



**FACET-II**

Facility for Advanced  
Accelerator Experimental Tests

# AAC Colliders: PWFA, LWFA & SWFA

Mark J. Hogan

*With input from*

John Power & Carl Schroeder

April 30, 2020



U.S. DEPARTMENT OF  
**ENERGY**

Office of Science

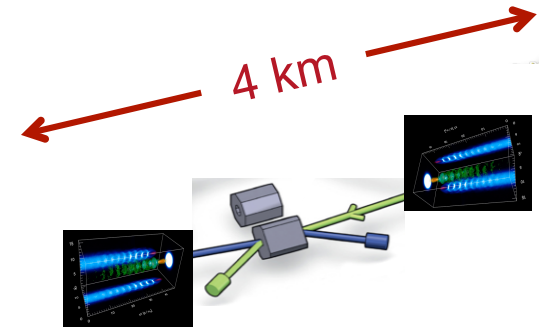


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# The Scale for a TeV Linear Collider

**Today's technology LC  
– a 31km tunnel:**



**Advanced Accelerator Technology LC:**

➔ GeV/m accelerating gradient

**The Luminosity Challenge:**

➔ High-efficiency

$$\mathcal{L} = \frac{P_b}{E_b} \left( \frac{N}{4\pi\sigma_x\sigma_y} \right)$$

...and must do it for positrons too!



## For More Information

- **PWFA, LWFA & SWFA Summary talks @ 2019 ABP Workshop**
  - [https://conferences.lbl.gov/event/279/contributions/3194/attachments/2281/388/Hogan\\_-\\_ABP\\_and\\_plasma\\_accelerators.pdf](https://conferences.lbl.gov/event/279/contributions/3194/attachments/2281/388/Hogan_-_ABP_and_plasma_accelerators.pdf)
  - [https://conferences.lbl.gov/event/279/contributions/3193/attachments/2278/382/conde\\_ABP\\_workshop.pptx](https://conferences.lbl.gov/event/279/contributions/3193/attachments/2278/382/conde_ABP_workshop.pptx)
- **AAC Strategy Report**
  - <https://www.osti.gov/biblio/1358081-advanced-accelerator-development-strategy-report-doe-advanced-accelerator-concepts-research-roadmap-workshop>
- **2019 ALEGRO Workshop @ CERN**
  - <https://indico.cern.ch/event/732810/overview>
- **AAC & EAAC Workshops**
  - <http://aac2018.org>
  - <https://agenda.infn.it/event/17304/overview>
- **USPAS & 2019 CERN Accelerator School on High Gradient Wakefield Accelerators**
  - <https://cas.web.cern.ch/schools/sesimbra-2019>



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# Plasma Wakefield Accelerator Based Linear Collider

Mark J. Hogan  
April 30, 2020



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# Beam Driven Plasma Accelerator Based Collider Concepts

J. Rosenzweig et al. / Nucl. Instr. and Meth. in Phys. Res. A 410 (1998) 532-543

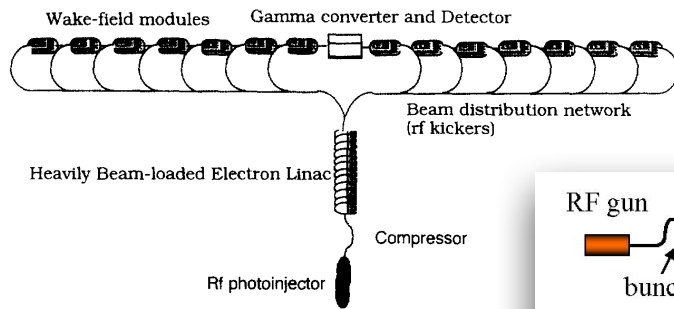


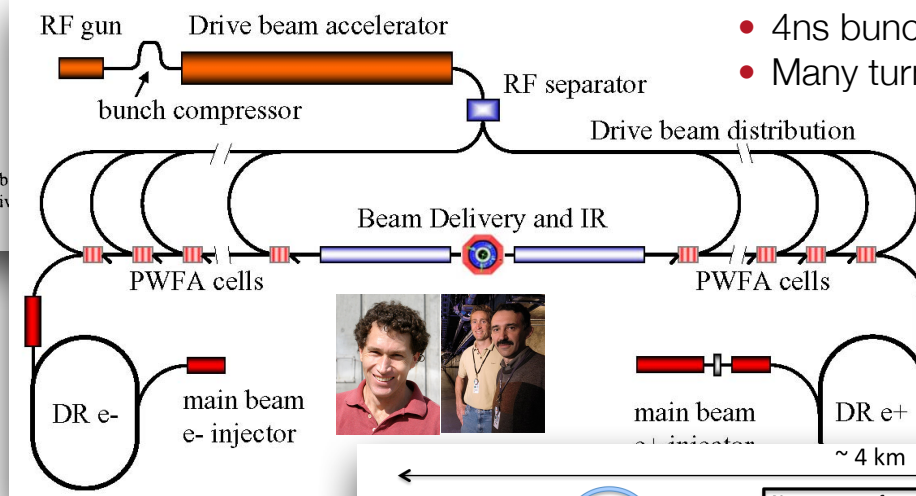
Fig. 6. Schematic of a  $\gamma\text{-}\gamma$  collider using a hardware transformer scheme. A large number of beamliners are fed by an RF photoinjector followed by a compressor. Separate wake modules are driven by a binary RF splitting scheme.



Rosenzweig et al (1998)

Seryi et al (2008) SLAC-PUB-13766

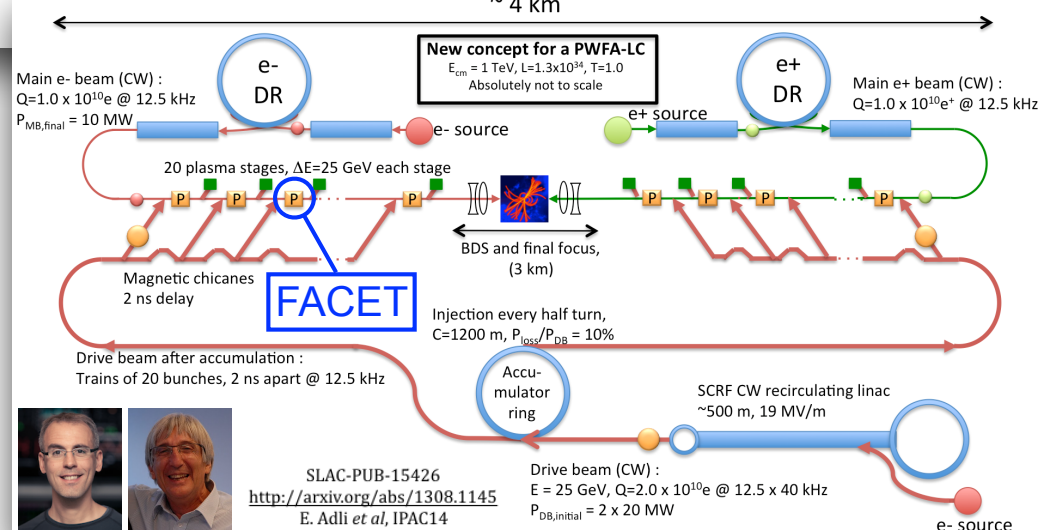
- 'Warm' Drive Linac
- 4ns bunch spacing
- Many turnarounds



Adli et al (2013) SLAC-PUB-15426

- 'Cold' Drive Linac
- 100 $\mu$ s bunch spacing
- Tricky delay chicanes

- Assume SLC/NLC/ILC/CLIC made smart choices that we can start from for main beam and driver
- Focus on the accelerator module itself (the plasma)
- **The plasma is a transformer**
- For luminosity – Power efficiency and beam quality are critical!



SLAC-PUB-15426  
<http://arxiv.org/abs/1308.1145>  
 E. Adli et al, IPAC14

Drive beam (CW) :  
 $E = 25 \text{ GeV}$ ,  $Q = 2.0 \times 10^{10} e$  @  $12.5 \times 40 \text{ kHz}$   
 $P_{D0,initial} = 2 \times 20 \text{ MW}$

## Input constraints



The main beam parameters for the current PWFA-LC design are **assumed to be the ILC main beam parameters**, with some modifications (allows reuse of earlier LC studies ):

Bunch length shortened to fit in plasma

Charge of  $1e10$  particles per bunch (1/2 the ILC nominal bunch charge)

Equal bunch spacing (“CW” collisions)

Other **input constraints** :

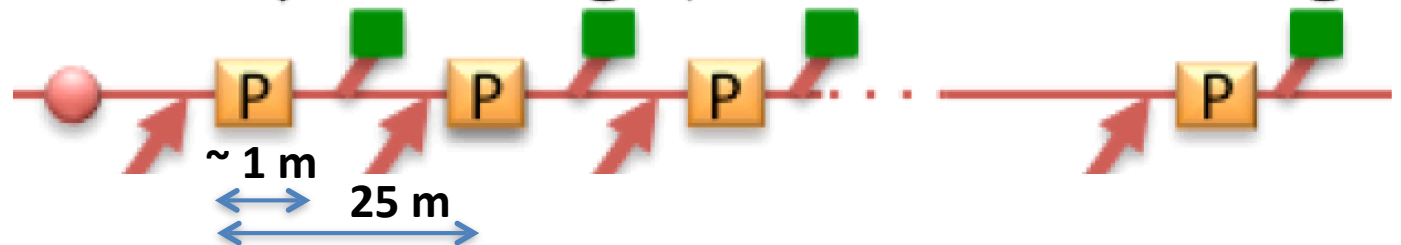
**1 GeV/m** average gradient along main linac (“CLIC x 10”) with 25 GeV energy gain per plasma stage, assuming 25 m average stage length (more on this later)

High transfer efficiency

Push towards low plasma density (see scalings later)

Parameter optimization assumes **e- drive bunch and e- witness bunch in the blow out regime, and no ion motion**

For 1 TeV : 20 plasma stages,  $\Delta E=25$  GeV each stage



**The drive beam parameters are results of plasma optimization process.**

# Plasma Density Considerations

## *Advantages of lower plasma density*

- plasma structure **length scale**

$$\lambda_p \sim n_0^{-1/2}$$

→ looser transverse and longitudinal tolerances; looser bunch length requirements for the drive and witness bunches

- **matched beta function** in the plasma

$$\beta_{\text{mat}} \sim n_0^{-1/2}$$

→ looser optics matching, looser transverse tolerances

- **synchrotron radiation losses** in the plasma (for matched beam)

$$W' \sim n_0^{3/2}$$

→ less synchrotron radiation loss in the plasma, looser transverse tolerances (SR for transverse offset beam)

- **head erosion** in a pre-ionized plasma

$$\sim n_0^{1/4}$$

→ less head erosion of the drive bunch

- the **hosing instability** grows as

$$x/x_0 \sim e^{c(k_p s)^{1/3} (k_p z)^{2/3}}, \quad k_p \sim n_0^{-1/2}$$

## *Main disadvantage of lower plasma density :*

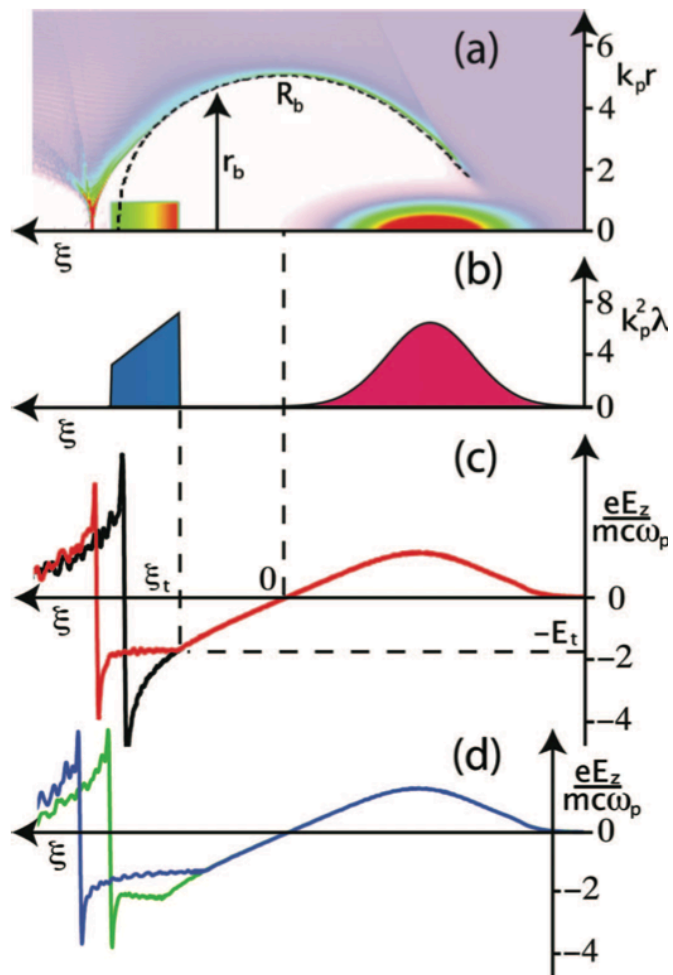
- **lower accelerating gradient**

$$E_{\text{wavebreak}} \sim cm_e \omega_p / e \sim n_0^{1/2}$$

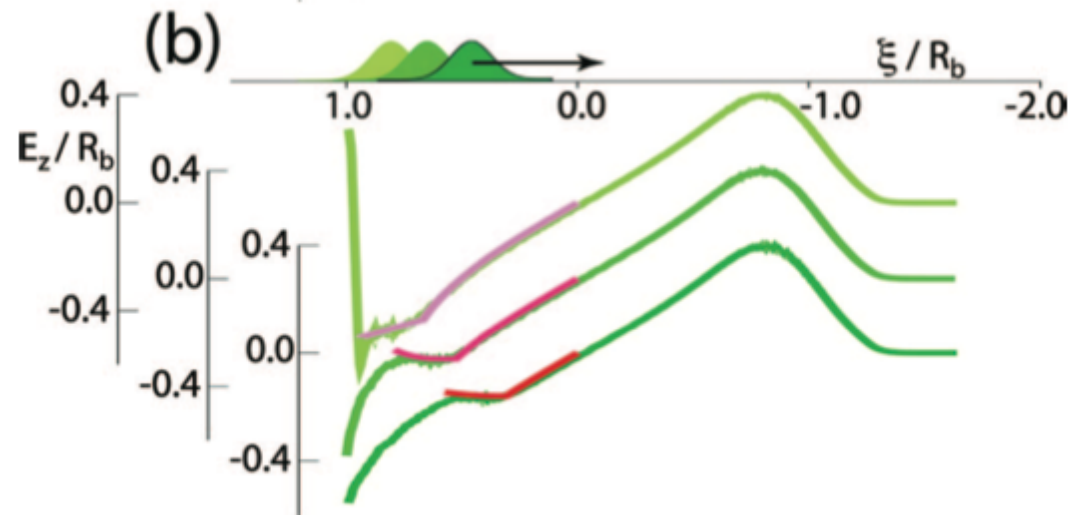


# Non-linear Beam Loading

Tzoufras et al. : beam-loading in the blow-out regime. More **than 80% energy transfer efficiency possible** for optimally shaped trapezoidal bunch. Flattening of the longitudinal field along the witness bunch, resulting in **small energy spread**. :



Almost flat beam loading and good efficiency also possible for **Gaussian witness bunches**. For a given blow out radius, and a given bunch separation,  $\Delta z$ , the optimal beam loading ratio is given by the appropriate witness bunch charge, bunch length ( $Q_{WB}$ ,  $\sigma_{z,WB}$ ).

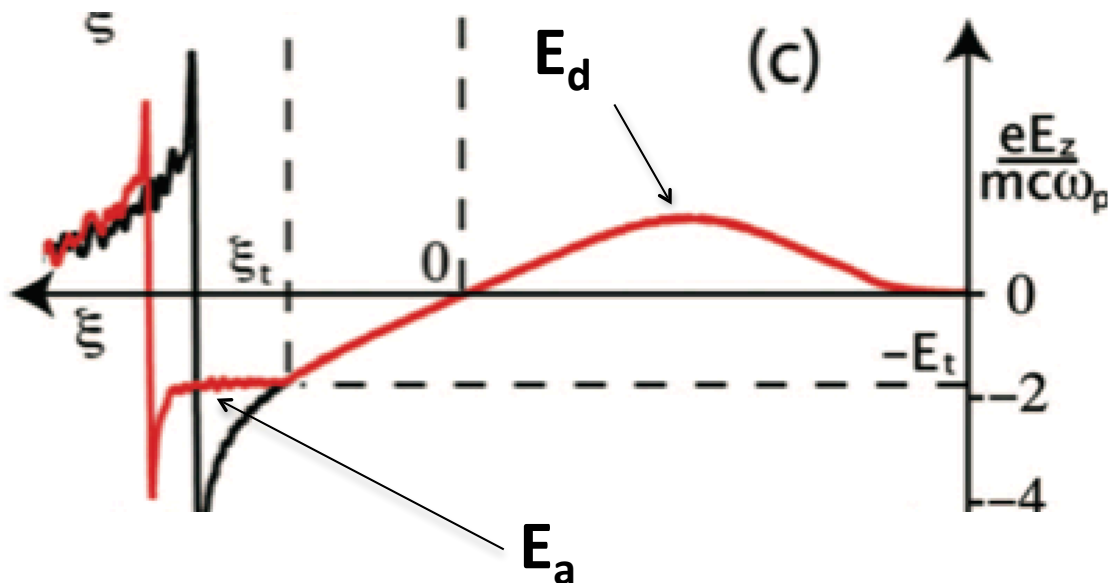


From Tzoufras et al., Physics of Plasmas, 16, 056705 (2009)

# Transformer Ratio

## Transformer ratio :

In the blow out regime the peak accelerating field may be several times the peak deceleration field. The transformer is up to a certain value a free parameter.



Peak decelerating field

$$E_d = \hat{E}_{dec}$$

Witness bunch mean energy gain

$$E_a = \langle E_{acc} \rangle_{WB}$$

Transformer ratio

$$T \equiv \frac{E_a}{E_d}$$

Drive bunch to witness bunch efficiency

$$\eta_{WB} = \frac{\Delta \mathcal{E}_{WB}}{\mathcal{E}_{0,DB}} \frac{Q_{WB}}{Q_{DB}} = T \frac{Q_{WB}}{Q_{DB}} \quad (1)$$

Last equality valid only if most decelerated particle in drive bunch is fully depleted.

## Consequences of higher transformer ratio :

- + Reduced drive beam energy  $\mathcal{E}_{0,DB}$
- Increased drive beam charge  $Q_{DB}$ , since

$$Q_{WB} \times E_a = const.$$

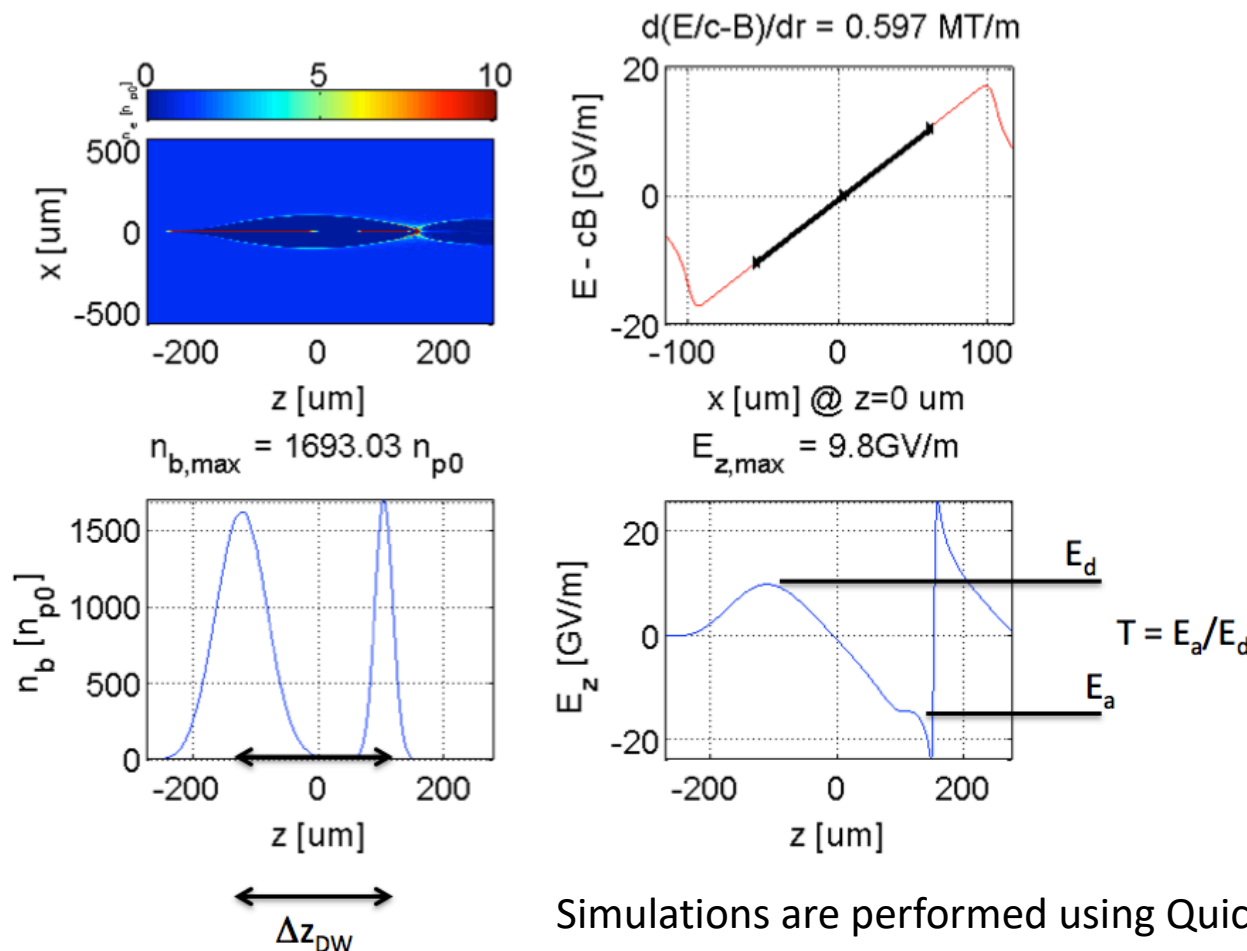
- shorter witness bunch length; tightened tolerances

# Plasma Stage Optimization

**Input constraints:** main beam parameters;  $Q_{WB}=1 \times 10^{10} e$ ,  $\Delta\epsilon=25$  GeV/stage,  $L_{cell} < \text{few m}$ , keep WB energy spread low, reasonable WB length

**Design choice:** plasma density  $n_0$ , transformer ratio  $T$

**Drive beams then set :**  $Q_{DB}$  (charge),  $\epsilon_{0,DB}$  (energy),  $\Delta z_{DW}$  (DB-WB separation),  $\sigma_{z,DB}$ ,  $\sigma_{z,WB}$

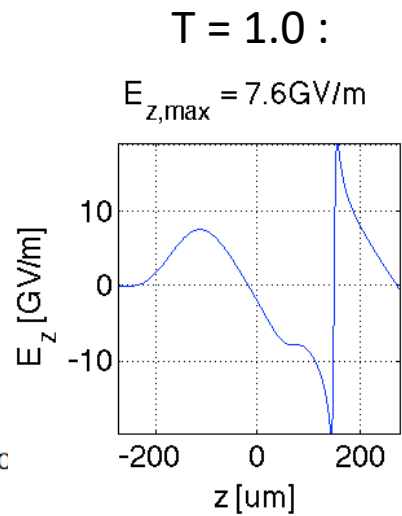
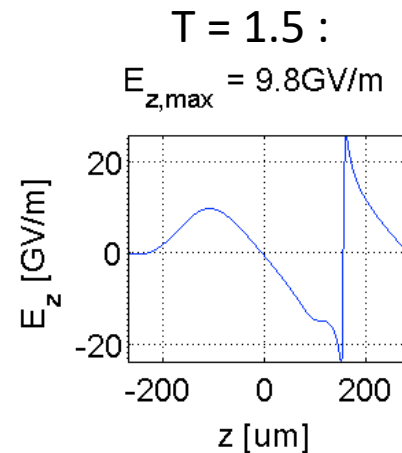


With main beam parameters given, plasma density and transformer ratio chosen, the drive bunch parameters are given by  $Q_{DB} \times E_{acc} = \text{const.}$ , plus the requirement of equal peak current in the drive and witness bunch.

Simulations are performed using QuickPIC (UCLA)

# 2013 Parameters

Parameters optimized following Tzoufras recipe, for two transformer ratios  $T=1$ ,  $T=1.5$ , verified using QuickPIC. No practical solution found for  $T \geq 2$ .



	T=1.5	T=1.0	Old value (2009)	Comments for new values
$n_0 [10^{16}/\text{cm}^3]$	2	2	10	Sufficient field to keep $L_{cell} \leq 3 \text{ m}$
$Q_{WB} [10^{10} e]$	1.0	1.0	1.0	Input constraint
$T$	1.5	1.0	1.0	Reduces drive beam energy by $1/T$
$\sigma_{z,DB} [\mu\text{m}]$	40	40	30	Imposed to give $\sigma_z k_p \sim 1$
$E_d [\text{GV/m}]$	10	7.6	25	Function of $n_0$ and $DB$ params
$E_a [\text{GV/m}]$	15	7.6	25	$E_d \times T$
$\mathcal{E}_{0,DB} [\text{GeV}]$	17	25	25	Results in full $DB$ depletion
$L_{cell} [\text{m}]$	1.7	3.3	1	Length required for 25 GeV gain
$Q_{DB} [10^{10} e]$	3.0	2.0	3.0	Non-linear wake optimization
$\sigma_{z,WB} [\mu\text{m}]$	14	20	10	Non-linear wake optimization
$\Delta z_{DW} [\mu\text{m}]$	225	187	110	Non-linear wake optimization
$\langle \sigma_E / \mathcal{E} \rangle_{WB}$	3%	(n/calc)	(n/avl)	Energy spread due to acc.
$\eta_{DW}$	50%	50%	33%	Increased efficiency
$\sigma_{\{x,y\},mat} [\text{nm}]$	{328,51}	{328,51}	{219,37}	$E=500\text{GeV}$
$W'_{loss,max} [\text{MeV/m}]$	6.1	6.1	70	$E=500\text{GeV}$ , $r_\beta = \sigma_{x,matched}$
$\Delta r @ 100 \text{ MeV/m} [\mu\text{m}]$	1.3	1.3	0.26	$\Delta r$ giving $W'_{loss} \sim 100 \text{ MeV/m}$

\* The efficiency of the two sets is the same; the optimization is done keeping  $Q_{WB} \times E_a = \text{const.}$

\* The plasma density is kept constant for the two cases for comparison, resulting in 3 m long plasma cell for  $T = 1.0$  case. If needed, the cell length can be reduced by increasing the plasma density.

\* The drive beam energy can be increased to yield smaller relative energy spread in the spent beam, at the cost of efficiency. For example, for set  $T = 1.5$ , increasing the drive beam energy to 20 GeV yields a minimum spent drive beam energy of 3 GeV instead of  $< 1 \text{ GeV}$ , and an efficiency reduction from  $\sim 50\%$  to  $\sim 40\%$ .

\* One potential disadvantage not yet quantified is the tolerance on  $\Delta z_{DW}$ . For both the 2012 and the 2009 parameters, however, the tolerance is very tight, in the order of  $1-10 \mu\text{m}$  (corresponding to relative injection timing of  $3 - 30 \text{ fs}$ ).

## Additional Comments

- Simulations confirm analytic choices for plasma, drive and witness beam parameters (gradient, energy gain...)
  - Gaussian beams produce strong beam loading with 50% drive to witness energy transfer (27% left in plasma, 23% left in drive beam) and 3% energy spread
- Shaped beams would offer additional advantages:
  - Higher transformer ratio for reduced drive beam energy and/or number of stages
  - Higher efficiency
  - Reduced energy spread
- Emittance preserved at mm-mrad level but further studies needed to understand interplay of lower emittance, strong beam loading, hosing, ion motion...
- Initial estimates suggest very tight timing and alignment tolerances

# Accelerator Physics Topics in An AAC-based Linear Collider

## Acceleration issues

- Beam loading for efficiency and % level energy spread
- Longitudinal beam shaping to maximize transformer ratio (minimize number of stages)
- Transverse shaping for quasi-linear regime or positrons
- Precise timing to provide acceleration in many sections
- Interstage optics designs to maximize average gradient
- Positron acceleration (plasma concepts) – see next slide

## Emittance preservation

- CSR (and inter bunch correlation) suppression
- Section by section alignment, corrections and feedbacks
- Inter-stage focusing, dispersion control
- Applicability of plasma lenses
- Multiple Coulomb Scattering, ion motion, mismatch...
- Transverse/longitudinal drive beam jitter  $< 1 \mu\text{m}$  (same reqs as for main beam)

## IP: Control of head-on collision $< 1 \text{ nm}$ for single bunch

- Ground motion, vibrations (jitter in beam position)
- Flat beams collision

## Technical issues:

- Plasma response time and heat removal, Synchrotron Radiation and activation

More holistic view beginning to be discussed in presentations and some publications, e.g. C. Lindstrom PhD Thesis “Emittance Growth and Preservation in a plasma-based linear collider” <https://www.duo.uio.no/handle/10852/66134>

PWFA-LC designs all assume common interstage distance ~25-100meters.

## A(PO)CHROMATIC CORRECTION (3/3)

> Example solution [22]:

- > Working staging optics for a 500 GeV, 0.5% rms energy spread, 80 cm matched beta
- > 39 m long, 5 dipoles, 8 quadrupoles
- > Cancels (1st order) chromaticity and (1st order) dispersion.
- > 1% emittance growth (due to 2nd order dispersion)

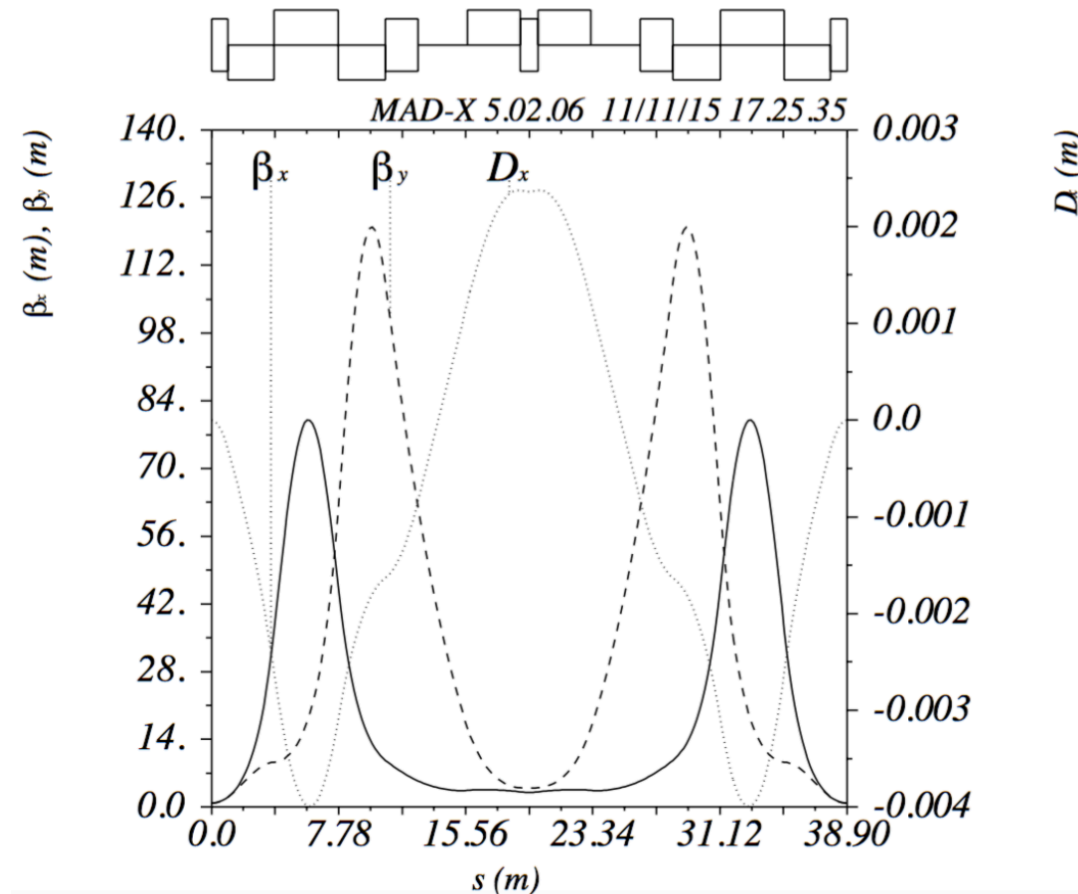
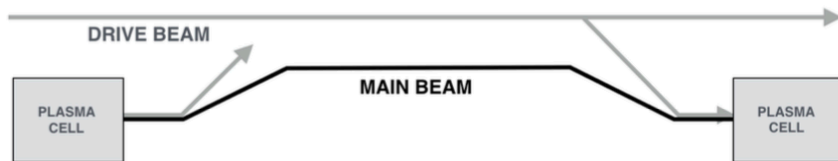


Image source: C. A. Lindstrøm et al., Nucl. Instrum. Methods Phys. Res. A 829, 224–228 (2016) [23]

[22] C. A. Lindstrøm et al., "Staging optics considerations for a plasma wakefield acceleration linear collider", *Nucl. Instrum. Methods Phys. Res. A* 829, 224–228 (2016).

See: C. Lindstrøm "STAGING IN HIGH GRADIENT WAKEFIELD ACCELERATORS"  
<https://cas.web.cern.ch/sites/cas.web.cern.ch/files/lectures/sesimbra-2019/casstaginglecture.pdf>

h 21, 2019 | Page 28

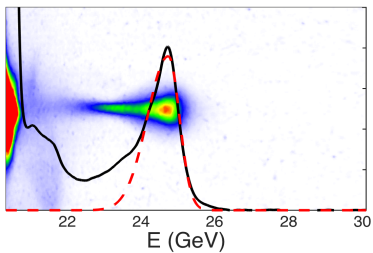
Further investigations (Carl/Erik U. Oslo) indicate this needs more work and scaling to multi-TeV is not favorable for effective gradients  $> 1\text{GeV/m}$ .

# FACET/FACET-II Have a Unique Role in Addressing Plasma Acceleration of Positrons for Linear Collider Applications



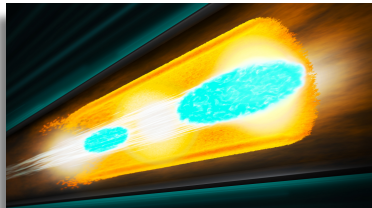
## Demonstrated @ FACET

Non-linear wakes in self-loaded regime of PWFA



Corde et al., *Nature* August 2015

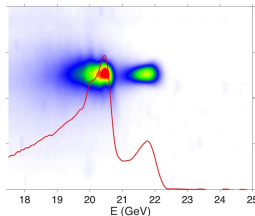
Hollow Channel Plasma Wakefield Acceleration



Gessner et al., *Nature Communications* 2016  
Lindstrom et al., *Phys. Rev. Lett.* 2018

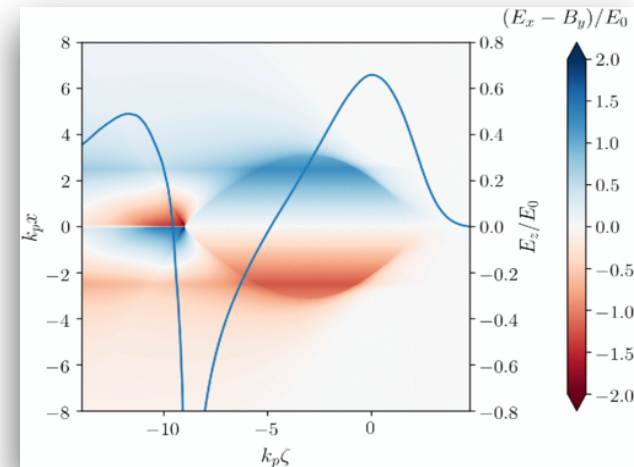
Quasi-linear Wakefield Acceleration

Doche et al., *Scientific Reports* 2017



## Proposed @ FACET-II

- New regime for positron PWFA
- Finite-channel plasmas are predicted to preserve emittance
- Concepts are testable with proposed FACET-II capabilities
- LBNL, DESY and SLAC collaboration



S. Diederichs et al., *Phys. Rev. Accel. Beams* 22, 081301 (2019)

Start Time	Presentation
09:00 am	Summary of FNAL Crystal Workshop & Opportunities @ FACET-II
09:30 am	Roadmap towards linear colliders based on plasma accelerators
09:45 am	New directions in positron acceleration research
10:30 am	Coffee Break
11:00 am	Transversely tailored plasmas
11:30 am	Transversely tailored plasmas
12:00 pm	Non-linear hollow channel plasmas
12:20 pm	Lunch
01:20 pm	Attosecond science
01:50 pm	Positron production and capture from a foil
02:10 pm	Quasi-hollow channels + other IST ideas
02:50 pm	Coffee Break
03:20 pm	Neutral beam filamentation
03:50 pm	Experimental progress in LWFA to PWFA staging
04:20 pm	Machine/physics studies towards FACET-III stability
04:50 pm	Discussion towards new directions
05:30 pm	Adjourn

39. Homogeneous and identical focusing of train of relativistic positron bunches in plasma  
 Denis Bondar (Kazan Kharkov Natl...)  
 17/09/2019, 18:00

WSB - Advanced and novel task WSB - Positrons

Focusing of electron and positron beams in collider is important [1-7]. The focusing mechanism in the plasma, in which all electron bunches are focused identically, has been proposed [5-7]. This idea is researched by simulation by Itoke [8] in

341. Efficiency and beam quality in a loaded quasilinear plasma wakefield positron accelerator  
 Siyi Yu (State Polytechnic)  
 17/09/2019, 18:20

WSB - Advanced and novel task WSB - Positrons

Being promising alternatives to conventional accelerators and for application to high-energy physics also linear colliders, it is crucial for plasma accelerators to accelerate positrons, wh

88. Overview of positron acceleration in plasma-based  
 Carl A. Lindstrom (OSU)  
 18/09/2019, 09:00

Invited Plenary Talk task Plenary Session 5

One of the main motivations for research in plasma wakefield acceleration is the possibility of accelerating high-energy particles in particular the combination of a linear electron-positron

205. Positron transport and acceleration in beam-driven plasma column  
 Severin Diederichs (University of Hamburg...)  
 18/09/2019, 17:00

WSB-WSB Joint Session task WSB-WSB Joint Session

The transport and acceleration of positron beams is a crucial challenge on the path towards plasma-based particle colliders. We propose a scheme that allows for the simultaneous acceleration and transport of positron beams in plasmas

179. Stable positron acceleration in self-generated hollow channels  
 Thales Silva (Osaka Prefecture Super...)  
 18/09/2019, 18:00

WSB - Theory and simulation task WSB - Proposed solution...

Hollow plasma channels are promising candidates for the acceleration of electron and positron beams as the transverse forces are nearly vanishing inside the hollow channel. The acceleration is effective as long as the accelerated bunches

Talks on Positron PWFA at EAAC and FACET-II Science Workshops in 2019

Worldwide theoretical studies focused on beam parameters that will be achievable at FACET-II





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# Laser Wakefield Accelerator Based Linear Collider

Carl Schroeder (LBNL)  
April 30, 2020



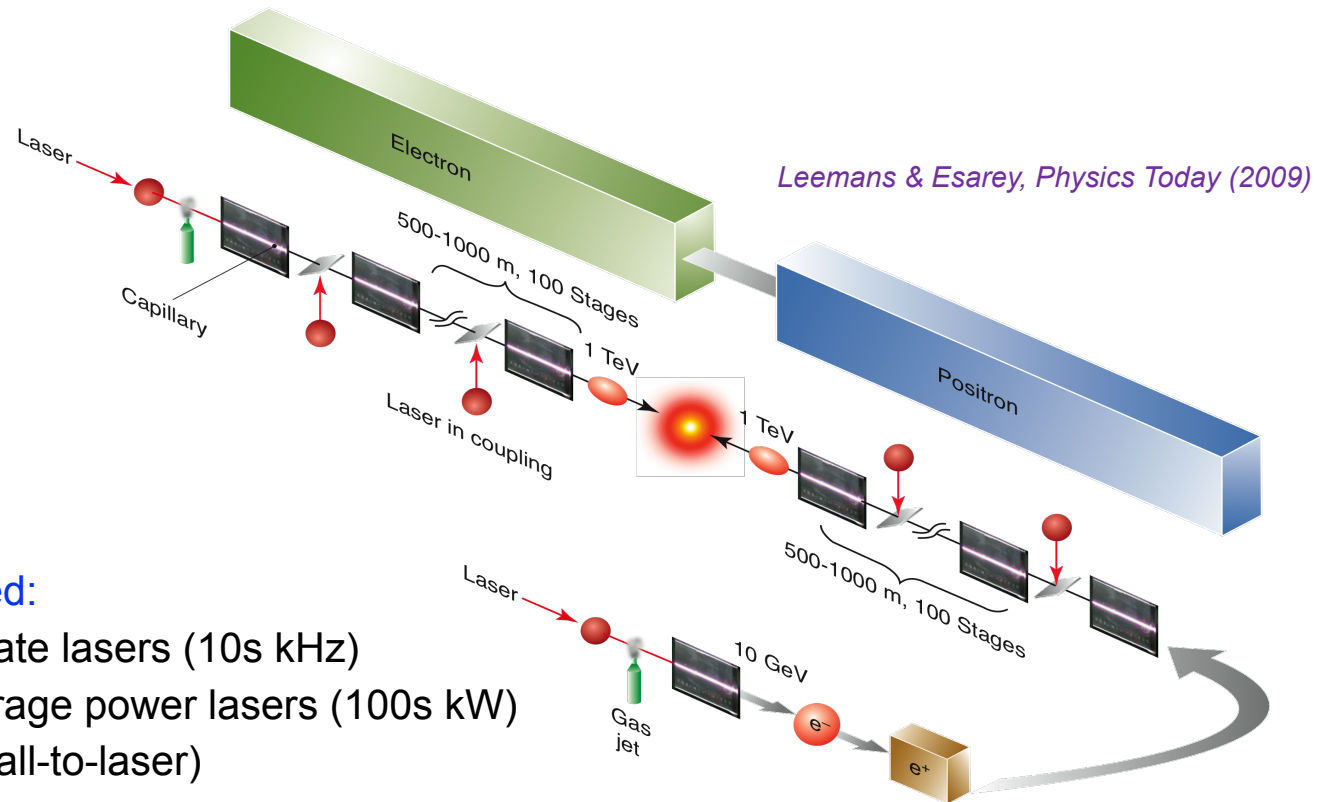
# Laser-plasma collider concept

## Basic concept: Staged laser-plasma accelerators:

- Plasma density scalings indicates operation at  $n \sim 10^{17} \text{ cm}^{-3}$  [high average gradient and low wall plug power]
- Quasi-linear regime ( $a \sim 1$ ):  $e^+$  and  $e^-$  focusing and acceleration; focusing control
- Staging & laser coupling into plasma channels (for laser guiding):
  - Tens of J laser/energy per stage
  - Energy gain/stage  $\sim$  few GeV in  $< 1 \text{ m}$

*C. B. Schroeder et al., PR ST-AB (2010)*

*C. B. Schroeder et al., NIMA (2016)*



## Laser technology development required:

- High luminosity requires high rep-rate lasers (10s kHz)
- Requires development of high average power lasers (100s kW)
- High laser efficiency ( $\sim$ tens of % wall-to-laser)

# Collider design optimization

Basic collider parameter scalings with density and laser wavelength:

*C. B. Schroeder et al., PR ST-AB (2010)*

$$N_{\text{stages}} \propto n\lambda^2$$

$$L_{\text{linac}} \propto n^{-1/2}$$

$$f_{\text{rep}} \propto n$$

$$P_b \propto n^{1/2}$$

$$P_{\text{avg laser}} \propto n^{-1/2}\lambda^{-2}$$

$$P_{\text{wall}} \propto n^{1/2}$$

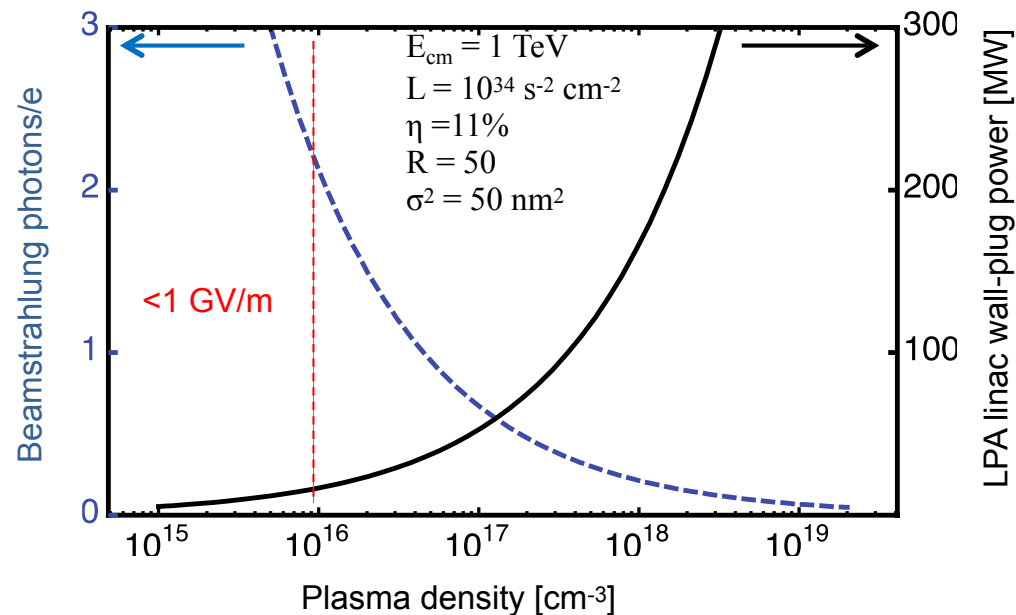
$$n_\gamma \propto n^{-1/2}$$

## Optimization of operational plasma density:

- Density high enough for sufficient gradient (reduced total linac length)
- Density low enough for sufficient charge/bunch (reduced power requirements)
- Density determines required laser parameters (energy/pulse, duration, peak power, rep. rate)

$$E_z \propto n^{1/2}$$

$$N_b \propto n^{-1/2}$$

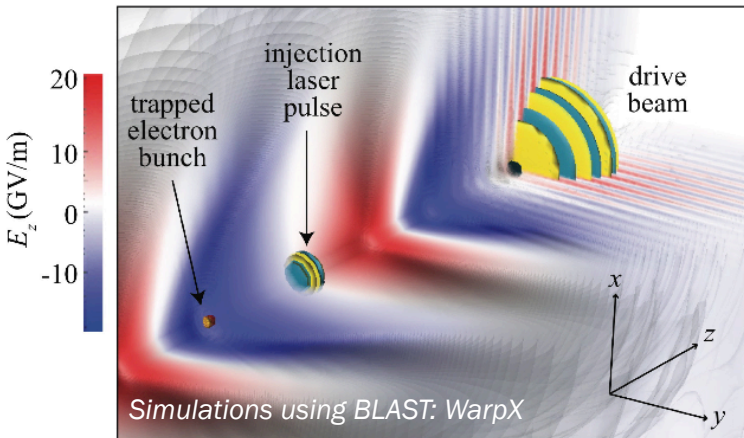


# R&D on LWFA beam physics questions

## Generation of ultra-low emittance beams –

Can laser-plasma interactions (laser-triggered injection) be used to generate beams with ultra-low ( $\sim 10$  nm) emittances?

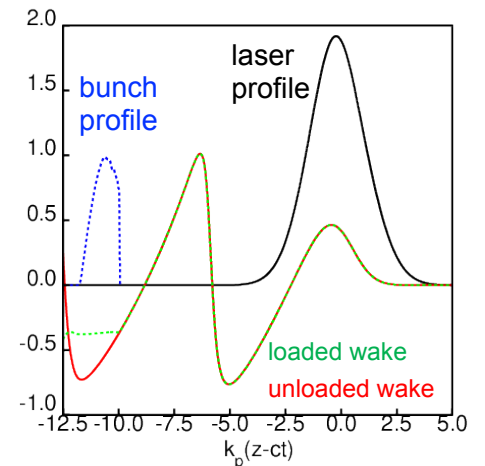
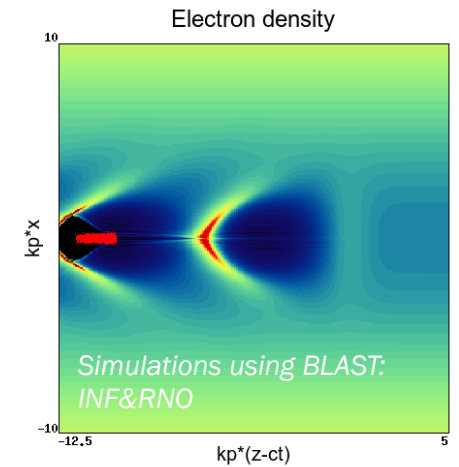
*Lu et al., PRL (2014); C. B. Schroeder et al., PRAB (2014)*



Experiments at BELLA in preparation for 2-color ionization injection.

## Shaped particle beams for high driver-to-beam efficiency -

What is the beam shape to load to eliminate energy spread with high efficiency? How to achieve shape in lab?



**Ion motion induced emittance growth** - Small emittance and plasma focusing yields dense beams and ion motion, creating nonlinear focusing forces. Can beams be matched to the ion-motion-modified wakefields?

*Benedetti et al., PRAB (2017)*

**Beam-break up (BBU) / hosing instability** - What are possible mitigation methods (ion motion, focusing force chirp, etc.)?

*Mehrling et al. PRL (2018); Lehe et al., PRL (2017)*



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# Structure Wakefield Accelerator Based Linear Collider

John Power (ANL)  
April 30, 2020



# SHORT-PULSE SWFA 3 TEV COLLIDER CONCEPT

□ Based on dielectric TBA technology

- HIGH GRADIENT: Short RF pulses (20ns)
- LOW CONSTRUCTION COST: Dielectric structures
- LOW OPERATING COST: Wall plug efficiency ~15%

REF



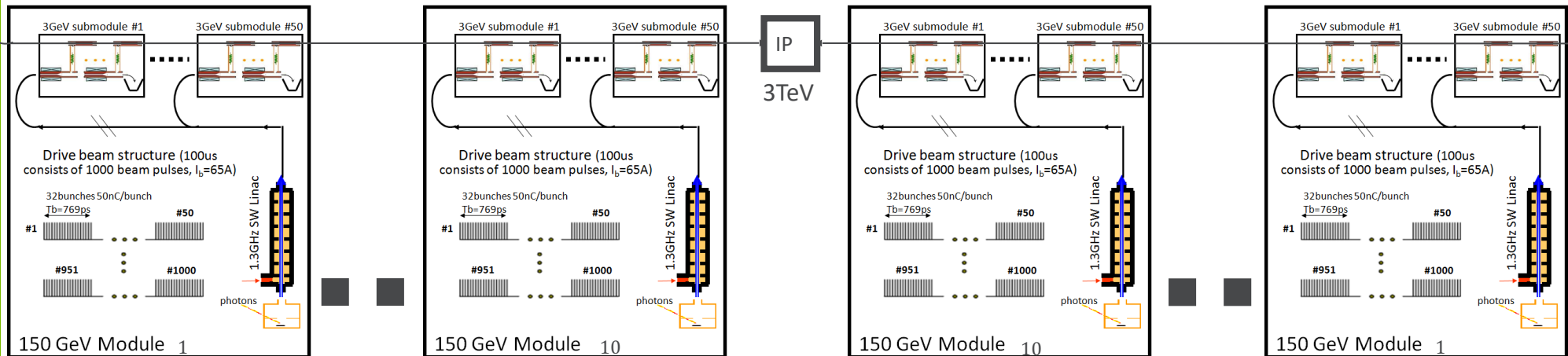
## ARGONNE FLEXIBLE LINEAR COLLIDER

main beam booster linac

e<sup>-</sup> generation

e<sup>+</sup> generation

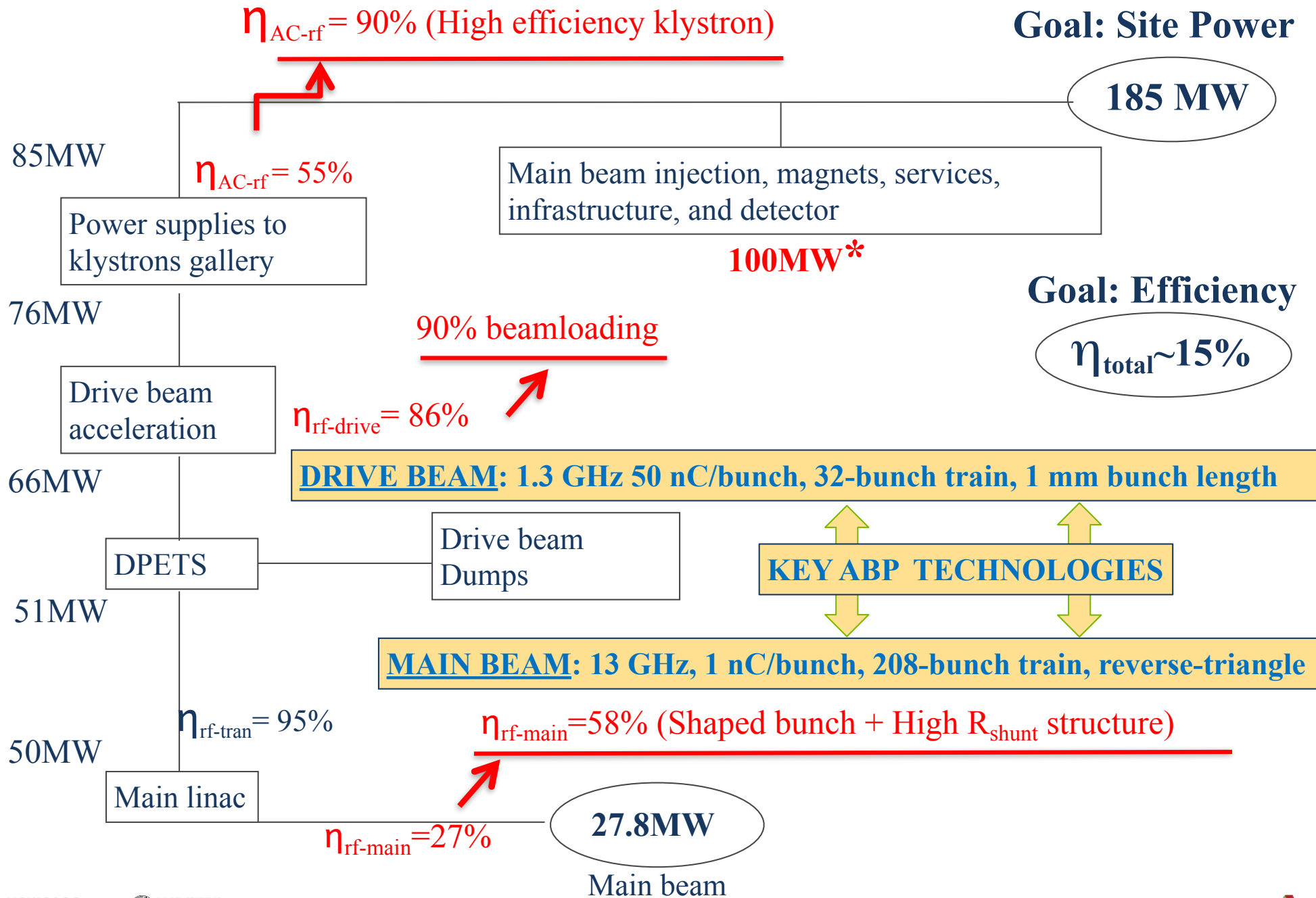
main beam structure



**Modular design**  
(easily staged)

**e<sup>+</sup> e<sup>-</sup> 267 MeV/m of loaded gradient**  
(200 MeV/m effective gradient)

# COST(STRUCTURE, EFFICIENCY,...)



# ACCELERATOR BEAM PHYSICS ISSUES FOR SWFA

## Drive Bunch Train:

1.3 GHz, 50 nC, 32-bunch train, 1 mm bunch length

- High-intensity, High-power (50 GW) beam : beam loading, brightness, ...
- Beam control for high charge bunch train (e.g. , BBU control, shaping, ...)
- Simulation of high charge bunch train (e.g. simulation for bunch train ...)
- .....

## Main beam:

13 GHz, 1 nC/bunch, 208-bunch train, reverse-triangle

- Generation of nanocoulomb-level high brightness beam
- Preservation of beam quality (e.g. collective effect mitigation, ...)
- Phase space control of nanocoulomb beam (e.g. compression, shaping, flat beam, ...)
- .....



## Concluding Thoughts

- Many accelerator beam physics challenges en route to a collider (and even to first applications) – see partial list slide 14
- US and International collaborations have proposed many exciting and challenging experiments to address key physics issues on US Roadmap – success will require theory, computation, diagnostic development and facilities to test
- Each ‘Advanced Accelerator’ technology has prioritized milestones but there are also many common issues:
  - Beam loading and beam shaping for narrow energy spread and high efficiency
  - Emittance preservation at  $\mu\text{m}$  and sub- $\mu\text{m}$  levels
  - Knowledge of structure dynamics at long timescales
  - Investigations of paths to positron acceleration comparable to electrons
- Applying lessons learned to update collider designs will take community involvement and motivated/dedicated personnel with time to do so

**<https://snowmass21.org/start>**