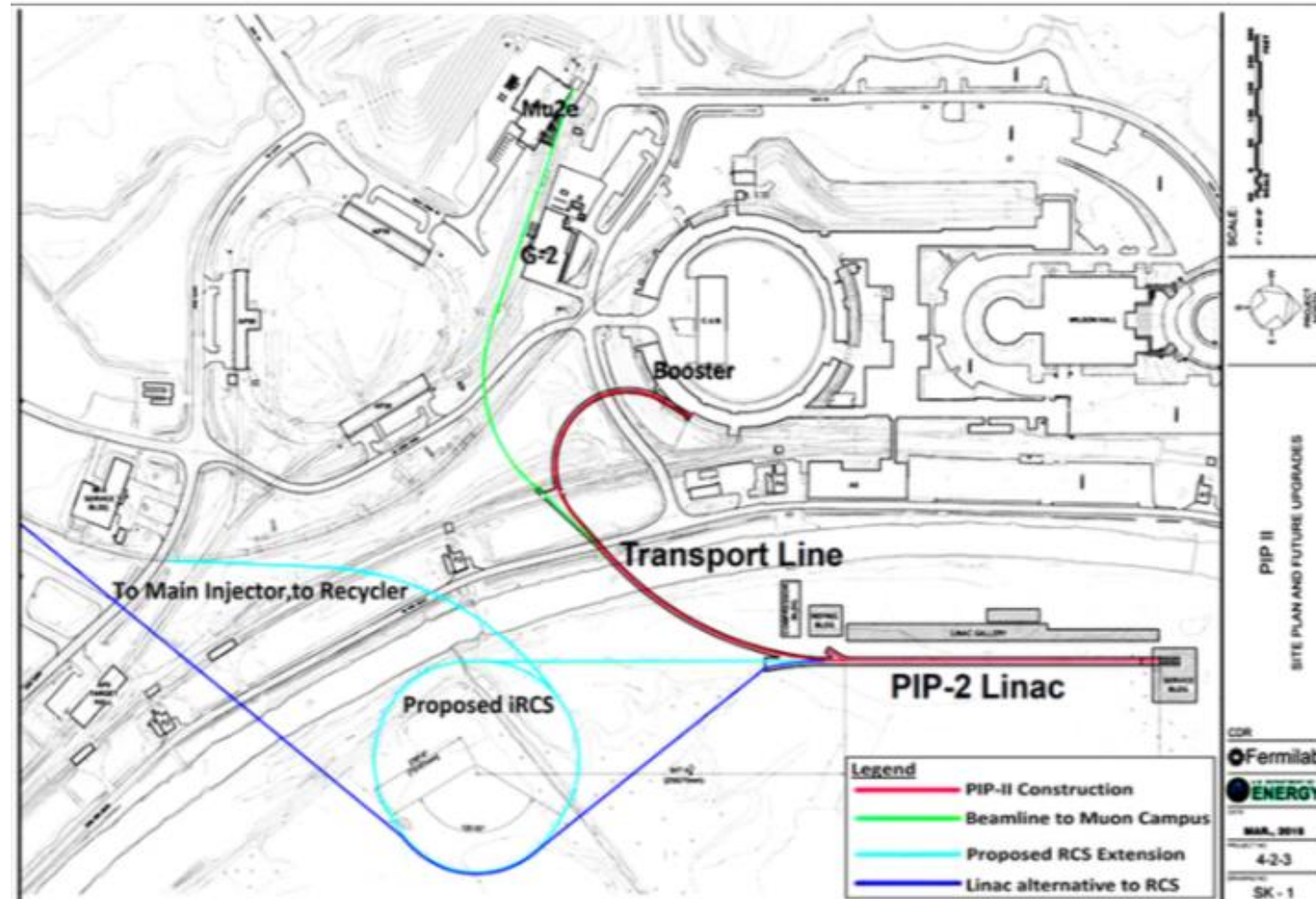


# Nonlinear Magnet for a Rapid-Cycling Synchrotron at Fermilab

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Ron Agustsson  
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**FAST/IOTA Collaboration Meeting**  
June 15 – 17, 2020

- Pole-face design and 3D model optimization
- Preliminary Tolerance Study
- Engineering Design
- Future Outlook



# Design Progress

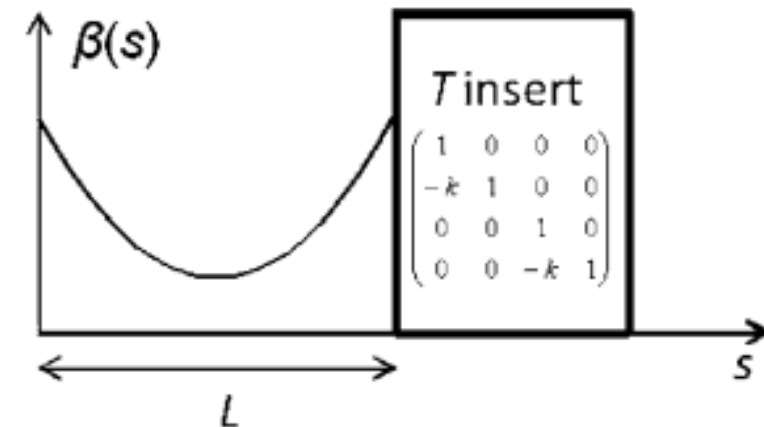
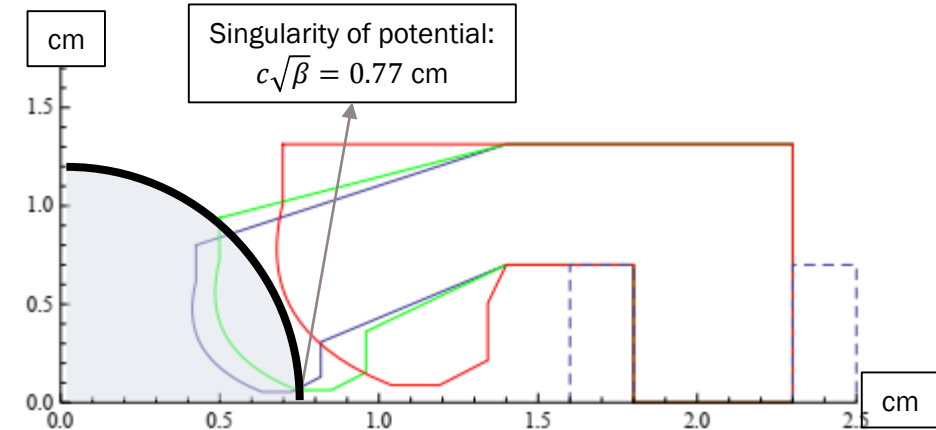
| Technical Objective   | Comments / Results  |
|---|---|
| Analytic solution to allow proper harmonic content                        | Pole-face contour definition outside convergence circle allows exploration of designs with larger physical aperture, required for iRCS  |
| Perform 3D simulations to obtain the required field                       | A full 8m-long NLI consisting of 20 segments has been designed, the required field profile is achieved  |
| Simulate the effect of manufacturing errors to set fabrication tolerances | The transverse misalignments of the segments, pole profile deviation and gap between the poles should be less than $\pm 125\mu\text{m}$ in order to maintain $<0.5\%$ of harmonic content error |
| Develop engineering design for the prototype                              | Mechanical engineering model for the NLI based on 3D magnetic simulations has been developed along with cost-effective manufacturing plan to be followed in Phase II                            |

- IOTA was a testbed for NLI that will eventually be used in iRCS
- The more rigid beam of iRCS requires larger magnets, which is favorable for manufacturing

| Parameter                      | IOTA     | iRCS   | Units |
|--------------------------------|----------|--------|-------|
| Particle                       | Electron | Proton |       |
| Beam Energy                    | 150      | 800    | MeV   |
| Momentum Rigidity, $B\rho$     | 0.5      | 4.9    | T×m   |
| Minimum Beta Function, $\beta$ | 0.73     | 5      | m     |
| Drift Length For NLI           | 2        | 8      | m     |
| Singularity = $c\sqrt{\beta}$  | 0.77     | 2.5    | cm    |

# IOTA Non-Linear Inserts (NLI)

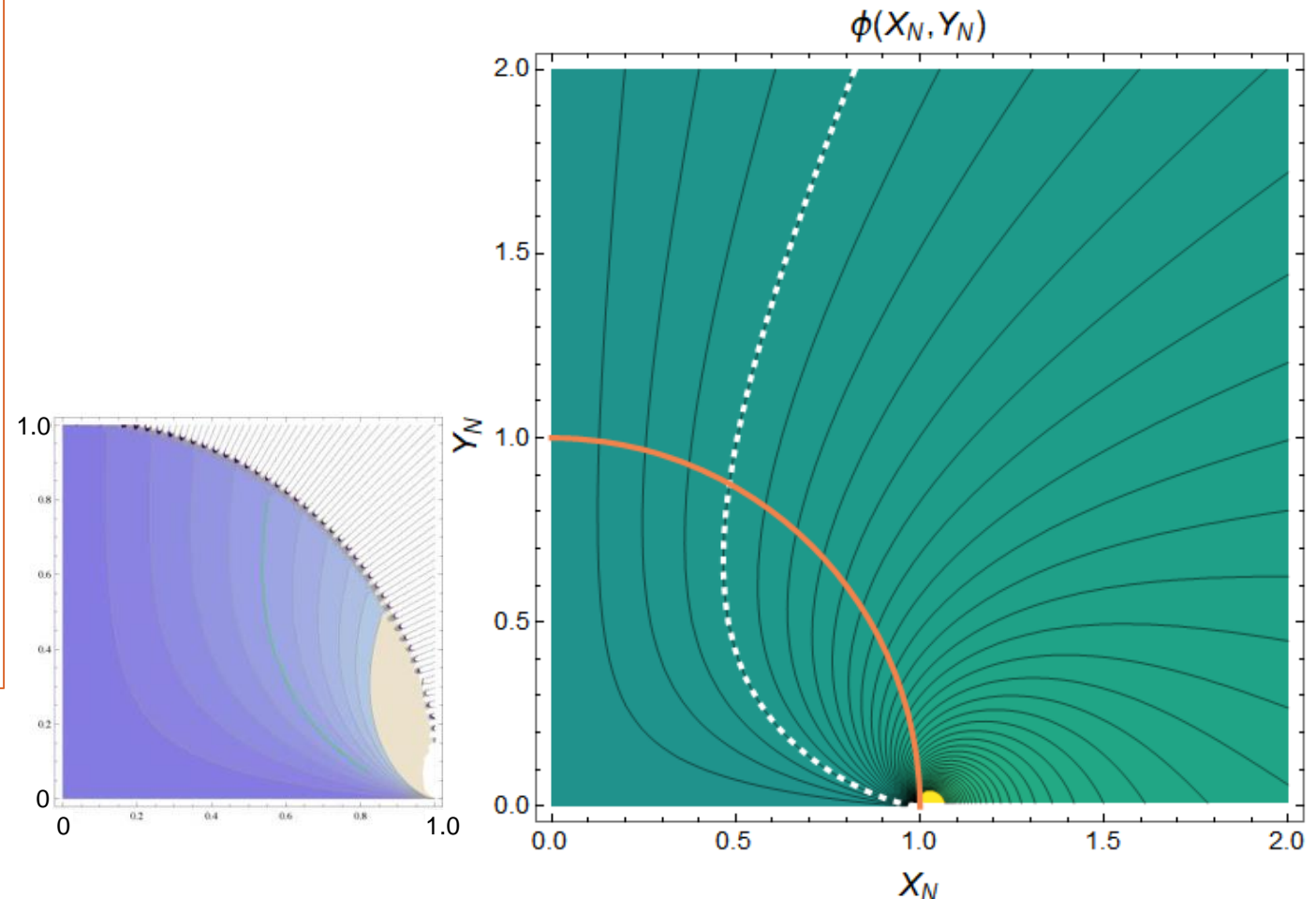
- The non-linear potential has a singularity on the x-axis, given by  $c\sqrt{\beta} = 0.77$  cm,  $c$  is a scaling constant and  $\beta$  is the beta function of the beam at that location
  - For reference, quadrupoles have a singularity in their potential at infinity
  - Note that the pole-face must protrude well into the aperture radius defined by the singularity (and reduce the real beam aperture), in order to produce the desired non-linear fields close to the beam axis.
- These NLI will be placed in a drift space where the beta function is  $\beta(s) = \frac{L-sk(L-s)}{\sqrt{1-(1-\frac{Lk}{2})^2}}$ , for a drift length of  $L$ , and  $k$  is the focusing strength of upstream optics (symmetric in  $x$  and  $y$ ).
- Therefore the size of the NLI must change along its length as depicted by the blue, green, and red outlines.



# Pole-face Definition

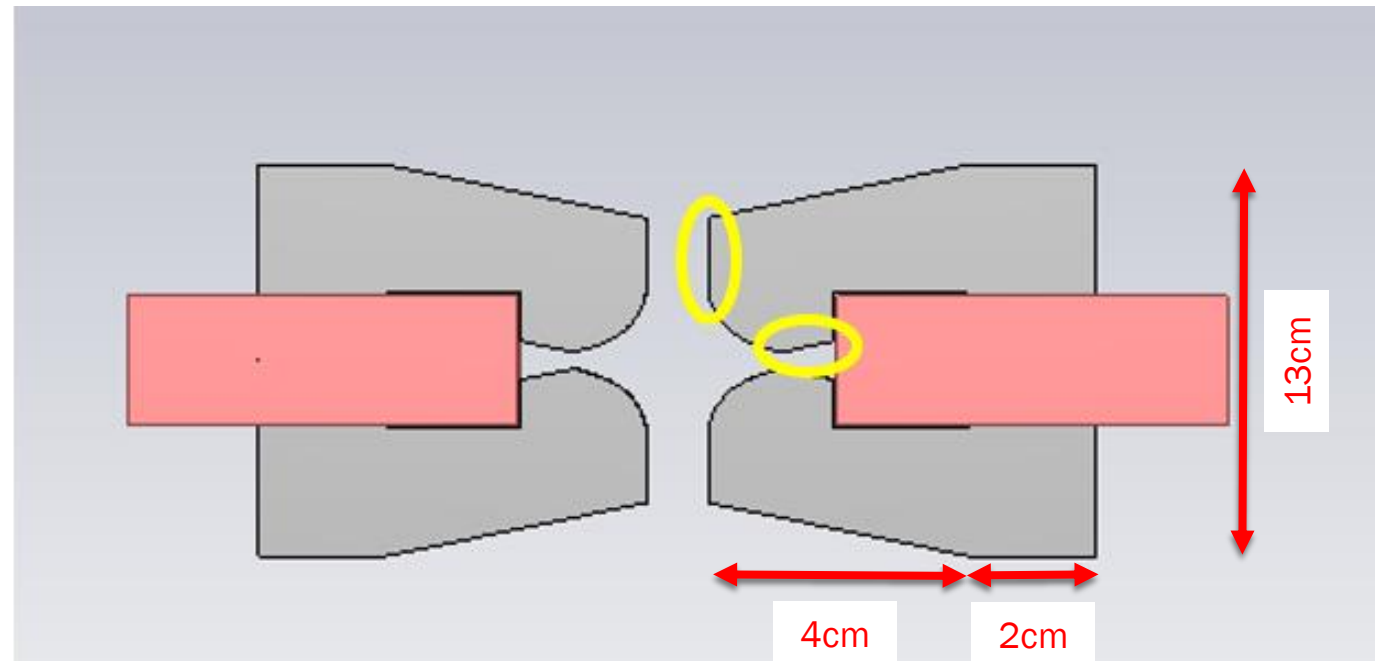
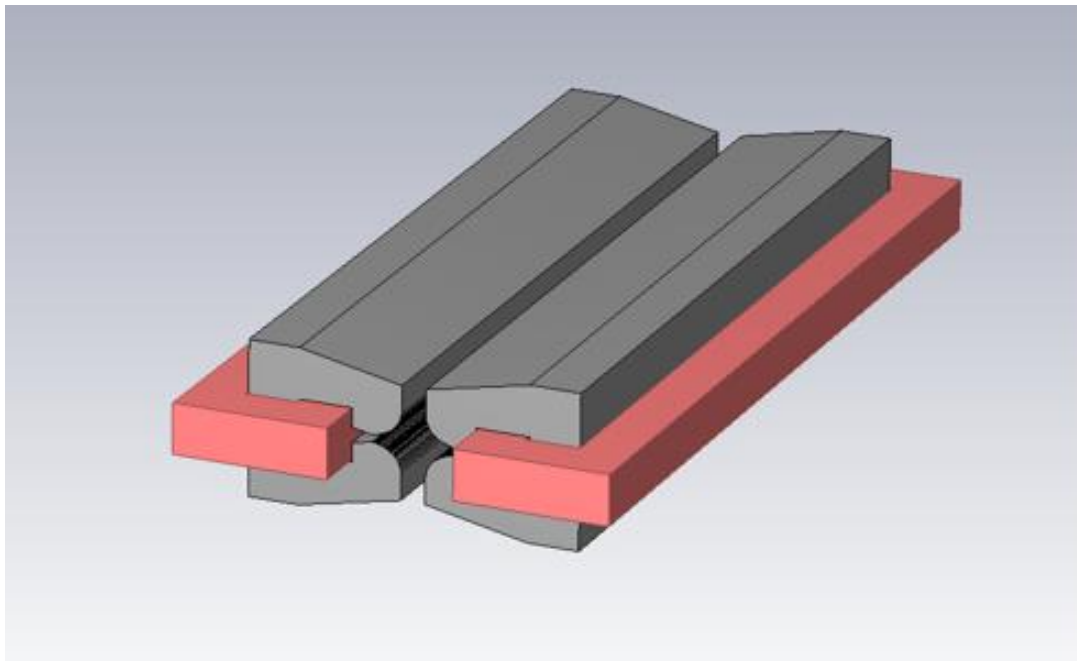
- Defining the pole face is done by picking a equipotential line from the imaginary part of the auxiliary transverse magnetic potential
  - $F(z) = \frac{A+i\phi}{B\rho}$
- The pole face contour is highlighted in the figure
- Only the positive x and y quadrant is shown due to symmetry
- The full analytic form of the potential has been derived by Mitchell, 2018
  - This allows for a faster computation of the pole face and extends the validity of the solution beyond a region close to the beam axis

C. Mitchell, F. O'Shea, and R. Ryne, "Accurate Modeling of Fringe Field Effects on Nonlinear Integrable Optics in IOTA," *Proceedings of the 9th Int. Particle Accelerator Conf.*, vol. IPAC2018, p. Canada-, 2018, doi: 10.18429/jacow-ipac2018-thpak036.  
 C. E. Mitchell, "Complex Representation of Potentials and Fields for the Nonlinear Magnetic Insert of the Integrable Optics Test Accelerator," LBNL-1007217, 1468609, Mar. 2017. doi: 10.2172/1468609.



# 3D Modeling of NLI Magnet Segments

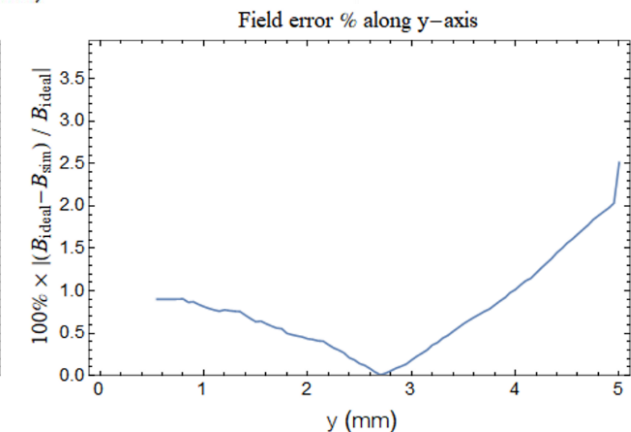
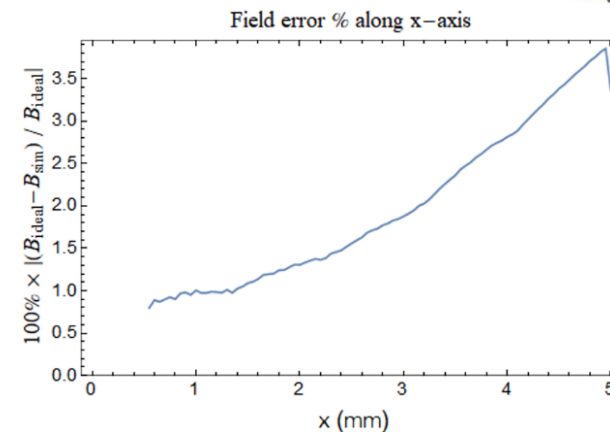
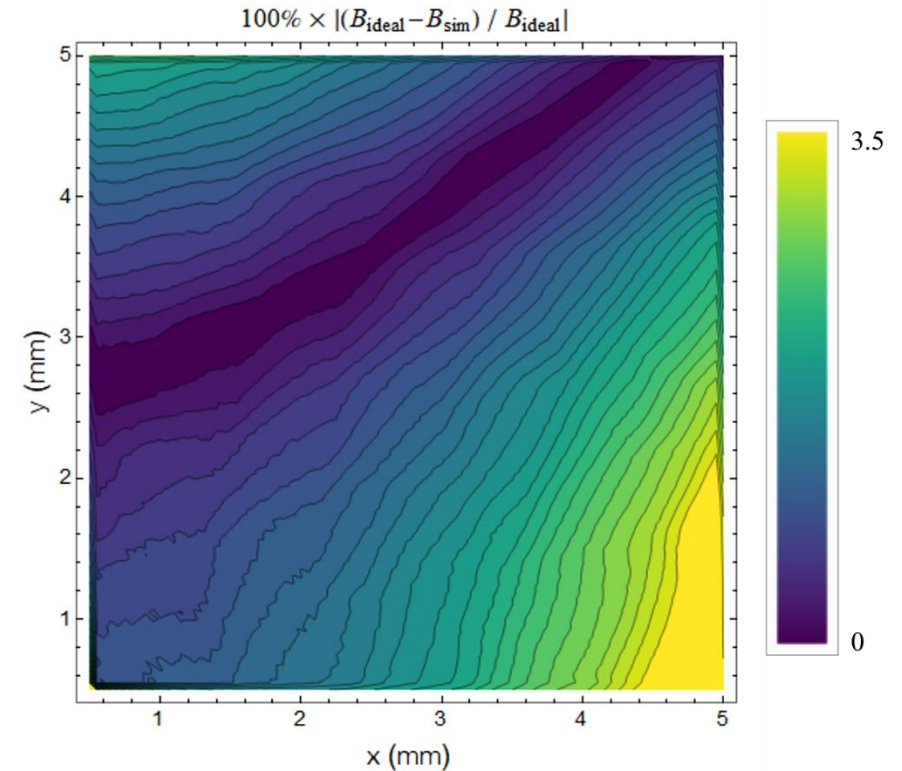
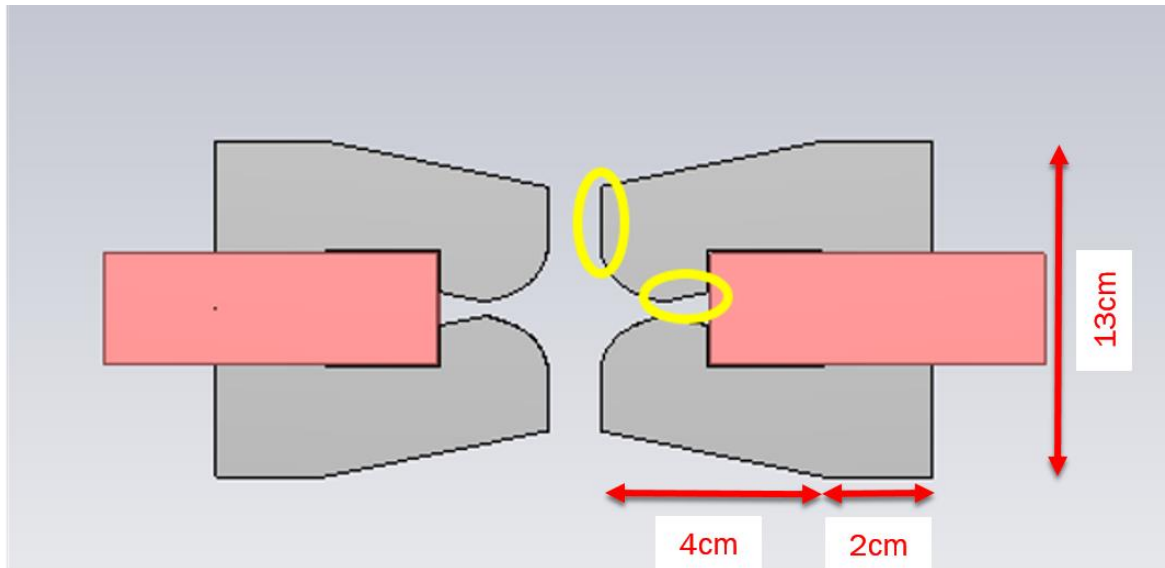
- Basic 3D model of the NLI magnet segment
- The truncation of the pole-face and its connection to the rest of the yoke has a strong impact on the transverse field
  - Future optimization will focus on this connection





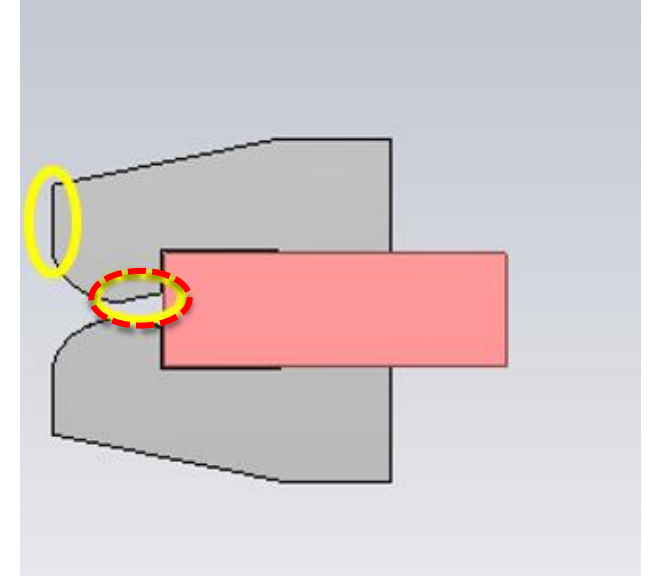
# Field Error from Ideal

- Error from ideal transverse field increases toward the singularity
- Error is due to the finite terminations of the pole-face
- Further iterative optimization is required



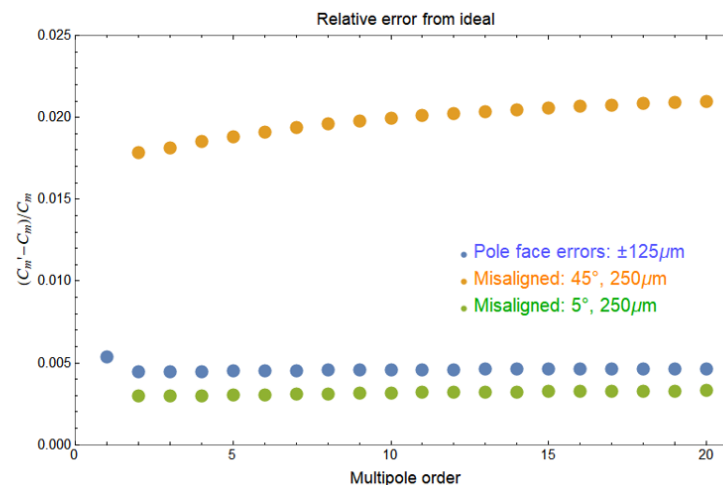
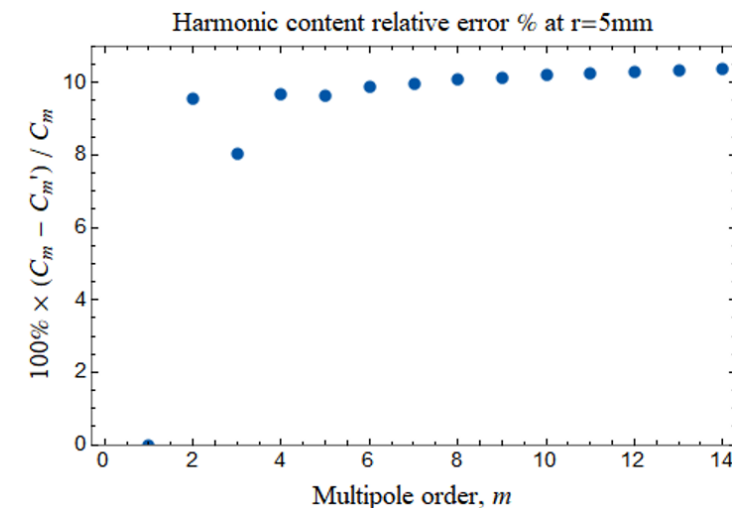
# Harmonic Content

- Multipole expansion of transverse potential:  $F(z) = \sum_m C_m z^m = \sum_m C_m e^{im\theta} r^m$
- Harmonic content error at 5 mm is 10% for the 3D model presented above
  - Further iterative optimization is required
- Harmonic content is sensitive to pole-face misalignment in the vertical direction (pole-face gap is small in the vertical direction)
- Harmonic content is less sensitive to horizontal misalignment and pole face errors



Tolerances

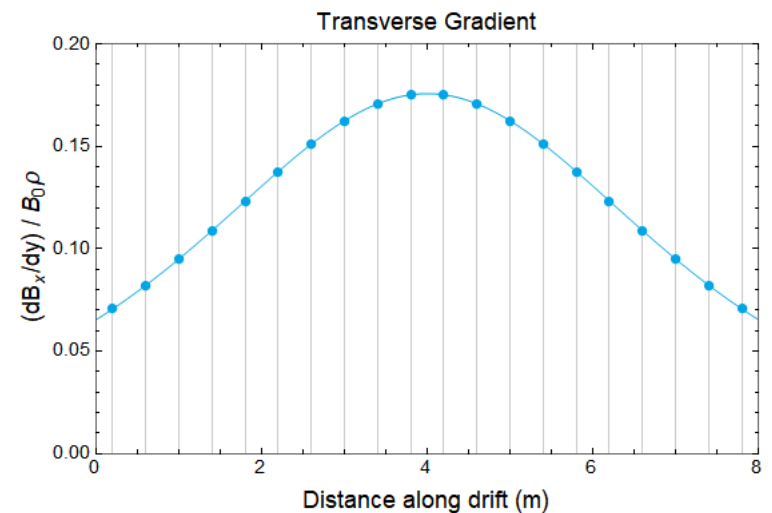
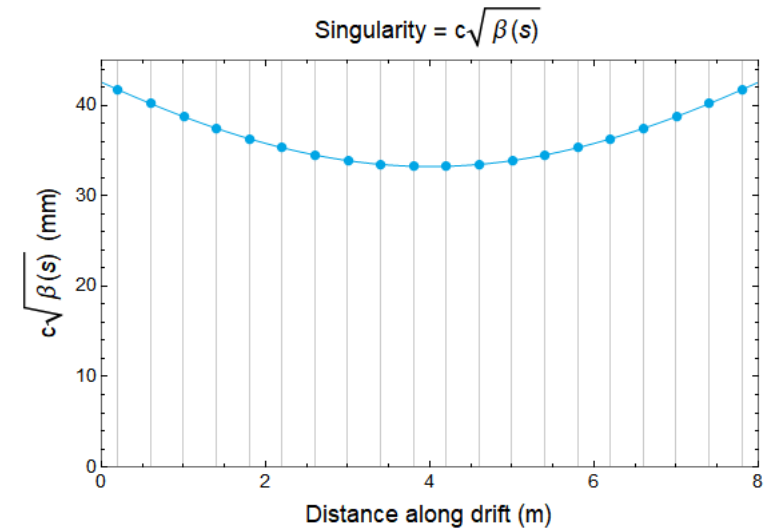
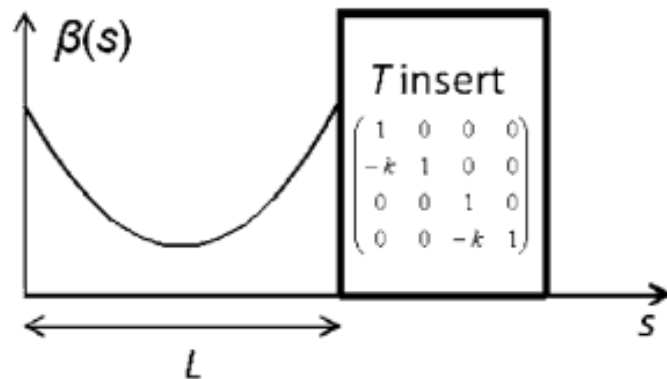
|                                    | IOTA | IRCS | unit |
|------------------------------------|------|------|------|
| surface roughness of pole face cut | 50   | 125  | μm   |
| horizontal offset between poles    | 50   | 250  | μm   |
| vertical offset between poles      | 25   | 125  | μm   |
| segment to segment alignment       | 50   | 200  | μm   |



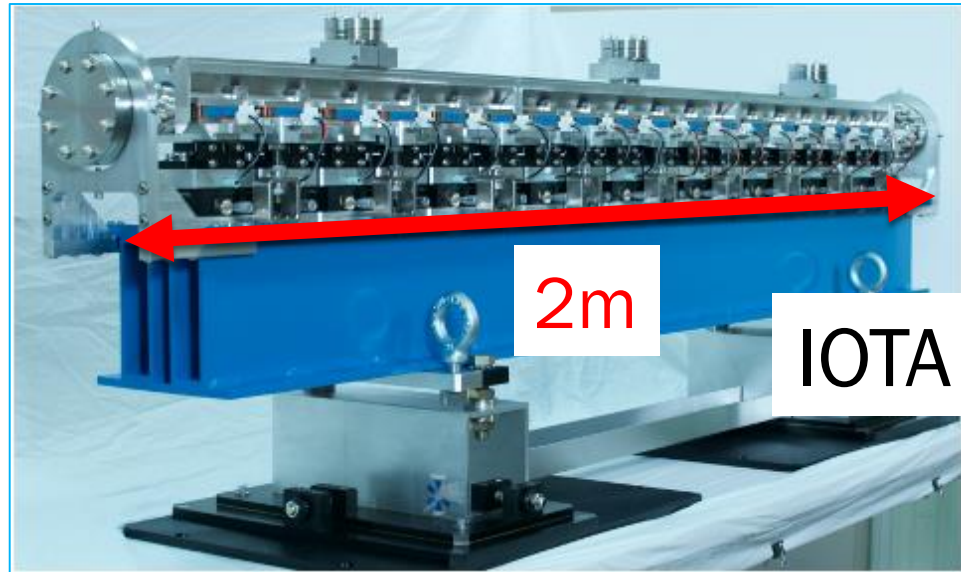


# Longitudinal Variation of NLI

- The size and strength of the NLI will vary along the drift space
- In the plots, there are 20 segments of magnets
  - Good compromise between field quality and fabrication complexity
  - Transferred over from IOTA NLI design
- Each is 30 cm long with 10 cm gap between segments
- The singularity position scales the size of the magnet
- The vertical lines indicate the beginning edge of each magnet segment
- The beta function along the drift is:  $\beta(s) = \frac{L-sk(L-s)}{\sqrt{1-\left(1-\frac{Lk}{2}\right)^2}}$

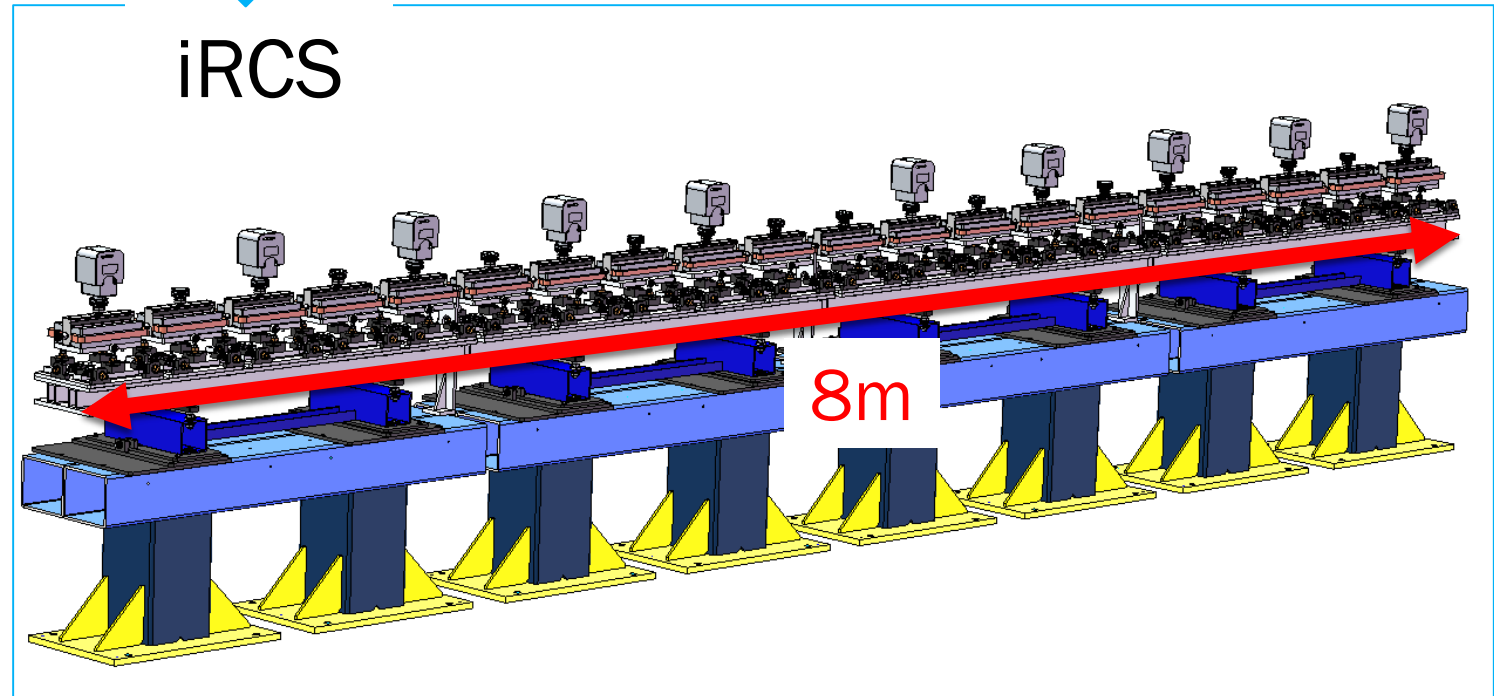


# Scaling to iRCS NLI



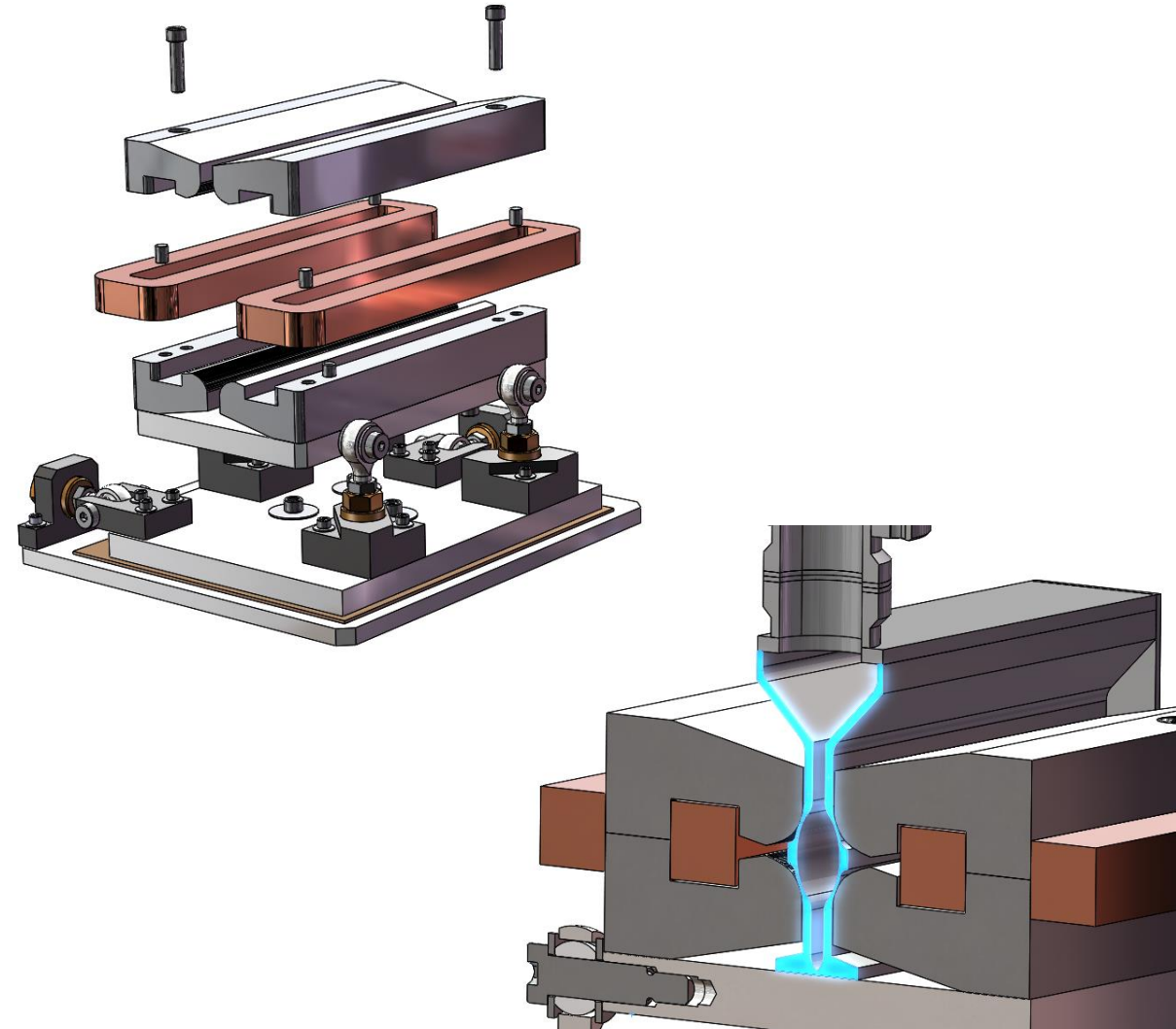
Advantage of more forgivable tolerance stack-up

iRCS



# Preliminary Engineering Considerations

- Iron yokes with copper wire coils
- Will examine high phosphor electronless nickel plating in order to reduce field deviations
  - Nickel may have adverse effect on magnetic field due to its magnetic susceptibility
- Each magnet segment will be mounted on a precision kinematic stand (designed at RadiaBeam)
  - Differential screws with  $<0.001''$  resolution
- Vacuum chamber:
  - Vacuum required:  $<10^{-10}$  Torr
  - Antechamber on top of beam tube to increase conductance of vacuum chamber
  - Ion pumps are located on top of chamber, but want to move to side or bottom for decreased moment.
    - Prevent undesirable influence from stray fields or increased conductivity



| Sub-task  | Objective  |
|---|--|
| 1. Finalize iRCS engineering  | Complete the full iRCS system engineering  |
| 2. Magnet Fabrication and validation                                      | Machine the poles and yokes, facilitate machine shop work  |
| 3. Chamber Fabrication and validation                                     | Machine vacuum chamber components and weld.  |
| 4. Support and kinematic fabrication                                      | Machine all components of the support system   |
| 5. Magnetic validation system development and magnet segment measurements | Ensure full magnetic validation suite is functional and measure the field components and locate the magnetic field to tooling features |
| 6. System assembly  | Integrate the components into full system  |

Q4 2022

**THANK YOU**