$$+ \mathcal{L}_L(\Phi(x, y = L), \chi(x))]$$