chamber data in NUISANCE

Autumn 2017

• Code is **open source** so analyses can be reproduced and extended





31/08/17

MINERvA school, Summer 2017 <sup>1</sup>/<sub>200</sub> <sup>1</sup>/<sub>400</sub> <sup>600</sup>/<sub>p<sub>n</sub></sub>(MeV)</sub>

Generate NuWro ANI events and compare them to CC1ni+1n pion momentur

ANL 1Dopi Data

NuWro (30.5/14)



Oprah, Summer, 2004

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#### Who are we working with?



# **Some Example Comparisons**

- Bubble Chamber lepton variables
- Nuclear-target CC0 $\pi$  lepton variables
- Nuclear-target CCO $\pi$  lepton-hadron correlation variables
- (more than 300 measurements in NUISANCE)



#### **Meet the Generators**

					,	
	Version/ Tune Used	Nuclear-mod el + QE-like	Single Pion Production	Higher W	Fragmentation	FSI
NEUT	5.4.0	Valencia: - 1p1h+RPA - 2p2h	Rein-Sehgal + lepton mass effects	Bodek-Yang Iow Q <sup>2</sup>	Pythia 5	Tuned Salcedo-Oset cascade
GENIE	v3.0.4 G1810a_0211 + bug-fixed splines	Valencia: - 1p1h+RPA - 2p2h	Rein-Sehgal 16 resonances non-interferin g (BC Tuned)	Bodek-Yang Iow Q <sup>2</sup>	AGKY+Pythia 6	Tuned effective single interaction (hA)
NuWRO	v19.02	- Benhar SF w/ opt. pot. - Valencia: RPA & 2p2h	Delta + Pythia Low W	Bodek-Yang Iow Q <sup>2</sup>	Pythia 6	Tuned Salcedo-Oset cascade



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#### **Comparisons to Bubble Chamber data**

- (quasi-)free of any nuclear effects.
  - Granular reconstruction and unambiguous final state topologies.
  - Allows tuning of 'primary' neutrino nucleon/part interaction.
- Data is old with large statistical errors and often unknown systematic errors (largely flux).





## Nuclear data: MiniBooNE CCQE

- Data sets without published, correlated errors are difficult to use in a global fit.
- MiniBooNE CCQE(like):
  - Many bins, no published error matrix. Ο MiniBooNE, PRD 81 092005 (2010), vuCCQE-Like NuWro 19.02 GOF **GENIE 3.0.4 NEUT 5.4.0** 0.2<cos(0,)<0.3 0.3<cos(0,)<0.4 0.4<cos(0,)<0.5 20 20 20



 $\chi^2_{
m min}/N_{
m DOF}$ 

117.9/228

30.3/13

65.7/21269.1/142

46.1/83

117.9/228

117.9/228





#### MINERvA Opi neutrino-mode

Sensitive to neutrino energy ( $p_{II}$ ) and momentum transfer ( $p_t$ ) in a known flux



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#### Transverse missing momentum

- Signal phase space cuts chosen for detector capabilities:
  - Results in less model-dependent efficiency Ο correction.
  - T2K: 0
    - 500 MeV < p<sub>p</sub>
    - 250 MeV < p<sub>\_</sub>, 1 < cos(θ<sub>\_</sub>) < -0.6
  - MINERVA: Ο
    - 450 <  $p_p$  < 1200 MeV, 0 <  $\theta_p$  < 70° 1.5 <  $p_\mu$  < 10 GeV, 0 <  $\theta_\mu$  < 20°



#### **MINERvA CCInclusive: Low recoil**

 Inclusive models described by q0/q3:

0

- Requires model-dependent reconstruction of EAvail and true momentum transfer.
- GOF is awful for all available models:
  - Inconclusive when comparing one bad fit to another bad fit.





#### **Comparisons to Nuclear data: MicroBooNE**

c/A ×10<sup>39</sup>

GeV<sup>-1</sup>

cm<sup>2</sup>

do/d/

-1<cos(0.)<-0.5

0.27<cos(0,)<0.45

0.76<cos(0\_)<0.86

1.5

- Need to understand neutrino interactions on Ar40 target.
- Data release:
   Reconstructed distributions
   True→reco folding matrix
- Potentially useful technique to reduce model bias in published data.

MicroBooNE, arXiv:1905.09694,  $\nu_{\mu}$ CCInc - NuWro 19.02,  $\chi^2$ =73/37 bins - GENIE 3.0.4,  $\chi^2$ =84/37 bins NEUT 5.4.0,  $\chi^2$ =87/37 bins



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#### What have we done so far?

- Uncertainties on interaction systematics T2K oscillation analysis from external data and comparisons to other generators (see T2K oscillation papers)
- Evaluating goodness of new NEUT models for T2K analyses choices (PRD93, 072010)
- Pittsburgh Tensions cross-experiment cross-generator workshops, evaluating generator vs generator vs data (Physics Reports 773–774)
- MINERvA-NOvA workshop: comparing MINERvA fit (MnvGENIE) to NOvA fit and data
- NOvA-T2K workshop: comparing models and uncertainty bands,
   Find overlap in treatment of systematics
- T2K, MINERvA publications for multi-generator predictions
- MINERvA pion tuning paper (PRD 100, 072005)
- Discussions about the future of data releases, e.g. NuInt, NuSTEC

#### Shared goals with NuSTEC and NuInt



#### What do we want to do?

- Large survey of the current generators, publish in some reference journal
  - Hopefully happening this winter/spring
- Continue providing community with ad-hoc tunes
  - <u>Does not</u> replace good solid theory! We're accounting for uncertainties, not trying to build a wholesome model
- Formalise suggestions for future data releases in high statistics era
- Expand NUISANCE to have representatives on each experiment?
- Neutrino experiments often have their own tune: compare and discuss these
  - e.g. MINERvA, T2K, NOvA, MicroBooNE tunes
- Produce a container with all generators and tools pre-installed for easy use
  - Prepared for recent T2K-NOvA workshop, largely successful
- Expand electron scattering interface
- Support pion and nucleon scattering

#### Shared goals with NuSTEC and NuInt

#### Summary

- NUISANCE is a tool for generator--data comparisons
  - Contains a large number of datasets and associated signal definitions for you to use.
  - Has tools for performing 'global' cross-section comparisons and tunes.
  - But: You have to be aware of the details of the data you comparing to!
- We've worked with experiments and generators on making predictions, evaluating models, producing ad-hoc tunes
- Many goals shared with NuSTEC and NuInt
- If any of this sounds interesting, **get in touch**, plenty of work and development that can be done by people with a range of experiences!



# **Thanks for listening**

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# THERE IS ALWAYS HOPE

(NuFACT2018, VT, Blacksburg)



- Minimize model bias while maximising efficacy of data:
  - Well-understood selection efficiency over signal phase space.
  - Projections the require minimal MC correction.
- Publish errors with bin-to-bin correlations.





## Why NUISANCE might be right for you

- Consistently comparing your model predictions to many data-sets.
- Producing comparisons to your new data set with a variety of MCs --without having to be an expert.
- Ensure that comparisons to your data are done correctly.
- Tools make cross-section parameter fitting mechanically simple:
  - But, garbage in  $\rightarrow$  garbage out.
  - Choice of data, choice of parameters, structure of fit is the tough bit.





# Data Comparison: $\delta p_{T}$

- T2K: 1802.05078
- MINERvA: 1805.05486
- (GENIE norm may not be quite right to a few %, its fine for here, but probably not best to show these plots as is elsewhere)



https://doi.org/10.1016/j.physrep.2018.08.003

 $\nu_{\mu}$  Flux (arbitrary norm.)

MiniBooNE/SBN

T2K: ND off-axis

MINER $\nu$ A L.E

NuWro v11q,  $\sigma_{\nu,C}(E_{\nu})$ 

CC-SPP

CCQE

CC-Total

....

 $\tau_{\nu_{\mu}C} (10^{-38} \text{cm}^2 \text{nucleon})$ 

# Signal definitions

- T2K: 1802.05078
- MINERvA: 1805.05486
- (GENIE norm may not be quite right to a few %, its fine for here, but probably not best to show these plots as is elsewhere)

500 MeV < pp 250 MeV < pmu, 1 < cos(theta\_mu) < -0.6



#### 450 < pp < 1200 MeV, 0 < theta\_p < 70° 1.5 < pmu < 10 GeV, 0 < theta\_mu < 20°







## More pn

- Also wanted to look at stuck pi vs. 2p2h
  - GiBUU predicts no second peak for QEL, but NEUT does.
- And FSI/Nuclear momentum/binding model changes:
  - LFG/SF in NEUT qualitatively similar, contrary to NuWro
  - FSI mostly interacts with signal selections





### MINERvA 1pi neutrino-mode

- For the charged pion analyses:
  - ~100% efficiency correction at high angle.
  - Where is this 'MC fill-in' in other distributions?
- Upcoming re-analysis still no phase space cuts.
- No covariance between distributions (pµ, θµ, Tπ, θπ, Q<sup>2</sup>) or samples (π+, π0, υ, υ):
  - Difficult to consistently use together in a meta-analysis.



#### MiniBooNE 1Pi+

- Rejection only in selection, not signal definition:
  - Will be efficiency corrected back with NUANCE-calculated efficiency.
  - Better to include analysis cuts in both signal and selection where possible, then handle new out-of-phase space backgrounds, but smaller, less model dependent efficiency corrections.





#### **MINERvA: Initial state neutron momentum**

 Momentum imbalance in all three dimensions is sensitive to initial state fermi nucleon momentum distribution.
 GOF is poor for all models.





#### **Notable Recent Developments**

#### • NEUT:

- Nieves 1p1h, LFG nuclear model
- Improved multi-pion production from BC tune
- MK pion production, Bug fixes in R-S pion production

#### **Notable Recent Developments**

Phys. Rev. C 100, 015505 (2019)



• Integration of electron scattering simulation.



#### **Notable Recent Developments**

Phys. Rev. C 100, 015505 (2019)



#### **Transverse missing momentum**

• MINERvA error matrix provides a tight shape constraint around the peak which drives the high GOF.



MINERVA: PRL 121 (2018)



#### **Transverse missing momentum**

- MINERvA error matrix provides a tight shape constraint around the peak which drives the high GOF.
- Equivalent matrix for the T2K result exhibits anti-correlations between neighbouring bins:
  - More expected for uncertainties that cause bin migrations.



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#### **Gen Summary**

- The loftiest goals of neutrino oscillation physics depend on the accuracy of event generator predictions and associated uncertainties.
- Recent u<sub>µ</sub>→0π data releases have been more statistically robust, but GOF between available models is generally poor
  - Room for improvement in generator predictions, xsec analyses and data releases and global fitting methodology.
  - Correct, correlated errors are a comparators best friend!
- More recent work on removing assumptions in generator factorization and implementing state-of-the-art predictions is promising!



#### Why do we need good interaction Models?

- The aim is to perform measurements of neutrino oscillations.
  - Oscillation occurs as a function of true neutrino energy, which is **not observable**.
- We use models to estimate:  $D(\mathbf{x}_{obs}|\mathbf{x}_{true})$ : *If we see*  $\mathbf{x}_{obs'}$  *what was the true neutrino energy?* We need to understand:
  - Selected backgrounds
  - Selection efficiency
  - Exclusive channel interaction rates and kinematics
- Wrong model  $\rightarrow$  wrong inferred  $P_{osc}(E_{\nu})$ .

$$N_{\text{near}}(\mathbf{x}_{\text{obs}}) = \int d\mathbf{x}_{\text{true}} \underbrace{\mathbf{D}_{\text{near}}(\mathbf{x}_{\text{obs}} | \mathbf{x}_{\text{true}})}_{\text{Smearing, Eff., Pur.}} \underbrace{N_{\text{targ}}\sigma(\mathbf{x}_{\text{true}})\Phi(E_{\nu})}_{N_{\text{Int}}(\mathbf{x}_{\text{true}})}$$

$$N_{\text{far}}\left(\mathbf{x}_{\text{obs}}\right) = \int d\mathbf{x}_{\text{true}} \underbrace{\mathbf{D}_{\text{far}}\left(\mathbf{x}_{\text{obs}} | \mathbf{x}_{\text{true}}\right)}_{\text{Smearing, Eff., Pur.}} \underbrace{N_{\text{targ}}\sigma\left(\mathbf{x}_{\text{true}}\right)\Phi\left(E_{\nu}\right)P_{osc}\left(E_{\nu}\right)}_{N_{\text{Int}}\left(\mathbf{x}_{\text{true}}\right)}$$

#### What is a Neutrino Event Generator

- Selects neutrino 'events' from interaction models:
  - Over a range of neutrino energy and species,
  - For a number of 'primary' channels:
    - Neutrino--nucleus (COHPi, CvNS)
    - Neutrino--multi-nucleon (2p2h)
    - Neutrino--nucleon (QE, RESPi)
    - Neutrino--parton (DIS)
  - In a nuclear environment:
    - Fermi motion distribution
    - Removal energy
    - Collective effects (RPA)
    - Final state re-interactions of primary particles
- Often factorises the simulation of nuclear model, primary interaction, and FSIs.



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#### MINERvA Opi anti-neutrino-mode

- χ-by-eye GOF seems ≤ vorse (to me) than calculated GOF.
- Possibly because of PPP:
  - Smaller MC normalization can give 'artificially' low  $\chi^2$  if uncertainty is not fully characterized.
- Need to be wary of PPP when fitting.



#### MINERvA 1pi neutrino-mode

- MINERvA have released a number of pion datasets, each with multiple projections
  - Lots of information, much more than shown here.
  - Fairly poorly predicted all around.
- arXiv:1903.01558: discusses some of the difficulties seen fitting these data.



#### **Gen Future: 1**

- Last few years seen increase in sophistication of Opi analyses
  - Lepton/hadron correlations
  - Less Model-dependent selections and projections
  - Would be very useful to see similar renaissance in pion production datasets.
- Future MicroBooNE (and SBND) data sets will be critical for model builders to benchmark and develop before DUNE and Fermilab Short Baseline program.

#### Gen Future: 2

- These last two years have seen an uptick in model development:
  - GENIE tuning, v3, NEUT and NuWro model developments, ECT\* Trento workshops
  - Lots of progress due to closer interaction with theory community, need to continue!
- But given how much LBL programs will rely on the predictions and uncertainties, the community is quite under person-powered...
   Plenty of room for important work and novel intellectual contribution
- Can learn a lot of the necessary nuclear physics from electron scattering: GENIE + NuWro have e-A modes, ongoing work by e4nu.
- See what GiBUU has to say for itself...



(b) Thisanalysis

# The data is the data is the data

- Sometimes the data is not the data is not the data.
- ANL/BNL CC1pi+1proton discrepancy: ۲
  - Data biased by problems in the neutrino flux models 0
  - ~ Reconciled by re-analysis. 0
  - But, no correction for Q2 distribution! 0
- Need to be familiar with included data sets and tensions between them.
  - May need to assign confidence weights to samples in Ο the global GOF.









## Hidden Model Biases 1

- Un-smearing and efficiency corrections introduce bias.
- From a fitters point of view, it is better to cut out regions of very poor efficiency:
  - Don't want to compare to model-of-the-day contaminated 'data'.
- Very helpful that such plots are in the publication!
- *N.B.* These problems are tricky and ubiquitous, not specifically calling out this publication.



#### Hidden Model Biases 2: Stealth mode



- It isn't always so clear: e.g. ND280 CCIncl
  - Practically cannot measure  $\cos(\theta\mu) < 0$ .
  - But, publish total cross-section.
- Similar out-of-acceptance corrections in many recent measurements: *Fiducial* cross-sections are much preferred!



## **Experimental Signal Definitions**

- Not always fully clear from the publication:
  - Getting this correct is essential for interpreting the data.
- e.g. MiniBooNE CCQE C12 data, subtracts:
  - Wrong-sign background CH2.08 component
  - H2.08 component
  - non-QE component (PDD)
  - o Mis-ID'd π-
- All predicted by NUANCE...
- But, the background subtractions are provided:
  - Might be better to produce H and v-C12 predictions and compare to the less-corrected data.



## MiniBooNE CCQE-Like

- Not possible to calculate useful GOF, so I'm not going to attempt to...
- The data here is the 'less corrected' CCQE-like data:
  - No pionless delta decay subtraction (subset of MEC diagrams).



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#### Data In NUISANCE

#### **Bubble Chamber:**

ANL: 7 selections, 56 projections
BEBC: 6 sel. nu+nubar, 11 proj.
BNL: 4 sel., 15 proj.
FNAL: 3 sel., nu+nubar, 5 proj.
Gargamelle: 1 sel., 1 proj.

#### Nuclear:

**C:** 

```
MINERvA: 3 sel., 6 proj.
```

#### CH:

**T2K:** 9 sel. 24 proj.

MINERvA: 10 sel., nu+nubar, 106 proj.Electron Scattering:SciBooNE: 1 sel. 16 proj.Virginia QE Arc

CH<sub>2</sub>:

```
MiniBooNE: 5 sel., 33 proj.
```

#### Nuclear: H,0: **K2K:** 1 sel., 1 proj. T2K: 1 sel. 7proj. Ar: ArgoNeuT: 3 sel., nu+nubar, 12 proj. MicroBooNE: 1 sel. 1 proj. Fe: MINERvA: 3 sel., 6 proj. Pb: MINERvA: 3 sel., 6 proj. Virginia QE Archive

#### How do we try and improve them: Theory

- Improve nuclear response models in generators:
  - e.g. SuSAv2 lplh+2ph2 PRD 94, 093004
     (2016)
- Improve primary interaction models in generators:
  - e.g. MK single pion production PRD 97, 013002 (2018)
- Improve simplifications in the MC:
  - Un-doing factorisation
  - Better-capture:
    - initial and final state physics
    - lepton-hadron correlations.



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#### What about uncertainties?

- Need plausible variations of models that can 'cover' the extant data.
- Compare to historic data ⇒ well-motivated prediction and uncertainties:
  - Then assume model is predictive for new data
- If experimentalists don't have the ability to vary 'theory' parameters:
  - Have to make something up...





 Ideal world: model describes nature up to some unknown parameter values.



- Ideal world: model describes nature up to some unknown parameter values:
  - We don't live in that world.



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  - We don't live in that world.

#### Dangers of tuning:

- Absorb data/MC discrepancy into poor parameterization.
- Propagate CV+uncerts from well-described projection to poorly described projection.
- *e.g.* Tune in inclusive lepton variables and predict hadronic shower.



 $\sigma_{\nu_{\mu}C} \; (10^{-38} {\rm cm^2 nucleon^{-1}})$ NuWro v11q,  $\sigma_{\nu_{\mu}C}(E_{\nu})$ Range of:  $\nu_{\mu}$  Flux (arbitrary norm.) ----- CC-Total MiniBooNE/SBN ····· CC-SPP T2K: ND off-axis - CCOE MINER<sub>2</sub>A L E Ο Neutrino energies 3













- Range of:
  - Neutrino energies
  - Targets
  - Final state topologies
  - Observable projections
- Sensitivity to:
  - Model choice
  - Free parameter central values
  - / Free parameter uncertainties

Plots: arXiv:1810.06043





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 $_{\mu C} (10^{-38} {\rm cm}^2)$ 

Plots: arXiv:1810.06043

- Range of:
  - Neutrino energies Ο
  - Ο Targets
  - Final state topologies Ο
  - Observable projections 0
- Sensitivity to:
  - Model choice 0
  - Free parameter central values Ο
  - Free parameter uncertainties 0
- Ability to make quantitative statements about GOF



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#### Anatomy of a Cross-section Fit



- Cross-section tune recipe:
  - Add all the data you can find

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  - Serve for updated interaction model and correlated uncertainties!



- Cross-section tune recipe:
  - Add all the data you can find
  - Stir free parameters until mixture is golden brown
  - Serve for updated interaction model and correlated uncertainties!
- But... have to take care:
  - Model parameterizations can be hard to uniquely constrain.
  - Hard to consistently evaluate test statistics.
  - Incomplete data coverage:
    - e.g. Many measurements focus on just charged lepton kinematics.
    - Need to be predictive in hadron kinematics...
  - Signal definitions not always clear/well defined in the context of an experiment.
- These are problems that the community is working on together: we know things now that we didn't before, but it is still worth highlighting specifics in historic data to be aware of.



- Minimize model bias while maximising efficacy of data:
  - Well-understood selection efficiency over signal phase space.
  - Projections the require minimal MC correction.
- Publish errors with bin-to-bin correlations.





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- Minimize model bias while maximising efficacy of data:
  - Well-understood selection efficiency over signal phase space.
  - Projections the require minimal MC correction.
- Publish errors with bin-to-bin correlations.
  - Wherever possible:
    - Between projections
    - Between datasets.





## Nuclear data: MiniBooNE CCQE

- Data sets without published correlated errors are difficult to use in a global fit.
- MiniBooNE CCQE(like):
  - Many bins, no published error matrix.
  - $\circ$   $\;$  What should the contribution to the global GOF be
    - Fully uncorrelated:  $\sim \sum_{i \in \text{bins}} (\text{Data}-\text{MC})_i^2$
    - Fully correlated:  $\sim \sum_{i \in \text{bins}} (\text{Data}-\text{MC})_i^2 / \text{NBins}$
  - In reality, probably somewhere in between.
  - If used naively, will incorrectly dominate a tune and more data won't help...
- But, we want to use the information that this data holds, unsatisfactory to just ignore it...







#### MINERvA Opi neutrino-mode

- Sensitive to neutrino energy (p<sub>II</sub>) and momentum transfer (p<sub>t</sub>) in a known flux
- Predicted ~well for bulk of distribution:
  - Higher angle poorly predicted



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#### Single Transverse Variables

- Recent interest in lepton-hadron correlations:
  - Can be more sensitive to certain effects than lepton-/hadron-only
  - Efficiency/smearing corrections need to be treated with more care.
- Direction/magnitude of momentum imbalance is sensitive to initial and final state effects PRD 98 032003 (2018).



