

$$\left|\partial_y e^{iny/R}\right|^2 = \frac{n^2}{R^2}$$