

# Top Mass at Electron-Positron Colliders

Esteban Fullana Torregrossa, IFIC & Frank Simon, MPP Munich

Snowmass21 EF03 Kick-off Meeting, May 2020



MAX-PLANCK-INSTITUT  
FÜR PHYSIK

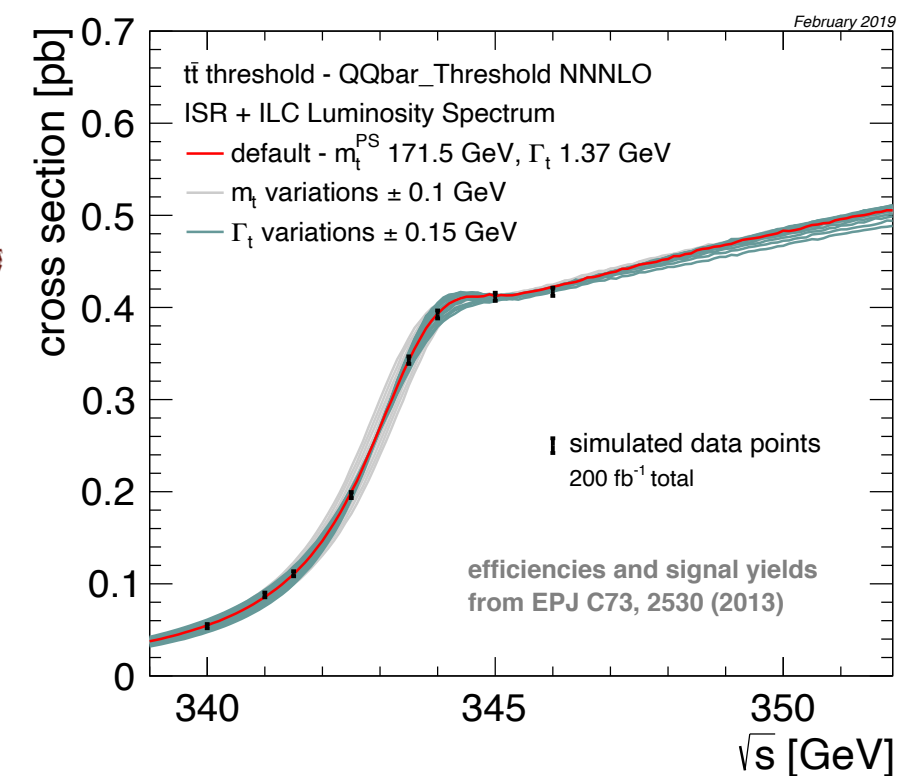
# Top Mass Measurements in $e^+e^-$ Colliders

## Overview

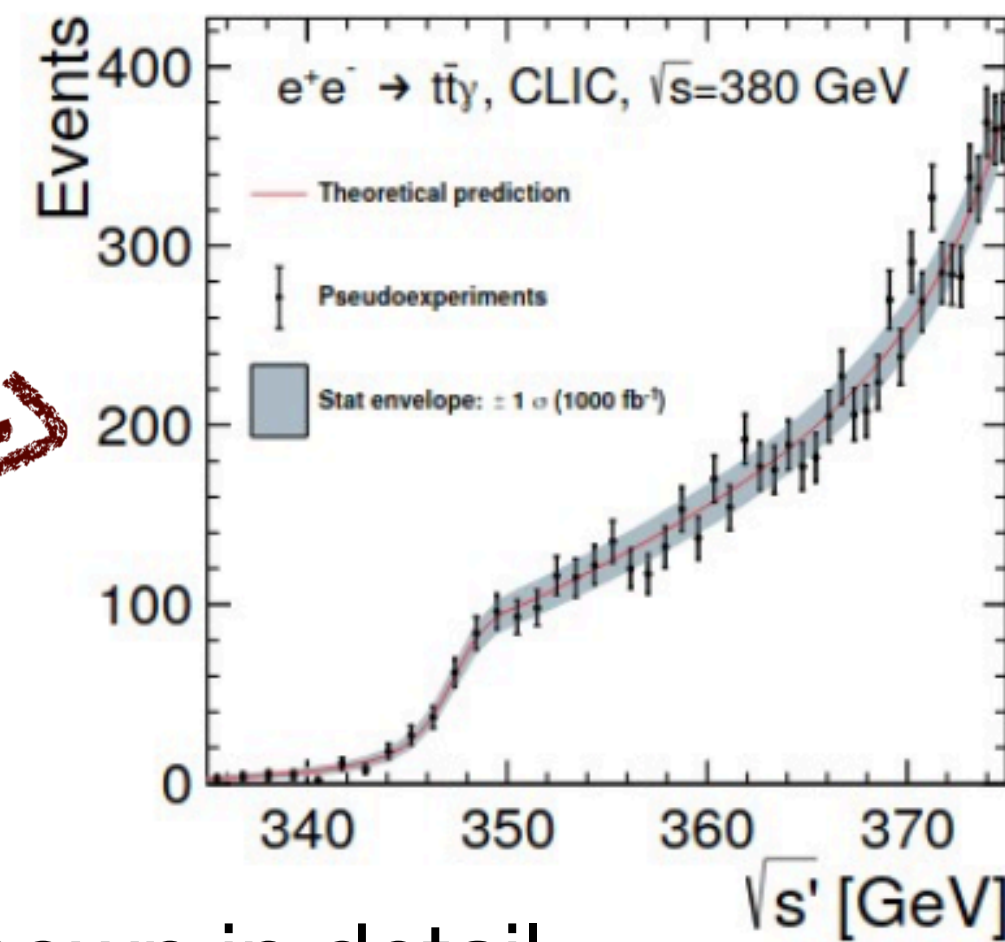
- The accelerator side: Requires sufficient collision energy for top pair production
  - So far thoroughly studied for ILC, CLIC, some derivative studies for FCCee

Three approaches to the top mass

The threshold scan around 350 GeV

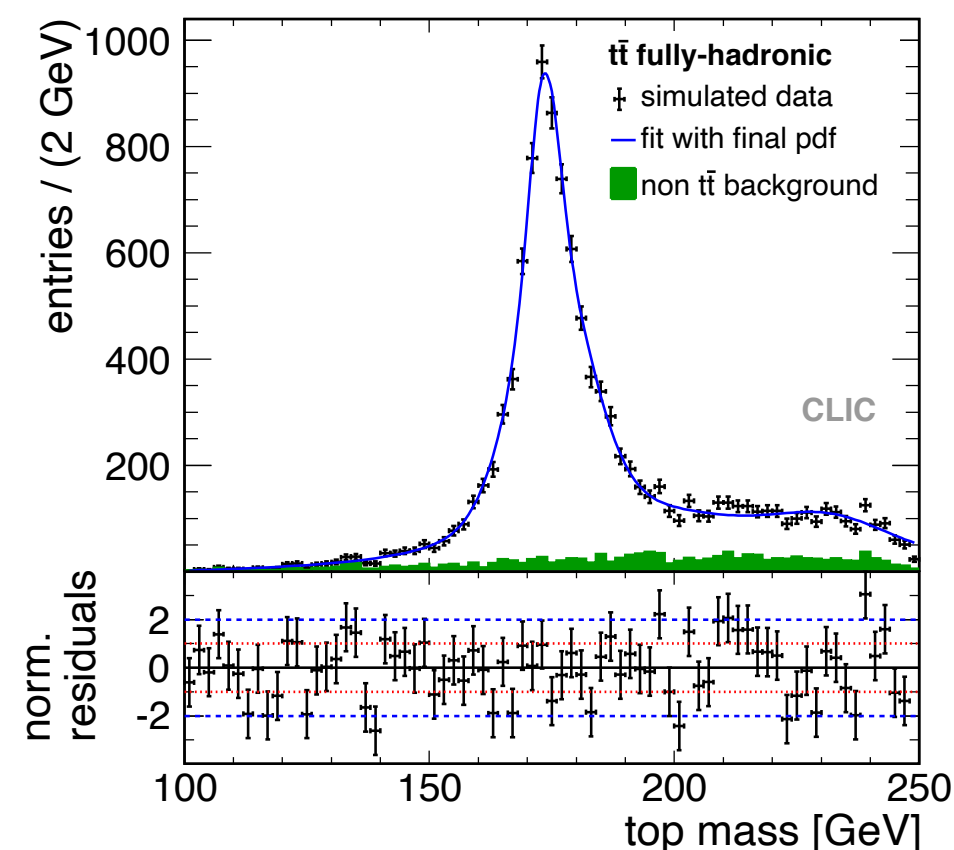


The top mass from radiative events



not shown in detail,  
stat: ~ 20 - 40 MeV

Direct kinematic reconstruction



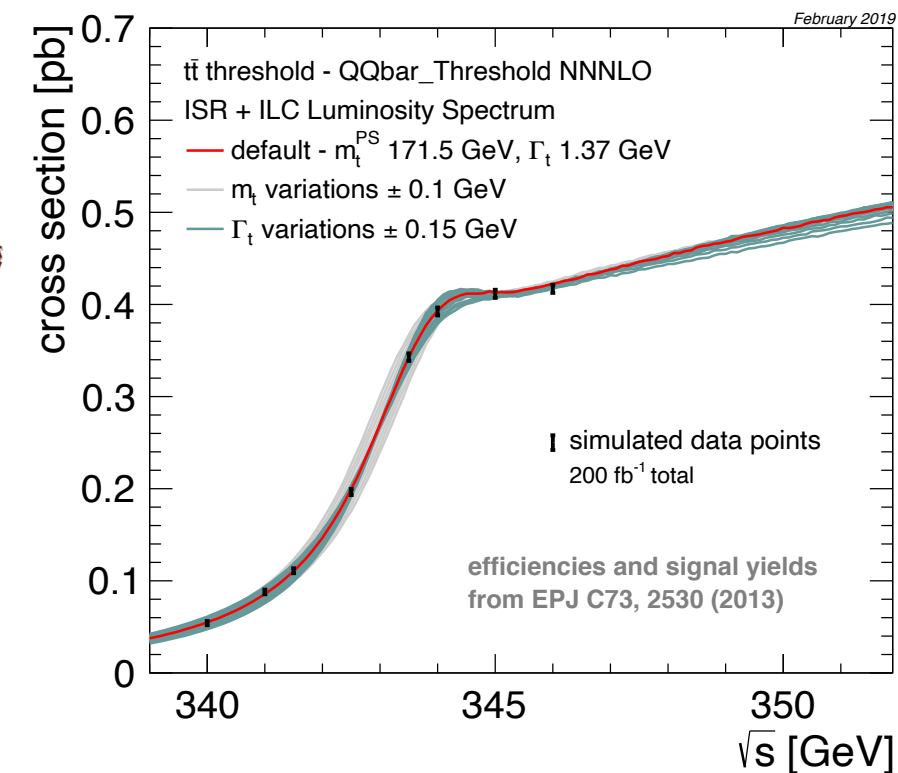
# Top Mass Measurements in $e^+e^-$ Colliders

## Overview

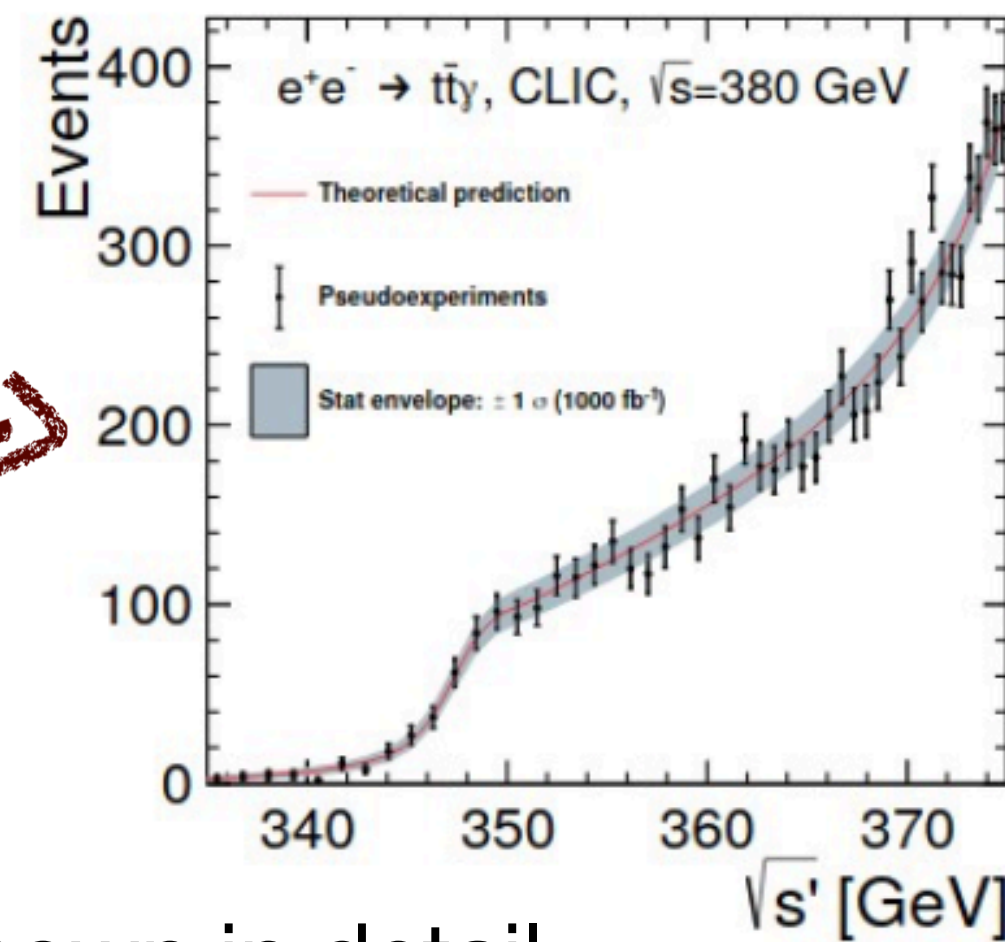
- The accelerator side: Requires sufficient collision energy for top pair production
  - So far thoroughly studied for ILC, CLIC, some derivative studies for FCCee

Three approaches to the top mass

The threshold scan around 350 GeV

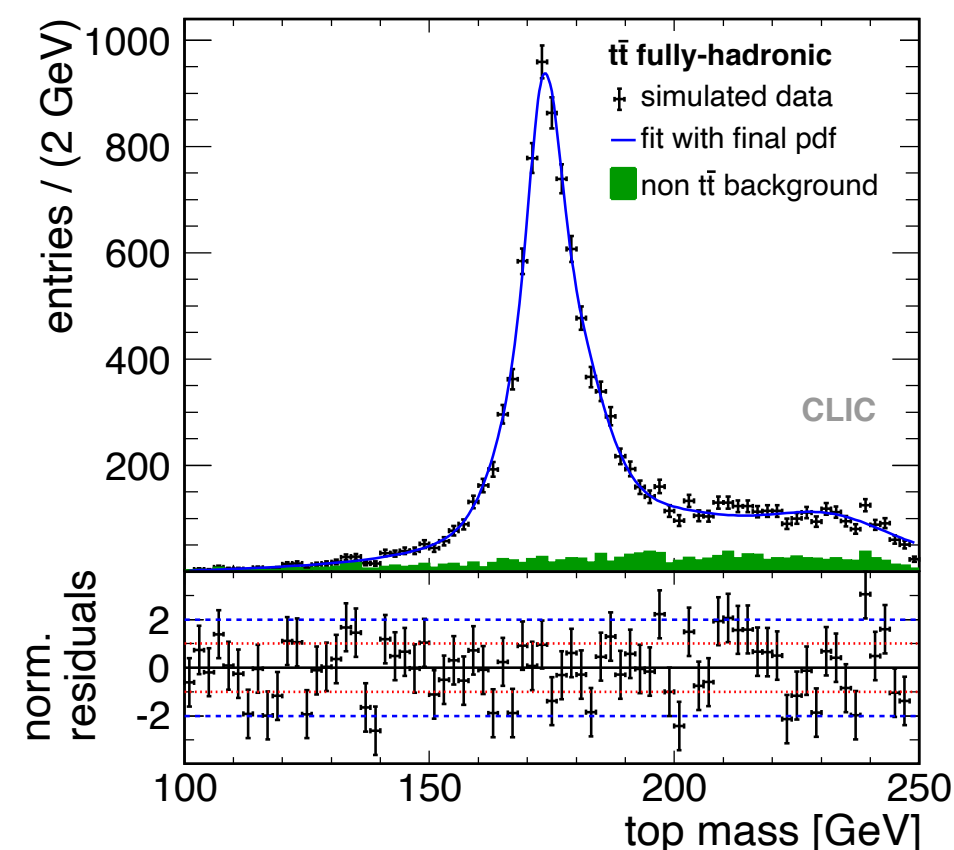


The top mass from radiative events



not shown in detail,  
stat: ~ 20 - 40 MeV

Direct kinematic reconstruction



### Key references:

EPJ C73, 2530 (2013)  
(CLIC, (ILC): Threshold, direct)

JHEP 11, 003 (2019)  
(CLIC: Threshold, radiative, direct)

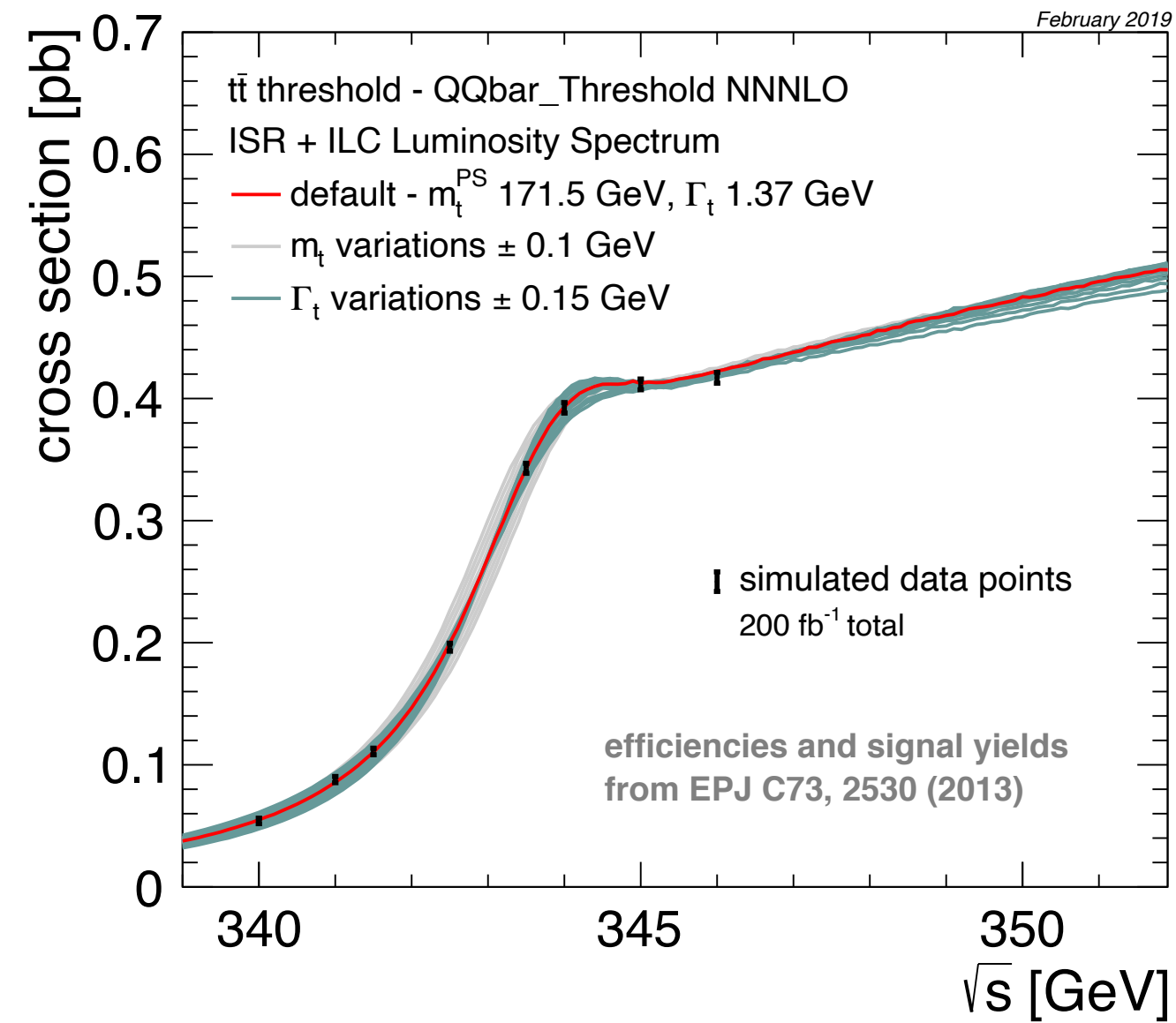
PLB 804, 135353 (2020)  
(ILC, CLIC: radiative)

+ a rich set of reports and conference proceedings on arXiv

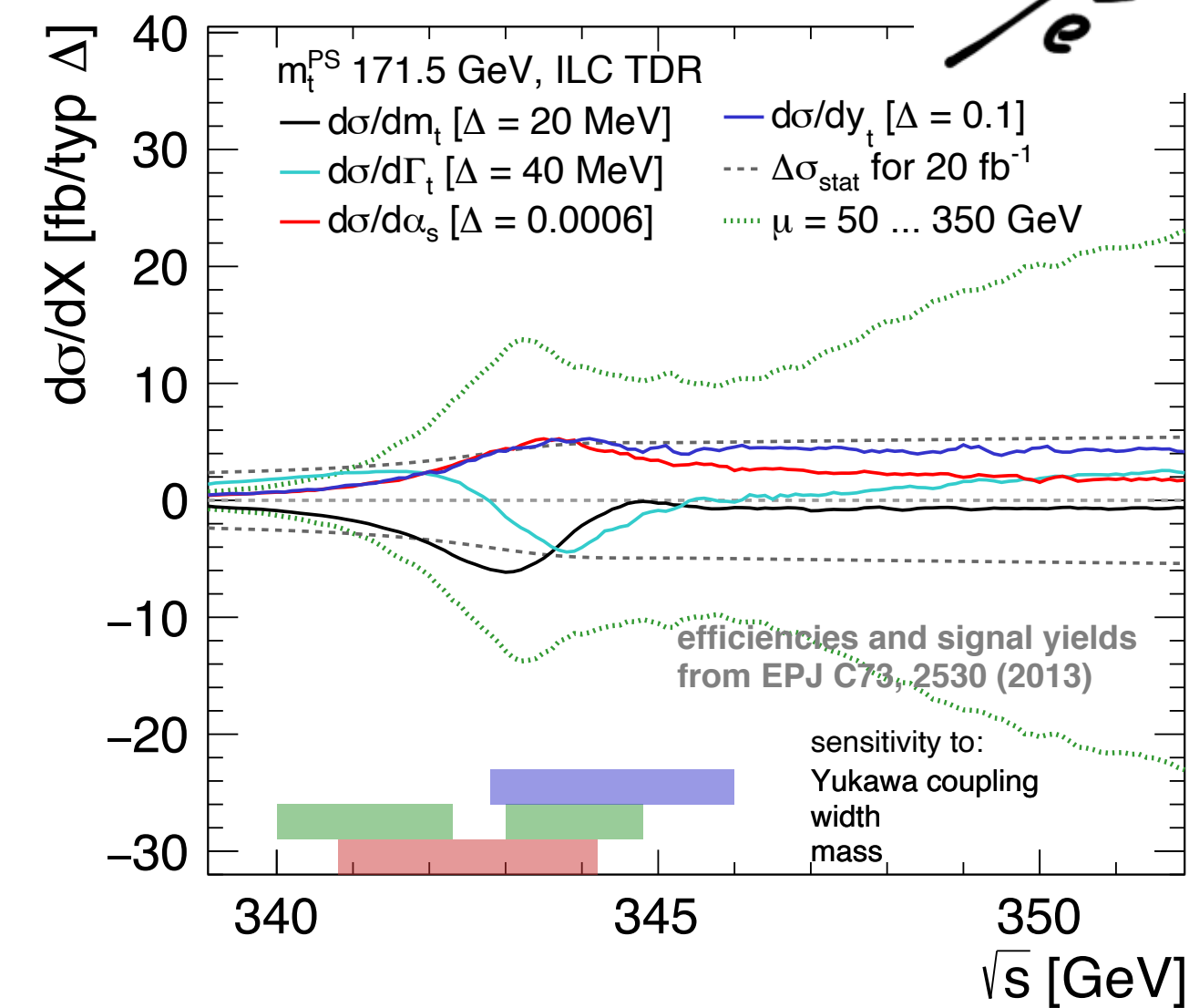
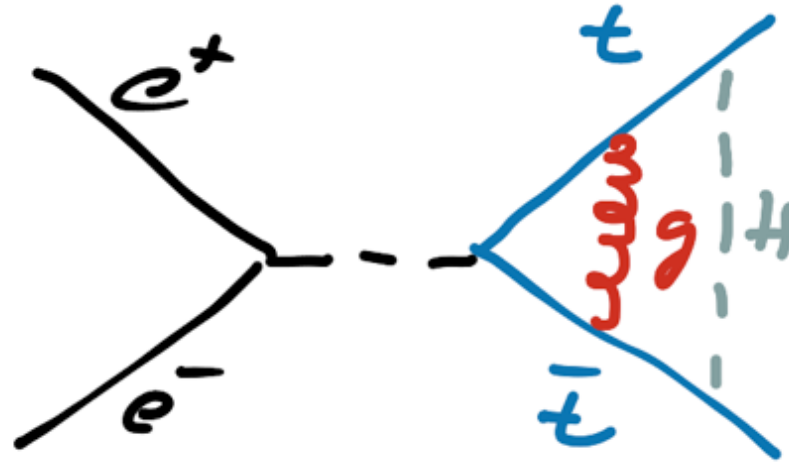
# Mass at the Threshold

At CLIC, ILC, FCCee

- The top threshold provides excellent sensitivity to the mass and other top quark properties
- Measurement of the top quark mass in theoretically well-defined mass schemes



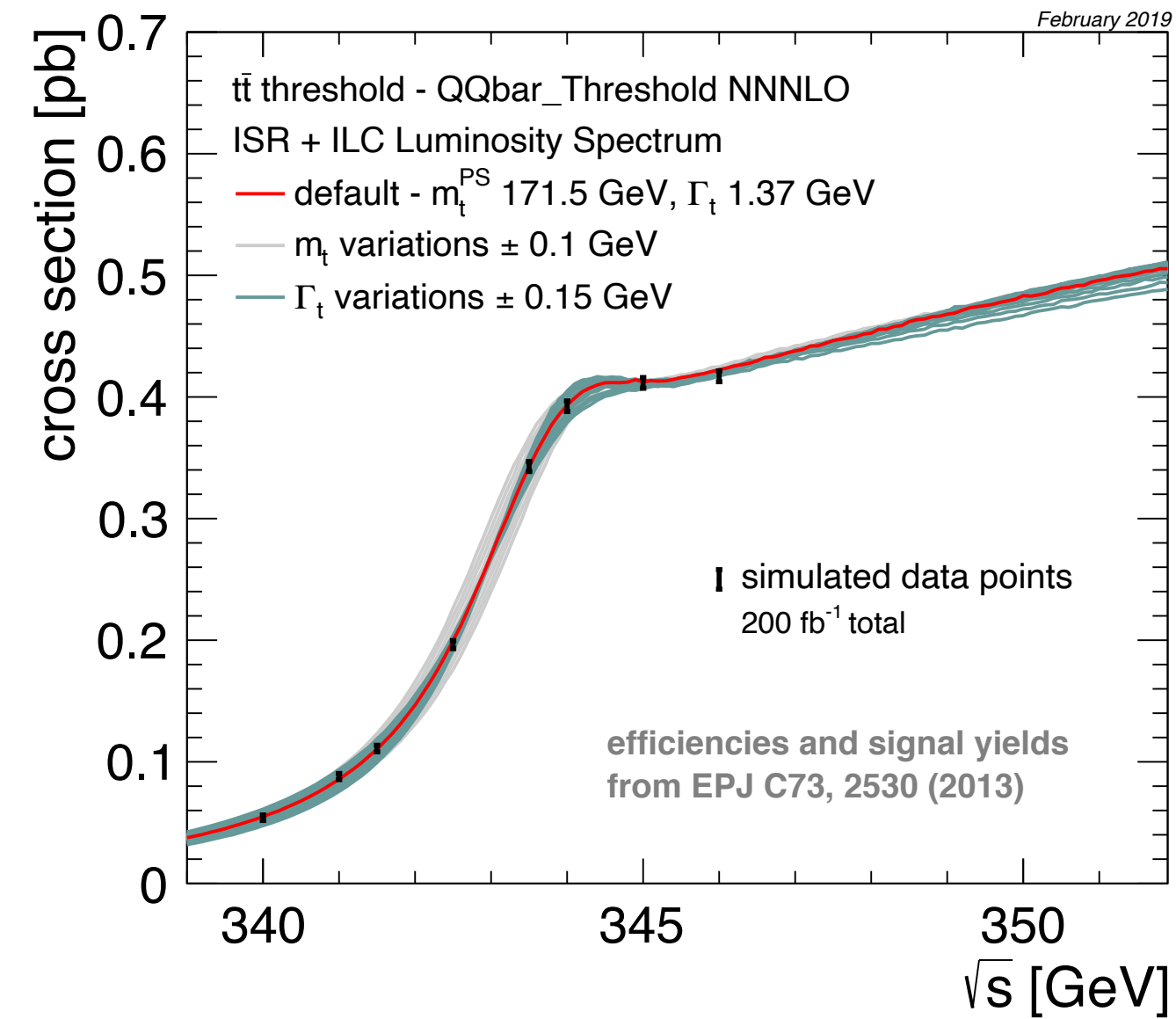
- Assuming an integrated luminosity of  $200 \text{ fb}^{-1}$  (default for ILC, FCCee, x2 of CLIC standard scenario)
- Standard fit of mass only:  
ILC 12.2 MeV [stat]  
CLIC 13.3 MeV [stat]  
FCCee 10.4 MeV [stat]



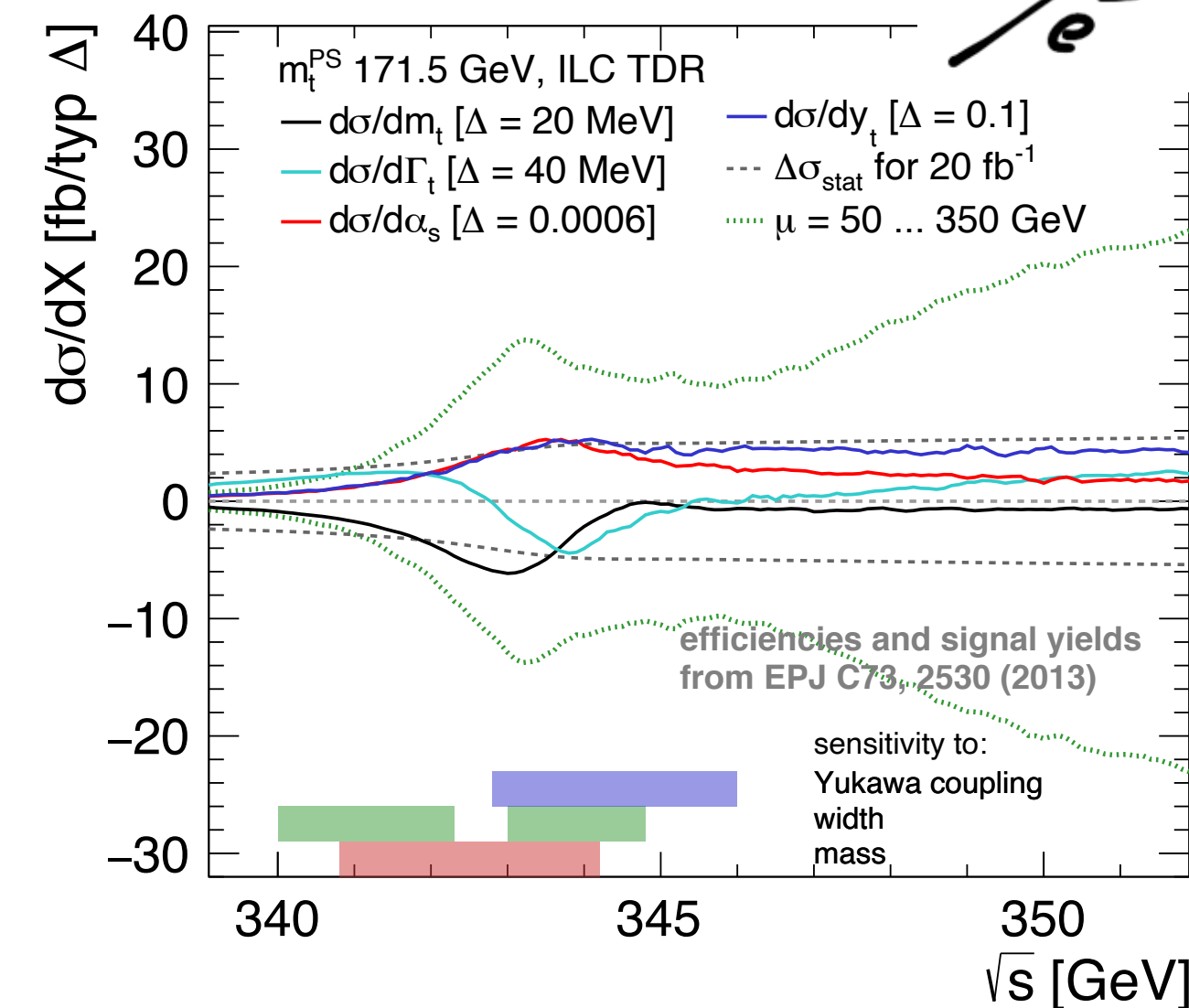
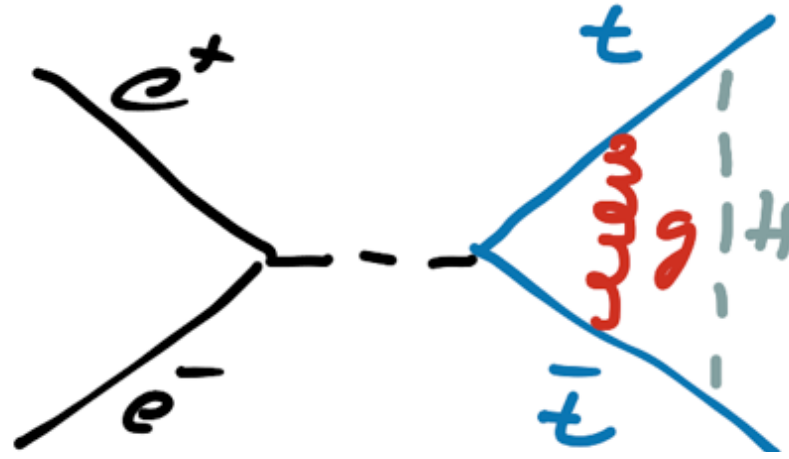
# Mass at the Threshold

At CLIC, ILC, FCCee

- The top threshold provides excellent sensitivity to the mass and other top quark properties
- Measurement of the top quark mass in theoretically well-defined mass schemes



- Assuming an integrated luminosity of 200 fb<sup>-1</sup> (default for ILC, FCCee, x2 of CLIC standard scenario)
- Standard fit of mass only:  
ILC 12.2 MeV [stat]  
CLIC 13.3 MeV [stat]  
FCCee 10.4 MeV [stat]



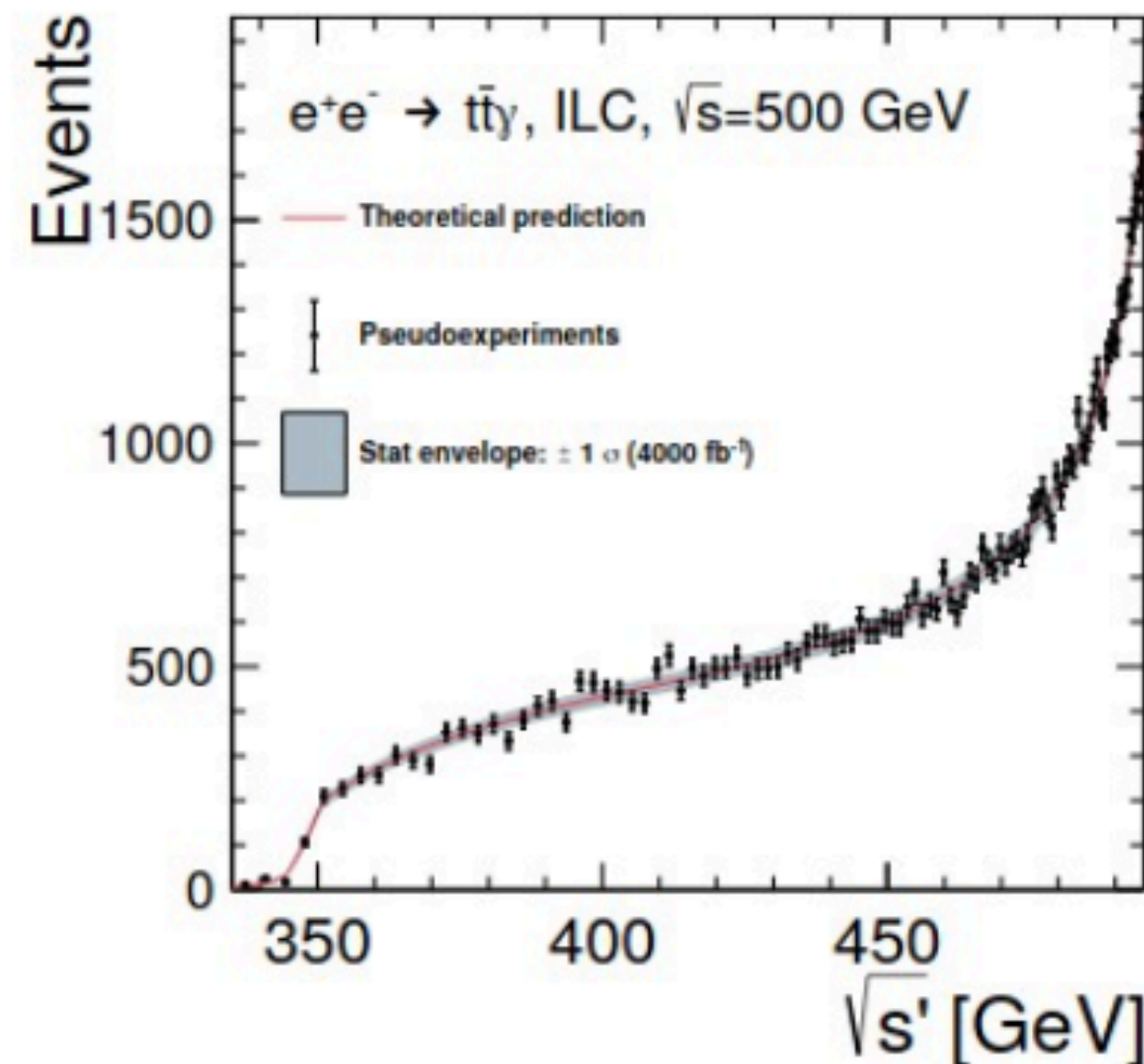
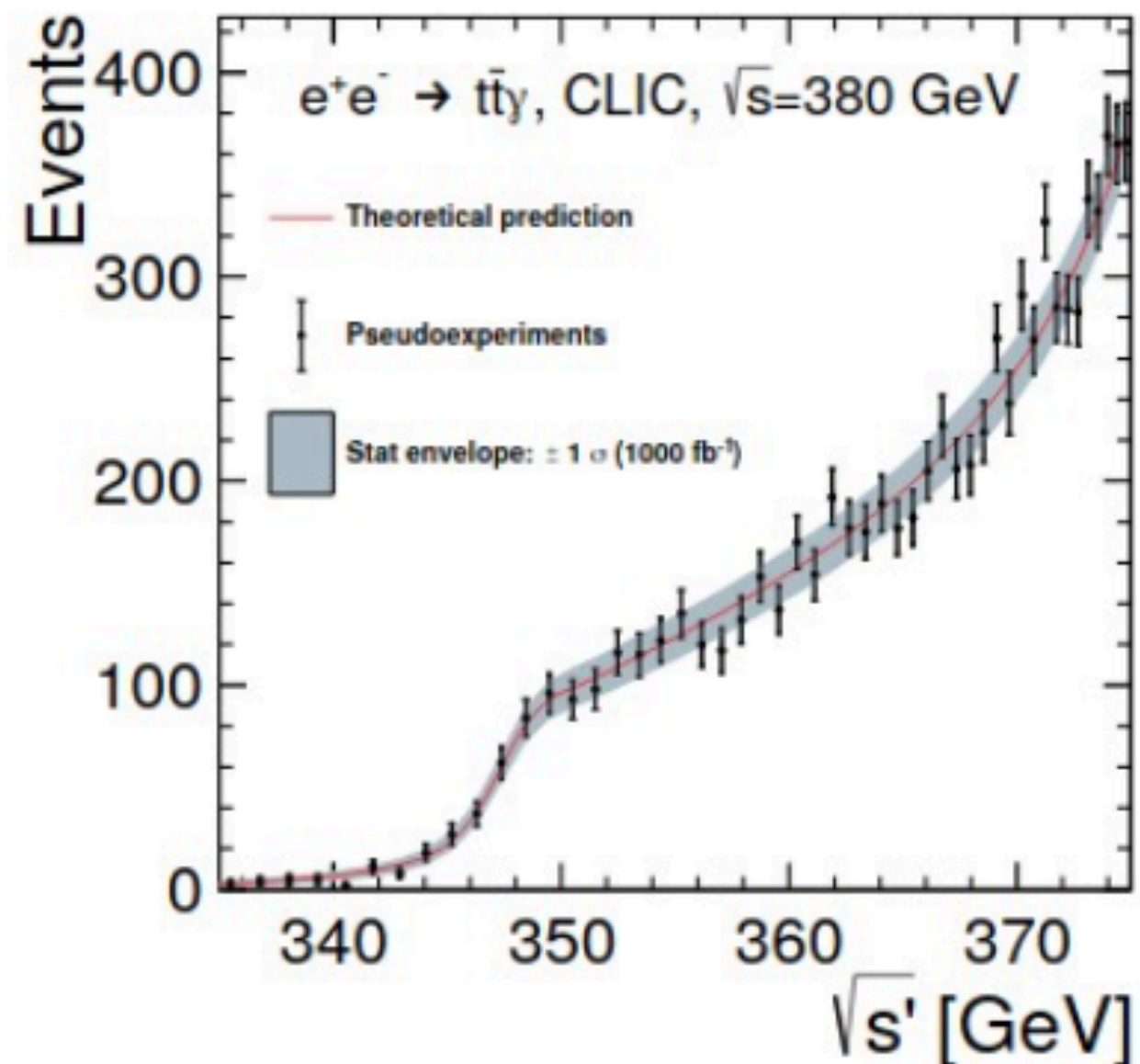
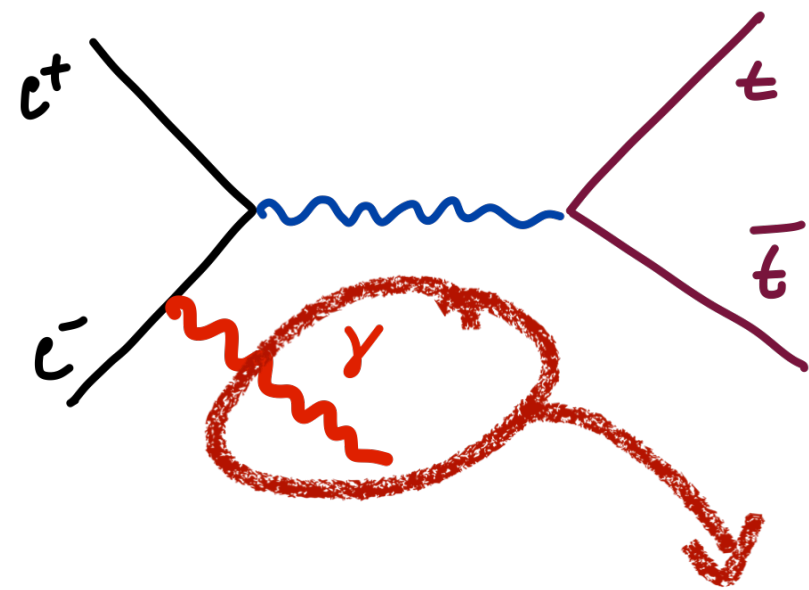
| error source                                    | $\Delta m_t^{\text{PS}}$ [MeV] |
|---|--------------------------------|
| stat. error (200 fb <sup>-1</sup> )             | 13                             |
| theory (NNNLO scale variations, PS scheme)      | 40                             |
| parametric ( $\alpha_s$ , current WA)           | 35                             |
| non-resonant contributions (such as single top) | < 40                           |
| residual background / selection efficiency      | 10 – 20                        |
| luminosity spectrum uncertainty                 | < 10                           |
| beam energy uncertainty                         | < 17                           |
| combined theory & parametric                    | 30 – 50                        |
| combined experimental & backgrounds             | 25 – 50                        |
| total (stat. + syst.)                           | 40 – 75                        |

- Detailed evaluation of systematic uncertainties
- Multi-parameter fits (mass, width,  $\alpha_s$ ,  $y_t$ ), scan optimization...

# Mass from Radiative Events

At CLIC, ILC - 380 and 500 GeV

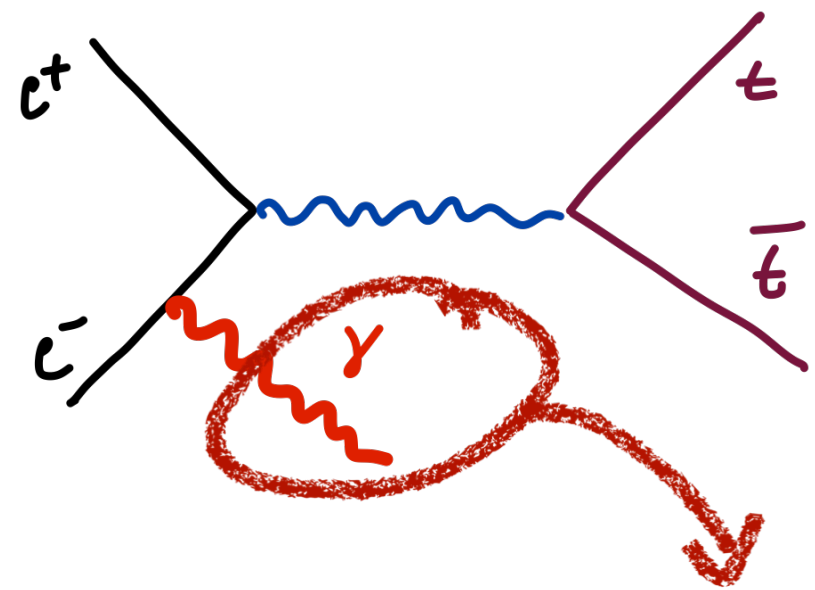
- A new(er) idea to measure the top mass in a theoretically well-defined scheme in high-energy running above the threshold



# Mass from Radiative Events

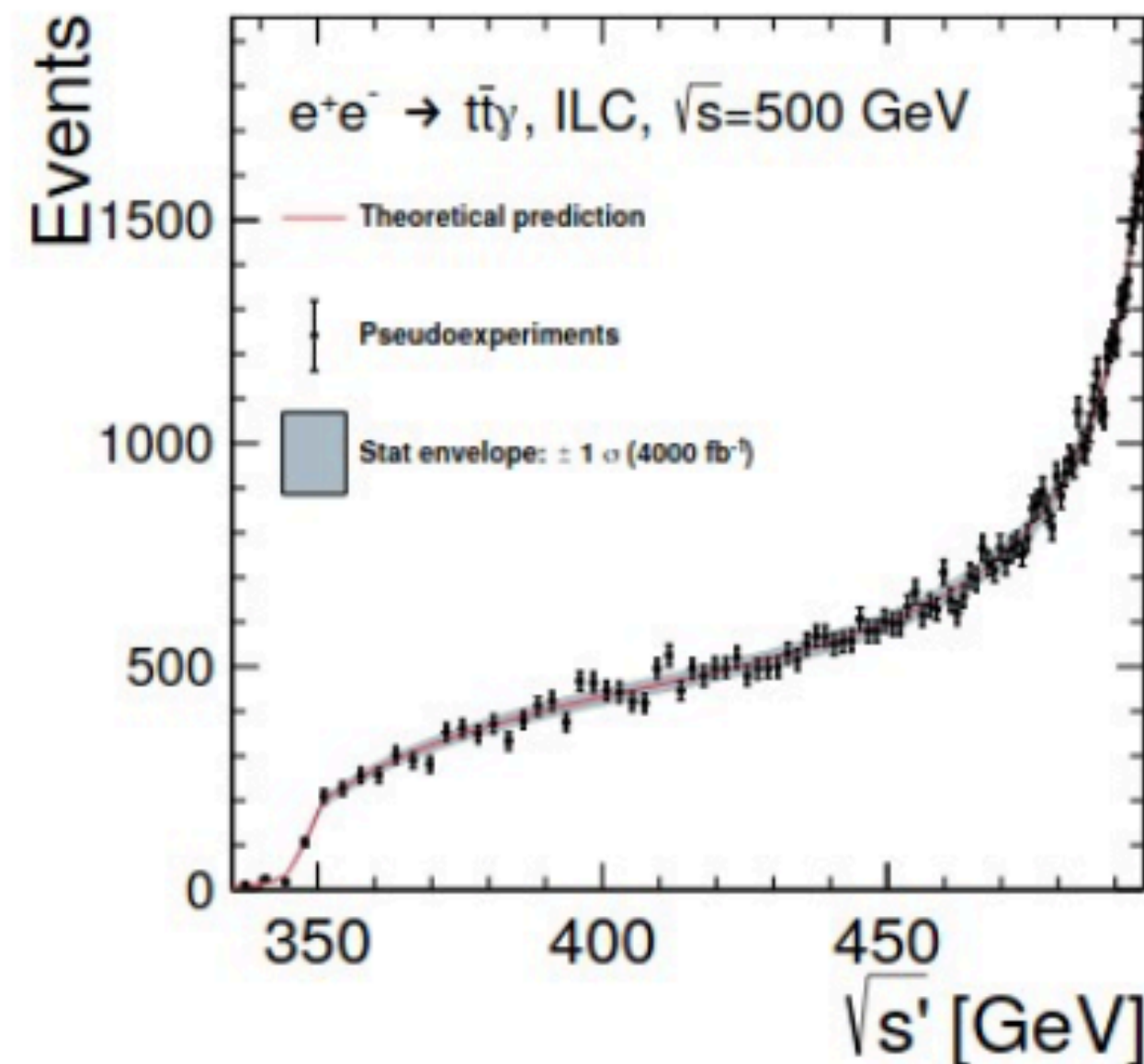
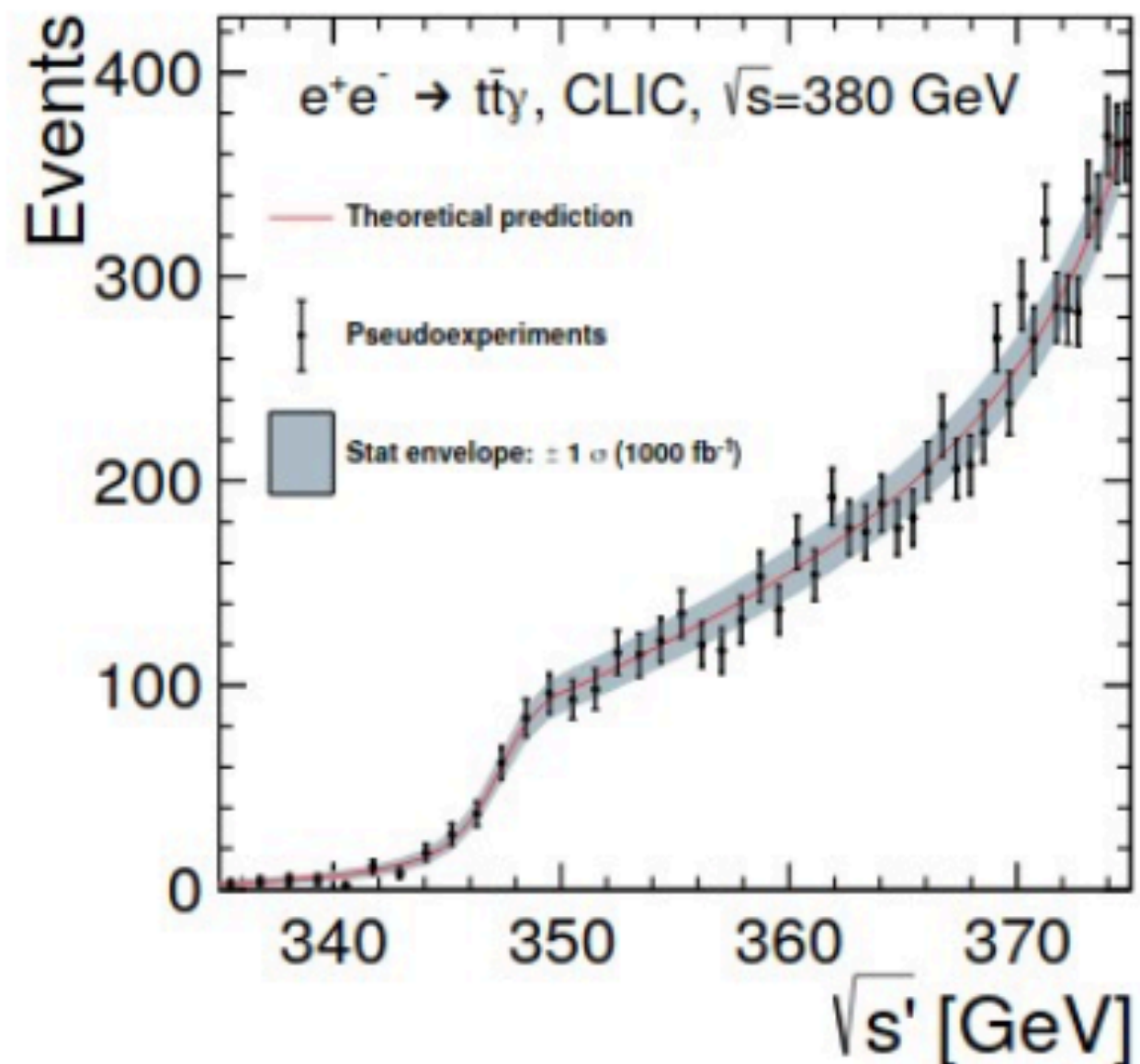
At CLIC, ILC - 380 and 500 GeV

- A new(er) idea to measure the top mass in a theoretically well-defined scheme in high-energy running above the threshold



matched NNLO + NNLL calculation,  
luminosity spectrum folded in explicitly;  
Extraction of short distance MSR mass

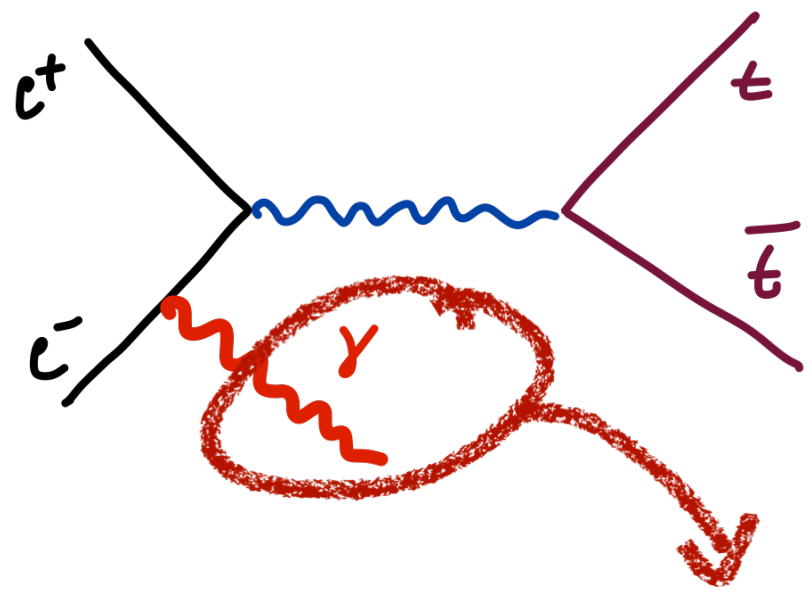
| cms energy                      | CLIC, $\sqrt{s} = 380$ GeV |         | ILC, $\sqrt{s} = 500$ GeV |         |
|---------------------------------|----------------------------|---------|---------------------------|---------|
| luminosity [ $\text{fb}^{-1}$ ] | 500                        | 1000    | 500                       | 4000    |
| statistical                     | 140 MeV                    | 90 MeV  | 350 MeV                   | 110 MeV |
| theory                          | 46 MeV                     |         | 55 MeV                    |         |
| lum. spectrum                   | 20 MeV                     |         | 20 MeV                    |         |
| photon response                 | 16 MeV                     |         | 85 MeV                    |         |
| total                           | 150 MeV                    | 110 MeV | 360 MeV                   | 150 MeV |



# Mass from Radiative Events

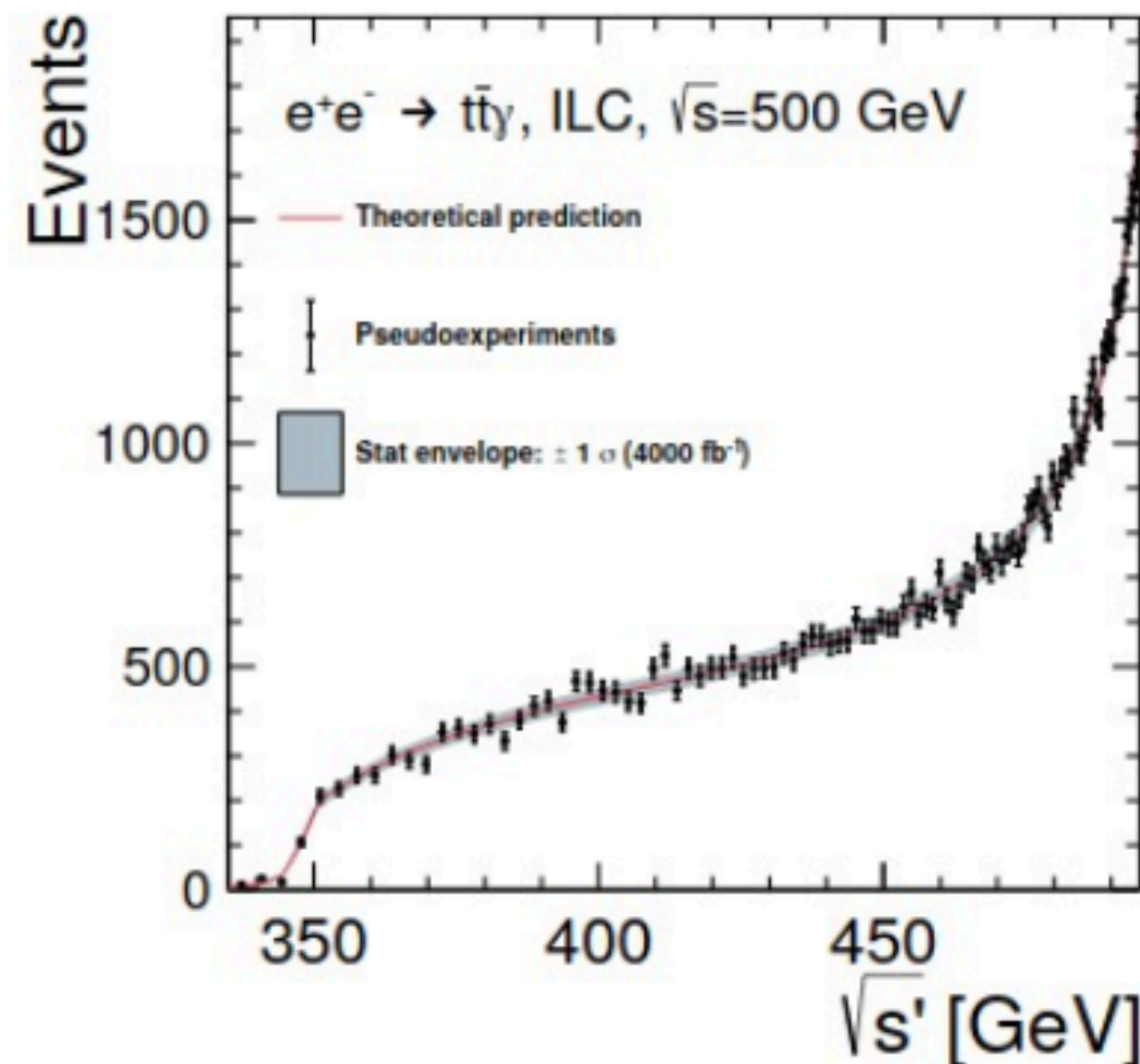
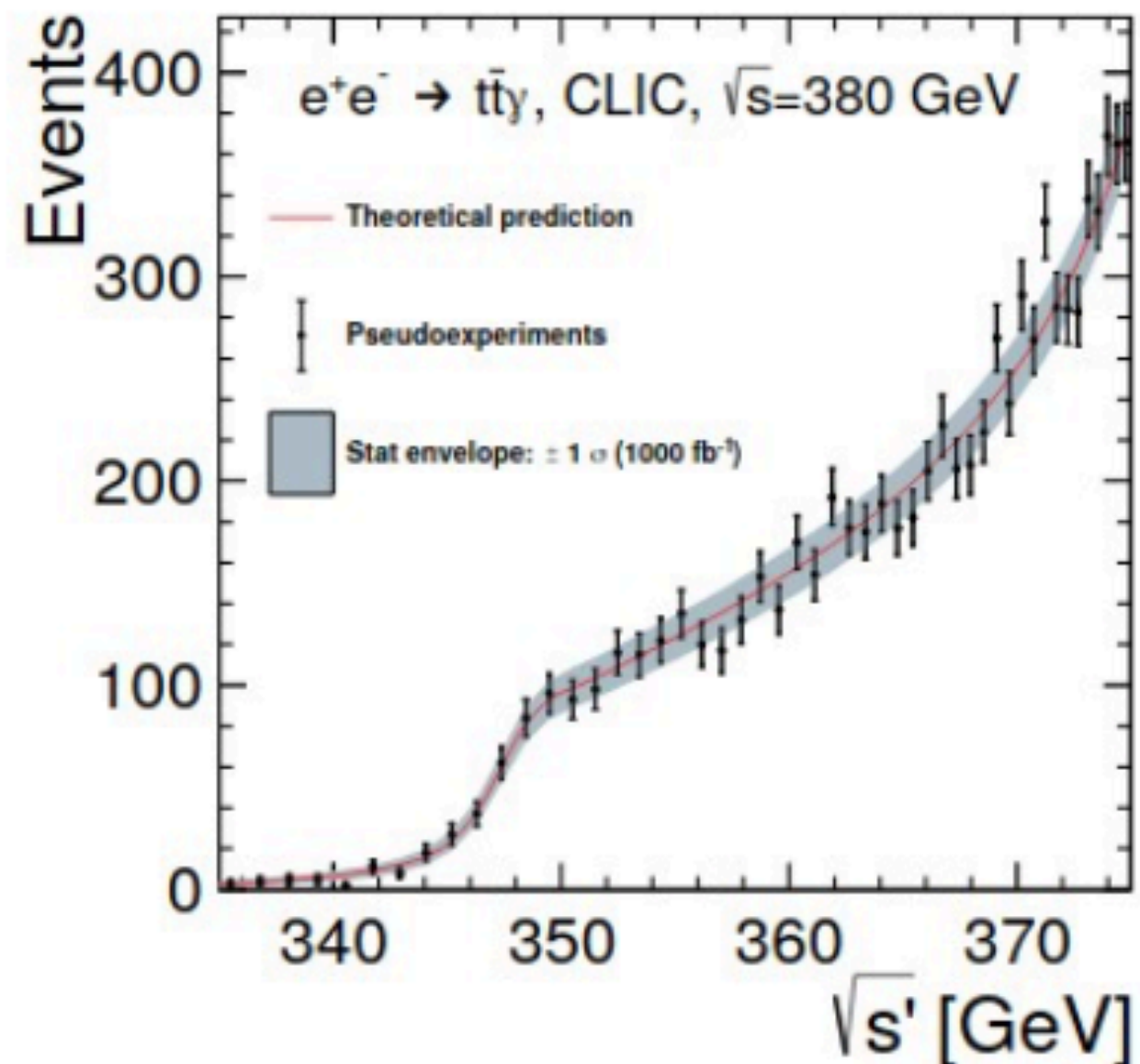
At CLIC, ILC - 380 and 500 GeV

- A new(er) idea to measure the top mass in a theoretically well-defined scheme in high-energy running above the threshold

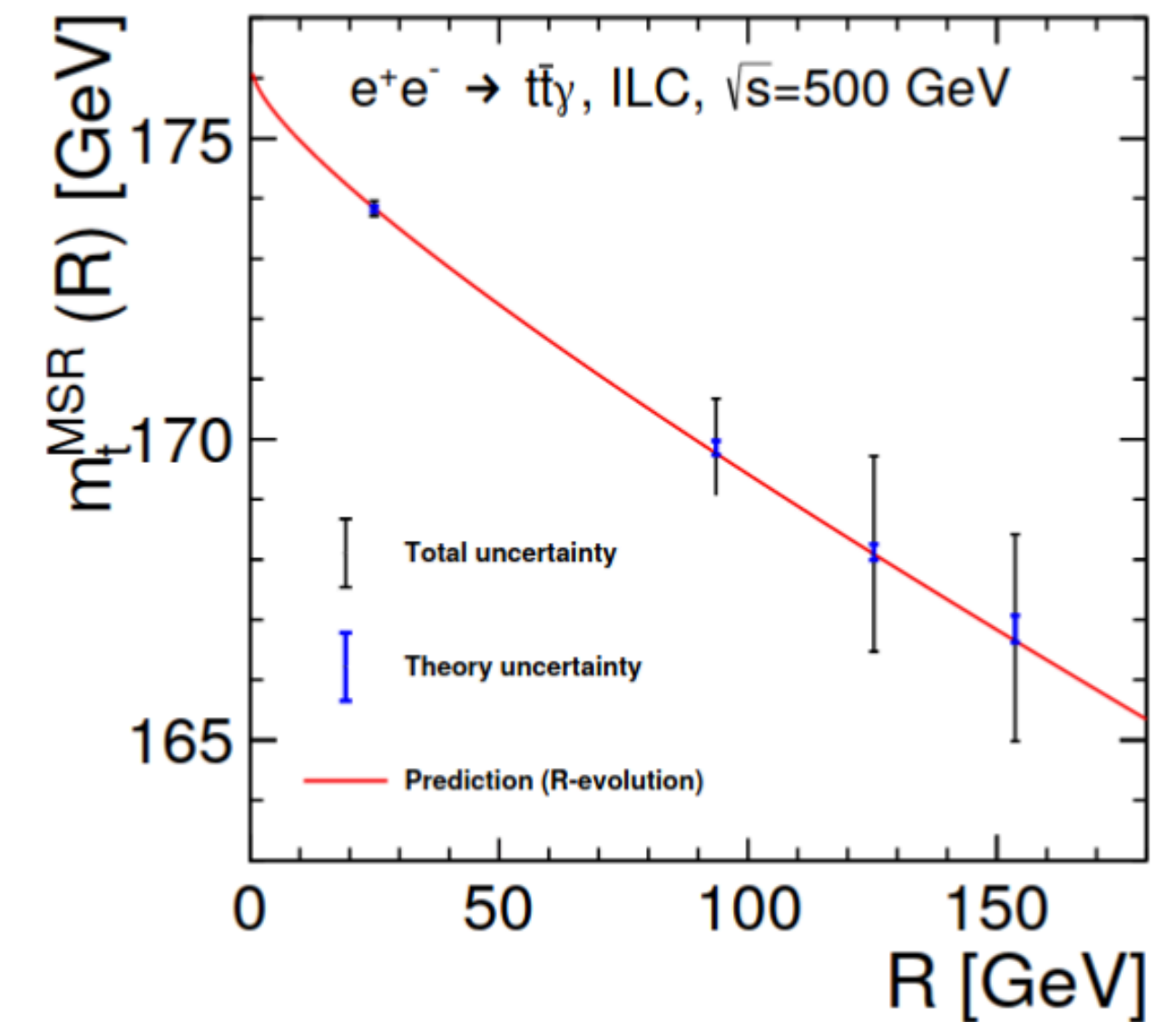


matched NNLO + NNLL calculation,  
luminosity spectrum folded in explicitly;  
Extraction of short distance MSR mass

| cms energy                      | CLIC, $\sqrt{s} = 380$ GeV |         | ILC, $\sqrt{s} = 500$ GeV |         |
|---------------------------------|----------------------------|---------|---------------------------|---------|
| luminosity [ $\text{fb}^{-1}$ ] | 500                        | 1000    | 500                       | 4000    |
| statistical                     | 140 MeV                    | 90 MeV  | 350 MeV                   | 110 MeV |
| theory                          | 46 MeV                     |         | 55 MeV                    |         |
| lum. spectrum                   | 20 MeV                     |         | 20 MeV                    |         |
| photon response                 | 16 MeV                     |         | 85 MeV                    |         |
| total                           | 150 MeV                    | 110 MeV | 360 MeV                   | 150 MeV |



can provide  $5\sigma$  evidence for scale evolution (“running”) of the top quark MSR mass from ILC500 data alone





- Threshold studies - standard total cross-section studies already very complete, personally planning an updated summary of results for CLIC, ILC, FCCee) - ideas beyond:
  - additional observables at the threshold: asymmetries (AFB, maybe also LR with polarisation), kinematic observables, ... -
  - Study of the evolution of signal efficiency and background rejection in the threshold region with event generators - at the moment the studies use constant numbers
  - Unfolding with measured luminosity spectrum
- More generally
  - Explore possibilities to combine threshold and above-threshold measurements, possibly breaking degeneracies of  $\alpha_s$ ,  $y_t$
  - Further development of mass measurements in the continuum, connection to theory to establish the best precision in theoretically well-defined mass schemes
    - Includes systematics in kinematic reconstruction
  - Identify the best strategy to measure the top quark width (threshold, continuum)
- ... Many interesting possibilities!