

# Proton-pion Transverse Kinematic Imbalance analysis

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University of Oxford

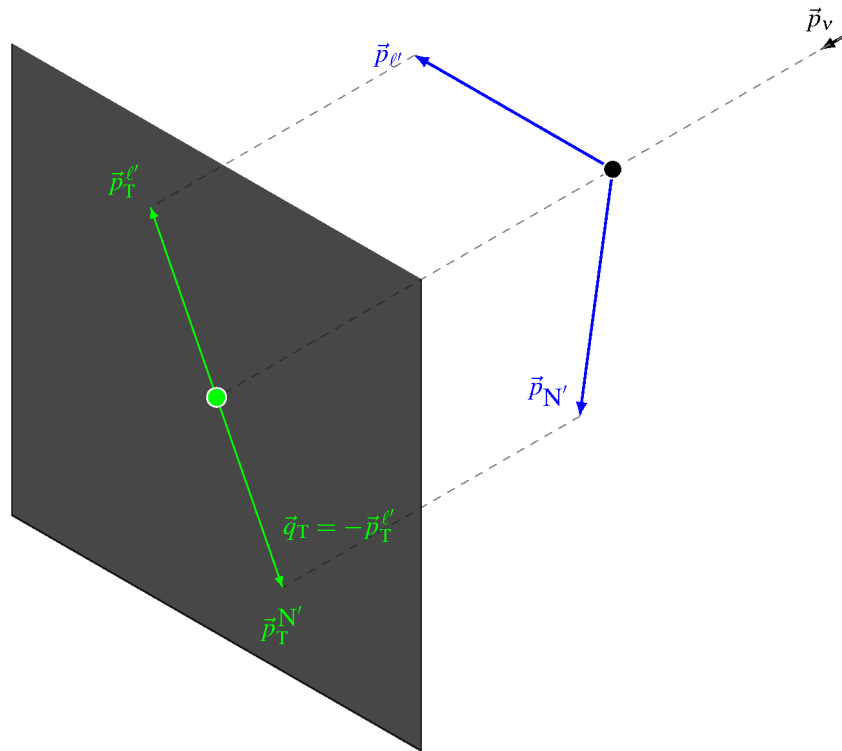
2020 May 21  
ProtoDUNE Analysis Meeting

# Transverse Kinematic Imbalance (TKI)

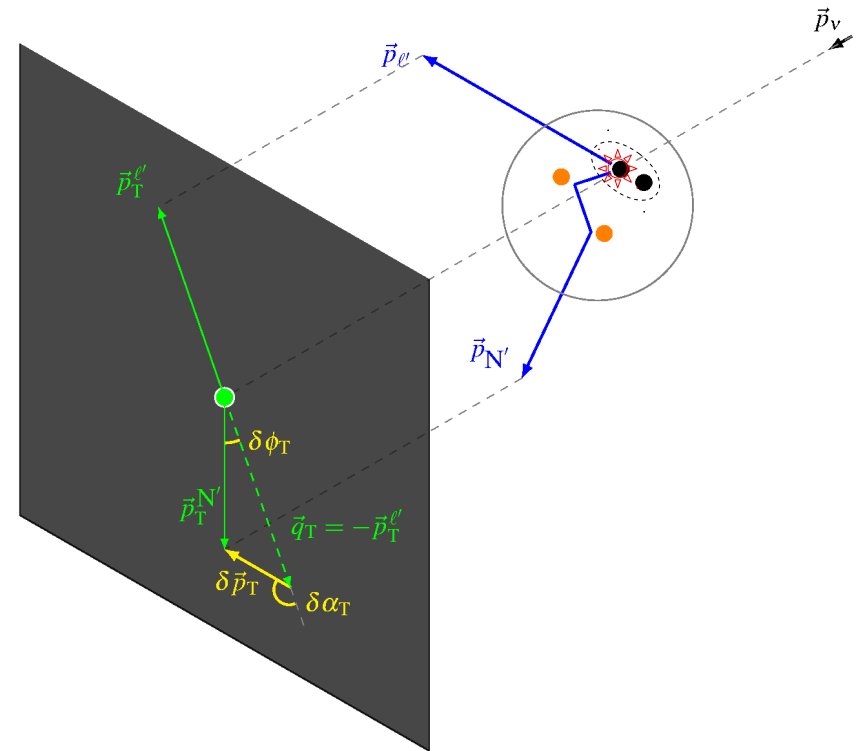
to precisely identify intranuclear dynamics and the absence thereof

XL *et al.* Phys. Rev. D92, 051302 (2015), arXiv:1507.00967 [hep-ex]

XL *et al.* Phys. Rev. C94, 015503 (2016), arXiv:1512.05748 [nucl-th]



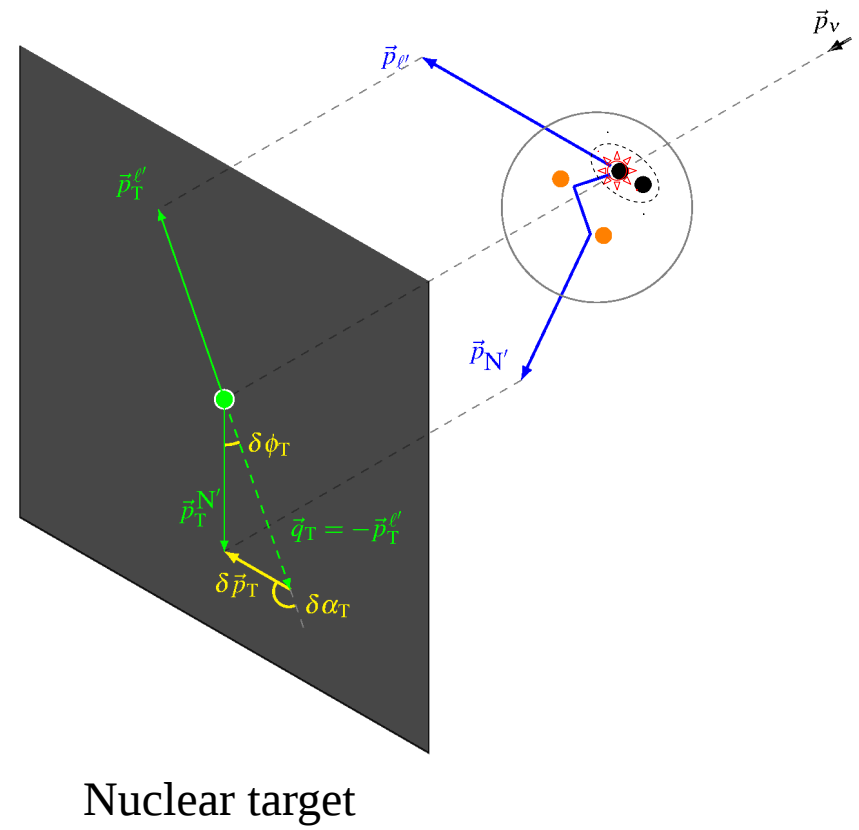
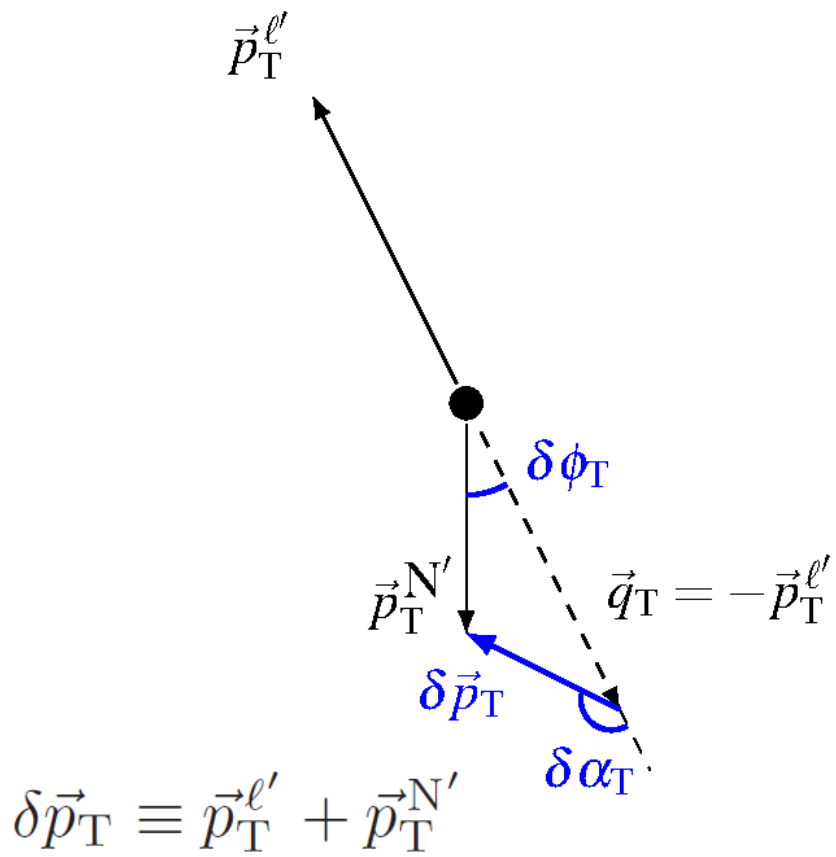
Stationary nucleon target

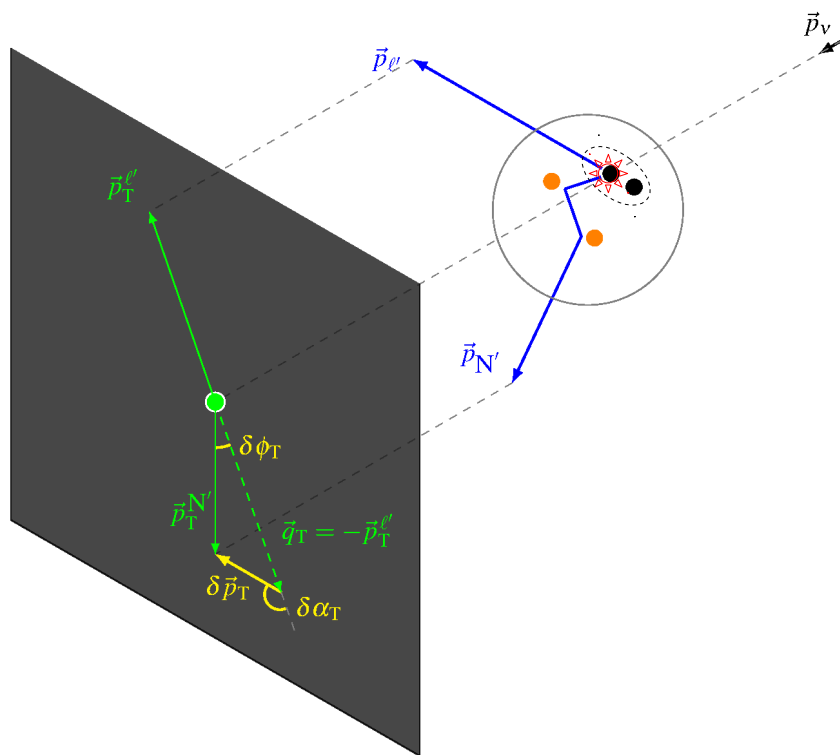


Nuclear target  
( $A > 1$ )

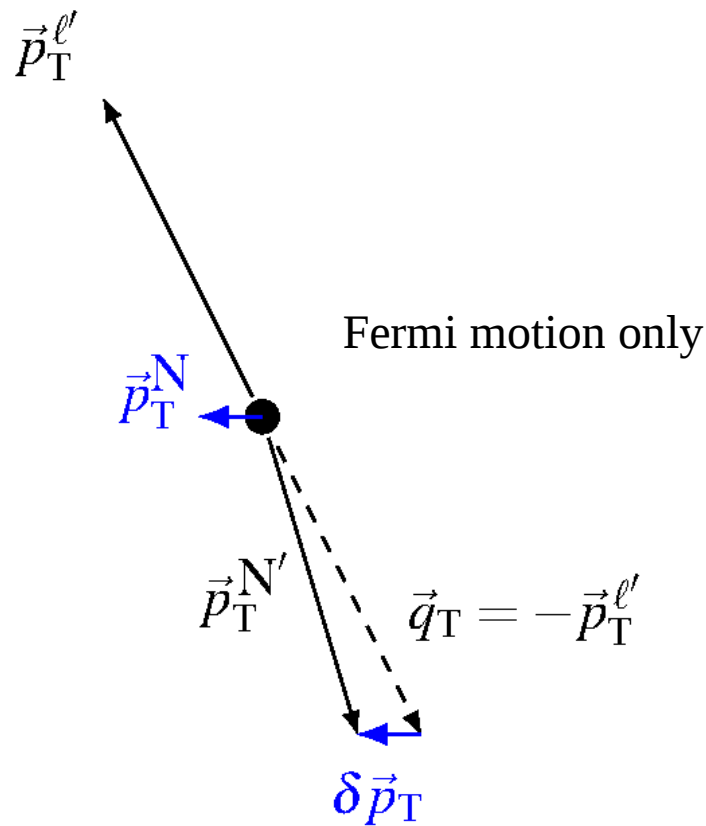
Fermi motion  
Final-state interactions  
Pion absorption  
2p2h

...





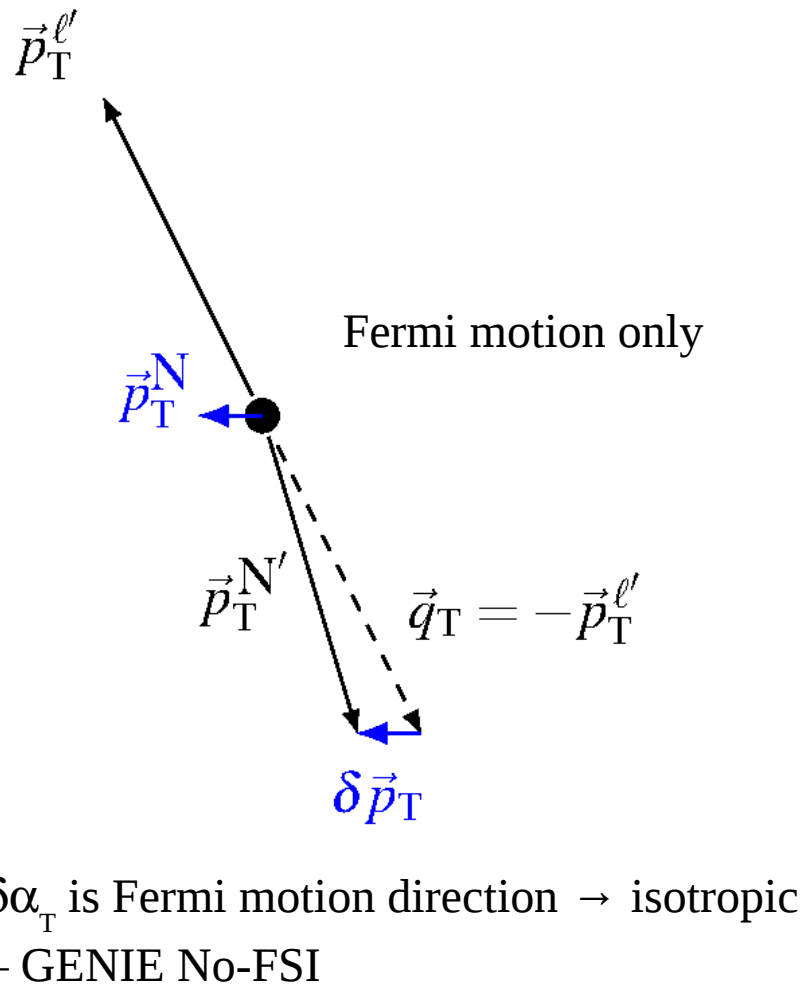
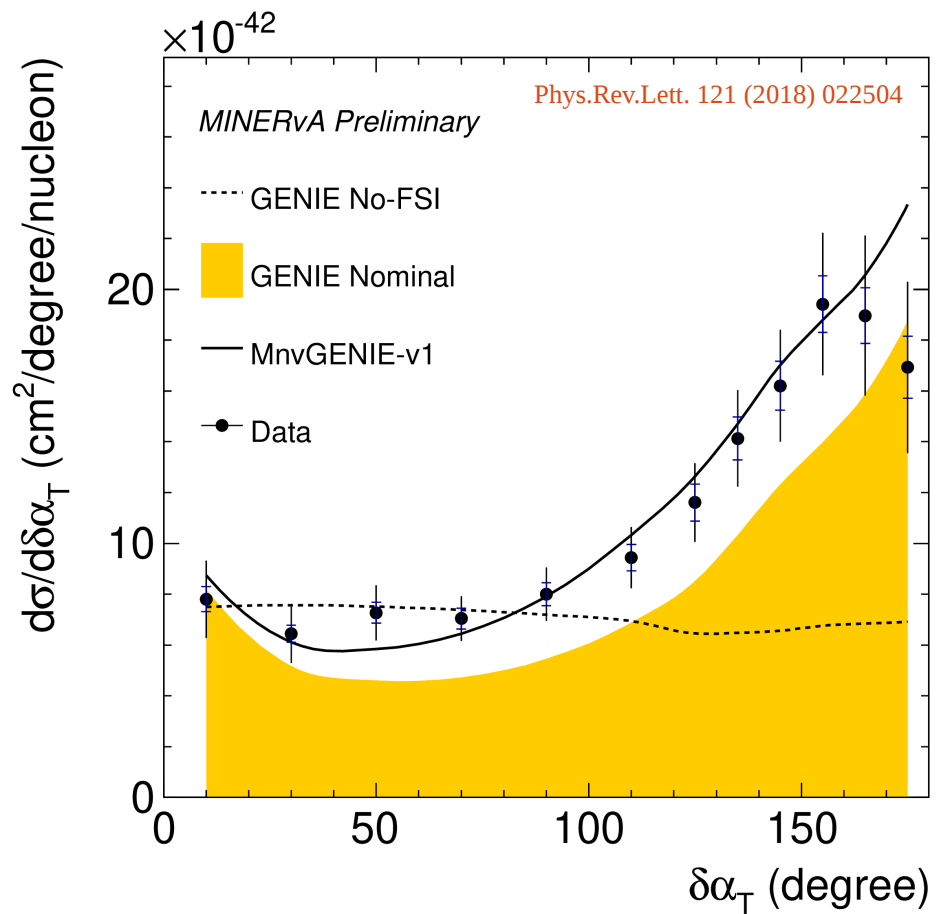
Nuclear target

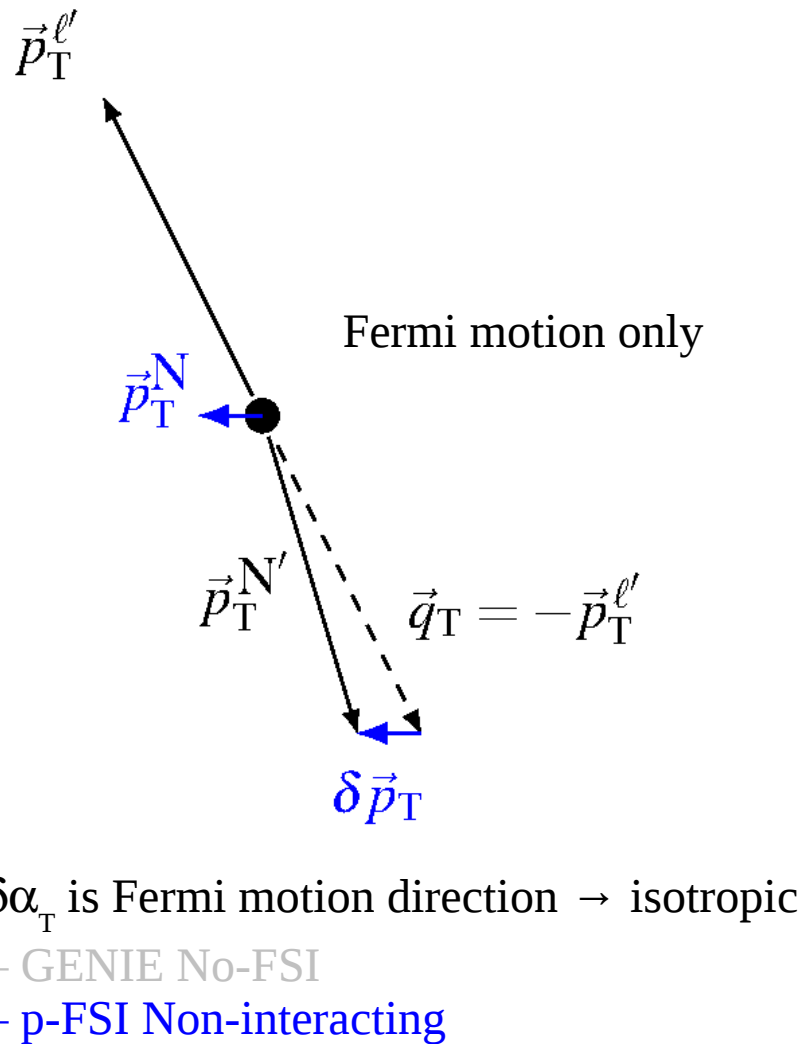
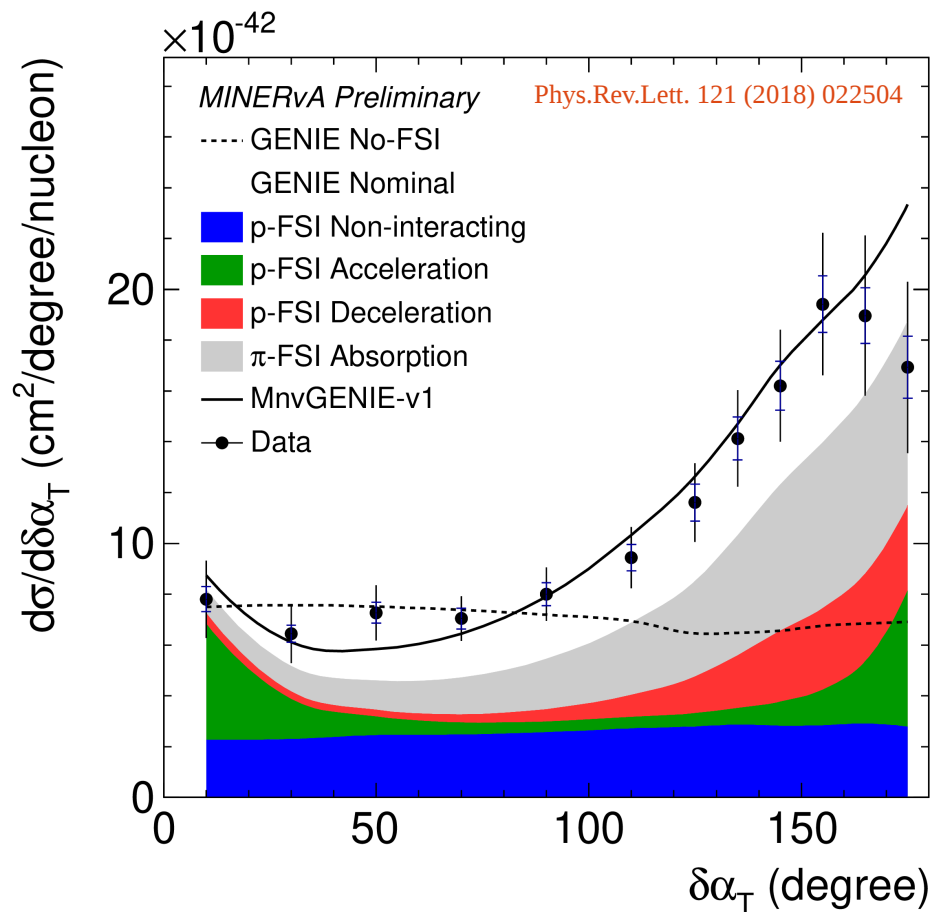


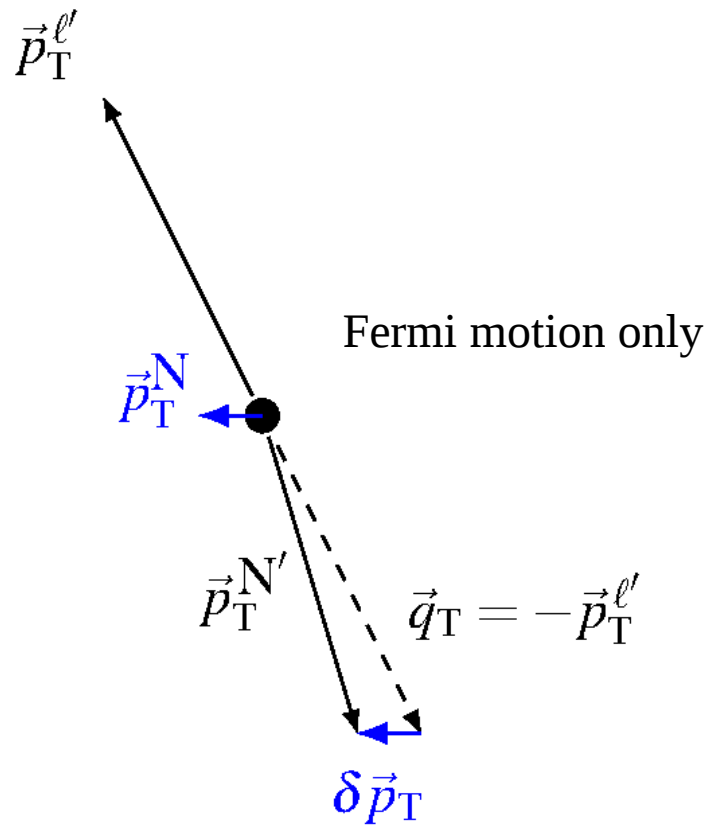
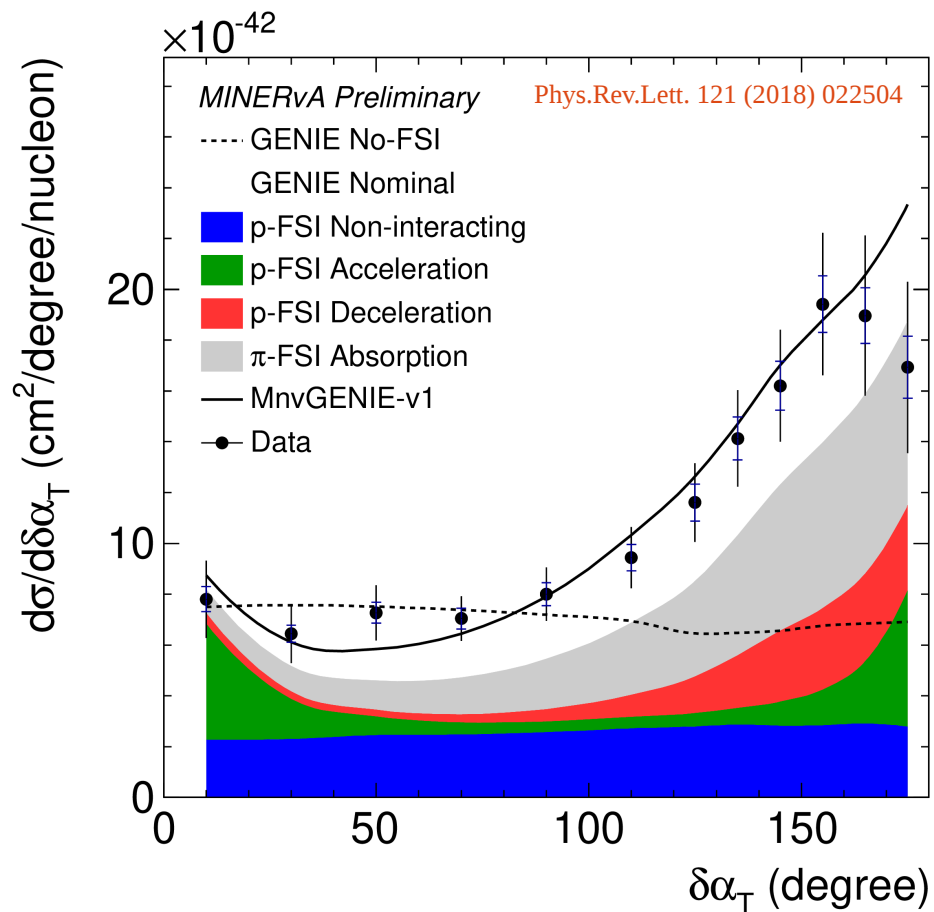
Fermi motion only

$$\delta \vec{p}_T = \vec{p}_T^N$$

$\delta \alpha_T$  is Fermi motion direction  $\rightarrow$  isotropic



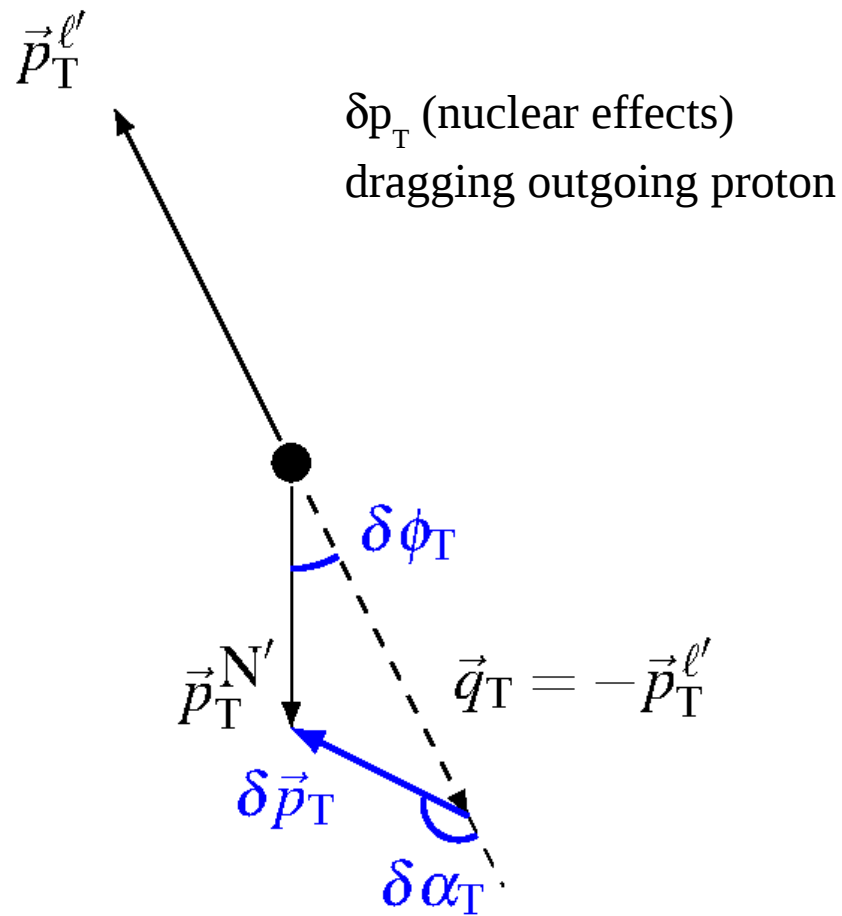
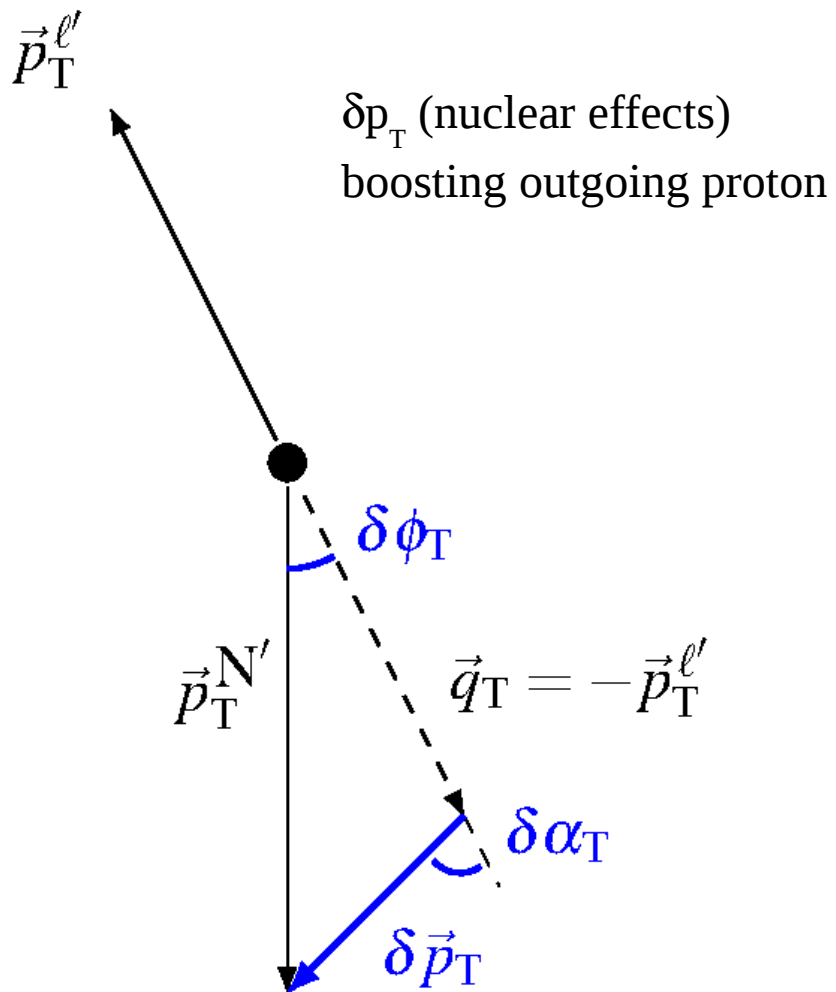




$\delta\alpha_T$  is Fermi motion direction  $\rightarrow$  isotropic  
 – GENIE No-FSI  
 – p-FSI Non-interacting

- Impact from interaction on nucleon canceled by lepton-hadron correlation;
- Impact from Fermi motion also canceled due to isotropy.

# Transverse Boosting Angle

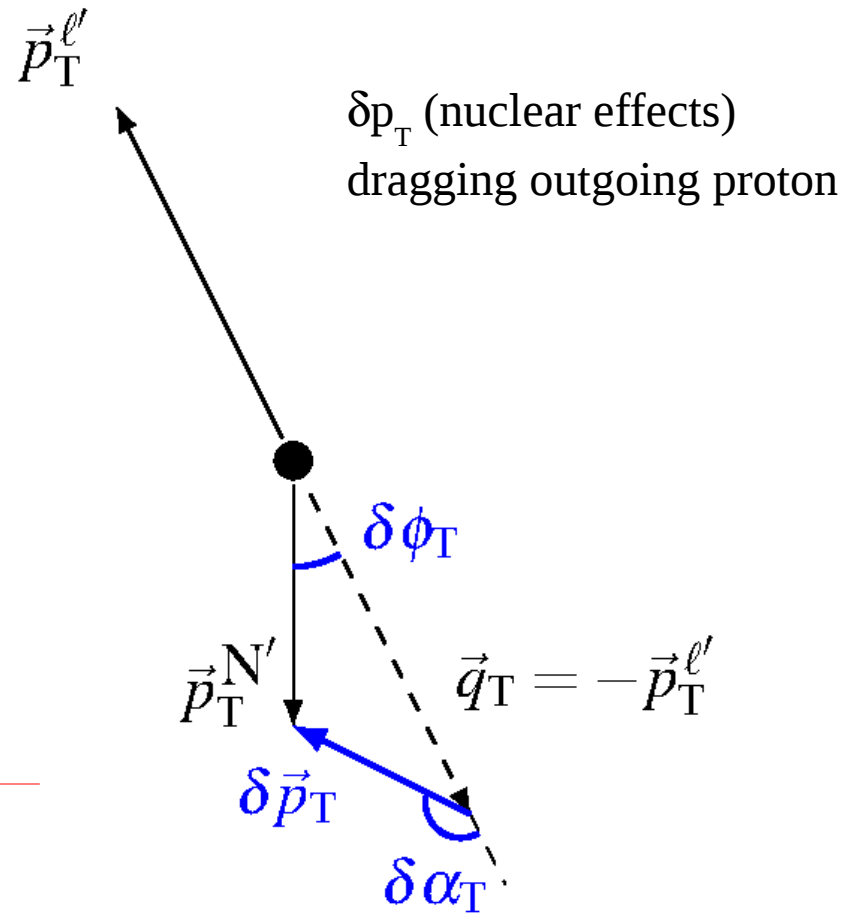
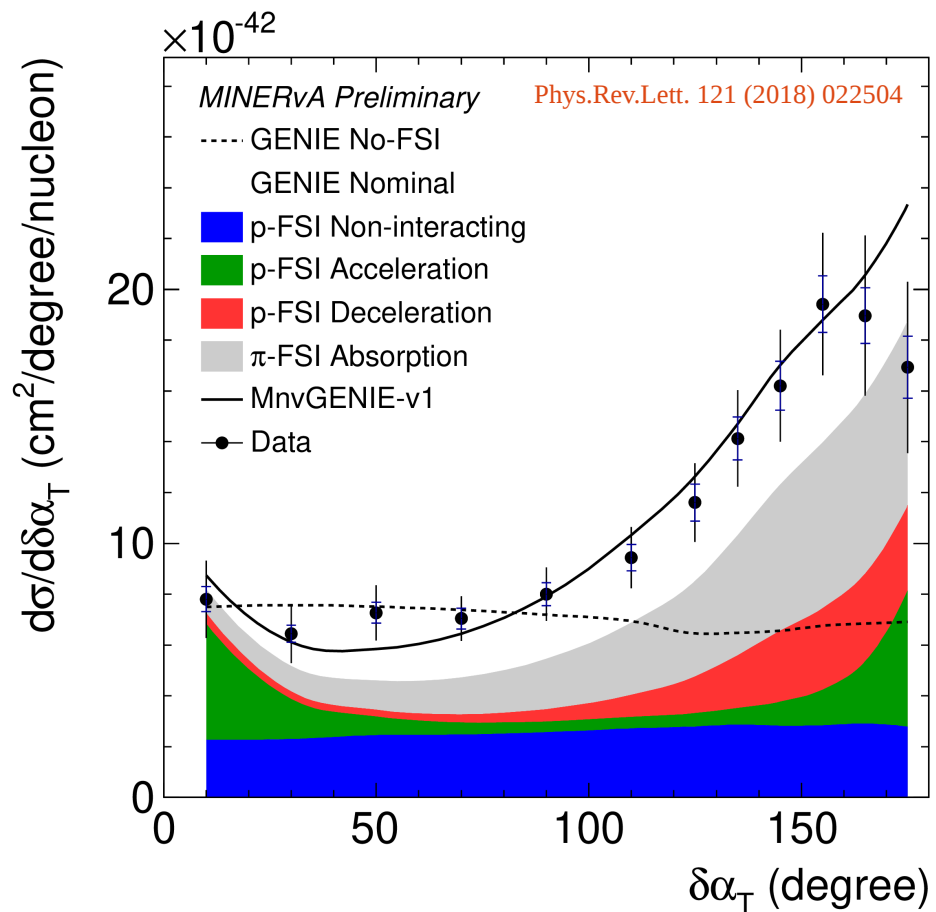


With full nuclear effects

$$\delta\vec{p}_T = \vec{p}_T^{N'} - \Delta\vec{p}_T \quad \text{non-Fermi motion effects}$$

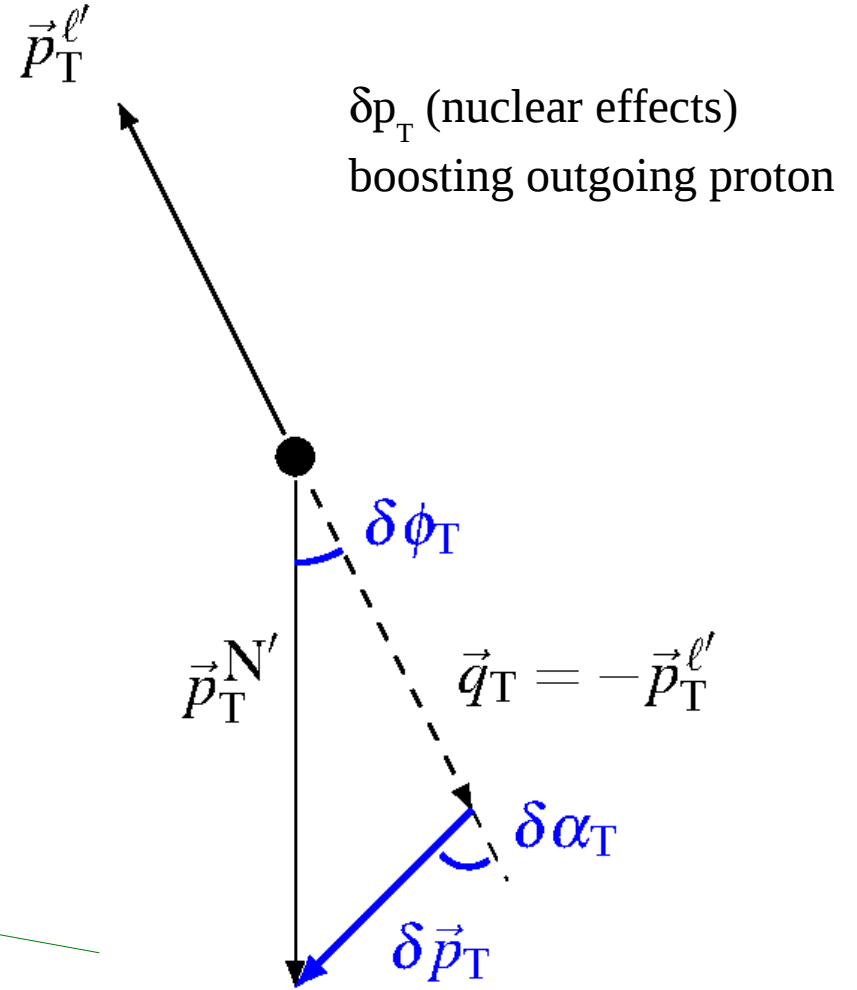
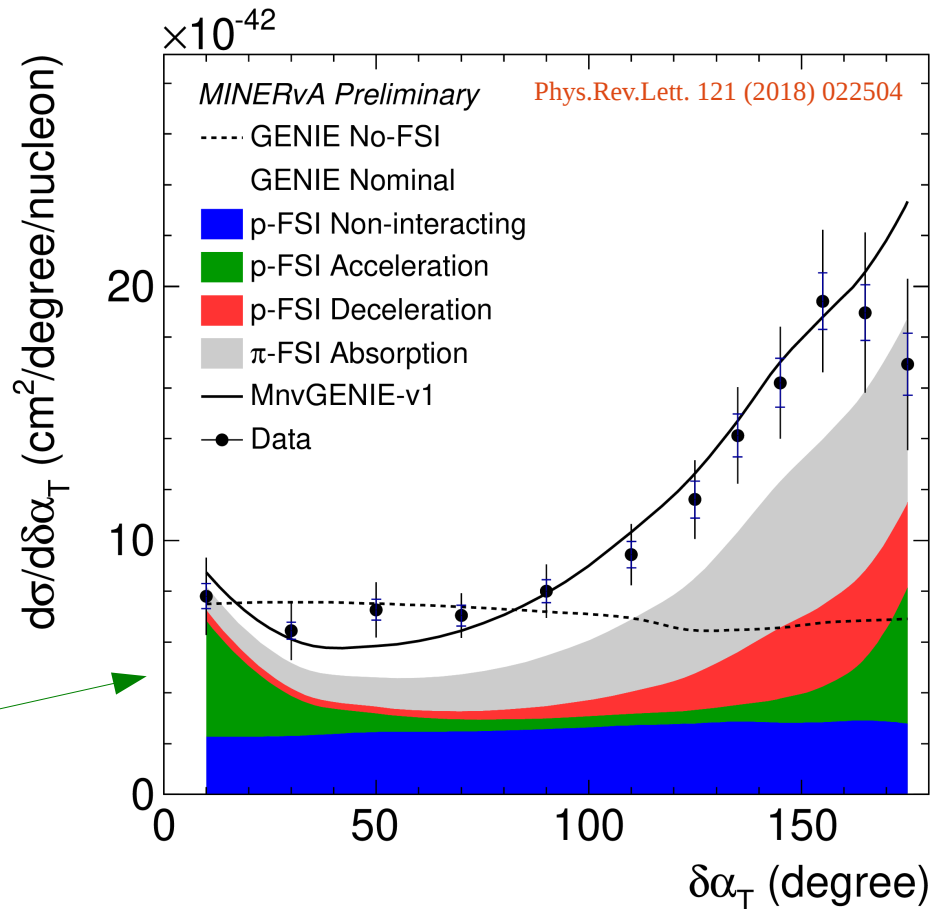


# Transverse Boosting Angle



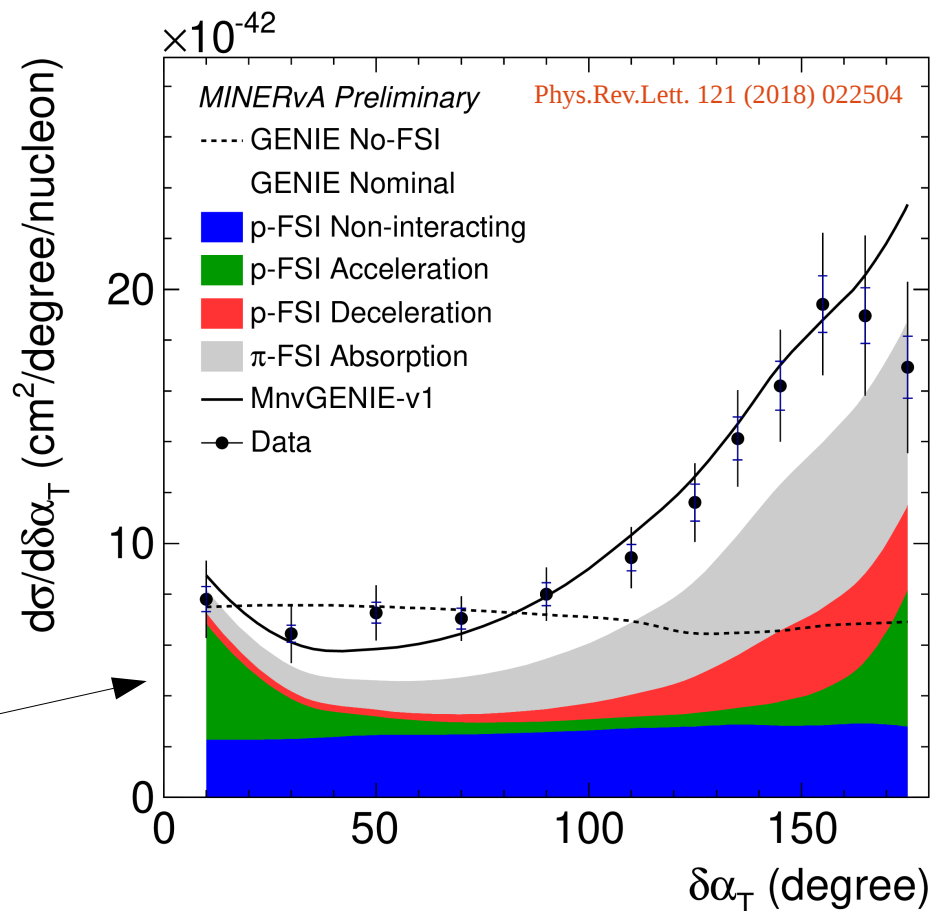
Deceleration at large  $\delta\alpha_T$

# Transverse Boosting Angle

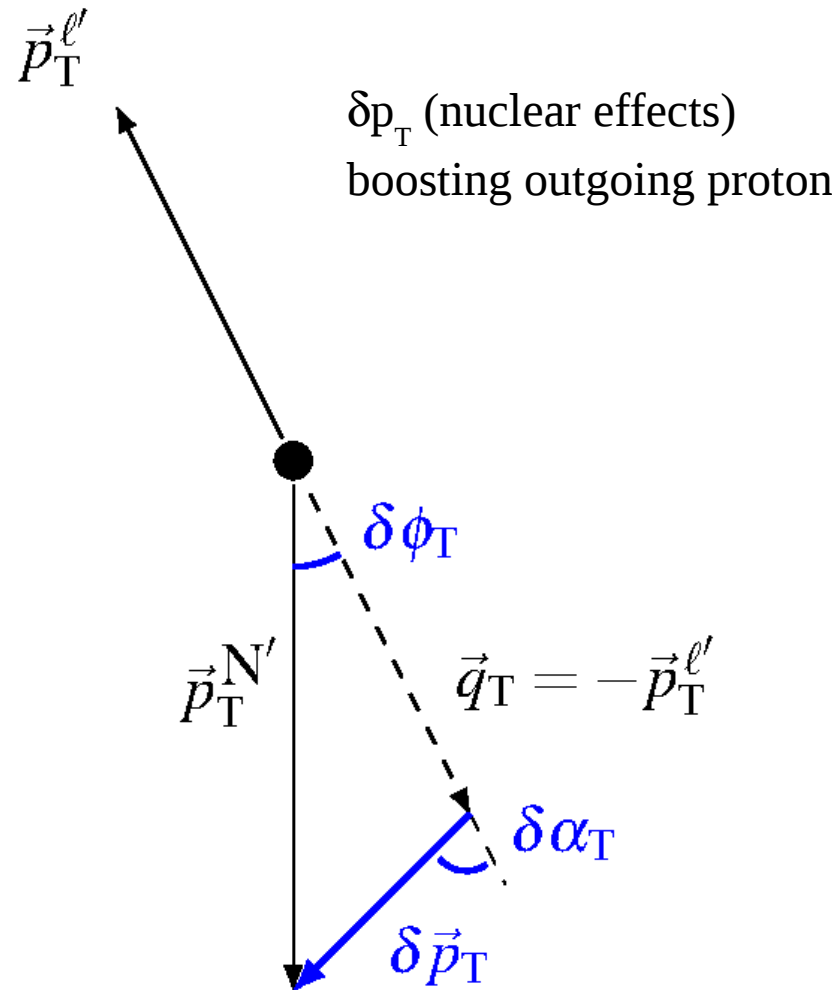


Deceleration at large  $\delta\alpha_T$   
 Acceleration at both small and (due to transverse projection) large  $\delta\alpha_T$

# Transverse Boosting Angle

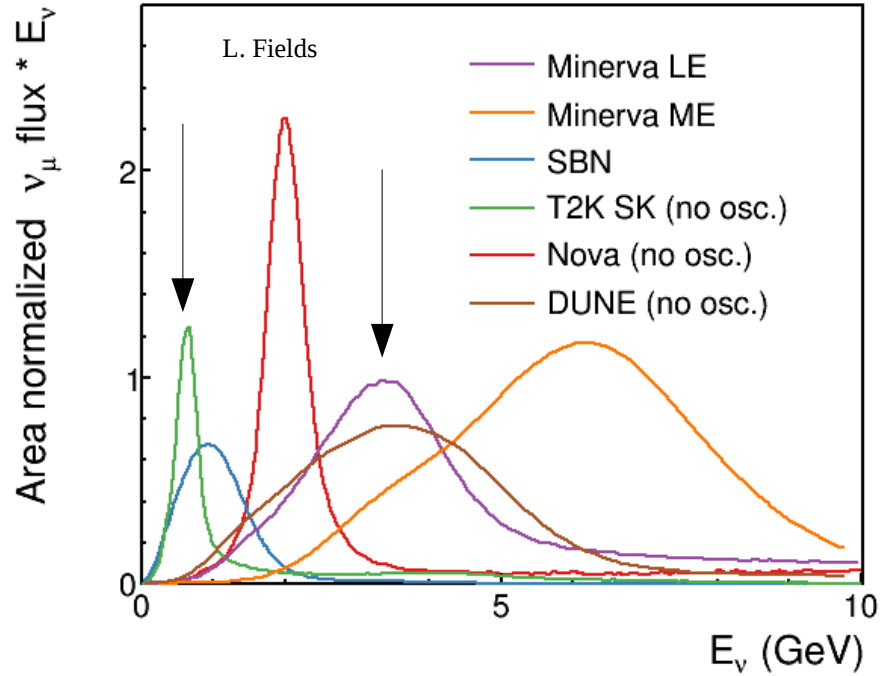


- Accelerating FSI is singled out
- Discovered from model for the first time



Deceleration at large  $\delta\alpha_T$   
 Acceleration at both small and (due to transverse projection) large  $\delta\alpha_T$

# Transverse Boosting Angle



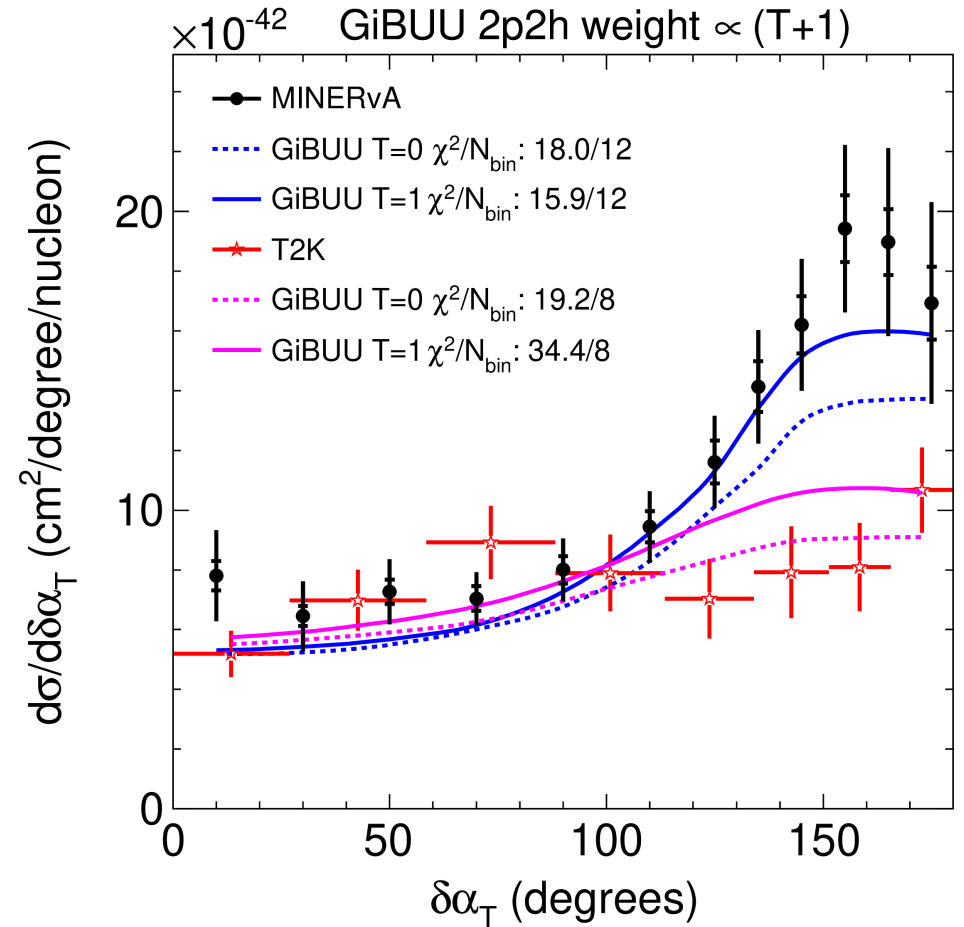
T2K neutrino beam peak at 0.6 GeV

[T2K, Phys. Rev. D 98, 032003 (2018)]

MINERvA at 3 GeV

[MINERvA, Phys. Rev. Lett. 121, 022504 (2018)]

- Gross feature of energy dependence confirmed by data



# Emulated Nucleon Momentum

A more general analysis of kinematic imbalance

Transverse:  $0 = \vec{p}_T^{\ell'} + \vec{p}_T^{N'} - \delta\vec{p}_T$

Longitudinal:  $E_\nu = p_L^{\ell'} + p_L^{N'} - \delta p_L$

New variable:  $p_n \equiv \sqrt{\delta p_T^2 + \delta p_L^2}$

[Furmanski, Sobczyk, Phys.Rev. C95 (2017) 065501]

Neutrino energy is unknown (in the first place), equations are not closed.

Assuming exclusive  $\mu$ -p-A' final states  
Use energy conservation to close the equations

$$E_\nu + m_A = E_{\ell'} + E_{N'} + E_{A'}$$

$$E_{A'} = \sqrt{m_{A'}^2 + p_n^2}$$

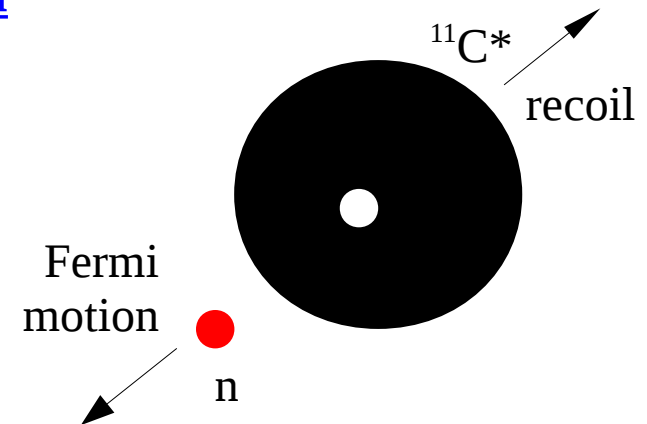
$p_n$ : recoil momentum of the nuclear remnant

final-state

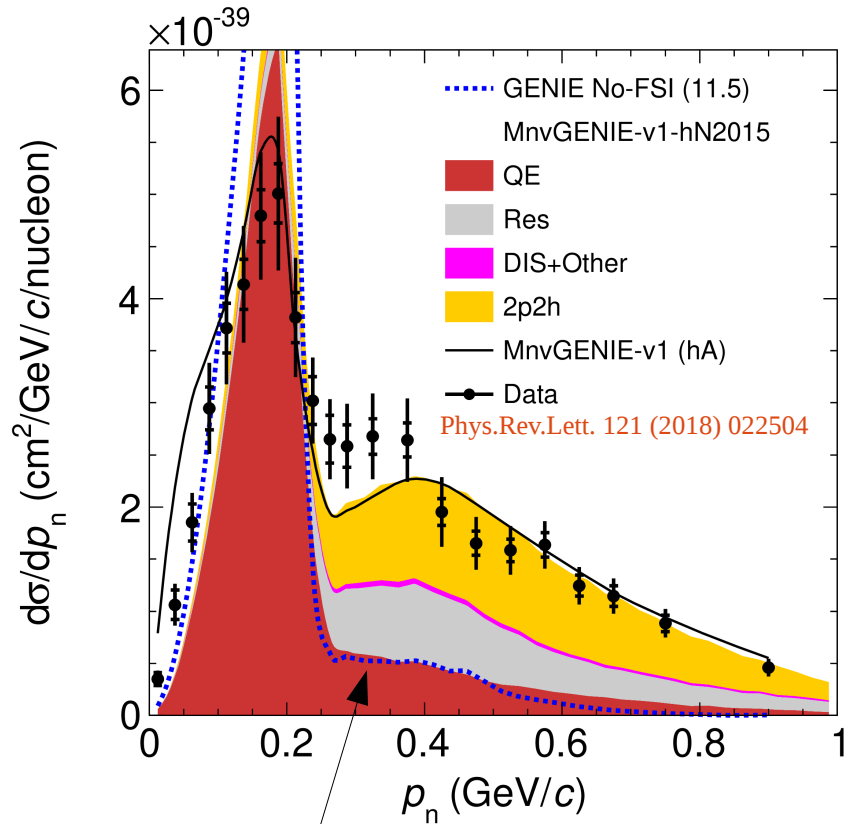
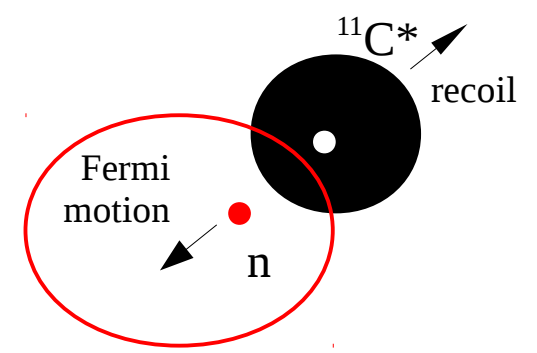
**Dual Interpretation**

For CCQE,  $A' = {}^{11}\text{C}^*$   
No more unknowns  
 $p_n$ : neutron Fermi motion

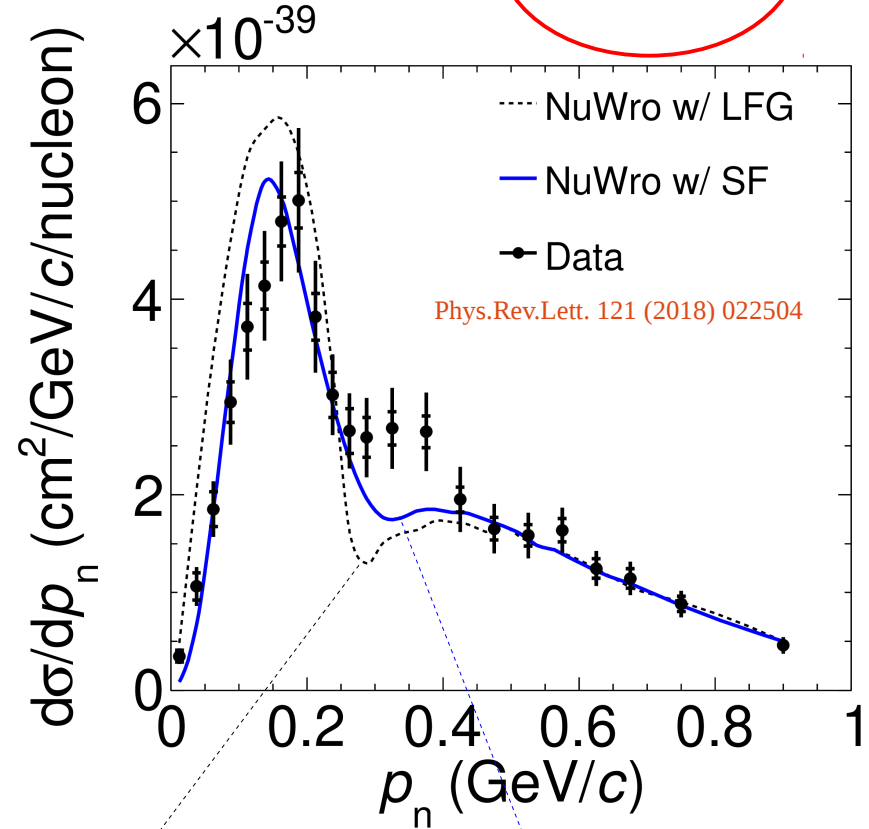
initial-state



# Emulated Nucleon Momentum



Global Fermi Gas with Bodek-Ritchie tail



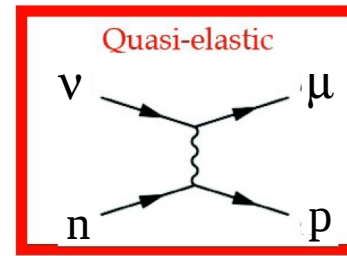
Local Fermi Gas

Spectral Function

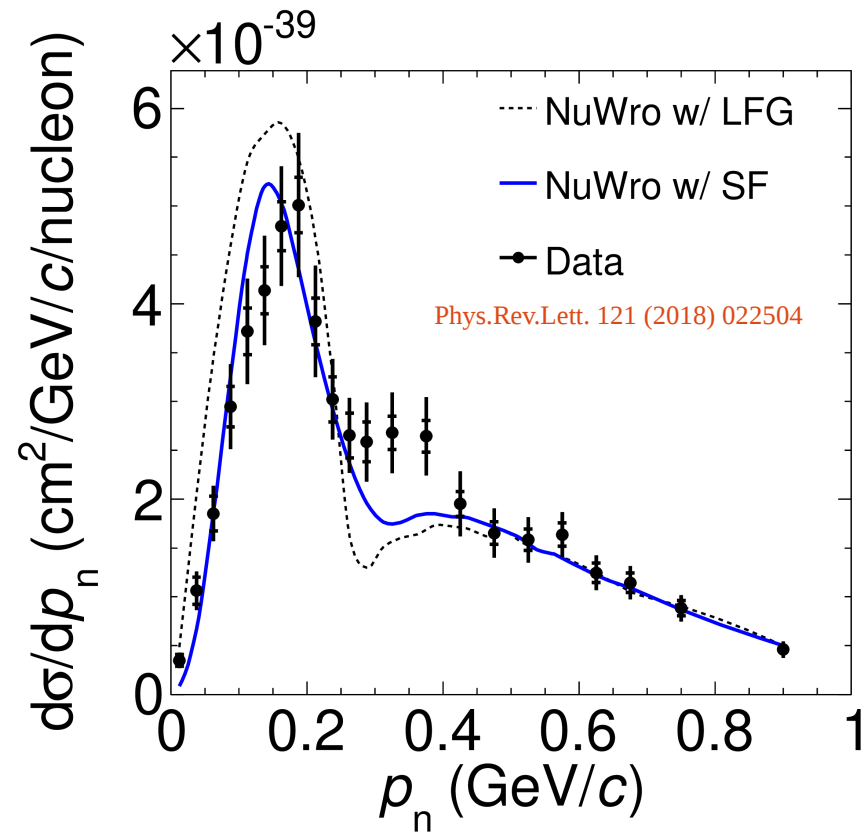
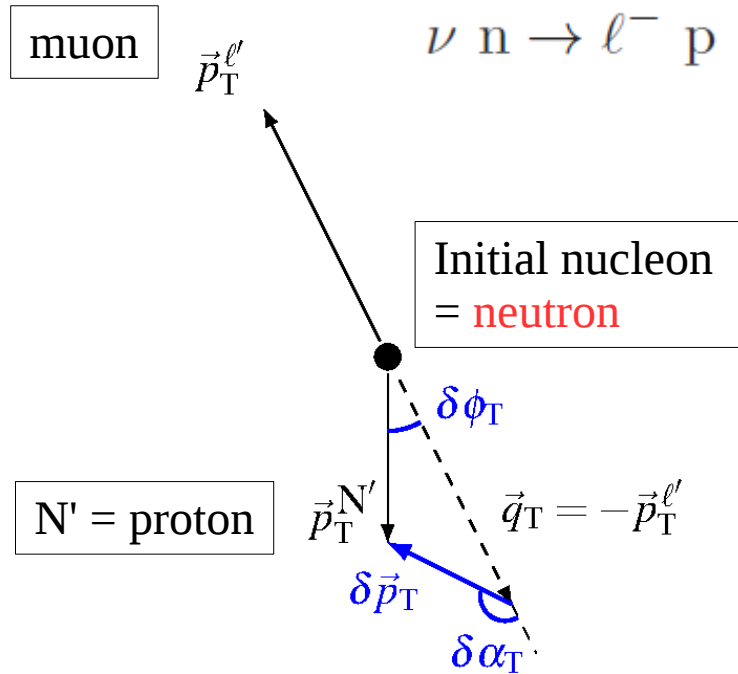
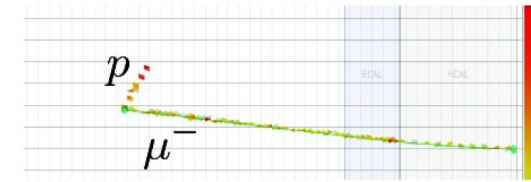
$$p_n \equiv \sqrt{\delta p_T^2 + \delta p_L^2}$$

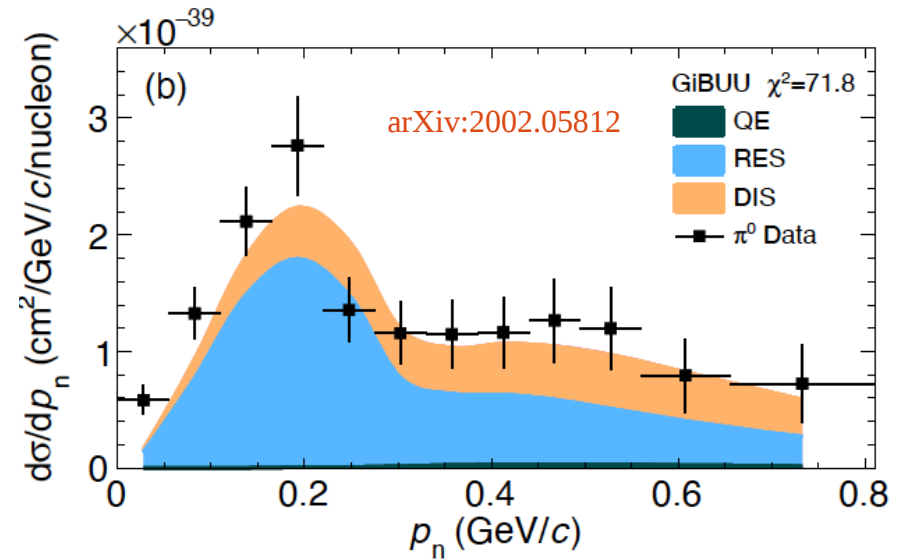
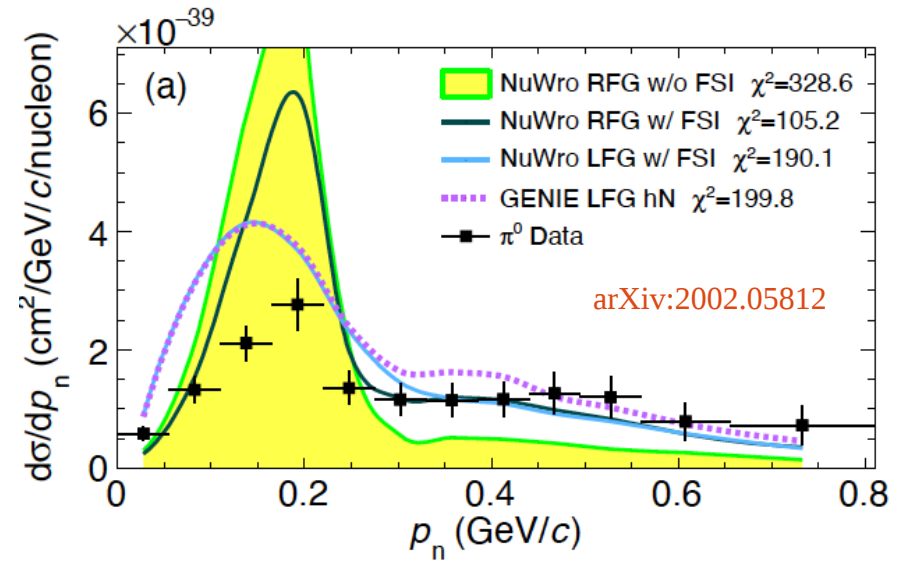
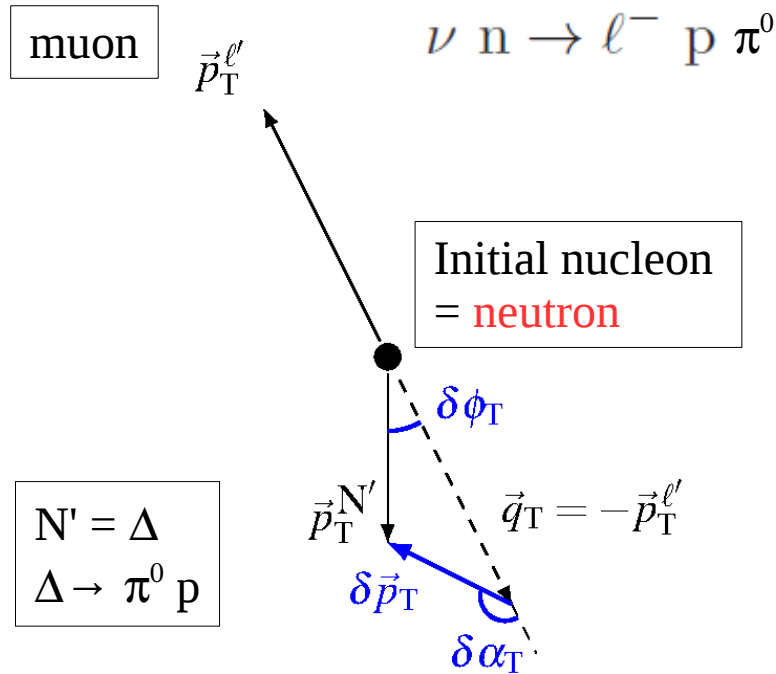
# TKI

## – Neutron initial-state kinematics



QE

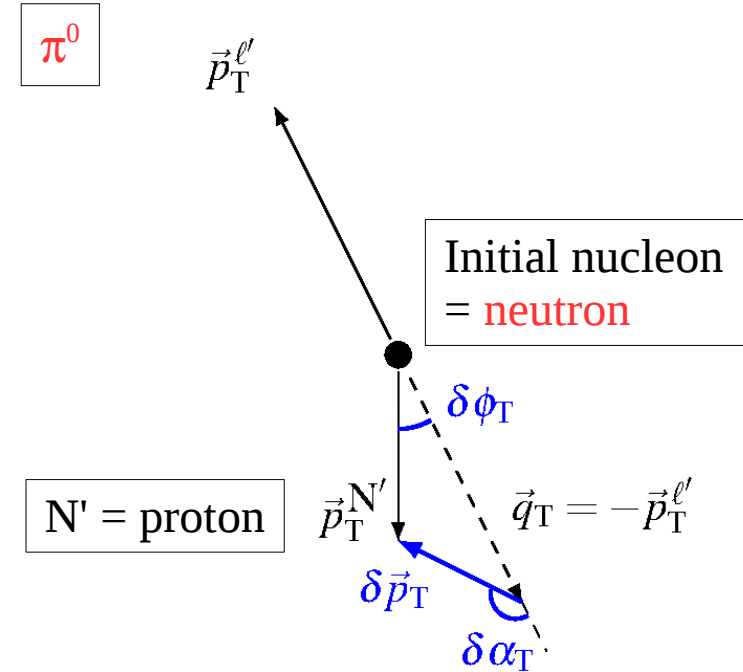
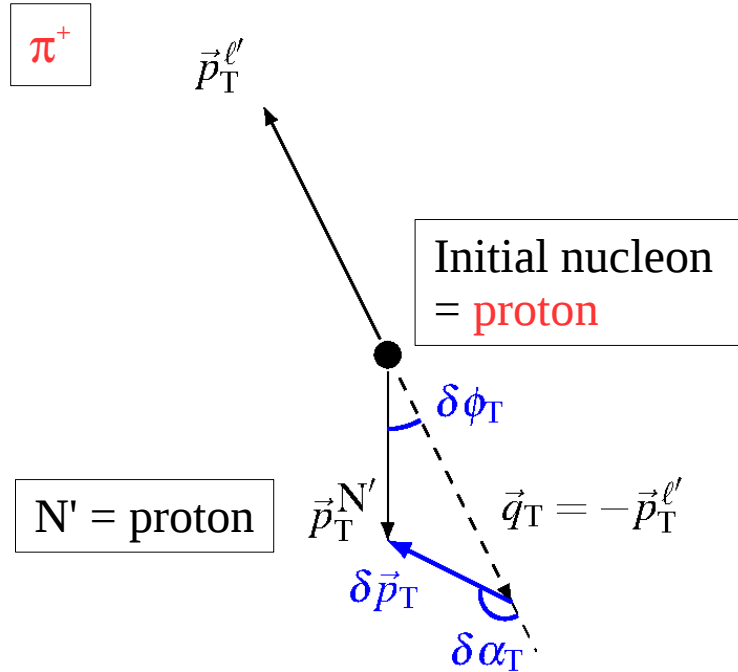
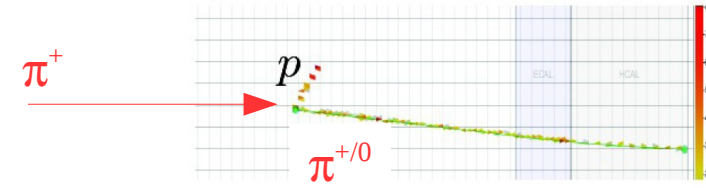


– *Neutron* initial-state kinematics



# TKI + protoDUNE

– *Proton/Neutron* initial-state kinematics



Data set:

calcuttj\_PDSPProd2\_MC\_1GeV\_reco\_sce\_datadriven\_forced\_reco  
3447 out of all 3486 files finished without error

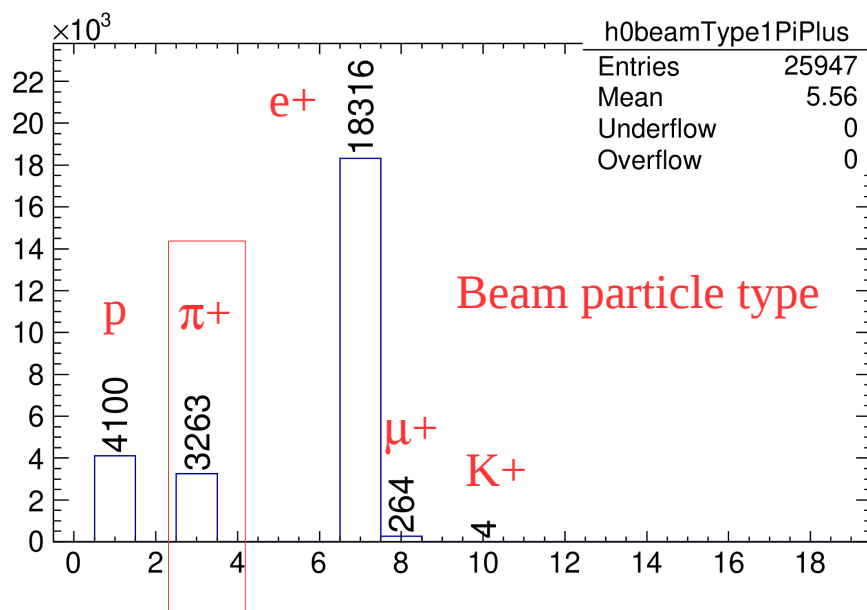
statistics: the total merged file size is 381M. The merged tree has 25947 entries.

The following **true-level** variables are used:

```
vector<int> *true_beam_daughter_PDG=0x0;  
vector<double> *true_beam_daughter_startPx=0x0;  
vector<double> *true_beam_daughter_startPy=0x0;  
vector<double> *true_beam_daughter_startPz=0x0;  
double true_beam_endPx = -999;  
double true_beam_endPy = -999;  
double true_beam_endPz = -999;  
int true_beam_PDG = -999;
```

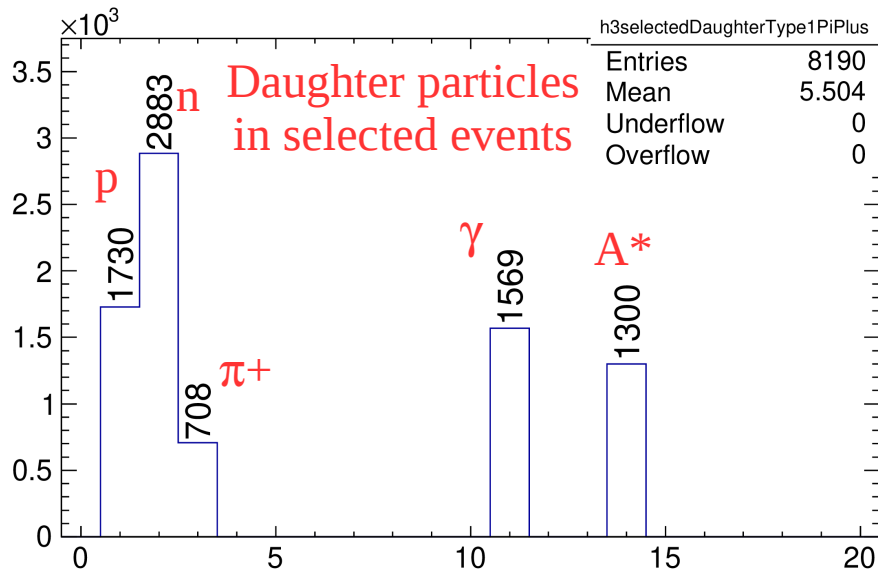
## Purpose of this feasibility study:

- Figure out signal definition
- Estimation statistics



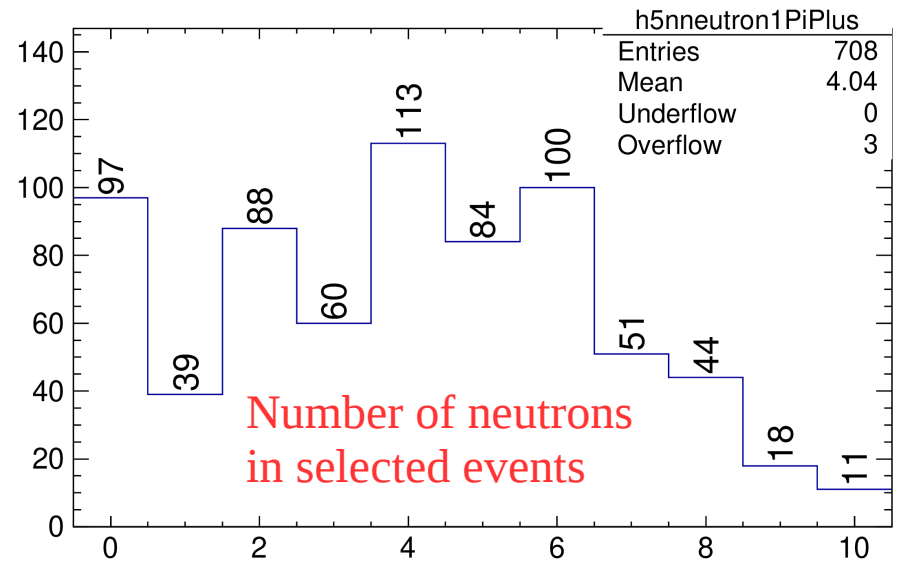
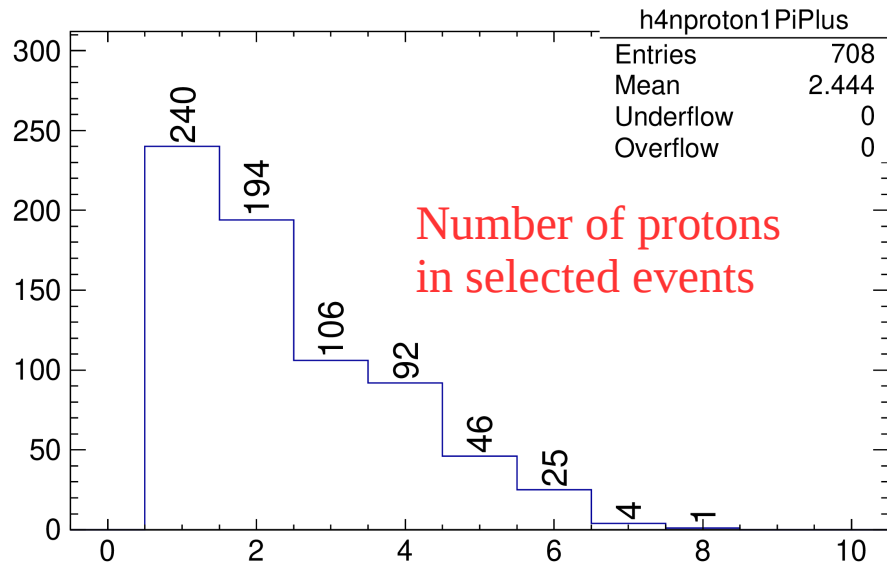
3263 pi+ beam events  
(3263/25947 = 12.6%)

Q: are these true events AFTER reconstruction?  
(That is, already suppressed by 1-efficiency?)



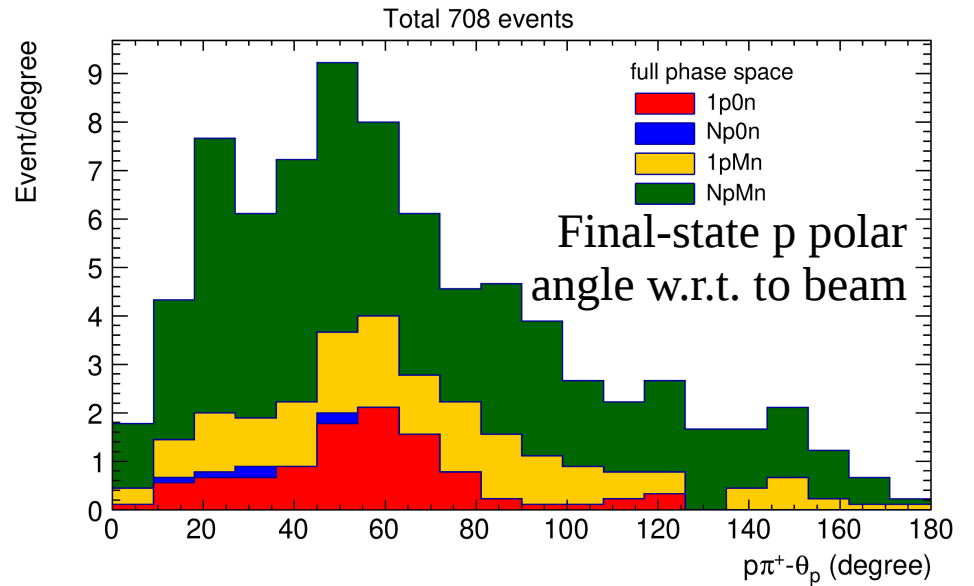
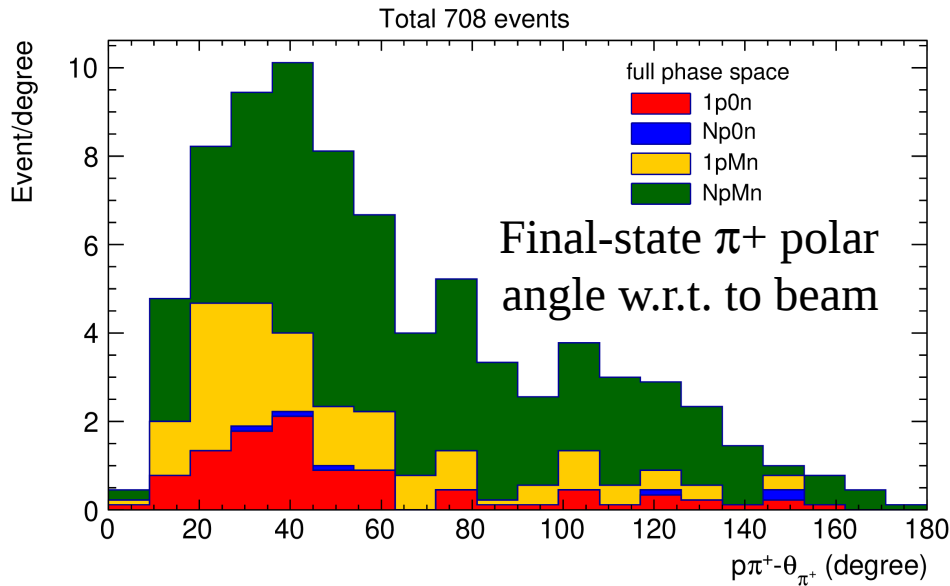
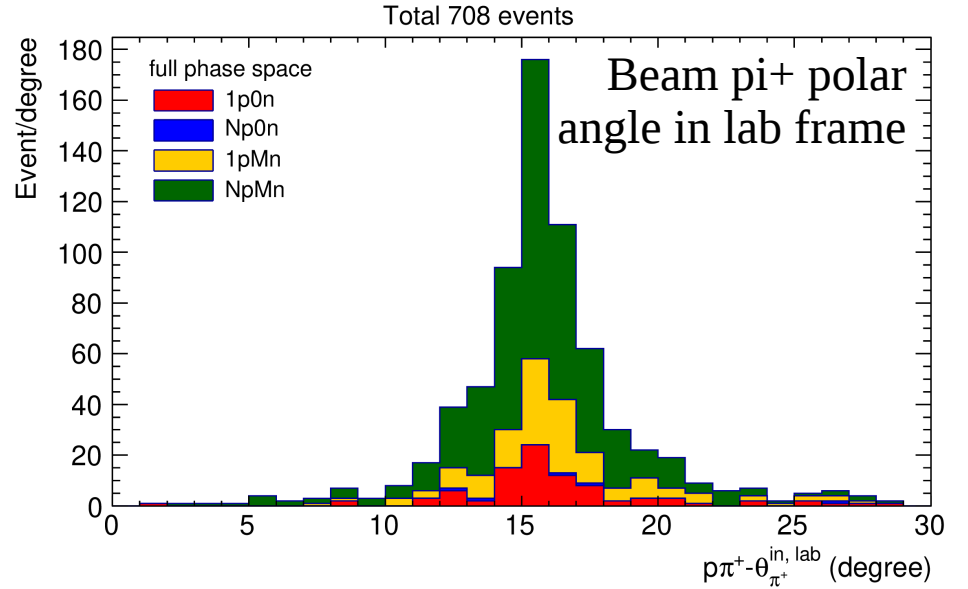
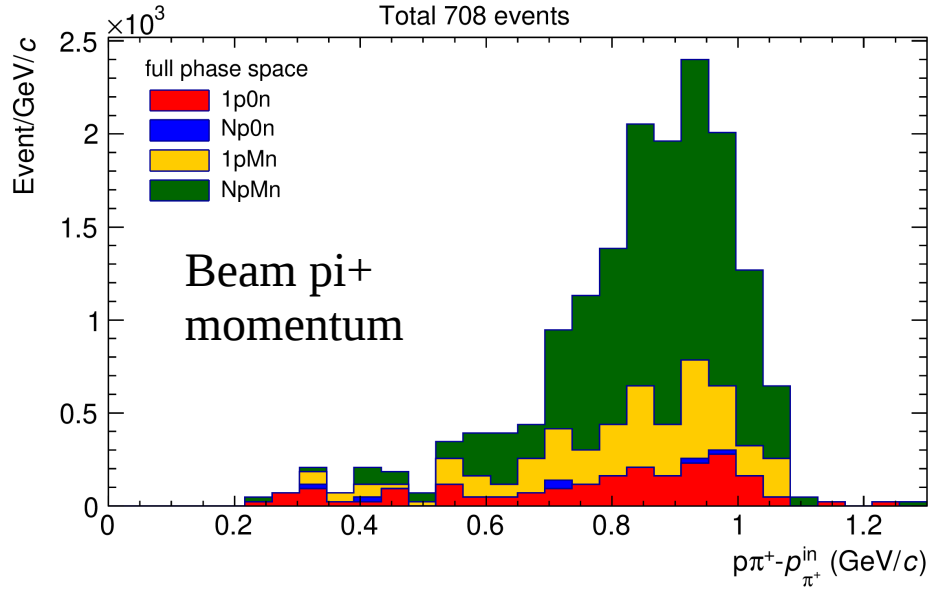
### Exclusive $p\pi^+$ event selection:

- At least 1 proton (leading proton kinematics used in calculation)
  - Exactly 1  $\pi^+$ , no other pions
  - Don't care about neutron, gamma, nucleus
  - Phase space cut (to be added after a few slides)
- 708  $p\pi^+$  events selected  
(708/3263= 22%)



# Selected $p\pi^+$ events

Decomposed into proton-neutron topology  
 $1p0n$  expected to be sensitive to initial state

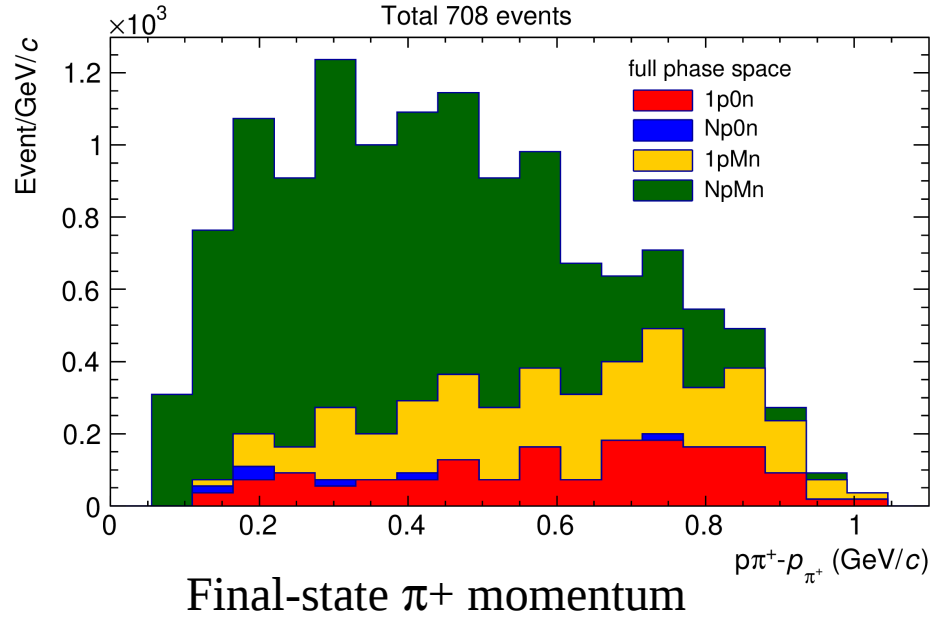


→  $1p0n$  proton angle resembles neutrino QE proton angle distribution

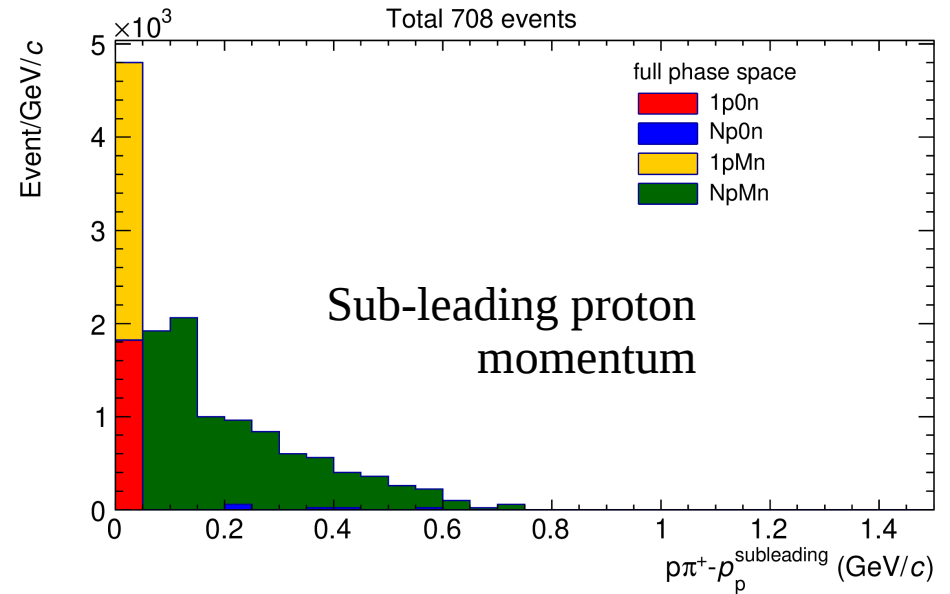
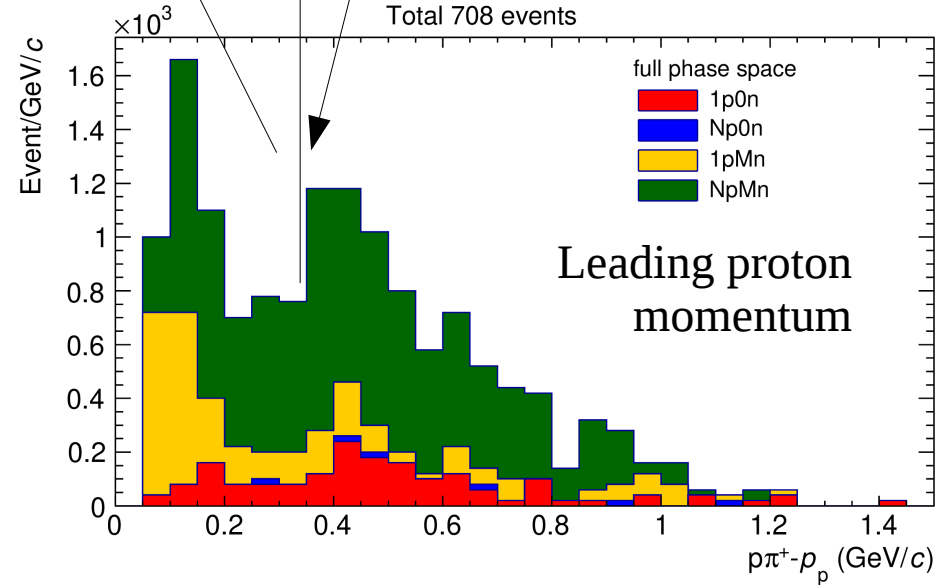
# Selected $p\pi^+$ events

Mis-reconstructed as  $\pi^+$ ?

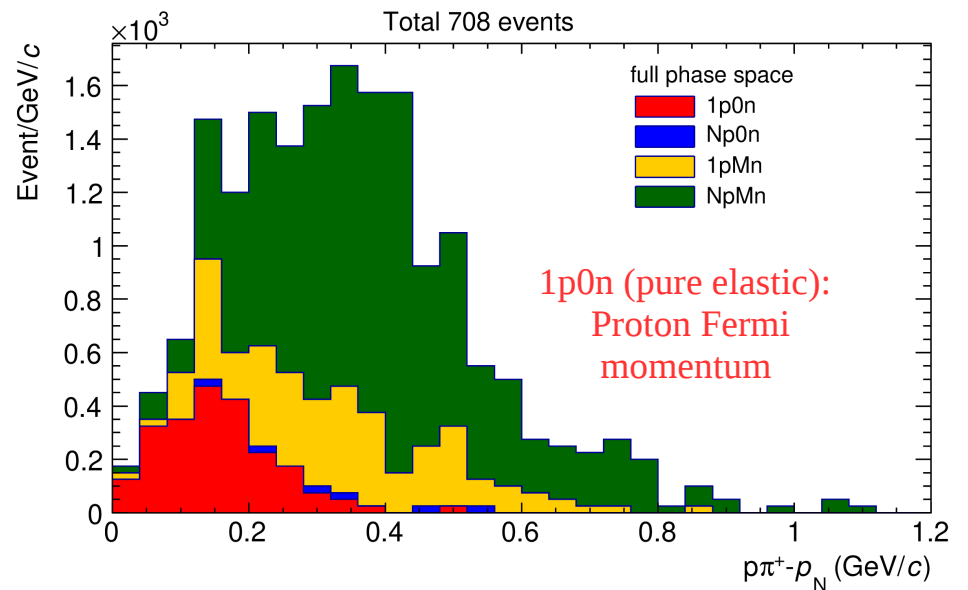
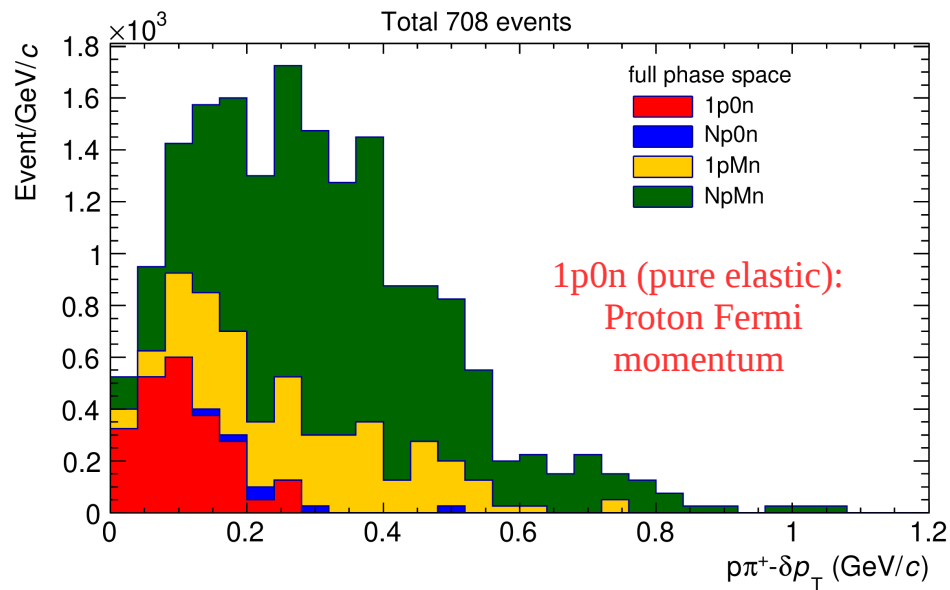
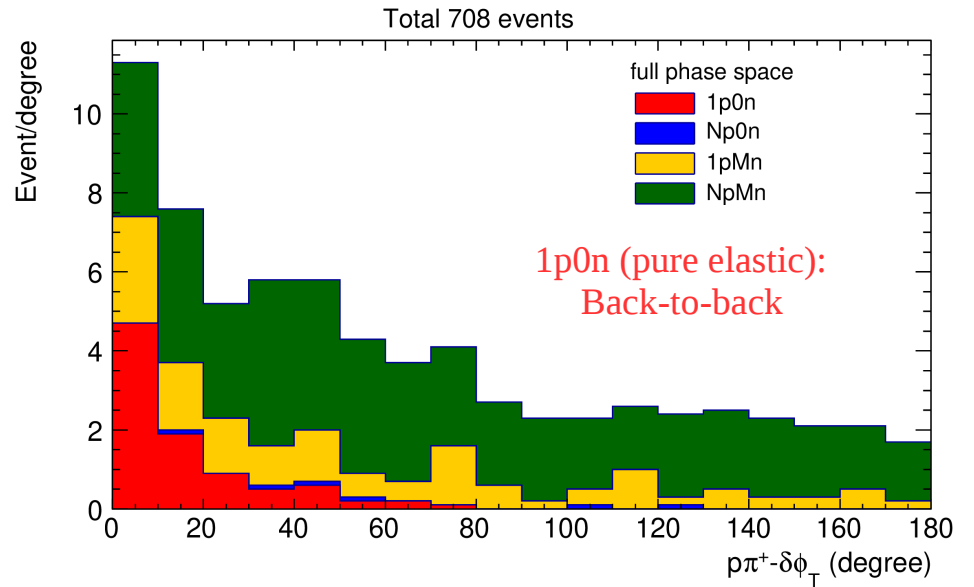
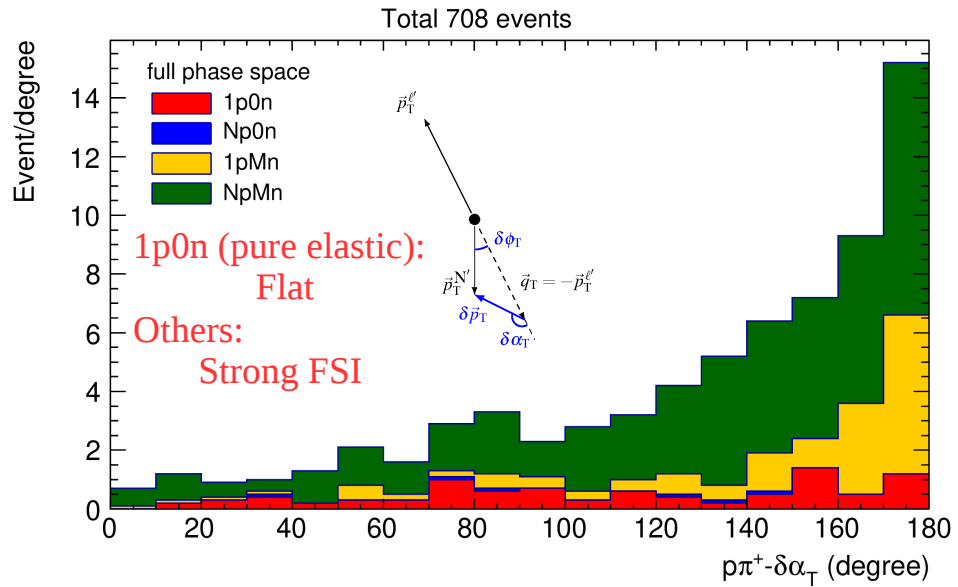
proton reconstruction efficiency onset?



(Recap: all true-level quantities)



# Selected $p\pi^+$ events



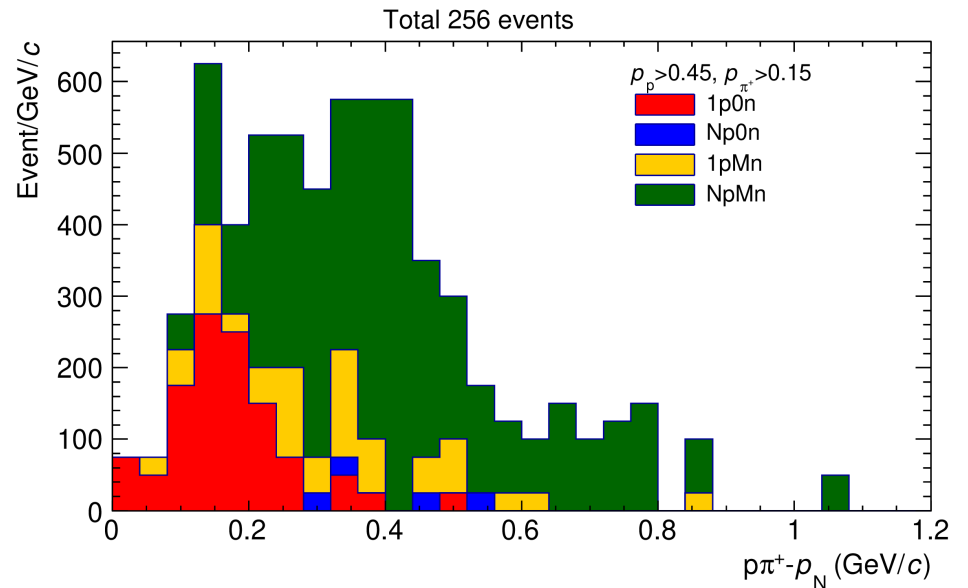
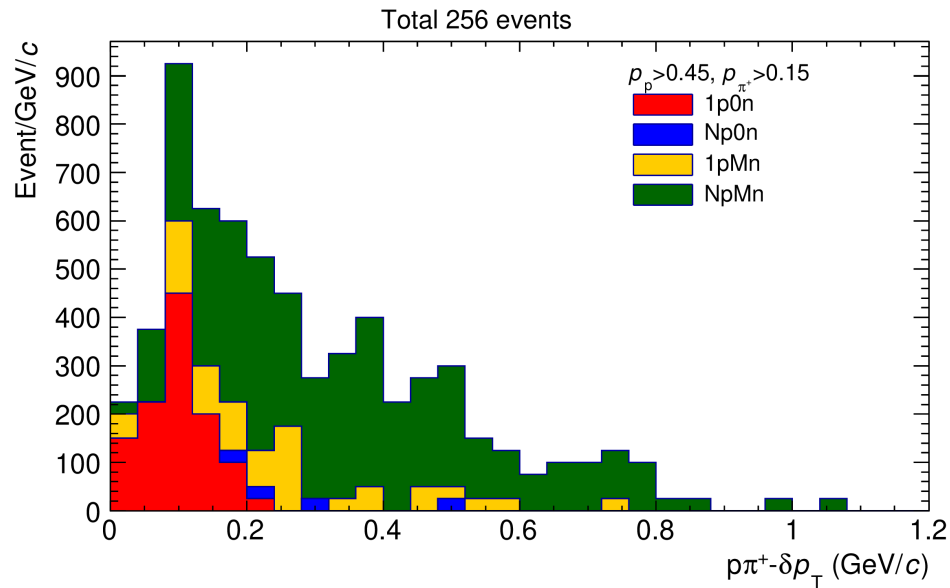
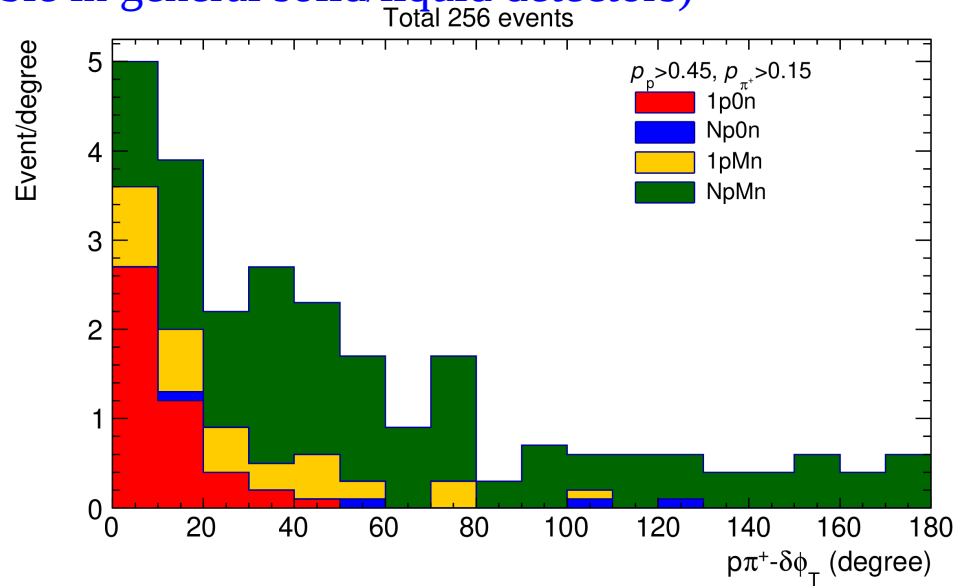
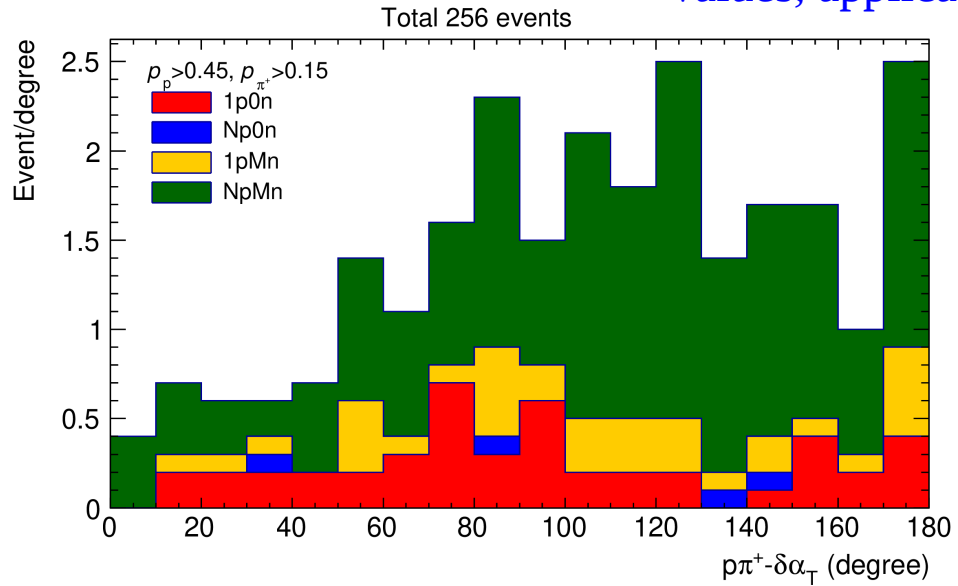
→ Proton Fermi momentum is indeed observed

→ need to reduce Np contributions (strong FSI)

# Selected $p\pi^+$ events

Impose kinetic energy threshold for  $p\pi^+$

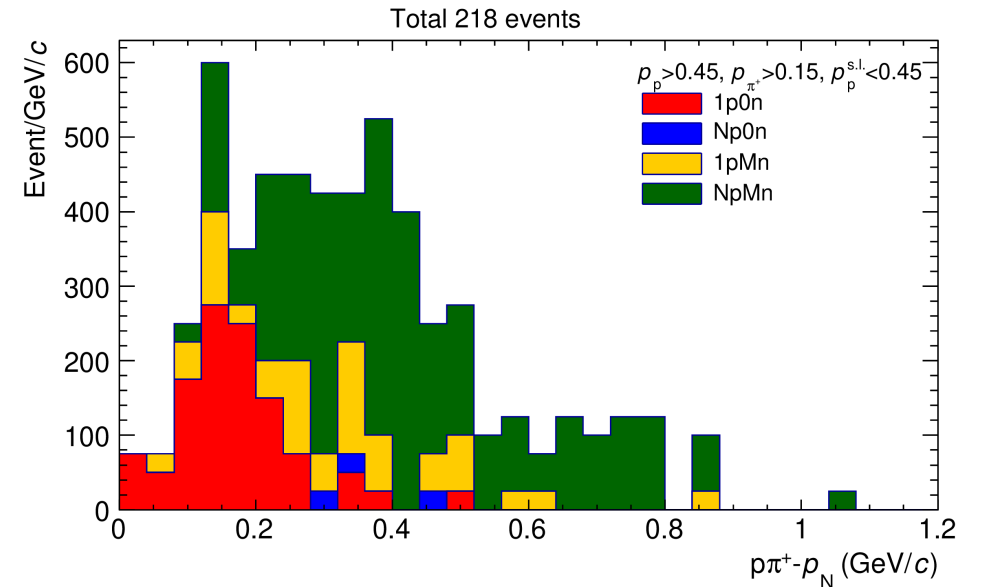
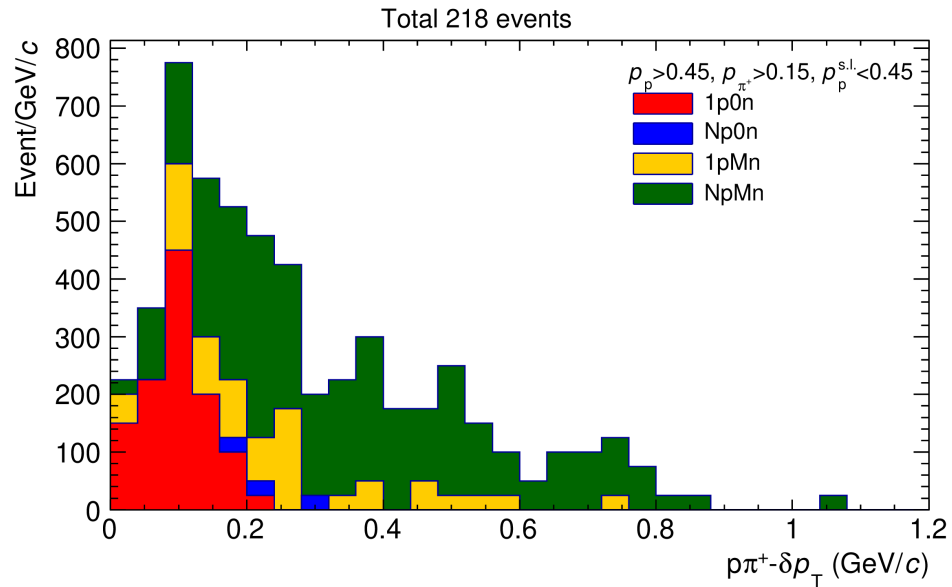
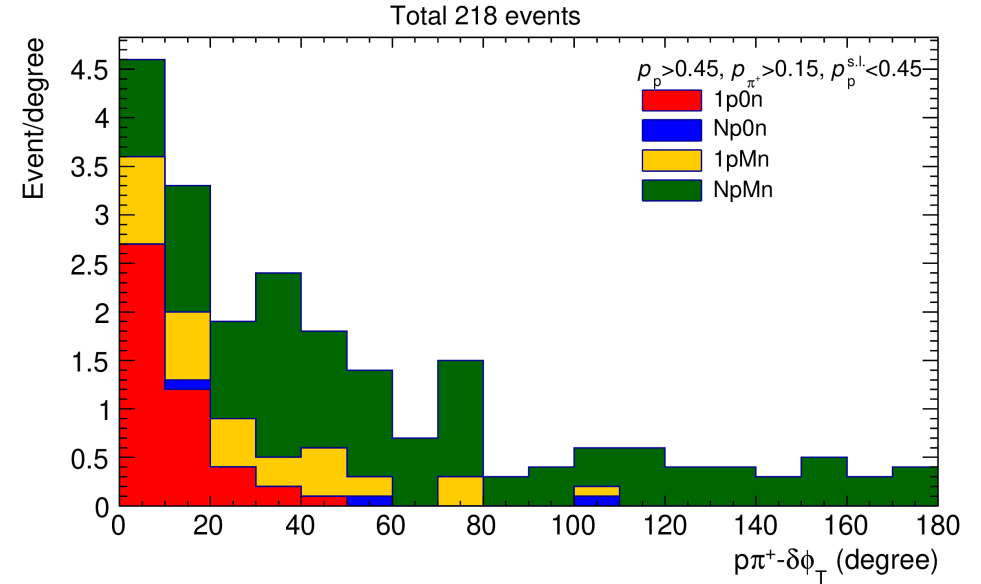
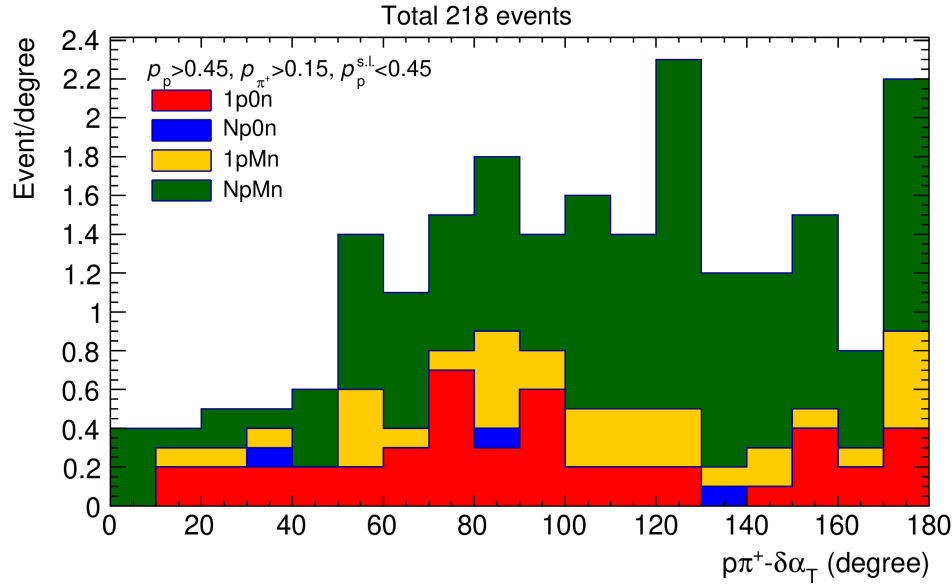
$T_p > \sim 100$  MeV ( $\sim 9$  cm range) and  $T_{\pi^+} > \sim 70$  MeV (MINERvA values, applicable in general solid/liquid detectors)



→ Strong FSI part reduced (below threshold events are most likely mis-reconstruction any way)

# Selected $p\pi^+$ events

- Impose kinetic energy threshold for  $p\pi^+$
- require exactly 1 proton above threshold (=remove events with subleading proton above threshold)

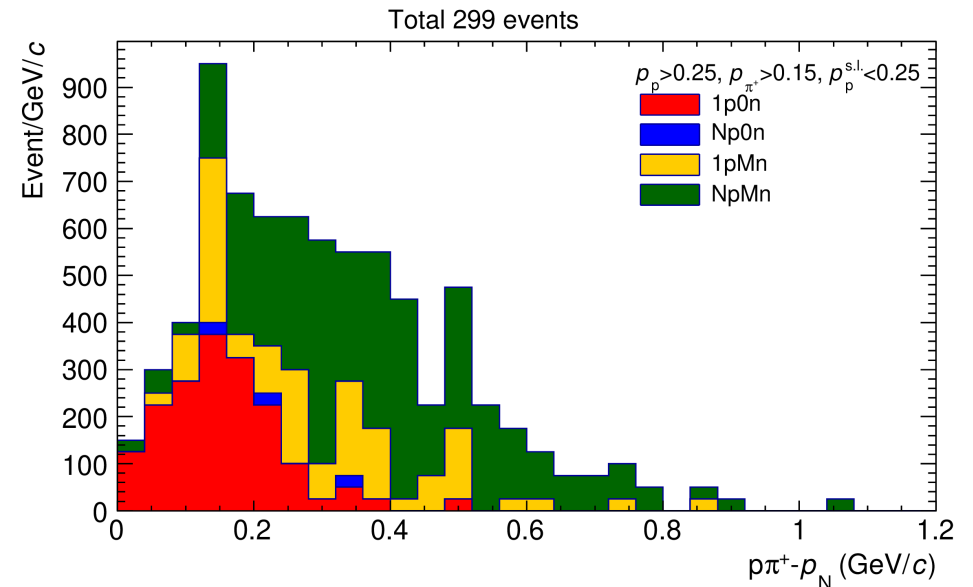
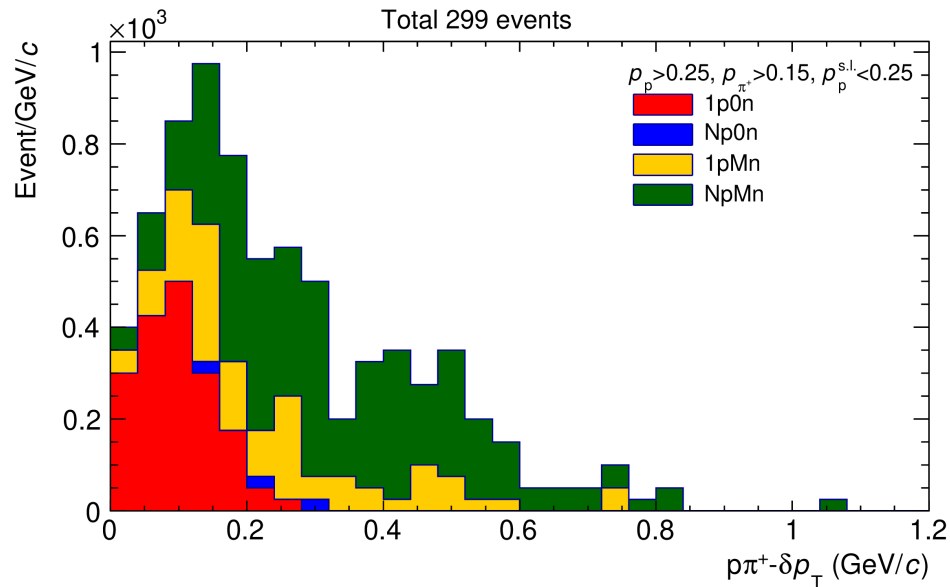
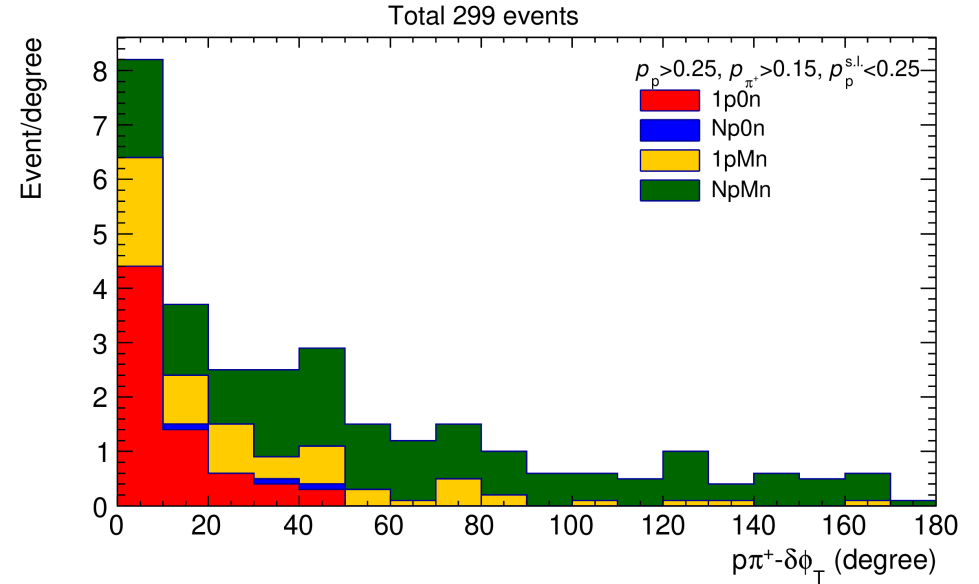
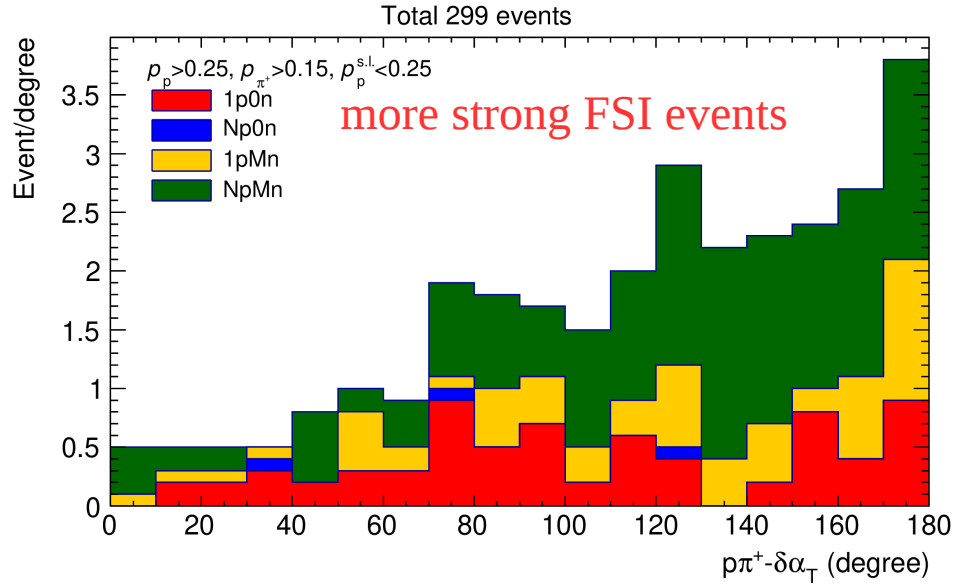


→ Further clean-up. Total 218 events.  
 (218 phase-space cut exclusive events / 3263  $\pi^+$  beam events = 6.7%)



# Selected $p\pi^+$ events

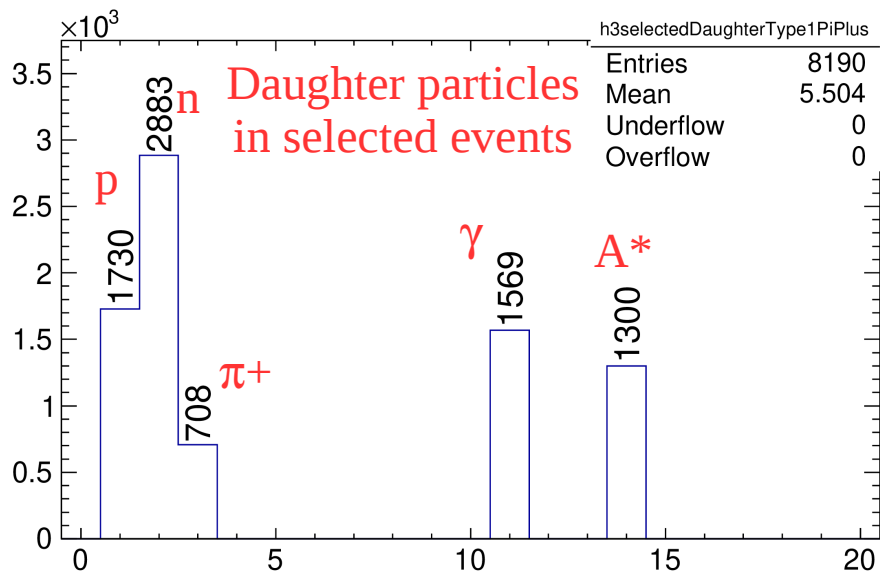
Alternative **hypothetical** proton threshold  
 $T > 33$  MeV (1cm proton range)



→ Lower threshold accepts more strong FSI events.  
 (299 hypothetical phase-space cut exclusive events / 3263  $\pi^+$  beam events = 9.1%)



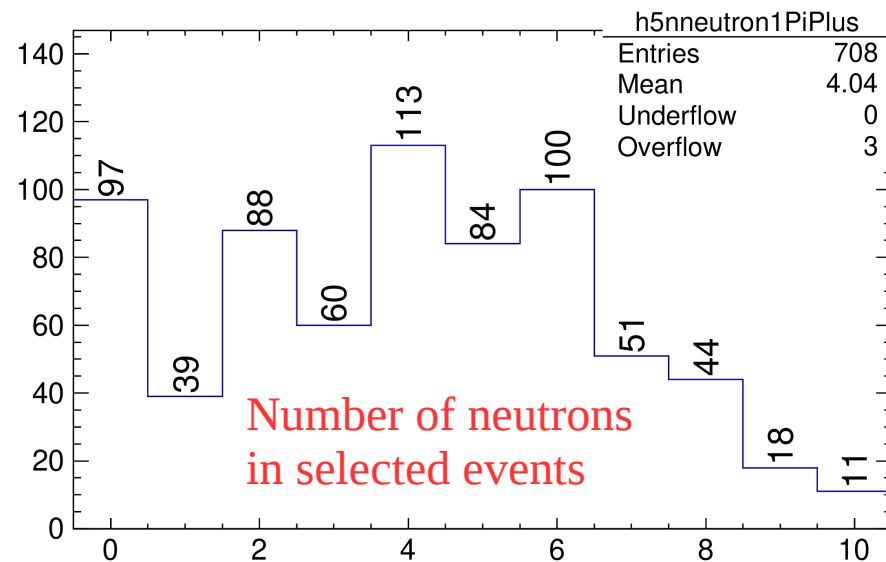
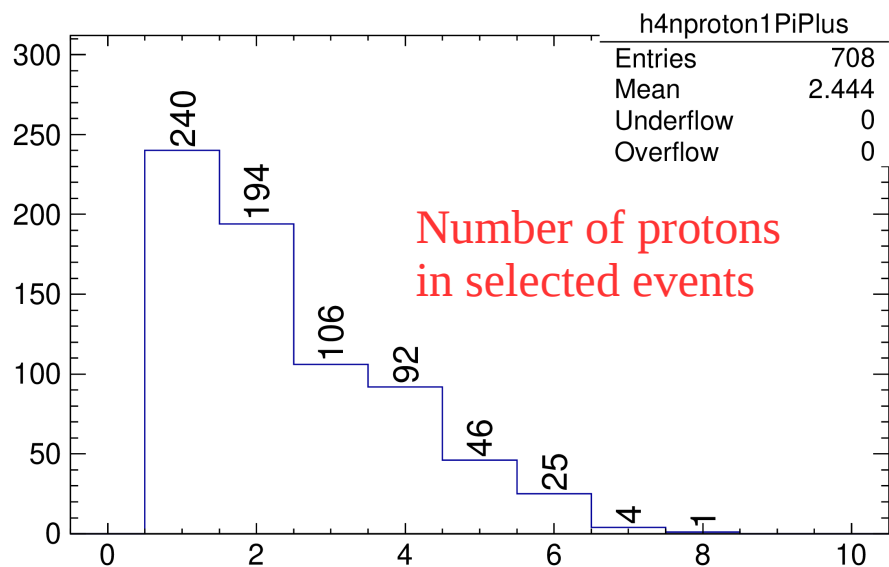
# Recap

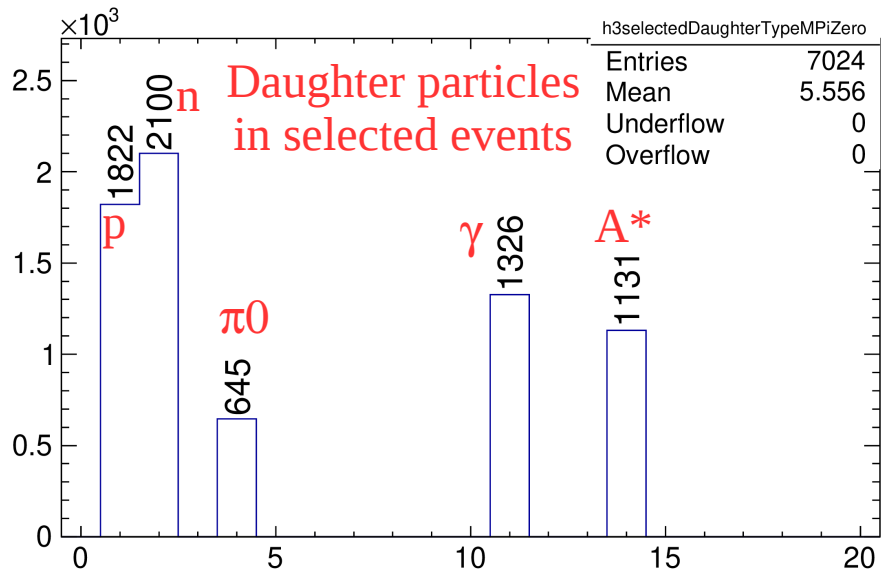


Exclusive  $p\pi^+$  event selection:

- At least 1 proton (leading proton kinematics used in calculation)
- Exactly 1  $\pi^+$ , no other pions
- Don't care about neutron, gamma, nucleus
- Phase space cut (to be added after a few slides)

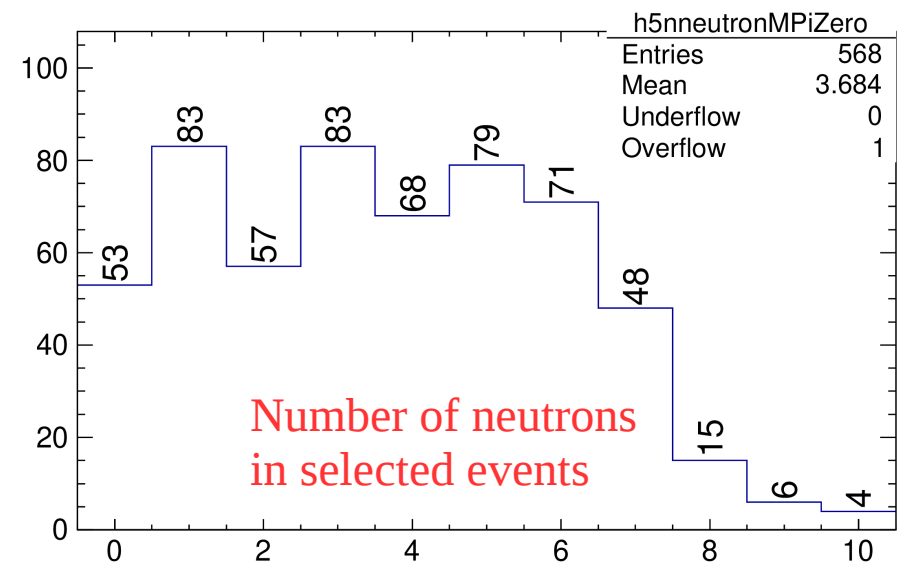
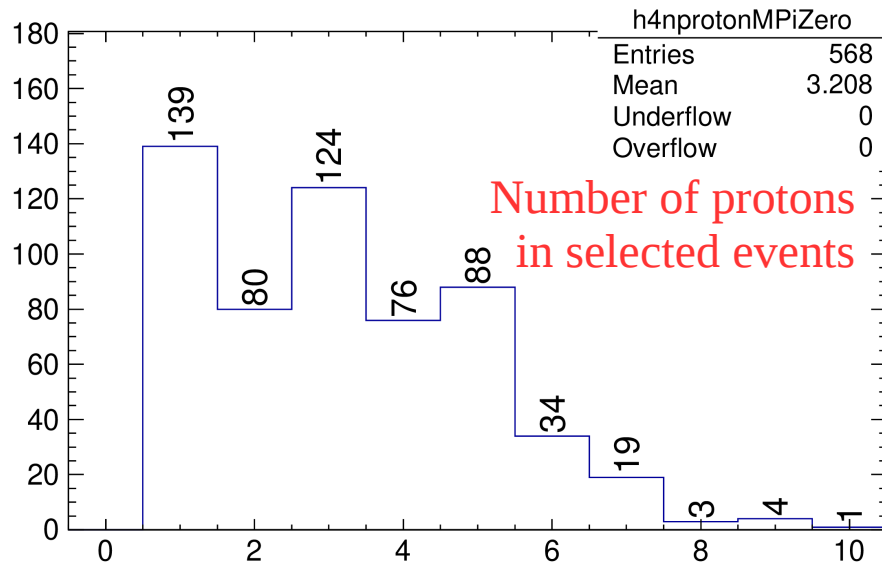
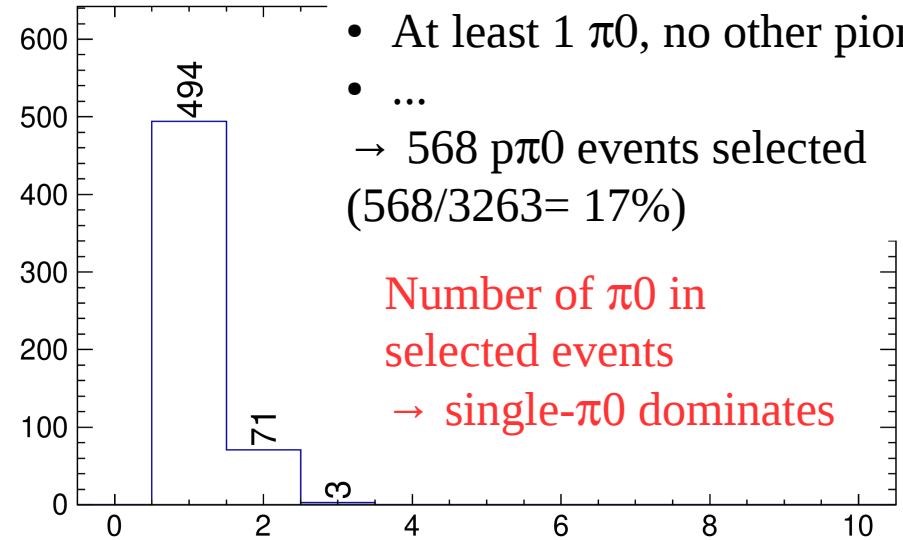
→ 708  $p\pi^+$  events selected  
(708/3263= 22%)





Exclusive  $p\pi^0$  event selection:

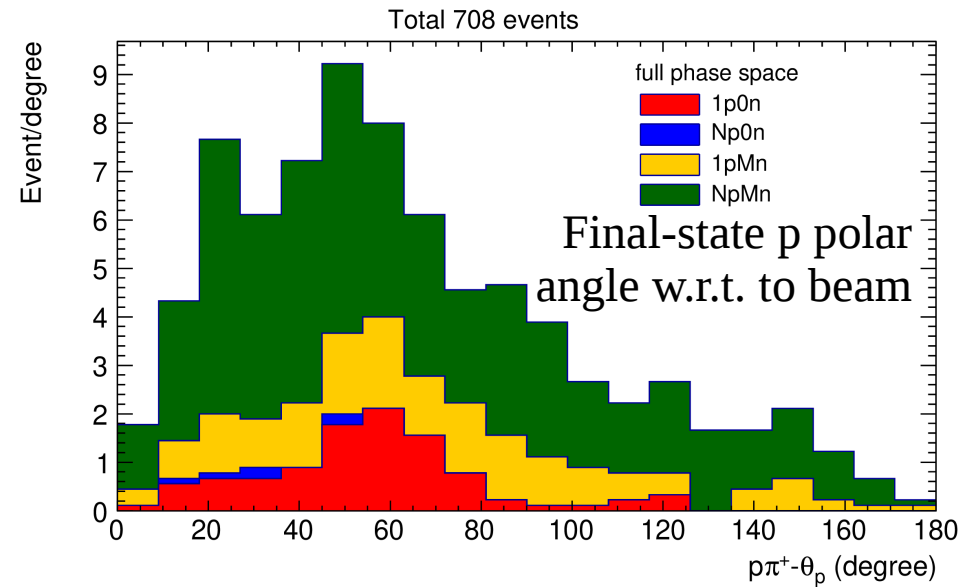
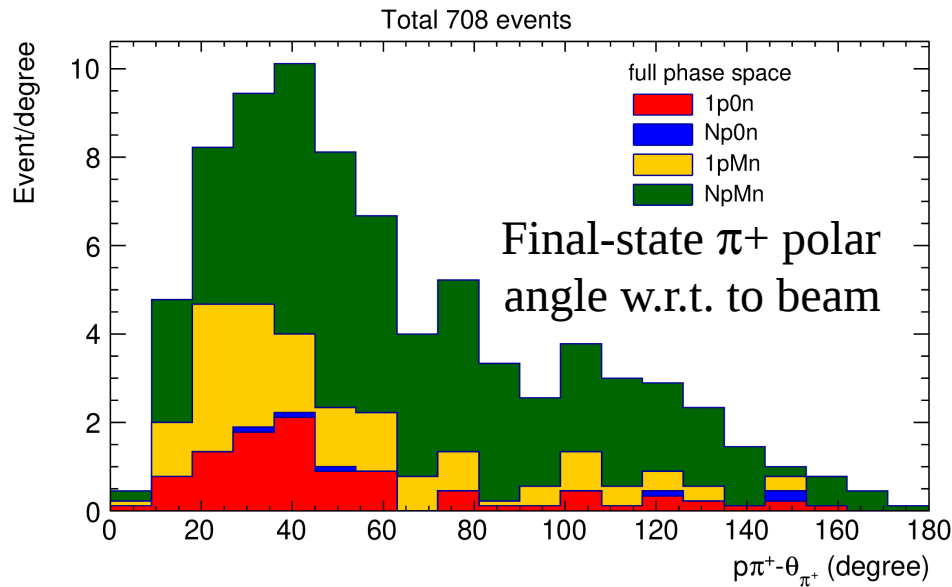
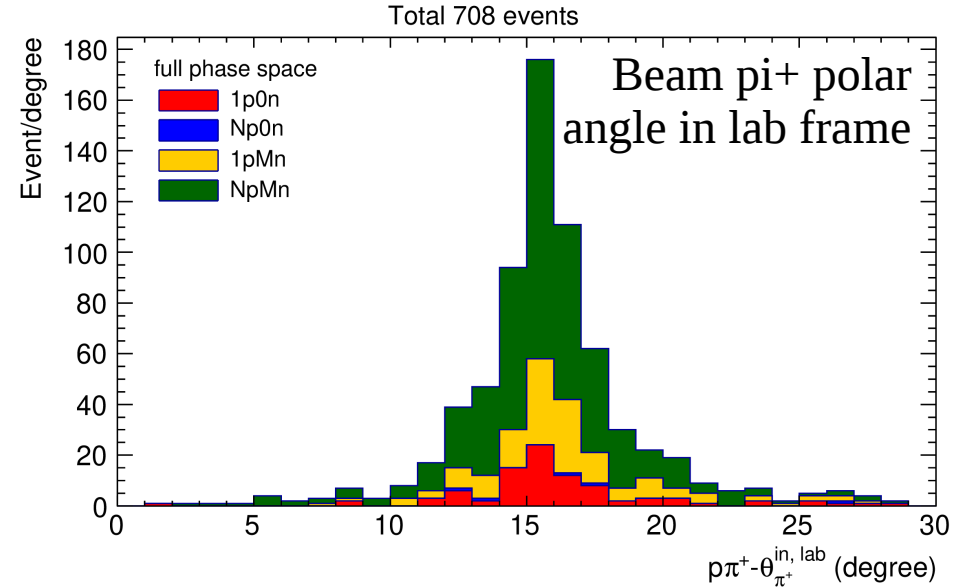
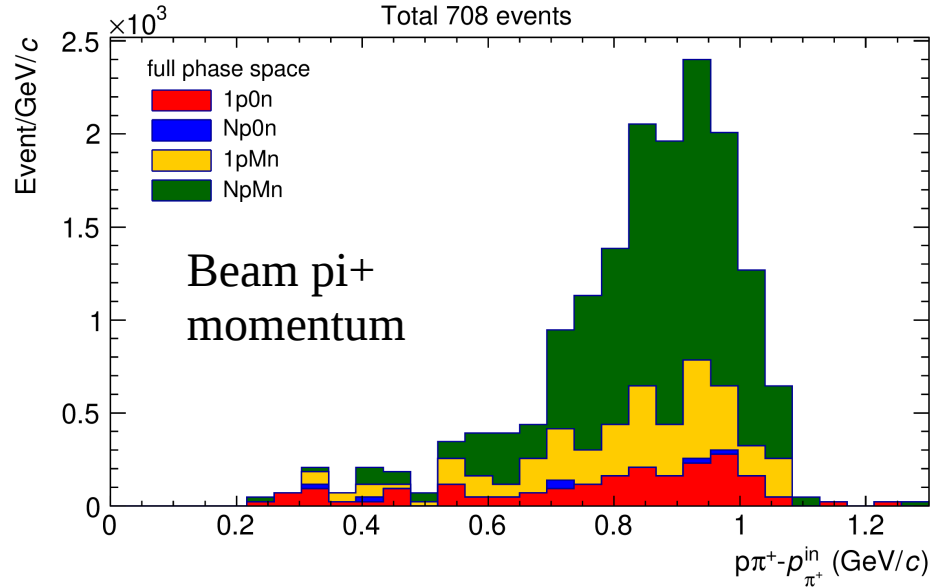
- ...
  - At least 1  $\pi^0$ , no other pions
  - ...
- 568  $p\pi^0$  events selected (568/3263= 17%)



# Selected $p\pi^+$ events

Decomposed into proton-neutron topology  
 $1p0n$  expected to be sensitive to initial state

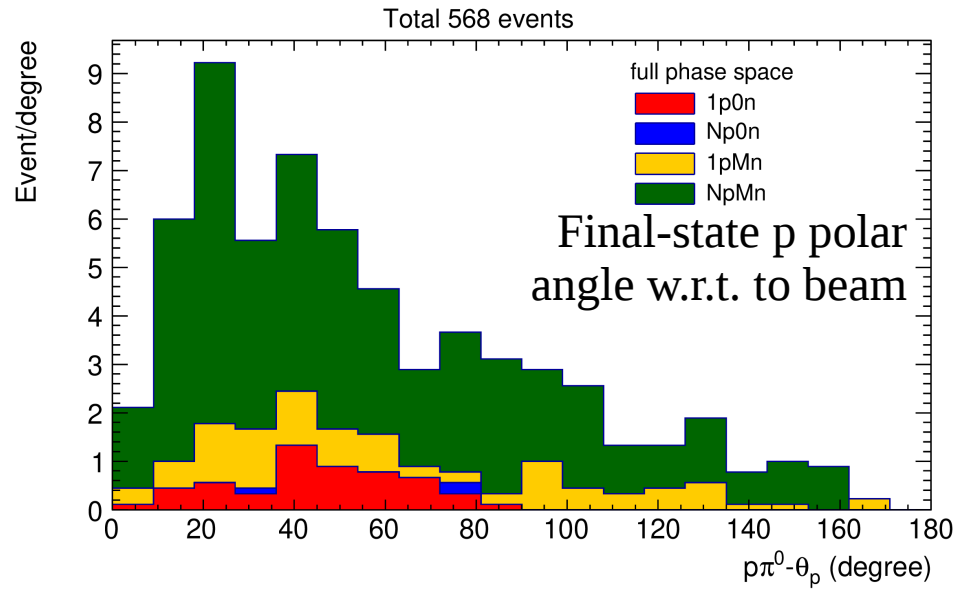
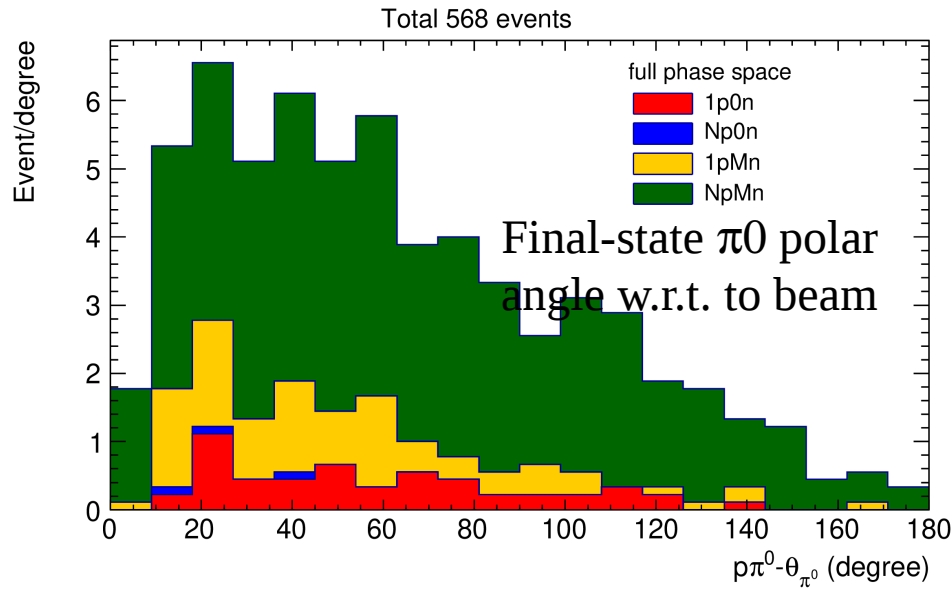
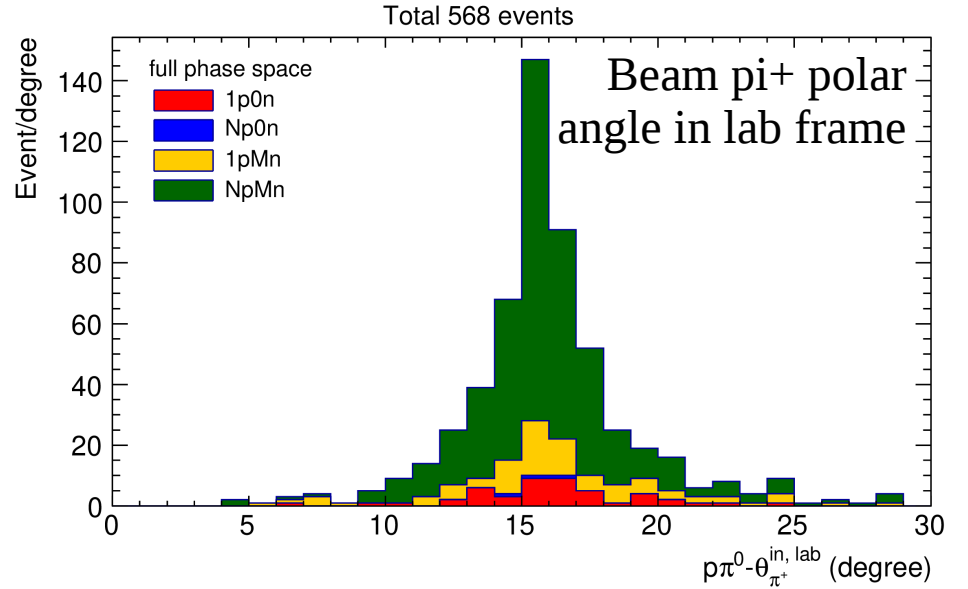
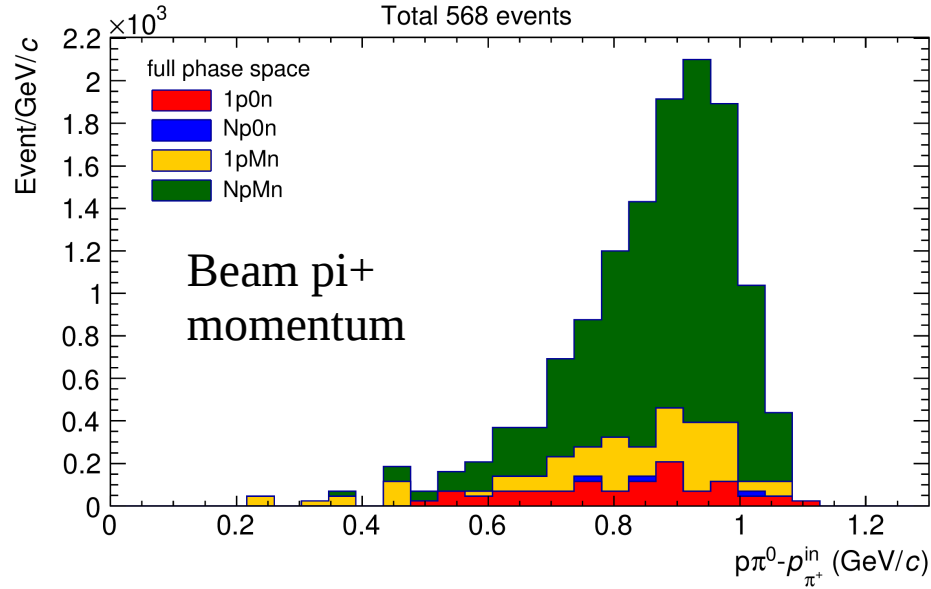
Recap



→  $1p0n$  proton angle resembles neutrino QE proton angle distribution

# Selected $p\pi^0$ events

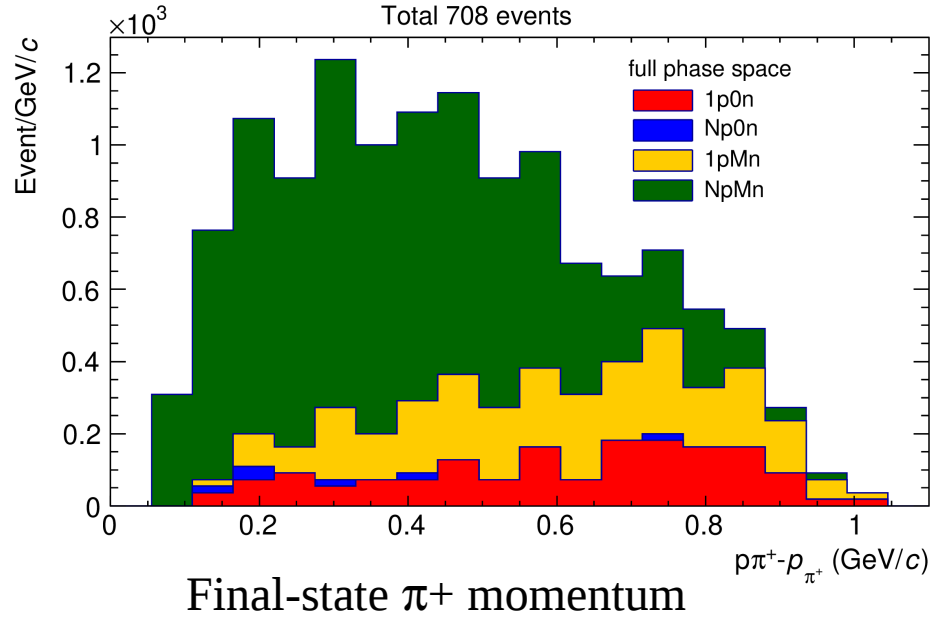
Decomposed into proton-neutron topology  
 $1p0n$  expected to be sensitive to initial state



# Selected $p\pi^+$ events

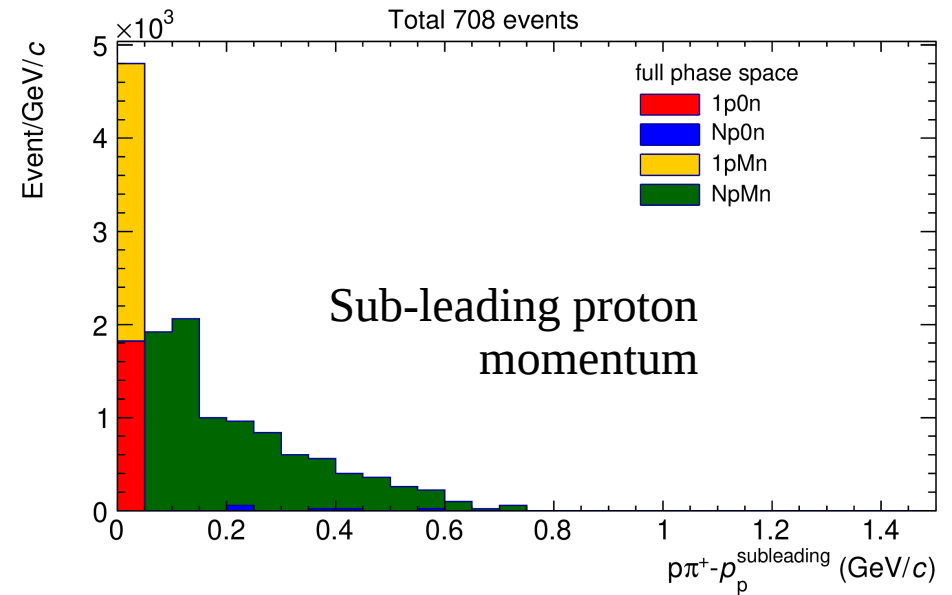
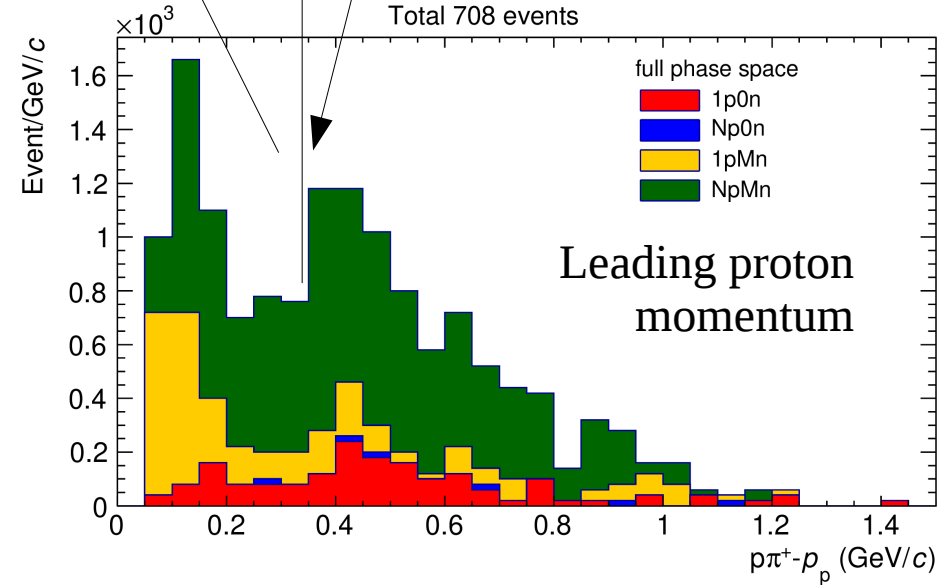
Mis-reconstructed as  $\pi^+$ ?

proton reconstruction efficiency onset?



(Recap: all true-level quantities)

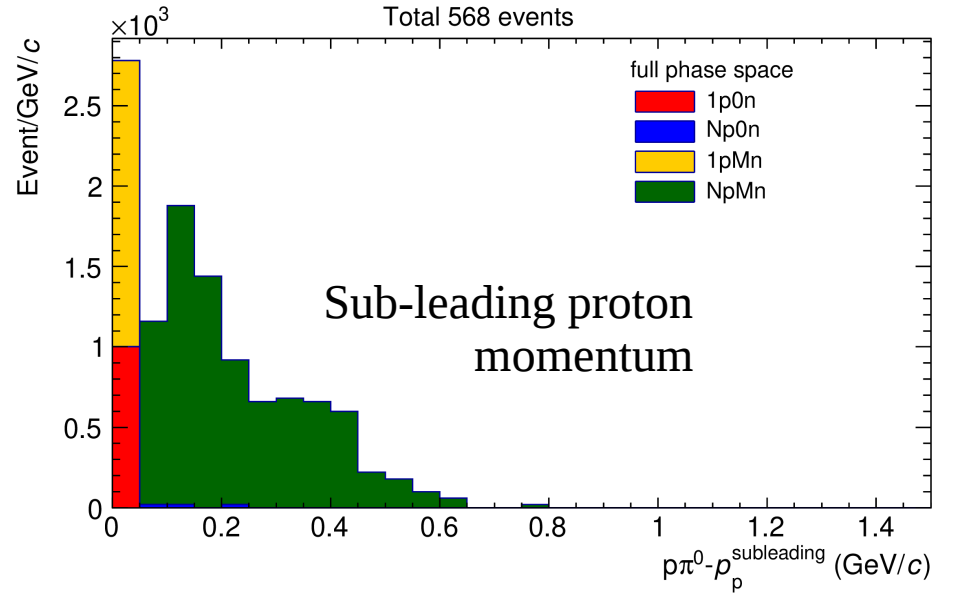
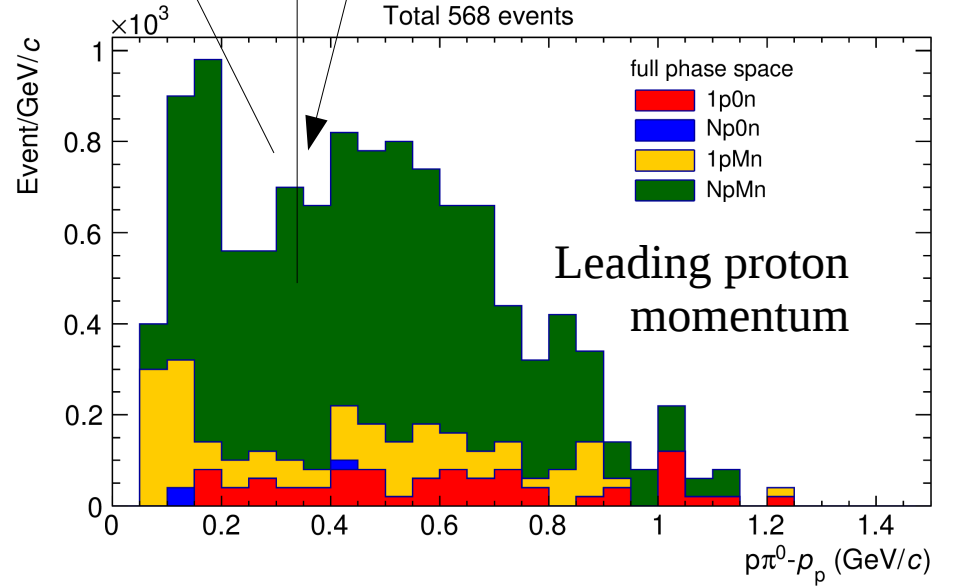
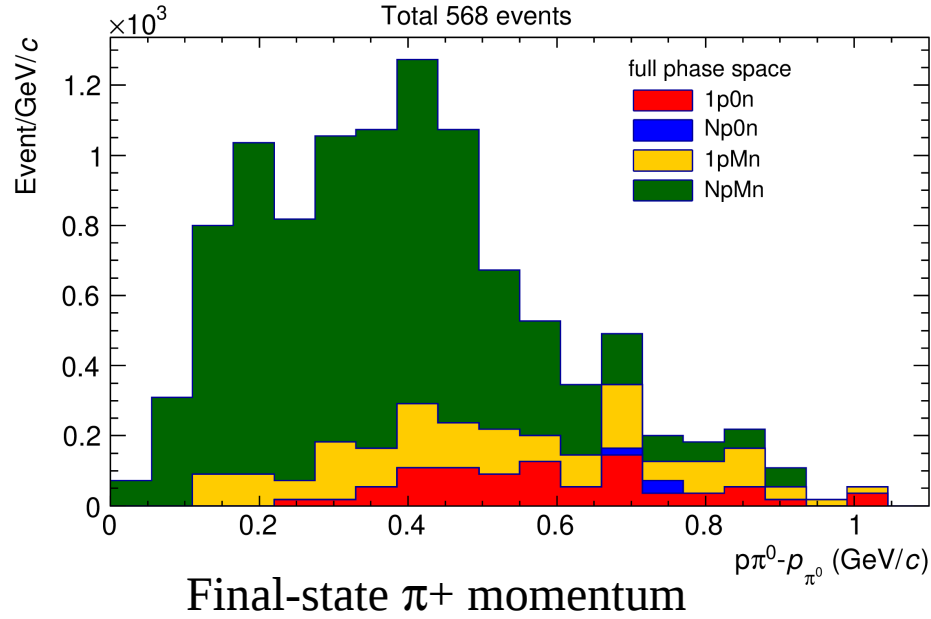
**Recap**



# Selected $p\pi^0$ events

Mis-reconstructed as  $\pi^+$ ?  
(no true  $\pi^+$ , but still reco  $\pi^+$ ?)

proton reconstruction  
efficiency onset?

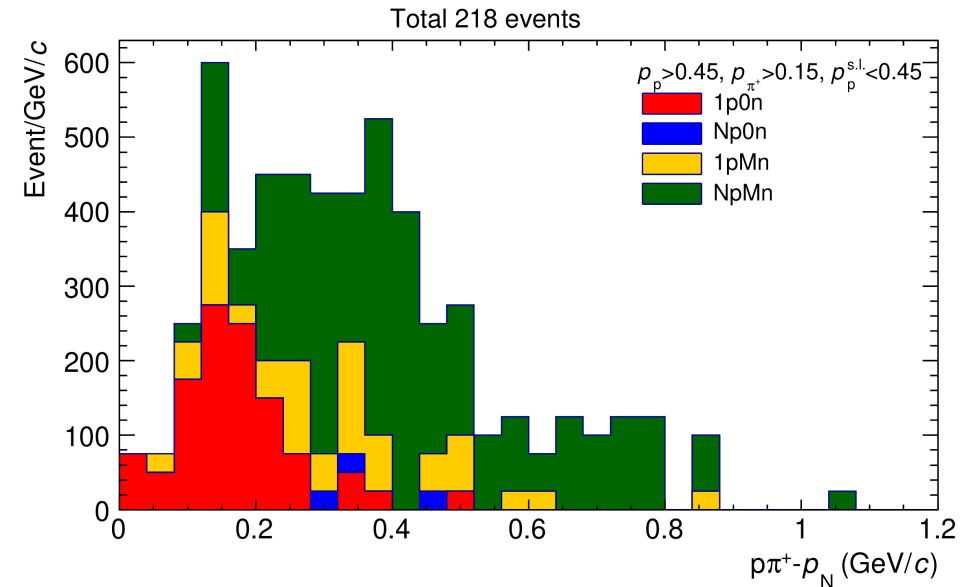
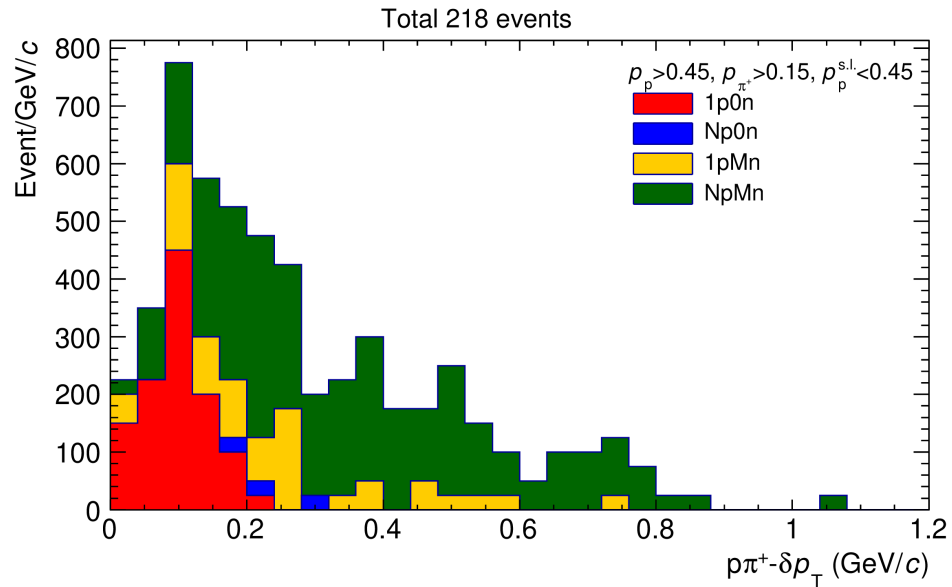
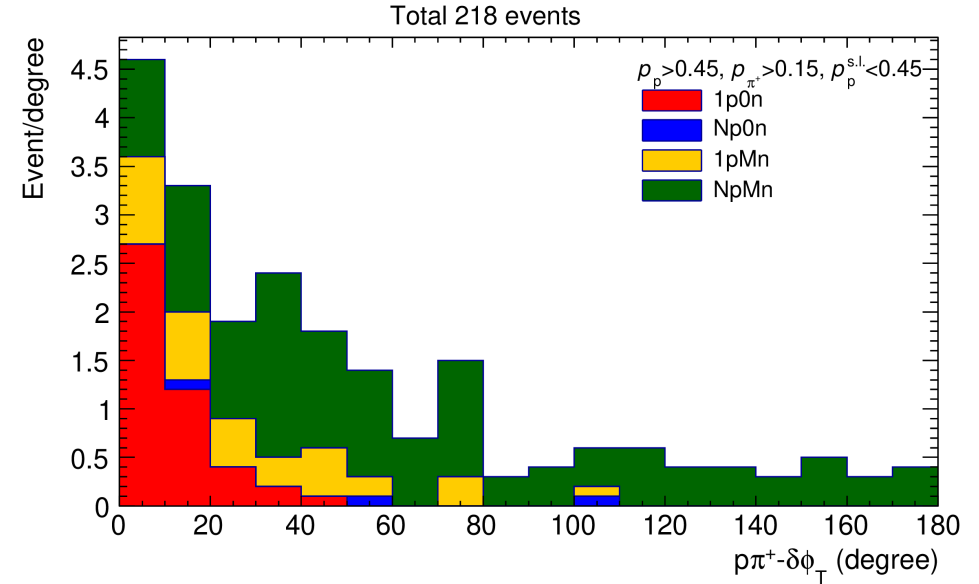
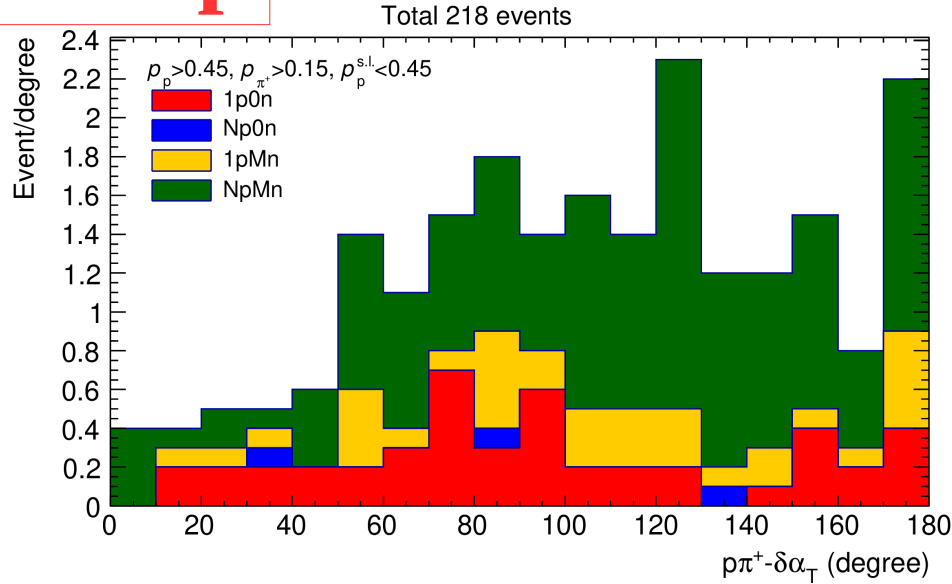




# Selected $p\pi^+$ events

## Recap

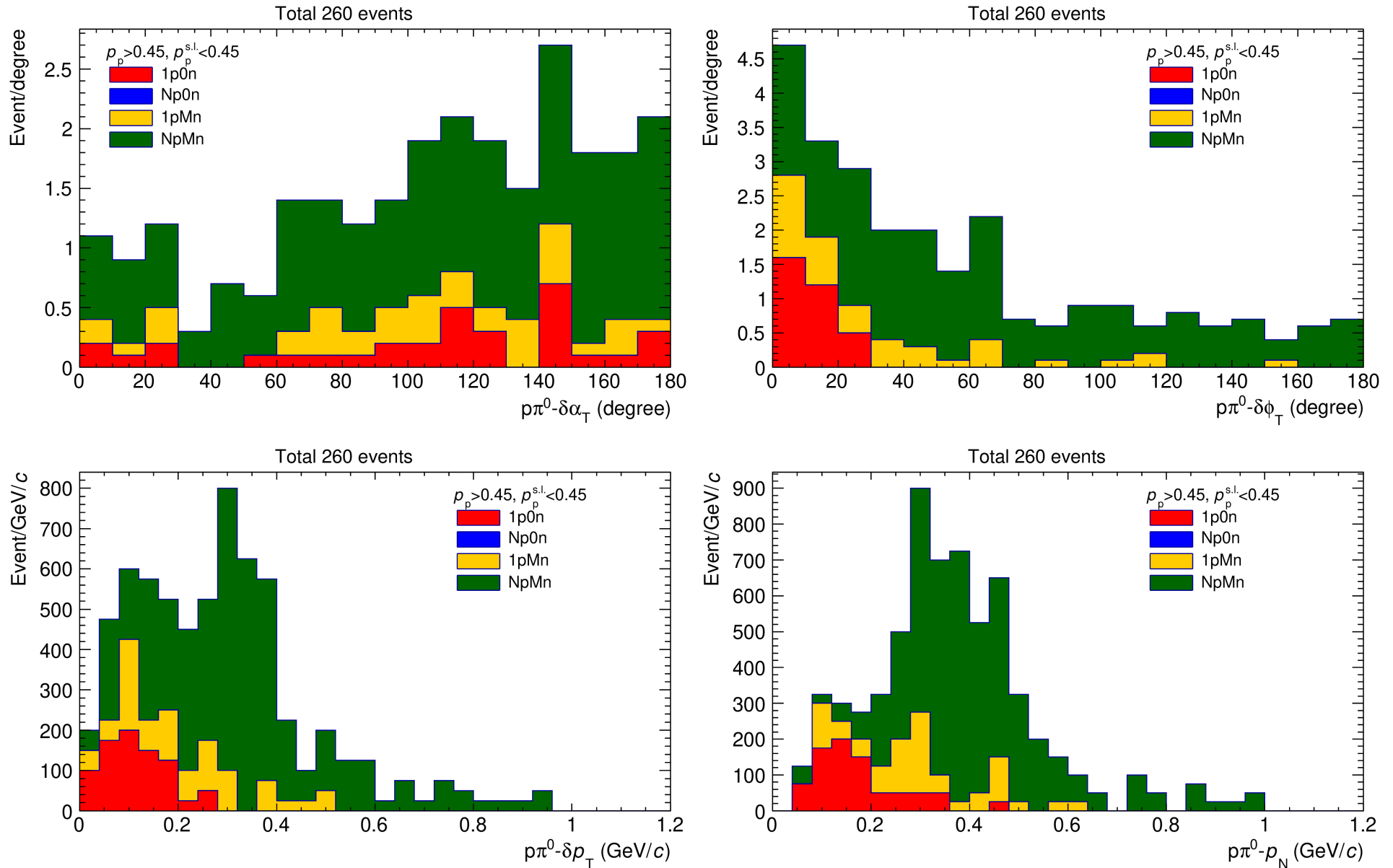
- Impose kinetic energy threshold for  $p\pi^+$
- require exactly 1 proton above threshold (=remove events with subleading proton above threshold)



→ Further clean-up. Total 218 events.  
(218 phase-space cut exclusive events / 3263  $\pi^+$  beam events = 6.7%)

# Selected $p\pi^0$ events

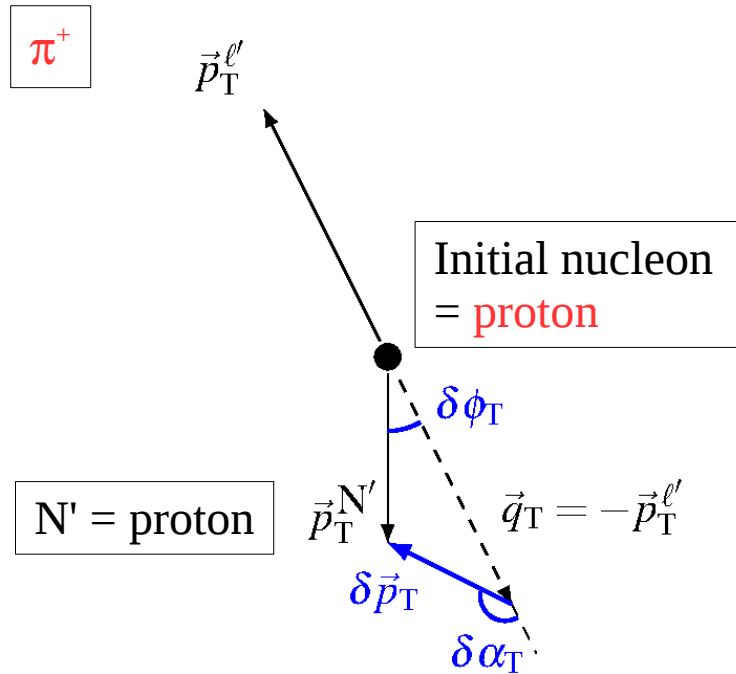
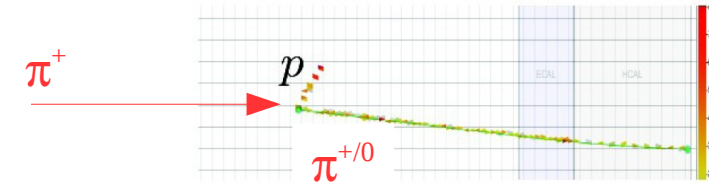
- Impose kinetic energy threshold for p ONLY (100MeV K.E.)
- require exactly 1 proton above threshold (=remove events with subleading proton above threshold)



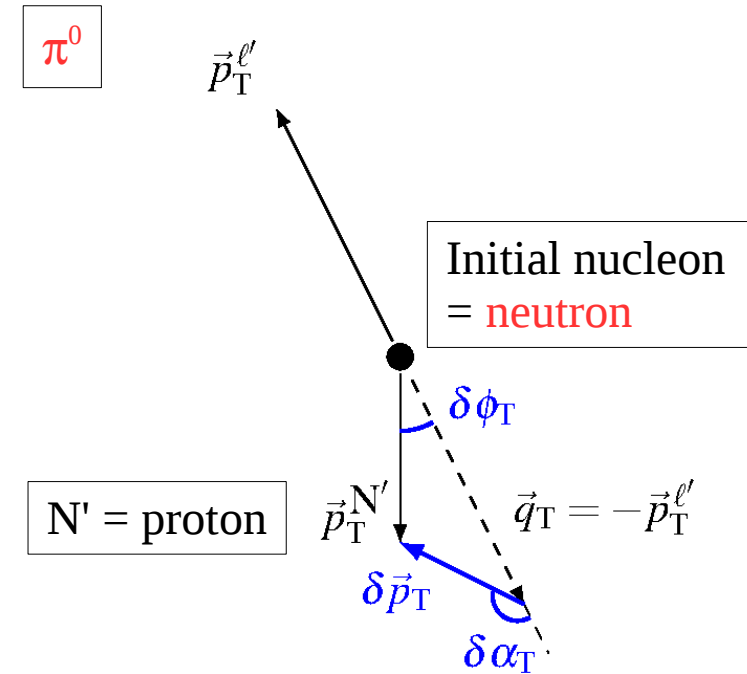
→ Neutron Fermi momentum is indeed observed  
 (260 phase-space cut exclusive events / 3263  $\pi^+$  beam events = 8.0%)

# TKI + protoDUNE

– *Proton/Neutron* initial-state kinematics



- **Proton** Fermi motion observed
- 218 phase-space cut exclusive events / 3263 pi+ beam events = **6.7%**



- **Neutron** Fermi motion observed
- 260 phase-space cut exclusive events / 3263 pi+ beam events = **8.0%**

# Summary and discussions

1. TKI + protoDUNE → argon intranuclear dynamics: Fermi motion + FSI
  - No need to know the beam particle momentum, just need direction
    - Because the beam momentum (right before interaction) can be measured, we can trade one final-state momentum magnitude as follows:
      - Compare the momentum resolution of the incoming and outgoing particles
      - For the one with the worst resolution, don't require its momentum magnitude, just measuring the direction is enough
    - This opens up other possibilities: neutron final-state, need direction only
  - Argon 18 protons, 22 neutrons: Fermi motion might be different
  - $p\pi^0$  channel is in fact charge exchange channel we've been talking about
2. Even though true variables used, doesn't seem to be true/theoretical shape due to reconstruction efficiency (cf. Final-state proton momentum spectra).
3. How many events do we expect in full data set?
4. How is proton and  $\pi^0$  reconstruction? Can be used?
5. Currently using tracking threshold to reject N-proton events. Need to optimize because non-trackable activities with much lower energy can also be rejected.
6. Would be very interesting to parallelize both measurements
  - elastic  $p\pi^+$  to probe proton in argon
  - charge-exchange  $p\pi^0$  to probe neutron in argon
7. More interesting to compare to (near-future) neutrino results on argon from, e.g. MicroBooNE.

# BACKUP

END