

# Inflation

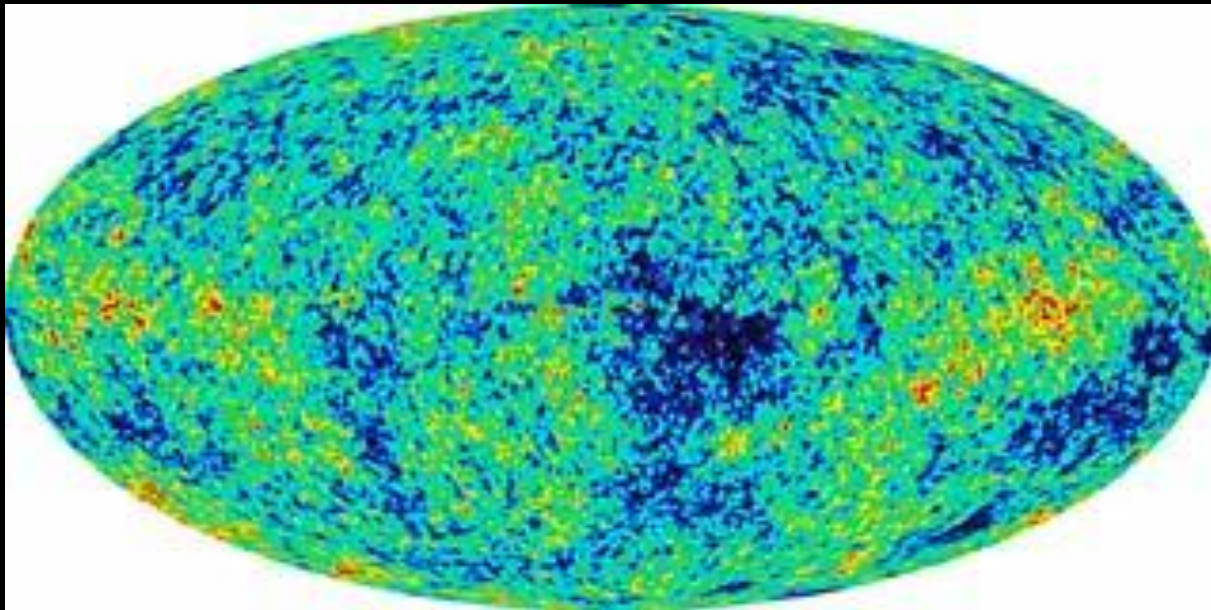
Evidence

Gravitational Waves

Non-Gaussianity

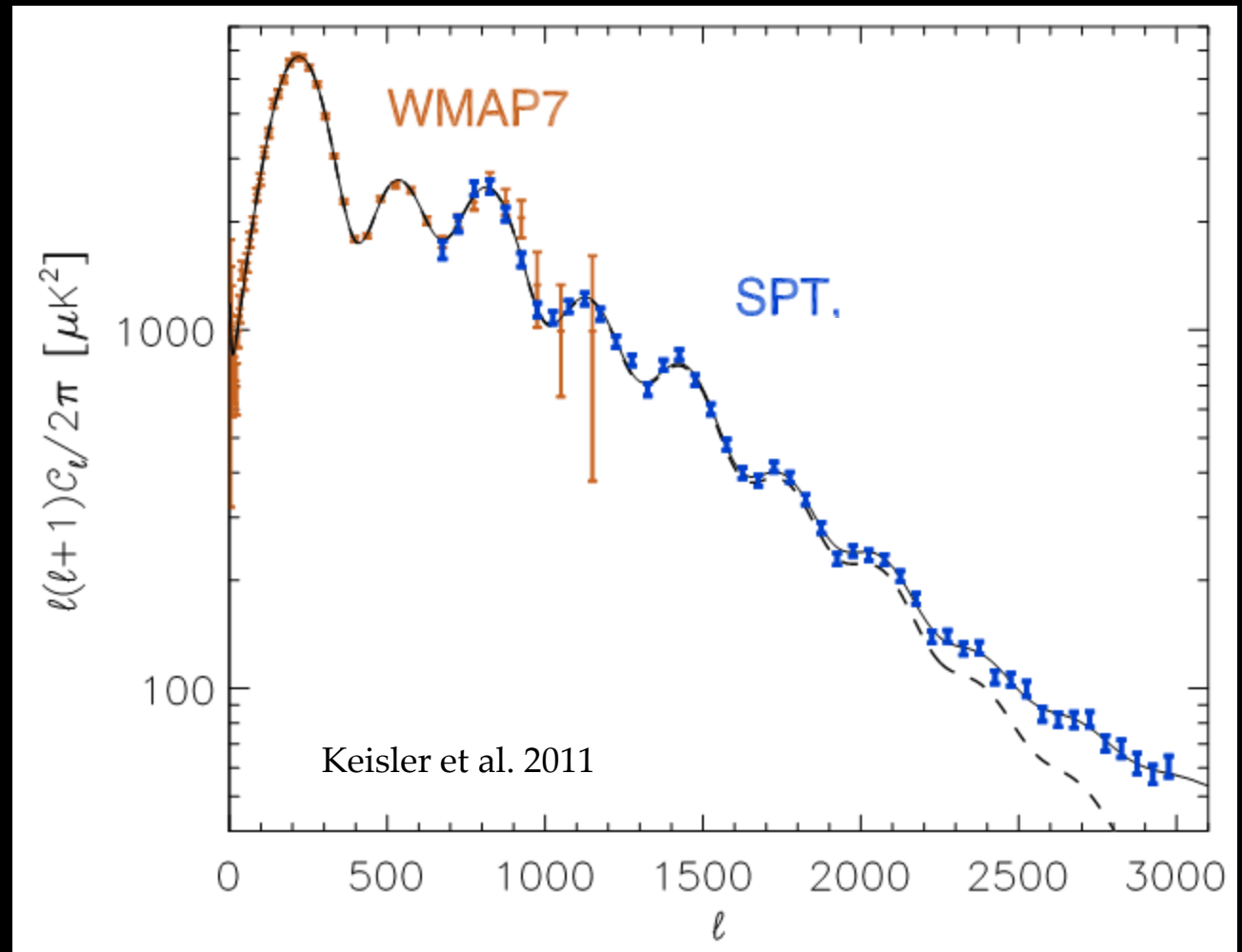
# Evidence

- Flatness (remember the 80's and 90's)
- Nearly Scale Invariant Spectrum
- Nearly Gaussian Perturbations
- Acoustic peaks (in CMB T, CMB E, LSS)

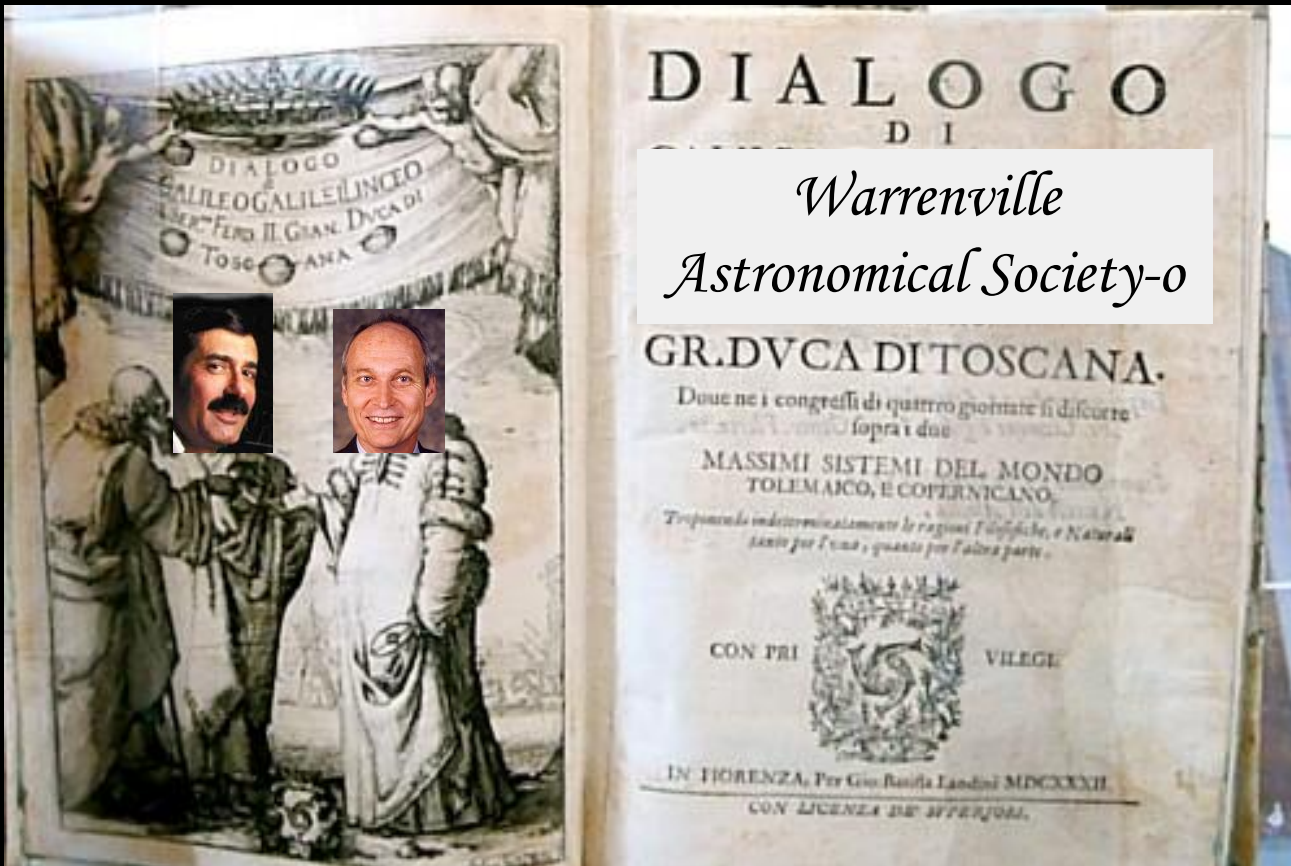


# Evidence

Observed series of peaks and troughs in temperature spectrum



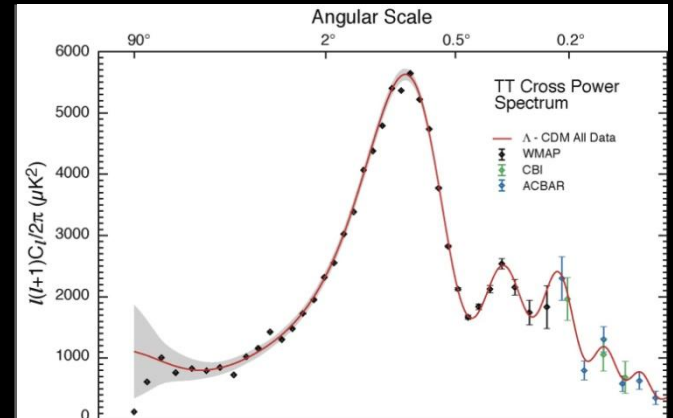
# Evidence



# Evidence

## Dialog

Mike: Why do we observe peaks and troughs in the temperature spectrum?

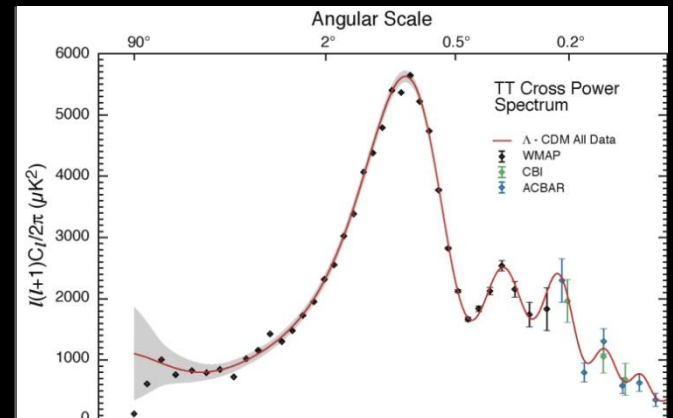


# Evidence

## Dialog

**Mike:** Why do we observe peaks and troughs in the temperature spectrum?

**Rocky:** Perturbations in the pre-recombination plasma (electrons, protons, photons) were governed by the wave equation. So there were acoustic oscillations, similar to those produced by musical instruments.



# Evidence

## Dialog

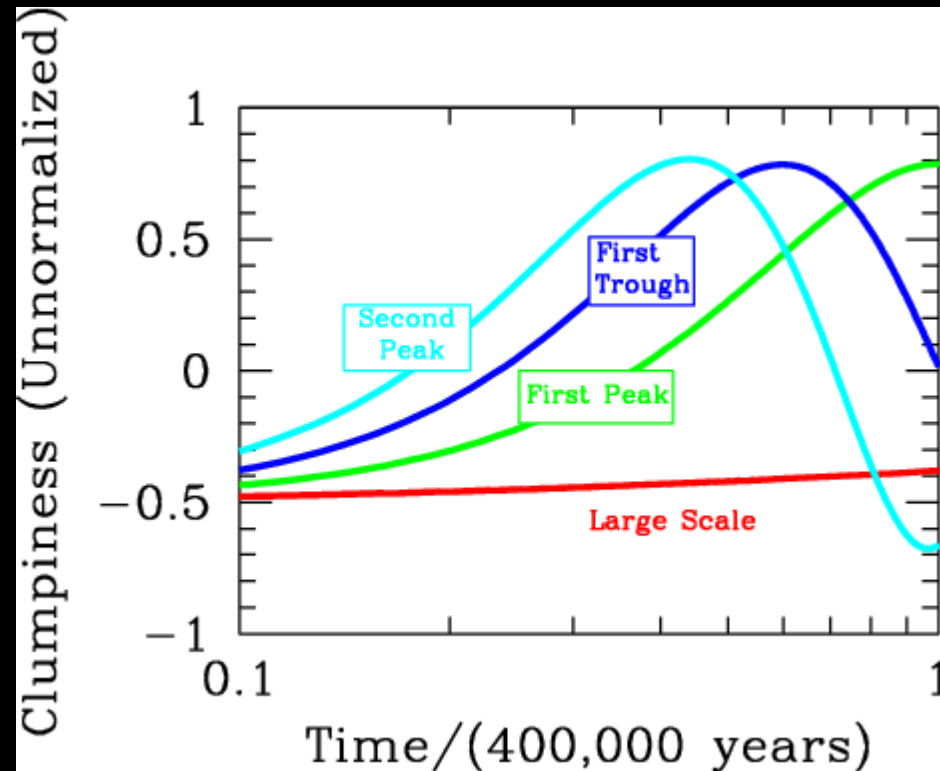
Mike: But you get a fundamental mode and harmonics in musical spectra because the ends of the strings are tied down; the Universe is not tied down!

# Evidence

## Dialog

Mike: But you get a fundamental mode and harmonics in musical spectra because the ends of the strings are tied down; the Universe is not tied down!

Rocky: Modes of different wavelengths start evolving at different times (short wavelength earlier; long wavelength later)



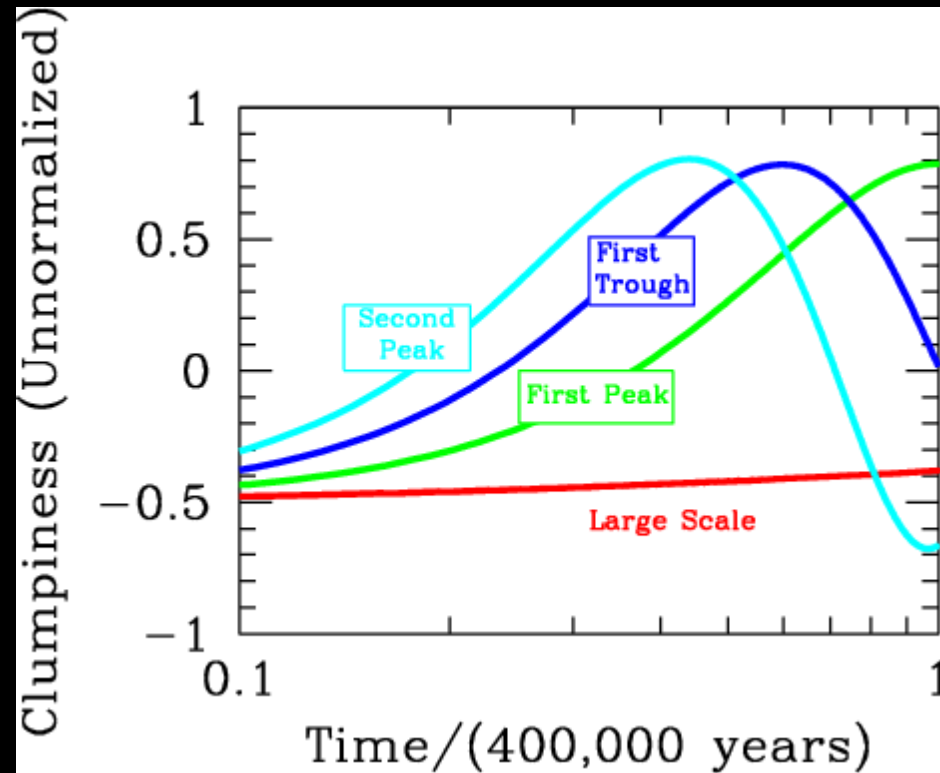


# Evidence

## Dialog

Mike: So what?

Rocky: Some modes have reached maximal amplitude at recombination. We see these as peaks. Others (“Michelle Bachmann” modes) peaked too soon; we see these as troughs. All modes exist: in our single snapshot, we see only some of them!

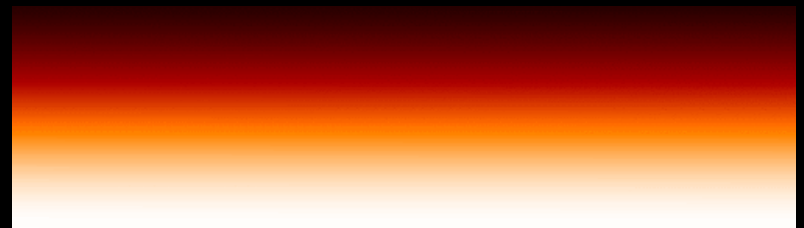
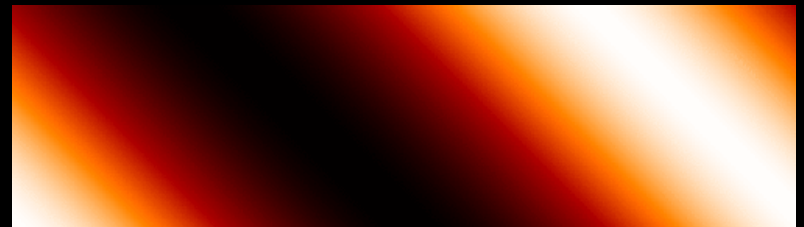
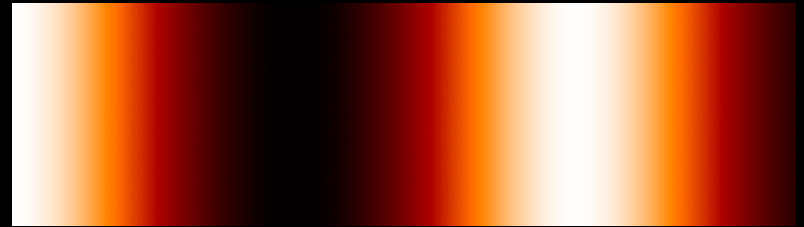


# Evidence

## Dialog

Mike: Well, that is a beautiful answer, but it neglects one key thing. A given wavelength has an infinite number of modes. The CMB first peak, first example, comes from a sum over an infinite number of Fourier modes, each with a different orientation.

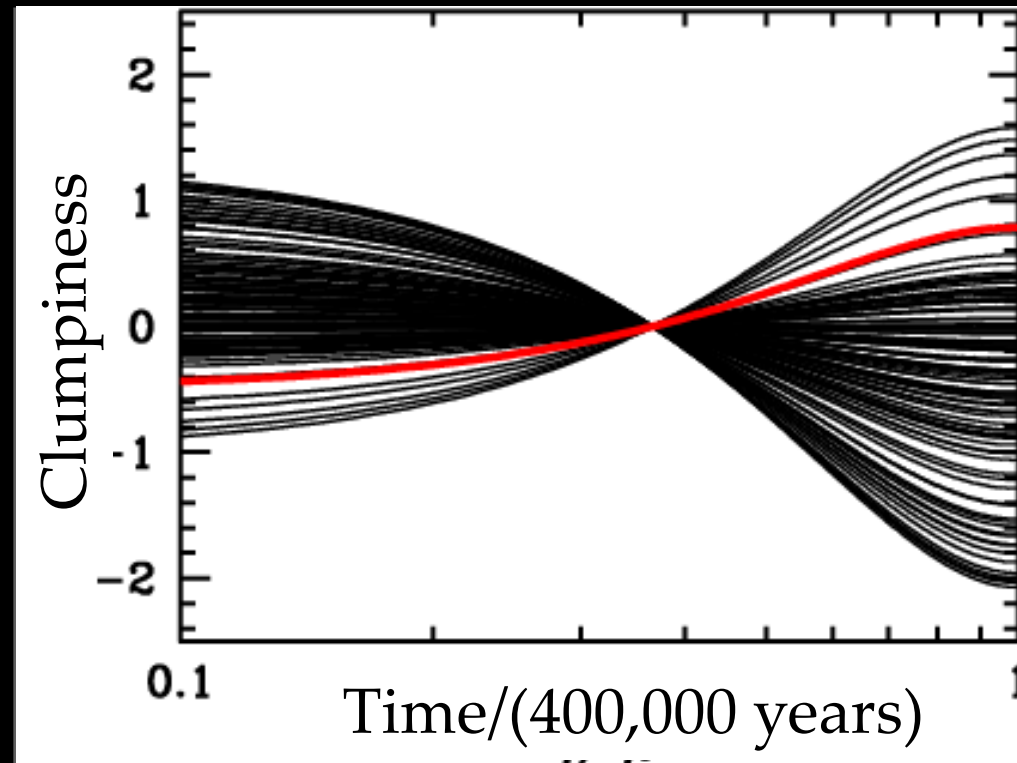
Rocky: So what?



# Evidence

## Dialog

Mike: You assumed in your plot that the first peak mode started with constant amplitude. Now, you've got to assume that *all* of the infinite modes start with constant amplitude. Who organized the phases so they were all the same?

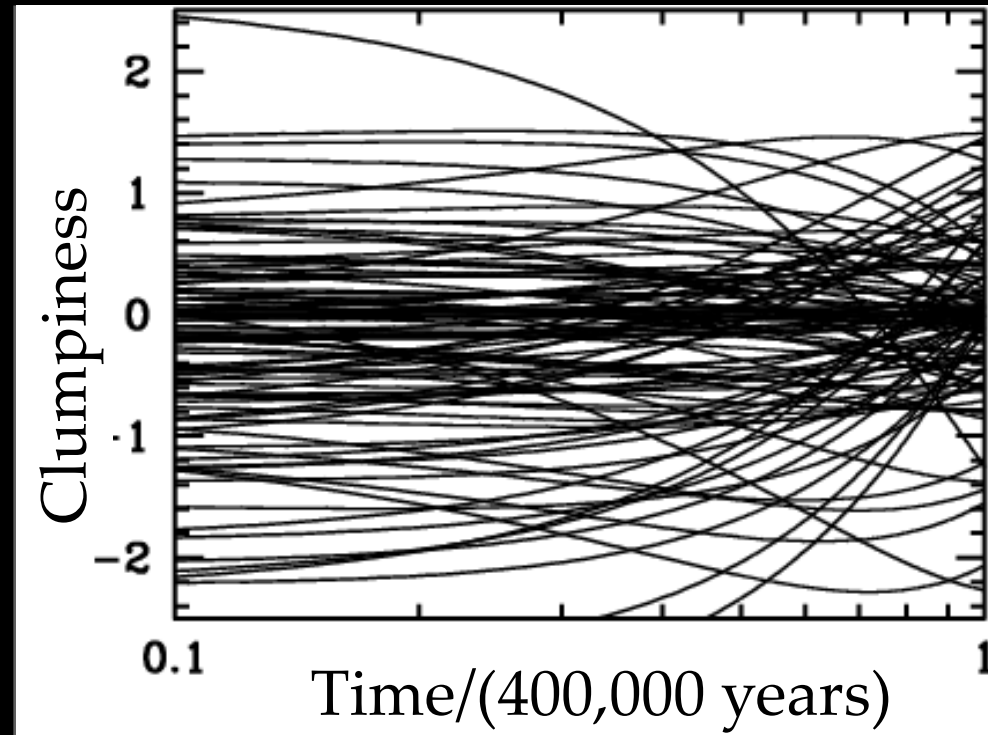


Rocky: Hmm

# Evidence

## Dialog

Mike: If the phases were random, the amplitudes of the first peak modes would look like this. Same with “first trough” modes, and we wouldn’t get a coherent series of peaks and trough. We’d just see noise.

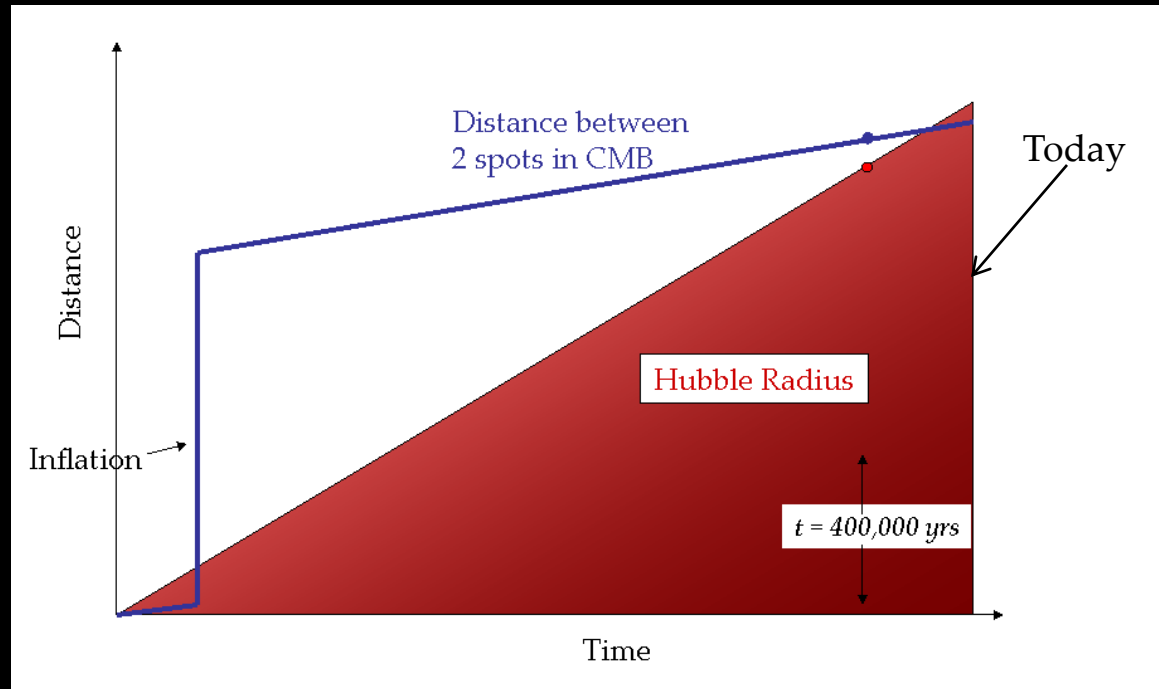


# Evidence

## Dialog

Rocky: Remember the diagram we made famous in the 80's?

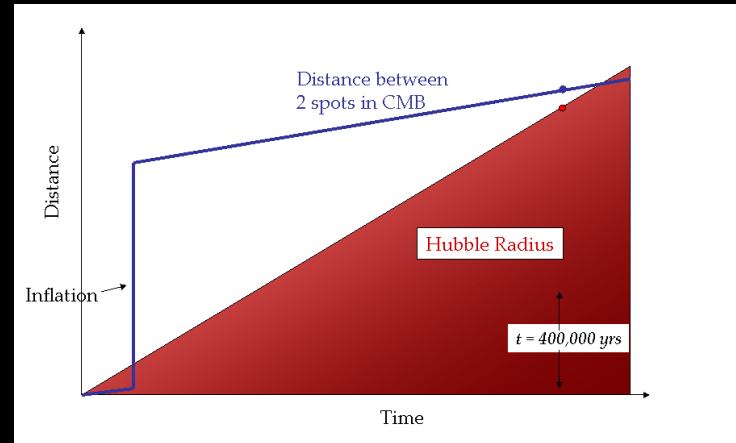
Mike: You remember the 80's?



# Evidence

## Dialog

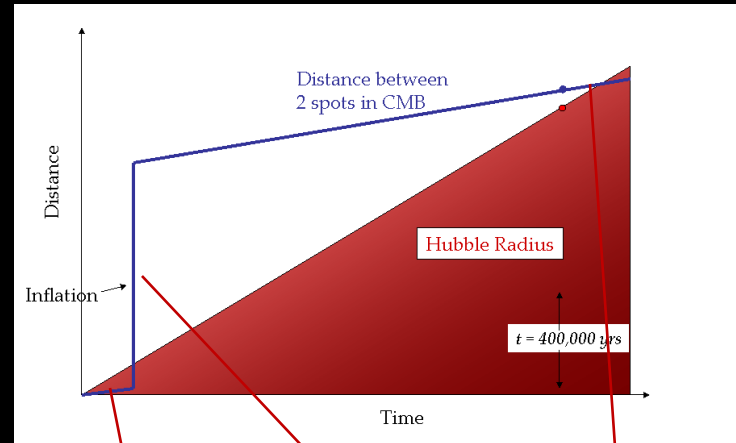
Rocky: Inflation sets the phases automatically. Quantum fluctuations during inflation freeze out as they leave the horizon and then begin oscillating much later when they re-enter. So all modes enter the horizon with constant amplitude



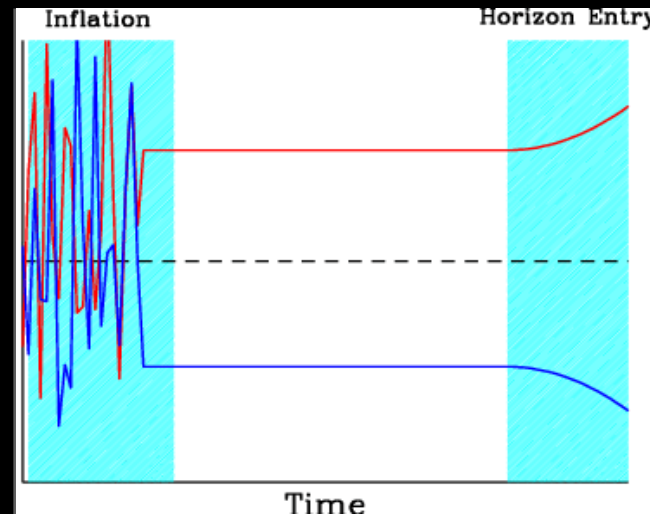
# Evidence

## Dialog

Rocky: Inflation sets the phases automatically. Quantum fluctuations during inflation freeze out as they leave the horizon and then begin oscillating much later when they re-enter. So all modes enter the horizon with constant amplitude



Distortions in Space-Time



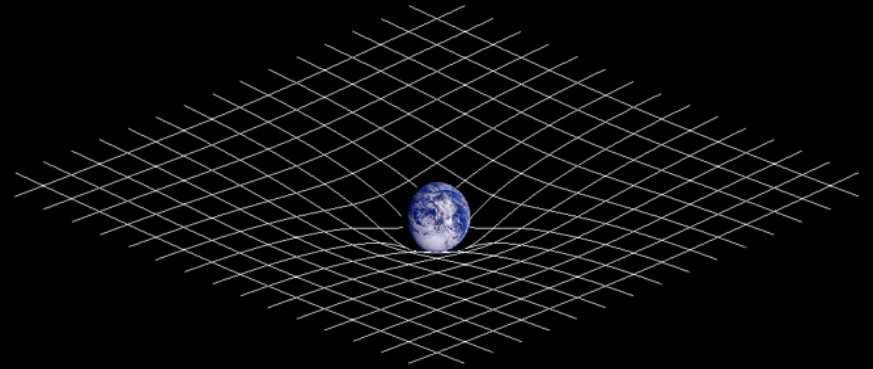
# Physics Behind Inflation

- Inflation has passed tests
- Challenge to understand underlying physics
- Gravitational Waves: Focus of Heroic Experimental Effort
- Non-Gaussianity: Exciting Recent Theoretical Developments

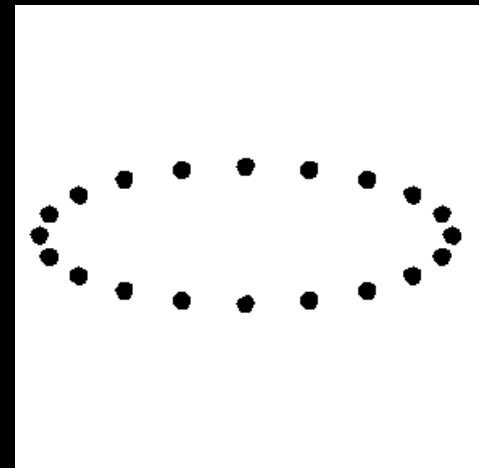


# Gravitational Waves

Inflation produces both *scalar* and *tensor* perturbations. The former have been produced: the goal is to detect the latter

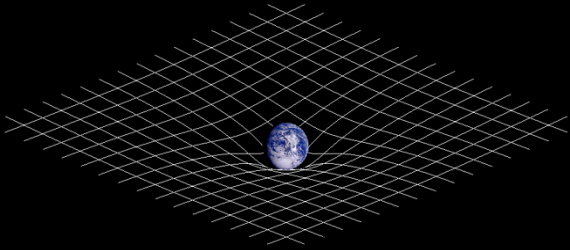


Scalar/Density

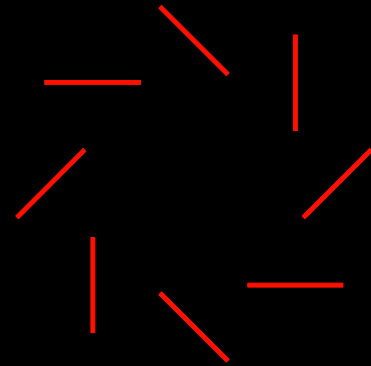
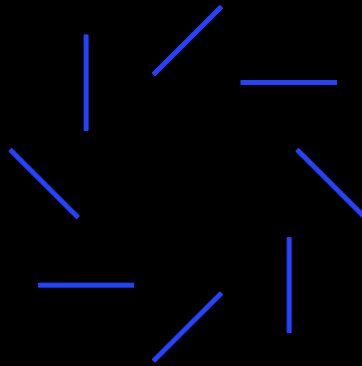
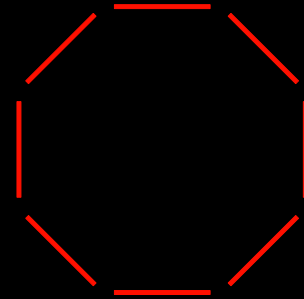
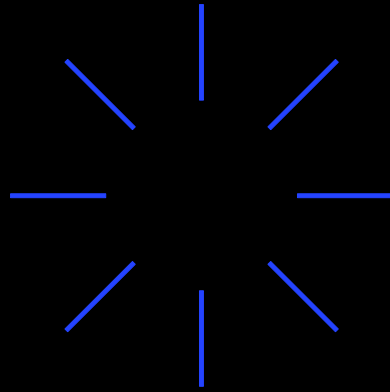


Tensor/Gravitational Waves

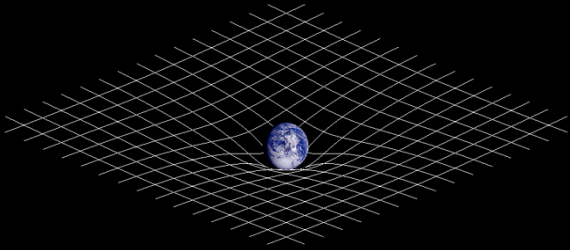
# Gravitational Waves



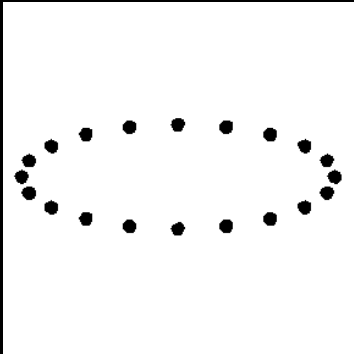
Density perturbations  
produce only E-modes



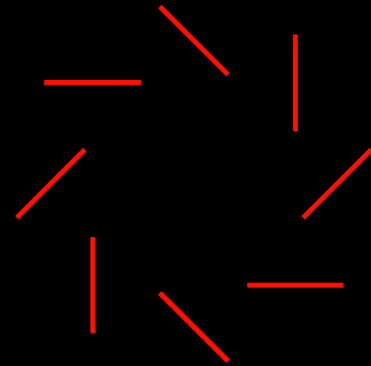
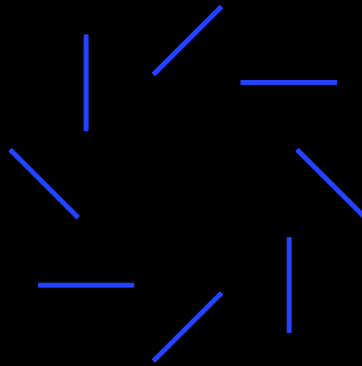
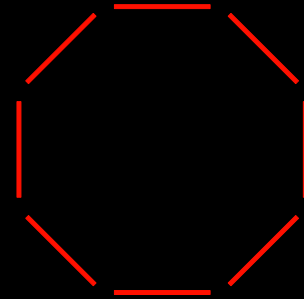
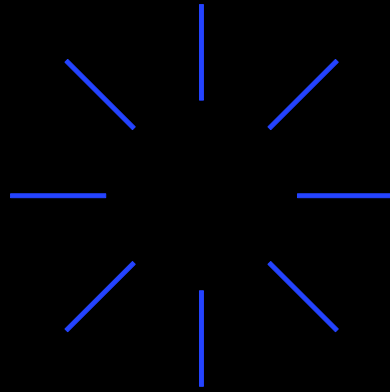
# Gravitational Waves



Density perturbations  
produce only E-modes

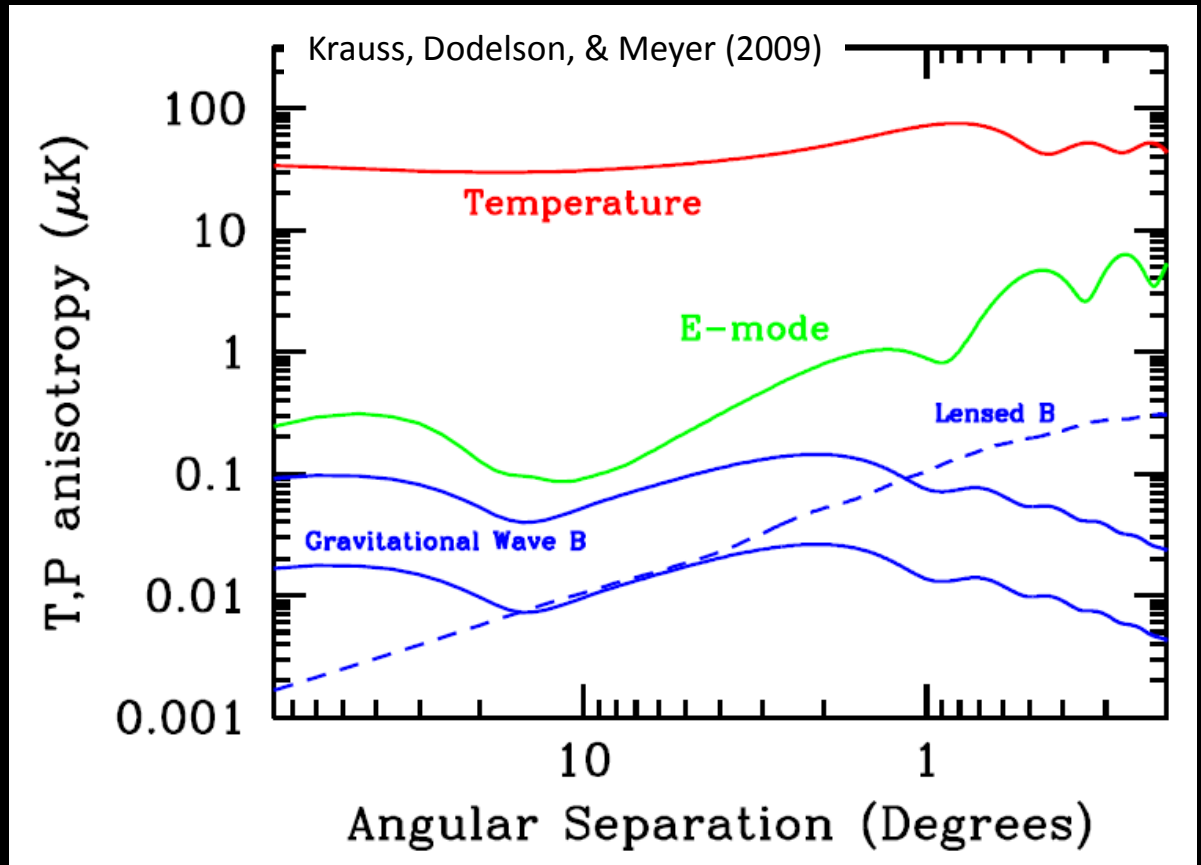


Gravity waves produce E-  
and B- modes

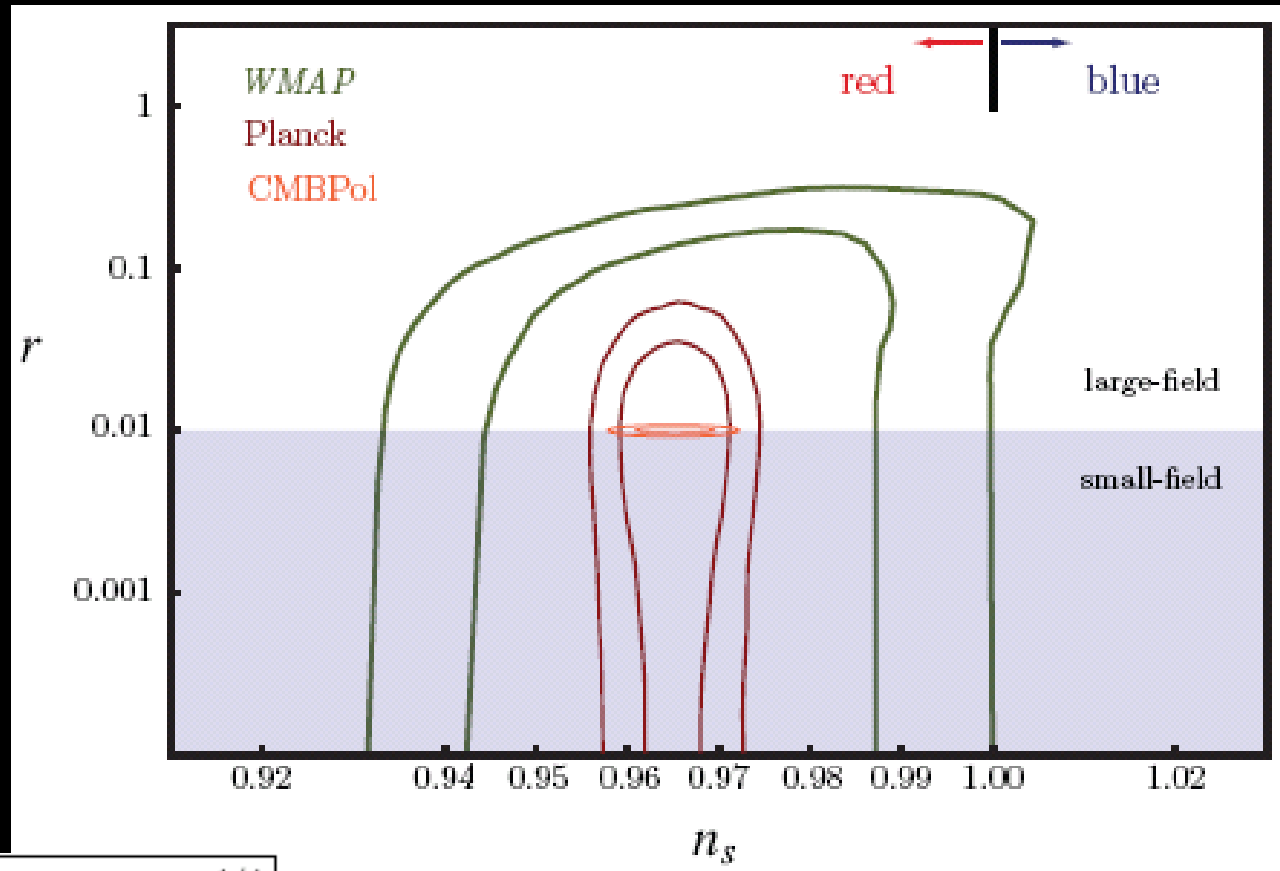


# Gravitational Waves

Amplitude of B-mode spectrum model-dependent, but characteristic spectral shape

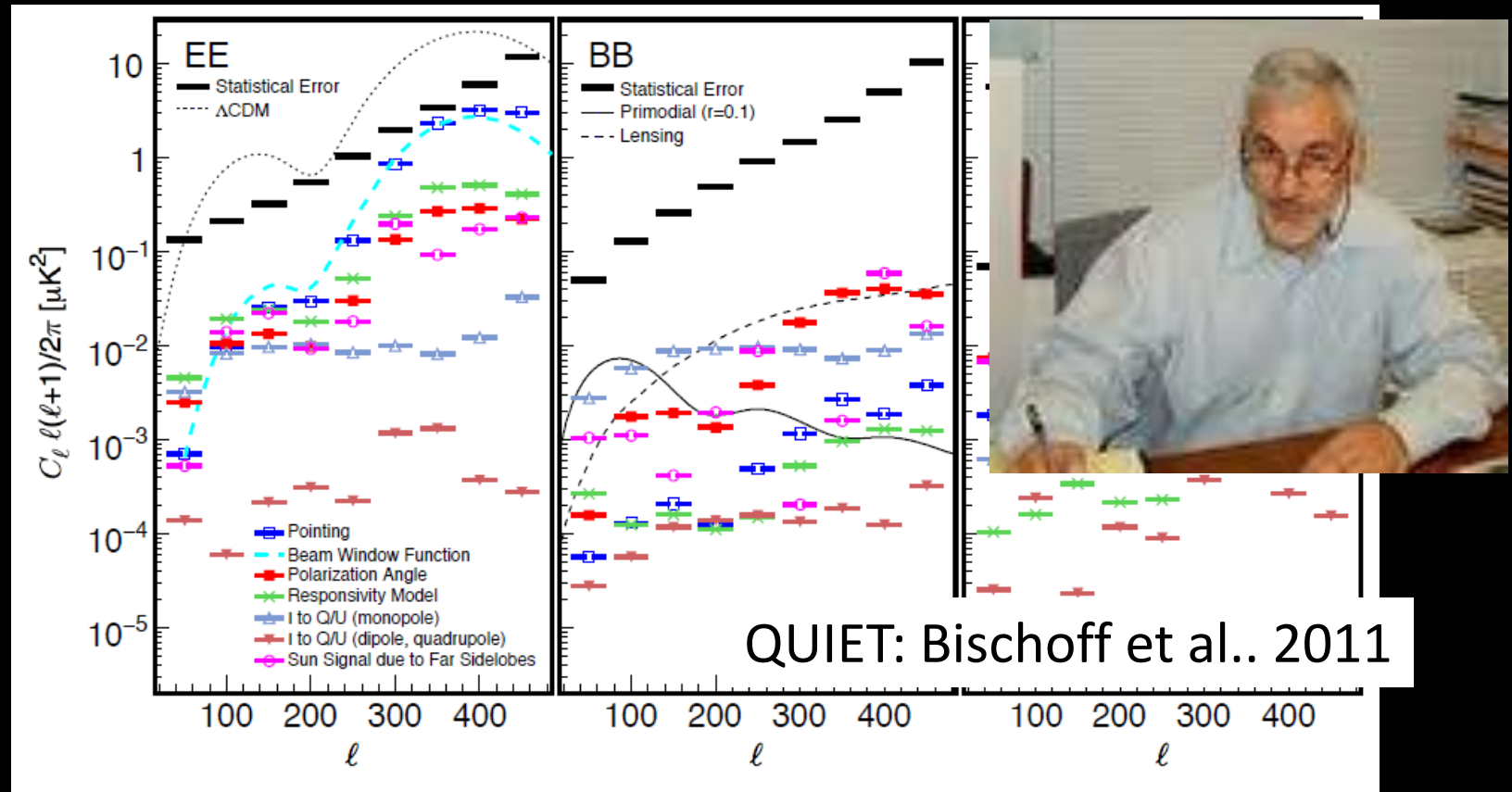


# Gravitational Waves



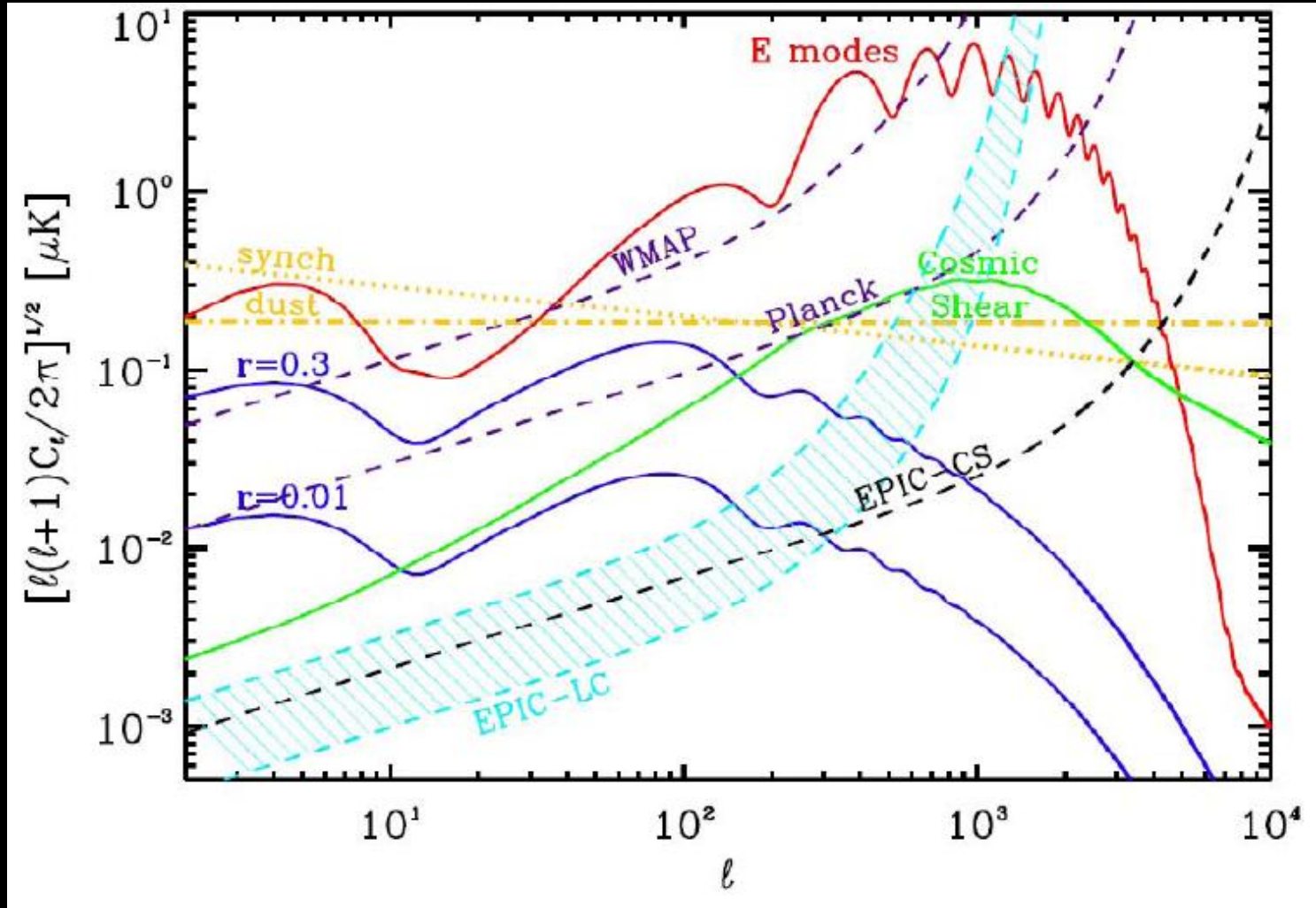
$$V^{1/4} = 1.06 \times 10^{16} \text{ GeV} \left( \frac{r_{\star}}{0.01} \right)^{1/4} *$$

# Gravitational Waves



# Gravitational Waves

Ambitious plans for the future



# Non-Gaussianity

Choose a gauge

$$ds^2 = -dt^2 + a(t)^2 e^{2\zeta(\mathbf{x})} dx_i dx_i$$

$\zeta$  describes perturbations  $(5/3)\Phi$

$$\langle \zeta(\vec{k}_1) \zeta(\vec{k}_2) \zeta(\vec{k}_3) \rangle = (2\pi)^3 \delta^3(\vec{k}_1 + \vec{k}_2 + \vec{k}_3) F(k_1, k_2, k_3)$$

3-point function basic  
measure of NG

Translation invariance  
implies  $k$ 's form a triangle

Shape/amplitude  
depends on 3 variables



# Non-Gaussianity

Generic prediction of single-field inflation (*consistency relation*):

$$\lim_{k_1 \rightarrow 0} \langle \zeta(\vec{k}_1) \zeta(\vec{k}_2) \zeta(\vec{k}_3) \rangle = (2\pi)^3 \delta^3(\vec{k}_1 + \vec{k}_2 + \vec{k}_3) P(k_1) P(k_2) (n-1)$$

Squeezed limit

Power spectra of long and short wavelength modes

Deviation from scale invariance ( $n=1$ ); amplitude constrained by observations to be at most  $\sim 0.05$

So  $4f_{NL} = n-1$  is generically 0.01 in single field models

# Non-Gaussianity

## Current observations

WMAP	$-4 < f_{NL} < 80$ (95% CL)
------	-----------------------------

SDSS

$-1 < f_{NL} < 63$ (95% CL)
-----------------------------

Smith, Senatore, &  
Zaldarriaga (2009)

Slosar et al. (2008)

## Upcoming observations

Planck

$$f_{NL} < 3 - 5$$

DES

$$f_{NL} < 5 - 20$$

If local NG is found in the next decade, single field models  
of inflation will be falsified

# Non-Gaussianity

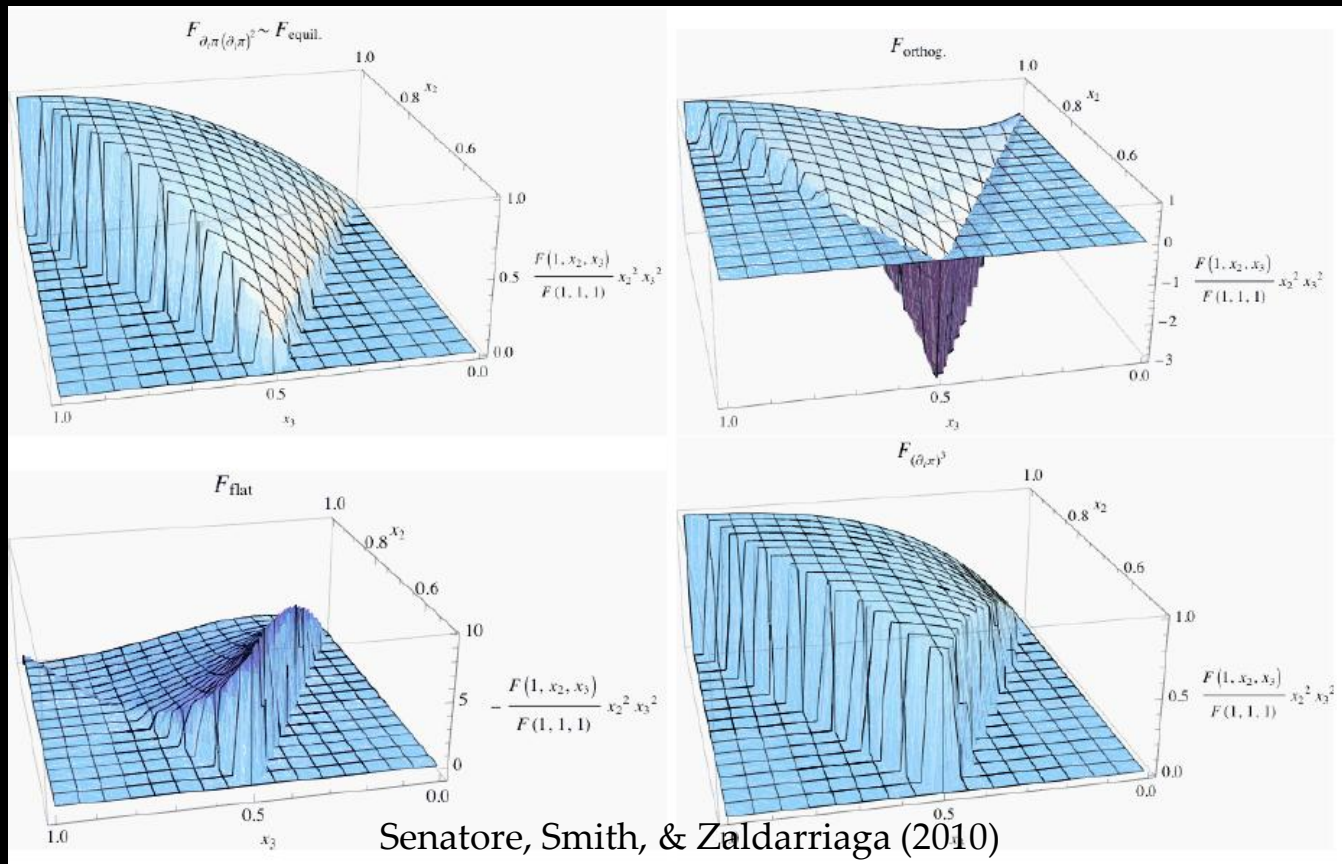
Over the last several years, theorists have imported Effective Field Theory techniques to analyze perturbations generated during inflation

$$S_\pi = \int d^4x \sqrt{-g} \left[ -\frac{M_{\text{Pl}}^2 \dot{H}}{c_s^2} \left( \dot{\pi}^2 - c_s^2 \frac{1}{a^2} (\partial_i \pi)^2 \right) \right. \\ \left. + \frac{\dot{H} M_{\text{Pl}}^2}{c_s^2} (1 - c_s^2) \dot{\pi} \frac{1}{a^2} (\partial_i \pi)^2 - \frac{\dot{H} M_{\text{Pl}}^2}{c_s^2} (1 - c_s^2) \left( 1 + \frac{2 \tilde{c}_3}{3 c_s^2} \right) \dot{\pi}^3 \right]$$

Time diffeomorphisms are broken (because inflation ends), leading to a Goldstone boson ( $\pi$ ) whose interactions are dictated by symmetry (spatial diffeomorphisms). This is the field whose fluctuations give rise to scalar perturbations.

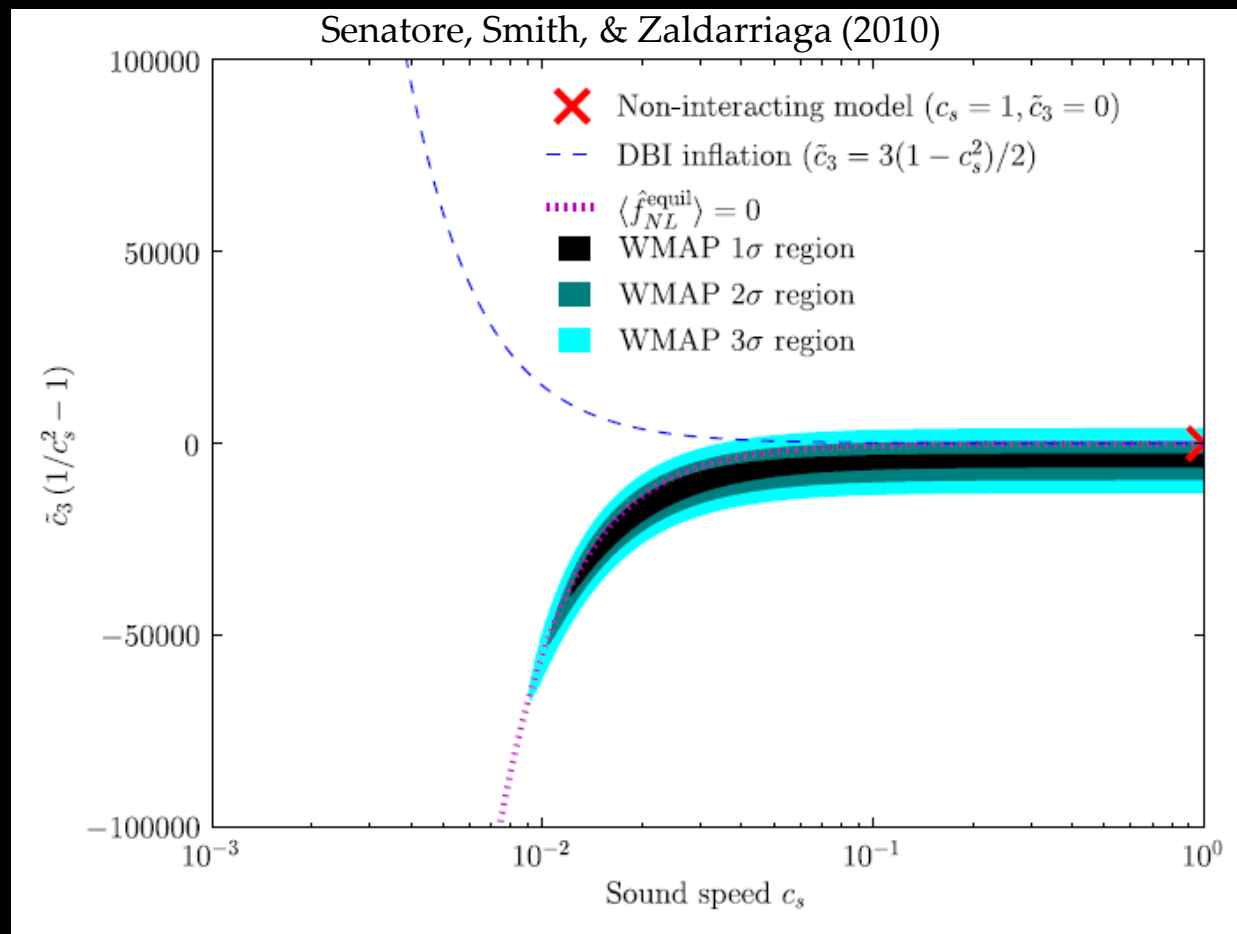
# Non-Gaussianity

Each term in the action corresponds to a distinctive bispectrum  $F$



# Non-Gaussianity

Use template fitting to extract constraints on each coefficient using, e.g., CMB data



# Non-Gaussianity

Local Non-Gaussianity corresponds to:

$$\Phi(x) = \Phi_G(x) + f_{NL}\Phi_G^2(x)$$

Dalal et al. (2008) showed that this leaves a characteristic imprint on large scale structure

# Non-Gaussianity

Start from

$$\Phi(x) = \Phi_G(x) + f_{NL} \Phi_G^2(x)$$

Take the Laplacian and consider potential well troughs

$$\begin{aligned} \nabla^2 \Phi &= \nabla^2 \Phi_G + 2f_{NL} \left[ \Phi_G \nabla^2 \Phi_G + |\nabla \Phi_G|^2 \right] \\ &\rightarrow \nabla^2 \Phi_G + 2f_{NL} \Phi_G \nabla^2 \Phi_G \end{aligned}$$

# Non-Gaussianity

$$\nabla^2\Phi = \nabla^2\Phi_G + 2f_{NL}\Phi_G\nabla^2\Phi_G$$

Apply Poisson Equation

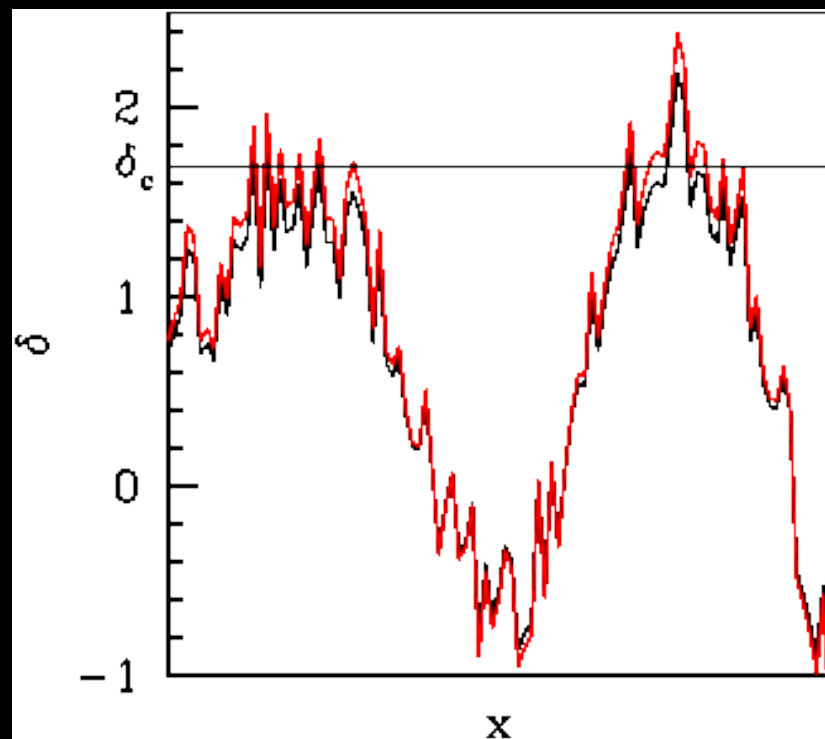
$$\delta = \delta_G + 2f_{NL}\Phi_G\delta_G$$

NG term leads to enhancement in overdensity near peaks  
for positive  $f_{NL}$



# Non-Gaussianity

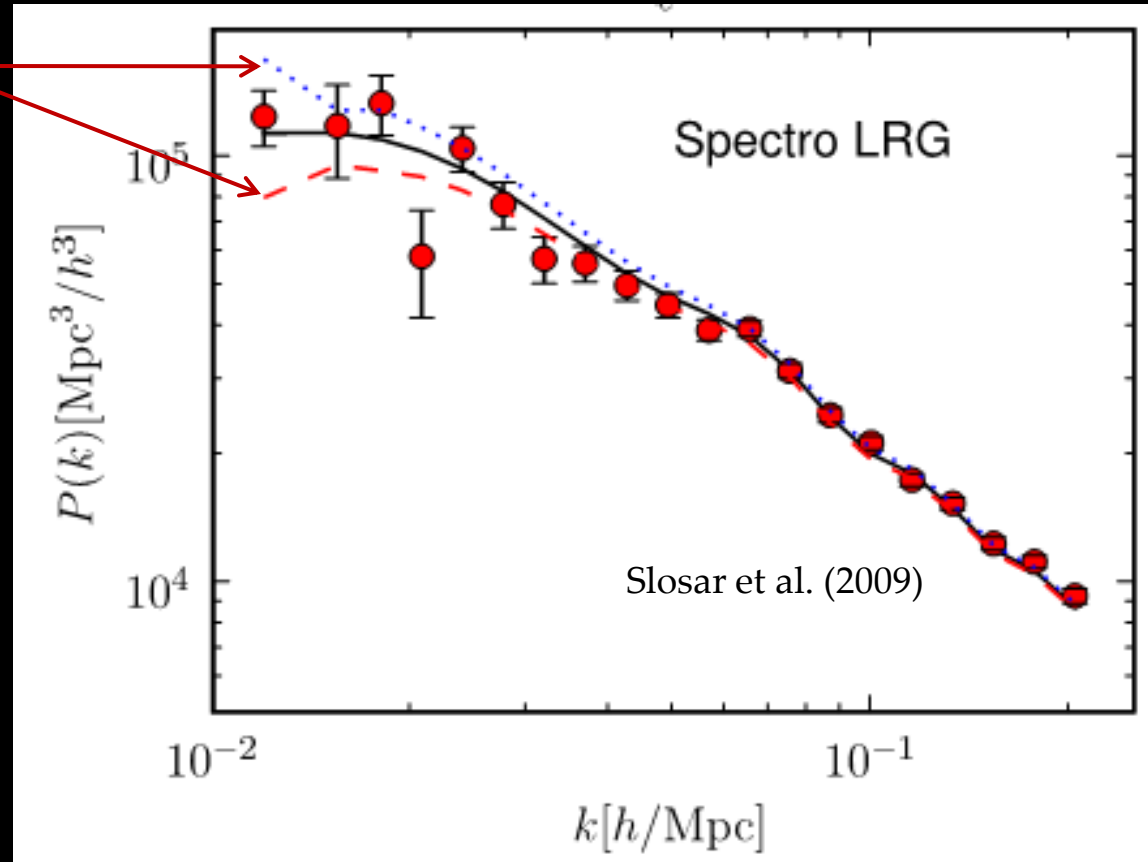
NG term leads to enhancement in overdensity near peaks for positive  $f_{NL}$



$$\delta_{peaks} = \delta_G + 2f_{NL}\Phi_G\delta_G \Rightarrow \Delta\delta_{peaks} \propto \frac{f_{NL}}{k^2}$$

# Non-Gaussianity

$$f_{NL} = \pm 100$$



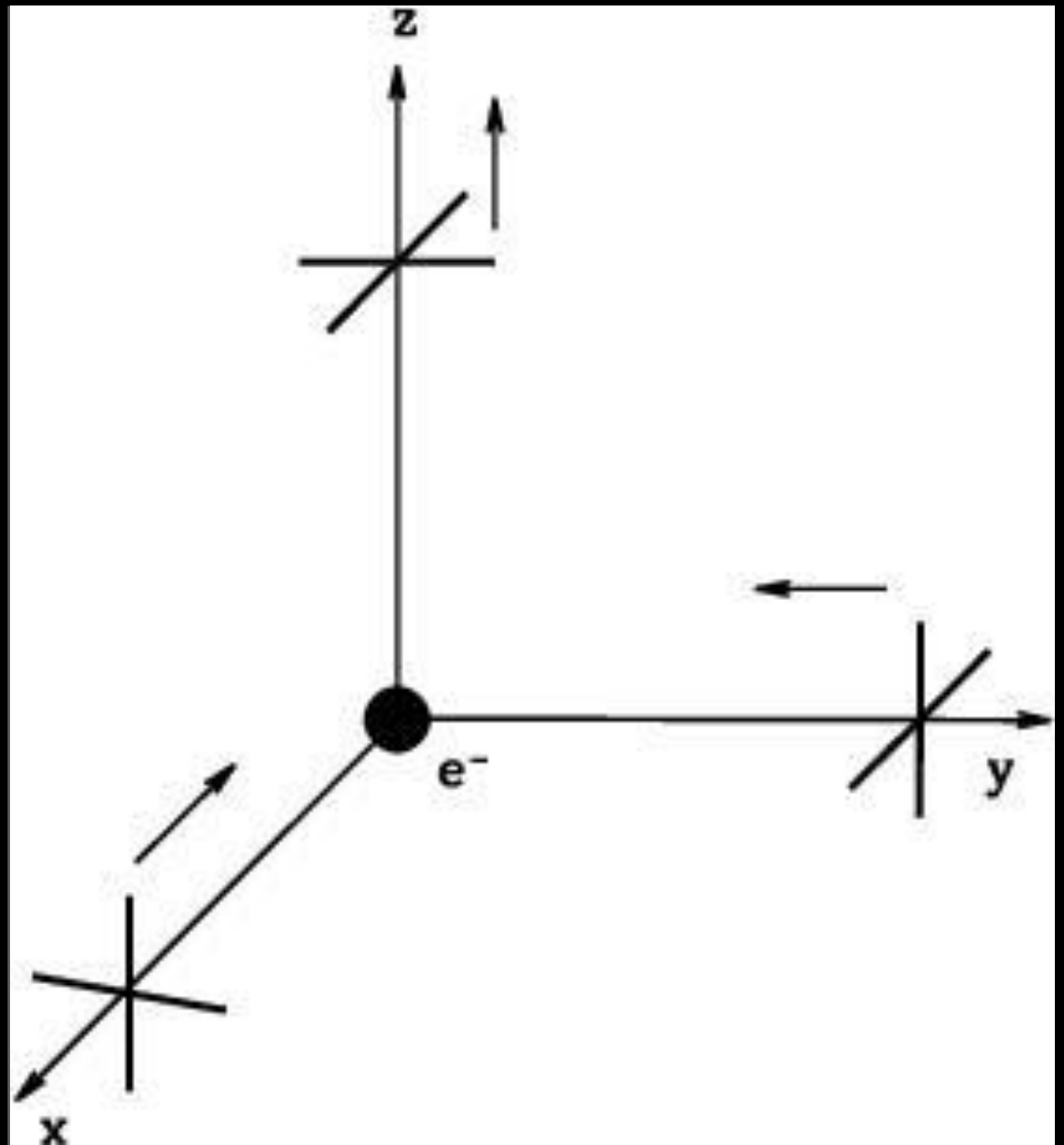
## 2020: Scenario I

- B-modes detected by ground-based experiments
- Gravitational wave amplitude precisely determined by 3 CMB experiments
- Scale of inflation together with SUSY discovery at LHC leads to unified model for dark matter and inflation

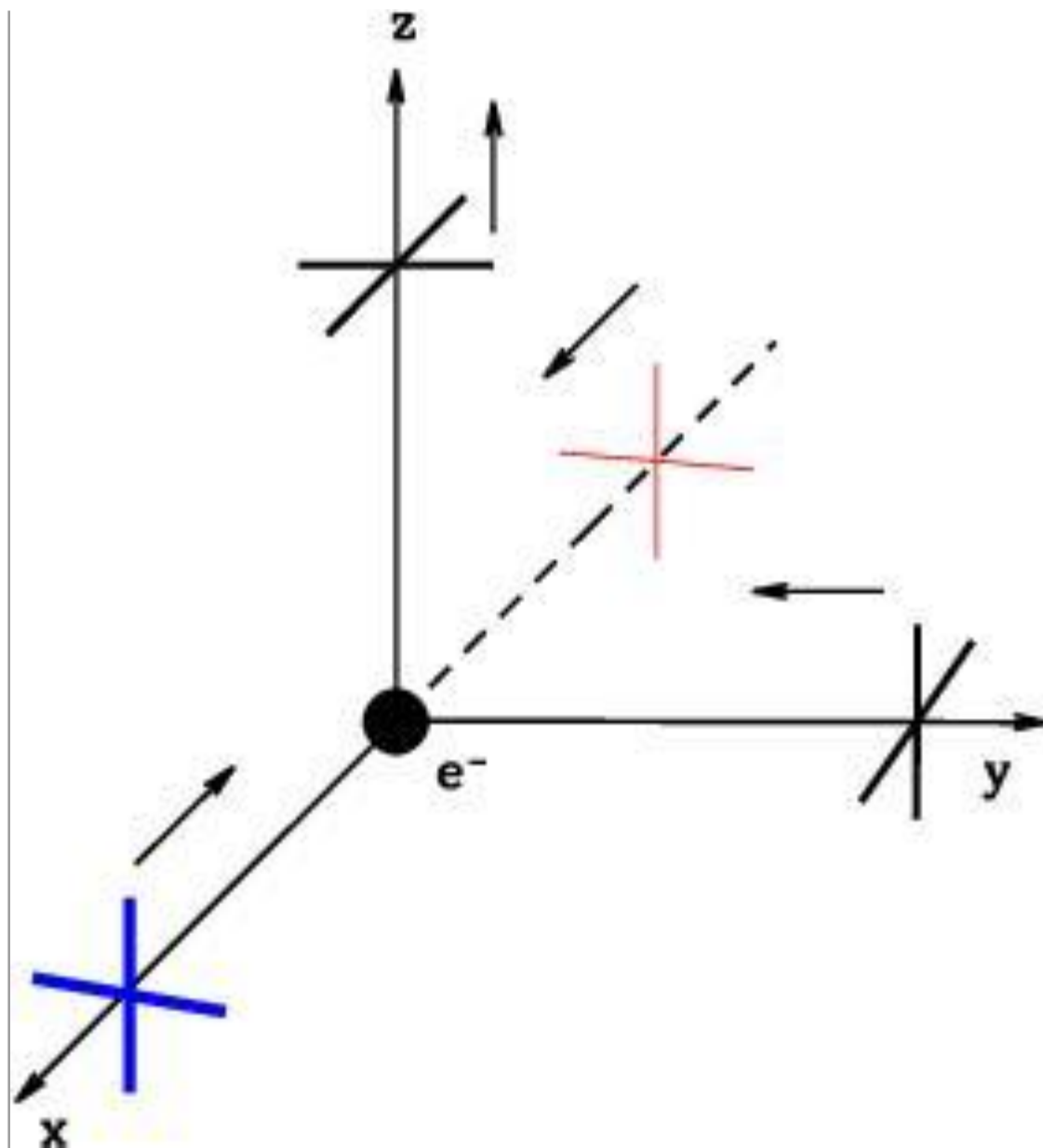
## 2020: Scenario II

- No B-modes detected
- Primordial Non-Gaussianity detected
- Cosmology in disarray: Is inflation right?  
Alternatives?

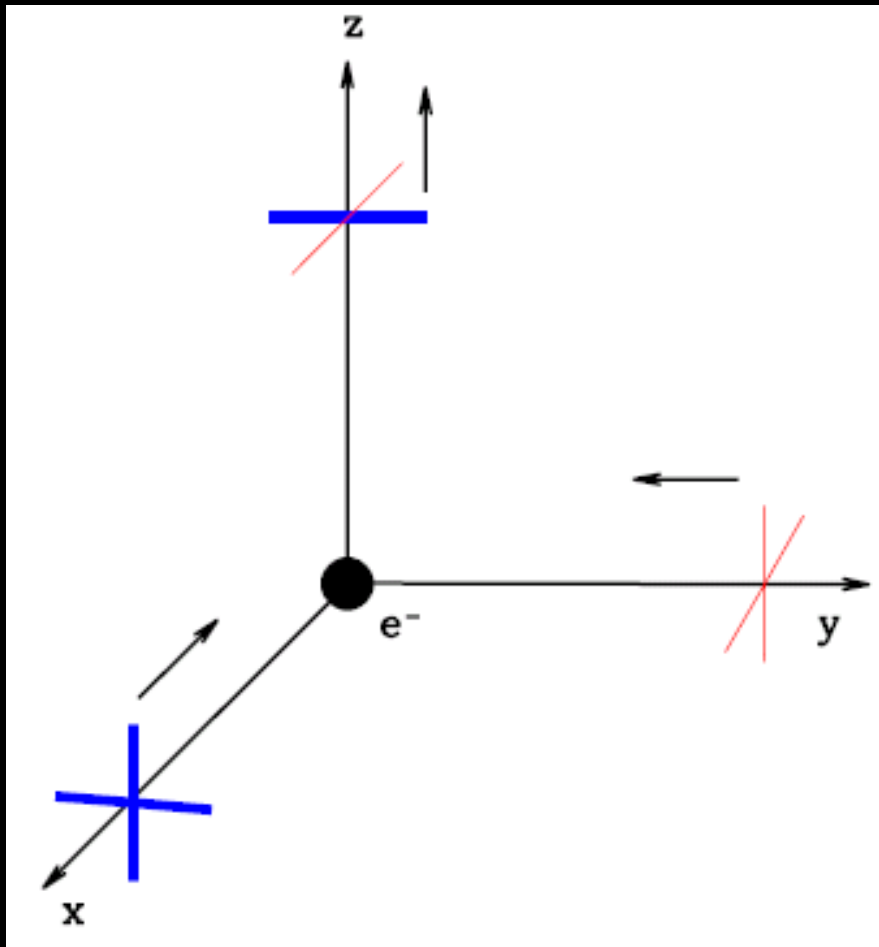
Isotropic radiation  
field produces no  
polarization after  
Compton scattering



Radiation with a dipole produces no polarization



# Compton scattering of unpolarized anisotropic radiation produces polarization



- Require Quadrupole (small before  $t=400,000$  yrs)
- Require Compton scattering (rare after  $t=400,000$  yrs)
- Signals factor of 10 smaller than temperature anisotropies