



Selected flow results in Pb+Pb collisions from ATLAS

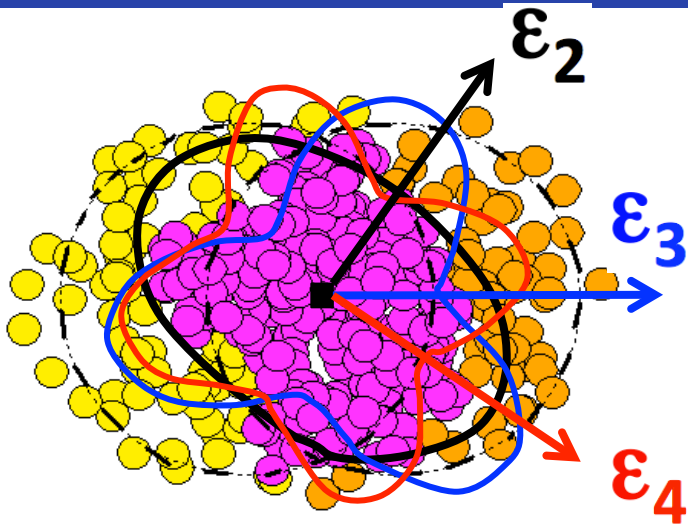
Jiangyong Jia on behalf of the ATLAS Collaboration

ISMD2013

XLIII International Symposium on Multiparticle Dynamics

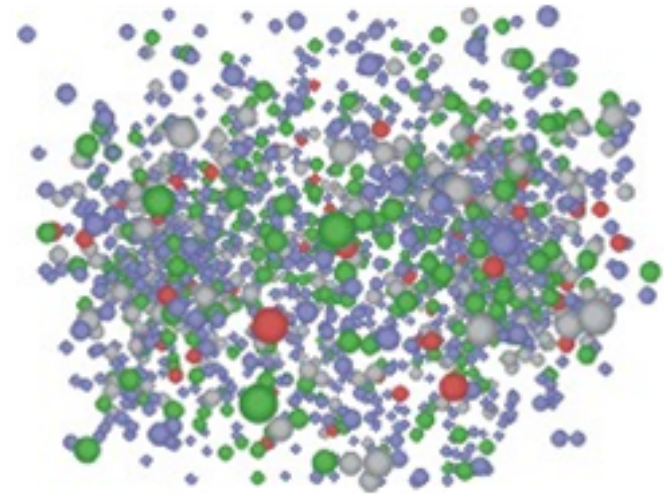


Correlation/flow observables



$$\epsilon_n = \frac{\sqrt{\langle r^n \cos(n\phi) \rangle^2 + \langle r^n \sin(n\phi) \rangle^2}}{\langle r^n \rangle}$$

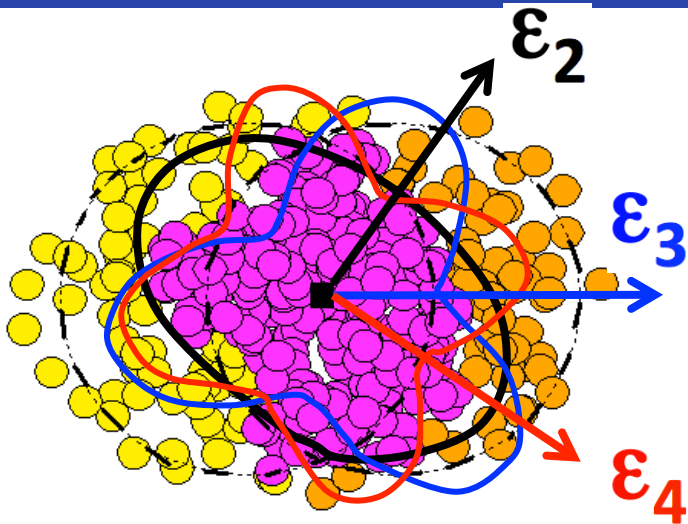
Collective expansion



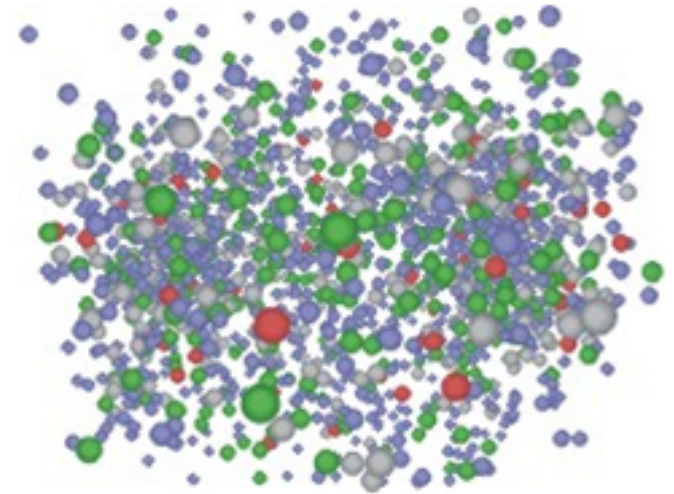
$$\frac{dN}{d\phi} \propto 1 + 2 \sum_n v_n \cos n(\phi - \Phi_n)$$

$$\langle v_n(p_T, \eta) \rangle$$

Correlation/flow observables

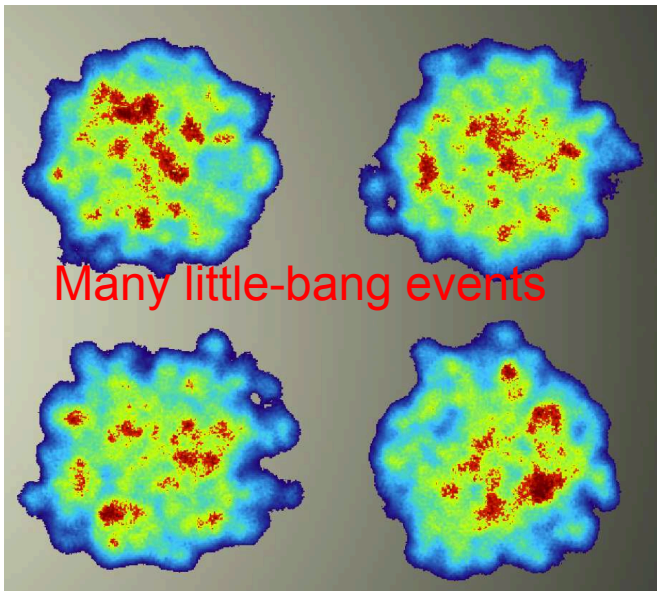


Collective expansion



$$\varepsilon_n = \frac{\sqrt{\langle r^n \cos(n\phi) \rangle^2 + \langle r^n \sin(n\phi) \rangle^2}}{\langle r^n \rangle}$$

$$\frac{dN}{d\phi} \propto 1 + 2 \sum_n v_n \cos n(\phi - \Phi_n) \quad \langle v_n(p_T, \eta) \rangle$$



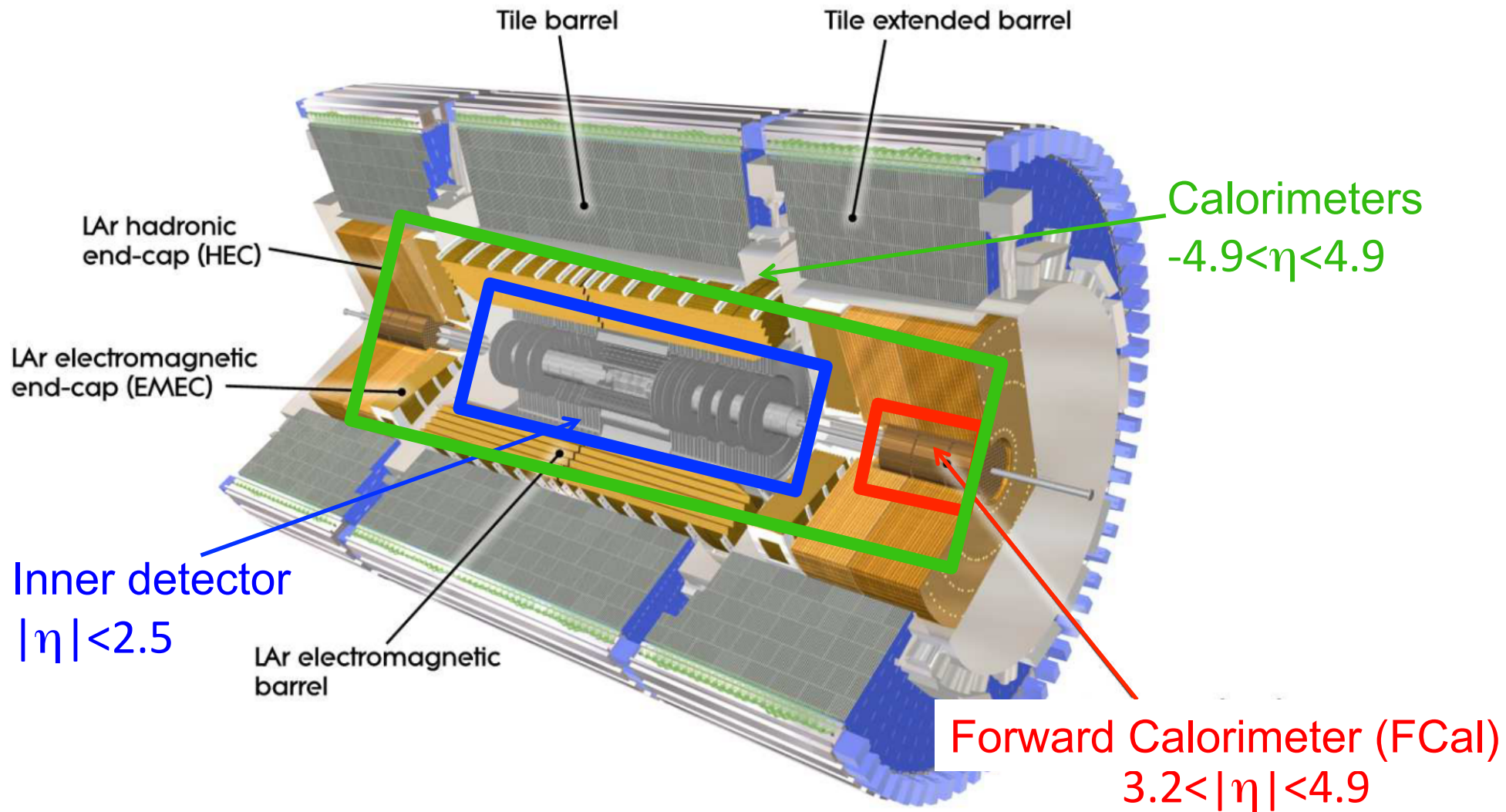
probability distributions:

$$p(v_n, v_m, \dots, \Phi_n, \Phi_m, \dots)$$

- Event plane correlation: $p(\Phi_n, \Phi_m)$ and $p(\Phi_n, \Phi_m, \Phi_L)$
- EbyE v_n : $p(v_2)$, $p(v_3)$ and $p(v_4)$

Probes: **initial geometry** and **transport properties** of the QGP

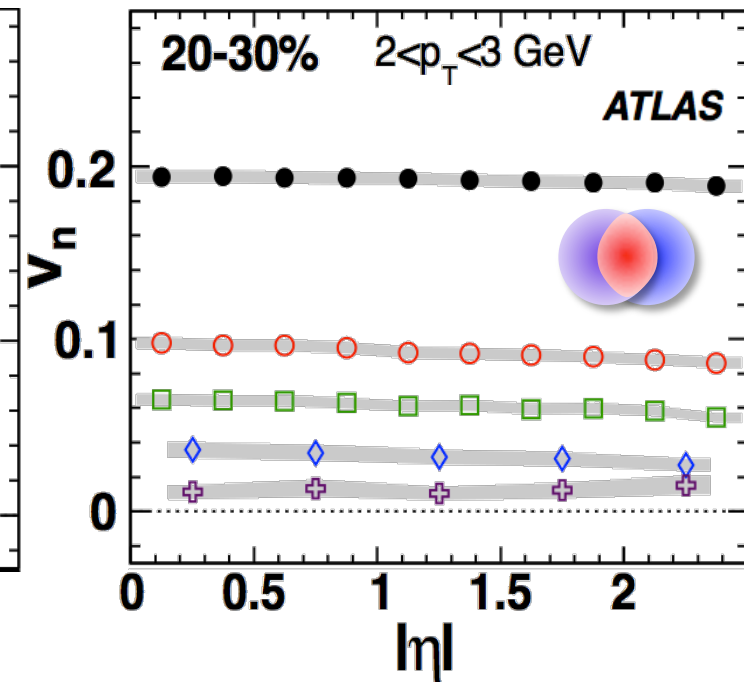
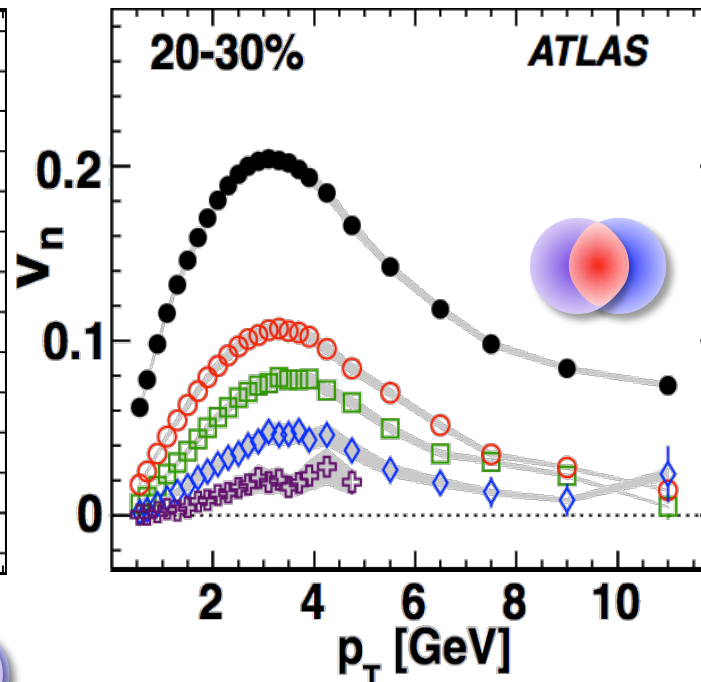
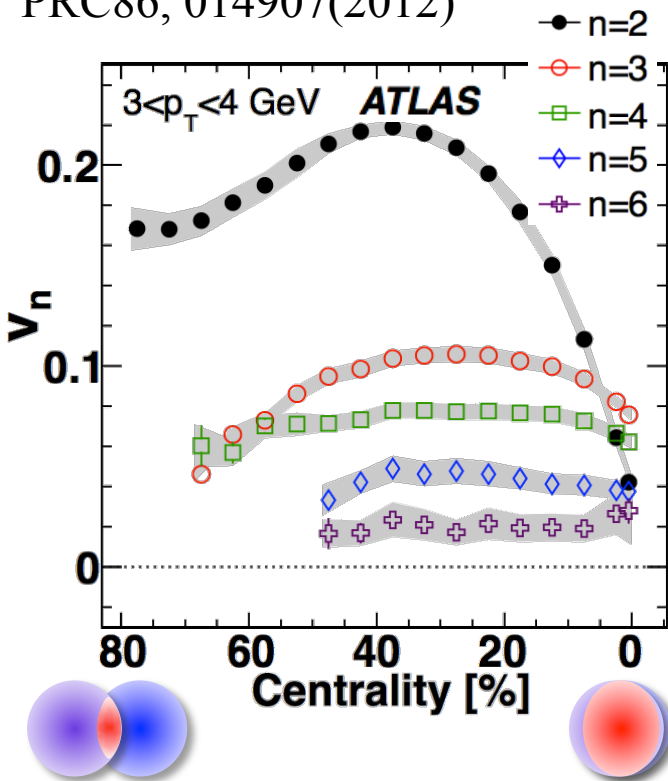
Observables at detector level



- E_T in forward calorimeter $3.2 < |\eta| < 4.9 \rightarrow$ centrality
- Tracks in inner detector $|\eta| < 2.5 \rightarrow$ for v_n measurement
- E_T in calorimeter $-4.9 < \eta < 4.9 \rightarrow$ Event plane correlations

Summary of average flow $v_n(\text{cent}, p_T, \eta, n)$

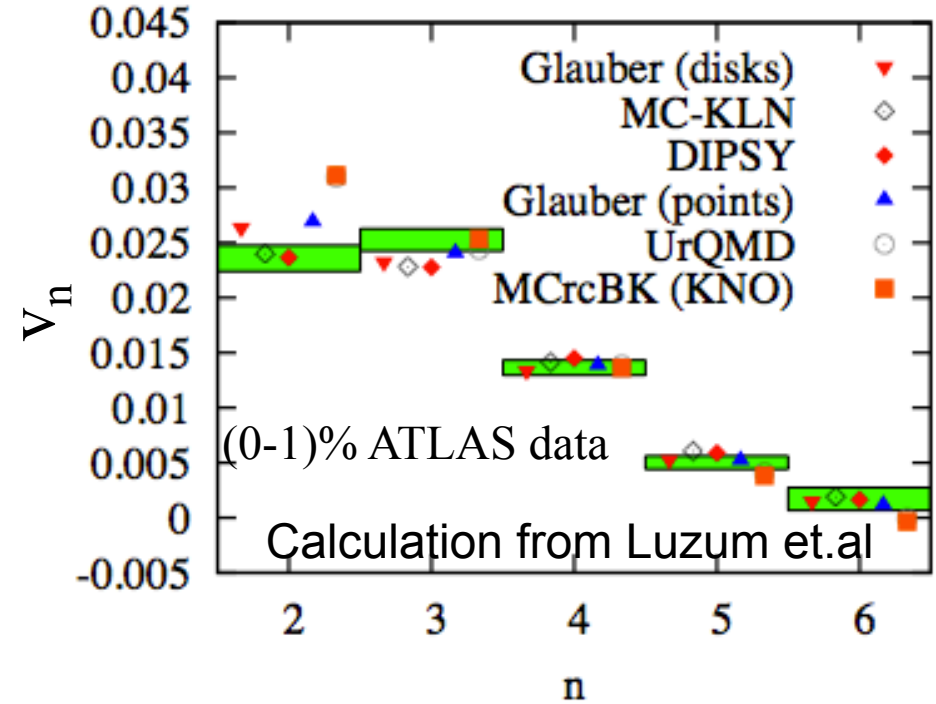
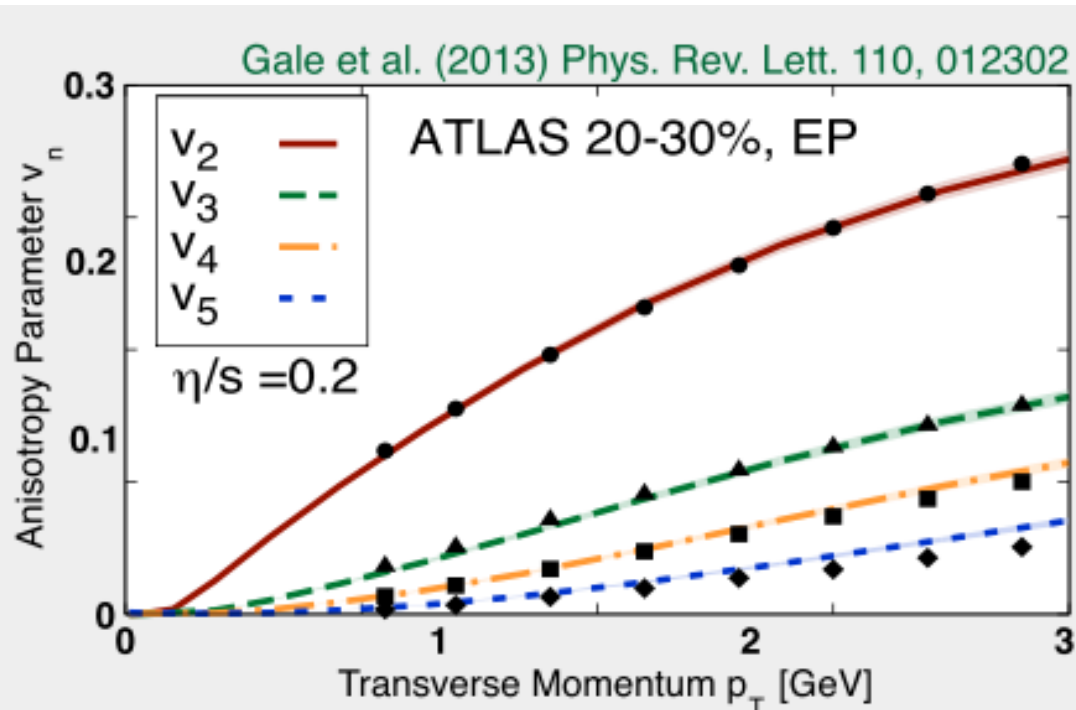
PRC86, 014907(2012)



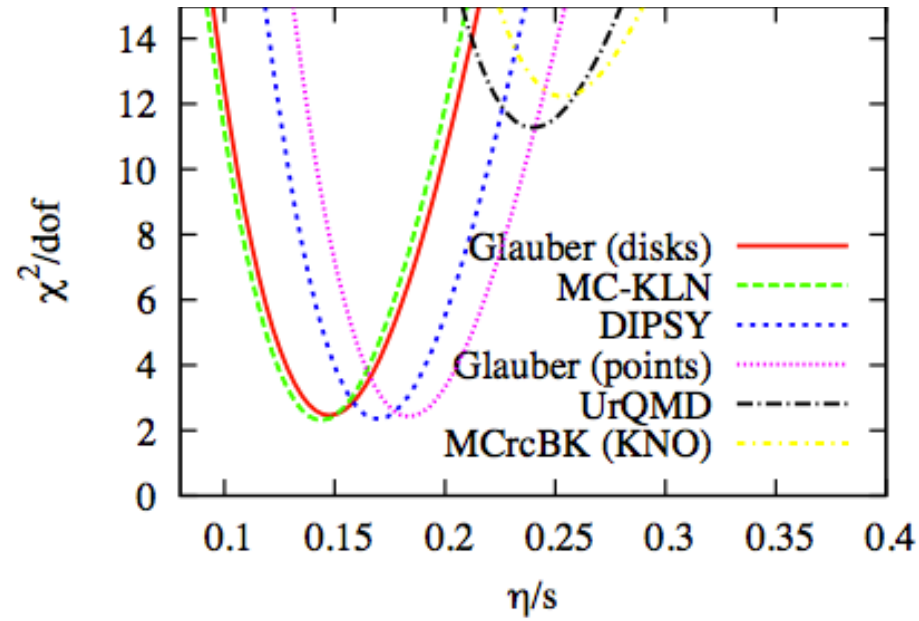
Features of Fourier coefficients

- v_n coefficients rise and fall with centrality → **collision geometry**
- v_n coefficients rise and fall with p_T . → **hydrodynamic response**
- v_n coefficients are \sim boost invariant. → **global event shape**

Comparison of v_n results with hydro models



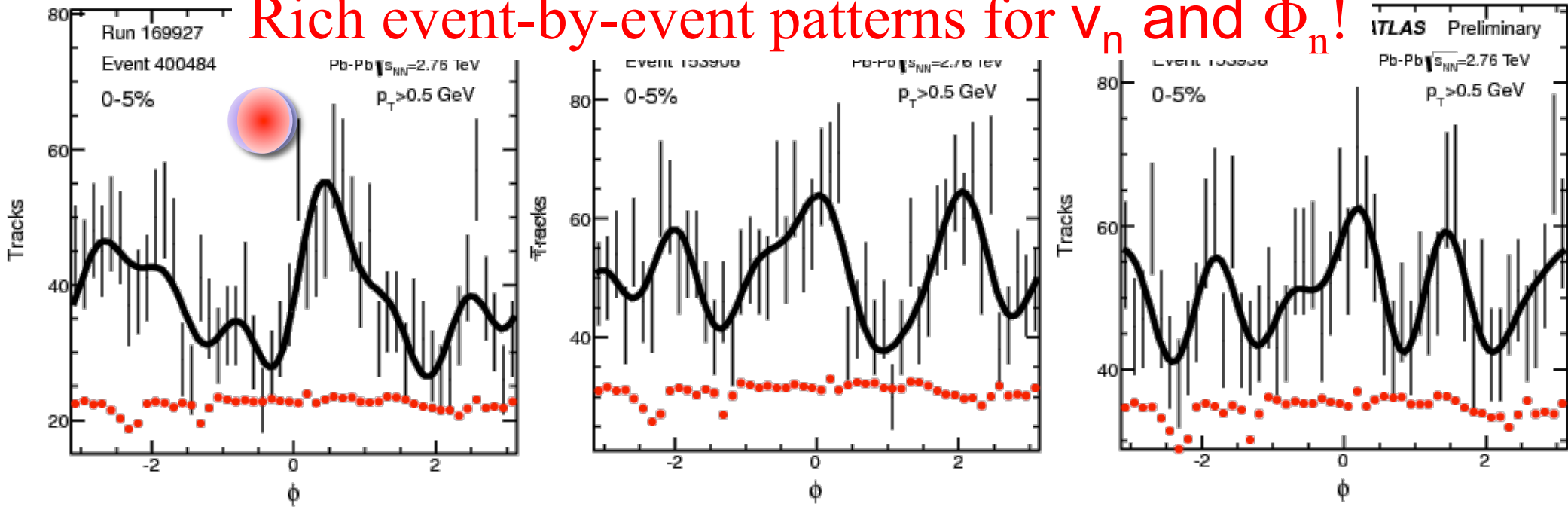
Constrain η/s & initial geometry



ATLAS data PRC86, 014907(2012)

Event-by-event fluctuation seen in data

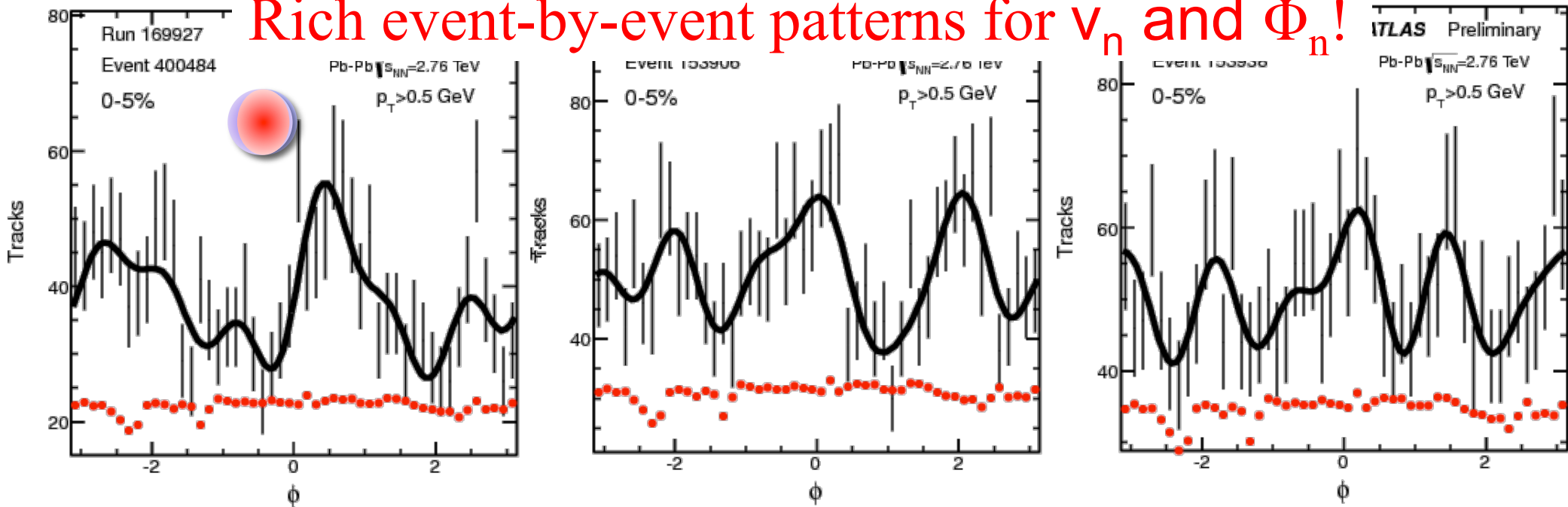
Rich event-by-event patterns for v_n and Φ_n !



$$\frac{dN}{d\phi} \propto 1 + 2 \sum_n v_n^{\text{obs}} \cos n(\phi - \Phi_n^{\text{obs}})$$

Event-by-event fluctuation seen in data

Rich event-by-event patterns for v_n and Φ_n !



$$\frac{dN}{d\phi} \propto 1 + 2 \sum_n v_n^{\text{obs}} \cos n(\phi - \Phi_n^{\text{obs}})$$

Obtain $p(v_n)$ from $p(v_n^{\text{obs}})$

response function: $p(v_n^{\text{obs}} | v_n)$

Obtain $p(\Phi_n, \Phi_m)$ from $p(\Phi_n^{\text{obs}}, \Phi_m^{\text{obs}})$

Determine resolution corrections

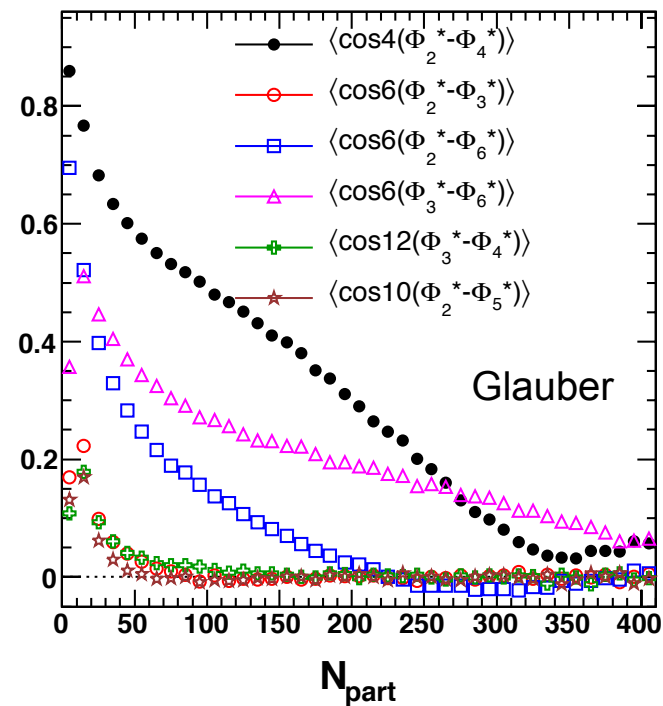
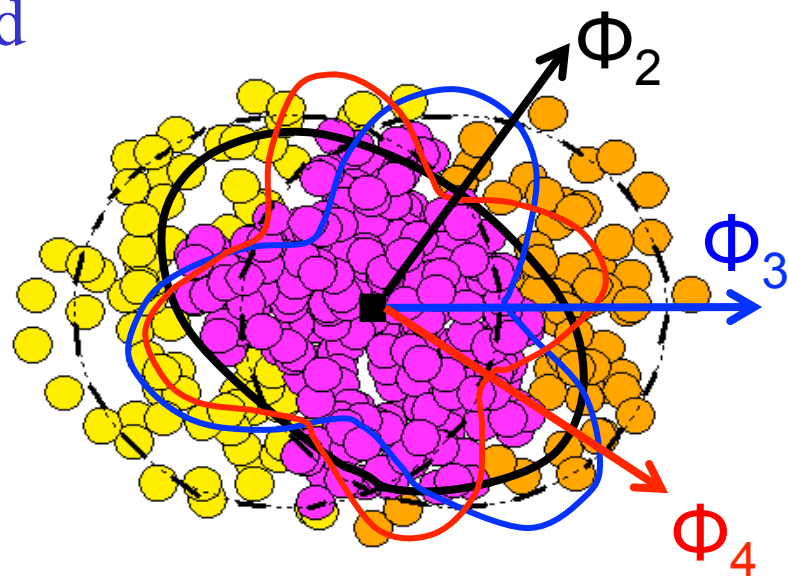
ATLAS-CONF-2012-49

ATLAS arXiv: 1305.2942

Event plane correlations: $\rho(\Phi_n, \Phi_m, \dots)$

- Correlations exist in the initial geometry and are also generated during hydro evolution: non-linear mixing, e.g.

$$v_4 e^{-i4\Phi_4} = k\varepsilon_4 + v_2 v_2 e^{-i4\Phi_2} + \dots$$



Event plane correlations: $\rho(\Phi_n, \Phi_m, \dots)$

- Correlations exist in the initial geometry and are also generated during hydro evolution: non-linear mixing, e.g.

$$v_4 e^{-i4\Phi_4} = k\varepsilon_4 + v_2 v_2 e^{-i4\Phi_2} + \dots$$

- The correlation quantified via correlators

$$\frac{dN_{events}}{d(4(\Phi_2 - \Phi_4))} = 1 + 2 \sum_{j=1}^{\infty} V^j \cos(4j(\Phi_2 - \Phi_4))$$

$$V^j = \langle \cos(4j(\Phi_2 - \Phi_4)) \rangle$$

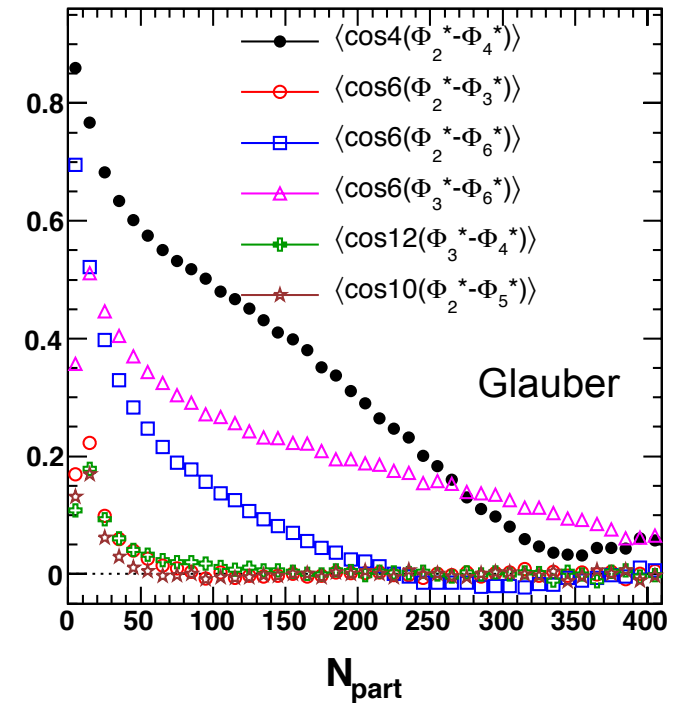
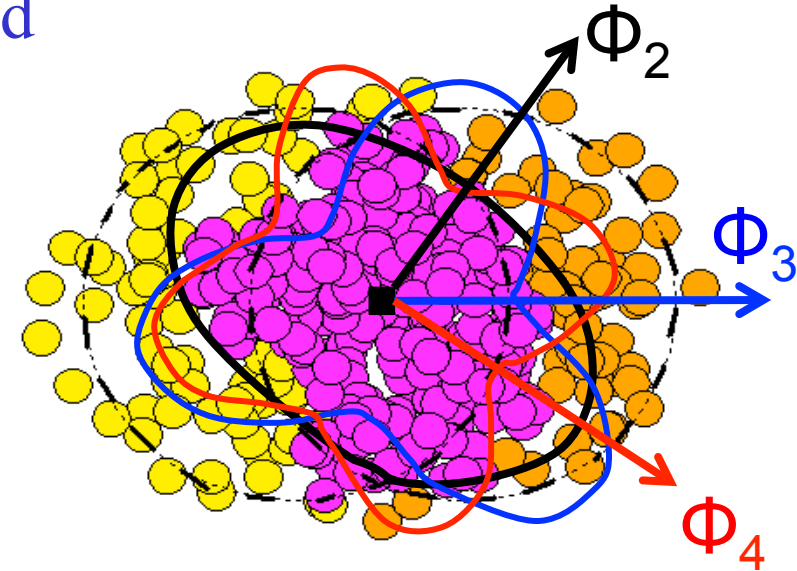
Jia, Soumya, Teany,
arXiv:1205.3585
arXiv:1203.5095

- Generalize to three-plane correlations

$$2\Phi_2 + 4\Phi_4 - 6\Phi_6 = 4(\Phi_4 - \Phi_2) - 6(\Phi_6 - \Phi_2)$$

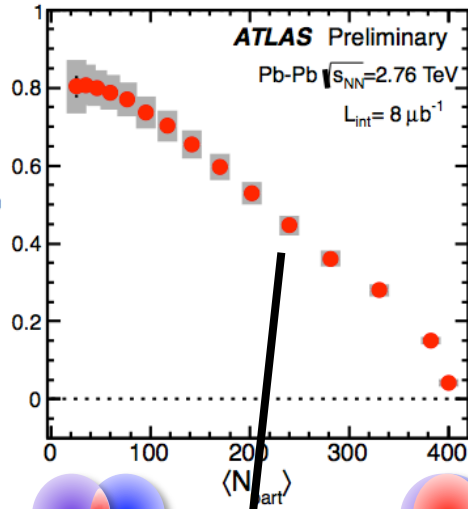
Measured correlators:

$\langle \cos 4(\Phi_2 - \Phi_4) \rangle$	$\langle \cos(2\Phi_2 + 3\Phi_3 - 5\Phi_5) \rangle$
$\langle \cos 8(\Phi_2 - \Phi_4) \rangle$	$\langle \cos(-8\Phi_2 + 3\Phi_3 + 5\Phi_5) \rangle$
$\langle \cos 12(\Phi_2 - \Phi_4) \rangle$	$\langle \cos(2\Phi_2 + 4\Phi_4 - 6\Phi_6) \rangle$
$\langle \cos 6(\Phi_2 - \Phi_3) \rangle$	$\langle \cos(-10\Phi_2 + 4\Phi_4 + 6\Phi_6) \rangle$
$\langle \cos 6(\Phi_2 - \Phi_6) \rangle$	$\langle \cos(2\Phi_2 - 6\Phi_3 + 4\Phi_4) \rangle$
$\langle \cos 6(\Phi_3 - \Phi_6) \rangle$	$\langle \cos(-10\Phi_2 + 6\Phi_3 + 4\Phi_4) \rangle$

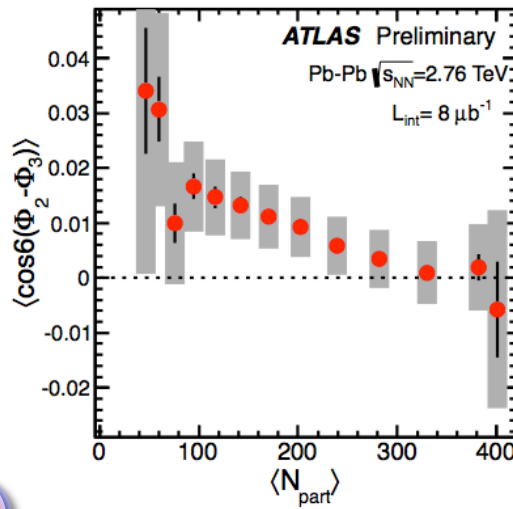


Event plane correlation results

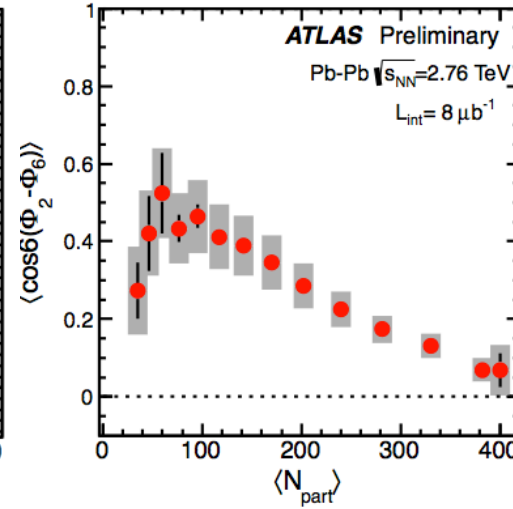
$$\langle \cos 4(\Phi_2 - \Phi_4) \rangle$$



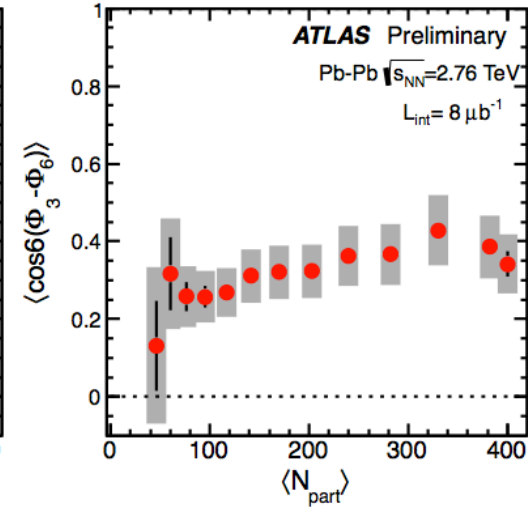
$$\langle \cos 6(\Phi_2 - \Phi_3) \rangle$$



$$\langle \cos 6(\Phi_2 - \Phi_6) \rangle$$

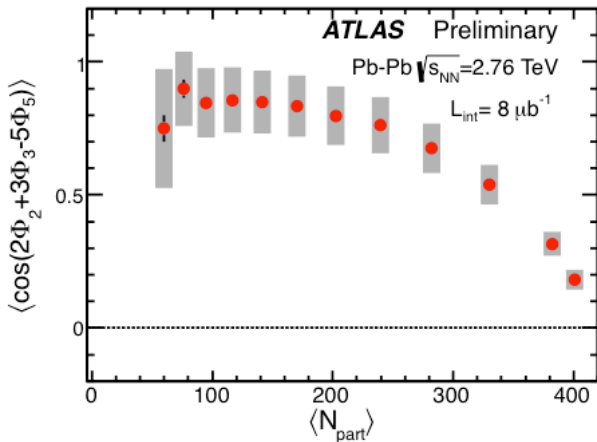


$$\langle \cos 6(\Phi_3 - \Phi_6) \rangle$$



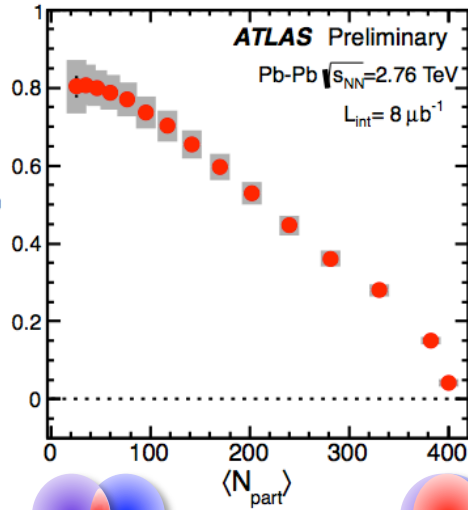
$$v_4 e^{-i4\Psi_4} = k\varepsilon_4 + v_2 v_2 e^{-i4\Psi_2} + \dots$$

$$\langle \cos(2\Phi_2 + 3\Phi_3 - 5\Phi_5) \rangle$$

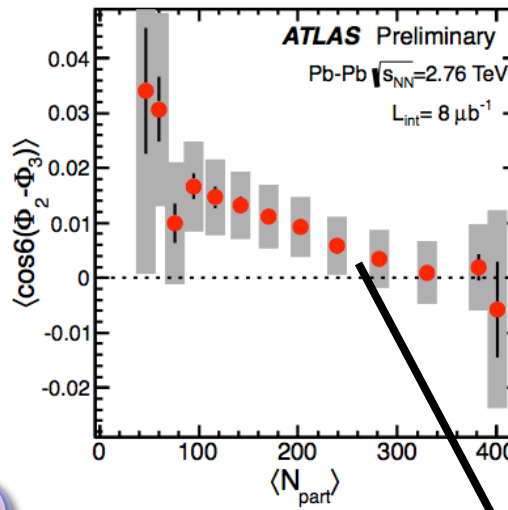


Event plane correlation results

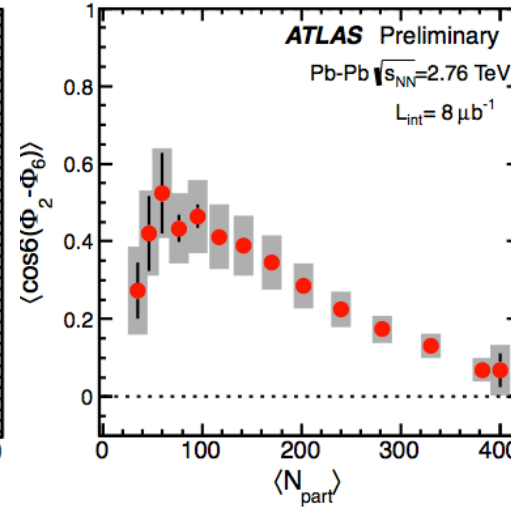
$$\langle \cos 4(\Phi_2 - \Phi_4) \rangle$$



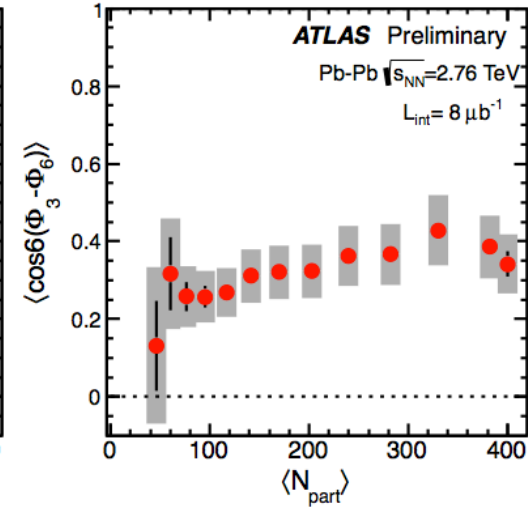
$$\langle \cos 6(\Phi_2 - \Phi_3) \rangle$$



$$\langle \cos 6(\Phi_2 - \Phi_6) \rangle$$



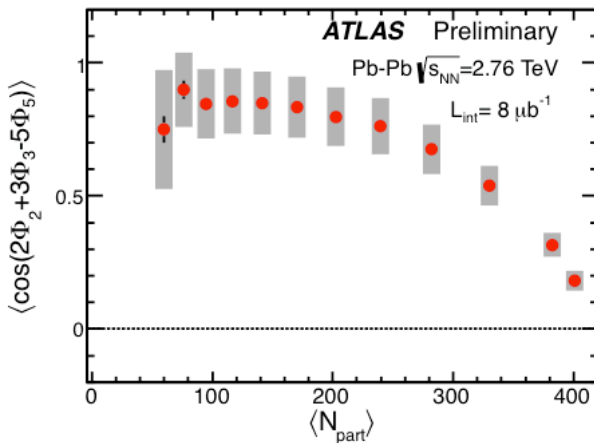
$$\langle \cos 6(\Phi_3 - \Phi_6) \rangle$$



$$v_2 e^{-i2\Psi_2} = k\varepsilon_2 + v_1 v_1 e^{-i2\Psi_1} + \dots$$

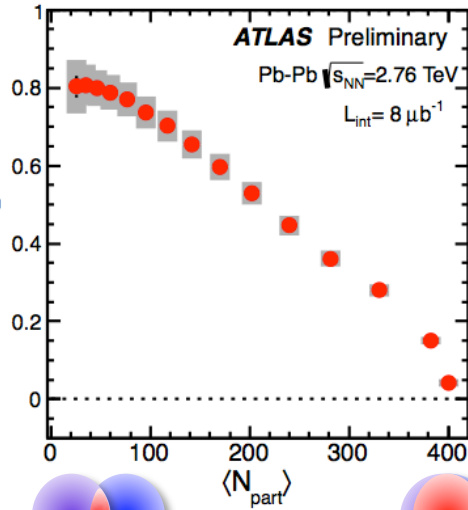
$$v_3 e^{-i3\Psi_3} = k\varepsilon_3 + v_1 v_2 e^{-i(\Psi_1 + 2\Psi_2)} + \dots$$

$$\langle \cos(2\Phi_2 + 3\Phi_3 - 5\Phi_5) \rangle$$

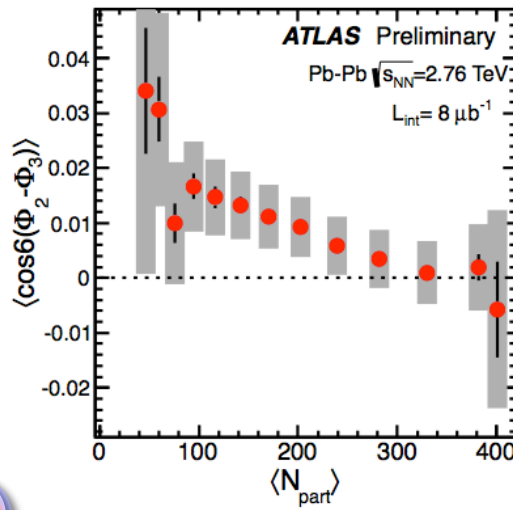


Event plane correlation results

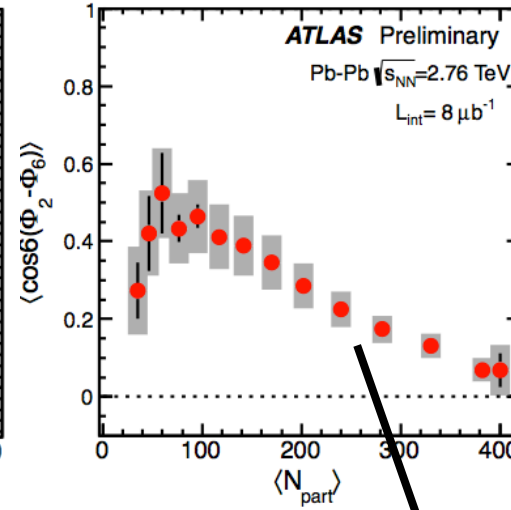
$$\langle \cos 4(\Phi_2 - \Phi_4) \rangle$$



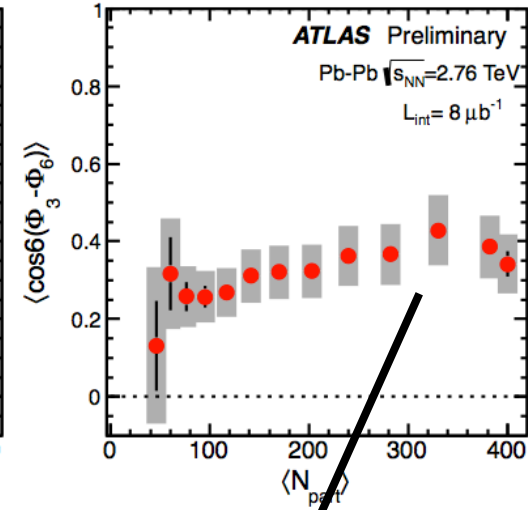
$$\langle \cos 6(\Phi_2 - \Phi_3) \rangle$$



$$\langle \cos 6(\Phi_2 - \Phi_6) \rangle$$

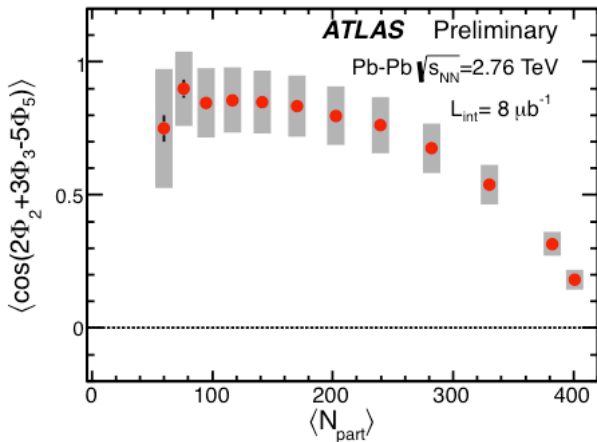


$$\langle \cos 6(\Phi_3 - \Phi_6) \rangle$$



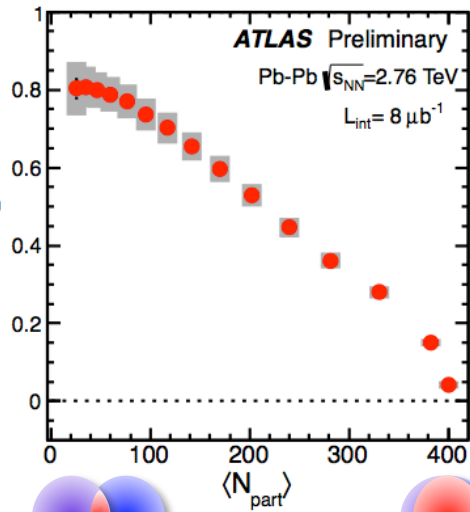
$$v_6 e^{-i6\Psi_6} = k\varepsilon_6 + v_2 v_2 v_2 e^{-i6\Psi_2} + v_3 v_3 e^{-i6\Psi_3} + \dots$$

$$\langle \cos(2\Phi_2 + 3\Phi_3 - 5\Phi_5) \rangle$$

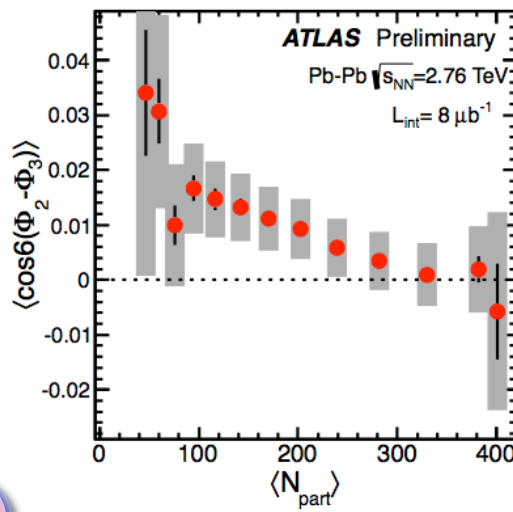


Event plane correlation results

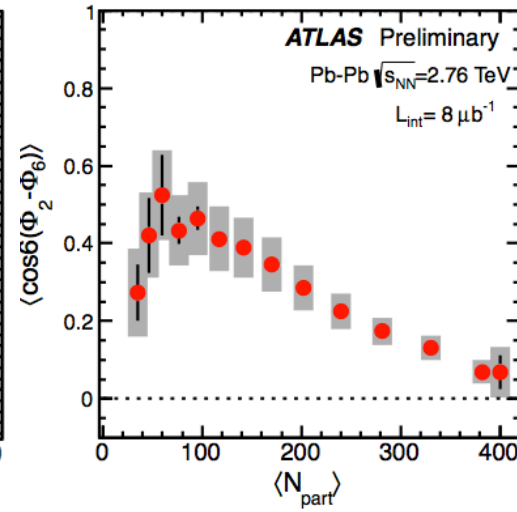
$$\langle \cos 4(\Phi_2 - \Phi_4) \rangle$$



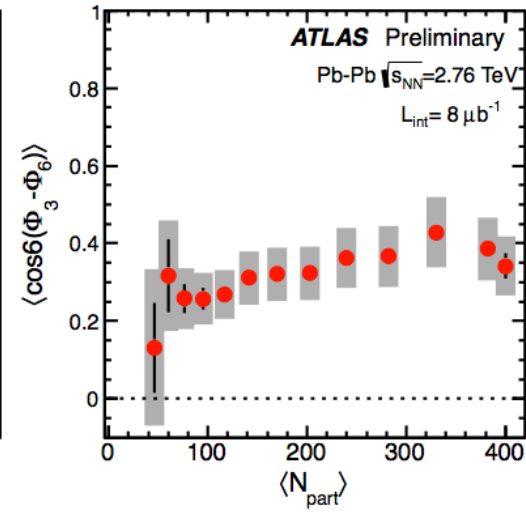
$$\langle \cos 6(\Phi_2 - \Phi_3) \rangle$$



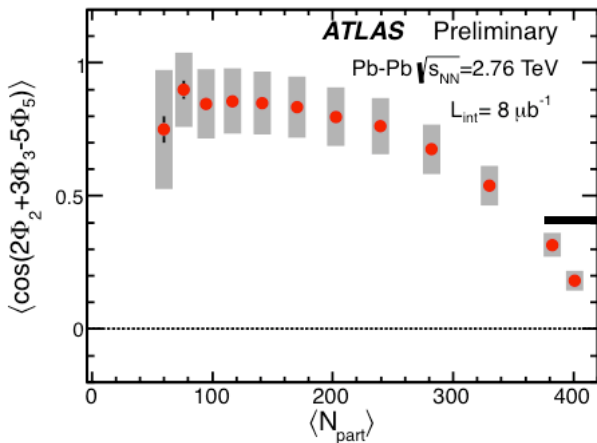
$$\langle \cos 6(\Phi_2 - \Phi_6) \rangle$$



$$\langle \cos 6(\Phi_3 - \Phi_6) \rangle$$



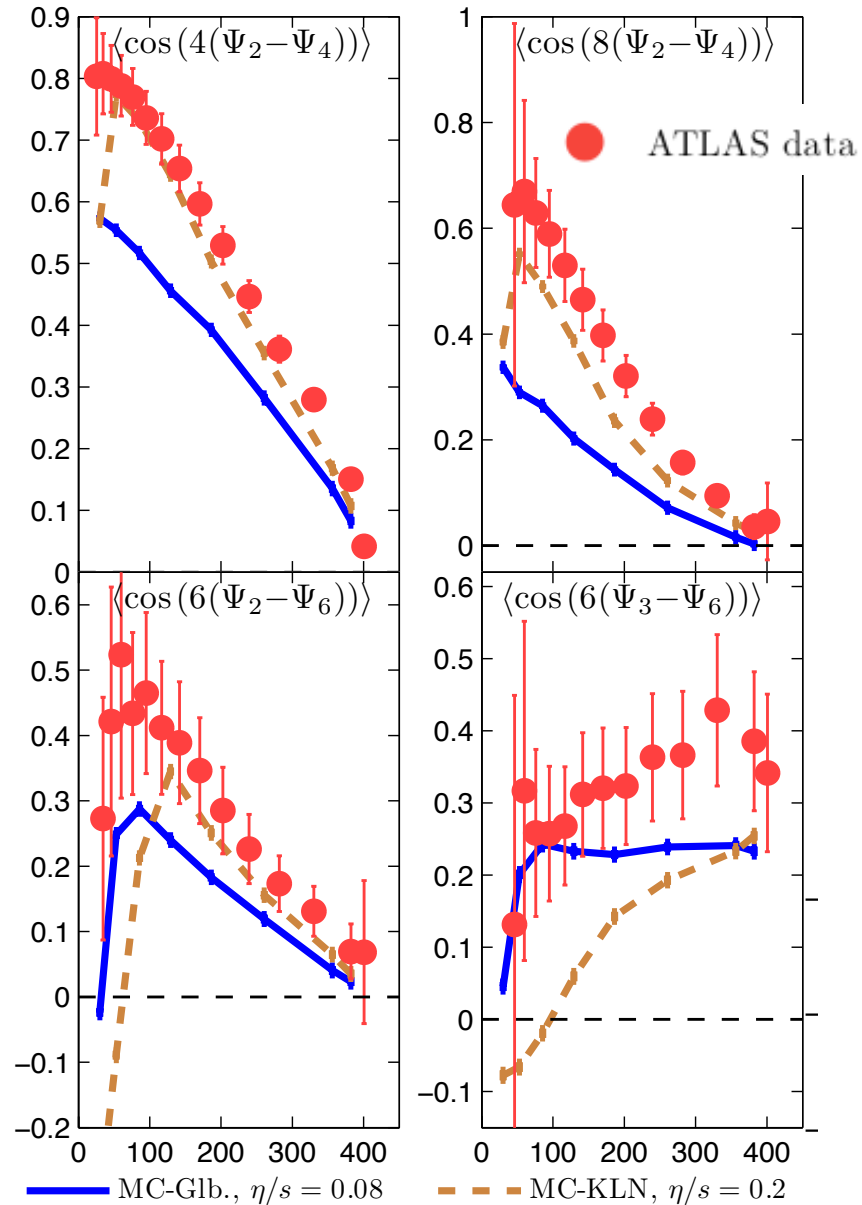
$$\langle \cos(2\Phi_2 + 3\Phi_3 - 5\Phi_5) \rangle$$



$$v_5 e^{-i5\Psi_5} = k\varepsilon_5 + v_2 v_3 e^{-i(2\Psi_2 + 3\Psi_3)} + \dots$$

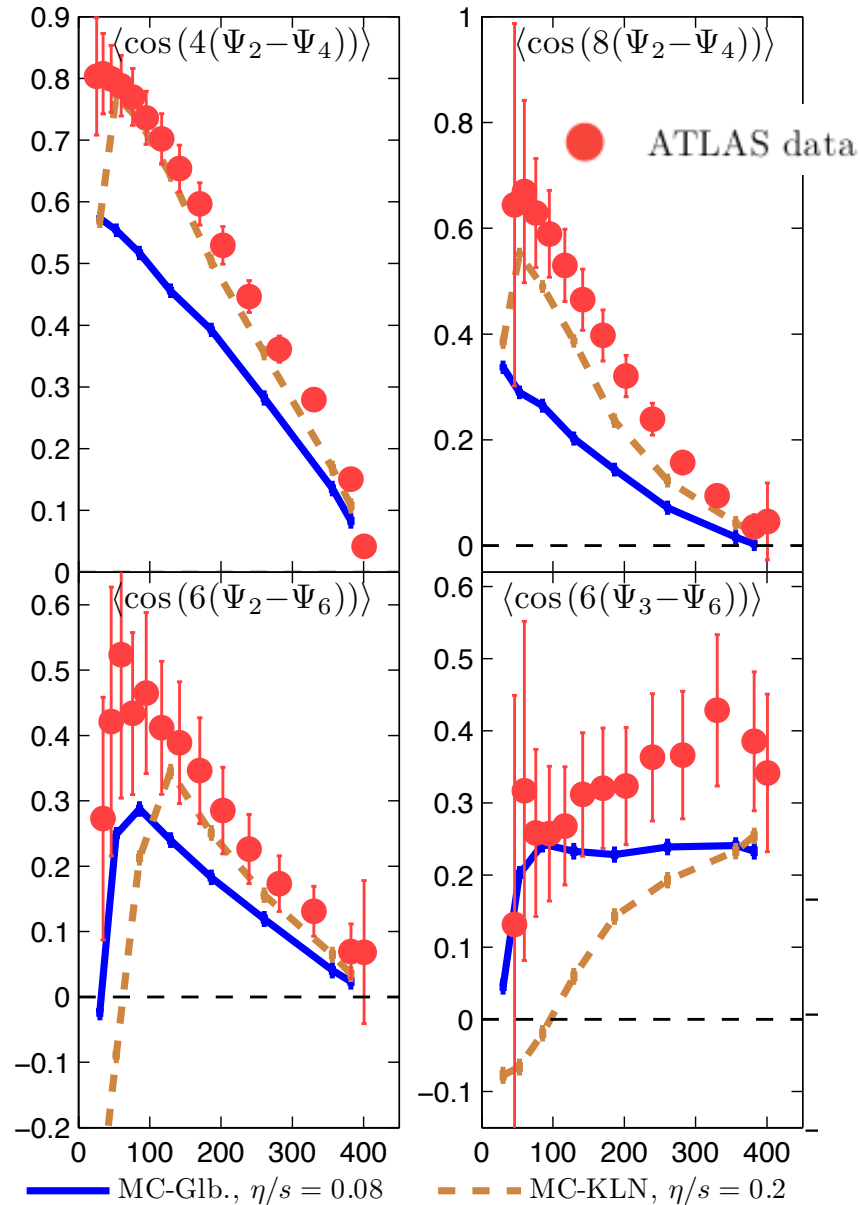
Compare with EbE hydro calculation

Initial geometry + hydrodynamic Zhe & Heinz 1208.1200

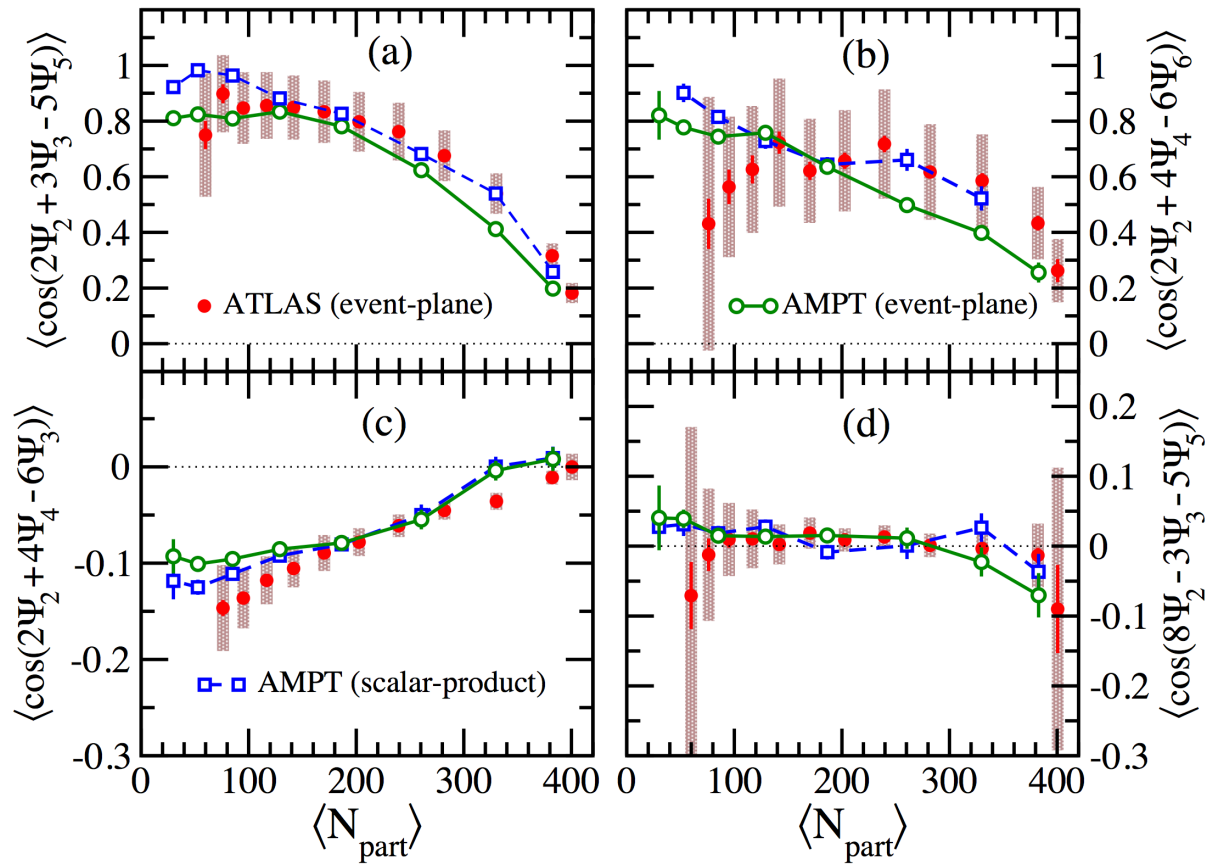


Compare with EbE hydro calculation

Initial geometry + hydrodynamic Zhe & Heinz 1208.1200

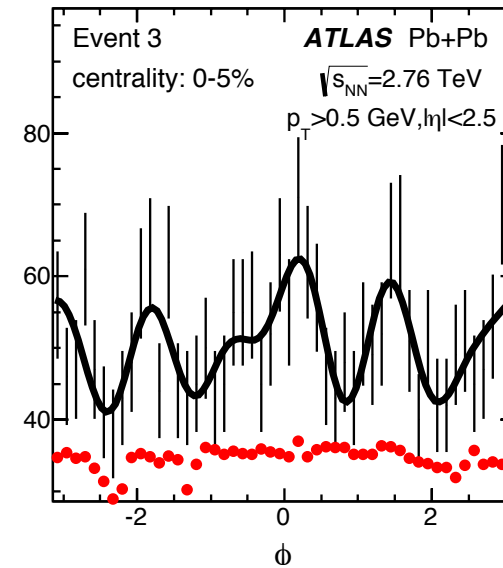
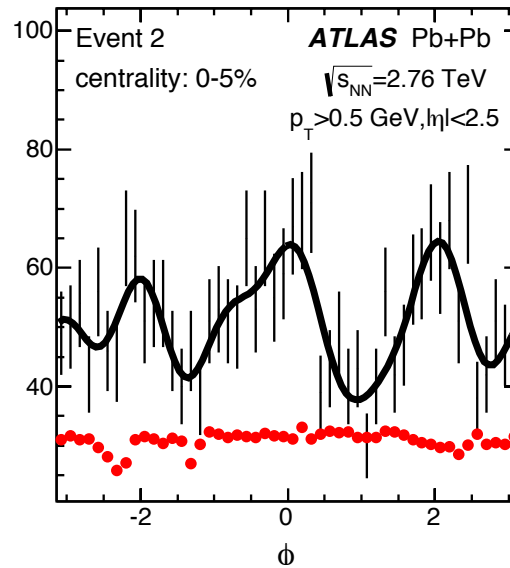
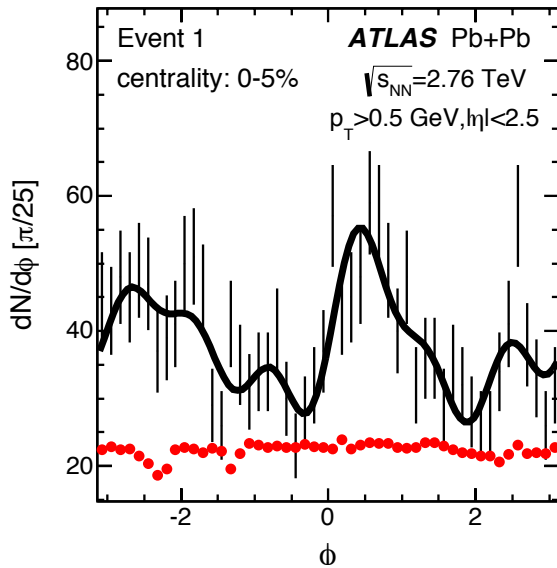


Initial geometry + transport 1307.0980
Bhalerao, et.al.



EbyE hydro and transport models reproduce features in the data

Measuring the $p(v_n)$ distributions

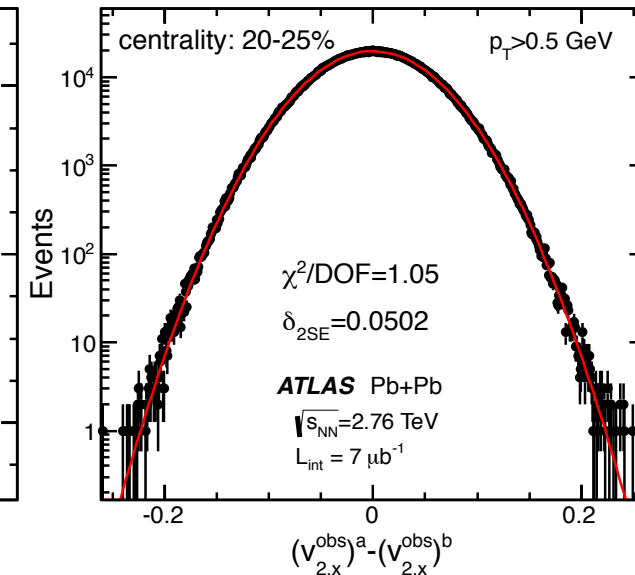
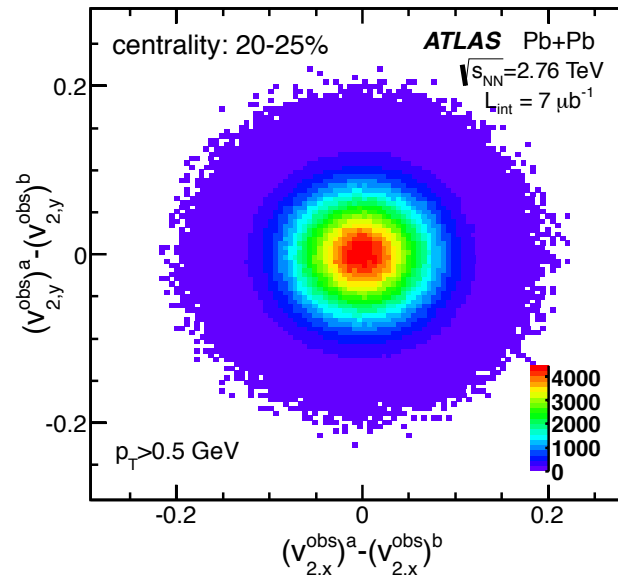


ATLAS
1305.2942

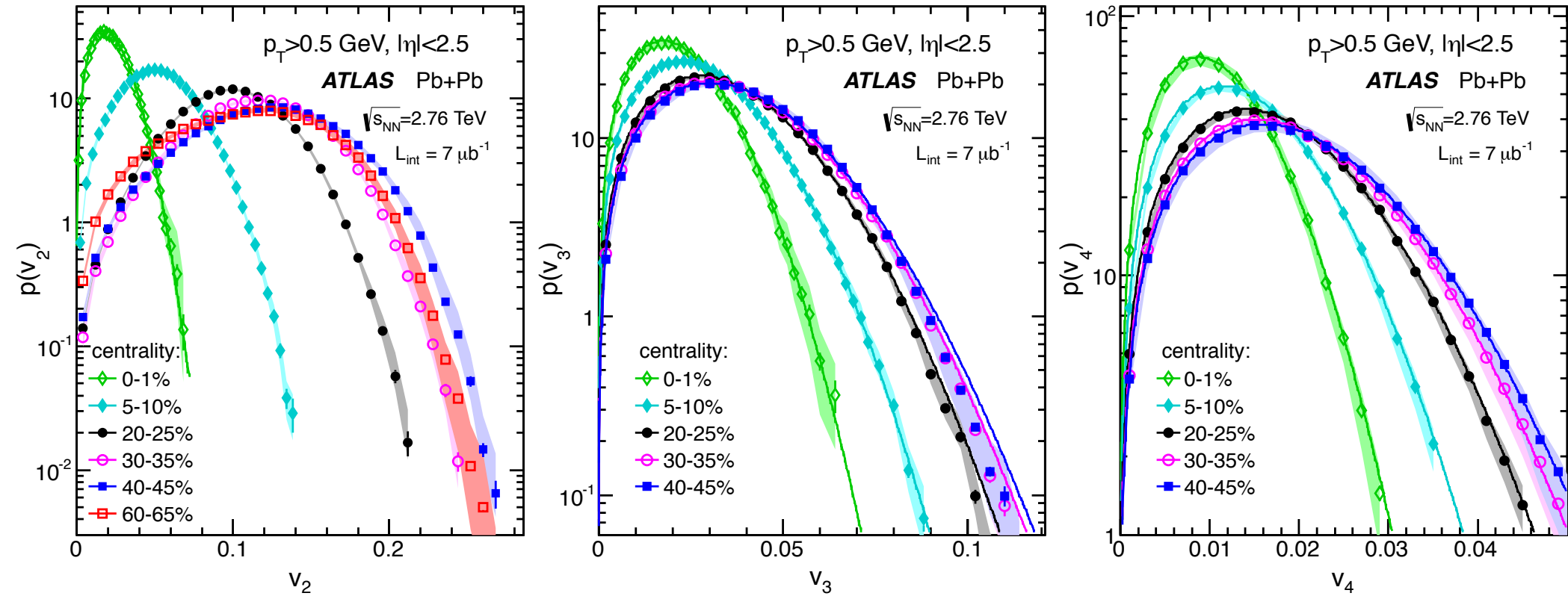
$$\frac{dN}{d\phi} \propto 1 + 2 \sum_n v_n^{\text{obs}} \cos n(\phi - \Phi_n^{\text{obs}})$$

Decompose the ϕ distributions in each event

Finite number & nonflow effects require unfolding (e.g. Bayesian) to recover original distribution



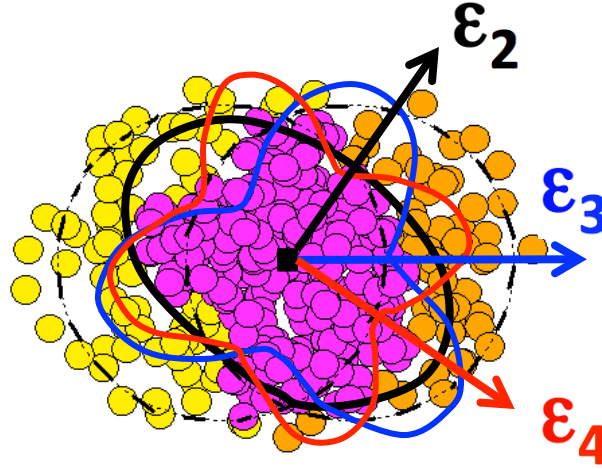
$p(v_n)$ distributions



Probability distribution for v_2 , v_3 and v_4 in many centrality ranges

ATLAS 1305.2942 Submitted to JHEP

Expectation for v_n fluctuations



arXiv: 0708.0800, 0809.2949

$$\vec{\epsilon}_n = \left(\frac{\langle r^n \cos(n\phi) \rangle}{\langle r^n \rangle}, \frac{\langle r^n \sin(n\phi) \rangle}{\langle r^n \rangle} \right)$$

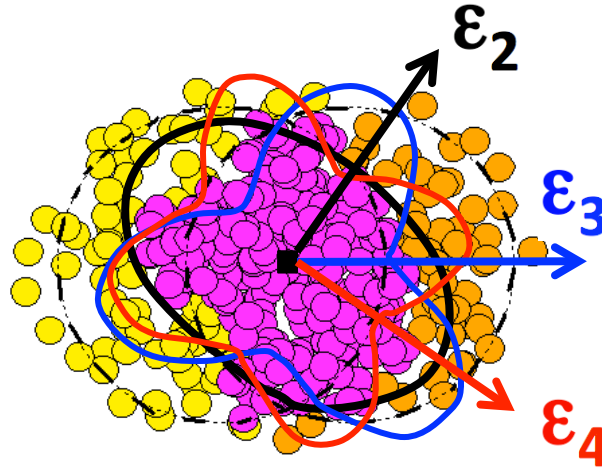
$$\vec{\epsilon}_n = \overset{\rightarrow\text{RP}}{\epsilon}_n + \overset{\rightarrow\text{fluc}}{\Delta}_n$$

$$p(\vec{\epsilon}_n) \propto \exp\left(\frac{-(\vec{\epsilon}_n - \vec{\epsilon}_n^{RP})^2}{2\delta_{\epsilon_n}^2} \right)$$

$\vec{\epsilon}_n^{RP} \rightarrow \text{Mean Geometry}$

$\delta_{\epsilon_n} \rightarrow \text{Fluctuations}$

Expectation for v_n fluctuations



arXiv: 0708.0800, 0809.2949

$$\vec{v}_n = (v_n \cos n\Phi_n, v_n \sin n\Phi_n)$$

$$\vec{v}_n = \vec{v}_n^{\text{RP}} + \vec{p}_n^{\text{fluc}}$$

$$p(\vec{v}_n) \propto \exp\left(\frac{-(\vec{v}_n - \vec{v}_n^{\text{RP}})^2}{2\delta_n^2}\right)$$

$\vec{v}_n^{\text{RP}} \rightarrow \text{Mean Geometry}$

$\delta_n \rightarrow \text{Fluctuations}$

$$\vec{\epsilon}_n = \left(\frac{\langle r^n \cos(n\phi) \rangle}{\langle r^n \rangle}, \frac{\langle r^n \sin(n\phi) \rangle}{\langle r^n \rangle} \right)$$

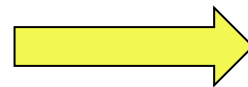
$$\vec{\epsilon}_n = \vec{\epsilon}_n^{\text{RP}} + \Delta_n^{\text{fluc}}$$

$$p(\vec{\epsilon}_n) \propto \exp\left(\frac{-(\vec{\epsilon}_n - \vec{\epsilon}_n^{\text{RP}})^2}{2\delta_{\epsilon_n}^2}\right)$$

$\vec{\epsilon}_n^{\text{RP}} \rightarrow \text{Mean Geometry}$

$\delta_{\epsilon_n} \rightarrow \text{Fluctuations}$

$$\vec{v}_n \propto \vec{\epsilon}_n$$

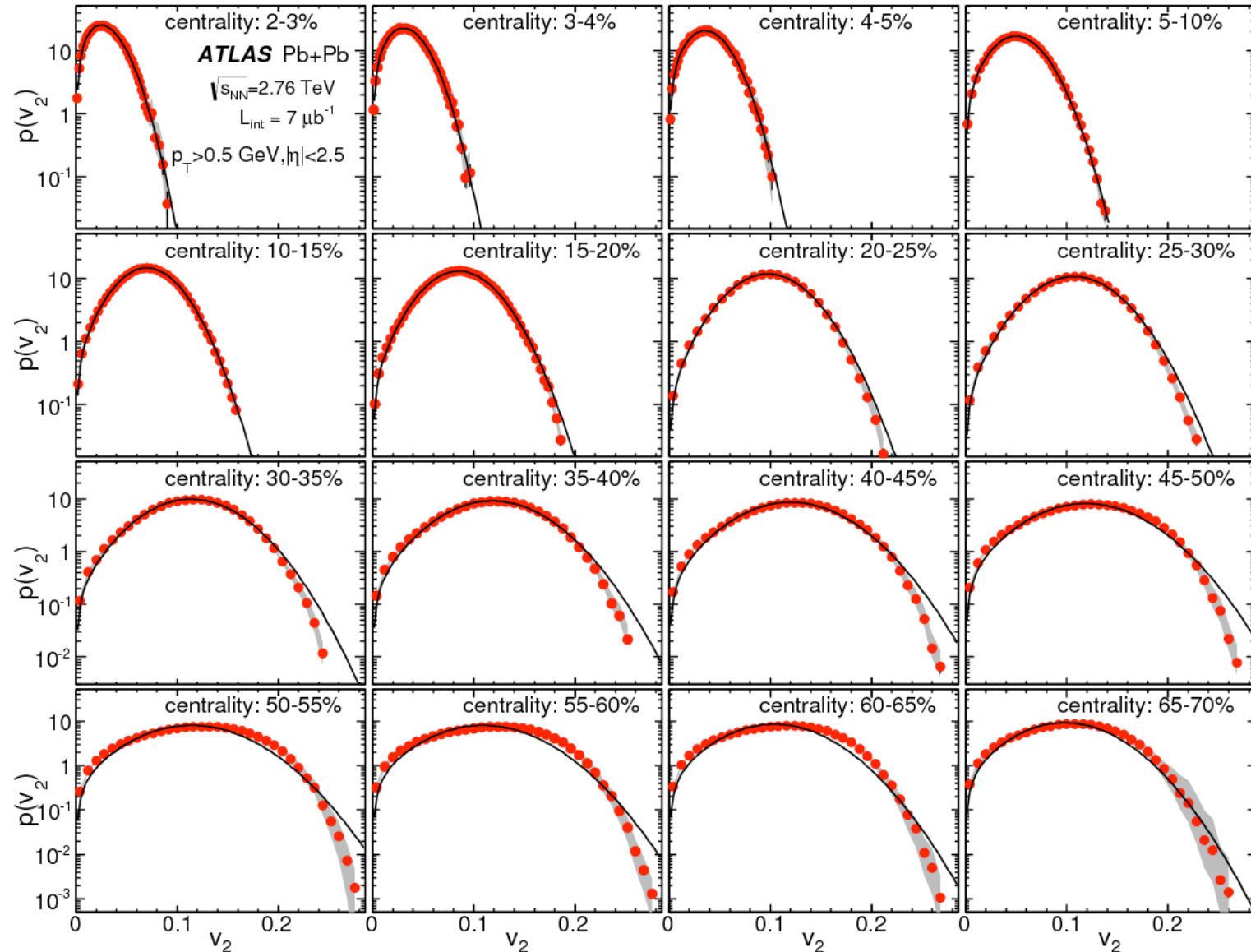


$$p(v_n) \propto v_n \exp\left(\frac{-(v_n^2 + (v_n^{\text{RP}})^2)}{2\delta_n^2}\right) I_0\left(\frac{v_n v_n^{\text{RP}}}{\delta_n^2}\right)$$

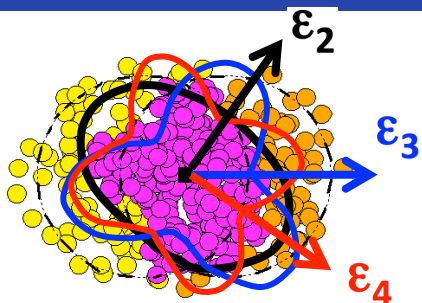
Are flow fluctuations Gaussian?

$$p(\vec{v}_2) \propto \exp\left(\frac{-(\vec{v}_2 - \vec{v}_2^{RP})^2}{2\delta^2}\right) \longrightarrow p(v_2) \propto v_2 \exp\left(\frac{-(v_2^2 + (v_2^{RP})^2)}{2\delta^2}\right) I_0\left(\frac{v_2 v_2^{RP}}{\delta^2}\right)$$

First indication of non-Gaussian behavior



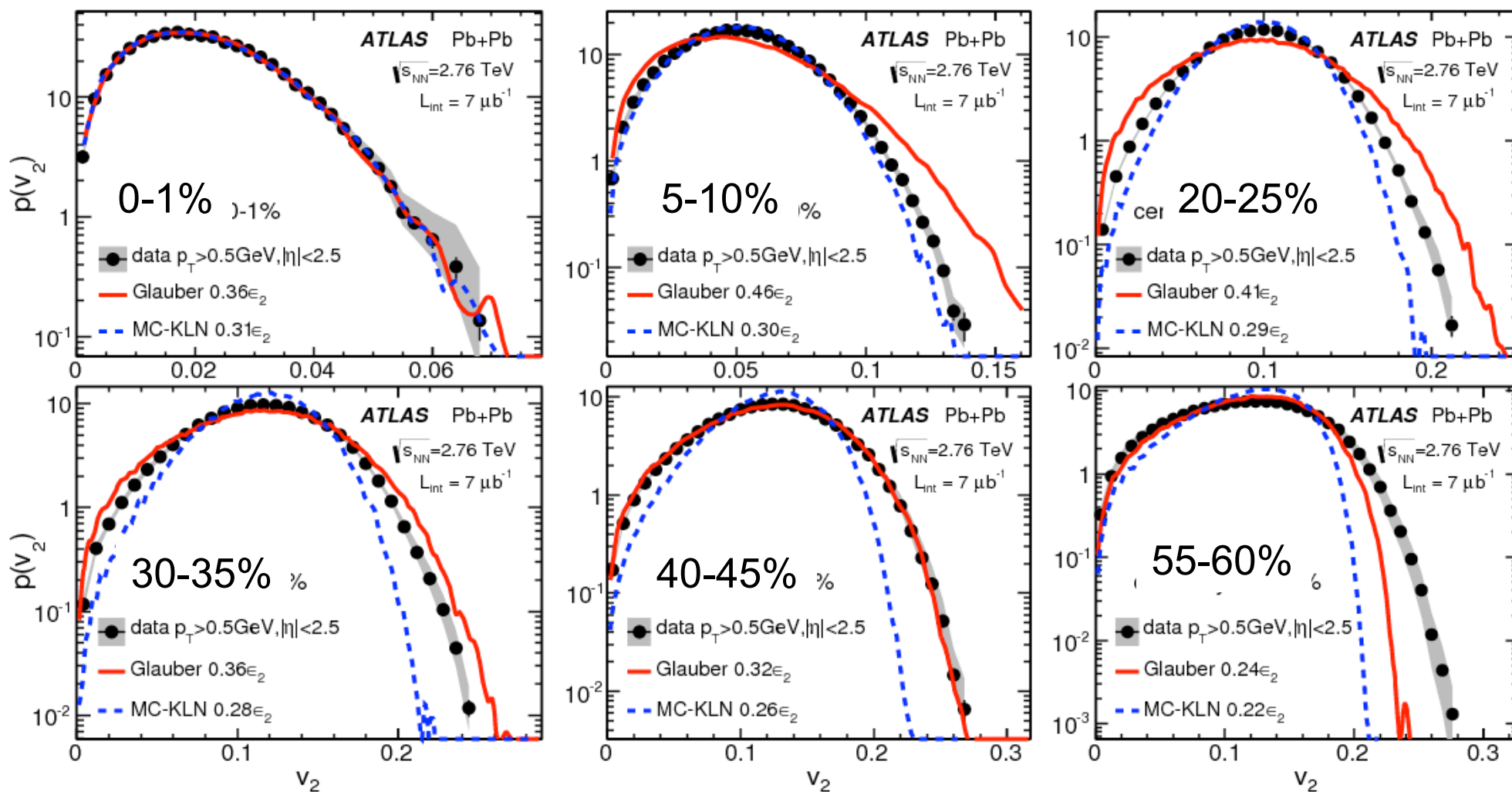
Measuring the hydrodynamic response



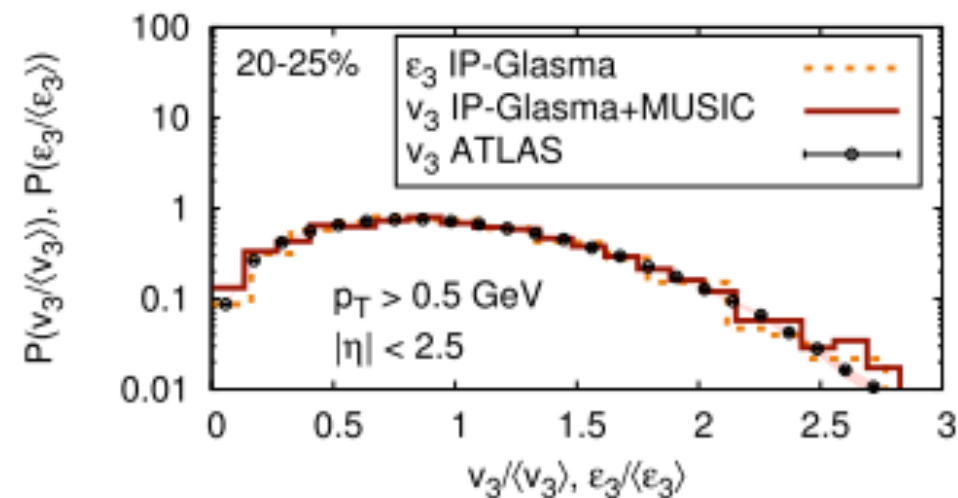
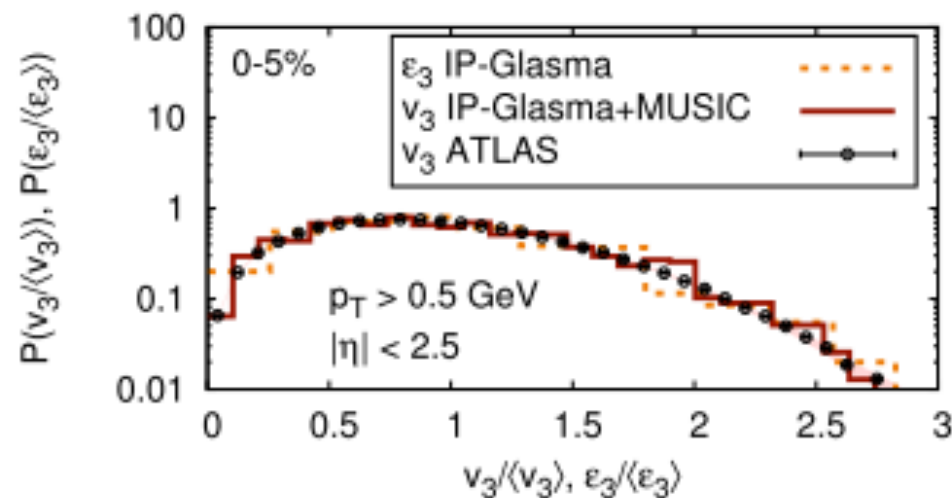
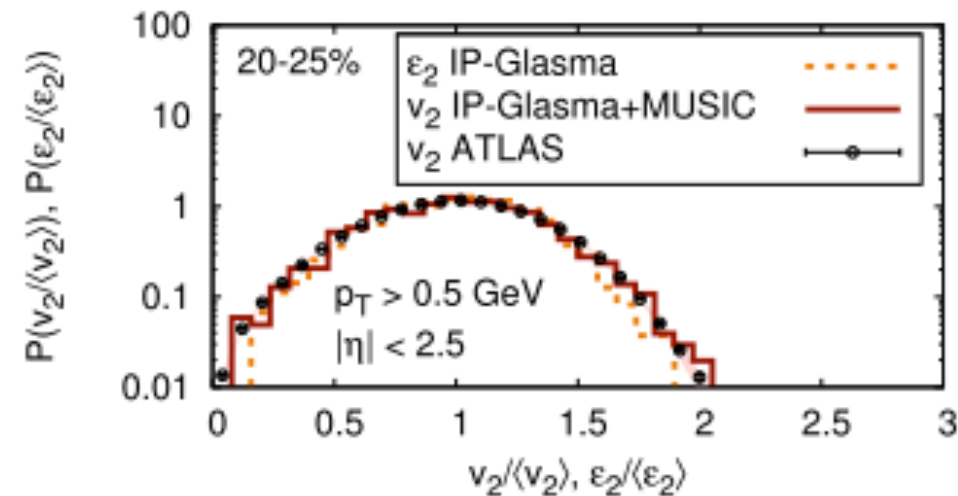
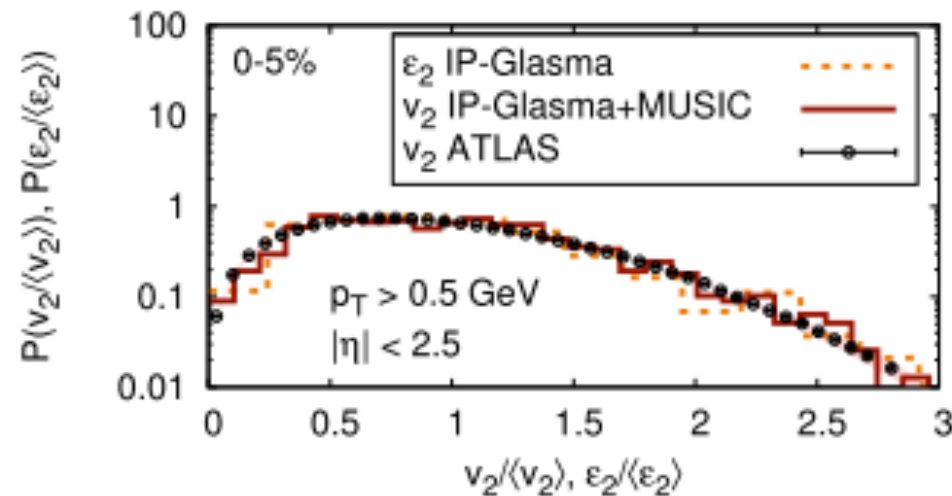
$$v_n \propto \epsilon_n = \frac{\sqrt{\langle r^n \cos n\phi \rangle^2 + \langle r^n \sin n\phi \rangle^2}}{\langle r^n \rangle}$$

Glauber and CGC mc-kln

ϵ_2 distribution is rescaled so $\langle \epsilon_2 \rangle = \langle v_2 \rangle$



arXiv:1301.5893 B. Schenke et.al.



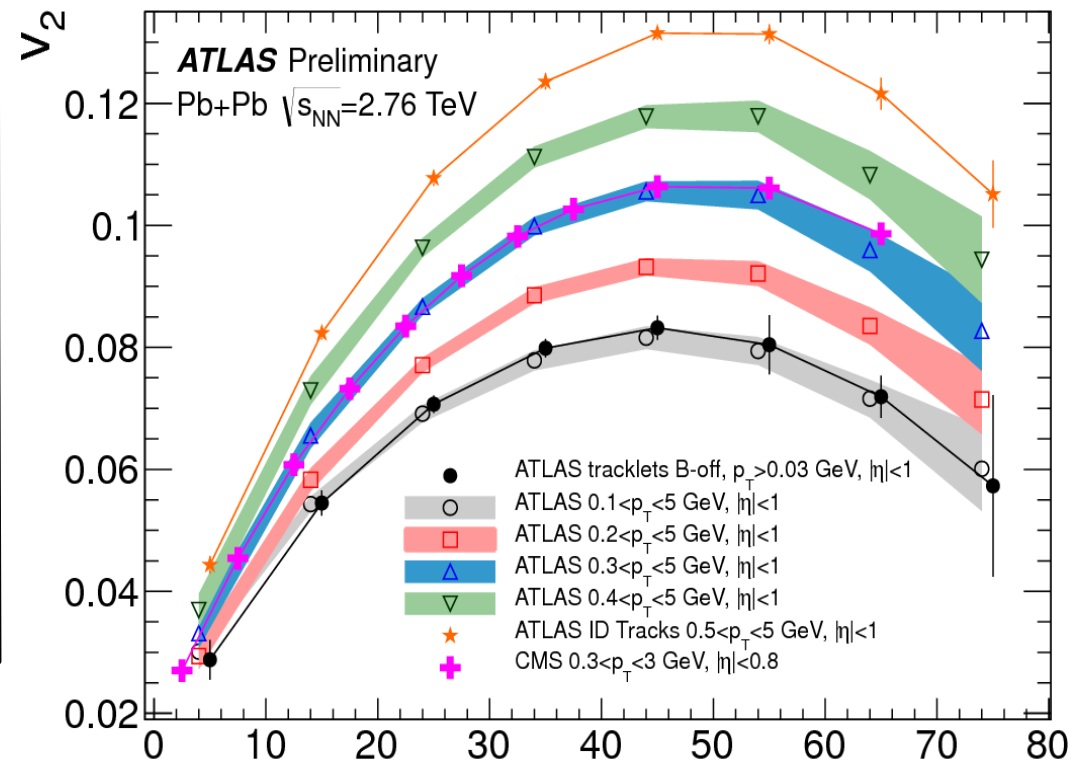
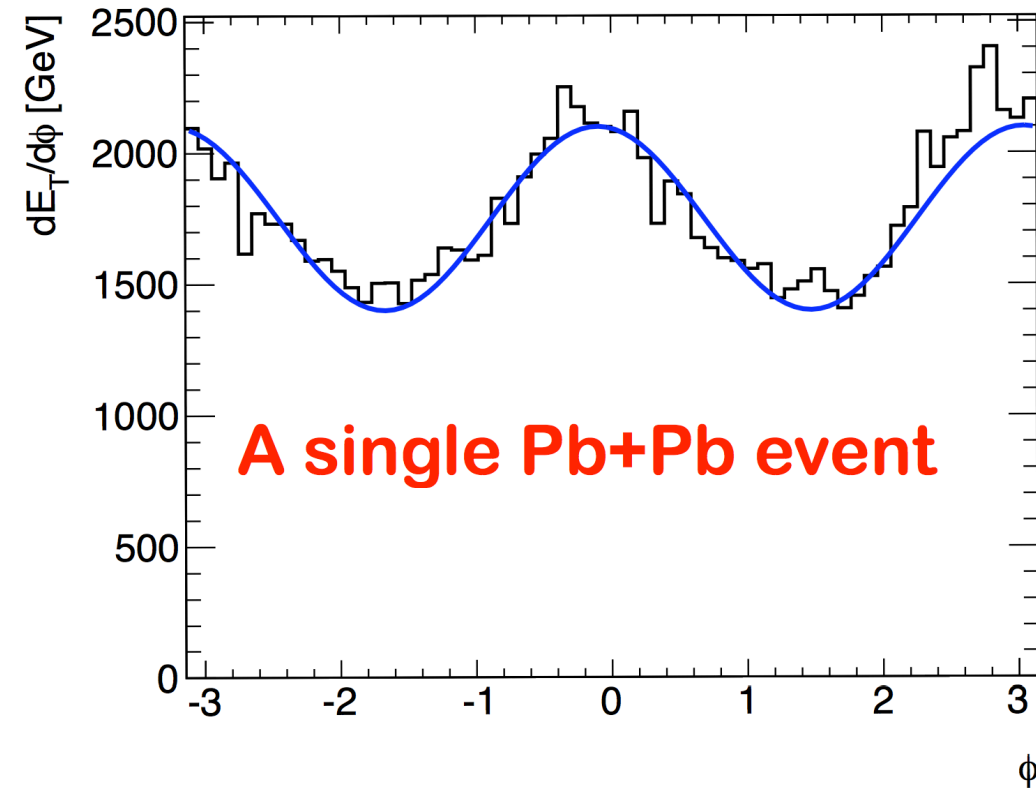
- Model calculation shows good consistency
- But more statistics in theory calculation are needed

Summary

- Detailed differential measurement of $v_n(p_T, \eta, \text{centrality})$ for $n=2-6$
 - Detailed constraints on geometry models and η/s

- Event-by-event fluctuation of the QGP and its evolution can be accessed via $p(v_n, v_m, \dots, \Phi_n, \Phi_m, \dots)$
 - First measurements of 2- and 3- event plane correlations: $p(\Phi_n, \Phi_m)$ and $p(\Phi_n, \Phi_m, \Phi_L)$.
 - First measurements of the $p(v_2)$, $p(v_3)$ and $p(v_4)$.
 - Strong non-linear effects in the hydrodynamic response to initial geometry fluctuations.

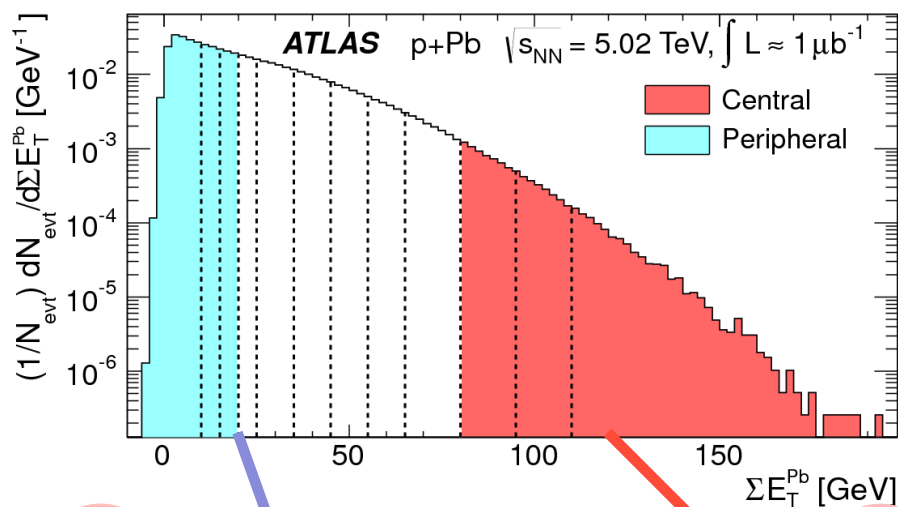
Event anisotropy is large



$$\frac{dN}{d\phi} = N_0 \left[1 + 2 \sum_n v_n \cos n(\phi - \Phi_n) \right]^{\text{tile}}$$

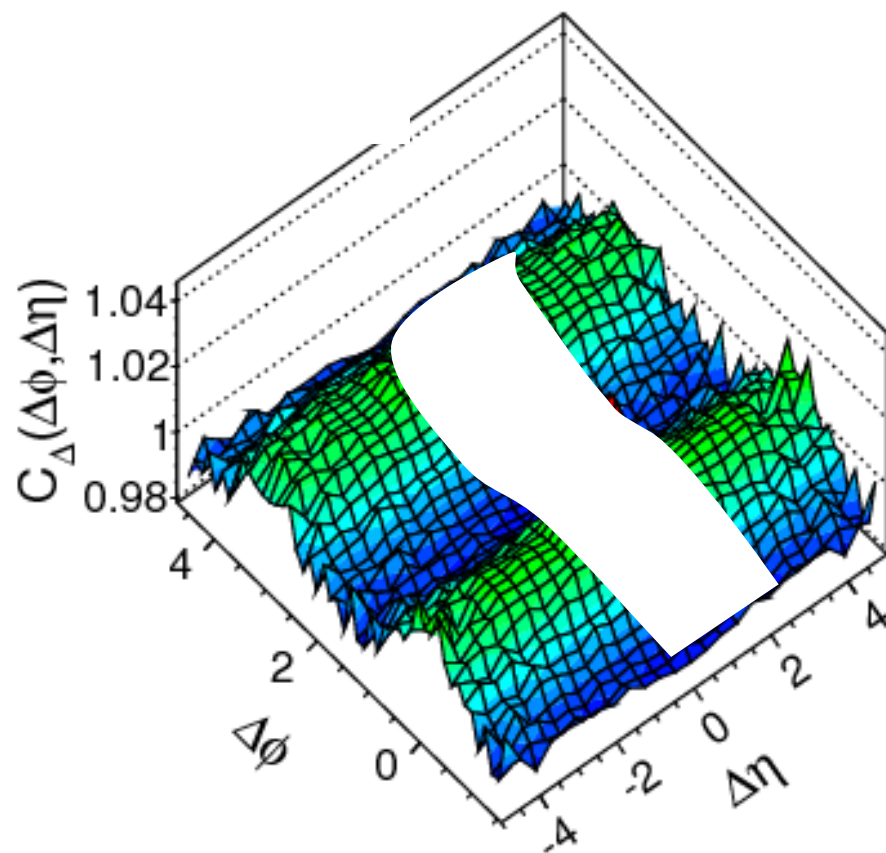
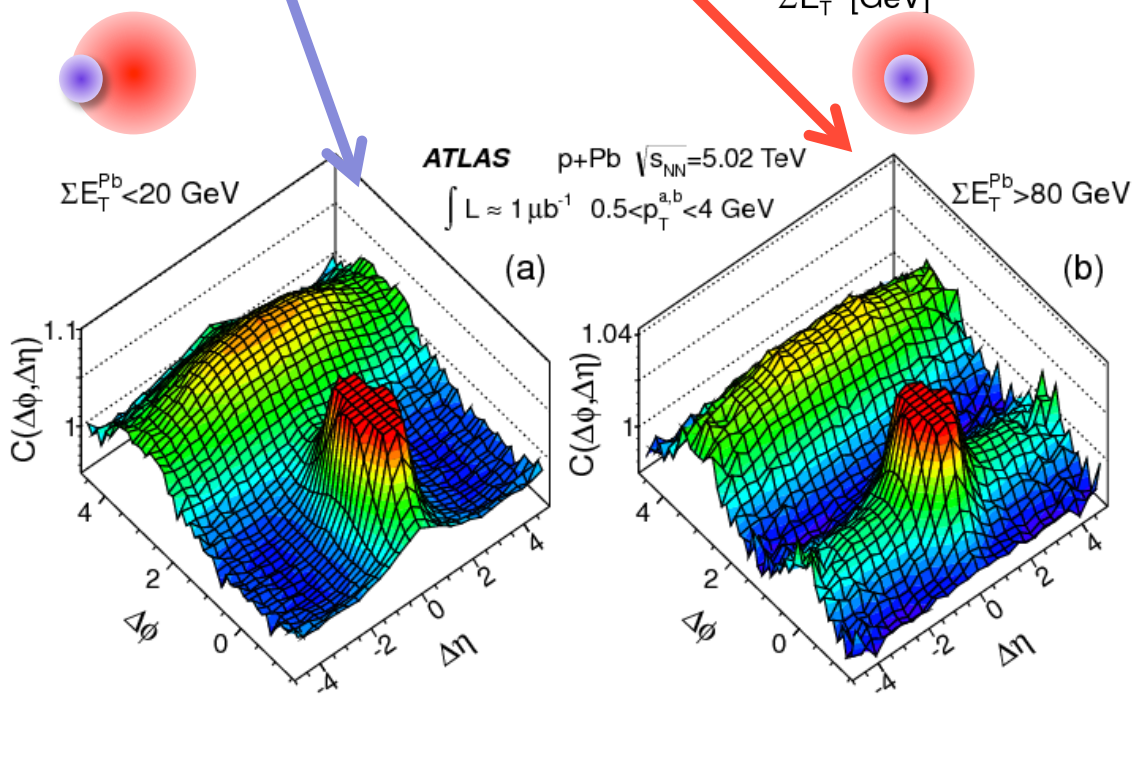
- Large energy modulation, $N_0 v_2$, on the order of hundreds of GeV.
 $N_0 v_2 \gg \sqrt{N_0}$ statistical fluctuations or $v_2 \gg 1/\sqrt{N_0}$
- The concept of collective flow and global event direction Φ_n , are valid.

Double ridge in p+Pb collisions



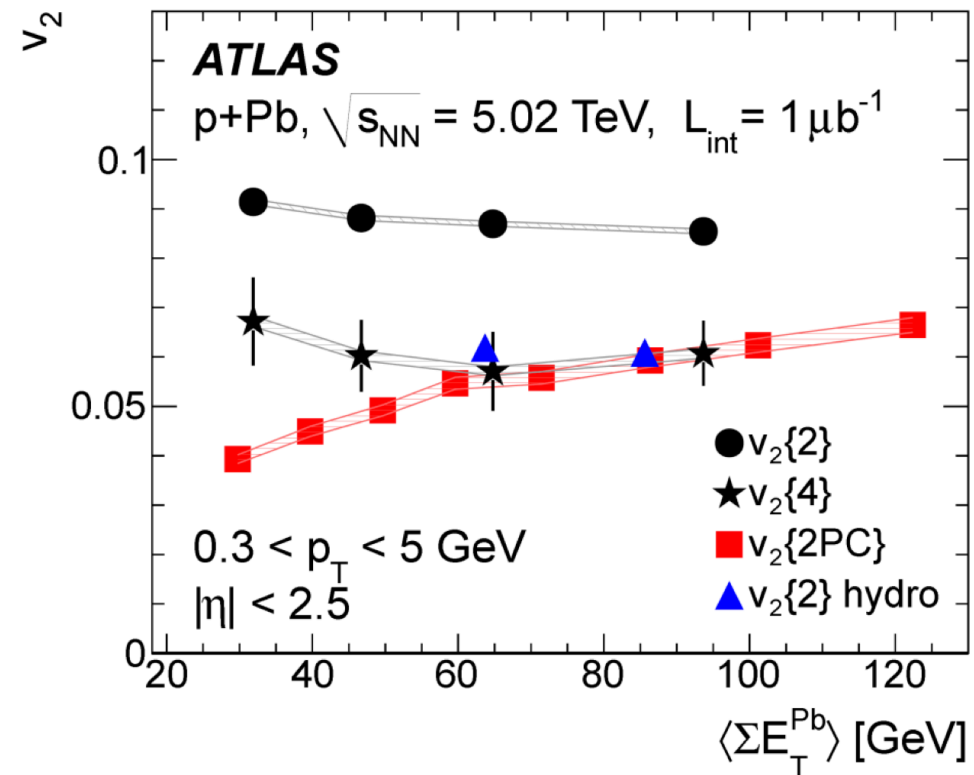
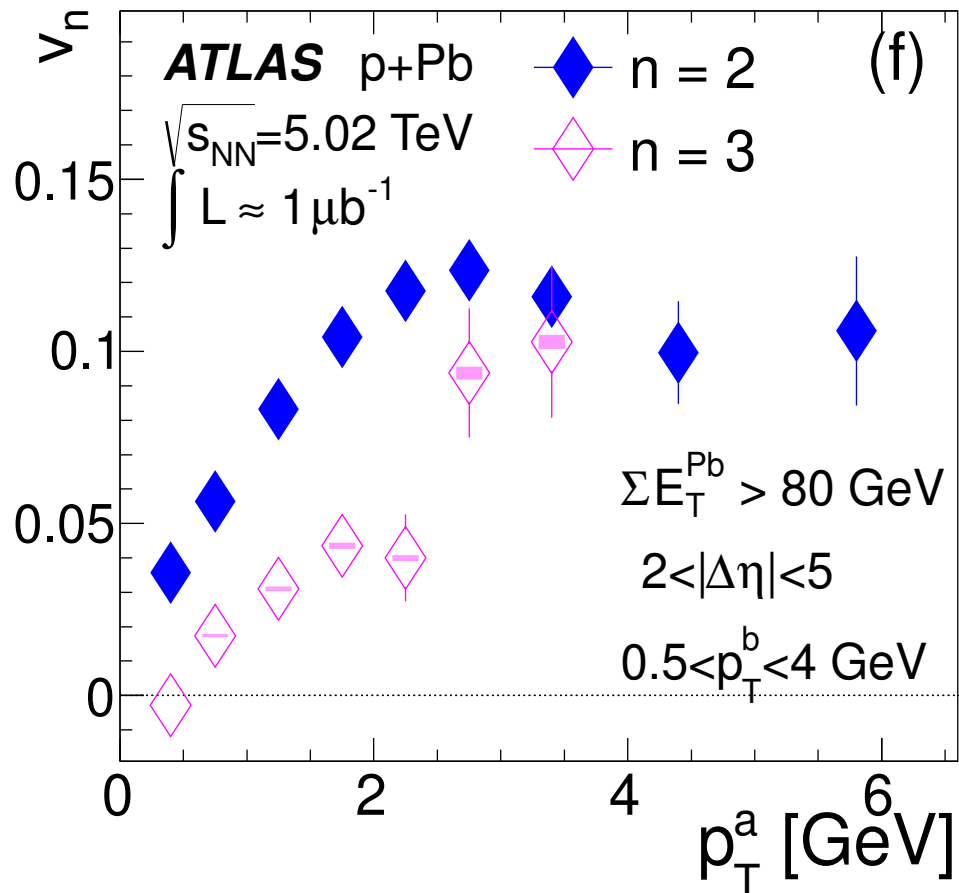
Influence of away-side jet estimated from low multiplicity events

Discovery of the double-ridge in high multiplicity p+Pb



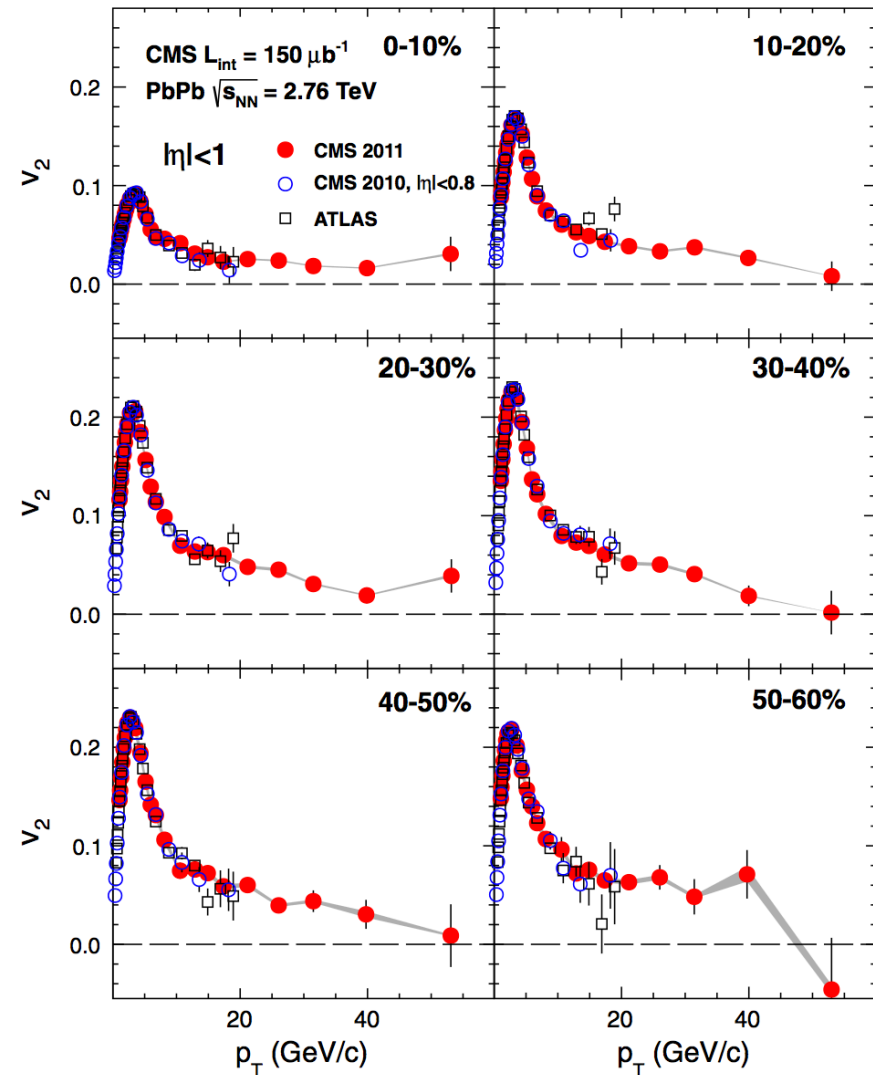
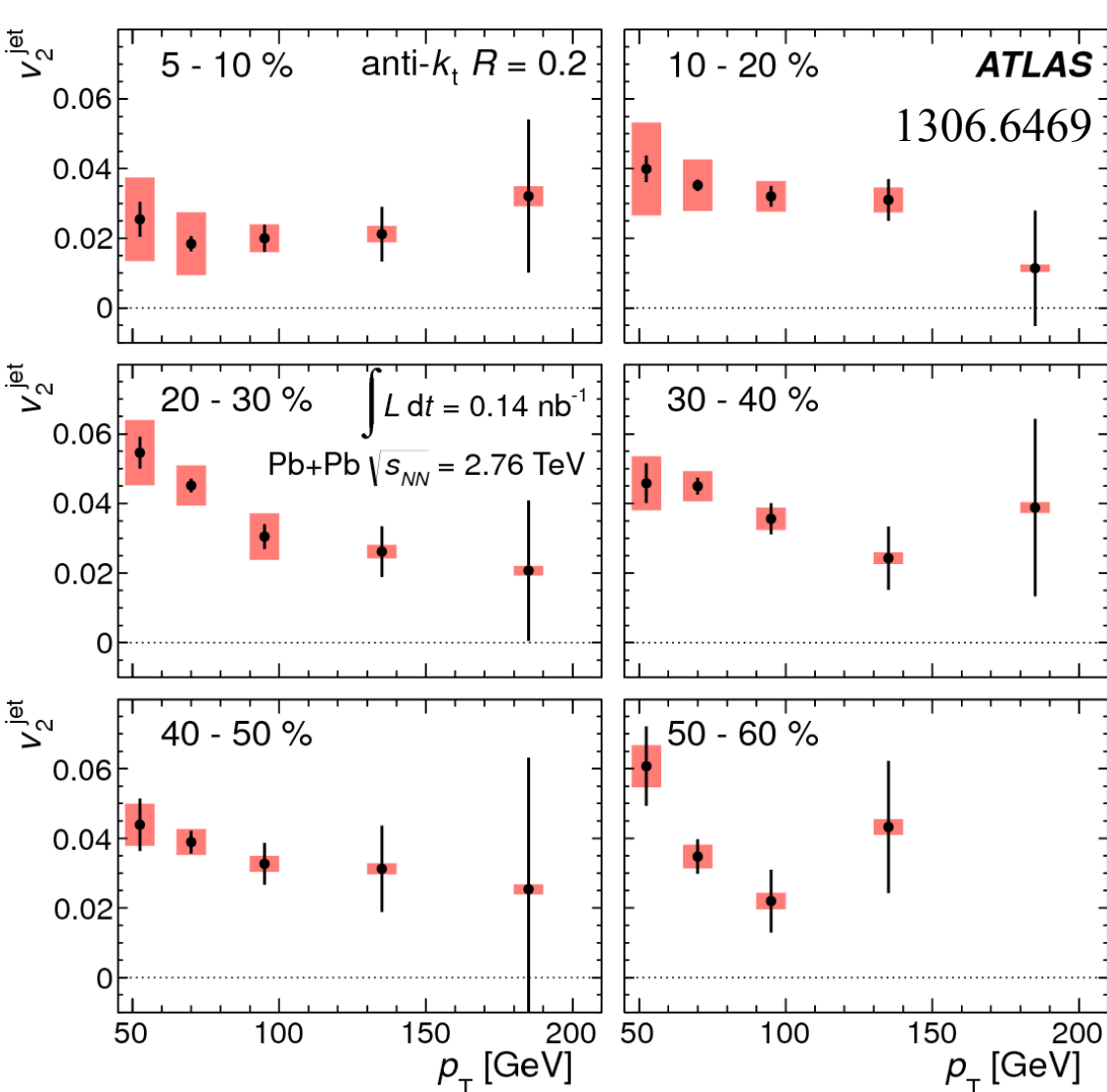
v_2 and v_3 from p+Pb

- Significant v_2 and v_3 , comparable to Pb+Pb collisions.
- Significant $v_2\{4\} \approx 0.06$ suggest large collective motion.
- v_2 values compatible with hydrodynamics (also CGC)
 - But v_3 , $v_2\{4\}$, and PID v_2 (ALICE) challenging for CGC.

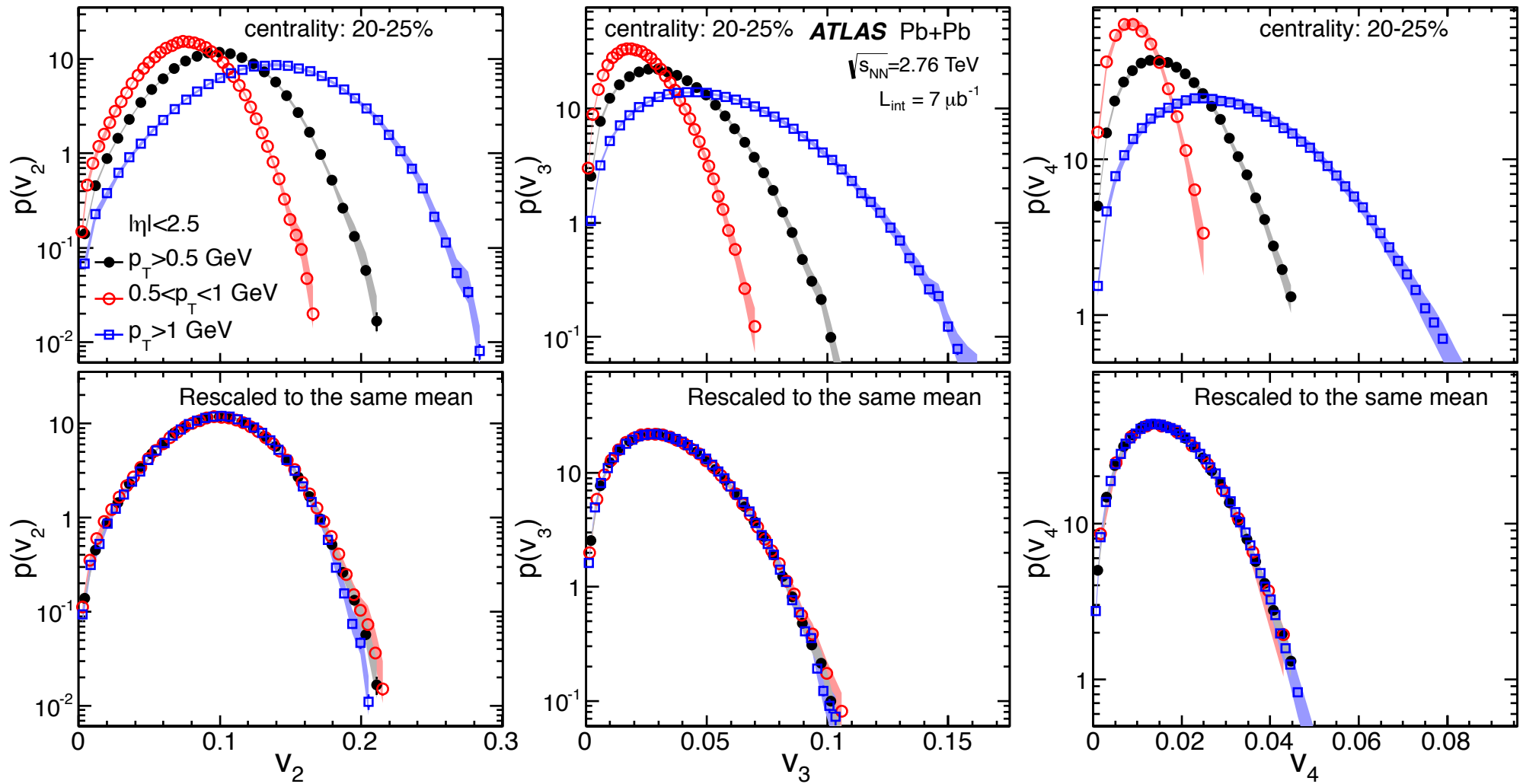


Jet tomography

- Significant jet v_2 over 50-200 GeV, clearly sensitive to Path length
 - Comparable to charged hadron v_2 at high p_T
- Better constraint on $\Delta E(L)$?



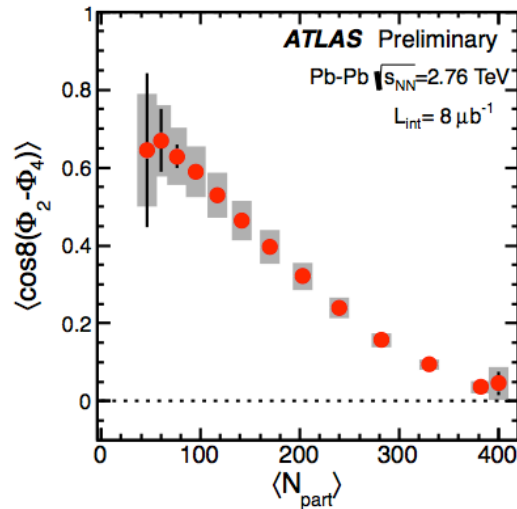
All p_T respond: same shape



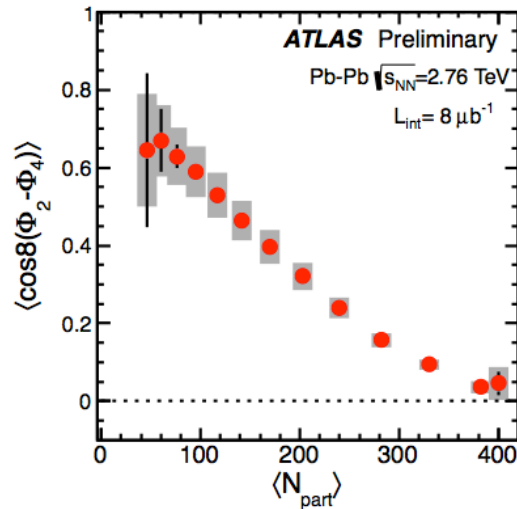
Low and high p_T appear different, but coincide when rescaled to same $\langle v_n \rangle$

Two-plane correlations

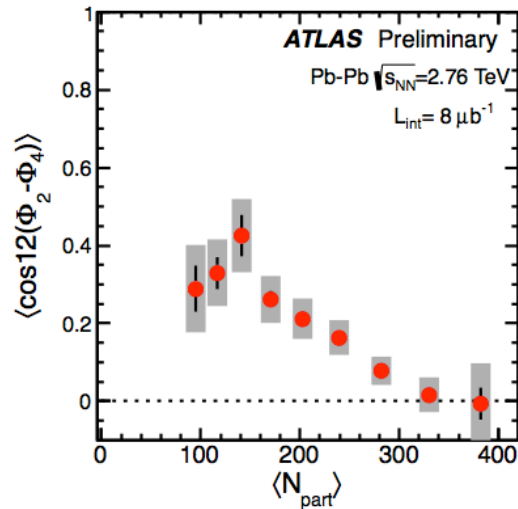
$$\langle \cos(1 \times 4(\Phi_2 - \Phi_4)) \rangle$$



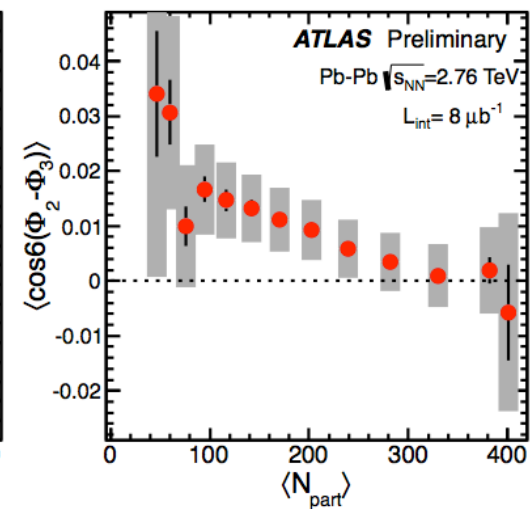
$$\langle \cos(2 \times 4(\Phi_2 - \Phi_4)) \rangle$$



$$\langle \cos(3 \times 4(\Phi_2 - \Phi_4)) \rangle$$

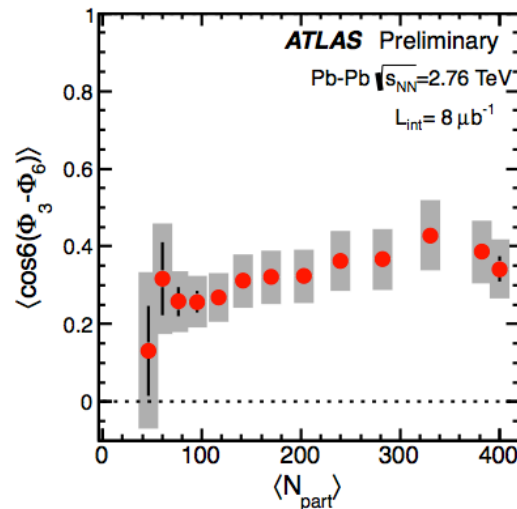


$$\langle \cos(1 \times 6(\Phi_2 - \Phi_3)) \rangle$$

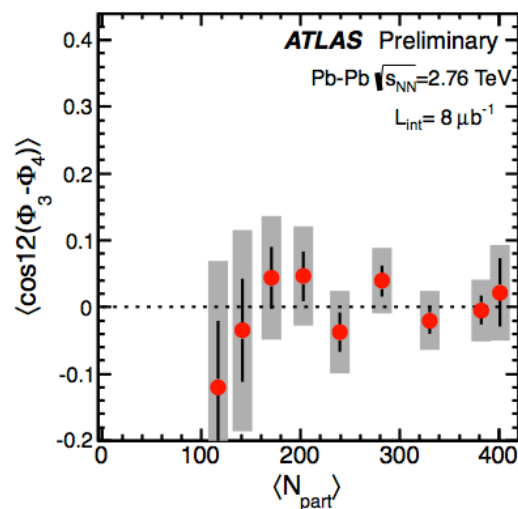


$$\langle \cos(1 \times 6(\Phi_2 - \Phi_6)) \rangle$$

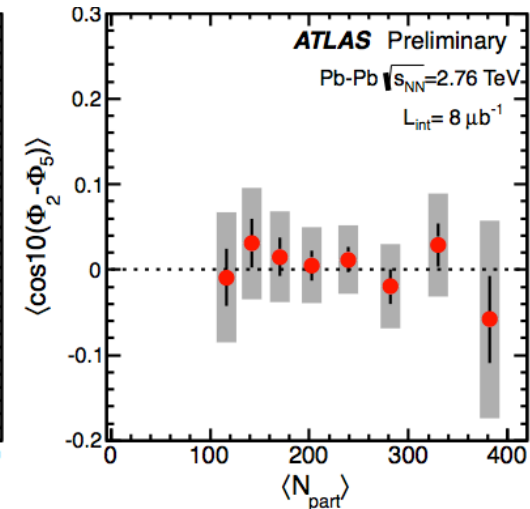
$$\langle \cos(1 \times 6(\Phi_3 - \Phi_6)) \rangle$$



$$\langle \cos(1 \times 12(\Phi_3 - \Phi_4)) \rangle$$

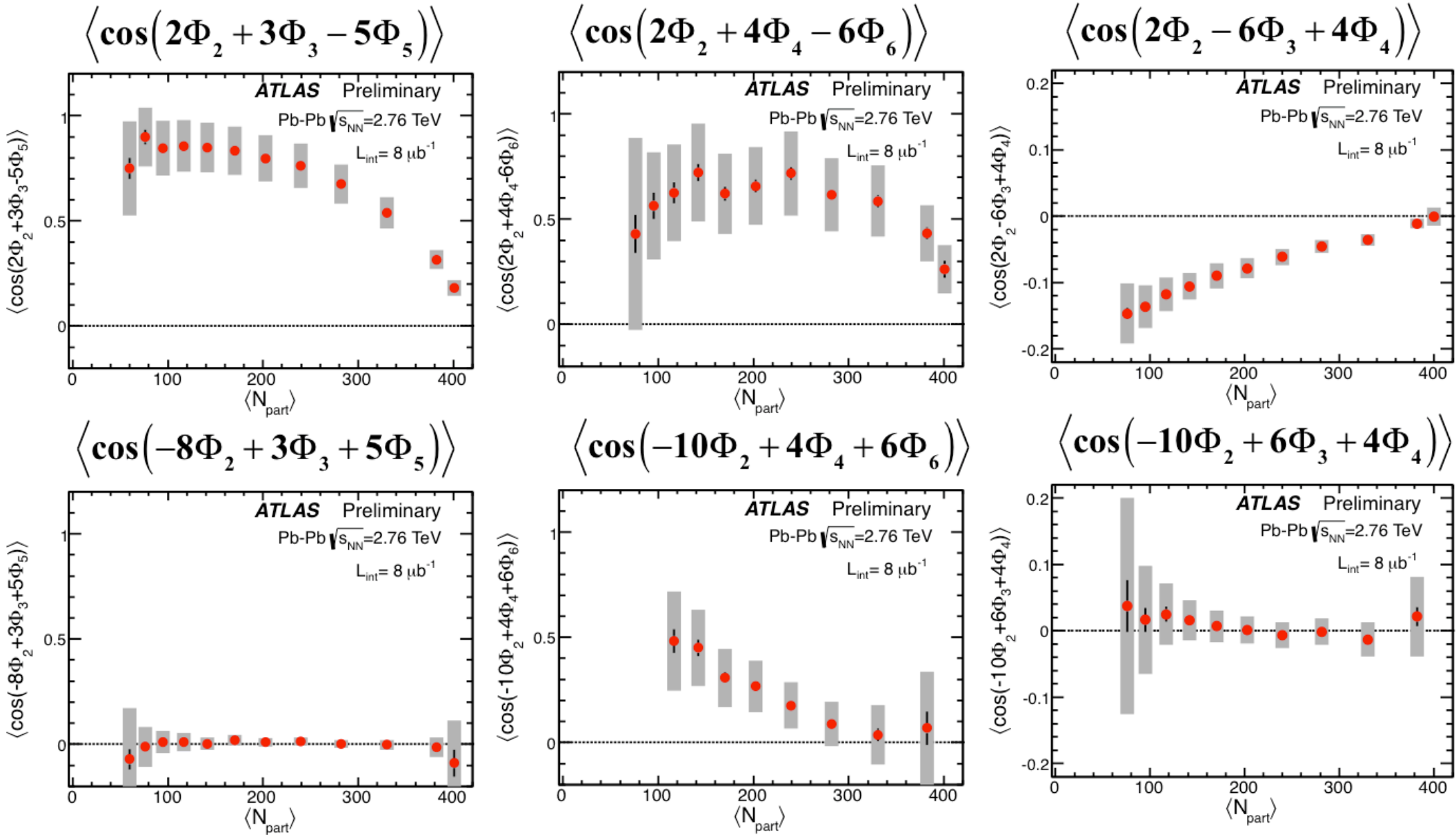


$$\langle \cos(1 \times 10(\Phi_2 - \Phi_5)) \rangle$$



Rich patterns for the centrality dependence

Three-plane correlations



Rich patterns for the centrality dependence