



# **(Quantum) Machine Learning for Astrophysics**

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SCD Postdoc Meeting

7 April 2020

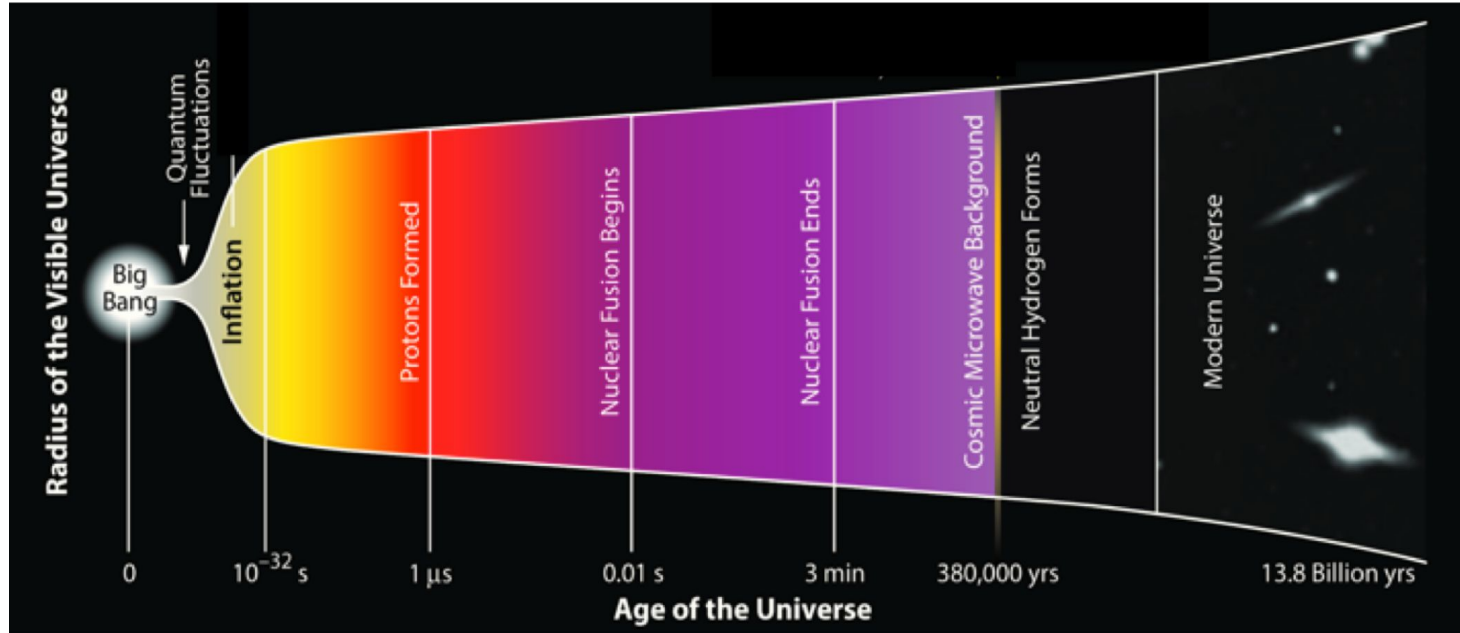
# Overview

- From before: DeepCMB (1810.01483 + 20xx.xxxxx)
- Using quantum computing for machine learning (1911.06259 + 20xx.xxxxx)
- Uncertainty quantification for deep learning (2004.xxxxx)

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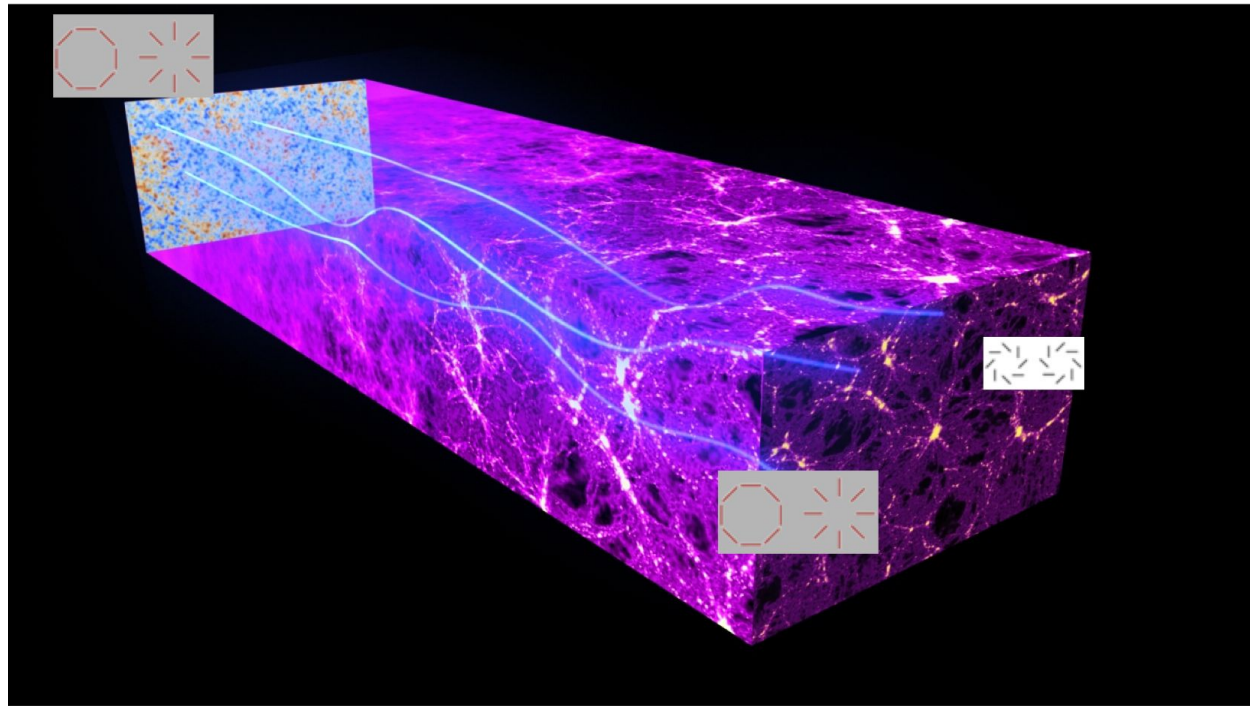
# The CMB, and lensing of the CMB



Credit: BICEP/Keck collaboration

- primordial gravitational waves
- new particles that behave like radiation in the early universe (dark radiation),  $N_{\text{eff}}$
- sum of neutrino masses

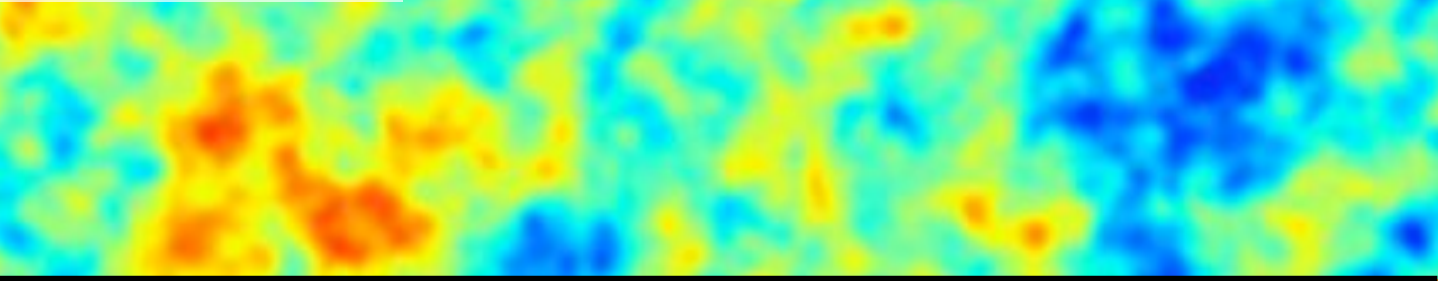
# Why CMB lensing?



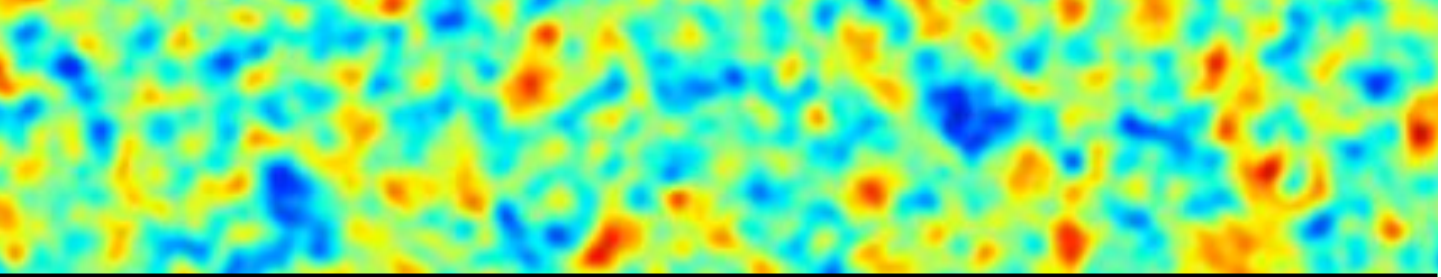
Credit: ESA

- info: provides handle on large-scale structure at low redshift
- nuisance: distorts primordial CMB  $\rightarrow$  use lensing potential to ‘undo’ the lensing (delensing)

$T(\hat{n}) (\pm 350 \mu K)$



$E(\hat{n}) (\pm 25 \mu K)$



$B(\hat{n}) (\pm 2.5 \mu K)$

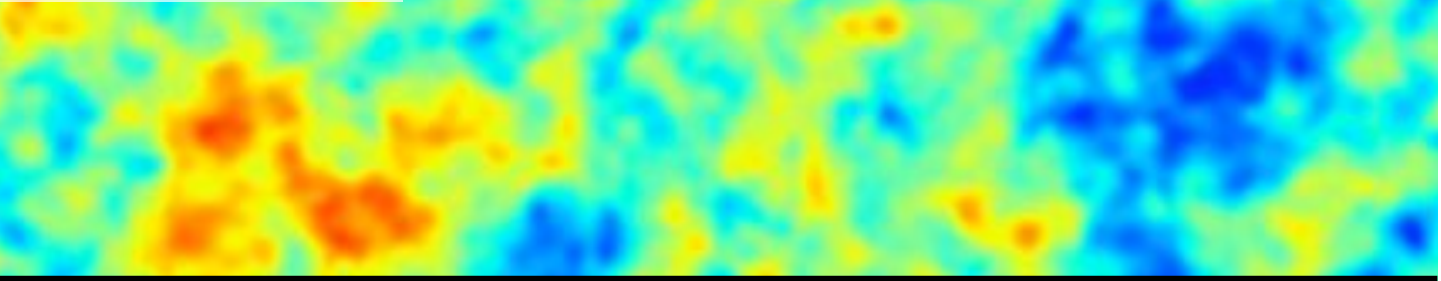


(no primordial B-modes)

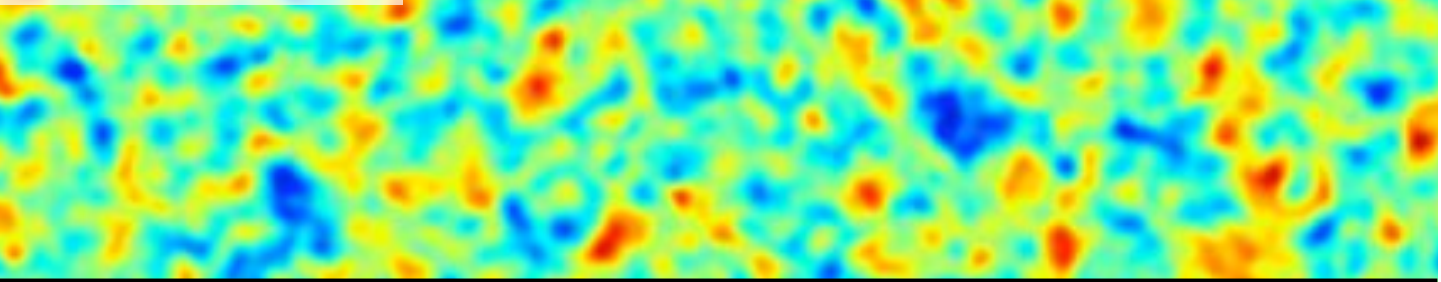
unlensed

Credit: Duncan Hanson

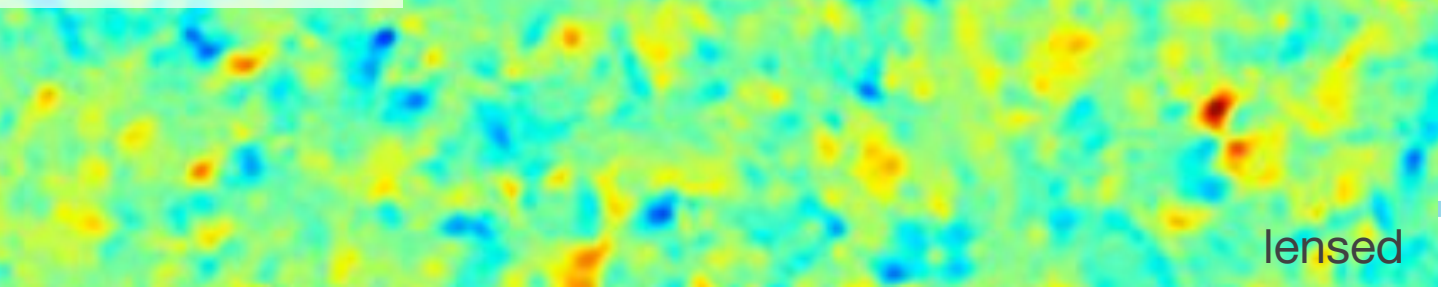
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Credit: Duncan  
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# Measuring lensing

Next-generation experiments (eg CMB-S4) will provide higher S/N CMB map measurements.

To optimally extract lensing information, we need

maximum-likelihood lensing estimators

that can deal with foregrounds, systematics, ...

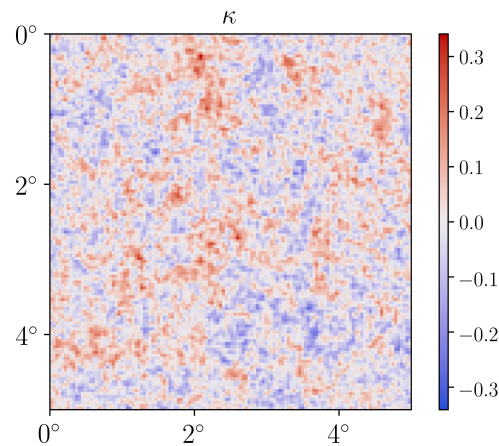
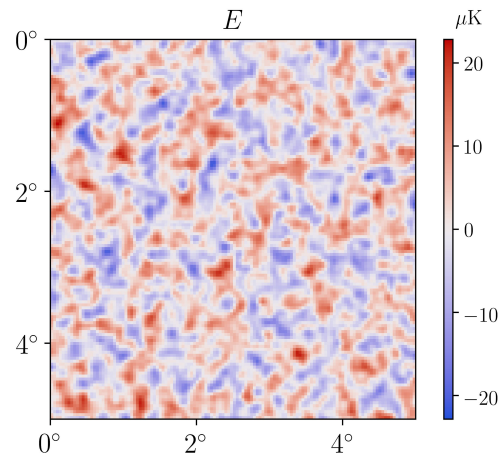
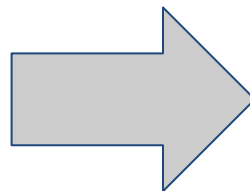
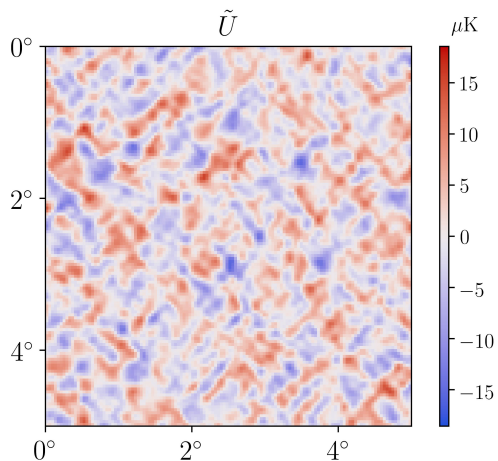
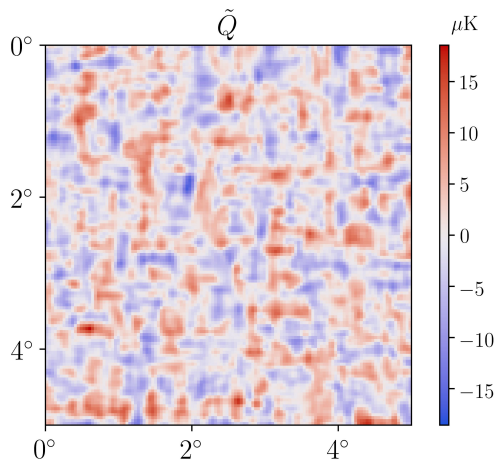


# CMB lensing reconstruction: problem statement

Left: lensed polarization maps from the CMB.

Right: unlensed map ( $E$ ) and lensing ( $\kappa$ ).

Image-to-image regression!



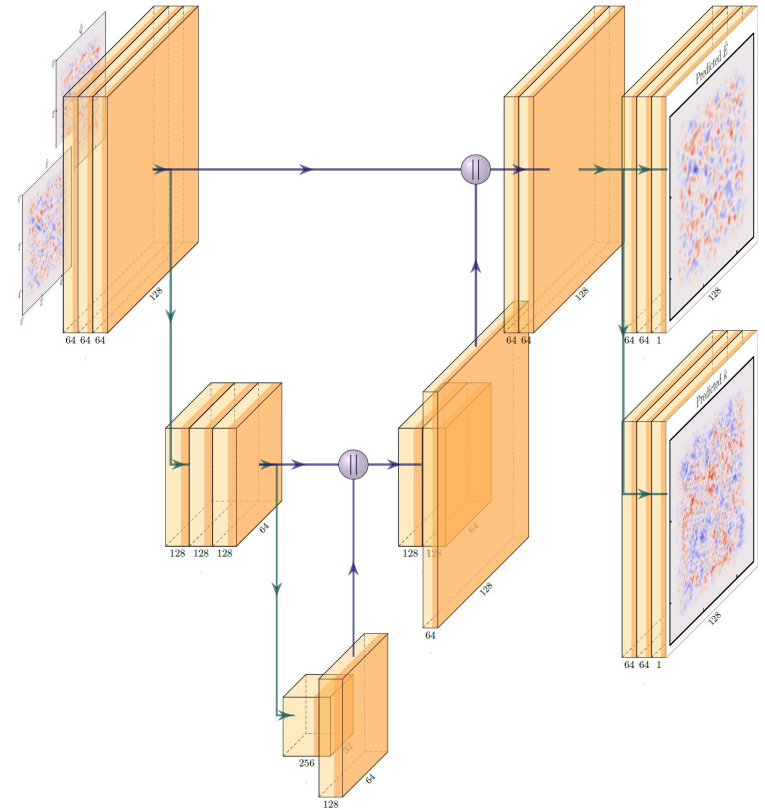
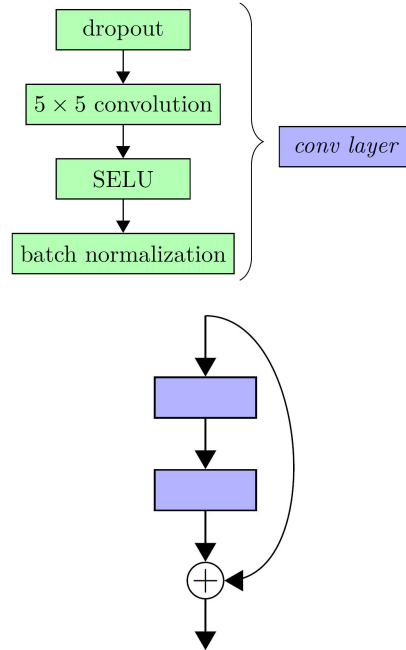
# Why neural networks?

- lots of image-based technology developed
- powerful non-linearities could be the right tool to deal with beyond-Gaussian information

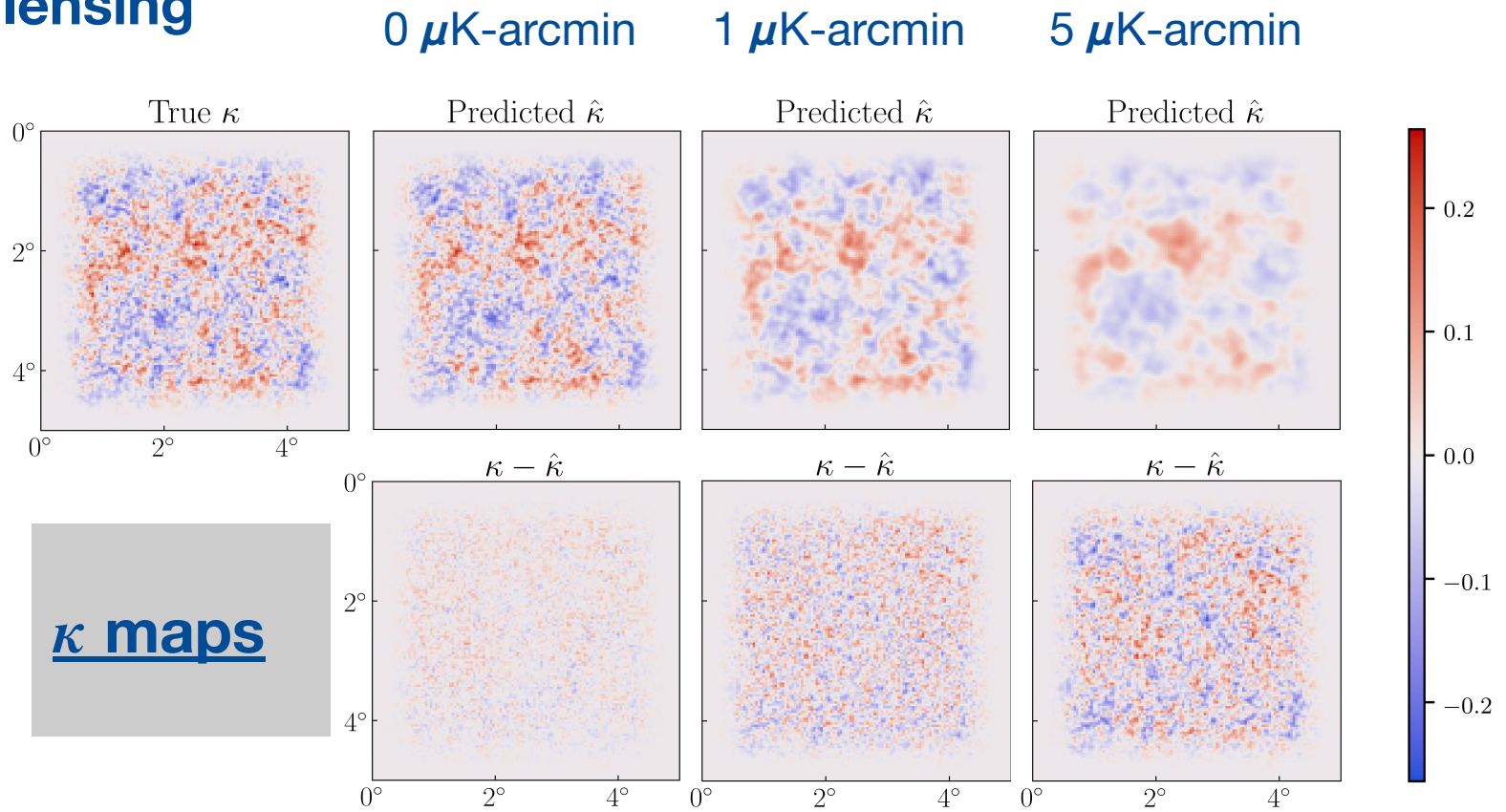
# ResUNet architecture

11200 simulated (Q, U, E,  $\kappa$ ) maps, divided 80:10:10 into training, validation and test sets.

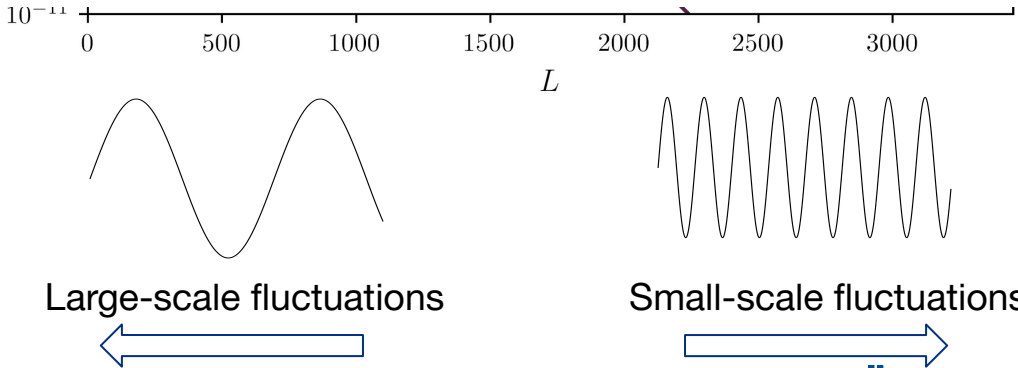
Loss function: MSE



# Results: lensing

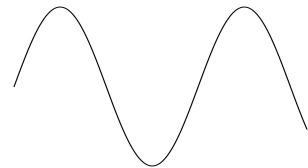
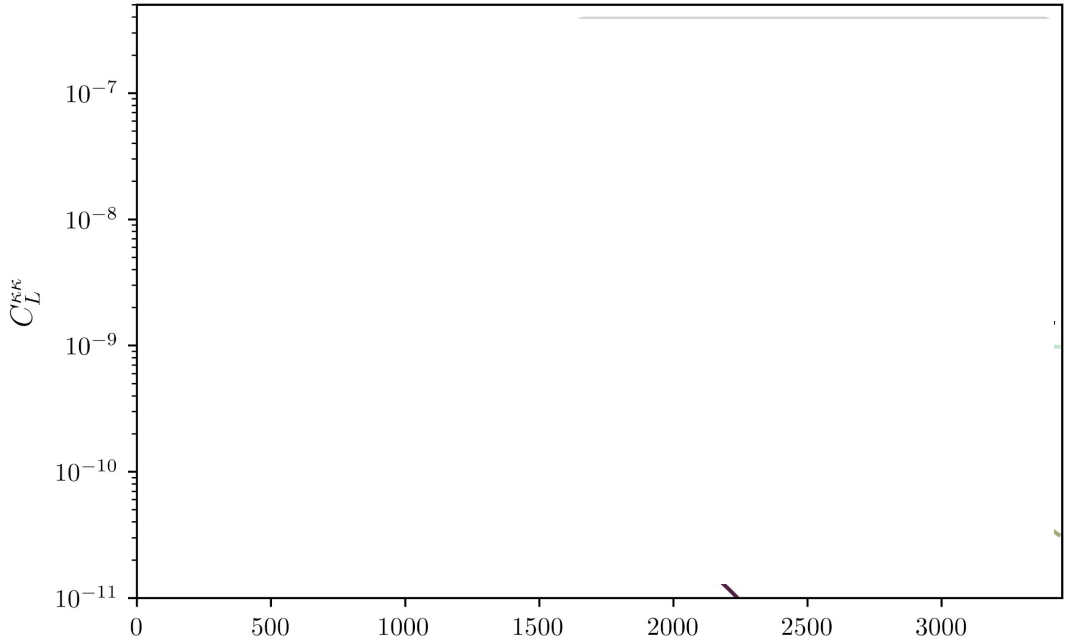


# Power spectra of $\kappa$

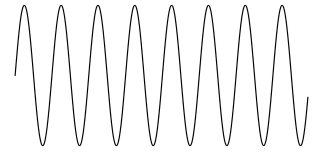


# Power spectra of $\kappa$

Intensity/power



Large-scale fluctuations

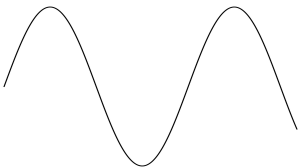
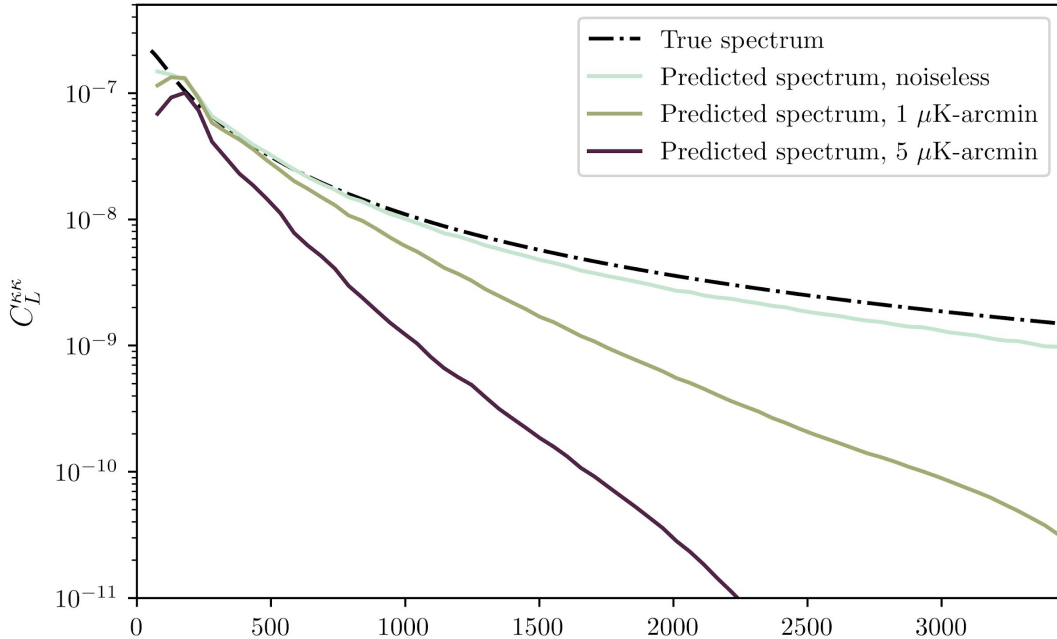


Small-scale fluctuations

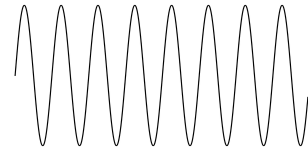


# Power spectra of $\kappa$

Intensity/power



Large-scale fluctuations



Small-scale fluctuations



# Comparison with physics-based methods

Previous methods fixed cross-spectrum to be equal, so to compare we rescale

$$\hat{\hat{\kappa}} = \frac{1}{R} \hat{\kappa} \quad R = \frac{\langle \kappa \hat{\kappa}^* \rangle}{\langle \kappa \kappa^* \rangle}$$

and then calculate the noise spectrum:

$$N_L^{\kappa\kappa} = \langle C_L^{\hat{\hat{\kappa}}\hat{\hat{\kappa}}} \rangle - \langle C_L^{\kappa\kappa} \rangle$$

$\kappa$  : true map

$\hat{\kappa}$  : predicted

$\hat{\hat{\kappa}}$  : rescaled



## Tests: different cosmologies

Q: The training, validation and test sets all have the same cosmology. Has the network just learned to reproduce that cosmology?

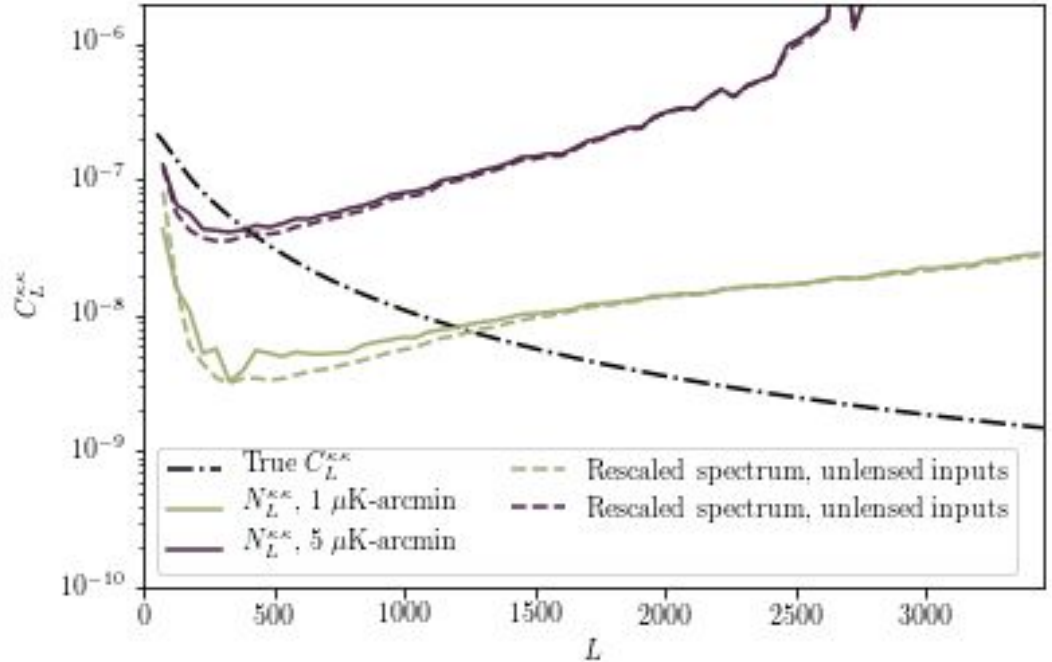
A: we have generated simulations with  $\Omega_{\text{CDM}} h^2 = 0.1085$  and  $0.1285$  ( $0.1185$  on fiducial cosmology), and ran those through the network.

We show that we can use the predicted lensing maps to estimate  $\Omega_{\text{CDM}} h^2$  after correcting for bias in the noise correction.

# Tests: no lensing

Q: What if we give the network unlensed Q and U maps? Does the network still try to reconstruct lensing?

A: No, it predicts a  $\kappa$  consistent with the noise spectrum we found.

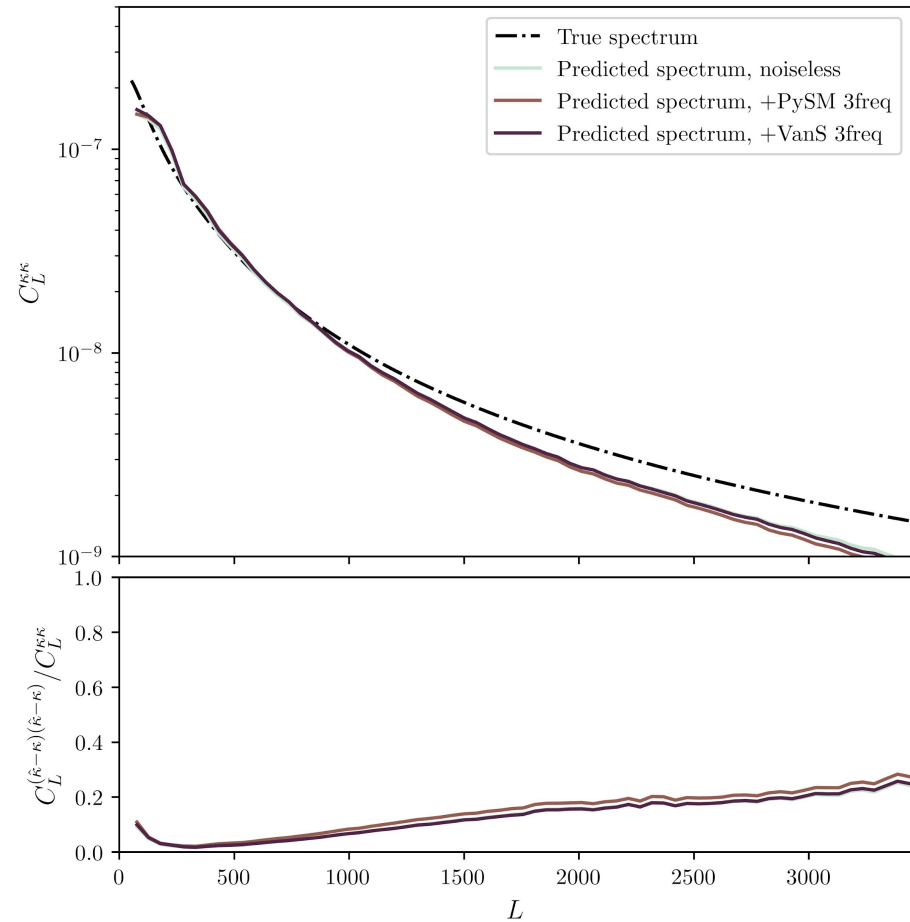


# Follow-ups: foreground removal

Inputs are now lensed (Q, U) + foregrounds at different frequencies (95, 155, 220 GHz), so six maps in total. Same outputs.

Preliminary results are promising.

Of course, only so good as the foreground model is realistic... But that's true of any method



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# We are entering the NISQ era

## Quantum Computing in the NISQ era and beyond

John Preskill

Institute for Quantum Information and Matter and Walter Burke Institute for Theoretical Physics,  
California Institute of Technology, Pasadena CA 91125, USA

30 July 2018

Noisy Intermediate-Scale Quantum (NISQ) technology will be available in the near future. Quantum computers with 50-100 qubits may be able to perform tasks which surpass the capabilities of today's classical digital computers, but noise in quantum gates will limit the size of quantum circuits that can be executed reliably. NISQ devices will be useful tools for exploring many-body quantum physics, and may have other useful applications, but the 100-qubit quantum computer will not change the world right away — we should regard it as a significant step toward the more powerful quantum technologies of the future. Quantum technologists should continue to strive for more accurate quantum gates and, eventually, fully fault-tolerant quantum computing.

# Current quantum computers

## Quantum annealers

- non-universal
- essentially draw samples from an Ising Hamiltonian

$$H = -b_i s_i - J_{ij} s_i s_j$$

- can dial couplings  $b, J$
- D-Wave 2000Q: 2048 qubits

## Gate-based

- different technologies: ion trap, superconducting systems, photonic systems...
- we're up to ~50 qubits
- universal

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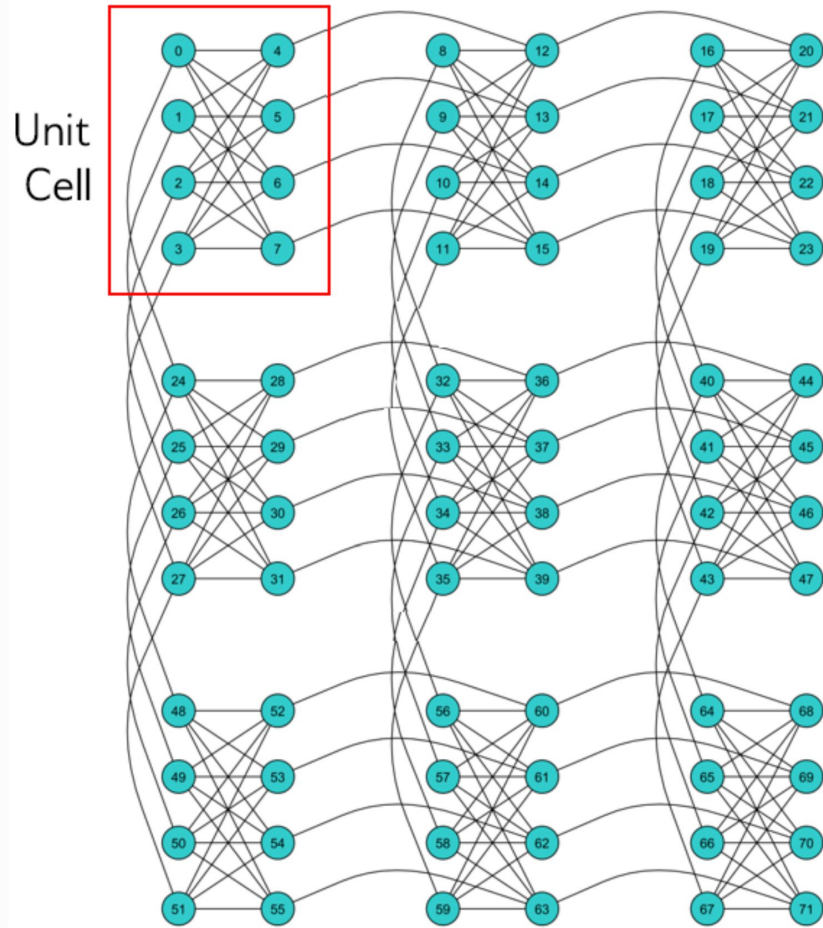
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# D-Wave (2000Q)

Chimera graph:

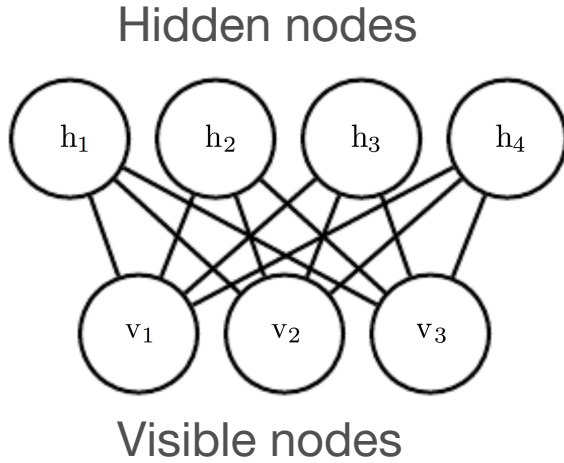


D-Wave 2000Q has  
16x16 cells: total  
2048 qubits

Need to embed  
problem graph into  
chimera graph  
(minor embedding)



# Restricted Boltzmann Machines (RBM)



Learn the probability distribution of the data (which goes into the visible nodes),

$$P(v, h) = \frac{1}{Z} e^{-E(v, h)}$$

$$E(v, h) = -b_i v_i - c_j h_j - J_{ij} v_i h_j$$

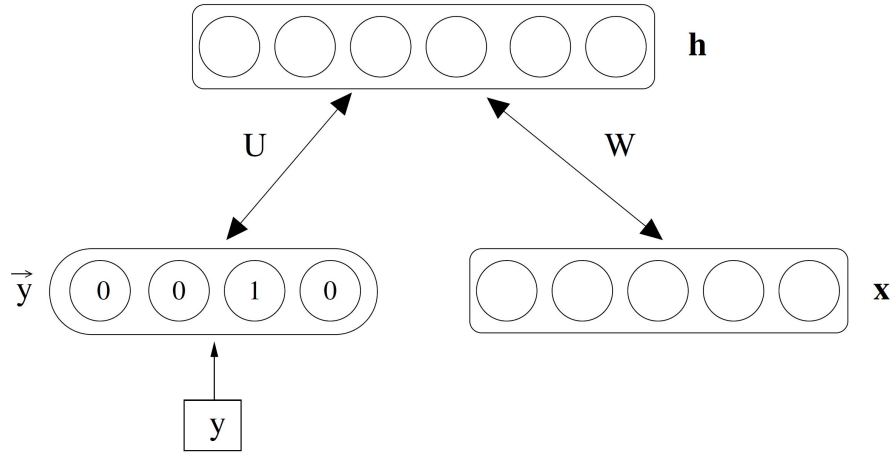
For inference, evaluate likelihood using free energy

$$\mathcal{F} = \log \sum_h e^{-E(v, h)}$$

Image credit:  
Goodfellow, Bengio  
and Courville, *Deep  
Learning*

# RBM for classification

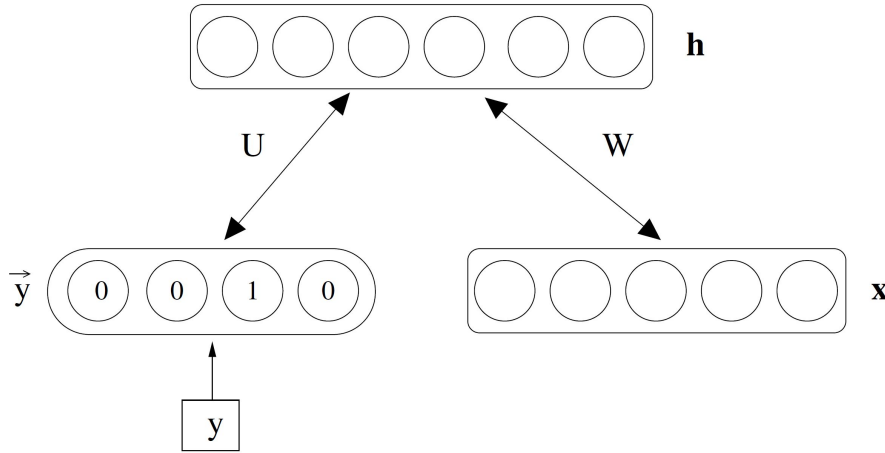
Encode label on visible nodes



For the test set, try data with all labels,  
predict the smallest free energy.

# RBM for classification

Encode label on visible nodes



For the test set, try data with all labels, predict the smallest free energy.

Training:

$$\delta w_{ij} = \langle v_i h_j \rangle_{\text{data}} - \langle v_i h_j \rangle_{\text{model}}$$

$$\delta b_i = \langle v_i \rangle_{\text{data}} - \langle v_i \rangle_{\text{model}}$$

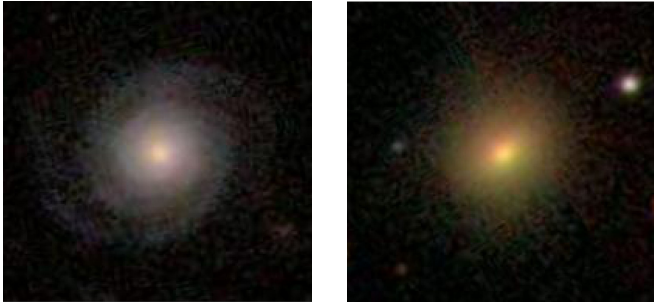
$$\delta c_j = \langle h_j \rangle_{\text{data}} - \langle h_j \rangle_{\text{model}}$$

Model expectations are hard to compute classically. Quantum advantage?

Image credit: Larochelle and Bengio (2008)

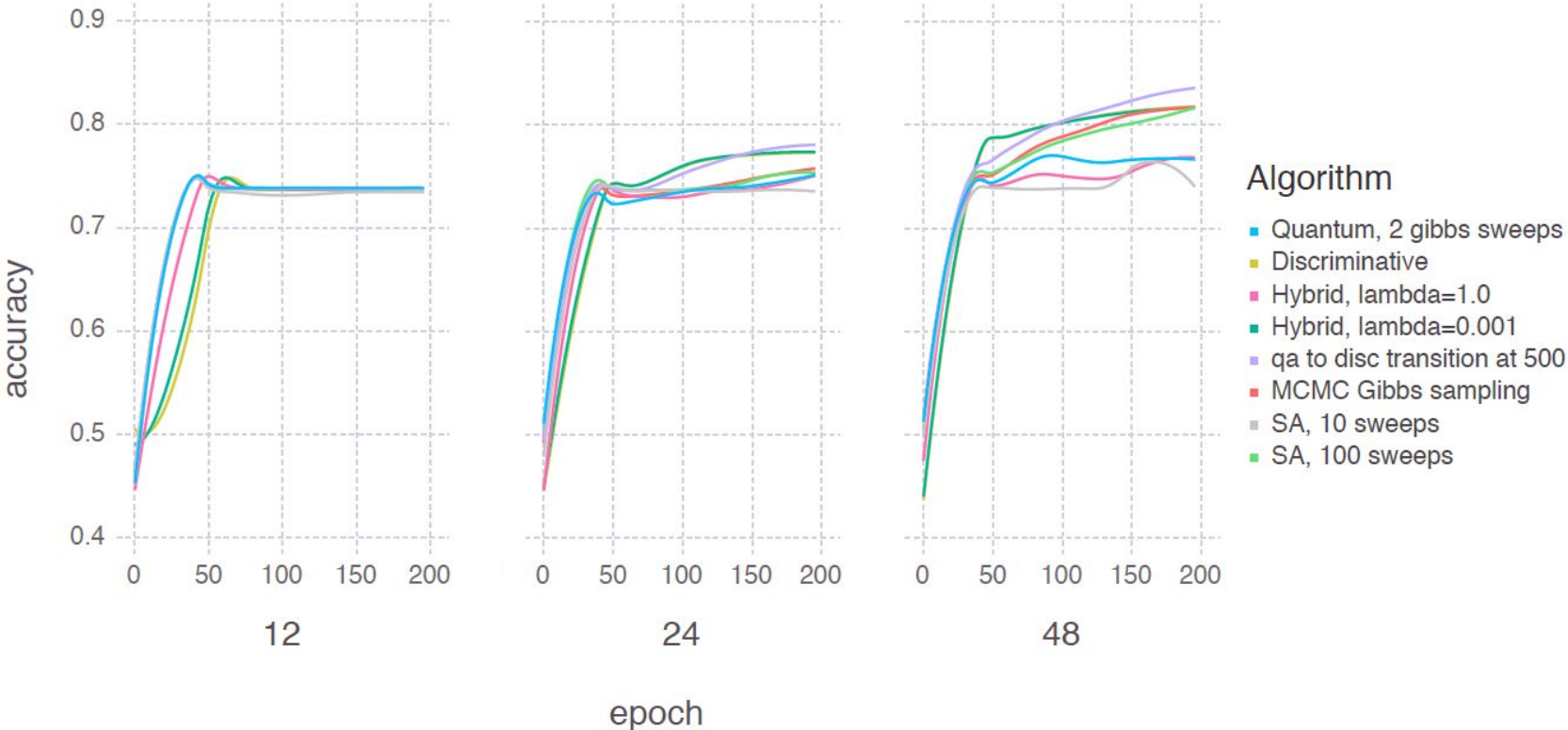
# Use case

Galaxy morphology: spirals vs rounded

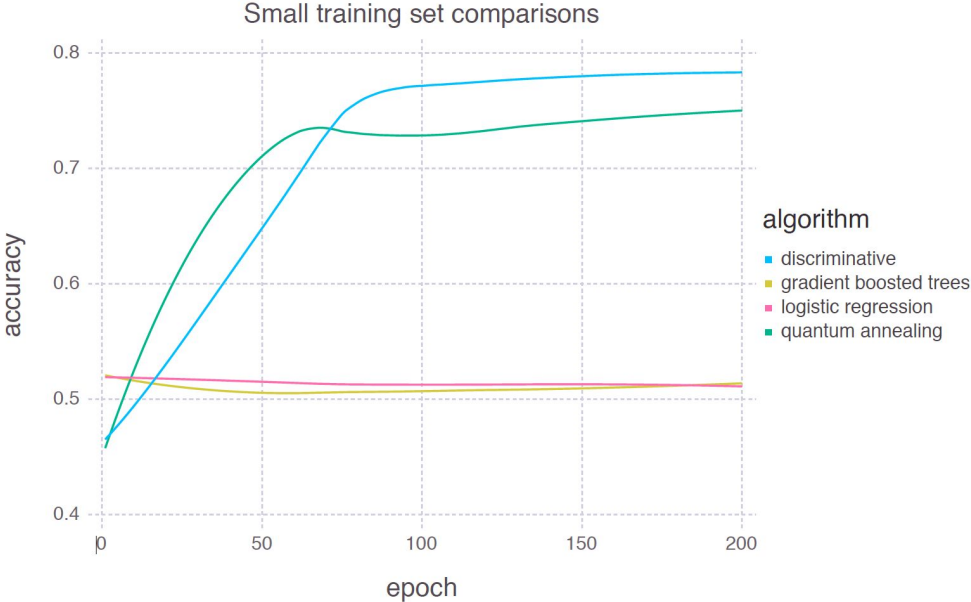


We tested quantum RBM vs classical RBM and other classical classifiers on this task. Note data has to be compressed a lot! We used PCA.

# Accuracy



# Silver linings: small training set, early training



## Other observations

- Unless quantum annealer is also used for inference, need the annealer to provide Boltzmann distribution at known temperature
- We saw distributions far from Boltzmann, so hard to use in this way. Would not currently recommend quantum annealer as a Boltzmann sampler
- Quantum gate models, on universal quantum computers, potentially more useful... (paper using Google's sycamore chip forthcoming)

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# How can you quantify uncertainty?

Many deep learning applications in physics and other fields. But we need accurate uncertainty quantification to trust the results.

In recent years, many methods have been put forward:

- deep ensembles
- concrete dropout
- bayesian neural networks
- ...

How should one choose?

# Epistemic and aleatoric, statistical and systematic

Uncertainty in deep learning is often divided into

*aleatoric or irreducible*: uncertainty related to corruption of input data, such as detector noise

*epistemic or reducible*: uncertainty stemming from an imperfect model, goes down with more data

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**Epistemic is always systematic**

**Statistical is always aleatoric**

**No statistical epistemic uncertainties**

- Problem summary:**
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  2. How to interpret the results

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**Our contribution:** Build simple sandbox with pendulum problem

From  $(L, T, m, \theta)$ , predict  $g = 4\pi^2 L / T^2$ : a problem any physics undergrad is familiar with

We include many measurements of  $T$ , to allow calculation of a statistical uncertainty

# Setup

3 hidden layers with 100 nodes each

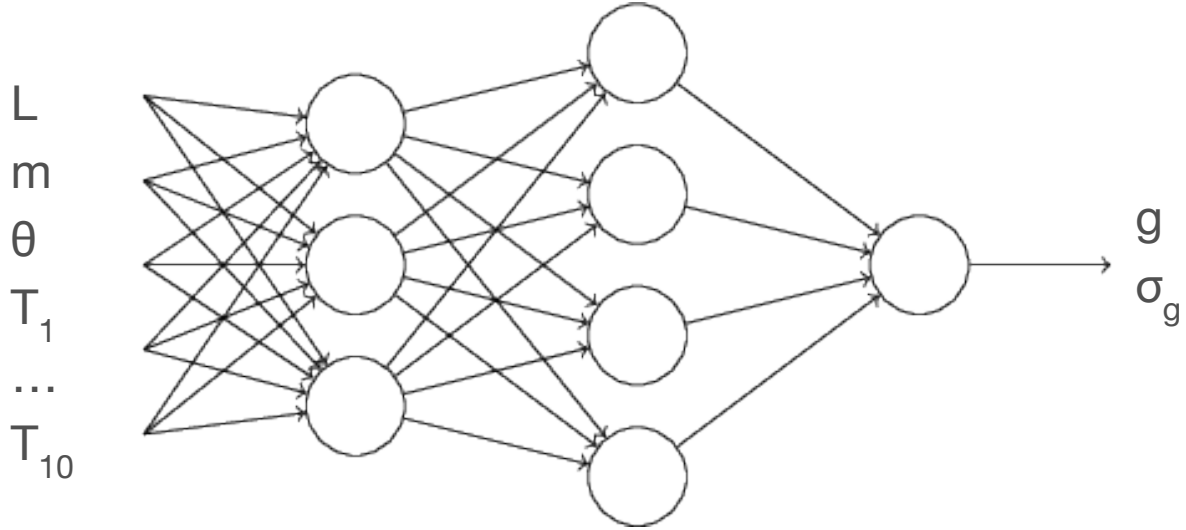


Image credit:  
Michael Nielsen

# Brief introduction to the UQ methods

For all these methods, optimize  $(g, \sigma_g)$  to maximize Gaussian log likelihood of right answer, so loss is

$$L = \log \sigma_g + \frac{1}{2} \left( \frac{g - g_{true}}{\sigma_g} \right)^2$$

$\sigma_g$  provides an estimate of the aleatoric uncertainty, while the variance between different models' predictions gives epistemic uncertainty

Deep ensembles: different models

Concrete dropout: dropping different neurons

Bayesian NN: each weight is sampled from distribution

# How to introduce noise

Statistical (aleatoric): add noise to the T measurements (sample them from a normal distribution)

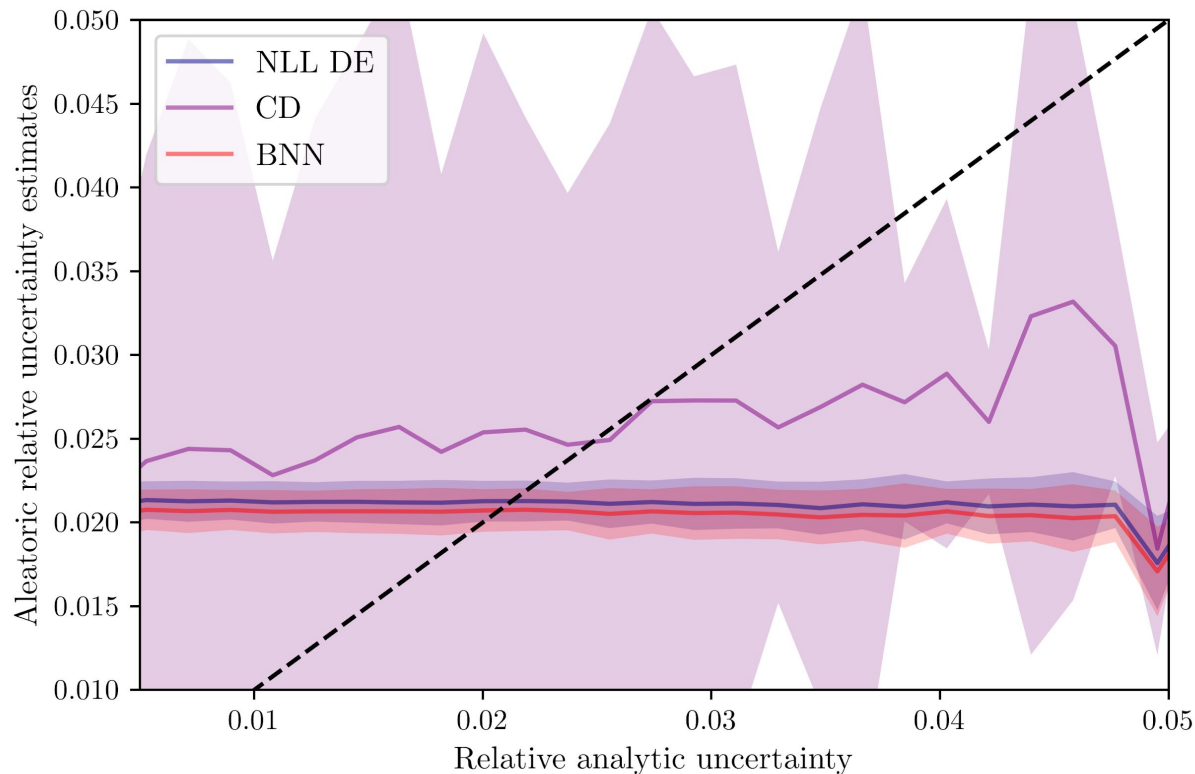
Systematic (aleatoric): add noise to the single L measurement

Systematic (epistemic): smaller training set, or test in different region from training set



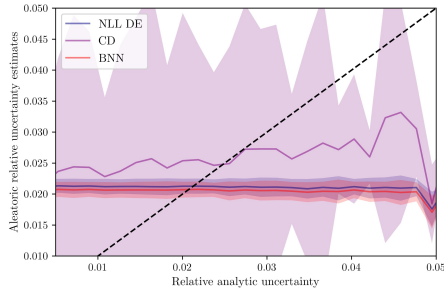
# Results: how well is aleatoric uncertainty captured?

Trained on data with  $T$  variation in range 1-5%:

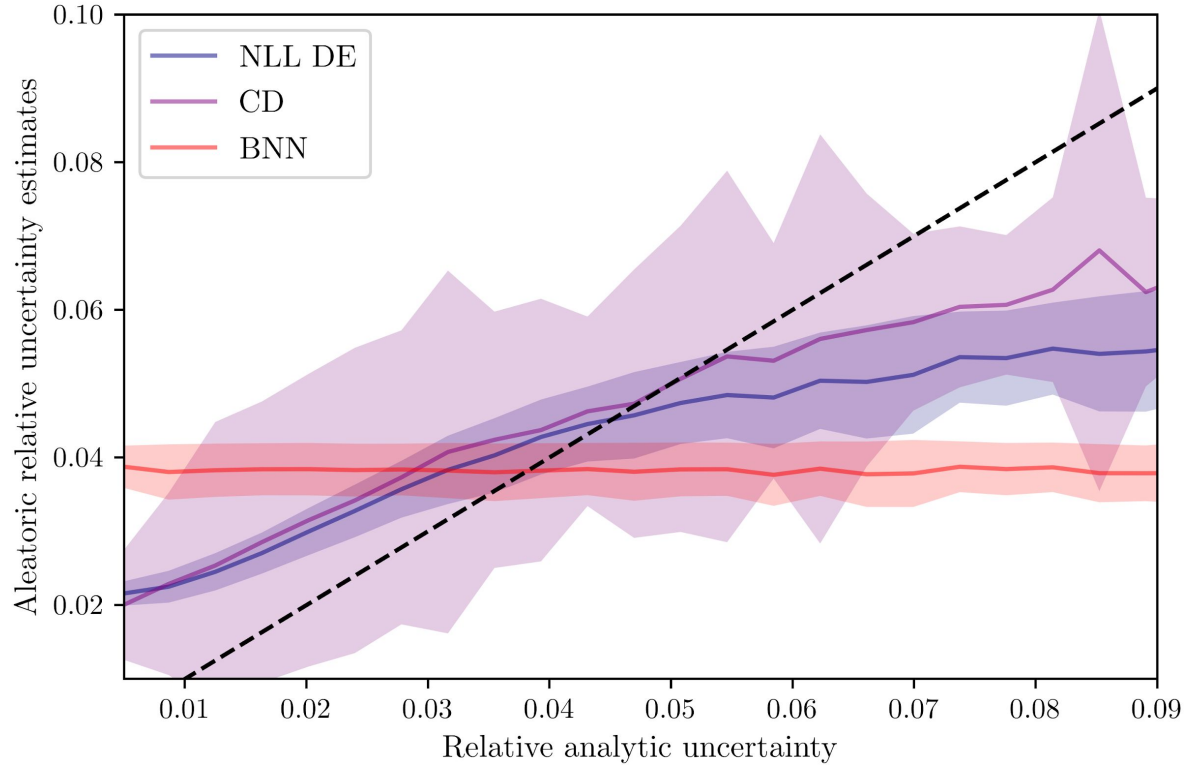


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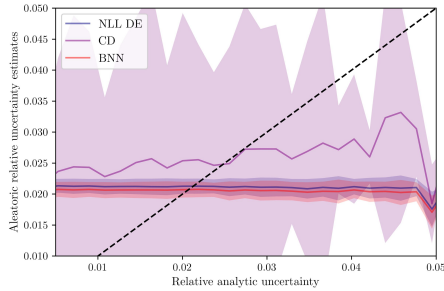
Trained on data with T variation in range 1-10%:



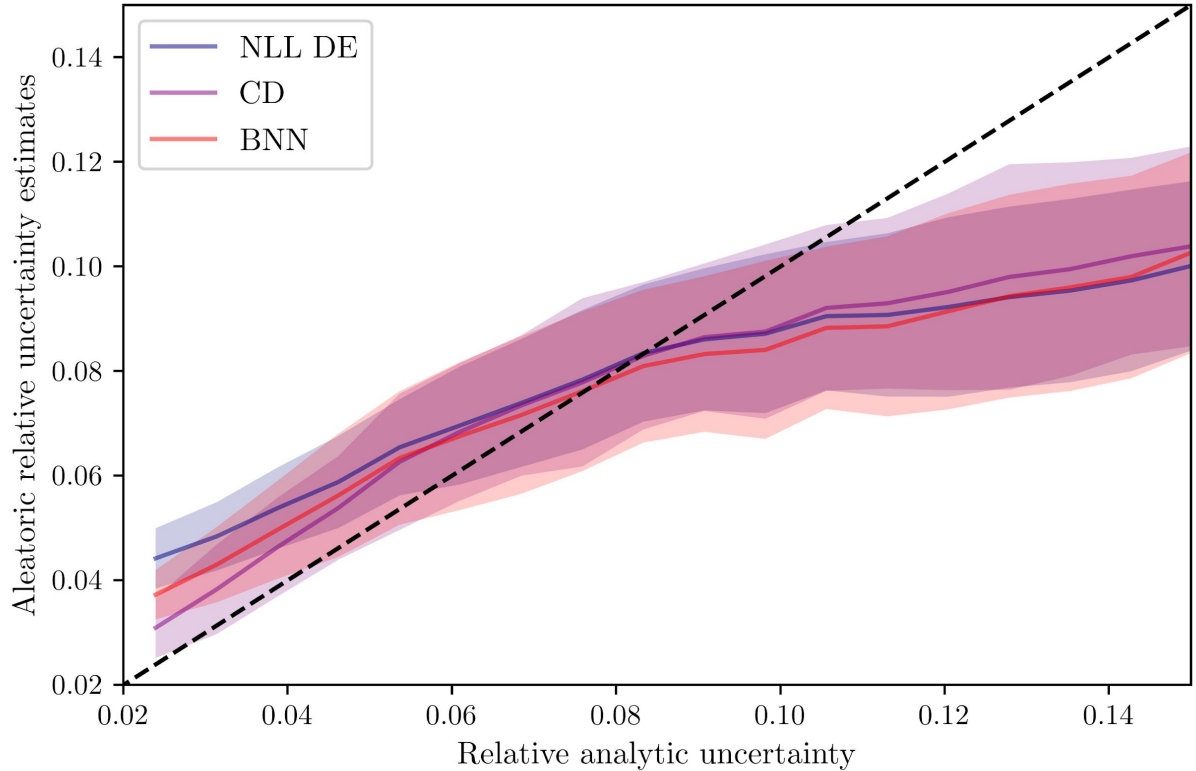
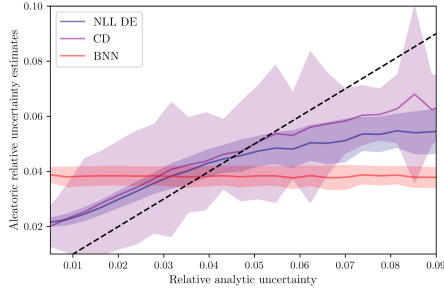
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Trained on data with T variation in range 1-20%:

Range 1-5%



Range 1-10%



# Results: out of distribution uncertainties

Several ways to go out of distribution. We train on

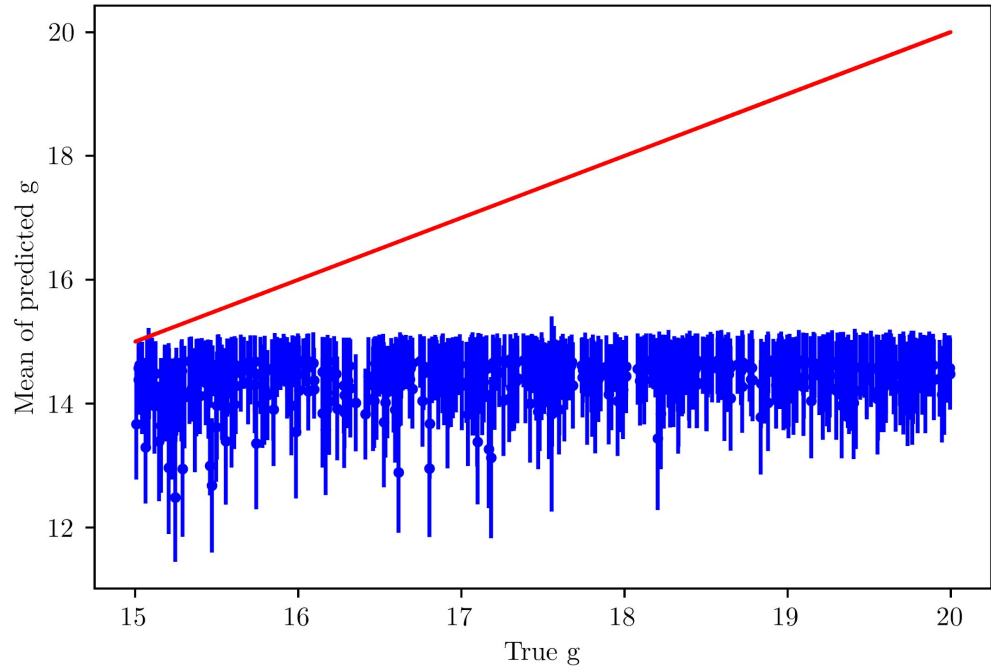
$g$  in  $[5, 15]$   $\text{m/s}^2$ .

Can test on  $g$  in  $[15, 20]$   $\text{m/s}^2$ :

Terrible results!

We can keep  $g$  same, vary  $L$   
and  $T$  out of distribution.

But that problem is too easy!



# Conclusions

- For aleatoric uncertainties, they are reasonably well-modeled: but we need to make sure to include a large range of uncertainties in the training set, or it won't see enough variation. Just like for predictions, but tricky!
  
- None of these methods know they go out of distribution in this simple test! Probably we need better methods in such a situation.

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