Precision Muon Physics

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- Muon primer
- Muons in support of the Standard Model
- Muons challenging the Standard Model
- Unique, "single purpose" experiments
 - Generally, do only 1 thing, but <u>very well</u>
 - I will emphasize why this is necessary



Muon Primer

• Mass ~ 207 m_e



- $(m_{\mu}/m_{e})^{2} \approx 43,000$ times more sensitive to "new physics" through quantum loops compared to electrons (taus would be better!)
- Lifetime ~2.2 μs
 - High-intensity beams; can stop and study; can possibly collide
- Primary production: $\pi^+ \rightarrow \mu^+ \nu_{\mu}$
 - Polarized naturally:



- Primary decay $\mu^+ \rightarrow e^+ \nu_e \overline{\nu}_{\mu}$
 - Purely weak; distribution in θ and *E* reveals weak parameters
- Lepton number is conserved



Establishing SM Parameters









Fermi Constant

Muonic "1-electron hydrogen-like" Atoms

- μ⁻p, μ⁻d, μ⁻A
 - Charge radius of proton,
 - Measure 2S \rightarrow 2P transition in μ -p
 - Which is related to r_p in clean way





 $\Delta E(2S - 2P) = 209.978(5) - 5.226 r_{\rm p}^2 + 0.0347 r_{\rm p}^3 \quad \text{meV}$

ΔE larger than expected \rightarrow proton is smaller by 3 – 5 σ .

- **µp results wrong**? (no, see next slide)
- ep scattering results wrong? (can check)
- Novel BSM physics between μ and e interactions ?
 - Possibly related to this puzzle and to g-2, but very constrained

Bottom line: No clear resolution yet



The Muonic Lamb shift method is robust

- 1. Stop μ^{-} in hydrogen
- 2. ~1% of μp arrive in 2S atomic state ... lifetime there ~1 μs
- 3. Trigger laser to excite $2S \rightarrow 2P$ transition
 - ... occurs only if laser frequency is at correct $\Delta \textbf{E}$
- 4. 2P de-excites to 1S

... emits 2 keV X-ray as "tag"



Update: 2013



Additional transitions: Proton Structure from the Measurement of 2S-2P Transition Frequencies of Muonic Hydrogen Science 25 January 2013:

MUSE: µp Scattering at PSI

Direct test of µp versus ep interactions in a scattering experiment Approved at PSI

MUSE Test Run Report

The MUon proton Scattering Experiment collaboration (MUSE):

W.J. Briscoe,¹ K. Deiters,² E. Downie,¹ R. Gilman,³ K.E. Myers,³ E. Piasetzsky,⁴ D. Reggiani,² P. Reimer,⁵ G. Ron,⁶ V. Sulkosky,⁷ and M. Taragin⁸

Muon Lifetime

Fundamental electro-weak couplings





MuLan Collaboration PRL 106, 041803 (2011) Phys. Rev. D 87, 052003 (2013)

Implicit to all EW precision physics

 $9 \text{ ppm} \rightarrow 0.5 \text{ ppm}$

G_F

$$rac{G_{
m F}}{\sqrt{2}}=rac{g^2}{8M_{
m W}^2}\left(1+\Delta r(m_{
m t},m_{
m H},\ldots)
ight)$$



 M_{7}



Uniquely defined by muon decay

$$\frac{1}{\tau_{\mu^+}} = \frac{{\pmb G_{\rm F}}^2 m_{\mu}^5}{192 \pi^3} \left(1 + {\pmb q}\right) \label{eq:Theta}$$
 QED



Extraction of G_F from τ_u : 1999 two-loop calc. reduced error from 15 to ~0.2 ppm



Detector has symmetric design around stops

Muon lifetime / Fermi constant



The most precise particle or nuclear or atomic lifetime ever measured

 τ (R06) = 2 196 979.9 ± 2.5 ± 0.9 ps τ (R07) = 2 196 981.2 ± 3.7 ± 0.9 ps

 τ (Combined) = 2 196 980.3 ± 2.2 ps (1.0 ppm) $\Delta \tau$ (R07 – R06) = 1.3 ps

New G_F (30x improved since 1999 PDG)

 $G_{F}(MuLan) = 1.166 378 7(6) \times 10^{-5} \text{ GeV}^{-2}$ (0.5 ppm)



The lifetime is also used in a precision "capture" campaign when compared to μ in p and d targets,



$$\Lambda_{S} = \Lambda_{\mu^{-}} - \Lambda_{\mu^{+}} = (\tau_{\mu^{-}})^{-1} - (\tau_{\mu^{+}})^{-1} \Longrightarrow \mathbf{g}_{\mathbf{P}}$$

Muon Capture on the proton and Axial Nucleon Structure $\mu^- + p \to n + \nu_\mu$

Capture rate
$$\Lambda_{\mathbf{S}}$$
:

$$\mathcal{M} = \frac{-iG_F V_{ud}}{\sqrt{2}} \overline{u}(p_{\nu})\gamma_{\alpha}(1-\gamma_5)u(p_{\mu})\overline{u}(p_f)\tau_{-} [V^{\alpha} - A^{\alpha}] u(p_i)$$
Lorentz, T invariance gives these possibilities
$$V_{\alpha} = g_V(q^2)\gamma_{\alpha} + \frac{i g_M(q^2)}{2M_N} \sigma_{\alpha\beta} q^{\beta}$$

$$A_{\alpha} = g_A(q^2)\gamma_{\alpha}\gamma_5 + \frac{g_P(q^2)}{m_{\mu}} q_{\alpha}\gamma_5$$

How does Λ_{s} depend on precision of the form factors ?



$$\frac{\Delta \Lambda_s}{\Lambda_s} = 1\% \quad \Rightarrow \quad \frac{\Delta g_P}{g_P} \approx 6.1\%$$

The least well known is g_P

Technique: Lifetime in ultra-pure hydrogen TPC



1st Precise and Unambiguous Result Verifies Basic Prediction of Low-Energy QCD 16 Phys.Rev.Lett. 110 (2013) 012504 ChPT 14 = -0.88m²) 12 RMC 10 g_p(q² : Physics 8 Axis MuCap Avg 6 MuCap is designed to "ignore" this problem OMC λ_{op}^{Th} _Σ Ex1 Ex2 op 'op ዔ λ_{op} ¹²⁰ (10³ s⁻¹) 20 40 80 100 60 140

Horizontal axis represents some not-well-known Mu-Molecular physics

 $g_{P}(MuCap) = 8.06 \pm 0.55$

 $g_{P}(theory) = 8.26 \pm 0.23$

MuSun: muon capture on the deuteron

Goal: Measure rate Λ_d from $\mu d(\uparrow\downarrow)$ to < 1.5 %

Several fundamental astrophysics processes depend on weak interaction in deuterium

Basic solar fusion: $p + p \rightarrow d + e^+ + v$

 $v_e + d \rightarrow p + p + e^-$ (CC) $v_x + d \rightarrow p + n + v_x$ (NC)





Experiment In Progress at PSI

The Muon's Role in Testing the Standard Model



Michel Parameters Anomalous Magnetic Moment Charged Lepton Flavor Violation





Michel Parameters







(well) Beyond Schwinger



Final results from *TWIST*

□ Is muon decay purely V-A?

Sensitive to attractive SM extensions:

L-R symmetric models, which would permit a W_R

Basic idea:

- □ Measure the energy and angular of e⁺ from $\mu^+ \rightarrow e^+ \nu_e \nu_\mu$
- Compare to Monte Carlo



The formalism, "Michel" parameters

- Muon decay parameters ρ , η , $\mathcal{P}_{\mu}\xi$, δ
- ▶ Differential decay rate *vs.* energy and angle:

$$egin{array}{rcl} rac{d^2\Gamma}{dx\;d\cos heta}&=&rac{1}{4}m_\mu W^4_{\mu e}G^2_F\sqrt{x^2-x_0^2}\,\cdot\ &\{\mathcal{F}_{IS}(x,oldsymbol{
ho},oldsymbol{\eta})+\mathcal{P}_\mu\cos heta\cdot\mathcal{F}_{AS}(x,oldsymbol{\xi},oldsymbol{\delta})\}+R.C. \end{array}$$







Final results: "SM still okay"

Mostly constrains right-handed muon terms



A. Hillairet et al., Phys. Rev. D 85, 092013 (2012)

Flagship efforts being mounted at the new Fermilab Muon Campus: g-2 & Mu2e



For g-2, achieves

- 1) Long decay channel
- 2) Rapid ring cycle
- 3) No hadronic flash

For Mu2e, achieves

- 1) Ideal proton bunches for mu formation
- 2) High intensity / Extinction



A Case for Challenging the Standard Model: Muon g-2



a_{μ} (Expt.)=116592089(63)×10⁻¹¹ (0.54 ppm)

Summary of Standard Model Contributions



 $\Delta a_{\mu}(Expt - Thy) = 297 \pm 81 \times 10^{-11}$ 3.6 σ

Three sigma is not enough: Do it better



(Would exceed 7 σ even with modest theory improvements and same Δa_{μ})

$\Delta a_{\mu}(Expt - Thy) = 297 \pm 81 \times 10^{-11}$ 3.6 σ

In search of what?

New physics enters through loops

- Supersymmetry
 - Attractive option that fits data well
- Universal Extra Dimensions,
 - Possible, but ~ 0 for 1 UED
- Dark Photons
 - Many efforts emerging to test this idea
- The Uninvented
 - Perhaps the most important of all







Chirality flipping interactions for mass and charge (moment) terms

$$\mathcal{O} = rac{\delta m_{\mu}(\mathrm{N.P.})}{m_{\mu}}, \quad \delta a_{\mu}(\mathrm{N.P.}) = \mathcal{O}(\mathcal{O}) \left(rac{m_{\mu}}{M}
ight)^{2}$$





q-2

m

 μ_{R}

 $\mu_{R'}$

 μ_{L}

 μ

From D. Stockinger (See many of this g-2 presentations about new physics impact)

SUSY contribution to a_{μ} :



Difficulty to measure at the LHC

Related processes in SUSY

$$\mu^+ \to e^+ \gamma; \ \mu^- + \mathcal{N} \to e^- + \mathcal{N}$$

How have the LHC results affected things?

- No new particles → "SUSY is dead!"
- Wait ... lots of new conversations now
- $H \rightarrow \gamma\gamma$ excess?
 - Connects g-2, dark photons, etc. !
- M_H at 125 GeV... what's compatible
 - Split supersymmetry ?
 - Other models?

Muon g-2 and 125 GeV Higgs in Split-Family Supersymmetry

Masahiro Ibe $^{(a,b)}$, Tsutomu T. Yanagida $^{(b)}$, Norimi Yokozaki $^{(b)}$



Figure 1: Contours of δa_{μ} , the squark mass, the gluino mass, and the lightest slepton mass (the masses are shown in the unit of GeV) on $m_0 - M_{1/2}$ plane. The blue (green) dash-lines correspond to the squark (gluino) masses. The magenta dotted lines show the contours of the lightest slepton masses (from top to bottom, 500 GeV, 250 GeV, 100 GeV). In the orange (yellow) region, δa_{μ} is explained within 1σ (2σ) level. On the left region of the black dot-dashed line, the LSP is a slepton. The stop mass is $\simeq 8.5 (10)$ TeV for $m_3 = 10 (12)$ TeV.

arXiv:1303.6995v1 [hep-pk] 27 Mar 2013

An older but illustrative study connecting SUSY and g-2: The power to resolve among models and break LHC degeneracies



SPS benchmark points

Note: Δa_{μ} centered at 255 here

Method The anomaly is obtained from three well-measured quantities



Polarized muons delivered and stored in the ring at the magic momentum, 3.094 GeV/c







MEG: $\mu \rightarrow e\gamma$ at **PSI**

The SM theory is clear: Unobservable





Signal is back-to-back 53 MeV γ and e^{+} from muons at rest

2013: BR($\mu \rightarrow e\gamma$) < 5.7 x 10⁻¹³ @ 90%C. ... another x4 improvement from 1st results.

New MEG Upgrade approved: Expect to improve by another factor of 10 !

New constraint on the existence of the $\mu^+ \rightarrow e^+ \gamma$ decay

J. Adam,^{1,2} X. Bai,³ A. M. Baldini^a,⁴ E. Baracchini,^{3,5,6} C. Bemporad^{ab},⁴ G. Boca^{ab},⁷ P. W. Cattaneo^a,⁷ G. Cavoto^a,⁸ F. Cei^{ab},⁴ C. Cerri^a,⁴ A. de Bari^{ab},⁷ M. De Gerone^{ab},⁹ T. Doke,¹⁰ S. Dussoni^a,⁴ J. Egger,¹ K. Fratini^{ab},⁹ Y. Fujii,³ L. Galli^a,^{1,4} G. Gallucci^{ab},⁴ F. Gatti^{ab},⁹ B. Golden,⁶ M. Grassi^a,⁴ A. Graziosi,⁸ D. N. Grigoriev,¹¹ T. Haruyama,⁵ M. Hildebrandt,¹ Y. Hisamatsu,³ F. Ignatov,¹¹ T. Iwamoto,³ D. Kaneko,³ P.-R. Kettle,¹ B. I. Khazin,¹¹ N. Khomotov,¹¹ O. Kiselev,¹ A. Korenchenko,¹² N. Kravchuk,¹² G. Lim,⁶ A. Maki,⁵ S. Mihara,⁵ W. Molzon,⁶ T. Mori,³ D. Mzavia,¹² R. Nardò,⁷ H. Natori,^{5,3,1} D. Nicolò^{ab},⁴ H. Nishiguchi,⁵ Y. Nishimura,³ W. Ootani,³ M. Panareo^{ab},¹³ A. Papa,¹ R. Pazzi^{ab},⁴ G. Piredda^a,⁸ A. Popov,¹¹ F. Renga^a,^{8,1} E. Ripiccini,⁸ S. Ritt,¹ M. Rossella^a,⁷ R. Sawada,³ F. Sergiampietri^a,⁴ G. Signorelli^a,⁴ S. Suzuki,¹⁰ F. Tenchini^{ab},⁴ C. Topchyan,⁶ Y. Uchiyama,^{3,1} R. Valle^{ab},⁹ C. Voena^a,⁸ F. Xiao,⁶ S. Yamada,⁵ A. Yamamoto,⁵ S. Yamashita,³ Z. You,⁶ Yu. V. Yudin,¹¹ and D. Zanello^{a8} (MEG Collaboration)

arXiv:1303.0754v1 [hep-ex] 4 Mar 2013



Design for a *unique* signature

4

- e and γ are back-to-back, $\Delta \theta = 180^{\circ}$
- e and γ are simultaneous, $\Delta t = 0$
- $E_e = E_{\gamma} = m_{\mu}/2$



Constraints on New Physics



Muon-to-Electron Conversion: Mu2e



The SM theory also clear: Unobservable (BR: 10⁻⁵⁴)

$$\mathcal{L}_{\text{CLFV}} = \frac{m_{\mu}}{(\kappa+1)\Lambda^2} \bar{\mu}_R \sigma_{\mu\nu} e_L F^{\mu\nu} + \frac{\kappa}{(1+\kappa)\Lambda^2} \bar{\mu}_L \gamma_{\mu} e_L (\bar{u}_L \gamma_{\mu} u_L + \bar{d}_L \gamma_{\mu} d_L)$$



Contributions to µe Conversion



Muon to electron conversion is potentially the most sensitive test for new physics

Images Bernstein

Connection between a_{μ} , EDM and the charged Lepton Flavor Violating transition moment $\mu \rightarrow e$



Method and Goal



- This signature is quite unique
- Goal $R_{\mu\epsilon}$ to < 6 x 10⁻¹⁷ (90% C.L.) – Present is < 7 x 10⁻¹³ \rightarrow So this is <u>very ambitious</u>

How it is done

- Need intense pulsed source of low-energy muons
- Stop in thin AI target
- Form muonic Al atoms.
- Observe
 - 40% will decay "in orbit";
 - 60% will capture (hadronic junk emitted)



This experiment is in R&D and Pre-Construction Mode with CD1 approval

Start date close to 2020





Challenge: find signal above "Decay in Orbit" tail



Similar: COMET in Japan

- Staged approach.
- Approved for Phase-1
 - Sensitivity: < 7x10⁻¹⁵
- Full phase later



Next-generation: $\mu \rightarrow eee$ (2013: approved at PSI)

The SM theory still clear: Unobservable (BR: 10⁻⁵⁰)





- Goal:
 - Finding 1 in 10¹⁶ muon decays



- Special technique
 - High-voltage monolithic active pixel sensors



- The detector
 - Minimum material, maximum precision

Compared to other channels ...



Again, a unique and challenging signature

e

- 2 e⁺, 1 e⁻
- Common vertex
- Common time
- Σ energies = m_{μ}
- No energy > m_{μ} / 2





 e^+

Summary: Muon Experiments

In Support of the Standard Model

•Lifetime – G_F

-MuLan: 1 ppm lifetime; 0.5 ppm G_F

Capture on protons and deuterons

MuCap g_P: Unambiguous confirmation of low-energy QCD-based theory
 MuSun L₁₂ Fundamental astrophysics implications

Muonic Atoms

Lamb shift in hydrogen, r_p proton radius puzzle
 Lamb shift in other light systems in prep

Physics Beyond the Standard Model Tests

Michel parameters

-TWIST ρ , δ , η , $P_{\mu}\xi$: constrains right handed terms in WI

Anomalous magnetic moment (g-2)

-BNL: a hint of something interesting

•FNAL: Improved precision will provide definitive test

-Lepton Flavor Violation

•MEG: $\mu \rightarrow e\gamma$ New limits at ... Plans to go to xx •Mu2e: $\mu \rightarrow e$ conversion in prep to improve by > 3 orders of magnitude •COMET: Similar long term goal with nearer term intermediate result

-EDM –

Parasitic from g-2 data; can improve by x100

-Lorentz / CPT violation test -

Similar improvements expected from higher statistics data sets

