Testing neutrino mass generation mechanism at the e^-e^+ collider

Arindam Das
Osaka University

7th July 2020, Snowmass Joint BSM Session

Introduction

Standard Model

very stable

1. Neutrino mass and flavor mixing
2. Dark Matter candidate
3. May be more

New physics is strongly suggested

Theoretical

Experimental

We definitely need new physics to provide missing pieces

Particle content of the model

	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$			$U(1)_X$
q_L^i	**3**	**2**	$+1/6$	x_q	$=$	$\frac{1}{6}x_H + \frac{1}{3}x_\Phi$
u_R^i	**3**	**1**	$+2/3$	x_u	$=$	$\frac{2}{3}x_H + \frac{1}{3}x_\Phi$
d_R^i	**3**	**1**	$-1/3$	x_d	$=$	$-\frac{1}{3}x_H + \frac{1}{3}x_\Phi$
ℓ_L^i	**1**	**2**	$-1/2$	x_ℓ	$=$	$-\frac{1}{2}x_H - x_\Phi$
e_R^i	**1**	**1**	-1	x_e	$=$	$-x_H - x_\Phi$
H	**1**	**2**	$+1/2$	x'_H	$=$	$\frac{1}{2}x_H$
N_R^i	**1**	**1**	0	x_ν	$=$	$-x_\Phi$
Φ	**1**	**1**	0	x'_Φ	$=$	$2x_\Phi$

$$m_{Z'} = 2\, g_X v_\Phi$$

x_H, x_Φ will appear the coupling with Z'

3 generations of SM singlet right handed neutrinos (anomaly free)

Charges before the anomaly cancellations

Charges after Imposing the anomaly cancellations

$U(1)_X$ breaking

$$\mathcal{L}_Y \supset -\sum_{i,j=1}^{3} Y_D^{ij}\overline{\ell_L^i} H N_R^j - \frac{1}{2}\sum_{i=k}^{3} Y_N^k \Phi \overline{N_R^{k\,c}} N_R^k + \text{h.c.},$$

$$m_D^{ij} = \frac{Y_D^{ij}}{\sqrt{2}} v_h$$

$$m_{N^i} = \frac{Y_N^i}{\sqrt{2}} v_\Phi$$

$$m_\nu = \begin{pmatrix} 0 & M_D \\ M_D^T & M_N \end{pmatrix} \qquad m_\nu \simeq -M_D M_N^{-1} M_D^T$$

Seesaw mechnism

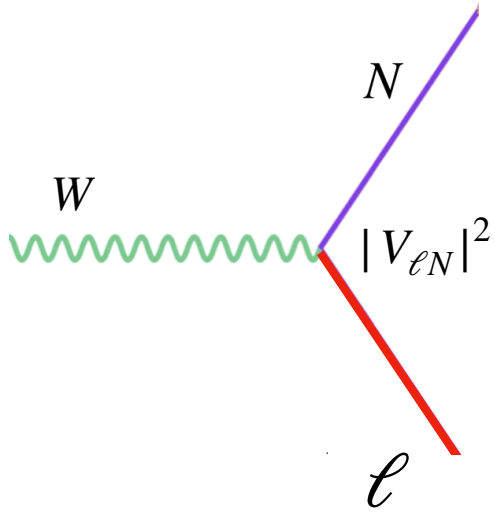
Direct interaction of the Right Handed Neutrinos through light – heavy mixing

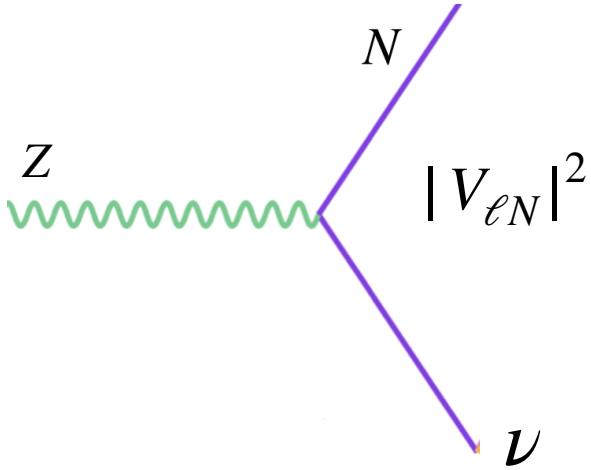
Flavor eigenstate can be expressed in terms of the mass eigenstate

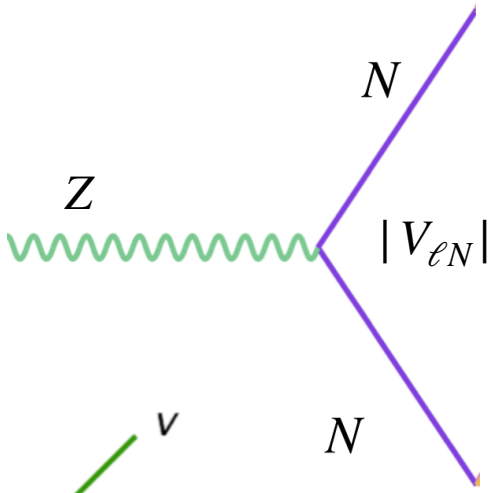
$$\nu_\ell \simeq U_{\ell m}\nu_m + V_{\ell n}N_n$$

PMNS matrix

$M_D M^{-1}$

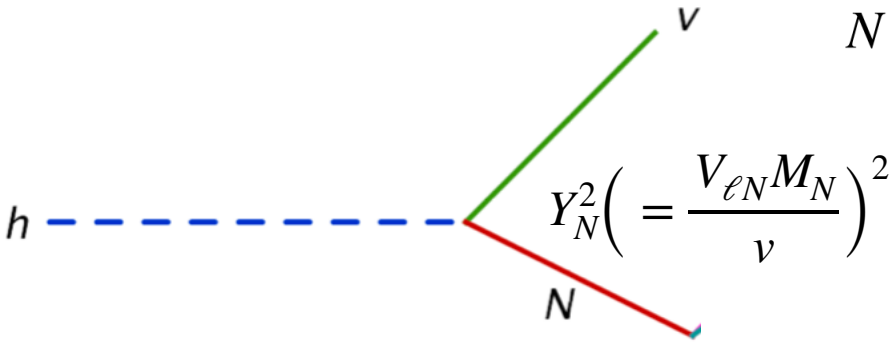


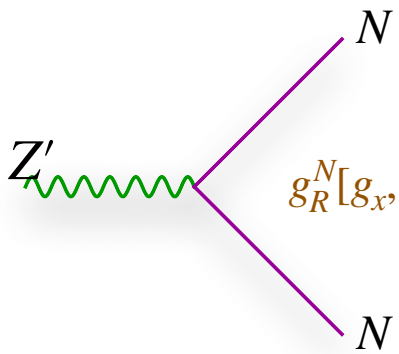




Suppressed

Direct interaction of the RHNs





$$g_R^N[g_x, x_H] = \left(0\ x_H + (-1)\right)g_x$$

Heavy neutrino search strategies

We focus only on the processes related to the e^-e^+ collider

with SM sector

through the light−heavy mixings

Past works(LHC/ Future collider)

1207.3734	1405.0177	1510.04790
1604.00608	1702.04668	1709.09712
1801.00797	1704.00880	1704.00881

W, Z, H

Direct Search strategy

Ongoing(LHC/FCC)

visible final sates

Multi − lepton/ multi − jet

Prompt/ boosted/ displaced

Limits mass − mixing plane

with BSM sector

Z', BSM Higgs

Past works(LHC)

1710.03377	1711.09896
1906.04132	1908.09838

Pair procuction

Ongoing(LHC/FCC)

Prompt/ boosted/ displaced

Limits mass − mixing plane

mass reconstruction :

BSM gauge boson search

Impression/s at the ILC

$$\sigma(e^+e^- \to \overline{\nu_\alpha} N_i) = \sigma_{\rm ILC} |\mathcal{R}_{\alpha i}(\delta, \rho, y)|^2$$

1207.3734

Using the general parameters and Casas – Ibarra conjecture

$|\mathcal{R}_{\alpha i}(\delta, \rho, y)|^2$

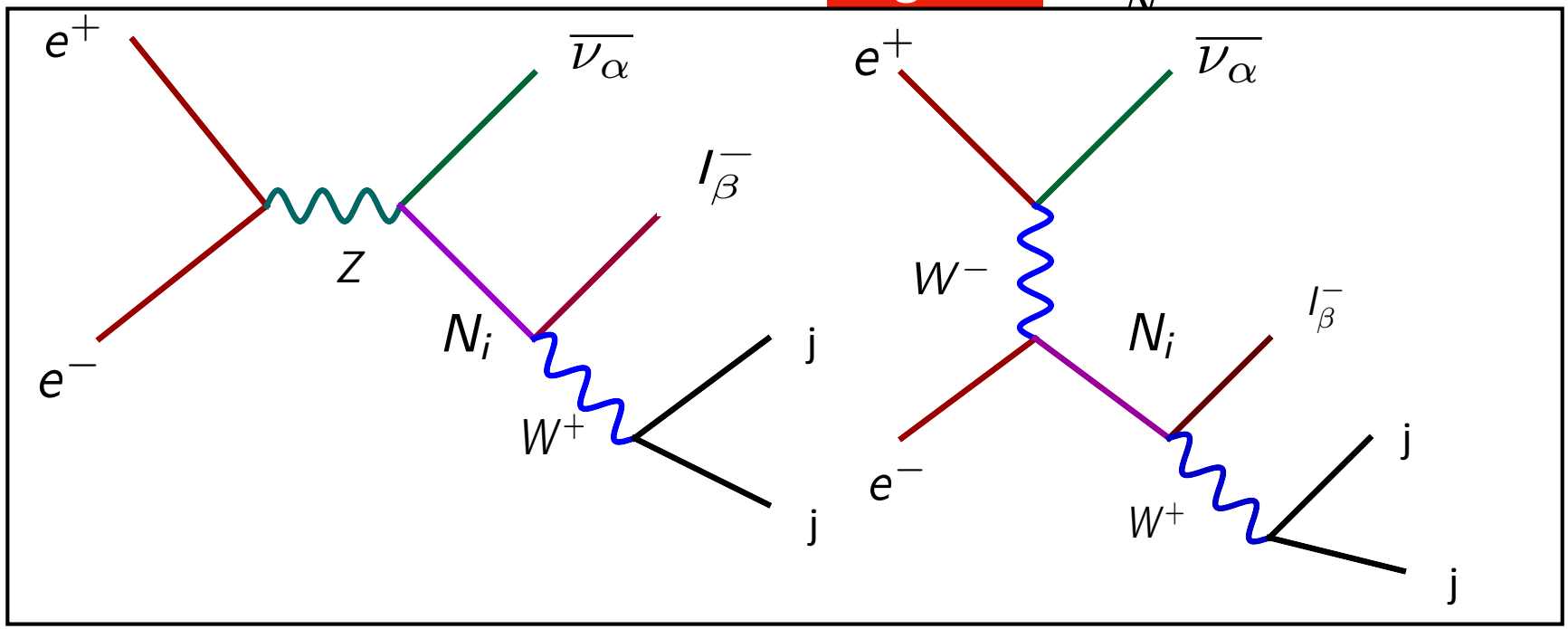
branching ratios

$$N_i \to \ell_\alpha^- W^+ / \nu_\alpha Z / \nu_\alpha h$$

$\mathcal{N}^\dagger \mathcal{R} \simeq U_{\rm MNS}^\dagger \mathcal{R}$ because $|\epsilon_{\alpha\beta}| \ll 1$

Leading mode

Signals $M_N = 150$ GeV

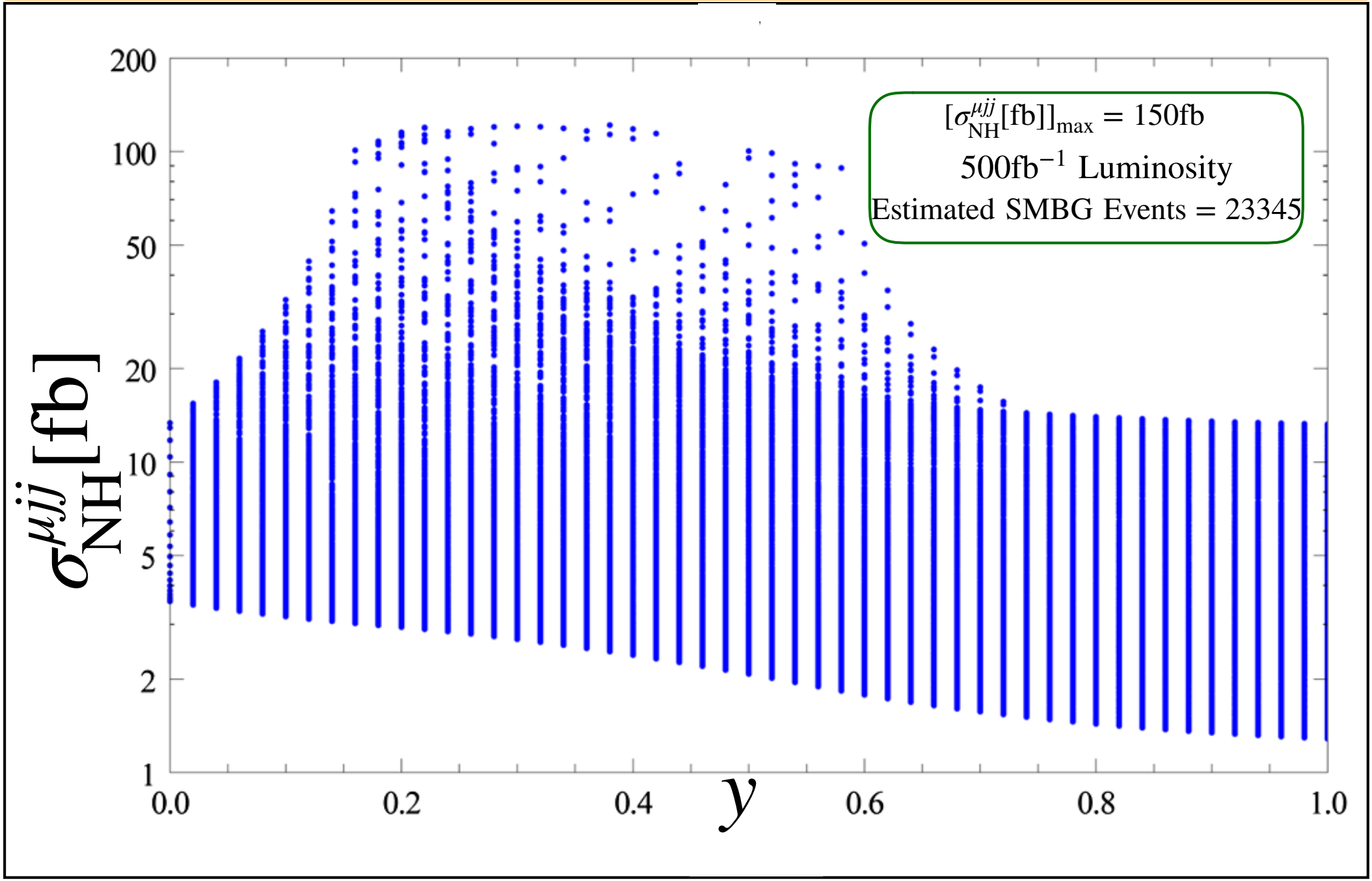


We scan over the phases and then general parameter to find the cross section as a function of the general parameter 'y', $-\pi < \delta, \rho < \pi, \;\; 0 < y < 1$

$e^+e^- \to \nu N$, followed by the decay $N \to \ell W$ ($\ell = \mu$) $W \to q\bar{q}'$

$M_N = 150$ GeV $\sqrt{s} = 500$ GeV

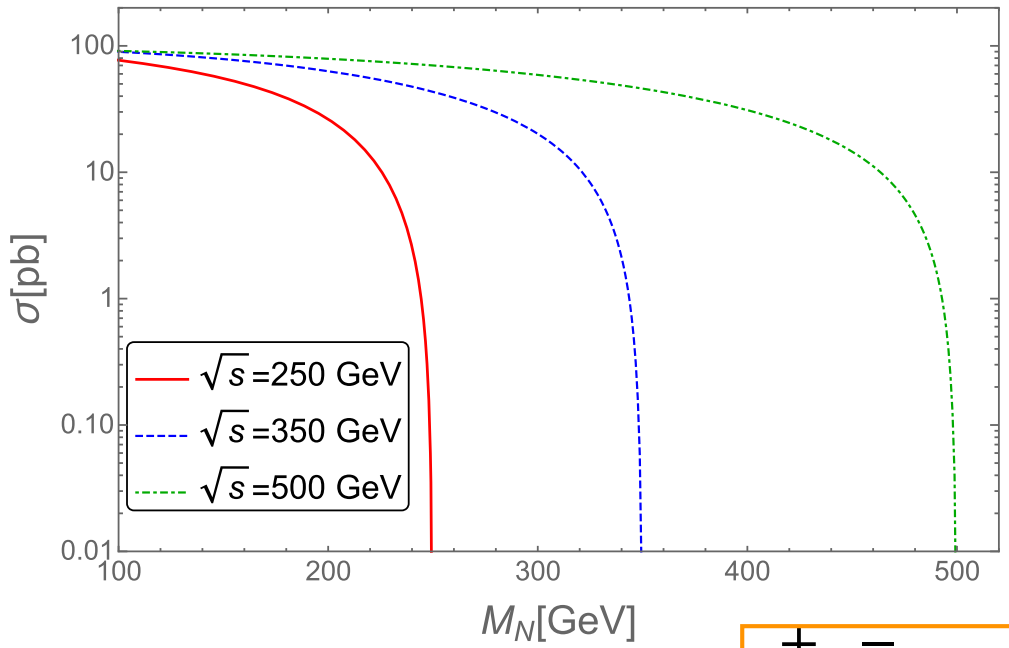
1207.3734

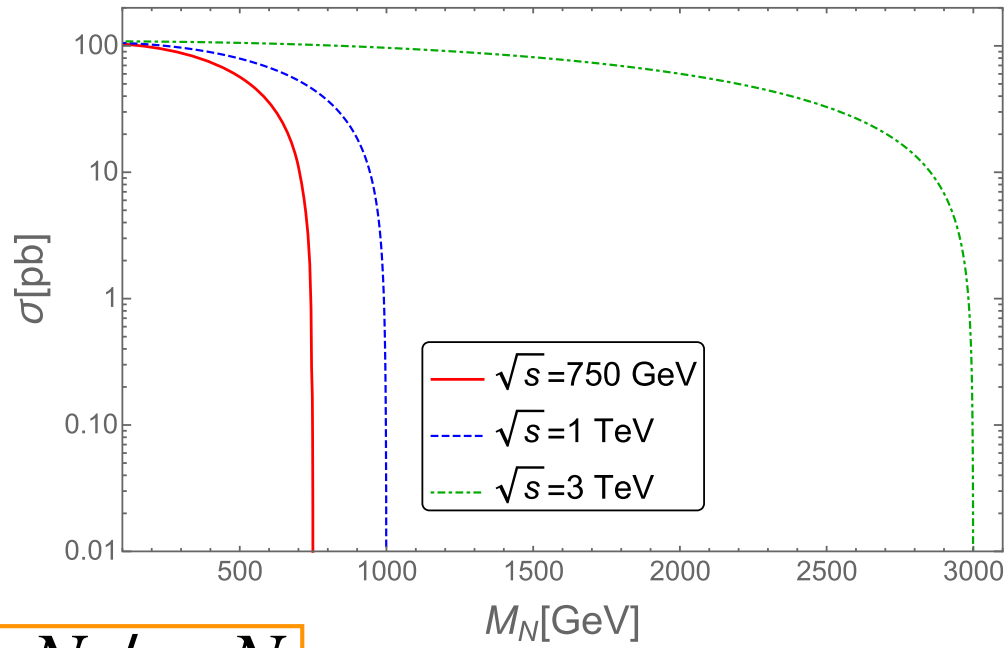


Production of the heavy neutrinos at the Linear Collider using fat jet

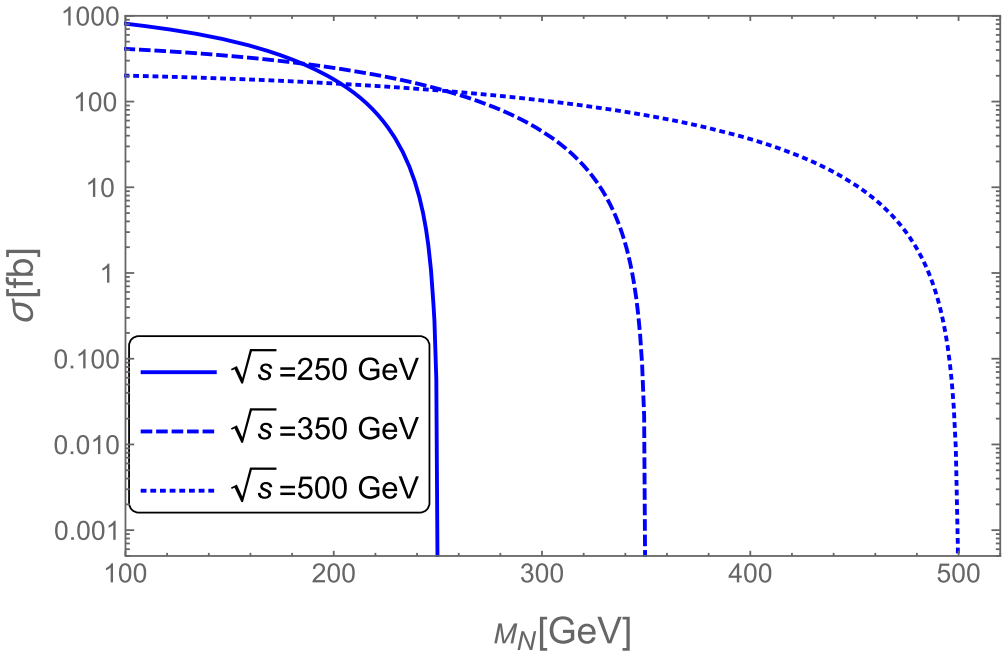
1811.04291

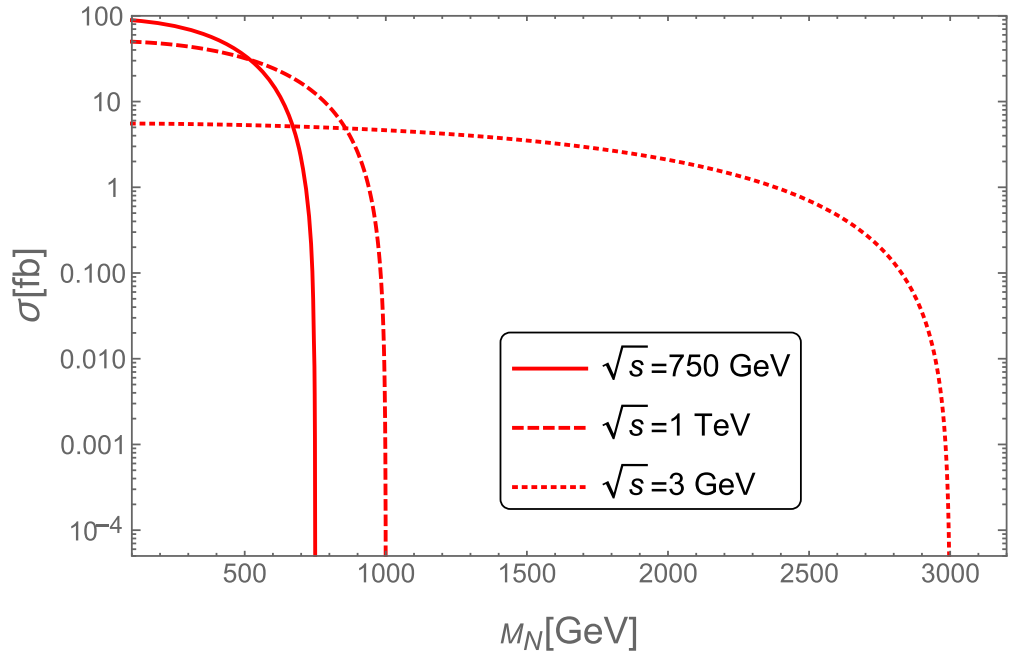
$$e^+e^- \to \nu_1 N_1$$





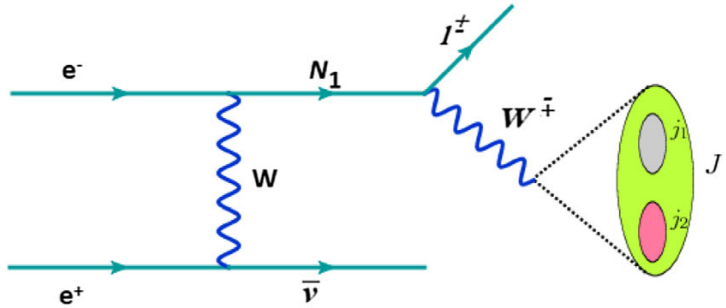
$$e^+e^- \to \nu_2 N_2 / \nu_3 N_3$$



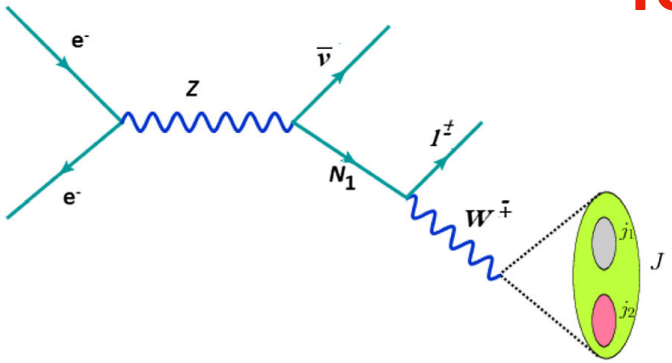


$e + J + p_T^{\text{miss}}$ final states at the linear colliders.

1811.04291



$R = 0.8$



$R = 0.8$

- Transverse momentum for fat-jet $p_T^J > 150$ GeV for M_N mass range 400 GeV-600 GeV and $p_T^J > 250$ GeV for M_N mass range 700 GeV-900 GeV.
- Transverse momentum for leading lepton $p_T^{e^\pm} > 100$ GeV for M_N mass range 400 GeV-600 GeV and $p_T^{e^\pm} > 200$ GeV for M_N mass range 700 GeV-900 GeV.
- Polar angle of lepton and fat-jet $|\cos\theta_e| < 0.85$, $|\cos\theta_J| < 0.85$.
- Fat-jet mass $M_J > 70$ GeV.

1 TeV e^-e^+ collider

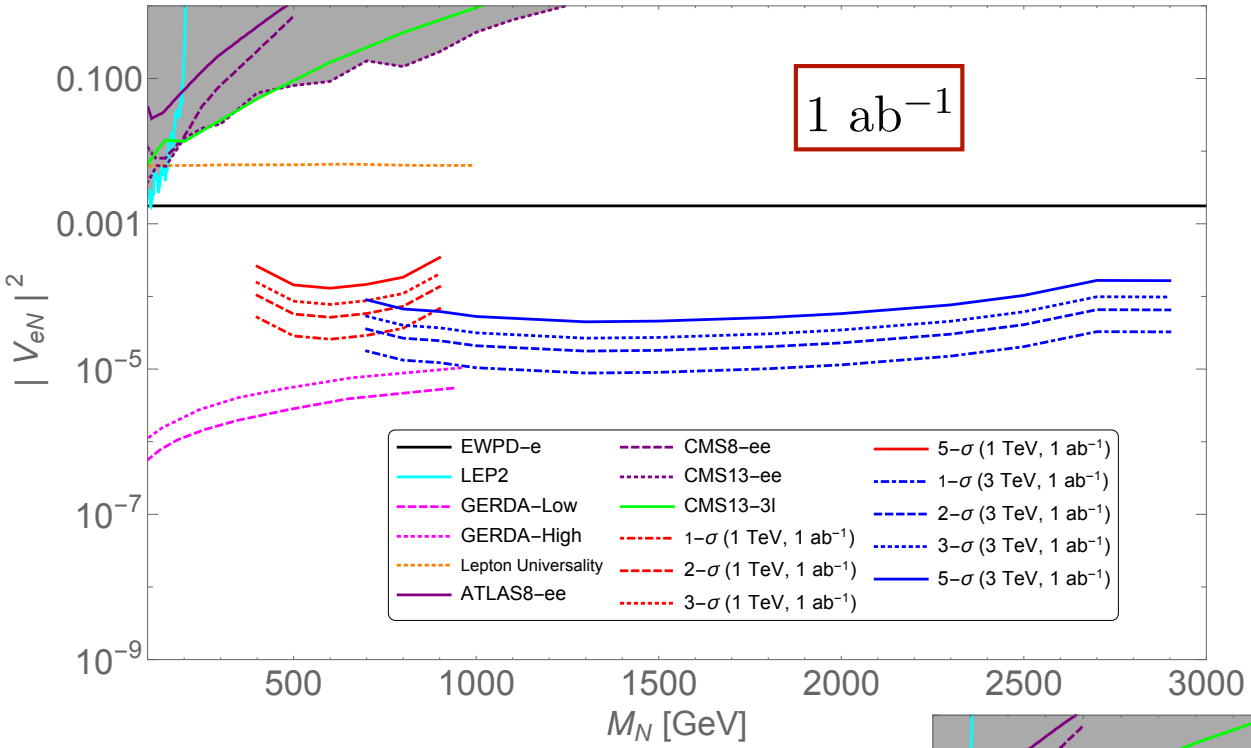
- Transverse momentum for fat-jet $p_T^J > 250$ GeV for the M_N mass range 700 GeV-900 GeV and $p_T^J > 400$ GeV for M_N mass range $1 - 2.9$ TeV.
- Transverse momentum for leading lepton $p_T^{e^\pm} > 200$ GeV for M_N mass range $700 - 900$ GeV and $p_T^{e^\pm} > 250$ GeV for M_N mass range $1 - 2.9$ TeV.
- Polar angle of lepton and fat-jet $|\cos\theta_e| < 0.85$, $|\cos\theta_J| < 0.85$.
- Fat-jet mass $M_J > 70$ GeV.

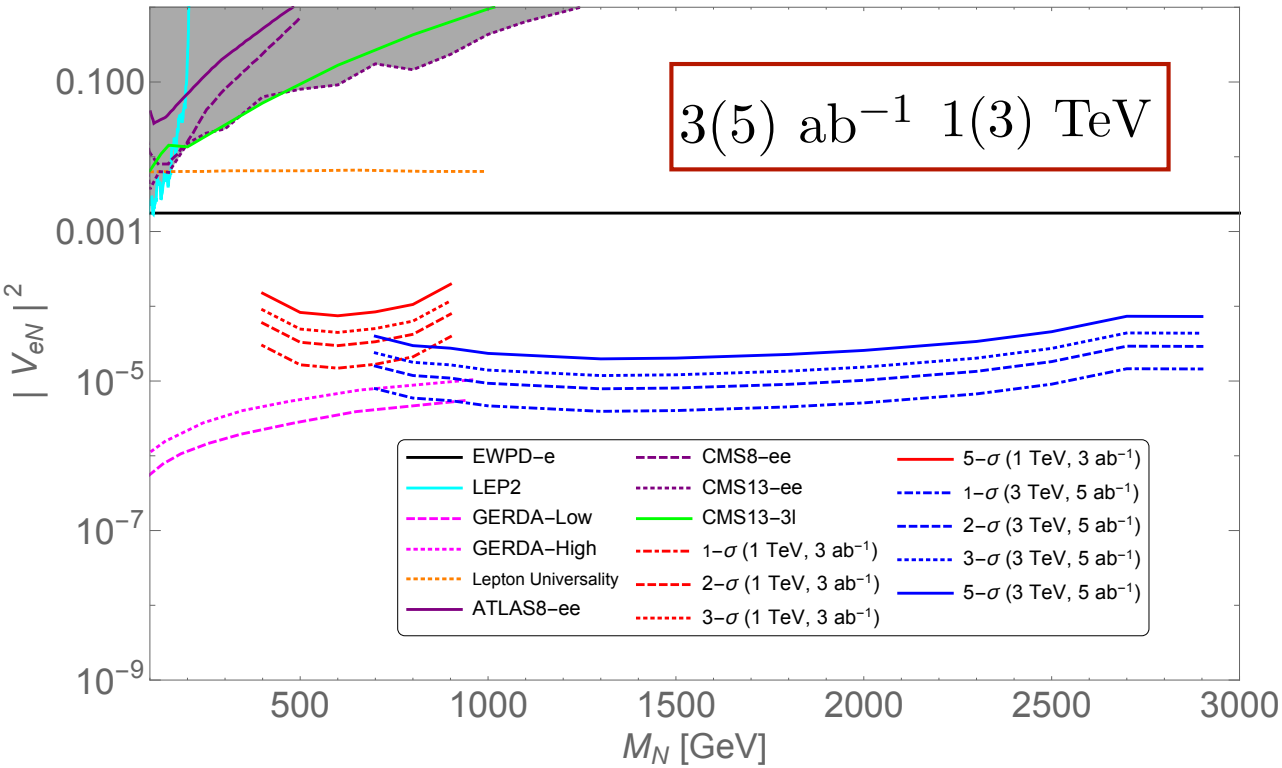
3 TeV e^-e^+ collider

Mass-mixing limit plots

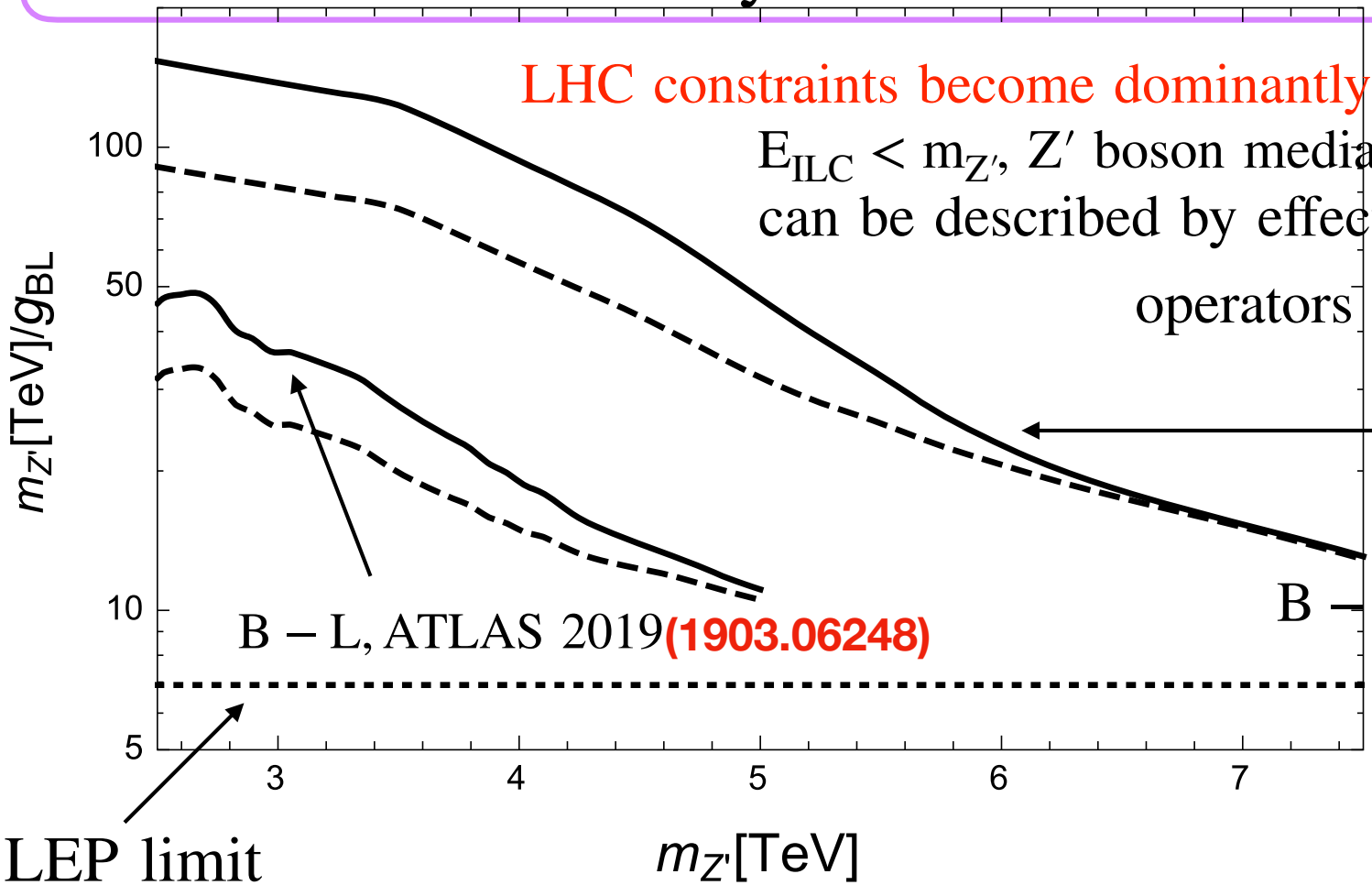
$\sqrt{s} =$ 1 TeV (red band) and 3 TeV (blue band)

1811.04291





Production of the heavy neutrino at the ILC 1812.11931



LHC constraints become dominantly weaker with heavier Z'

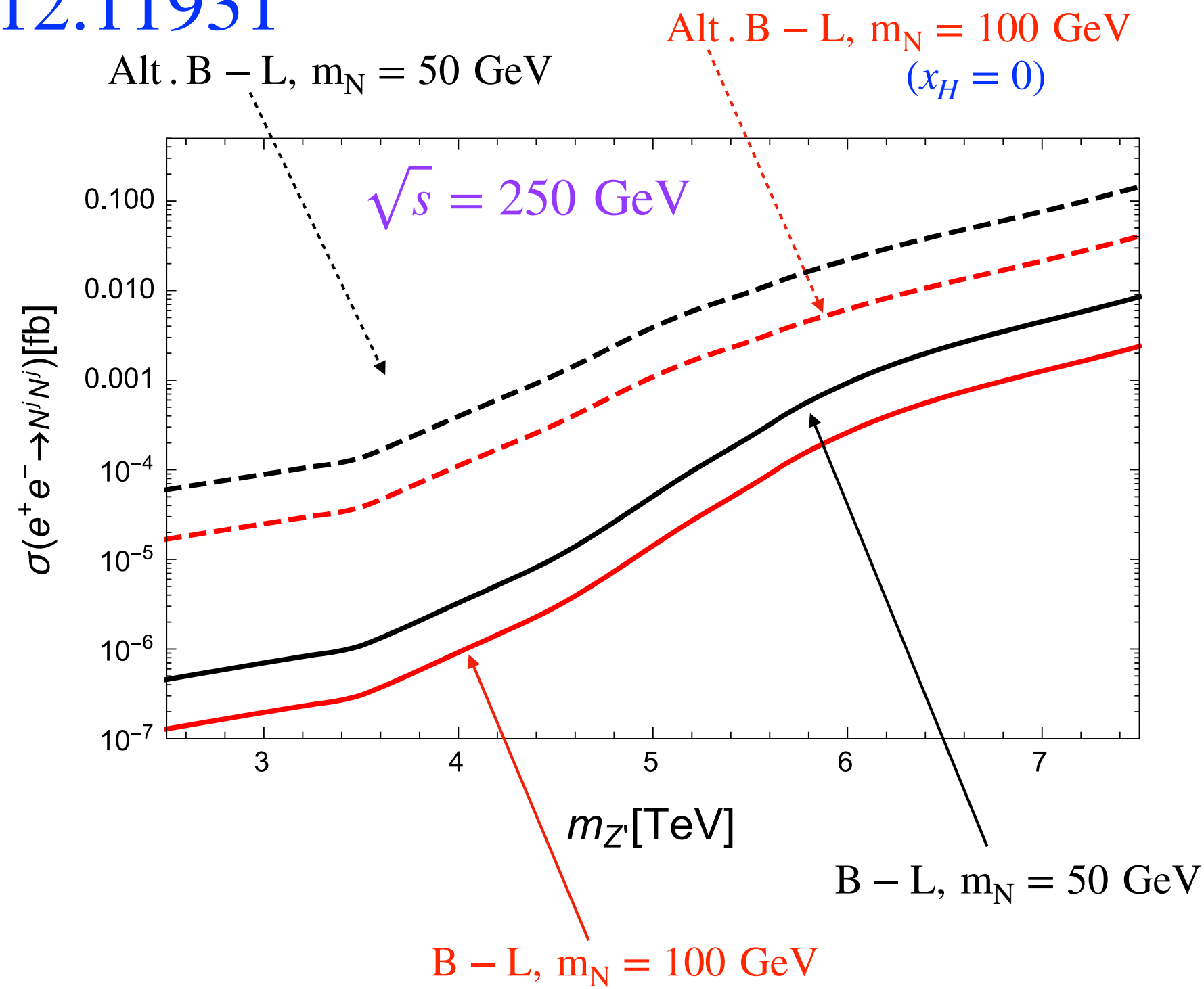
$E_{ILC} < m_{Z'}$, Z' boson mediated processes at the ILC can be described by effective higher dimensional operators $\propto \left(\frac{m_{Z'}}{g_{BL}}\right)^2$

Dashed lines represent the Atl. B – L case

$$\sigma(e^+e^- \to Z'^* \to N^i N^i) \simeq \frac{(Q_{N^i})^2}{24\pi} s \left(\frac{g_{BL}}{m_{Z'}}\right)^4 \left(1 - \frac{4m_{N^i}^2}{m_{Z'}^2}\right)^{\frac{3}{2}}.$$

As a result ILC is a powerful machine to probe Z' beyond HL – LHC

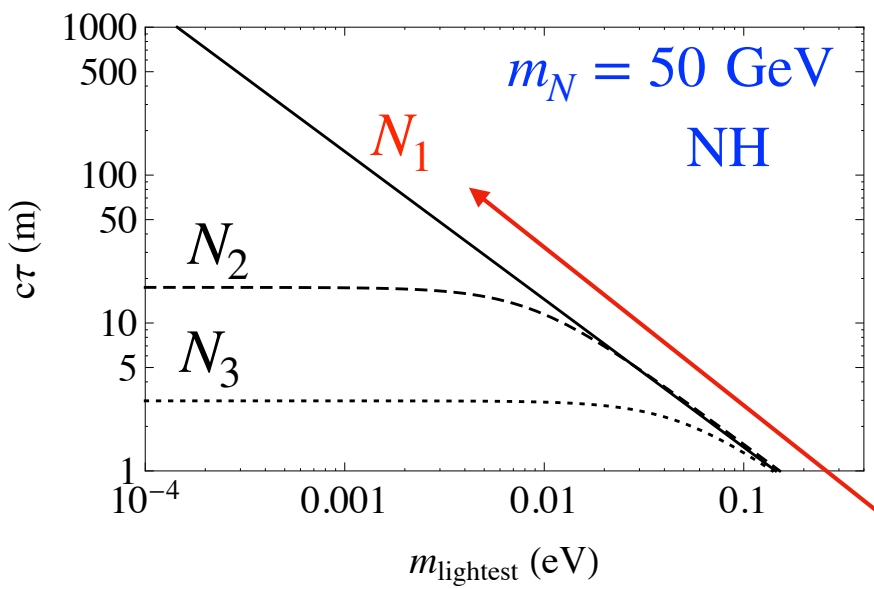
1812.11931

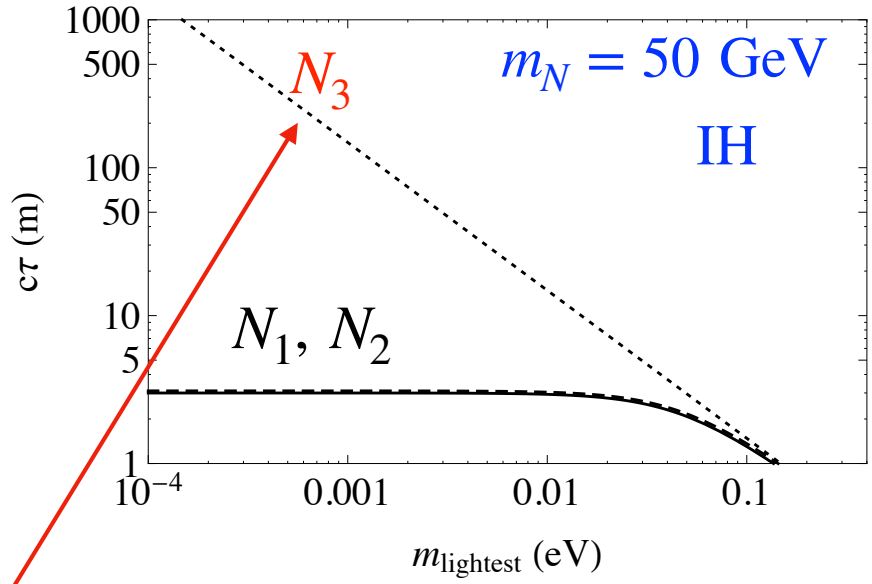

Alt. B − L, m_N = 100 GeV
(x_H = 0)
Alt. B − L, m_N = 50 GeV
√s = 250 GeV
0.100
0.010
0.001
10^−4
10^−5
10^−6
10^−7
σ(e^+e^− → N^iN^j)[fb]
3
4
5
6
7
m_Z'[TeV]
B − L, m_N = 50 GeV
B − L, m_N = 100 GeV

Long lived RHNs

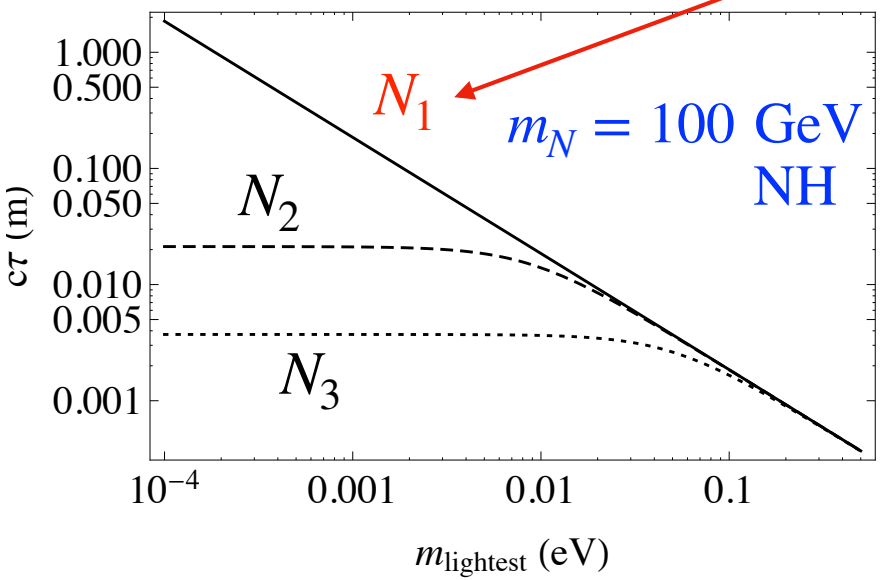
B – L case

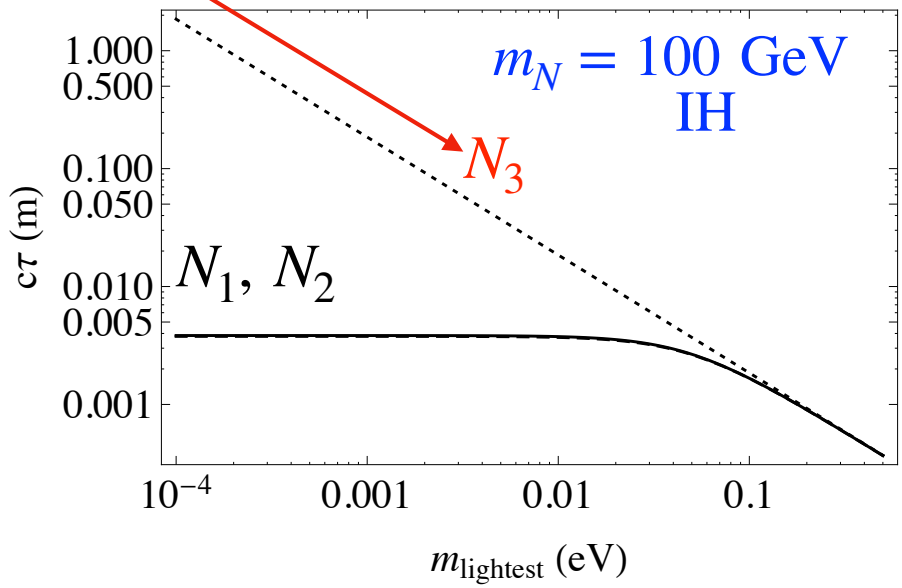
1812.11931





Longest lived RHN life time is inversely proportional to $m_{\rm lightest}$
$m_{\rm lightest} \to 0$ leads to the long lived species as a potential DM candiadte





Type – III seesaw

2005.02267, 2006.04123

$$\mathcal{L} = \mathcal{L}_{\rm SM} + {\rm Tr}(\overline{\Psi} i\gamma^\mu D_\mu \Psi) - \frac{1}{2} M {\rm Tr}(\overline{\Psi}\Psi^c + \overline{\Psi^c}\Psi) - \sqrt{2}(\overline{\ell_L} Y_D^\dagger \Psi H + H^\dagger \overline{\Psi} Y_D \ell_L)$$

$$\Psi = \begin{pmatrix} \Sigma^0/\sqrt{2} & \Sigma^+ \\ \Sigma^- & -\Sigma^0/\sqrt{2} \end{pmatrix} \text{ and } \Psi^c = \begin{pmatrix} \Sigma^{0c}/\sqrt{2} & \Sigma^{-c} \\ \Sigma^{+c} & -\Sigma^{0c}/\sqrt{2} \end{pmatrix}$$

$$-\mathcal{L}_{\rm mass} = \begin{pmatrix} \overline{e}_L & \overline{\Sigma}_L \end{pmatrix} \begin{pmatrix} m_\ell & Y_D^\dagger v \\ 0 & M \end{pmatrix} \begin{pmatrix} e_R \\ \Sigma_R \end{pmatrix} + \frac{1}{2} \begin{pmatrix} \overline{\nu_L^c} & \overline{\Sigma_R^0} \end{pmatrix} \begin{pmatrix} 0 & Y_D^T \frac{v}{\sqrt{2}} \\ Y_D \frac{v}{\sqrt{2}} & M \end{pmatrix} \begin{pmatrix} \nu_L \\ \Sigma_R^{0c} \end{pmatrix} + h.c.$$

$$m_\nu \simeq -\frac{v^2}{2} Y_D^T M^{-1} Y_D = M_D M^{-1} M_D^T$$

$$\Gamma(\Sigma^\pm \to \nu W) = \frac{g^2 |V_{\ell\Sigma}|^2}{32\pi} \left(\frac{M^3}{M_W^2}\right) \left(1 - \frac{M_W^2}{M^2}\right)^2 \left(1 + 2\frac{M_W^2}{M^2}\right)$$

$$\Gamma(\Sigma^\pm \to \ell Z) = \frac{g^2 |V_{\ell\Sigma}|^2}{64\pi \cos^2\theta_W} \left(\frac{M^3}{M_Z^2}\right) \left(1 - \frac{M_Z^2}{M^2}\right)^2 \left(1 + 2\frac{M_Z^2}{M^2}\right)$$

$$\Gamma(\Sigma^\pm \to \ell h) = \frac{g^2 |V_{\ell\Sigma}|^2}{64\pi} \left(\frac{M^3}{M_W^2}\right) \left(1 - \frac{M_h^2}{M^2}\right)^2,$$

$$\Gamma(\Sigma^\pm \to \Sigma^0 \pi^\pm) = \frac{2 G_F^2 V_{ud}^2 \Delta M^3 f_\pi^2}{\pi} \sqrt{1 - \frac{m_\pi^2}{\Delta M^2}}$$

$$\Gamma(\Sigma^\pm \to \Sigma^0 e \nu_e) = \frac{2 G_F^2 \Delta M^5}{15\pi}$$

$$\Gamma(\Sigma^\pm \to \Sigma^0 \mu \nu_\mu) = 0.12 \Gamma(\Sigma^\pm \to \Sigma^0 e \nu_e)$$

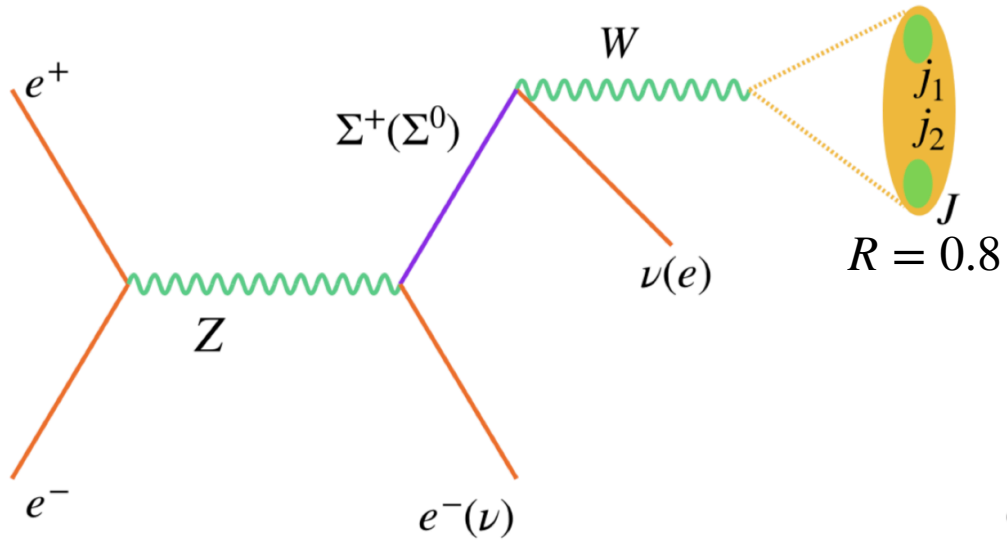
$$\Gamma(\Sigma^0 \to \ell^+ W) = \Gamma(\Sigma^0 \to \ell^- W) = \frac{g^2 |V_{\ell\Sigma}|^2}{64\pi} \left(\frac{M^3}{M_W^2}\right) \left(1 - \frac{M_W^2}{M^2}\right)^2 \left(1 + 2\frac{M_W^2}{M^2}\right)$$

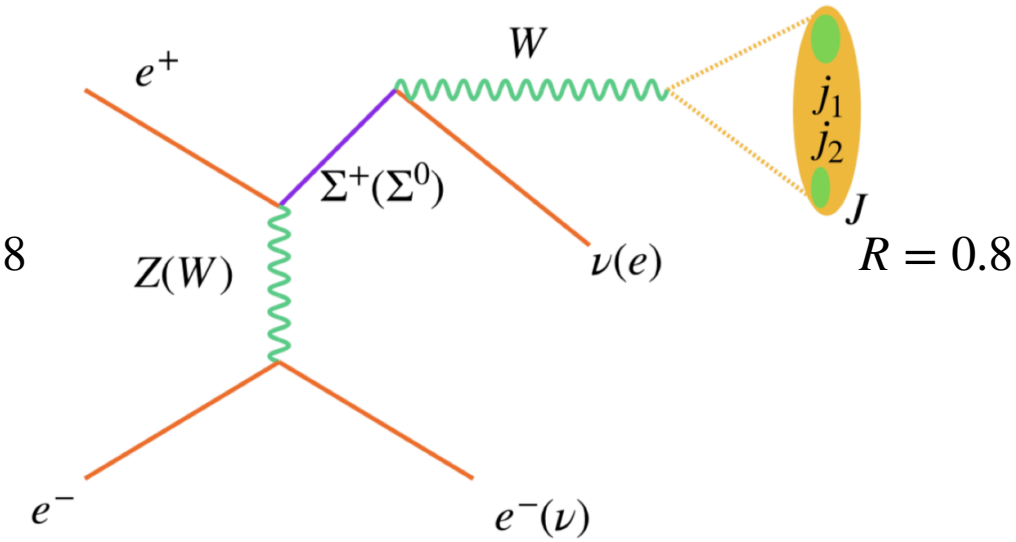
$$\Gamma(\Sigma^0 \to \nu Z) = \Gamma(\Sigma^0 \to \overline{\nu} Z) = \frac{g^2 |V_{\ell\Sigma}|^2}{128\pi \cos^2\theta_W} \left(\frac{M^3}{M_Z^2}\right) \left(1 - \frac{M_Z^2}{M^2}\right)^2 \left(1 + 2\frac{M_Z^2}{M^2}\right)$$

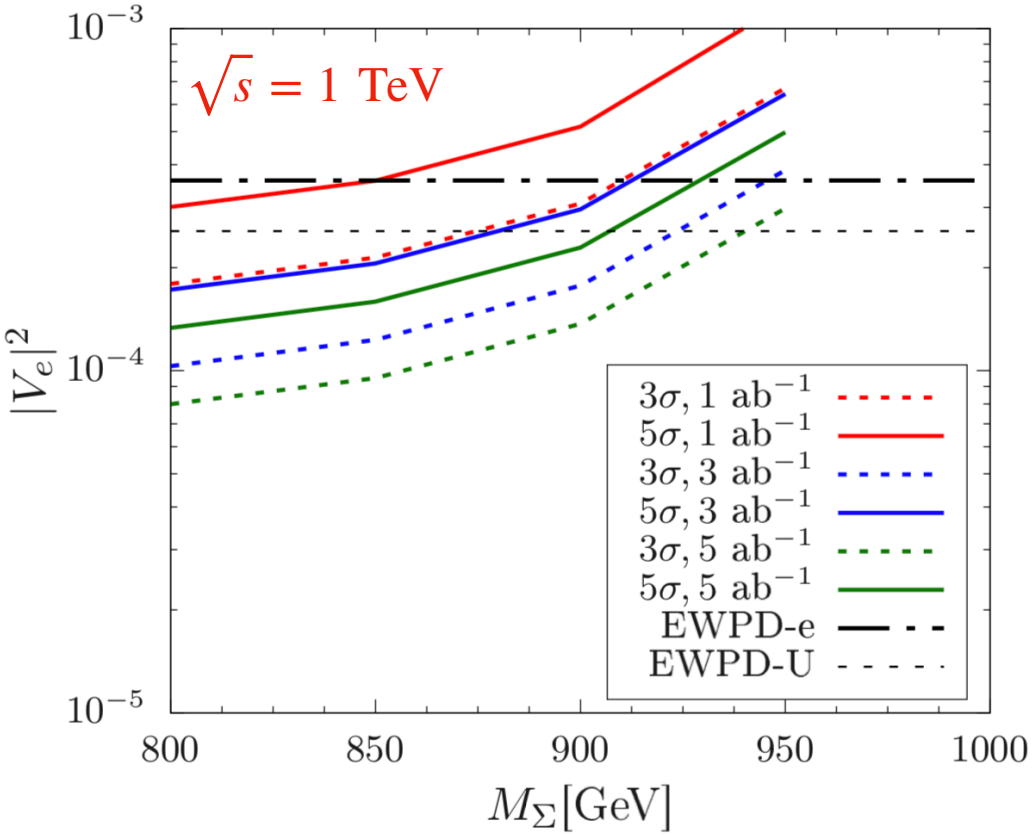
$$\Gamma(\Sigma^0 \to \nu h) = \Gamma(\Sigma^0 \to \overline{\nu} h) = \frac{g^2 |V_{\ell\Sigma}|^2}{128\pi} \left(\frac{M^3}{M_W^2}\right) \left(1 - \frac{M_h^2}{M^2}\right)^2,$$

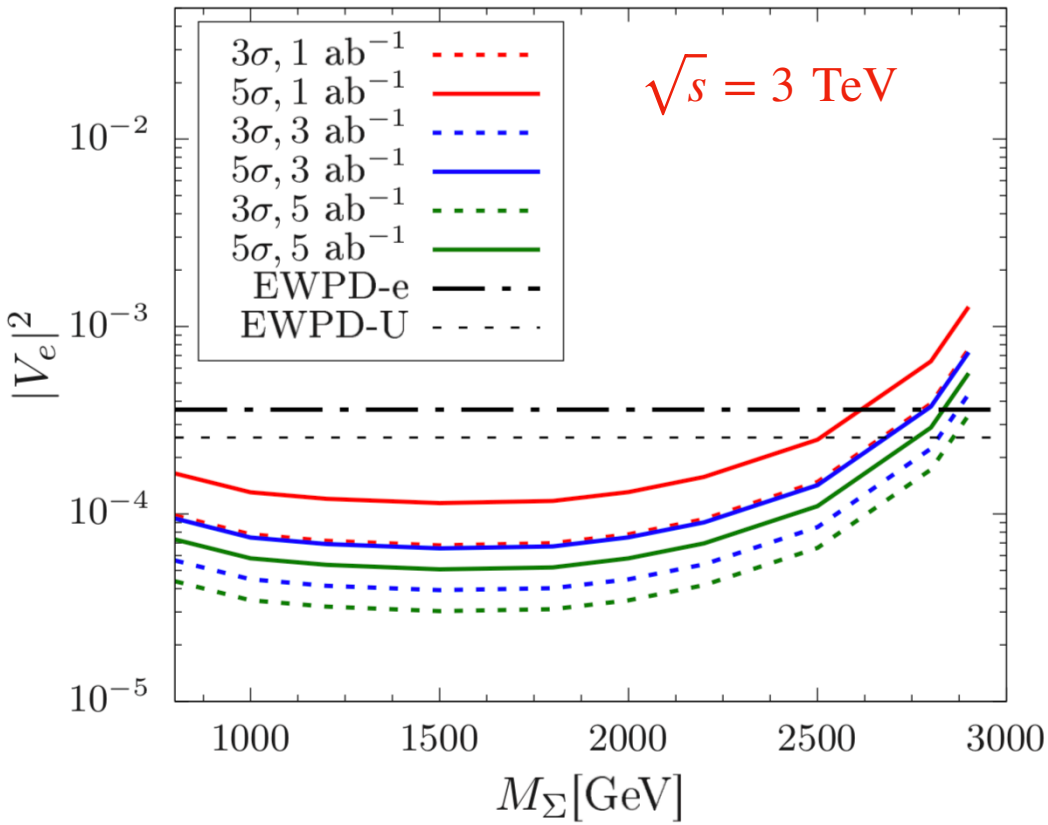
Mass-mixing limit plots

2005.02267









Conclusions

We study the models with the heavy leptons under the simple extensions of the SM where the neutrino mass is generated by the seesaw mechanism to reproduce the neutrino oscillation data.

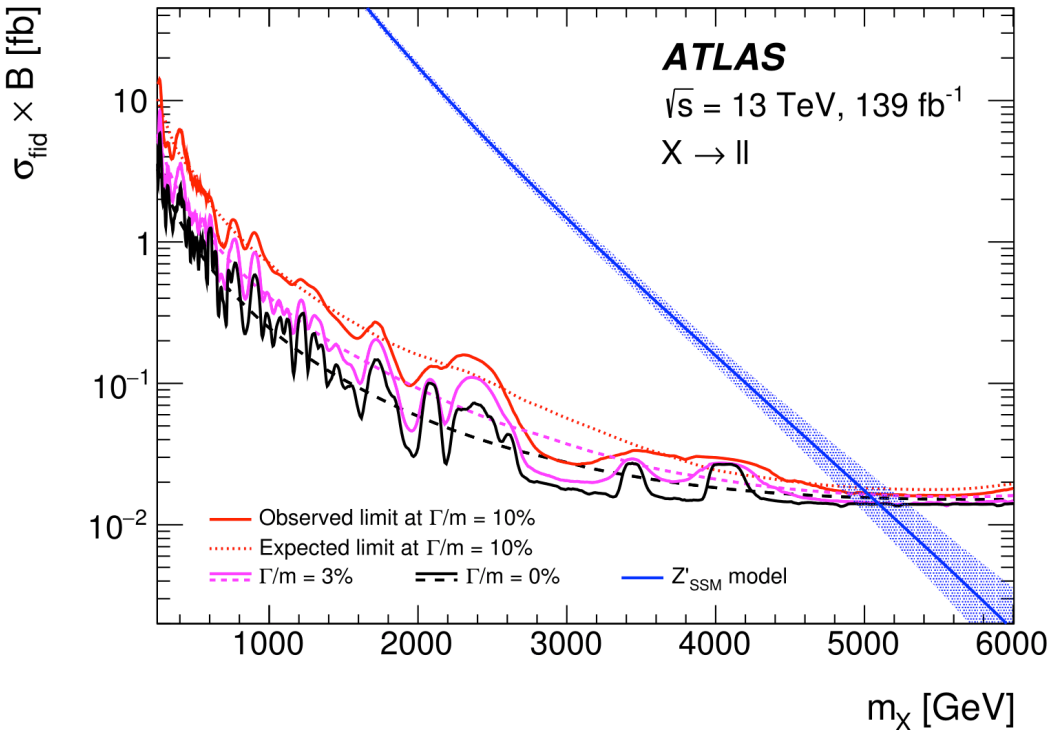
We find that such heavy fermions can be tested at the underground experiments at the electron positron collider. We have calculated the bounds on the light-heavy mixings for the electron-positron collider which could be probed in the near future.

Thank You

Backup slides

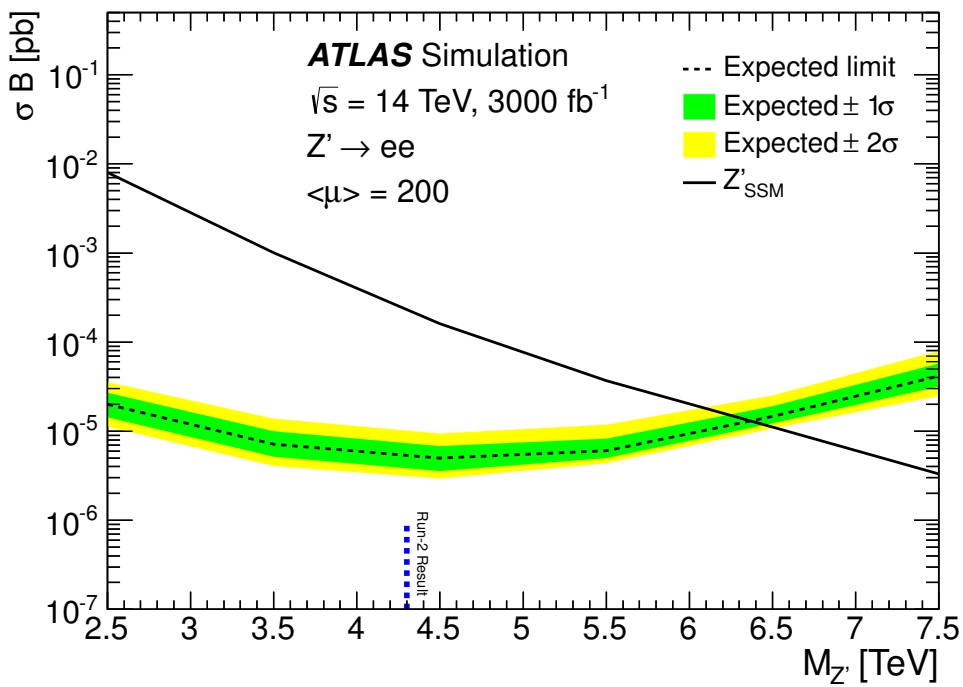
Bounds on the $U(1)_X$ gauge coupling

ATLAS: 1903.06248 (139/fb)



CMS (36/fb) and ATLAS (139/fb) searches at the LHC Run-1 and Run-2 respectively

ATLAS-TDR-027 (prospective)



$m_{Z'} = 7.5$ TeV $\sqrt{s} = 250$ GeV 1812.11931

$$\sigma(e^+e^- \to Z'^* \to N^i N^i) = 0.0085 \text{ fb } (B-L)$$
$$= 0.14 \text{ fb } (\text{Alt. } B-L)$$

$$m_{N^{1,2,3}} = 50 \text{ GeV and } m_{N^{1,2}} = 50 \text{ GeV}$$

degenerate RHNs @ $\sum_{i=1}^{3} \sigma(e^+e^- \to Z'^* \to N^i N^i) = 0.026$ fb $(B-L)$
$\sum_{i=1}^{2} \sigma(e^+e^- \to Z'^* \to N^i N^i) = 0.29$ fb $(\text{Alt. } B-L)$

Luminosity = 2000 fb^{-1} 52 and 576 events respectively

satisfying constraints from the HL – LHC

Majorana RHNs will show $\ell^\pm\ell^\pm$4j signal which can be a smoking gun signature
data fitting.
at the ILC to probe Majorana nature. Let's find the branching ratios after the neutrino

1812.11931

B – L

$m_N = 50$ GeV	$e + jj$	$\mu + jj$	$\tau + jj$
N^1	0.412	0.104	0.104
N^2	0.204	0.224	0.224
N^3	0.0154	0.310	0.310

$m_N = 100$ GeV	$e + jj$	$\mu + jj$	$\tau + jj$
N^1	0.587	0.148	0.148
N^2	0.276	0.304	0.304
N^3	0.0208	0.431	0.431

Alt. B – L

NH case

$m_N = 50$ GeV	$e + jj$	$\mu + jj$	$\tau + jj$
N^1	0.194	0.213	0.213
N^2	0.0154	0.318	0.318

$m_N = 100$ GeV	$e + jj$	$\mu + jj$	$\tau + jj$
N^1	0.276	0.304	0.304
N^2	0.0208	0.431	0.431

IH case

$m_N = 50$ GeV	$e + jj$	$\mu + jj$	$\tau + jj$
N^1	0.412	0.104	0.104
N^2	0.204	0.224	0.224

$m_N = 100$ GeV	$e + jj$	$\mu + jj$	$\tau + jj$
N^1	0.587	0.148	0.148
N^2	0.276	0.304	0.304

Finally NN $\to 2\ell^{\pm}4$j will dominantly be between 16% – 34 % for the final results for the B – L $\to$ Alt. B – Lscenario.