

# New Developments in SM Predictions

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University at Buffalo, SUNY

US ATLAS meeting at ANL, July 15, 2013

# Outline

The exploration of the Higgs sector and the search for new physics at the LHC requires accurate, stable and flexible higher-order QCD+EW predictions involving jets, heavy quarks,  $W$ ,  $Z$ ,  $\gamma$  and the Higgs boson.

Recent advances in Higgs predictions: please see R.Boughezal's talk

Please note that this is a personal selection of results illustrating recent activities in:

- **Fixed order**(+resummed): NNLO QCD+NNLL resummation, NLO EW and weak Sudakov logs (recent advances in resummation not covered here, please see Radja's talk for examples)
- **Automation**: aMC@NLO (MadLoop+MadFKS+Madgraph), Sherpa (GOSAM+MC@NLO)
- **NLO and PS merging**: NLO QCD $\times$ PS (Sherpa+MC@NLO), NLO(QCD+EW) $\times$ PS

For a more exhaustive overview see, e.g.,:

The LoopFest XII (2013): <http://indico.cern.ch/conferenceDisplay.py?confId=223649>

Les Houches 2013: <http://phystev.in2p3.fr/wiki/2013:programme>

# NNLO for more hadron collider processes!

- For a long time, only color singlet final states available at full NNLO, mostly  $2 \rightarrow 1$  at Born level:  $H, W, Z, \gamma\gamma$
- 2013 will be remembered as the year of  $2 \rightarrow 2$  at NNLO

From:

LoopFest 2013 summary talk by Lance Dixon

# pp→jj @ NNLO QCD

- Provides information of the gluon content of the proton, needed for NNLO PDFs
- Determination of  $\alpha_s$
- Precision test of QCD

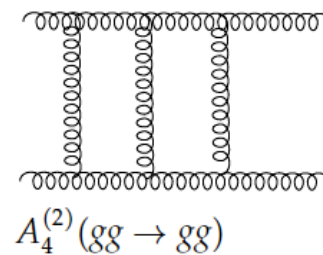
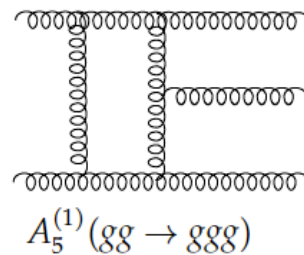
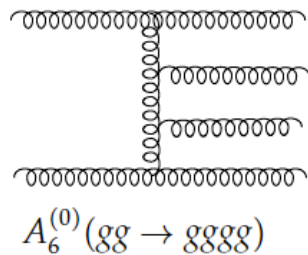
A.Gehrmann-de Ritter, T. Gehrmann, E.W.N Glover, J. Pires, [arXiv:1301.7310](https://arxiv.org/abs/1301.7310):

- Fully differential di-jet and inclusive jet cross sections at NNLO accuracy
- implemented in parton level generator NNLOJET
- based on gluonic channels and leading color (quark channels are work in progress)

# Challenge: complex structure of IR singularities

Jao Pires @ LoopFest 2013:

$pp \rightarrow 2j$  AT NNLO: GLUONIC CONTRIBUTIONS



[Berends, Giele '87], [Mangano, Parke, Xu '87], [Britto, Cachazo, Feng '06]

[Bern, Dixon, Kosower '93]

[Anastasiou, Glover, Oleari, Tejeda-Yeomans '01],[Bern, De Freitas, Dixon '02]

$$d\hat{\sigma}_{NNLO} = \int_{d\Phi_4} d\hat{\sigma}_{NNLO}^{RR} + \int_{d\Phi_3} d\hat{\sigma}_{NNLO}^{RV} + \int_{d\Phi_2} d\hat{\sigma}_{NNLO}^{VV}$$

- ▶ explicit infrared poles from loop integrations
- ▶ implicit poles in phase space regions for single and double unresolved gluon emission
- ▶ procedure to extract the infrared singularities and assemble all the parts in a parton-level generator

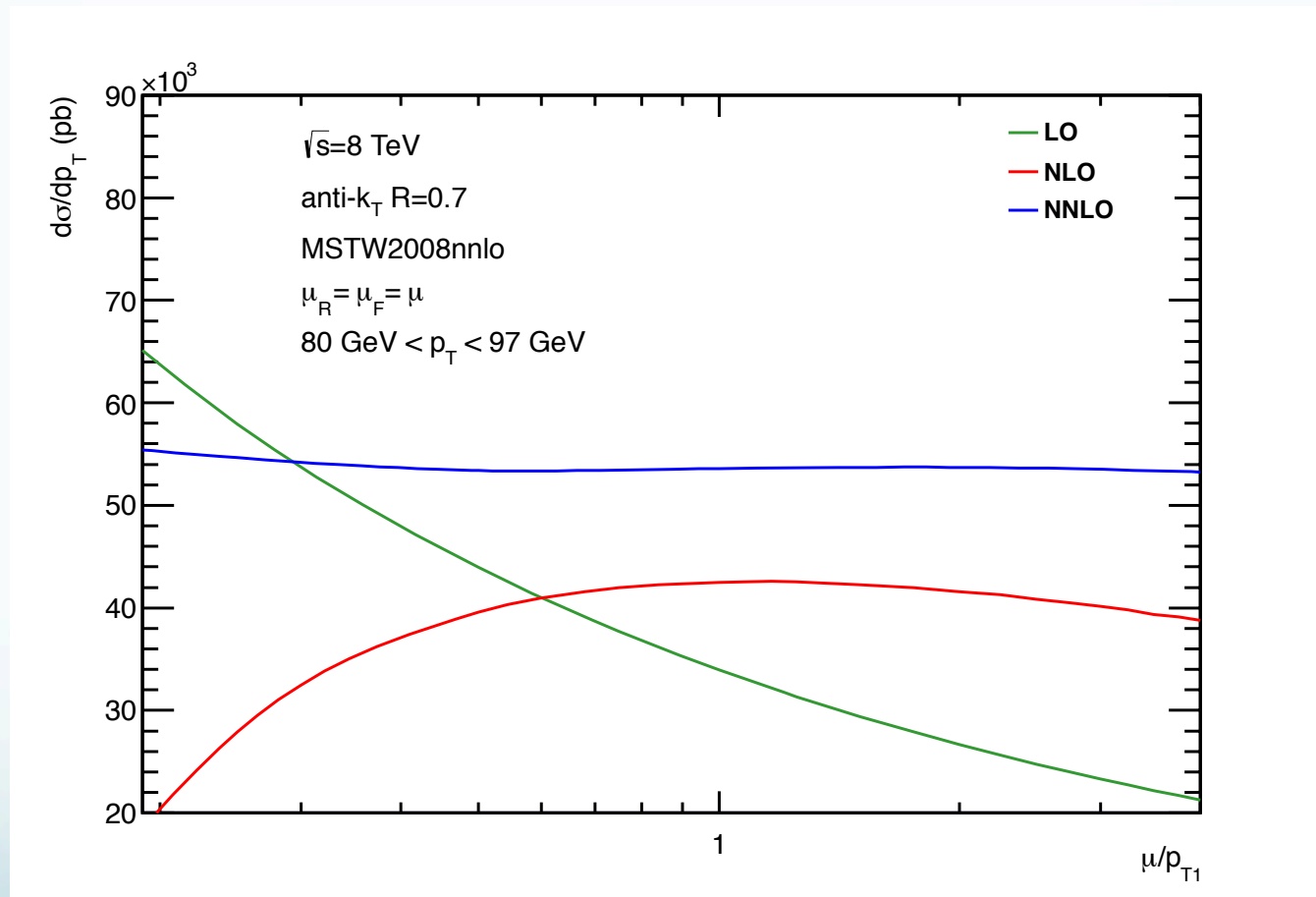
# Antenna subtraction now also for IS partons

Jao Pires @ LoopFest 2013:

$$\begin{aligned} d\hat{\sigma}_{NNLO} &= \int_{d\Phi_4} \left( d\hat{\sigma}_{NNLO}^{RR} - d\hat{\sigma}_{NNLO}^S \right) \\ &+ \int_{d\Phi_3} \left( d\hat{\sigma}_{NNLO}^{RV} - d\hat{\sigma}_{NNLO}^T \right) \\ &+ \int_{d\Phi_2} \left( d\hat{\sigma}_{NNLO}^{VV} - d\hat{\sigma}_{NNLO}^U \right) \end{aligned}$$

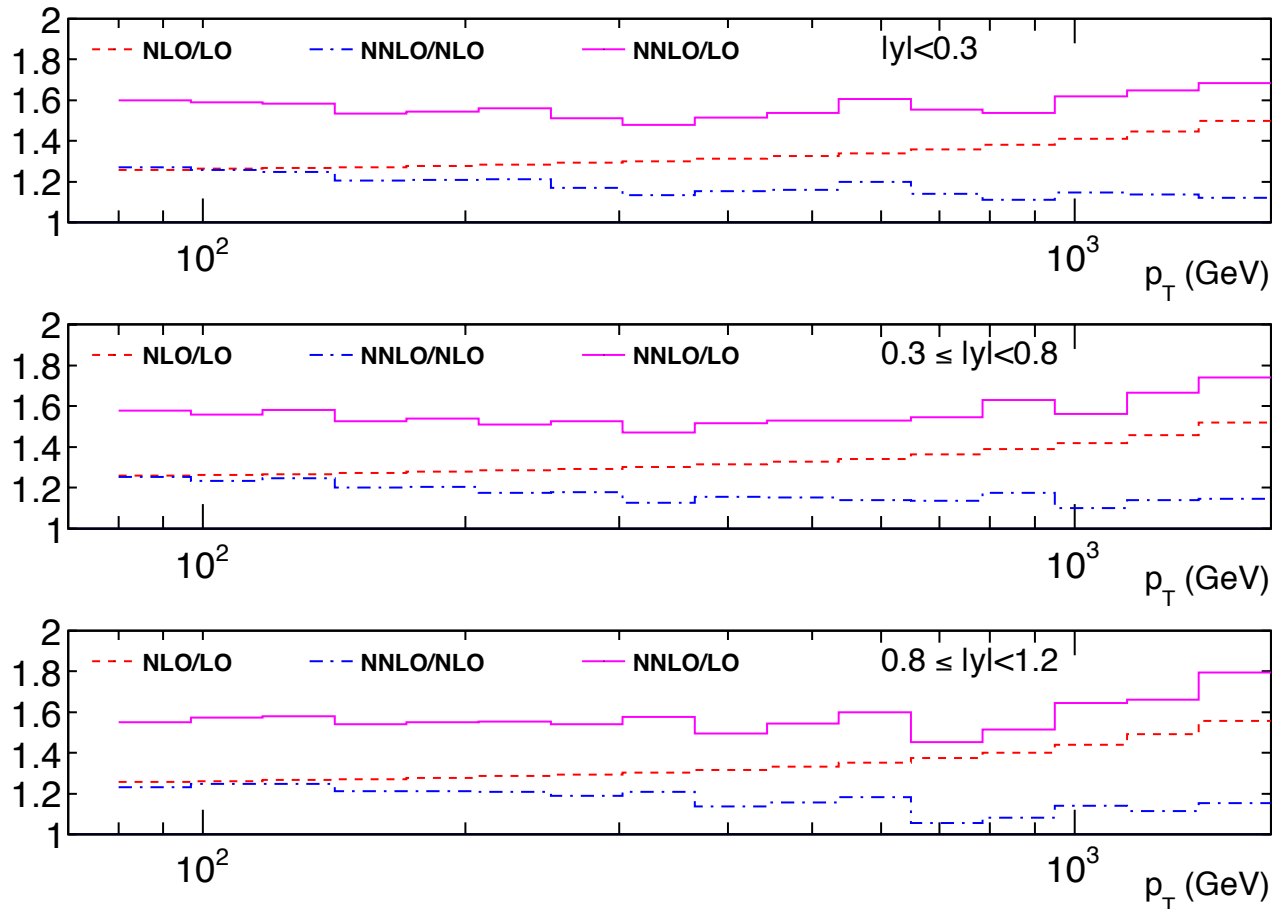
- ▶  $d\hat{\sigma}_{NNLO}^S$ : real radiation subtraction term for  $d\hat{\sigma}_{NNLO}^{RR}$
- ▶  $d\hat{\sigma}_{NNLO}^T$ : one-loop virtual subtraction term for  $d\hat{\sigma}_{NNLO}^{RV}$
- ▶  $d\hat{\sigma}_{NNLO}^U$ : two-loop virtual subtraction term for  $d\hat{\sigma}_{NNLO}^{VV}$
- ▶ subtraction terms constructed using the antenna subtraction method at NNLO for hadron colliders → presence of initial state partons to take into account
- ▶ contribution in each of the round brackets is finite, well behaved in the infrared singular regions and can be evaluated numerically

# Scale dependence of inclusive jet $P_T$ cross section at the 8 TeV LHC



A.Gehrmann-de Ritter, T. Gehrmann, E.W.N Glover, J. Pires, arXiv:1301.7310

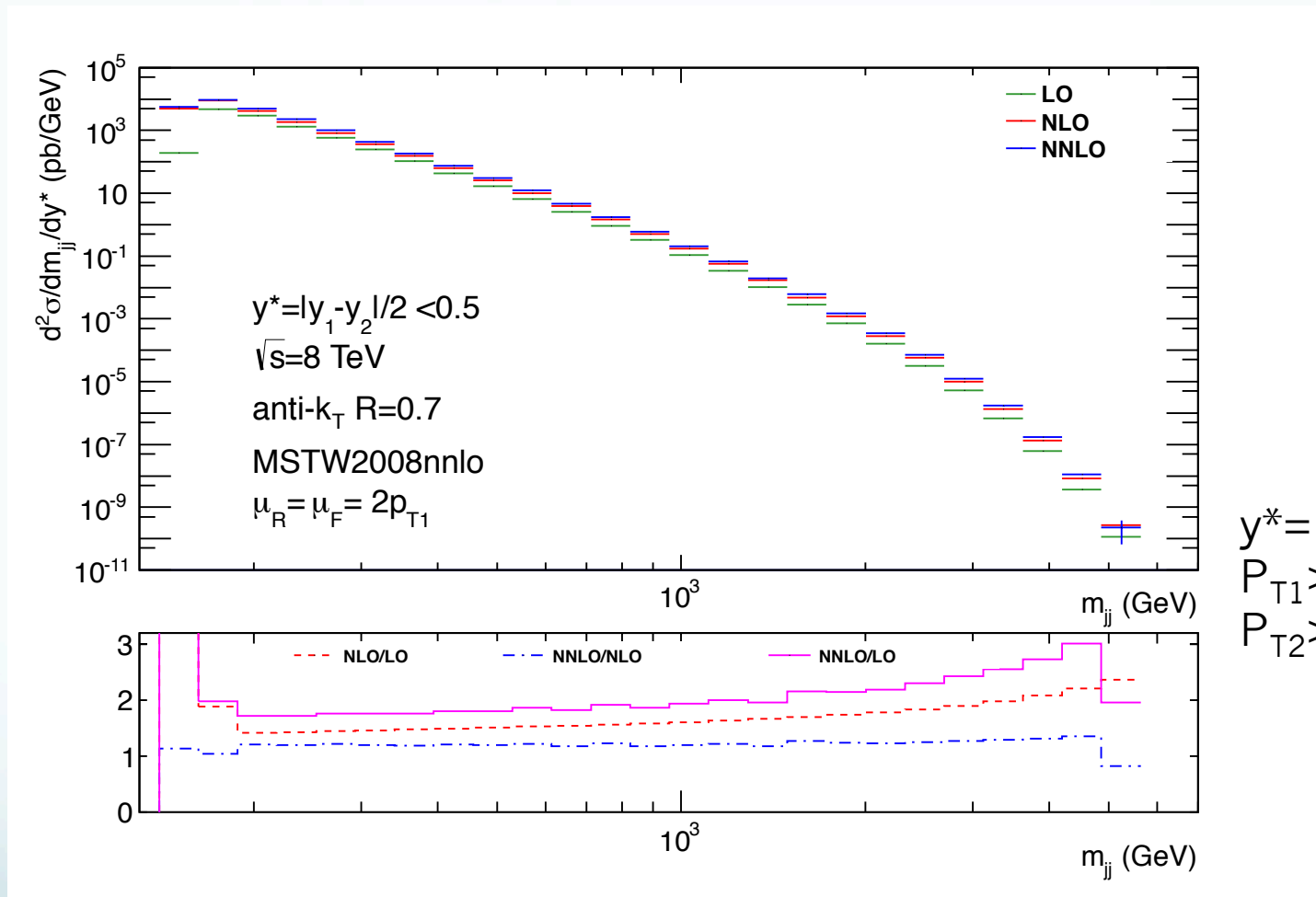
# K factors for inclusive jet for different $|y|$ slices



A.Gehrmann-de Ritter, T. Gehrmann, E.W.N Glover, J. Pires, arXiv:1301.7310



# Exclusive di-jet $d^2\sigma/dm_{jj} dy^*$ distribution

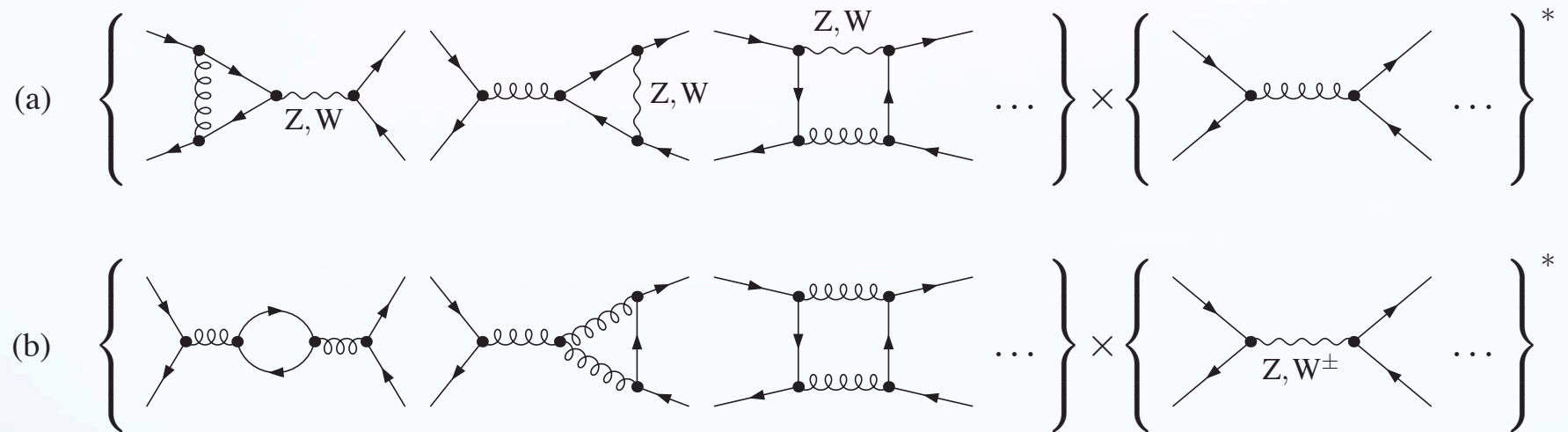


$y^* = |y_1 - y_2| < 0.5$   
 $P_{T1} > 80 \text{ GeV}$ ,  
 $P_{T2} > 60 \text{ GeV}$

A.Gehrmann-de Ritter, T. Gehrmann, E.W.N Glover, J. Pires, arXiv:1301.7310

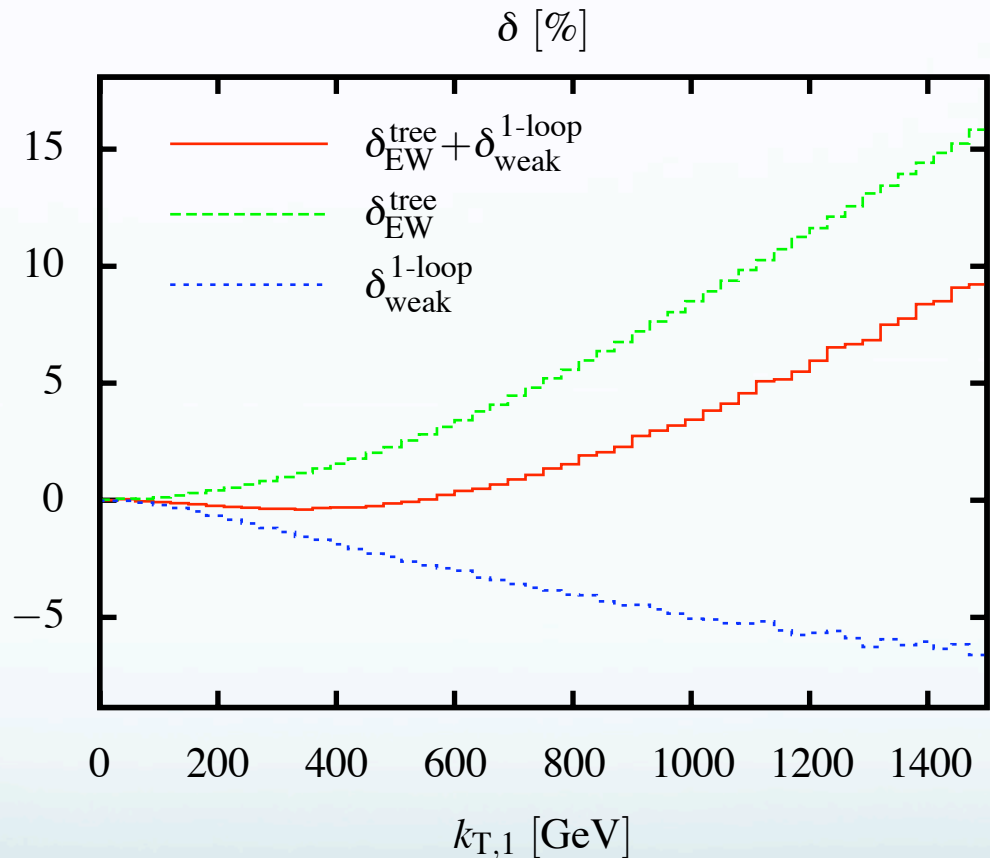
# Weak 1-loop corrections to di-jet production

Examples of 1-loop weak corrections:



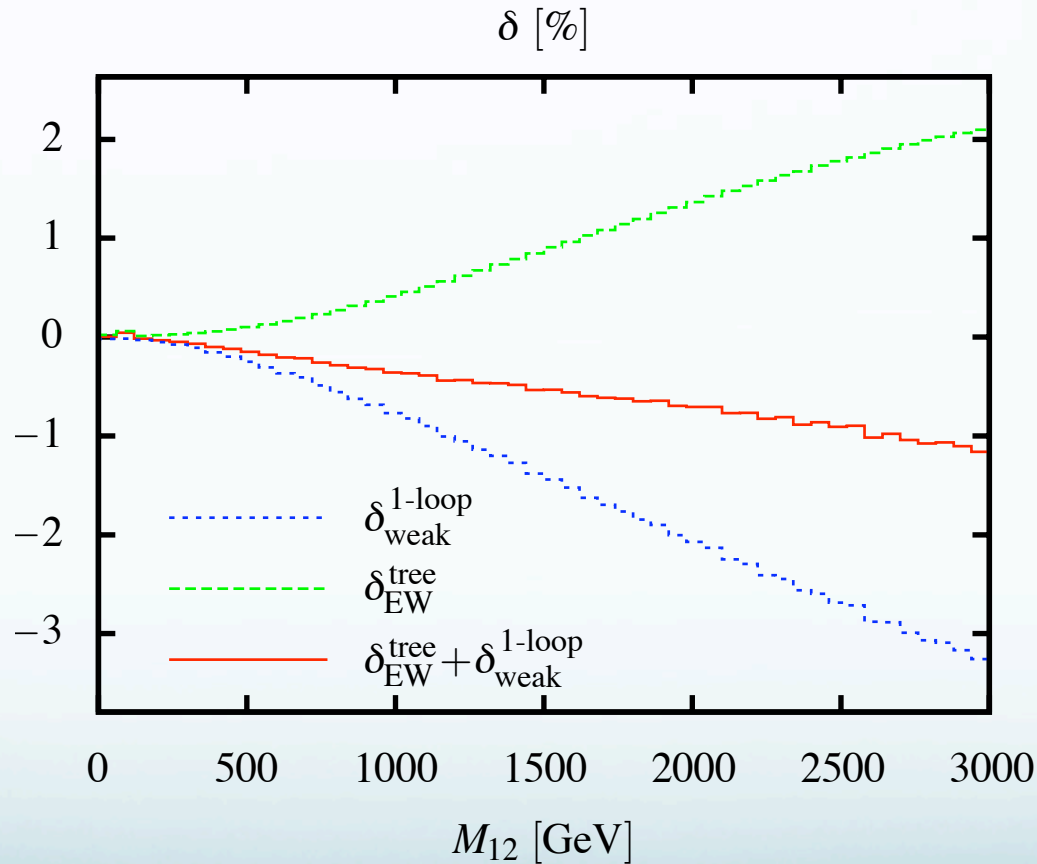
S.Dittmaier, A.Huss, C.Speckner, arXiv:1306.6298

# Relative weak corrections to leading kT distribution to pp->jj+X at the 8 TeV LHC



S.Dittmaier, A.Huss, C.Speckner, arXiv:1306.6298

# Relative weak corrections to di-jet invariant mass distribution to $pp \rightarrow jj+X$ at the 8 TeV LHC



S.Dittmaier, A.Huss, C.Speckner, arXiv:1306.6298

# Top-pair production at NNLO QCD

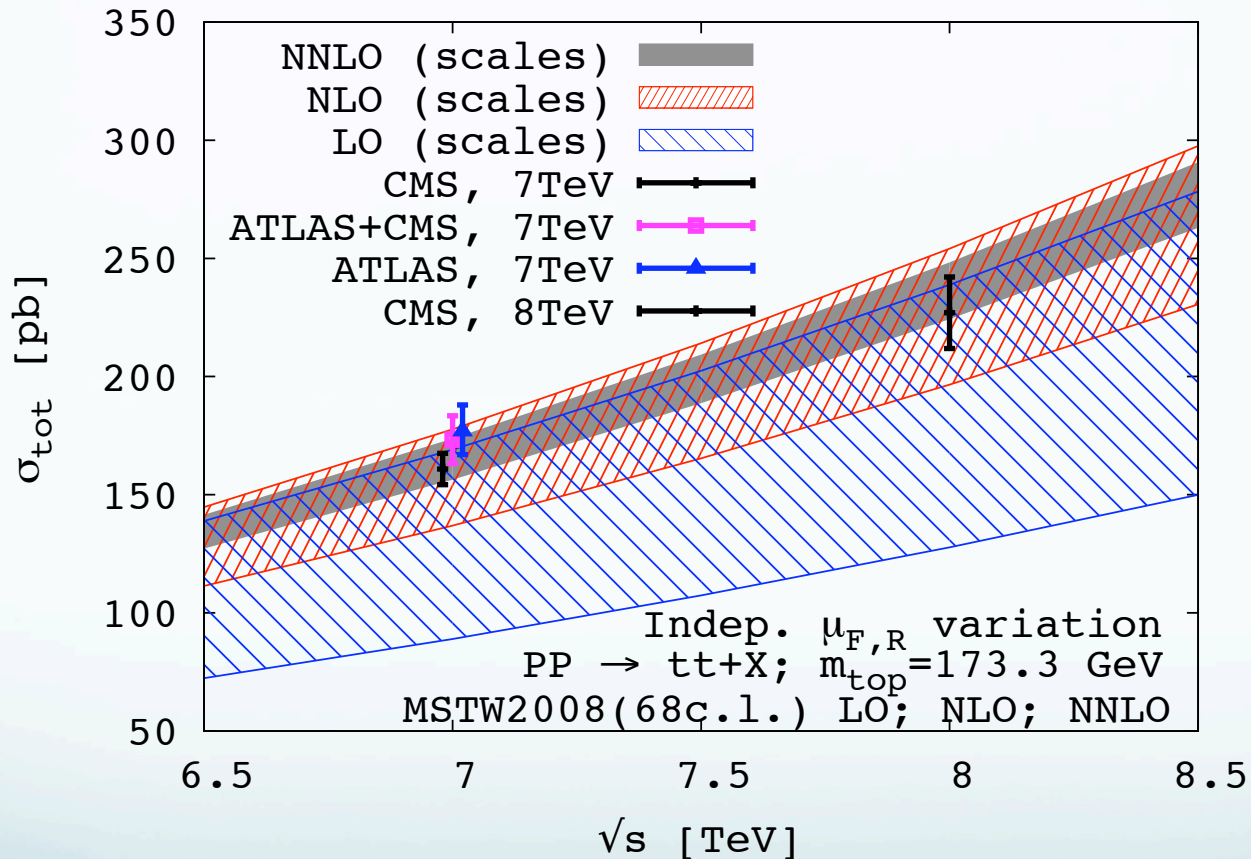
$$\sigma_{\text{tot}} = \sum_{i,j} \int_0^{\beta_{\text{max}}} d\beta \Phi_{ij}(\beta, \mu_F^2) \hat{\sigma}_{ij}(\beta, m^2, \mu_F^2, \mu_R^2).$$

$$\Phi_{ij}(\beta, \mu_F^2) = \frac{2\beta}{1-\beta^2} \mathcal{L}_{ij} \left( \frac{1-\beta_{\text{max}}^2}{1-\beta^2}, \mu_F^2 \right) \quad \mathcal{L}_{ij}(x, \mu_F^2) = x (f_i \otimes f_j)(x, \mu_F^2)$$

$$\hat{\sigma}_{ij}(\beta) = \frac{\alpha_S^2}{m^2} \left( \sigma_{ij}^{(0)} + \alpha_S \sigma_{ij}^{(1)} + \alpha_S^2 \sigma_{ij}^{(2)} + \mathcal{O}(\alpha_S^3) \right)$$

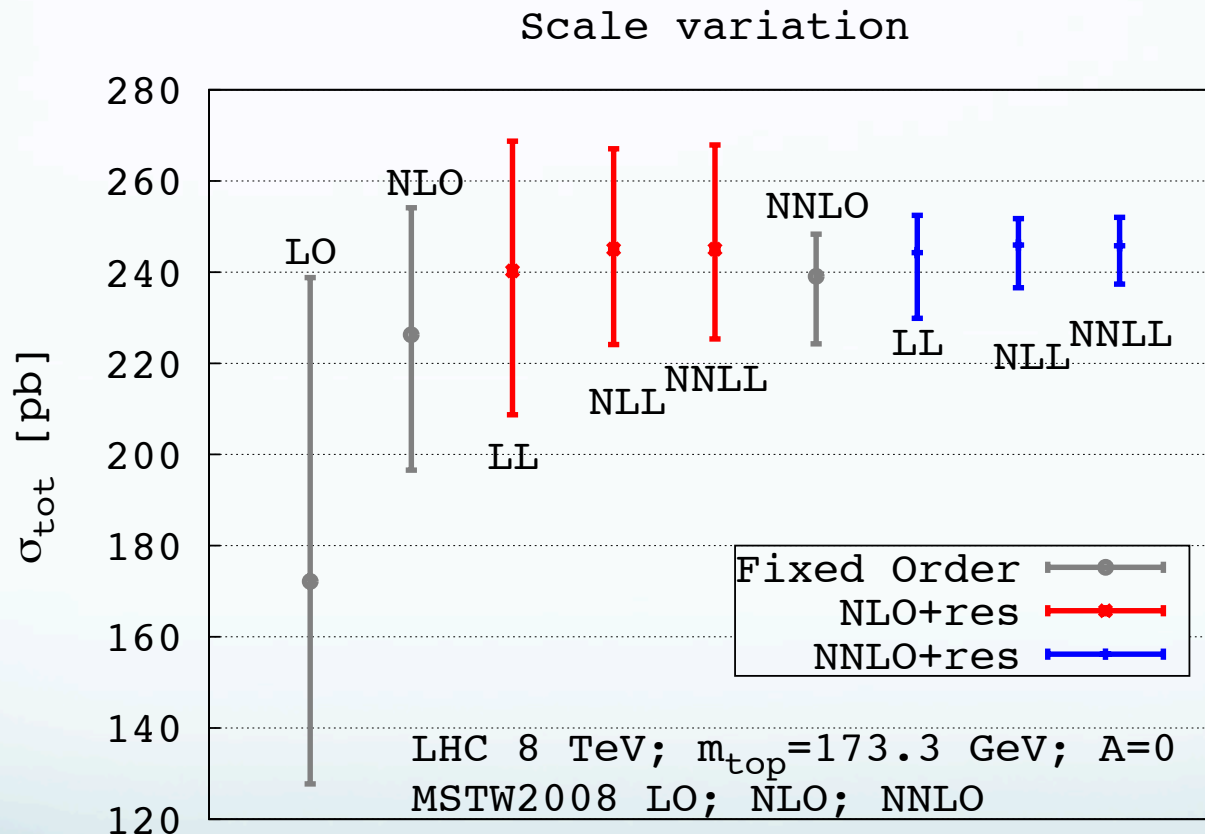
M.Czakon, P. Fiedler, A. Mitov, arXiv:1303.6254  
Implemented in publicly available code Top++:  
<http://www.alexandermitov.com/software/>

# Independent $\mu_R$ and $\mu_F$ variation at LO, NLO, NNLO of $\sigma_{\text{tot}}$ at the LHC



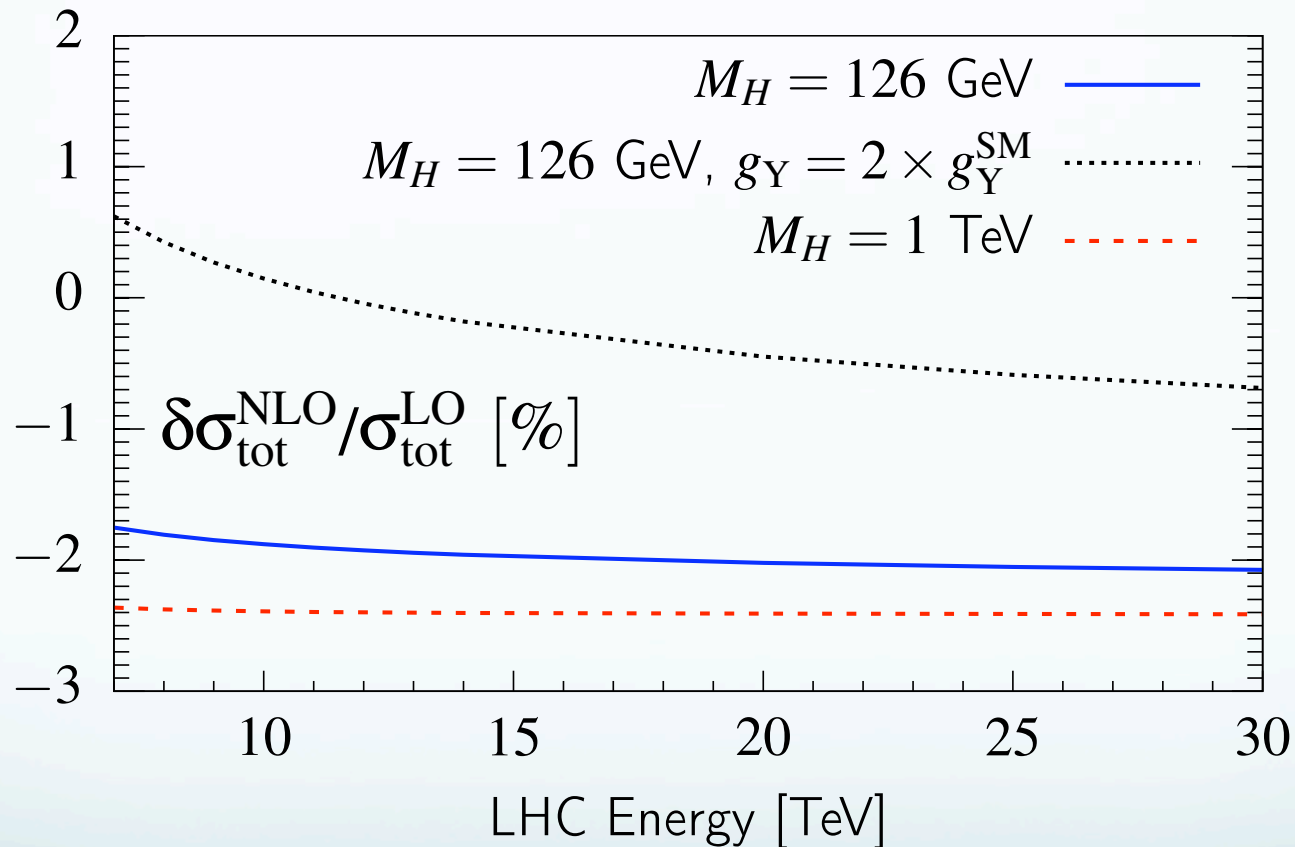
M.Czakon, P. Fiedler, A. Mitov, J. Rojo, arXiv:1305.3892

# Scale variation at LO, NLO, NNLO and when including LL, NLL, NNLL resummation



M.Czakon, P. Fiedler, A. Mitov, J. Rojo, arXiv:1305.3892

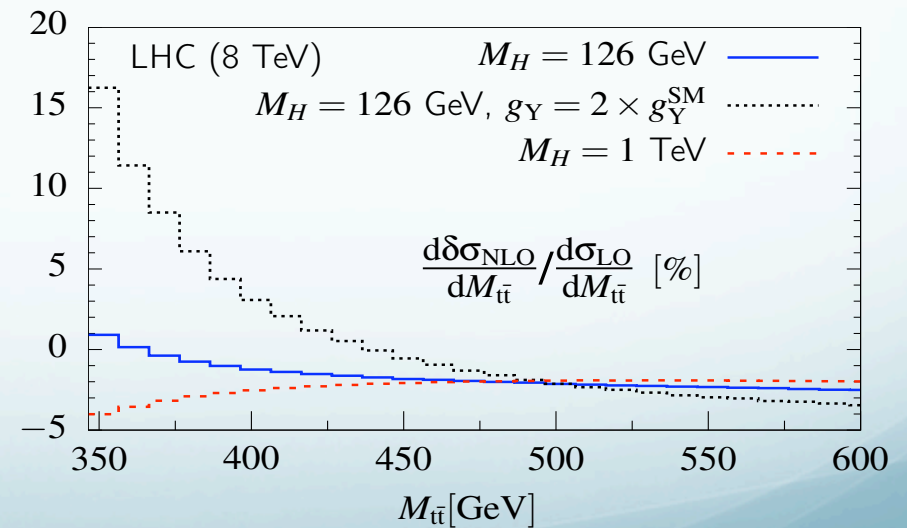
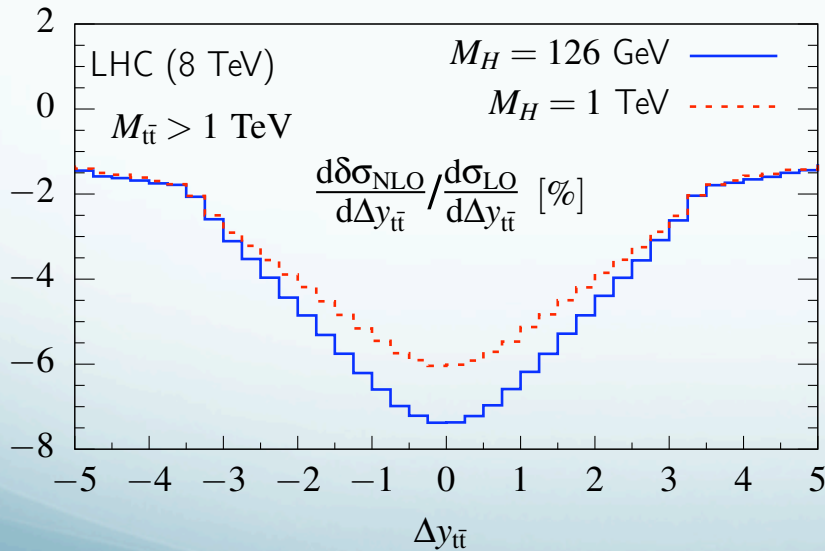
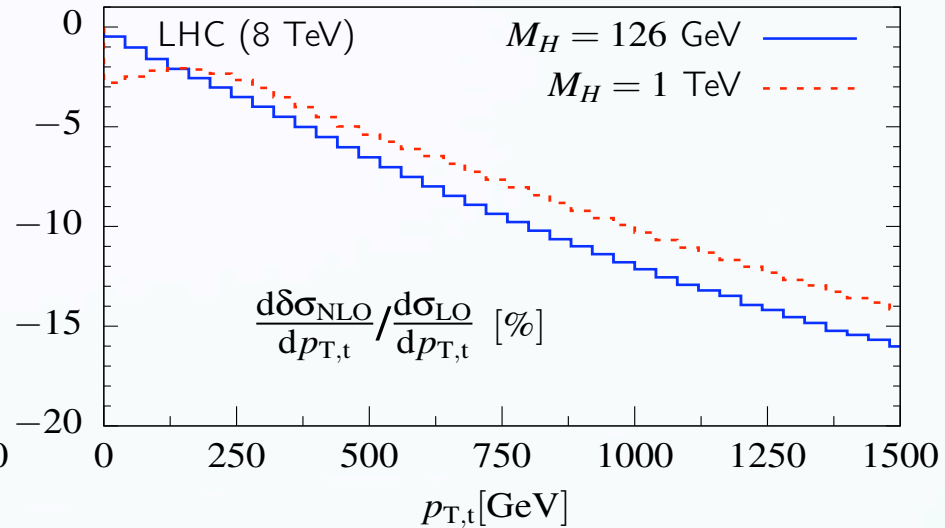
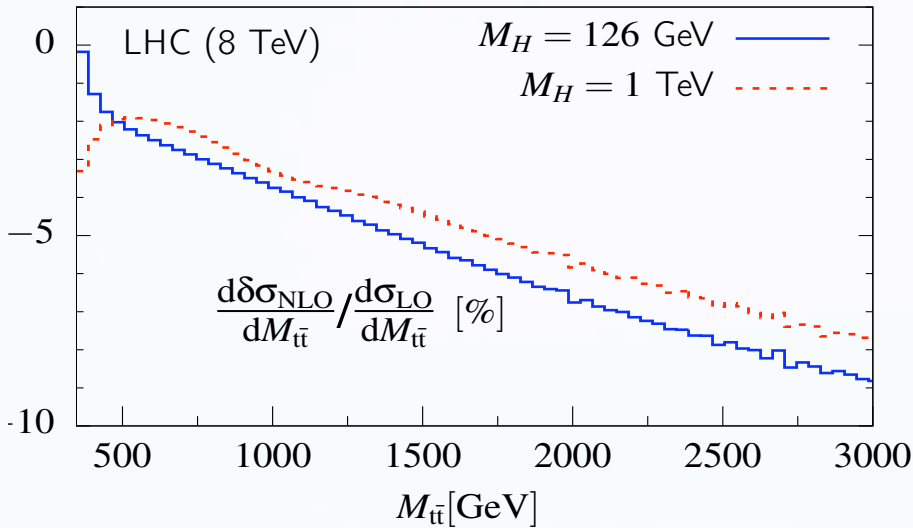
# Impact of weak 1-loop corrections in top-pair production at the 8 TeV LHC



H.Kühn, A. Scharf and P. Uwer, arXiv:1305.5773



# Impact of weak 1-loop corrections in top-pair production at the 8 TeV LHC



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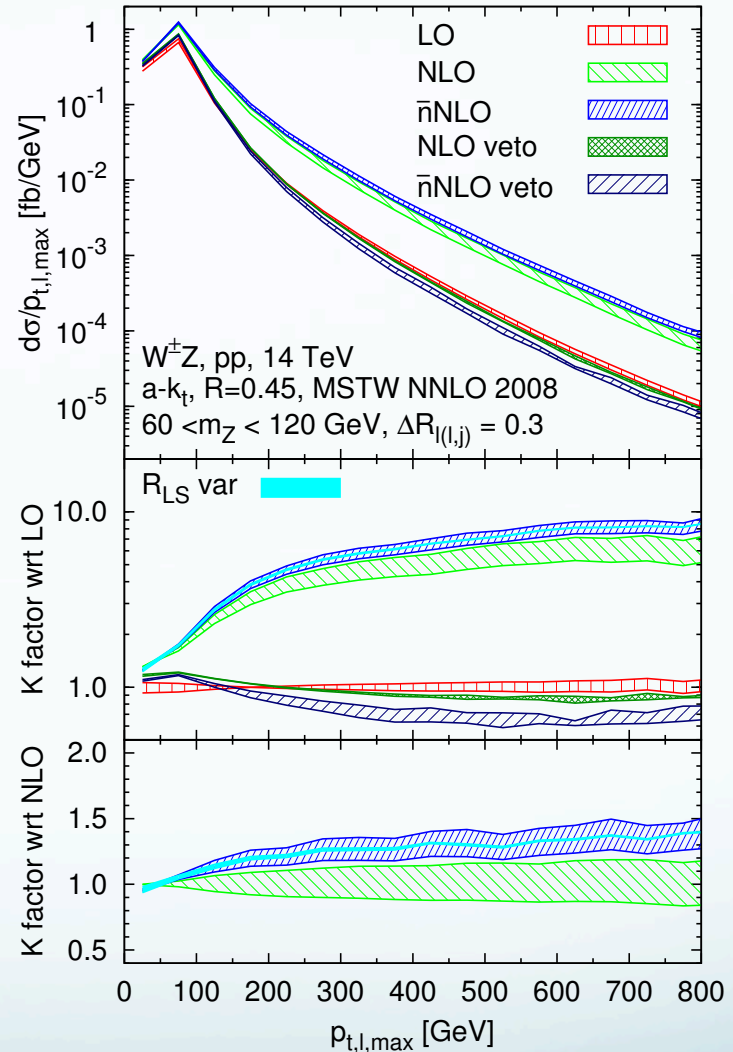
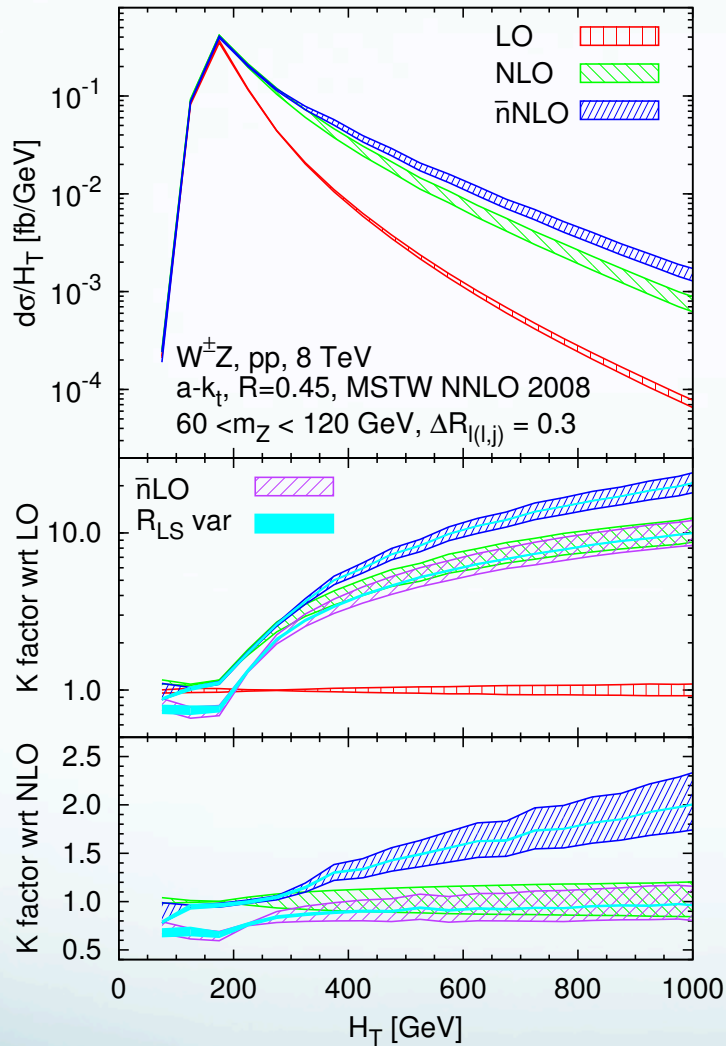
# VV and VVV (w/o jets) processes

- NLO QCD prediction available for VV, VVV, WWj, WZj,  $W\gamma j$ , ZZj, WWjj,  $W\gamma\gamma j$ , WZjj (new in VBFNLO)
- Electroweak corrections at NLO to  $Z\gamma$ , WW, WZ, ZZ

Large K-factors: how about di-boson@NNLO QCD ?

- di-photon@NNLO QCD: [Catani et al \(2012\)](#)
- **VBFNLO+LOOPSIM**: approximate NNLO for WZ production (LO:  $qq \rightarrow WZ$ ) [Campanario et al, 1307.2261](#); LOOPSIM: [M.Rubin et al \(2010\)](#): 2-loop master integrals for  $qq \rightarrow VV$ : [T.Gehrman et al \(1306.6344\)](#), WZj@NLO from MCFM or VBFNLO
- LOOPSIM produces approximate 2-loop virtual corrections needed to cancel IR uncertainties.

# WZ@nNLO (approximate NNLO) at the 14 TeV LHC

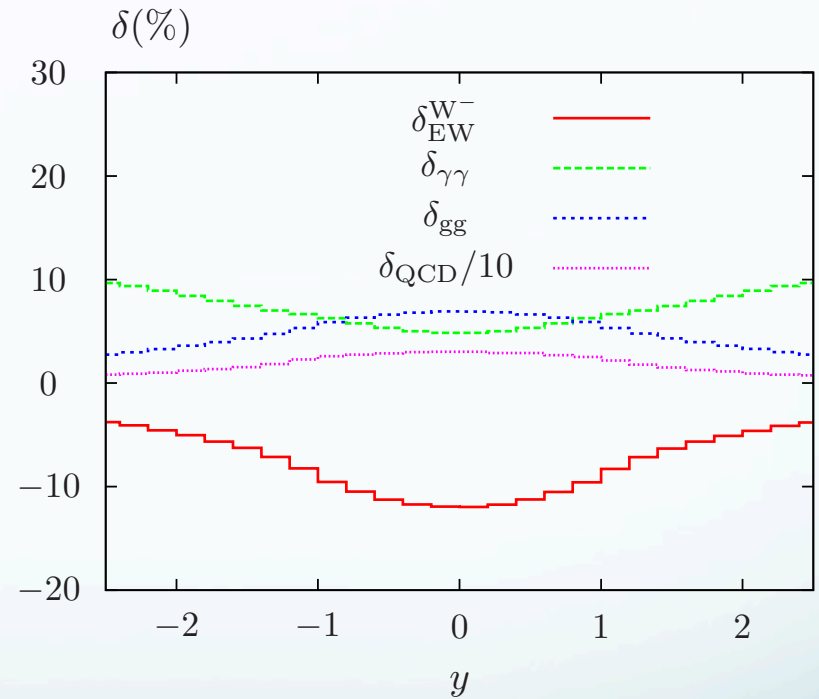
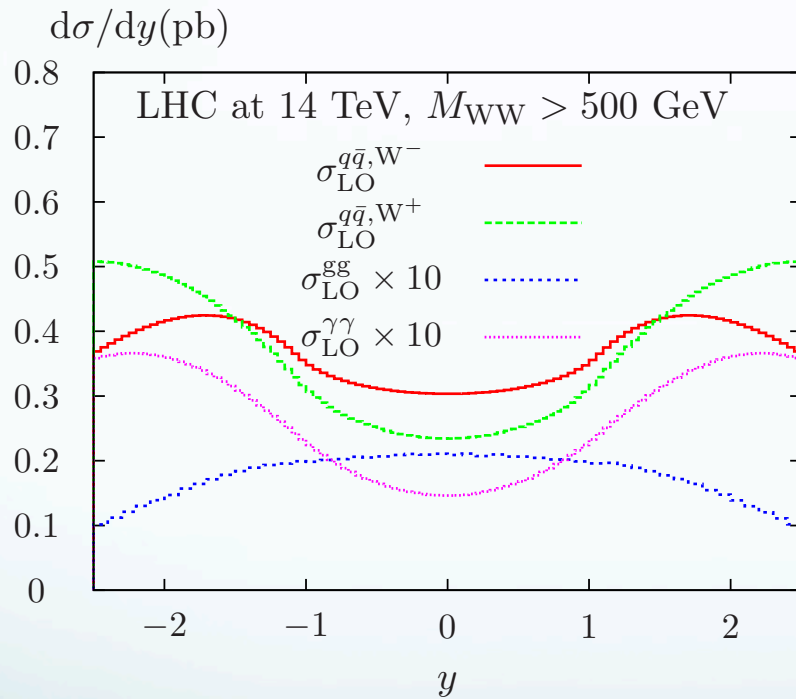


$p_{T,\ell} \geq 15(20)$ ,  $|y_l| \leq 2.5$ ,  $E_{T,miss} > 30$  GeV,  $60 < m_{l+l^-} < 120$  GeV

Campanario et al, 1307.2261

# $pp \rightarrow W^+W^-$ at NLO EW at the LHC

W rapidity LO distributions and relative NLO EW corrections for different initial states:



Bierweiler *et al*, 1208.3147; WZ,ZZ: 1305.5402

# NLO predictions for processes with high multiplicity

# NLO QCD with Blackhat+Sherpa

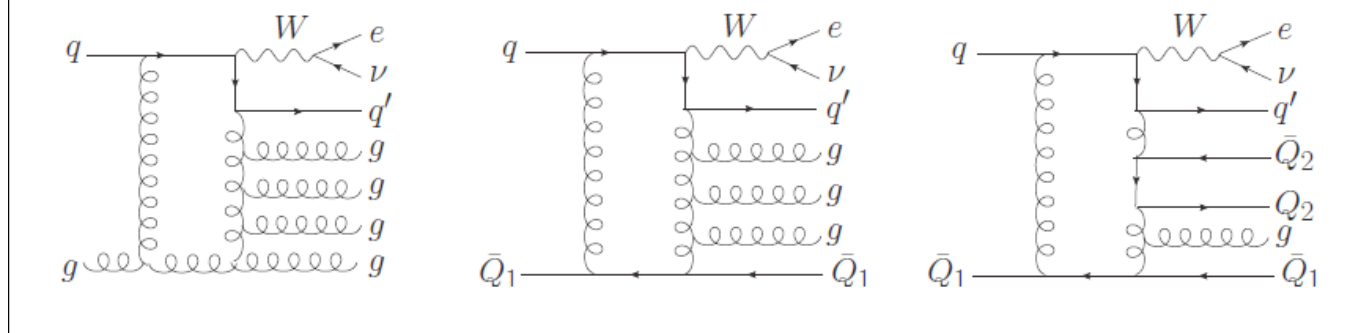
From talk by F. Febres Cordero at LoopFest 2013:

## ***W+5 Jets Calculation Setup***

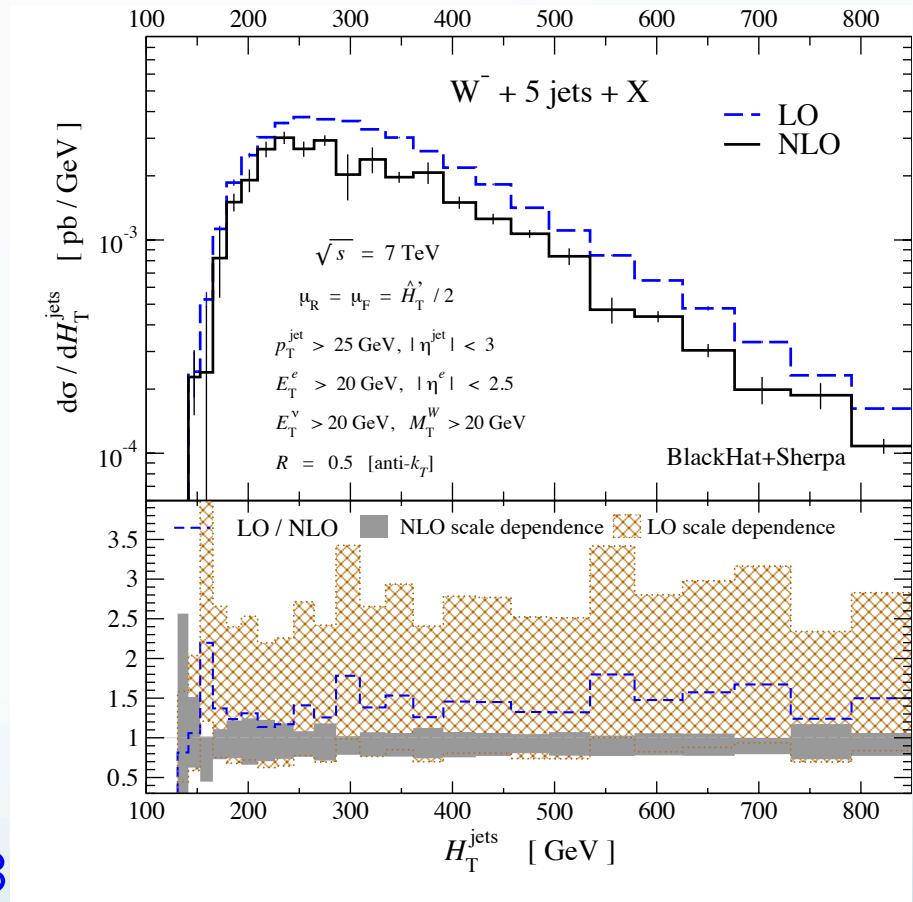
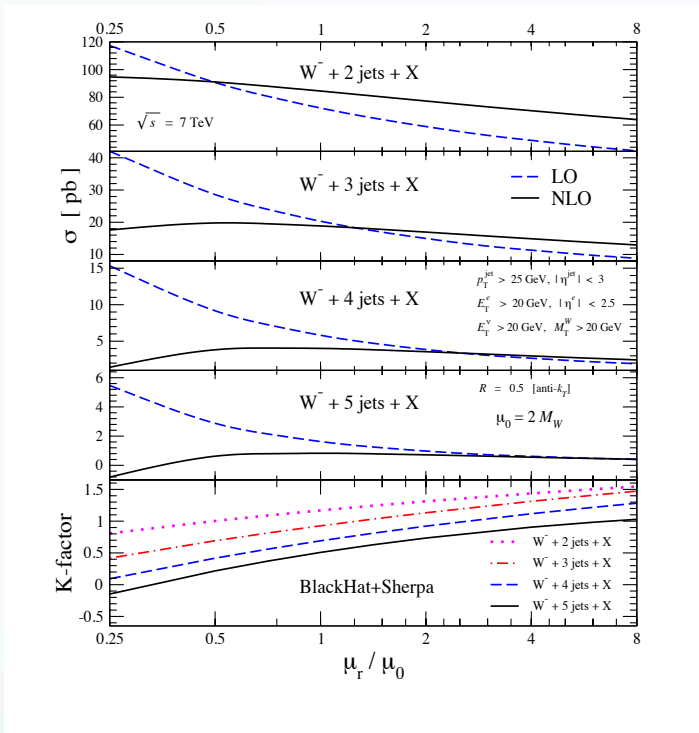
$$\sigma_n^{NLO} = \int_n \sigma_n^{tree} + \int_n (\sigma_n^{virt} + \Sigma_n^{sub}) + \int_{n+1} (\sigma_{n+1}^{real} - \sigma_{n+1}^{sub})$$

The diagram illustrates the NLO calculation setup. It features a dark blue background with a mathematical equation at the top. Below the equation, there are two images: a black hat on the left and a climber on the right. Four orange arrows originate from these images and point to the terms in the equation: one from the hat to  $\sigma_n^{tree}$ , one from the climber to  $\sigma_n^{virt} + \Sigma_n^{sub}$ , one from the hat to  $\sigma_{n+1}^{real}$ , and one from the climber to  $\sigma_{n+1}^{sub}$ .

### Sample of Loop Parent Diagrams



# W+5 jets@NLO QCD



Z. Bern *et al.*, arXiv:1304.1253

# Electroweak 1-loop corrections to Z/W+n jets

- Exact 1-loop EW corrections are known for W/Z+1 jet [Kuhn et al, hep-ph/057178, 0708.0476](#); [Denner et al, 1211.507,0906.1656](#)
  - and for Z+2 jet (only gluonic contributions, 4-quark contributions in progress) , [Actis et al, arXiv:1211.6316](#)
  - At energy scales above the electroweak scale EW corrections are dominated by weak Sudakov logarithms
- for a review see, e.g., [H.Kuhn, Acta Physica Polonia B39\(2008\)](#); talk by [S.Dittmaier at Les Houches 2013](#)
- Weak 1-loop Sudakov corrections to Z+1,2,3 jets production are now implemented in Alpgen 1.4.1.2, [Chiesa et al. arXiv:1305.6837](#)



# Weak Sudakov logs: $(\alpha_w/\pi)^l \text{Log}^n(Q^2/M^2), n \leq 2l$

- **Origin:** remnants of UV singularities after renormalization and soft/collinear emission of real and virtual W and Z bosons.
- In contrast to QED and QCD, these corrections do not cancel in inclusive observables [Ciafaloni, Ciafaloni, Comelli \(2000\)](#)

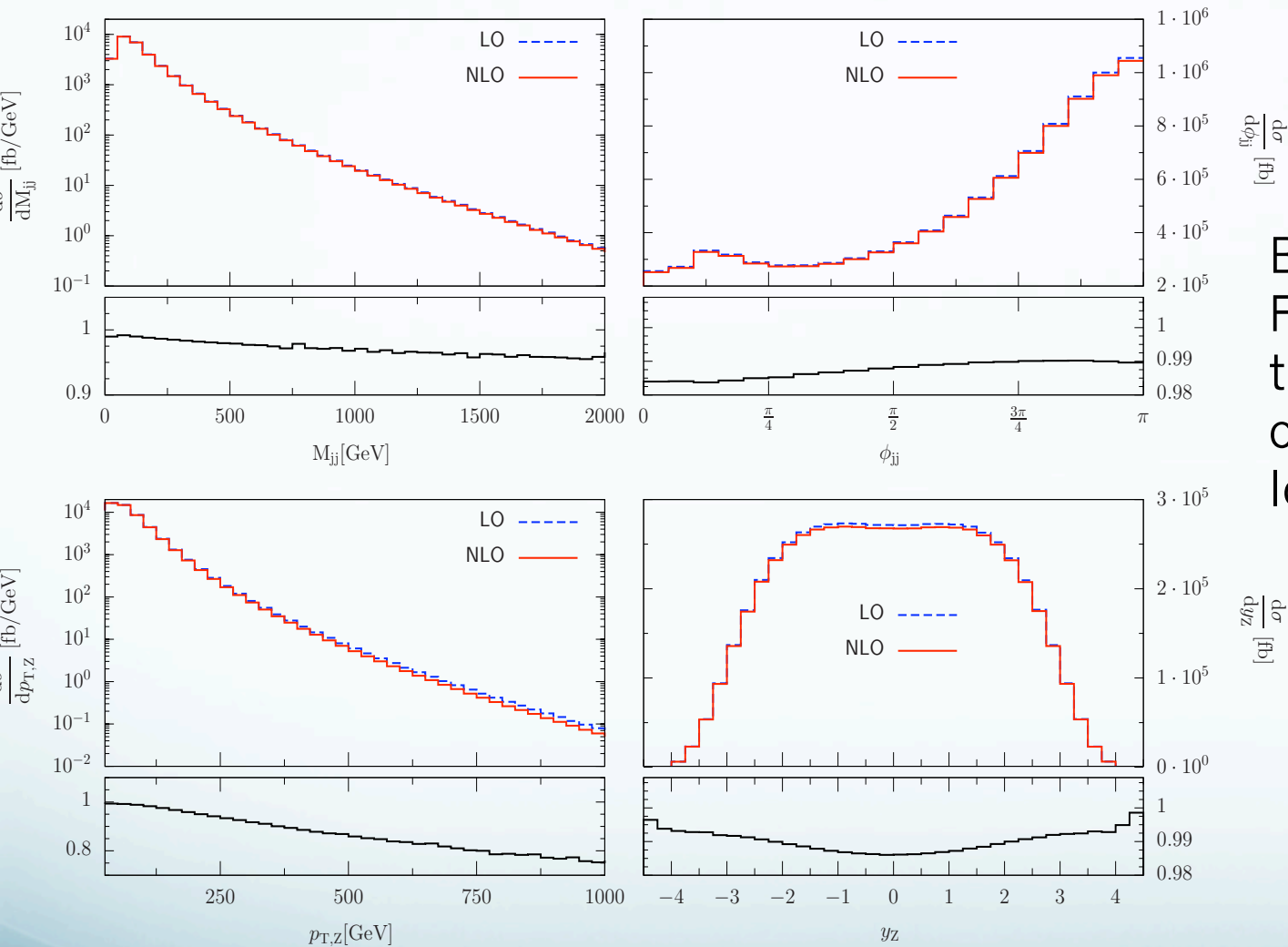
In the high-energy limit,  $\frac{Q}{M_{W,Z}} \rightarrow \infty$ , EW Sudakov logarithms have been studied in analogy to soft/collinear logarithms in QED, QCD.

- 1-loop: LL and NLL are universal and factorize [Denner, Pozzorini \(2001\)](#)
- Beyond 1-loop: Resummation techniques based on IR evolution equations (IREE) or SCET yield results up to NNLL ( $\ln^n(\frac{s}{M_W^2})$ ,  $n = 2, 3, 4$ ).
  - IREE: EW theory splits into symmetric  $SU(2) \times U(1)$  ( $M_W = M_Z = M_\gamma = M$  for  $\mu > M$ ) and QED regime and effect of EW symmetry breaking neglected. [Fadin, Lipatov, Martin, Melles \(2000\)](#)
  - SCET: At  $\mu = Q$  match full theory to SCET( $M = 0$ ), evolve to  $\mu = M$  SCET( $M \neq 0$ ), match to SCET with no gauge bosons.
  - SCET and IREE Sudakov form factors are equivalent. [Chiu, Golf, Kelley, Manohar \(2008\)](#); [Chiu, Fuhrer, Hoang, Kelley, Manohar \(2009\)](#); [Chiu, Fuhrer, Kelley, Manohar \(2010\)](#), [Fuhrer et al \(2011\)](#)

Resummation results at LL and NLL confirmed by explicit diagrammatic one-loop and two-loop calculations.

[Melles \(2000\)](#), [Hori et al \(2000\)](#), [Beenakker, Werthenbach \(2000,2002\)](#), [Pozzorini \(2004\)](#); [Feucht et al \(2003,2004\)](#); [Jantzen et al \(2005,2006\)](#); [Denner et al \(2003,2008\)](#)

# Z+2j @ NLO EW at the 8 TeV LHC

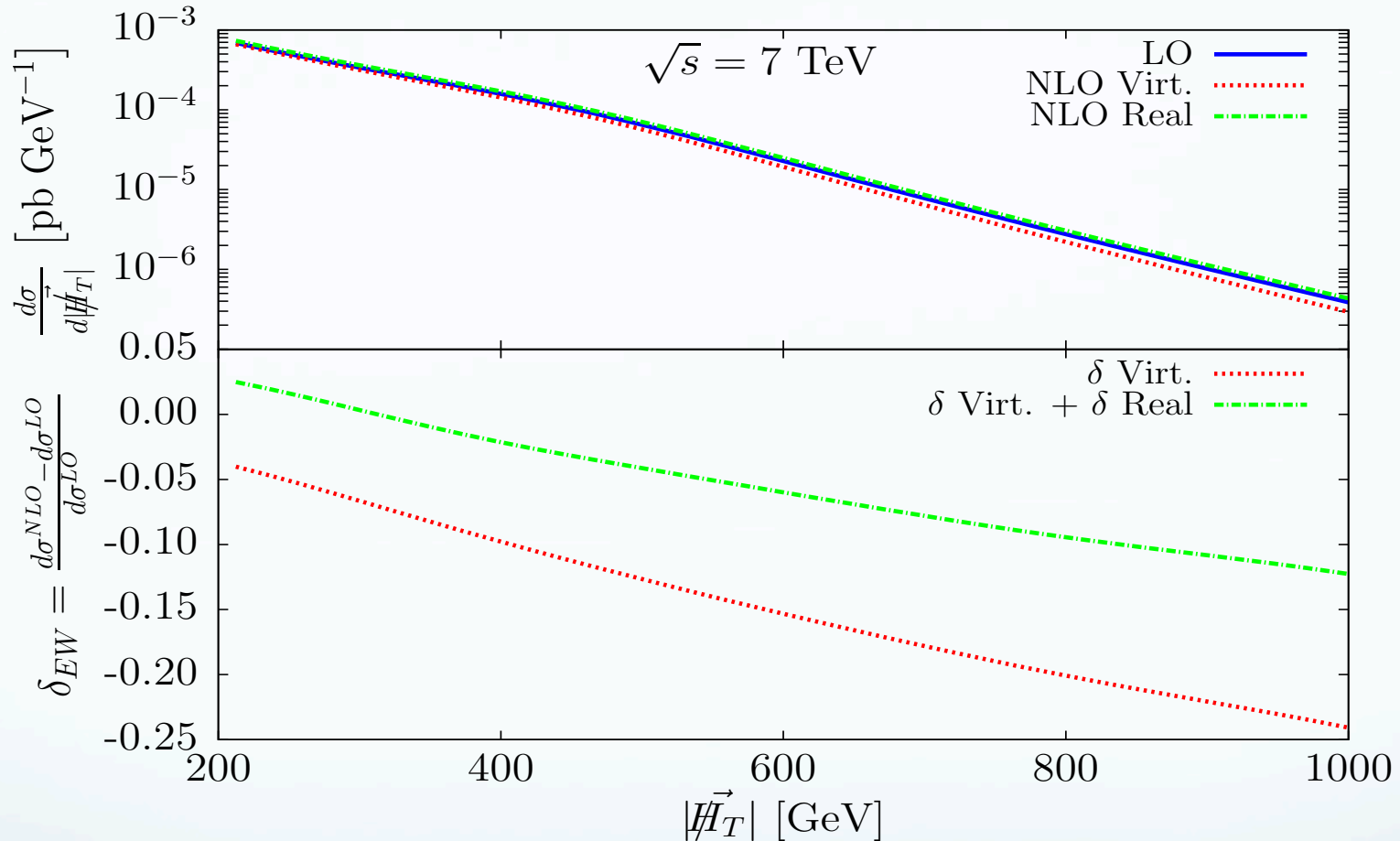


Based on REcola:  
Fortran90 code for  
the recursive  
calculation of one-  
loop amplitudes

Actis et al, arXiv:1211.6316

$p_{T,\text{jet}} > 25 \text{ GeV}, \quad |y_{\text{jet}}| < 4.5$

# Z+3j: Weak 1-loop Sudakov corrections in Alpgen



$$H_T > 500 \text{ GeV}$$

$$|\vec{H}_T| > 200 \text{ GeV}$$

$$p_T^j > 50 \text{ GeV}$$

$$|\eta_j| < 2.5 \quad \Delta R_{(j_i, j_k)} > 0.5$$

$$\vec{H}_T = - \sum_i \vec{p}_{t_i}$$

$$\Delta\phi(\vec{p}_T^{j_1, j_2}, \vec{H}_T) > 0.5$$

$$\Delta\phi(\vec{p}_T^{j_3}, \vec{H}_T) > 0.3$$

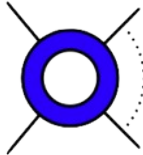

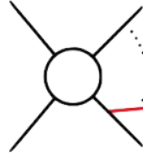
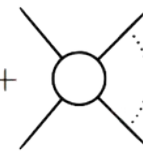
Chiesa et al. arXiv:1305.6837

# Automation of NLO predictions: “Madgraph for loops”

# aMC@NLO

Talk by O.Mattelaer at LoopFest 2013:

## NLO Basics

NLO	Virtual	Real	Born			
	=		+		+	
$\sigma^{NLO} = \int_m d^{(d)} \sigma^V + \int_{m+1} d^{(d)} \sigma^R + \int_m d^{(4)} \sigma^B$						

Need to deal with singularities

$$\sigma^{NLO} = \int_m d^{(d)} (\sigma^V + \int_1 d\phi_1 C) + \int_{m+1} d^{(d)} (\sigma^R - C) + \int_m d^{(4)} \sigma^B$$

MadLoop

MadFKS

MadGraph

MadLoop based on CutTools (OPP reduction method)

Ossala, Papadopoulos, Pittau (2006)

Talk by O.Mattelaer at LoopFest 2013:

## results

- Errors are the MC integration uncertainty only
- Cuts on jets,  $\gamma^*/Z$  decay products and photons, but **no cuts on b quarks** (their mass regulates the IR singularities)
- Efficient handling of **exceptional phase-space points**: their uncertainty always at least two orders of magnitude smaller than the integration uncertainty
- Running time: **two weeks on ~150 node cluster** leading to rather small integration uncertainties

Process	$\mu$	$n_f$	Cross section (pb)	
			LO	NLO
a.1 $pp \rightarrow t\bar{t}$	$m_{top}$	5	$123.76 \pm 0.05$	$162.08 \pm 0.12$
a.2 $pp \rightarrow tj$	$m_{top}$	5	$34.78 \pm 0.03$	$41.03 \pm 0.07$
a.3 $pp \rightarrow tjj$	$m_{top}$	5	$11.851 \pm 0.006$	$13.71 \pm 0.02$
a.4 $pp \rightarrow t\bar{b}j$	$m_{top}/4$	4	$25.62 \pm 0.01$	$30.96 \pm 0.06$
a.5 $pp \rightarrow t\bar{b}jj$	$m_{top}/4$	4	$8.195 \pm 0.002$	$8.91 \pm 0.01$
b.1 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e$	$m_W$	5	$5072.5 \pm 2.9$	$6146.2 \pm 9.8$
b.2 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e j$	$m_W$	5	$828.4 \pm 0.8$	$1065.3 \pm 1.8$
b.3 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e jj$	$m_W$	5	$298.8 \pm 0.4$	$300.3 \pm 0.6$
b.4 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^-$	$m_Z$	5	$1007.0 \pm 0.1$	$1170.0 \pm 2.4$
b.5 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^- j$	$m_Z$	5	$156.11 \pm 0.03$	$203.0 \pm 0.2$
b.6 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^- jj$	$m_Z$	5	$54.24 \pm 0.02$	$56.69 \pm 0.07$
c.1 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e b\bar{b}$	$m_W + 2m_b$	4	$11.557 \pm 0.005$	$22.95 \pm 0.07$
c.2 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e t\bar{t}$	$m_W + 2m_{top}$	5	$0.009415 \pm 0.000003$	$0.01159 \pm 0.00001$
c.3 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^- b\bar{b}$	$m_Z + 2m_b$	4	$9.459 \pm 0.004$	$15.31 \pm 0.03$
c.4 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^- t\bar{t}$	$m_Z + 2m_{top}$	5	$0.0035131 \pm 0.0000004$	$0.004876 \pm 0.000002$
c.5 $pp \rightarrow \gamma t\bar{t}$	$2m_{top}$	5	$0.2906 \pm 0.0001$	$0.4169 \pm 0.0003$
d.1 $pp \rightarrow W^+ W^-$	$2m_W$	4	$29.976 \pm 0.004$	$43.92 \pm 0.03$
d.2 $pp \rightarrow W^+ W^- j$	$2m_W$	4	$11.613 \pm 0.002$	$15.174 \pm 0.008$
d.3 $pp \rightarrow W^+ W^+ jj$	$2m_W$	4	$0.07048 \pm 0.00004$	$0.1377 \pm 0.0005$
e.1 $pp \rightarrow HW^+$	$m_W + m_H$	5	$0.3428 \pm 0.0003$	$0.4455 \pm 0.0003$
e.2 $pp \rightarrow HW^+ j$	$m_W + m_H$	5	$0.1223 \pm 0.0001$	$0.1501 \pm 0.0002$
e.3 $pp \rightarrow HZ$	$m_Z + m_H$	5	$0.2781 \pm 0.0001$	$0.3659 \pm 0.0002$
e.4 $pp \rightarrow HZ j$	$m_Z + m_H$	5	$0.0988 \pm 0.0001$	$0.1237 \pm 0.0001$
e.5 $pp \rightarrow Ht\bar{t}$	$m_{top} + m_H$	5	$0.08896 \pm 0.00001$	$0.09869 \pm 0.00003$
e.6 $pp \rightarrow Hb\bar{b}$	$m_b + m_H$	4	$0.16510 \pm 0.00009$	$0.2099 \pm 0.0006$
e.7 $pp \rightarrow Hjj$	$m_H$	5	$1.104 \pm 0.002$	$1.036 \pm 0.002$

# NLO and PS merging

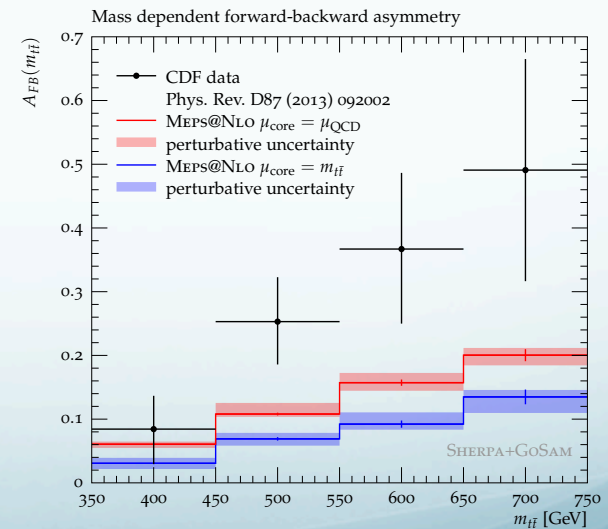
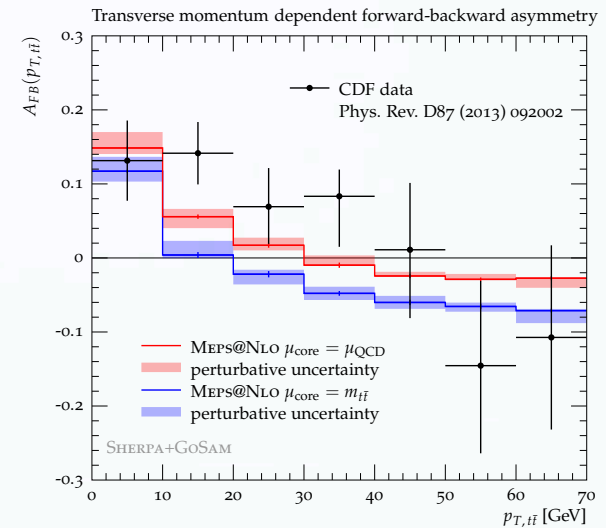
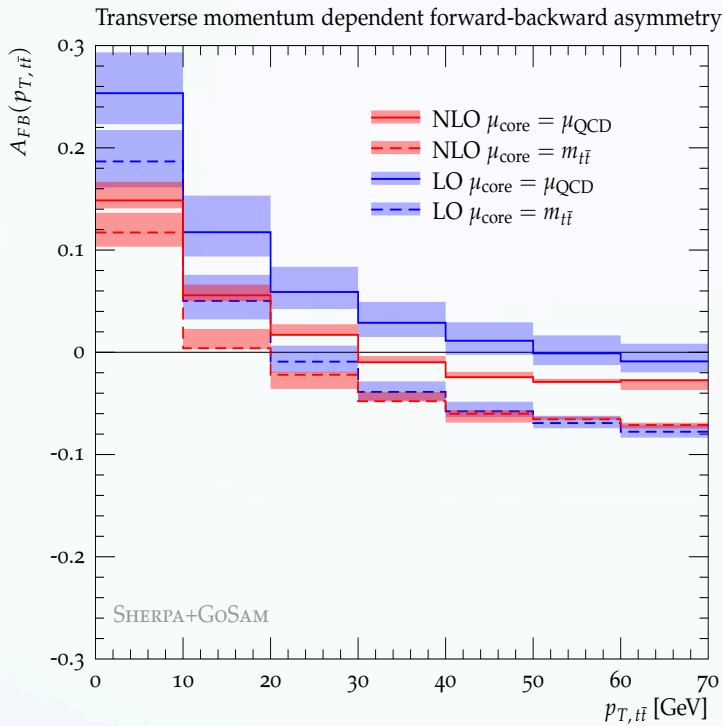
# Merging of multiple NLO QCD calculations with different jet multiplicity with PS in Sherpa

- Recent application: 0+1jet combined NLO analysis of  $A_{FB}$  in top-pair production
- MEPS@NLO: combines multiple NLO with PS => merged simulation of  $t\bar{t}$  and  $t\bar{t}$  +jet production which preserves both the NLO accuracy of the fixed-order prediction and the logarithmic accuracy of the parton shower
- GOSAM (Samurai+Golem): virtual NLO QCD corrections (interface to Sherpa with BLHA) [G.Cullen et al. 1111.2034](#)
- MC@NLO automated in Sherpa: modified subtraction to avoid overlap between NLO and PS

[S.Hoche et al, 1306.2703](#)



# $A_{FB}(P_T)$ and $A_{FB}(M_{t\bar{t}})$ : Comparison with CDF data



S.Höche et al, 1306.2703

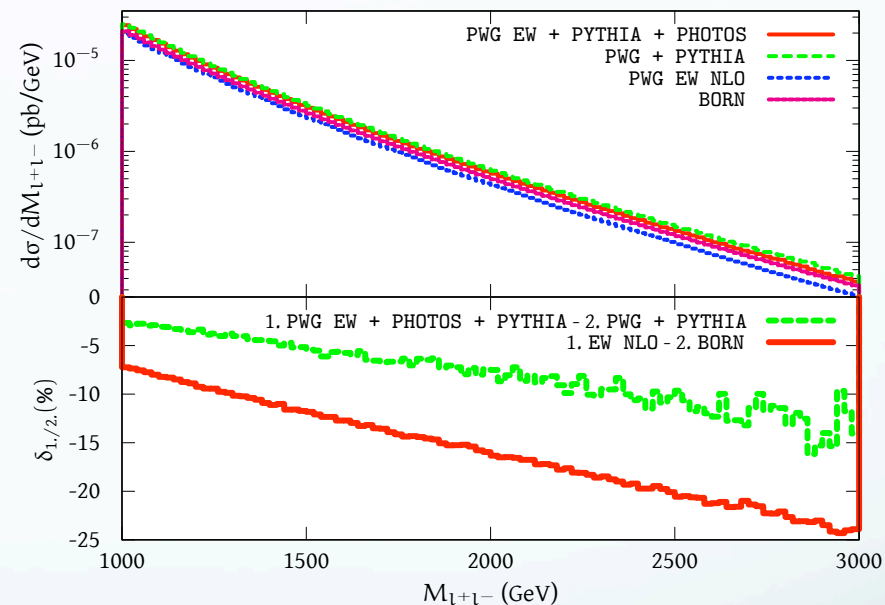
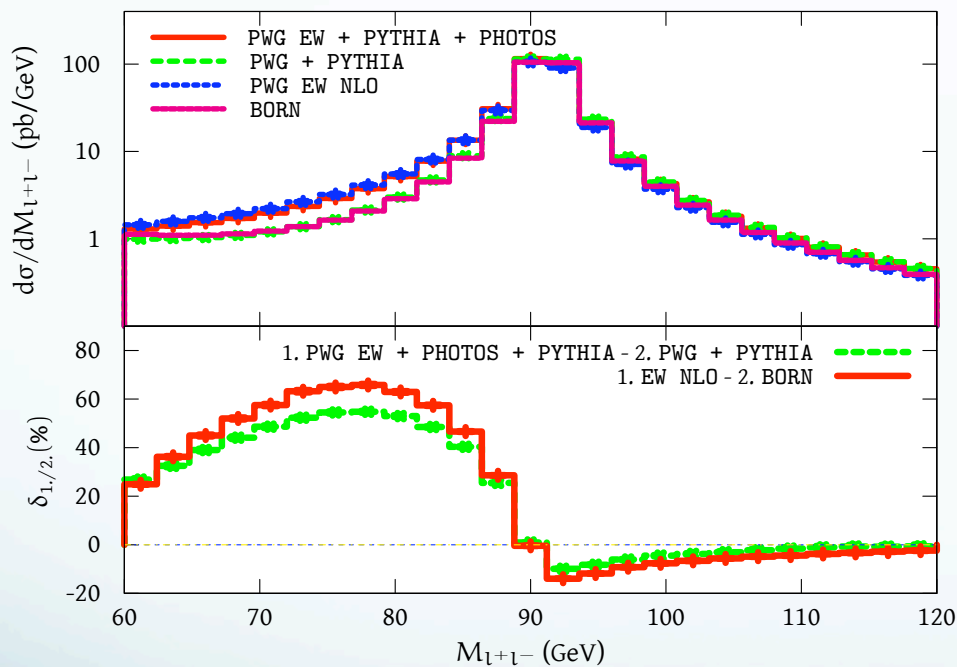
# Combining QCD and EW NLO predictions

# NLO EW×QCD to W and Z production in POWHEG

$$d\sigma = \sum_{\text{flavors}} \bar{B}(\Phi_n) d\Phi_n \left\{ \Delta(\Phi_n, p_T^{\min}) + \sum_{\alpha_r} \frac{[d\Phi_{\text{rad}} \Delta(\Phi_n, k_T > p_T^{\min}) R(\Phi_{n+1})]}{B(\Phi_n)} \right\}$$

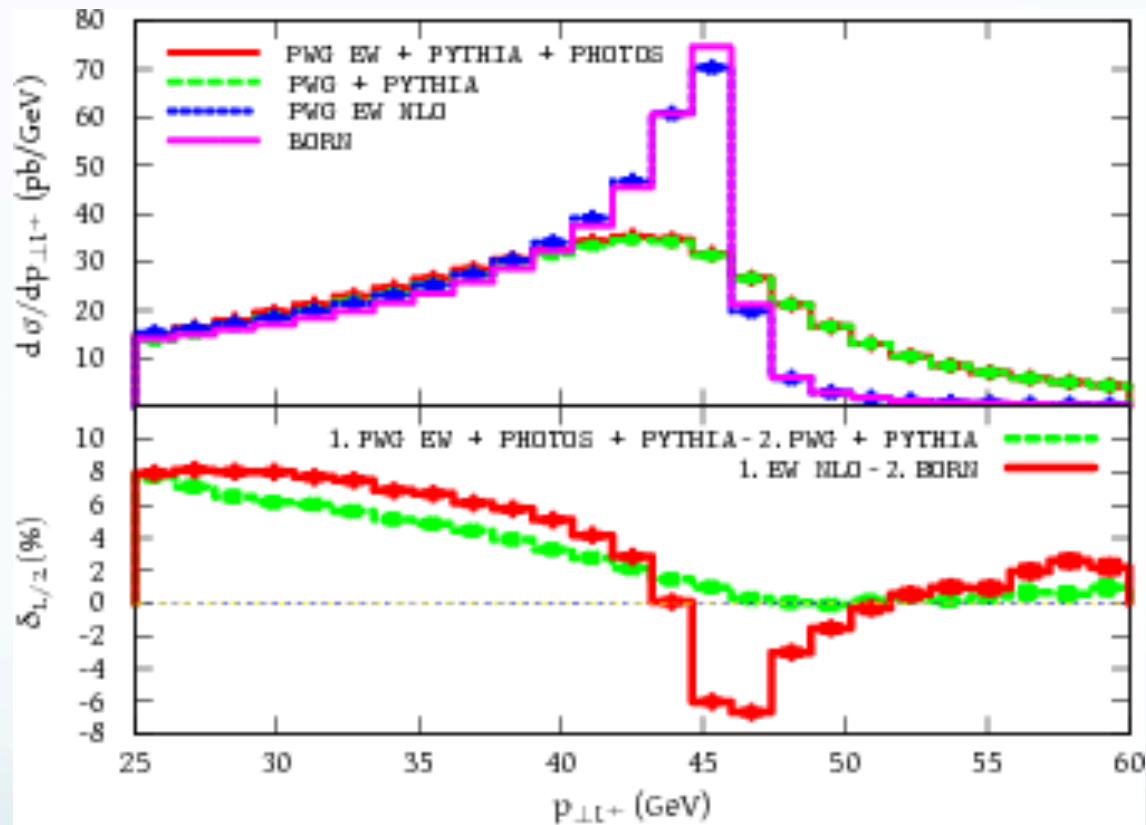
- Implementation in POWHEG-W by [Bernaciak et al 1201.4804](#) and [Barze et al. 1202.0465](#)
- **New:** Implementation in POWHEG-Z by [Barze et al, 1302.4606](#)

# Impact of NLO EW in presence of QCD corrections on $M(l\bar{l})$ in $pp \rightarrow \gamma, Z \rightarrow l^+l^-$ at the LHC



Barze *et al*, 1302.4606

# Impact of NLO EW in presence of QCD corrections on $P_T(\text{lepton})$ in $pp \rightarrow \gamma Z \rightarrow l^+ l^-$



Barze *et al*, 1302.4606

# Instead of conclusions an invitation (see also J.Rosners' talk)

- **Snowmass Study group: Quantum Chromodynamics and the Strong Force**
- **Conveners:** John Campbell, Kenichi Hatakeyama, Joey Huston, Frank Petriello
- **Selection of questions (see Snowmass webpage):** What are the prospects for future higher order calculations at NLO and matched with parton showers? What subtleties remain to be understood for precision measurements? **What is the best way to distribute the results of complex NLO, and emerging NNLO, calculations to the experimental community?** Survey of the importance of electroweak corrections (both those already calculated and possible impact of as-yet uncalculated contributions).

# Instead of conclusions an invitation

- **Snowmass study group: Precision Study of Electroweak Interactions**
- **Conveners:** Ashutosh Kotwal, Michael Schmitt, D. W.
- **Charge (see webpage for more details):** Identify the most important precision observables that can reveal deviations from the standard model. Identify the thresholds of precision that needs to be achieved for each of these observables in order to be definitively sensitive to new physics. Study the precision that can be achieved at each proposed facility on these observables, and ask what machine and detector parameters are required to reach the discovery threshold. **Identify the calculational tools needed to predict standard model rates and distributions in order to perform these measurements at the required precision.**