

# Theory Overview: Searching for the Second Higgs



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# The Second Higgs

Additional Higgs scalars often arise  
in natural theories of EWSB:

- Higgs sector of the MSSM/NMSSM...
- Little Higgs, Composite Higgs...
- Twin Higgs, Neutral Naturalness...

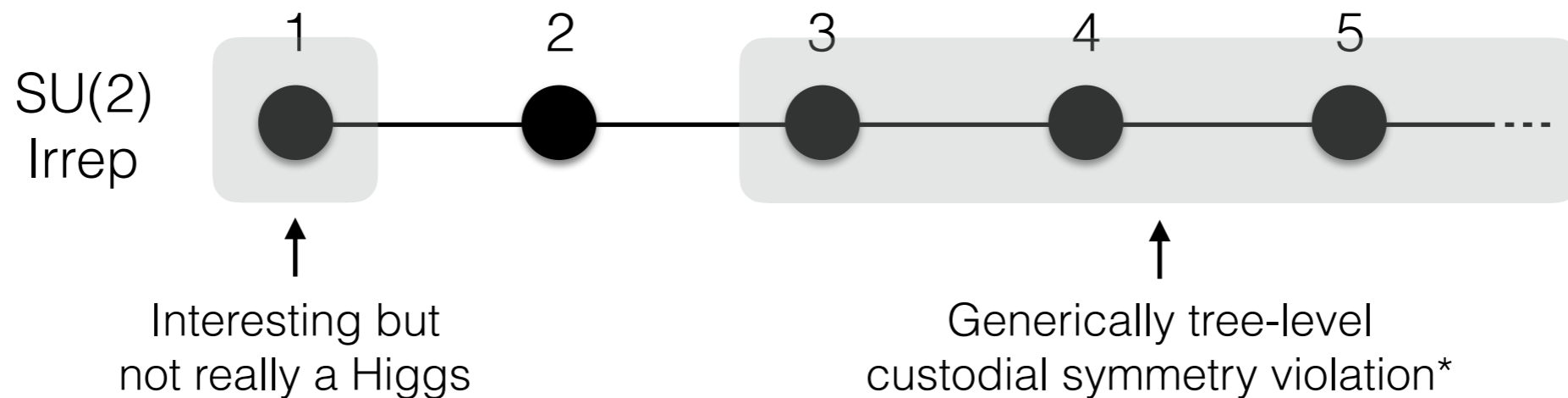
## **More broadly:**

The spin-1/2 and spin-1 sectors of our universe  
are rich in multiplicity.

*Why not also the spin-0 sector?*

# Why 2HDM?

Add another scalar (w/ vev) to the SM...



Indirect signals of a **doublet**:  $\mathcal{O}\left(\frac{v^2}{M^2}\right)$  Higgs coupling deviations

5% precision  $\Leftrightarrow M \gtrsim 1$  TeV

Indirect signals of **higher reps**:  $\mathcal{O}\left(\frac{v^2}{M^2}\right)$  rho parameter (w/o tuning)

.02% precision  $\Leftrightarrow M \gtrsim 17$  TeV

\*Georgi-Machacek model is custodial bi-triplet

# Where 2HDM?

Generically, mass scale of second Higgs only constrained by distribution of vev; can naturally be (reasonably) asymmetric.

E.g. SUSY:

$$\Delta \approx \sin^2(2\beta) \frac{m_H^2}{m_h^2} + \mathcal{O}(m_H^0)$$

At large  $\tan\beta$ , suppressed tuning:

$$\Delta(\tan\beta = 50) \leq 1 \rightarrow m_H \lesssim 3.1 \text{ TeV}$$

Multi-TeV Higgs states consistent with naturalness in this framework. Not feasible @ 14 TeV, but within reach of 100 TeV.

# Simplified parameter space

Physical d.o.f. are (8-3=5):  $h, H, A, H^\pm$

After EWSB, 9 free params in CP-conserving potential.

Useful basis of 4 physical masses, 2 angles, 3 couplings:

$$m_h, m_H, m_A, m_{H^\pm} \qquad \tan \beta \equiv \langle \Phi_2 \rangle / \langle \Phi_1 \rangle$$

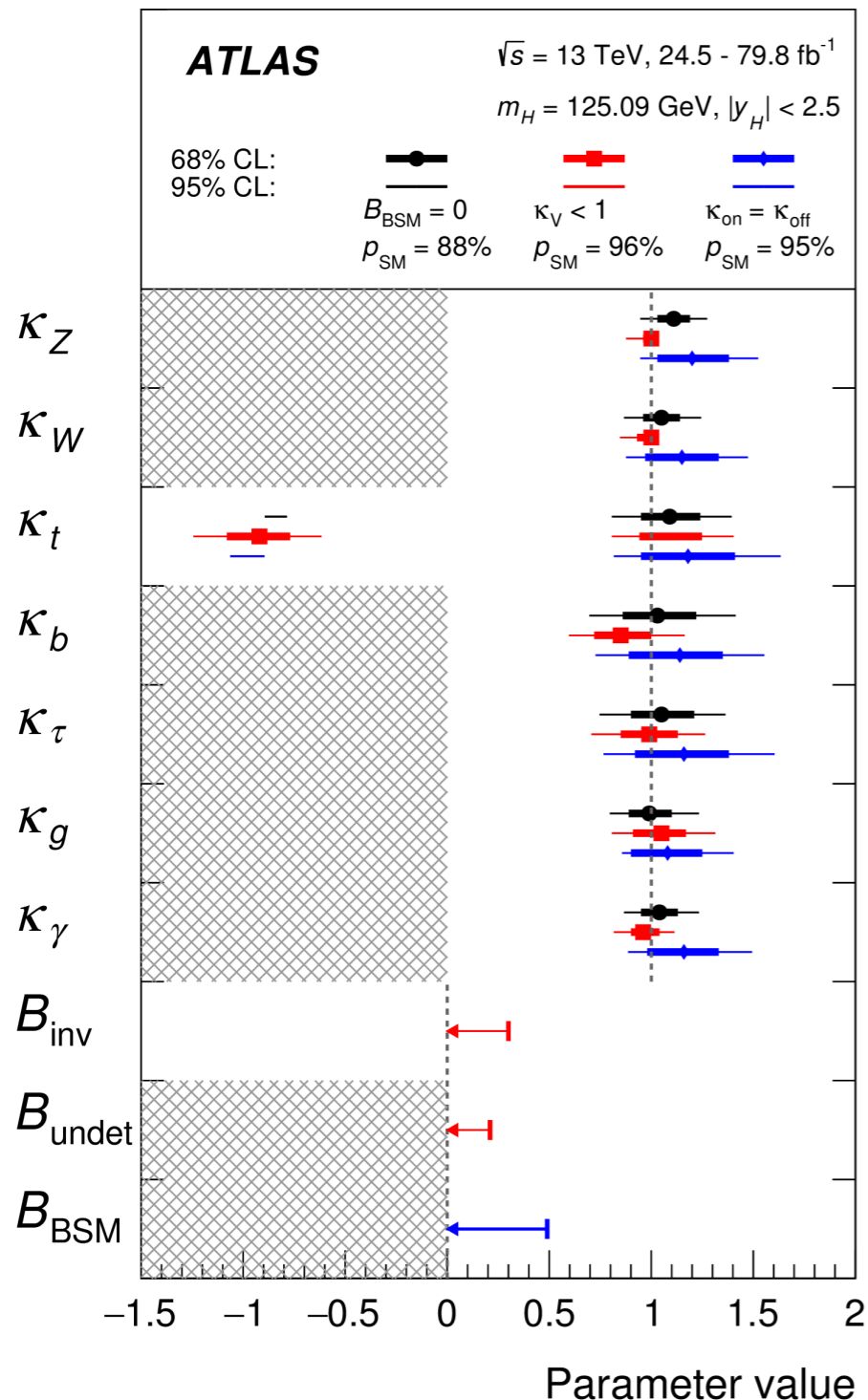
$$\alpha : \begin{pmatrix} \sqrt{2} \operatorname{Re}(\Phi_2^0) - v_2 \\ \sqrt{2} \operatorname{Re}(\Phi_1^0) - v_1 \end{pmatrix} = \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} h \\ H \end{pmatrix}$$

$$\lambda_5, \lambda_6, \lambda_7 \quad (\text{only appear in trilinear couplings})$$

Couplings of scalars to fermions, vectors only depend on angles.

$$\text{Discrete symm. for flavor: } \lambda_{6,7} = 0 \qquad \text{MSSM: } \lambda_{5,6,7} = 0$$

# Alignment limit



- Couplings of the observed Higgs so far approximately SM-like.

- Suggests proximity to alignment limit

$$\alpha \approx \beta - \pi/2$$

- In this limit, h is fluctuation around the vev, remaining scalars are spectators to EWSB

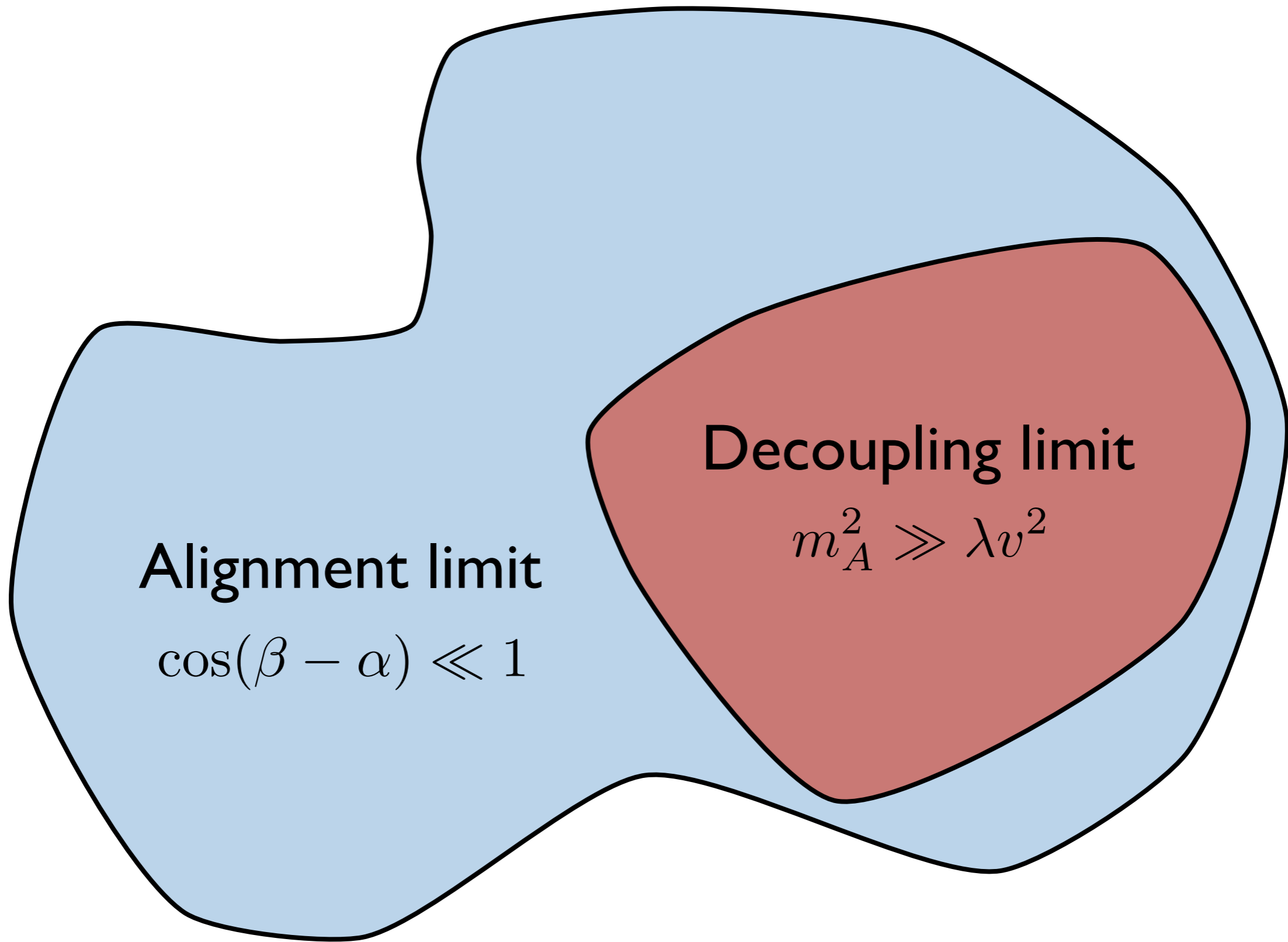
- (Achievable via decoupling in mass or accidentally, via dimensionless couplings)

- Useful to expand in

$$\delta = \beta - \alpha - \pi/2$$

$$\approx -\cos(\beta - \alpha)$$

[Haber, Gunion '02; NC, Thomas '12; NC, Galloway,  
Thomas '13; Carena, Low, Shah, Wagner '13]



Four discrete 2HDM types. All couplings to SM states fixed in terms of two angles.

	2HDM I	2HDM II	2HDM III	2HDM IV
$u$	$\Phi_2$	$\Phi_2$	$\Phi_2$	$\Phi_2$
$d$	$\Phi_2$	$\Phi_1$	$\Phi_2$	$\Phi_1$
$e$	$\Phi_2$	$\Phi_1$	$\Phi_1$	$\Phi_2$

$y_{2\text{HDM}}/y_{\text{SM}}$	2HDM 1	2HDM 2
$hVV$	$1 - \delta^2/2$	$1 - \delta^2/2$
$hQu$	$1 - \delta/t_\beta$	$1 - \delta/t_\beta$
$hQd$	$1 - \delta/t_\beta$	$1 + \delta t_\beta$
$hLe$	$1 - \delta/t_\beta$	$1 + \delta t_\beta$
$HVV$	$-\delta$	$-\delta$
$HQu$	$-\delta - 1/t_\beta$	$-\delta - 1/t_\beta$
$HQd$	$-\delta - 1/t_\beta$	$-\delta + t_\beta$
$HLe$	$-\delta - 1/t_\beta$	$-\delta + t_\beta$
$AVV$	0	0
$AQu$	$1/t_\beta$	$1/t_\beta$
$AQd$	$-1/t_\beta$	$t_\beta$
$ALe$	$-1/t_\beta$	$t_\beta$

$$\delta = \beta - \alpha - \pi/2$$

- Scalar self-couplings have additional parametric freedom.
- Gives a map between current fits to the Higgs couplings and the possible size of NP signals.
- H, A are similar d.o.f. in alignment limit; H<sup>+</sup> couplings analogous to A.
- Focus on the two most familiar, Types 1 and 2.
- Work at tree level, but loops matter [e.g. Chen, Han, Su, Su, Wu '18]



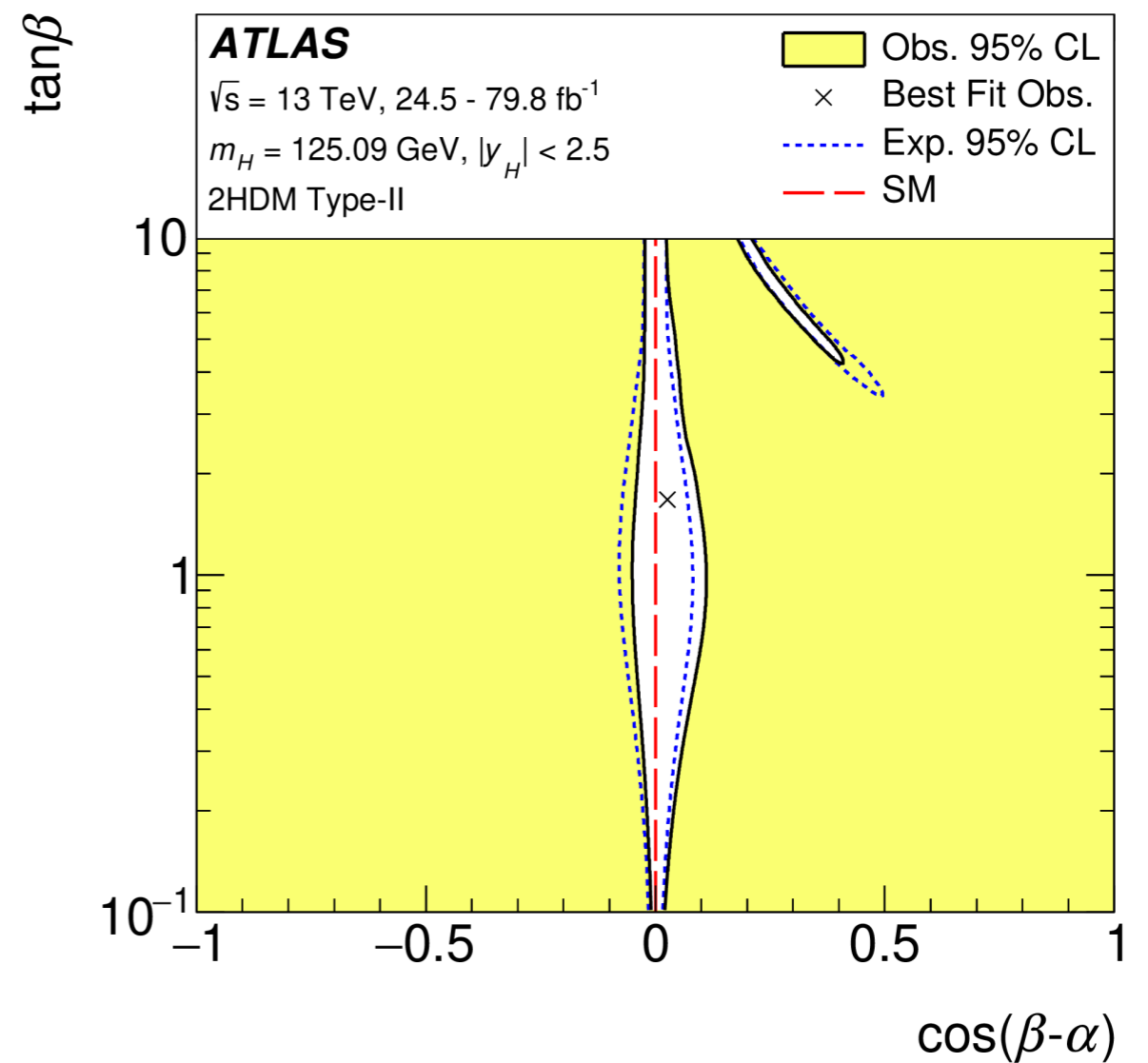
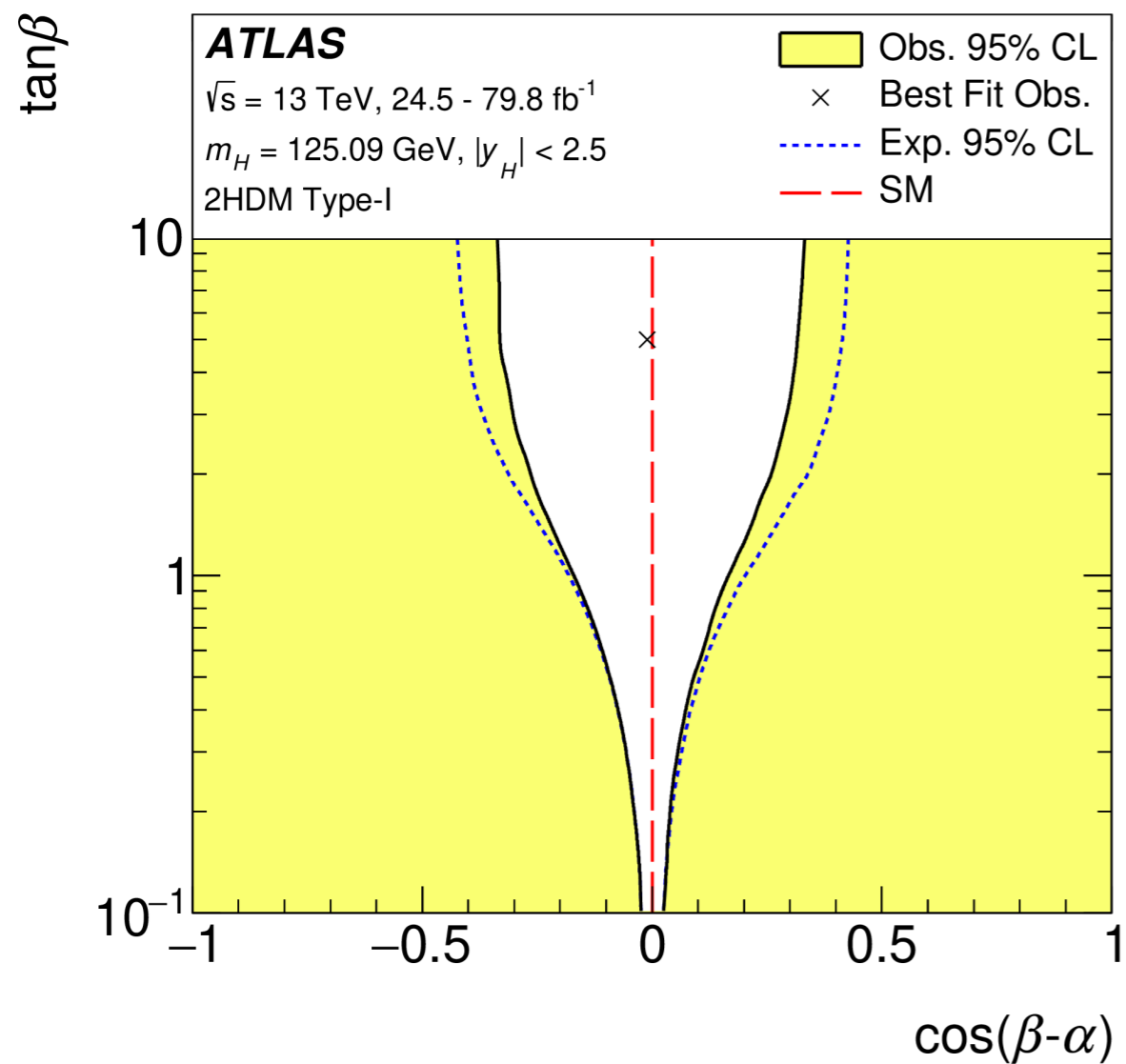
# Complementarity

**Indirect:**  
Measure  
 $h(125)$

$y_{2\text{HDM}}/y_{\text{SM}}$	2HDM 1	2HDM 2
$hVV$	$1 - \delta^2/2$	$1 - \delta^2/2$
$hQu$	$1 - \delta/t_\beta$	$1 - \delta/t_\beta$
$hQd$	$1 - \delta/t_\beta$	$1 + \delta t_\beta$
$hLe$	$1 - \delta/t_\beta$	$1 + \delta t_\beta$
$HVV$	$-\delta$	$-\delta$
$HQu$	$-\delta - 1/t_\beta$	$-\delta - 1/t_\beta$
$HQd$	$-\delta - 1/t_\beta$	$-\delta + t_\beta$
$HLe$	$-\delta - 1/t_\beta$	$-\delta + t_\beta$
$AVV$	0	0
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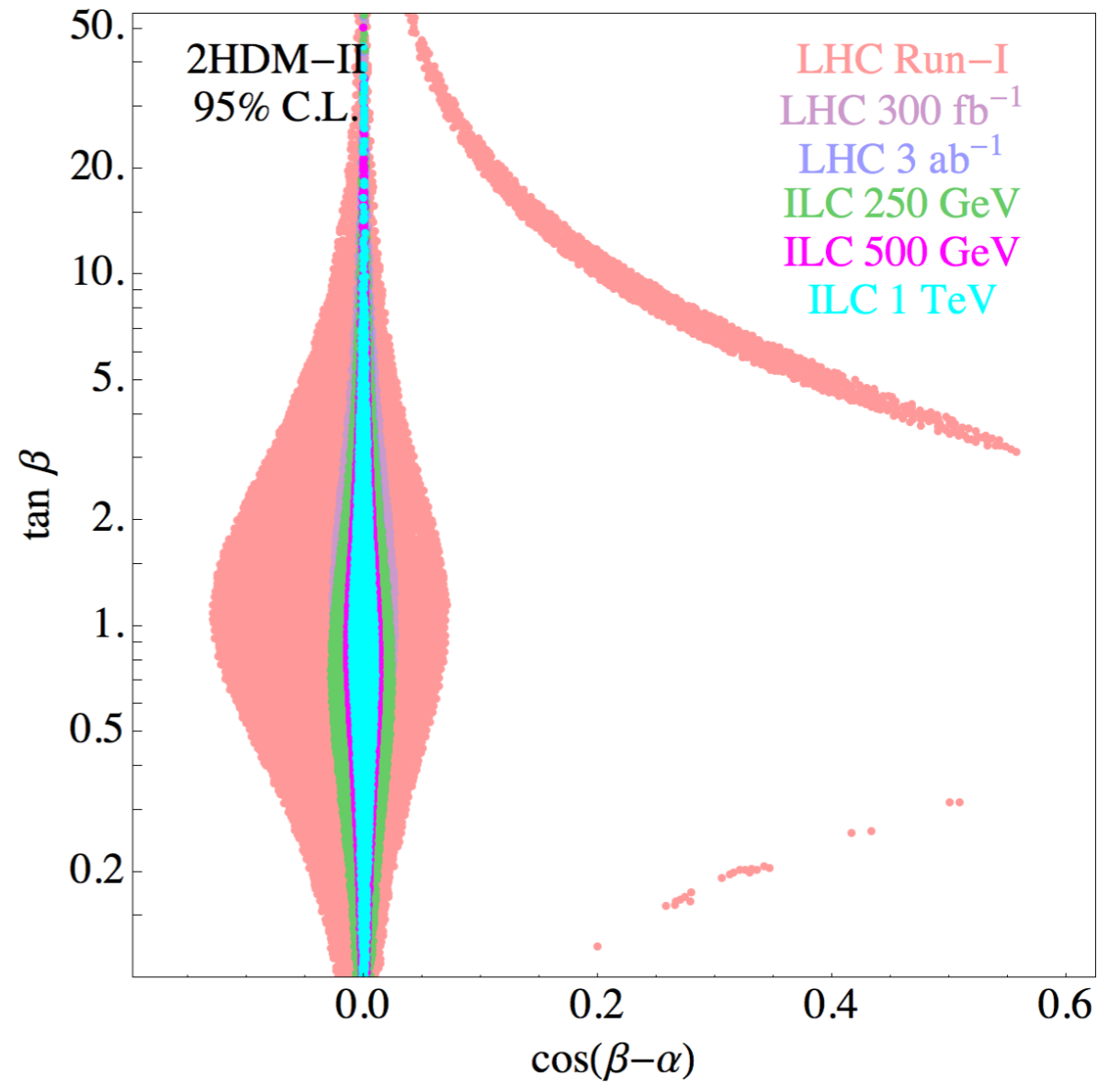
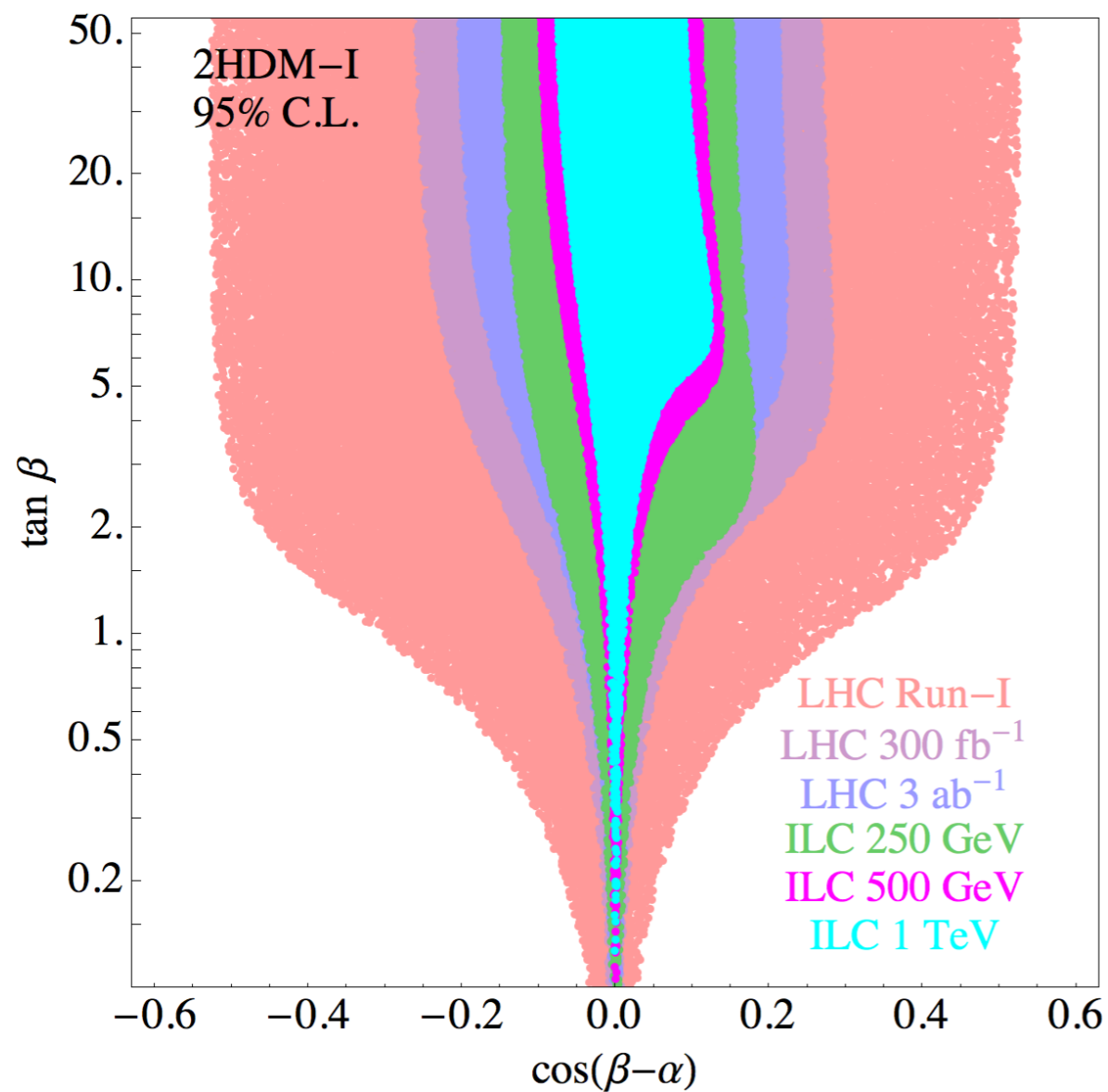
**Direct:**  
Search for  
 $H/A/H^\pm$

# Indirect: Where now?



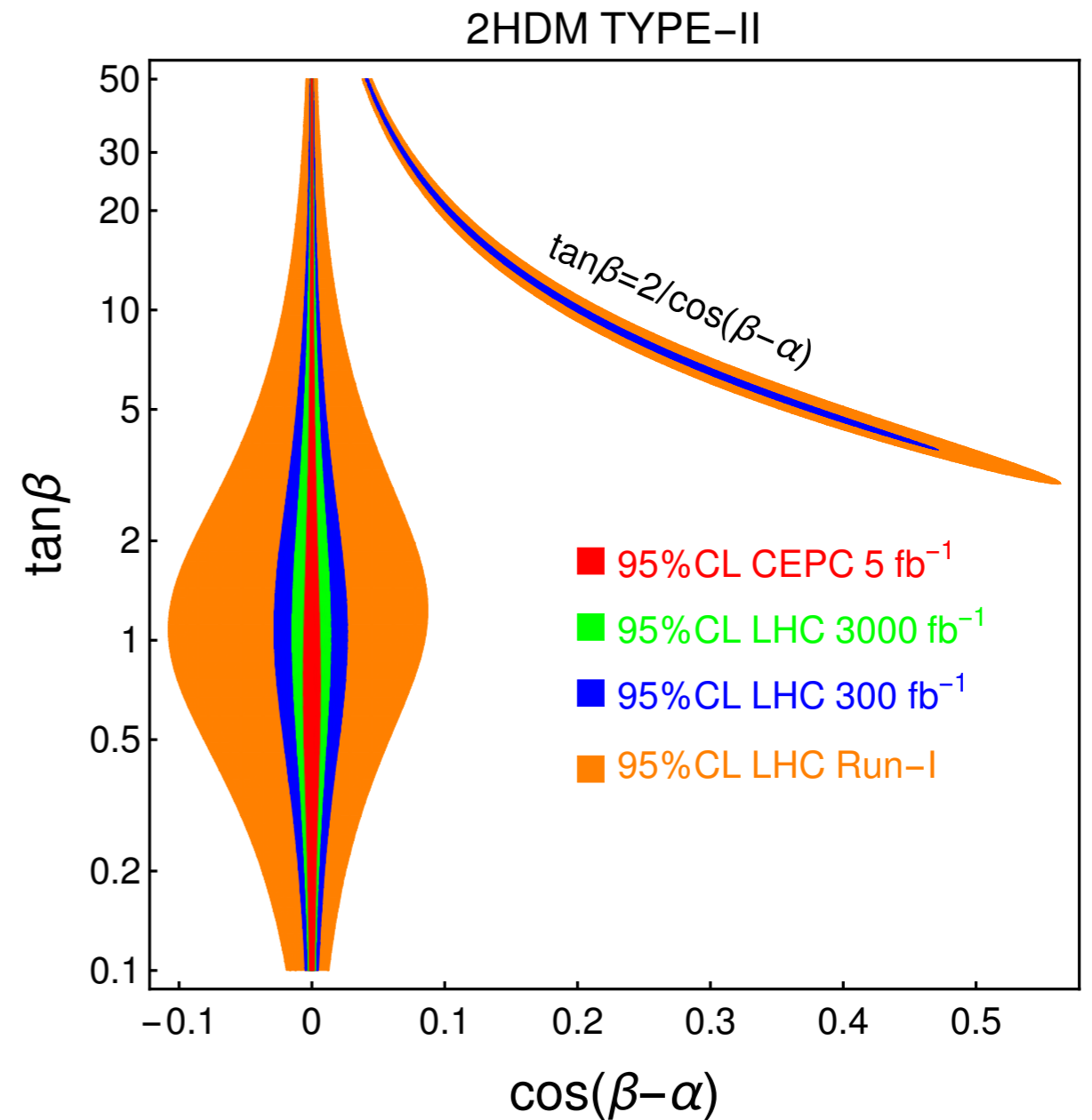
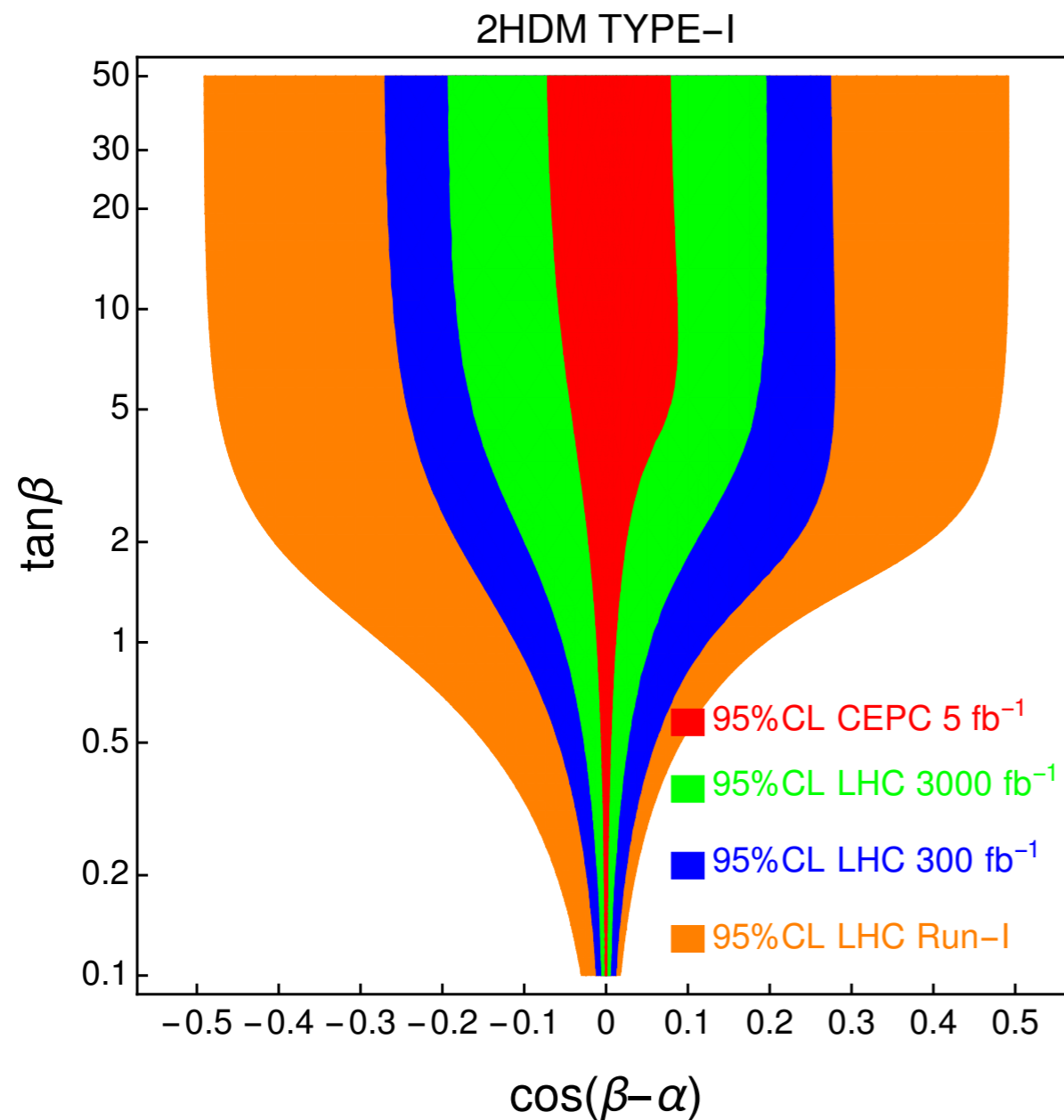
# Indirect: Whither?

[Barger, Everett, Logan, Shaughnessy '13]



# Indirect: Whither?

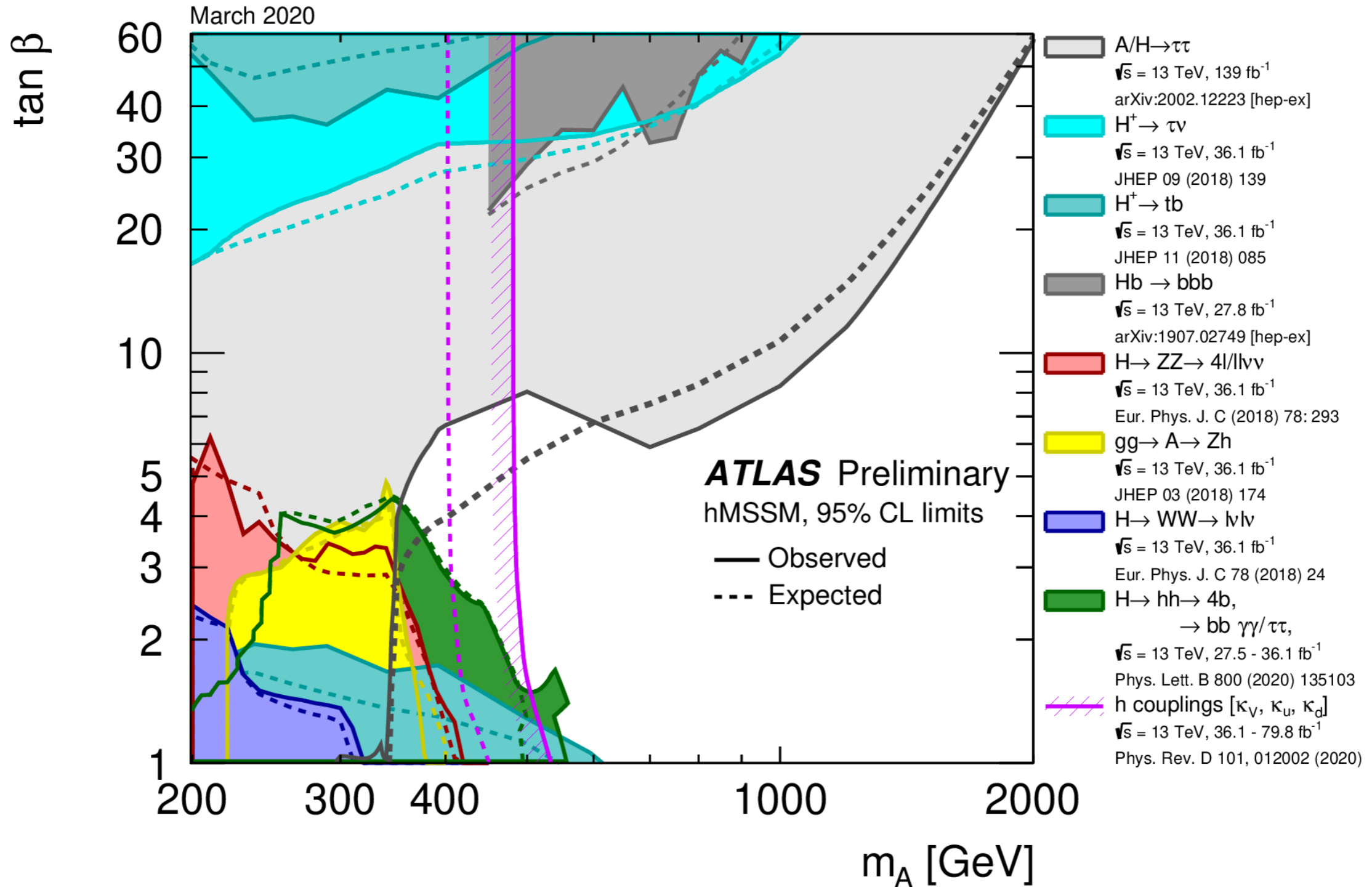
[Gu, Li, Liu, Su, Su 1709.06103]



See also: [Chen, Han, Su, Su, Wu '18, ibid + Li '19]

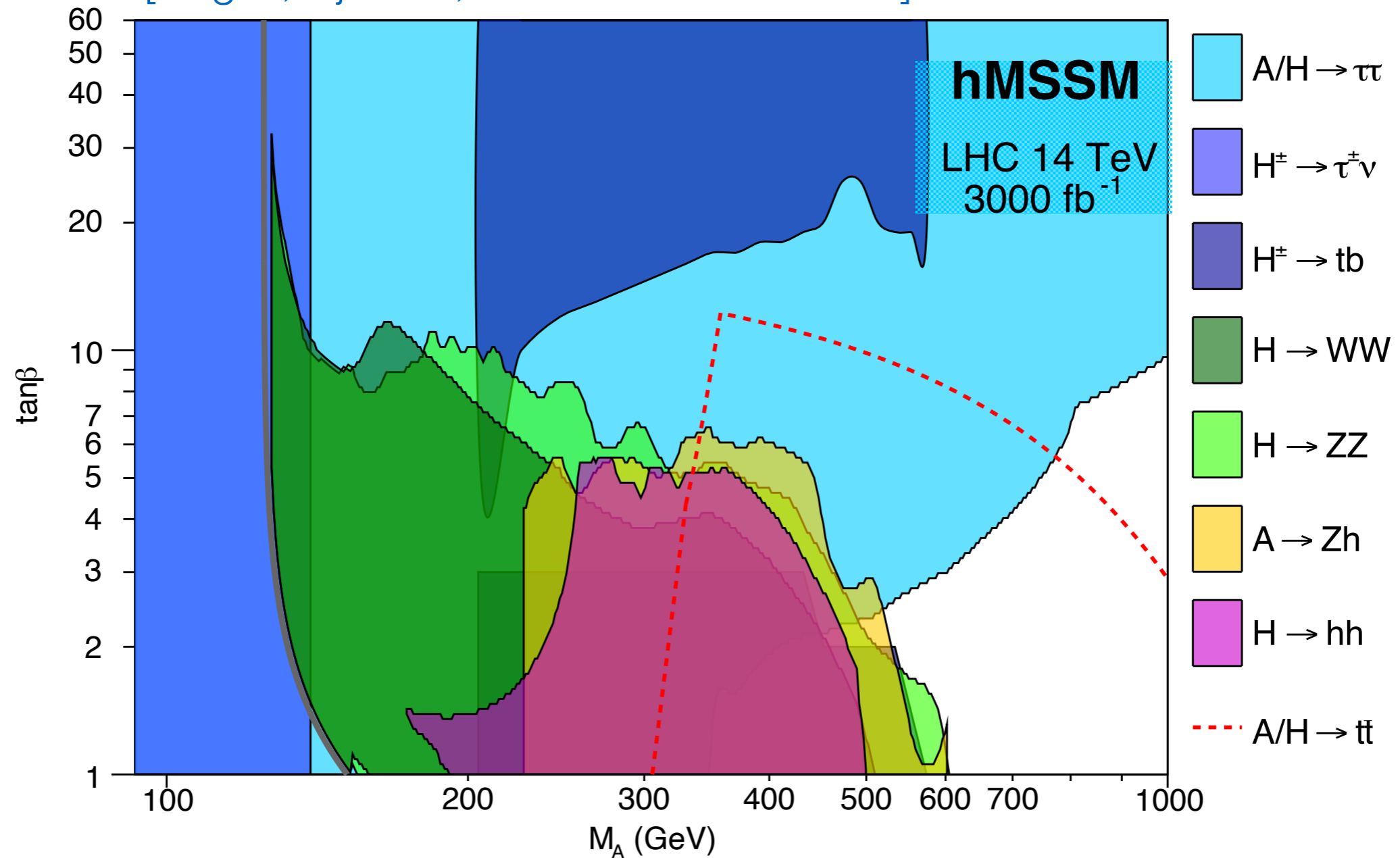
# Direct: Where now?

*hMSSM for illustration*



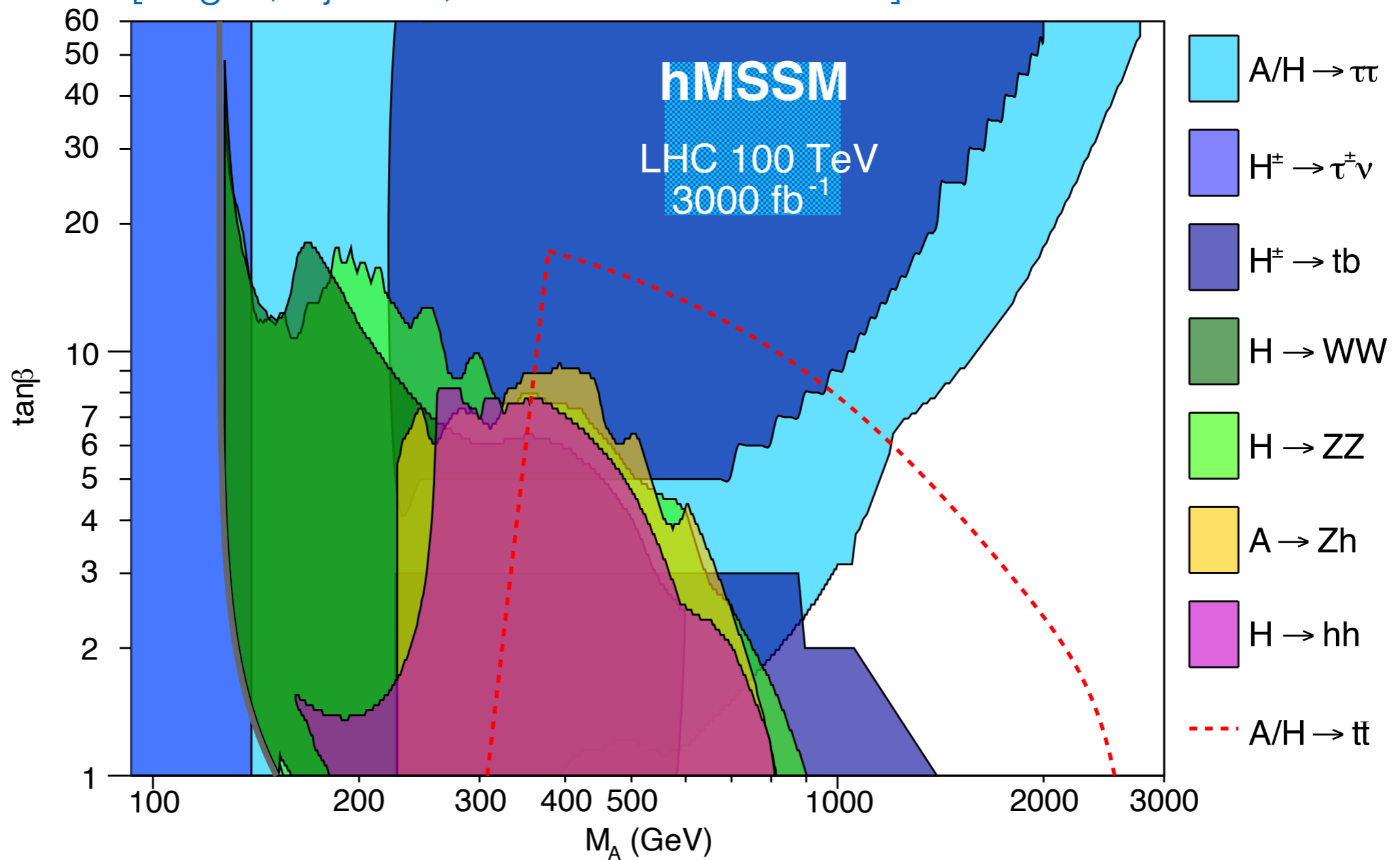
# Direct: Whither?

[Baglio, Djouadi, Quevillon 1511.07853]

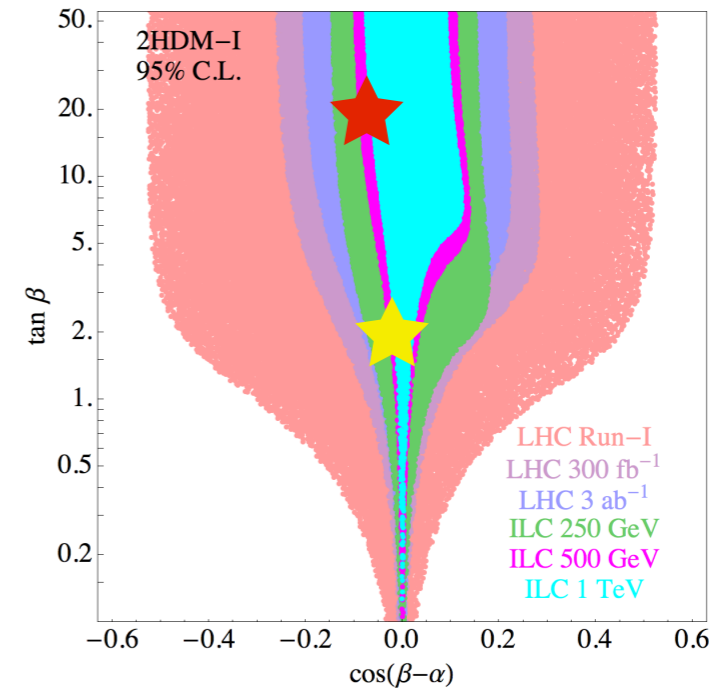


# Direct: Whither?

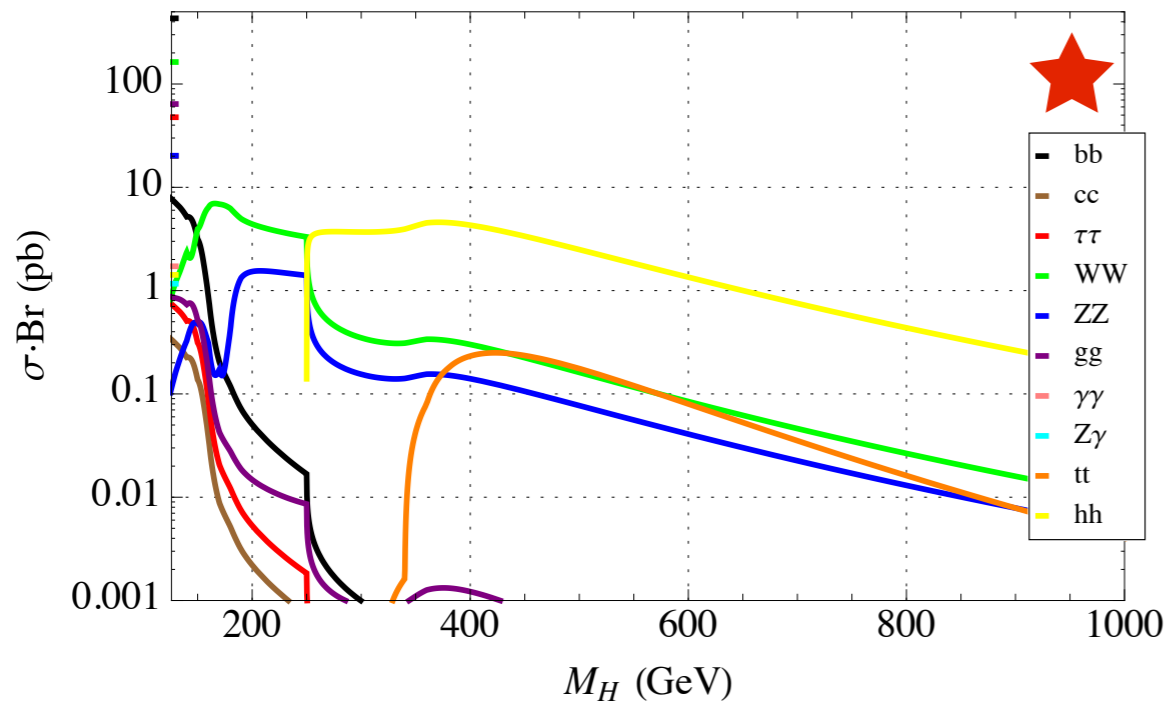
[Baglio, Djouadi, Quevillon 1511.07853]



# Where's the signal?

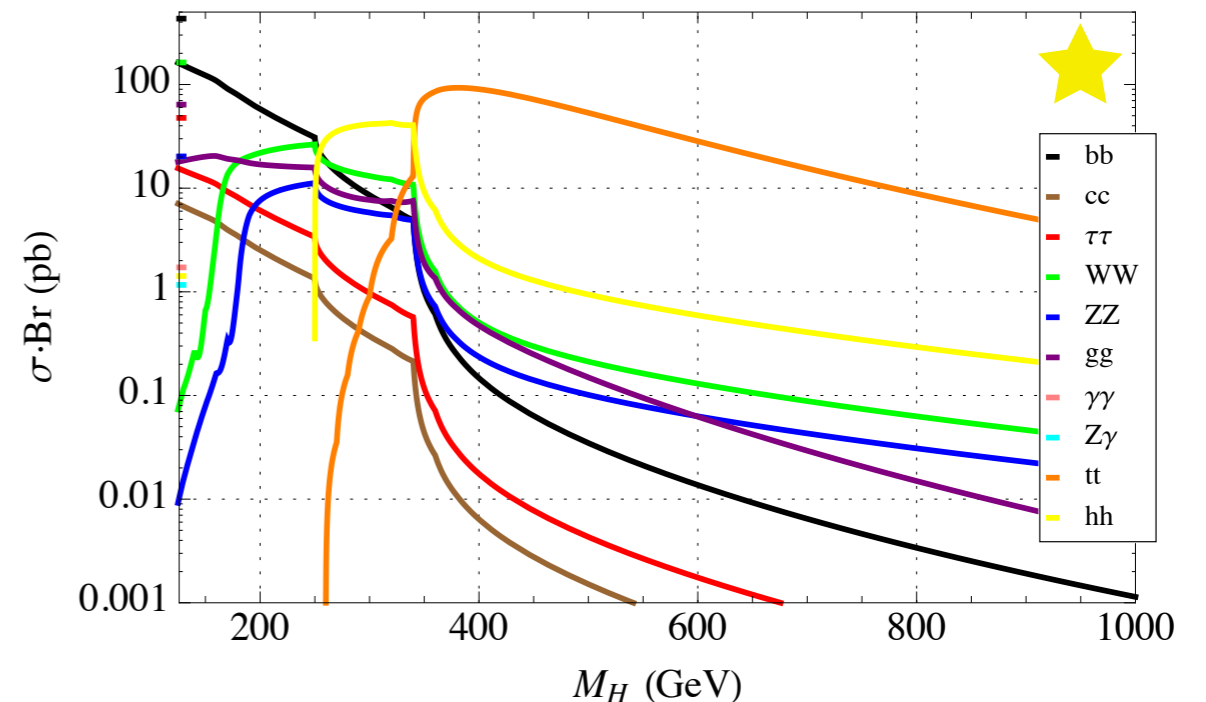


TYPE 1:  $\sigma \cdot \text{Br}(gg \rightarrow H \rightarrow X), \sqrt{s} = 100 \text{ TeV}, \tan\beta = 20, \cos(\beta - \alpha) = -0.07$



High  $\tan\beta$  dominated by  $hh, Zh, VV, tt$

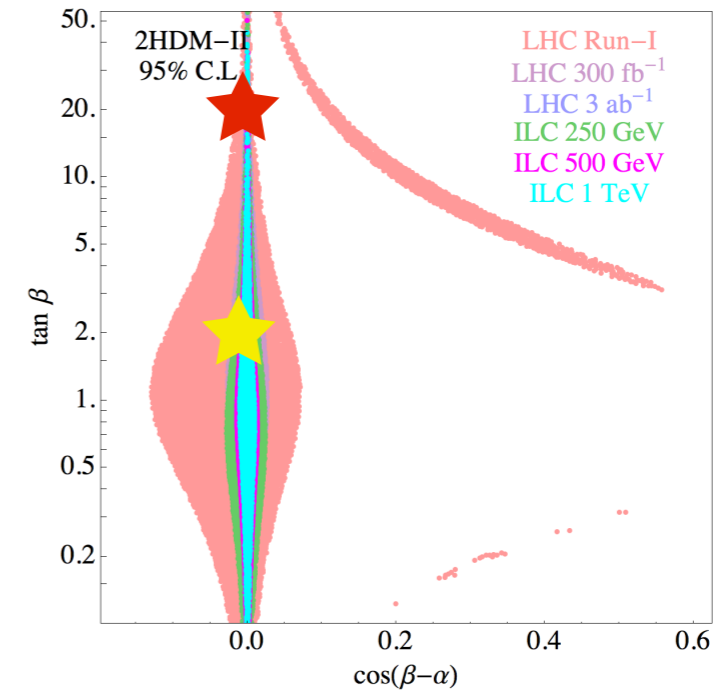
TYPE 1:  $\sigma \cdot \text{Br}(gg \rightarrow H \rightarrow X), \sqrt{s} = 100 \text{ TeV}, \tan\beta = 2, \cos(\beta - \alpha) = -0.02$



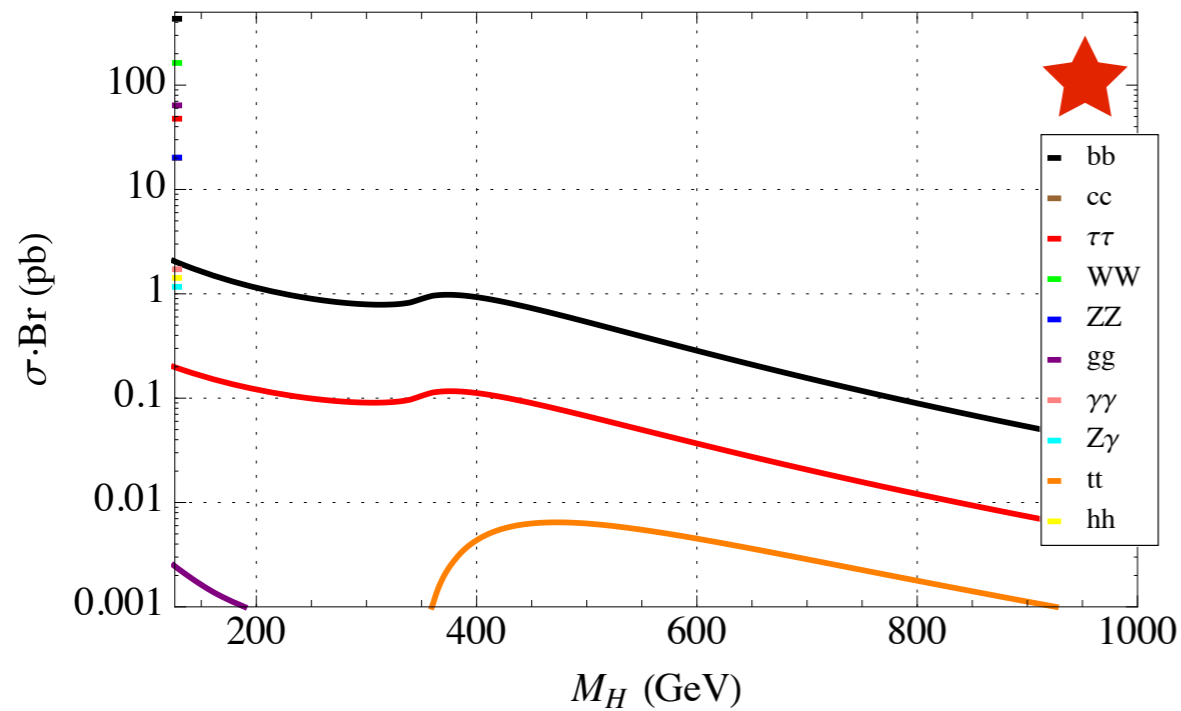
Low  $\tan\beta$  dominated by  $tt, hh, Zh$ , still some distance from alignment



# Where's the signal?

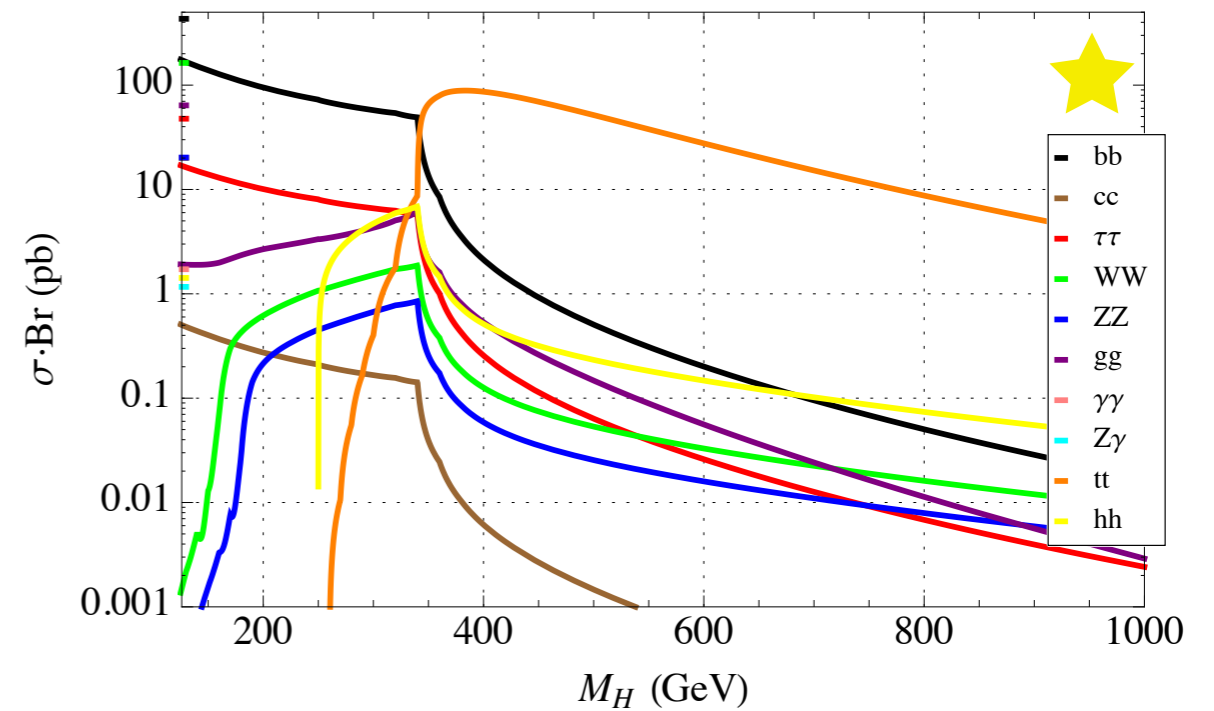


TYPE 2:  $\sigma \cdot \text{Br}(gg \rightarrow H \rightarrow X), \sqrt{s} = 100 \text{ TeV}, \tan\beta = 20, \cos(\beta - \alpha) = -0.005$



High  $\tan\beta$  dominated by  $bb, \tau\tau$ , as expected from MSSM

TYPE 2:  $\sigma \cdot \text{Br}(gg \rightarrow H \rightarrow X), \sqrt{s} = 100 \text{ TeV}, \tan\beta = 2, \cos(\beta - \alpha) = -0.01$



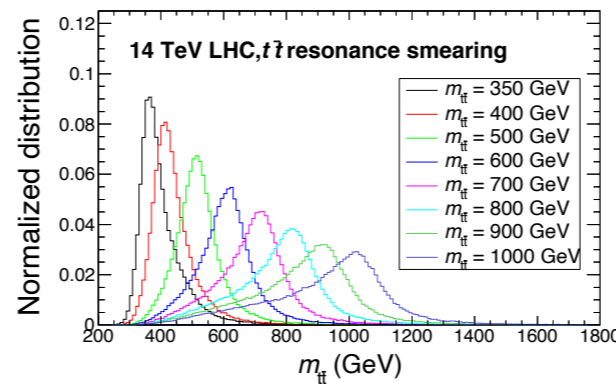
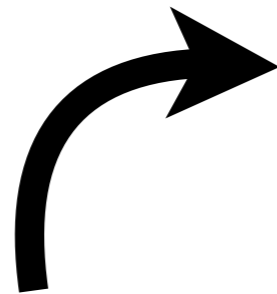
Low  $\tan\beta$  dominated by  $tt, bb$ ; vectors suppressed by alignment

# What's the problem?

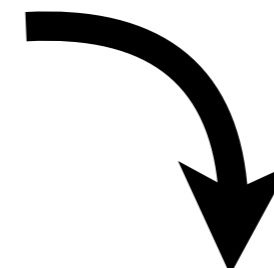
[Gaemers, Hoogeveen '84;  
Dicus, Stange, Willenbrock  
'94; Barger, Han, Walker '06;  
NC, F. D'Eramo, P. Draper, S.  
Thomas, H. Zhang '15; Gori,  
Kim, Shah, Zurek '16; Hespel,  
Maltoni, Vryonidou '16;  
Czakon, Heymes, Mitov '16,...]

*Spin-0 resonance decaying to  $t\bar{t}$  interferes w/ SM  $t\bar{t}$*

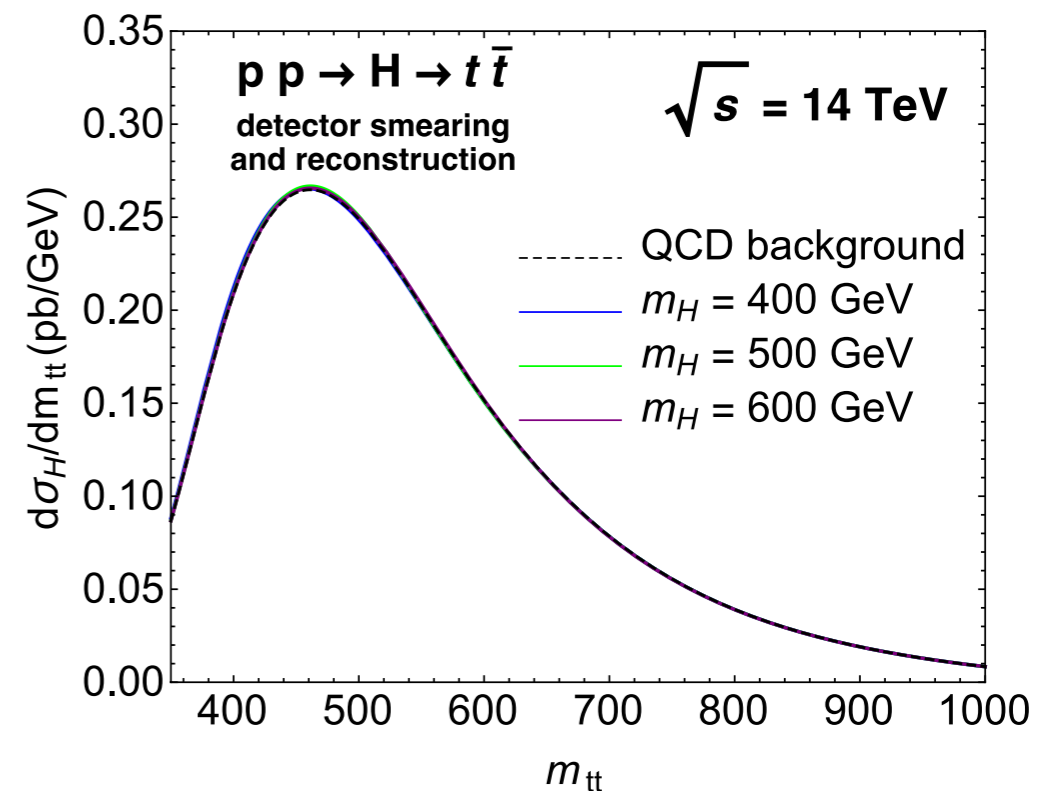
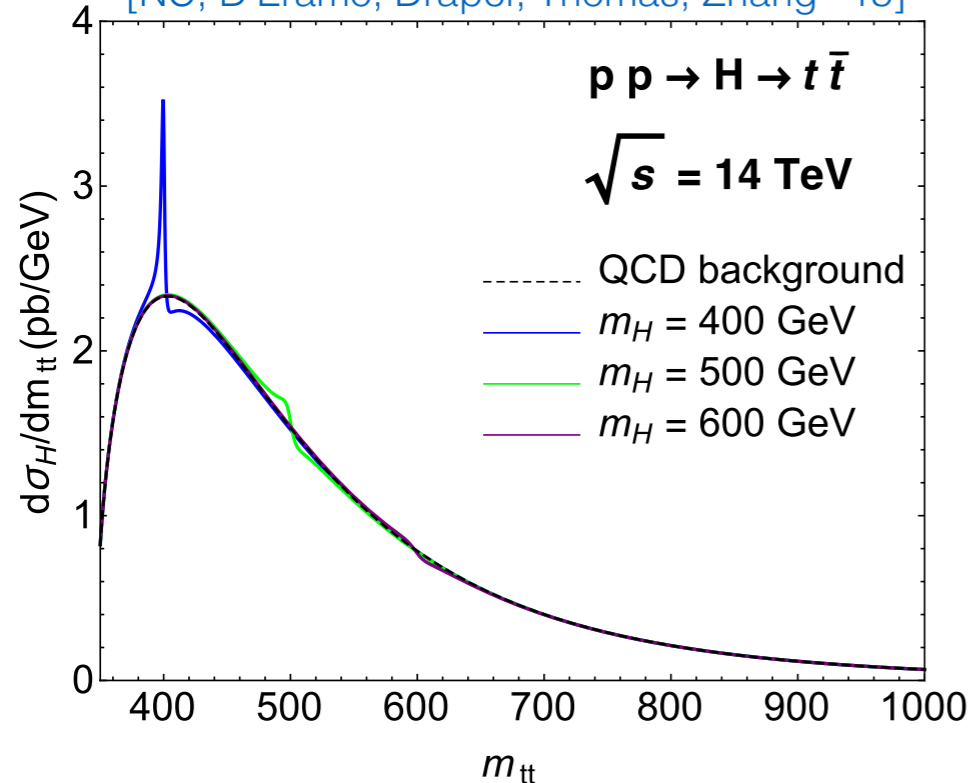
Not fatal  
in itself



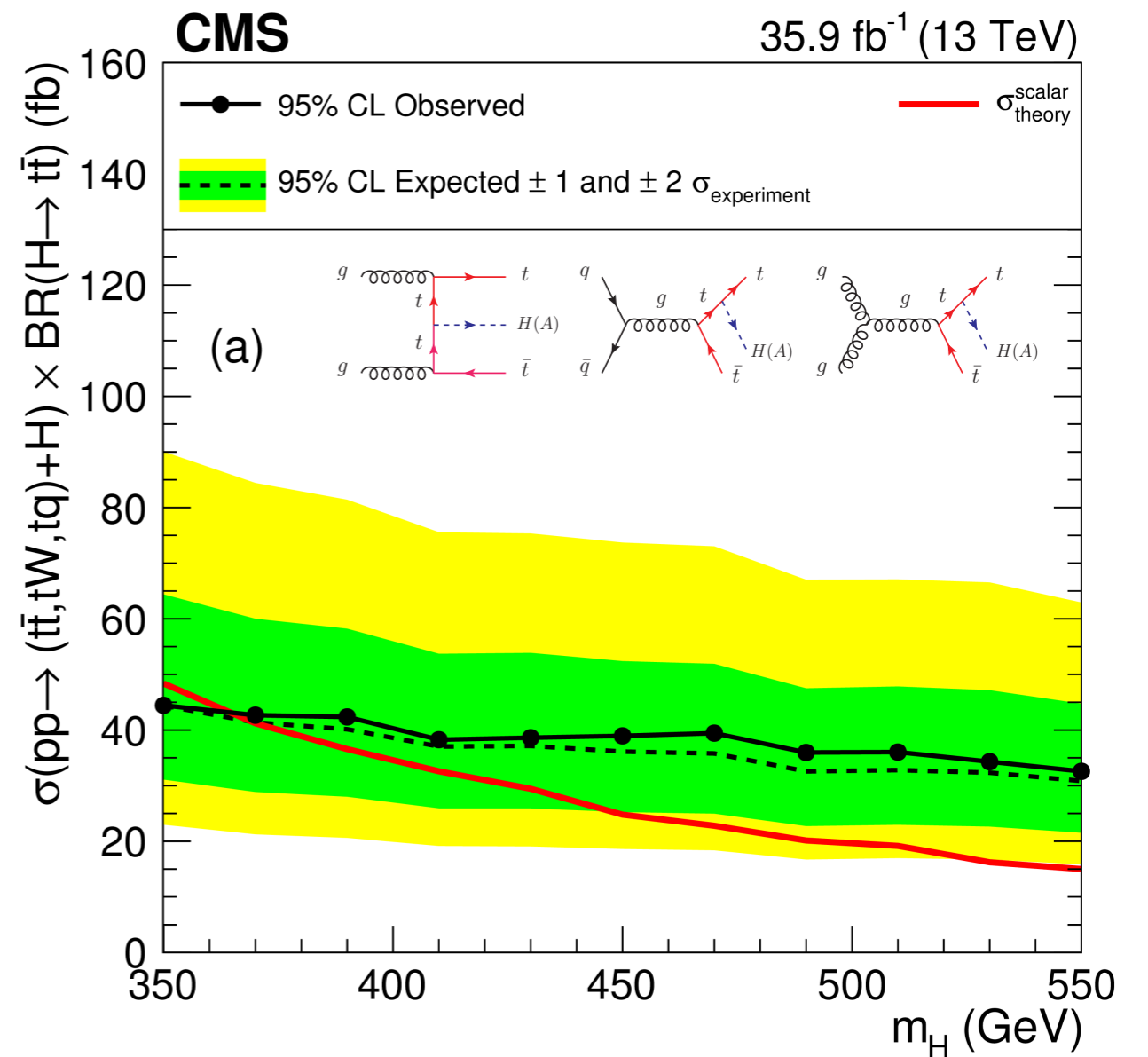
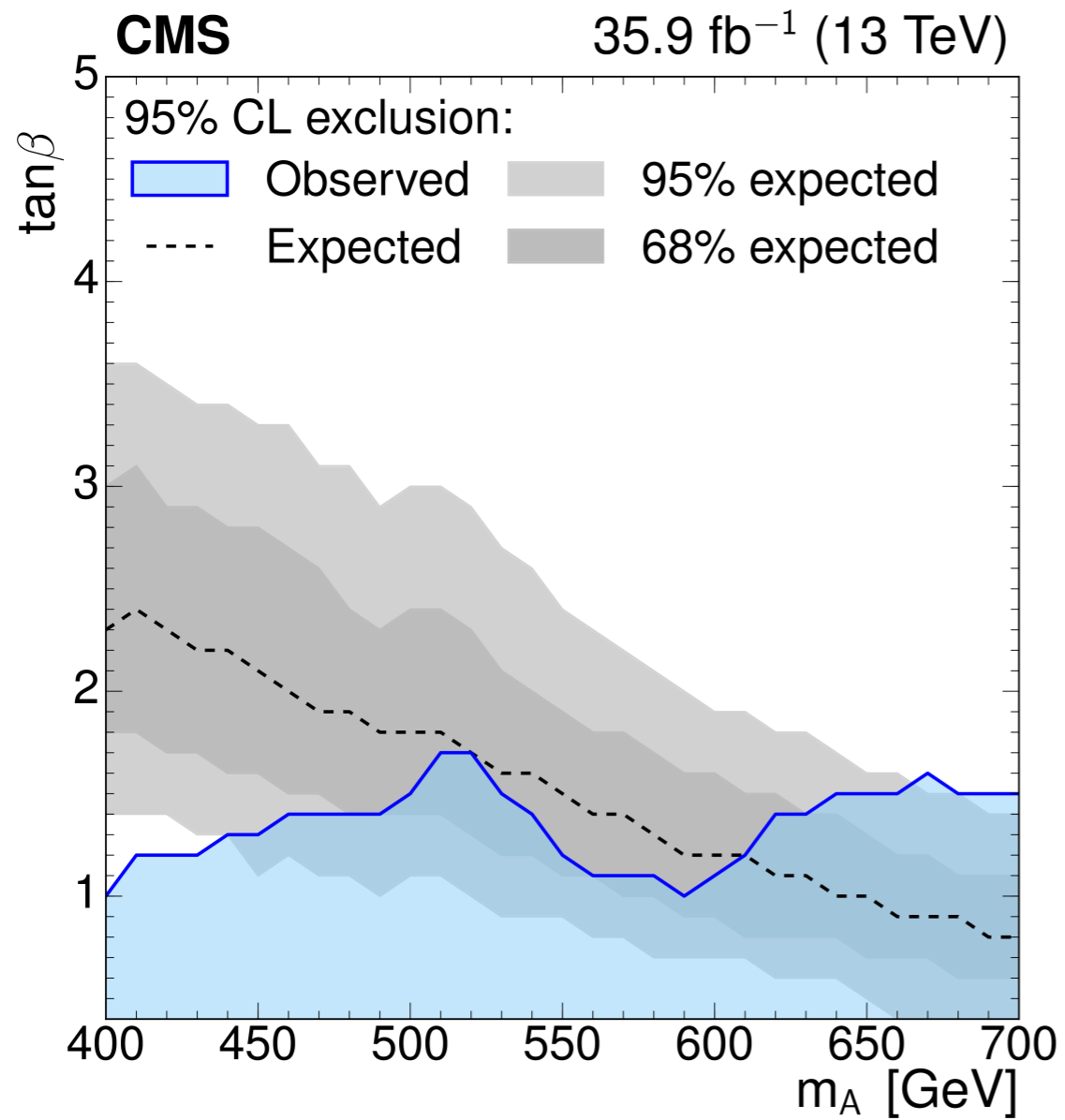
But made  
challenging by  
resolution



[NC, D'Eramo, Draper, Thomas, Zhang '15]

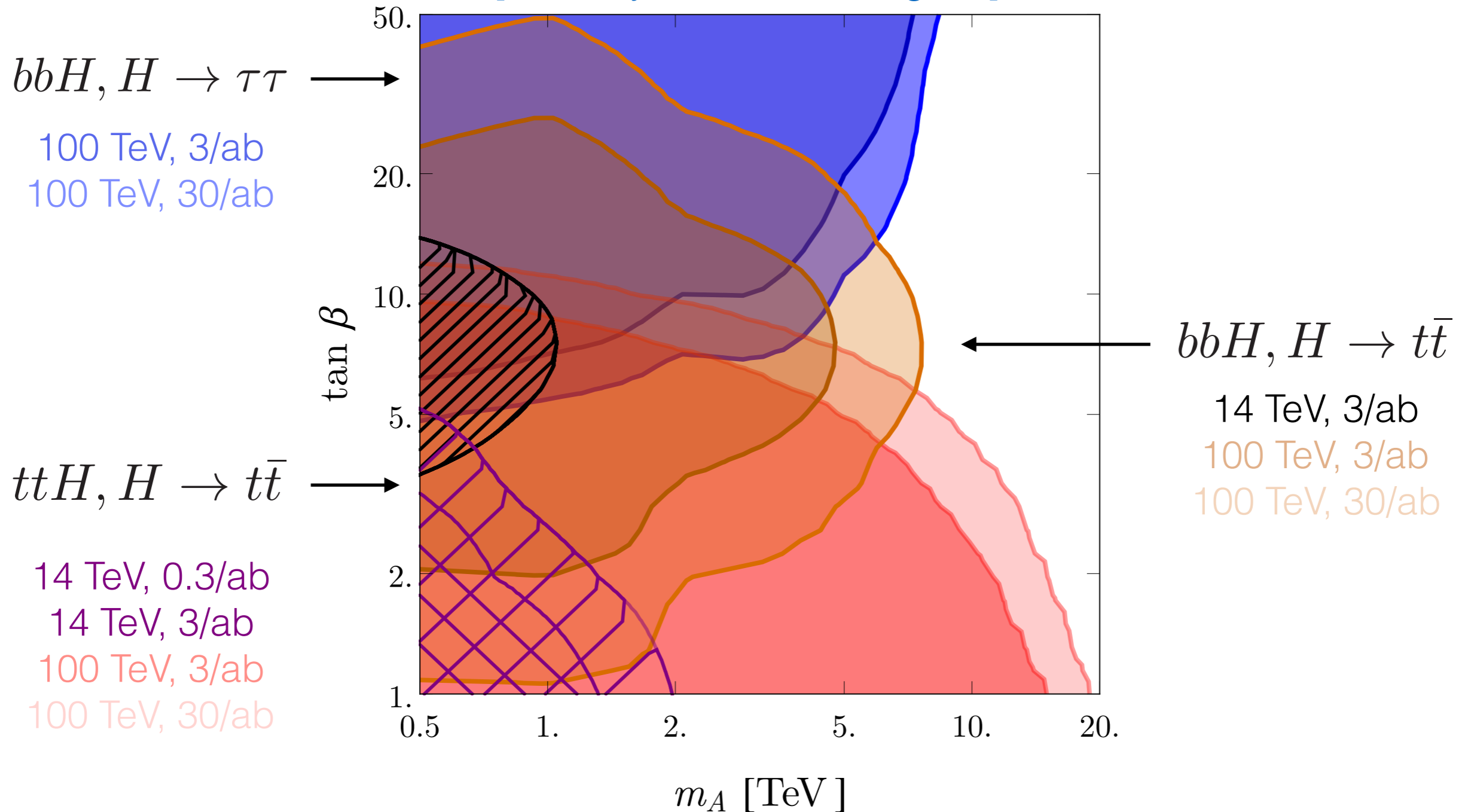


# What's being done?



# Where to go?

[NC, Hajer, Li, Liu, Zhang '16]



# More generally

Production channels (for 2HDM) in the alignment limit

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Single Heavy Higgs  
Strong Production

$$\mathcal{O}(g_s^4 \lambda_f^2)$$

$$gg \rightarrow H, A$$

Single Heavy Higgs  
Associated Strong Production

$$\mathcal{O}(g_s^4 \lambda_f^2)$$

$$gg \rightarrow bbH, bbA, tbH^\pm, ttH, ttA$$

Single Heavy Higgs  
Associated Weak Production

$$\mathcal{O}(g_s^2 g_w^4 \lambda_f^2)$$

$$gq \rightarrow bq' bH^\pm, bq tH, bq tA$$

Double Heavy Higgs  
Weak Production

$$\mathcal{O}(g_w^4)$$

$$q\bar{q} \rightarrow HA, HH^\pm, AH^\pm, H^+H^-$$

Light + Heavy Higgs  
Strong Production

$$\mathcal{O}(g_s^4 \lambda_f^4)$$

$$gg \rightarrow hH, hA$$

Double Heavy Higgs  
Strong Production

$$\mathcal{O}(g_s^4 \lambda_f^4)$$

$$gg \rightarrow HH, HA, AA, H^+H^-$$

# Heavy Higgs Cascades

Distinctive single modes may have small production rates (e.g.  $H_{\pm}$ )

Dominant single modes may be hard to see (e.g.  $gg \rightarrow H/A \rightarrow tt$ )

Multi-mode cascades provide an opportunity (e.g.  $gg \rightarrow H \rightarrow WH_{\pm}$ )

Organizing principle:  
*alignment limit.*

Many multi-Higgs couplings vanish in this limit; focus on non-vanishing couplings

Multi-Higgs Couplings in the alignment limit:

- $hHH$
- $hAA$
- $HHH$
- $HAA$  ←
- $HH^+H^-$  ←
- $ZAH$  ←
- $HW^{\pm}H^{\mp}$  ←
- $AW^{\pm}H^{\mp}$  ←

# Snowmass 2021

- 2HDM are a key benchmark for future colliders, Snowmass!
- Continue exploring indirect constraints on 2HDM from Higgs factories using state-of-the-art coupling projections.
- Significant room to improve forecasting for sensitivity to  $tt$  final states at pp machines, both in  $ggH$  and  $ttH$ .
- Significant opportunities in other associated production modes, Higgs cascades.
- Challenges for pp machines largely avoided by high center-of-mass lepton colliders. Muon collider, anyone?

**Thank you!**