

# Top Mass Measurements with/without Grooming



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Advances in QCD and Applications to Hadron Colliders  
Workshop at Argonne National Lab  
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# Outline

- Top Mass Measurements at the LHC

$$M_t^{\text{peak}} = m_t + (\text{nonperturbative effects}) + (\text{perturbative effects})$$

- Factorization for  $e^+e^- \rightarrow t\bar{t}$
- Top Mass Calibration for Monte Carlo Generators  
[Butenschoen, Dehnadi, Hoang, Mateu, Preisser, IS arXiv:1608.01318]
- Factorization for  $pp \rightarrow t\bar{t}$  with & without Jet grooming
- Predictions for LHC top mass measurements with SoftDrop  
[A.Hoang, S.Mantry, A.Pathak, IS (soon)]
- Conclude

# LHC & Tevatron Top Mass Measurements

Use Direct Reconstruction to obtain sensitivity:

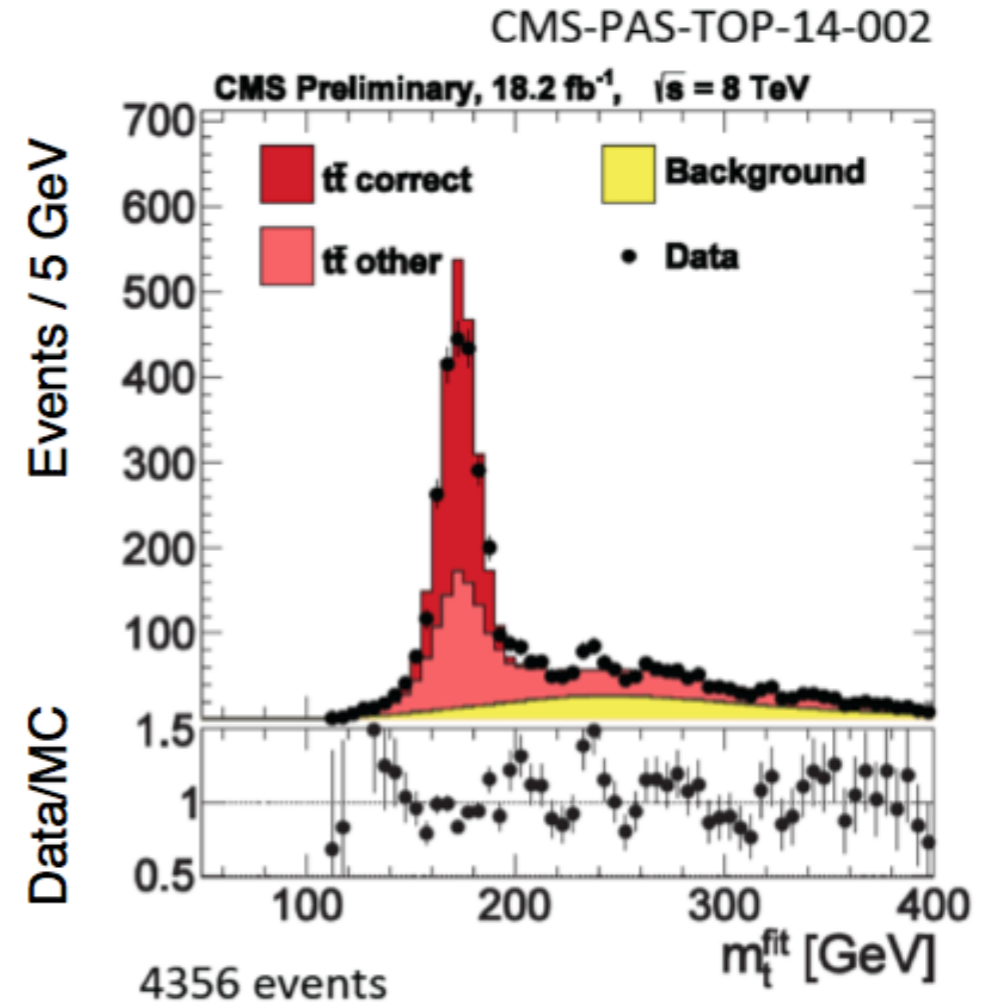
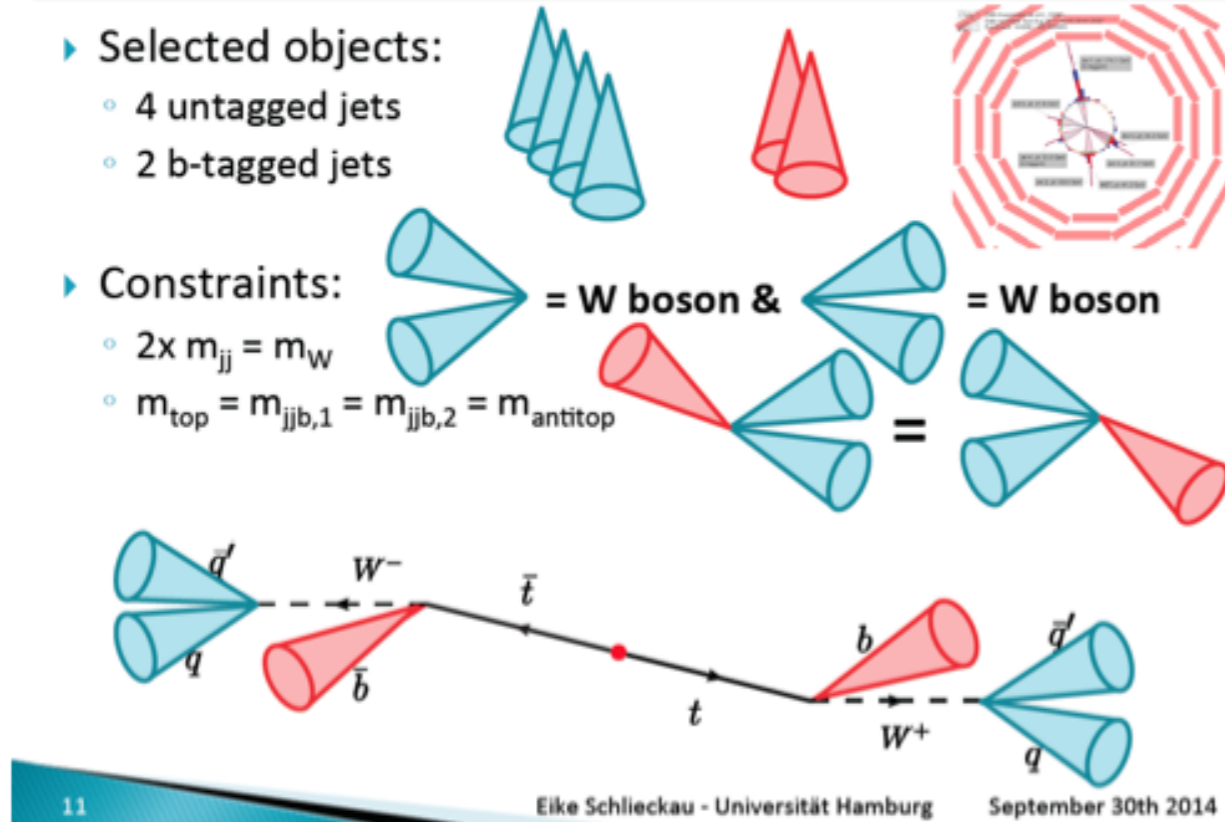
## Kinematic Fit

▶ Selected objects:

- 4 untagged jets
- 2 b-tagged jets

▶ Constraints:

- $2 \times m_{jj} = m_W$
- $m_{\text{top}} = m_{jjb,1} = m_{jjb,2} = m_{\text{antitop}}$



Use Monte Carlo Templates

Determine best fit value of Monte Carlo top-mass parameter:

$$\text{CMS: } m_t^{\text{MC}} = 172.44 \pm 0.49 \quad \text{ATLAS: } m_t^{\text{MC}} = 172.84 \pm 0.70$$

# What is $m_t^{\text{MC}}$ ?

- Natural to think it is the pole mass, but its not.

- ◆ Pole Mass has an infrared renormalon:

Factorial growth in pert. series:  $(2\beta_0)^n n! \alpha_s^{n+1}$

Ambiguity:  $\delta m_t^{\text{pole}} \sim \Lambda_{\text{QCD}}$

Due to the shower cutoff,  $m_t^{\text{MC}}$  does not.

- ◆ Pole Mass involves virtual integration over all momenta.

MC has shower cutoff which restricts real radiation. Due to unitarity, this cutoff also affects virtual radiation &  $m_t^{\text{MC}}$  defn.

# What is $m_t^{\text{MC}}$ ?

- It is not the  $\overline{\text{MS}}$  mass.

$$\overline{m}_t \alpha_s \gg \Gamma_t \simeq 1.4 \text{ GeV}$$

Not compatible with Breit-Wigner in Monte Carlo.

$$\frac{1}{\left(\frac{q^2 - m_t^2}{m_t}\right)^2 + \Gamma_t^2}$$

# What is $m_t^{\text{MC}}$ ?

- It is most like a short distance mass with cutoff  $R \simeq 1 \text{ GeV}$

**MSR mass:**  $m_t^{\text{MSR}}(R \simeq 1 \text{ GeV}) \simeq m_t^{\text{MC}}$

vary R: definition uncertainty  $\sim 0.5 \text{ GeV}$

MS Scheme:  $(\mu > \bar{m}(\bar{m}))$

$$\bar{m}(\bar{m}) - m^{\text{pole}} = -\bar{m}(\bar{m}) [0.42441 \alpha_s(\bar{m}) + 0.8345 \alpha_s^2(\bar{m}) + 2.368 \alpha_s^3(\bar{m}) + \dots]$$

MSR Scheme:  $(R < \bar{m}(\bar{m}))$

↓ Hoang, Jain, Scimemi, IS arXiv:0803.4214

$$m_{\text{MSR}}(R) - m^{\text{pole}} = -R [0.42441 \alpha_s(R) + 0.8345 \alpha_s^2(R) + 2.368 \alpha_s^3(R) + \dots]$$

$$m_{\text{MSR}}(m_{\text{MSR}}) = \bar{m}(\bar{m})$$

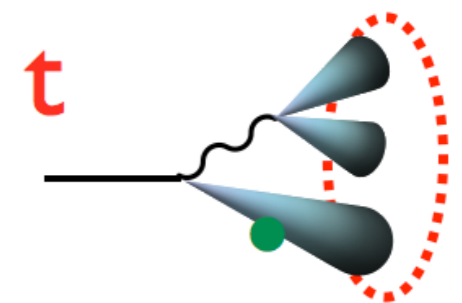
# Extracting a Short Distance Top Mass at the LHC

To improve on the current experimental measurements:

- must use a kinematically sensitive LHC observable
- theoretically tractable (= factorization at Hadron level), to obtain a measurement in a precise mass scheme defined at Lagrangian level.
- control contamination (ISR, Underlying Event, ...)

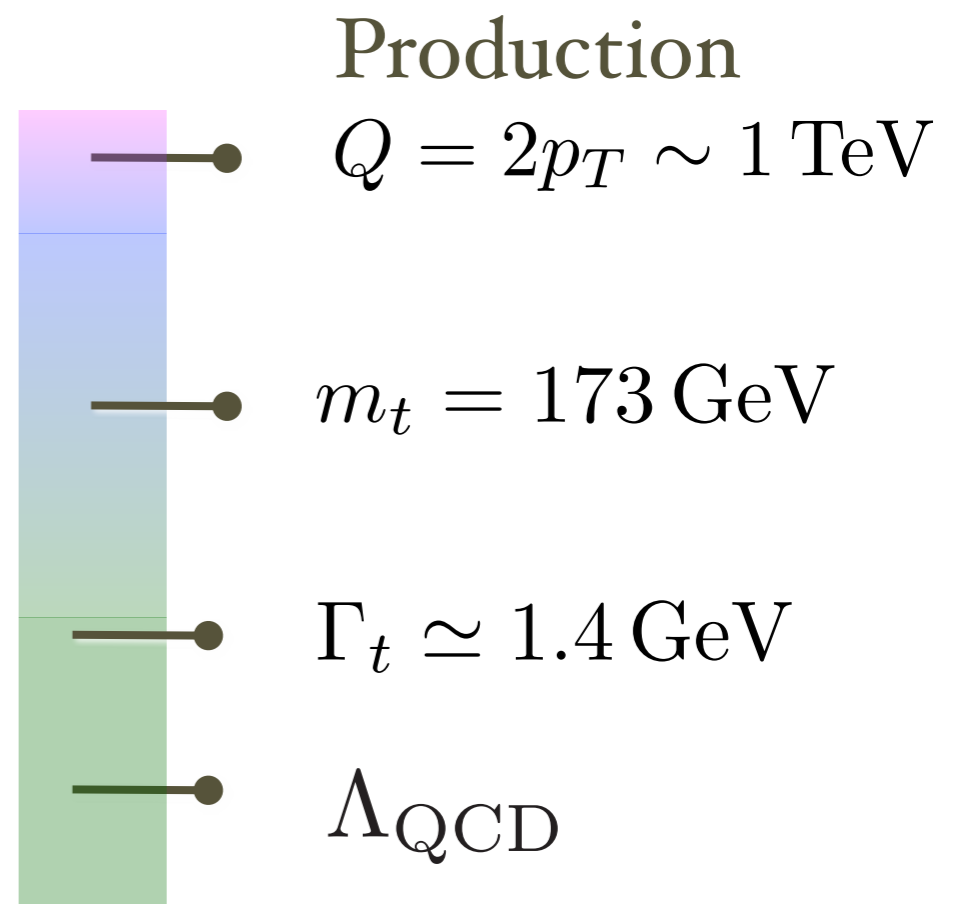
First simplification:

- boosted top quarks,  $Q = 2p_T \gg m_t$   
enables us to be inclusive over decay products



# Theory Issues for $pp \rightarrow t\bar{t}X$

- jet observable
- suitable top mass for jets
- initial state radiation
- final state radiation
- underlying event/MPI
- color reconnection
- beam remnant
- parton distributions
- sum large logs  $Q \gg m_t \gg \Gamma_t$





# Theory Issues for $pp \rightarrow t\bar{t}X$

- jet observable ★★
- suitable top mass for jets ★
- initial state radiation
- final state radiation ★
- underlying event/MPI
- color reconnection ★
- beam remnant
- parton distributions
- sum large logs  $Q \gg m_t \gg \Gamma_t$  ★

First  
 $e^+e^- \rightarrow t\bar{t}X$   
and the issues ★

$$e^+ e^- \rightarrow t \bar{t}$$

Measure what observable?

$$\frac{d^2 \sigma}{dM_t^2 dM_{\bar{t}}^2}$$

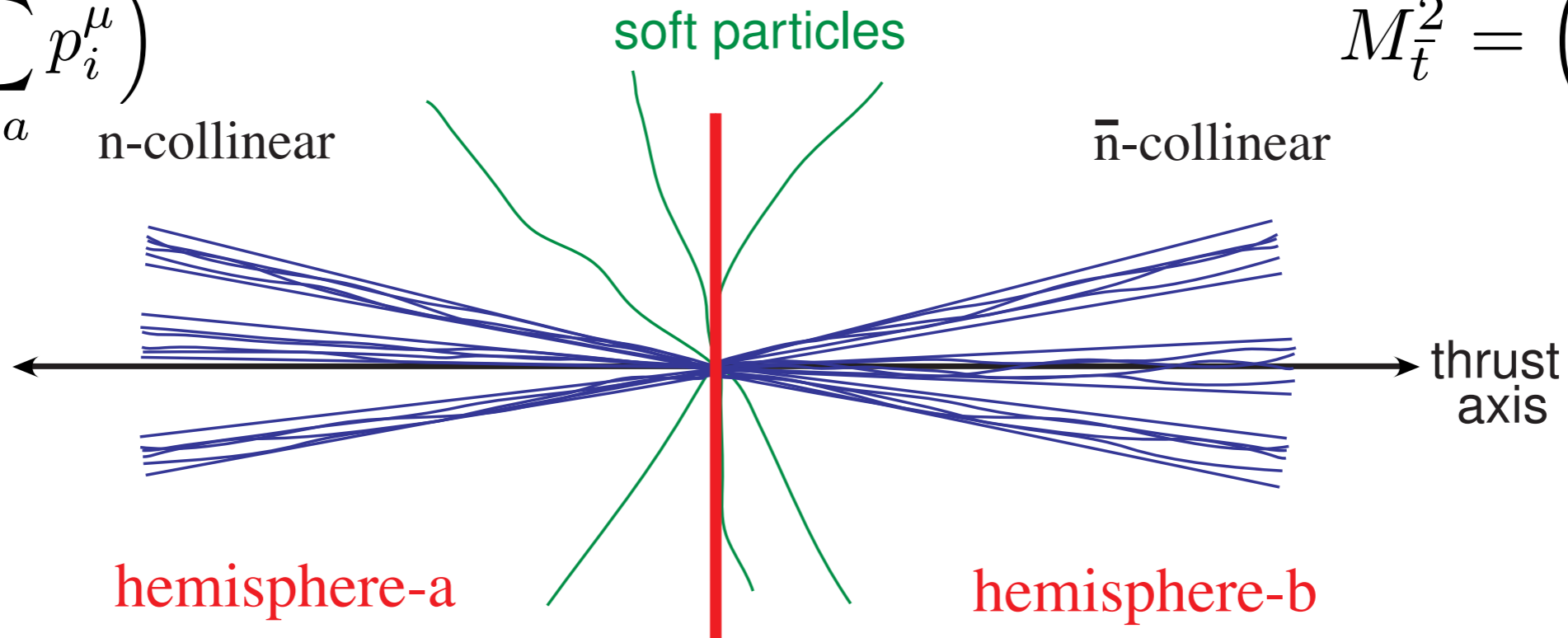
Hemisphere Invariant Masses

$$M_t^2 = \left( \sum_{i \in a} p_i^\mu \right)^2$$

n-collinear

$$M_{\bar{t}}^2 = \left( \sum_{i \in b} p_i^\mu \right)^2$$

$\bar{n}$ -collinear



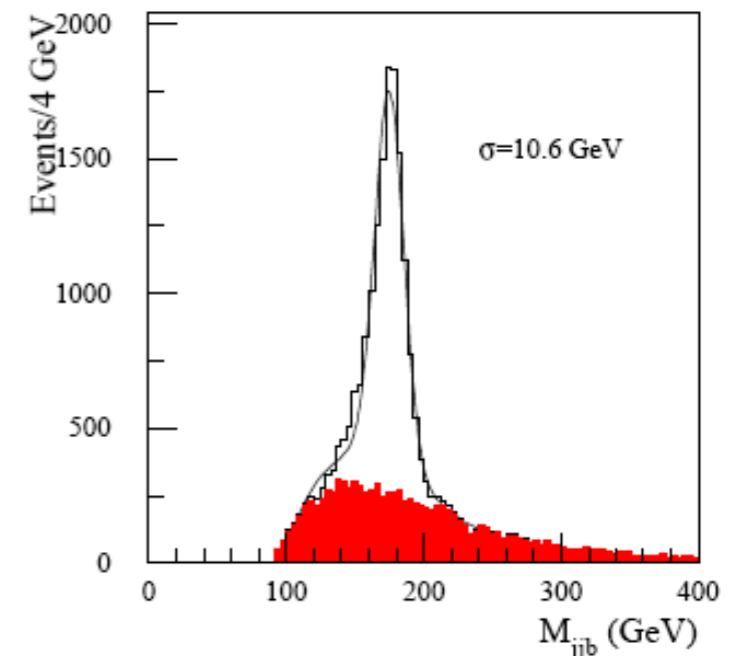
Peak region:

$$s_t \equiv M_t^2 - m^2 \sim m\Gamma \ll m^2$$

$$\hat{s}_t \equiv \frac{M_t^2 - m^2}{m} \sim \Gamma \ll m$$

Breit Wigner:

$$\frac{m\Gamma}{s_t^2 + (m\Gamma)^2} = \left( \frac{\Gamma}{m} \right) \frac{1}{\hat{s}_t^2 + \Gamma^2}$$



# Factorization:

Fleming, Hoang, Mantry, IS

hep-ph/0703207

hep-ph/0711.2079

Hard Functions

$$\left( \frac{d^2\sigma}{dM_t^2 dM_{\bar{t}}^2} \right)_{\text{hemi}} = \sigma_0 H_Q(Q, \mu_m) H_m\left(m, \frac{Q}{m}, \mu_m, \mu\right) \times J_B\left(\hat{s}_t - \frac{Q\ell}{m}, \Gamma, \delta m, \mu\right) J_B\left(\hat{s}_{\bar{t}} - \frac{Q\ell'}{m}, \Gamma, \delta m, \mu\right) S_{\text{hemi}}(\ell - k, \ell' - k', \mu) F(k, k')$$

**Answer**

Hadronization

QCD

(boosted HQET)  
Jet Functions

Soft

Function

Evolution and decay of top quark close to mass shell

Perturbative Cross talk

control over mass scheme

SCET

HQET

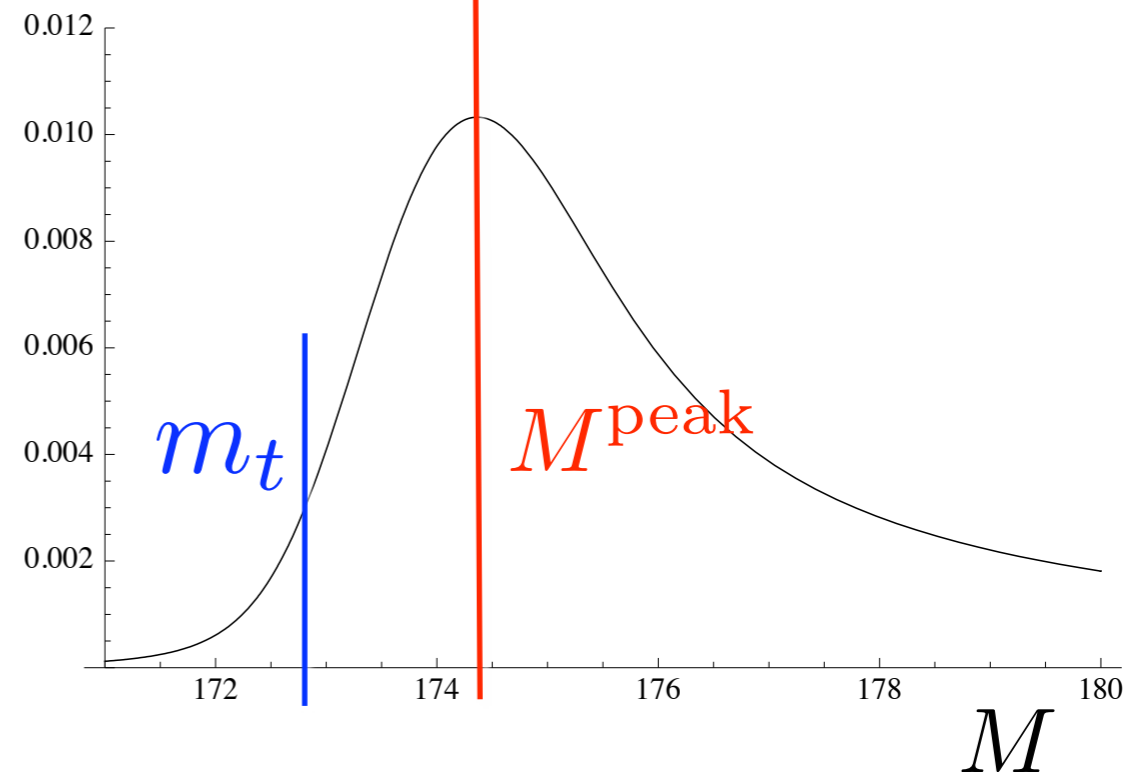
$$\left( \frac{d^2\sigma}{dM_t^2 dM_{\bar{t}}^2} \right)_{\text{hemi}} = \sigma_0 H_Q(Q, \mu_m) H_m\left(m, \frac{Q}{m}, \mu_m, \mu\right) \times J_B\left(\hat{s}_t - \frac{Q\ell}{m}, \Gamma, \delta m, \mu\right) J_B\left(\hat{s}_{\bar{t}} - \frac{Q\ell'}{m}, \Gamma, \delta m, \mu\right) S_{\text{hemi}}(\ell - k, \ell' - k', \mu) F(k, k')$$

Answer

$$M^{\text{peak}} = m_t + \Gamma_t(\alpha_s + \alpha_s^2 + \dots) + \frac{Q\Lambda_{\text{QCD}}}{m_t}$$

measure  
this

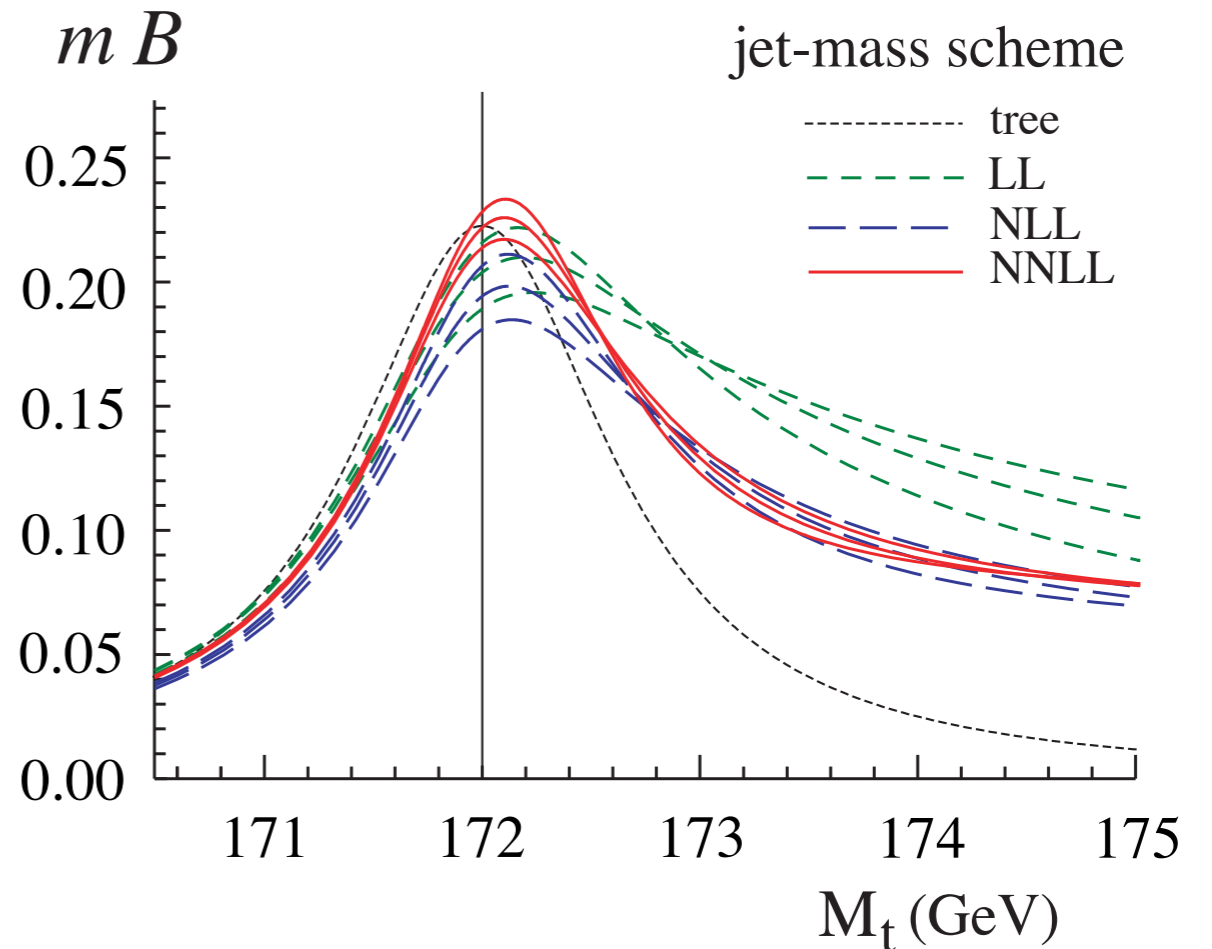
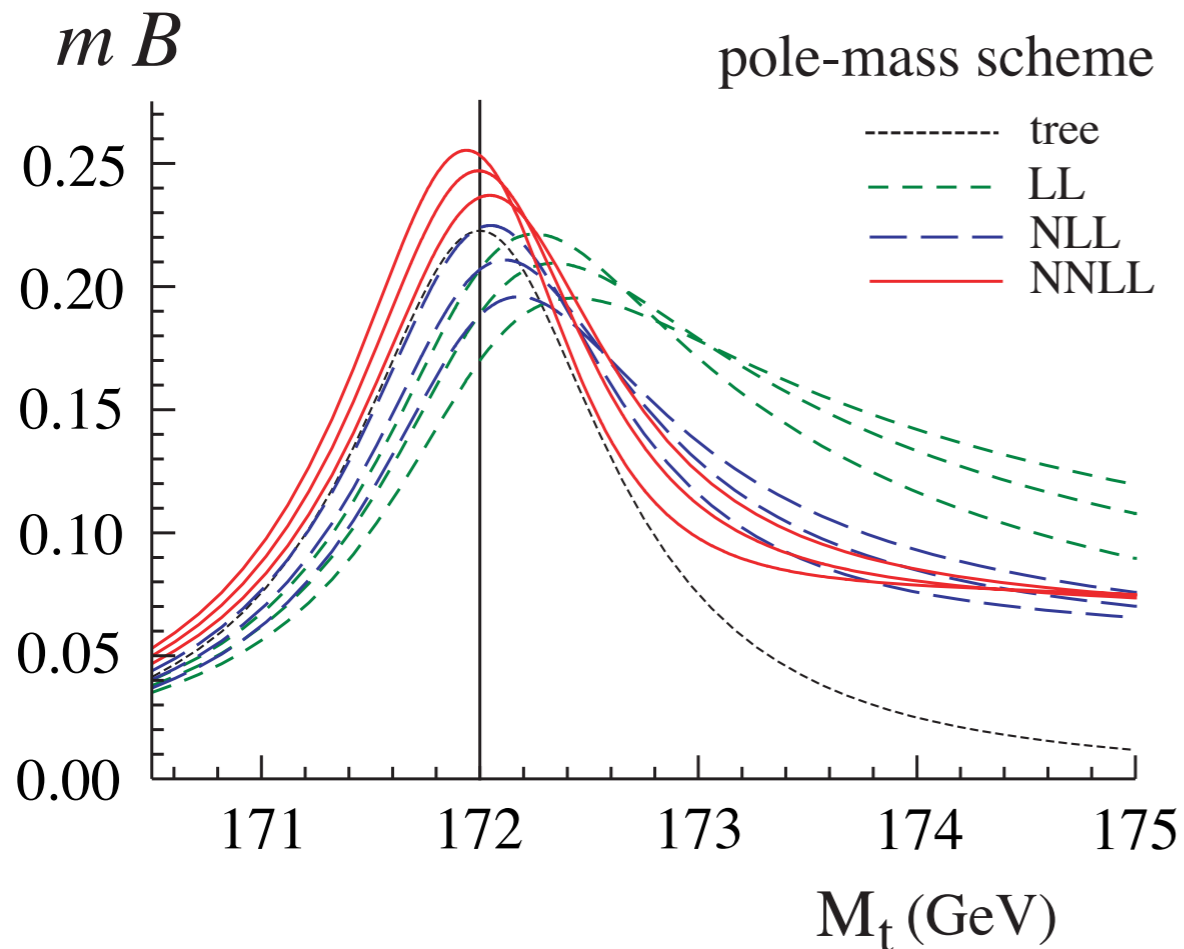
extract  
this

$$\frac{d\sigma}{dM}$$


Short distance  $m_t$  can (in principle) be determined to better than  $\Lambda_{\text{QCD}}$

# Jet Function Results up to $\mathcal{O}(\alpha_s^2)$ & NNLL:

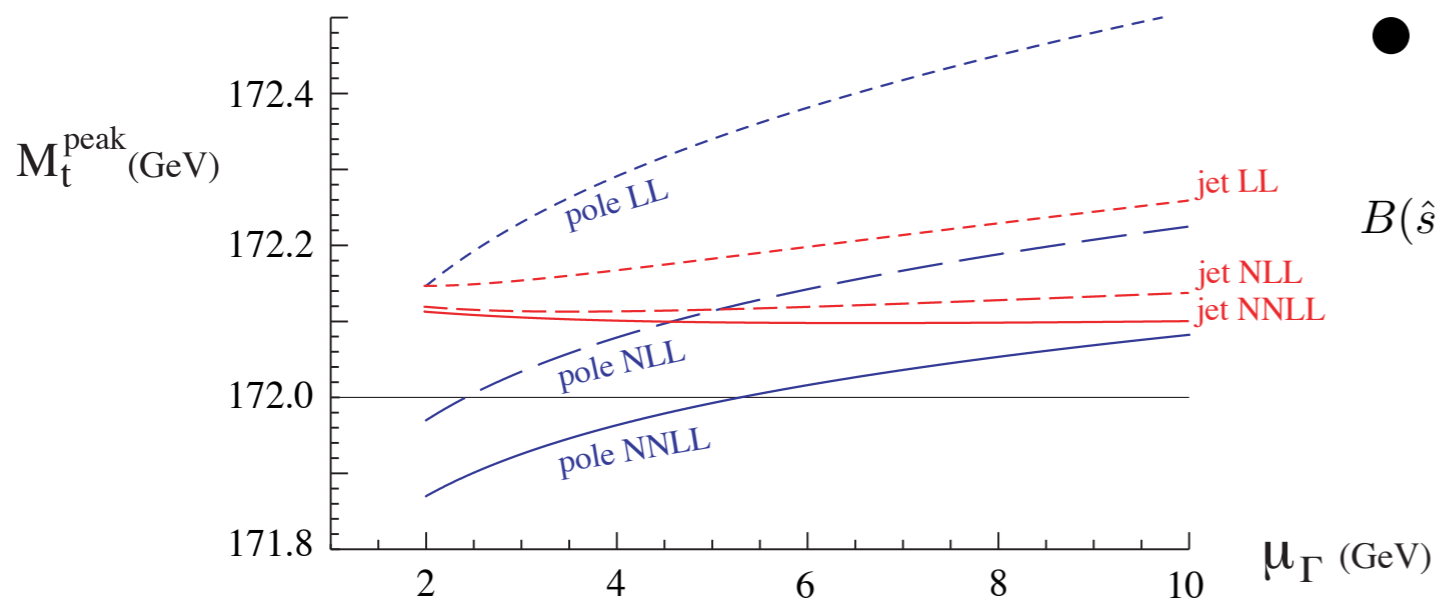
Jain, Scimemi, I.S. arXiv:0801.0743



- 3 curves vary  $\mu_\Gamma$

$$B(\hat{s}, \delta m_J, \Gamma_t, \mu_\Lambda, \mu_\Gamma) \equiv \int d\hat{s}' U_B(\hat{s} - \hat{s}', \mu_\Lambda, \mu_\Gamma) B(\hat{s}', \delta m_J, \Gamma_t, \mu_\Gamma)$$

$$= \int d\hat{s}' d\hat{s}'' U_B(\hat{s} - \hat{s}', \mu_\Lambda, \mu_\Gamma) B(\hat{s}' - \hat{s}'', \delta m_J, \mu_\Gamma) \frac{\Gamma_t}{\pi(\hat{s}''^2 + \Gamma_t^2)}$$



# Top Mass Calibration of Monte Carlo

[Butenschoen, Dehnadi, Hoang, Mateu, Preisser, IS arXiv:1608.01318]

Calibrate the  $m_t^{\text{MC}}$  parameter in **Monte Carlo** against **Hadron level theory predictions** with definite  $m_t$  parameter

$e^+e^- \rightarrow t\bar{t}$  theory:

- NNLL + NLO + nonsingular + hadronization + renormalon subt.

- VFNS for final state jets with massive quarks

[Gritschacher, Hoang, Jemos, Mateu, Pietrulewicz 2013, 2014]

[Butenschon, Dehnadi, Hoang, Mateu (to appear)]

- MSR mass, Soft Gap Scheme, and R-evolution

[Hoang, Jain, Scimemi, Stewart 2010]

[Hoang, Kluth 2008]

- 2-jettiness variable:  $\tau_2 = 1 - \max_{\vec{n}_t} \frac{\sum_i |\vec{n}_t \cdot \vec{p}_i|}{Q}$

$$\frac{d\sigma}{d\tau} = f(m_t^{\text{MSR}}, \alpha_s(m_Z), \Omega_1, \Omega_2, \dots, \mu_H, \mu_J, \mu_S, \mu_M, R, \Gamma_t)$$

any scheme

non-perturbative

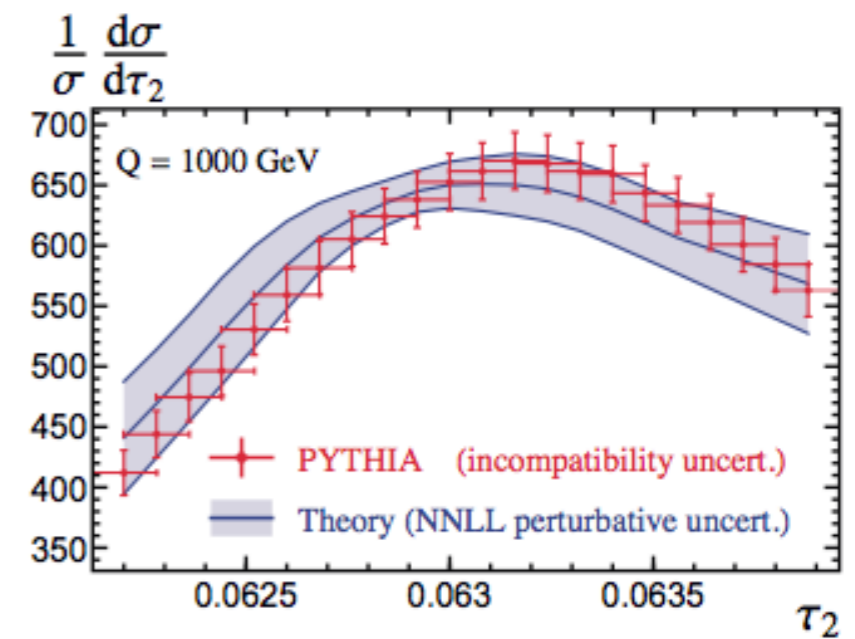
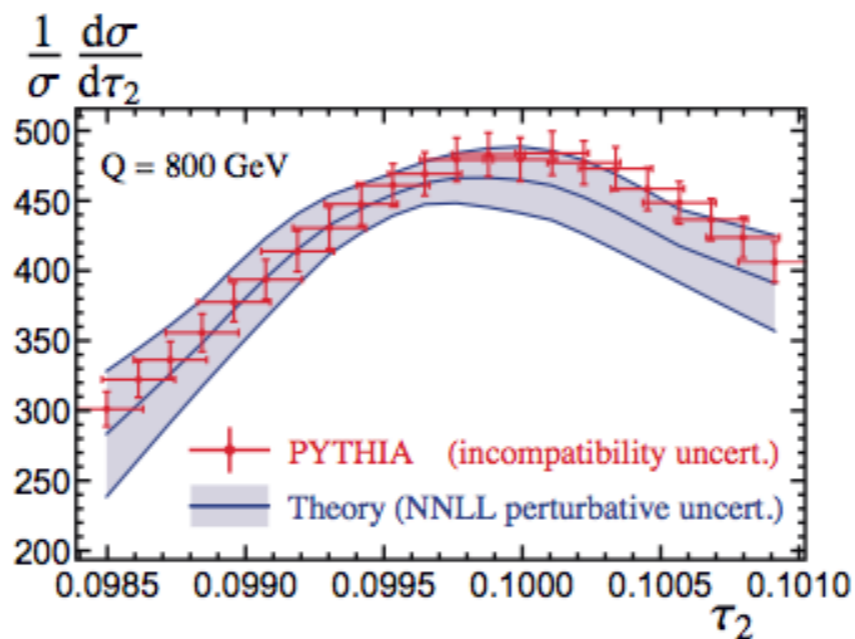
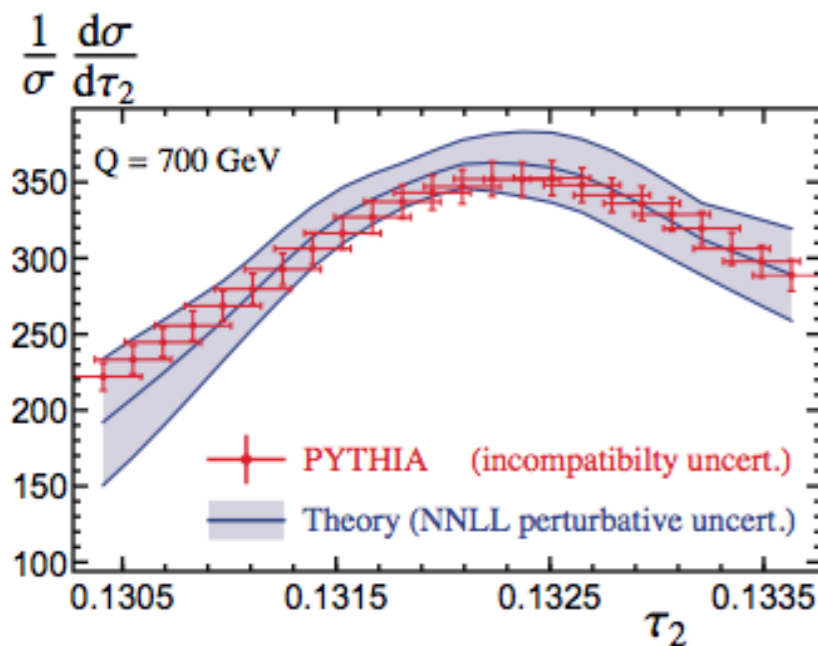
renorm. scales

finite lifetime

# Fit Procedure:

PYTHIA 8.205

- Fix  $m_t^{\text{MC}}$ . Generate MC data with  $Q = 700, 800, \dots, 1300, 1400$  GeV.
- For given  $\mu_i$ , Fit theory in peak region to determine  $\Omega_i$  and  $m_t$
- Repeat 500 times for different  $\mu_i$  to obtain perturbative uncertainty



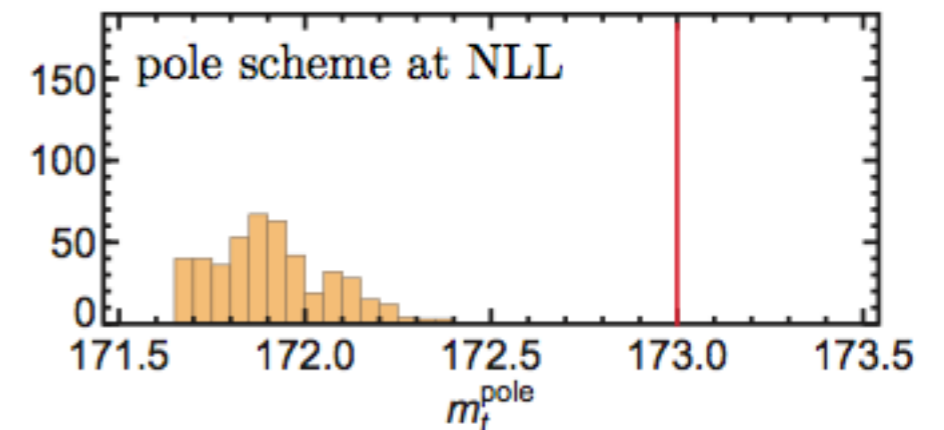
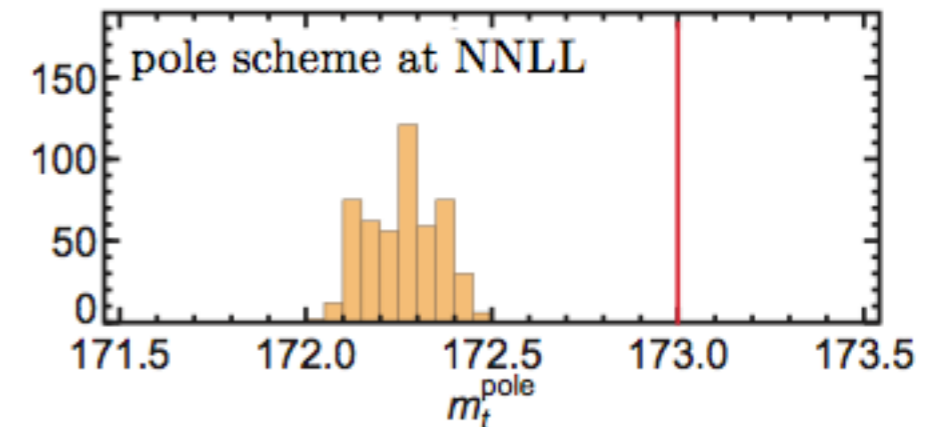
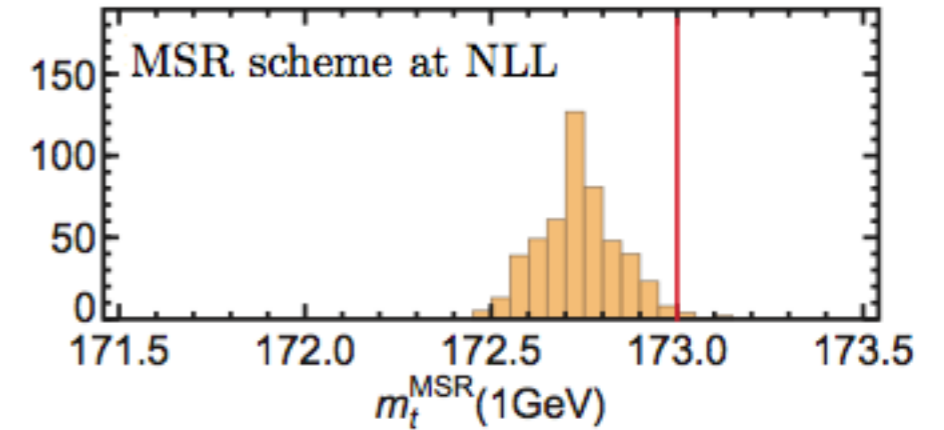
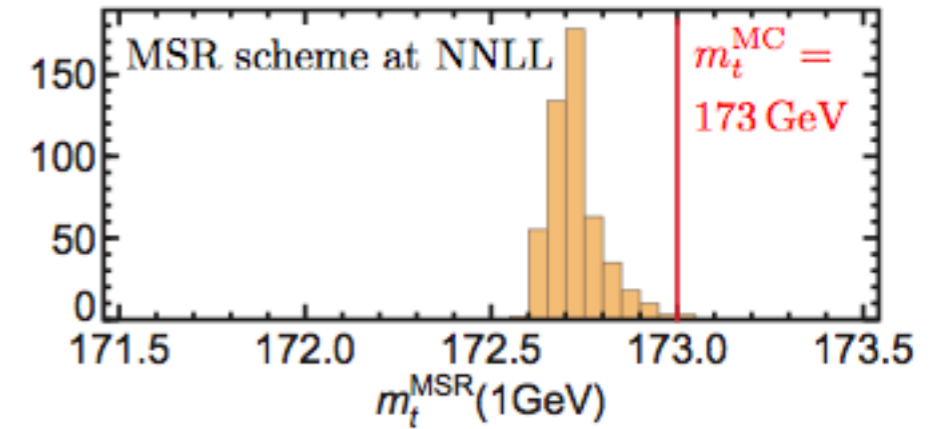


# Results:

- $m_t^{\text{MC}}$  differs from  $m_t^{\text{pole}}$  by 0.9 GeV (NNLL) or 0.6 GeV (NLL)
- $m_t^{\text{MC}}$  compatible with  $m_t^{\text{MSR}}(R = 1 \text{ GeV})$

$$m_t^{\text{MC}} = 173 \text{ GeV} \quad (\tau_2^{e^+e^-})$$

mass	order	central	perturb.	incompatibility	total
$m_{t,1 \text{ GeV}}^{\text{MSR}}$	NLL	172.80	0.26	0.14	0.29
$m_{t,1 \text{ GeV}}^{\text{MSR}}$	N <sup>2</sup> LL	172.82	0.19	0.11	0.22
$m_t^{\text{pole}}$	NLL	172.10	0.34	0.16	0.38
$m_t^{\text{pole}}$	N <sup>2</sup> LL	172.43	0.18	0.22	0.28





# Theory Issues for $pp \rightarrow t\bar{t}X$

- jet observable ★★
- suitable top mass for jets ★
- initial state radiation
- final state radiation ★
- underlying event/MPI
- color reconnection ★
- beam remnant
- parton distributions
- sum large logs  $Q \gg m_t \gg \Gamma_t$  ★

Can apply this to current measurements if we trust Pythia extrapolation for remaining items

# Theory Issues for $pp \rightarrow t\bar{t}X$

- jet observable      ★ ★      Jet Mass in Jet of radius R
- suitable top mass for jets      ★
- initial state radiation      ★      Better: factorization  
for pp
- final state radiation      ★
- underlying event/MPI      ←      Note: no star here
- color reconnection      ★
- beam remnant      ★      Jet veto
- parton distributions      ★      multiple channels
- sum large logs       $Q \gg m_t \gg \Gamma_t$       ★

$pp \rightarrow t\bar{t}$

A. Hoang, S. Mantry, A. Pathak, IS

- Can be extended to pp (using N-jettiness) (Stewart, Tackmann, Waalewijn)

$$\frac{d^2\sigma}{dM_{J_1}^2 dM_{J_2}^2 d\mathcal{T}^{\text{cut}}} = \text{tr} \left[ \hat{H}_{Q_m} \hat{S}(\mathcal{T}^{\text{cut}}, R, \dots) \otimes F \right] \otimes J_B \otimes J_B \otimes \mathcal{I} \otimes f f$$

QCD



SCET



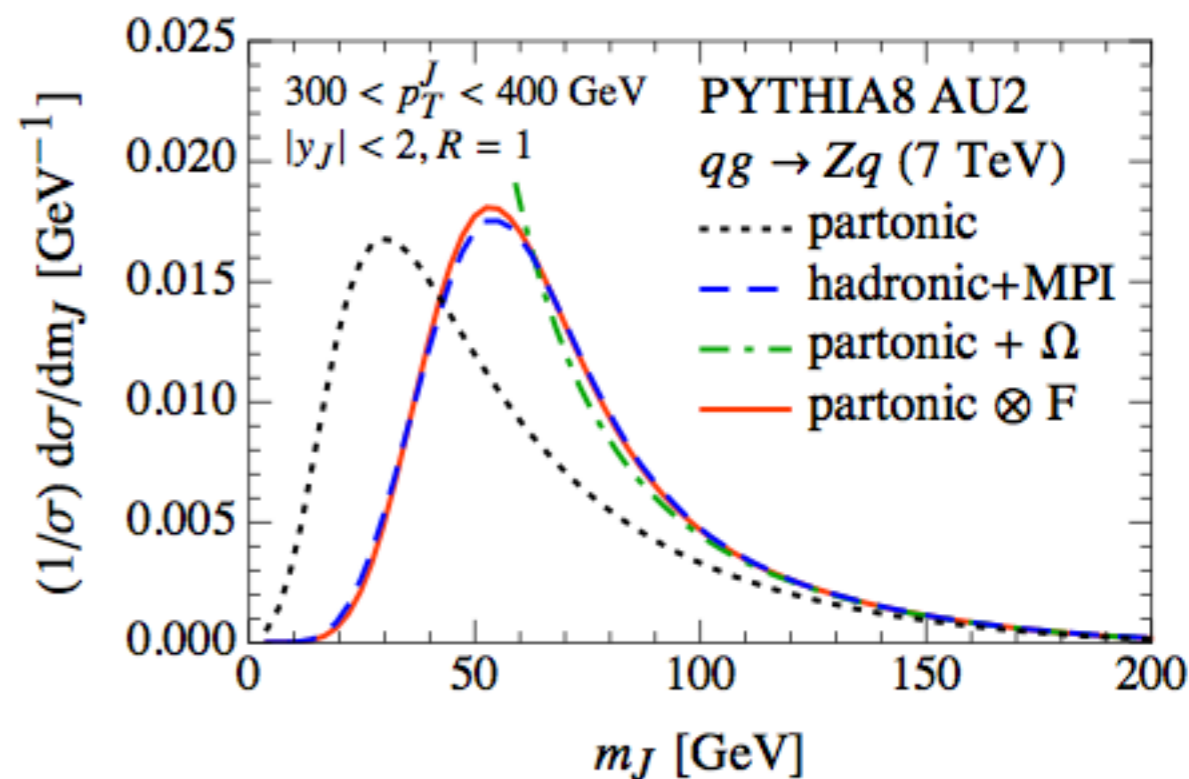
HQET

same jet functions!

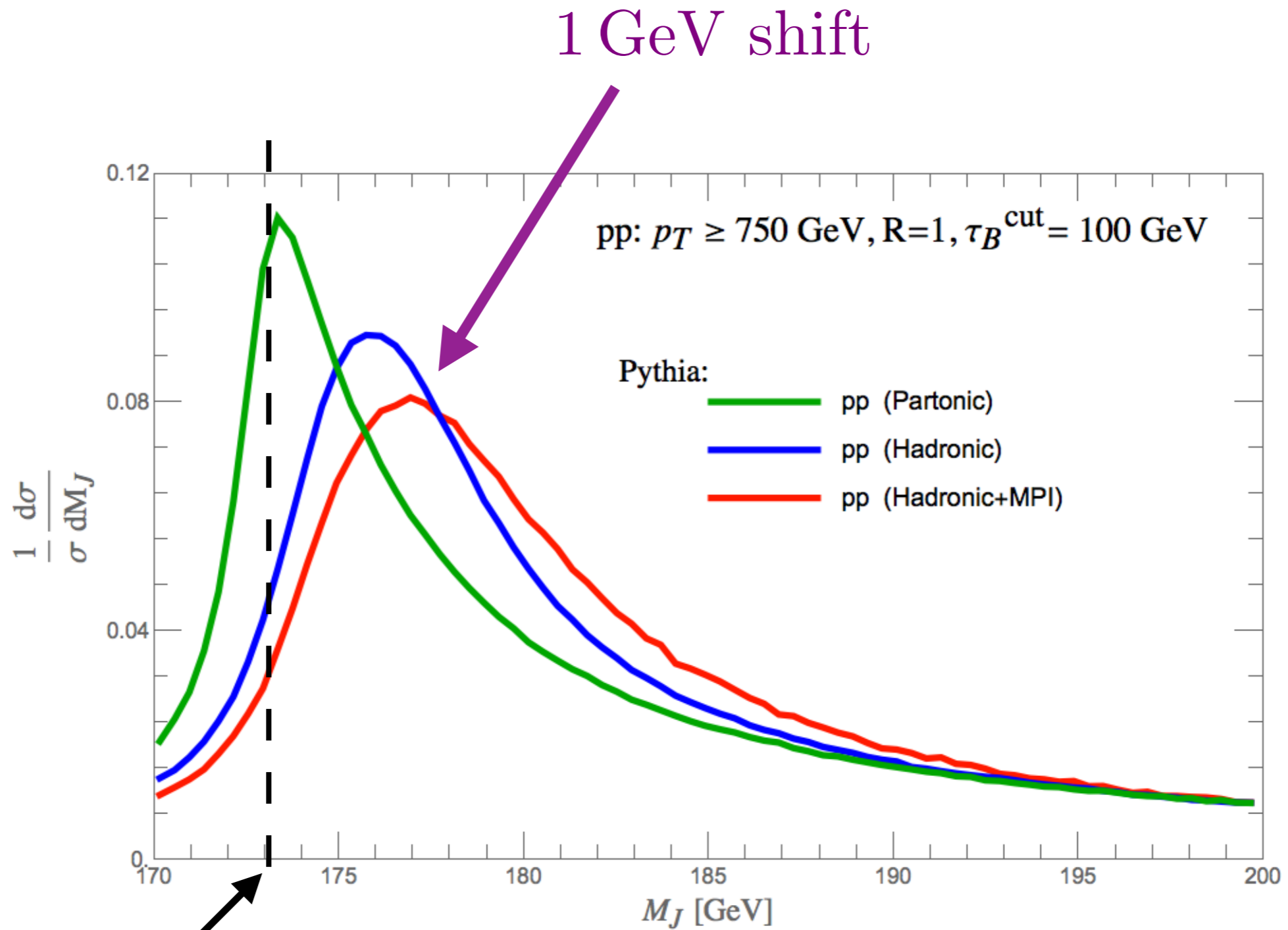
- BUT control of underlying event is model dependent.

Simple one parameter function  $F$  does give a reasonable model which reproduces Pythia

(IS, Tackmann, Waalewijn 2015)



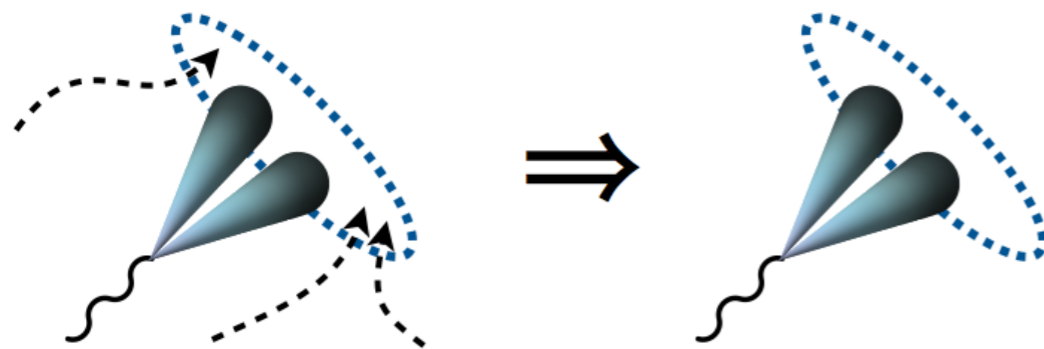
Issue is that UE / MPI is significant:



# Jet Substructure Interlude:

- key tools for:
- grooming jets
  - tagging subjets

eg. W/Z tagging in 2016



## Soft Drop

Larkoski, Marzani, Soyez, Thaler

## Trimming

Krohn, Thaler, Wang



## N-subjettiness

Thaler, van Tilburg  
(see also Stewart, Tackmann, Waalewijn)

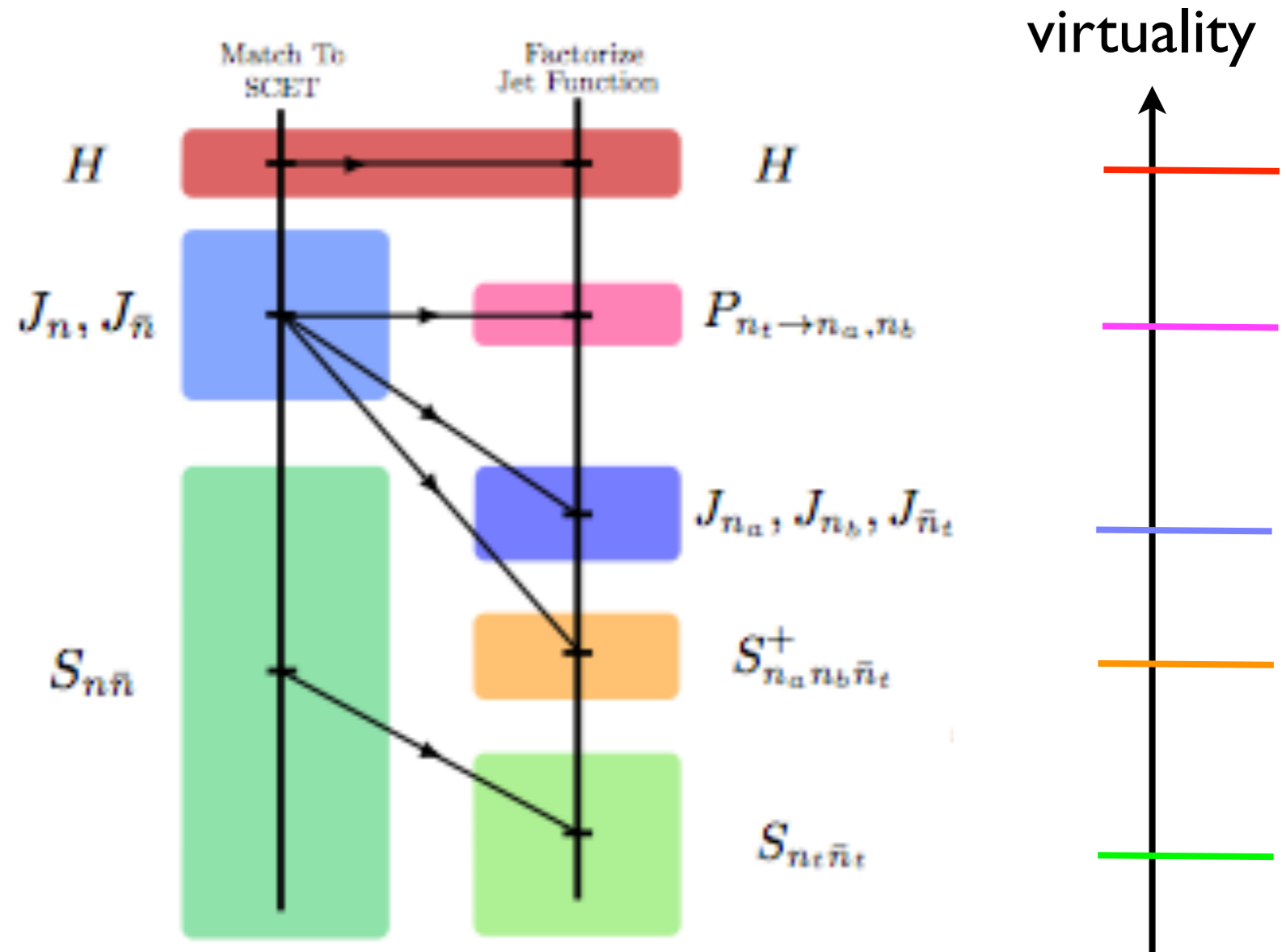
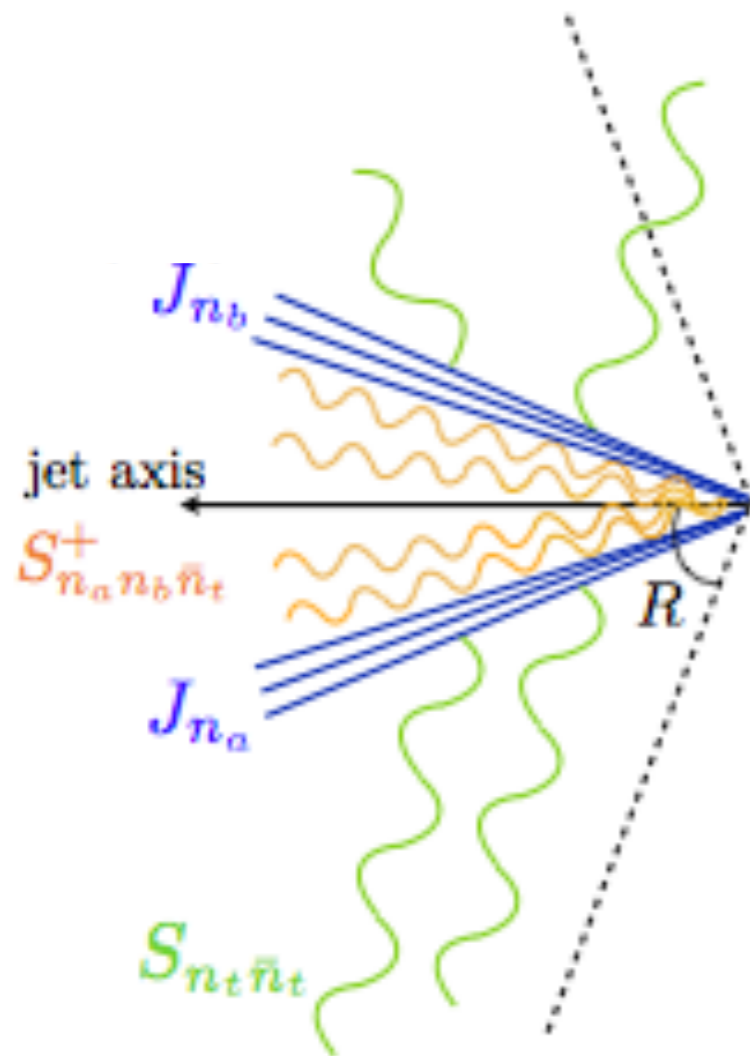
## $D_2$

Larkoski, Moult, Neill

# More scales:

## Collinear Subjets

Bauer, Tackmann, Walsh, Zuberi 2012



also used for:

Multiple Measurements:

Procura, Waalewijn, Zeune 2014

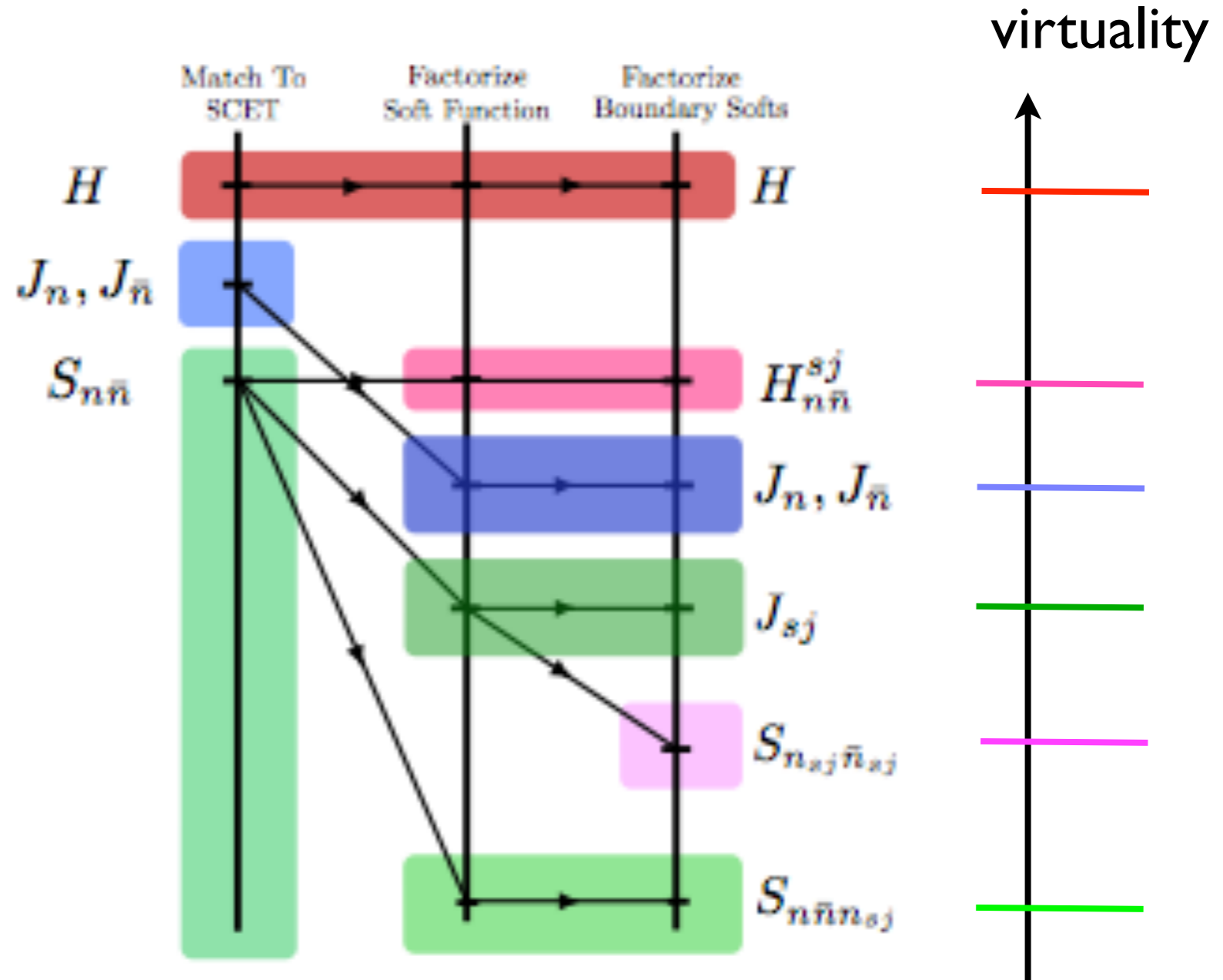
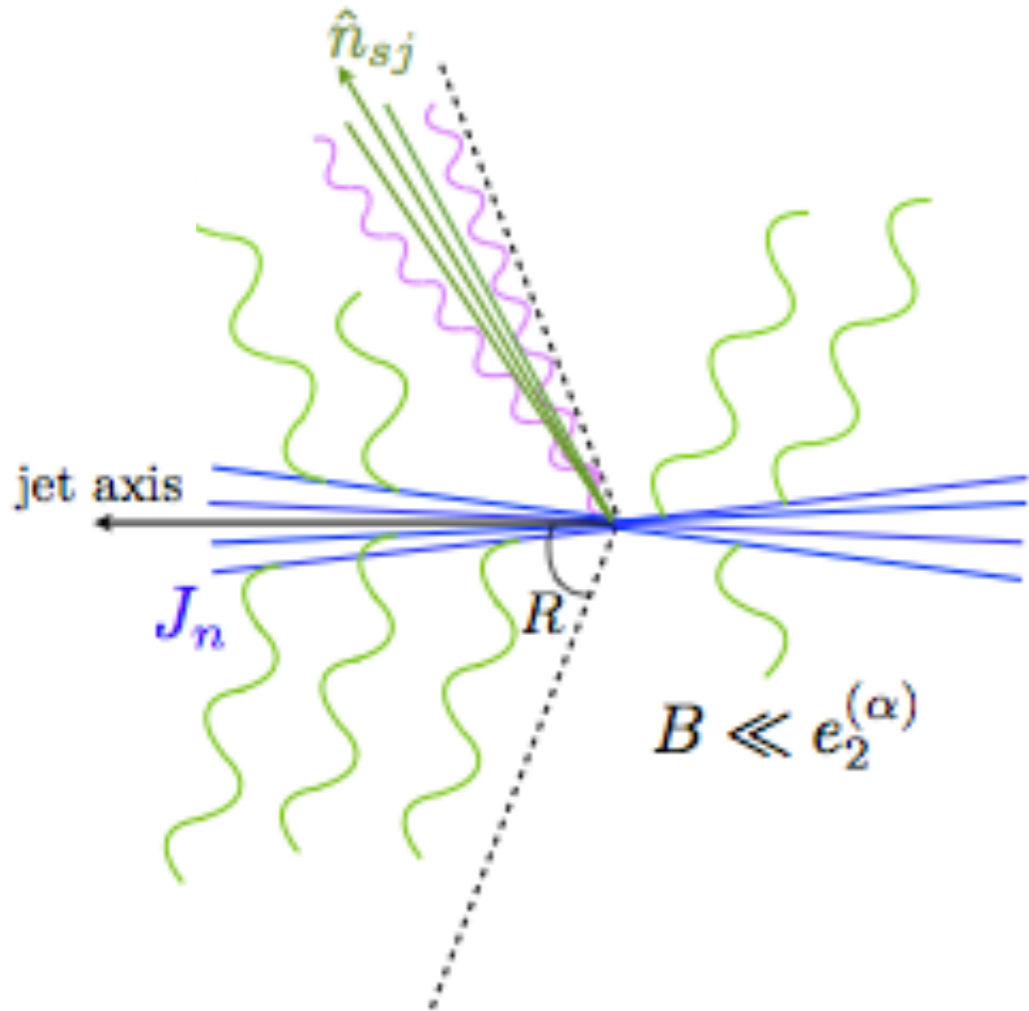
Sum Logs of Jet Radius,  $\ln(R)$ :

See Chris Lee's talk

# More scales:

## Soft Subject

Larkoski, Moult, Neill



Factorization theorems for both collinear and soft subjects were used for their calculation of  $D_2$

# Soft Drop

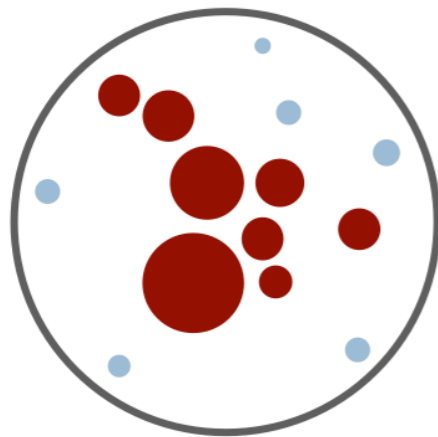
Larkoski, Marzani, Soyez, Thaler 2014

Grooms soft radiation from the jet

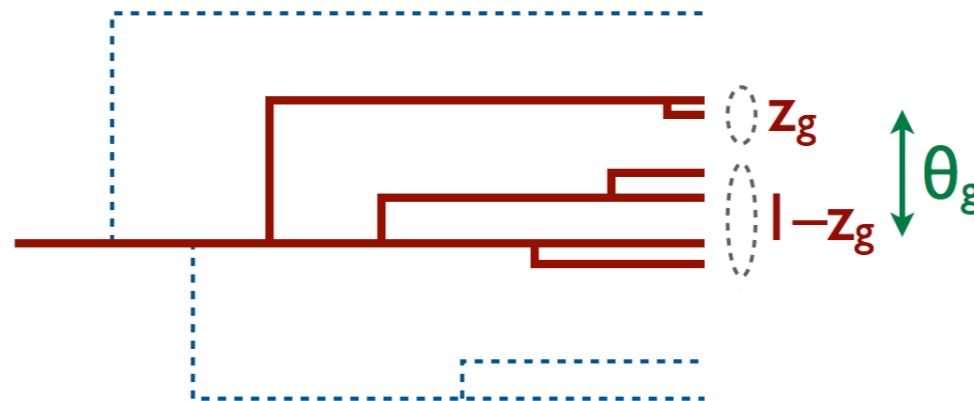
$$\frac{\min(p_{Ti}, p_{Tj})}{p_{Ti} + p_{Tj}} > z_{\text{cut}} \left( \frac{\Delta R_{ij}}{R_0} \right)^\beta \quad z > z_{\text{cut}} \theta^\beta$$

two grooming parameters

## Groomed Jet



## Groomed Clustering Tree



More Grooming

Less Grooming

$\beta \rightarrow -\infty$

$\beta < 0$

$\beta = 0$

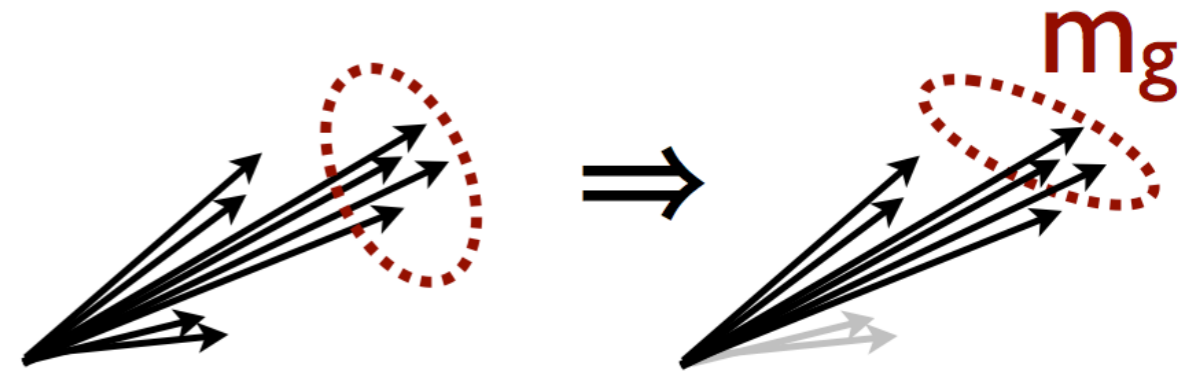
$\beta > 0$

$\beta \rightarrow \infty$

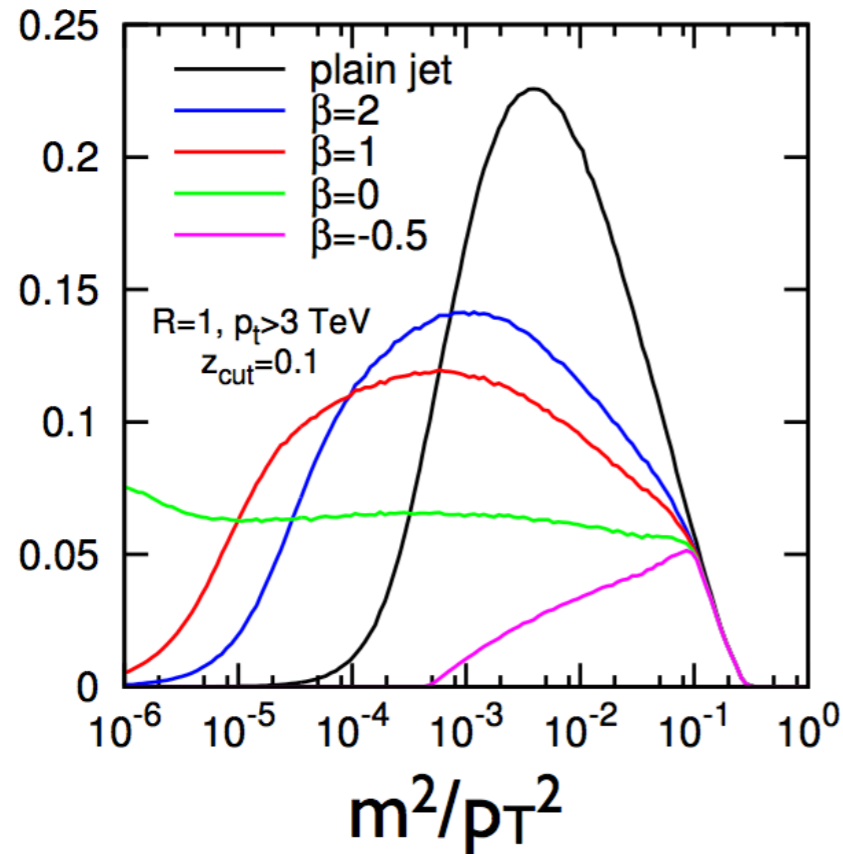


# Calculating Mass?

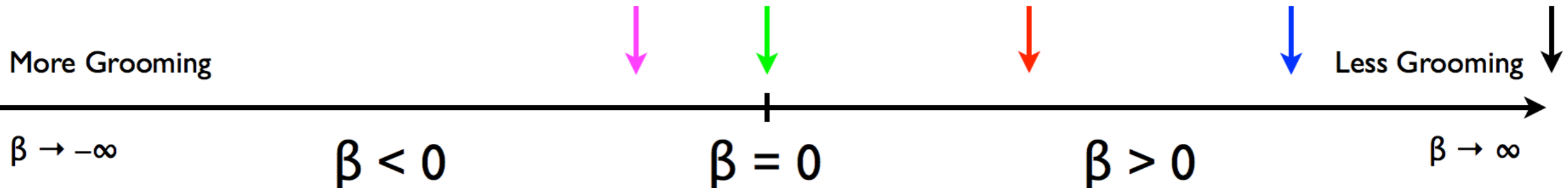
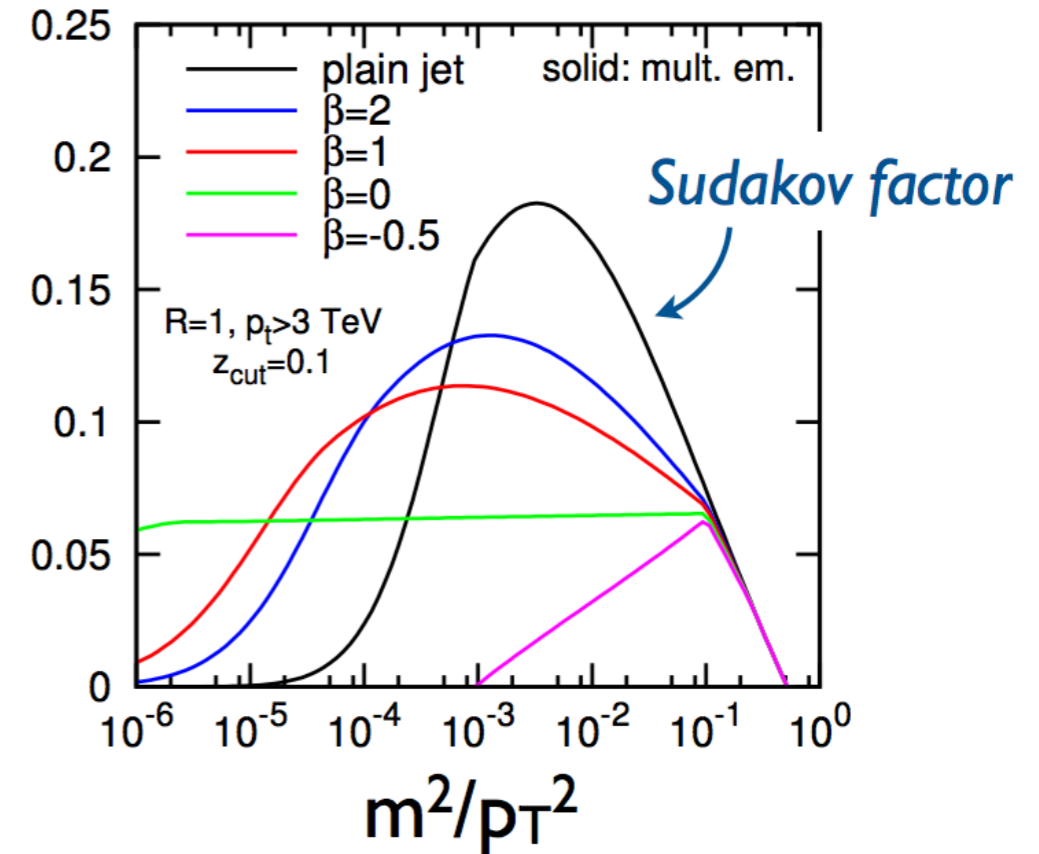
Larkoski, Marzani, Soyez, Thaler 2014



## Pythia 8, partonic

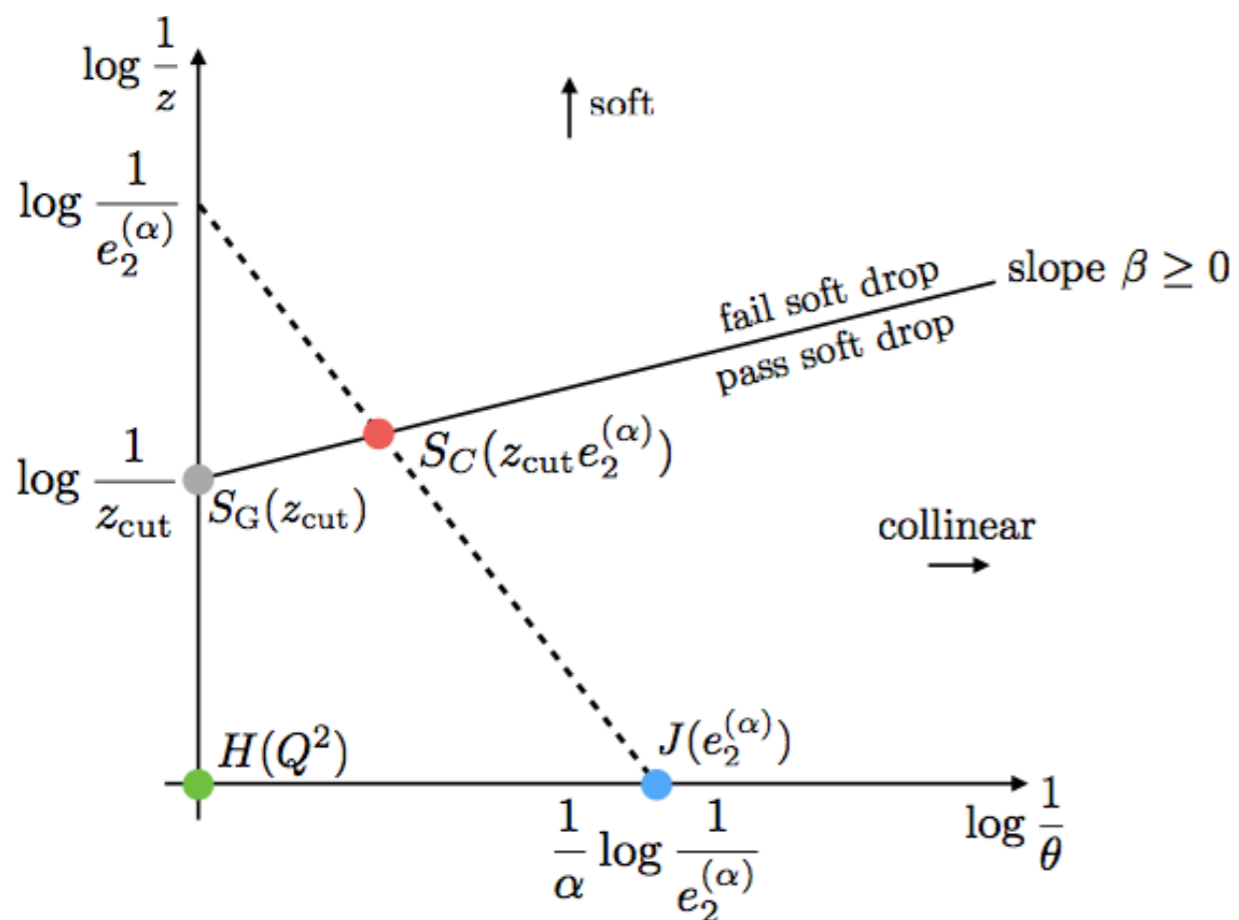
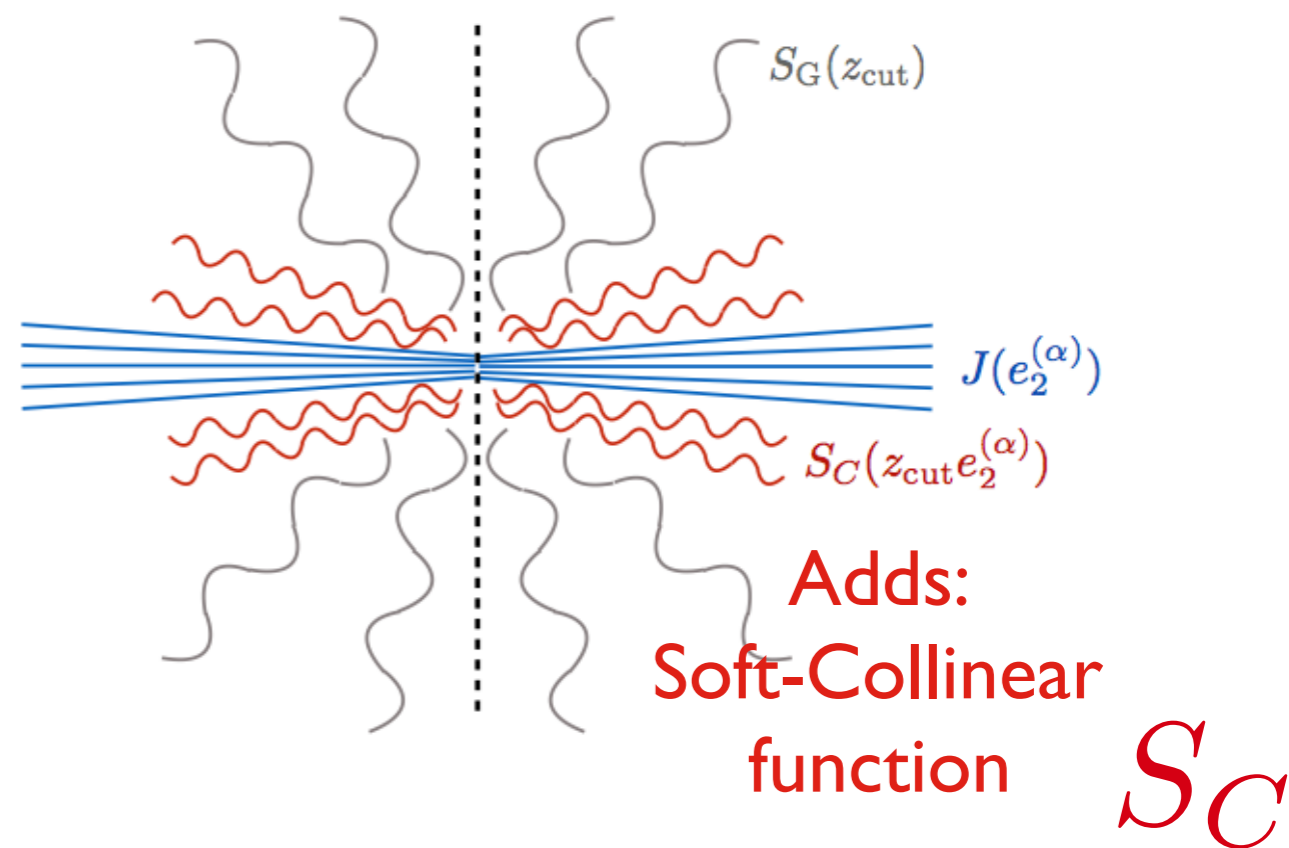
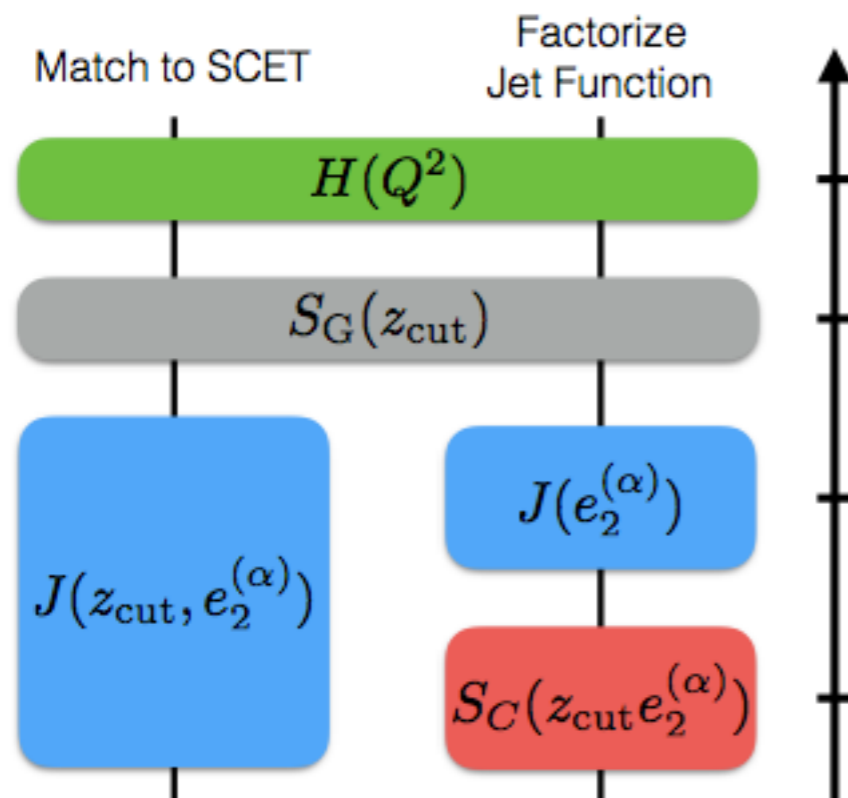


## Pert. QCD at $\simeq$ NLL



# Soft Drop Factorization

Frye, Larkoski, Schwartz, Yan 2016



$$\frac{d\sigma}{de_2 \dots} = H(Q^2) S_G(z_{\text{cut}}, \beta) \times \left[ S_C(e_2, z_{\text{cut}}, \beta) \otimes J(e_2) \right]$$

isolates measurement  
achieve NNLL precision

# Top Jet Mass with Soft Drop

$$pp \rightarrow t\bar{t}$$

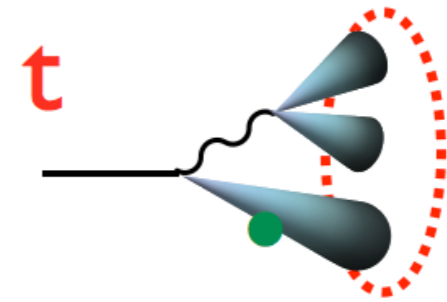
A. Hoang, S. Mantry, **A. Pathak**, IS (to appear)

$$p_T \gg m_t \gg \Gamma_t > \Lambda_{\text{QCD}}$$

● **Boosted Tops**  $p_T \gg m_t$

retain top decay products

● **Fat Jets**  $R \gg \frac{m_t}{p_T}$

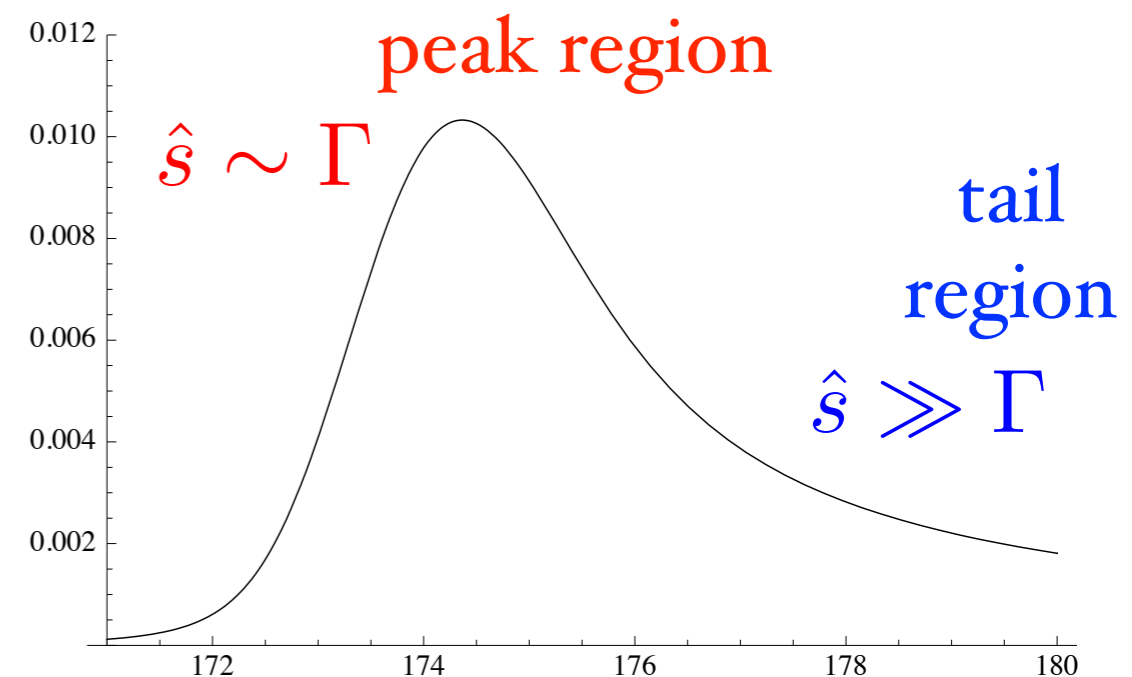


● **Sensitivity**  $\hat{s} \sim \Gamma_t$  for measurement of jet-mass  $m_J$

$$\hat{s} = \frac{m_J^2 - m_t^2}{m_t}$$

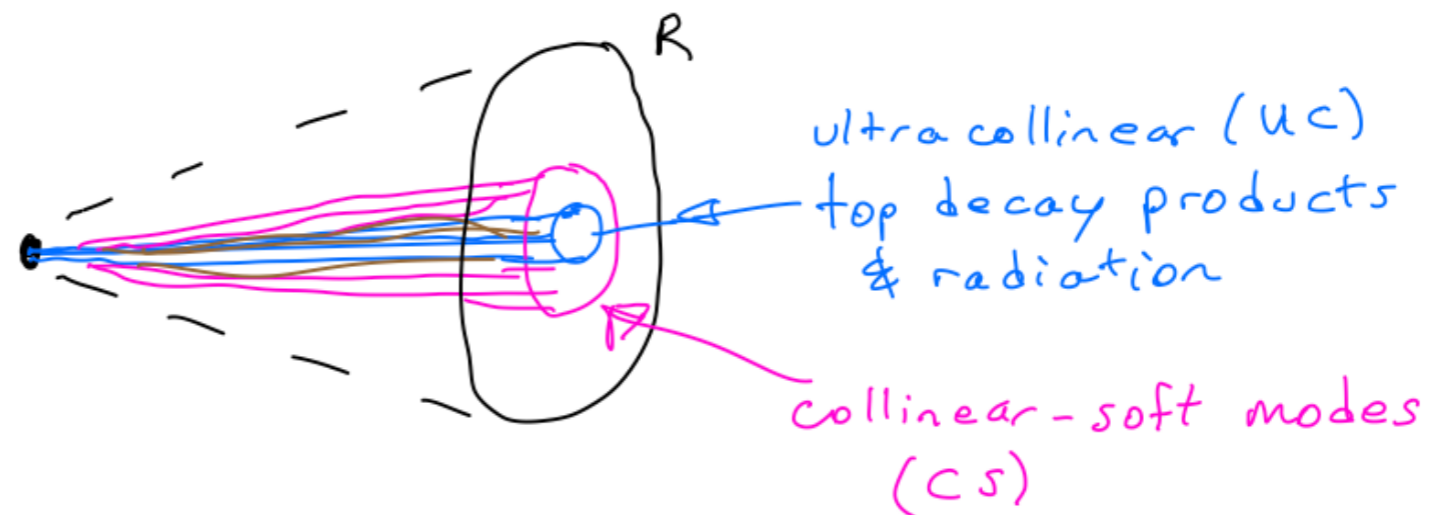
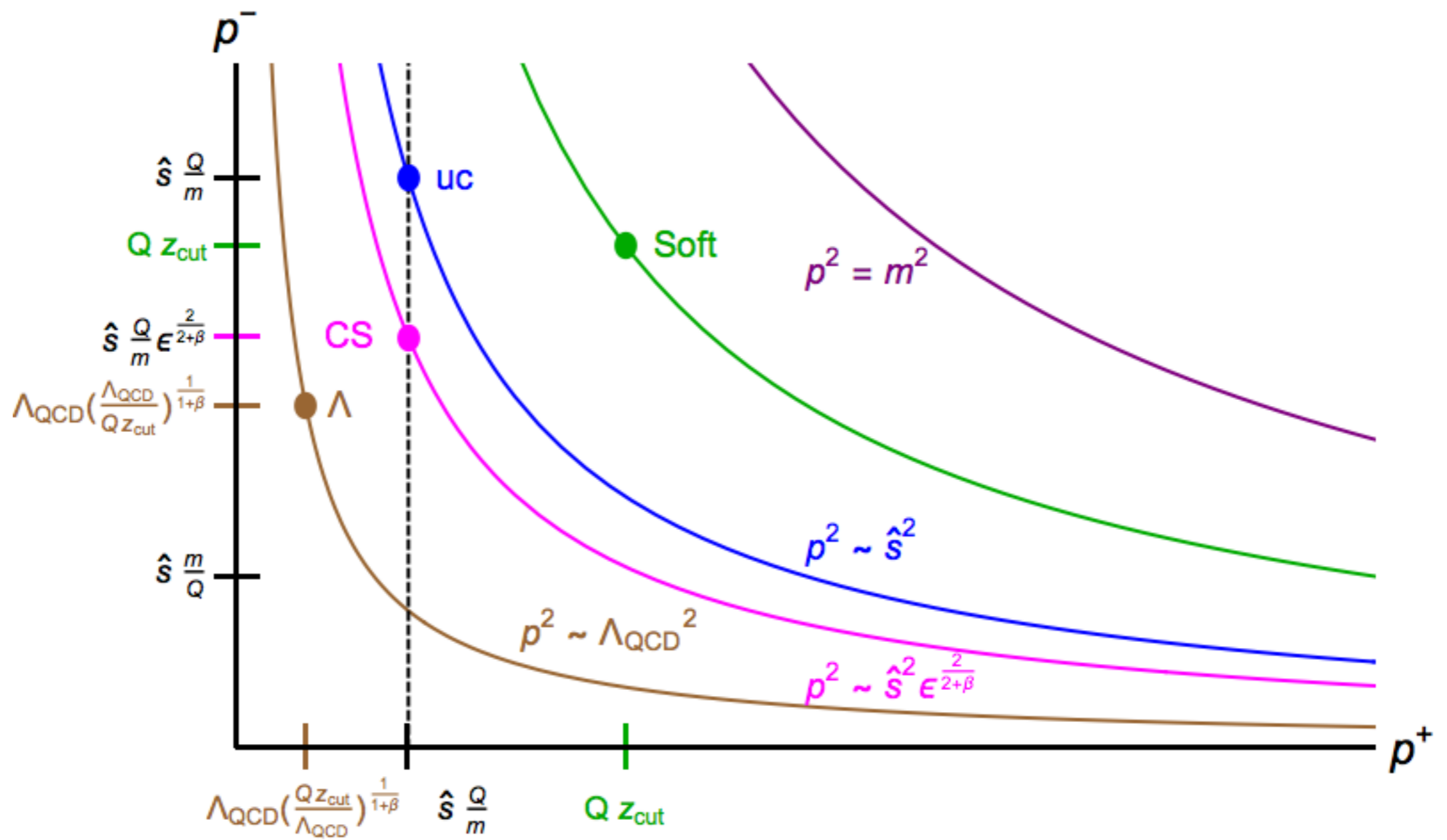
● **Grooming**  $z_{\text{cut}}, \beta$

● **Jet Veto**  $\mathcal{T}^{\text{cut}}$  or  $p_T^{\text{cut}}$

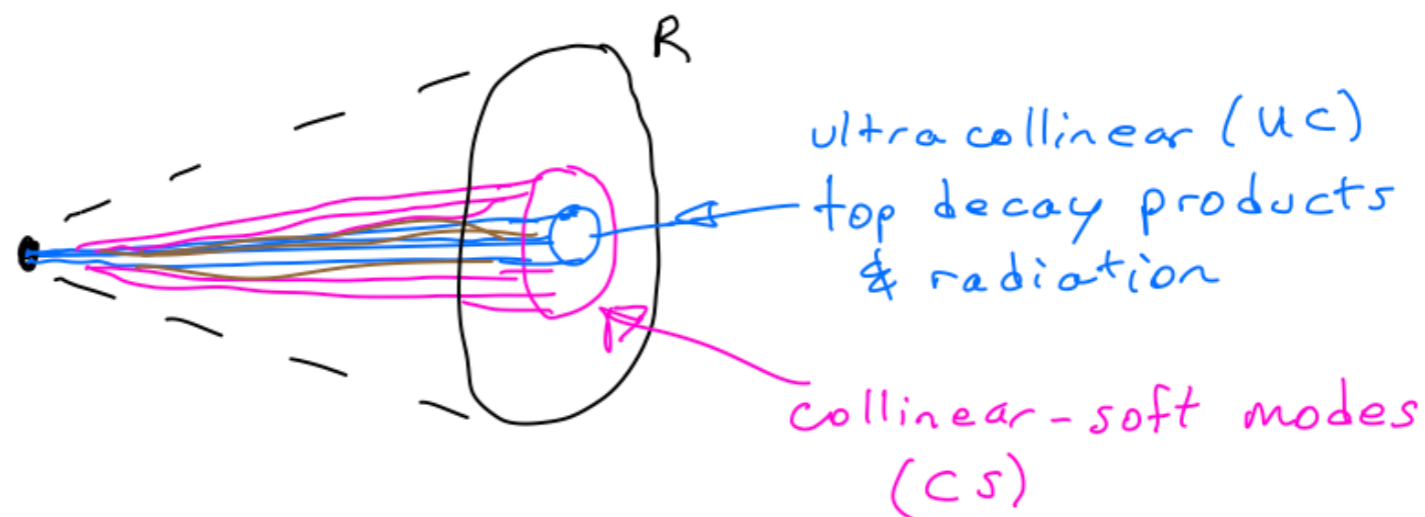
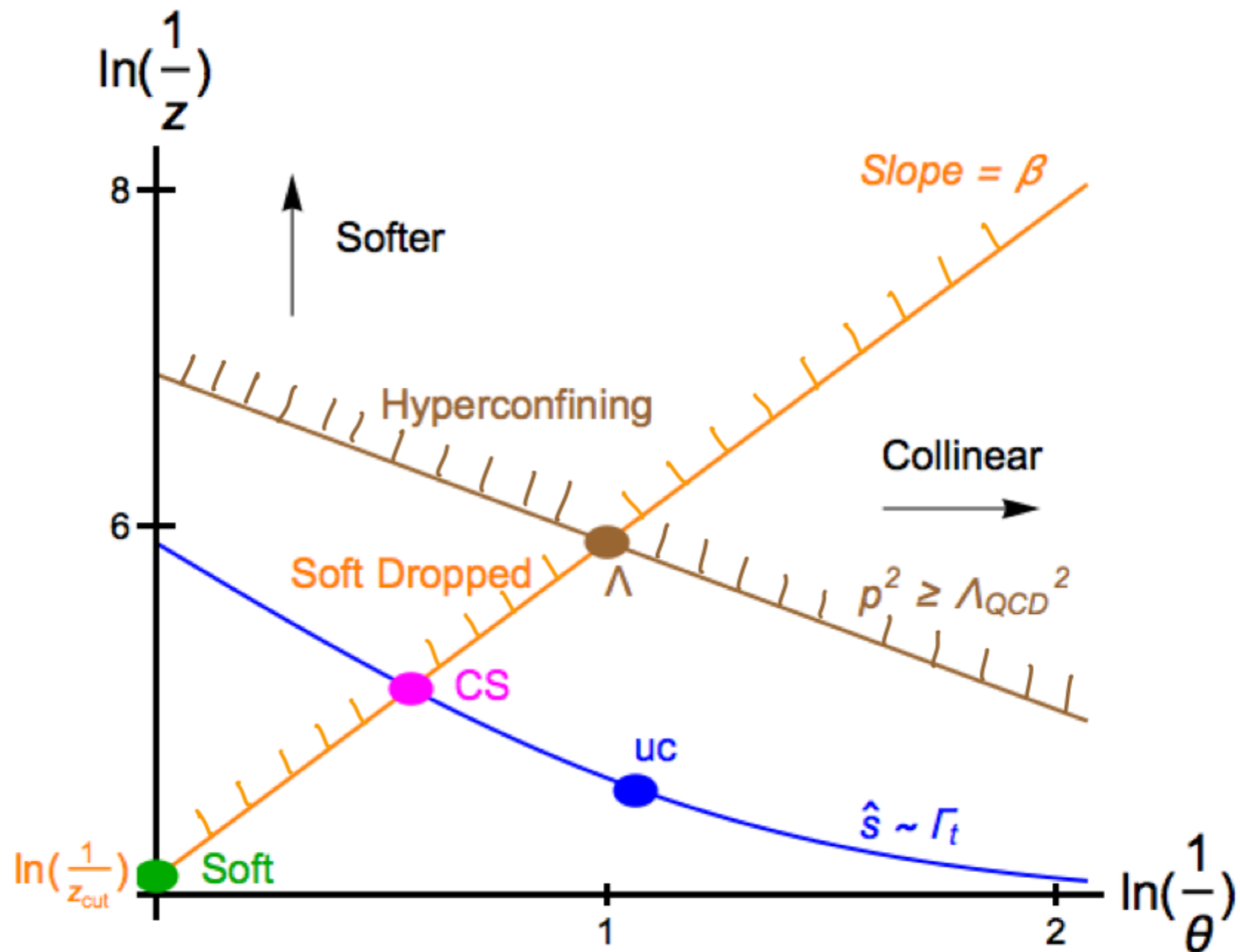


(Perturbative and Nonperturbative effects give  $\Gamma > \Gamma_t$  )

# Modes:



# Modes:

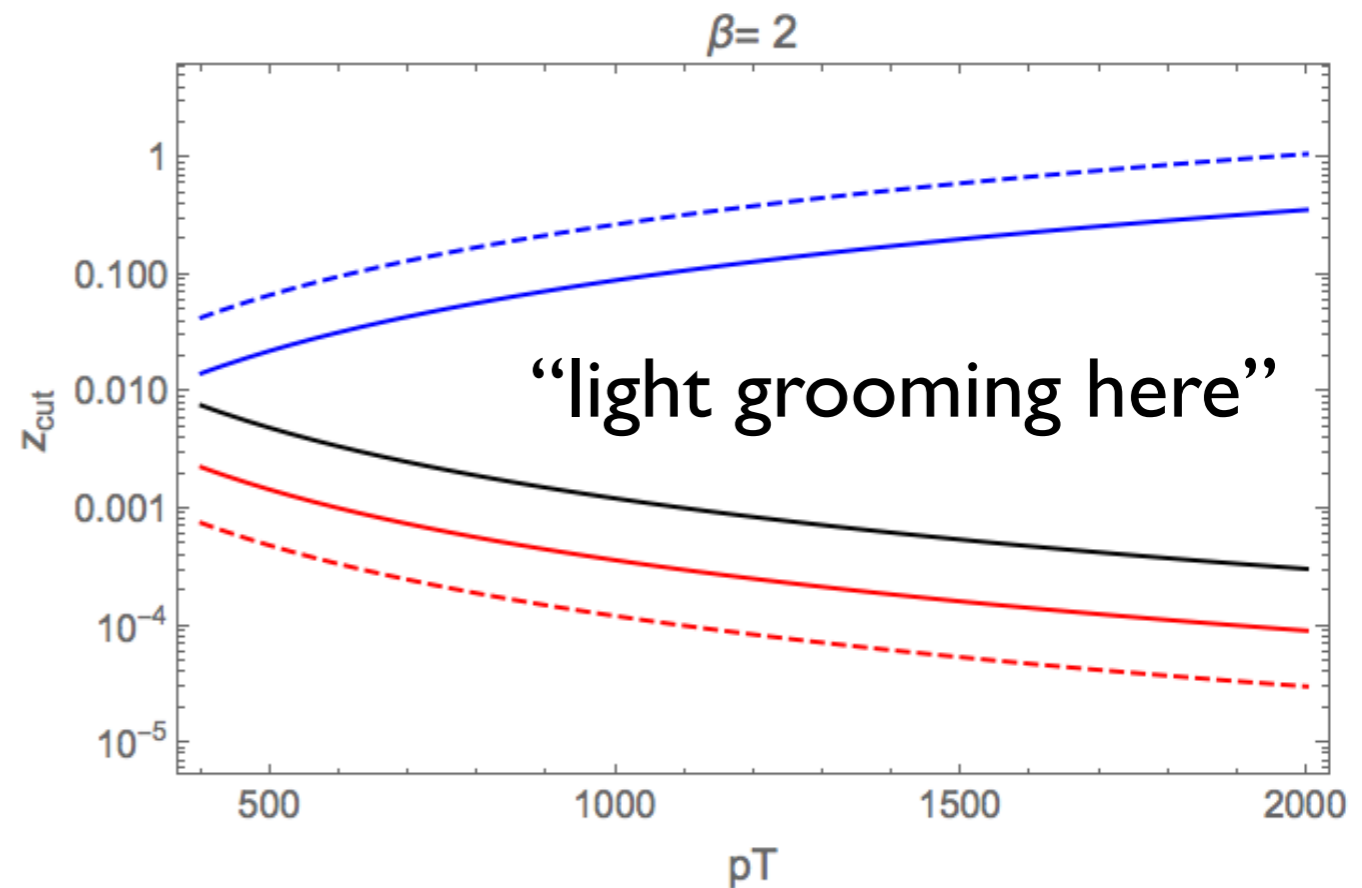


Can only apply a “light soft drop” for tops:

$$\frac{\Gamma_t}{m} \left( \frac{Q}{2m} \right)^\beta \gg z_{\text{cut}} \gg \frac{2m\Gamma_t}{Q^2}$$

Ensure soft drop does not touch  $J_B$

Ensure soft drop removes global soft radiation from measurement



Factorization with Soft Drop on one jet:

$$\frac{d^2\sigma}{dM_J^2 d\mathcal{T}^{\text{cut}}} = \text{tr} \left[ \hat{H}_{Qm} \hat{S}(\mathcal{T}^{\text{cut}}, Qz_{\text{cut}}, \beta, \dots) \otimes F \right] \otimes J_B \otimes \mathcal{I} \otimes f f$$

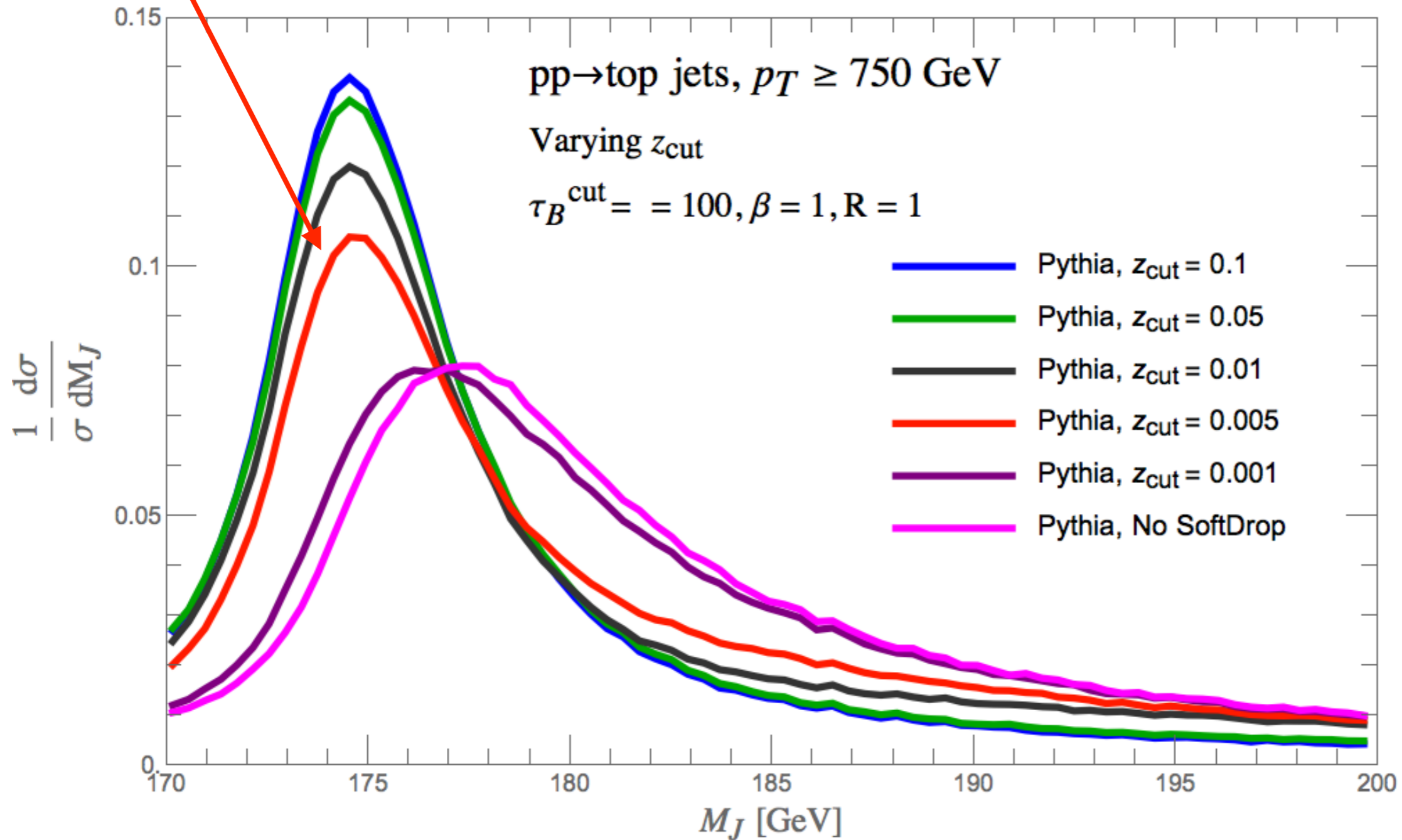
$$\times \left\{ \int d\ell dk J_B \left( \hat{s}_t - \frac{Q\ell}{m}, \Gamma_t, \delta m \right) S_C \left[ \ell - \left( \frac{k^{2+\beta}}{2^\beta Q z_{\text{cut}}} \right)^{\frac{1}{1+\beta}}, Qz_{\text{cut}}, \beta \right] F_C(k) \right\}$$

# Pythia Tests

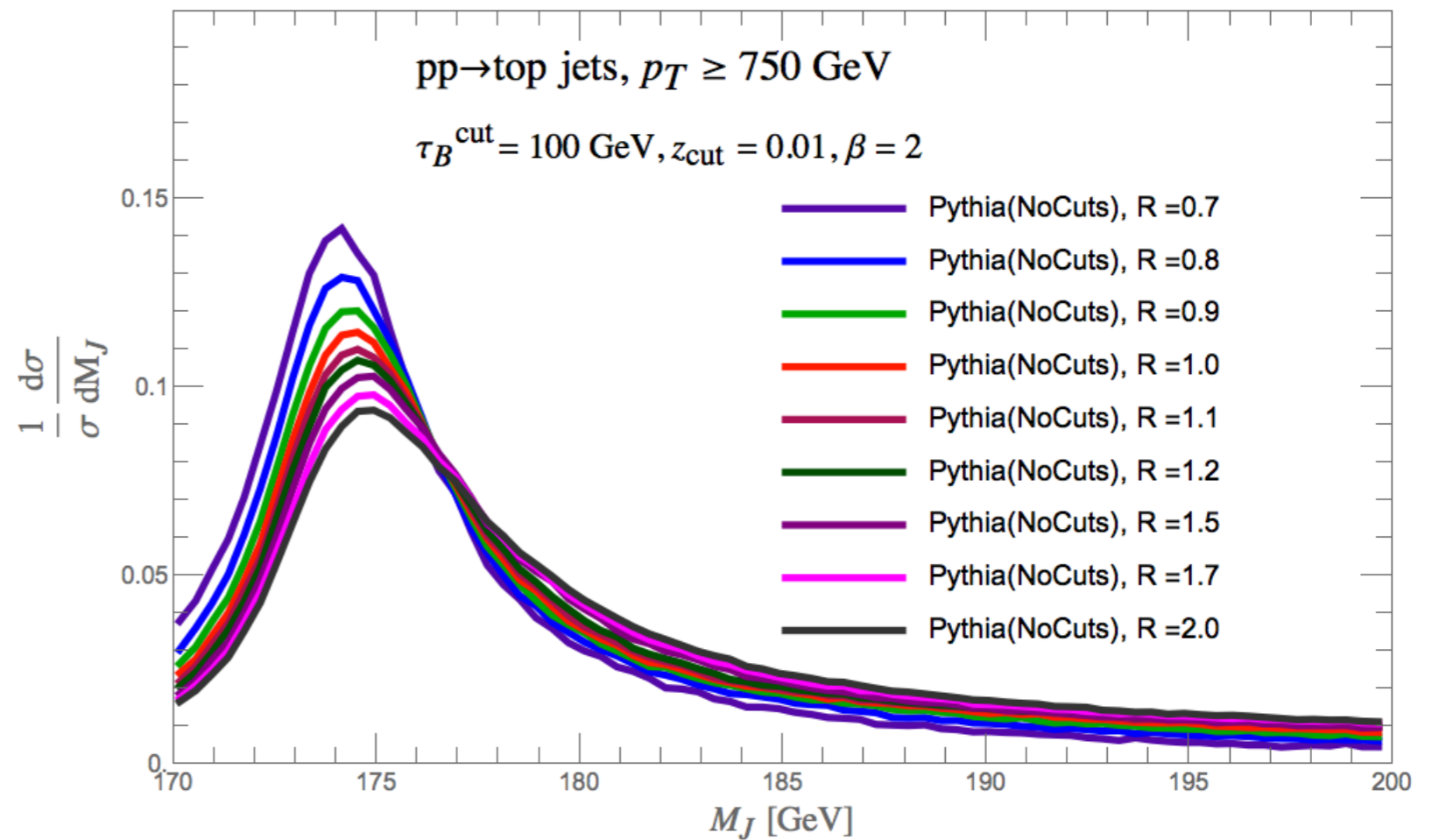
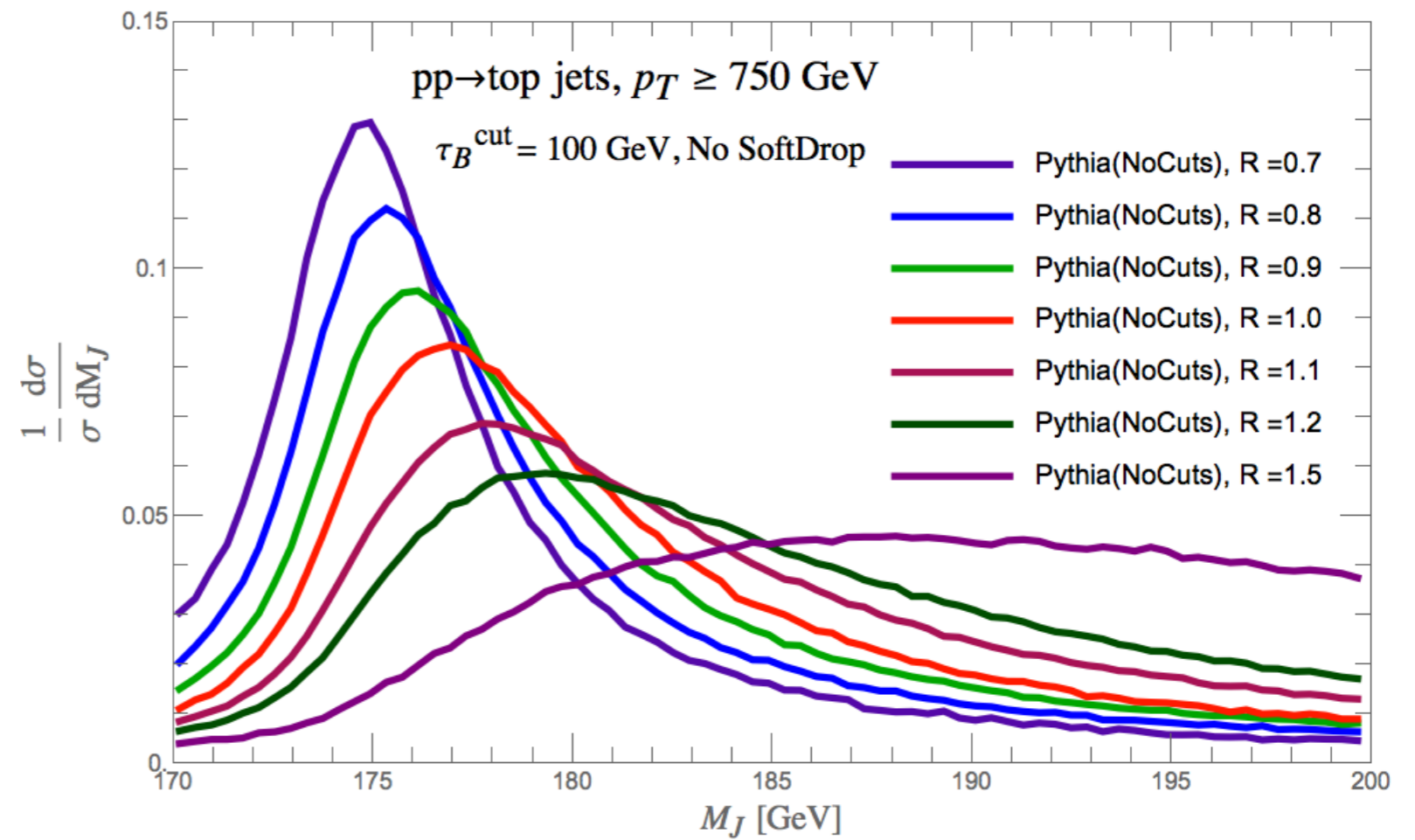


# $z_{\text{cut}}$ dependence

Transition for “light grooming”  
as predicted by factorization!

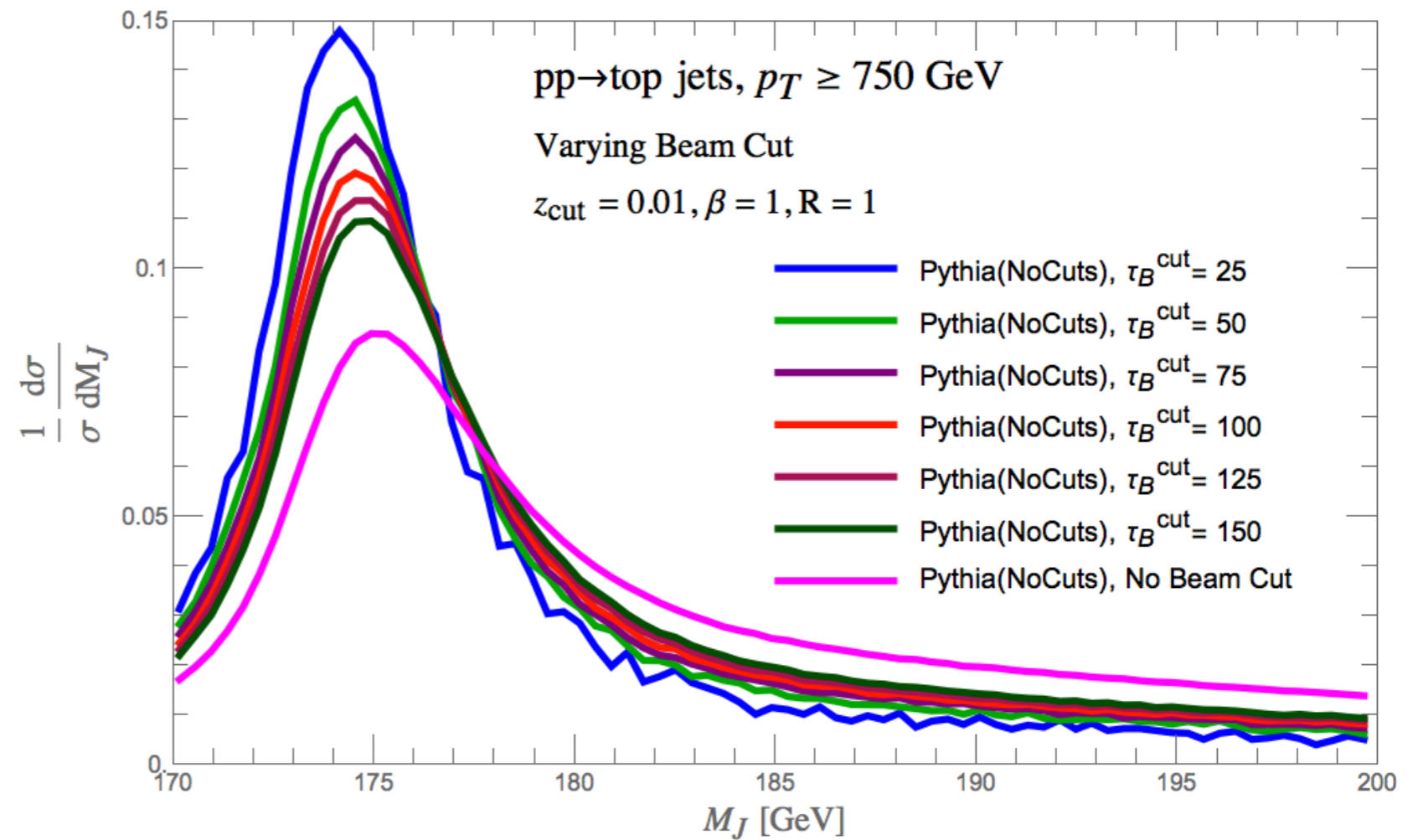
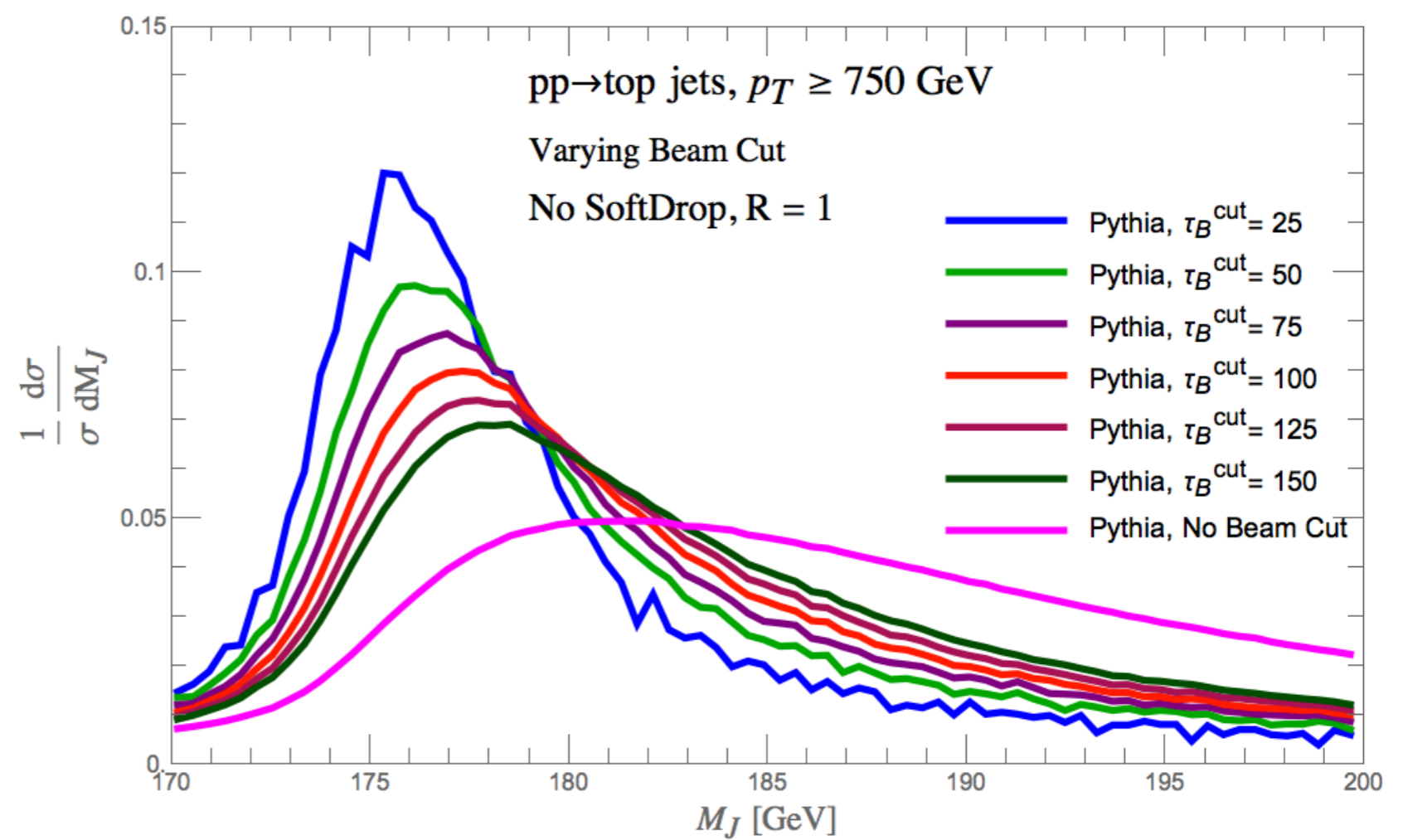


# Jet Radius Dependence

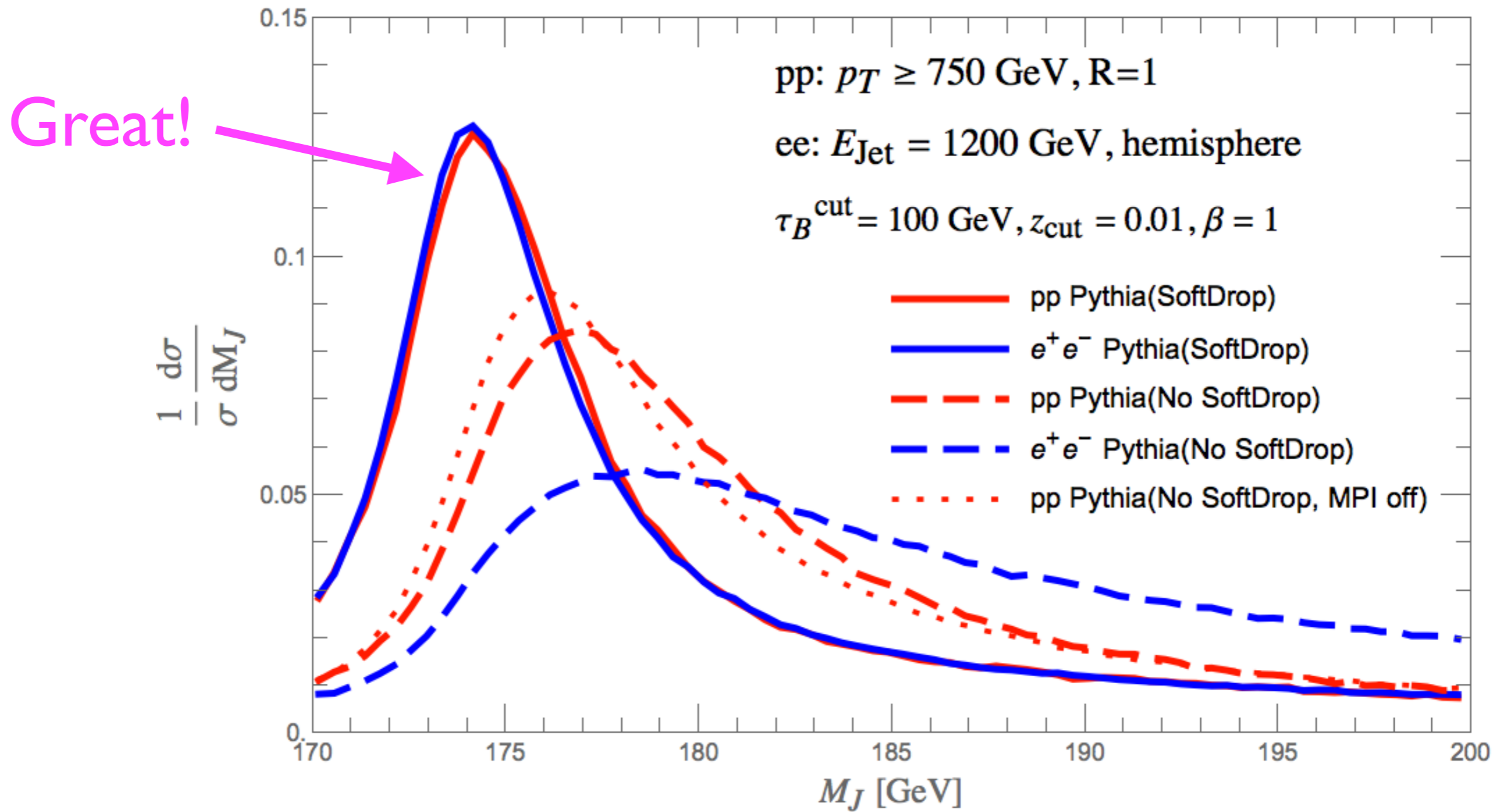


residual dependence  
 $\sim 200$  MeV (this  $p_T$ )

# Beam Cut Dependence

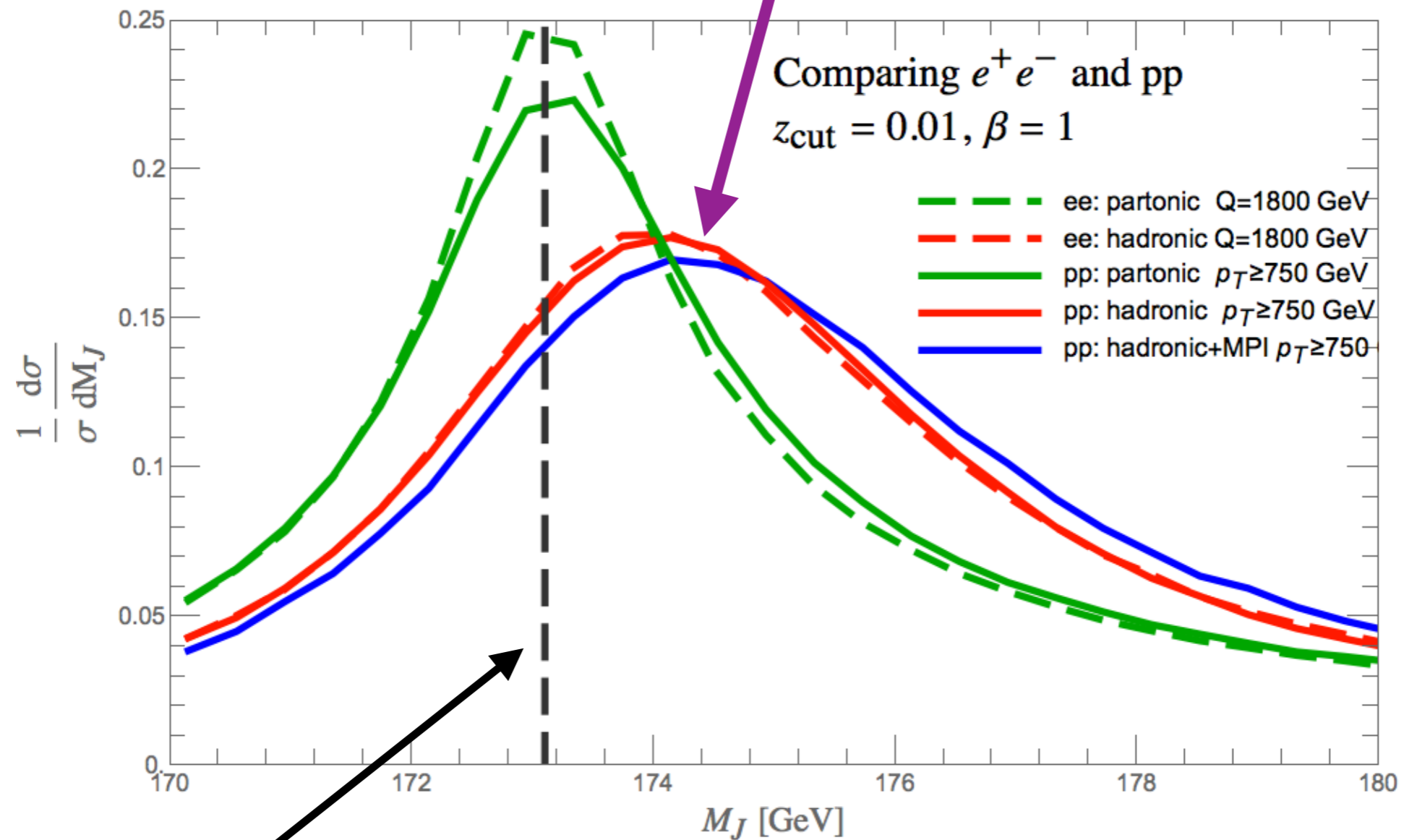


# Pythia (Hadronic e+e-) versus (Hadronic+MPI pp)



# e+e- comparison with pp: MPI and Hadronization effects (All curves with SoftDrop)

Only 0.19 GeV **shift** from MPI

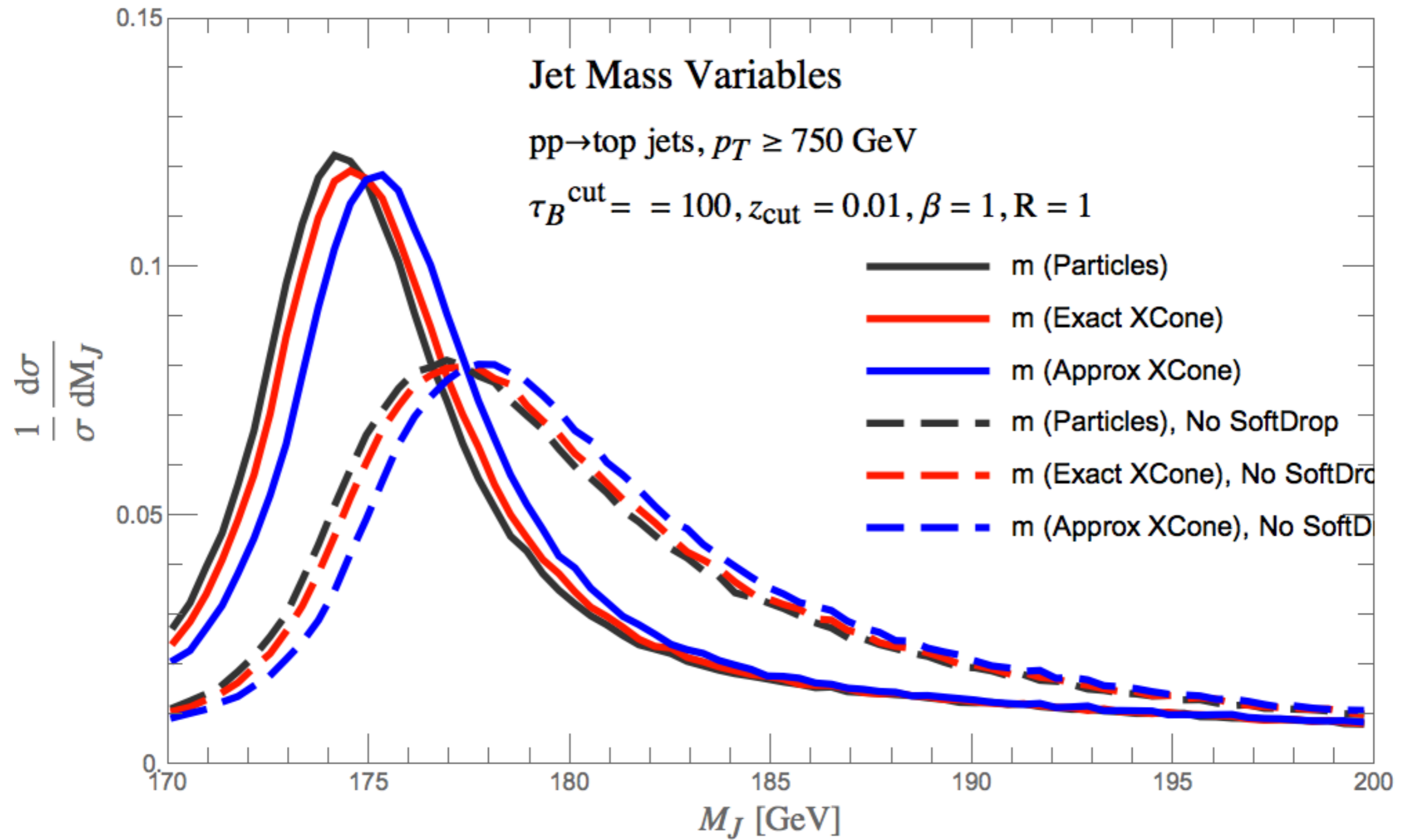


input mass in  
Pythia = 173.1 GeV

# Pythia vs. Factorization



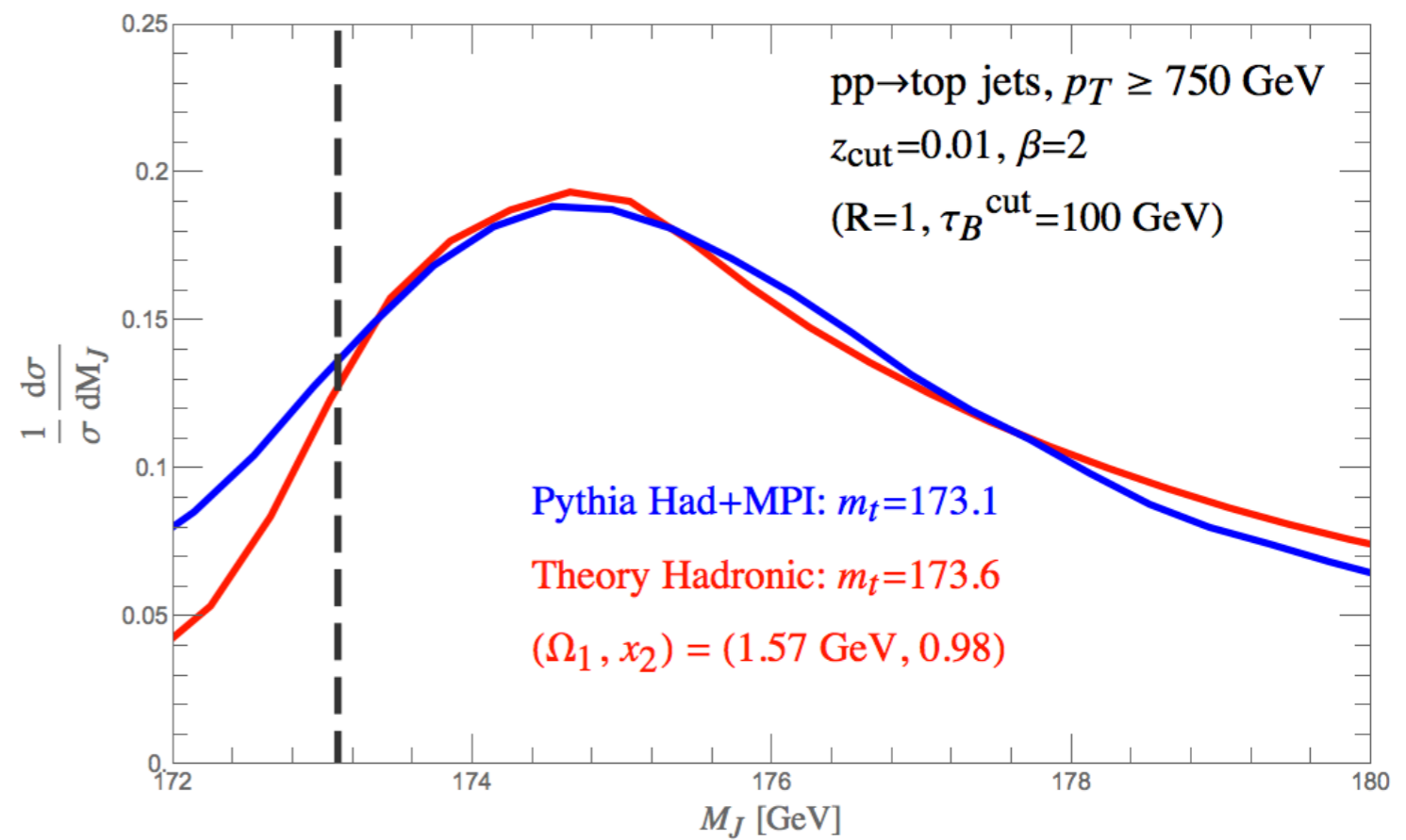
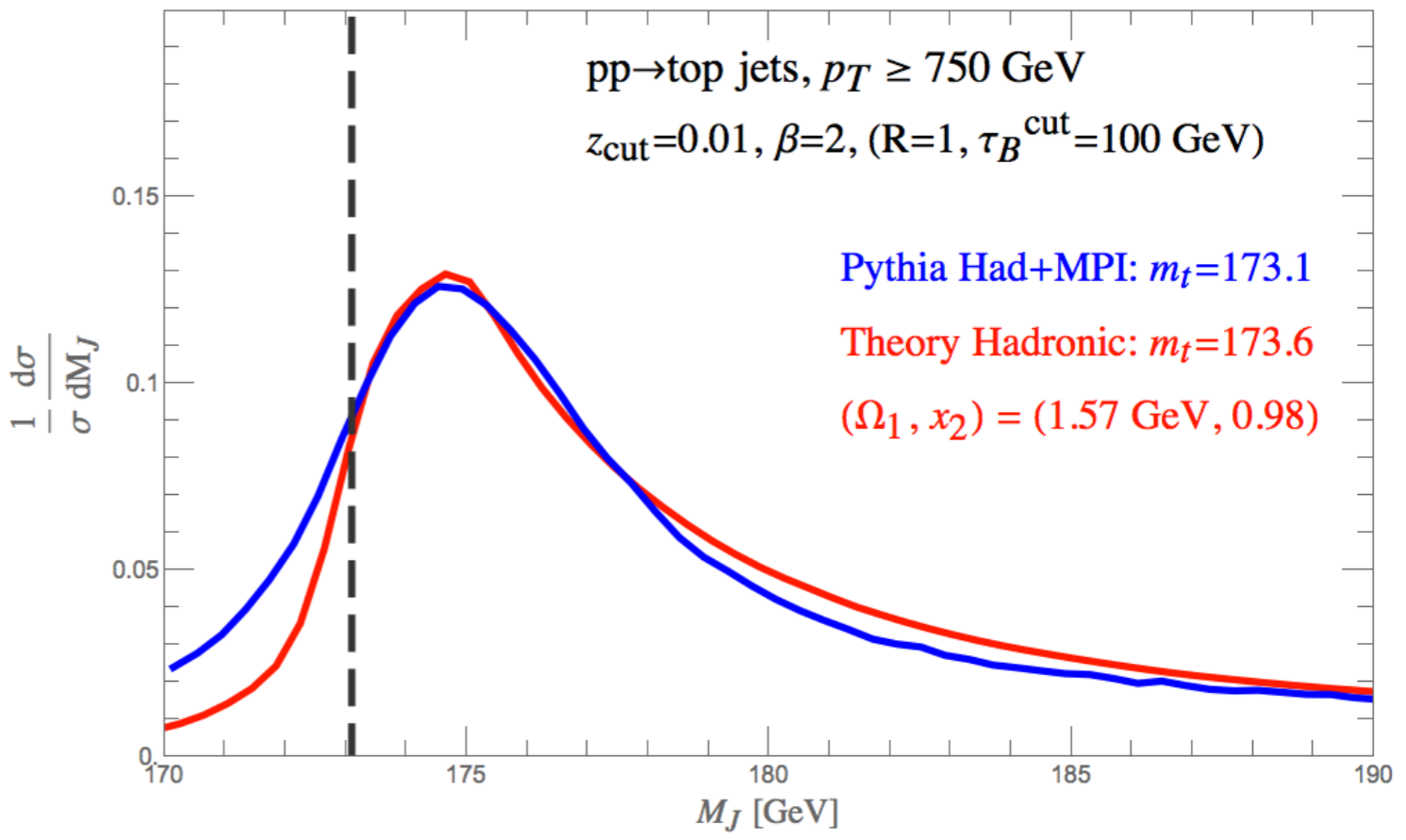
# Which $M_J$ Variable?



# Pythia vs. Factorization with SoftDrop

includes:  
Hadronization+MPI

input mass in  
Pythia = 173.1 GeV

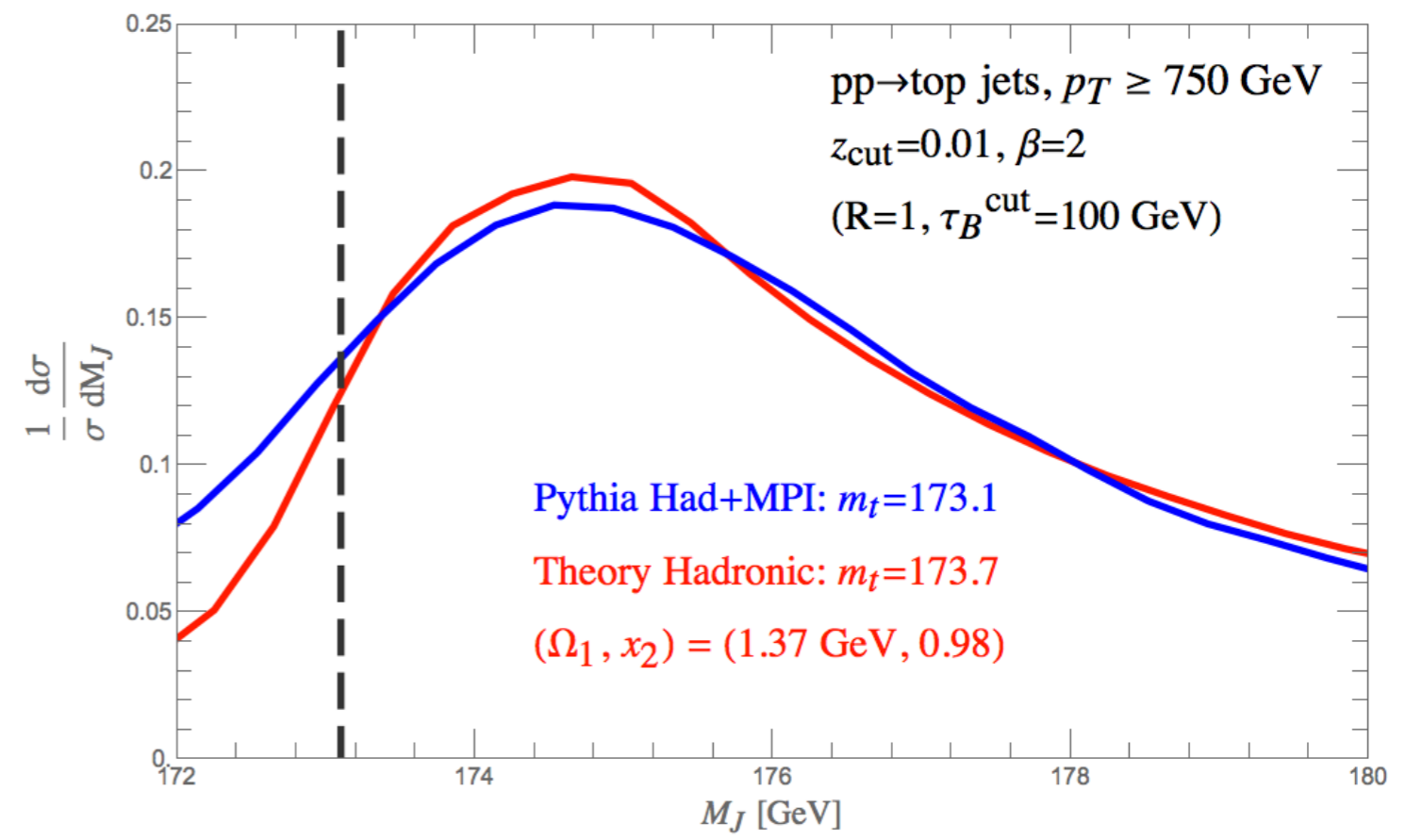
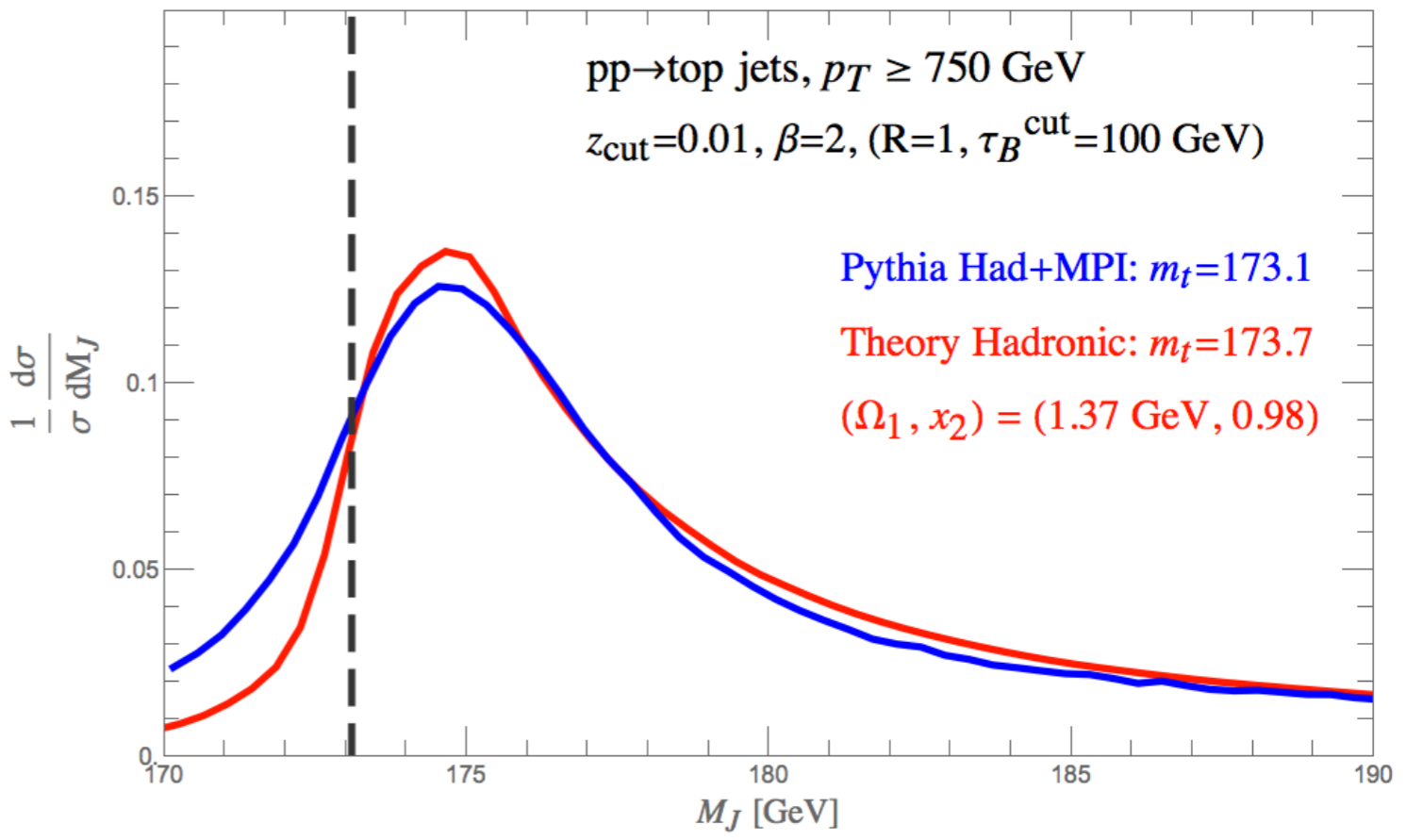




# Pythia vs. Factorization with SoftDrop

includes:  
Hadronization+MPI

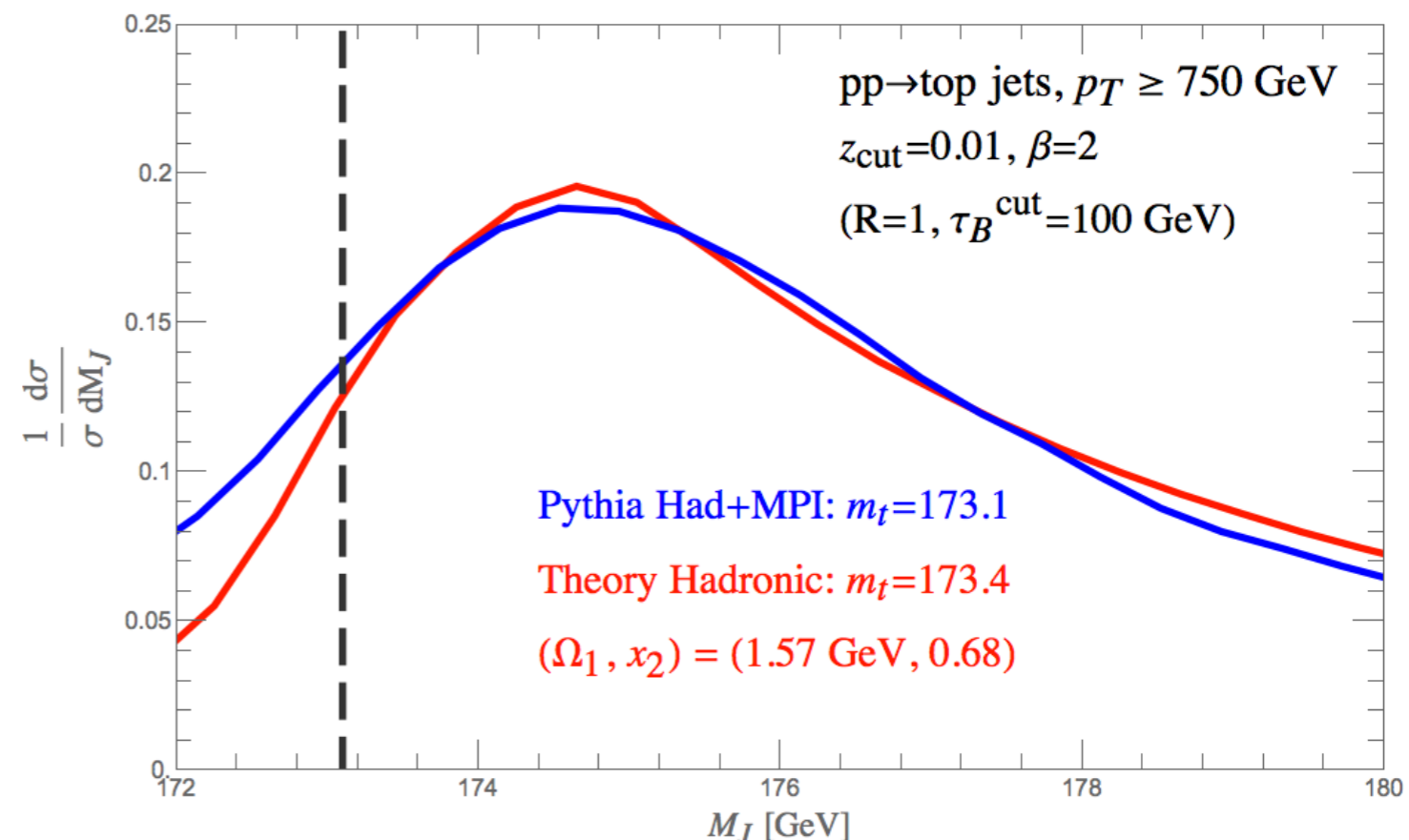
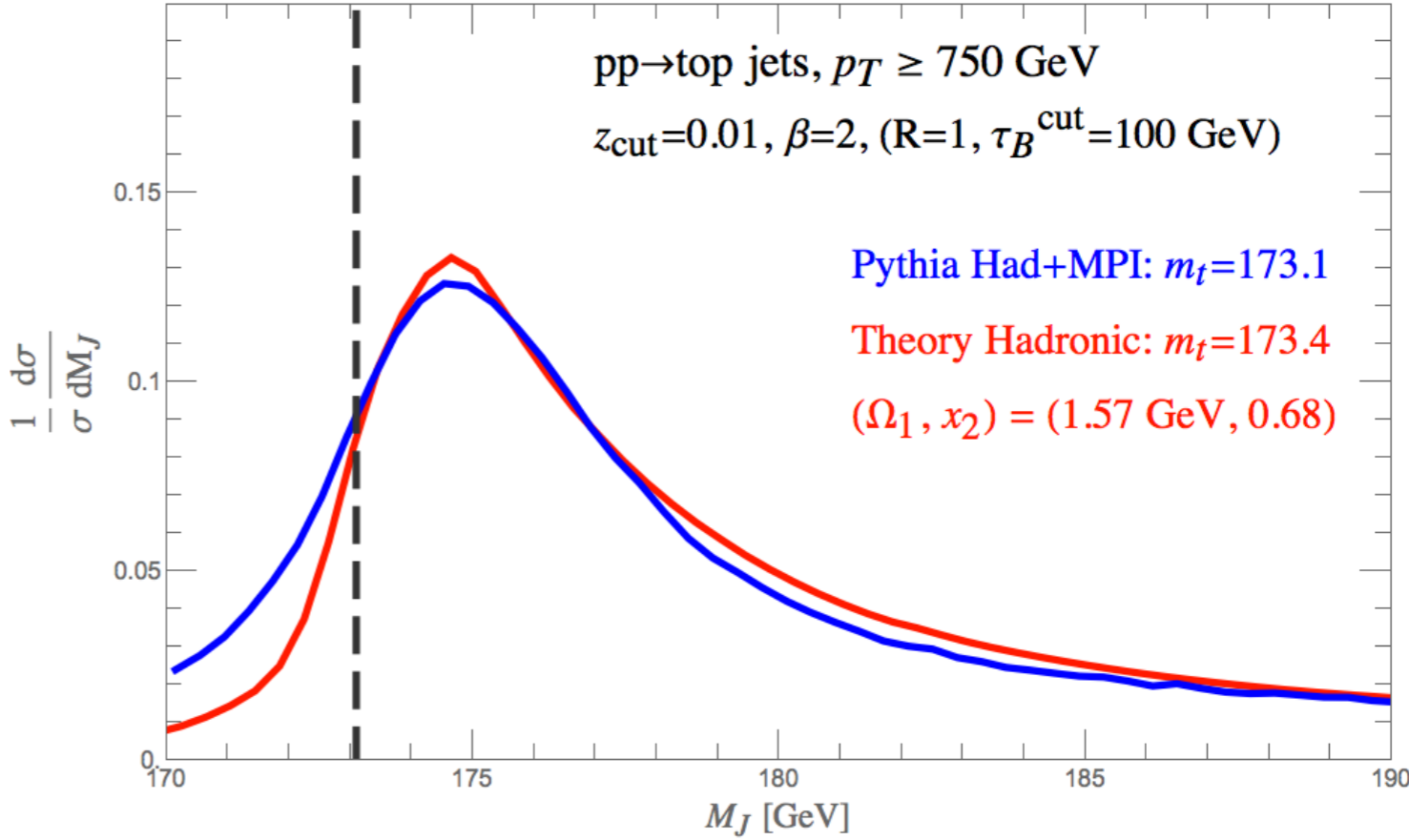
input mass in  
Pythia = 173.1 GeV



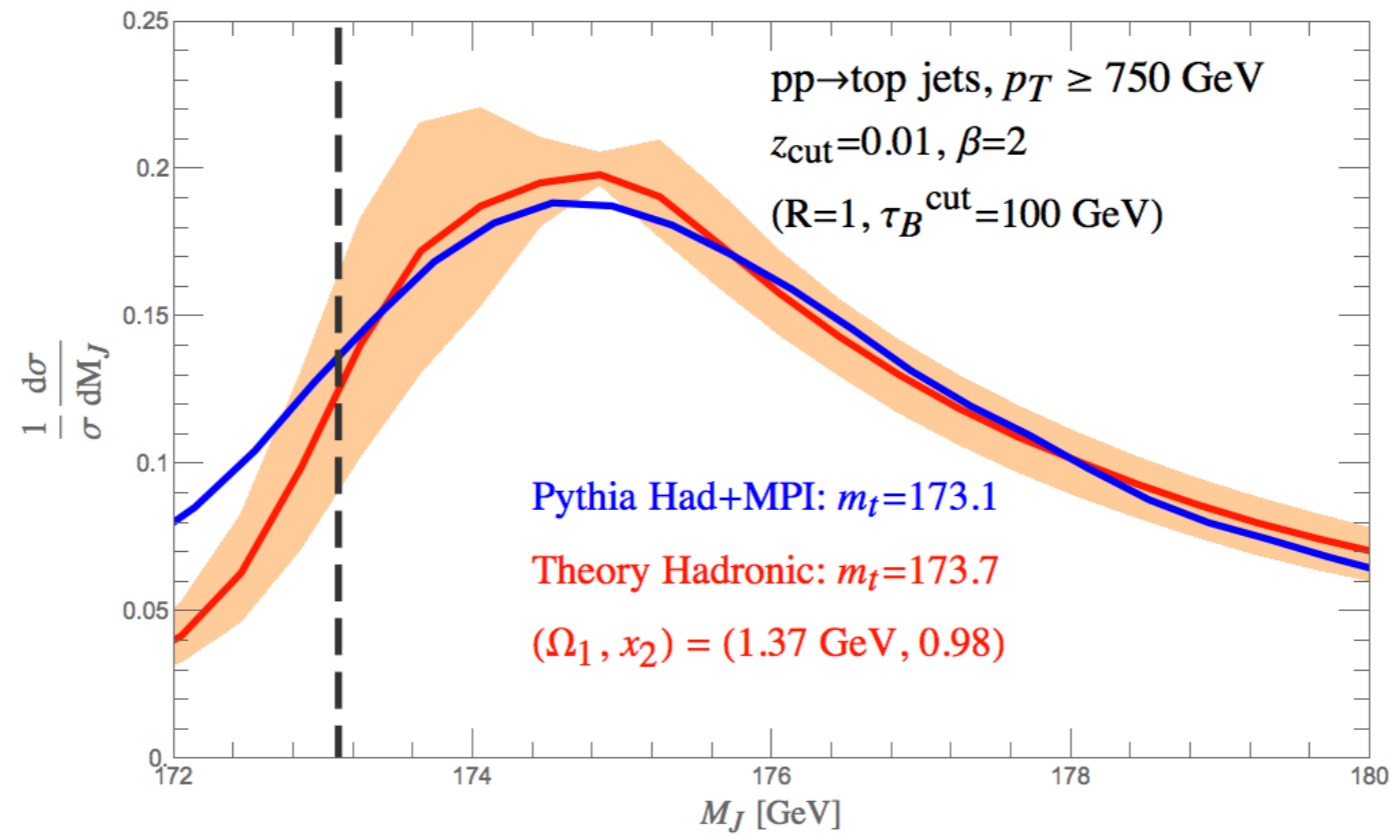
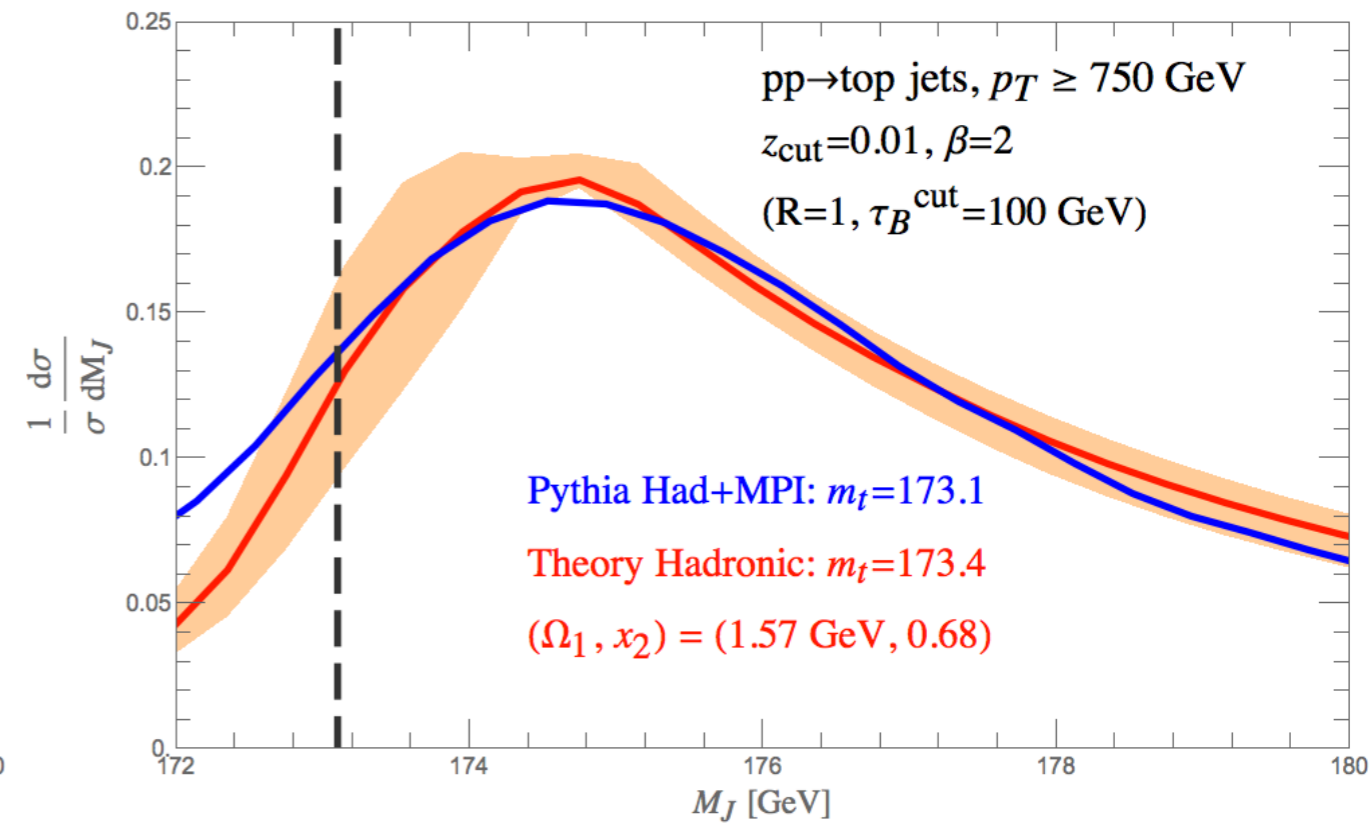
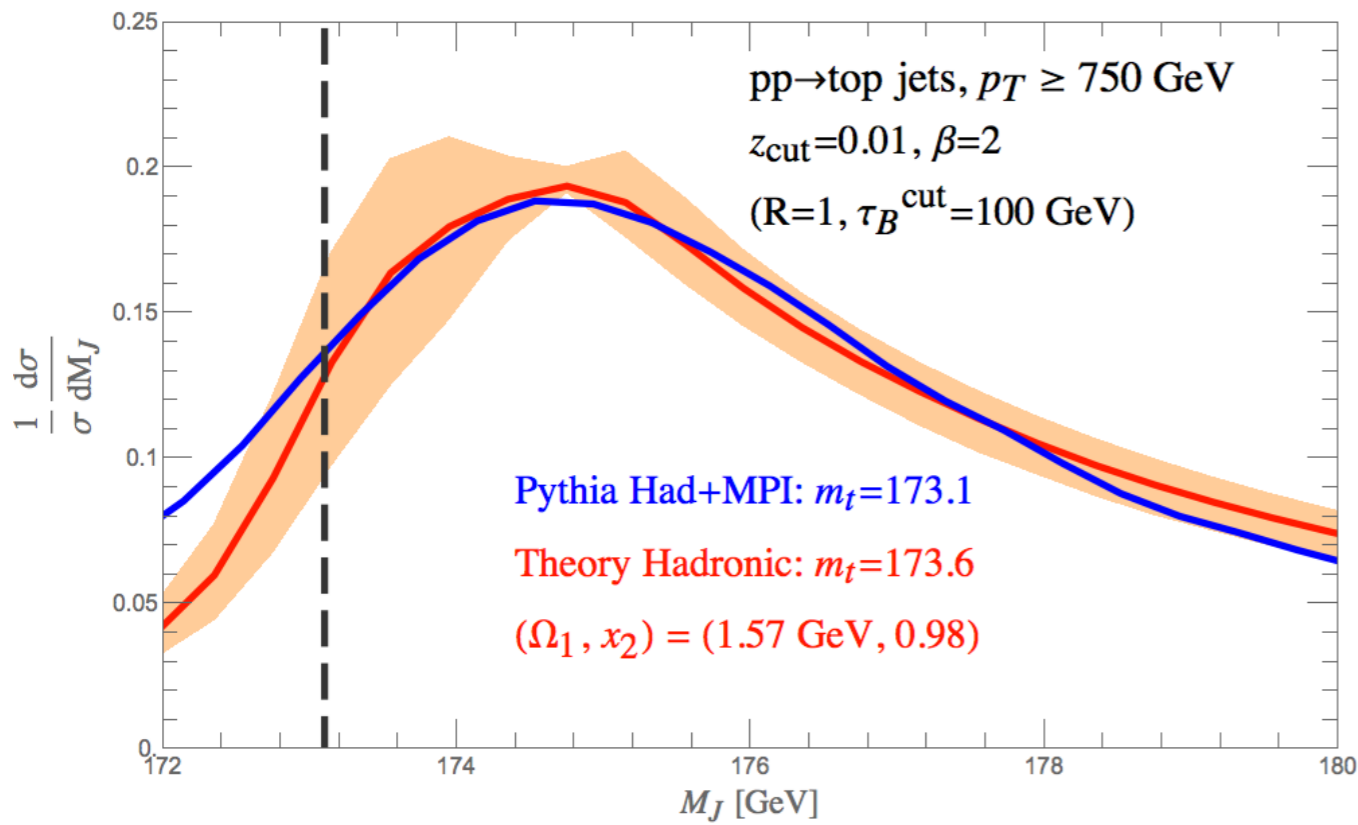
# Pythia vs. Factorization with SoftDrop

includes:  
Hadronization+MPI

input mass in  
Pythia = 173.1 GeV



# Adding NLL uncertainty bands



Looks very promising.

But do note that this was high  $p_T$ .

Pythia: curves do not change for lower  $p_T$  with  $R=1$

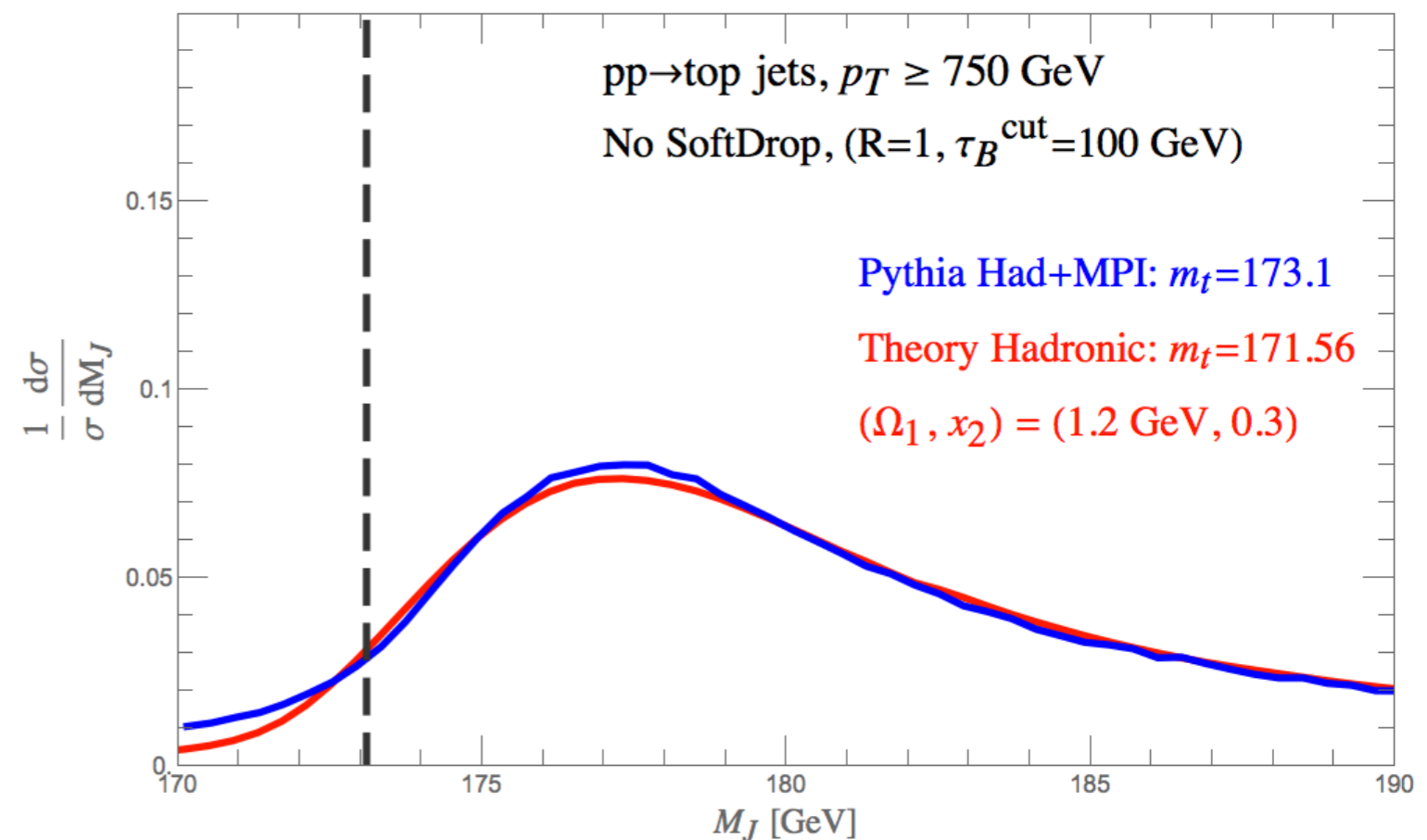
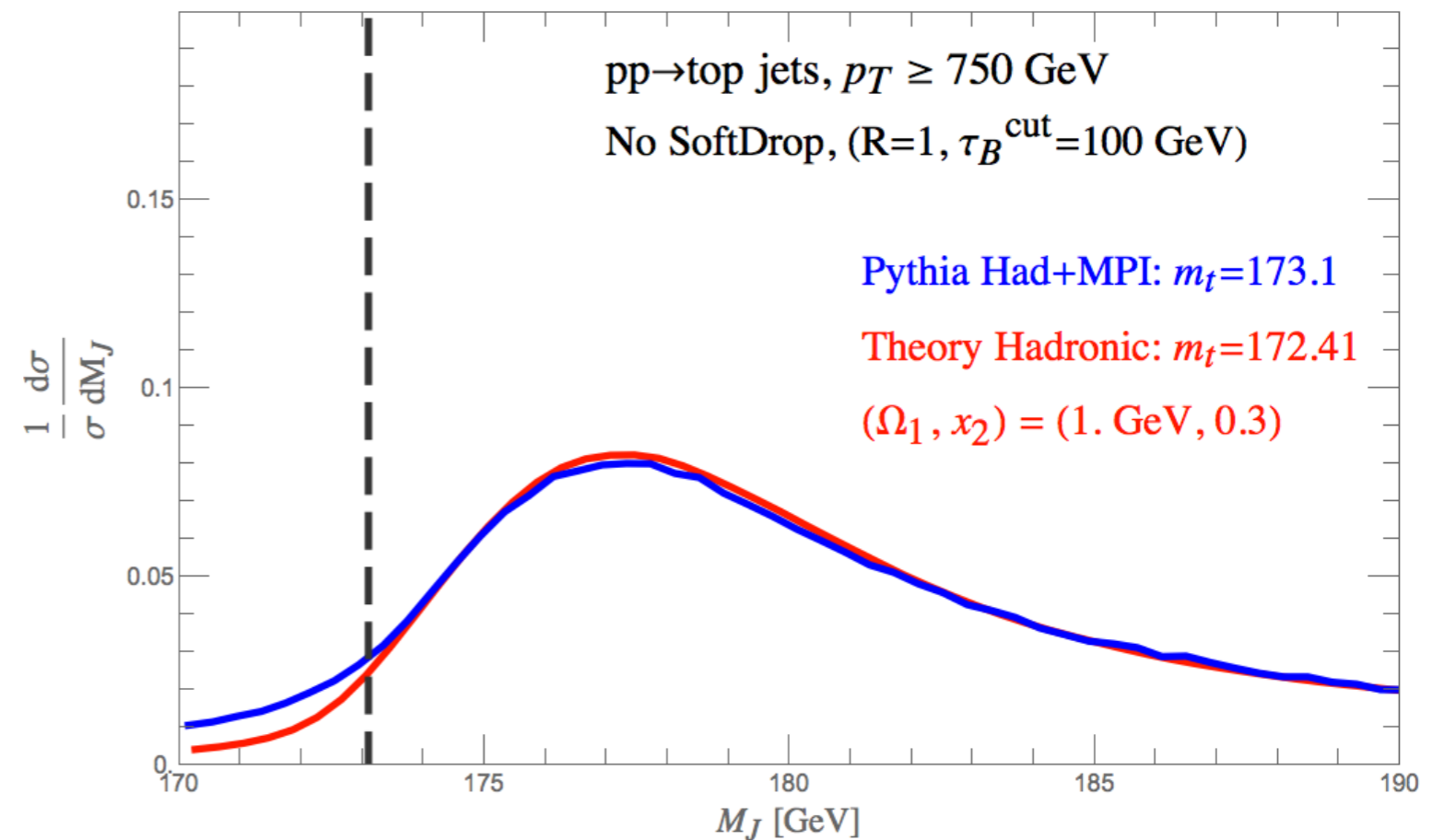
Not yet clear whether lower  $p_T$   
values can be predicted with  
SoftDrop.

For Comparison:

no SoftDrop

Pythia vs.  
Factorization

two reasonable fits with  
quite different masses



## Summary

- Largest uncertainty in the top mass is “what mass is it?”
- Factorization provides answers with short distance  $m_t$  parameters
- Can Calibrate MC to determine relation:  $m_t^{\text{MC}} = m_t + \dots$
- Discussed promising new method in pp to measure Top Quark Mass

## Future Directions

- More pT bins, NNLL, fits , combine SoftDrop & no SoftDrop, ...
- pp Monte Carlo calibration