SINGLE-INCLUSIVE JET PRODUCTION IN ELECTRON-NUCLEON COLLISIONS AT NNLO

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INTRODUCTION

- A large part of our knowledge about the internal structure of hadrons, and about QCD in general, comes from lepton-hadron scattering experiments.
- Traditionally we have studied the processes $lN \rightarrow lX$, $lN \rightarrow ljX$ and $lN \rightarrow lhX$
- ✤ Recently there has been a growing interest in $lN \rightarrow jX$ and $lN \rightarrow hX$ from both the theory and experimental communities. Applications include:
 - Measurement of the strong coupling constant
 - Extraction of fragmentation functions
 - * Better our understanding of single-spin asymmetries in $pp^{\uparrow} \rightarrow hX$. Large all the way from fixed-target to collider energies
 - Improve our understanding of factorization:
 - * Study of multiple parton interactions (MPI) and higher twist operators
 - Transverse-momentum-dependent (TMD) parton distributions

This talk: $lN \rightarrow jX$ through NNLO ($\mathcal{O}(\alpha^2 \alpha_s^2)$) in pQCD

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WHY NNLO?

(Semi)Inclusive DIS vs single-inclusive jet production

DIS $e^- N \to e^- X$

Inclusive jet production $e^- N \rightarrow j X$

★ Lepton observed
★ Cut on Q² = -q²
★ Hard scale Q

- * Inclusive over lepton * Cut on p_T^{jet} * Hard scale p_T^{jet}
- * Equivalent at LO. Lepton recoils against jet (A)

 $p_T^{jet} = Q \, \cos\left(\frac{\theta}{2}\right)$

- * At NLO, inclusive jet production probes the $Q^2 \sim 0$ region, unavailable in DIS
 - New singularities, new photon-initiated partonic channels
 - Large corrections from this region

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WHY NNLO?

NLO QCD correction is small for inclusive DIS (~5%), but it is huge for single-inclusive jet production (>100%).



[Hinderer, Schlegel, Vogelsang '15]

NNLO needed for:

Assessing stability of perturbative seriesPrecise theoretical predictions

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THE SETUP (LO)

At leading order, the process $lN \rightarrow jX$ is trivial

$$d\sigma_{\rm LO} = \int \frac{d\xi_1}{\xi_1} \frac{d\xi_2}{\xi_2} \sum_{q} \left[f_{q/H}^1 f_{l/l}^2 d\hat{\sigma}_{ql}^{(2,0)} + f_{\bar{q}/H}^1 f_{l/l}^2 d\hat{\sigma}_{\bar{q}l}^{(2,0)} \right]$$
$$f_{i/j}^k = f_{i/j}(\xi_k) \qquad \qquad f_{l/l}(\xi) = \delta(1-\xi) \qquad \qquad d\hat{\sigma}_{ql}^{(m,n)} \propto \alpha^n \alpha_s^m$$

The partonic cross sections are

$$\mathrm{d}\hat{\sigma}_{ql}^{(2,0)} = \frac{(4\pi\alpha)^2}{8s} e_q^2 \,\mathrm{d}\Phi_B(p_3, p_4; p_1, p_2) |\mathcal{M}_B|^2 J^{(1)}(p_3)$$



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THE SETUP (NLO)

At NLO

- * Real and virtual corrections to ql channel.
- * gl channel opens up

$$d\hat{\sigma}_{ql}^{(2,1)} = \int d\Phi_R |\mathcal{M}_R^{(ql)}|^2 J^{(2)}(p_3, p_5) + \int d\Phi_B |\mathcal{M}_V^{(ql)}|^2 J^{(1)}(p_3)$$
$$d\hat{\sigma}_{gl}^{(2,1)} = \int d\Phi_R |\mathcal{M}_R^{(gl)}|^2 J^{(2)}(p_3, p_5)$$

- We handle the QCD soft and collinear IR singularities with standard NLO techniques, and mass factorization as usual
- We also handle the QED singularity $(p_l || p_{l'})$ with standard NLO techniques and mass factorization
 - \implies Introduce (LO) photon-initiated processes



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THE SETUP (NLO)

•NLO correction to $lN \to jX$:

$$d\sigma_{\rm NLO} = \int \frac{d\xi_1}{\xi_1} \frac{d\xi_2}{\xi_2} \left\{ f_{g/H}^1 f_{l/l}^2 d\hat{\sigma}_{gl}^{(2,1)} + f_{g/H}^1 f_{\gamma/l}^2 d\hat{\sigma}_{g\gamma}^{(1,1)} \right. \\ \left. + \sum_q \left[f_{q/H}^1 f_{l/l}^2 d\hat{\sigma}_{ql}^{(2,1)} + f_{\bar{q}/H}^1 f_{l/l}^2 d\hat{\sigma}_{\bar{q}l}^{(2,1)} \right. \\ \left. + f_{q/H}^1 f_{\gamma/l}^2 d\hat{\sigma}_{q\gamma}^{(1,1)} + f_{\bar{q}/H}^1 f_{\gamma/l}^2 d\hat{\sigma}_{\bar{q}\gamma}^{(2,1)} \right] \right\}$$

Perturbative photon-in-lepton distribution (Weizsäcker-Williams)

$$f_{\gamma/l}(\xi) = \frac{\alpha}{2\pi} P_{\gamma l}(\xi) \left[\ln\left(\frac{\mu^2}{\xi^2 m_l^2}\right) - 1 \right] + \mathcal{O}(\alpha^2)$$
$$P_{\gamma l}(\xi) = \frac{1 + (1 - \xi)^2}{\xi}$$

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THE SETUP (NNLO)

♣At NNLO

- * Genuine NNLO corrections to ql and gl channels
 - QCD IR divergencies handled with N-Jettiness subtraction [Boughezal, Focke, Liu, Petriello '15; Gaunt, Stahlhofen, Tackmann, Walsh '15]
 - * QED IR divergencies $(p_l || p_{l'}, p_l || p_{l'} || p_q)$ handled with antenna subtraction [Daleo, Gehrmann, Gehrmann-De Ridder, Luisoni '10; Boughezal, Gehrmann-De Ridder, Ritzmann '10; Gehrmann, Gehrmann-De Ridder, Ritzmann '12]
- * NLO corrections to $q\gamma$ and $g\gamma$ channels. All singularities treated with antennae.
- *New $q\bar{q}$ and qg channels



THE SETUP (NNLO)

Quark-in-lepton distribution computed perturbatively from DGLAP equation

$$\mu^2 \frac{\partial f_{q/l}}{\partial \mu^2}(\xi, \mu^2) = e_q^2 \frac{\alpha}{2\pi} \int_{\xi}^1 \frac{\mathrm{d}z}{z} \left[P_{q\gamma}^{(0)}(z) f_{\gamma/l}\left(\frac{\xi}{z}, \mu^2\right) + \frac{\alpha}{2\pi} P_{ql}^{(1)}(z) f_{l/l}\left(\frac{\xi}{z}, \mu^2\right) \right]$$

$$P_{q\gamma}^{(0)}(x) = x^2 + (1-x)^2$$

$$P_{ql}^{(1)}(x) = -2 + \frac{20}{9x} + 6x - \frac{56x^2}{9} + \left(1 + 5x + \frac{8x^2}{3}\right)\log(x) - (1+x)\log^2(x)$$

• Boundary condition $f_{q/l}(\xi, m_l^2) = 0$

$$\begin{split} f_{q/l}(\xi,\mu^2) &= e_q^2 \left(\frac{\alpha}{2\pi}\right)^2 \left\{ \left[\frac{1}{2} + \frac{2}{3\xi} - \frac{\xi}{2} - \frac{2\xi^2}{3} + (1+\xi)\log\xi\right] \log^2\left(\frac{\mu^2}{m_l^2}\right) \right. \\ &+ \left[-3 - \frac{2}{\xi} + 7\xi - 2\xi^2 + \left(-5 - \frac{8}{3\xi} + \xi + \frac{8\xi^2}{3}\right)\log\xi - 3(1+\xi)\log^2\xi\right] \log\left(\frac{\mu^2}{m_l^2}\right) \right\} \end{split}$$

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1-JETTINESS SUBTRACTION

Starting point: dimensionless 1-jettiness event shape [Kang, Lee, Stewart '13]



1-JETTINESS SUBTRACTION



• Introduce internal cutoff \mathcal{T}_1^{cut} . Partition RR and RV phase space

$$d\sigma_{ql}^{(2,2)} = \int d\Phi_{\rm B} |\mathcal{M}_{\rm VV}|^2 + \int d\Phi_{\rm R} |\mathcal{M}_{\rm RV}|^2 \theta_1^< + \int d\Phi_{\rm RR} |\mathcal{M}_{\rm RR}|^2 \theta_1^< + \int d\Phi_{\rm R} |\mathcal{M}_{\rm RV}|^2 \theta_1^> + \int d\Phi_{\rm RR} |\mathcal{M}_{\rm RR}|^2 \theta_1^> \equiv d\sigma_{ql}^{(2,2)} (\mathcal{T}_1 < \mathcal{T}_1^{cut}) + d\sigma_{ql}^{(2,2)} (\mathcal{T}_1 > \mathcal{T}_1^{cut})$$

$$\theta_1^{<} = \theta(\mathcal{T}_1^{cut} - \mathcal{T}_1) \qquad \theta_1^{>} = \theta(\mathcal{T}_1 - \mathcal{T}_1^{cut})$$

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NNLO CROSS SECTION BELOW 1-JETTINESS CUT

All-orders resummation of \mathcal{T}_1 in DIS for the limit $\mathcal{T}_1 \ll 1$ known [Kang, Lee, Stewart '13]

$$\frac{\mathrm{d}\sigma}{\mathrm{d}\mathcal{T}_{1}} = \int \mathrm{d}\Phi_{B} \int \mathrm{d}t_{J} \mathrm{d}t_{B} \mathrm{d}k_{S} \,\delta\left(\mathcal{T}_{1} - \frac{t_{J}}{Q^{2}} - \frac{t_{B}}{Q^{2}} - \frac{k_{S}}{Q}\right)$$

$$\times \sum_{q} J_{q}(t_{J}, \mu) \,S(k_{S}, \mu) H_{q}(\Phi_{2}, \mu) B_{q}(t_{B}, x, \mu) + \dots$$
Power corrections $\propto \mathcal{T}_{1}^{cut}$

Small for small cutoffs

◆Expand through $\mathcal{O}\left(\alpha^2 \alpha_s^2\right)$ to obtain $d\sigma_{ql}^{(2,2)}(\mathcal{T}_1 < \mathcal{T}_1^{cut})$, $d\sigma_{gl}^{(2,2)}(\mathcal{T}_1 < \mathcal{T}_1^{cut})$ ◆All pieces known to this order

- * Jet function $J_q(t_J, \mu)$ [Becher and Neubert '06; Becher and Bell '10]
- * Beam function $B_q(t_B, x, \mu)$ [Gaunt, Stahlhofen, Tackmann '14]
- * Soft function $S(k_S, \mu)$ [Boughezal, Liu, Petriello '15]
- * Hard function $H_q(\Phi_2, \mu)$ [Matsuura, van der Marck, van Neerven '88 ; Becher, Neubert, Pecjak '06]

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DISTRESS: DIS Through a Robust Enabling Subtraction Scheme



Parton-level event generator for inclusive jet production in eN collisions at NNLO
Fully differential

Arbitrary cuts on jet and final state lepton

Parallelized Monte Carlo integration

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VALIDATION

Inclusive DIS cross section with $\sqrt{s} = 100 \text{ GeV}$, $Q^2 > 100 \text{ GeV}^2$, $\mu_R = \mu_F = Q$ and CT14nnlo PDFs

q channel *q* channel Check cutoff independence of 0.000 result -0.002 Determine range of cutoffs for which power corrections are -0.004negligibly small r_{NNLO}/σ_{LO} -0.006 Agreement with NNLO inclusive cross section -0.008computed with structure functions -0.010[Zijlstra, van Neerven '92; Moch, Vermaseren '99] $-0.012\frac{1}{10^{-5}}$ 10^{-5} 10^{-4} 5×10^{-5} $\mathcal{T}_1^{\mathrm{cut}}$ $\mathcal{T}_1^{\mathrm{cut}}$

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RESULTS

Using DISTRESS, we produced differential distributions with proposed EIC settings

- ★ √s = 100 GeV
 ★ $p_T^{jet} > 5 \text{ GeV}$ ★ $|\eta_{jet}| < 2$ ★ Anti-kt jet algorithm with R = 0.5★ $\mu_R = \mu_F = p_T^{jet}$ ★ α = 1/137.036
 ★ $m_e = 0.511 \text{ MeV}$
- CT14 (LO, NLO, NNLO) PDF sets

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RESULTS: Q^2 DISTRIBUTION



*NNLO correction is small in DIS region (high Q^2) region, but large (50%) at $Q^2 \sim 0$ *Shift is positive for $Q^2 \sim 0$, negative in DIS region

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RESULTS: JET TRANSVERSE MOMENTUM DISTRIBUTION



*NNLO correction is large and positive for low p_T^{jet} , small and negative for large p_T^{jet} *NNLO shows an increase in scale dependence at low p_T^{jet}

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RESULTS: JET TRANSVERSE MOMENTUM DISTRIBUTION



- * qq and gq channels dominate the NNLO correction (left) and the cross section at NNLO (right) for low p_T^{jet}
- *They are LO at $\mathcal{O}(\alpha^2 \alpha_s^2)$ and drive the increase in the scale dependence of the NNLO cross section at low p_T^{jet}
- No single partonic channel furnishes a good approximation to the shape of the full NNLO correction

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RESULTS: JET RAPIDITY DISTRIBUTION



♦NNLO correction is small for $\eta_{jet} < 1$, sizable as $\eta_{jet} \rightarrow 2$ ♦NNLO scale uncertainty in the region $\eta_{jet} < 0$ larger that at NLO

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RESULTS: JET RAPIDITY DISTRIBUTION



Large scale uncertainty in the region $\eta_{jet} < 0$ is driven by the quark-quark channel, which is effectively LO at $\mathcal{O}(\alpha^2 \alpha_s^2)$

As $\eta_{jet} \rightarrow 2$ the NNLO correction is largely dominated by the gluon-photon channel

No single partonic channel furnishes a good approximation to the shape of the full NNLO correction

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SUMMARY

- We have performed a full calculation of the $O(\alpha^2 \alpha_s^2)$ perturbative corrections to jet production in electron-nucleon collisions, using N-jettiness subtraction
- We have shown that upon integration over the final-state hadronic phase we reproduce the known NNLO result for the inclusive structure functions
- We have implemented our results in a fully differential parton-level event generator DISTRESS
- We have shown numerical results for jet production at a proposed future EIC
 - * Several new partonic channels appear at the $O(\alpha^2 \alpha_s^2)$ level, which have an important effect on the kinematic distributions of the jet
 - No single partonic channel furnishes a good approximation to the full NNLO result
 - * The magnitudes of the corrections we find indicate that higher-order predictions will play an important role in achieving the precision needed to understand the proton structure at the EIC

PHOTON AND QUARK IN LEPTON DISTRIBUTIONS



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