

# Higgs quartic coupling at a Muon Collider

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based on arXiv:2003.13628

in collaboration with Luca Mantani, Fabio Maltoni, Barbara Mele, Fulvio Piccinini  
and Xiaoran Zhao

## H self-couplings measurement: future colliders (HHHH)

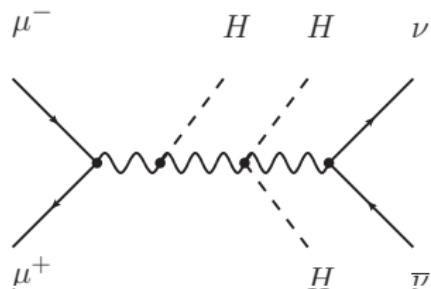
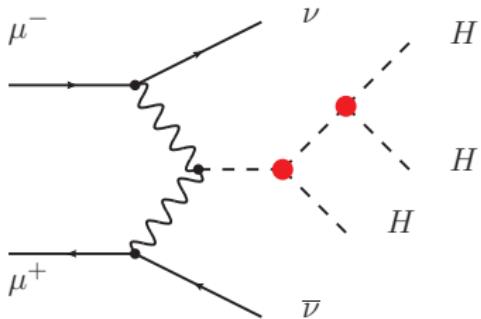
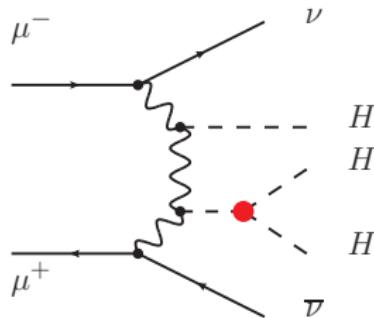
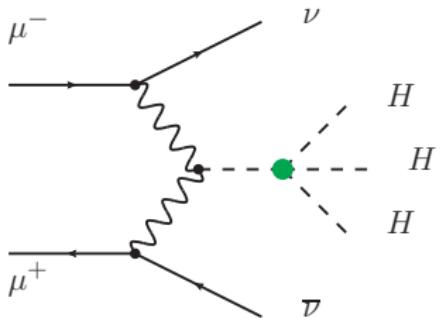
- the proposed future colliders can put strong constraints on the triple Higgs coupling  $\delta_3$ :  $\pm 10\%$   $1-\sigma$  bound at CLIC and ILC,  $\pm 5\%$  at FCC
- the bounds on the quartic couplings  $\delta_4$  are very loose (68% CL)
  - ILC:  $\sim [-10, +10]$  ( $\pm 1000\%!$ )
  - CLIC:  $\sim [-5, +5]$
  - FCC:  $\sim [-5, +15]$ , from  $pp \rightarrow HHH$
  - FCC:  $\sim [-2, +4]$ , from  $pp \rightarrow HH$

I will focus on the sensitivity of the muon collider to the quartic coupling

Spoiler:

under (reasonable) assumptions on the energy and the luminosity, the muon collider can do a pretty good job in constraining the quartic Higgs coupling

$$\mu^+ \mu^- \rightarrow HHH\nu\bar{\nu}$$



# $\mu^+ \mu^- \rightarrow HHH\nu\bar{\nu}$ : SM Higgs couplings (energy)

$\sqrt{s}$ (TeV) / L (ab $^{-1}$ )	1.5 / 1.2	3 / 4.4	6 / 12
$\sigma_{SM}$ (ab) [N <sub>ev</sub> ]			
$\sigma^{\text{tot}}$	0.03 [0]	0.31 [1]	1.65 [20]
$\sigma(M_{HHH} < 3\text{TeV})$	0.03 [0]	0.31 [1]	1.47 [18]
$\sigma(M_{HHH} < 1\text{TeV})$	0.02 [0]	0.12 [1]	0.26 [3]

$\sqrt{s}$ (TeV) / L (ab $^{-1}$ )	10 / 20	14 / 33	30 / 100
$\sigma_{SM}$ (ab) [N <sub>ev</sub> ]			
$\sigma^{\text{tot}}$	4.18 [84]	7.02 [232]	18.51 [1851]
$\sigma(M_{HHH} < 3\text{TeV})$	2.89 [58]	3.98 [131]	6.69 [669]
$\sigma(M_{HHH} < 1\text{TeV})$	0.37 [7]	0.45 [15]	0.64 [64]

$\sigma$  increases with  $\sqrt{s}$

# $\mu^+ \mu^- \rightarrow HHH\nu\bar{\nu}$ : SM Higgs couplings (luminosity)

$\sqrt{s}$ (TeV) / L (ab $^{-1}$ )	1.5 / 1.2	3 / 4.4	6 / 12
$\sigma_{SM}$ (ab) [N <sub>ev</sub> ]			
$\sigma^{\text{tot}}$	0.03 [0]	0.31 [1]	1.65 [20]
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The lower energy setups (1.5 and 3 TeV) do not have enough events to study the quartic Higgs self coupling

# $\mu^+ \mu^- \rightarrow H H H \nu \bar{\nu}$ : SM Higgs couplings (luminosity)

- the luminosities assumed for  $\sqrt{s} = 1.5, 3, 6, 14$  TeV are based on MAP studies

V. Shiltsev FERMILAB-FN\_1083-AD-APC,

talks by D. Shulte and M. Palmer <https://indico.cern.ch/event/847002/>

- at  $\sqrt{s} = 10, 30$  TeV, the luminosity is fixed by (see arXiv:1910.06150)  
**Luminosity:**

$$L \gtrsim \frac{5 \text{ years}}{\text{time}} \left( \frac{\sqrt{s}_\mu}{10 \text{ TeV}} \right)^2 2 \cdot 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$$

Set by asking for 100K SM “hard” SM pair-production events.

- for the 10 and 30 TeV setups, it might be that higher luminosity could be achieved

# Deviations from SM Higgs couplings

$$\mathcal{L} = -\frac{1}{2}M_H^2 H^2 - \left(1 + \delta_3\right) \frac{M_H^2}{2v} H^3 - \left(1 + \delta_4\right) \frac{M_H^2}{8v^2} H^4$$

We consider 3 different scenarios:

- 1  $\delta_3 = 0, \delta_4$  arbitrary
- 2  $\delta_3$  arbitrary,  $\delta_4 = 6\delta_3$  (well behaved SMEFT)
- 3  $\delta_3$  arbitrary and  $\delta_4$  arbitrary

S. Borowka et al. arXiv:1811.12366

# Sensitivity to $\delta_3$ and $\delta_4$

No background process considered:

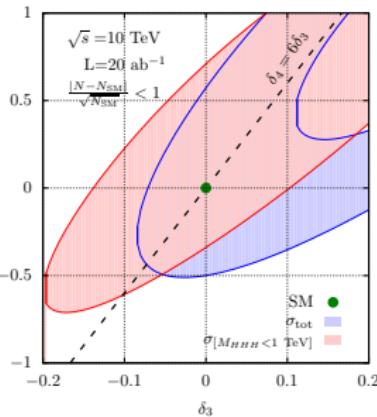
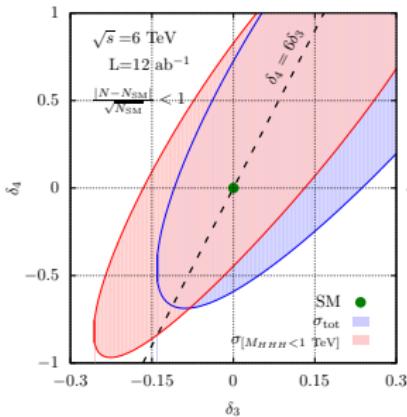
we quantify the sensitivity in terms of standard deviations from the SM expectation

$$\frac{|N - N_{\text{SM}}|}{\sqrt{N_{\text{SM}}}}$$

## Remarks

- no background is considered, but the environment should be rather clean
- no branching ratio is applied, but if the environment is clean enough all the main decay channels should be visible
- (almost) no optimization based on kinematics is performed, so there is room for improvement

# Sensitivity to $\delta_3$ and $\delta_4$ (small $\delta_3$ )



- no cuts
- $M_{HHH} < 1 \text{ TeV}$

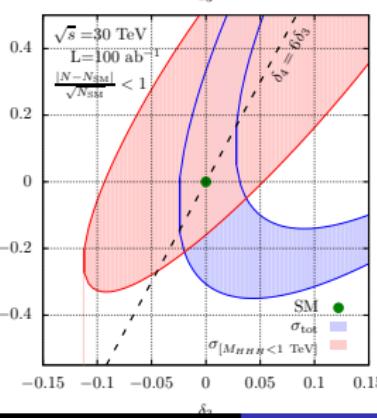
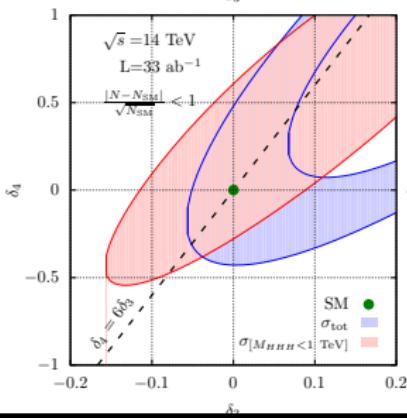
$$\delta_3 = 0$$

6 TeV  $\delta_4 \sim [-0.45, 0.8]$

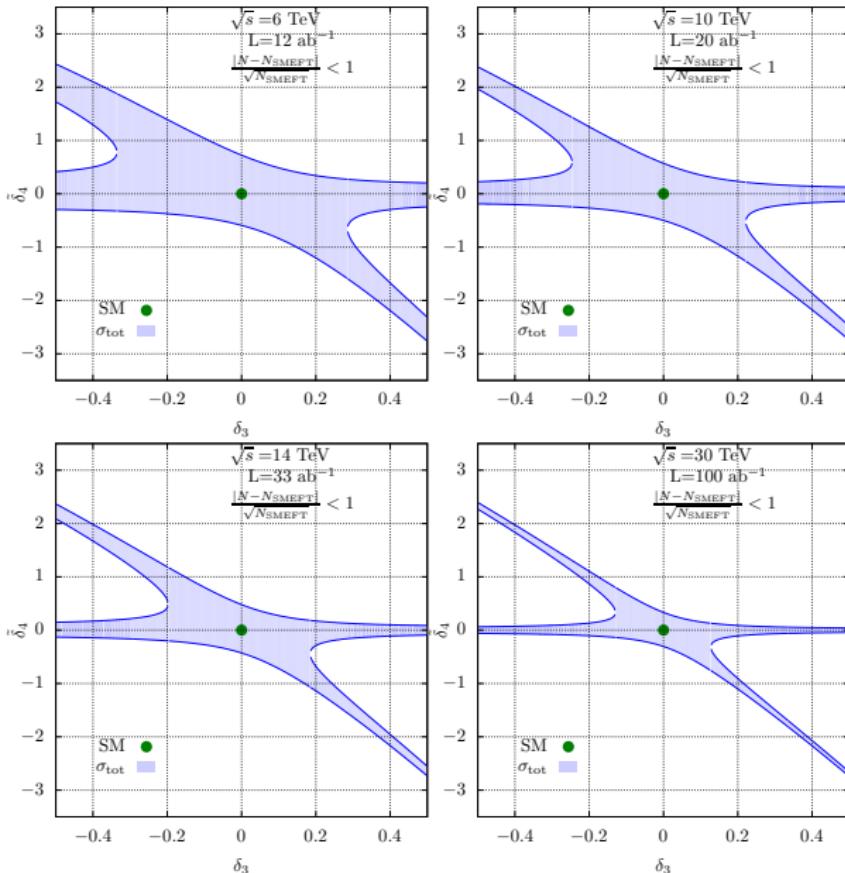
10 TeV  $\delta_4 \sim [-0.4, 0.7]$

14 TeV  $\delta_4 \sim [-0.35, 0.6]$

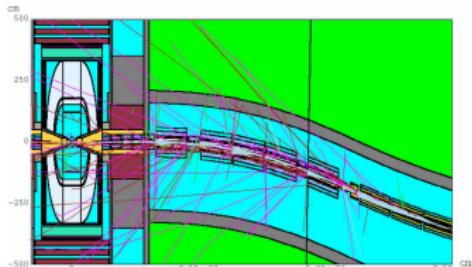
30 TeV  $\delta_4 \sim [-0.2, 0.5]$



# Sensitivity to $\tilde{\delta}_4$ (deviation from SMEFT)

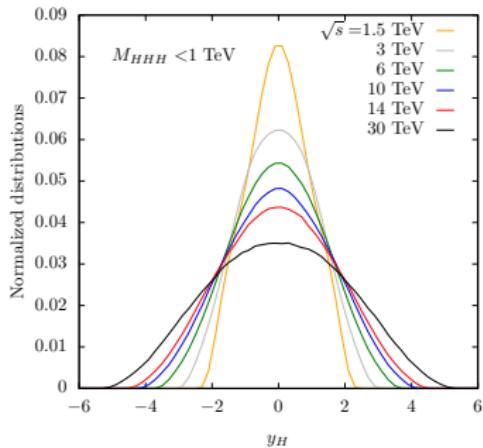
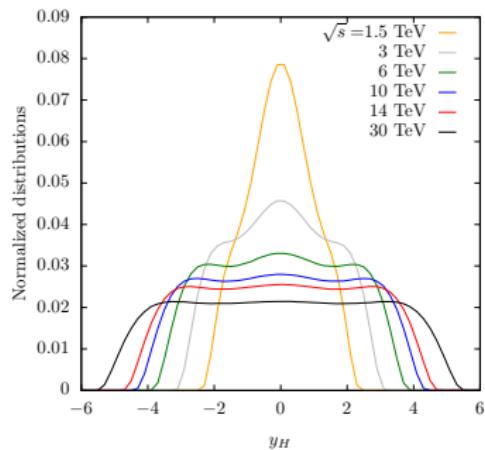


# Remark on detector acceptance (1)

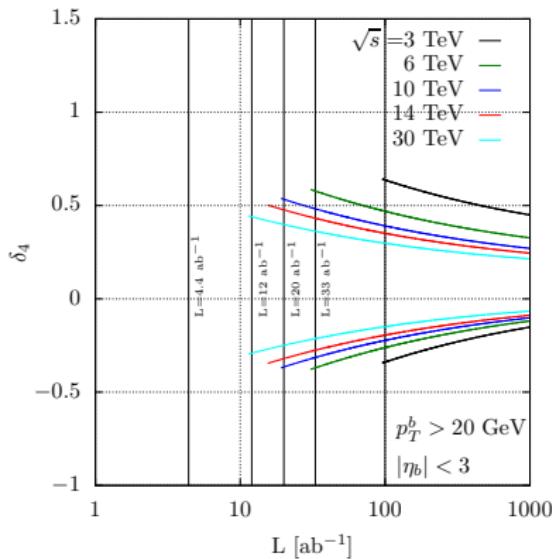
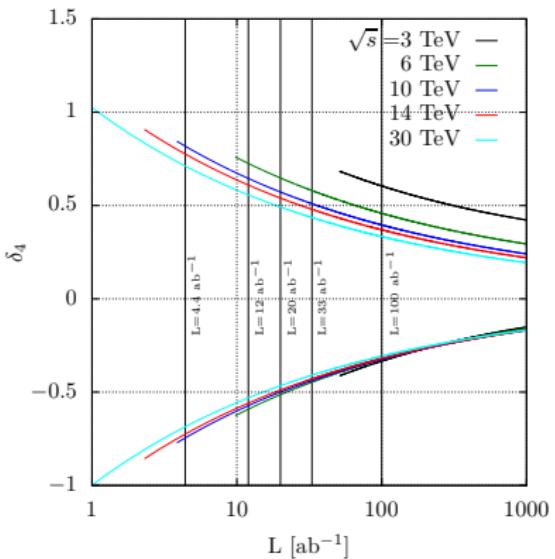


The detector must be shielded from the beam radiation

- 5-10 degrees blind spot in the forward region for  $\sqrt{s} = 3 \text{ TeV}$
- angle could be reduced at higher energies



## Remark on detector acceptance (2)



- only geometric acceptance considered (no BR applied)
- sensitivity increases because the SM production is forward, the BSM central

# Conclusions

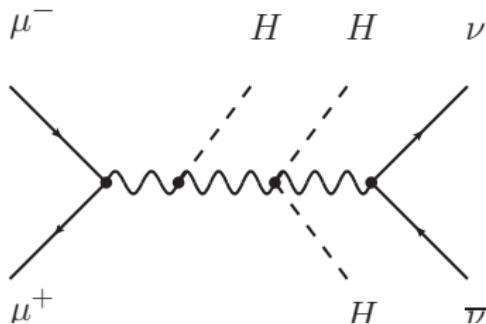
- we studied the sensitivity of the muon collider to the Higgs quartic coupling by considering the process  $\mu^+ \mu^- \rightarrow HHH\nu\bar{\nu}$
- no background was considered
- (almost) no optimization based on kinematics was performed
- the sensitivity increases with  $\sqrt{s}$  and/or the luminosity

$\sqrt{s}$ [TeV]	$L$ [ $\text{ab}^{-1}$ ]	$\delta_4$ (arbitrary $\delta_3$ )	$\delta_4$ ( $\delta_3 = 0$ )
6	12	[-1,1.7]	[-0.45,0.8]
10	20	[-0.7,1.55]	[-0.4,0.7]
14	33	[-0.55,1.4]	[-0.35,0.6]
30	100	[-0.35,1.2]	[-0.2,0.5]

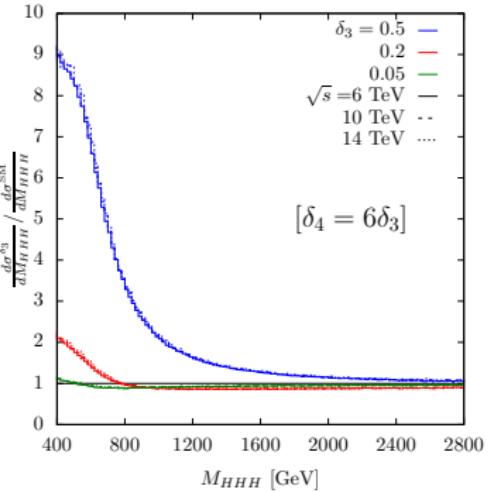
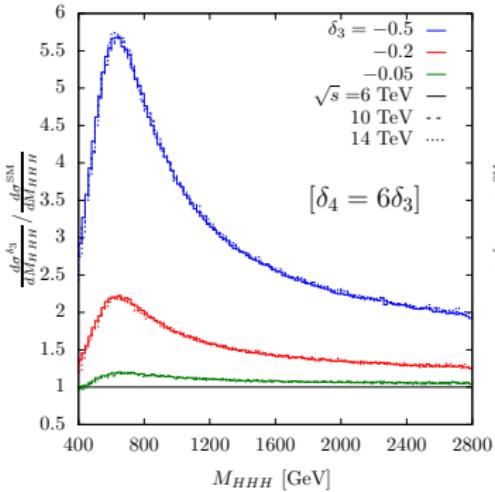
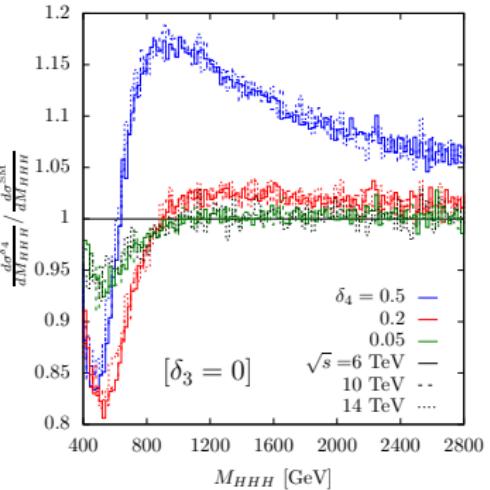
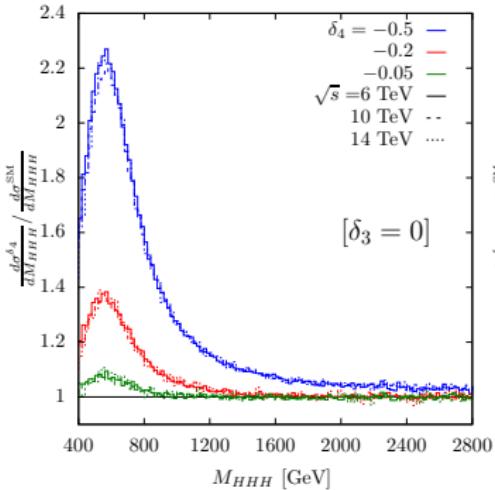
- under (reasonable) assumptions on the energy and the luminosity, the muon collider can do a pretty good job in constraining the quartic Higgs coupling

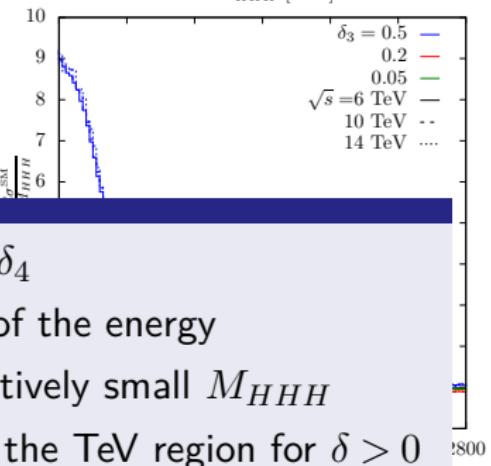
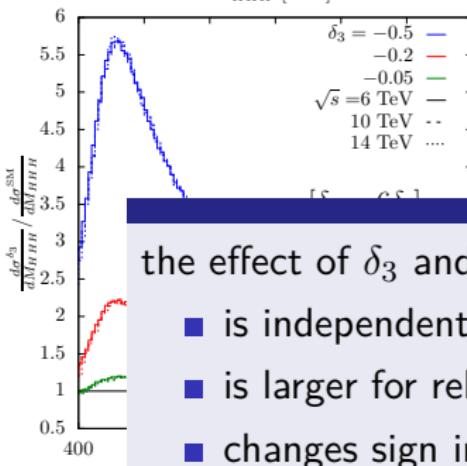
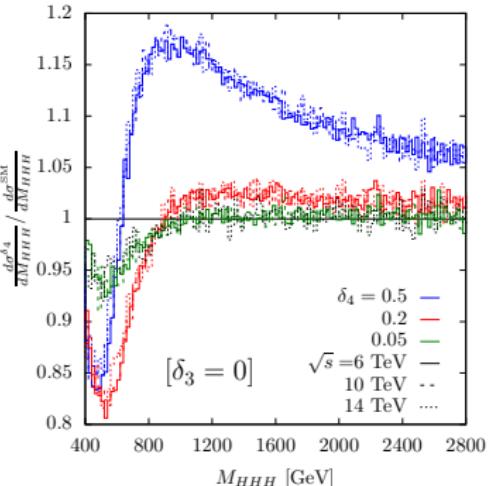
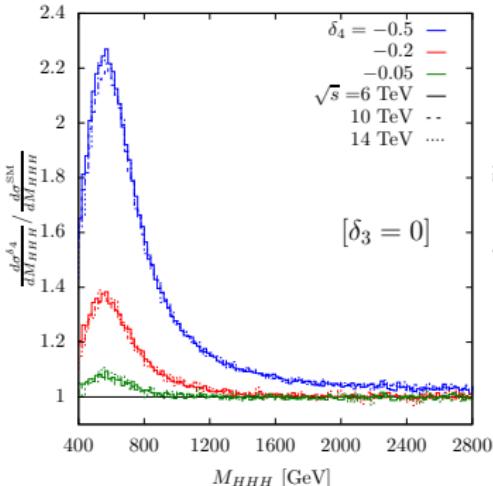
# Backup slides

## Details of the calculations



- $H$  produced on shell
- $H \rightarrow b\bar{b}$  (on-shell) decays added at the LHE level
- $\Gamma_W = \Gamma_Z = \Gamma_H = 0$  to avoid issues with gauge invariance
- technical cut  $M(\nu\bar{\nu}) > 150$  GeV
- $\sigma$  and  $d\sigma$  computed with WHIZARD at LO
- all results cross-checked with MadGraph and an independent calculation by X. Zhao

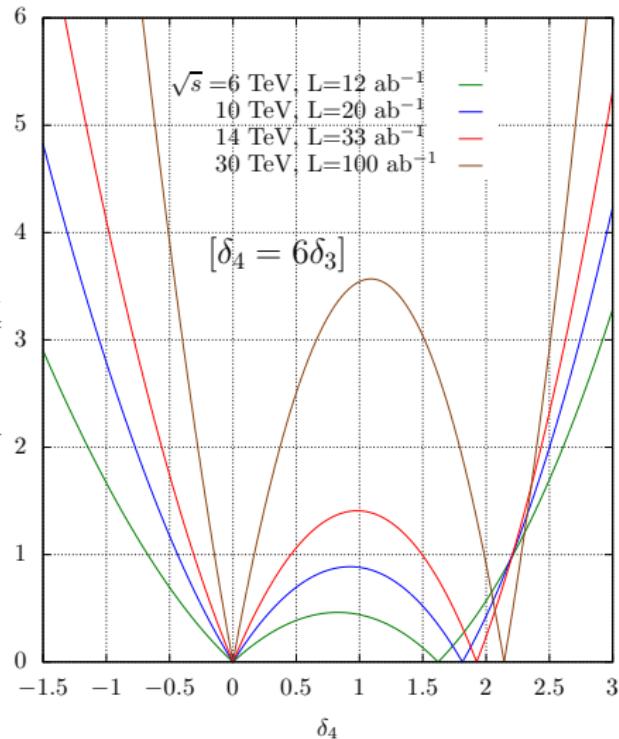
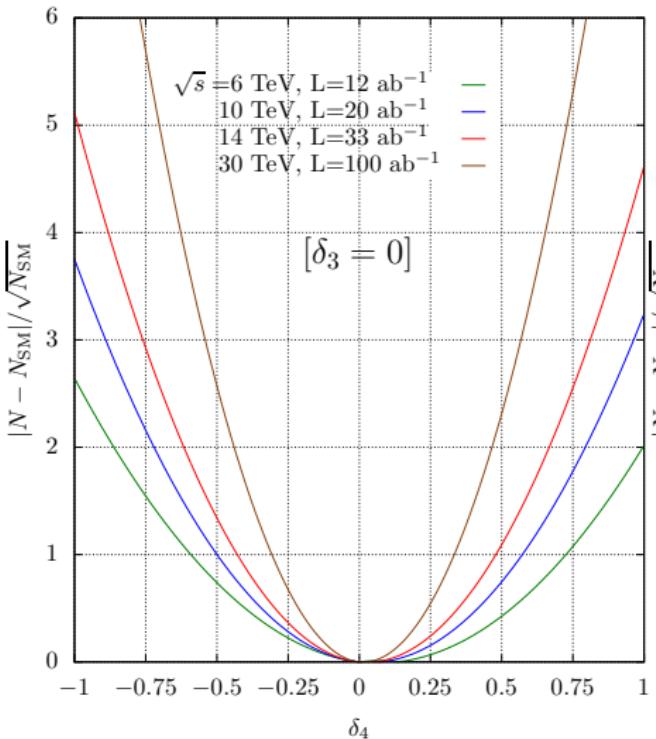




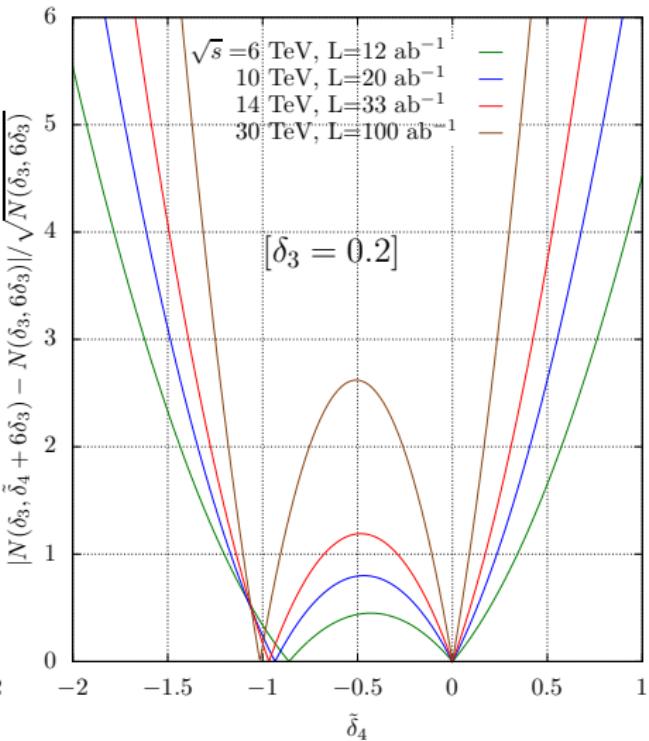
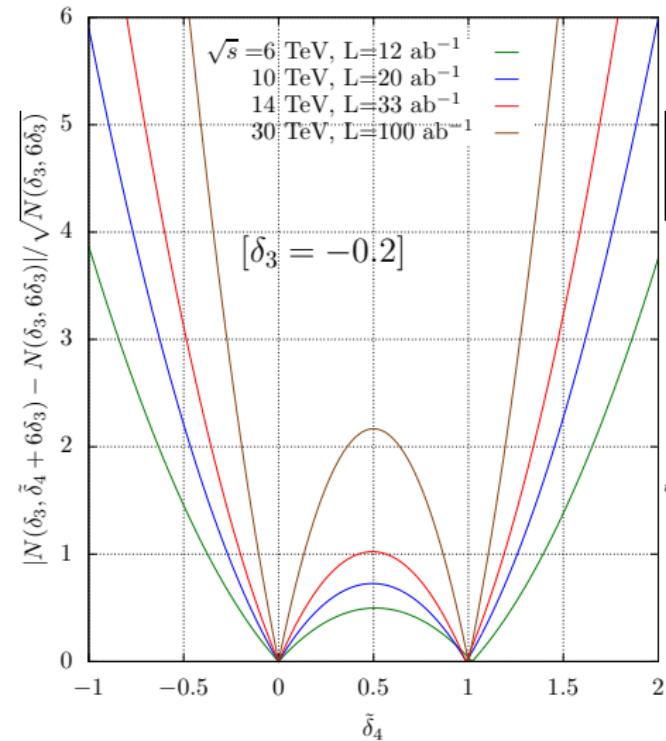
the effect of  $\delta_3$  and  $\delta_4$

- is independent of the energy
  - is larger for relatively small  $M_{HHH}$
  - changes sign in the TeV region for  $\delta > 0$

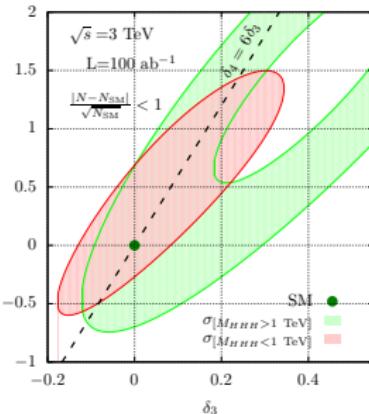
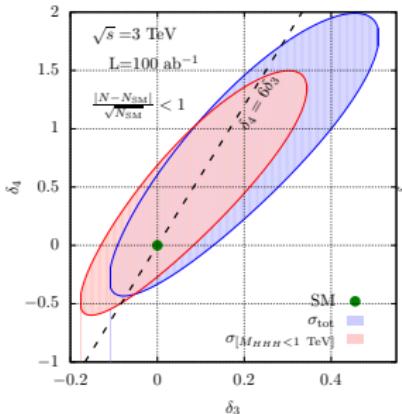
# Sensitivity to $\delta_3$ and $\delta_4$



# Sensitivity to $\tilde{\delta}_4$ (deviation from SMEFT)



# Sensitivity to $\delta_3$ and $\delta_4$ ( $\sqrt{s} = 3$ TeV, $L = 100 \text{ ab}^{-1}$ )



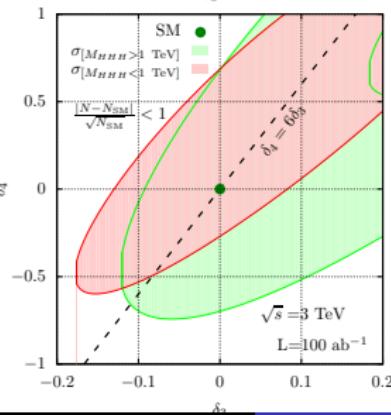
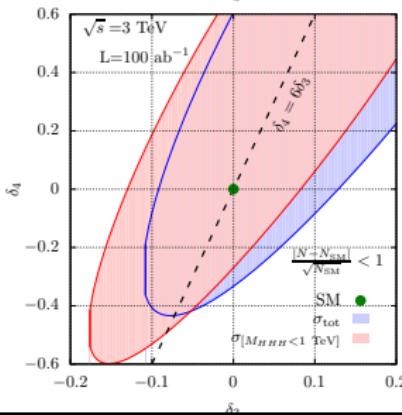
- no cuts
- $M_{HHH} < 1 \text{ TeV}$
- $M_{HHH} > 1 \text{ TeV}$

$$\delta_4 \sim [-0.6, 1.5]$$

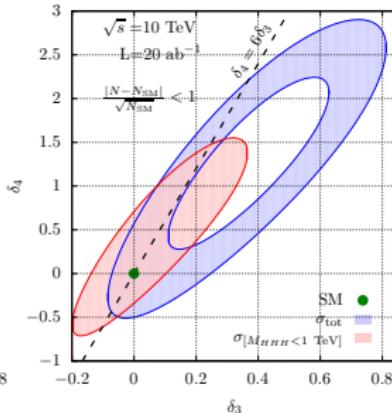
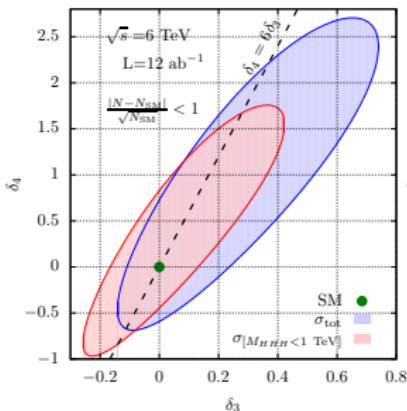
if  $\delta_3 = 0$

$$\delta_4 \sim [-0.3, 0.65]$$

Using 20 times the expected luminosity!



# Sensitivity to $\delta_3$ and $\delta_4$ (arbitrary $\delta_3$ )



- no cuts
- $M_{HHHH} < 1 \text{ TeV}$

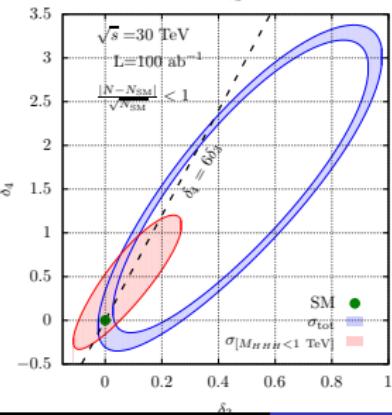
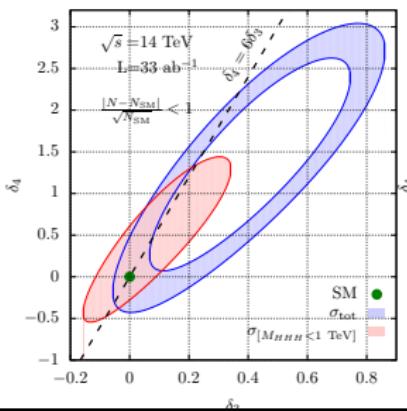
$$\delta_3 = 0$$

6 TeV  $\delta_4 \sim [-0.1, 1.7]$

10 TeV  $\delta_4 \sim [-0.7, 1.55]$

14 TeV  $\delta_4 \sim [-0.55, 1.4]$

30 TeV  $\delta_4 \sim [-0.35, 1.2]$



## Sensitivity to $\delta_3$ and $\delta_4$ : comments

- stronger constraints on negative  $\delta$ s
- constraints on positive  $\delta$ s improve with the cut  $M_{HHH} < 1$  TeV (provided that the cross section after the cut is large enough)
- the bounds improve at large  $\sqrt{s}$  because the cross section increases
- the most interesting region is  $\delta_3 \sim 0$ , as bounds on  $\delta_3$  can be obtained from other processes (i.e.  $\mu^+ \mu^- \rightarrow HH\nu\bar{\nu}$ ). It is reasonable to assume that such bounds will be competitive or stronger than the ones from linear colliders
- if  $\delta_3 \neq 0$ , one can constrain possible deviations from the SMEFT expectation for  $\delta_4$ :  $\tilde{\delta}_4 = \delta_4 - 6\delta_3$