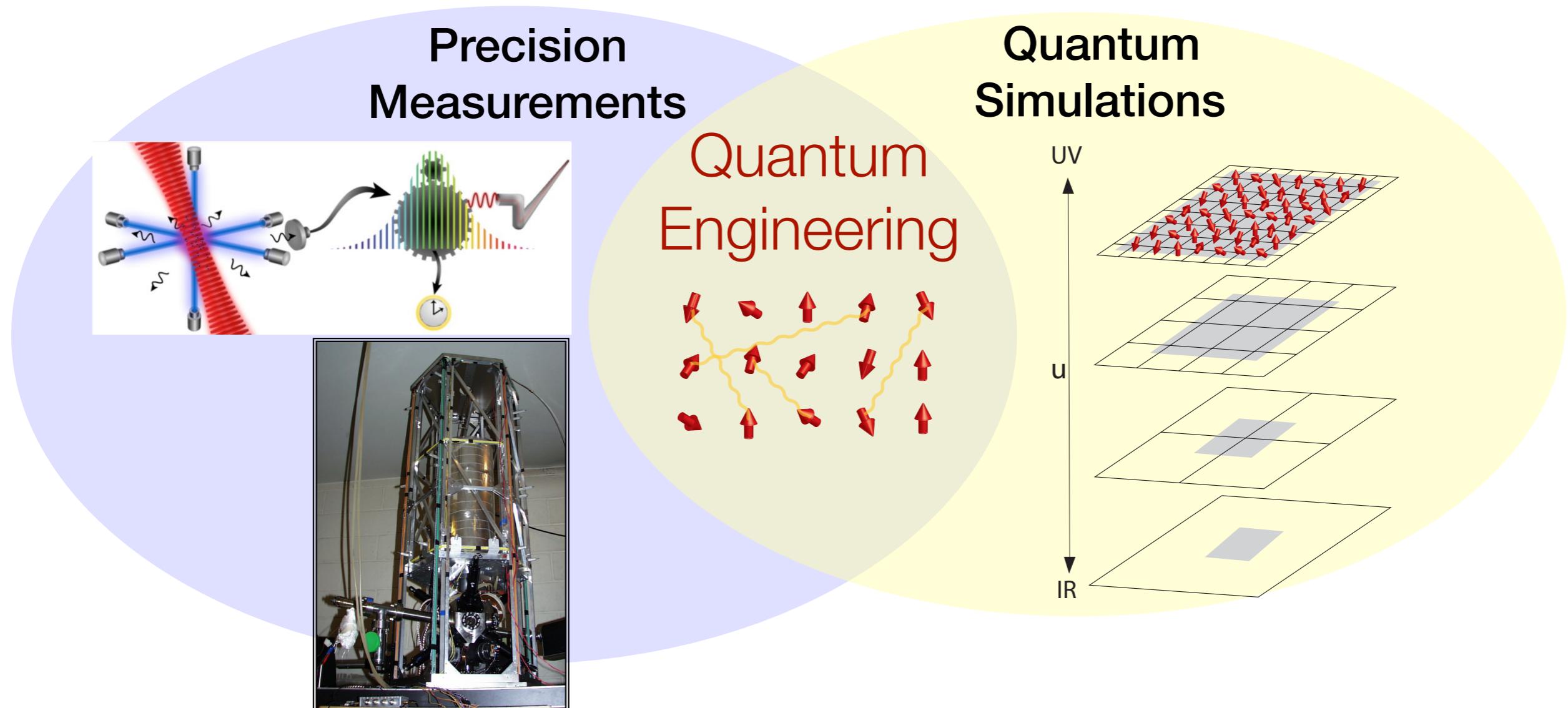


Quantum Engineering with Cold Atoms and Light

Monika Schleier-Smith

December 13, 2017

Quantum Engineering for Fundamental Physics

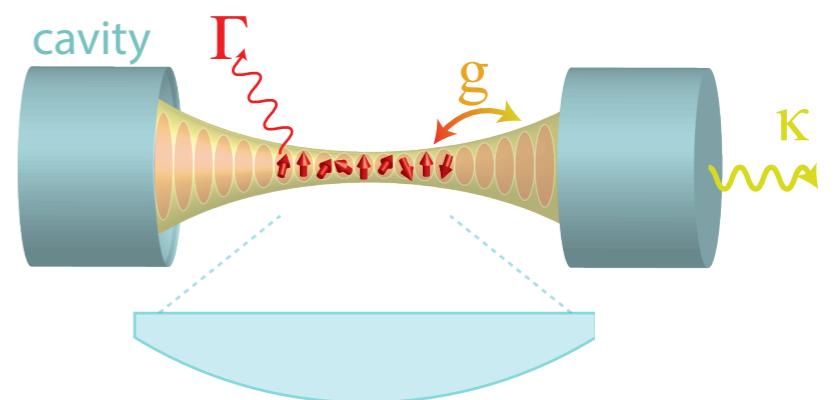


Outline

Motivation and Background

Quantum metrology

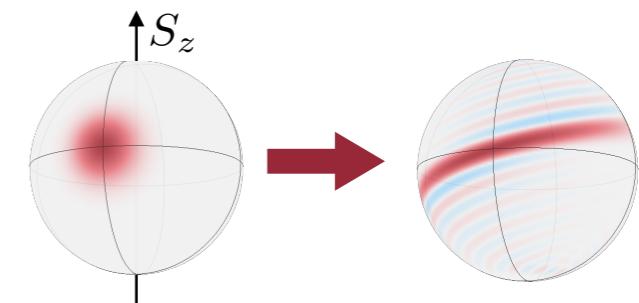
Entangling atoms with photons



Seeking the Heisenberg Limit

Engineering entanglement in a dissipative world

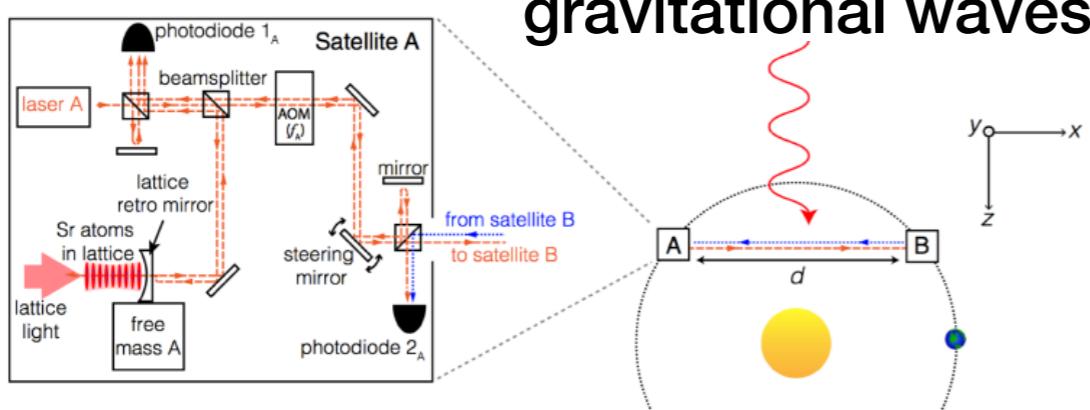
Harnessing entanglement in a noisy world



Summary & Outlook

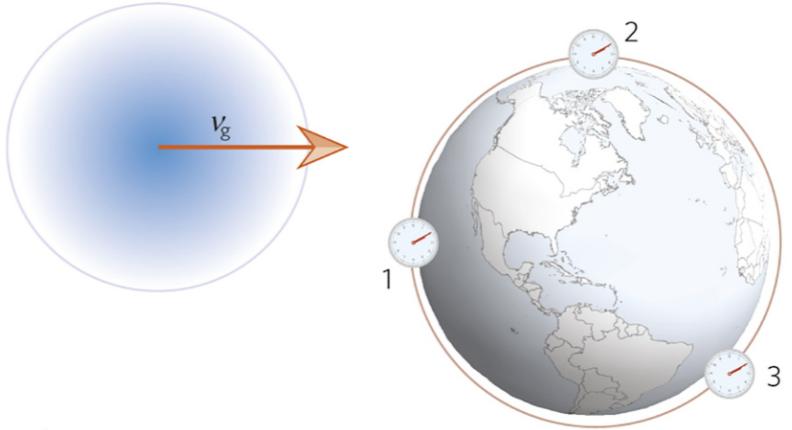
Quantum Metrology: Motivation

Ultra-stable clocks as sensors



Kolkowitz, ... & Ye, *Phys. Rev. D* (2016).

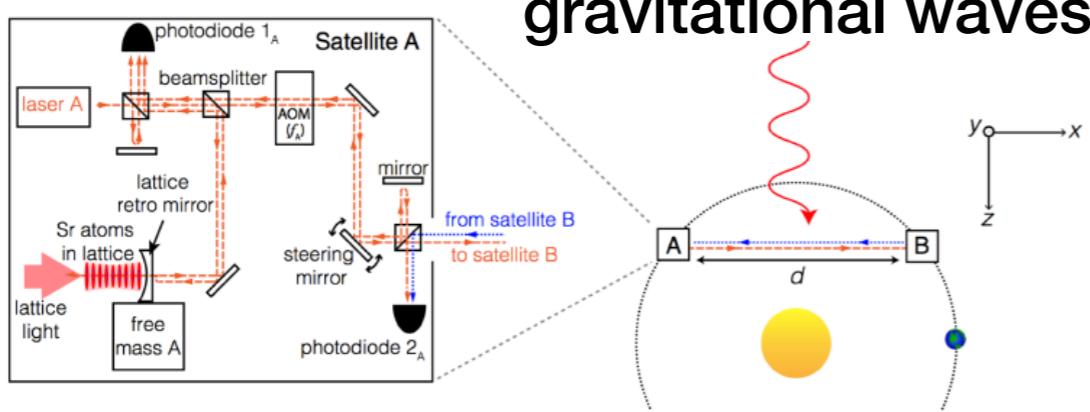
dark matter



Derevianko & Pospelov, *Nat. Phys.* (2014).
Arvanitaki, Huang, & Van Tilburg, *PRD* (2015).

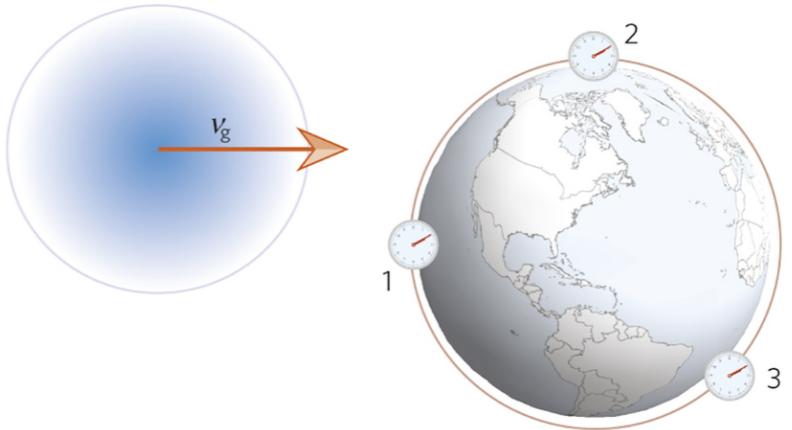
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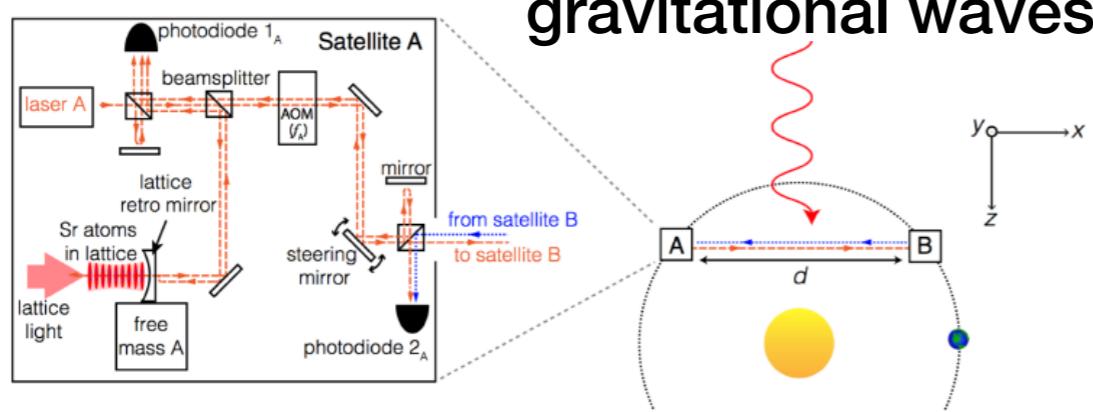
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Entanglement can enable...

→ higher precision in fixed time with finite atom number N

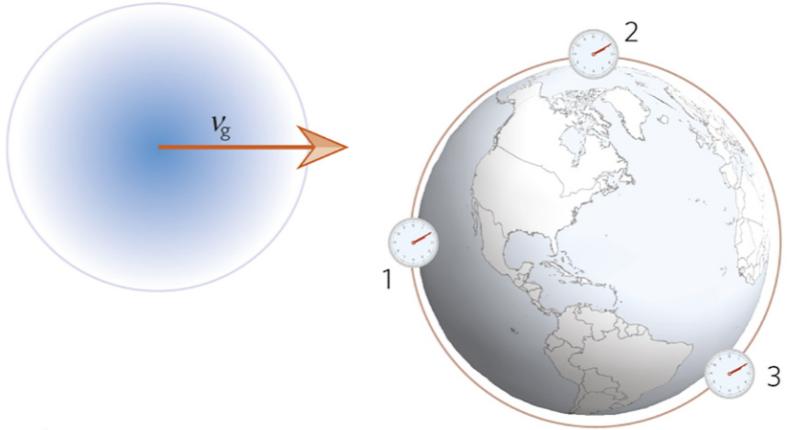
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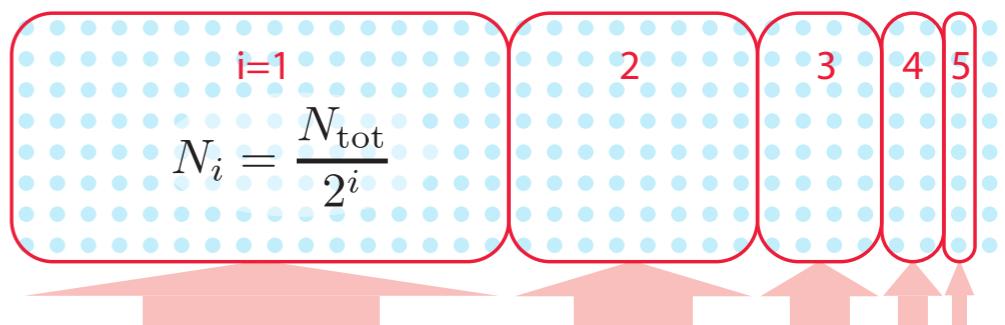
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Entanglement can enable...

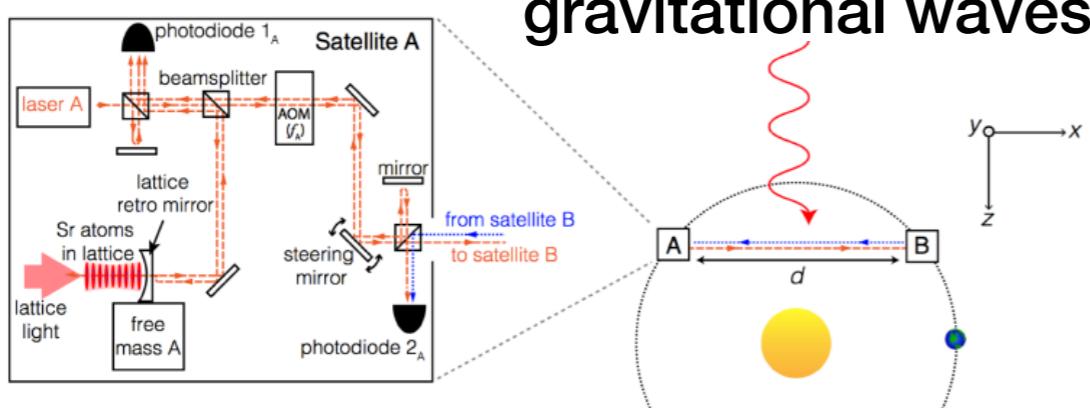
- higher precision in fixed time with finite atom number N
- distribution of resources for enhanced bandwidth or dynamic range



Inspiration: Kessler, ..., Sorensen, Ye, Lukin, *PRL* (2014).

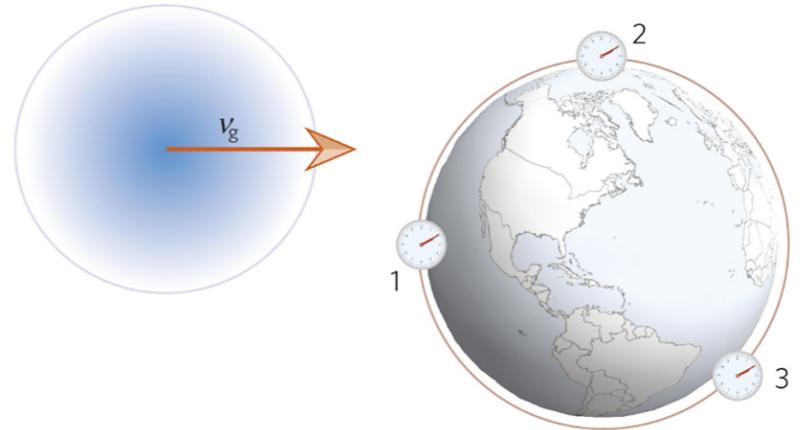
Quantum Metrology: Motivation

Ultra-stable clocks as sensors



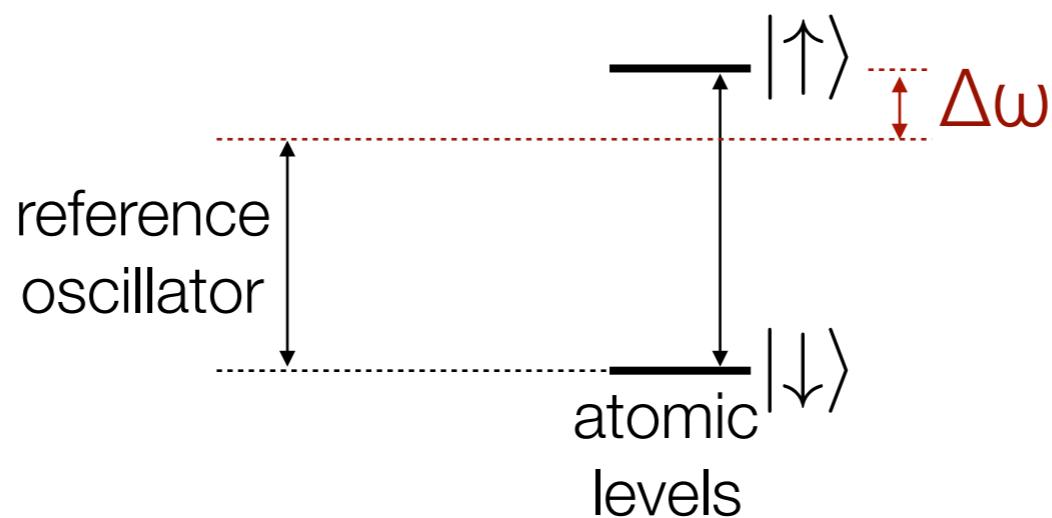
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dark matter



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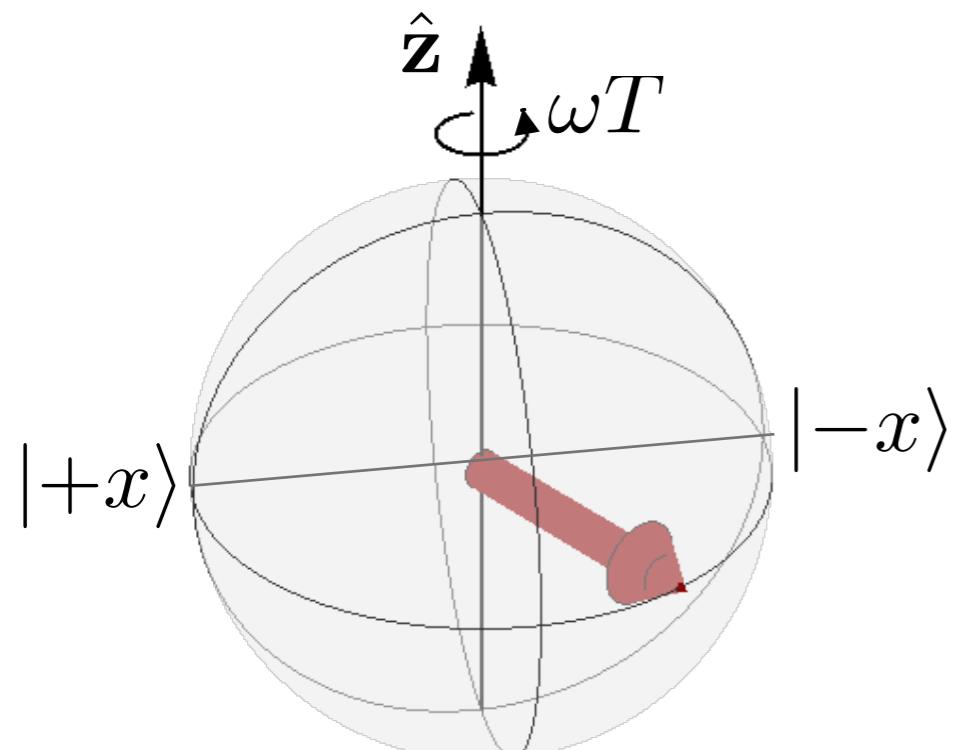
How fast can an atomic sensor detect a perturbation?



Speed Limits in Quantum Sensing

Time T for perturbation $\Delta\omega$ to appreciably change the quantum state

Single spin: $|\uparrow\rangle + e^{i\omega T} |\downarrow\rangle$

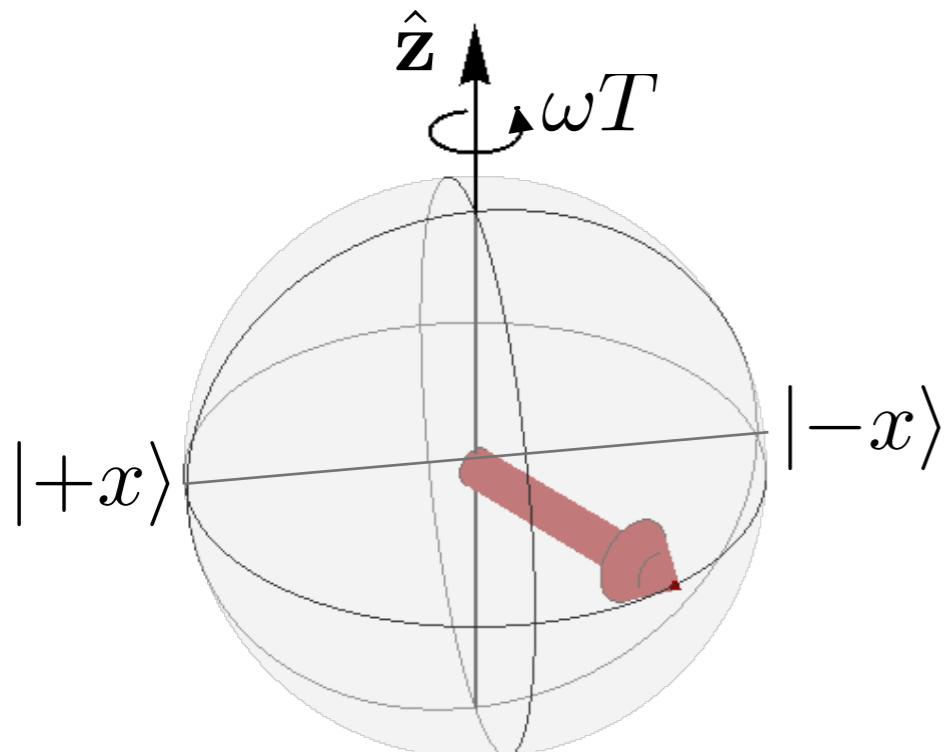


$$\Delta\omega T \sim 1$$

Speed Limits in Quantum Sensing

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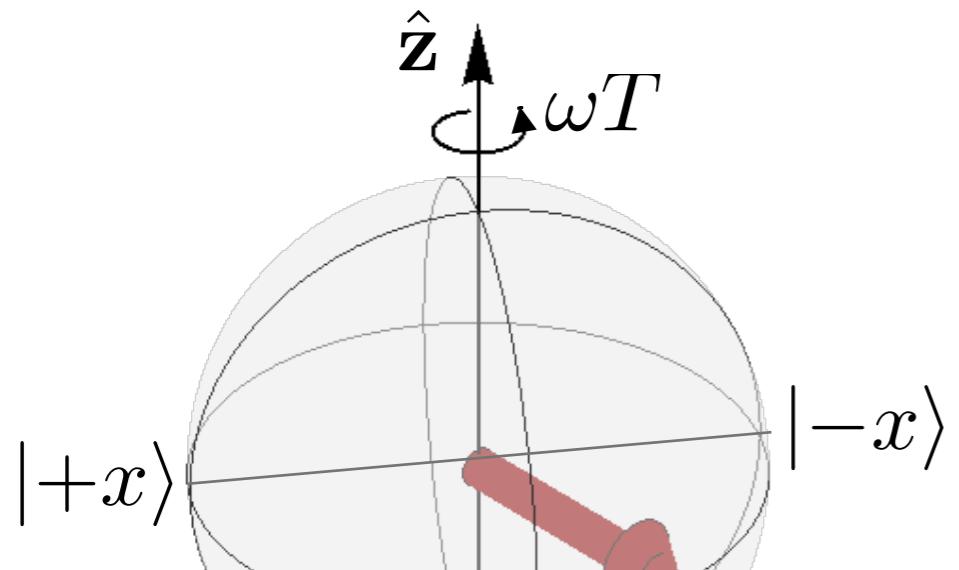
$$\Delta\omega T \sim 1$$

N spins: $|\uparrow\uparrow\dots\uparrow\rangle + e^{iN\omega T} |\downarrow\downarrow\dots\downarrow\rangle$

Speed Limits in Quantum Sensing

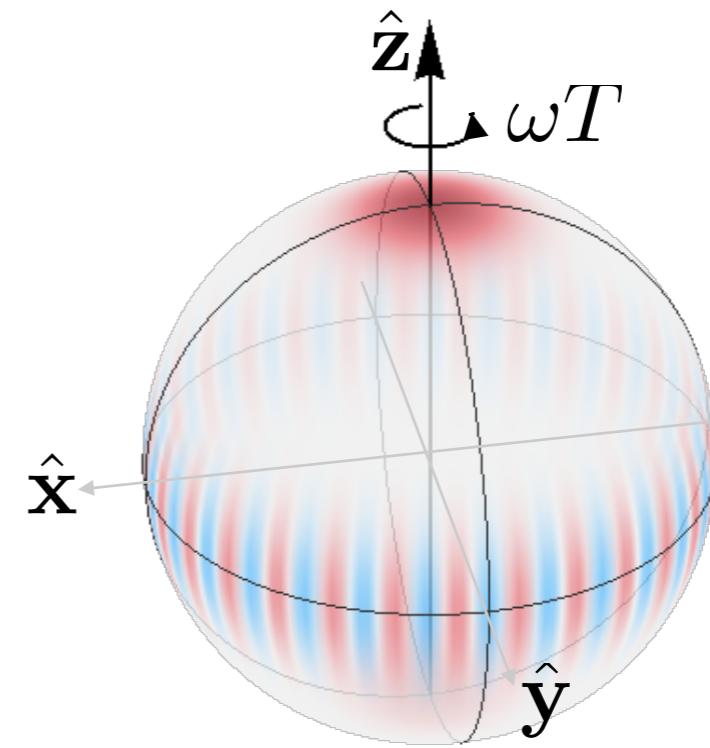
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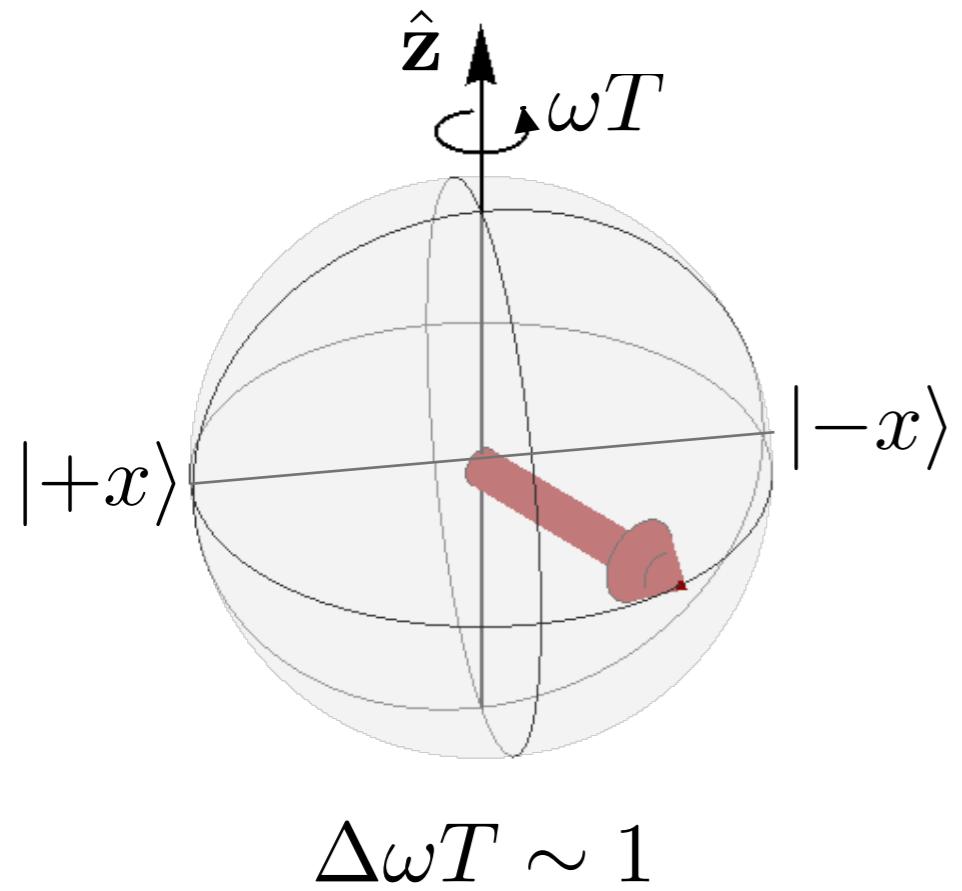
$$\Delta\omega T \sim 1/N$$

Heisenberg Limit

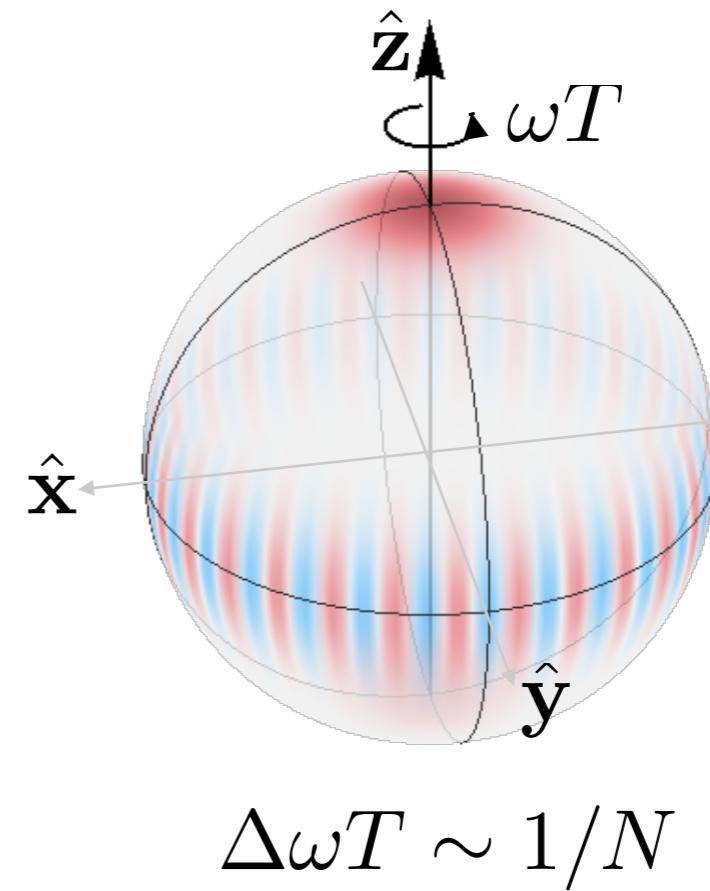
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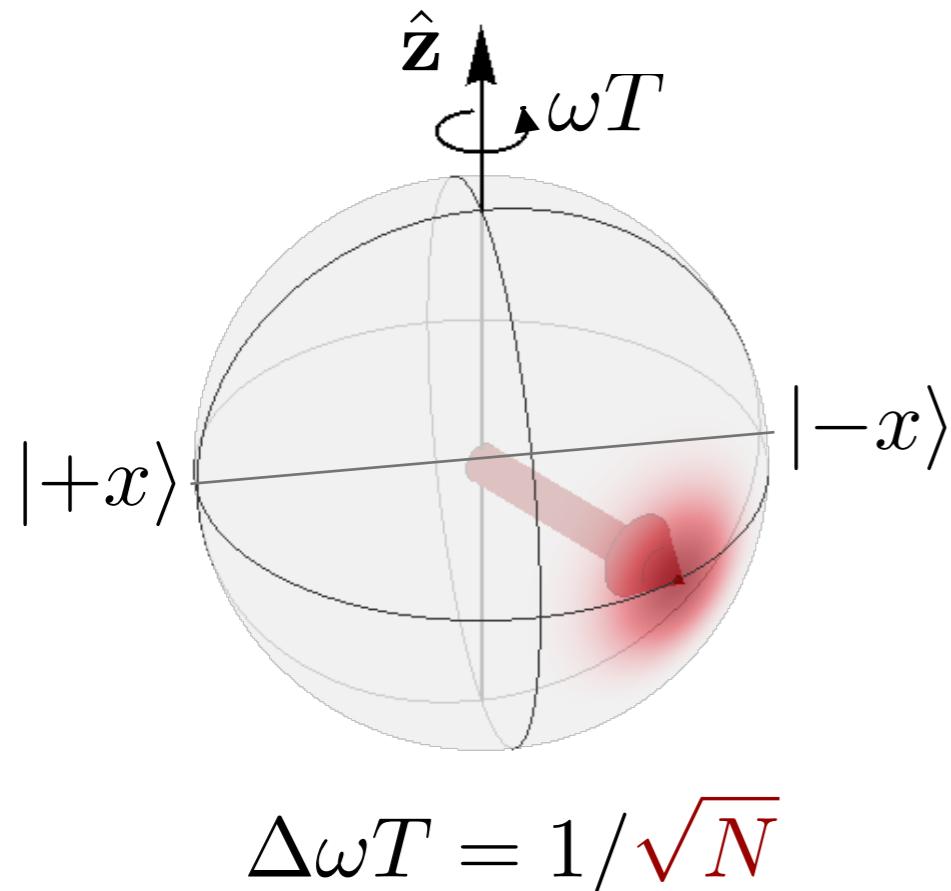


Heisenberg Limit
requires N -particle entanglement

Speed Limits in Quantum Sensing

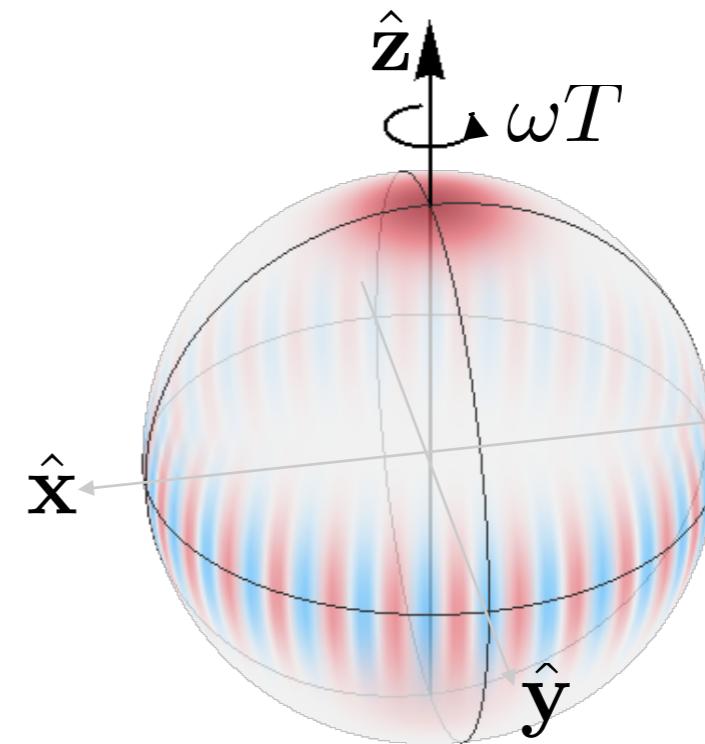
Time T for perturbation $\Delta\omega$ to appreciably change the quantum state

$$N \text{ spins: } (| \uparrow \rangle + e^{i\omega T} | \downarrow \rangle)^{\otimes N}$$



Standard Quantum Limit
for uncorrelated atoms

$$N \text{ spins: } | \uparrow \uparrow \dots \uparrow \rangle + e^{iN\omega T} | \downarrow \downarrow \dots \downarrow \rangle$$

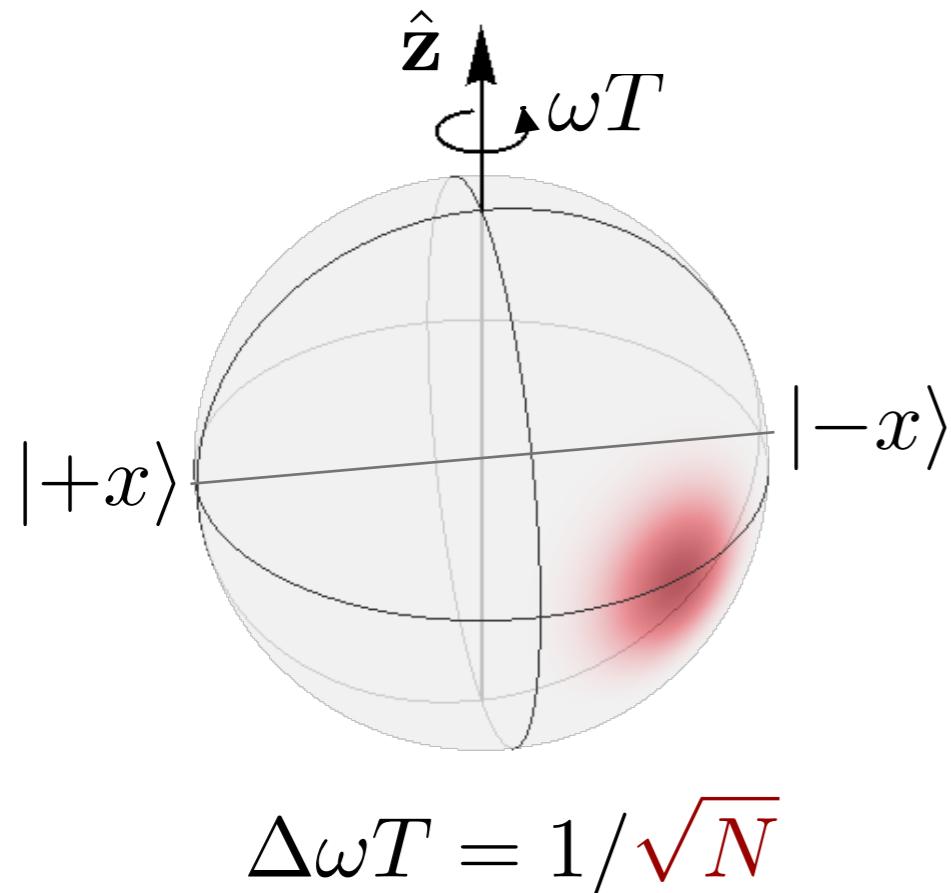


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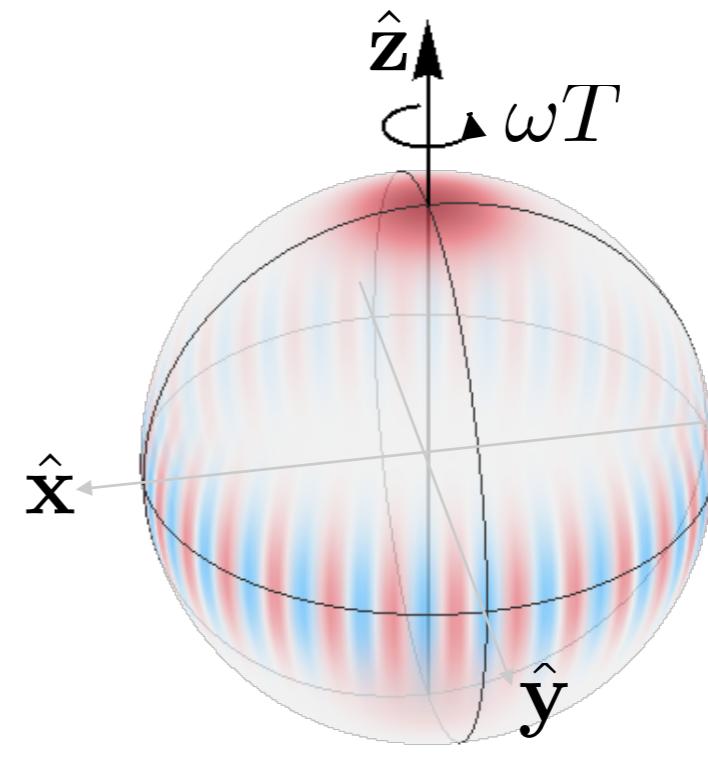
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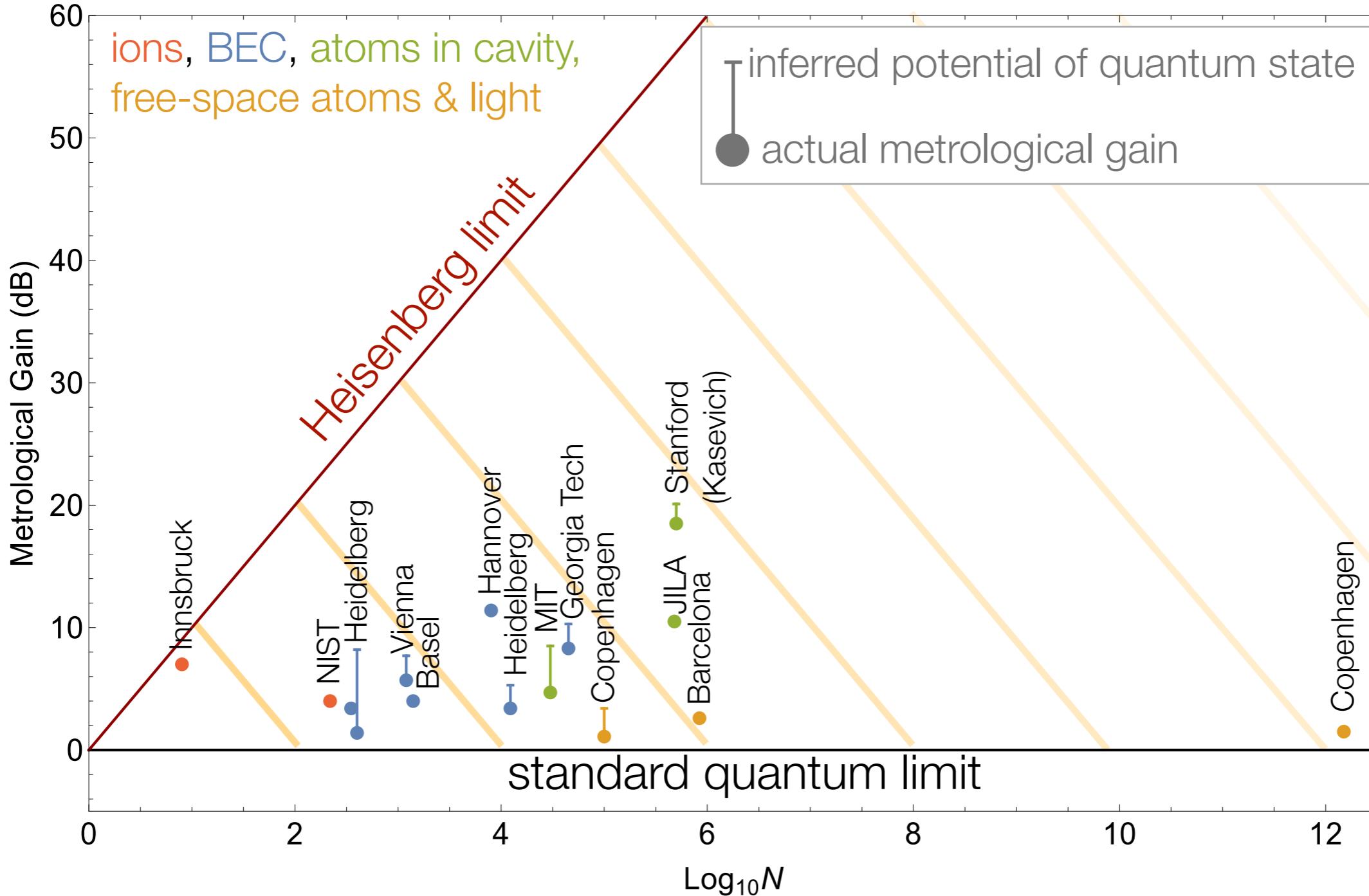
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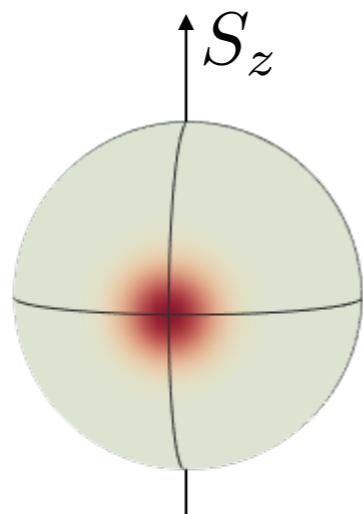
Entanglement-Enhanced Measurements



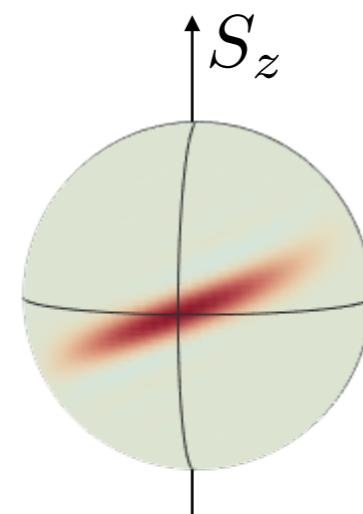
Generating Entanglement

...by spin-spin interactions

One-axis twisting [Kitagawa & Ueda, *PRA* 1993]



$$\text{Energy} \propto S_z^2$$



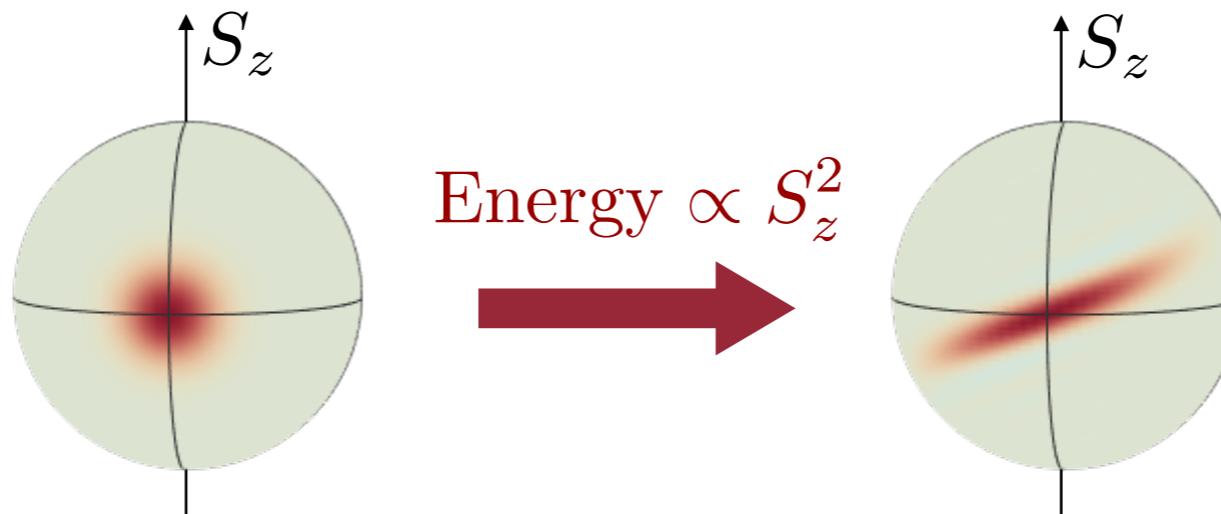
Collective spin

$$\mathbf{S} = \sum_{i=1}^N \mathbf{s}_i$$

Generating Entanglement

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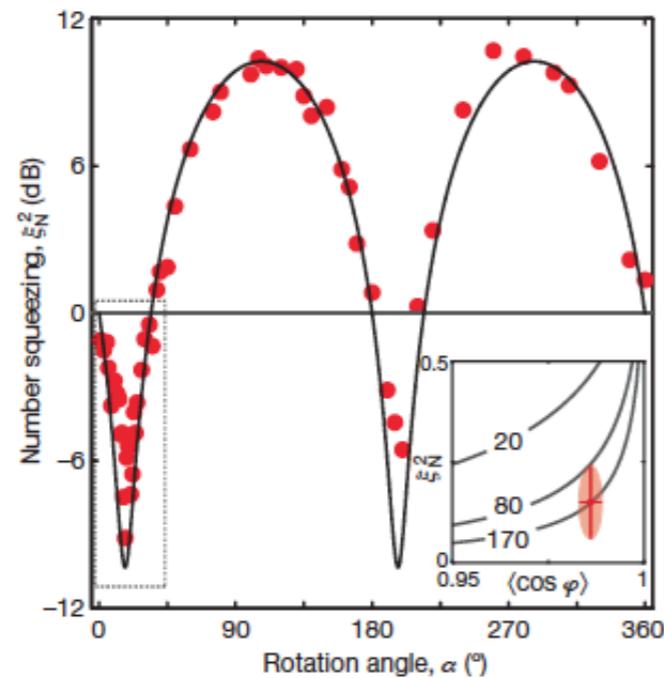
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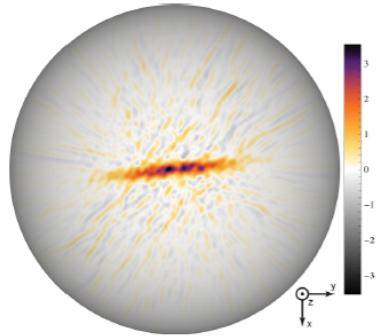
The one-axis twisting Hamiltonian corresponds to the energy proportional to the square of the population difference. The two-axis twisting Hamiltonian corresponds to the simultaneous excitation-deexcitation of two atoms. Although realistic physical schemes are yet to be found, these nonlinear Hamiltonians will provide some clues in the search for squeezed atomic states [21].

One-Axis Twisting: Implementations

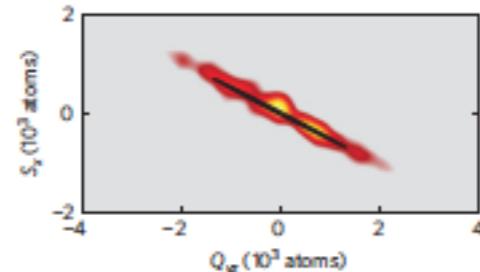
BECs



Gross, ... & Oberthaler, *Nature* (2010).

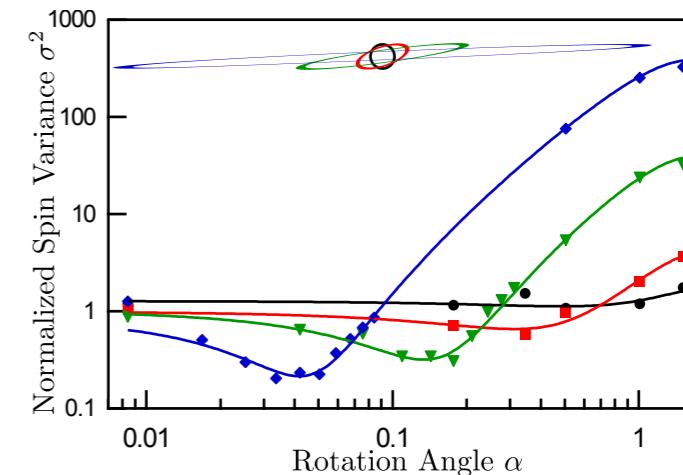


Riedl, ... & Treutlein,
Nature (2010).



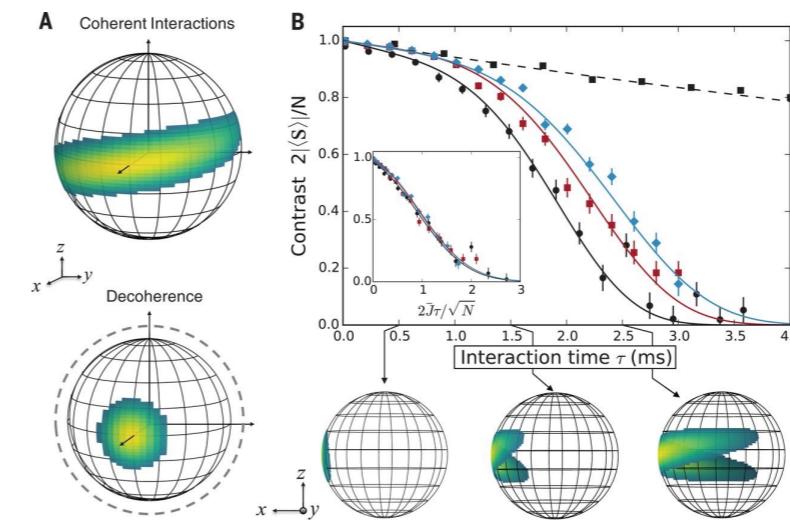
Hamley, ... & Chapman,
Nature Physics (2011).

Cavity QED



Leroux, MS-S & Vuletic, *PRL* (2010).
Hosten, ... & Kasevich, *Science* (2016).

Ion traps

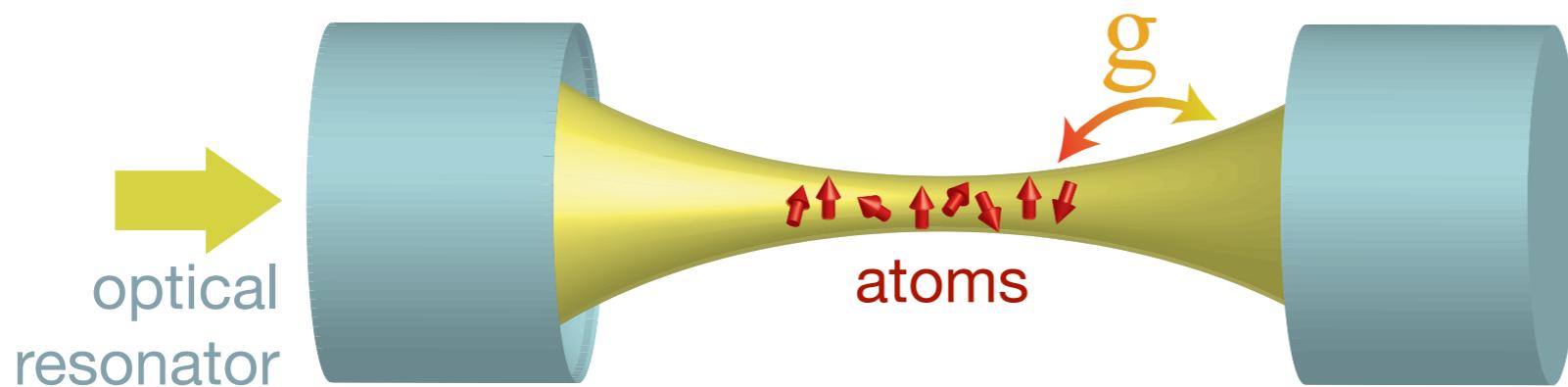


Bohnet, ... & Bollinger, *Science* (2016).

14-ion cat states: Monz, ... & Blatt *PRL* (2011).

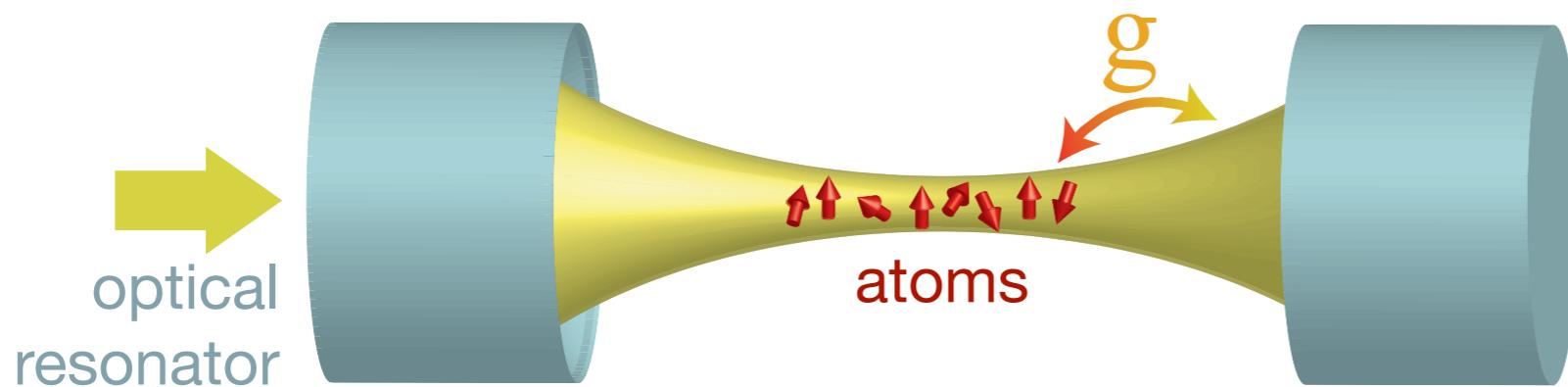
Photon-Mediated Interactions

Atoms “talk” to each other via **single mode** of light in an *optical resonator*



Photon-Mediated Interactions

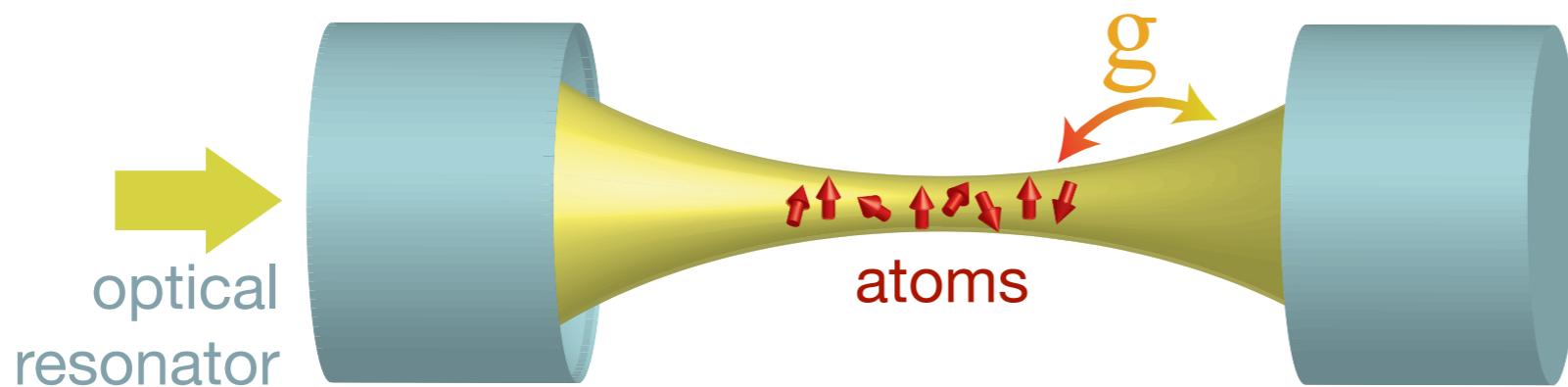
Atoms “talk” to each other via **single mode** of light in an *optical resonator*



- **Non-local** → entangling atoms even in a dilute system

Photon-Mediated Interactions

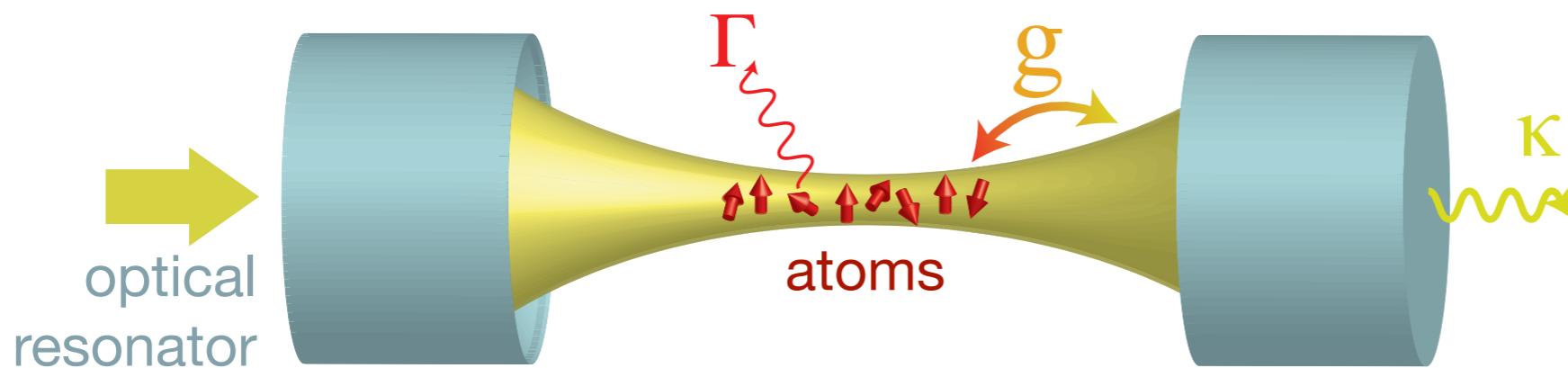
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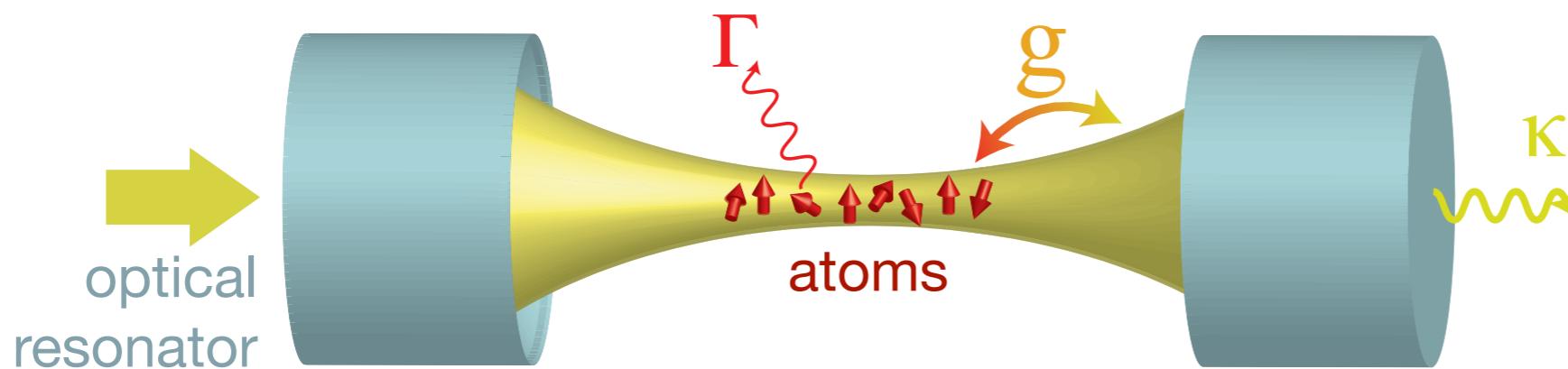
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- *Dissipation?*

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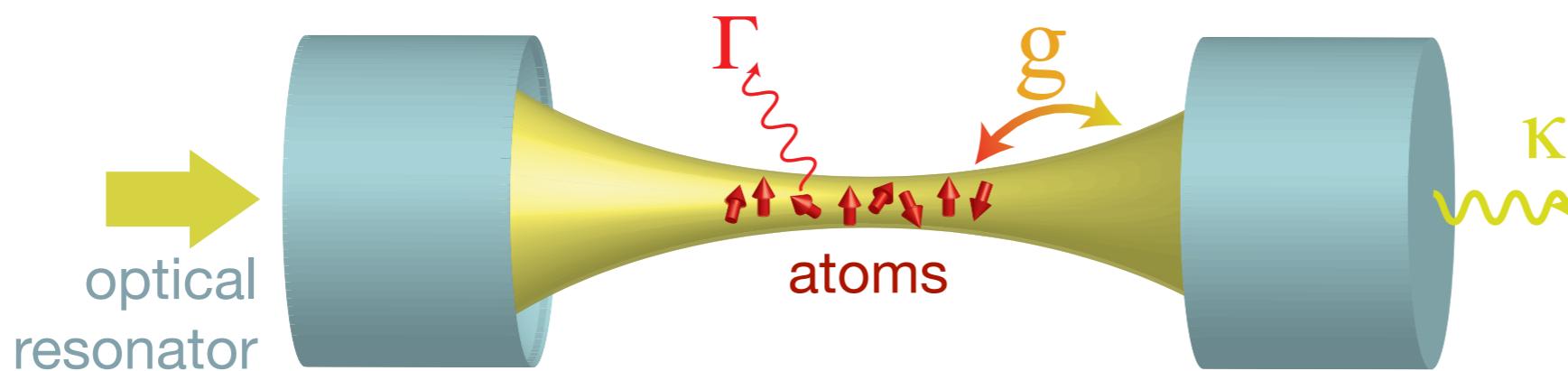
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 - Interactions can be coherent for strong coupling $\eta \equiv 4g^2/(\kappa\Gamma) \gg 1$

Photon-Mediated Interactions

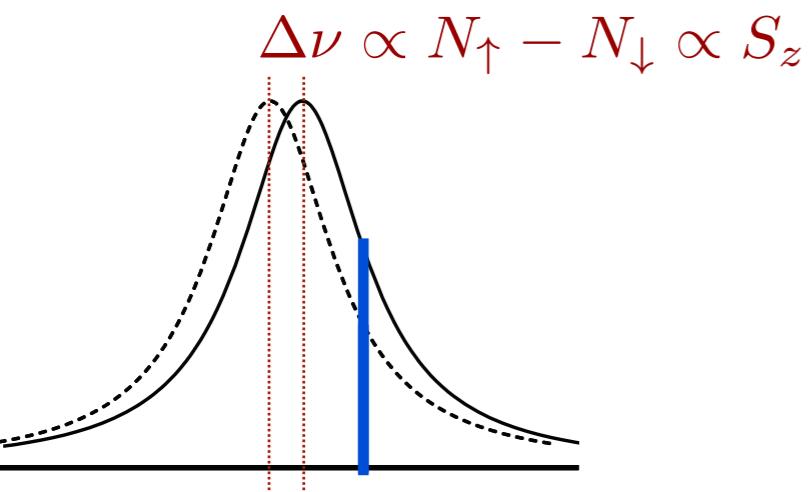
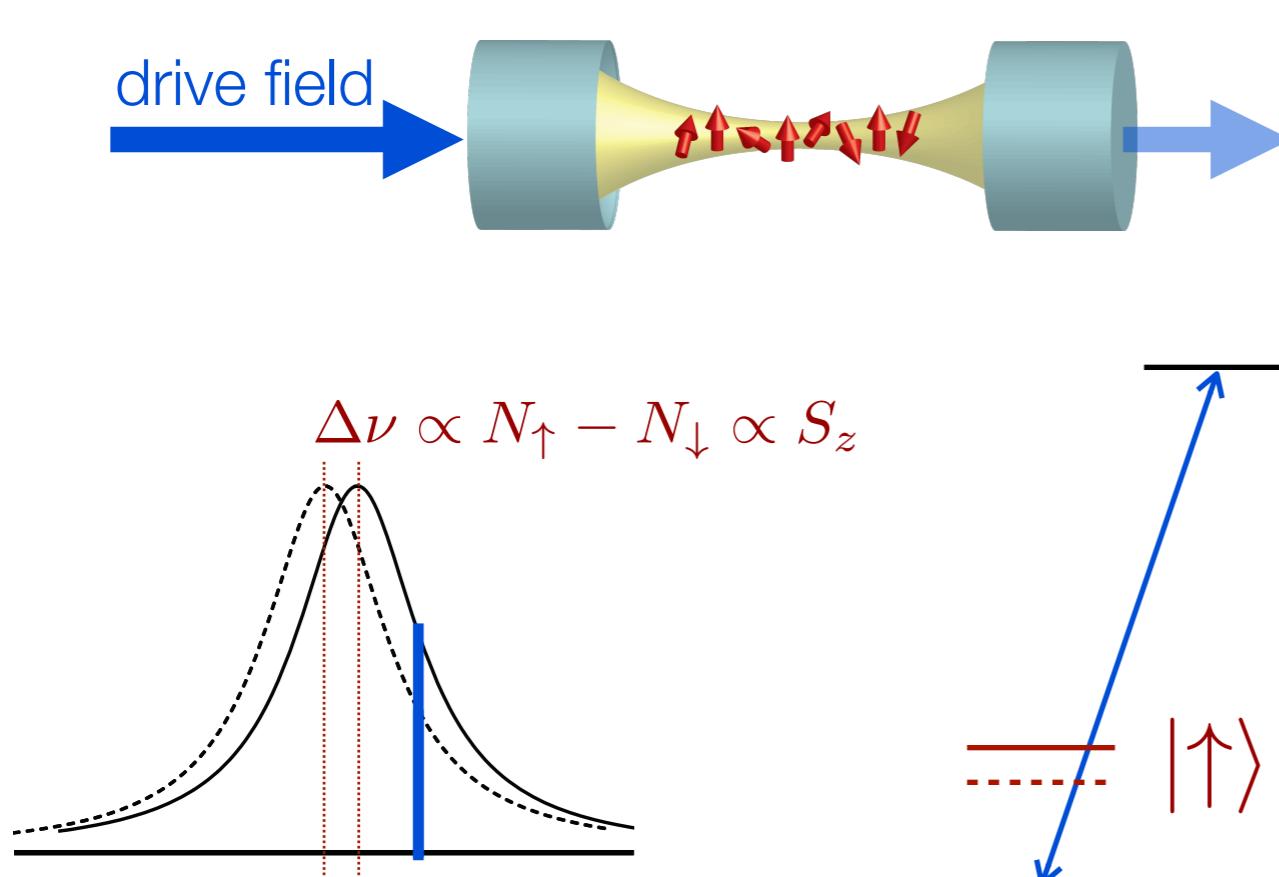
Atoms “talk” to each other via **single mode** of light in an *optical resonator*



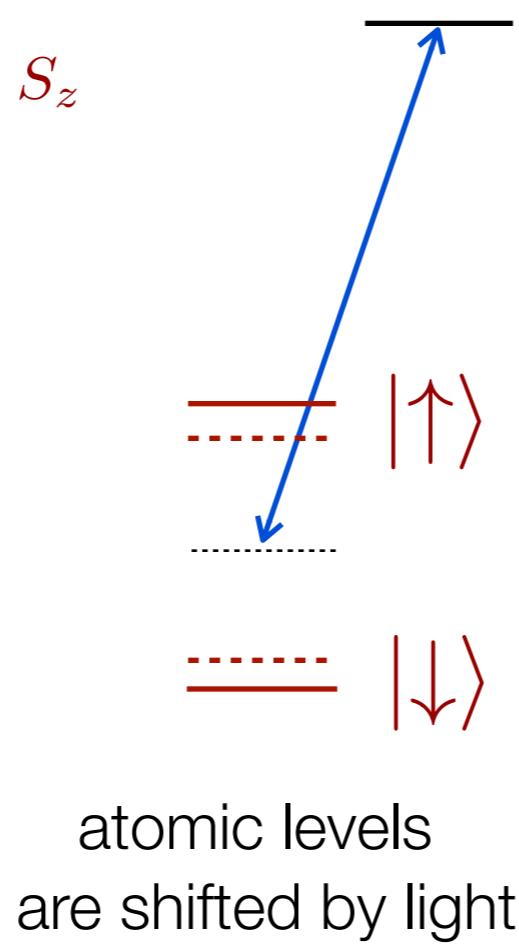
- **Non-local** → entangling atoms even in a dilute system
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 - Interactions can be coherent for strong coupling $\eta \equiv 4g^2/(\kappa\Gamma) \gg 1$
 - Or maximize info. in exiting light & entangle atoms by measurement

Photon-Mediated Ising Interactions

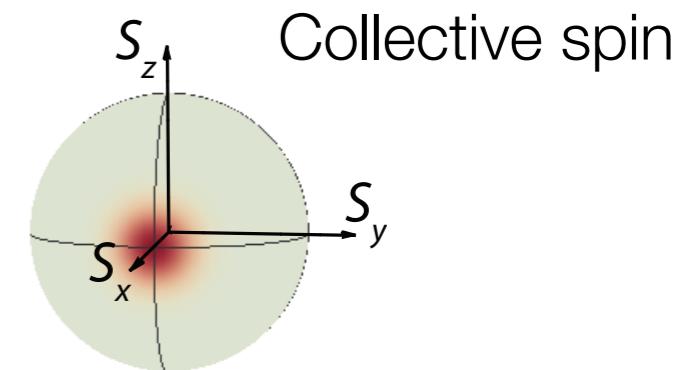
MS-S, ID Leroux & V Vuletic,
PRA **81**, 021804(R) (2010).



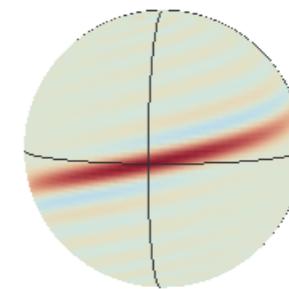
cavity resonance
is shifted by atoms



atomic levels
are shifted by light



Collective spin
 $H = \chi S_z^2$



effective interaction
mediated by light

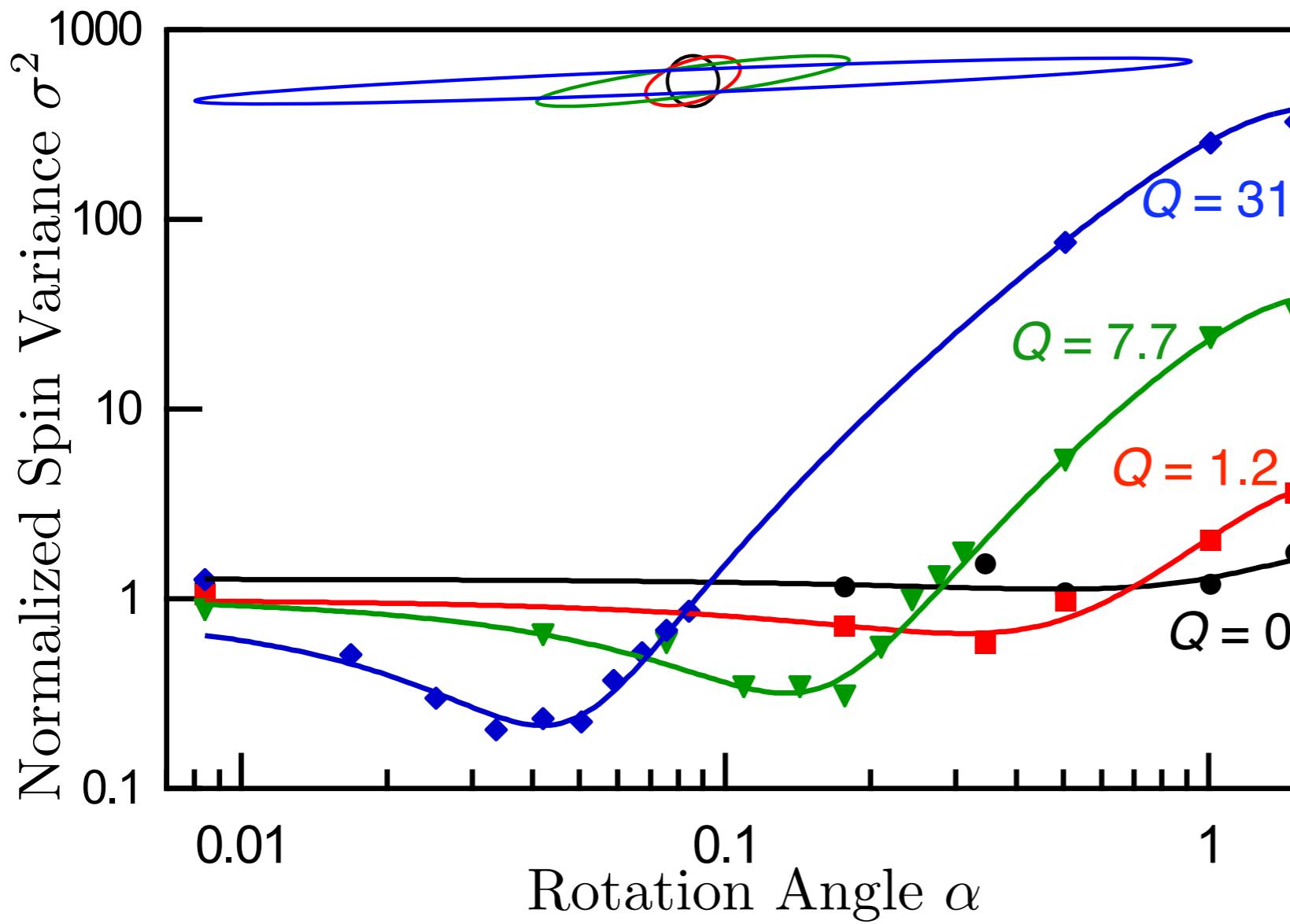
“one-axis twisting”
[Kitagawa & Ueda, PRA, 1993.]

Spin Squeezing

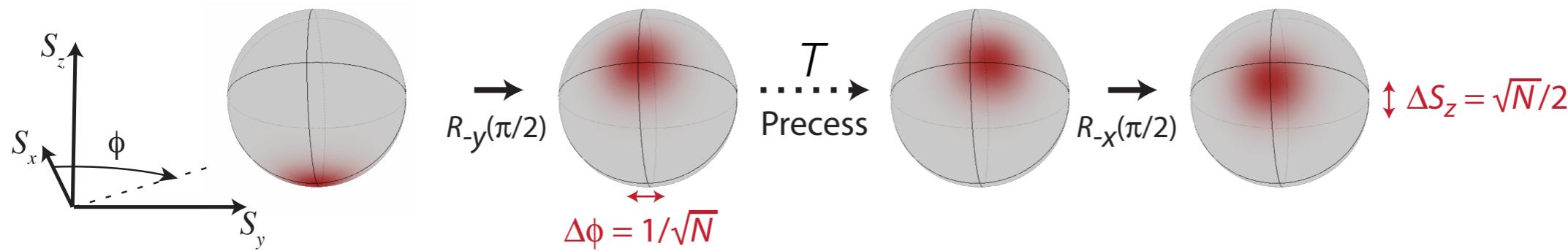
ID Leroux, MS-S & V Vuletic,
PRL **104**, 073602 (2010).

Twisting strength $Q = N\chi t = \left(\frac{\text{# of photons scattered}}{\text{into cavity per atom}} \right)$

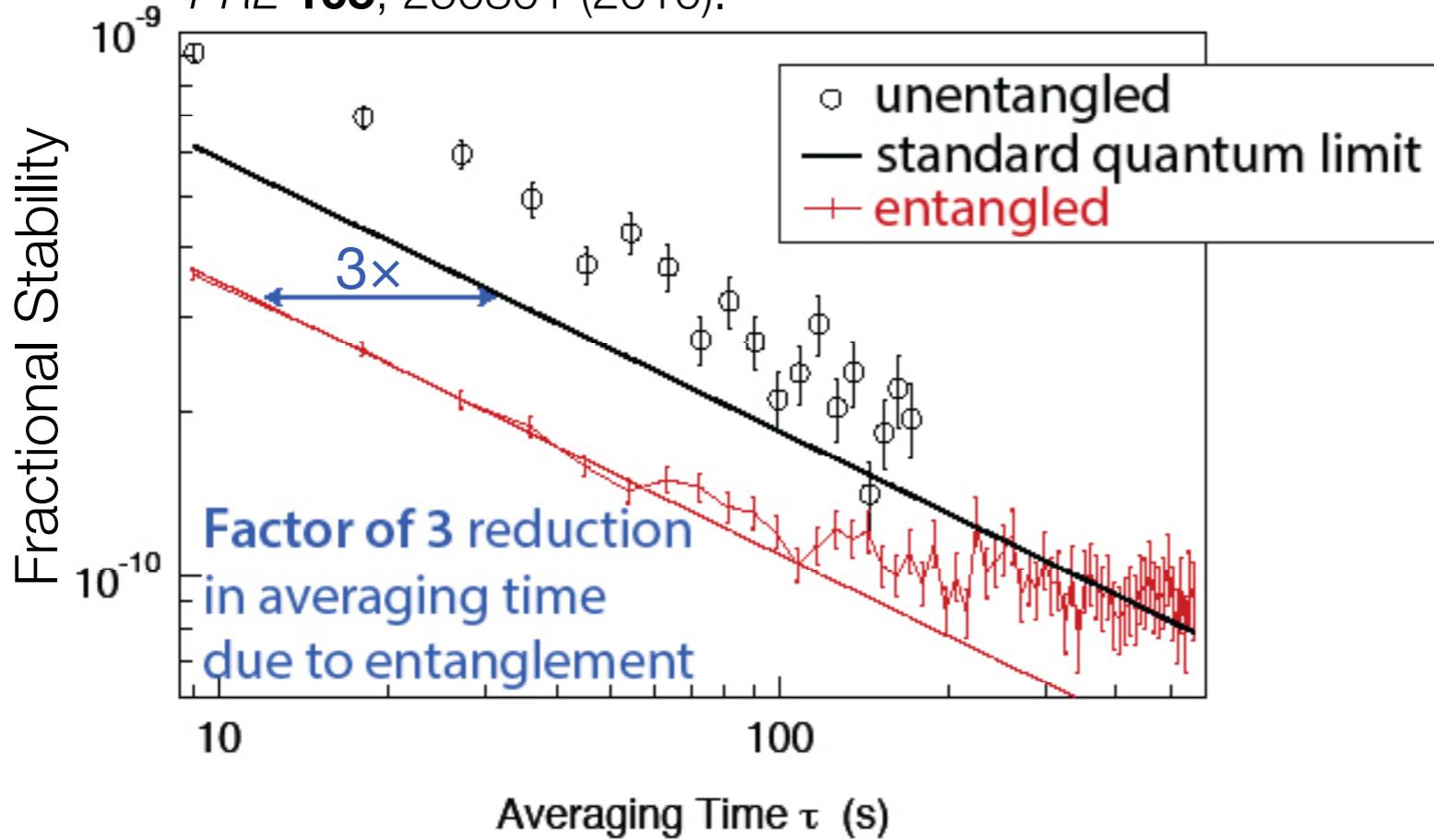
$N = 4 \times 10^4$ atoms
 $\eta = 0.1$, $\delta = \kappa/2$
 $\Rightarrow N\eta \gg 1$



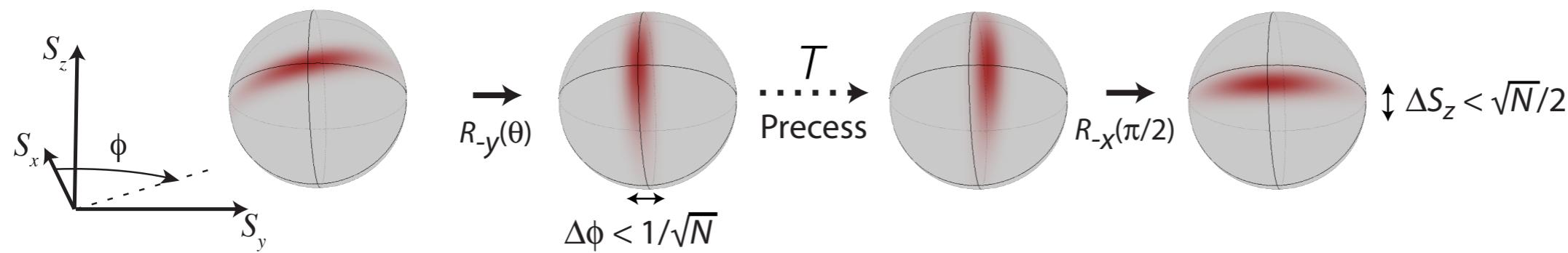
Enhanced Atomic Clocks



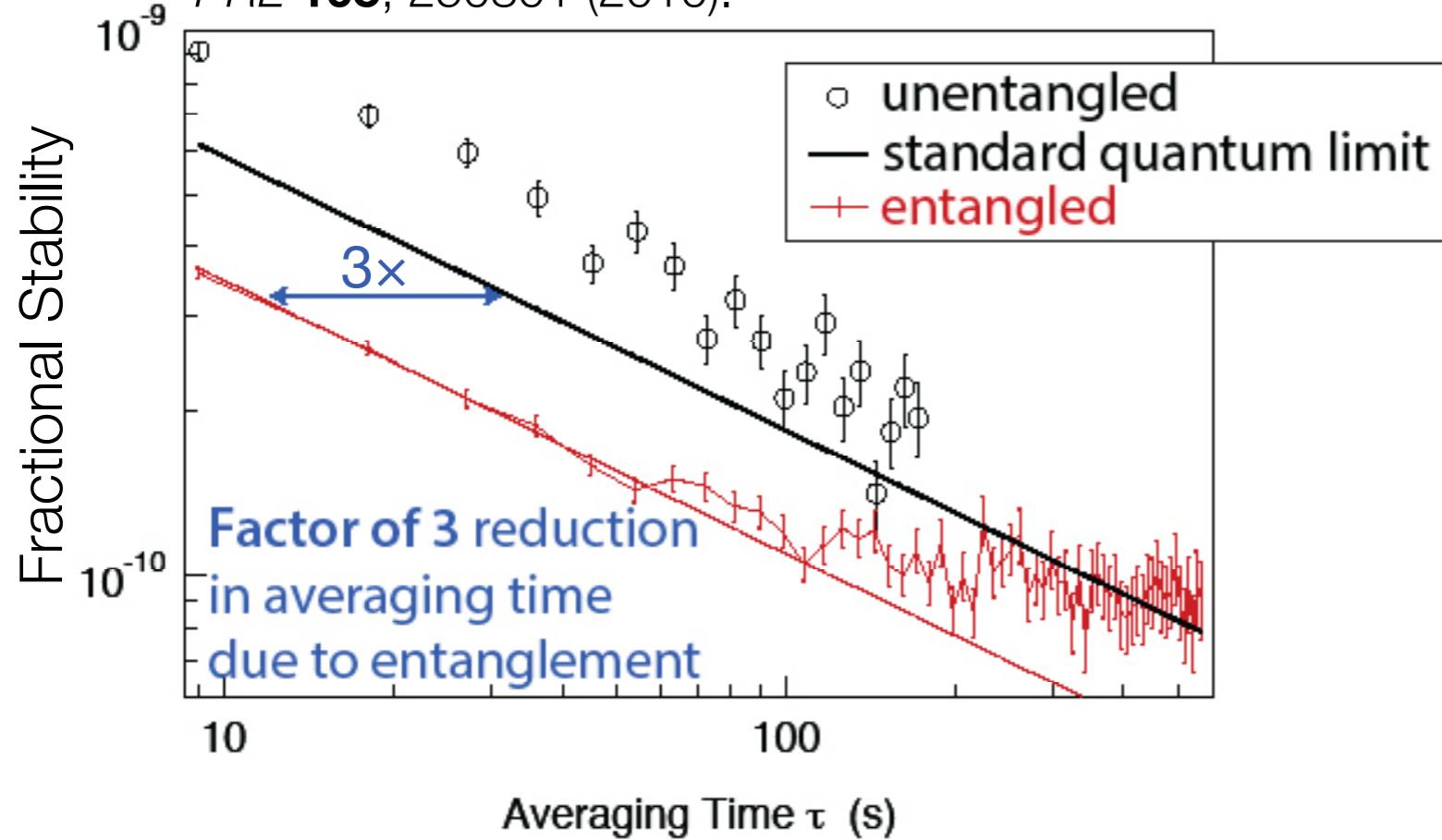
ID Leroux, MS-S & V Vuletic,
PRL **105**, 250801 (2010).



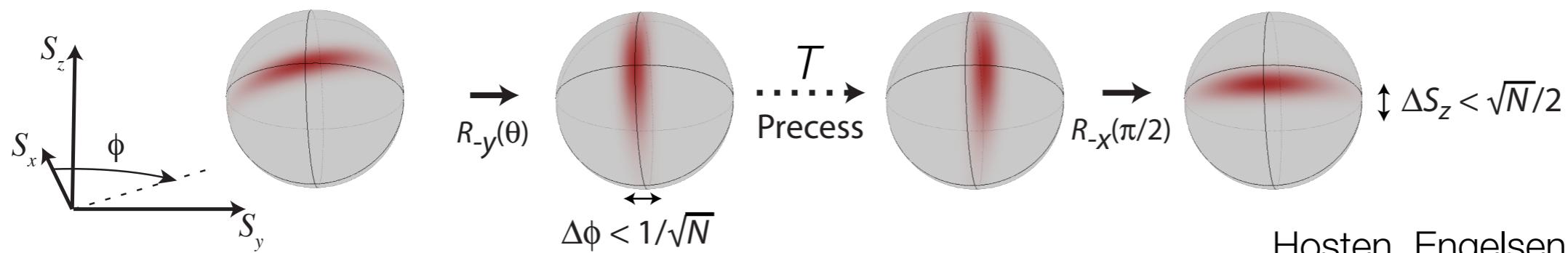
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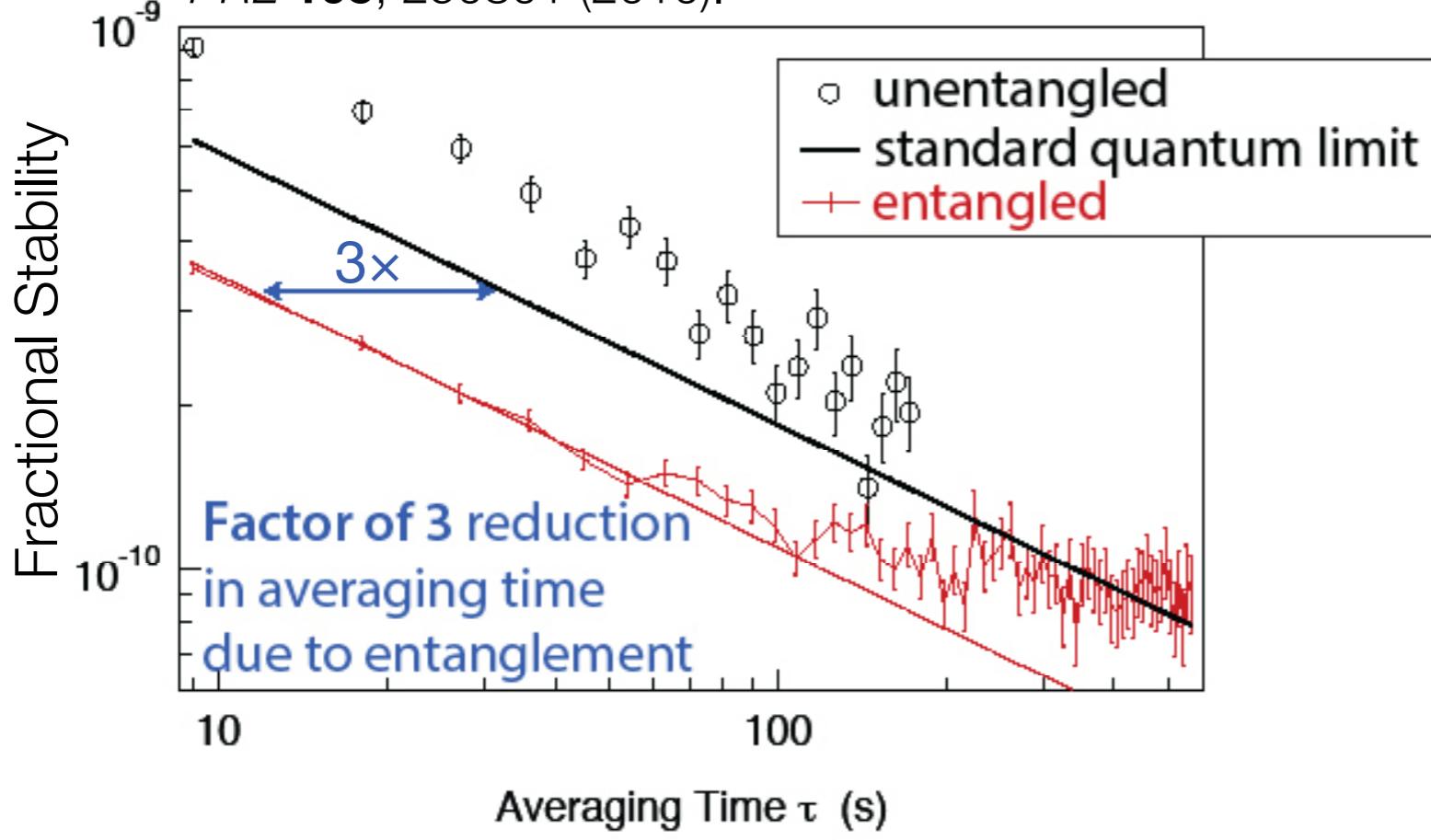
ID Leroux, MS-S & V Vuletic,
PRL **105**, 250801 (2010).



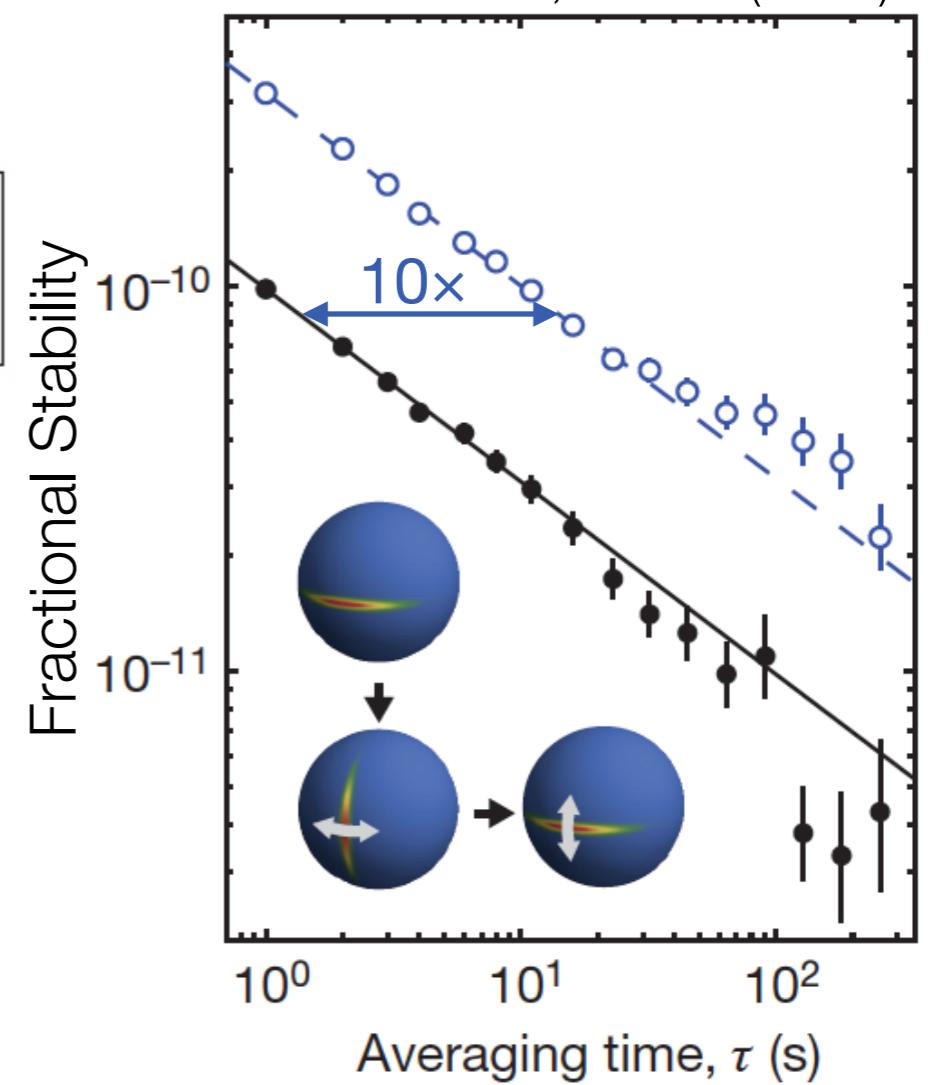
Enhanced Atomic Clocks



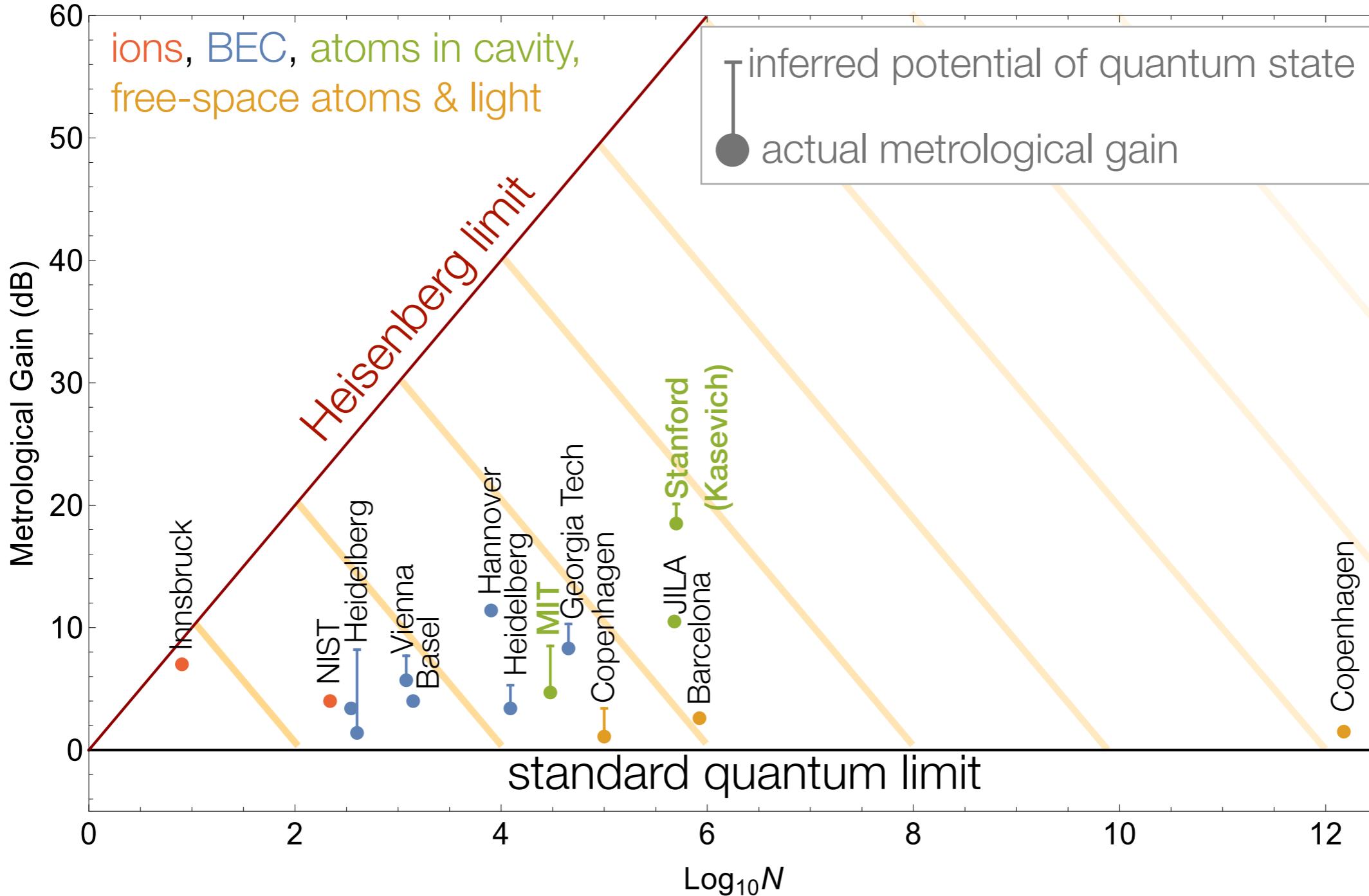
ID Leroux, MS-S & V Vuletic,
PRL **105**, 250801 (2010).



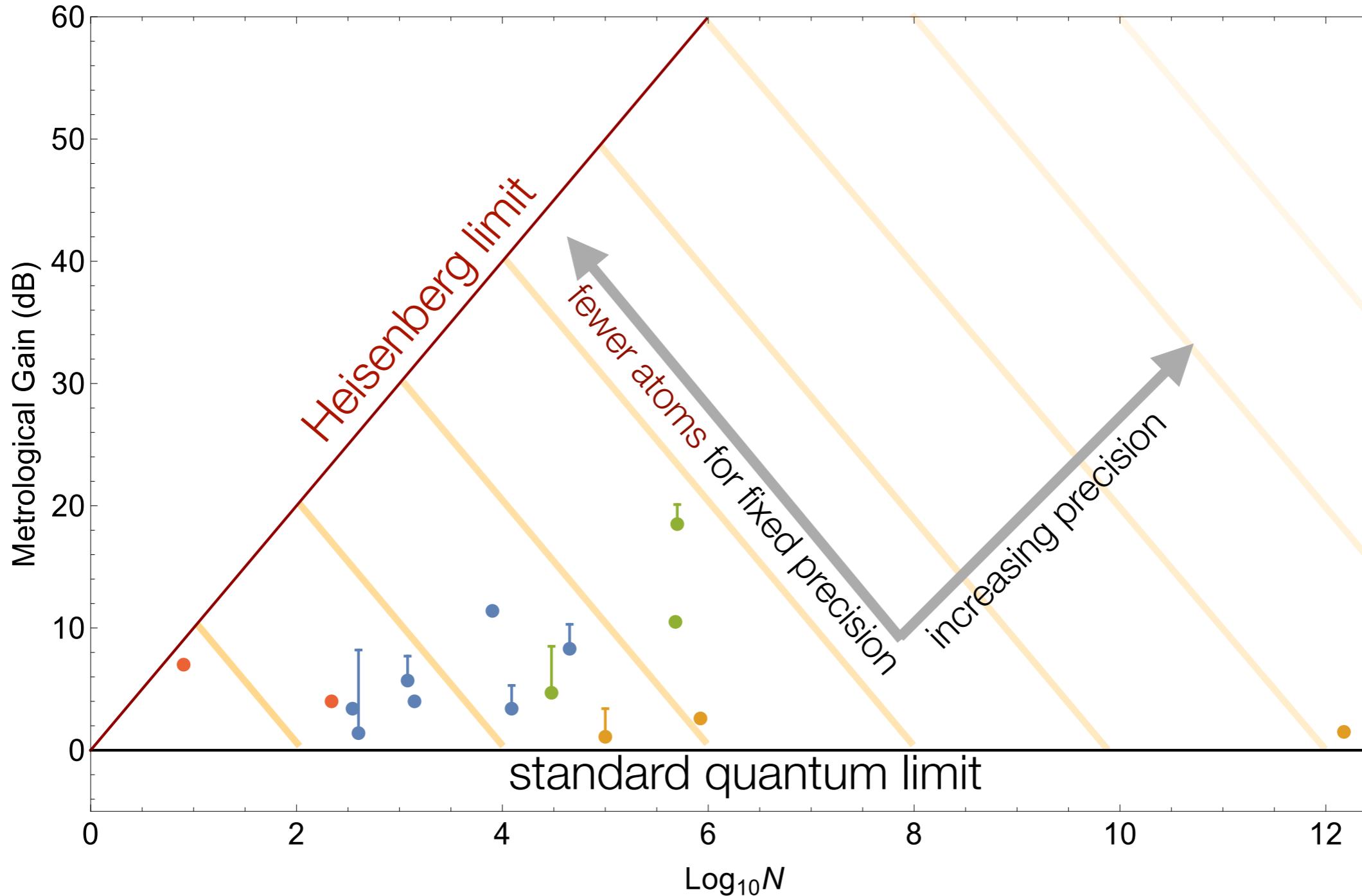
Hosten, Engelsen, Krishnakumar
& Kasevich, *Nature* (2016).



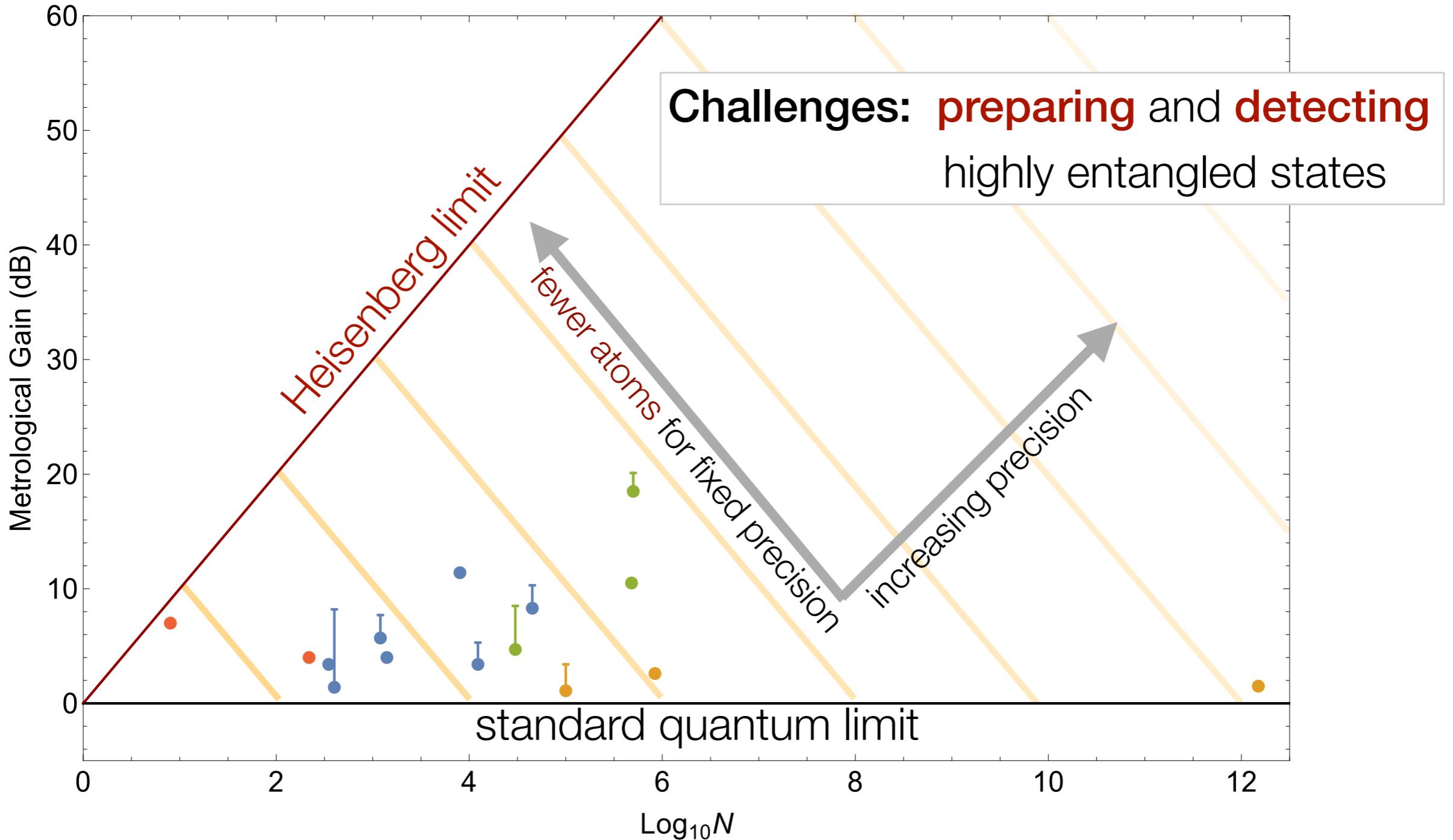
Entanglement-Enhanced Measurements



Approaching the Heisenberg Limit?

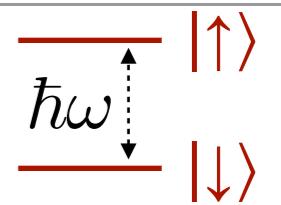


Approaching the Heisenberg Limit?



Towards the Heisenberg Limit?

Fundamental limit set by Heisenberg Uncertainty Principle $\Delta E \Delta T \geq \hbar/2$



$$\Delta E \leq \frac{N}{2} \hbar\omega \Rightarrow \Delta(\omega T) \geq \frac{1}{N} \quad \text{Heisenberg Limit}$$

Reaching the Heisenberg Limit requires a state with *maximum uncertainty* in energy

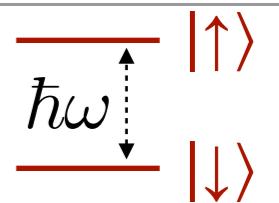
$$|\psi\rangle_{\text{cat}} = \frac{|\text{Alive}\rangle + |\text{Dead}\rangle}{\sqrt{2}}$$

GHZ (“cat”) state



Towards the Heisenberg Limit?

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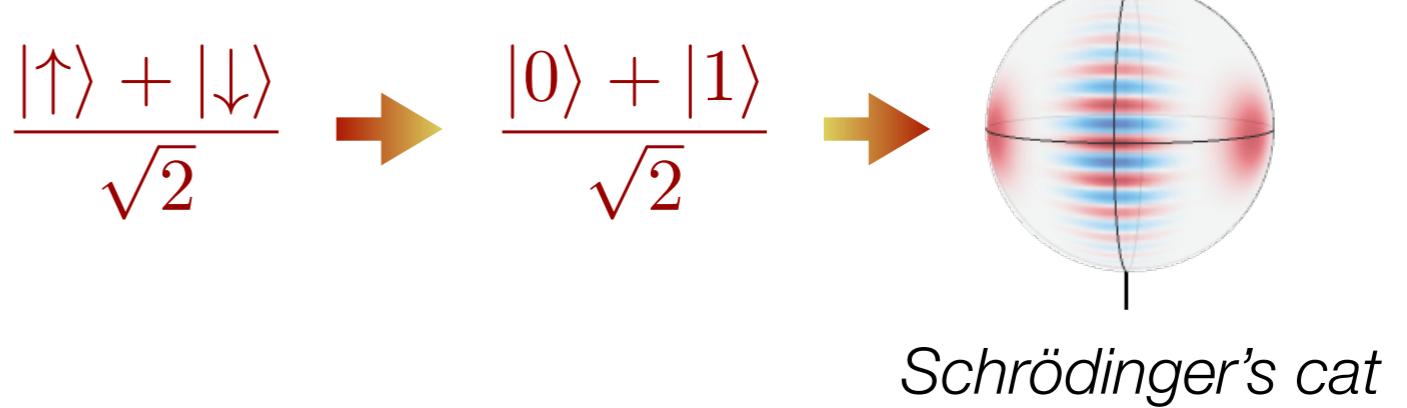
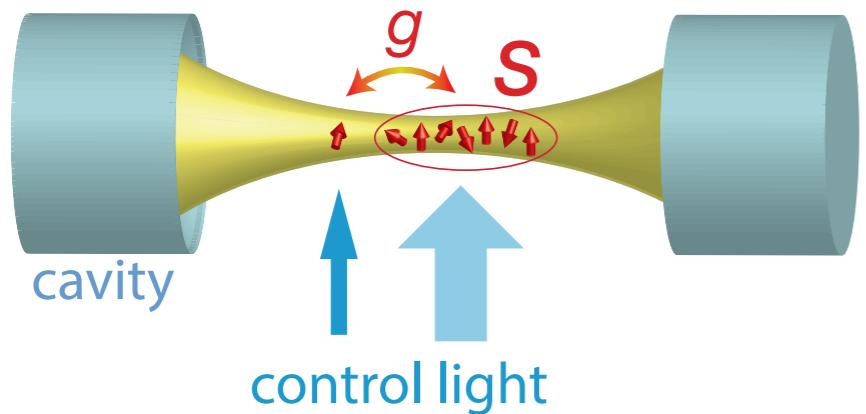
GHZ (“cat”) state

- *Making and detecting these states at large N?*
- *Easier alternatives?*



Routes to Cat States?

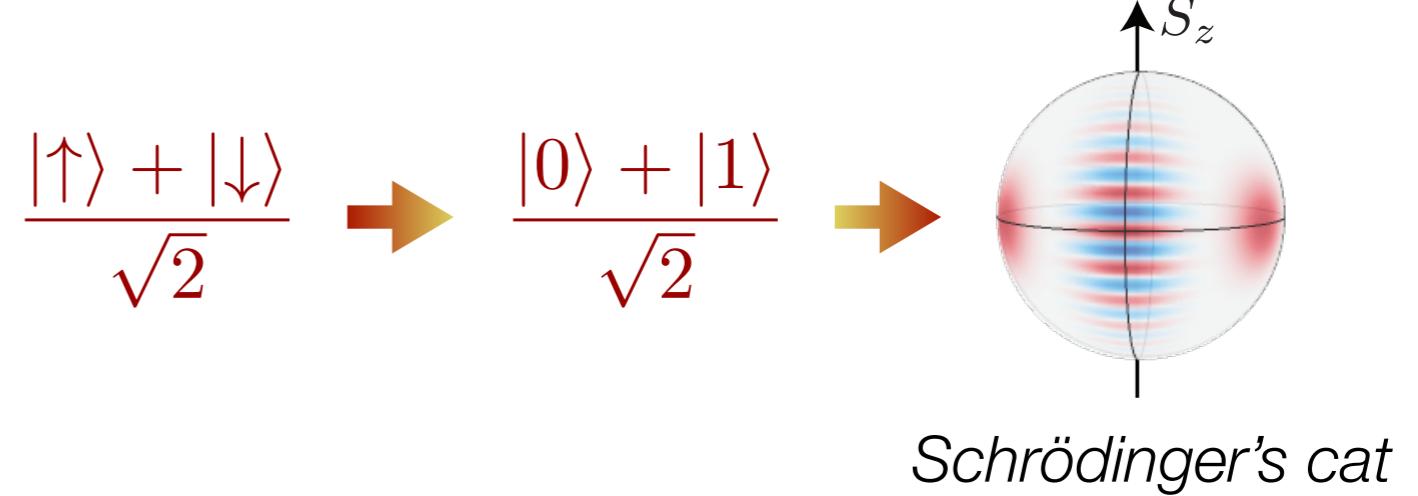
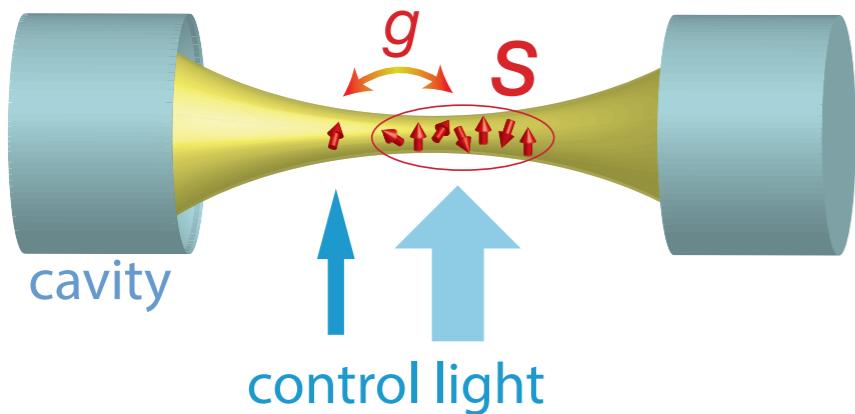
Qubit-Ensemble Interface



Schrödinger's cat

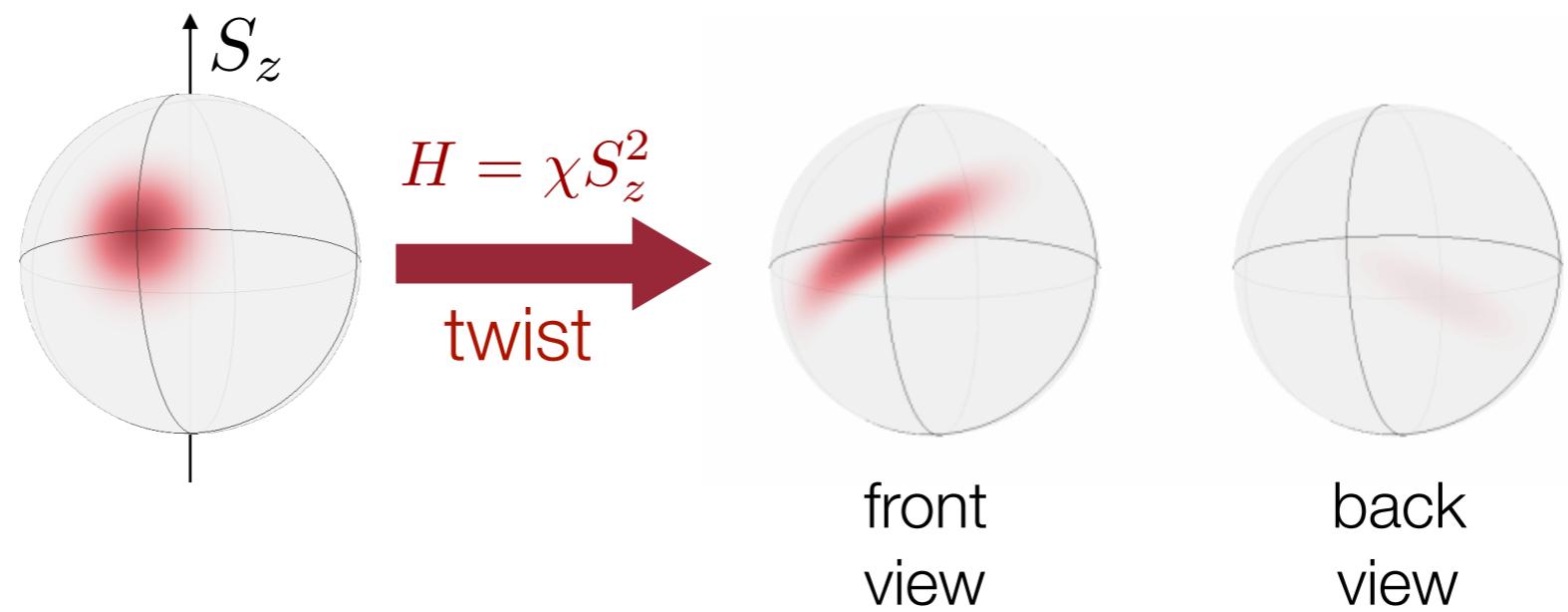
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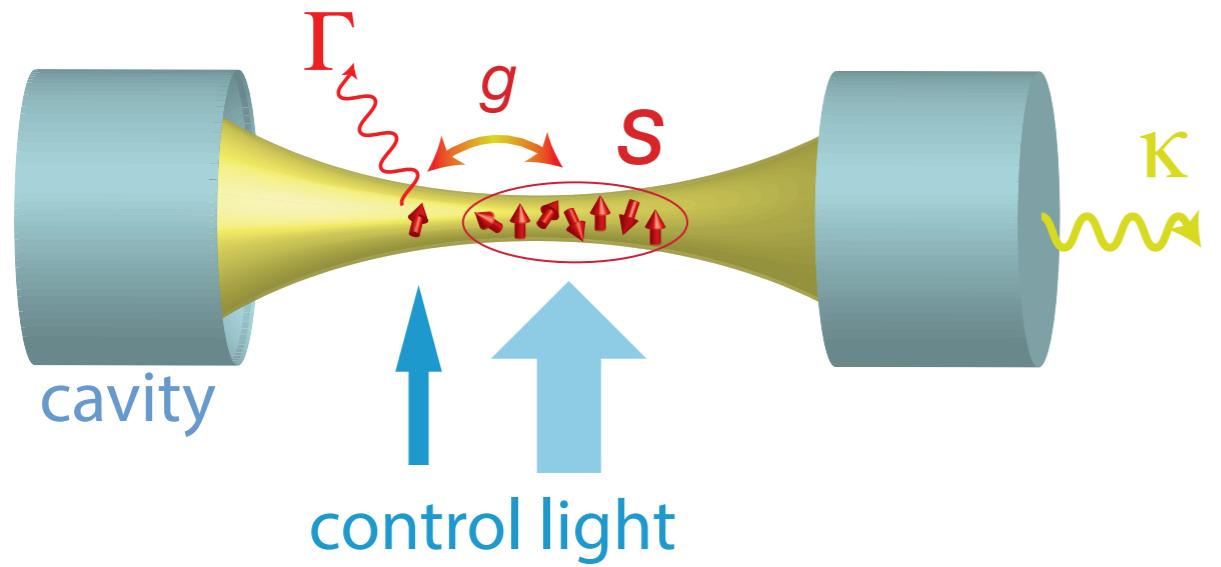


Collective Interactions

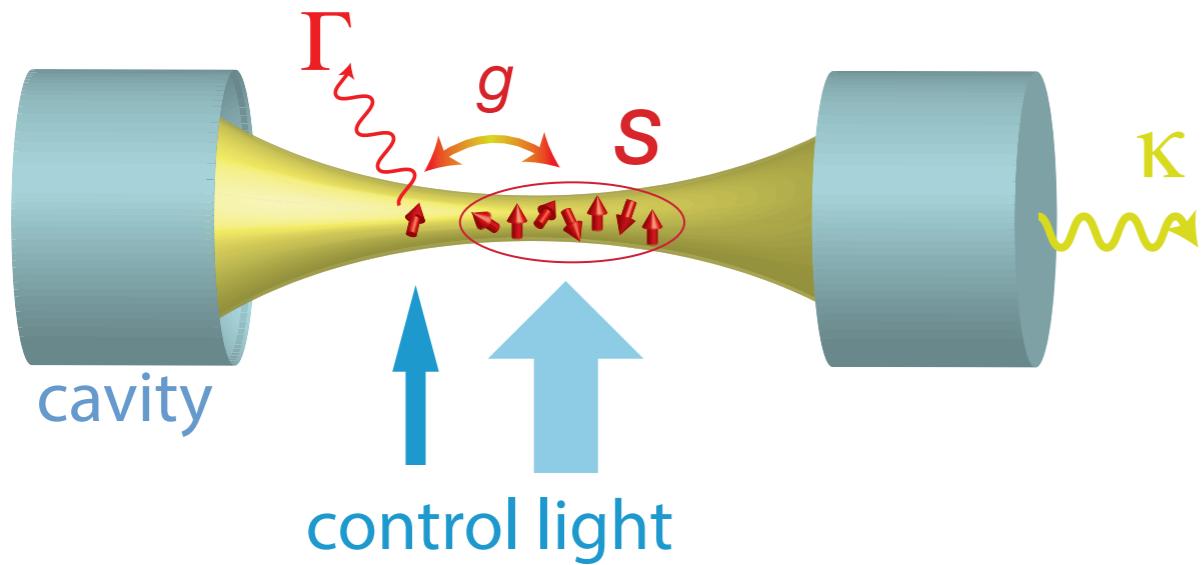
$$\text{collective spin } \mathbf{S} = \sum_{i=1}^N \mathbf{s}_i$$



Challenge: Dissipation



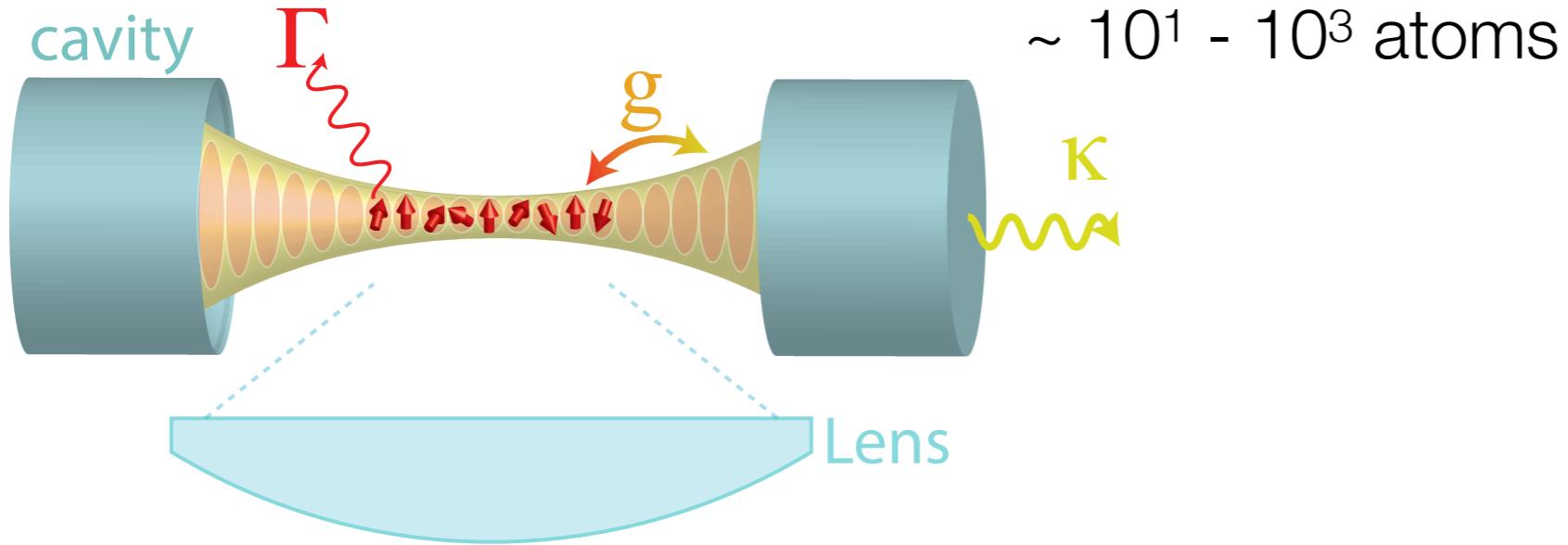
Challenge: Dissipation



Two-fold approach

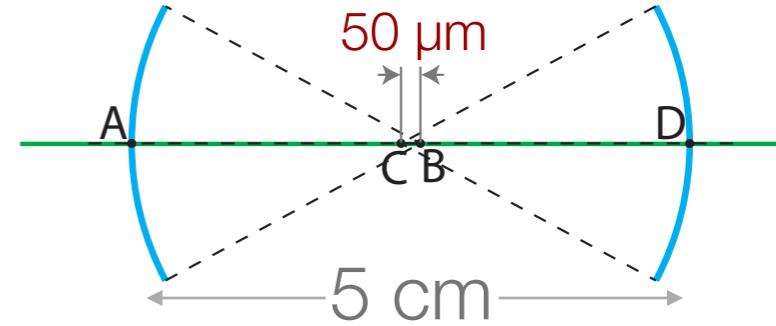
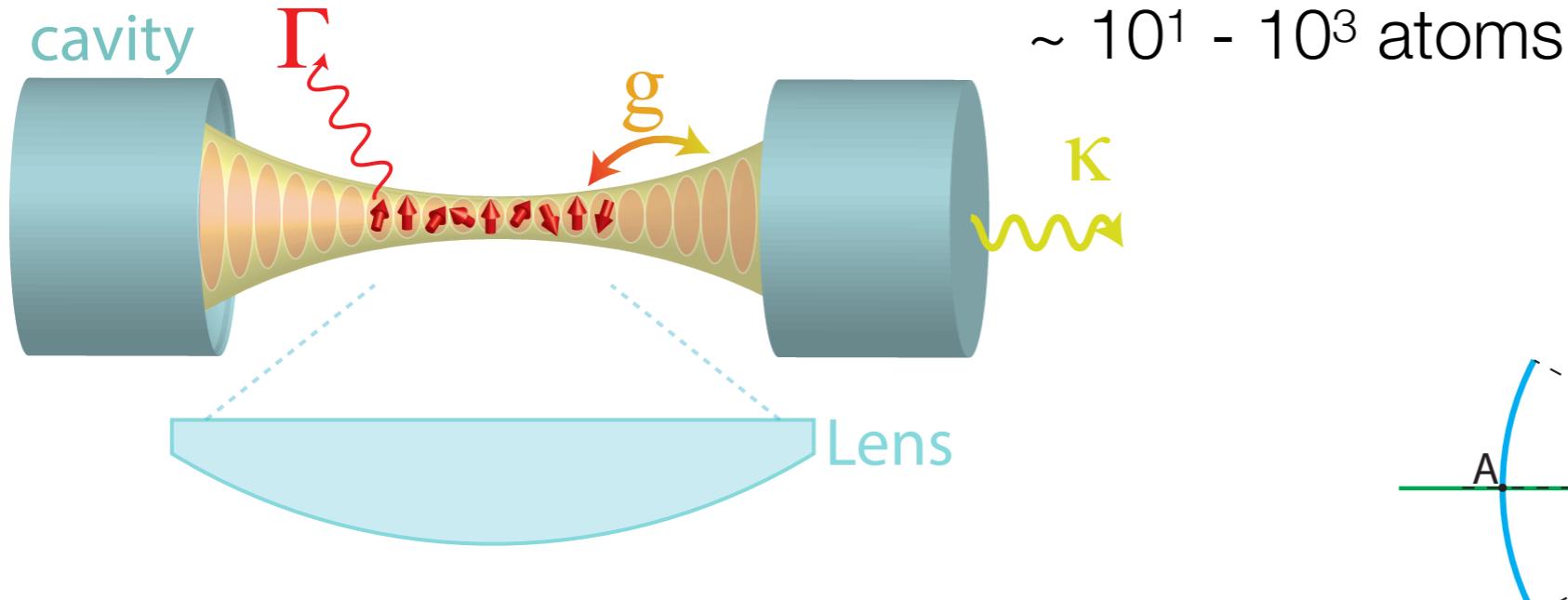
- Maximize interaction-to-decay ratio
- Devise entanglement schemes that are robust to photon loss

Experiment Design



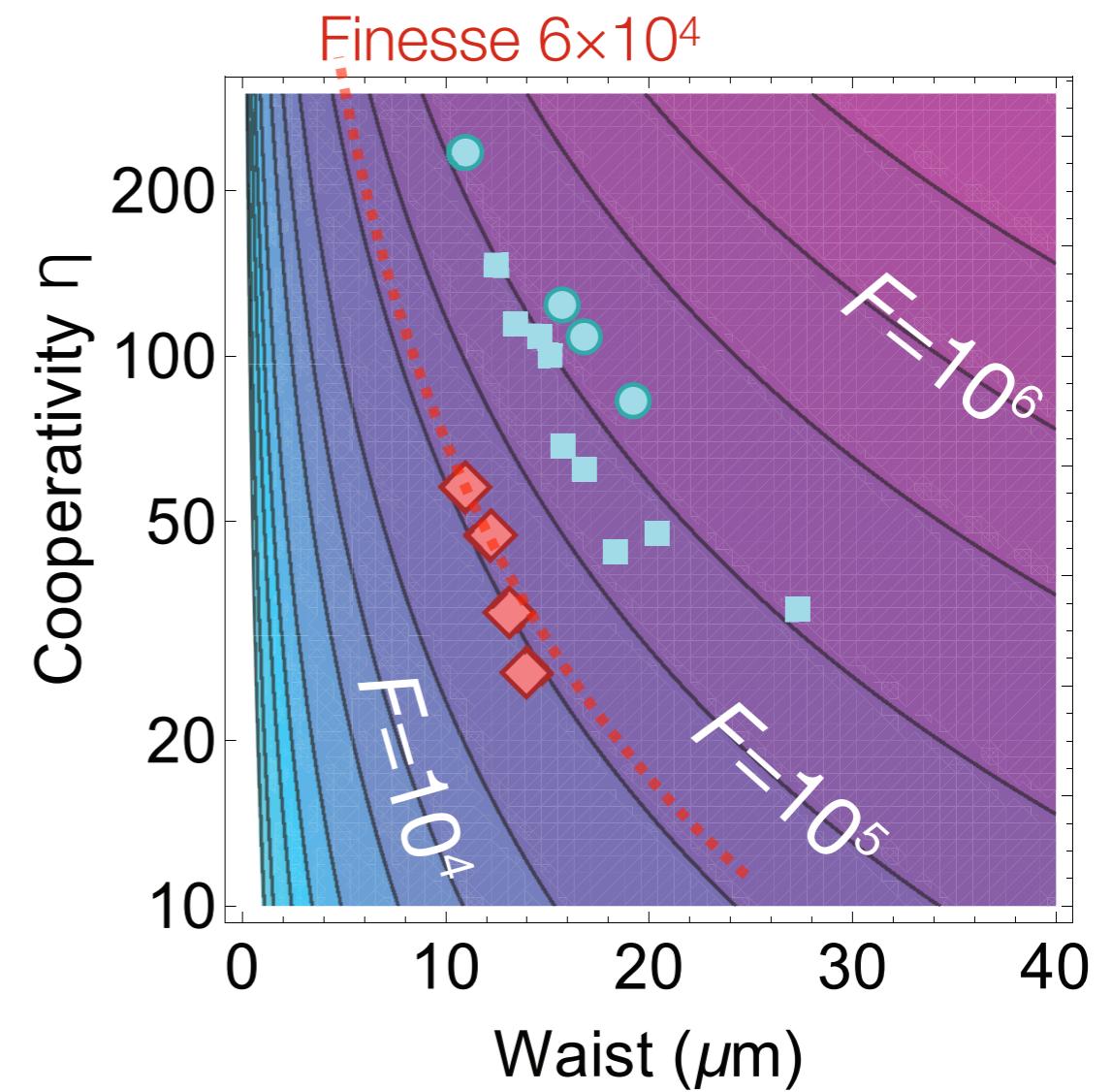
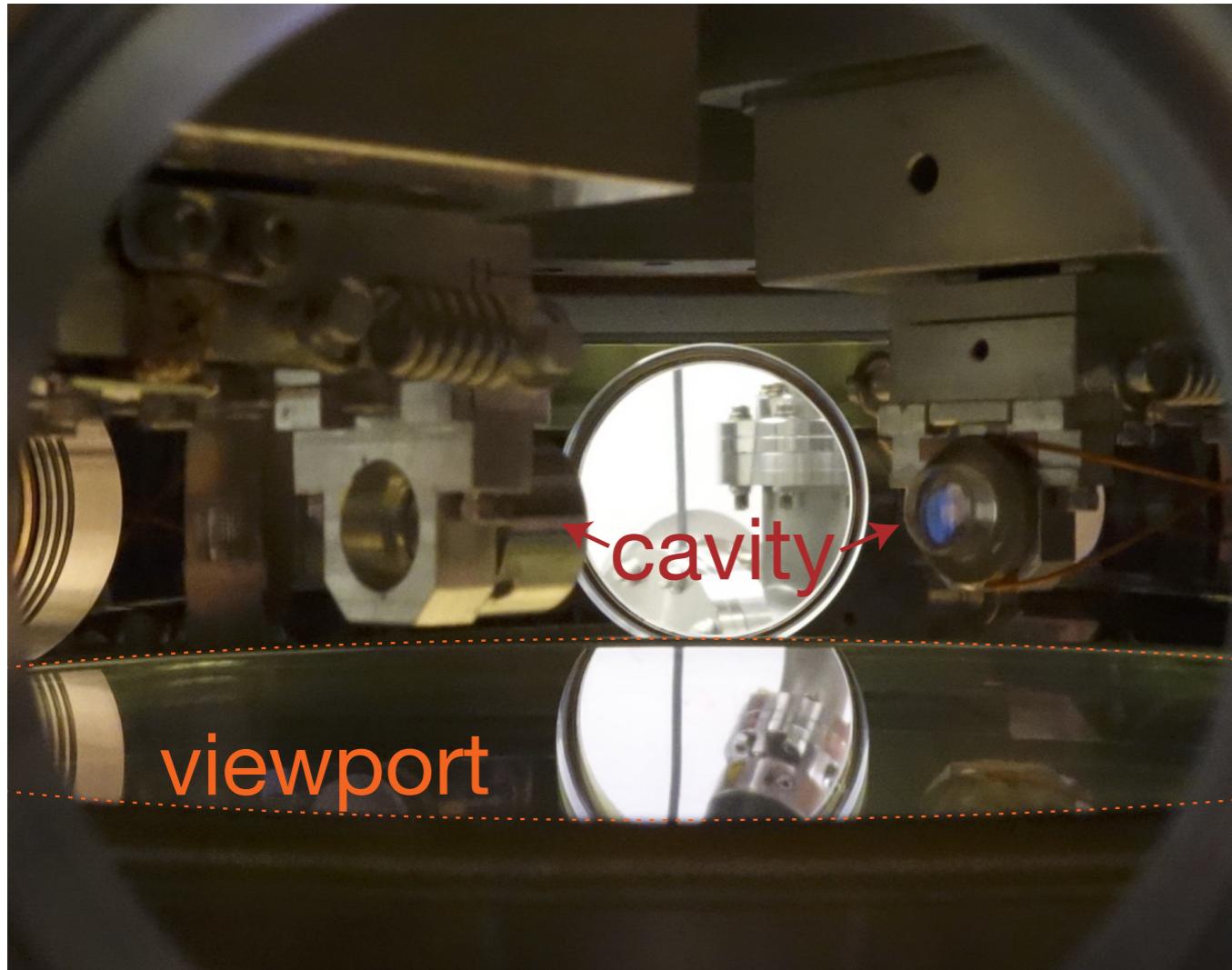
- Strong coupling: $\eta \equiv \frac{4g^2}{\kappa\Gamma} \sim \frac{F\lambda^2}{w^2} \gg 1$
- Optical access for imaging & addressing

Experiment Design



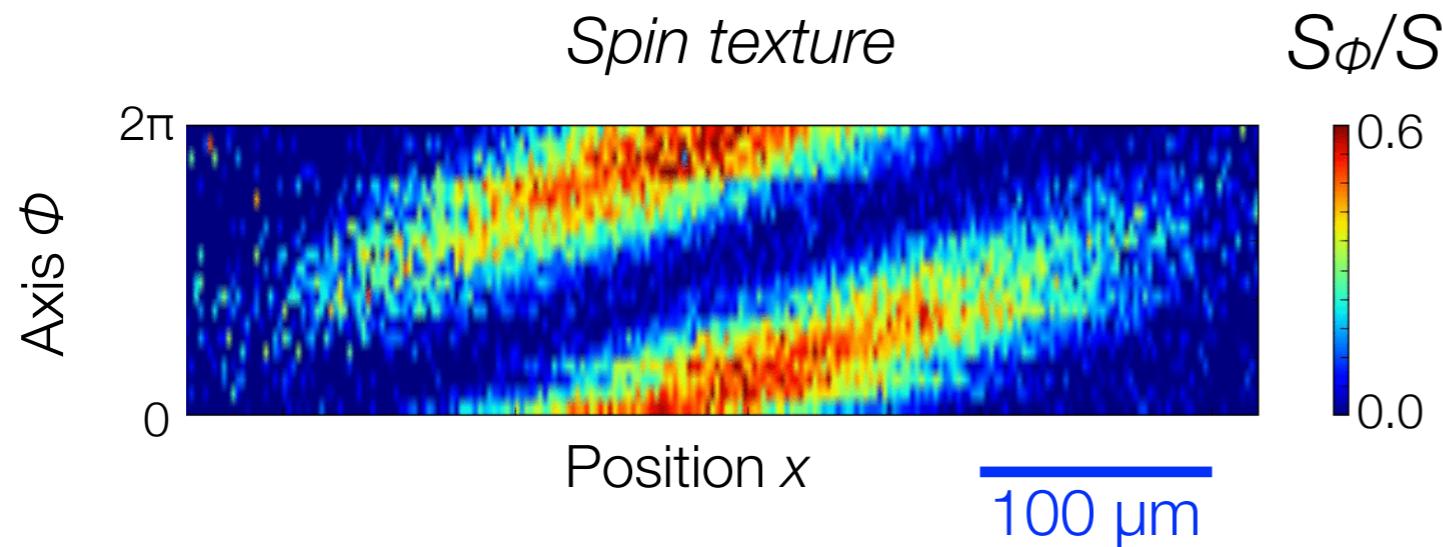
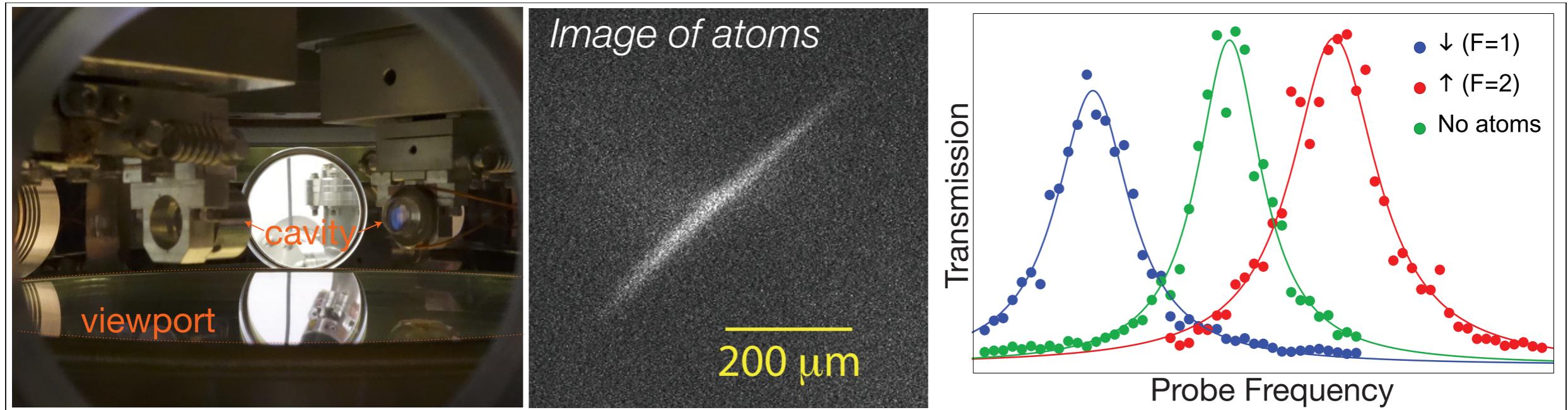
- Strong coupling: $\eta \equiv \frac{4g^2}{\kappa\Gamma} \sim \frac{F\lambda^2}{w^2} \gg 1$
 - Optical access for imaging & addressing
- } \Rightarrow Near-concentric resonator
Waist $w \sim 12 \mu\text{m}$
Finesse $F \sim 10^5$
Non-degenerate modes

Strong Coupling with Optical Access



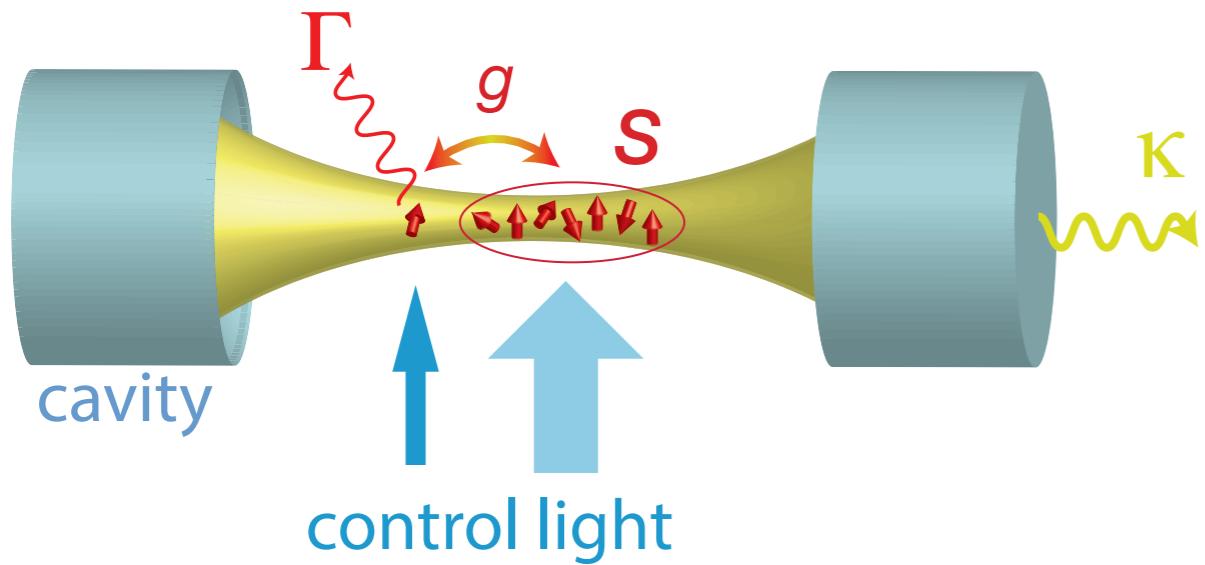
Single-atom cooperativity $\eta \sim 50$

Experimental Toolbox



State-sensitive imaging

Photon-Mediated Entanglement



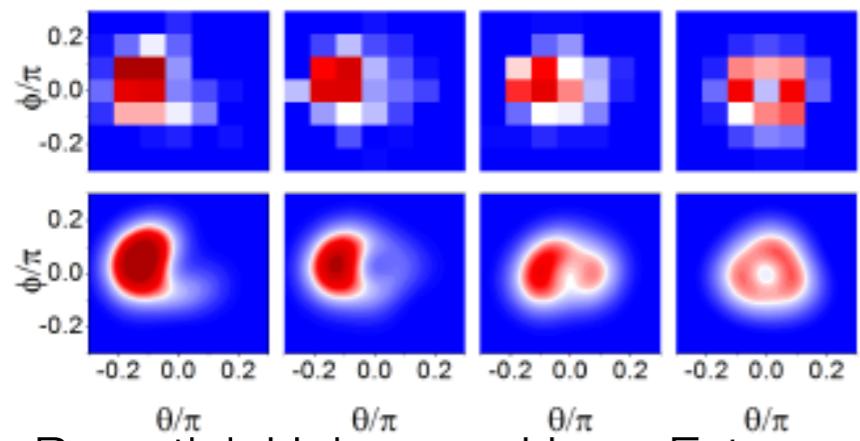
Two-fold approach

- ✓ Maximize interaction-to-decay ratio
- Devise entanglement schemes that are robust to photon loss

Approaches to Entanglement

E.g., collective spin excitation

Strong coupling: $\eta \sim 100$,
deterministic



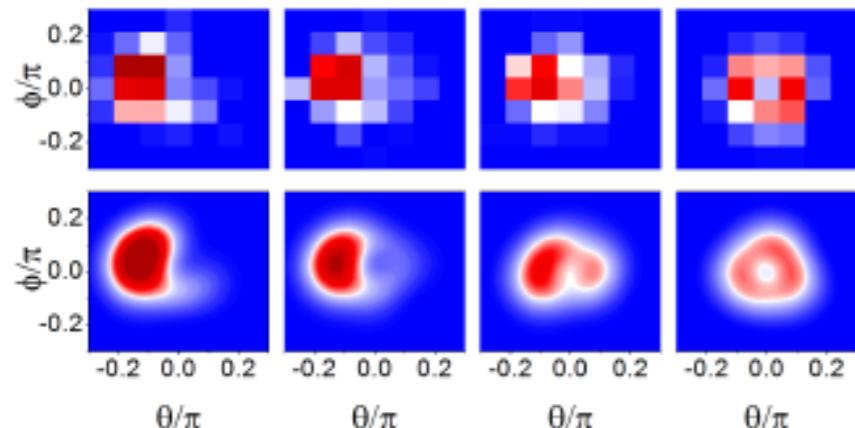
Barontini, Hohmann, Haas, Esteve
& Reichel, *Science* (2016).

Haas, Reichel, Volz, Gehr & Esteve,
Science (2016).

Approaches to Entanglement

E.g., collective spin excitation

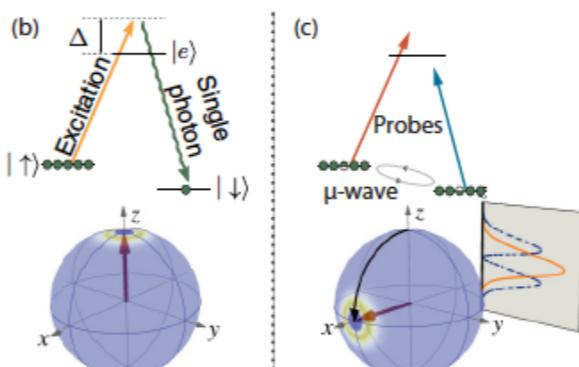
Strong coupling: $\eta \sim 100$,
deterministic



Barontini, Hohmann, Haas, Esteve
& Reichel, *Science* (2016).

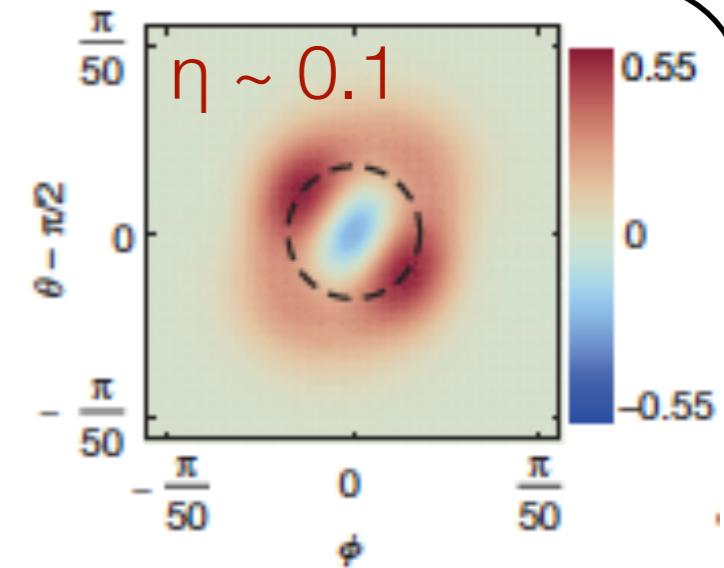
Haas, Reichel, Volz, Gehr & Esteve,
Science (2016).

Weak coupling,
heralded



Christensen, ... & Polzik,
PRA (2014).

Use the light leaking out of the cavity:

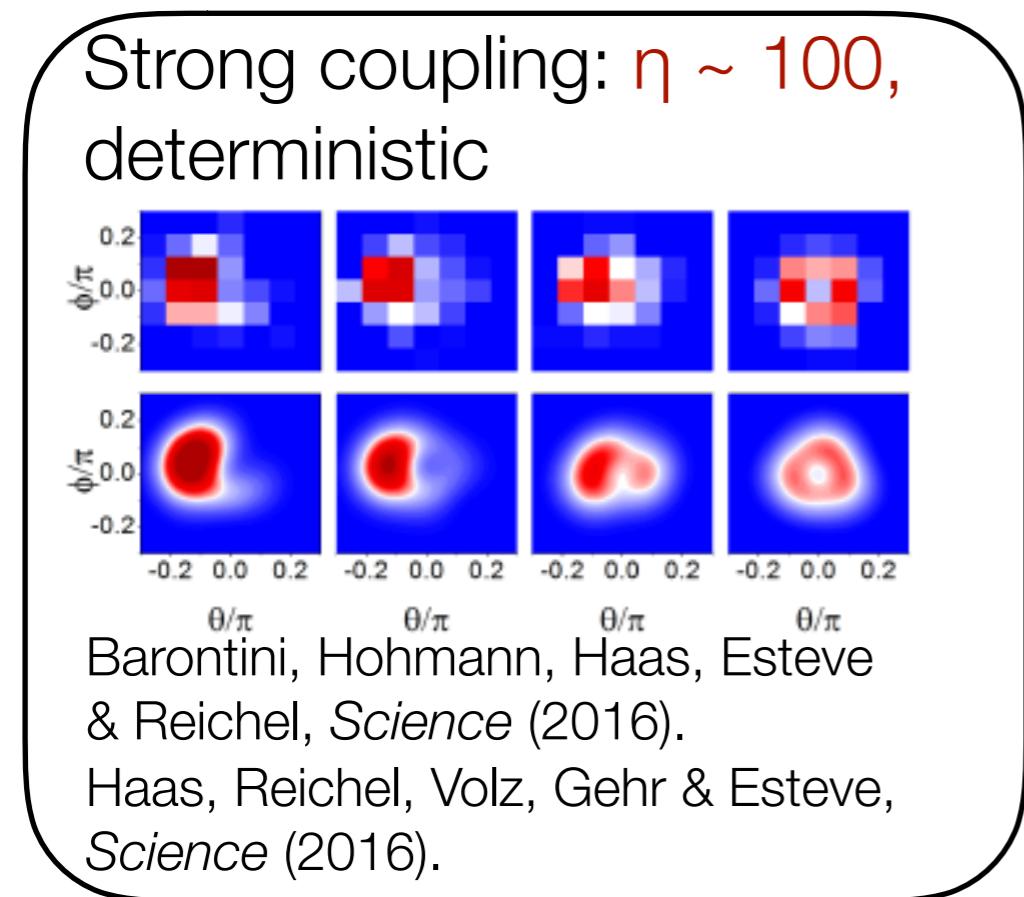


McConnell, Zhang, Hu, Cuk
& Vuletic, *Nature* (2015).

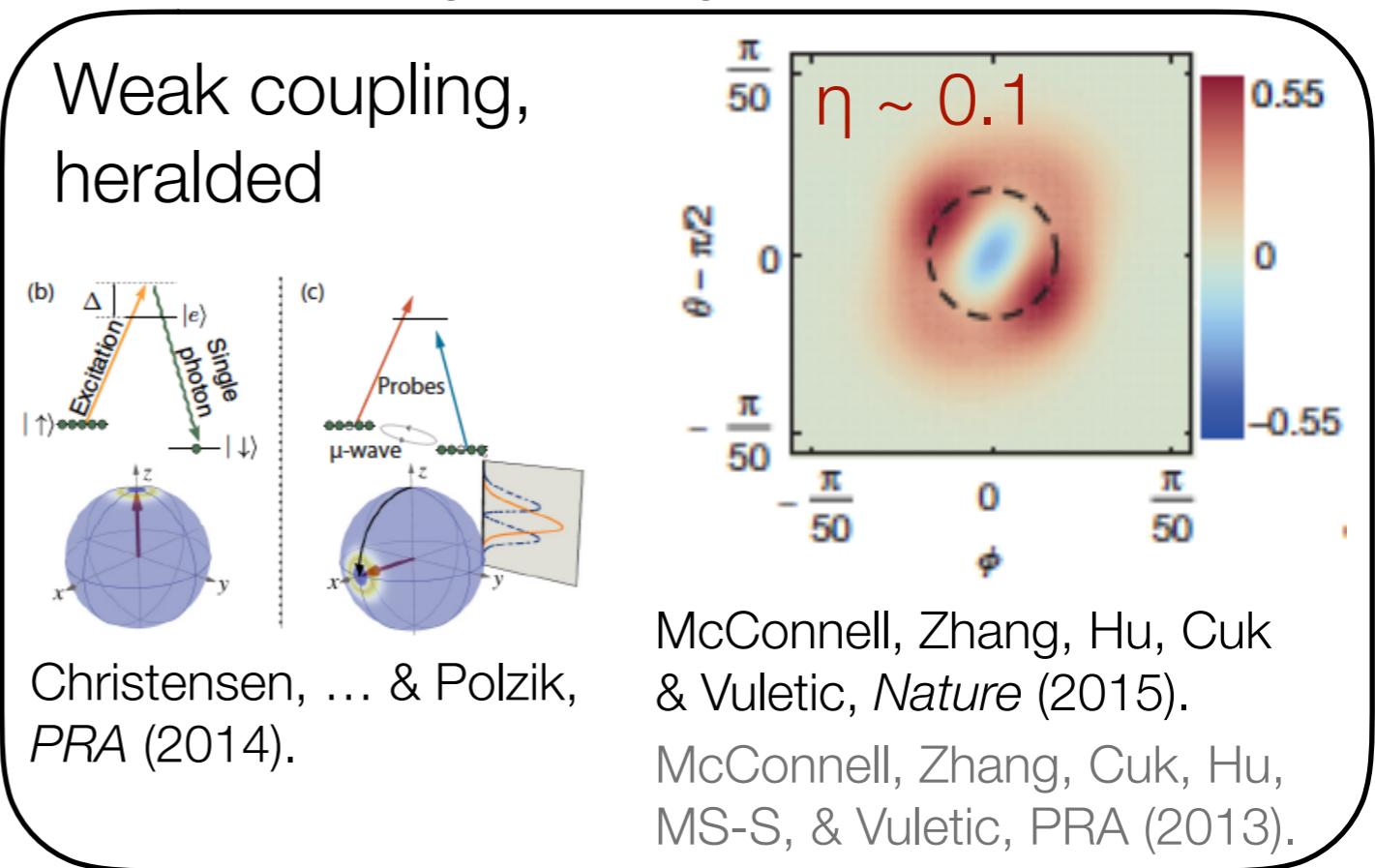
McConnell, Zhang, Cuk, Hu,
MS-S, & Vuletic, *PRA* (2013).

Approaches to Entanglement

E.g., collective spin excitation

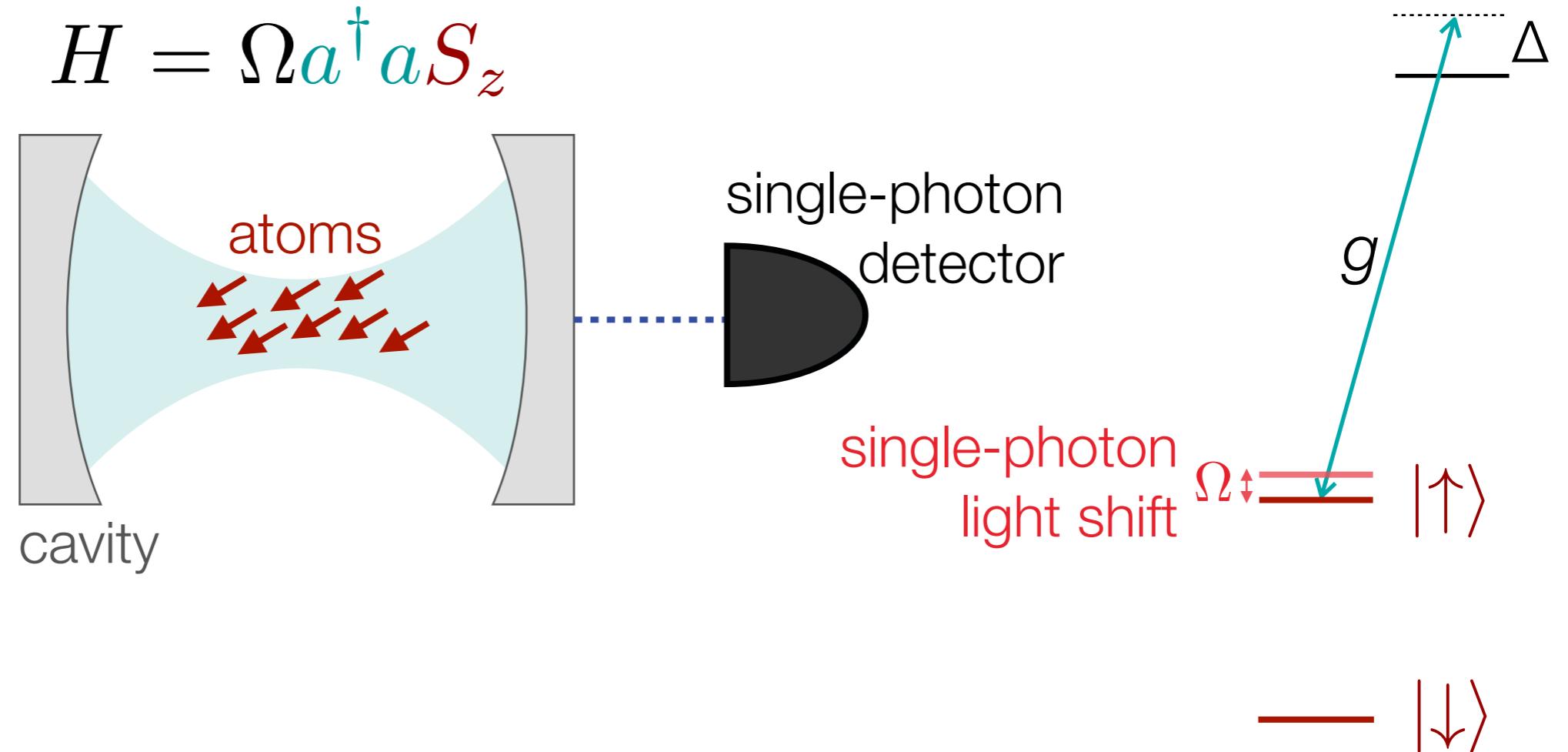


Barontini, Hohmann, Haas, Esteve & Reichel, *Science* (2016).
Haas, Reichel, Volz, Gehr & Esteve, *Science* (2016).

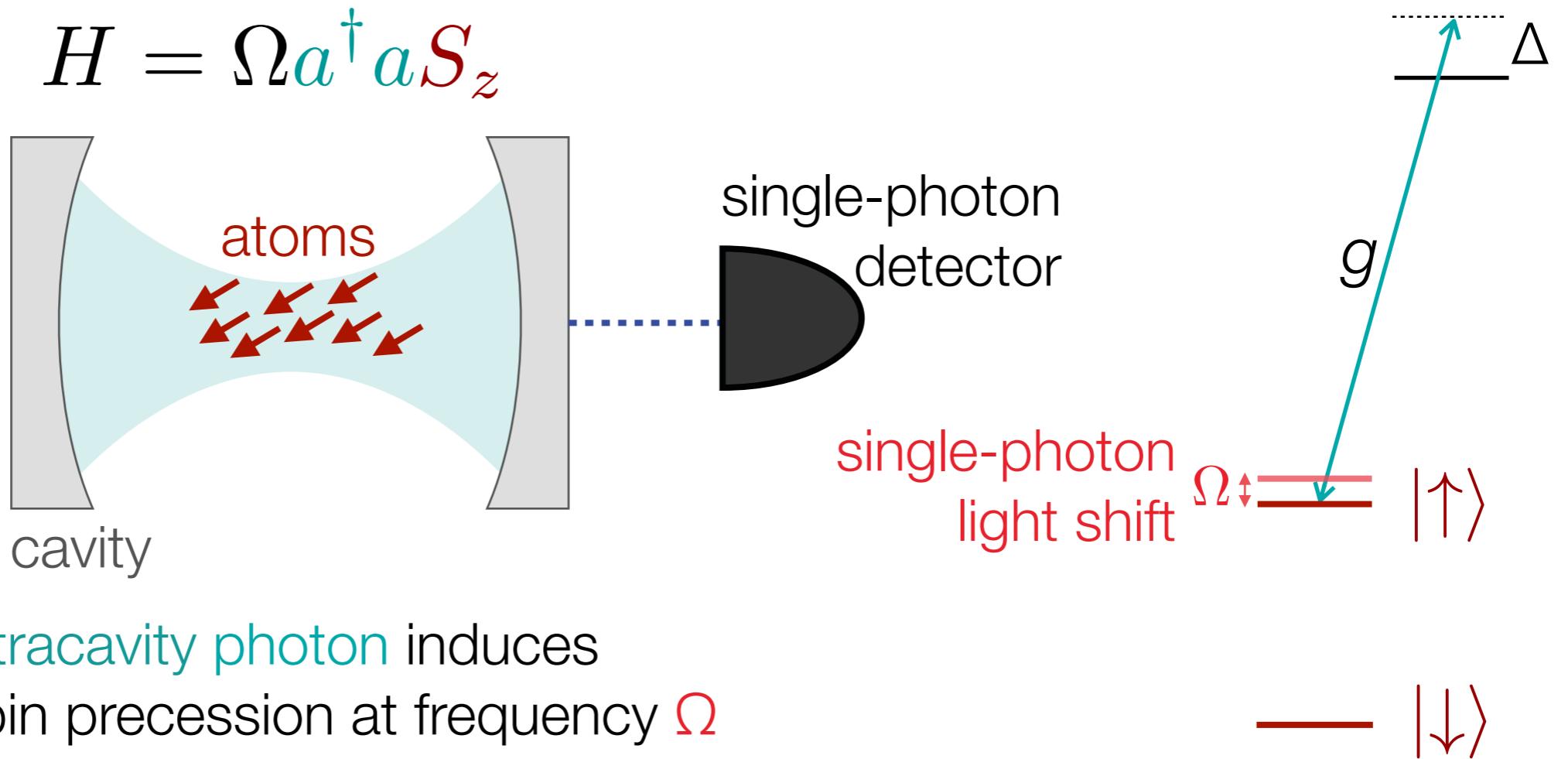


Heralding + strong coupling }  Schrödinger's cat states?
More versatile quantum control?

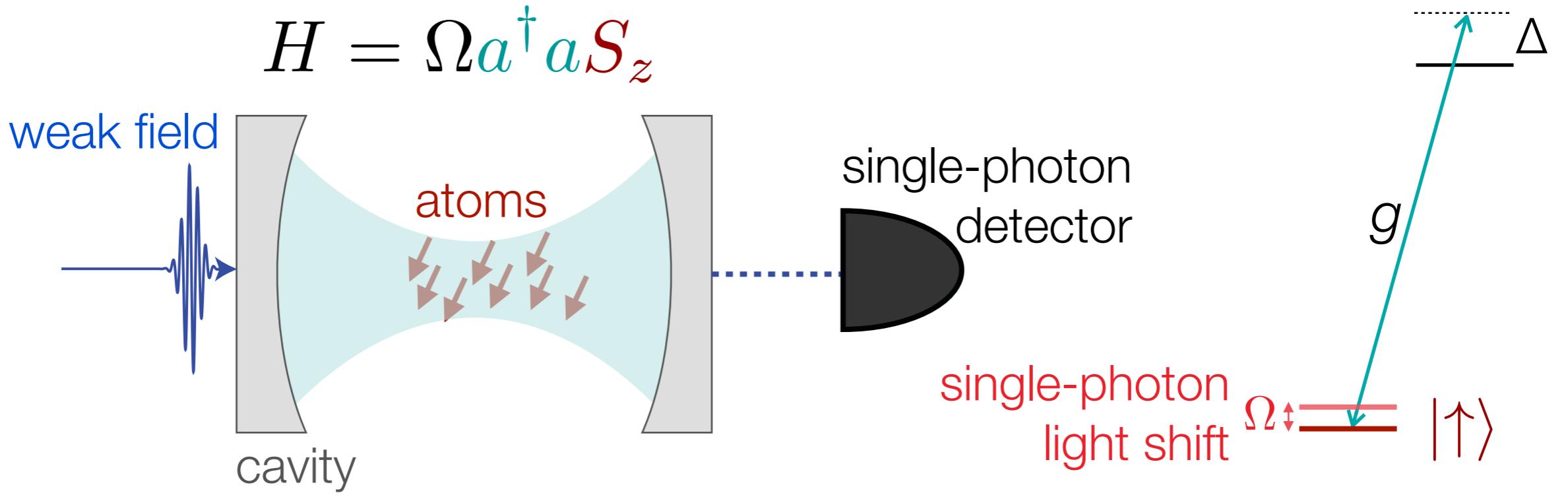
Dispersive Atom-Light Interaction



Dispersive Atom-Light Interaction



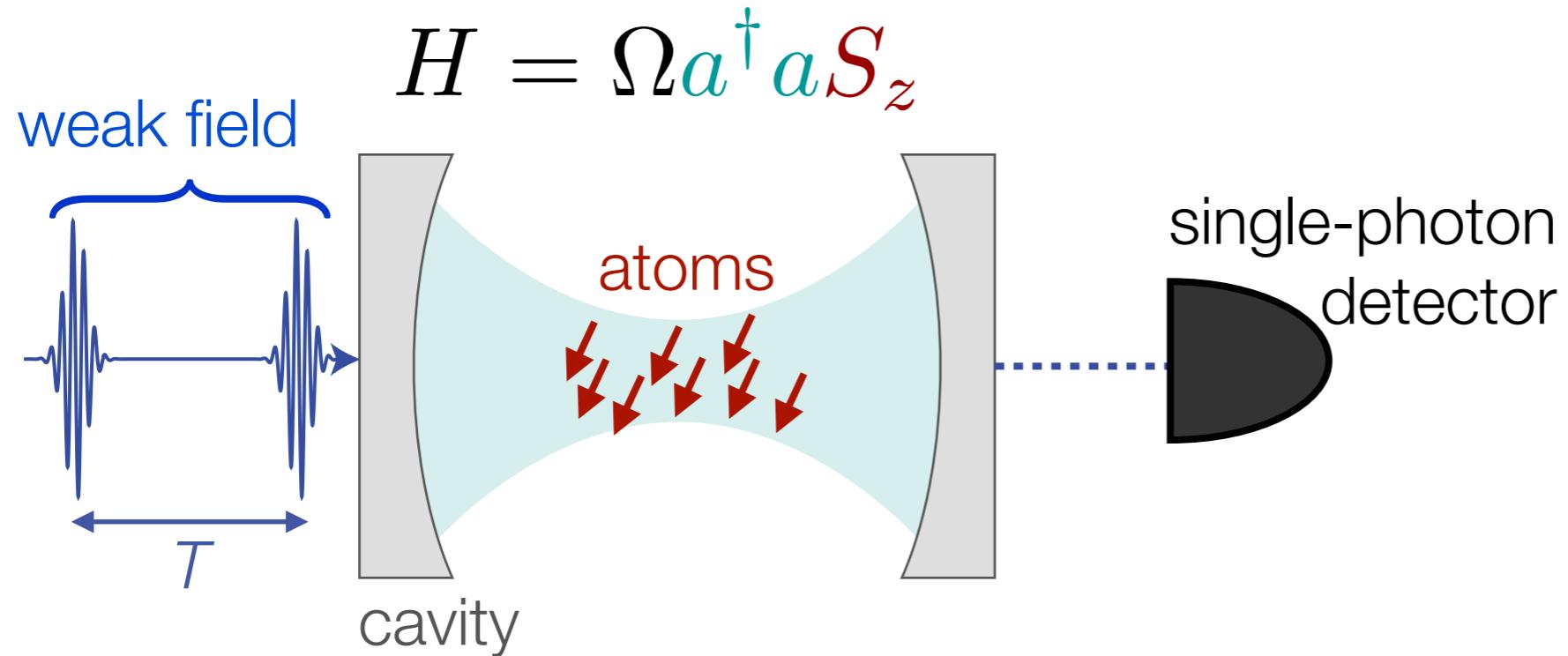
Dispersive Atom-Light Interaction



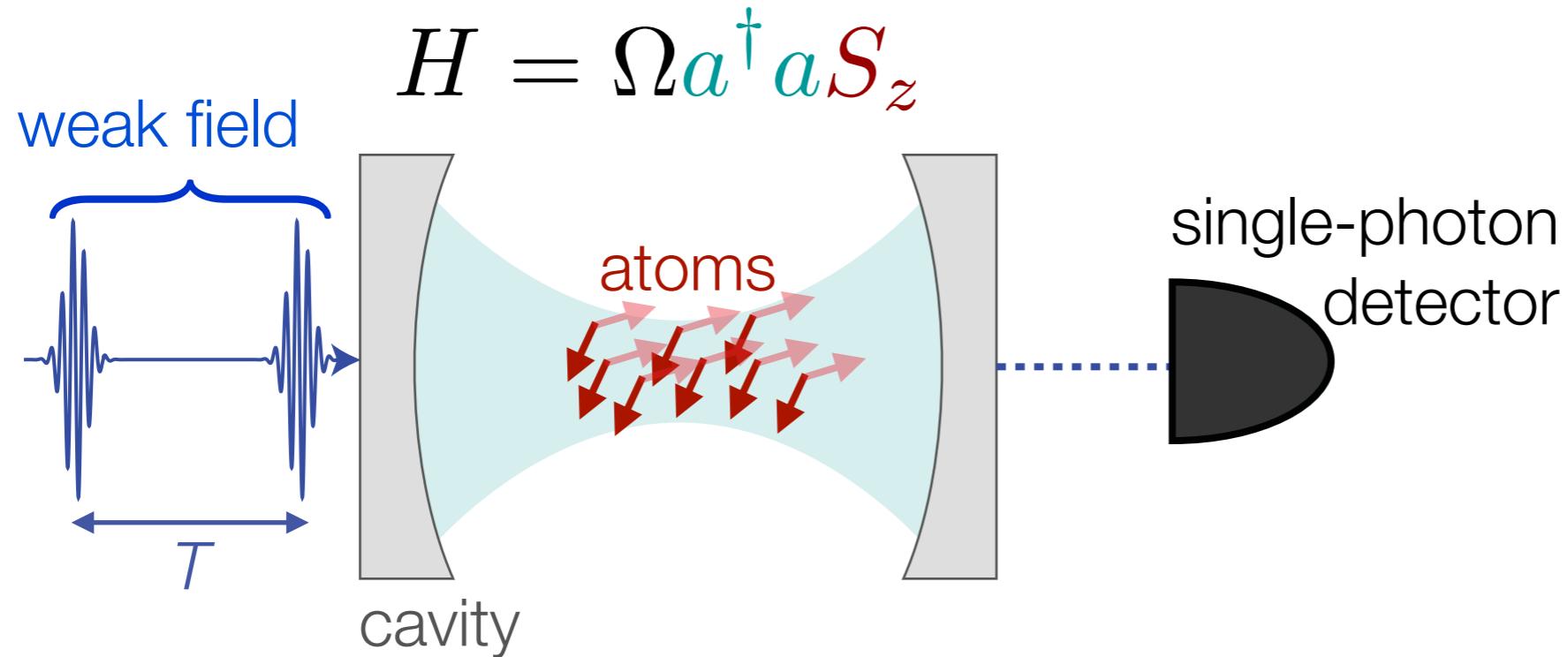
Intracavity photon induces
spin precession at frequency Ω

Short input pulse + detection a time t later
⇒ spins precessed by Ωt

Heralded Cat States

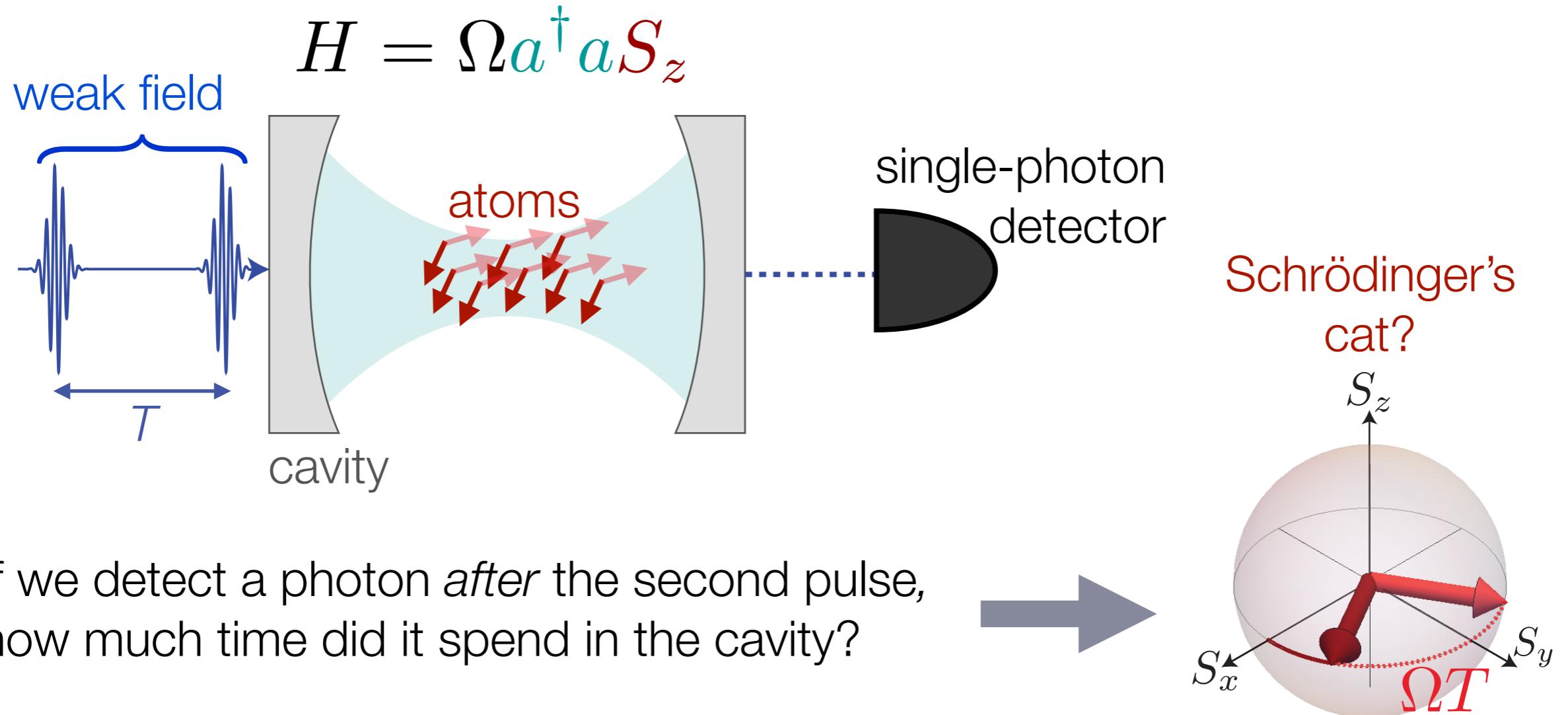


Heralded Cat States

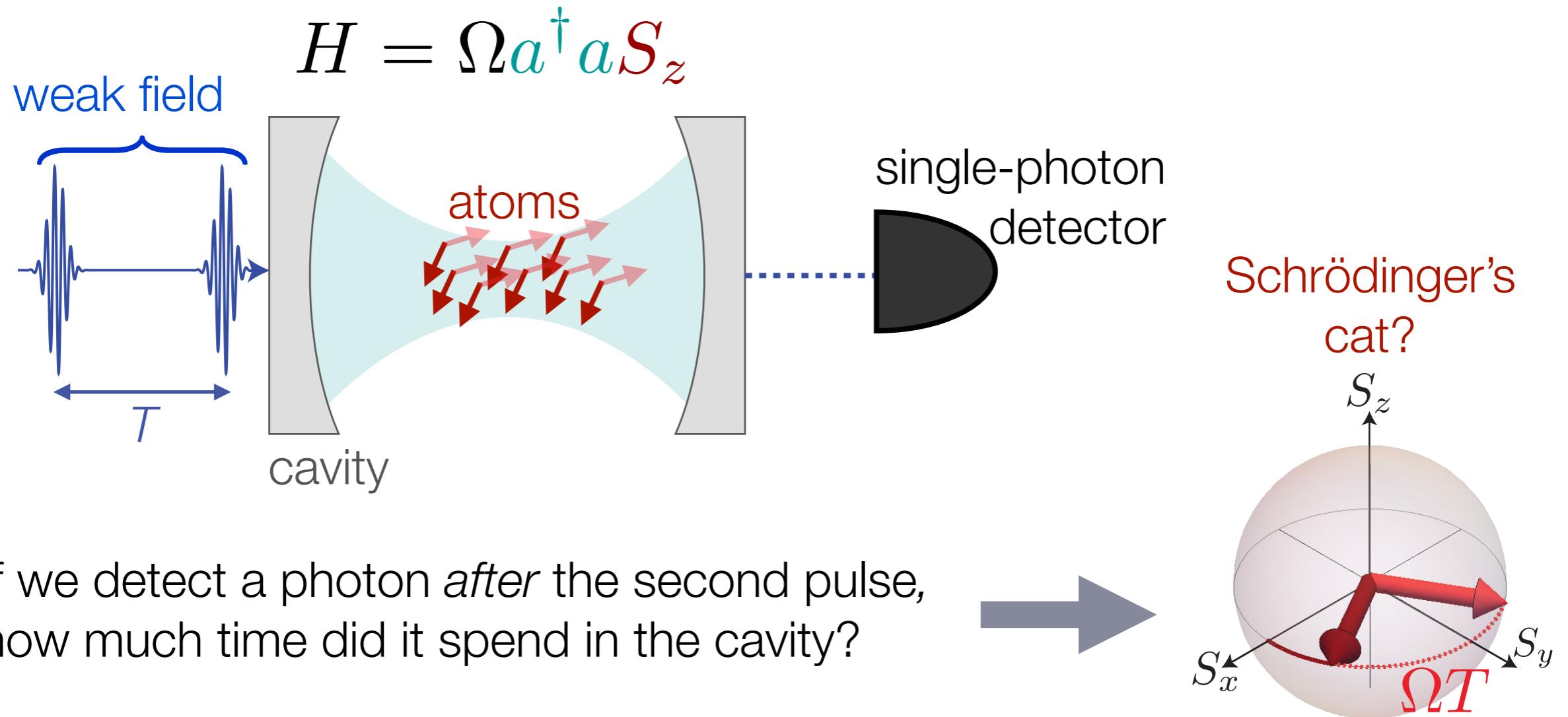


If we detect a photon *after* the second pulse,
how much time did it spend in the cavity?

Heralded Cat States



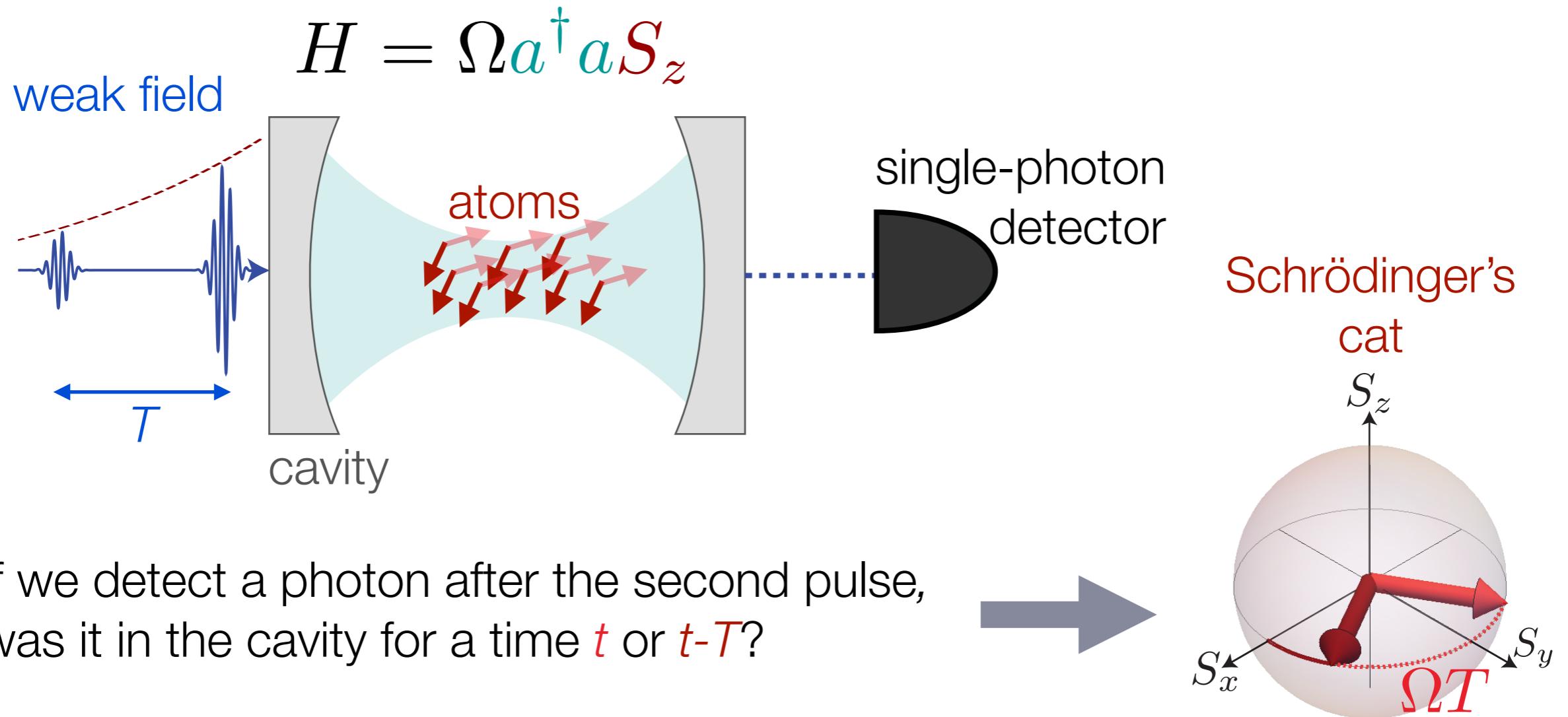
Heralded Cat States



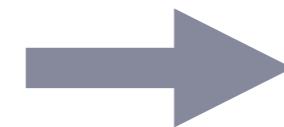
What if T is longer than the cavity lifetime $1/\kappa$?

Heralded Cat States

E. Davis, Z. Wang, G. Bentsen, T. Li,
A. Safavi-Naeini & MS-S (in prep).



If we detect a photon after the second pulse,
was it in the cavity for a time t or $t-T$?

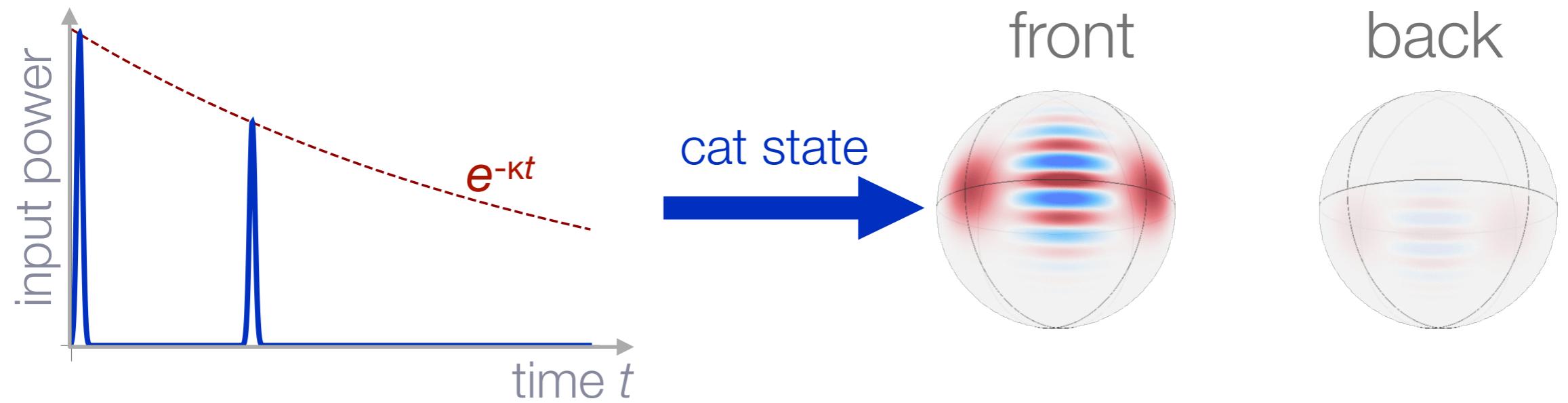


For equal superposition even at finite cavity lifetime $1/\kappa$:
Make second pulse weaker than first by $e^{-\kappa T}$

Single Photon as a Paintbrush

E. Davis, Z. Wang, G. Bentsen, T. Li,
A. Safavi-Naeini & MS-S (in prep.).

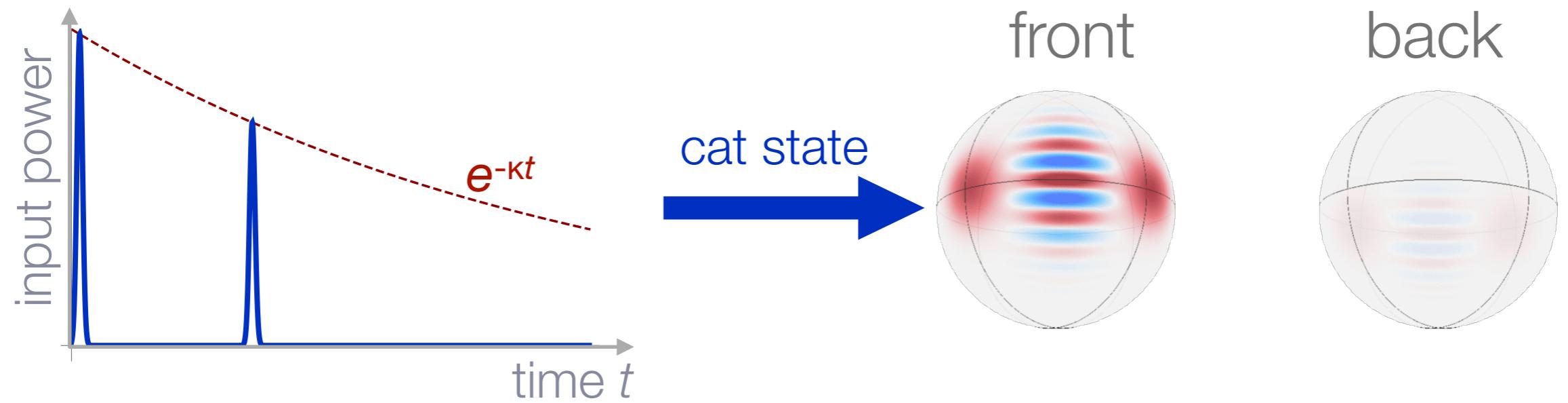
...for versatile quantum control:



Single Photon as a Paintbrush

E. Davis, Z. Wang, G. Bentsen, T. Li,
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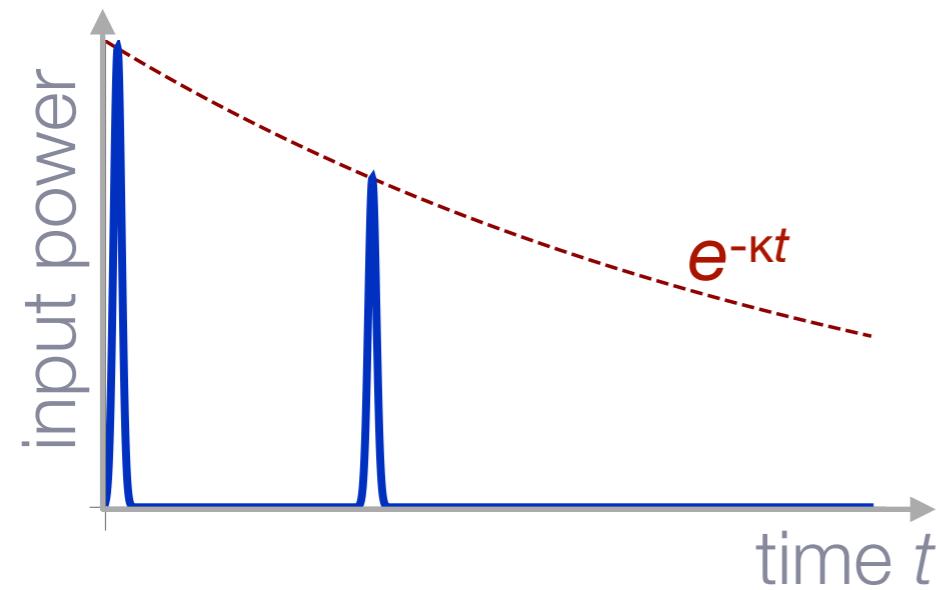
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Single Photon as a Paintbrush

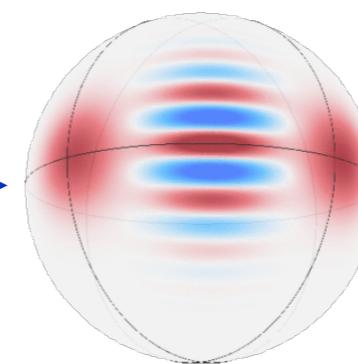
E. Davis, Z. Wang, G. Bentsen, T. Li,
A. Safavi-Naeini & MS-S (in prep.).

...for versatile quantum control:

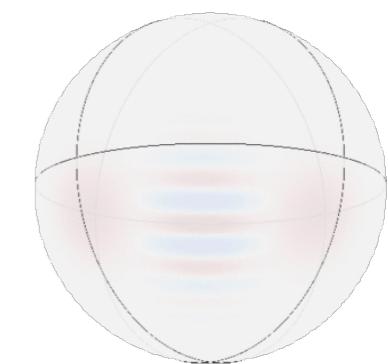


cat state
→

front

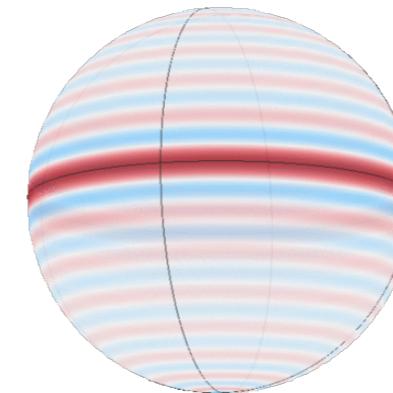


back

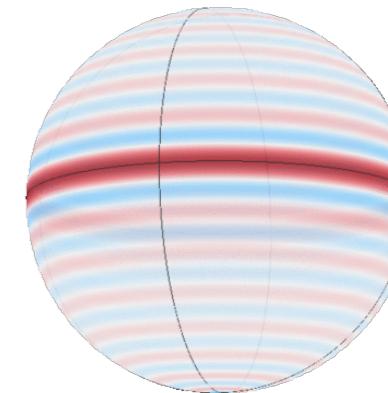


Dicke state
→

front



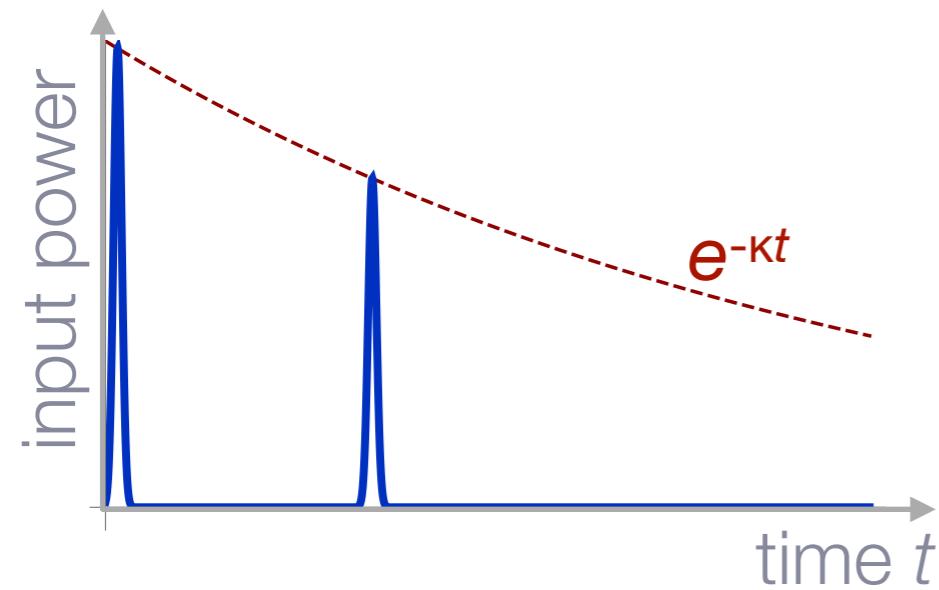
back



Single Photon as a Paintbrush

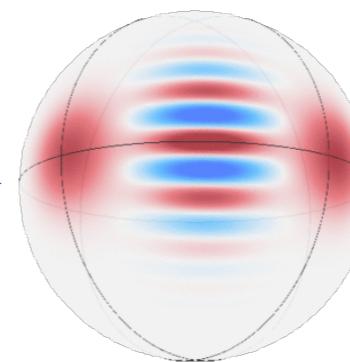
E. Davis, Z. Wang, G. Bentsen, T. Li,
A. Safavi-Naeini & MS-S (in prep.).

...for versatile quantum control:

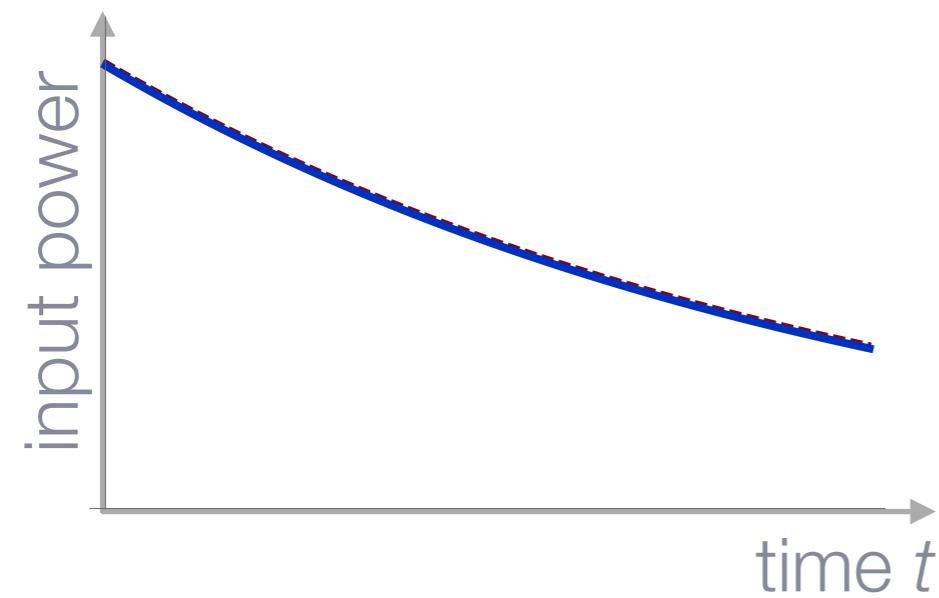
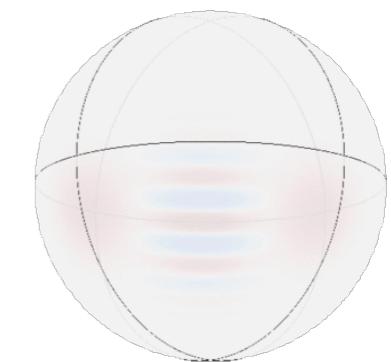


cat state
→

front

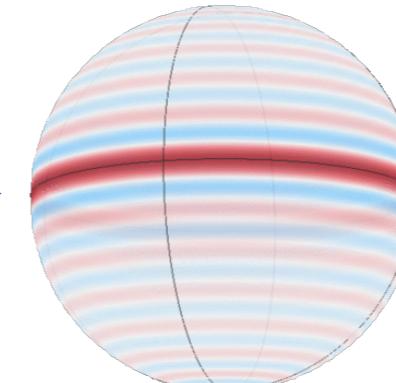


back

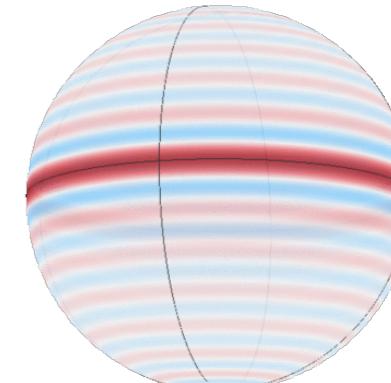


Dicke state
→

front



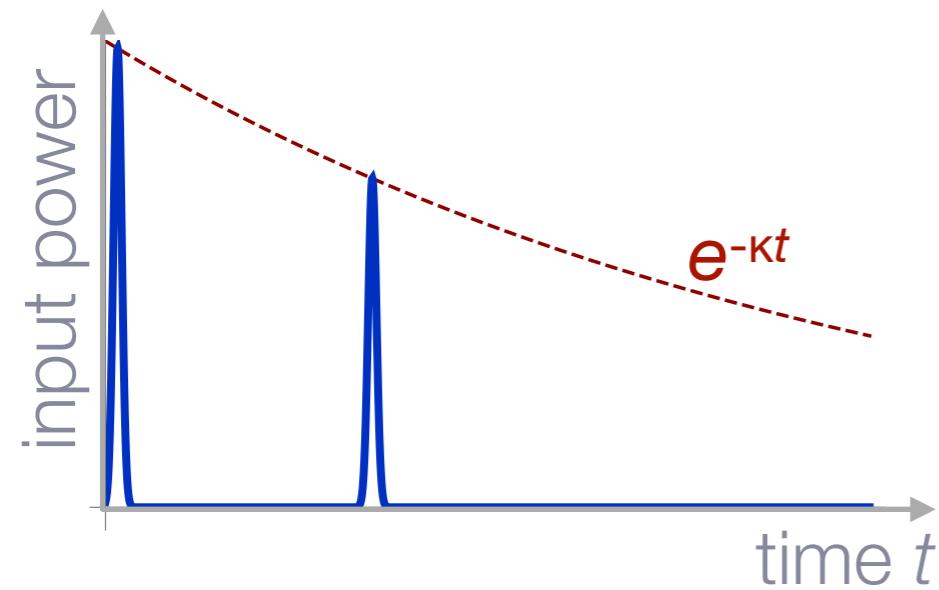
back



Single Photon as a Paintbrush*

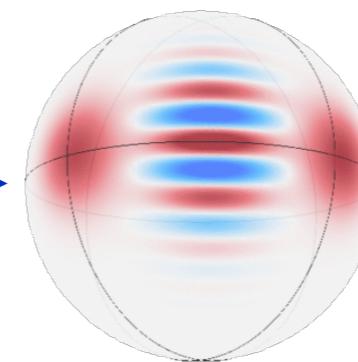
E. Davis, Z. Wang, G. Bentsen, T. Li,
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...for versatile quantum control:

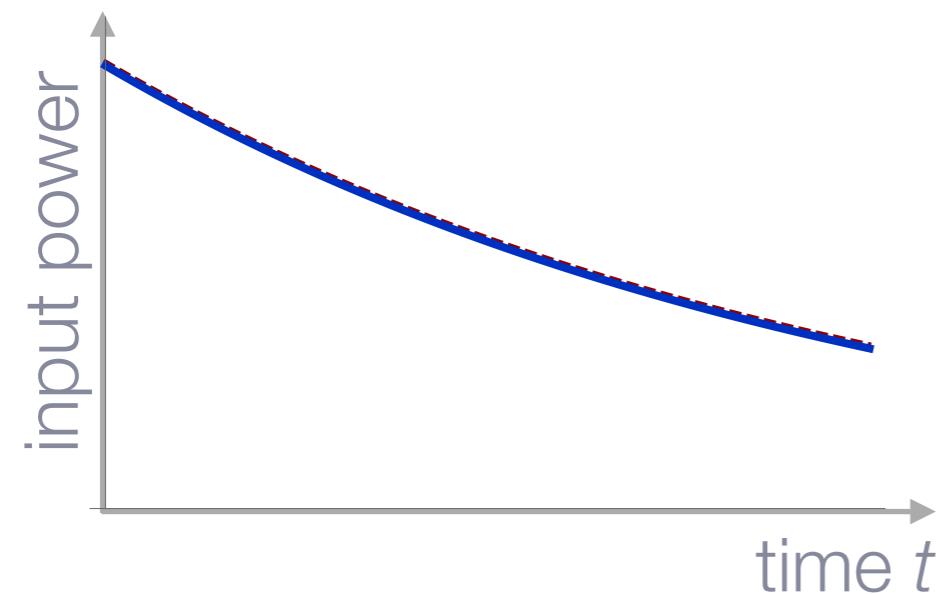
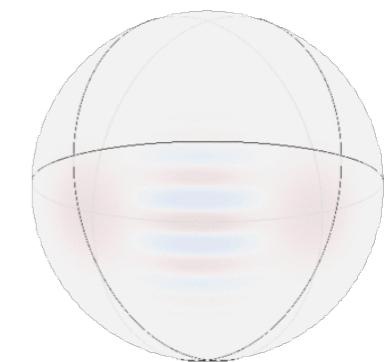


cat state
→

front

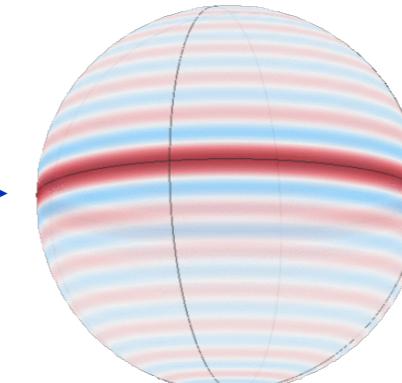


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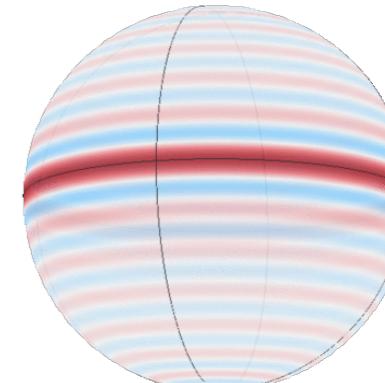


Dicke state
→

front

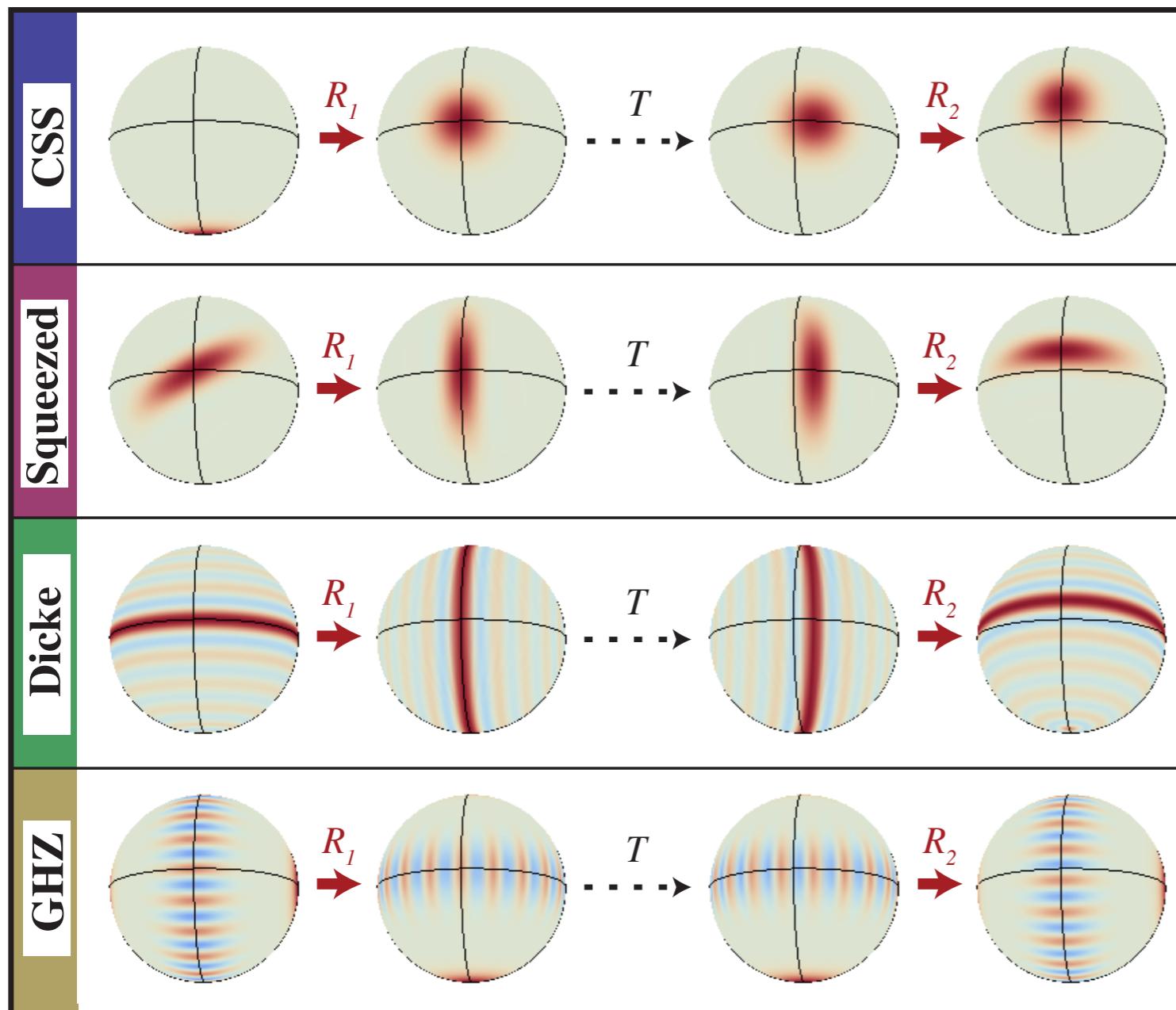


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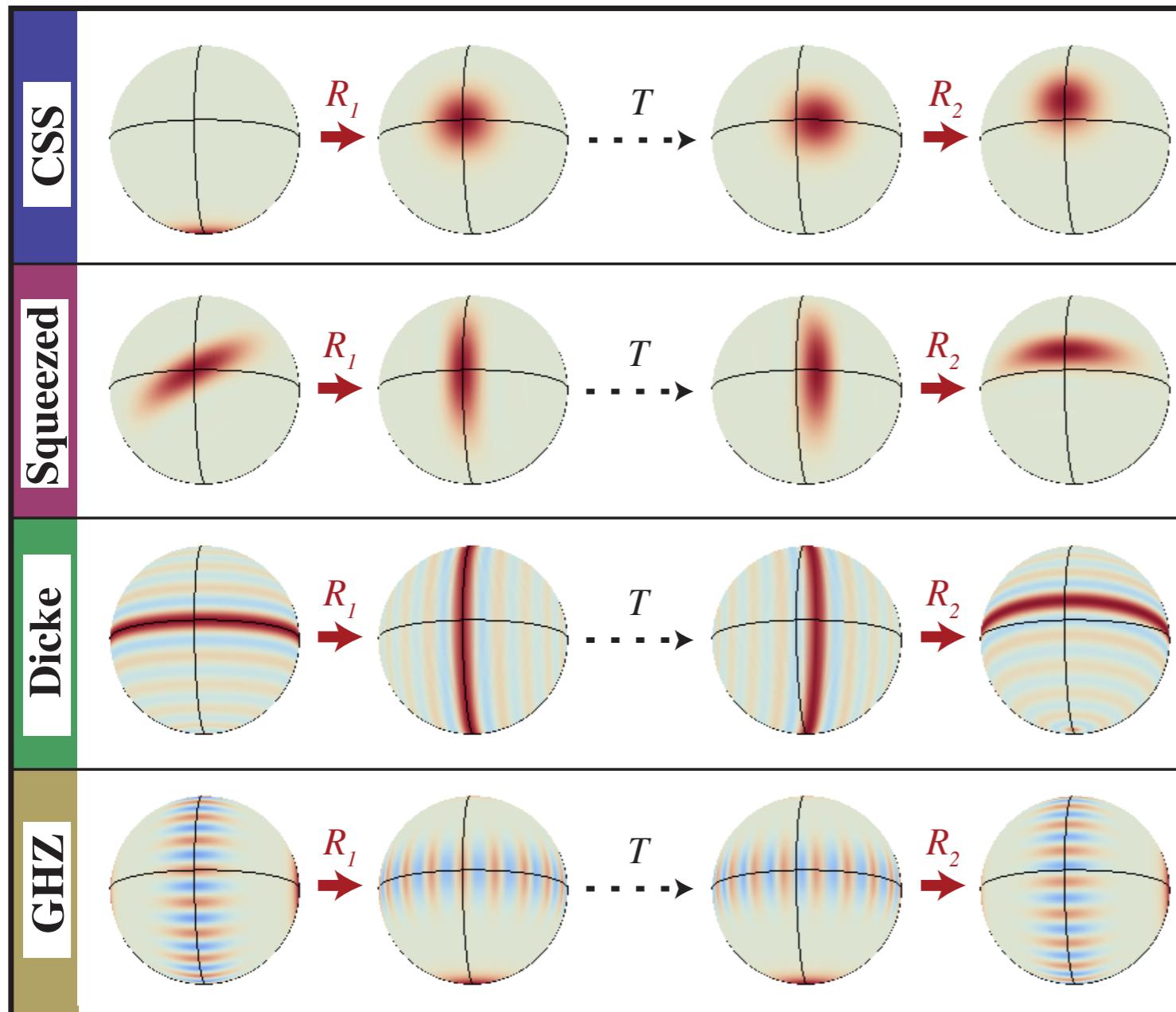


*vs. chisel (“carving”): Chen, Hu, Dong, Braverman, Zhang & Vuletic, *PRL* (2015).

Generalized Ramsey Spectroscopy

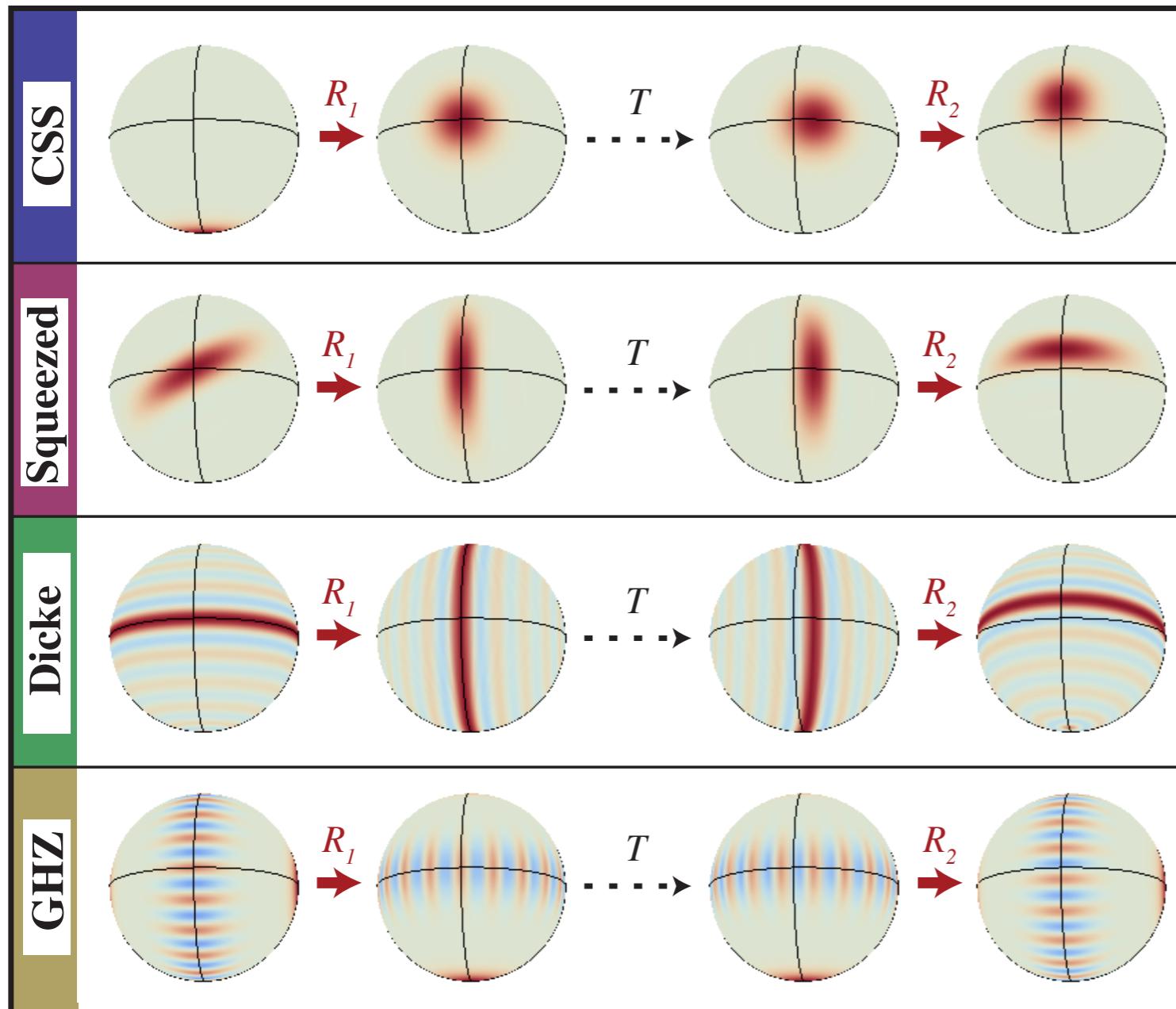


Generalized Ramsey Spectroscopy



*If we could make any state,
which would we choose?*

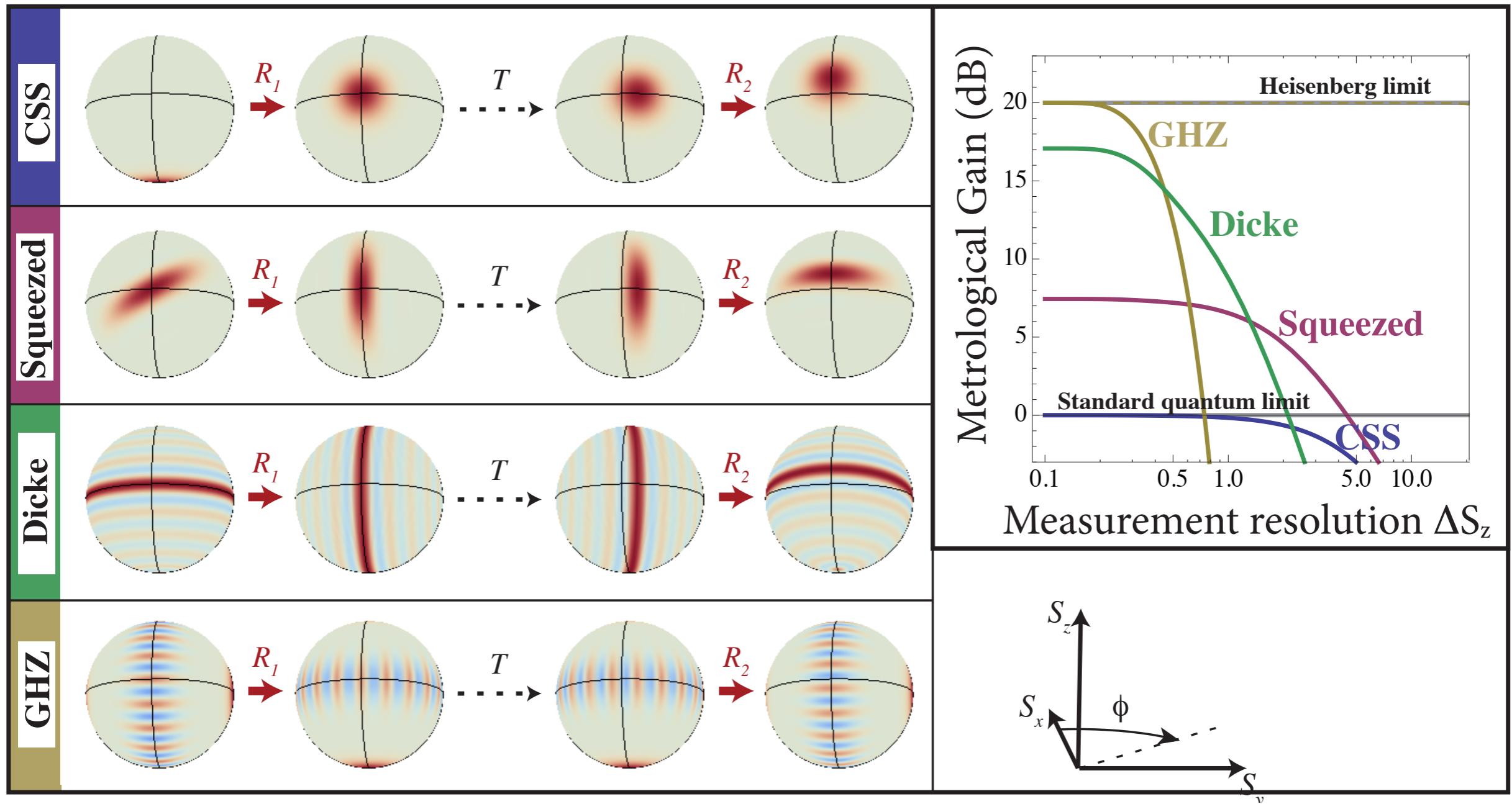
Generalized Ramsey Spectroscopy



*If we could make any state,
which would we choose?*

It depends.

Metrological Gain vs. Detection Noise

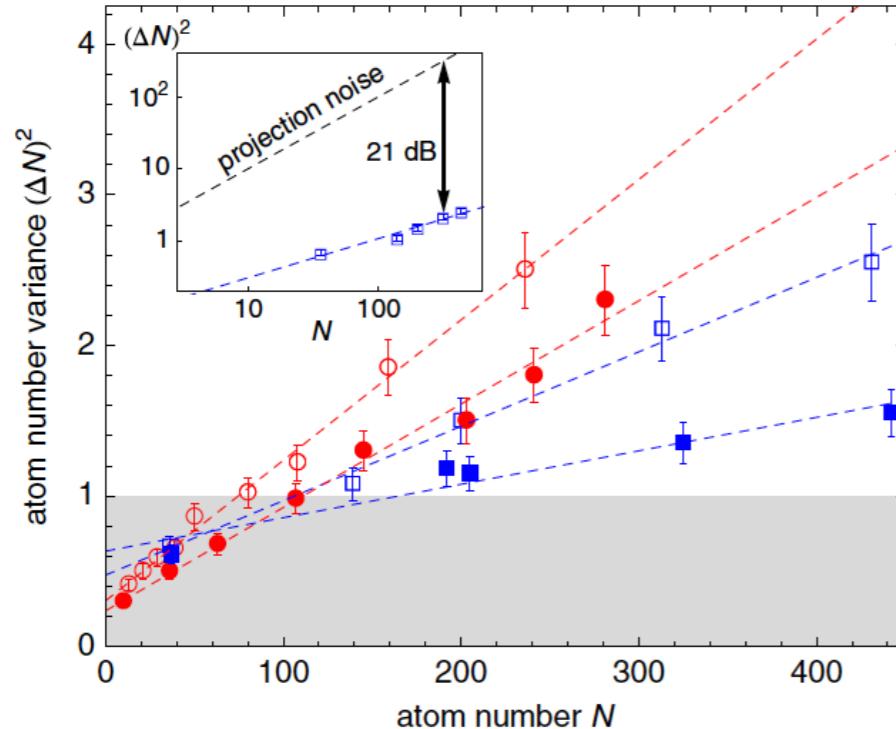


Reaping the Full Benefit of Entanglement

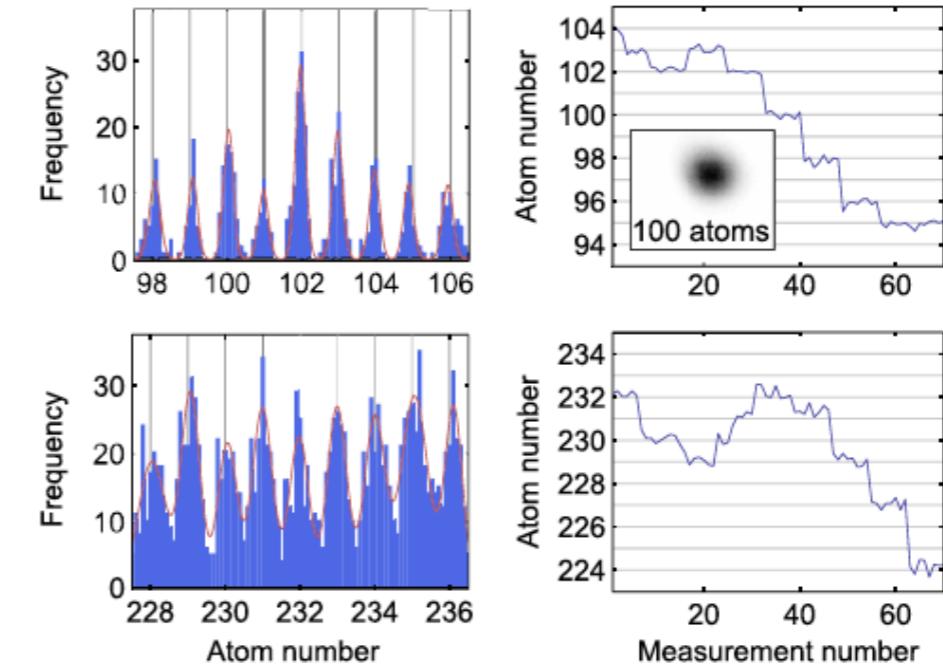
Approaches:

- Perfecting state detection

Cavity-aided state-sensitive single-atom resolution:
H. Zhang *et al.*, *PRL* **109**, 133603 (2012).

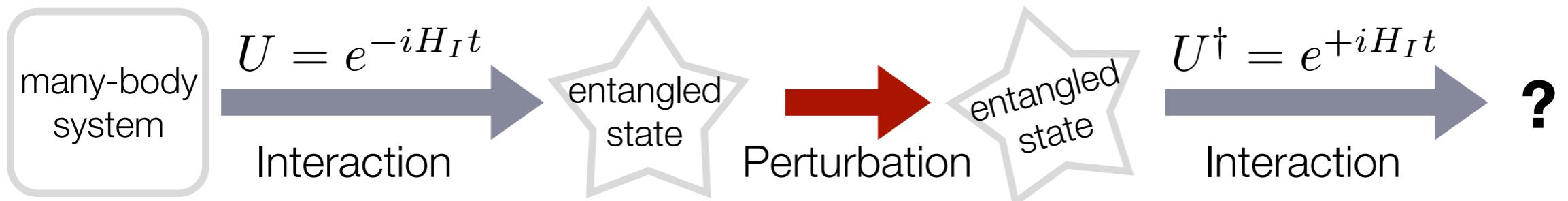


Free-space detection by MOT recapture:
Hume *et al.*, *PRL* (2013).

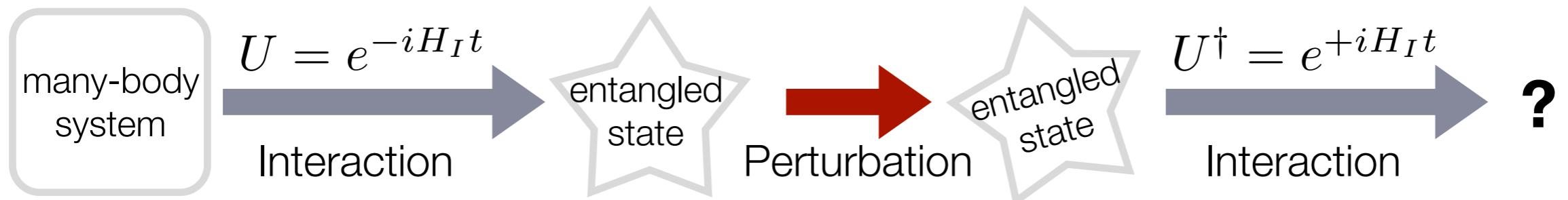


- *Circumventing the need to directly detect the entangled state?*

Echo Spectroscopy



Echo Spectroscopy

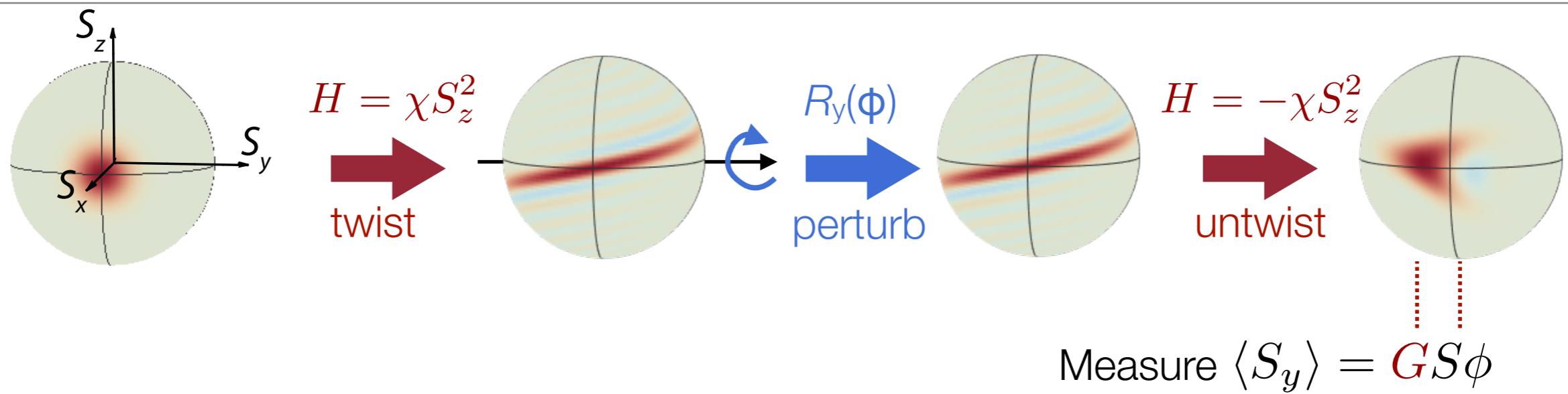


Detect perturbation by measuring whether system returns to *initial state*, rather than directly detecting the entangled state

Inspiration: Loschmidt echo (diagnostic of chaos)

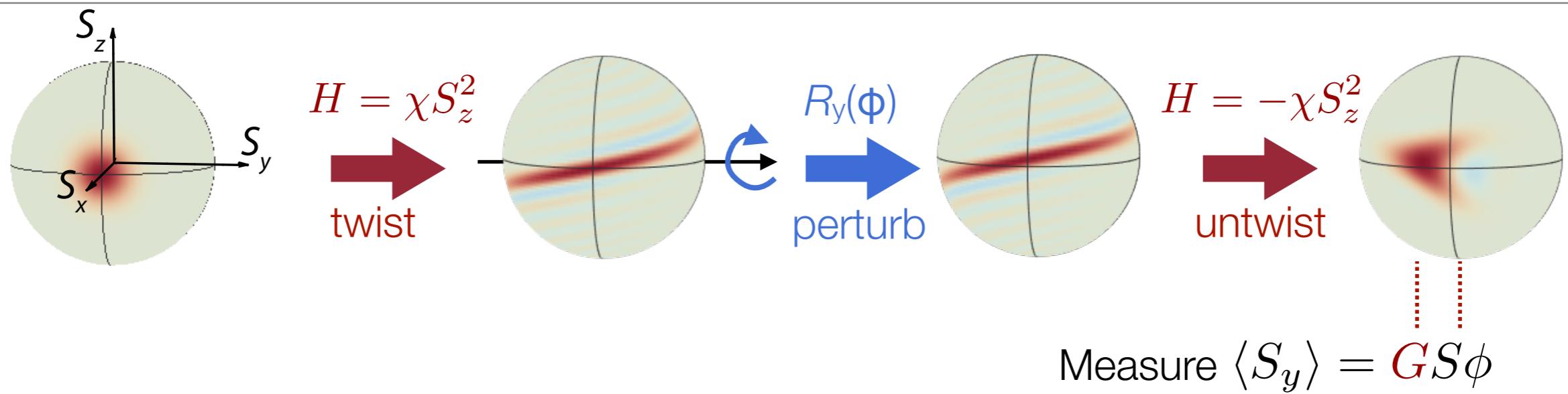
One-Axis Twisting Echo

E. Davis, G. Bentsen, & MS-S,
PRL **116**, 053601 (2016).



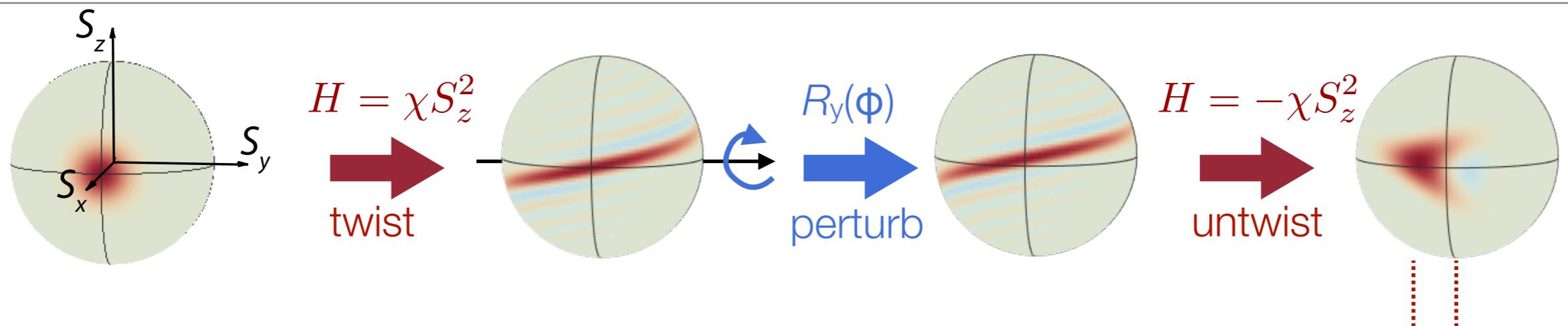
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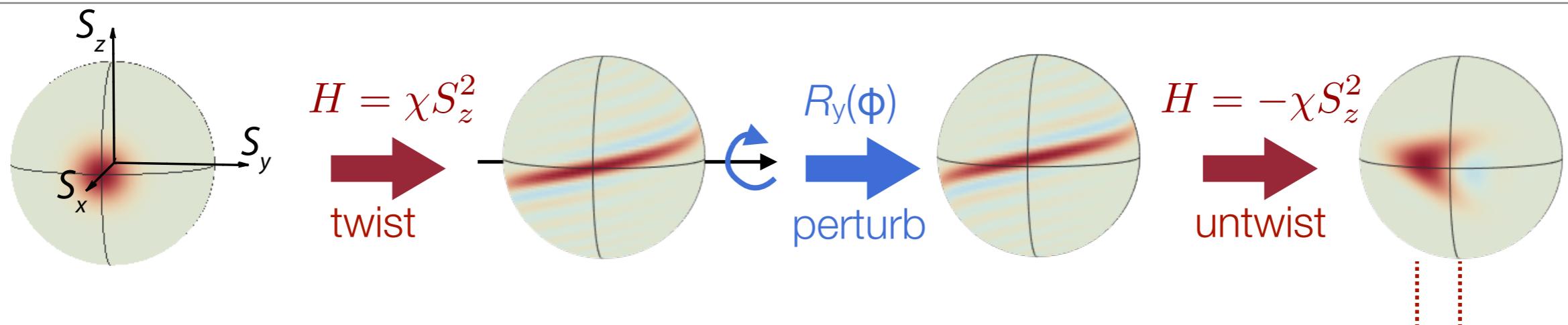
Signal amplified by factor G

Quantum noise is that of the *initial* state

Measure $\langle S_y \rangle = GS\phi$

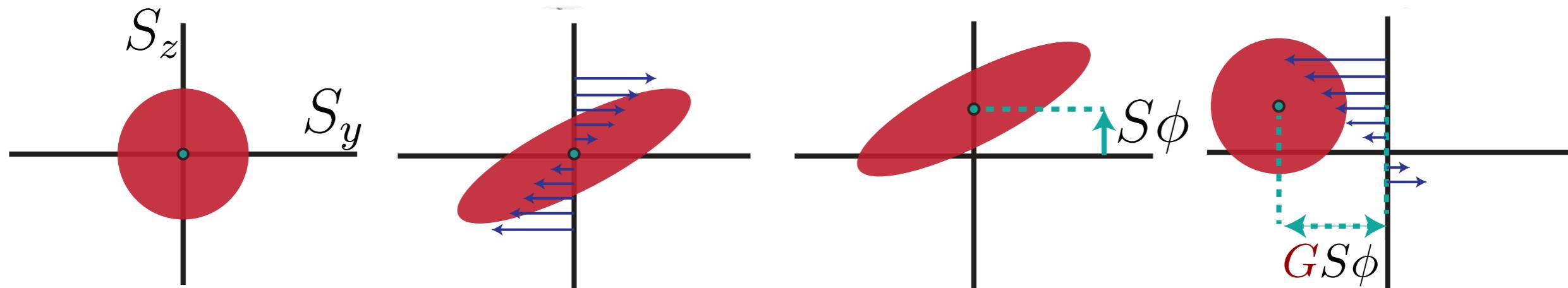
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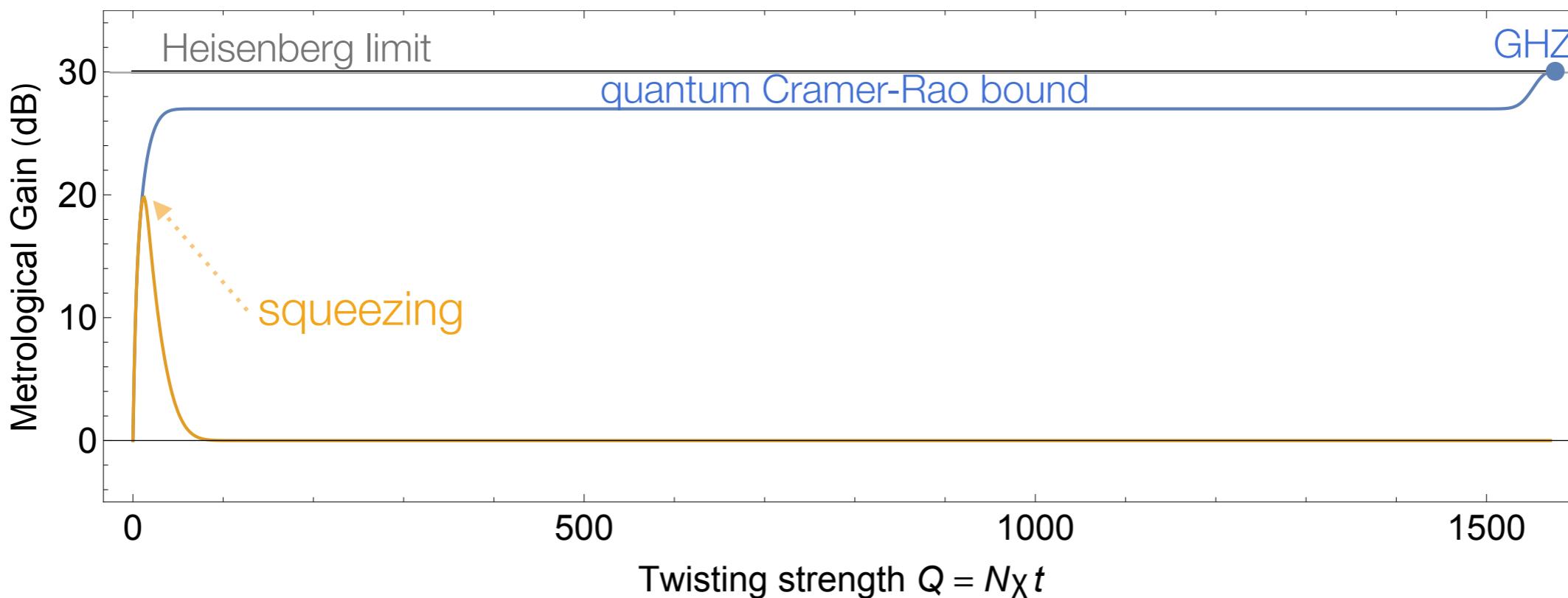
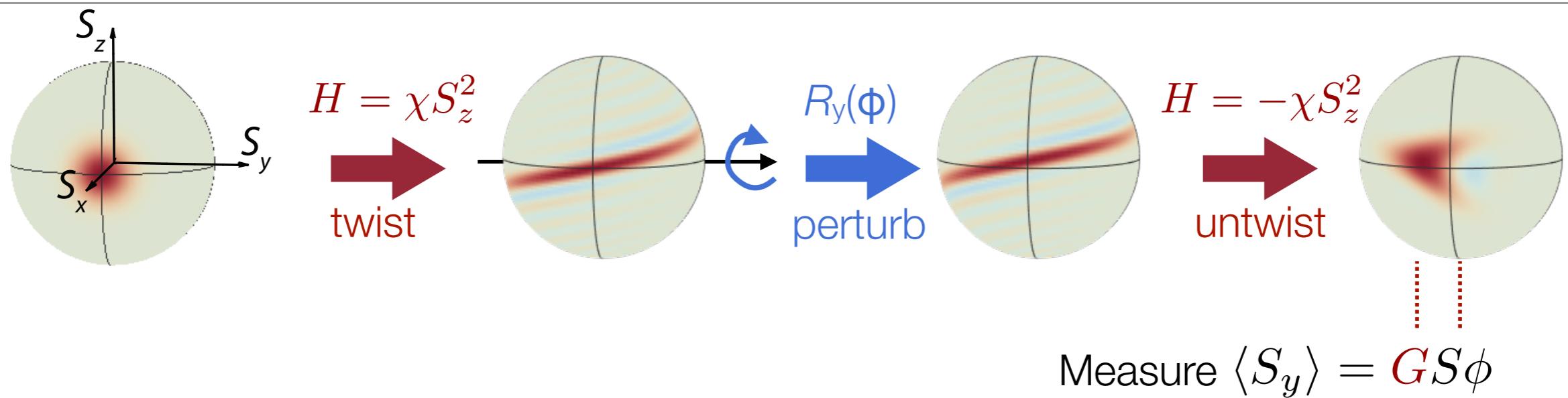
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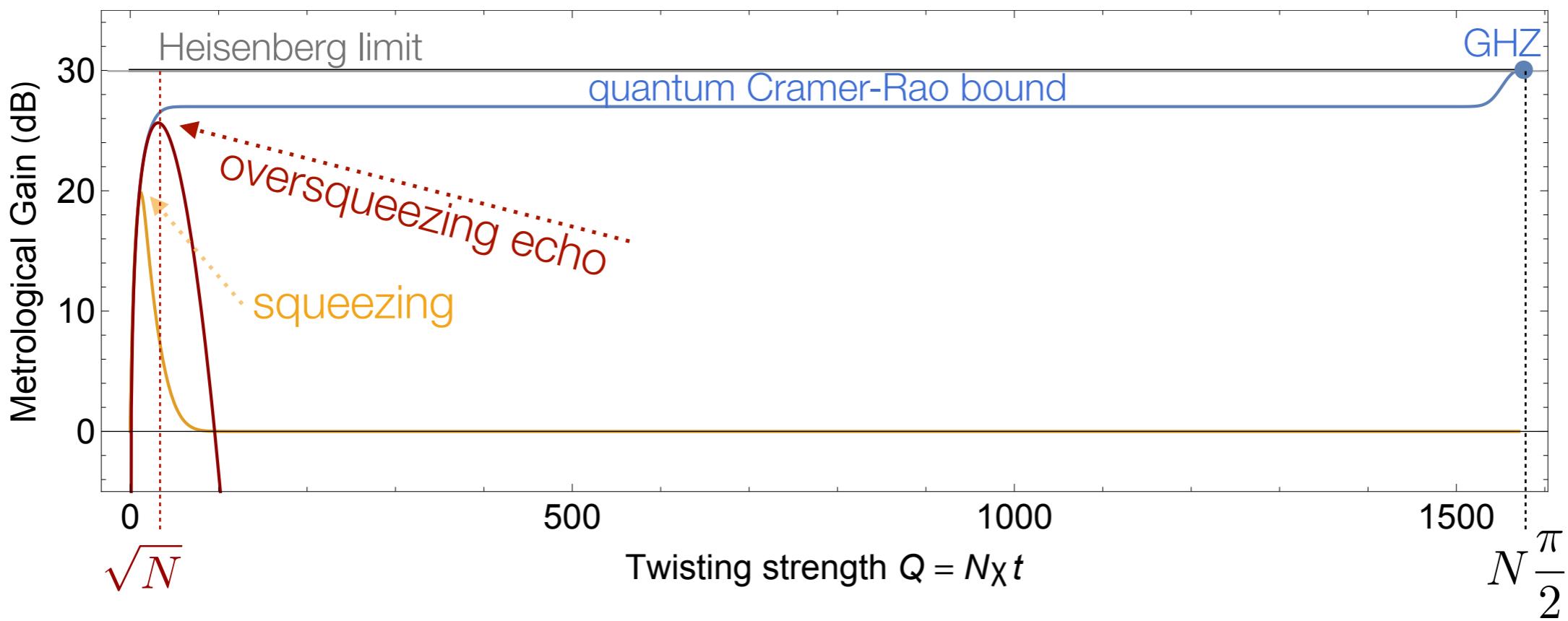
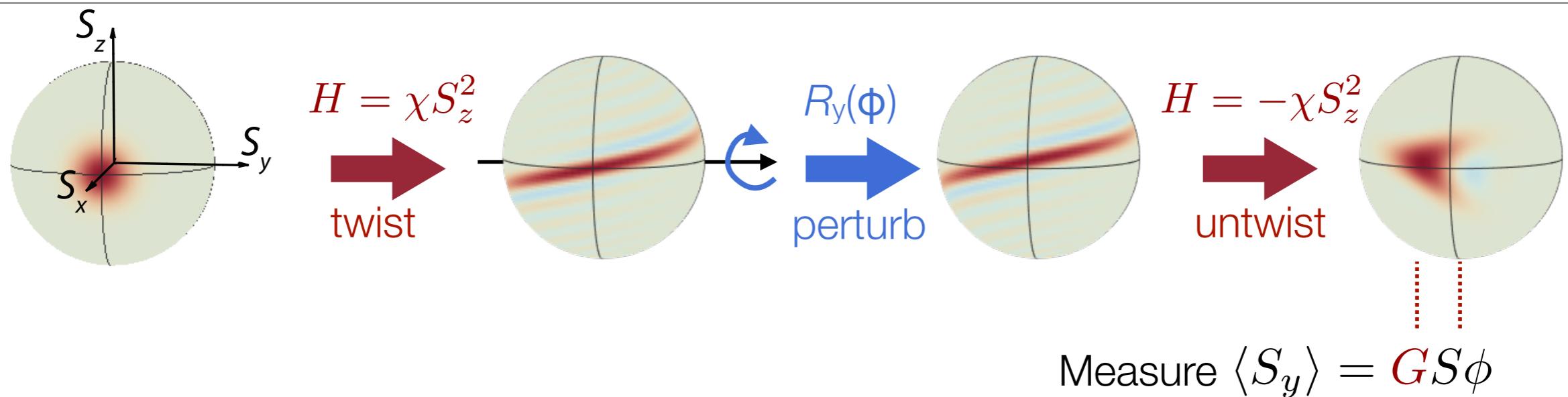
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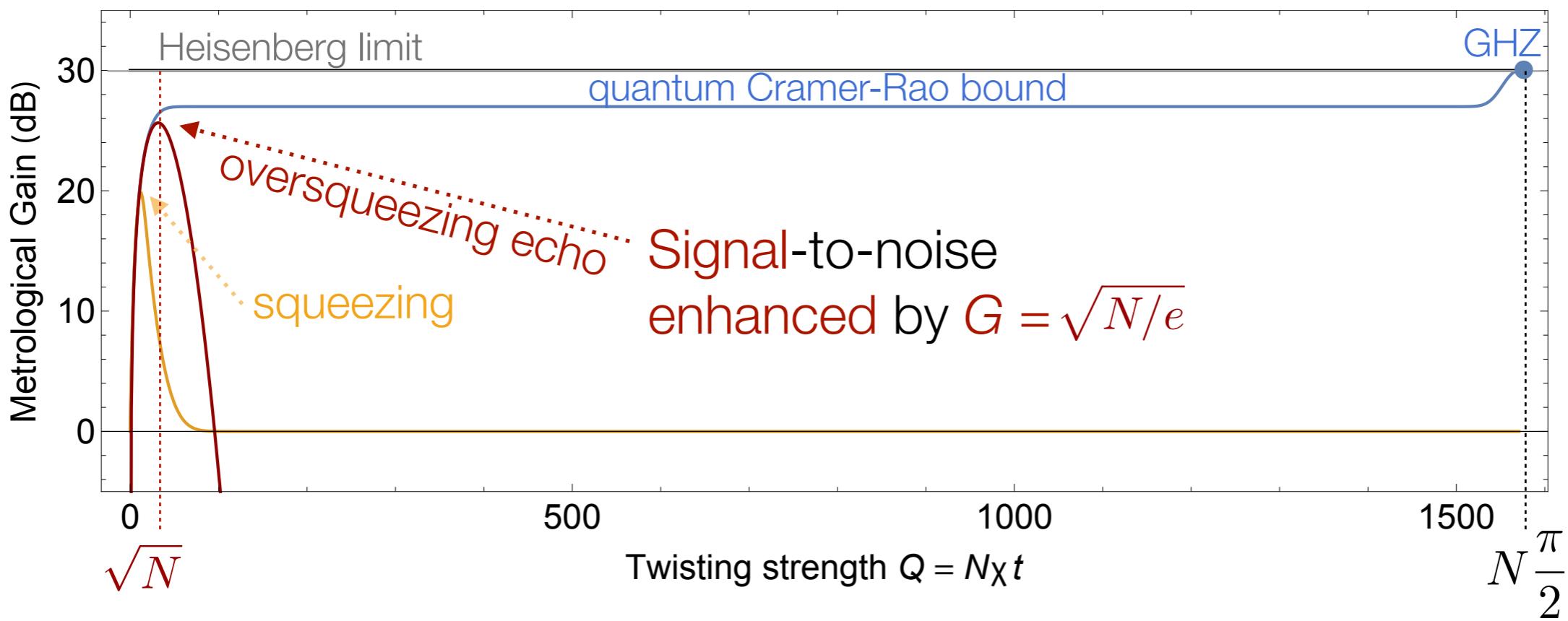
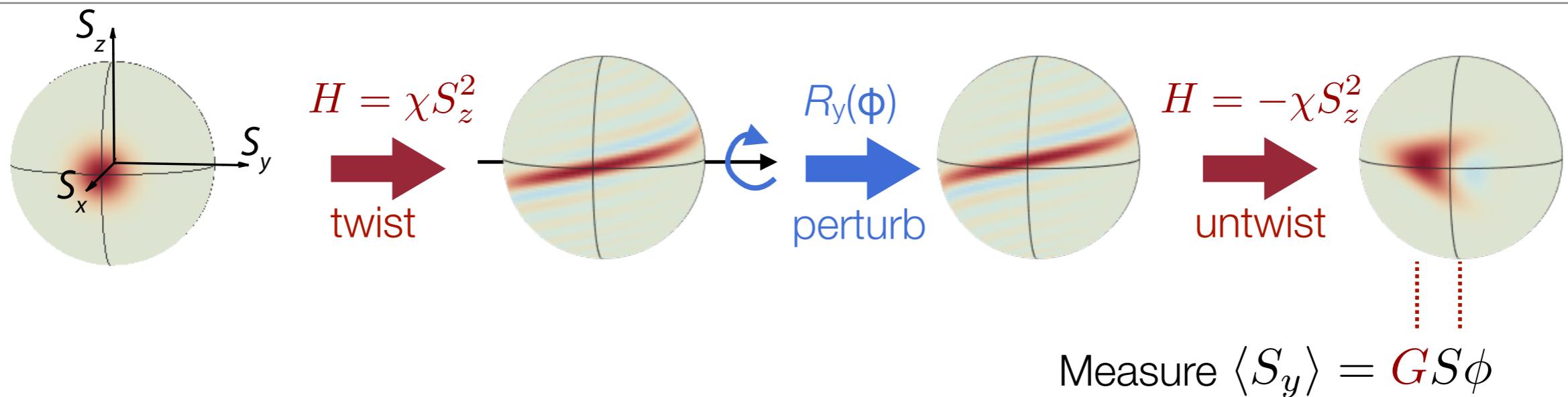
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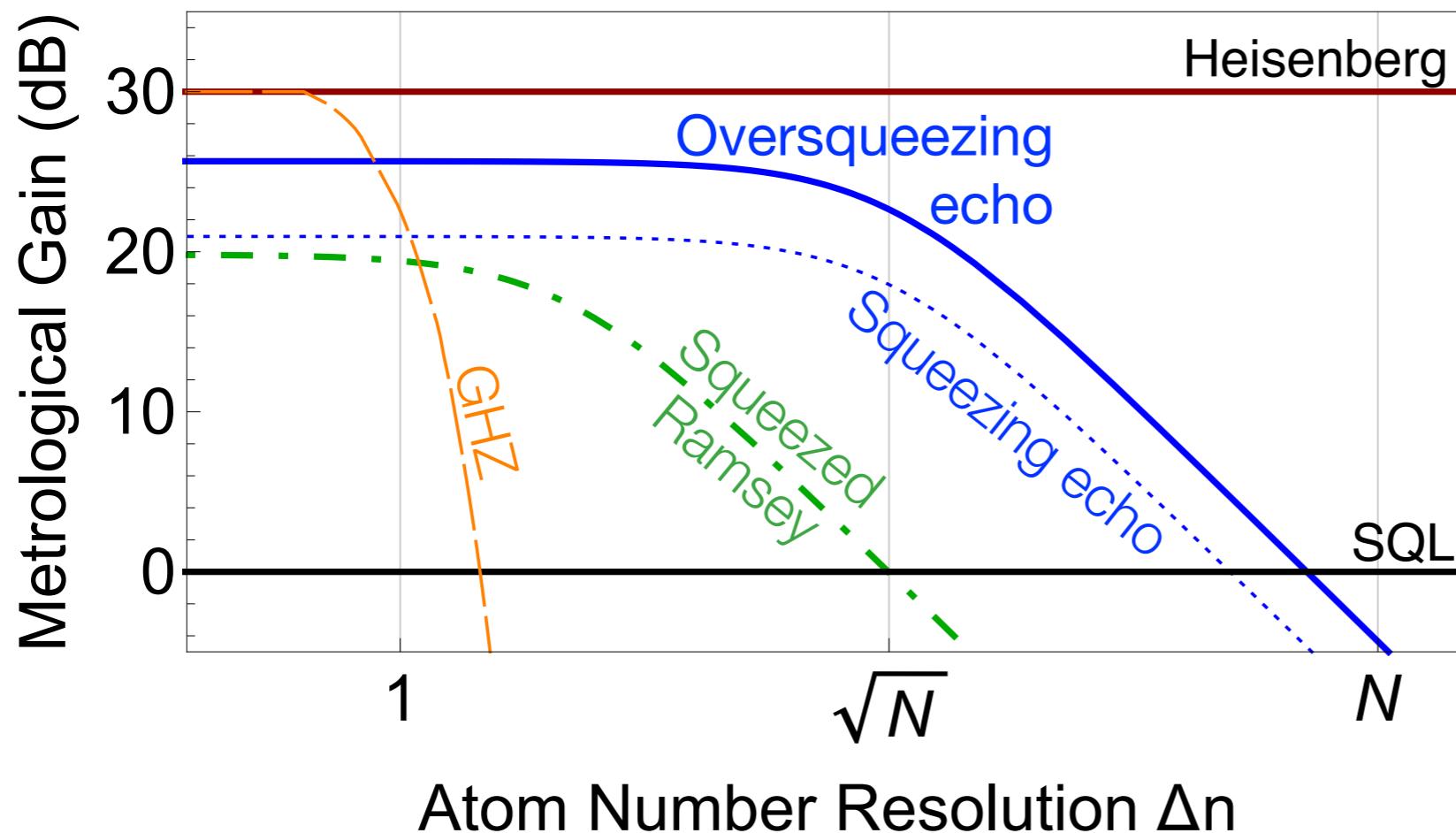
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One-Axis Twisting Echo

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PRL **116**, 053601 (2016).

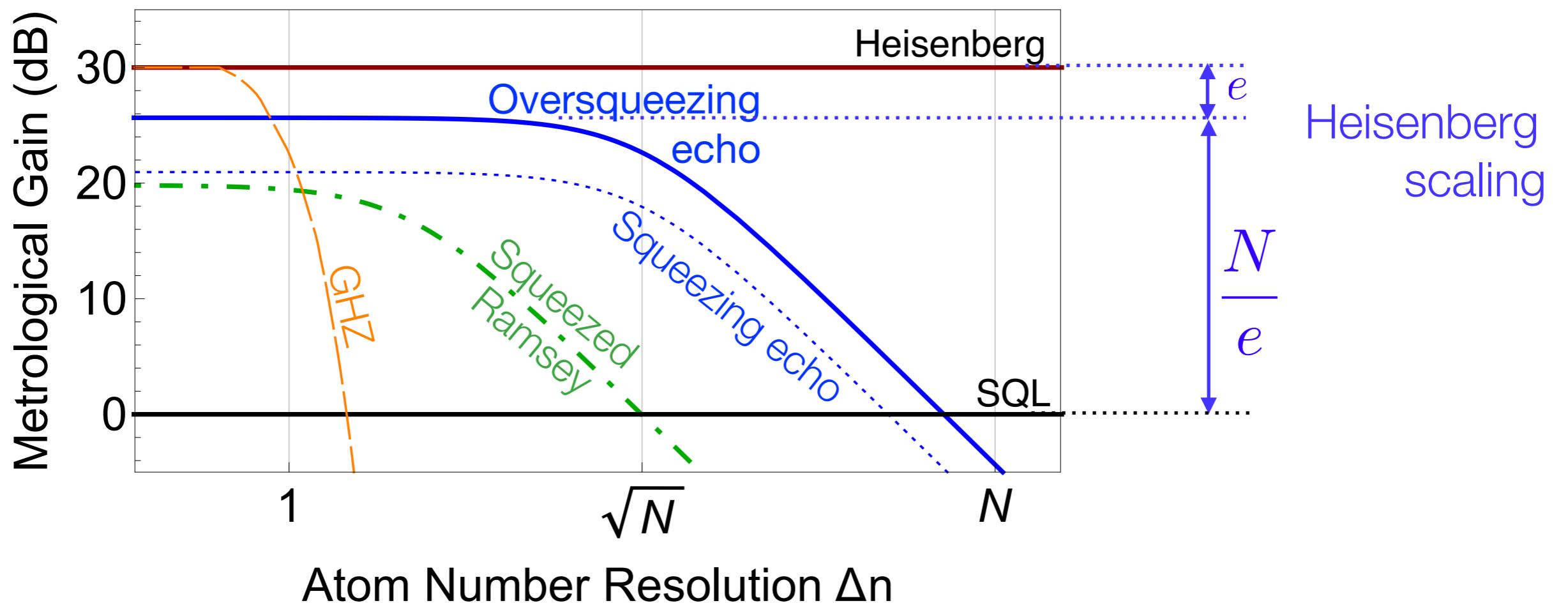
- Heisenberg scaling $\Delta\phi = \sqrt{e}/N$ reached after short twisting time
- Measurement resolution $\Delta S_{\text{meas}} \lesssim \sqrt{N}/2$ suffices!



One-Axis Twisting Echo

E. Davis, G. Bentsen, & MS-S,
PRL **116**, 053601 (2016).

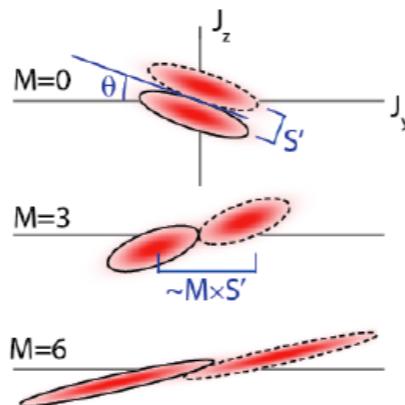
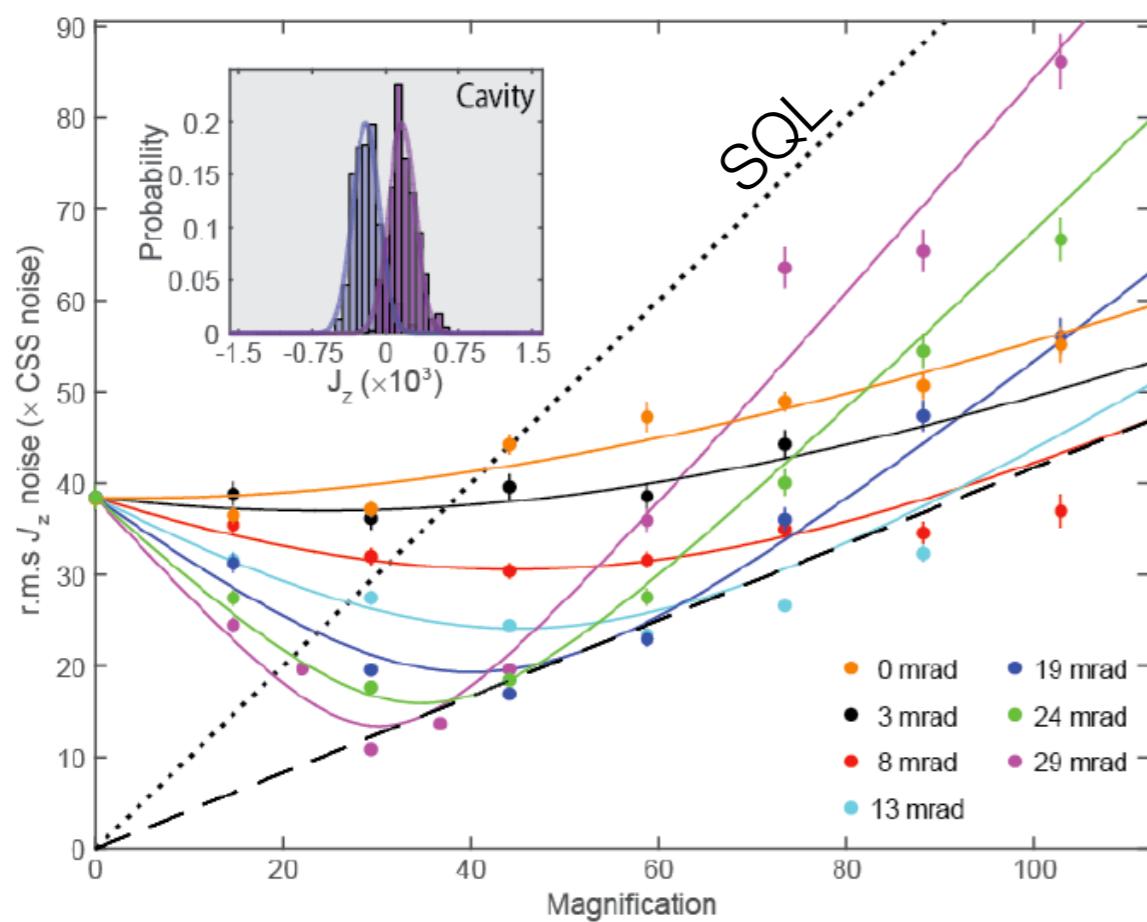
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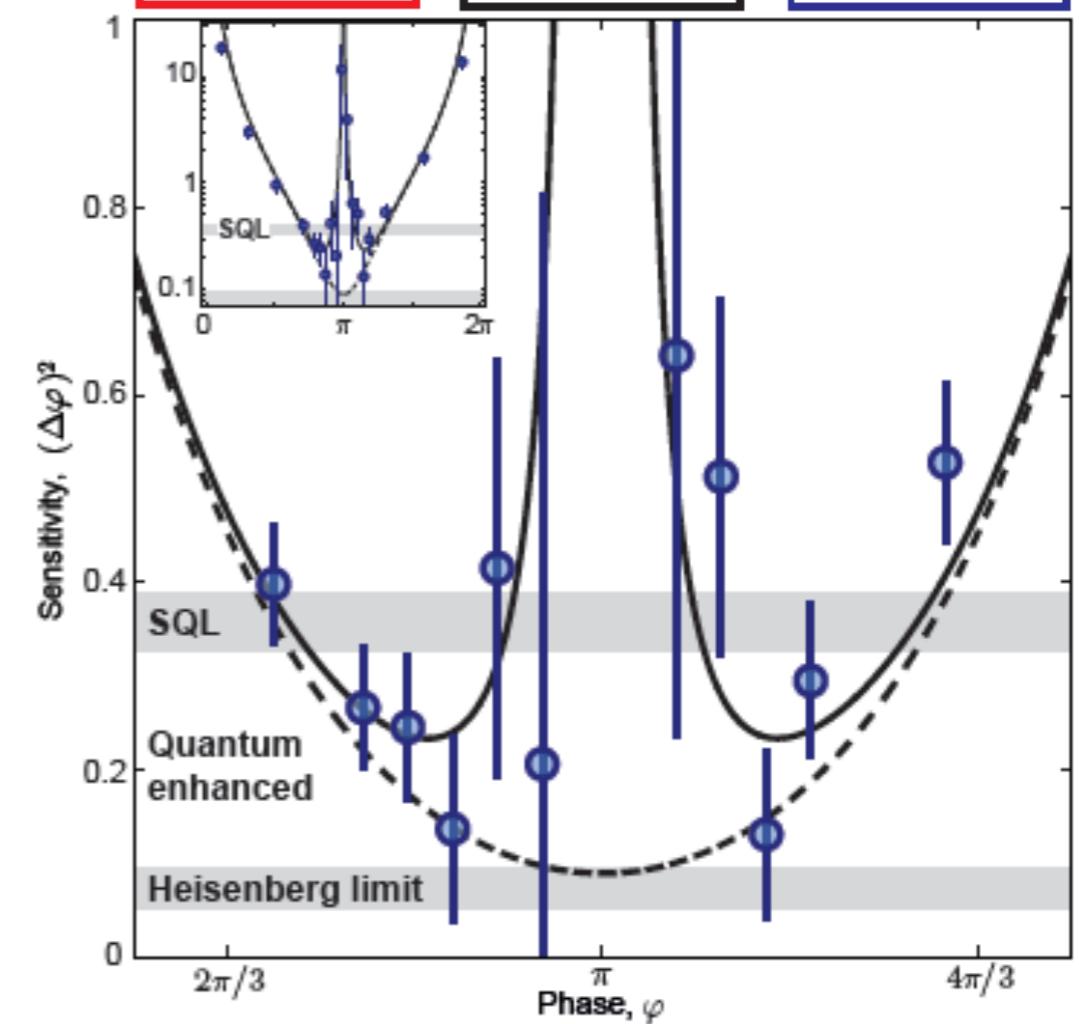
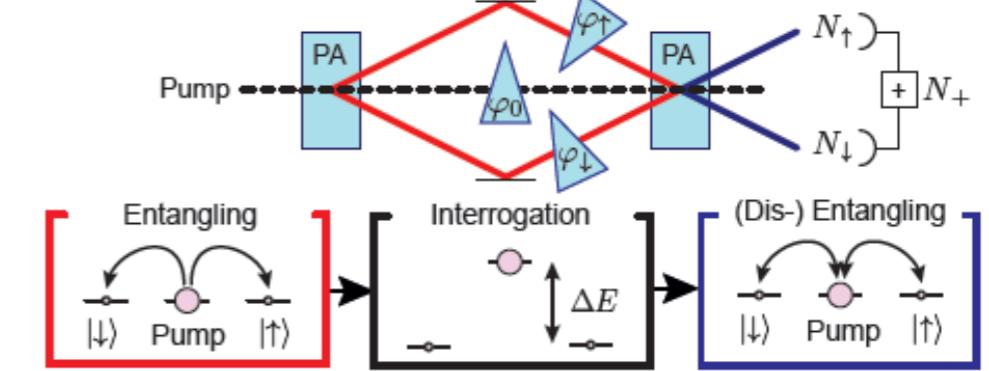
Interaction-Based Readout: Demonstrations

Hosten, Krishnakumar, Engelson & Kasevich,
Science (2016).

8 dB squeezing detected
with low-resolution
fluorescence imaging



Linnemann, Strobel, Muessel, Schulz,
Lewis-Swan, Kheruntsyan, & Oberthaler,
PRL 117, 013001 (2016).



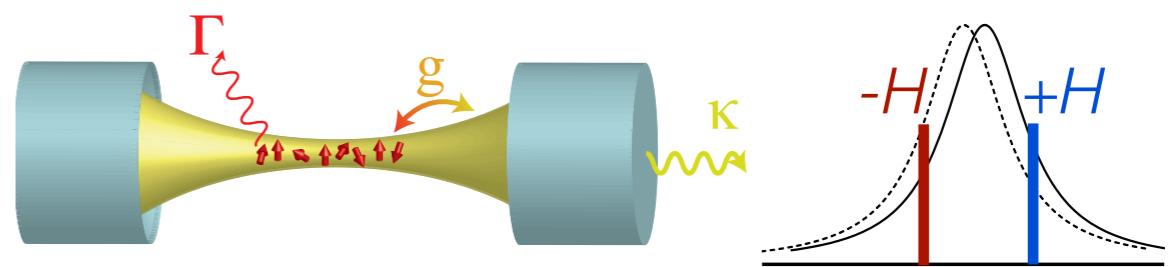
Oversqueezing Echo: Implementations?

Requirement: coherent interactions of switchable sign

Ion Penning trap

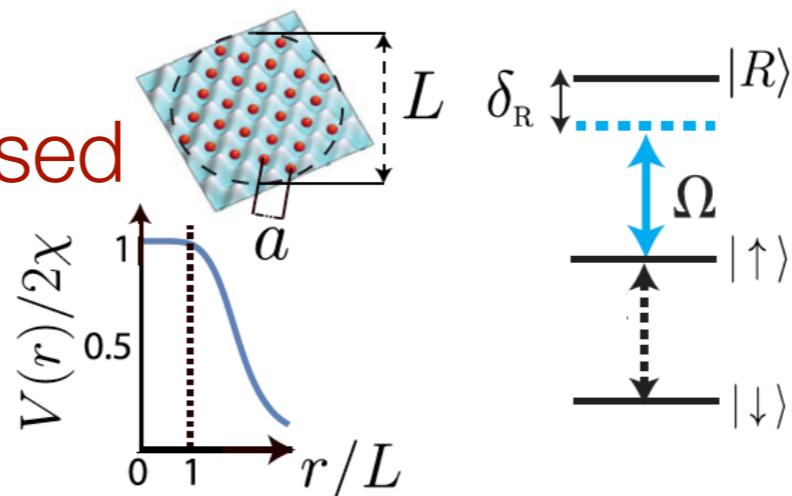


Gärttner, Bohnet, Safavi-Naini, Wall,
Bollinger, & Rey, *Nat. Phys.* (2017).



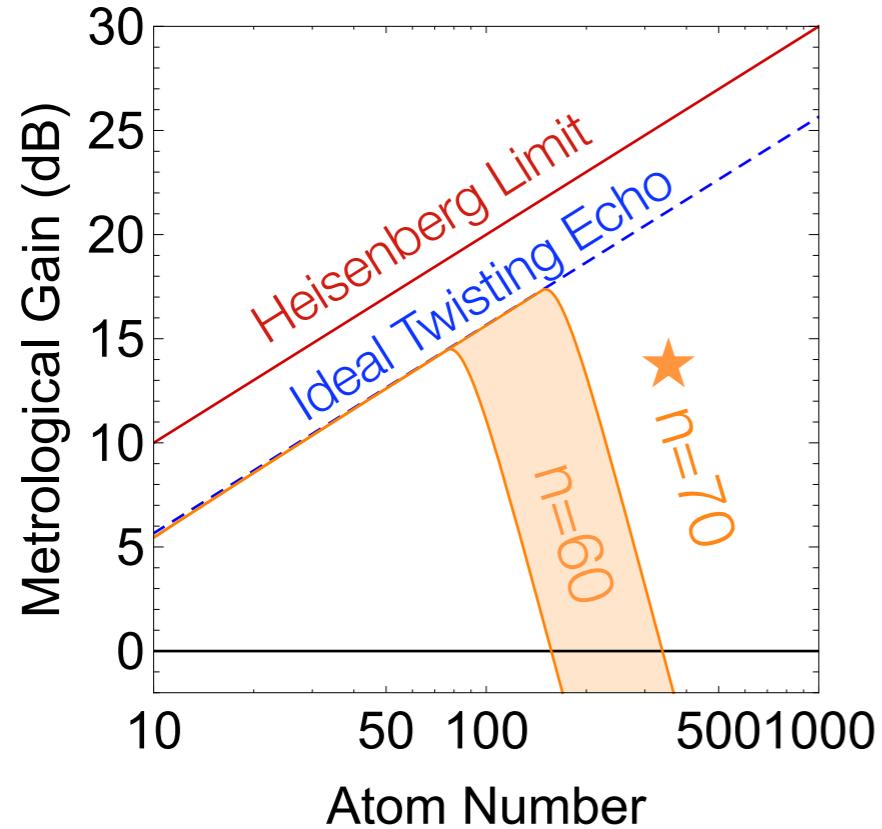
Atoms in strong-coupling cavity
Photon-mediated interactions

Rydberg-dressed
atoms



Prospects for Quantum Metrology

...by Rydberg dressing

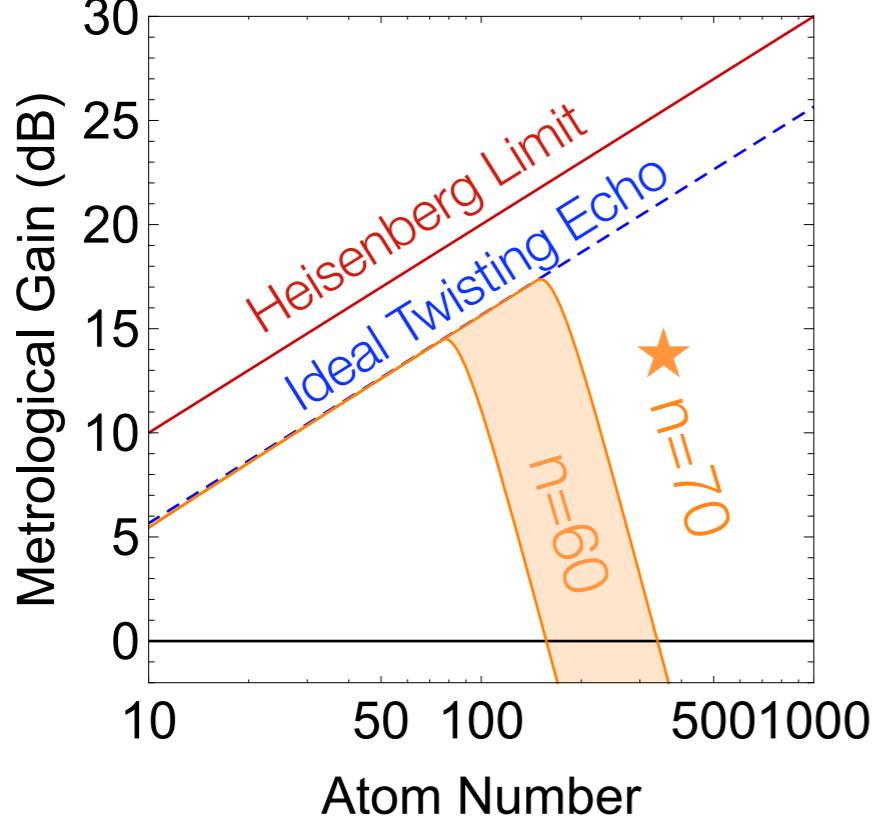


★ 200 entangled atoms with sensitivity
matching $\sim 10^4$ unentangled atoms

Inspiration: “Spin squeezing in a Rydberg lattice clock,”
Gil, Mukherjee, Bridge, Jones & Pohl, *PRL* (2014).

Prospects for Quantum Metrology

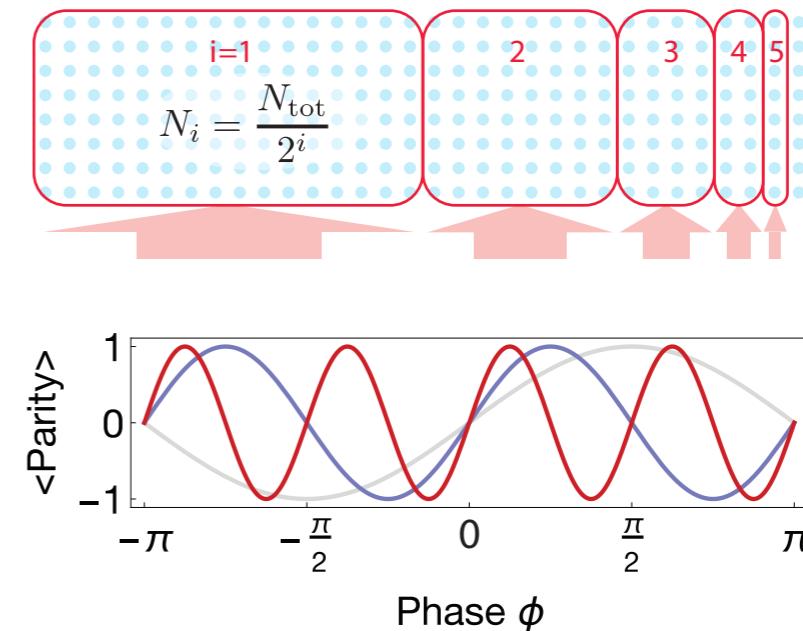
...by Rydberg dressing



★ 200 entangled atoms with sensitivity matching $\sim 10^4$ unentangled atoms

Inspiration: “Spin squeezing in a Rydberg lattice clock,”
Gil, Mukherjee, Bridge, Jones & Pohl, *PRL* (2014).

Arrays of entangled ensembles?



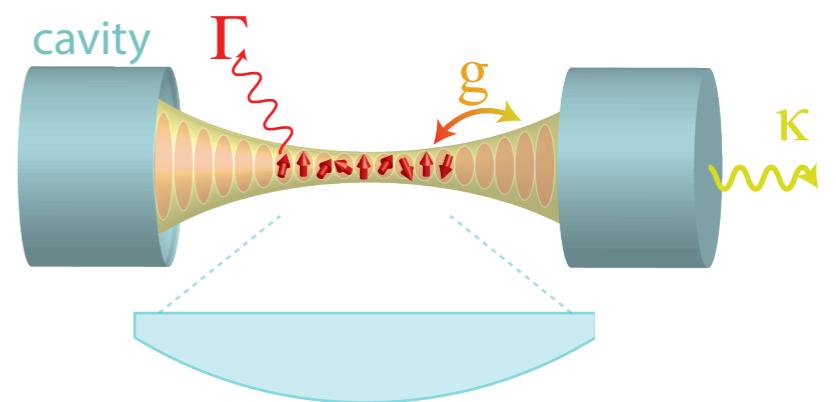
- tracking local oscillator phase in clock
Kessler, ..., Sorensen, Ye, Lukin, *PRL* (2014).
- broadband sensing
- spatially resolved sensing

Outline

✓ Motivation and Background

Quantum metrology

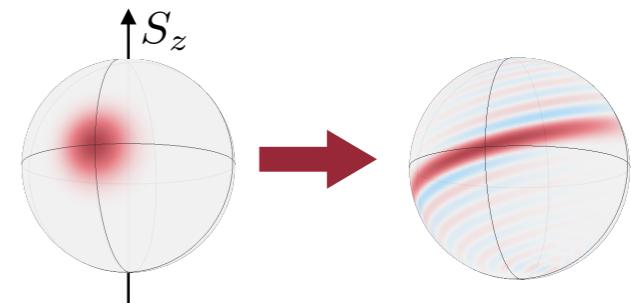
Entangling atoms with photons



✓ Seeking the Heisenberg Limit

Engineering entanglement in a dissipative world

Harnessing entanglement in a noisy world

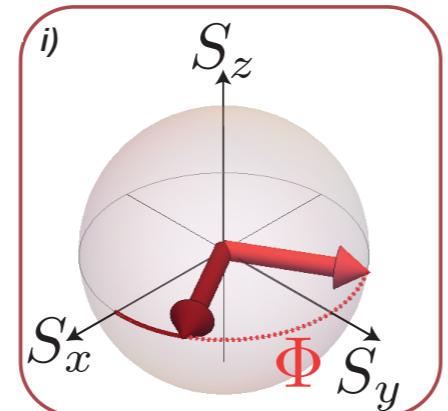
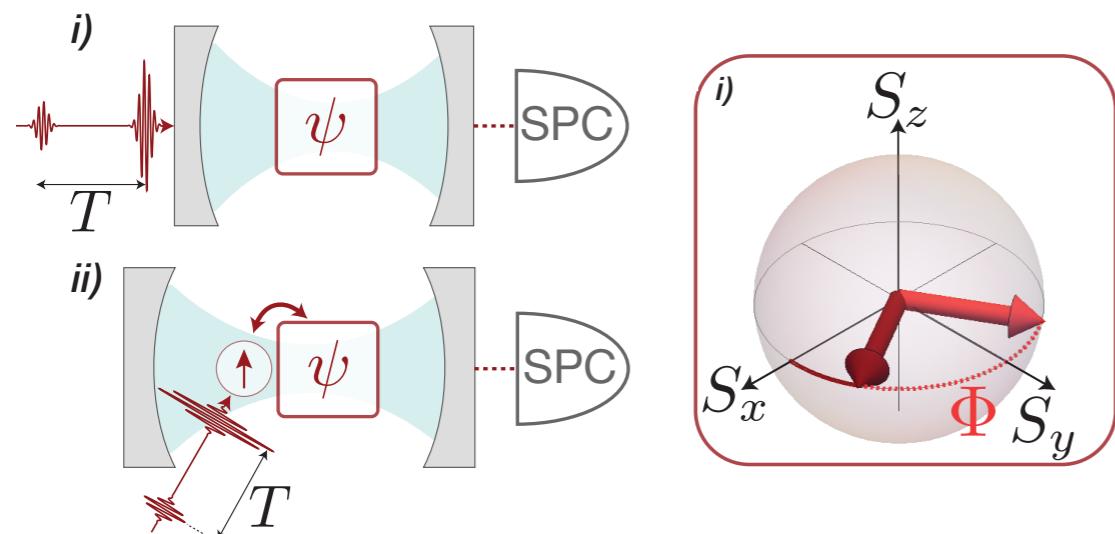


Summary & Outlook

Quantum Engineering in an Imperfect World

Harnessing entangled states in spite of detection noise:
Echo spectroscopy with over-squeezed, non-Gaussian states

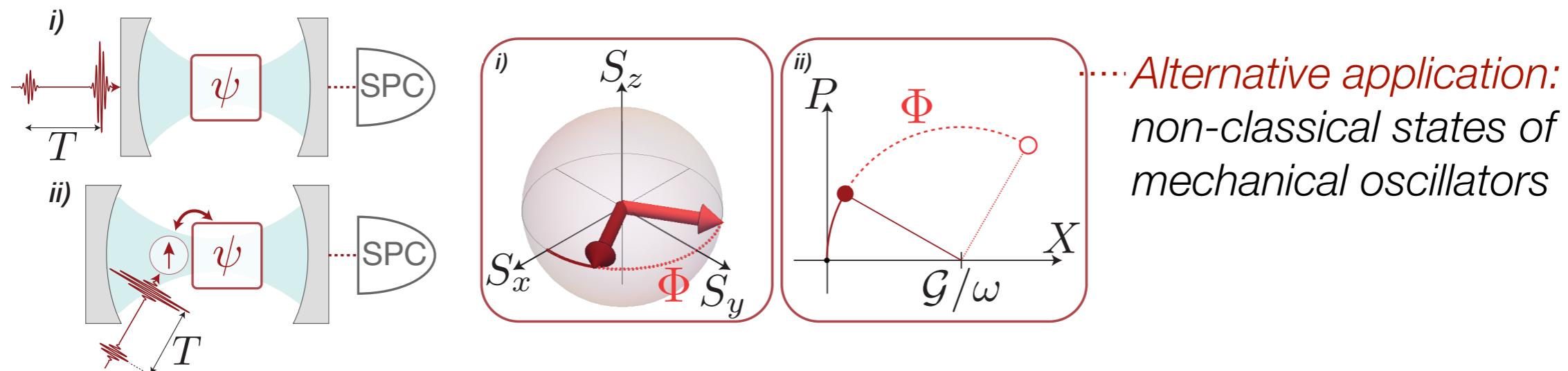
Engineering entangled states in spite of dissipation:
Single-photon paintbrush with robustness to photon loss



Quantum Engineering in an Imperfect World

Harnessing entangled states in spite of detection noise:
Echo spectroscopy with over-squeezed, non-Gaussian states

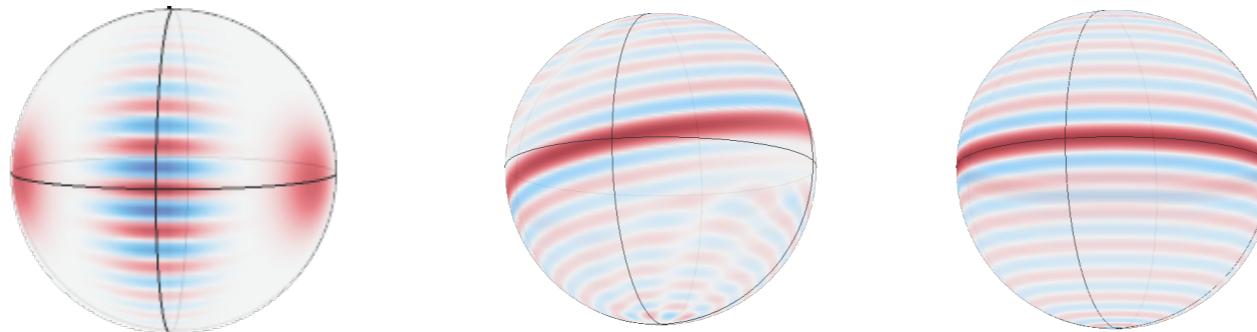
Engineering entangled states in spite of dissipation:
Single-photon paintbrush with robustness to photon loss



Summary

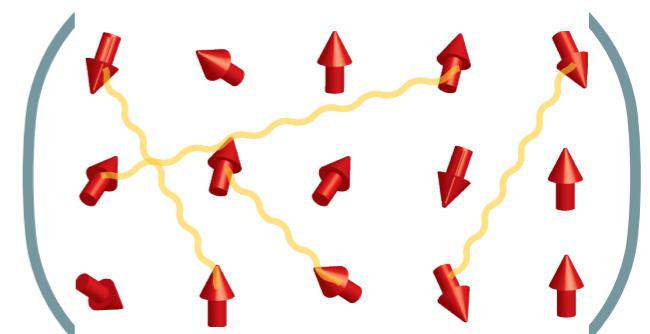
Atomic clocks and sensors have surpassed the Standard Quantum Limit, but still are **far from the Heisenberg Limit**

Which entangled states to use, how to generate, how best to detect?
Many open questions, but we are making progress!



Atom-light interactions provide a versatile toolbox

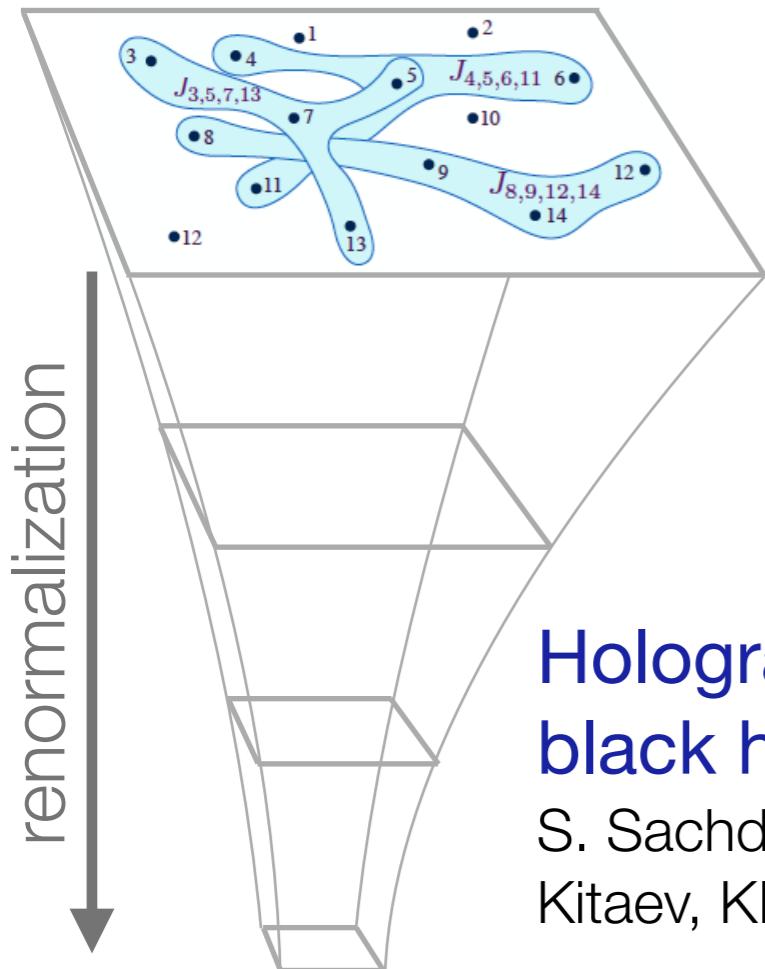
- near-term applications in atomic clocks
- advancing control & understanding of entanglement



Outlook: Quantum Simulation

Fermions
with non-local hopping

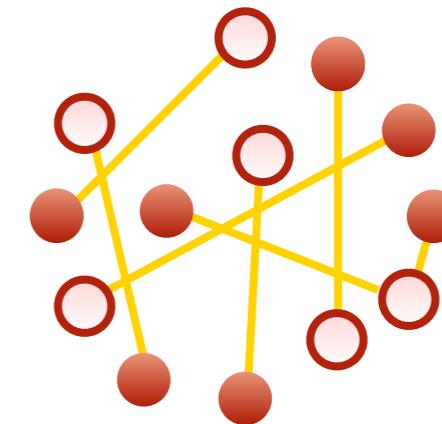
$$H = \frac{1}{(2N)^{3/2}} \sum_{i,j,k,\ell=1}^N J_{ij;k\ell} c_i^\dagger c_j^\dagger c_k c_\ell$$



Holographic dual:
black hole
S. Sachdev, *PRX* (2015).
Kitaev, KITP (2015).

Hard-core bosons
with non-local hopping?

$$H \propto \sum_{i,j} J_{ij} \sigma_+^i \sigma_-^j$$



Natural approach:
bosons = spin excitations,
hopping mediated by light

Acknowledgements



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Lukas Homeier



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Brian Swingle

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Andrew Daley

Amir Safavi-Naeini

Zhaoyou Wang

Past visitors

Anna Wang

Thomas Reimann

Sebastian Scherg



Extras

Fidelity of Single-Photon Paintbrush

Fidelity of Single-Photon Paintbrush

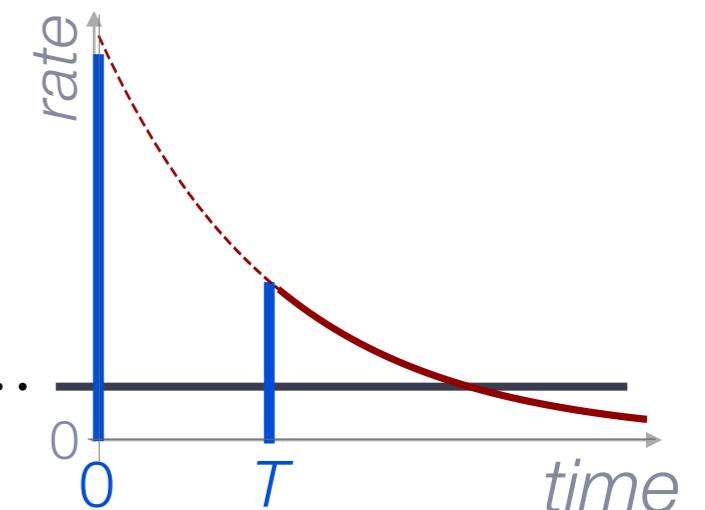
For weak input pulse, conditioned on detecting a single photon:
perfect fidelity even in presence of cavity losses & atomic scattering

Fidelity of Single-Photon Paintbrush

For weak input pulse, conditioned on detecting a single photon:
perfect fidelity even in presence of cavity losses & atomic scattering

Real-world limitations:

- Precession time T limited by competition between heralding rate and **dark counts of detector**

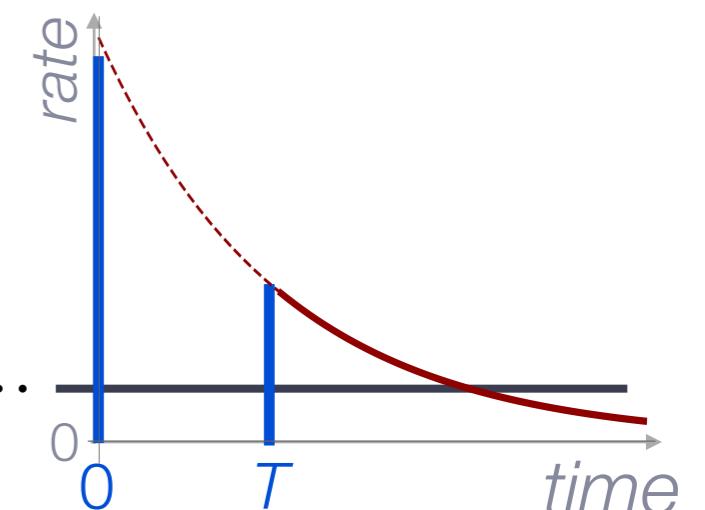


Fidelity of Single-Photon Paintbrush

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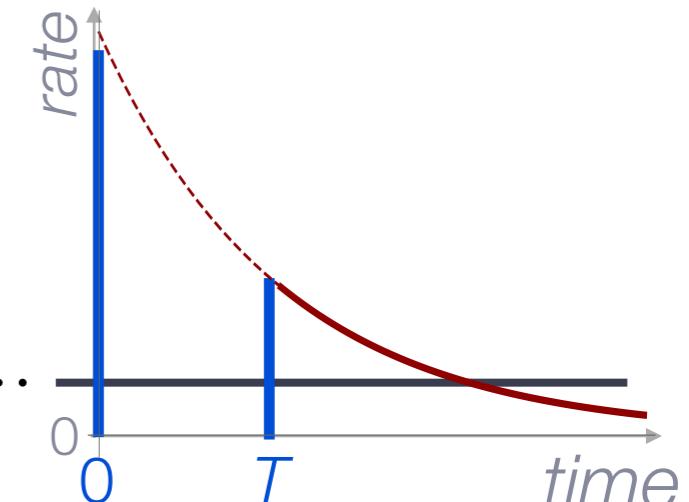
- Precession time T limited by competition between heralding rate and **dark counts of detector**
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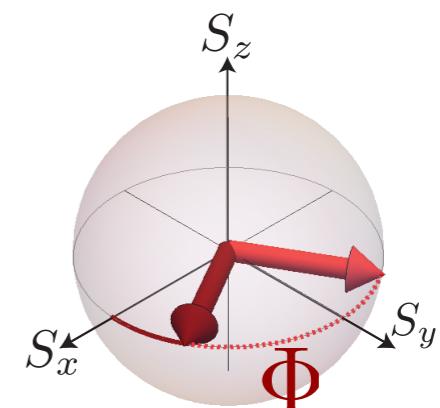
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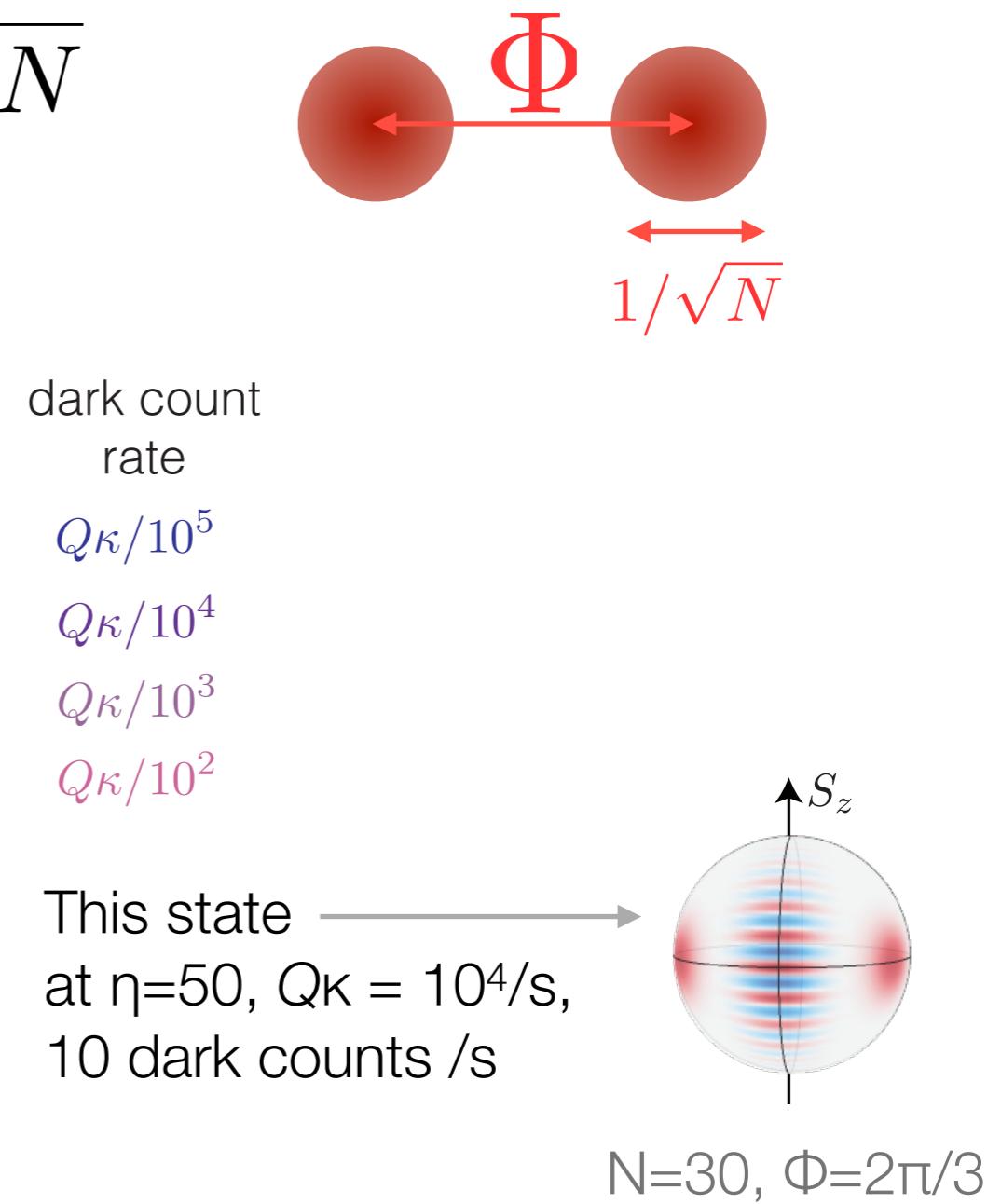
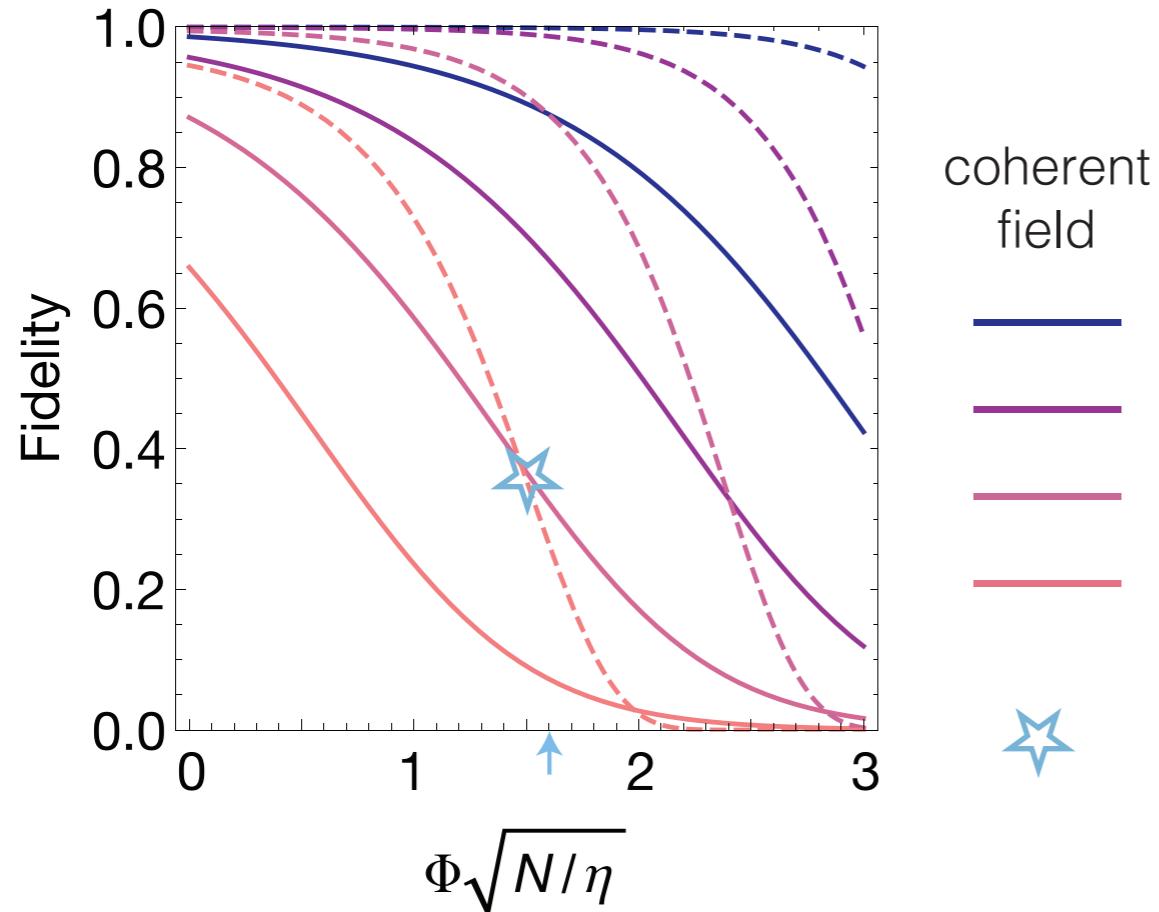
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Cooperativity η sets practical limit to phase $\Phi \equiv \Omega T$



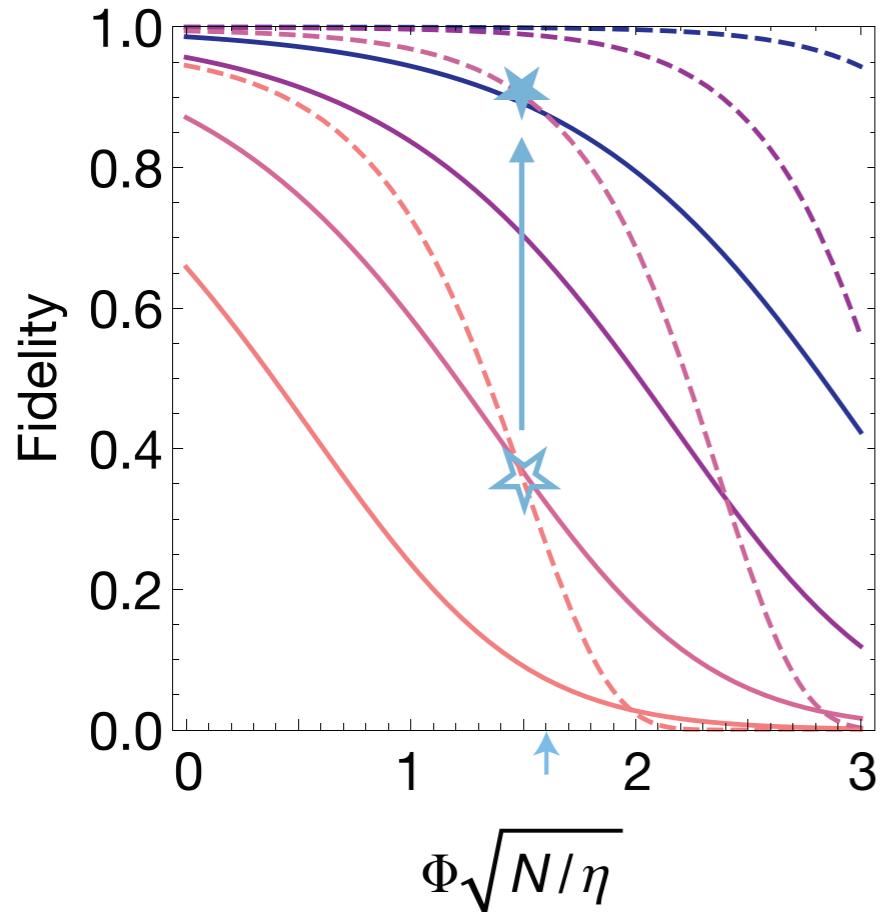
Cat Size vs. Cooperativity

“Size” of the cat quantified by $\Phi\sqrt{N}$



Cat Size vs. Cooperativity

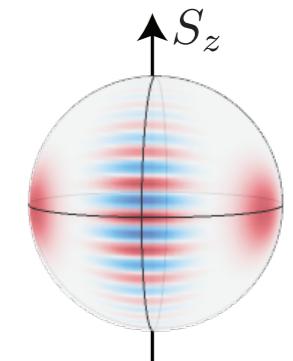
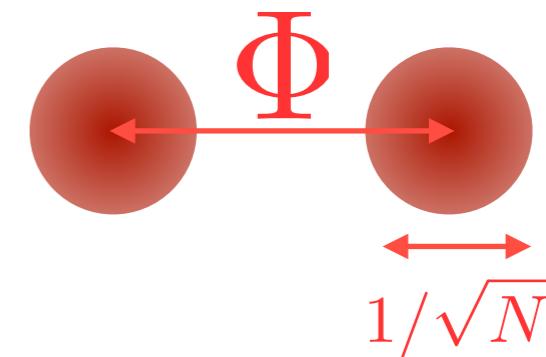
“Size” of the cat quantified by $\Phi\sqrt{N}$



coherent field	single photon	dark count rate
Q\kappa/10^5	solid dark blue	$Q\kappa/10^5$
Q\kappa/10^4	dashed purple	$Q\kappa/10^4$
Q\kappa/10^3	dashed pink	$Q\kappa/10^3$
Q\kappa/10^2	dashed red	$Q\kappa/10^2$



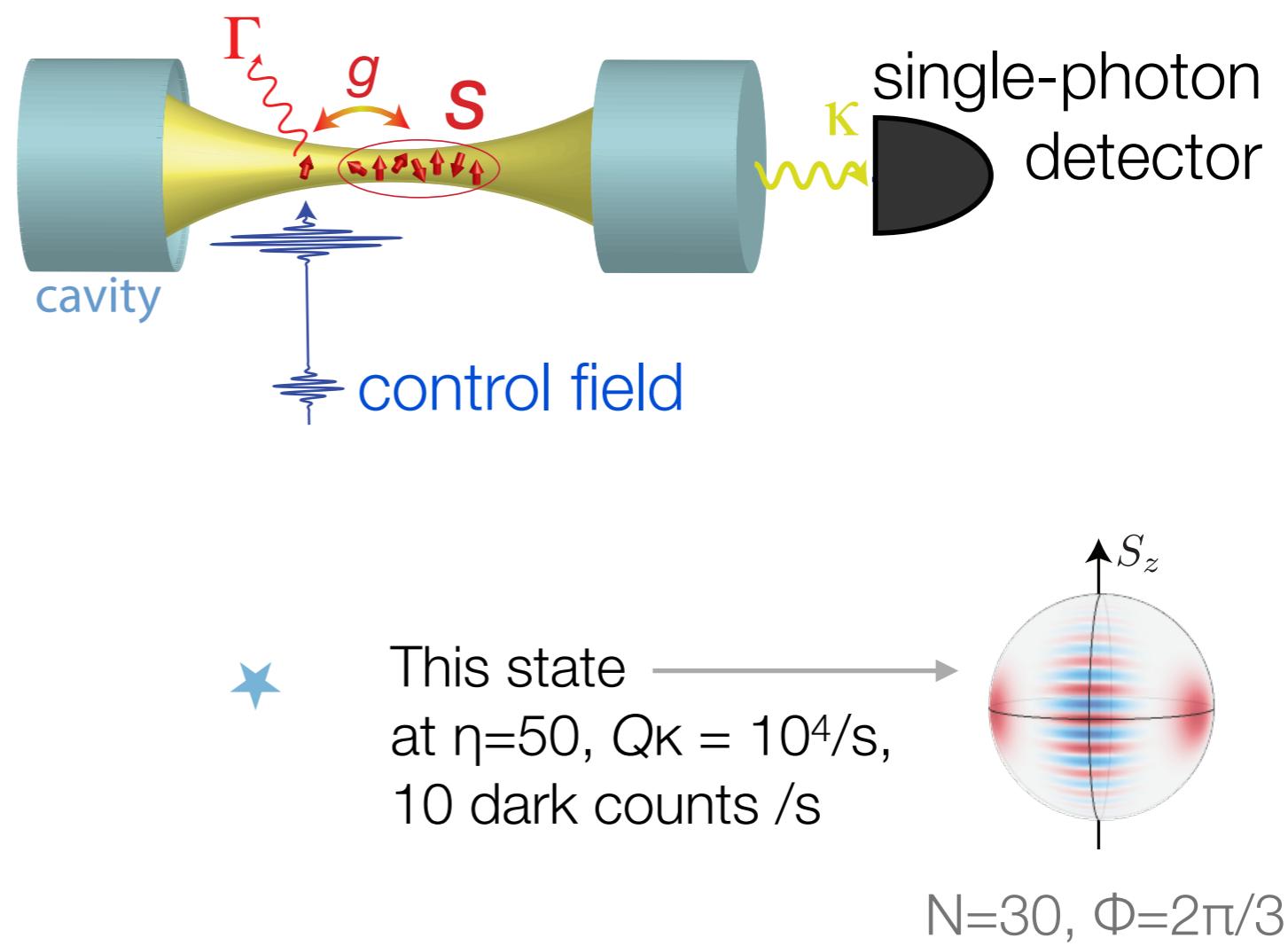
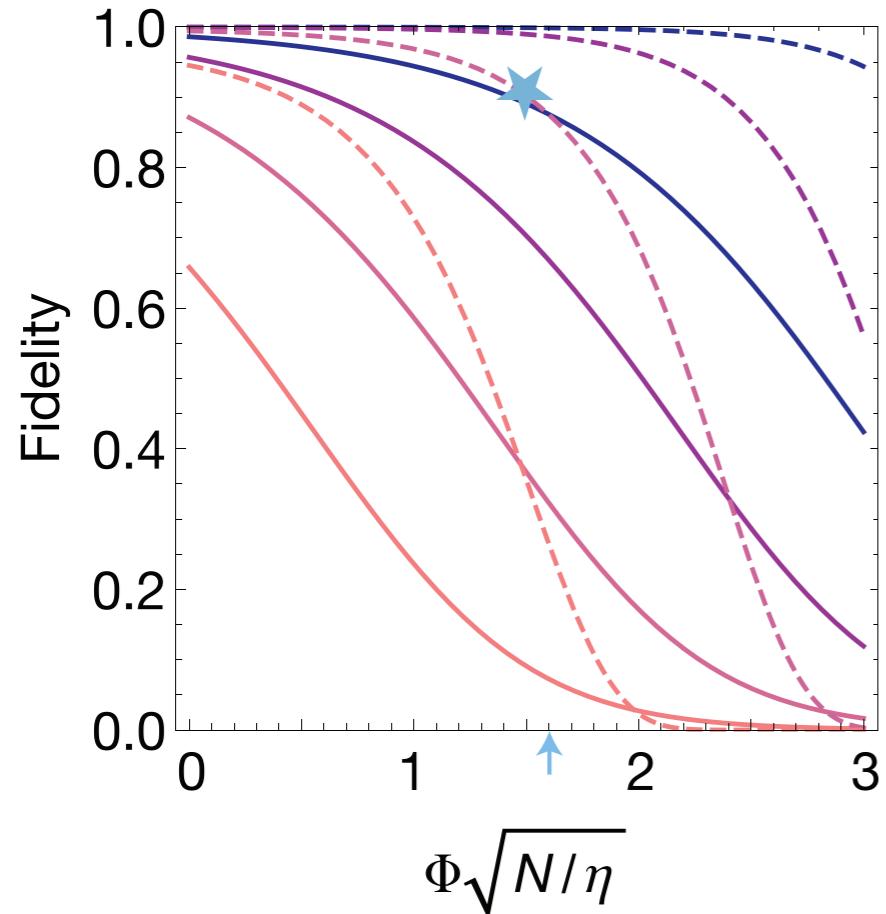
This state
at $\eta=50$, $Q\kappa = 10^4/s$,
10 dark counts /s



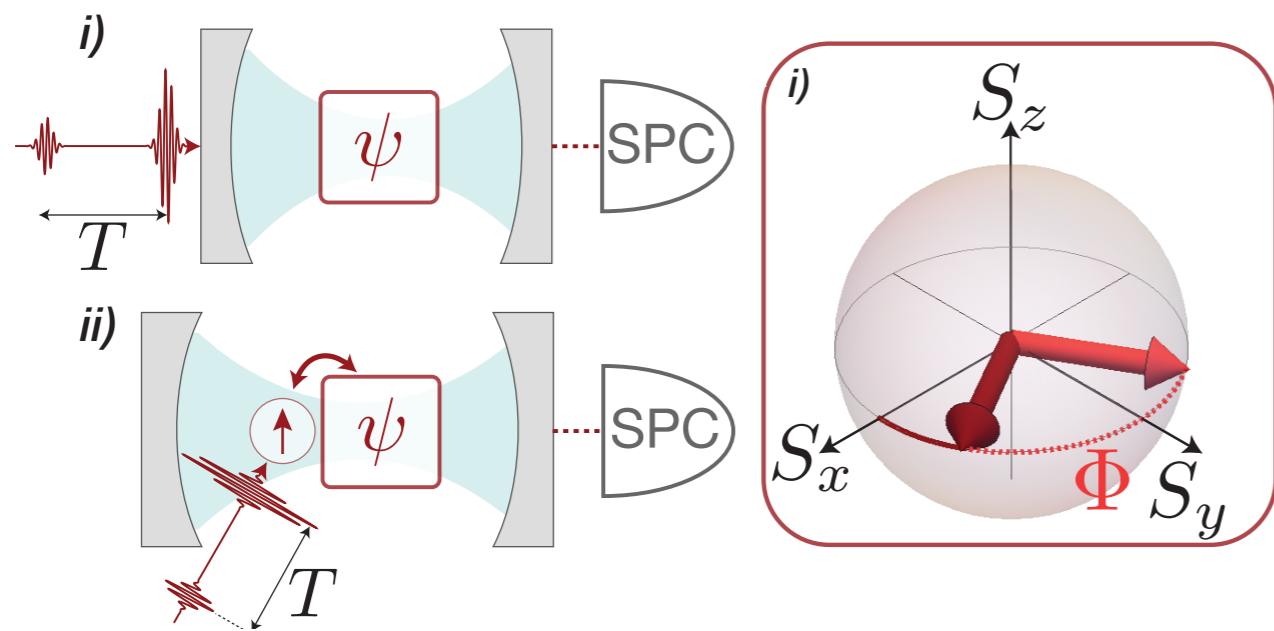
$N=30$, $\Phi=2\pi/3$

Cat Size vs. Cooperativity

“Size” of the cat quantified by $\Phi\sqrt{N}$

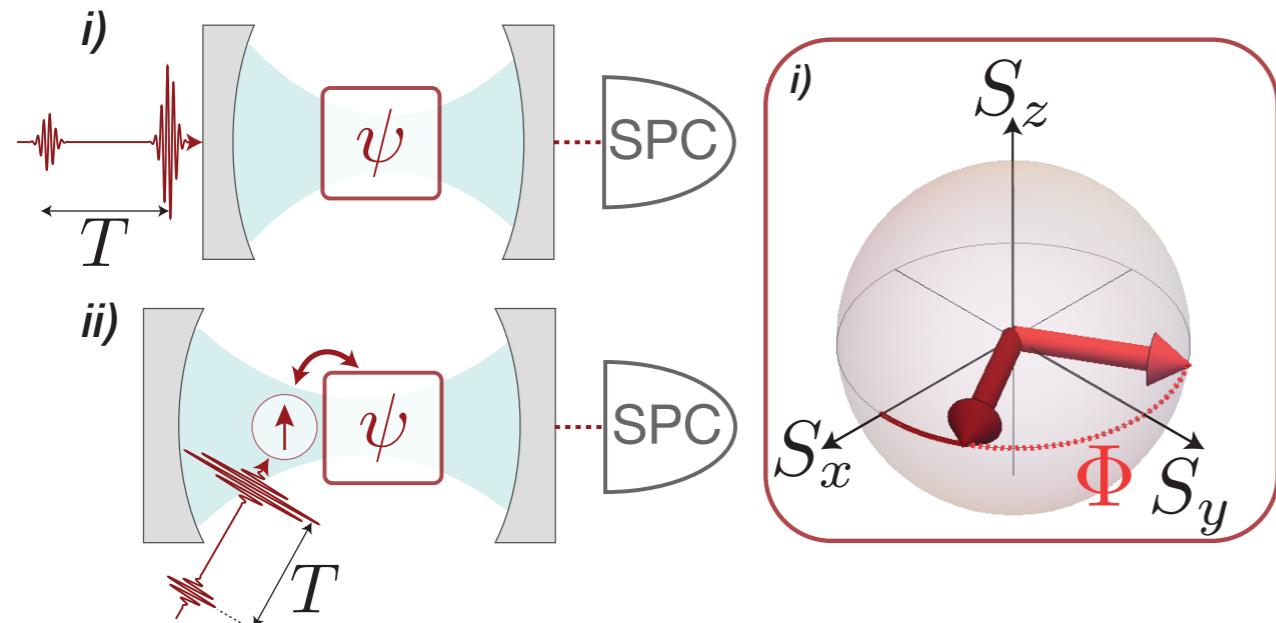


Painting Summary & Outlook



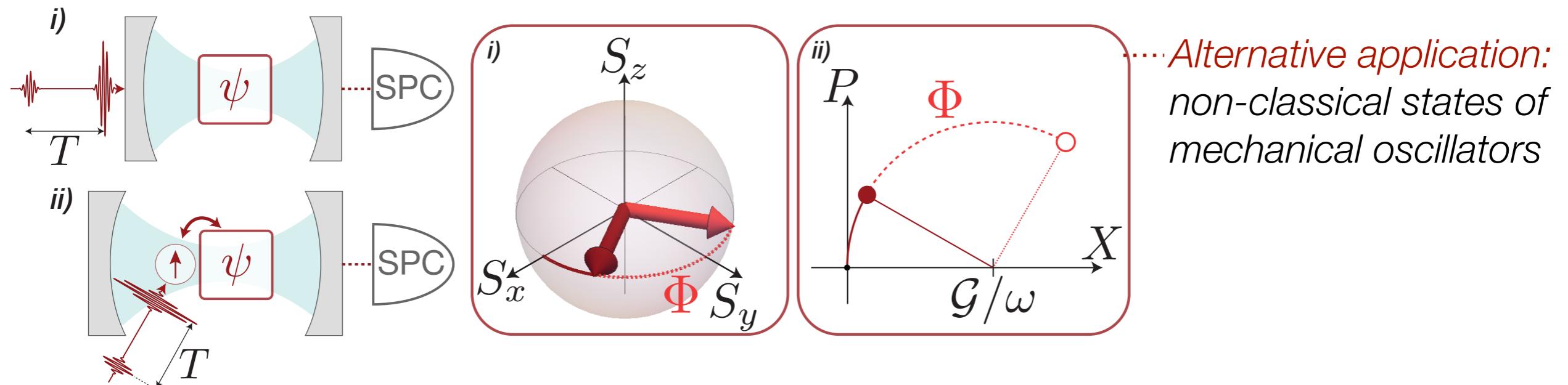
Painting Summary & Outlook

- Time-shaped photon “paints” the target state, heralded by detection
- Perfect fidelity even in the presence of loss (till limited by dark counts)



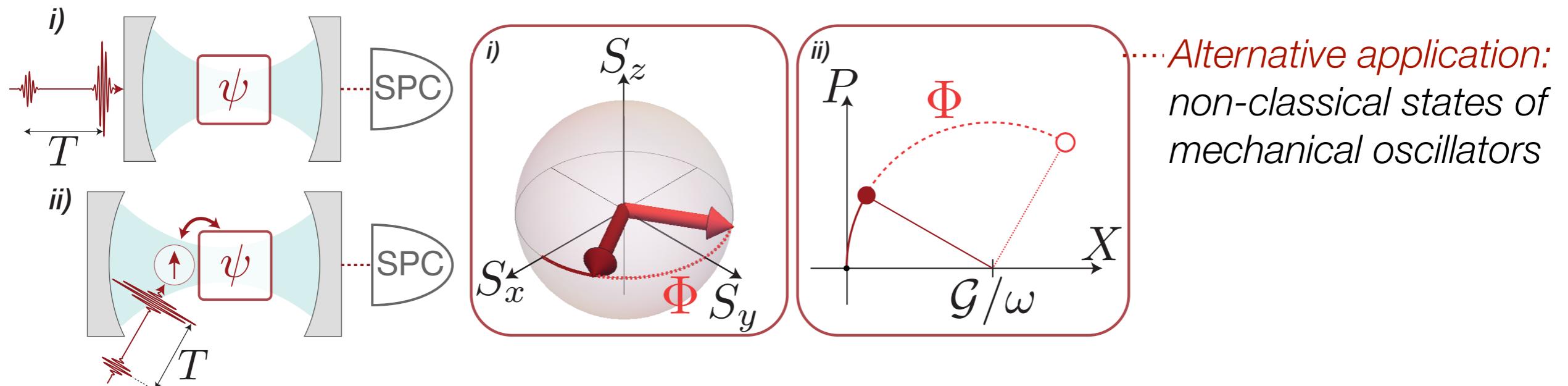
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Painting Summary & Outlook

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Outlook: simulating novel interactions conditioned on photodetection?