

CC coherent π

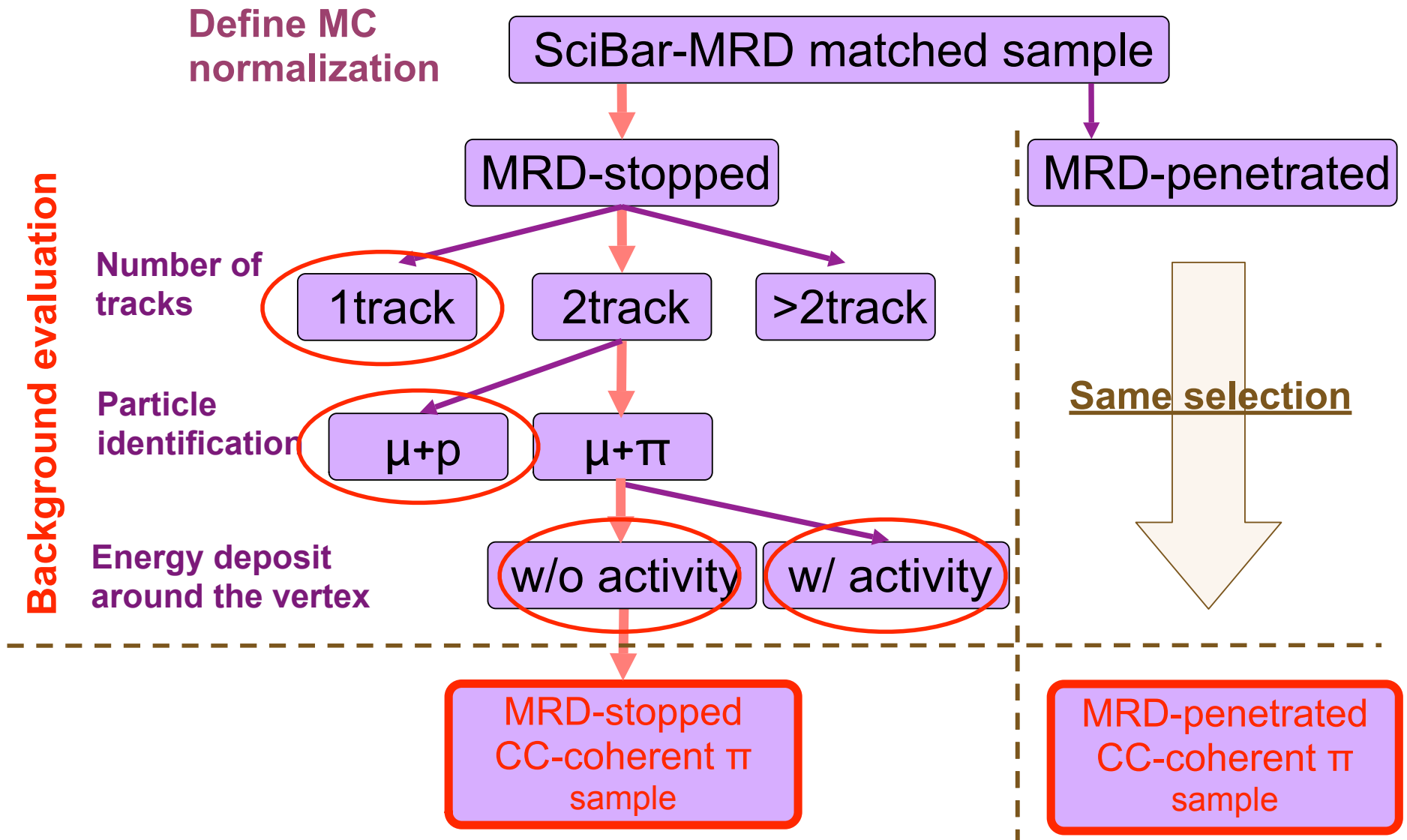
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SciBooNE Collab Mtg 2010/05/25

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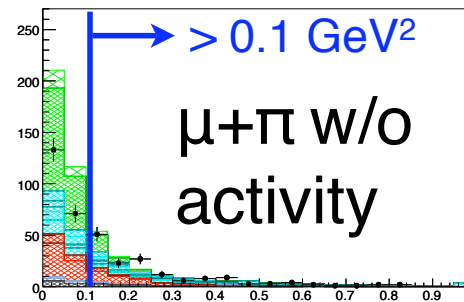
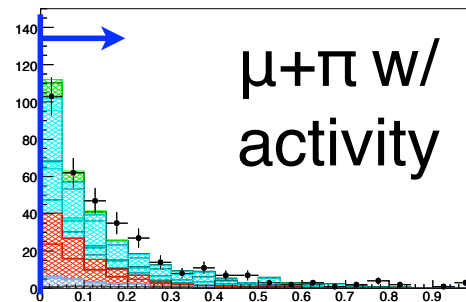
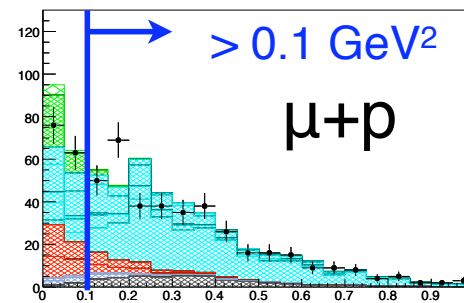
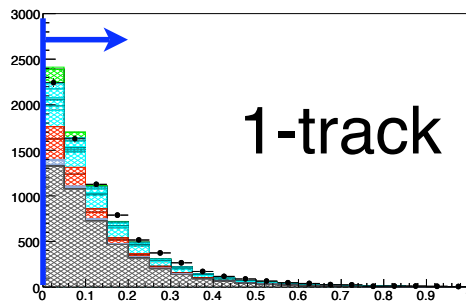
- Background evaluation (Q^2 -fit) in $\bar{\nu}$ mode

Event selection



Background evaluation

- Tune MC by fitting four Q^2 distributions with systematic parameters (fit parameters)
- Use the same χ^2 definition as in coh- π paper



χ^2 definition:

$$\chi^2 = \chi_{dist}^2 + \chi_{sys}^2$$

$$\chi_{dist}^2 = 2 \sum_{i,j} \left(N_{ij}^{exp} - N_{ij}^{obs} \times \ln \frac{N_{ij}^{obs}}{N_{ij}^{exp}} \right)$$

(use Poisson likelihood)

i : runs over four samples

j : runs over Q^2 -bins

N_{obs} : Observed #events

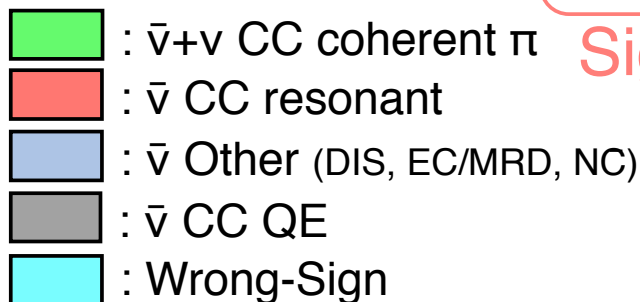
N_{exp} : Expected #events (next page)

$$\chi_{sys}^2 = (P_{sys} - P_0) V^{-1} (P_{sys} - P_0)$$

V : covariance matrix

P_0 : initial value

P_{sys} : fit parameters (next page)



Signal sample

Fit parameters

$$N_{i, 1\text{trk}}^{\text{exp}} = R_{\text{norm}} \cdot \left[n_{i, 1\text{trk}}^{\text{QE}} + R_{\text{res}} n_{i, 1\text{trk}}^{\text{res}} + R_{\text{other}} n_{i, 1\text{trk}}^{\text{other}} \right]$$

$$N_{i, \mu p}^{\text{exp}} = R_{\text{norm}} \cdot R_{2\text{trk}/1\text{trk}} \cdot R_{p/\pi} \cdot \left[n_{i, \mu p}^{\text{QE}} + R_{\text{res}} n_{i, \mu p}^{\text{res}} + R_{\text{other}} n_{i, \mu p}^{\text{other}} \right]$$

$$N_{i, \mu\pi\text{H}}^{\text{exp}} = R_{\text{norm}} \cdot R_{2\text{trk}/1\text{trk}} \cdot \left[n_{i, \mu\pi\text{H}}^{\text{QE}} + R_{\text{res}} n_{i, \mu\pi\text{H}}^{\text{res}} + R_{\text{other}} n_{i, \mu\pi\text{H}}^{\text{other}} \right]$$

$$N_{i, \mu\pi\text{L}}^{\text{exp}} = R_{\text{norm}} \cdot R_{2\text{trk}/1\text{trk}} \cdot R_{\text{act}} \cdot \left[n_{i, \mu\pi\text{L}}^{\text{QE}} + R_{\text{res}} n_{i, \mu\pi\text{L}}^{\text{res}} + R_{\text{other}} n_{i, \mu\pi\text{L}}^{\text{other}} \right]$$

new

$$n_{i, \text{sample}}^{\text{mode}} \equiv \left(n_{i, \text{sample}}^{\bar{\nu}-\text{mode}} + R_{\text{WS}} \cdot n_{i, \text{sample}}^{\nu-\text{mode}} \right)$$

new

- R_{WS} : scaling factor for Wrong-Sign (WS) events -- no constrained
- $R_{2\text{tr}/1\text{trk}}$: migration parameter between [1trk]-[2trk] samples
- $R_{p/\pi}$: migration param. between [μ +p]-[μ + π] samples
- R_{act} : migration param. between [with activity]-[w/o activity]
 - no constrained
- R_{res} : scale factor for resonant- π
- R_{other} : scale factor for “other” (\equiv multi- π , DIS, EC/MRD)
 - no constrained
- R_{pscale} : momentum scale
- R_{norm} : overall normalization -- no constrained
- κ : only for QE -- no constrained

Systematics: physics related

for covariance matrix

- Pion FSI
 - absorption, charge exchange, inelastic (variation: $\pm 30\%$)
- Nucleon FSI
 - re-scattering (variation: $\pm 10\%$)
- DIS cross section
 - (variation: $\pm 30\%$)
- non-QE/QE ratio
 - (variation: $\pm 20\%$)

Re-weighting method

for example:

$$w_{fsi} = \frac{P_{tot} - \mathcal{F}_{scale} \cdot P_{fsi}}{P_{tot} - P_{fsi}}$$

w_{fsi} : re-weighting factor

P_{tot} : probability of events w/ p/ π emission

\mathcal{F}_{scale} : scaling (e.g. 1.3 for +30% vary)

P_{fsi} : probability of p/ π FSI

Systematic errors on fit-params

~Physics related~

Source	Variation (+, -)	$\delta R_{2\text{trk}/1\text{trk}}$		$\delta R_{p/\pi}$		COV ($\times 10^{-4}$)
		+	-	+	-	
Fermi mom.	--, 212 MeV	--	TBA	--	TBA	TBA
M_A	--, 1.11 GeV	--	TBA	--	TBA	TBA
π abs.	$\pm 30\%$	-3.4%	+3.3%	+3.8%	-3.6%	-12.6
π charge ex.	$\pm 30\%$	-0.5%	+0.4%	+0.7%	-0.7%	-0.3
π inelastic	$\pm 30\%$	-1.3%	+1.1%	+1.1%	-0.9%	-1.2
Nucl. rescat.	$\pm 10\%$	-0.9%	+0.9%	+0.5%	-0.6%	+1.8
DIS x-sec	$\pm 30\%$	+0.5%	-0.5%	-0.2%	+0.2%	-0.1
nQE/QE	$\pm 20\%$	+5.5%	-5.9%	-2.8%	+3.5%	-17.9
Detector π -int	$\pm 10\%$	TBA	TBA	TBA	TBA	TBA

- Dominant systematic error on $R_{2/1\text{trk}}$ and $R_{p/\pi}$
 - pion absorption
 - non-QE/QE cross section ratio

Systematics: detector related

for covariance matrix

- Use identical NEUT vector
- Vary syst. parameters in detector simulation:
 - PMT 1 p.e. resolution (30%, 70%)
 - Scintillator quenching (0.0185, 0.0231)
 - PMT cross talk (2.75%, 3.55%)
 - Hit threshold (1.6 p.e., 2.4 p.e.) -- not done yet

Systematic errors on fit-params

~Detector response~

Source	Variation (+, -)	$\delta R_{2\text{trk}/1\text{trk}}$		$\delta R_{p/\pi}$		COV ($\times 10^{-4}$)
		+	-	+	-	
1pe resolution	70%, 30%	-0.3%	+0.3%	-1.6%	-0.3%	-0.2
Scint. quench	0.0231, 0.0185	-1.9%	+1.4%	-1.2%	-0.5%	-4.4
Hit threshold	2.4pe, 1.6pe	TBA	TBA	TBA	TBA	TBA
X-talk	3.55%, 2.75%	-1.2%	+0.7%	-6.1%	-3.2%	-2.4

- Dominant systematic error on $R_{2/1\text{trk}}$ and $R_{p/\pi}$
 - PMT cross-talk (?)
 - Scintillator quenching

In addition to these, μ -momentum scale error 2% is taken into account.

Covariance matrix

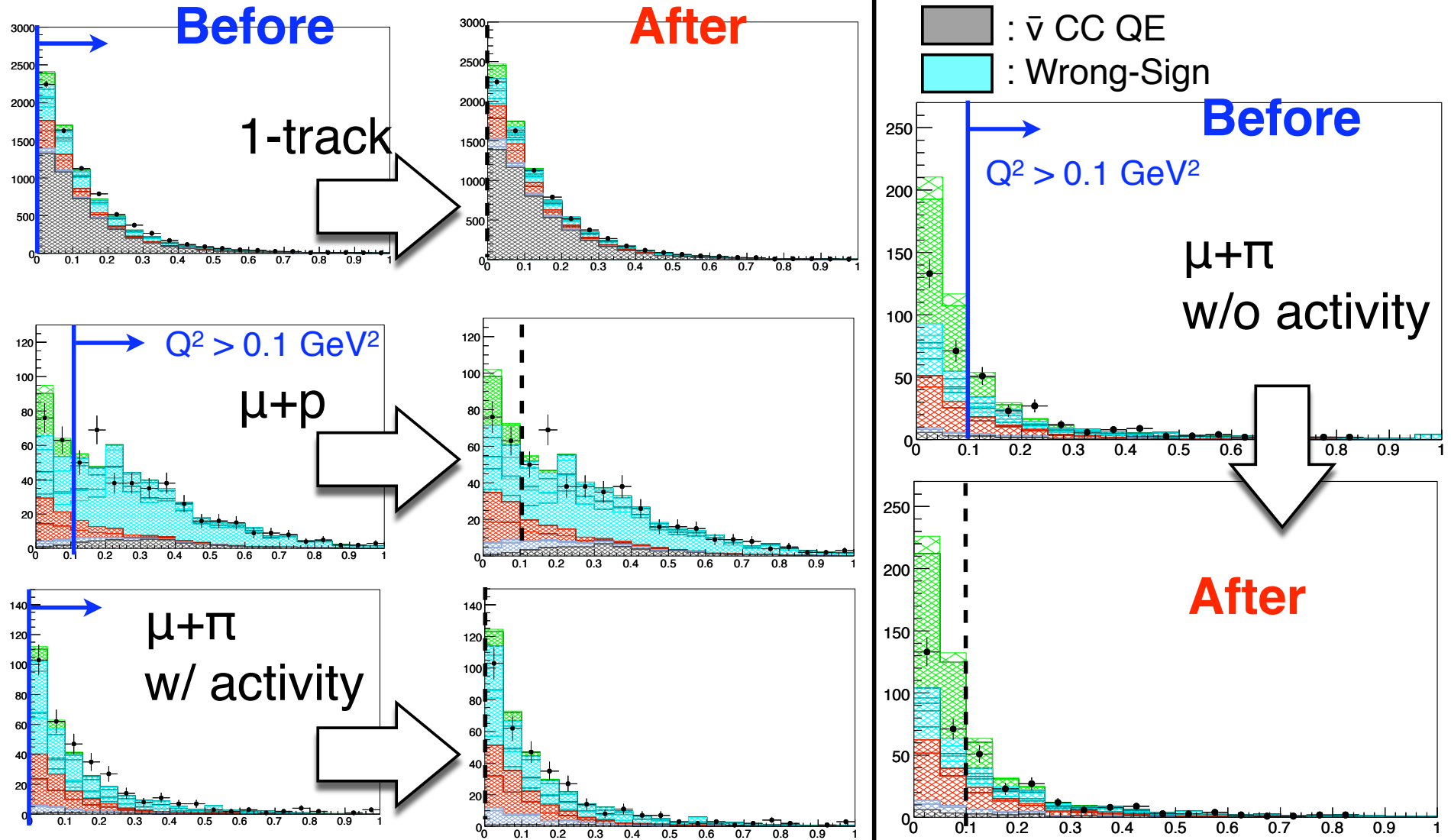
- Obtained covariance matrix:

$$V = \begin{matrix} & \begin{matrix} R_{2/1\text{-trk}} & R_{p/\pi} & R_{\text{res}} & R_{\text{pscale}} \end{matrix} \\ \begin{matrix} R_{2/1\text{-trk}} \\ R_{p/\pi} \\ R_{\text{res}} \\ R_{\text{pscale}} \end{matrix} & \begin{bmatrix} (0.071)^2 & -(0.062)^2 & (0.097)^2 & 0.0 \\ -(0.062)^2 & (0.079)^2 & -(0.072)^2 & 0.0 \\ (0.097)^2 & -(0.072)^2 & (0.157)^2 & 0.0 \\ 0.0 & 0.0 & 0.0 & (0.02)^2 \end{bmatrix} \end{matrix}$$

$$\chi_{\text{sys}}^2 = (P_{\text{sys}} - P_0)V^{-1}(P_{\text{sys}} - P_0)$$

$$P_{\text{sys}} = \begin{pmatrix} R_{2/1\text{trk}} \\ R_{p/\pi} \\ R_{\text{res}} \\ R_{\text{pscl}} \end{pmatrix} \quad P_0 = \begin{pmatrix} 1.0 \\ 1.0 \\ 1.0 \\ 1.0 \end{pmatrix}$$

Fit results



• χ^2/ndf : $162/75=2.16 \rightarrow 77/66=1.17$

Fit results

Antineutrino mode

Note: not full sys err yet

Param	Value	Error
R _{norm}	1.107	0.031
R _{2trk/1trk}	1.034	0.047
R _{pπ}	0.984	0.063
R _{act}	0.996	0.076
R _{pscale}	1.029	0.002
R _{res}	1.070	0.104
R _{other}	1.82	0.449
Kappa	1.056	0.014
R _{ws}	0.71	0.099

- Before: $\chi^2/\text{ndf} = 162/75=2.16$
- After: $\chi^2/\text{ndf} = 77/66=1.17$

cf. Neutrino mode

Param	Value	Error
R _{norm}	1.025	0.028
R _{2trk/1trk}	0.905	0.037
R _{pπ}	0.985	0.046
R _{act}	1.032	0.061
R _{pscale}	1.032	0.002
R _{res}	1.195	0.101
R _{other}	1.58	0.144
Kappa	1.020	0.005

- Before: $\chi^2/\text{ndf} = 423/75=5.64$
- After: $\chi^2/\text{ndf} = 152/67=2.27$

Error matrix

	R_{norm}	$R_{2/1\text{trk}}$	$R_{p\pi}$	R_{res}	R_{pscale}	Kappa	R_{act}	R_{other}	R_{ws}
R_{norm}	1.000	0.086	0.084	-0.064	-0.026	0.360	0.411	-0.467	-0.326
$R_{2/1\text{trk}}$	0.086	1.000	-0.584	0.669	-0.047	0.012	-0.413	-0.437	-0.164
$R_{p\pi}$	0.084	-0.584	1.000	-0.180	0.226	-0.000	0.451	0.378	-0.442
R_{res}	-0.064	0.669	-0.180	1.000	0.027	0.007	-0.302	-0.425	-0.286
R_{pscale}	-0.026	-0.047	0.226	0.027	1.000	-0.036	0.051	0.354	-0.413
Kappa	0.360	0.012	-0.000	0.007	-0.036	1.000	0.051	-0.058	-0.076
R_{act}	0.411	-0.413	0.451	-0.302	0.051	0.051	1.000	-0.040	-0.238
R_{other}	-0.467	-0.437	0.378	-0.425	0.354	-0.058	-0.040	1.000	-0.309
R_{ws}	-0.326	-0.164	-0.442	-0.286	-0.413	-0.076	-0.238	-0.309	1.000

Large correlations in:

$$R_{\text{res}} \Leftrightarrow R_{2/1\text{trk}}, R_{p/\pi} \Leftrightarrow R_{2/1\text{trk}}$$

$$R_{\text{other}} \Leftrightarrow [R_{\text{norm}}, R_{2/1\text{trk}}, R_{p/\pi}, R_{\text{res}}]$$

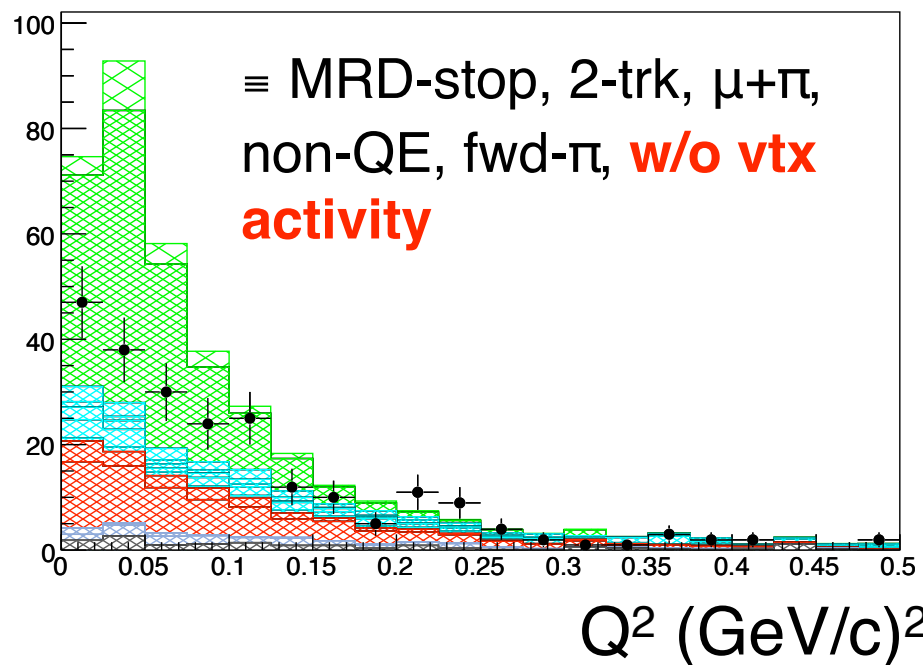
$$R_{\text{act}} \Leftrightarrow [R_{\text{norm}}, R_{2/1\text{trk}}, R_{p/\pi}, R_{\text{res}}]$$

$$R_{\text{ws}} \Leftrightarrow [R_{\text{norm}}, R_{p/\pi}, R_{\text{res}}, R_{\text{other}}] \text{ -- all negative corr}$$

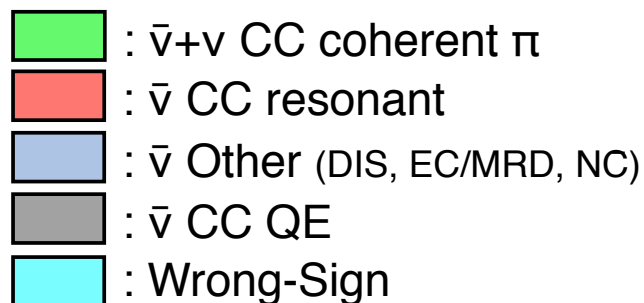
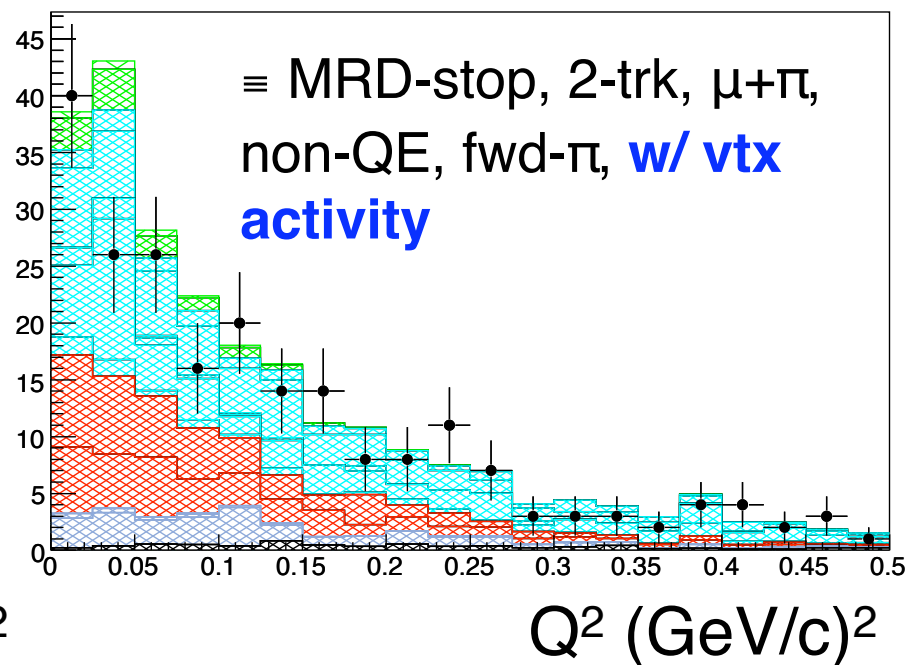
Reconstructed Q^2 dist

After fit

Coherent- π sample

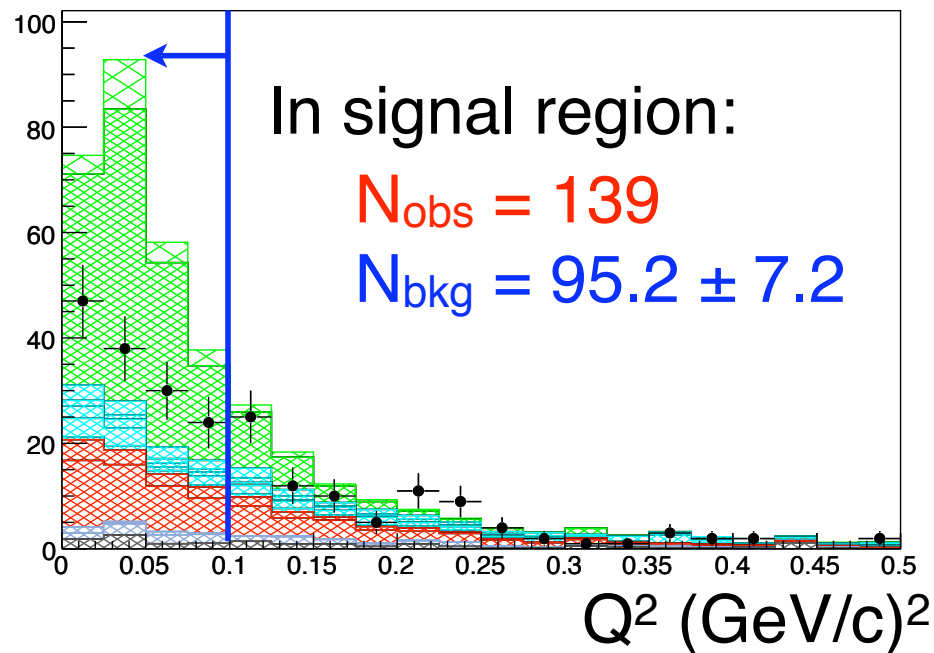


Coherent- π counter-sample



Number of events in coherent- π sample

Signal region $\equiv Q^2 < 0.1 \text{ (GeV/c)}^2$

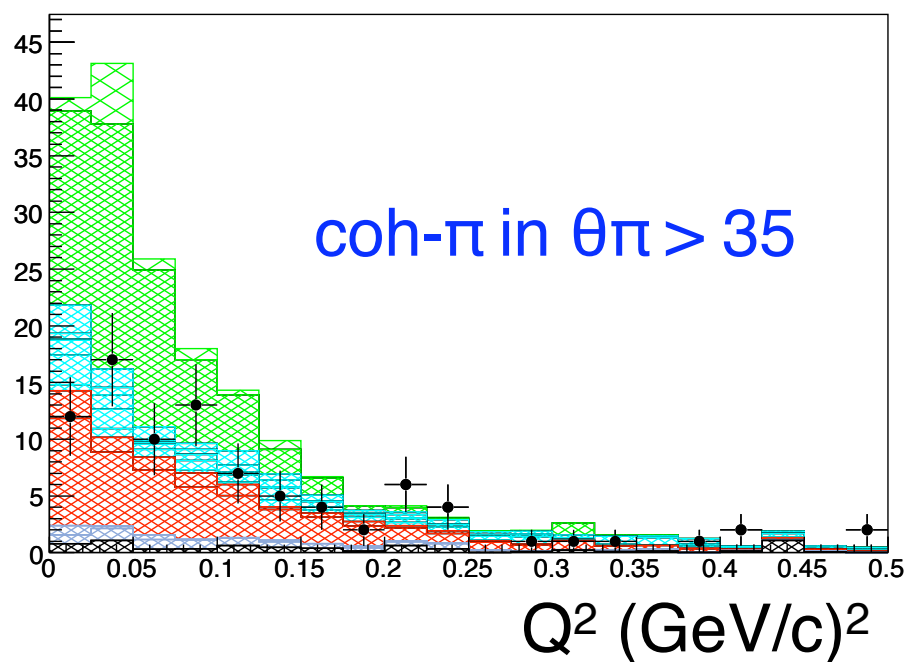
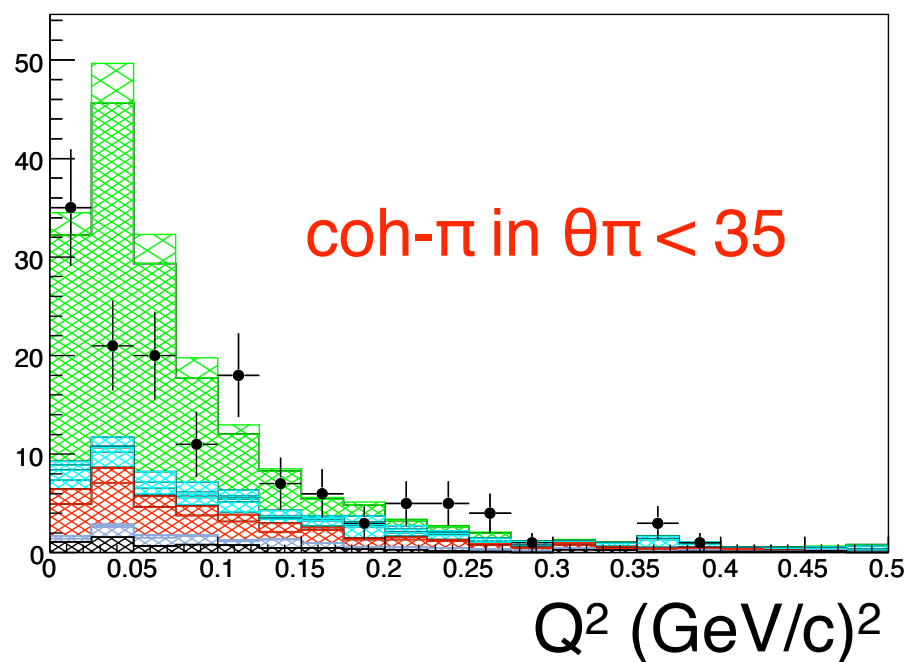


● !

Quick look...



- Divide coh- π sample (after fit) into two subsamples:
[$\theta\pi < 35$] and [$\theta\pi > 35$]



- !!

Summary

- Need to do...
 - $\bar{\nu}$ mode analysis:
 - Add remaining syst. errors to Q^2 -fit:
 - Fermi mom, M_A , Detector pion abs, Hit threshold
 - Reliability test of Q^2 -fit (background evaluation)
 - Cross section ratio
 - MC processing are underway
 - Look at distributions (other than Q^2)
 - ν & $\bar{\nu}$ systematic errors
 - Packing, packing, packing, packing,