

# A WIMPy Leptogenesis Miracle

Baryogenesis via WIMP freeze-out

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SUSY 2011  
August 31, 2011

# Outline

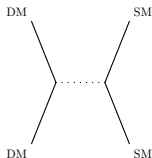
- Motivation
- Overview of WIMPy baryogenesis
- Toy model of WIMPy leptogenesis
- Detection possibilities

# Motivation

- There is a remarkable coincidence between the dark matter and baryon densities

$$\Omega_{\text{DM}} \approx 5 \Omega_{\text{baryon}}$$

- Traditional models of WIMP dark matter do not address this coincidence
  - ▶ Dark matter is a thermal relic
  - ▶ Relic density set by annihilation cross section: **WIMP miracle**



$$\frac{n_{\text{DM}}}{s} \propto \frac{1}{\sigma_{\text{ann}}}$$

# Motivation

- Nearly all models explaining the DM-baryon ratio use **asymmetric dark matter**
- Compelling scenario with many possible mechanisms and models
  - ▶ Transfer of the  $B$  asymmetry to dark matter
  - ▶ Transfer of a dark matter asymmetry to  $B$
  - ▶ Co-generation of the asymmetries
- New work: transfer by mass mixing (see arXiv:1106.4834 and Yanou's talk)

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(For more info, see SPIRES: [“find t asymmetric dark matter”](#) and references cited therein)

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However, asymmetric dark matter models give up the **WIMP miracle**.

# WIMPy baryogenesis

We present a model of **symmetric** DM that preserves the WIMP miracle and gives a connection between the DM and baryon densities.

## WIMPy baryogenesis:

- WIMP dark matter annihilates through baryon-violating couplings
- Physical  $CP$  phases in annihilation operators
- Out-of-equilibrium condition satisfied by WIMP freeze-out

*WIMP freeze-out can generate a baryon asymmetry!*

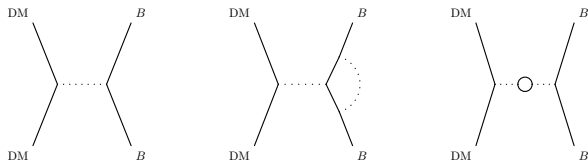
Also, baryogenesis is around the weak scale  $\Rightarrow$  new charged states and  $CP$ -phases

Asymmetry generation through annihilation first proposed by [Gu and Sarkar, 2009](#)

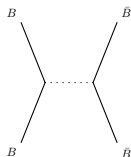
For another way of connecting the WIMP miracle and baryon density, see [McDonald, 1009.3227](#) and [1108.4653](#)

# Overview of WIMPy baryogenesis

Baryon asymmetry comes from interference of tree-level and loop annihilation diagrams:



The baryon-violating coupling also leads to washout processes:





# Overview of WIMPy baryogenesis: evolution

Consider dark matter particle  $X$

Boltzmann equations:

In terms of  $Y_i = n_i/s$  and  $x = m_X/T$ , the evolution is schematically:

$$\begin{aligned}\frac{dY_X}{dx} &= -A \langle \sigma_{\text{ann}} v \rangle [Y_X^2 - (Y_X^{\text{eq}})^2] + \text{back-reaction} \\ \frac{dY_{\Delta B}}{dx} &= \epsilon A \langle \sigma_{\text{ann}} v \rangle [Y_X^2 - (Y_X^{\text{eq}})^2] - C \langle \sigma_{\text{washout}} v \rangle Y_{\Delta B} \prod_i Y_i^{\text{eq}}\end{aligned}$$

- $\epsilon$  = fractional asymmetry produced per annihilation
- $A$  and  $C$  are coefficient functions including factors of  $s$ ,  $H$ , ...
- $Y_i$  are other baryon-number-carrying fields

# Overview of WIMPy baryogenesis: asymmetry

In the limit where back-reaction on  $X$  is small,

$$Y_{\Delta B}(x) \approx -\epsilon \int_0^x dx' \frac{dY_X(x')}{dx'} \exp \left[ - \int_{x'}^x dx'' C \langle \sigma_{\text{washout}} v \rangle \prod_i Y_i^{\text{eq}}(x'') \right]$$

Approximate  $\exp(\dots) \approx \theta(x - x_0)$ , where  $x_0$  is the time of washout freeze-out:

$$Y_{\Delta B}(x) \approx \epsilon [Y_X(x_0) - Y_X(x)] \theta(x - x_0)$$

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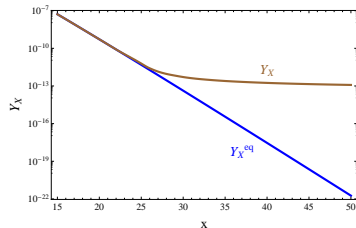
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*Asymmetry proportional to **change** in  $X$  density after washout processes freeze out*

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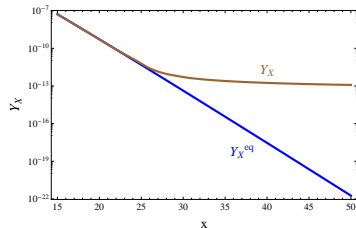
- Washout must freeze out before annihilations

$$Y_{\Delta B} \sim 10^{-10} \text{ and } \epsilon < 1 \Rightarrow x_0 \lesssim 20$$

Two possibilities for successful baryogenesis:

# Overview of WIMPy baryogenesis: asymmetry

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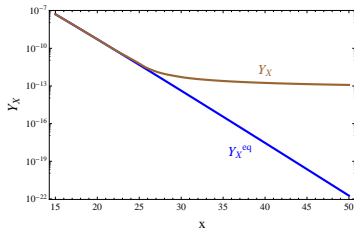
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Two possibilities for successful baryogenesis:

- 1  $\sigma_{\text{ann}} \gg \sigma_{\text{washout}}$

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Two possibilities for successful baryogenesis:

- 1  $\sigma_{\text{ann}} \gg \sigma_{\text{washout}}$
- 2 Heavy baryon states so that washout rate is Boltzmann suppressed

# Toy model: WIMPy leptogenesis

Toy model of annihilation to **leptons**:

- Vectorlike dark matter  $X, \bar{X}$
- Heavy pseudoscalars  $S_i$  (at least 2 needed for physical  $CP$  phase)
- Dark matter annihilates to Standard Model LH lepton doublet  $L_j$
- Vectorlike exotic lepton doublet  $\psi_j, \bar{\psi}_j$  (with lepton flavor charge)

$$\mathcal{L} \supset \mathcal{L}_{\text{mass}} - \frac{i}{2} (y_{X_i} X^2 + y'_{X_i} \bar{X}^2) S_i - i y_{L_{ij}} S_i L_j \psi_j + \text{h.c.}$$

Lepton asymmetry converted to baryon asymmetry by sphalerons

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Lepton asymmetry converted to baryon asymmetry by sphalerons

$$\sigma_{\text{ann}} \sim y_X^2 y_L^2$$

$$\sigma_{\text{washout}} \sim y_L^4$$



## Toy model: WIMPy leptogenesis

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- In this model,  $\psi$  carries generalized lepton number  $-1$
- $\psi$  decays to sterile sector with separately conserved global symmetry, asymmetry in sterile sector equal and opposite to SM lepton asymmetry  
ex. gauge singlet fermion  $n$

$$\mathcal{L} \supset y_n \psi H^\dagger n$$

# Toy model: WIMPy leptogenesis

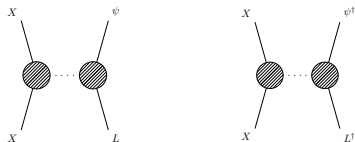
$Z_4$  symmetry:

- $X$  and  $n$  stable
- Prevent  $L - \bar{\psi}$  mixing

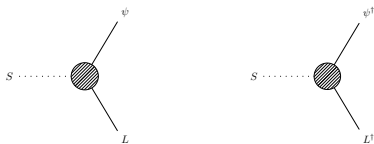
	$Z_4$
$X$	$i$
$\bar{X}$	$-i$
$S$	$-1$
$\psi$	$-1$
$\bar{\psi}$	$-1$
$n$	$-1$
SM fields	$+1$

# Toy model: asymmetry generation processes

Dark matter annihilations:

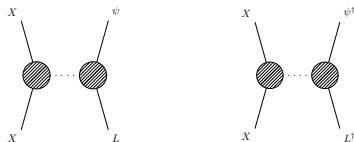


Decays and inverse decays:

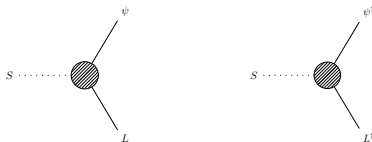


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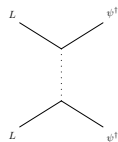
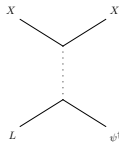
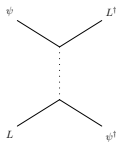
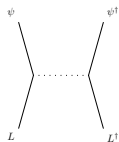
Decays and inverse decays:



For weak scale masses and couplings,  $\Gamma_S \gg H$  and asymmetry from decays is negligible

# Toy model: washout processes

Washout processes:



## Toy model: $CP$ -violation

$CP$ -violating factor:

$$\epsilon = \frac{\sigma(\mathbf{XX} \rightarrow \psi_i L_i) + \sigma(\bar{\mathbf{X}}\bar{\mathbf{X}} \rightarrow \psi_i L_i) - \sigma(\mathbf{XX} \rightarrow \psi_i^\dagger L_i^\dagger) - \sigma(\bar{\mathbf{X}}\bar{\mathbf{X}} \rightarrow \psi_i^\dagger L_i^\dagger)}{\sigma(\mathbf{XX} \rightarrow \psi_i L_i) + \sigma(\bar{\mathbf{X}}\bar{\mathbf{X}} \rightarrow \psi_i L_i) + \sigma(\mathbf{XX} \rightarrow \psi_i^\dagger L_i^\dagger) + \sigma(\bar{\mathbf{X}}\bar{\mathbf{X}} \rightarrow \psi_i^\dagger L_i^\dagger)}$$

There are many parameters! We make the assumptions

- Only one flavour of  $L$  relevant for WIMPy leptogenesis
- Annihilation through the lightest scalar  $S_1$  is dominant

Treat  $y_L = y_{L1}$  and  $\epsilon$  as free parameters subject to the above conditions and perturbativity

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$$\epsilon = \frac{1}{8\pi} \frac{\text{Im}(y_{L1}^2 y_{L2}^{*2})}{|y_{L1}|^2} f\left(\frac{m_{S1}}{m_{S2}}\right)$$

( $f$  is a loop function)

## Toy model: $CP$ -violation

- Solve Boltzmann equations numerically:

$$\begin{aligned}\frac{dY_X}{dx} &= -A \langle \sigma_{\text{ann}} v \rangle \left[ Y_X^2 - (Y_X^{\text{eq}})^2 \right] + B \langle \sigma_{\text{ann}} v \rangle Y_{\Delta L} (Y_X^{\text{eq}})^2 \\ \frac{dY_{\Delta L}}{dx} &= \epsilon A \langle \sigma_{\text{ann}} v \rangle \left[ Y_X^2 - (Y_X^{\text{eq}})^2 \right] - C \langle \sigma_{\text{washout}} v \rangle Y_{\Delta L} Y_L^{\text{eq}} Y_\psi^{\text{eq}}\end{aligned}$$



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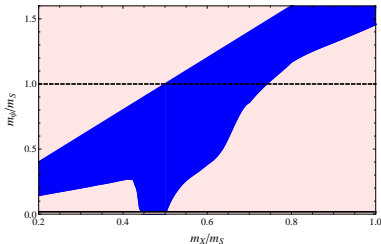
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- Also include effects of other equilibrium interactions (sphalerons and Yukawas) by including a **pre-factor** in the  $Y_{\Delta L}$  equation
  - ▶ Some of the  $L$  asymmetry is converted to asymmetry in  $\bar{E}$ ,  $Q$ ,  $\bar{d}$ ,  $\bar{u}$
  - ▶ Chemical potential relations come from sphalerons, Yukawas, conservation of gauge charges, conservation of  $U(1)_{B-L+n-\psi}$

## Toy model: Parameter scan

- 6 parameters:  $m_X$ ,  $m_\psi$ ,  $m_S$ ,  $y_X$ ,  $y_L$ , and  $\epsilon$
- Show masses for which WIMP $\psi$  leptogenesis gives correct relic density and asymmetry for which at least **one** set of perturbative couplings  $y_L$ ,  $y_X$ , and  $\epsilon$

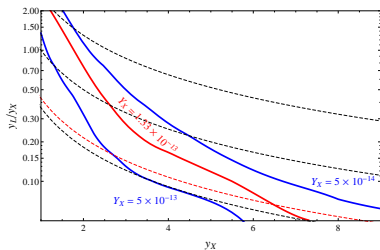


- $X$  and  $\psi$  mass typically constrained to lie within factor of a few
- Enhancement of  $\sigma_{\text{ann}}$  around  $m_X = m_S/2$  gives more parameter space there

- $m_S = 5$  TeV
- Asymmetry should be generated before sphalerons decouple  $\Rightarrow m_X \gtrsim \text{TeV}$

# Toy model: Parameter scan

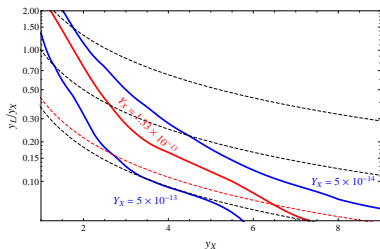
- How **tuned** do couplings have to be?
- Choose point in middle of parameter space
  - ▶  $m_X = 3 \text{ TeV}$ ,  $m_\psi = 4 \text{ TeV}$ ,  $m_S = 5 \text{ TeV}$ ,  $\epsilon = 0.1$



- Solid lines:  $X$  relic abundance
- Dotted lines: baryon asymmetry (from top,  $Y_{\Delta B} = 10^{-11}$ ,  $3 \times 10^{-11}$ ,  $8.85 \times 10^{-11}$ ,  $10^{-10}$ )
- Observed values shown in red

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- 
- Tuning of  $\sim 5\%$  to get observed values
  - Tuning more severe for lighter  $m_\psi$ , less severe for heavier  $m_\psi$
  - Less tuning for lighter  $m_X$  because  $Y_X$  is larger and washout is smaller due to large  $S$  width

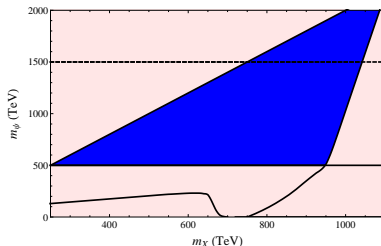
## Variations: annihilations to quarks

Dark matter can annihilate directly to quarks

- $\psi$  is now a colour triplet

$$W \supset y_{\bar{u}} S \psi \bar{u} + y_{\bar{d}} \bar{\psi} \bar{d} \bar{d}$$

- Asymmetry can be generated **after** sphalerons become inactive
- Collider constraint  $m_{\psi} \gtrsim 500$  GeV
- $X$  can be as light as 250 GeV

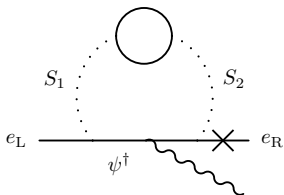


**PRELIMINARY!**

- Parameter space similar to that of toy model

## Detection: electric dipole moments

Contributions to electric dipole moments ( $e^-$  and neutron) are at two loops



$$\frac{d}{e} \sim \sum_i \frac{\text{Im}(y_{L11} y_{L21}^* y_{L1i} y_{L2i}^*)}{(16\pi^2)^2} \frac{m_e}{m_S^2}$$

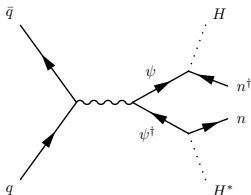
- Constraints depend predominantly on coupling to first-generation quarks/leptons
- ex. need  $y_{L1i} \lesssim 10^{-2} - 1$  for  $m_S = 5$  TeV from neutron/electron EDM
- For couplings near the current constraints, could see in next generation experiments

## Detection: colliders

New charged particles with TeV-scale mass

- Accessible at LHC?

## Leptogenesis case

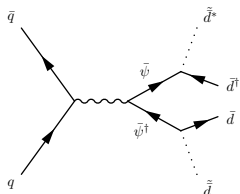


- Higgsino-like topology
- Signature is  $2b\bar{b} + \cancel{E_T}$

- No explicit bound on direct Higgsino production
- In principle bounded by gluino searches
  - ▶ Better to add  $b$ -tags,  $H$  mass reconstruction, etc.
- Also look for decay of charged  $\psi$  through longitudinal  $W$ 
  - ▶ 3-body decay to  $b\bar{b}W$  and/or 2-body decay to  $b\bar{c}$

# Detection: colliders

## Direct baryogenesis case



- Gluino-like topology with different group theory factors
- $4j + \cancel{E}_T$  final state
- Current LHC bound excludes  $m_\psi \lesssim 500$  GeV

LHC should (hopefully) eventually test  $m_\psi$  up to  $\sim 3$  TeV



# Conclusions

- WIMPy baryogenesis: WIMP annihilations can generate a baryon asymmetry
- Generate baryon asymmetry at weak scale (directly or via leptogenesis)
- Predicts new TeV-scale gauge-charged particles
- Toy model representative of models of WIMPy baryogenesis
- Possible signals in EDM experiments and at the LHC

# Back-up slides

Back-up slides

# Back-up slides: Boltzmann equations

$$\begin{aligned} \frac{H(m_X)}{x} \frac{dY_X}{dx} &= -4s \langle \sigma_{XX \rightarrow L_i \psi_i} \nu \rangle [Y_X^2 - (Y_X^{\text{eq}})^2] - 2s \epsilon \frac{\xi Y_{\Delta L_i}}{Y_\gamma} \langle \sigma_{XX \rightarrow L_i \psi_i} \nu \rangle (Y_X^{\text{eq}})^2 \\ &\quad - \text{Br}_X^2 \langle \Gamma_S \rangle Y_S^{\text{eq}} \left( \frac{Y_X}{Y_X^{\text{eq}}} \right)^2 + \text{Br}_X \langle \Gamma_S \rangle (Y_S - \text{Br}_L Y_S^{\text{eq}}) - \epsilon \frac{\xi Y_{\Delta L_i}}{2Y_\gamma} \text{Br}_X \text{Br}_L \langle \Gamma_S \rangle Y_S^{\text{eq}}; \end{aligned}$$

$$\frac{H(m_X)}{x} \frac{dY_S}{dx} = -\langle \Gamma_S \rangle Y_S + \langle \Gamma_S \rangle Y_S^{\text{eq}} \left[ \text{Br}_L + \text{Br}_X \left( \frac{Y_X}{Y_X^{\text{eq}}} \right)^2 \right];$$

$$\begin{aligned} \frac{H(m_X)}{x \eta} \frac{dY_{\Delta L_i}}{dx} &= \frac{\epsilon}{2} \text{Br}_L \langle \Gamma_S \rangle \left[ Y_S + Y_S^{\text{eq}} \left( 1 - 2\text{Br}_L - \text{Br}_X \left[ 1 + \frac{Y_X^2}{(Y_X^{\text{eq}})^2} \right] \right) \right] + 2s \epsilon \langle \sigma_{XX \leftrightarrow L_i \psi_i} \nu \rangle [Y_X^2 - (Y_X^{\text{eq}})^2] \\ &\quad - \frac{\xi Y_{\Delta L_i}}{Y_\gamma} \left[ s \langle \sigma_{XX \leftrightarrow L_i \psi_i} \nu \rangle (Y_X^{\text{eq}})^2 + 2s [ \langle \sigma_{L_i \psi_i \leftrightarrow L_i^\dagger \psi_i^\dagger} \nu \rangle + \langle \sigma_{L_i \psi_i \leftrightarrow L_j^\dagger \psi_j^\dagger}^{(i \neq j)} \nu \rangle ] Y_L^{\text{eq}} Y_\psi^{\text{eq}} \right] \\ &\quad - \frac{2\xi Y_{\Delta L_i}}{Y_\gamma} s \langle \sigma_{L_i \psi_j \leftrightarrow L_j^\dagger \psi_i^\dagger} \nu \rangle Y_L^{\text{eq}} Y_\psi^{\text{eq}} \\ &\quad - \frac{\xi Y_{\Delta L_i}}{Y_\gamma} \left[ s \langle \sigma_{X \psi_i \leftrightarrow X L_i^\dagger} \nu \rangle Y_X Y_\psi^{\text{eq}} + 2s \langle \sigma_{\psi_i \psi_j \leftrightarrow L_i^\dagger L_j^\dagger} \nu \rangle (Y_\psi^{\text{eq}})^2 + 2s \langle \sigma_{\psi_i \psi_j \leftrightarrow L_i^\dagger L_j^\dagger}^{(i \neq j)} \nu \rangle (Y_\psi^{\text{eq}})^2 \right] \\ &\quad + \frac{\epsilon^2 \xi Y_{\Delta L_i}}{4Y_\gamma} \text{Br}_L^2 \langle \Gamma_S \rangle Y_S^{\text{eq}}. \end{aligned}$$

# Back-up slides: chemical potential relations

- 1 The  $\psi$  mass:  $\mu_\psi = -\mu_{\bar{\psi}}$ .
- 2 The SU(2) sphalerons:  $3\mu_Q + \mu_L = 0$ .
- 3 The up quark Yukawa:  $\mu_Q + \mu_H - \mu_u = 0$ .
- 4 The down quark Yukawa:  $\mu_Q - \mu_H - \mu_d = 0$ .
- 5 The lepton Yukawa:  $\mu_L - \mu_H - \mu_E = 0$ .
- 6 The  $\psi$  Yukawa:  $\mu_\psi - \mu_H + \mu_\chi = 0$ .
- 7 Hypercharge conservation:  
$$\mu_Q + 2\mu_u - \mu_d - \mu_L - \mu_E + (\mu_\psi - \mu_{\bar{\psi}}) \times (n_\psi^{\text{eq}}/n_\gamma^{\text{eq}}) + 2\mu_H/3 = 0.$$
- 8 Conservation of generalized  $B + \psi - L - \chi$  symmetry:  
$$2\mu_Q + \mu_u + \mu_d - 2\mu_L - \mu_E - \mu_\chi + 2(\mu_\psi - \mu_{\bar{\psi}}) \times (n_\psi^{\text{eq}}/n_\gamma^{\text{eq}}) = 0.$$

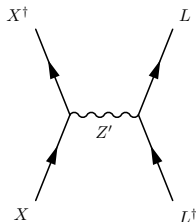
## Back-up slides: chemical potential solutions

$$\begin{aligned}\mu_Q &= -\frac{1}{3} \mu_L, \\ \mu_u &= \frac{5 - 19r}{21 + 84r} \mu_L, \\ \mu_d &= -\frac{19 + 37r}{21 + 84r} \mu_L, \\ \mu_E &= \frac{3 + 25r}{7 + 28r} \mu_L, \\ \mu_H &= \frac{4 + 3r}{7 + 28r} \mu_L, \\ \mu_\chi &= -\frac{79 - 9r}{21 + 84r} \mu_L \\ \mu_\psi &= \frac{13}{3 + 12r} \mu_L,\end{aligned}$$

## Variations: new annihilation channels

What happens if we move beyond the minimal model?

- May generically expect additional annihilation channels



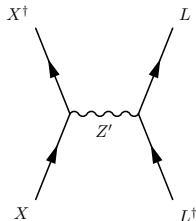
- DM relic density constraints mean that lepton violating coupling is smaller  $\Rightarrow$  less washout
- If  $\sigma_{\text{ann}} \rightarrow \alpha \sigma_{\text{ann}}$ , then  $Y_{\Delta L} \rightarrow Y_{\Delta L}/\alpha$

Does smaller  $y_L$  compensate for smaller  $Y_{\Delta L}$ ?

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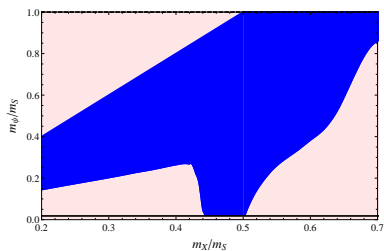
Does smaller  $y_L$  compensate for smaller  $Y_{\Delta L}$ ?

- Yes, if  $m_\psi \ll m_X$

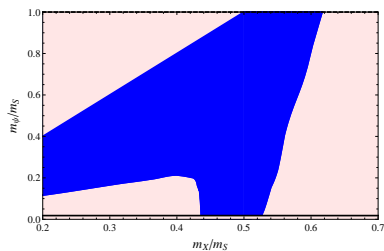
# Variations: new annihilation channels

$$m_S = 5 \text{ TeV}$$

$$\alpha = 1$$



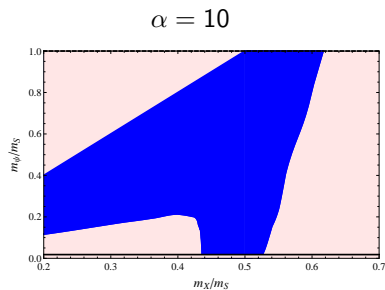
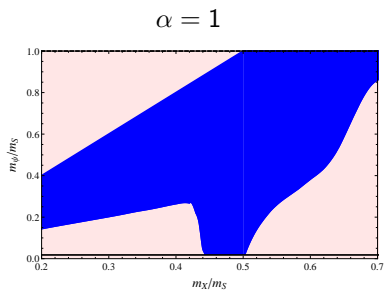
$$\alpha = 10$$





# Variations: new annihilation channels

$$m_S = 5 \text{ TeV}$$



- More parameter space open at low  $m_X$ ,  $m_\psi$
- More restricted at high  $m_X$ ,  $m_\psi$