

$$\Rightarrow (p^2 + \partial_y^2) f_n(y) = 0$$