

# Split UED

Park, JS, arXiv:0901.0720,  
Phys. Rev. D 79, 091702 (R)

Chen, Nojiri, Park, JS,  
Takeuchi, arXiv:0903.1971

Chen, Nojiri, Park, JS,  
work in progress

Jing Shu

IPMU



# Outline



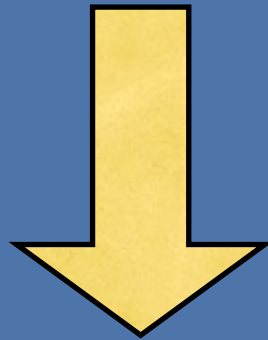
- Motivation.
- Model, mass spectrum and modified couplings.
- Cosmic rays in LKP annihilation.
- Resonance searches from the dijets channel at LHC.
- Missing energy + multi-jets at LHC
- Summary.



# Motivation

Recent results in the high energy cosmic rays (PAMELA, ATIC/PPB-BETS) tell us that there are excesses in  $e^+$ ,  $e^-$ , but not anti- $p$ .

More recently FERMI

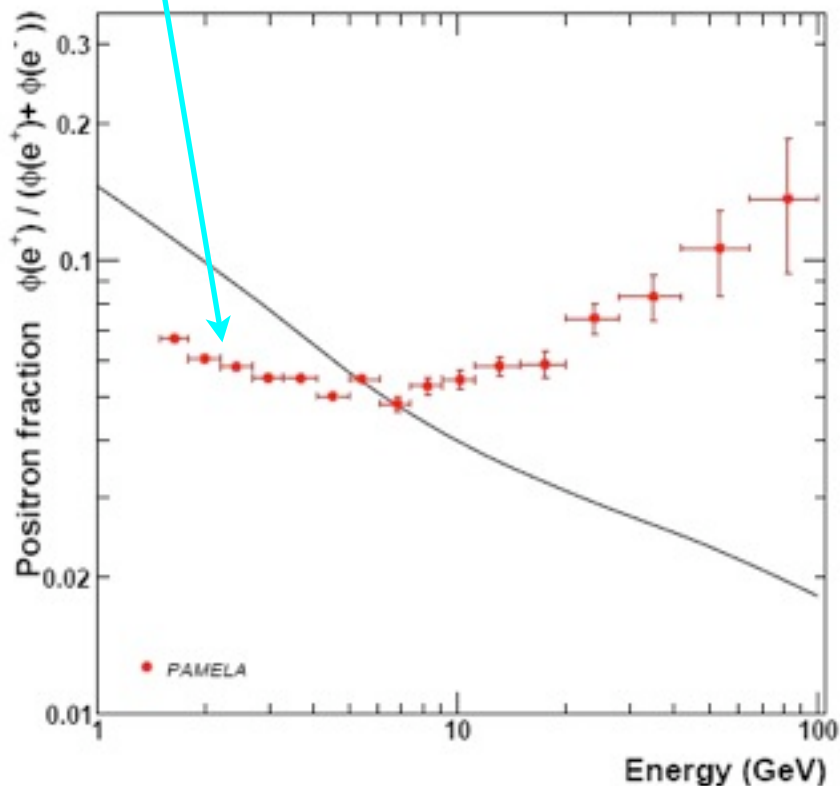


The new challenge begins.....

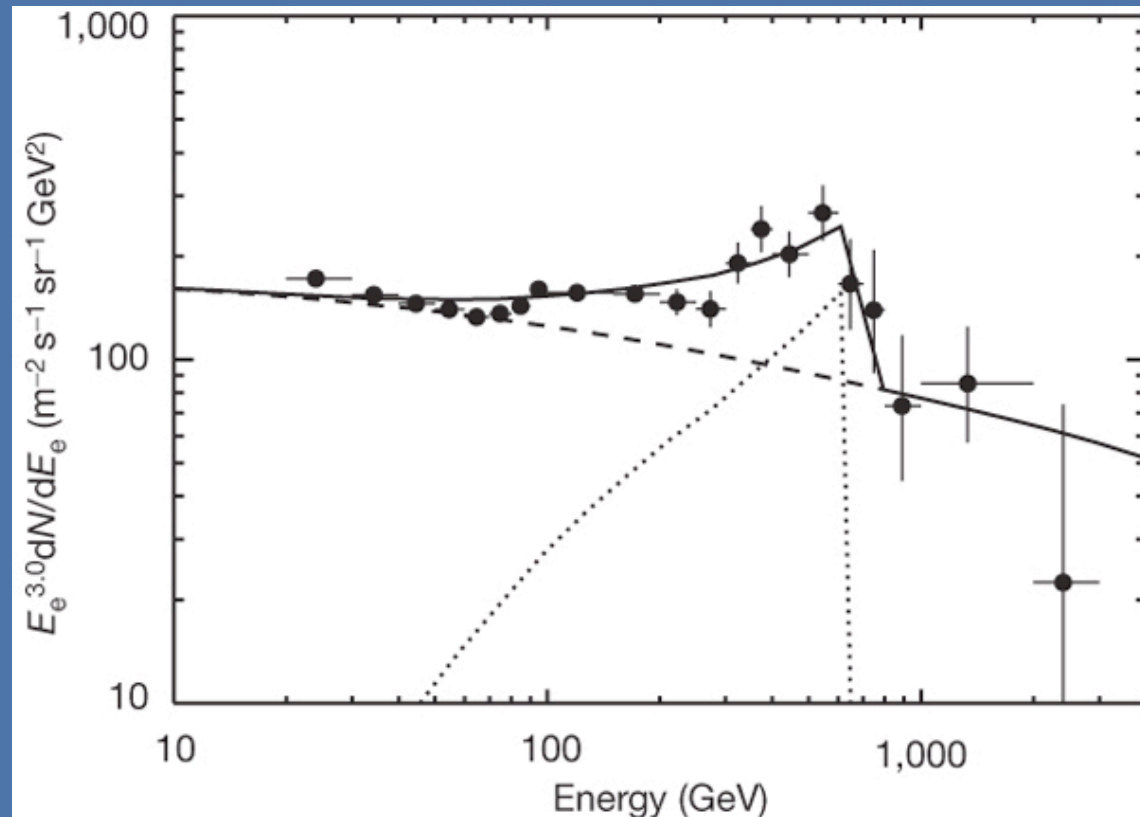
# Motivation

We see  $e^-$  and  $e^+$  excesses in different experiments (PAMELA and ATIC).....

Solar modulation



O. Adriani et al., Nature 458: 607 (2009).

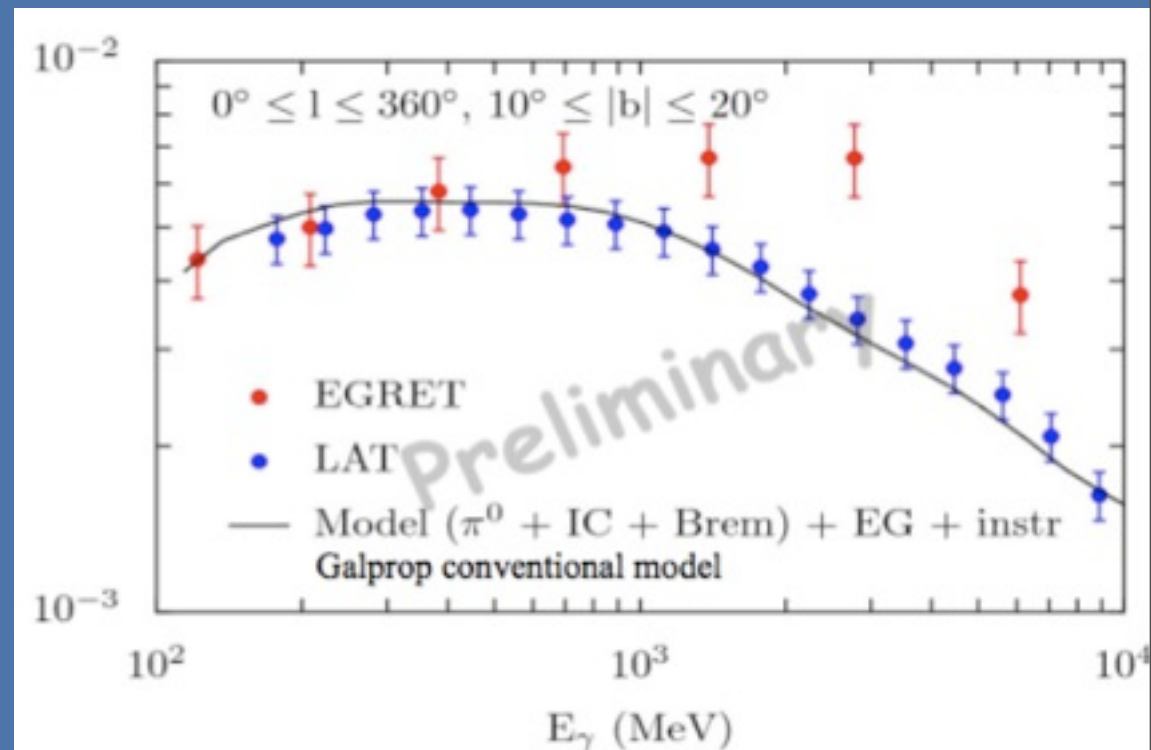
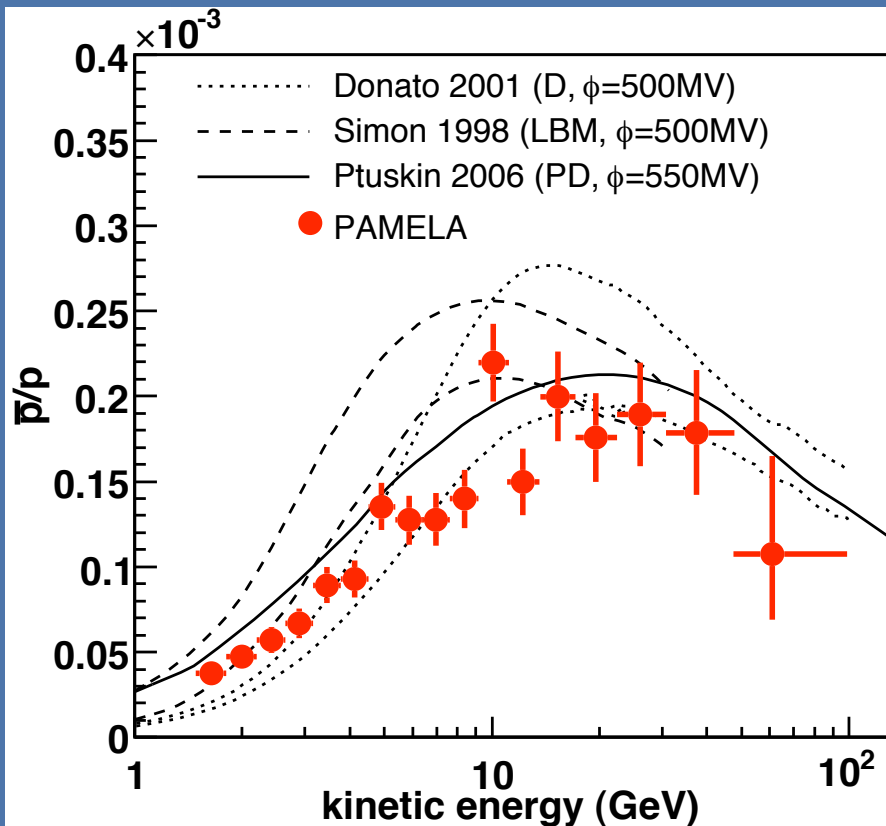


J. Chang et al., Nature 456 (2008) 362.



# Motivation

However, cosmic rays from quarks (anti-proton and gamma rays) are quite suppressed!



# Motivation

If the cosmic ray excess is interpreted by the DM annihilation scenario, the DM will mainly annihilate **into leptons.**

N.Arkan-Hamed, D. Finkbeiner, T. Slatyer, N. Weiner Phys. Rev. D 79: 015014 (2009)

Conventional wisdom: DM is in the leptonic sector.



**“Lepton Jets”**

N.Arkan-Hamed, N. Weiner JHEP 0812: 104 (2008)

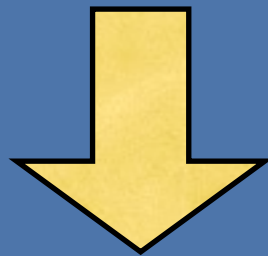
M. Baumgart, C. Cheung, J. Ruderman, L-T. Wang, I. Yavin arXiv: 0901.0283

Y. Bai, Z-Y. Han JHEP arXiv: 0902.0006

# Motivation

What if we modify the DM matter model in the quark sector instead???

We consider to **suppress the hadronic BR** in mUED to explain the cosmic rays signals from DM annihilation.



Explain **all** the cosmic anomalies above.  
**Novel Jet signals** at the LHC.....

# MUED

We consider a well motivated DM scenario: mUED

Fixed point

$S^1/Z_2$  Orifolds:

$$\psi(x, y) = \psi(x, 2L + y) \quad \phi(x, y) = \phi(x, 2L + y)$$

5D Dirac fermion

$$\psi(x, -y) = \gamma_5 \psi(x, y)$$

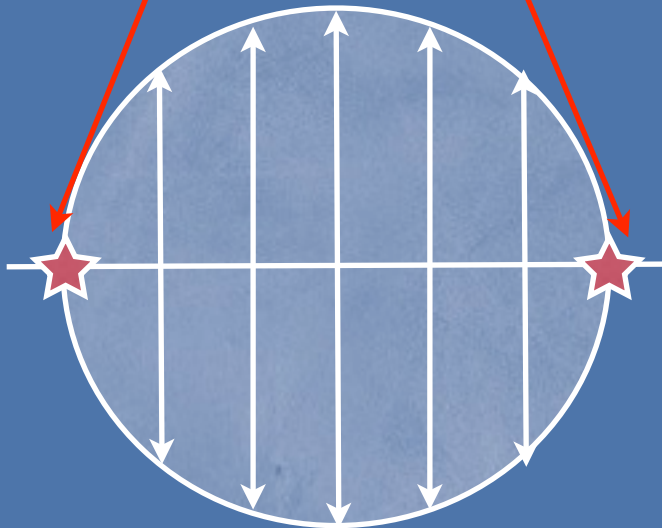
The two weyl components have opposite orififold condition

$$\psi(x, L + y) = \gamma_5 \psi(x, L - y)$$

“+”, “-” stands for the orififold even or odd fields

$$\phi(x, -y) = \pm \phi(x, y)$$

$$\phi(x, L + y) = \pm \phi(x, L - y)$$



# MUED

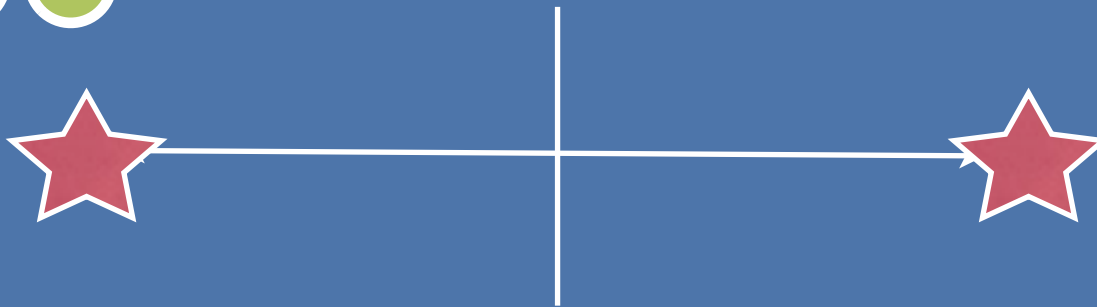
● ○ ● KK decomposition:

$$\begin{aligned}\Phi_+(x, x_5) &= \frac{1}{\sqrt{\pi R}} \phi_+^{(0)}(x) + \sqrt{\frac{2}{\pi R}} \sum_{n=1}^{\infty} \cos \frac{nx_5}{R} \phi_+^{(n)}(x), \\ \Phi_-(x, x_5) &= \sqrt{\frac{2}{\pi R}} \sum_{n=1}^{\infty} \sin \frac{nx_5}{R} \phi_-^{(n)}(x).\end{aligned}$$

The **flat** zero mode.

- All SM fields are zero modes with FLAT profiles propagating in the bulk.
- Higher KK modes are sine (oribifold odd) and cosine (oribifold odd) functions .
- The wave fuctions and couplings are “universal”.

# KK parity



- The reflection **symmetry about the mid point** + a orbifold  $Z_2$  transformation.
- momentum conservation along 5th direction=translational invariance which is broken by **fixed points**



# KK photo is LKP

Masses quite degenerate at the tree level!

$$\delta(m_{B^{(n)}}^2) = \frac{g'^2}{16\pi^2 R^2} \left( \frac{-39}{2} \frac{\zeta(3)}{\pi^2} - \frac{n^2}{3} \ln \Lambda R \right)$$

$$\delta(m_{W^{(n)}}^2) = \frac{g^2}{16\pi^2 R^2} \left( \frac{-5}{2} \frac{\zeta(3)}{\pi^2} + 15n^2 \ln \Lambda R \right)$$

$$\delta(m_{g^{(n)}}^2) = \frac{g_3^2}{16\pi^2 R^2} \left( \frac{-3}{2} \frac{\zeta(3)}{\pi^2} + 23n^2 \ln \Lambda R \right)$$

$$\delta(m_{Q^{(n)}}) = \frac{n}{16\pi^2 R} \left( 6g_3^2 + \frac{27}{8}g^2 + \frac{1}{8}g'^2 \right) \ln \Lambda R$$

$$\delta(m_{u^{(n)}}) = \frac{n}{16\pi^2 R} (6g_3^2 + 2g'^2) \ln \Lambda R$$

$$\delta(m_{d^{(n)}}) = \frac{n}{16\pi^2 R} \left( 6g_3^2 + \frac{1}{2}g'^2 \right) \ln \Lambda R$$

$$\delta(m_{L^{(n)}}) = \frac{n}{16\pi^2 R} \left( \frac{27}{8}g^2 + \frac{9}{8}g'^2 \right) \ln \Lambda R$$

$$\delta(m_{e^{(n)}}) = \frac{n}{16\pi^2 R} \frac{9}{2}g'^2 \ln \Lambda R.$$

$$(m_n)^2 = \left( \frac{\pi}{L} \right)^2 + (m_0)^2$$

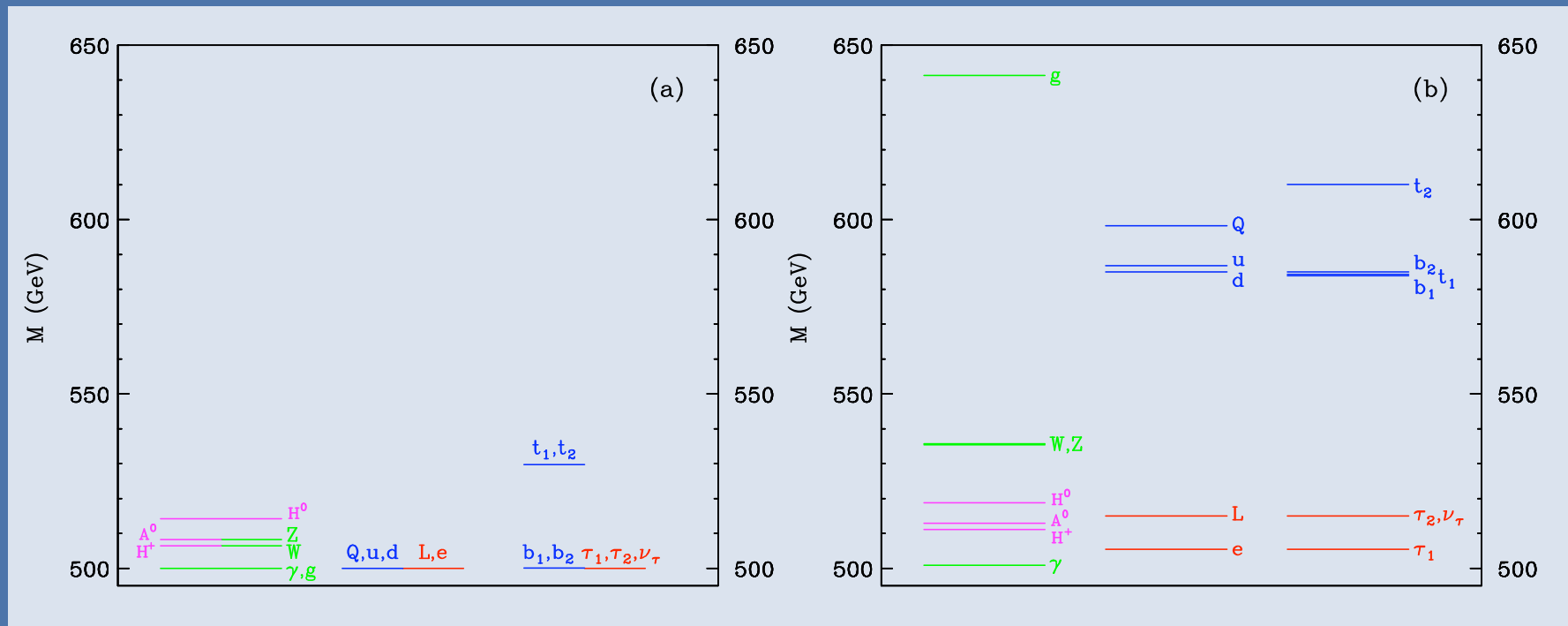
## RG-running

1. KK photon -0.2%
2. KK gluon +30%
3. KK quarks +14%
4. KK leptons +1%

# MUED-Spectra

Free parameter:  $(1/R, \Lambda)$

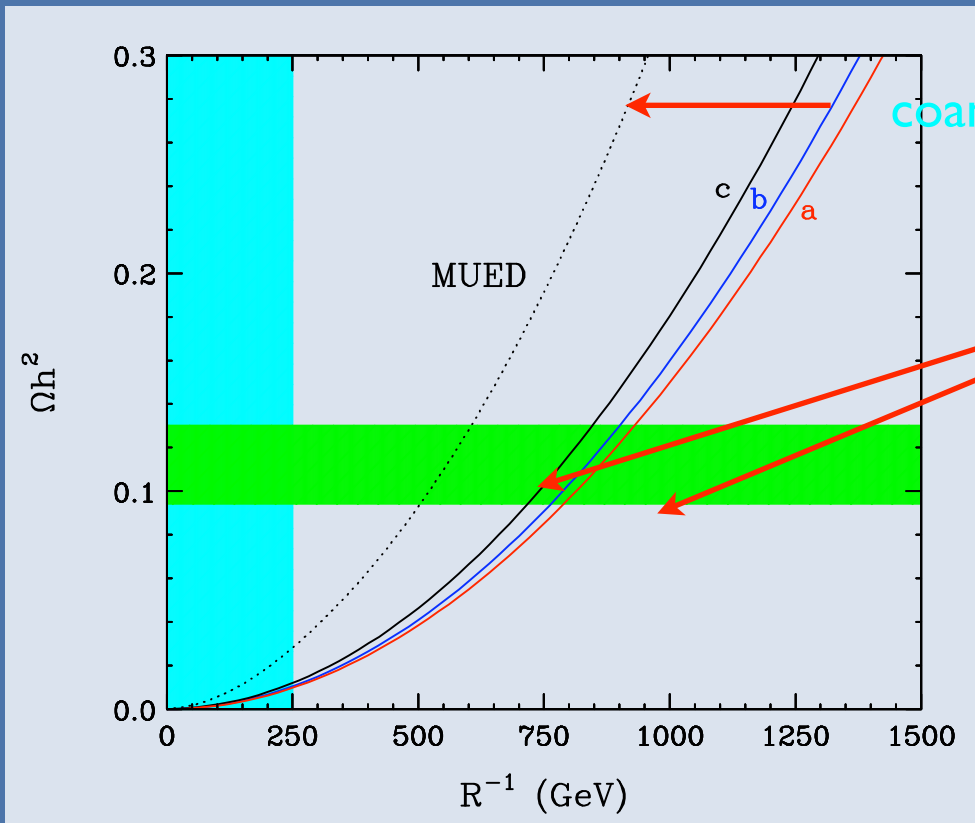
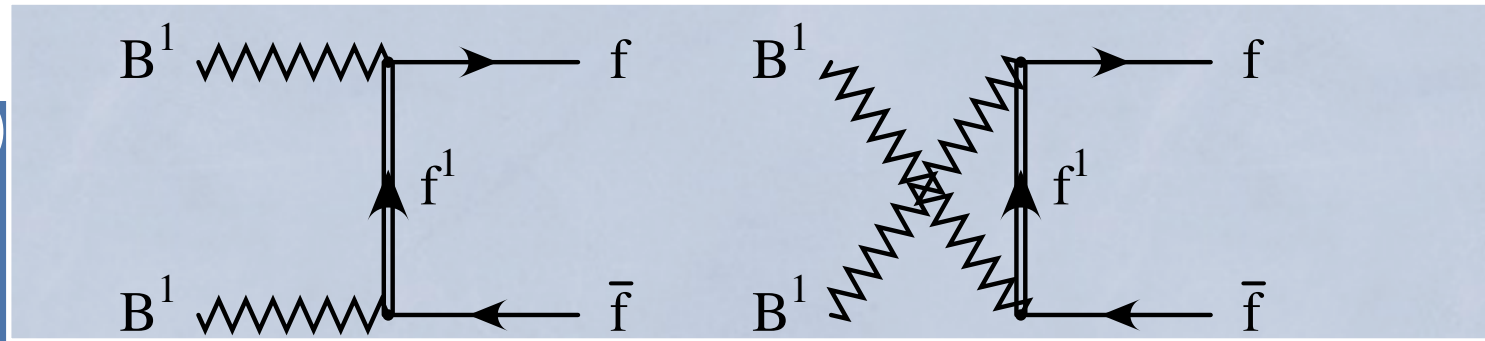
Tree level mass spectra, very degenerate      With radiative corrections, quasi-degenerate



H-C. Cheng, K. Matchev, M. Schmaltz, Phys. Rev. D 66, 036005 (2002)



# DM in MUED



It naturally **predicts**  
the LKP mass around  
**600 ~ 800 GeV**

Coincident with  
the ATIC peak!

K. Kong, K. Matchev, JHEP 0601:038, (2006)

# DM in MUED

$$\langle \sigma v \rangle_{B_1 B_1 \rightarrow f \bar{f}} \simeq \frac{2g_1^4 C_f}{9\pi m_{B_1}^2} \frac{1}{(1 + r_f^2)^2}$$

$$C_f = N_c Y_f^4 \quad r_f = \frac{m_f}{m_{B_1}}$$

$$l_R : q_R = 1^4 : 3 \times (2/3)^4 = 1 : 16/27$$

• Slightly hadrophobic (~40%)

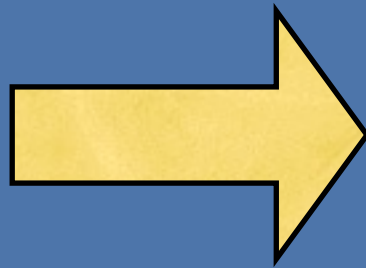
• but still hadronic BF is sizable

We need to  
suppress it!

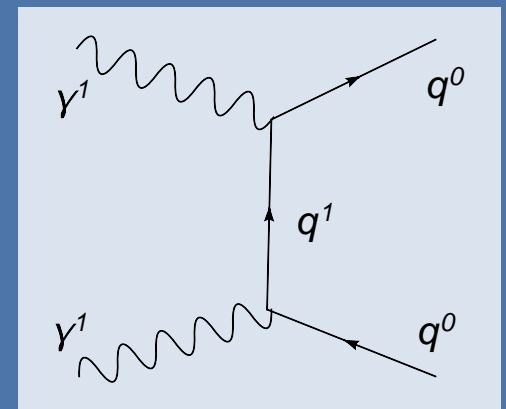
# Solution.....

A obvious solution.....

Increase the  
mass of  $q^1$



suppress



In the NR limit,

$$\langle \sigma v \rangle_{q\bar{q}} \propto m_{\gamma^1}^2 / (m_{\gamma^1}^2 + m_{q^1}^2)^2$$

We need a **self-consistent way to increase the KK quark masses while preserve the KK parity!**

# Model

One way to increase the KK fermion mass is to introduce the 5D bulk fermion mass  $\mu$ .

$$\text{In flat space, } m_n = \sqrt{\mu^2 + k_n^2}$$

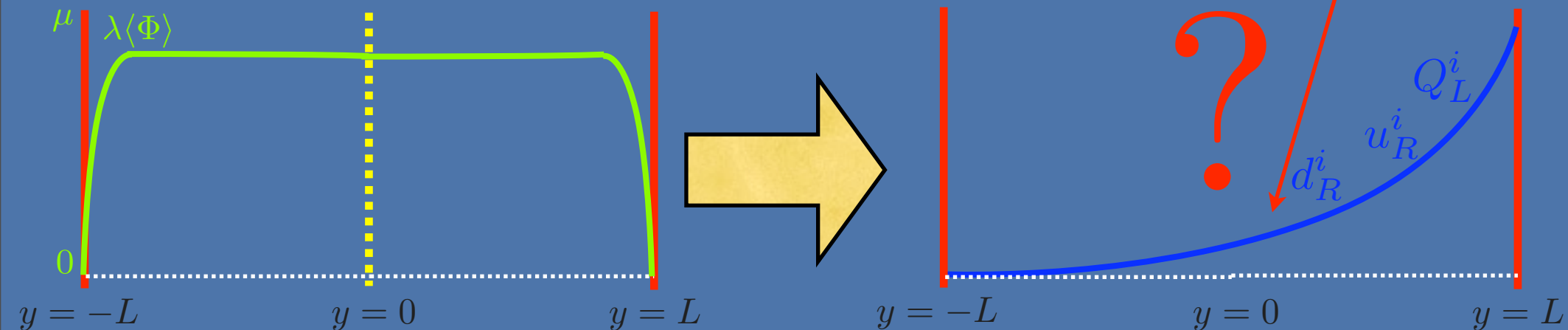
However, a conventional 5D bulk mass will

**violate** the KK parity

**No inversion symmetry**

5D bulk mass

SM zero mode



# KK parity in ED

I start with -L not 0 here.

For a general 5D Lagrangian in the orbifolds  $y \in [-L, L]$

$$\Phi(x, y) \rightarrow \pm \Phi(x, -y)$$

only "+" if there is a cubic term

$$\Psi(x, -y) \rightarrow \pm \gamma_5 \Psi(x, y)$$

depends on how one emded the zero mode fermion

$$\Psi_+(y) \rightarrow \pm \Psi_+(-y)$$

$$\Psi_-(y) \rightarrow \mp \Psi_-(-y)$$

For the interaction with fermions

$$S = \int d^5x \left( \frac{i}{2} (\bar{\Psi} \Gamma^M \partial_M \Psi - \partial_M \bar{\Psi} \Gamma^M \Psi) - \lambda \Phi(y) \bar{\Psi} \Psi \right)$$

$$\Phi(y) (\bar{\Psi}_+ \Psi_- + \bar{\Psi}_- \Psi_+)$$



$$\Phi(y) = -\Phi(-y)$$

# KK decomposition

K. Agashe, A. Falkowski, I. Low, G. Servant, JHEP 0804:027, (2008)

Consider SM quark is embedded in the “+” component:

$$\Psi_+(x, y) = \sum_n g_n(y) \chi_n(x) \quad \text{5D KK “+” parity}$$

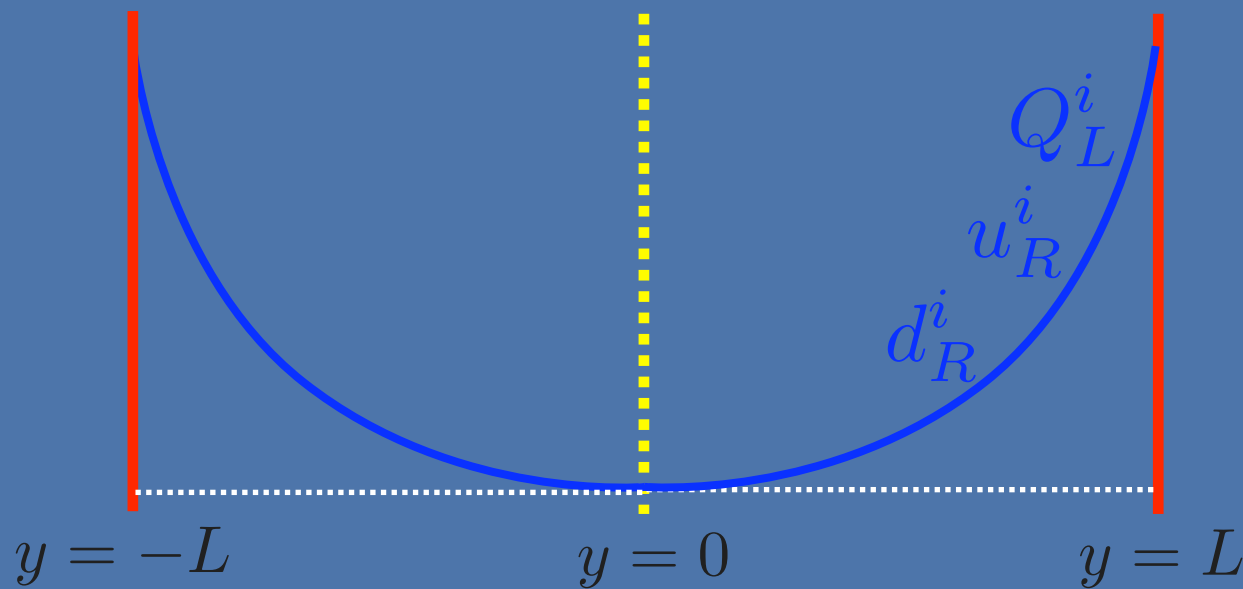
$$\Psi_-(x, y) = \sum_n f_n(y) \psi_n(x) \quad \text{5D KK “-” parity}$$

For the 4D KK even/odd field  $\chi_n(x)$ ,  $g_n(y)$  must be symmetric/asymmetric around  $y=0$ , which satisfy the +/- boundary condition.

The 5D profile with even/odd KK parity in the interval  $-L$  to  $L$  is the same as the one with +/- boundary condition at  $y=0$ .

# The set-up

Theoretical considerations suggest that SM quarks are localized at the **boundary**, not the center.

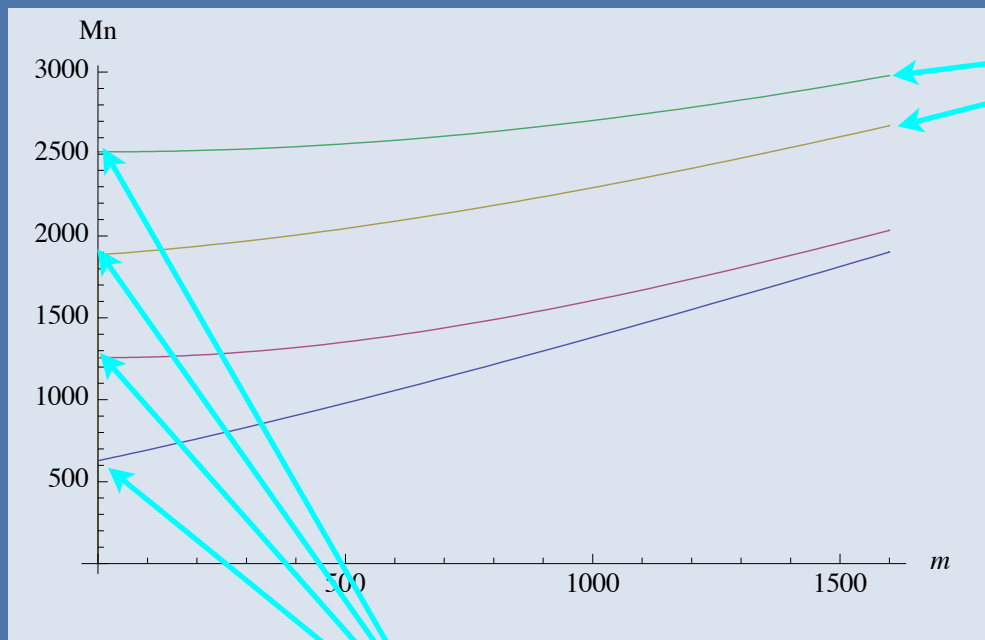


No light mode!

5D anomaly free!

# The masses

In case  $\mu > 0$



$m=0$ , the same as MUED!

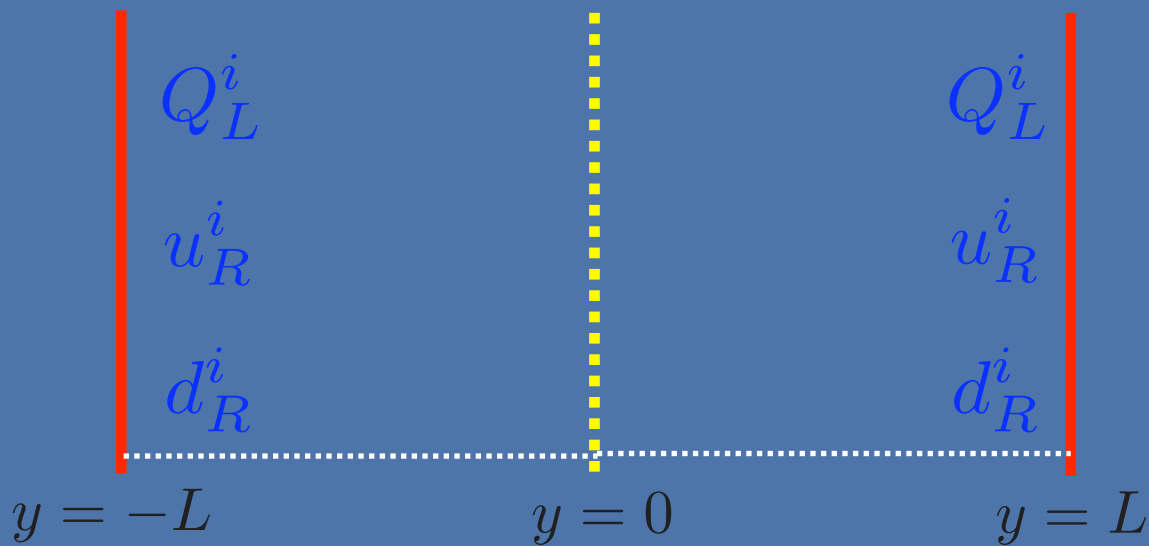
For large negative mass  $m$ , the  $n$ th KK odd and even quarks tend to be degenerate.

For very large negative mass  $m$ , the KK quark mass could be decoupled!



# The “well localized” case

$$\mu \rightarrow +\infty$$

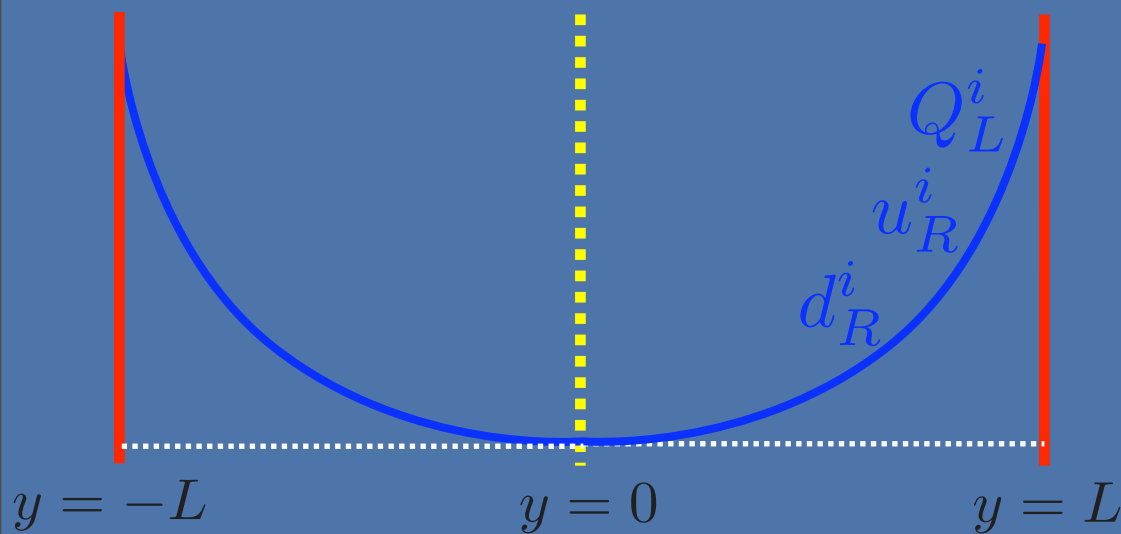


No KK quarks!

$$\frac{g_{200}}{g_0} = \sqrt{2} \mathcal{F}_{2n}(x) = \sqrt{2} \frac{2x}{1 - e^{2x}} \int_0^1 ds e^{2xs} \cos(\pi ns) \rightarrow \sqrt{2}$$

# Violation of KK #

5D translational invariance is violated  
by the bulk profile



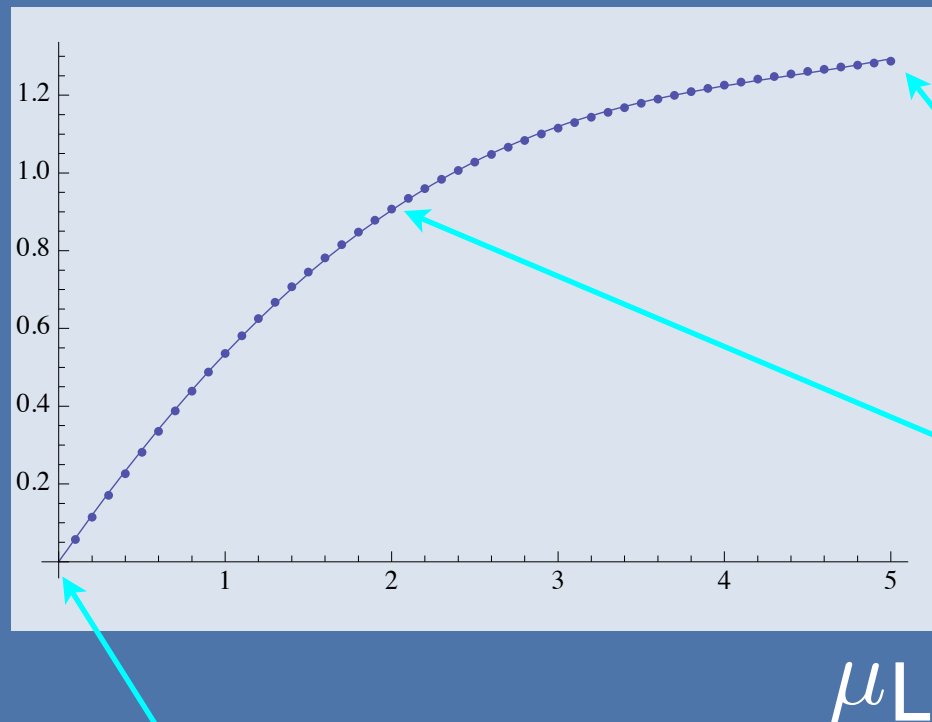
KK # violation at  
the tree level!

KK even gauge bosons/scalars  
directly coupled to quarks!

# The couplings

$g_{200}/g_0$

Coupling that violate KK number



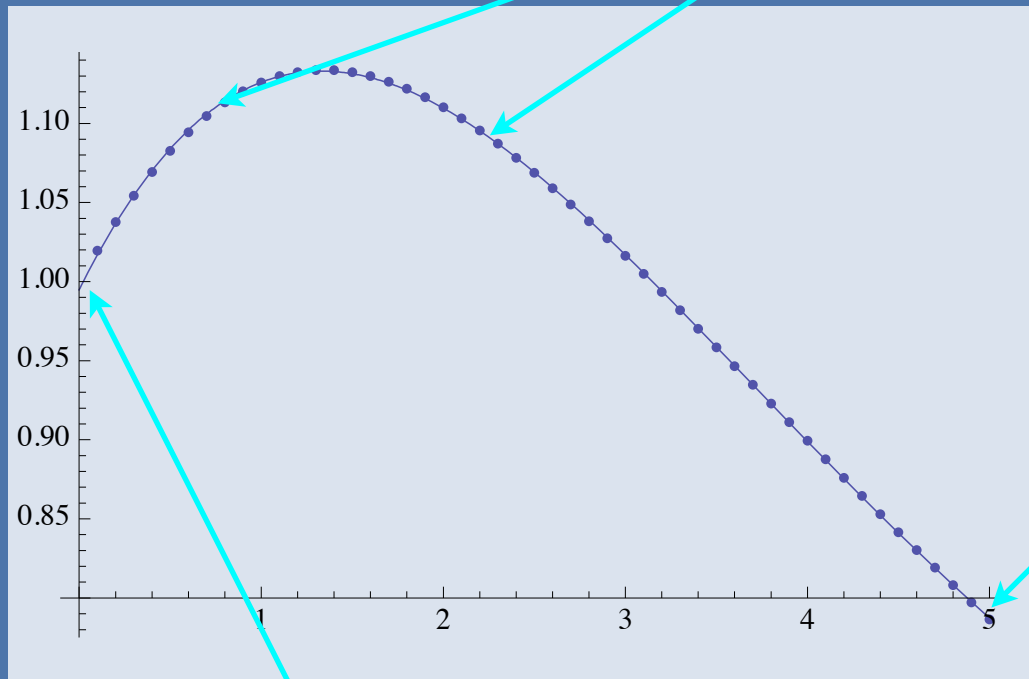
saturated to 1.4142.....

always increases

$m=0$ , KK# conservation as  
in MUED!

# The couplings

$g_{||0}/g_0$



coupling first increases,  
then decreases!

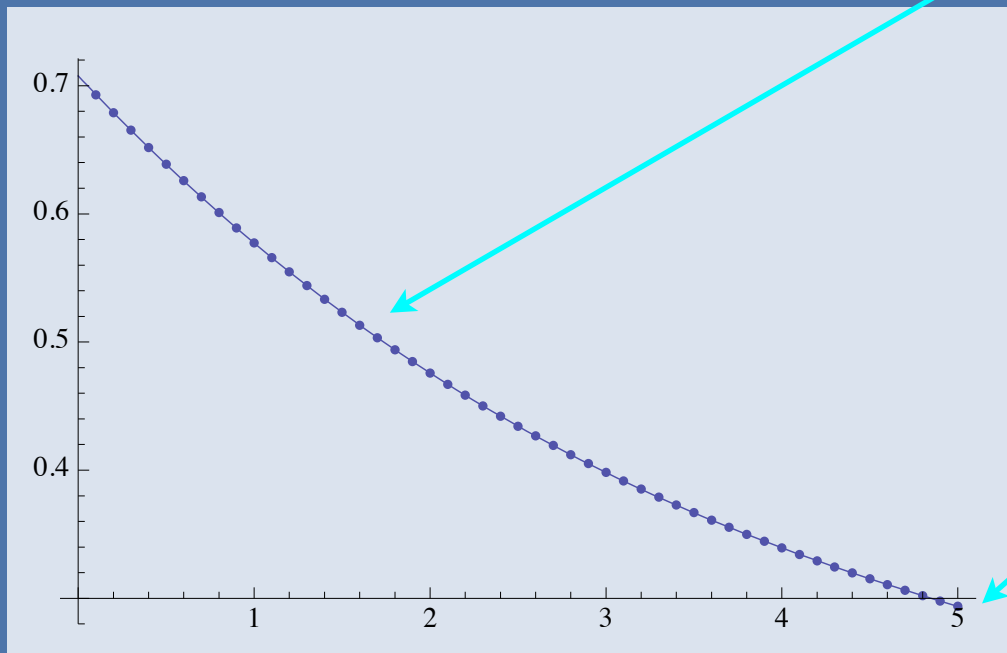
decreases to zero

$m=0$ , the same as the zero  
mode coupling

$\mu_L$

# The couplings

$g_{211}/g_0$



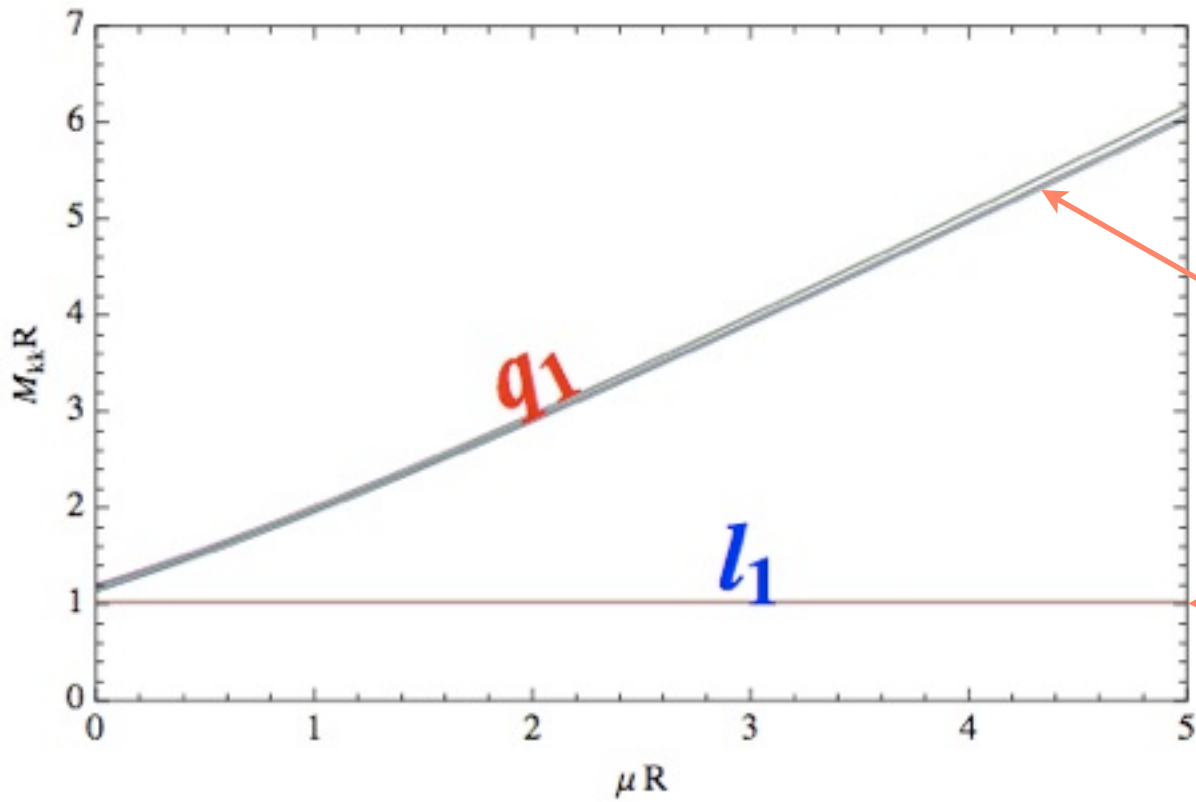
coupling always decreases!

decreases to zero

$\mu_L$

# Split-Mass spectrum

Consider the one-loop radiative corrections:



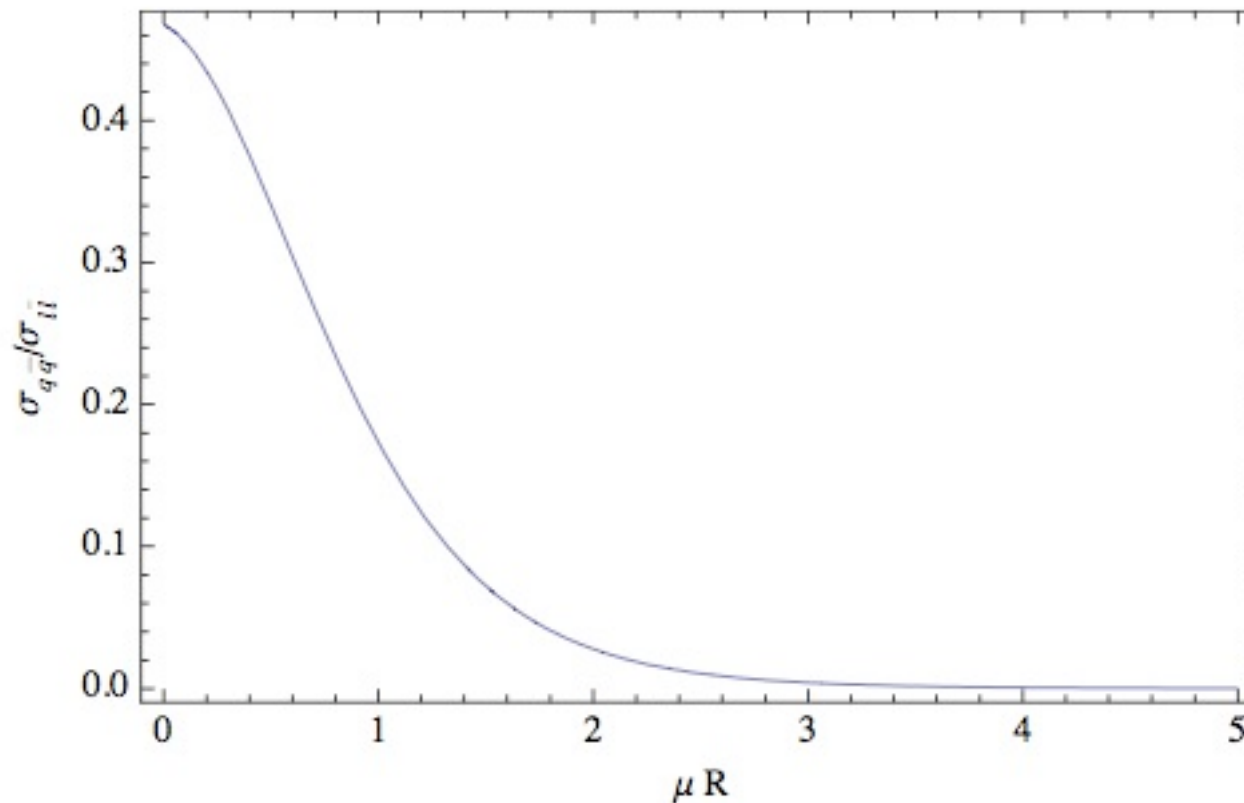
$$\lambda_q \langle \Phi(y) \rangle = \mu \epsilon(y)$$

$$m_n^2 = \mu^2 + k_n^2$$

$$m_n^2(\text{lepton}) = \frac{n^2}{R^2}$$

# Branching Fraction

$$\frac{\sigma_{qq}}{\sigma_{ll}} = \frac{\sum_q Y_q^4}{\sum_l Y_l^4} \left( \frac{m_{B_1}^2 + m_{l_1}^2}{m_{B_1}^2 + m_{q_1}^2} \right)^2 \simeq 0.42 \times \left( 1 + m_{q_1}^2 / m_{B_1}^2 \right)^{-2}$$



Chen, Nojiri, Park, JS, Takeuchi, arXiv:0903.1971

# Branching Fraction

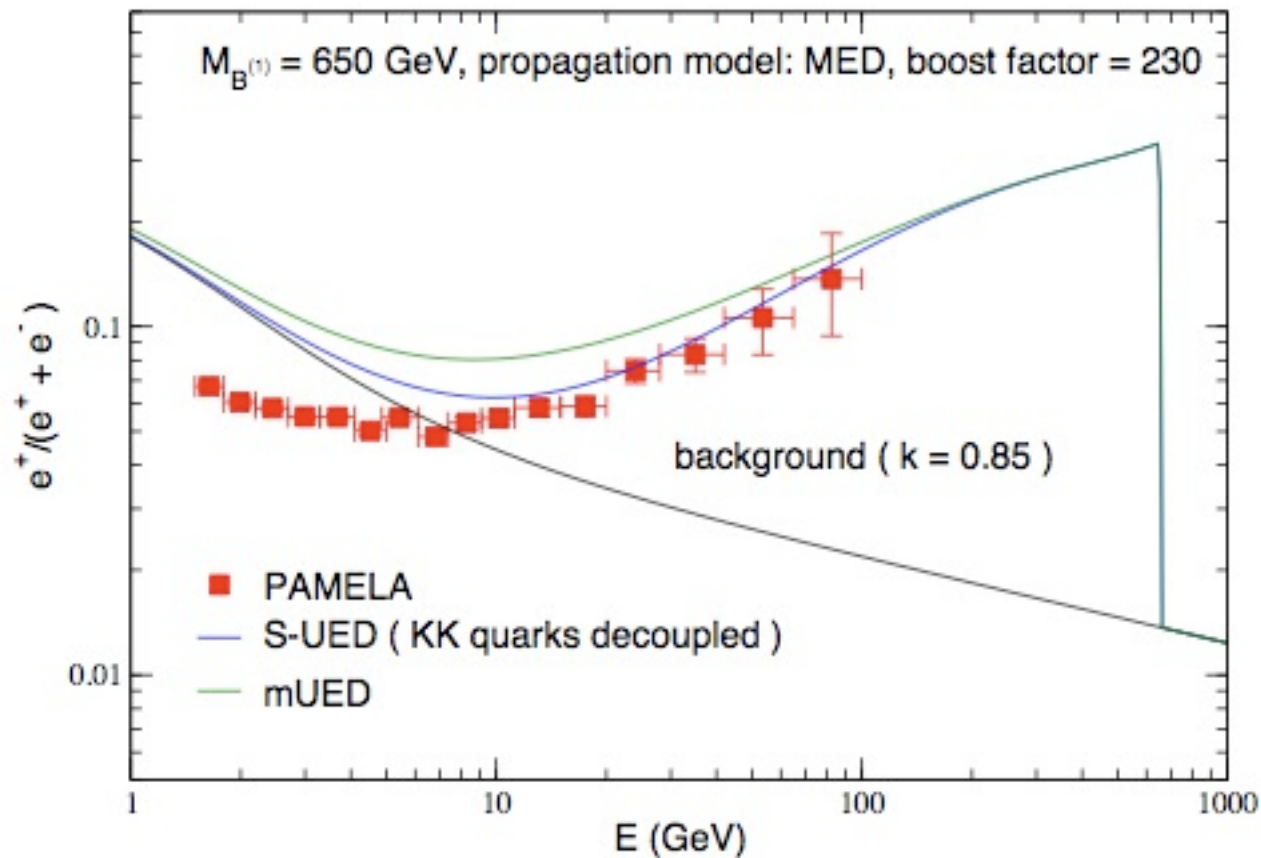
All possible branching fractions:

$\mu$ (GeV)	0	200	400	600	800	1000
$M_{q_1}$ (GeV)	713	863	1026	1198	1378	1566
$\text{BR}(B_1 B_1 \rightarrow q\bar{q})$	29.4%	26.4%	20.6%	14.3%	8.9%	5.2%
$\text{BR}(B_1 B_1 \rightarrow l\bar{l})$	64.3%	67.1%	72.3%	78.2%	83.0%	86.5%
$\text{BR}(B_1 B_1 \rightarrow \nu\bar{\nu})$	3.8%	3.9%	4.3%	4.6 %	4.9%	5.1%
$\text{BR}(B_1 B_1 \rightarrow \phi\phi^*)$	2.3%	2.4%	2.6%	2.8%	3.0%	3.1%

Chen, Nojiri, Park, JS, Takeuchi, arXiv:0903.1971

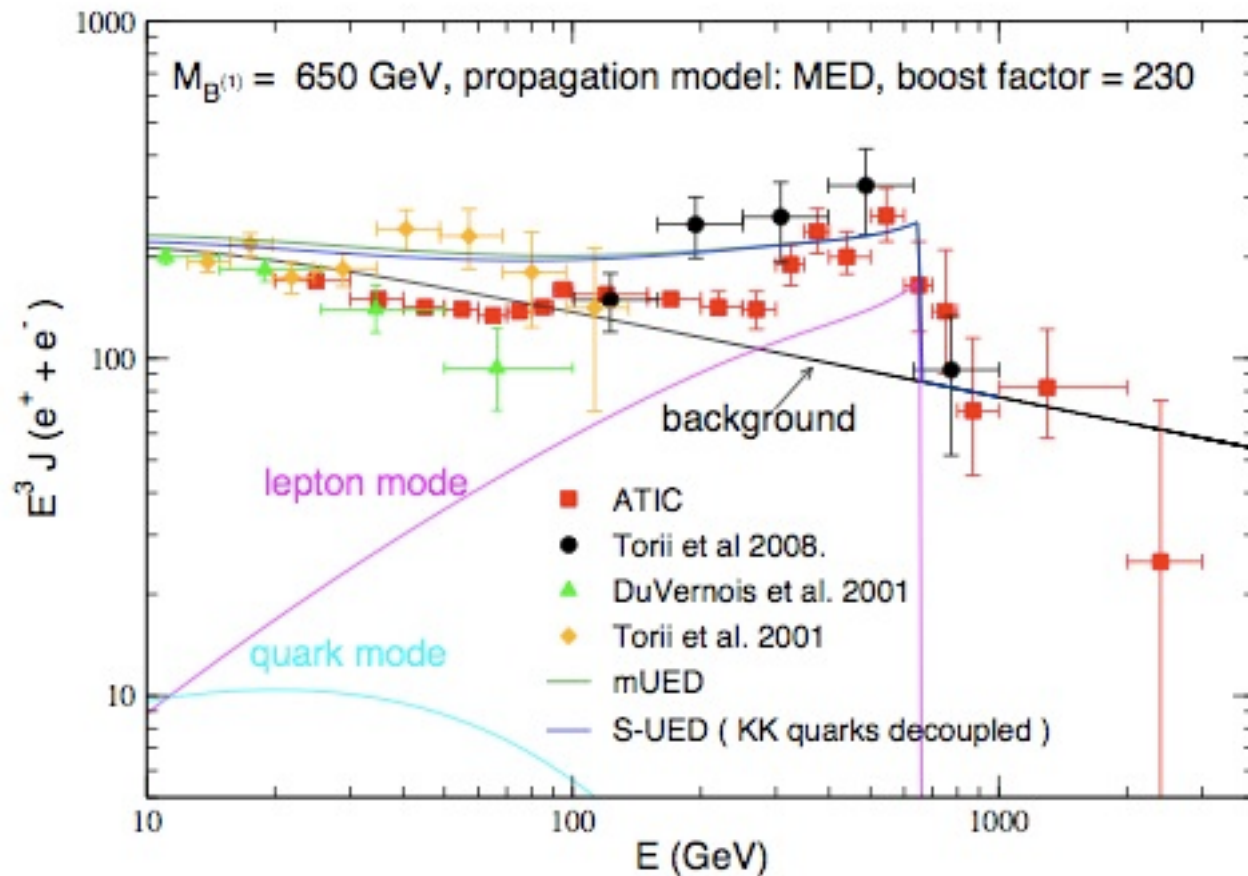


# Fitting PAMELA Positron



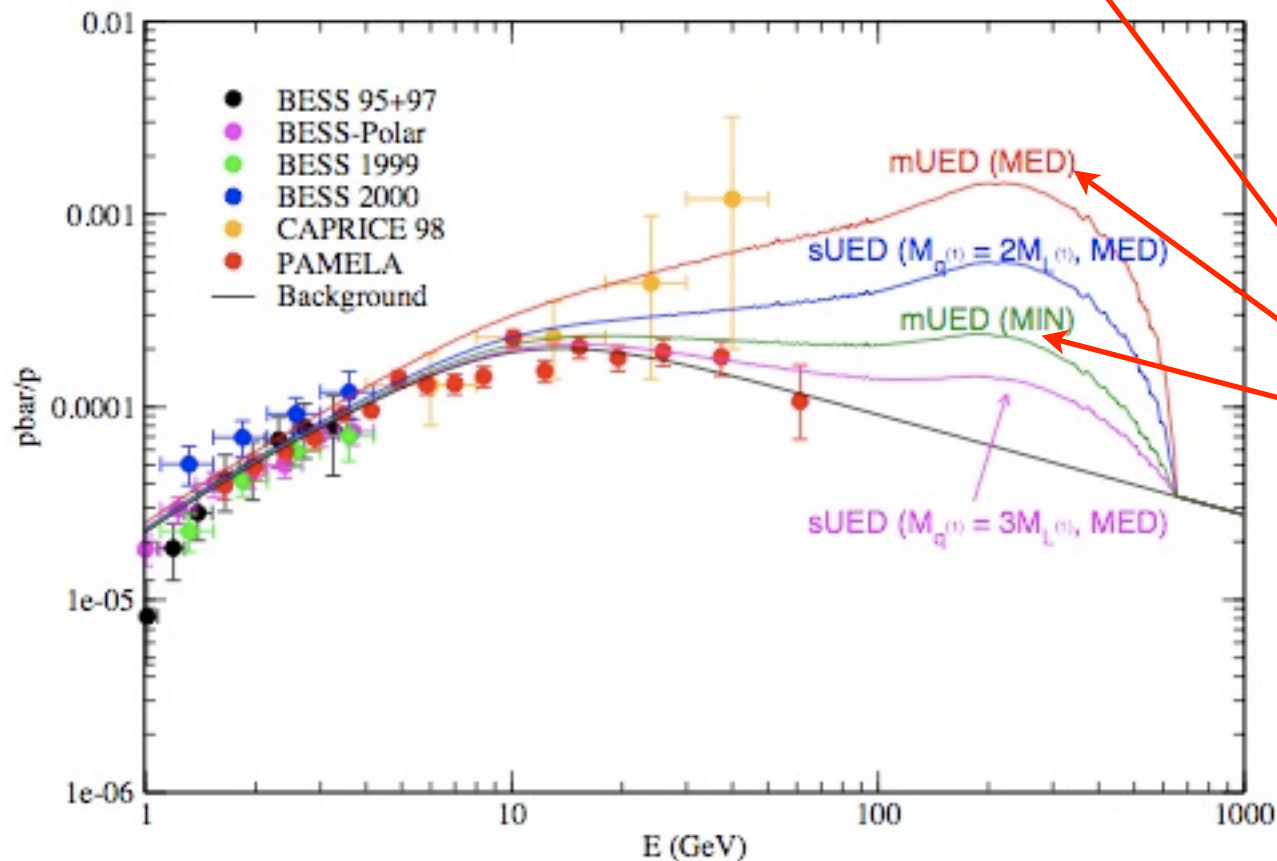
Chen, Nojiri, Park, JS, Takeuchi, arXiv:0903.1971

# Fitting ATIC/PPB-BETS



Chen, Nojiri, Park, JS, Takeuchi, arXiv:0903.1971

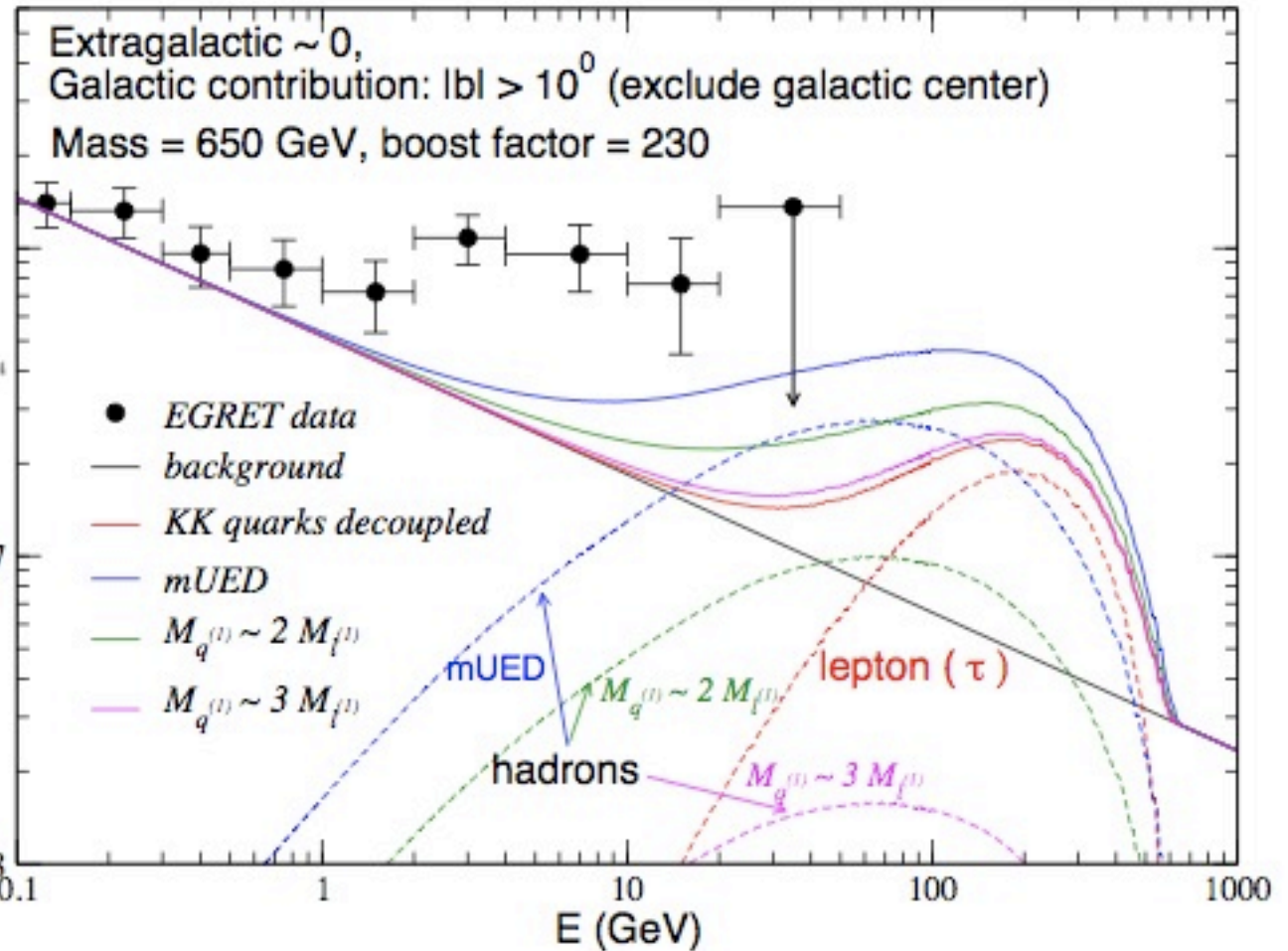
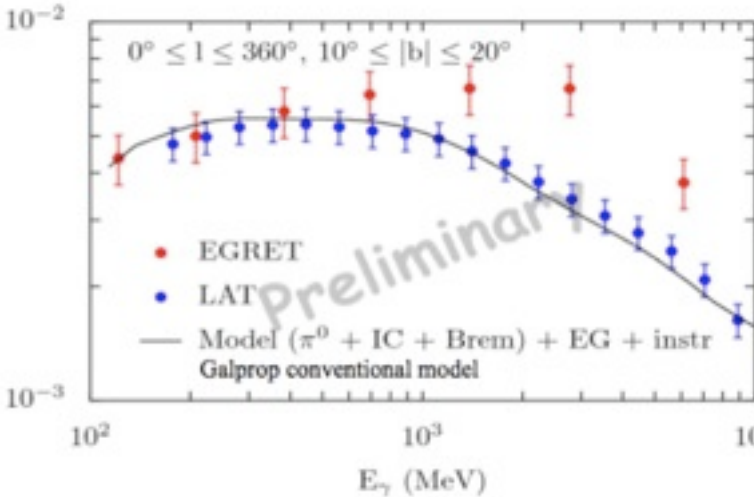
# No Anti-Protons



The results, however, is very sensitive to the propagation model.

Change propagation model from MAX to MIN will increase the anti proton flux by **2 orders of magnitude!**

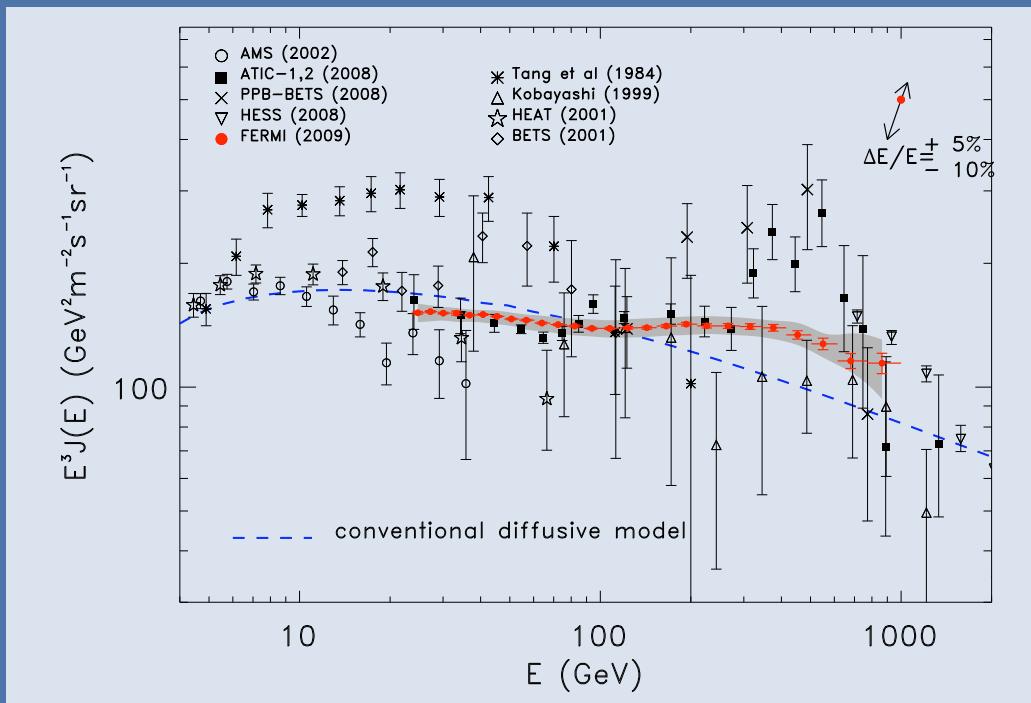
# Gamma Rays



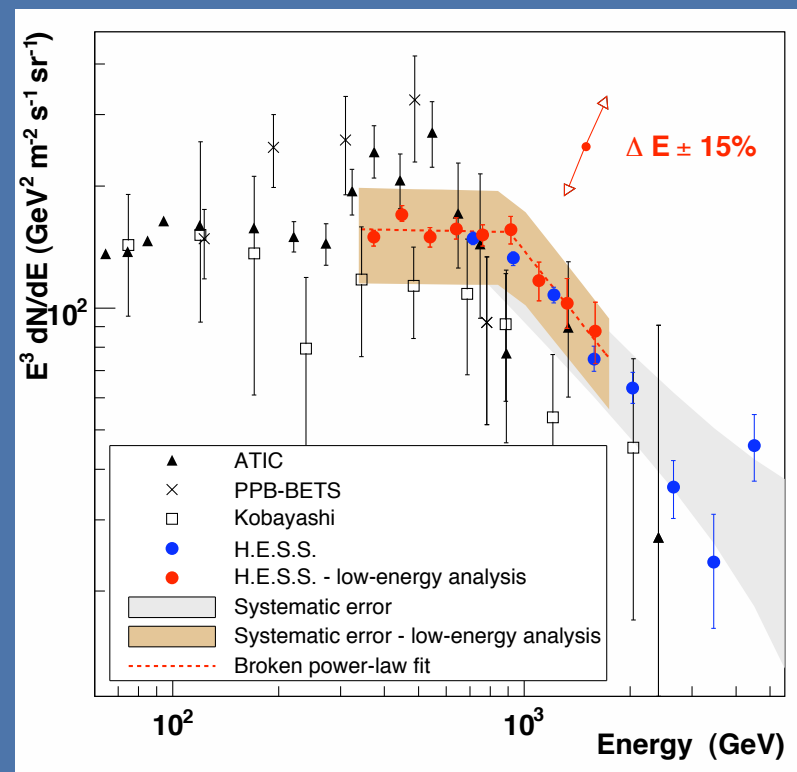
The gamma rays, however, is independent of the propagation model.

# KK DM after FERMI

We may have to explain it and  
Split-UED can explain it!



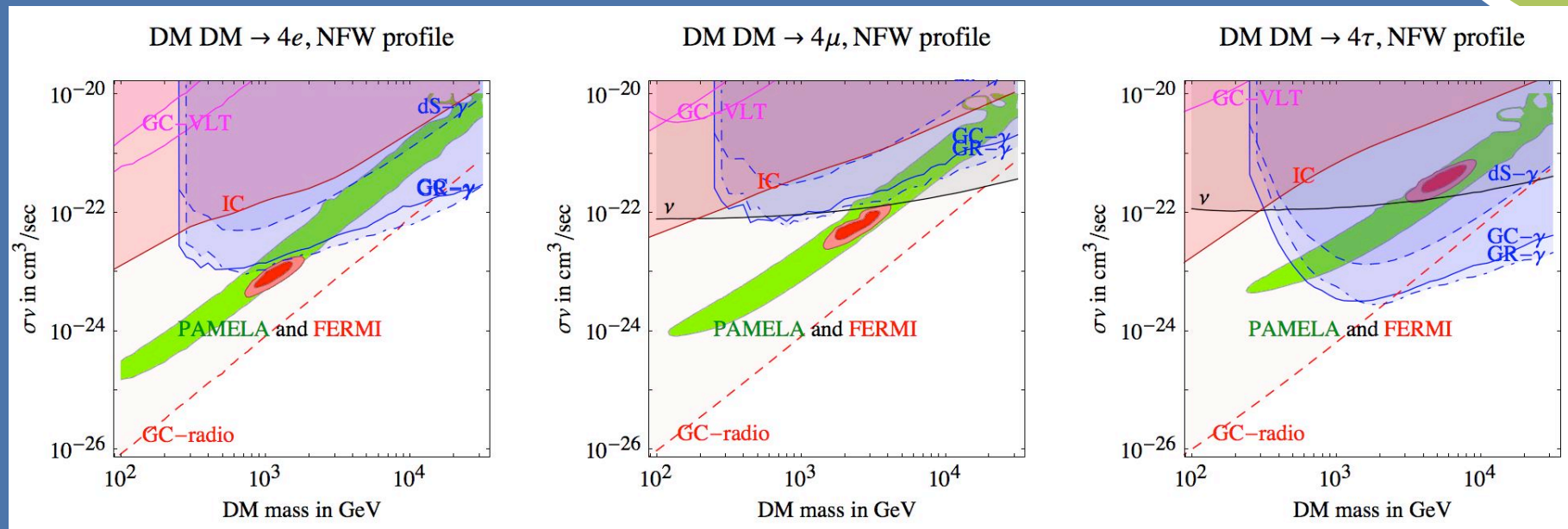
FERMI LAT, arXiv:0905.0025



HESS, arXiv:0905.0105

# KK DM after FERMI

## NFW profile



P. Meade, M. Papucci, A. Strumia, T. Volansky, arXiv:0905.0480

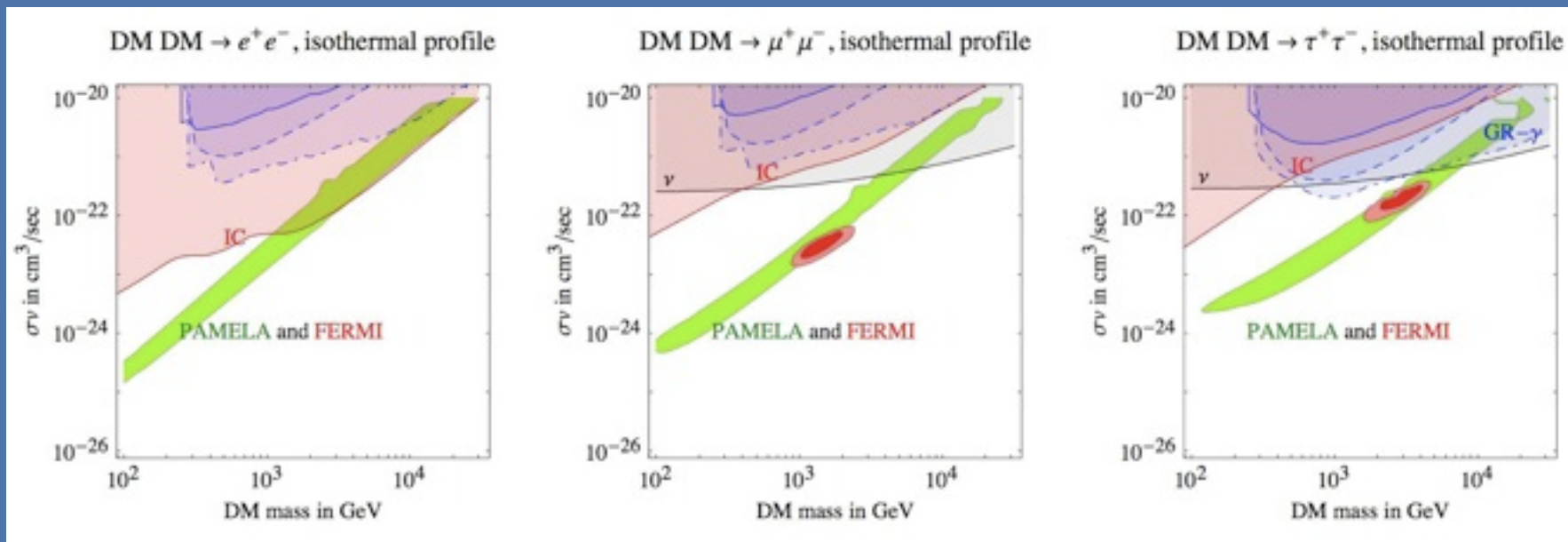
Pure annihilation into  **$e^-/e^+$**  is ruled out.

In direct leptonic annihilation scenario, the gamma ray flux at the GC is highly constrain



# KK DM after FERMI

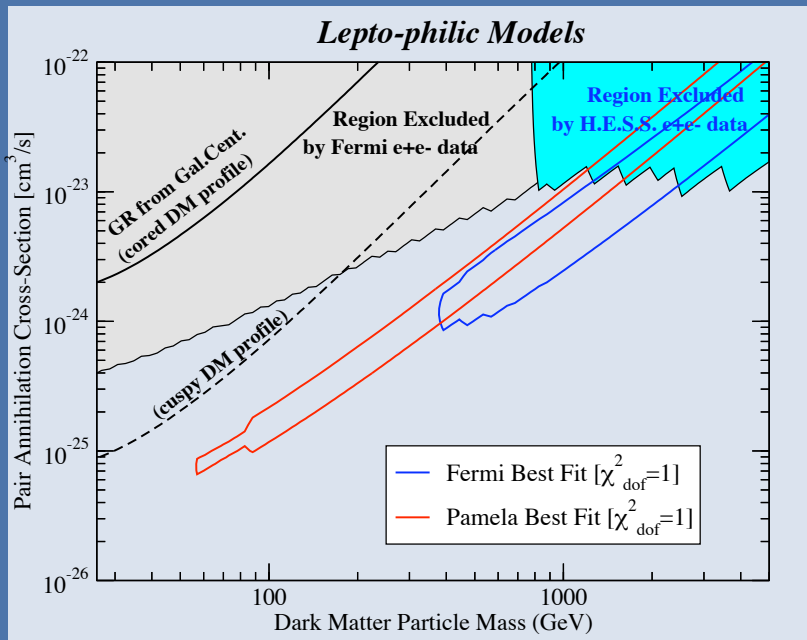
## Isothermal profile



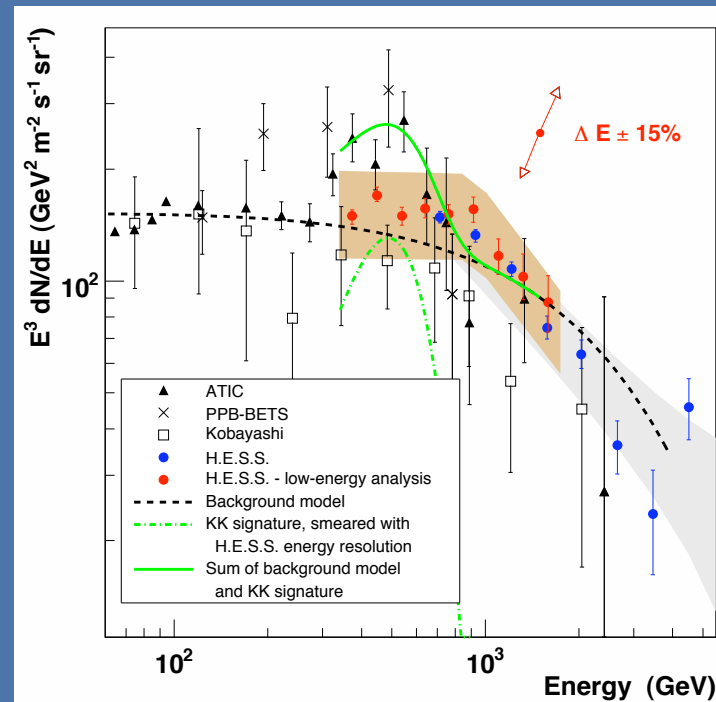
P. Meade, M. Papucci, A. Strumia, T. Volansky, arXiv:0905.0480

It can only work in the DM profiles which is rather **flat at GC**.

# KK DM after FERMI



FERMI LAT, arXiv:0905.0636



HESS, arXiv:0905.0105

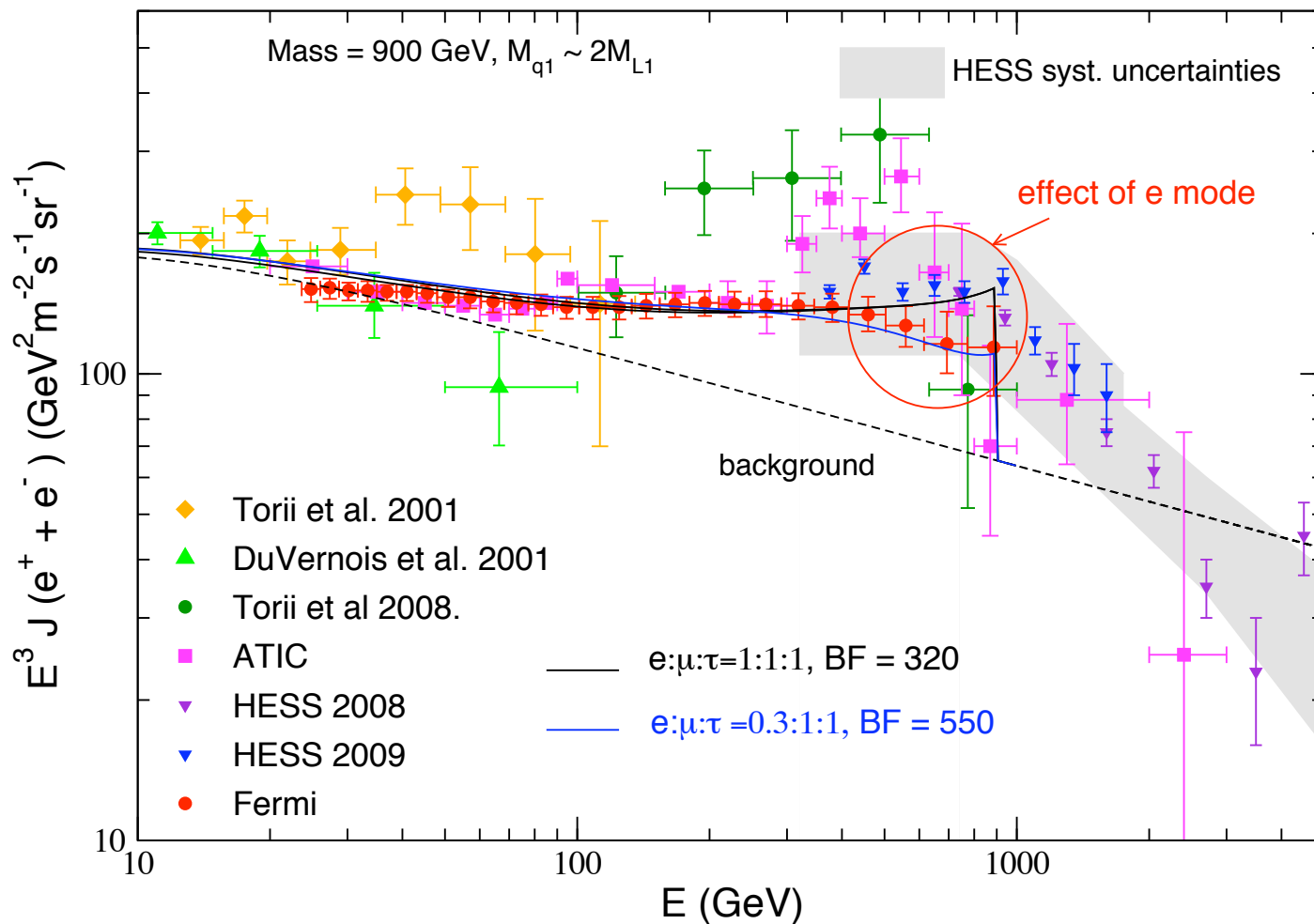
Annihilation into charged lepton families **1:1:1** can explain FERMI

KK DM with 620GeV ruled out?

So misleading, what they claimed ruled out 99% is the **KK model** used to explain ATIC.



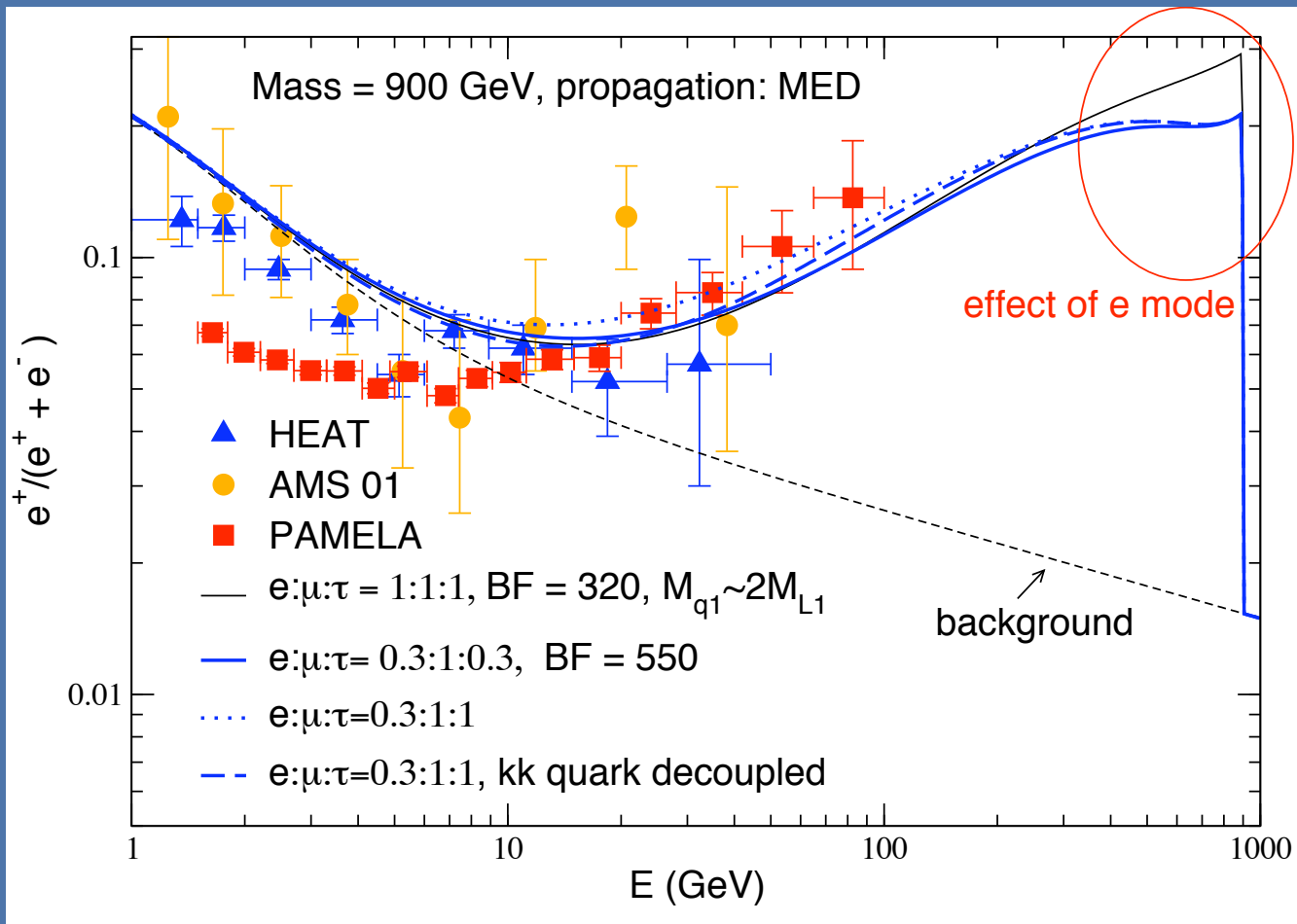
# KK DM after FERMI



Can not split  
too much for  
e- boz of LEP  
bounds

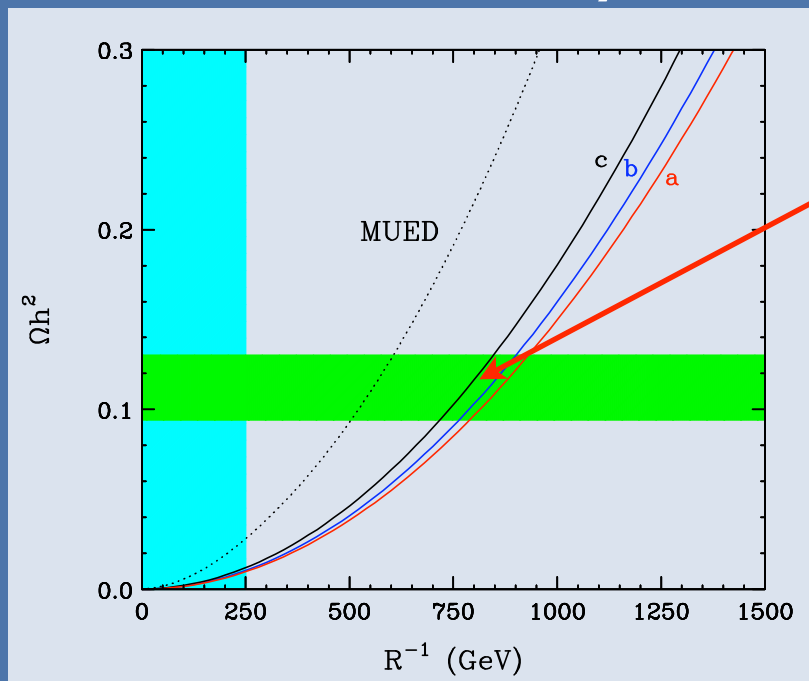
But enough to  
fit the data  
very well.

# KK DM after FERMI



# KK DM after FERMI

The relics density can work



no coannihilation

Mass around 800~900GeV

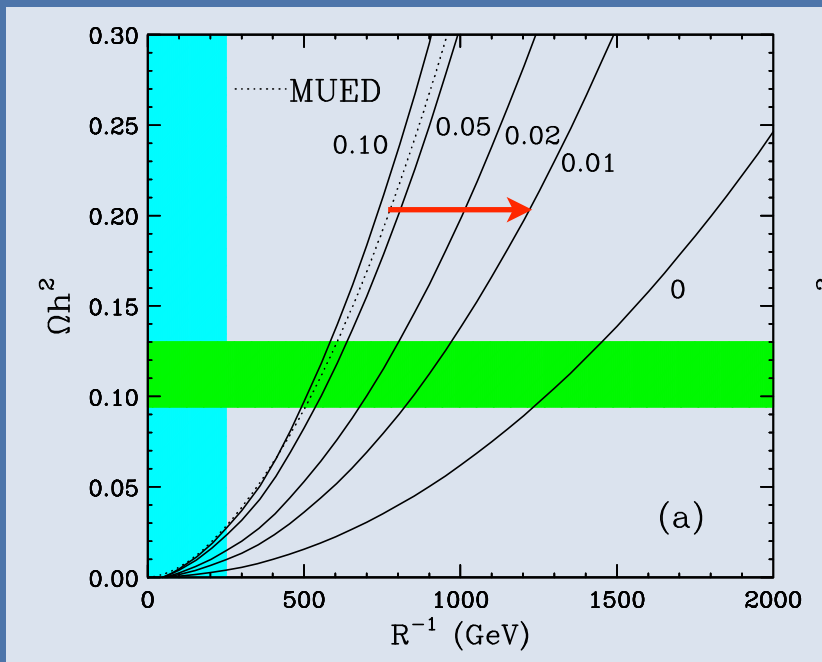
GOOD for FERMI

K. Kong, K. Matchev, JHEP 0601:038, (2006)

A small bulk mass for leptons will remove the coannihilation from the charged leptons

# KK DM after FERMI

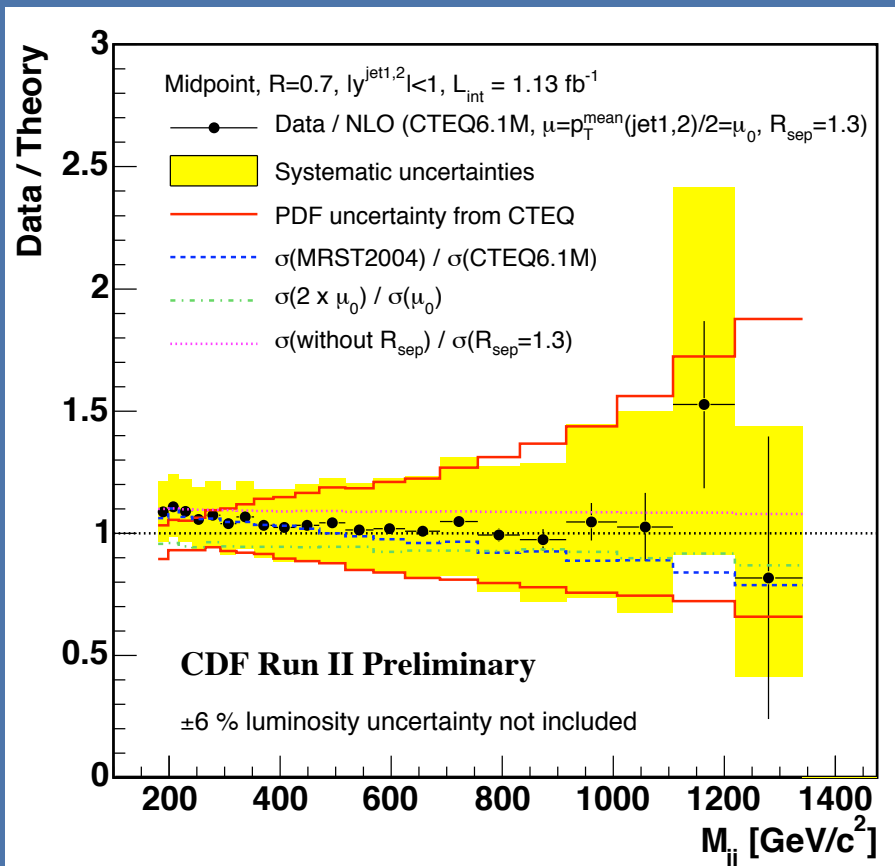
If one wants even more massive DM, coannihilation from EW gauge bosons can make it work



Quite degenerate BI, ZI, WI,  
novel signal at the LHC

K. Kong, K. Matchev, JHEP 0601:038, (2006)

# Bounds from Tevatron

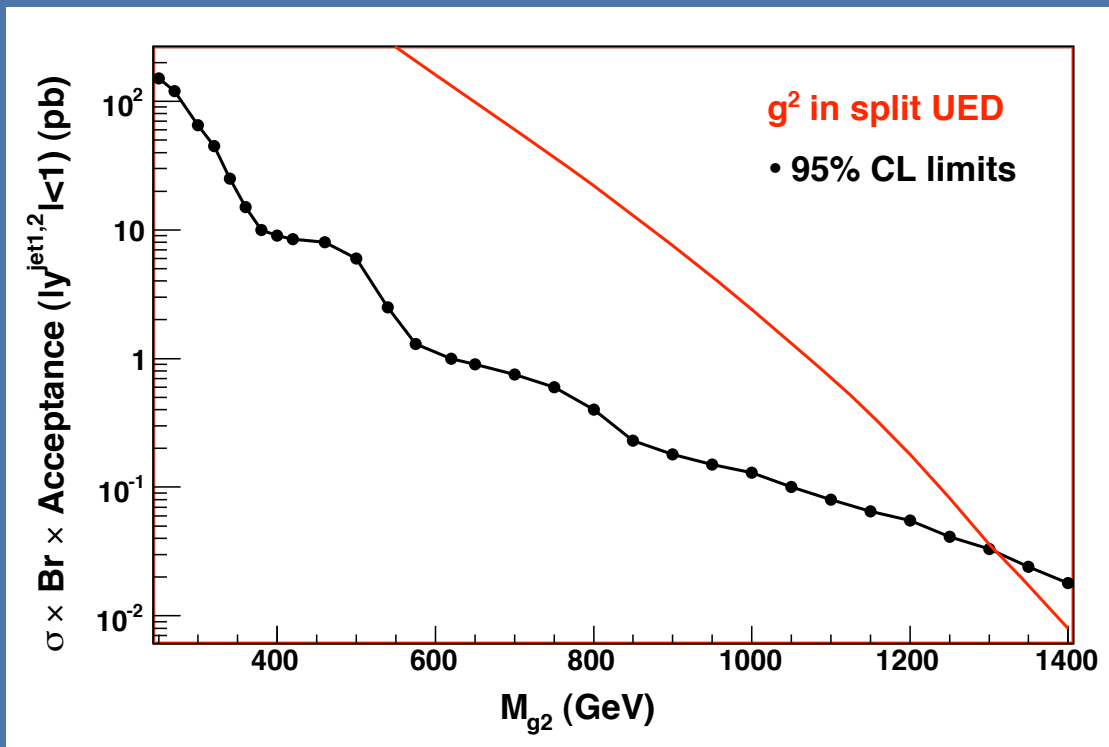


The most stringent bound is from four quark interactions.

The bound is loose due to the large uncertainties in high invariant mass

CDF notes 9246

# Bounds from Tevatron



$$M_{g^2} > 1.3 \text{ TeV}$$

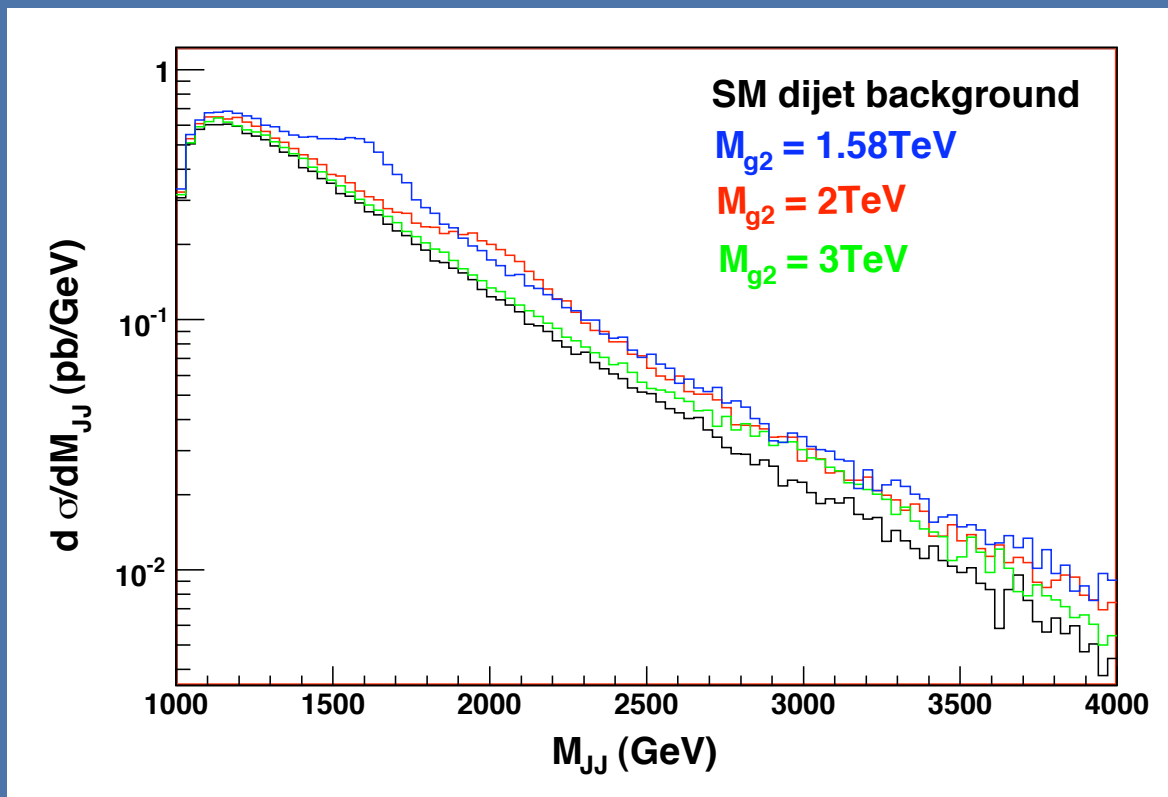
$$\frac{1}{R} > 510 \text{ GeV}$$

OK for ATIC  
and FERMI

CDF notes 9246

# LHC resonances

At LHC, the even KK gauge bosons (gluons) are copiously produced.



Cuts:  $|\eta| < 2.5$   
 $p_T > 500$  GeV

$p_{\text{QCD}}$  is reliable

# Discovery

Broad resonances

At the **early stage**,  
up to **4 TeV**

Full LHC running  
time, more than  
**6 TeV**

$M_{g2}$ (TeV)	1.58	2	3	4	5	6
$\Gamma_{g2}$ (GeV)	270	334	482	627	769	909
$S/\sqrt{B}$ (100 pb <sup>-1</sup> )	66.5	38.2	11.9	4.3	—	—
$S/\sqrt{B}$ (100 fb <sup>-1</sup> )	2103	1208	376	137	86	22



# MET search.....

In MUED, the MET + jets is hopeless because the jets are so soft.

Standard search with well studied background

In sUED, the jets from KK quark decay are **very hard**.

Mass reconstruction in MET + jets is possible.

Kinematic here is independent of spin, we rescale the SUSY events with the same spectra.

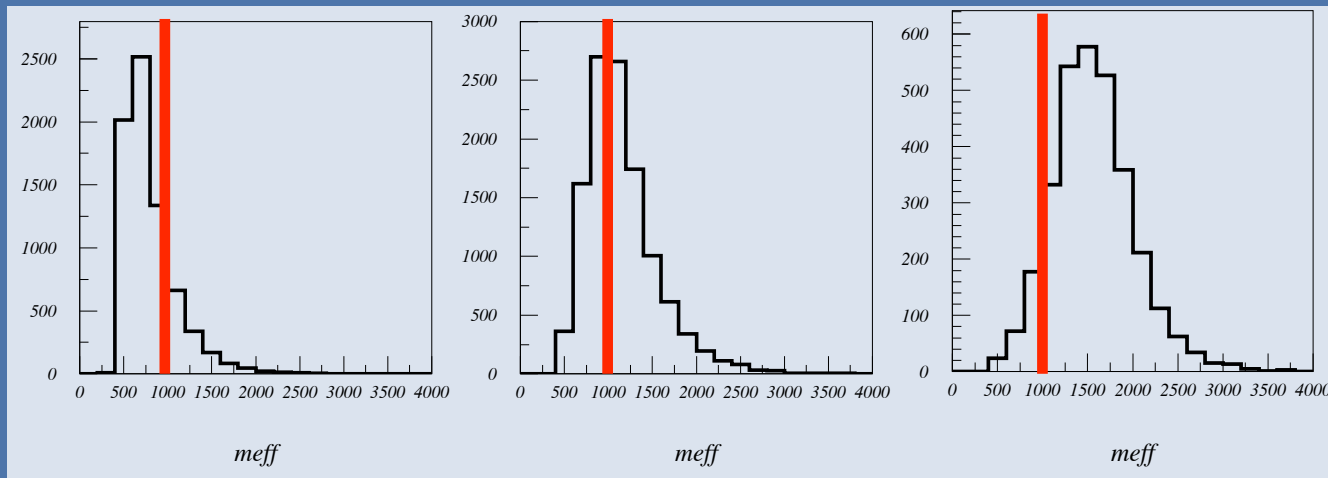
**Big Cross** section for **fermion** pair production.

SUED		SUSY	
$q_{L1}$	1347 GeV	$\tilde{u}_L, \tilde{d}_L$	1355, 1358
$u_{R1}$	1322	$\tilde{u}_R$	1304
$d_{R1}$	1318	$\tilde{d}_R$	1263
$g_1$	794	$\tilde{g}$	799
$A_1$	621	$\tilde{\chi}_1^0$	622

# MET search.....

We consider the KK quark pair production.....

HERWIG + ACERJET



$\tilde{g}\tilde{g}$

$\tilde{g}\tilde{q}$

$\tilde{q}\tilde{q}$

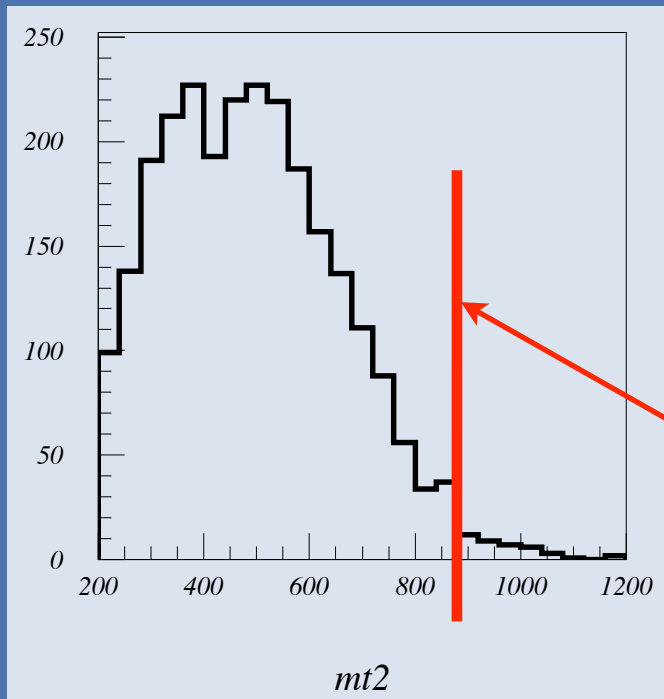
$m_{eff}$  cuts ( $> 1$  TeV) easily select the KK quark events

scalar sum of the leading jets and  $p_{Tmiss}$

# MT2

For 2 leading jets + MET

$$M_{T2} = \min_{p_{Tmiss} = p_1^T + p_2^T} [\max(M_T(p_1, p_{j_1}) M_T(p_2, p_{j_2}))]$$



$p_1, p_2$  are the test invisible particle momenta that make up  $p_{Tmiss}$ .

For  $A \rightarrow Xq$

$$M_{T2}^{end} = m_A - \frac{m_X^2}{m_A}$$

For  $q_1 \rightarrow g_1q$

$$M_{T2}^{end} \approx 882 \text{ GeV}$$

Confirm the theoretical  $g_1$  masses.

More physics has to be done in this direction!

# Summary

- We build the double kink mass background to localize the SM fermions while preserve the KK parity.
- It explains all the cosmic ray excesses.
- The model violate the KK # at the tree level in the quark sector, one can discover 2nd KK gauge bosons at LHC.
- Mass reconstruction is possible through MET + mutijets.

# Some clarification!

The model here is **NOT** nothing but a model lies in the parameter space of origin UED with BLK.

- The BLK will only **decrease** the KK masses, so one can **never decouple the KK modes** (KK quarks) in the theory.
- BLK will never affect the **zero mode**, so one can **never localize** the SM fermions.
- One can explain the flavor hierarchy in flat space with KK parity.

Reproduce some kind of RS behavior if higgs at the enter

Csaki, Heinonen, Park, JS, work in progress

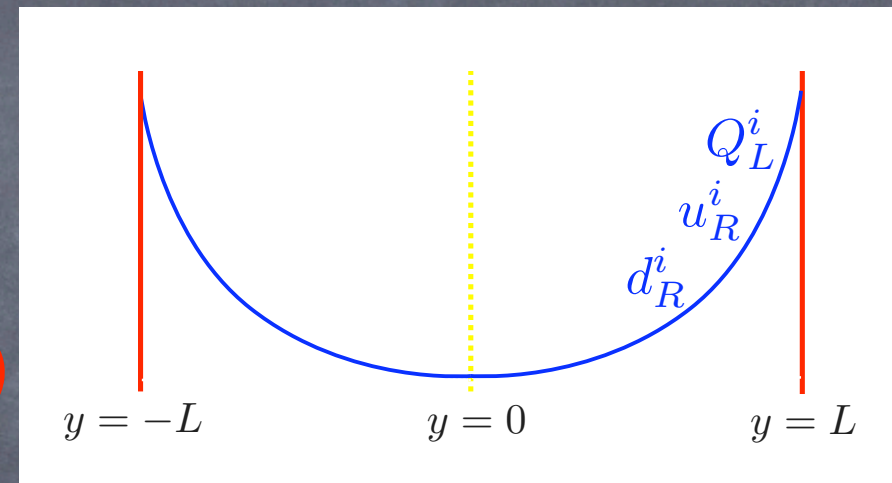
# Backup slices



# Split-UED

SCP, Jing Shu[arXiv:0901.0720] PRL submitted

- Double Kink-mass for quarks introduced (1 new parameter)
- Quarks are quasi-localized on boundaries (split-wave function)
- KK parity respected :-)
- KK quarks are heavier by 5D mass term (split-spectrum)



$$m_n^2 = \mu^2 + k_n^2$$



# MET search.....

The jets from KK quark is hard, and measurable.

	cross section(pb)	generated	standard cut	$M_{\text{eff}} > 1 \text{ TeV}$	$M_{\text{eff}} > 1.5 \text{ TeV}$
$\tilde{q}\tilde{q}$	0.13	7595	3069	2799	1629
$\tilde{g}\tilde{q}$	0.62	37584	11448	6829	1851
$\tilde{g}\tilde{g}$	0.61	37381	6609	1356	257



# KK decomposition

Consider SM quark is embedded in the “+” component:

$$\Psi_+(x, y) = \sum_n g_n(y) \chi_n(x) \quad \text{5D KK “+” parity}$$

$$\Psi_-(x, y) = \sum_n f_n(y) \psi_n(x) \quad \text{5D KK “-” parity}$$

For the 4D KK even/odd field  $\chi_n(x)$ ,  $g_n(y)$  must be symmetric/asymmetric around  $y=0$ , which satisfy the +/- boundary condition.

The 5D profile with even/odd KK parity in the interval  $-L$  to  $L$  is the same as the one with +/- boundary condition at  $y=0$ .

# KK decomposition

$$\Psi_+(x, y) = \sum_{n^+, n^-} g_{n^+}(|y|)\chi_{n^+}(x) + \epsilon(y)g_{n^-}(|y|)\chi_{n^-}(x)$$

$$\Psi_-(x, y) = \sum_{n^+, n^-} \epsilon(y)f_{n^+}(|y|)\psi_{n^+}(x) + f_{n^-}(|y|)\psi_{n^-}(x)$$

$$\text{E. O. M.:} \quad \begin{aligned} \partial_y g_n + \mu g_n - m_n f_n &= 0 \\ \partial_y f_n - \mu f_n + m_n g_n &= 0 \end{aligned}$$

$$\text{BCs:} \quad \begin{array}{cc} g_{n^+} & (+, +) & g_{n^-} & (-, +) \\ f_{n^+} & (-, -) & f_{n^-} & (+, -) \end{array}$$



# KK decomposition



The 5D profiles for the even modes:

$$g_{0+} = A_0 e^{-my}$$

$$m \sim -\mu$$

$$g_{n+} = A_{n+} \left( \cos(k_{n+} y) - \frac{m}{k_{n+}} \sin(k_{n+} y) \right)$$

$$f_{n+} = -A_{n+} \frac{m_{n+}}{k_{n+}} \sin(k_{n+} y)$$

The Masses:

$$m_{n+} = \sqrt{m^2 + k_{n+}^2}$$

$$k_{n+} = n\pi/L$$





# KK decomposition



The solution for the odd modes ( $m < 0$ ):

$$g_{n^-} = -A_{n^-} \frac{m_{n^-}}{k_{n^-}} \sin(k_{n^-} y)$$

$$f_{n^-} = A_{n^-} \left( \cos(k_{n^-} y) - \frac{m}{k_{n^-}} \sin(k_{n^-} y) \right)$$

Masses:

$$m_n = \sqrt{m^2 + k_n^2}$$

$$k_{n^-} = m \tan(k_{n^-} L)$$

When  $m$  increases from  $-\infty$  to  $0$

$k_n$  decreases from  $n\pi/L$  to  $(n - 1/2)\pi/L$



# KK decomposition

In case  $m > 0$

When  $m$  increases from  $0$  to  $+\infty$

$kn_-$  increases from  $(n - 1)\pi/L$  to  $(n - 1/2)\pi/L$

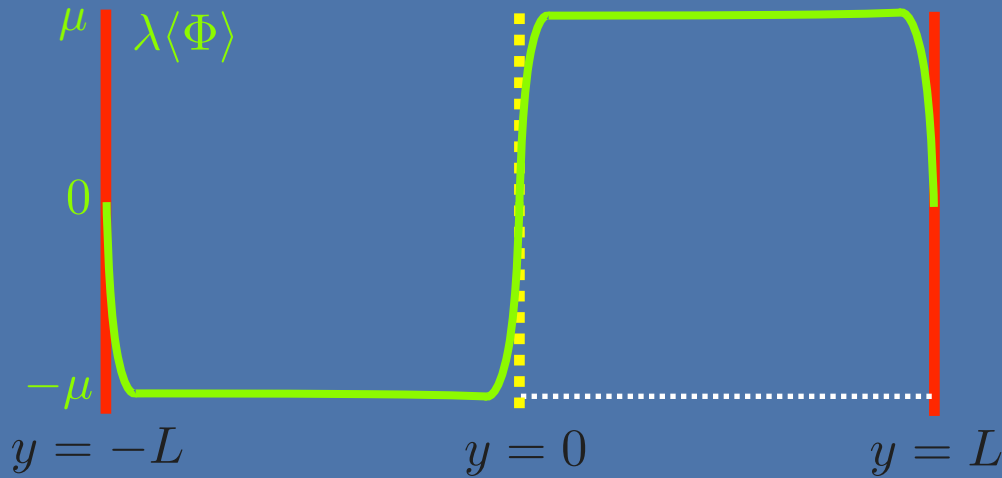
There is a special solution (light mode) when  $n=1$

$$g_{1-} = -A_{1-} \frac{m_{1-}}{k_{1-}} \sinh(k_{1-} y)$$

$$f_{1-} = A_{1-} \left( \cosh(k_{1-} y) - \frac{m}{k_{1-}} \sinh(k_{1-} y) \right)$$

$$m_{1-} = \sqrt{m^2 - k_{1-}^2} \quad m \rightarrow +\infty \quad m_{1-} \rightarrow 0$$

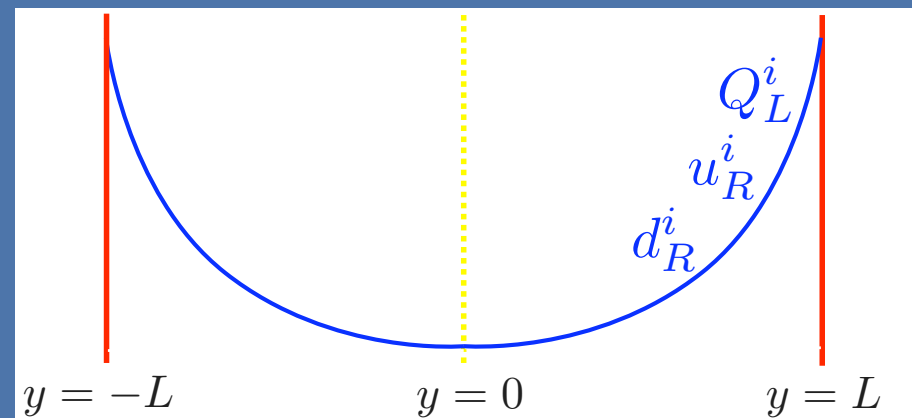
# Zero mode



“kink” like profile  
simplest: “step” function

$$\lambda\Phi(y) = m(y) = \mu\epsilon(y)$$

$$g_{0+}(y) = N_+ \exp\left(-\int_0^y \Phi(s) ds\right)$$



# KK decomposition

Consider SM quark is embedded in the “+” component:

$$\Psi_+(x, y) = \sum_n g_n(y) \chi_n(x) \quad \text{5D KK “+” parity}$$

$$\Psi_-(x, y) = \sum_n f_n(y) \psi_n(x) \quad \text{5D KK “-” parity}$$

For the 4D KK even/odd field  $\chi_n(x)$ ,  $g_n(y)$  must be symmetric/asymmetric around  $y=0$ , which satisfy the +/- boundary condition.

The 5D profile with even/odd KK parity in the interval  $-L$  to  $L$  is the same as the one with +/- boundary condition at  $y=0$ .

# KK decomposition

$$\Psi_+(x, y) = \sum_{n^+, n^-} g_{n^+}(|y|)\chi_{n^+}(x) + \epsilon(y)g_{n^-}(|y|)\chi_{n^-}(x)$$

$$\Psi_-(x, y) = \sum_{n^+, n^-} \epsilon(y)f_{n^+}(|y|)\psi_{n^+}(x) + f_{n^-}(|y|)\psi_{n^-}(x)$$

$$\text{E. O. M.:} \quad \begin{aligned} \partial_y g_n + \mu g_n - m_n f_n &= 0 \\ \partial_y f_n - \mu f_n + m_n g_n &= 0 \end{aligned}$$

$$\text{BCs:} \quad \begin{array}{cc} g_{n^+} & (+, +) & g_{n^-} & (-, +) \\ f_{n^+} & (-, -) & f_{n^-} & (+, -) \end{array}$$





# KK decomposition



The 5D profiles for the even modes:

$$\begin{aligned}g_{0+} &= A_0 e^{-my} \\g_{n+} &= A_{n+} \left( \cos(k_{n+} y) - \frac{m}{k_{n+}} \sin(k_{n+} y) \right) \\f_{n+} &= -A_{n+} \frac{m_{n+}}{k_{n+}} \sin(k_{n+} y)\end{aligned} \quad m \sim -\mu$$

The Masses:

$$m_{n+} = \sqrt{m^2 + k_{n+}^2}$$

$$k_{n+} = n\pi/L$$


# KK decomposition

The solution for the odd modes ( $m < 0$ ):

$$g_{n^-} = -A_{n^-} \frac{m_{n^-}}{k_{n^-}} \sin(k_{n^-} y)$$

$$f_{n^-} = A_{n^-} \left( \cos(k_{n^-} y) - \frac{m}{k_{n^-}} \sin(k_{n^-} y) \right)$$

Masses:

$$m_n = \sqrt{m^2 + k_n^2}$$

$$k_{n^-} = m \tan(k_{n^-} L)$$

When  $m$  increases from  $-\infty$  to  $0$

$k_n$  decreases from  $n\pi/L$  to  $(n - 1/2)\pi/L$

# KK decomposition

In case  $m > 0$

When  $m$  increases from  $0$  to  $+\infty$

$k_{n-}$  increases from  $(n-1)\pi/L$  to  $(n-1/2)\pi/L$

There is a **special solution (light mode)** when  $n=1$

$$g_{1-} = -A_{1-} \frac{m_{1-}}{k_{1-}} \sinh(k_{1-} y)$$

$$f_{1-} = A_{1-} \left( \cosh(k_{1-} y) - \frac{m}{k_{1-}} \sinh(k_{1-} y) \right)$$

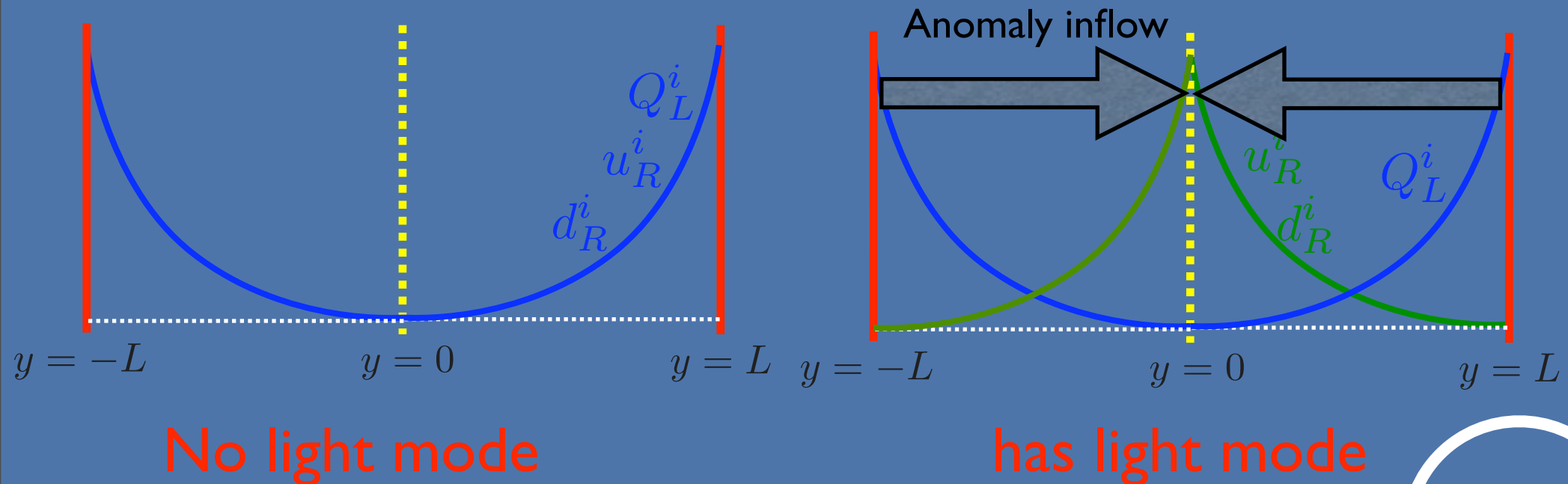
$$m_{1-} = \sqrt{m^2 - k_{1-}^2} \quad m \rightarrow +\infty \quad m_{1-} \rightarrow 0$$

Troublesome in phenomenology, we have to forbid it.



# KK decomposition

Indeed, such a sign ( $\mu < 0$ ) controls the zero mode localized at the center.



# The anomaly cancellation

In a 5D theory, one has to worry about the **localized anomaly** even when the zero mode is anomaly free.

$$U(1)_Y^3$$

$$SU(2)_L^2 - U(1)_Y$$

$$U(1)_Y - \text{gravitational}$$

Can not be cancelled in the quark/lepton sector alone!

The 5D anomalies from the lepton sector is localized at the boundary  $y=-L, L$ .

# The anomaly cancellation

For for a 5D quark field whose left/right-handed has the  $(\alpha_0, \alpha_1)$  boundary condition at  $y=0, L$

$$\partial_C J^C = \frac{Q}{2} [\alpha_0 \delta(y) + \alpha_1 \delta(y - L)]$$

$Q$  is the corresponding consistent anomaly of a left/right-handed spinor

Notice the anomalies induced by the KK even state (“+” at  $y=0$ ) will cancel those by the KK odd state (“-” at  $y=0$ ) at  $y=0$ .

The 5D anomalies from the quark sector is also localized at the boundary  $y=-L, L$ .

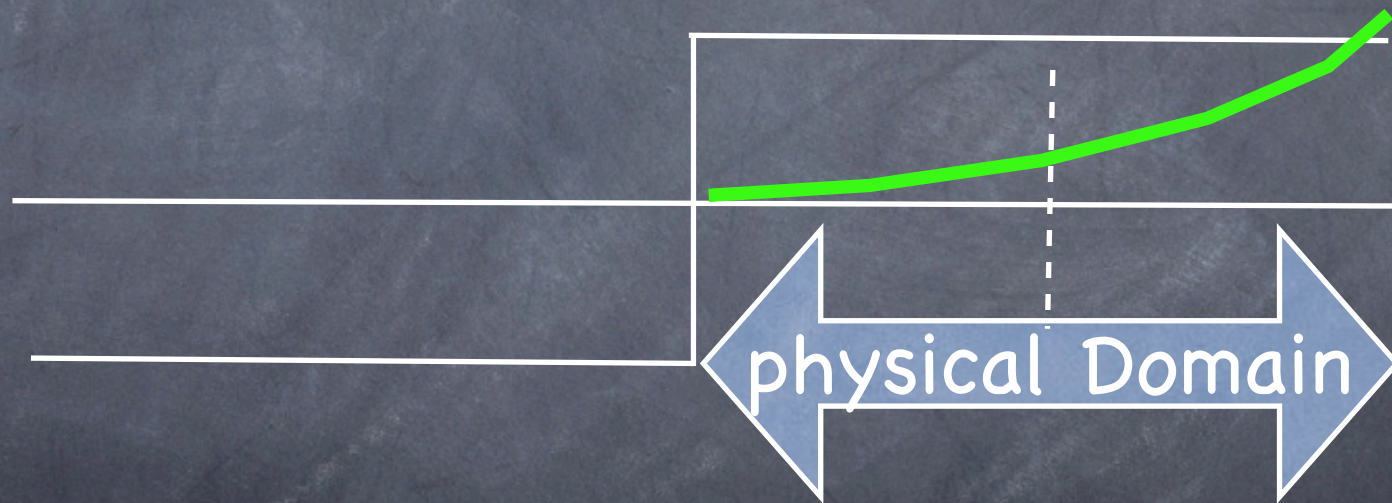
The two will cancel each other!



# Kink-Mass

$$S = \int d^5 \bar{\Psi} i \Gamma_M D^M \Psi - \lambda \Phi(y) \bar{\Psi} \Psi$$

$$m_n^2 = \mu^2 + k_n^2$$



Zero mode  
wave function

$$f(y) \sim e^{\mu y}$$

KK-parity is not respected.

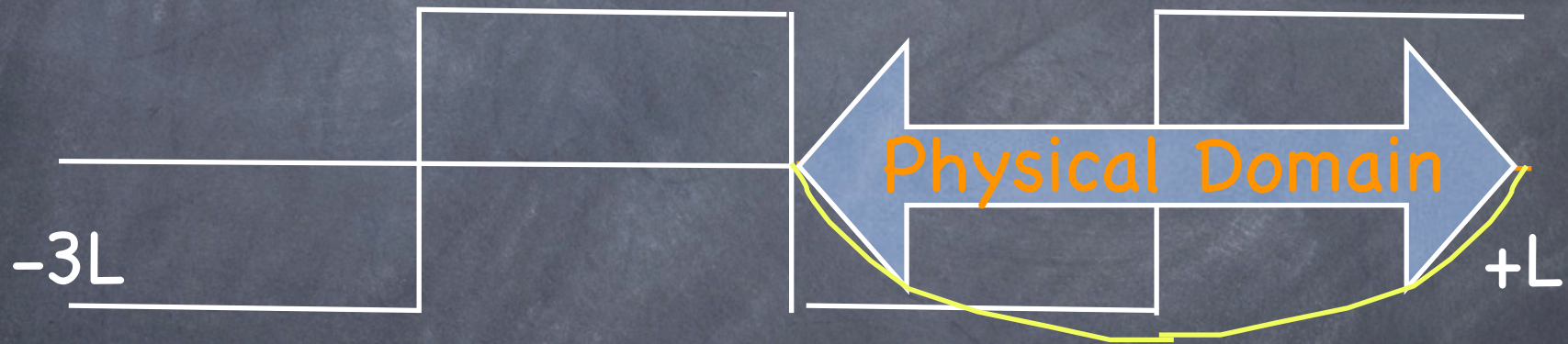


# Double kink-mass

SCP, Jing Shu[arXiv:0901.0720] PRL submitted

$$m_n^2 = \mu^2 + k_n^2$$

$$S = \int d^5 \bar{\Psi} i \Gamma_M D^M \Psi - \lambda \Phi(y) \bar{\Psi} \Psi$$



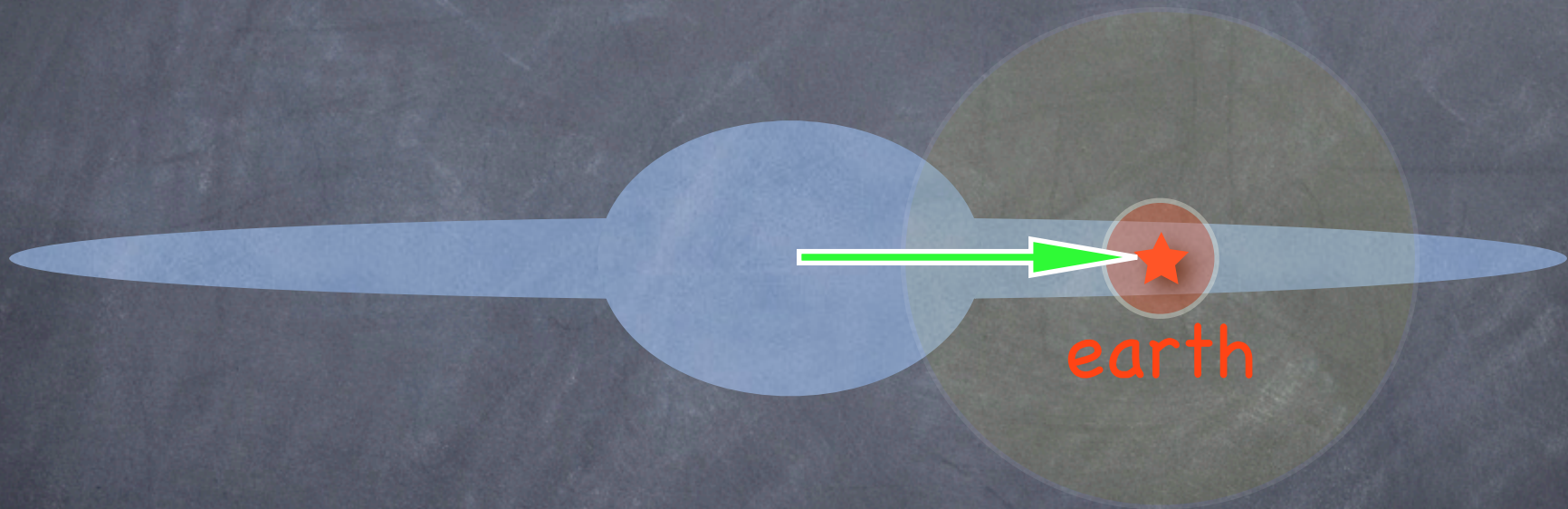
Zero-mode  
profile

$$\begin{aligned} f(y) &= e^{\int_{-L}^y m(y) dy} \\ &= e^{-m(y-L)} \quad (y < 0) \\ &= e^{m(y+L)} \quad (y > 0) \end{aligned}$$

KK-parity respected

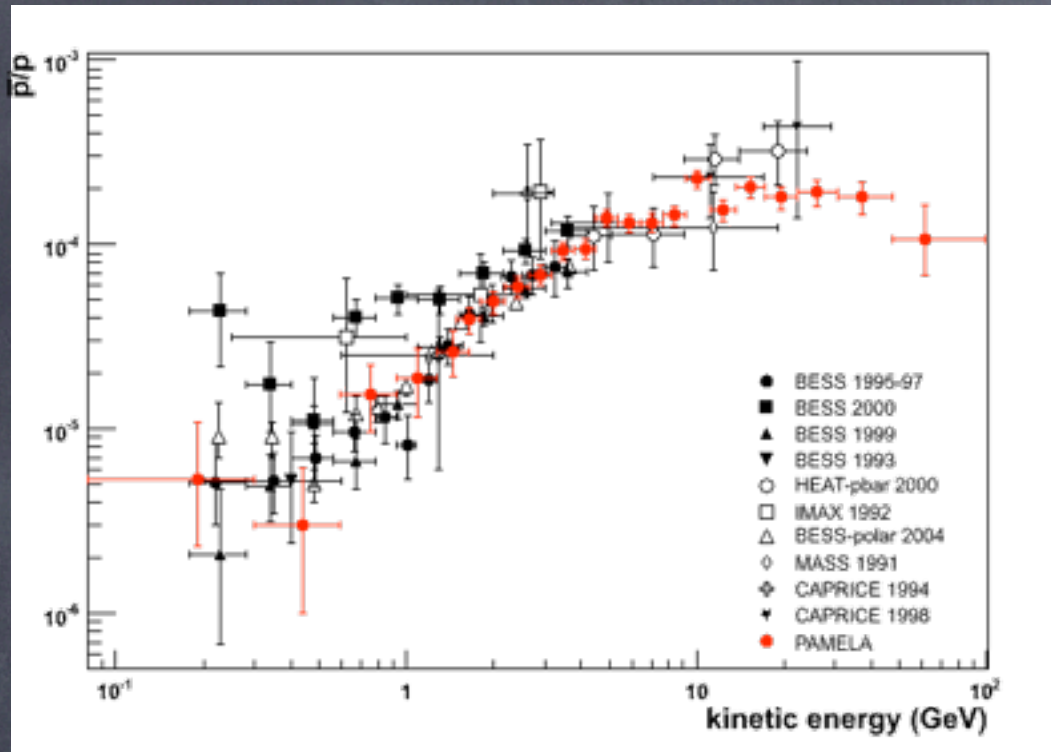


$B1+B1 \rightarrow e+, \text{gamma}, p-..$



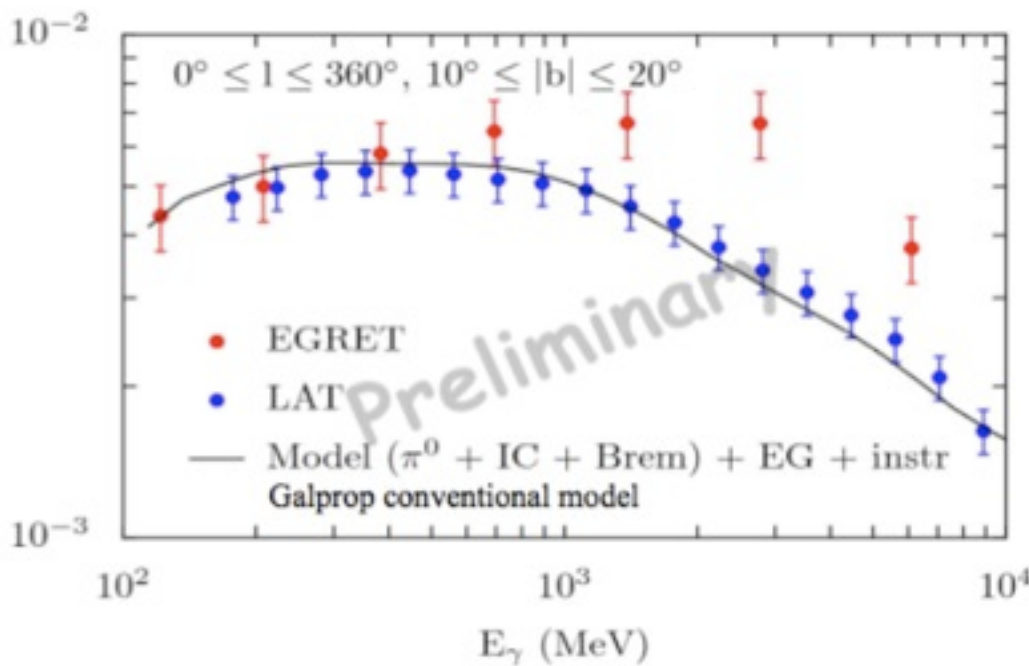
- \*Positron mostly from "local" source
- \*Photon goes straight (mostly from the center)
- \*Antiproton diffuses longer





However!  
 No excess in  
 anti-proton  
 PAMELA, PRL(2009)

(T\_T)

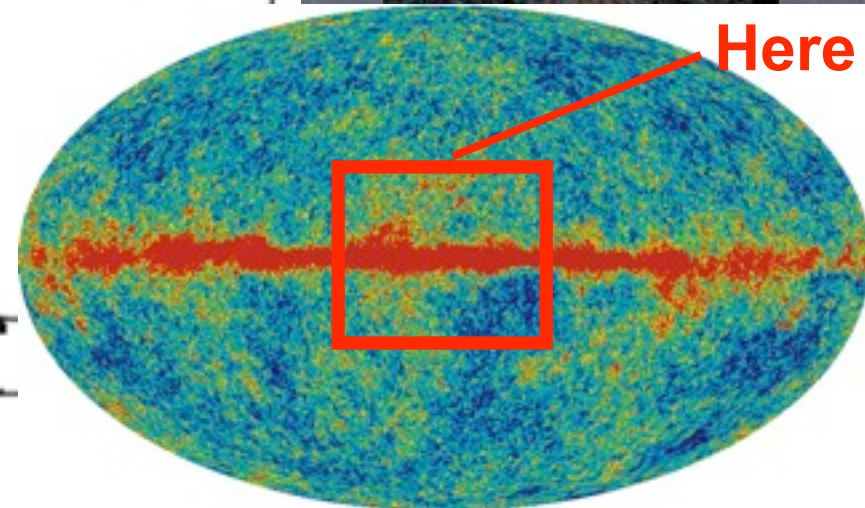
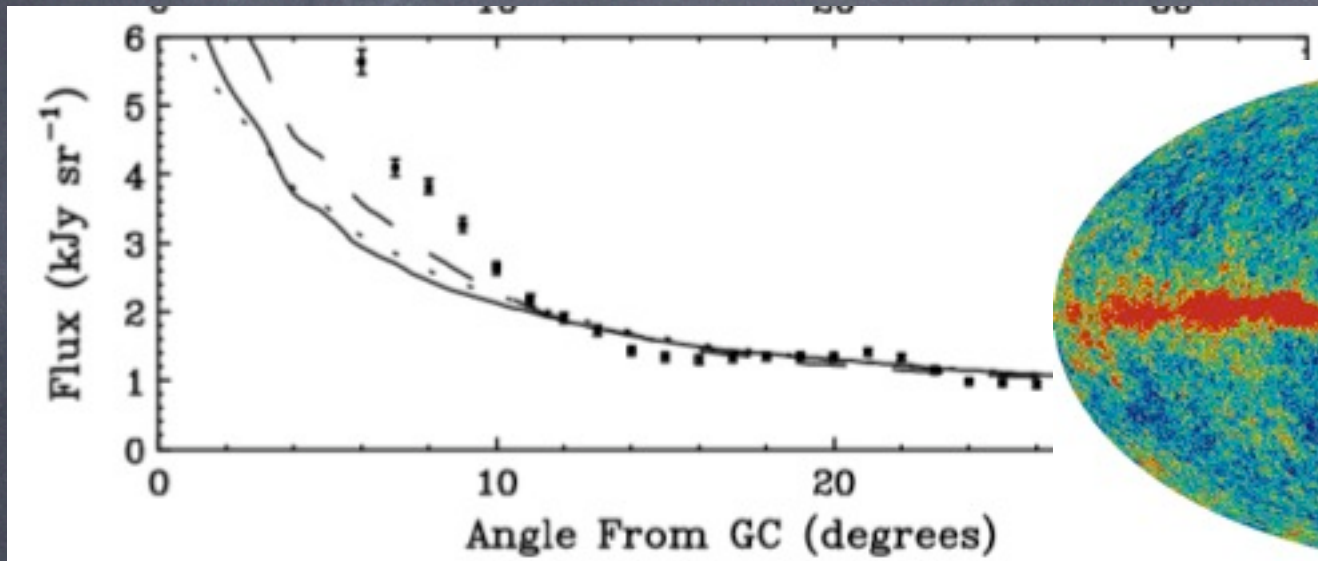
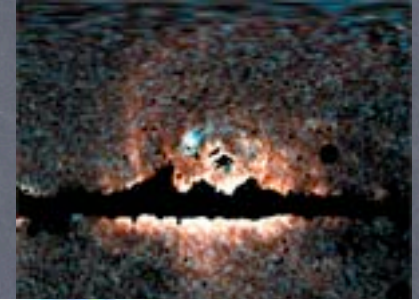


No excess in  
 gamma-ray  
 from Halo  
 Fermi, preliminary

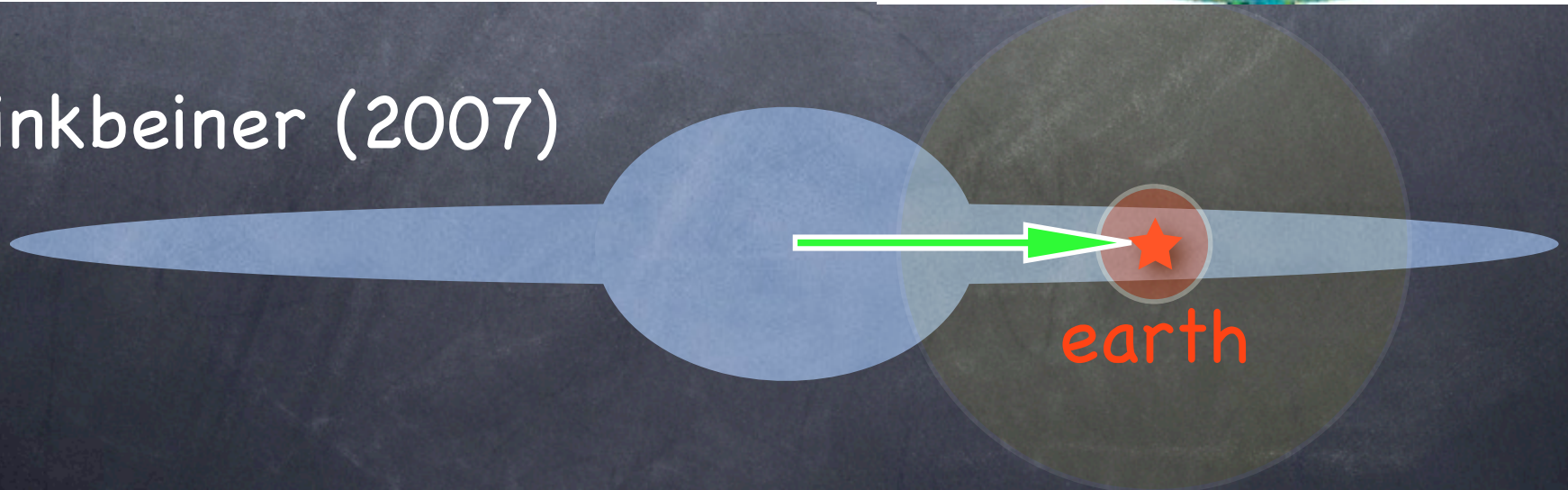
==> need for extension



# WMAP Haze: photon from GC



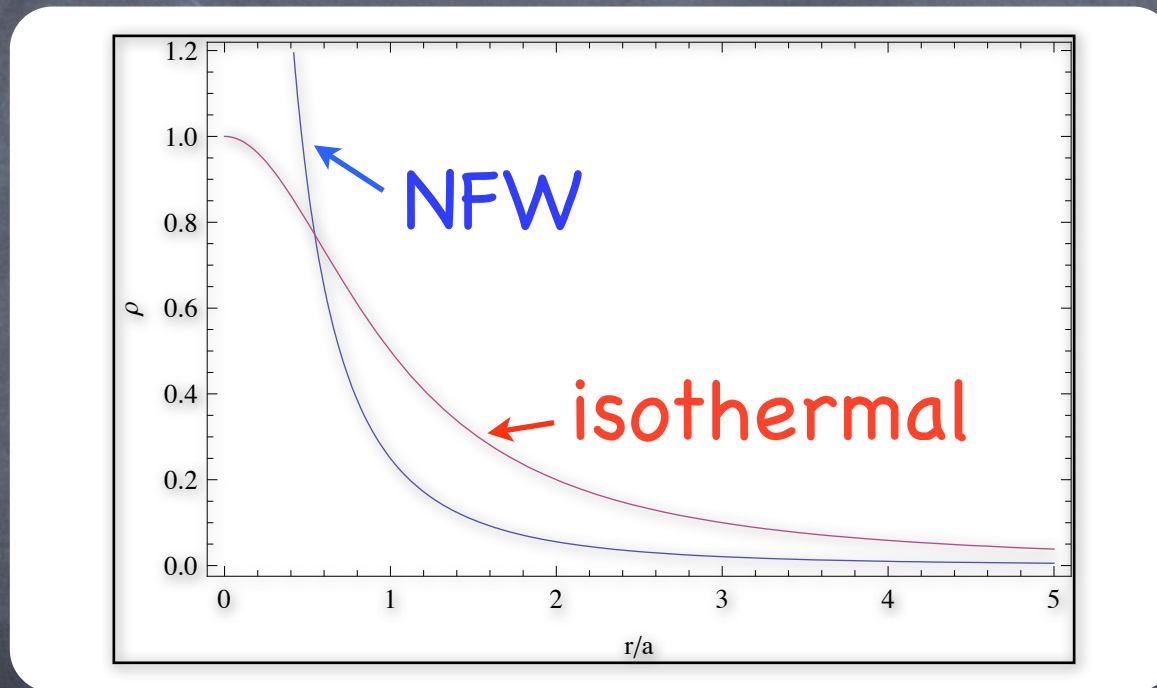
Finkbeiner (2007)





# Supple: Halo profile

$$\rho(r) = \frac{\rho_0}{(r/a)^\gamma [1 + (r/a)^\alpha]^{(\beta-\gamma)/\alpha}}$$



Profile	alpha	beta	gamma
NFW	1	3	1
Isothermal	2	2	0