

# LIGHT NEW PHYSICS IN MUON DECAYS

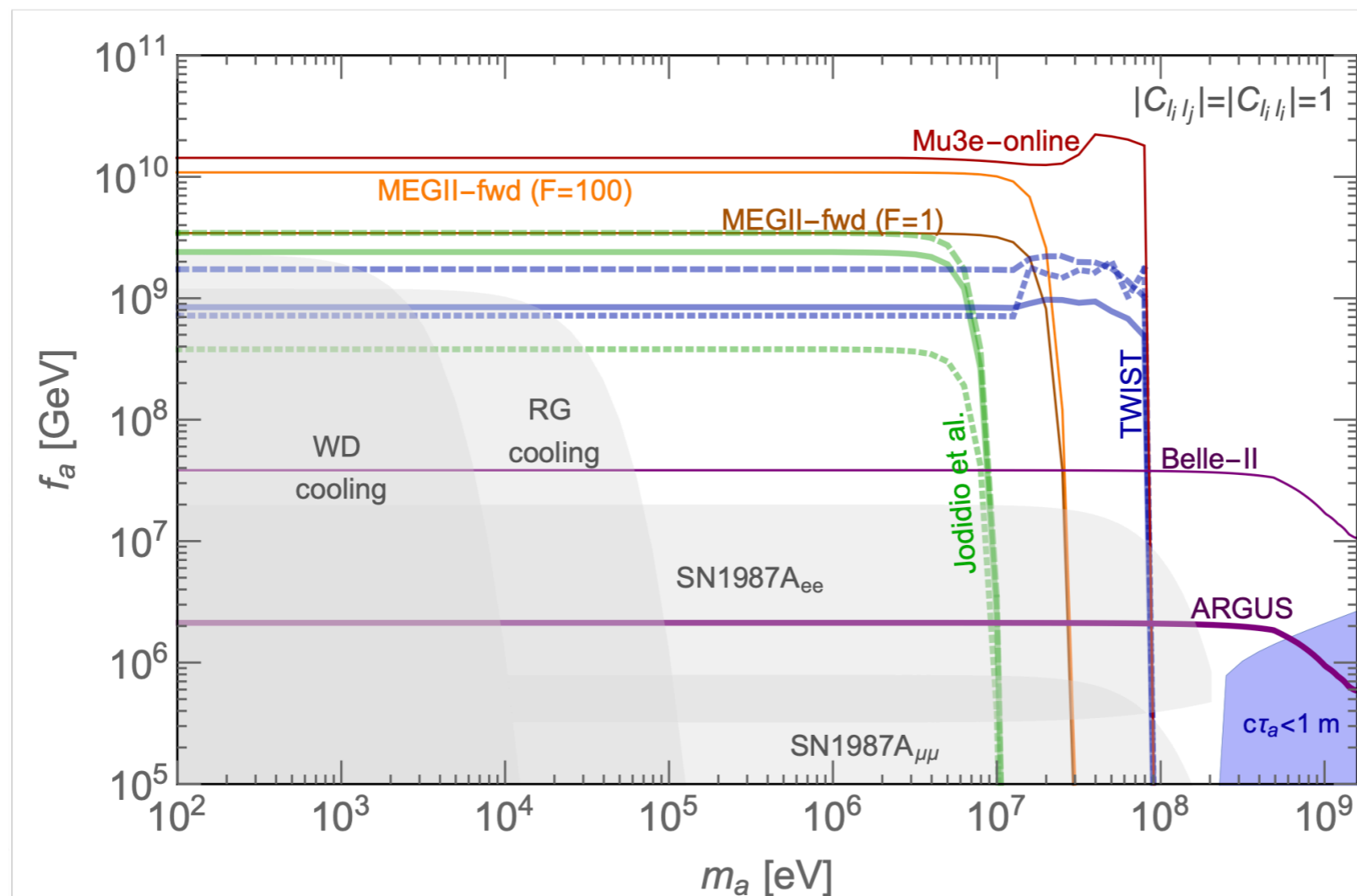
JURE ZUPAN  
U. OF CINCINNATI

based on Calibbi, Redigolo, Ziegler, JZ, 2006.04795

RF05: CLFV - Muon Decays and Transitions, Jul 2 2020

# UPSHOT

- $\mu \rightarrow e\gamma, \mu \rightarrow 3e, \mu \rightarrow e$  conv., from dim-6 ops, will reach NP scales of  $\sim 10^7 - 10^8 \text{ GeV}$
- $\mu \rightarrow ea$  from dim-5 ops., can reach NP scales  $\sim 10^{10} \text{ GeV}$ 
  - higher than astrophysics constraints



# MOTIVATION FOR AXION-LIKE PARTICLES

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- any spontaneously broken global symmetry  $\Rightarrow$  (p)NGB
  - if "light enough" can be DM
- in general couplings to gluons, photons, SM fermions

$$\mathcal{L}_{\text{eff}} = \frac{\alpha_s}{8\pi} \frac{a}{f_a} G\tilde{G} + \frac{E}{N} \frac{\alpha_{\text{em}}}{8\pi} \frac{a}{f_a} F\tilde{F} + \frac{\partial_\mu a}{2f_a} \bar{f}_i \gamma^\mu (C_{f_i f_j}^V + C_{f_i f_j}^A \gamma_5) f_j$$

- our goal: implications of flavor violating couplings
  - do FCNC experiments probe interesting parameter space?
  - possible improvements on search strategies?
  - in many cases FV leptonic couplings highest reach, focus on these

# LFV ALPs

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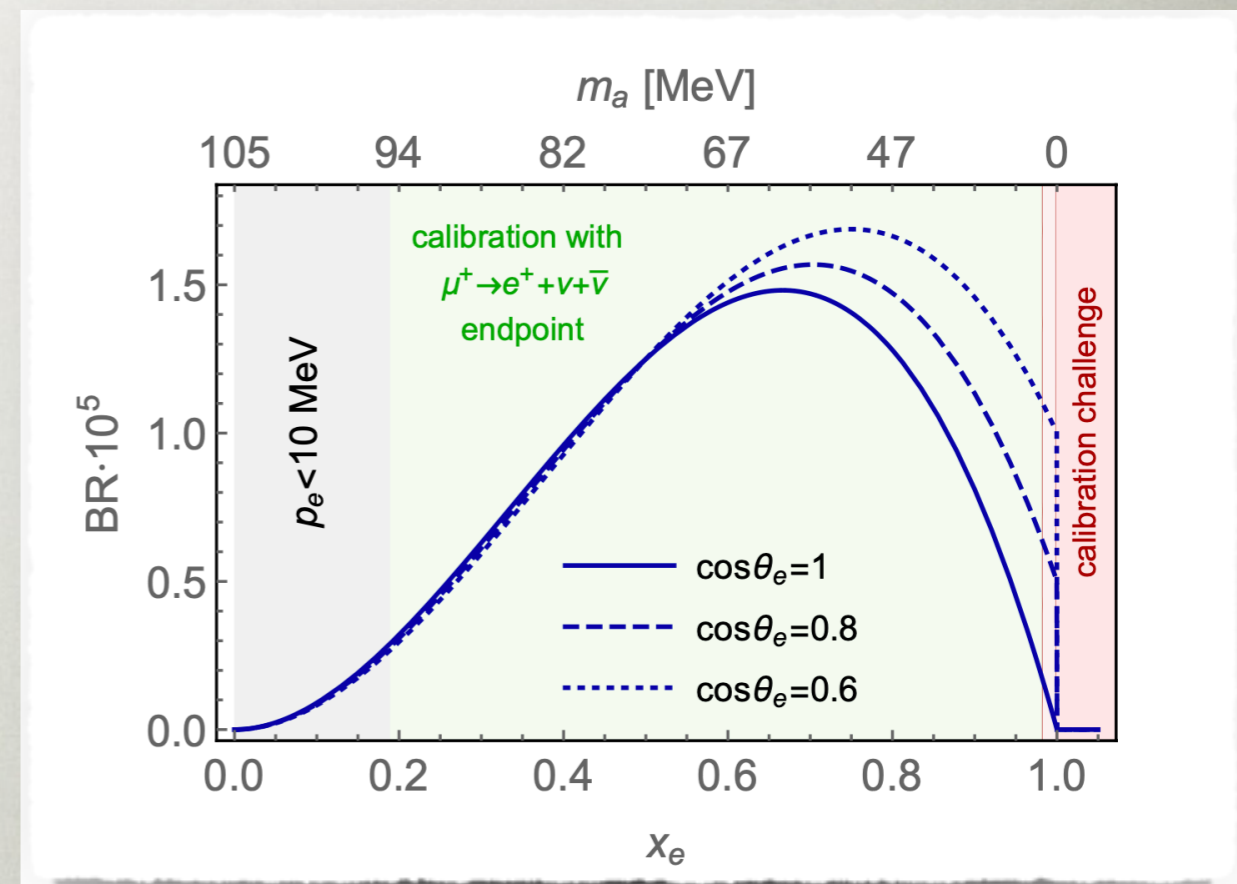
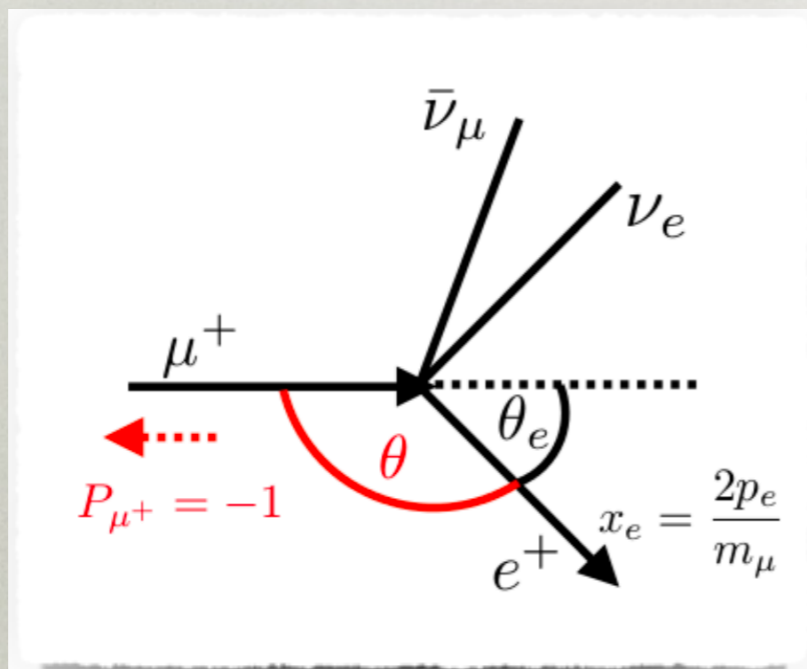
Calibbi, Redigolo, Ziegler, JZ, 2006.04795

- assume ALP with (predominantly) FV leptonic couplings
  - will allow for varying ALP masses
- main question
  - what does  $\mathcal{O}(10^{15} - 10^{17})$  muons at MEG-II, Mu3e, Mu2e buy us?
  - compare with  $2 \times 10^7 \mu$  @ Jodidio et al. (1986), and  $6 \times 10^8 \mu$  @ TWIST (2015)

# $\mu^+ \rightarrow e^+ a$ SEARCHES

- two types of searches for  $\mu^+ \rightarrow e^+ a$  positron line
- suppress the SM bckg.,  $\mu \rightarrow e \nu \bar{\nu}$ 
  - use polarized muons  $\langle P_\mu \rangle \simeq -1$ , in the forward region  
SM suppressed
  - sensitive only to RH ALP

Jodidio et al. 1986



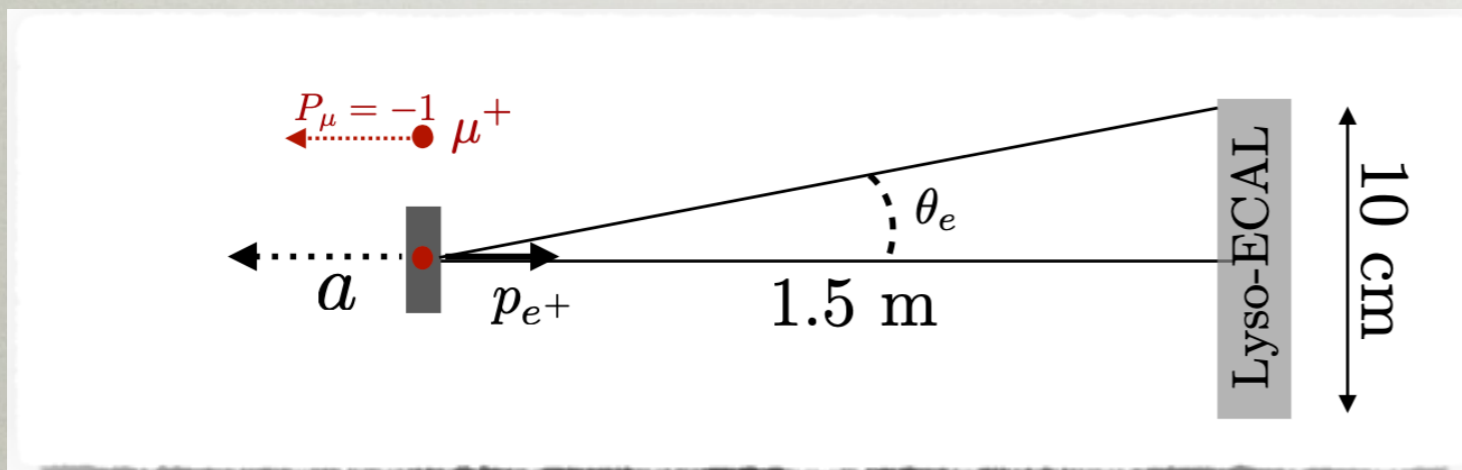
- do not suppress the SM, also sensitive to LH ALP, TWIST

TWIST, 2015

# MEGII-FWD

- MEGII is designed to search for  $\mu \rightarrow e\gamma$ 
  - could be repurposed for  $\mu^+ \rightarrow e^+a$  search  $\Rightarrow$  MEGII-fwd
- already has polarized muons
- place a Lyso ECAL downstream

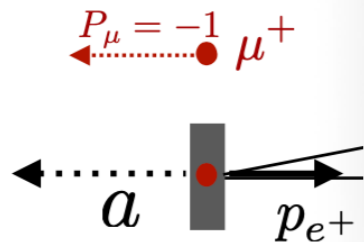
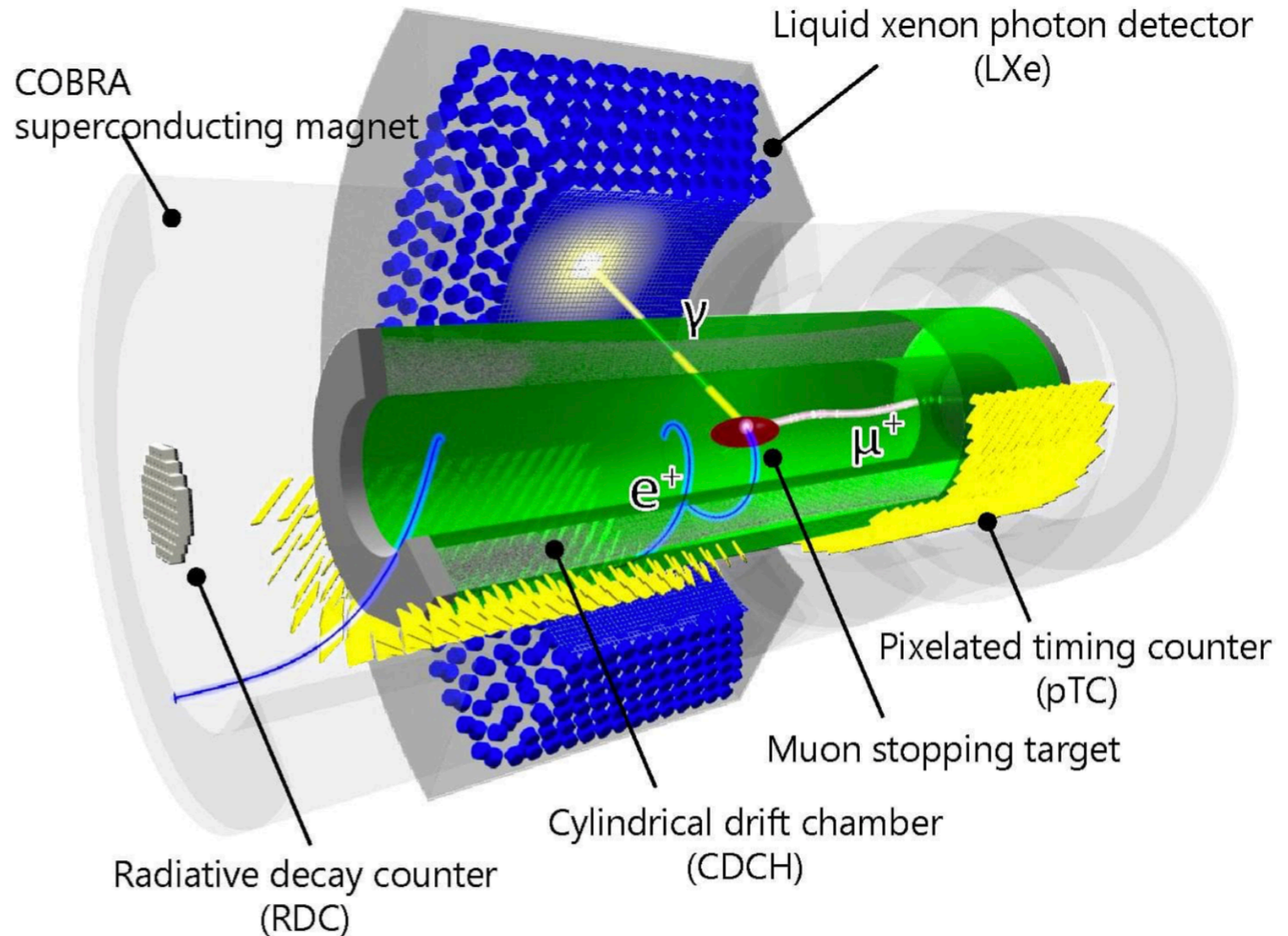
Calibbi, Redigolo, Ziegler, JZ, 2006.04795



- need to reconfigure the magnetic field
  - most conservative no focusing,  $F=1$
  - possibly more realistic  $F=100$
- interesting reach already with 2weeks of running\*

\* projections done for  $10^8 \mu^+/s$ , PSI  $\pi E5$  beamline potentially  $10^{10} \mu^+/s$  in 2025+

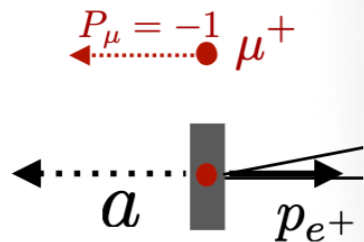
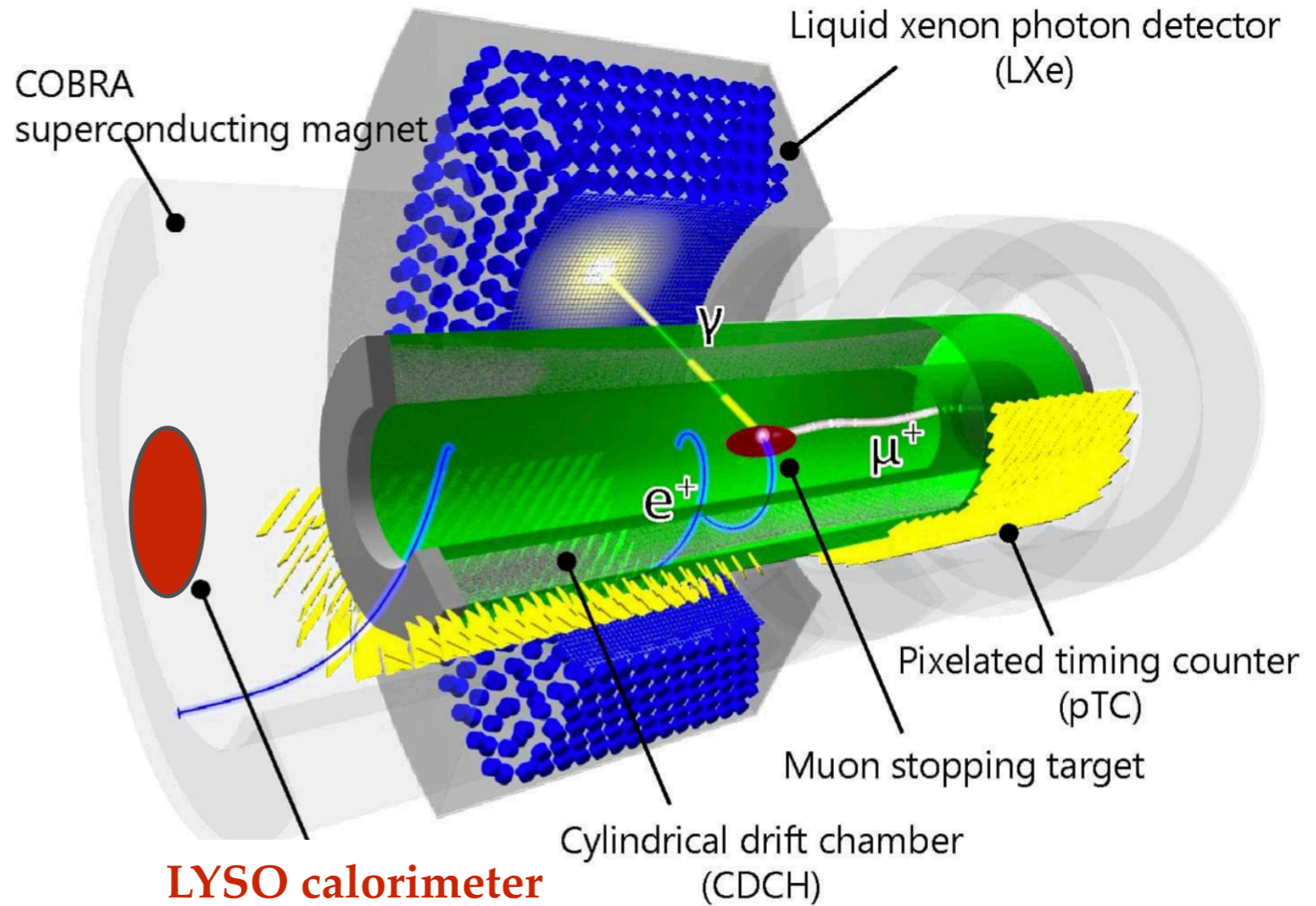
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- could be
- already has
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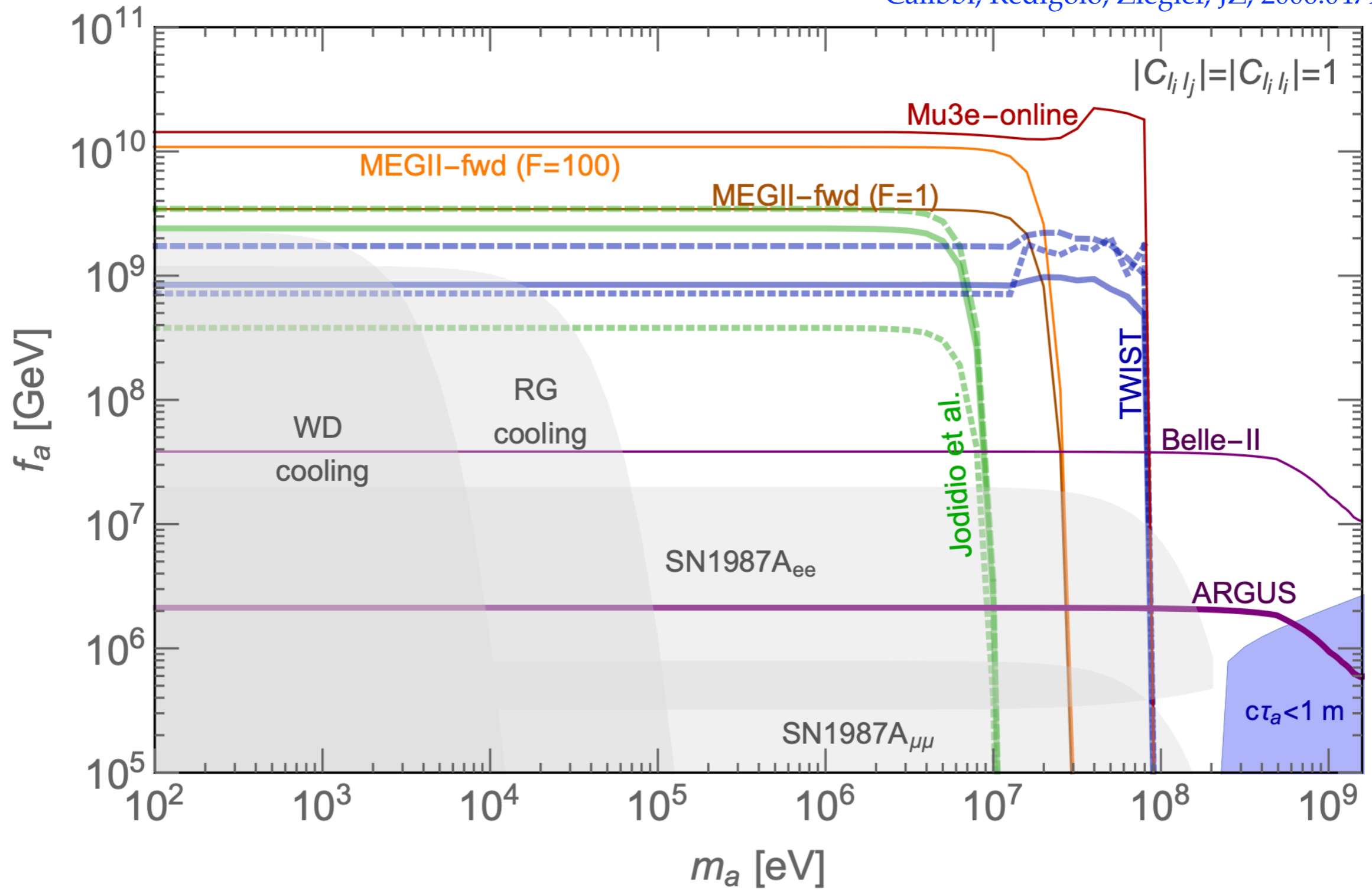
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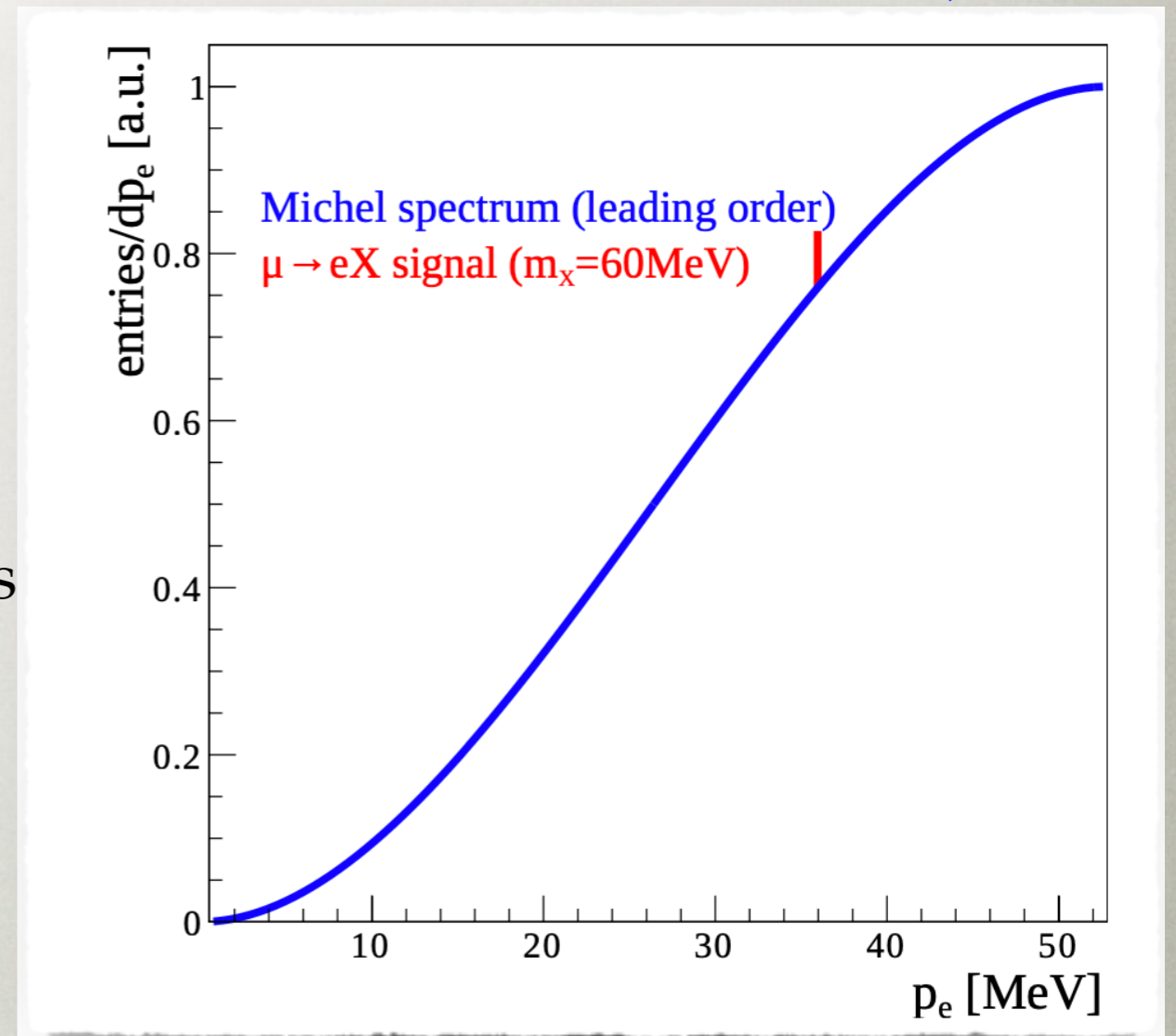




# Mu3e-online

A.-K. Perrevoort, PhD thesis  
Mu3e, 1812.00741

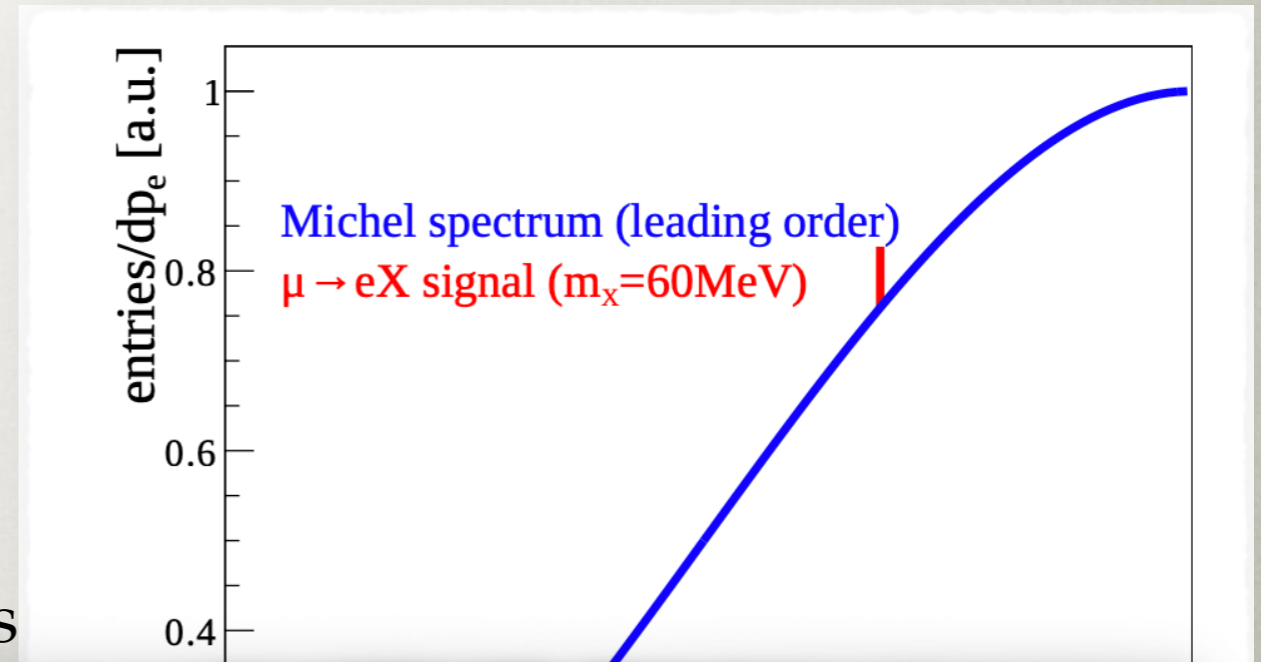
- Mu3e-online: a dedicated search strategy at Mu3e
- online event reconstruction with fgpa's
  - $p_e^\mu$  on tape from reduced info ("short tracks"=4 hits in 4 layers)
- bump hunt on Michel spectrum
  - sensitive to both LH and RH ALPs



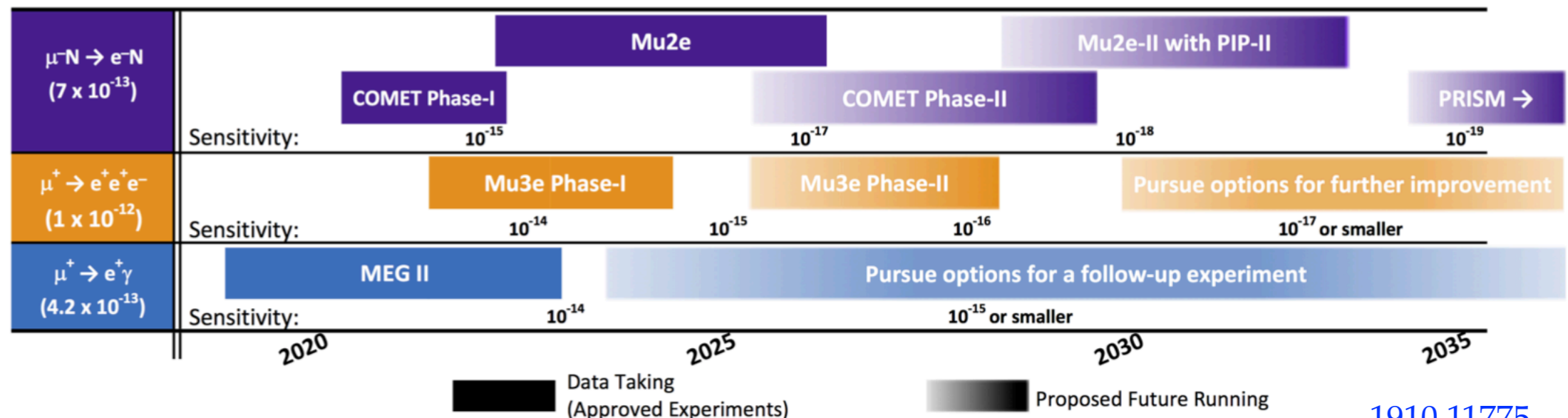
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Searches for Charged-Lepton Flavor Violation in Experiments using Intense Muon Beams



1910.11775

# ASTROPHYSICS BOUNDS

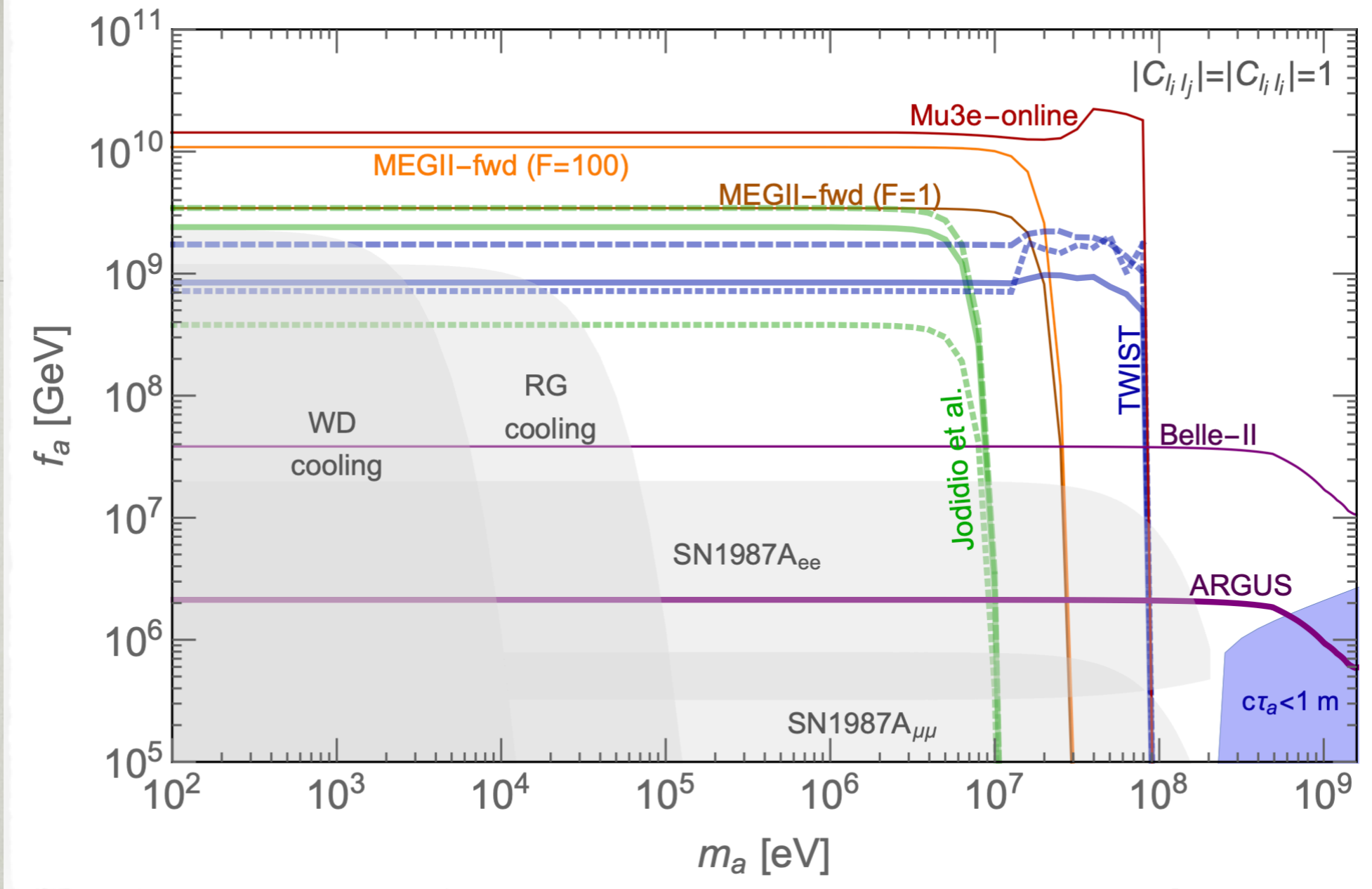
Raffelt, Weiss , hep-ph/9410205

- bounds on massless ALP-electron from red giants and white-dwarf cooling well known
  - due to  $e^- + N \rightarrow e^- + N + a$
  - we rescale to nonzero ALP masses
- above  $m_a \gtrsim 0.1$  MeV SN bounds become important (new!)
- also bounds on couplings to muons, but less severe

Bollig et al., 2005.07141

Calibbi, Redigolo, Ziegler, JZ, 2006.04795

Process	BR Limit	Present best limits		masless ALP
		Decay constant	Bound (GeV)	Experiment
Star cooling	–	$F_{ee}^A$	$4.6 \times 10^9$	WDs [44]
	–	$F_{\mu\mu}^A$	$1.6 \times 10^6$	SN $_{\mu\mu}$ [45]
	$4 \times 10^{-3}$	$F_{\mu e}$	$1.4 \times 10^8$	SN $_{\mu e}$ (Sec. 6.1)



arXiv:1904.0205

et al., 2005.07141

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# LFV ALP DARK MATTER

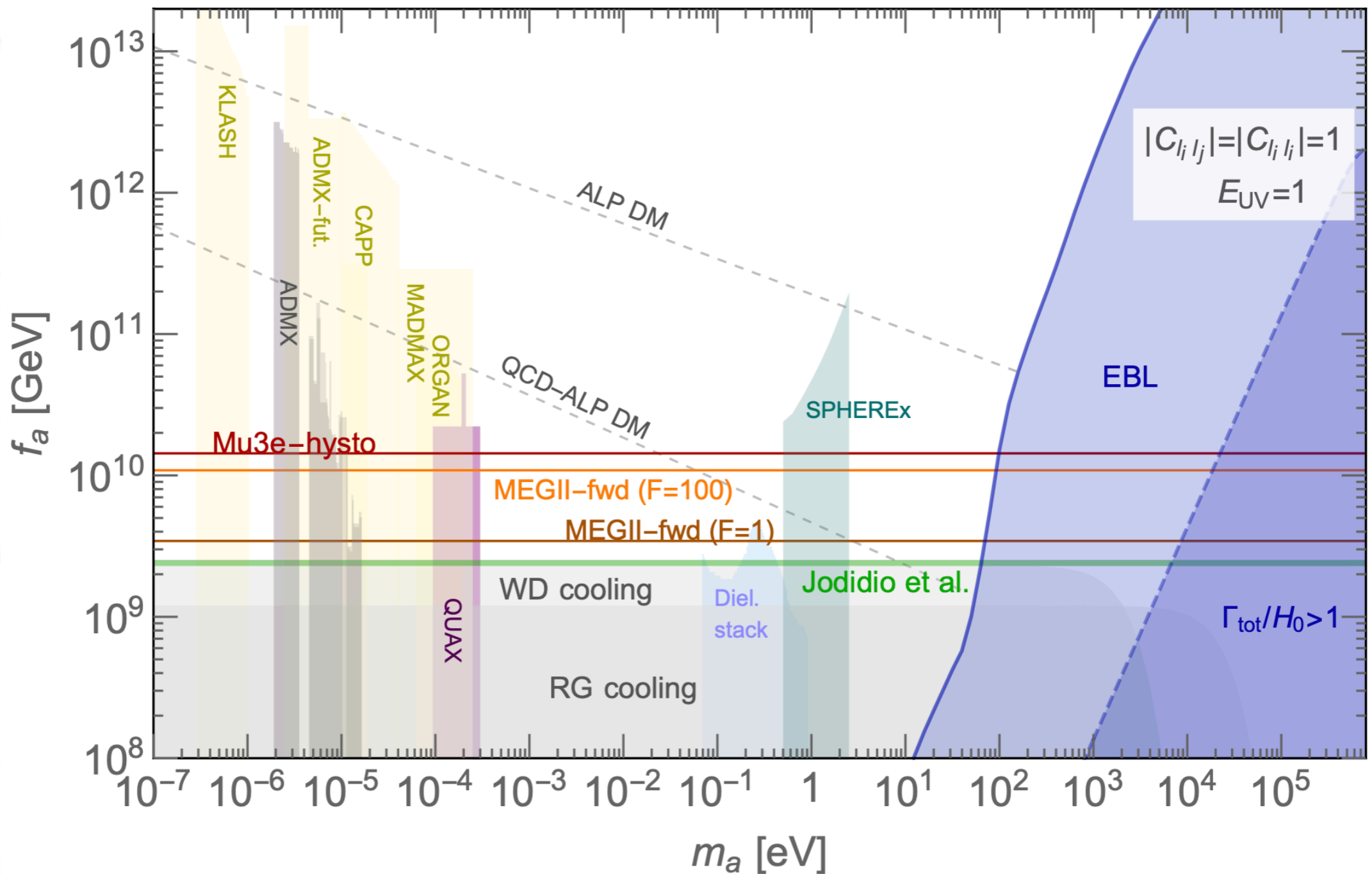
- 0-th order condition for ALP to be a DM: be stable on Hubble time
  - assume  $a \rightarrow \gamma\gamma$  dominates

$$\mathcal{L}_{\text{eff}} = E_{\text{UV}} \frac{\alpha_{\text{em}}}{4\pi} \frac{a}{f_a} F \tilde{F}$$

$$\frac{H_0}{\Gamma_{\text{tot}}} = H_0 \tau_a > 1, \quad \text{where} \quad H_0 \tau_a \simeq 5.4 \left( \frac{1}{E_{\text{eff}}^2} \right)^2 \left( \frac{10 \text{ keV}}{m_a} \right)^3 \left( \frac{f_a}{10^{10} \text{ GeV}} \right)^2.$$

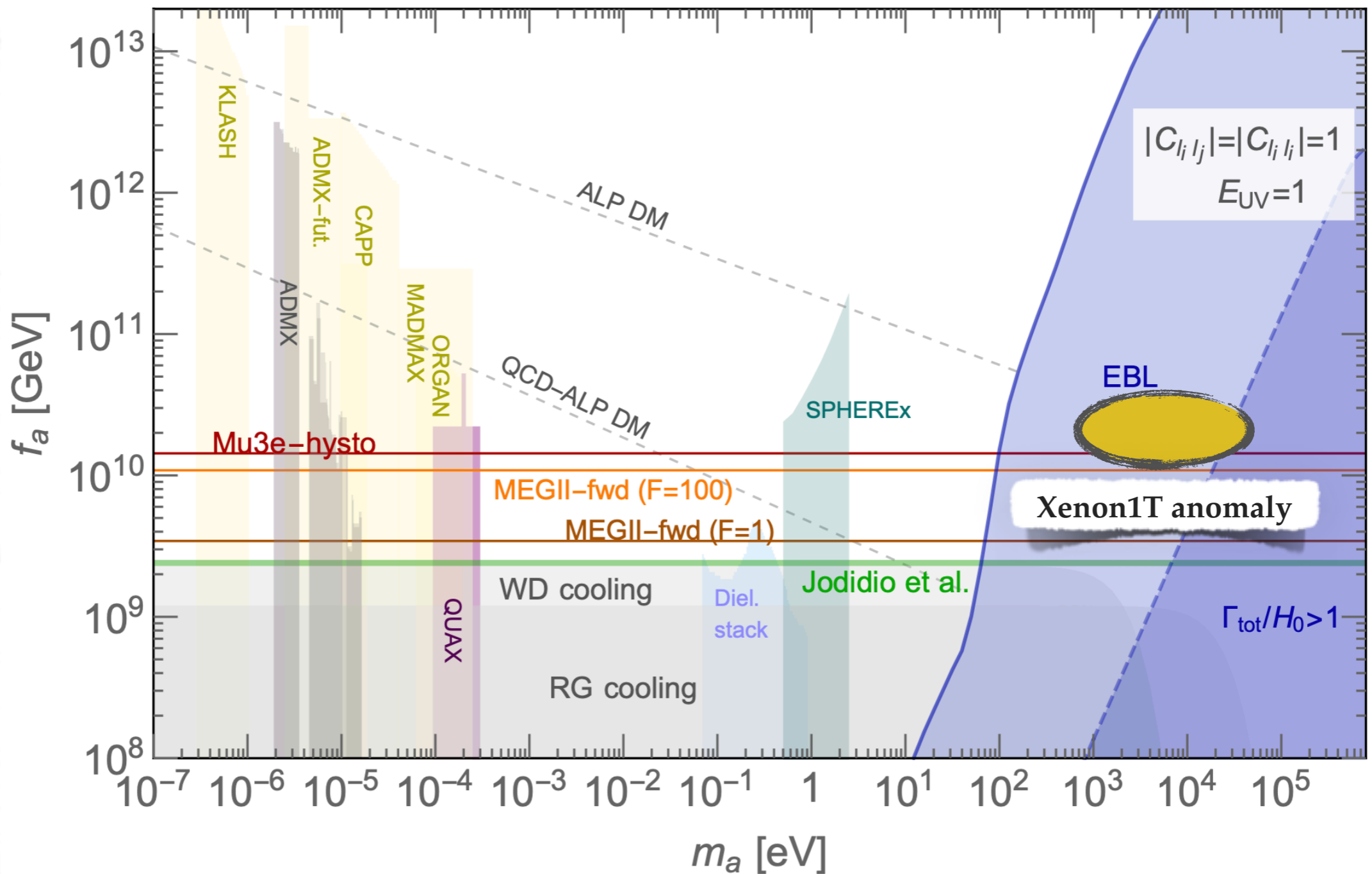
- more stringent bounds from extragalactic background light
- if ALP DM observed in a LFV process  $\Rightarrow$  for generic coupling to photons:  $m_a \lesssim 0.1 \text{ keV}$ 
  - LFV experiments most sensitive for some  $m_a$
- $a \rightarrow \gamma\gamma$  couplings may be suppressed (e.g. majoron)
  - if Xenon1T anomaly persists, MEGII-fwd and Mu3e-online can probe the relevant region

$$\frac{H_0}{\Gamma_{\text{tot}}} = H_0 \tau$$



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# SAMPLE LEPTON FLAVOR VIOLATING ALP MODELS

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Calibbi, Redigolo, Ziegler, JZ, 2006.04795

- possible to have sizeable lepton FV but small or no quark FV
  - LFV QCD axion
    - flavor structure external (by hand)
  - LFV axiflavor
    - PQ symmetry part of  $SU(2)_F \times U(1)_F$ , for quark FV CKM suppressed, for leptons PMNS mixings  $\Rightarrow$  large
  - leptonic familon
    - $U(1)$  FN separately for quarks and leptons,  $f_a$  for quarks larger
  - majoron
    - PNOB due to spontaneous breaking of the lepton number
- relation between flavor conserving and FV probes

LEPTON FLAVOR  
VIOLATING QCD AXION

# STRONG CP PROBLEM

- Lorentz and gauge invariance allow a CP violating term in QCD

$$\mathcal{L} = \theta \frac{\alpha_s}{8\pi} G_a^{\mu\nu} \tilde{G}_{a,\mu\nu} = \theta \frac{\alpha_s}{16\pi} \epsilon_{\mu\nu\rho\sigma} G_a^{\mu\nu} G_a^{\rho\sigma}$$

- physically observable is the combination

$$\bar{\theta} \equiv \theta + \arg \det(\mathcal{M}_u \mathcal{M}_d)$$

- experimentally :

$$d_n \approx 4 \times 10^{-16} \bar{\theta} \text{ e cm} \quad \longleftrightarrow \quad |d_n|_{\text{exp}} < 3 \times 10^{-26} \text{ e cm}$$

- why  $\bar{\theta}$  so small?

$$\bar{\theta} < 10^{-10}$$

- very puzzling given large CPV phase in the CKM

# QCD AXION

- if  $\bar{\theta}(x)$  a dynamical field and couples only to  $\bar{\theta}G\tilde{G} \Rightarrow$   
potential min. at  $\bar{\theta}(x) = 0$ 
  - new ultra-light particle - axion

$$F_{f_i f_j}^{V,A} \equiv \frac{2f_a}{C_{f_i f_j}^{V,A}}$$

$$\mathcal{L}_{\text{eff}} = \frac{\alpha_s}{8\pi} \frac{a}{f_a} G\tilde{G} + \frac{E}{N} \frac{\alpha_{\text{em}}}{8\pi} \frac{a}{f_a} F\tilde{F} + \frac{\partial_\mu a}{2f_a} \bar{f}_i \gamma^\mu (C_{f_i f_j}^V + C_{f_i f_j}^A \gamma_5) f_j$$

- obtains mass from QCD anomaly

$$m_a = 5.70(7) \mu\text{eV} \left( \frac{10^{12} \text{ GeV}}{f_a} \right)$$

- viable dark matter candidate (from misalignment mechanism)

$$10^{-8} \text{ eV} \lesssim m_a \lesssim 10^{-4} \text{ eV}$$

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whether FV or not  
depends on flavor structure  
of PQ symmetry

- viable dark matter candidate (from misalignment mechanism)

$$10^{-8} \text{ eV} \lesssim m_a \lesssim 10^{-4} \text{ eV}$$

# LFV QCD AXION

- DFSZ-like model: 2HDM+S:  $X_S = 1, X_{H_2} = 2 + X_{H_1}$
- flavor universal  $U(1)_{PQ}$  charges in quark sector, non-universal in leptonic

Yukawa coupl. to  $H_1$

Yukawa coupl. to  $H_2$

$$y_e = \begin{pmatrix} 0 & x & x \\ x & 0 & 0 \\ x & 0 & 0 \end{pmatrix}, \quad y'_e = \begin{pmatrix} 0 & 0 & 0 \\ 0 & x & x \\ 0 & x & x \end{pmatrix}$$

⇒ gives lepton FV coupl.s of axion

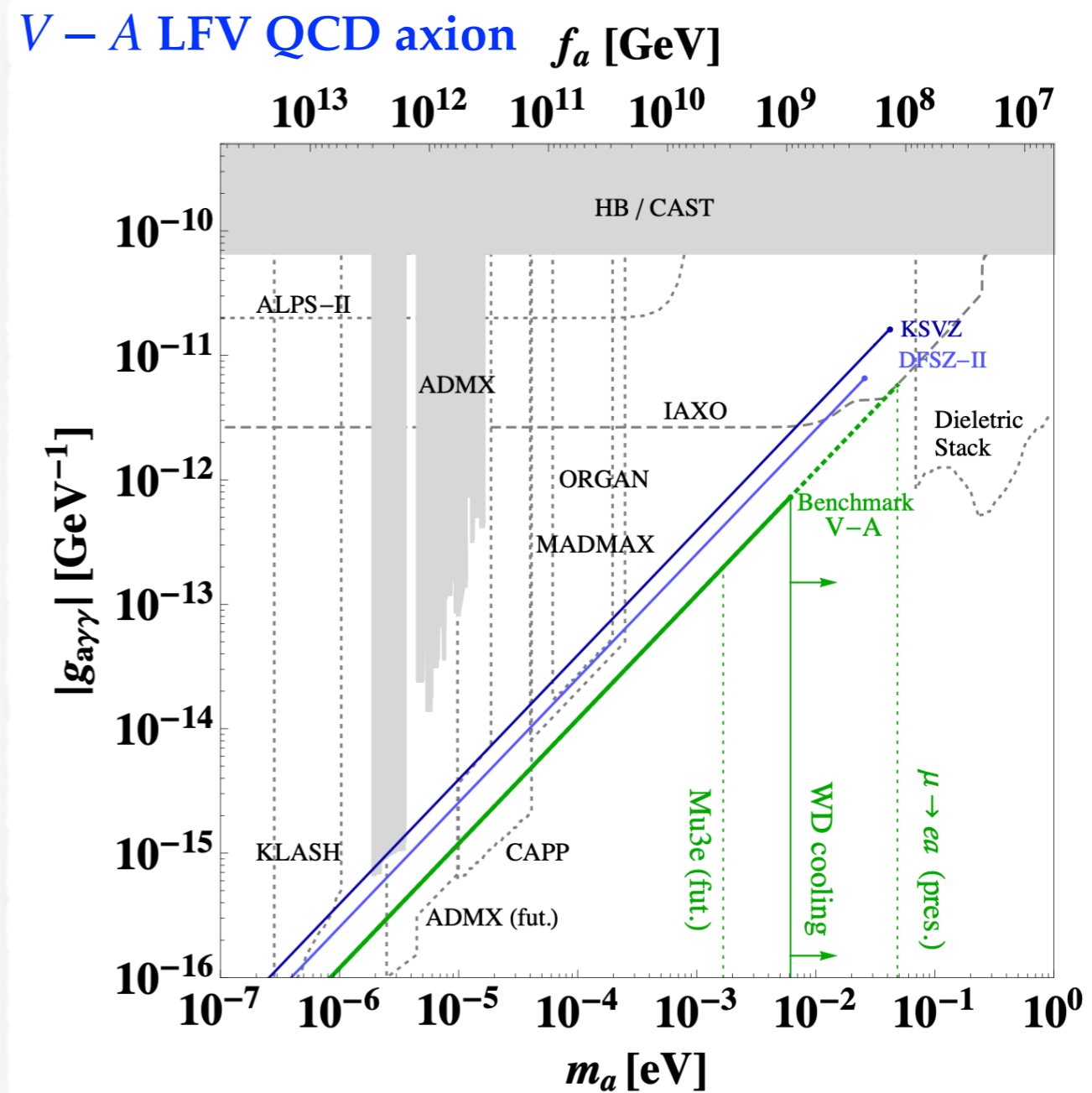
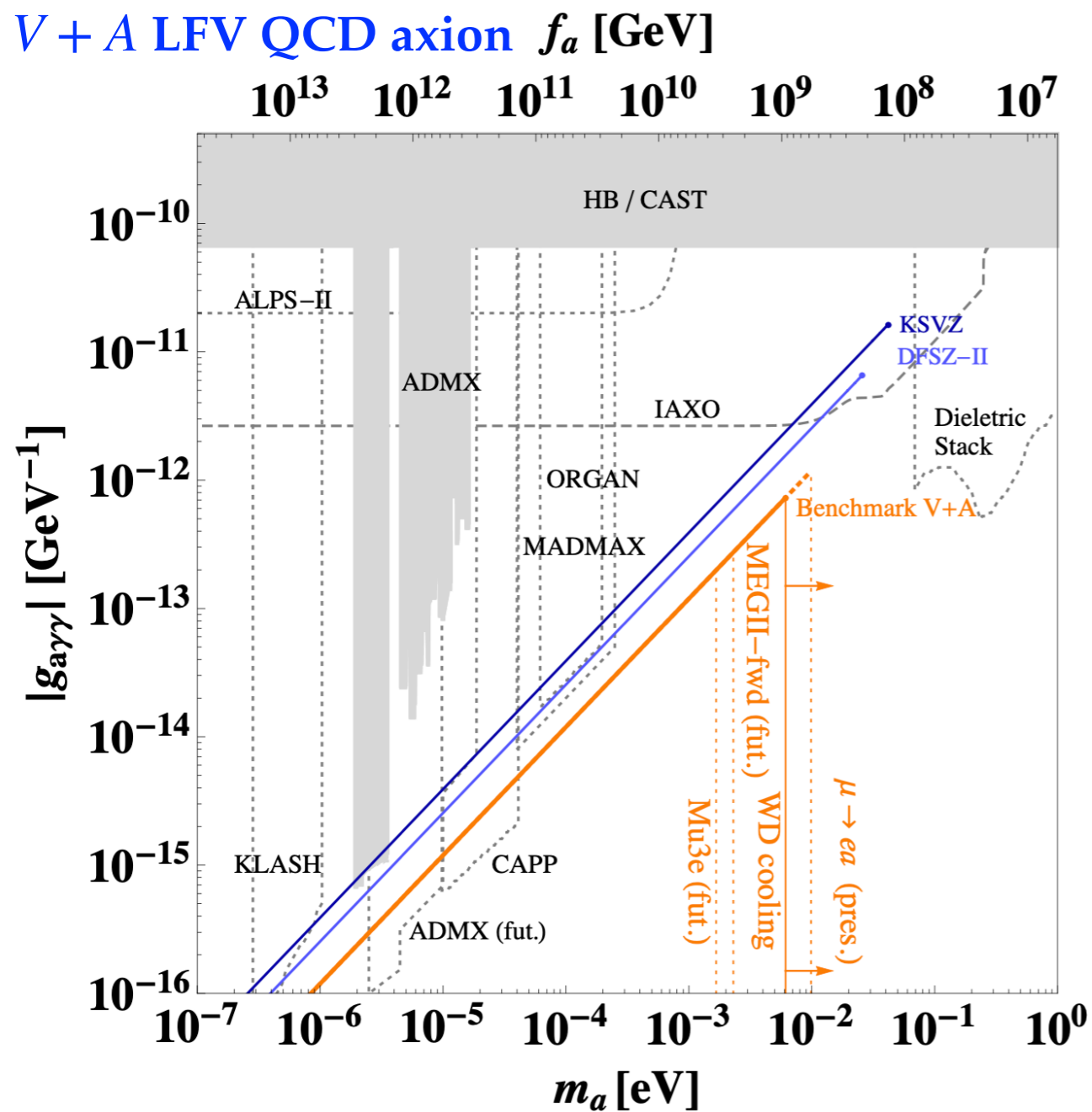
$$y_u = \begin{pmatrix} x & x & x \\ x & x & x \\ x & x & x \end{pmatrix}, \quad y_d = \begin{pmatrix} x & x & x \\ x & x & x \\ x & x & x \end{pmatrix}$$

⇒ axion-quark couplings flavor diagonal

- hierarchy of entries external input

# LFV QCD AXION

- reach of MEGII-fwd depends on RH couplings



LEPTON FLAVOR  
VIOLATING AXIFLAVON



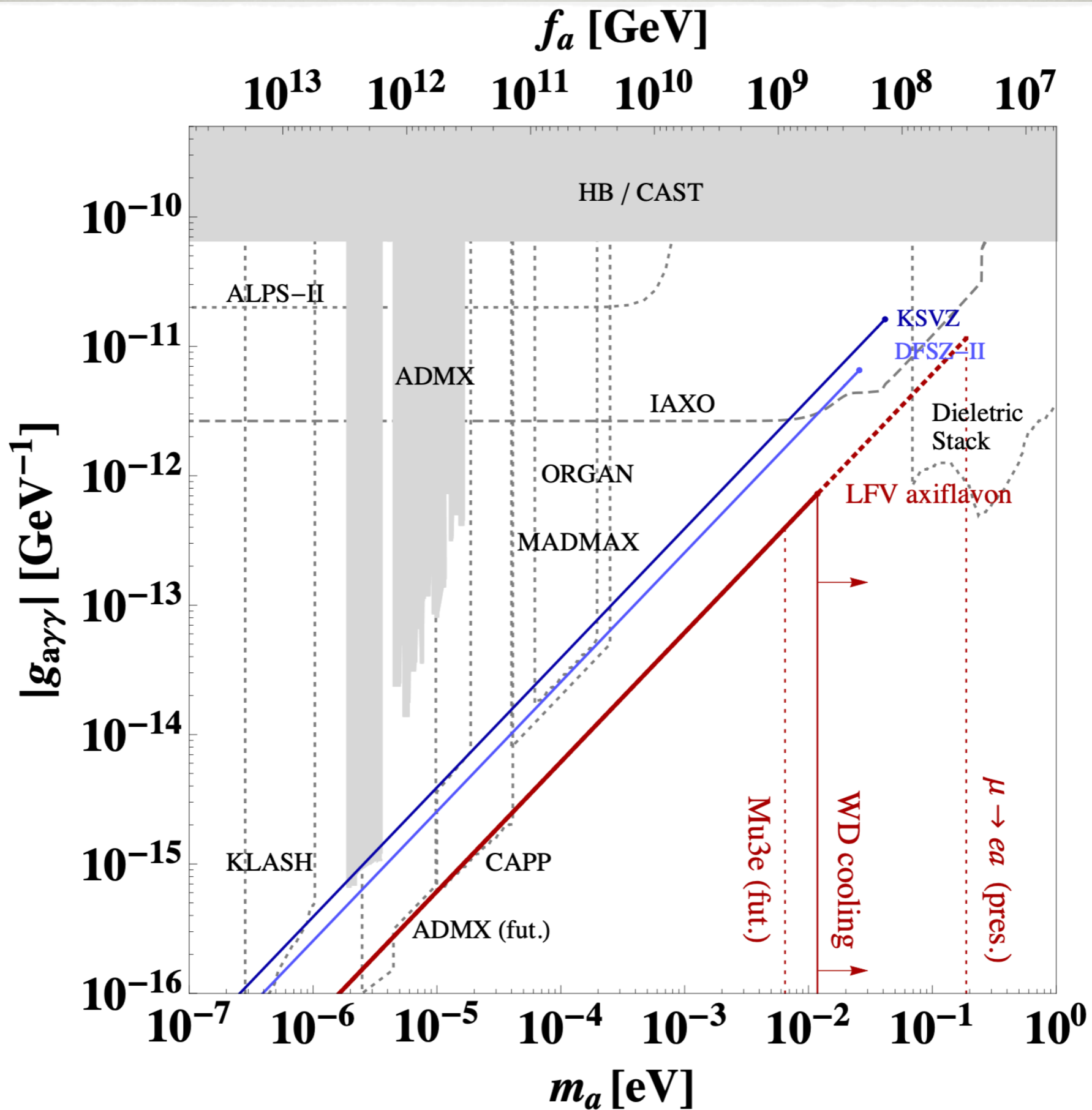
# LFV AXIFLAVON

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Calibbi, Redigolo, Ziegler, JZ, 2006.04795

see also, Linster, Ziegler, 1805.07341

- the PQ symmetry is part of  $SU(2)_F \times U(1)_F$  flavor group
  - all FV couplings need to go through 3rd generation
  - for leptons 1-2 and 1-3 mixings are larger (in LH sector to reproduce PMNS matrix)
- $\Rightarrow$  unlike minimal axiflavoron,  $K \rightarrow \pi a$  suppr.
  - the observation mode is  $\mu \rightarrow ea$



Z, 2006.04795  
r, 1805.07341

# LEPTONIC FAMILON

# LEPTONIC FAMILON

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- separate Froggatt-Nielsen U(1) for quarks and leptons
  - leptonic  $f_a$  scale assumed lower  $\Rightarrow$  these couplings dominate
  - familon mass a free parameter
- two benchmark charge assignments

$$([L]_1, [L]_2, [L]_3) = (L, L, L), \quad [\text{Pure Anarchy}].$$

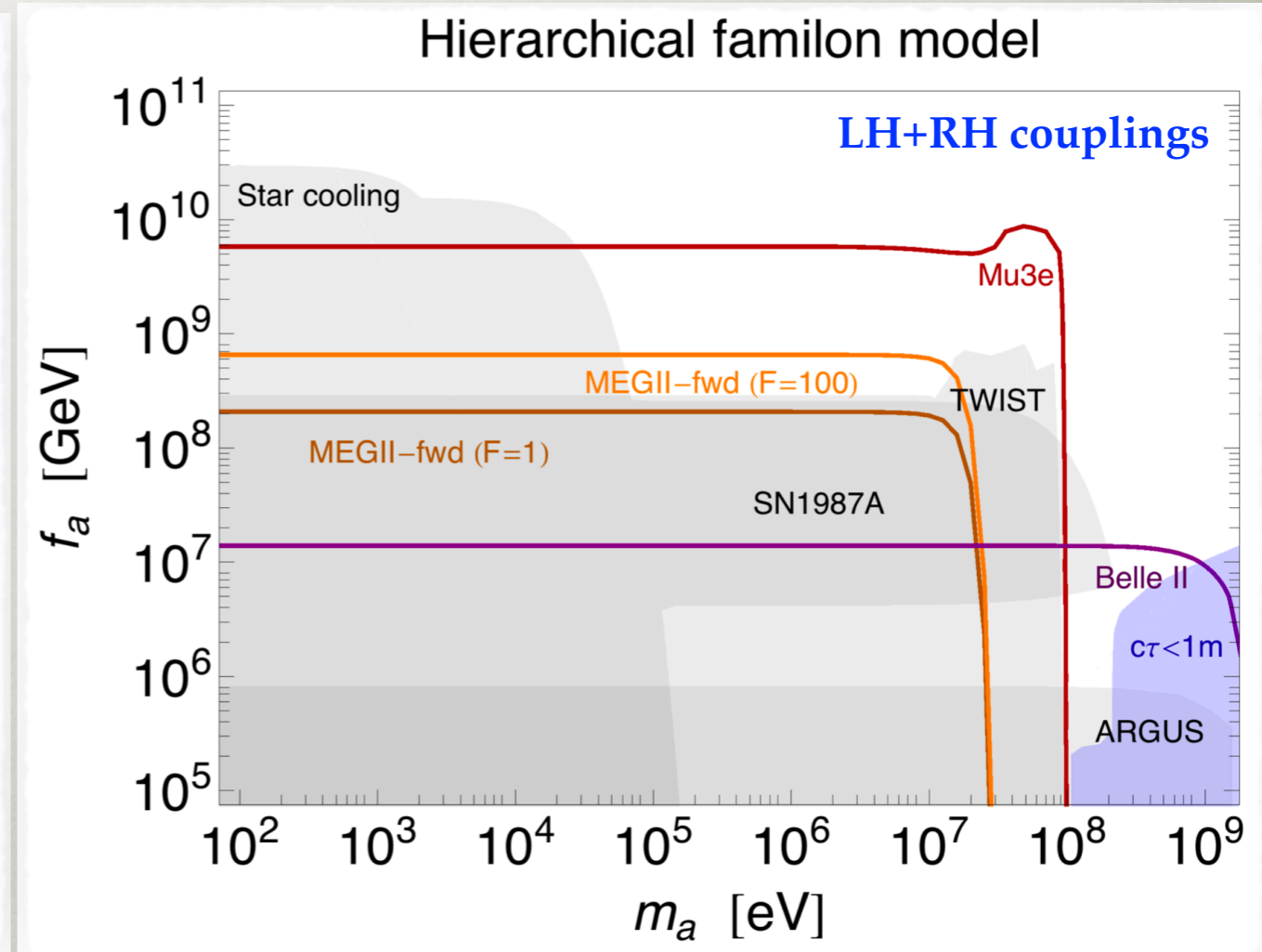
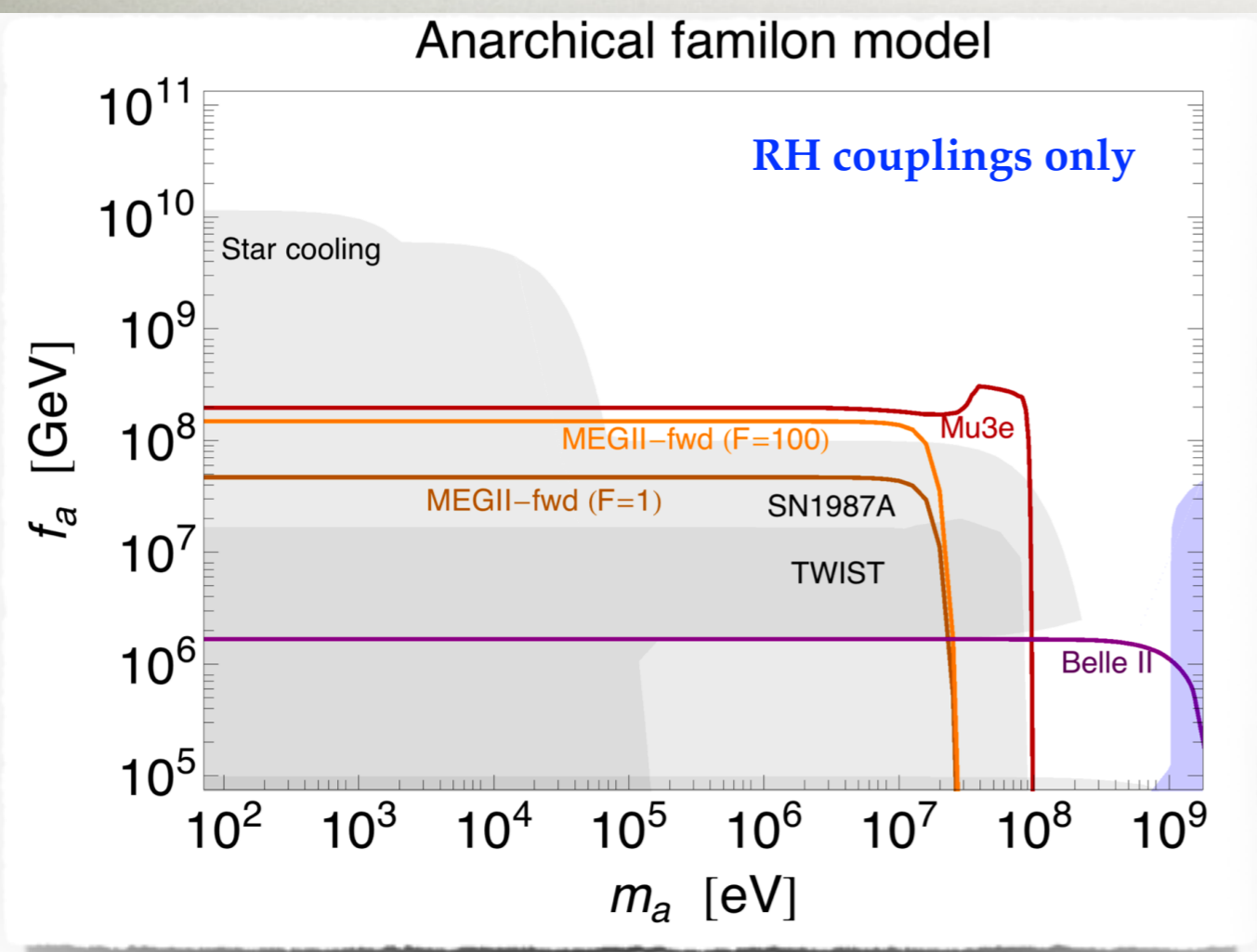
$\Rightarrow$  RH ALP

$$([L]_1, [L]_2, [L]_3) = (L + 2, L + 1, L), \quad [\text{Hierarchy}].$$

$\Rightarrow$  LH and  
RH couplings

# LEPTONIC FAMILON

- reach of MEGII-fwd depends on RH couplings



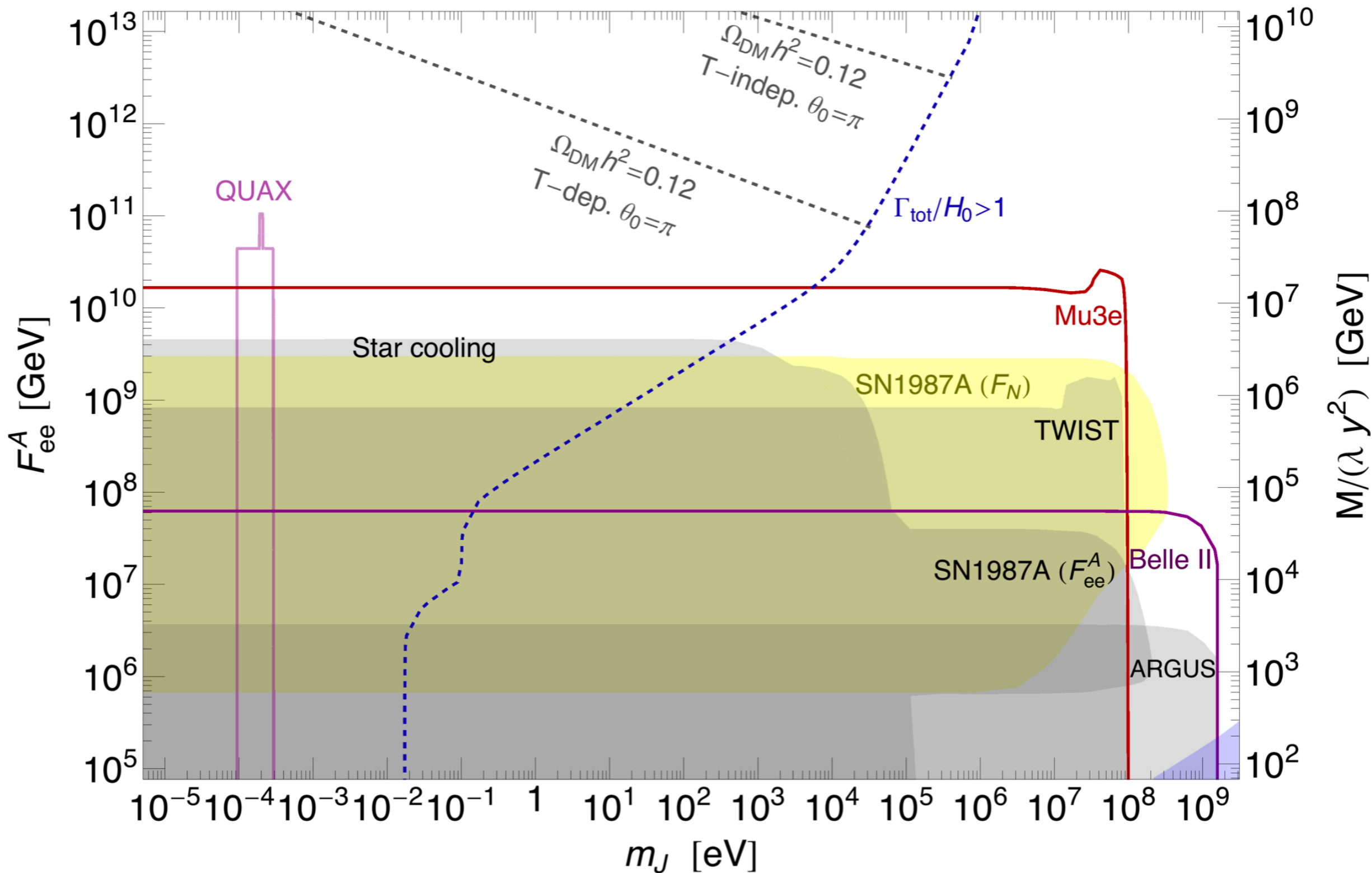
# MAJORON

# MAJORON

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- majoron- PNGB due to spontaneous breaking of the lepton number
- neutrino masses  $m_\nu \propto y_\nu y_\nu^T v^2 / m_N$
- majoron couplings,  $C_{ij} \propto y_\nu y_\nu^\dagger$
- if  $m_\nu$  suppressed by global U(1)
  - $\Rightarrow$  majoron observable
  - "low energy see-saw"

# Majoron from low-energy seesaw



● low energy see-saw



# CONCLUSIONS

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- CLFV transitions a powerful tool to search for axion like particles
- advocated for MEGII-fwd phase of MEG-II experiment
- reach well above previous experiments and above astrophysical bounds
- complementary in timing to Mu3e-online

# BACKUP SLIDES

# MOTIVATION

- FV couplings of ALPs arise quite generically
- in mass basis ( $V_L^{f\dagger} y_f V_R^f = y_f^{\text{diag}}$ ) the couplings are

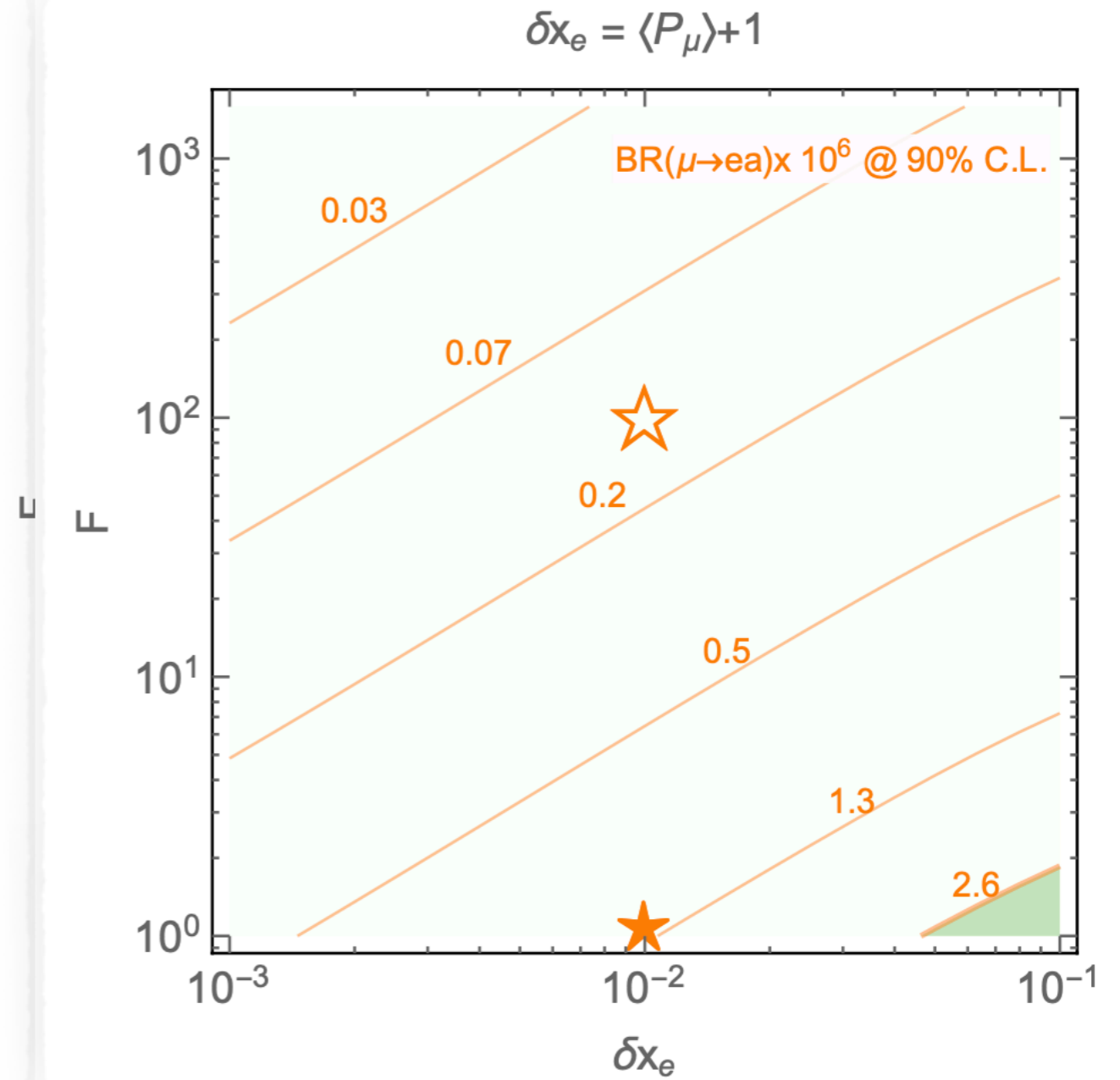
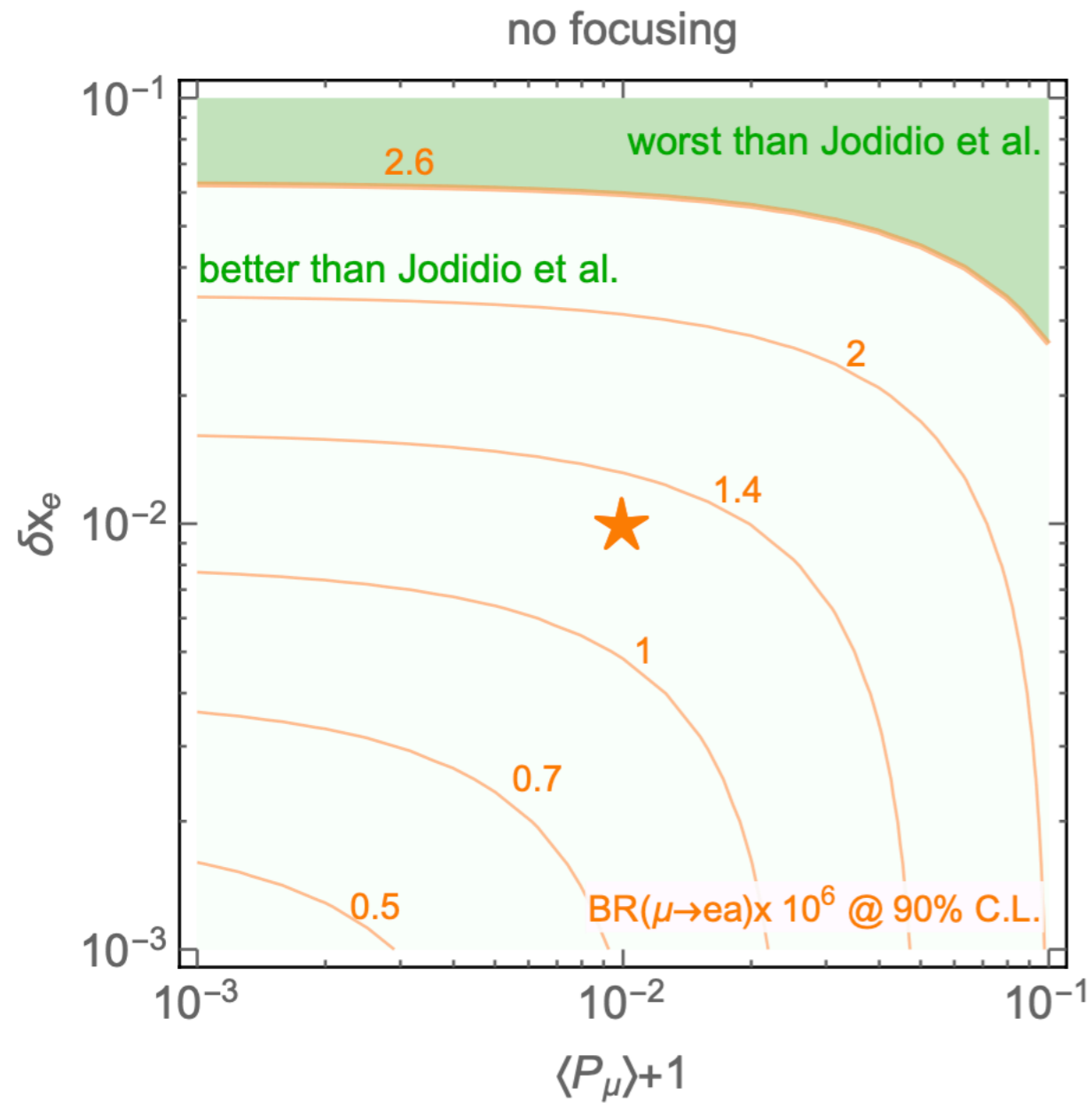
$$C_{f_i f_j}^{V,A} = \frac{1}{2N} \left( V_R^{f\dagger} X_{fR} V_R^f \pm V_L^{f\dagger} X_{fL} V_L^f \right)_{ij}$$

$$\mathcal{L}_{aff} = \frac{\partial_\mu a}{2f_a} \bar{f}_i \gamma^\mu (c_{f_i f_j}^V + c_{f_i f_j}^A \gamma_5) f_j,$$

- FV unless PQ charge matrices  $X_{f_{L,R}}$  aligned with  $y_f y_f^\dagger, y_f^\dagger y_f$
- note: we will often use

$$F_{f_i f_j}^{V,A} \equiv \frac{2f_a}{c_{f_i f_j}^{V,A}}$$

$$F_{l_i l_j} = \frac{2f_a}{\sqrt{|C_{l_i l_j}^V|^2 + |C_{l_i l_j}^A|^2}}$$



# EXPLICIT MODEL - AXIFLAVON

Froggatt, Nielsen, NPB 147, 277 (1979),...

- Large hierarchies in quark + lepton masses and in CKM matrix
  - can be addressed via horizontal  $U(1)_H$  symmetry
  - SM LH and RH fermions have different  $U(1)_H$  charges
  - hierarchical Higgs Yukawas after  $U(1)_H$  broken via vev of scalar field, the flavon  $\Phi$

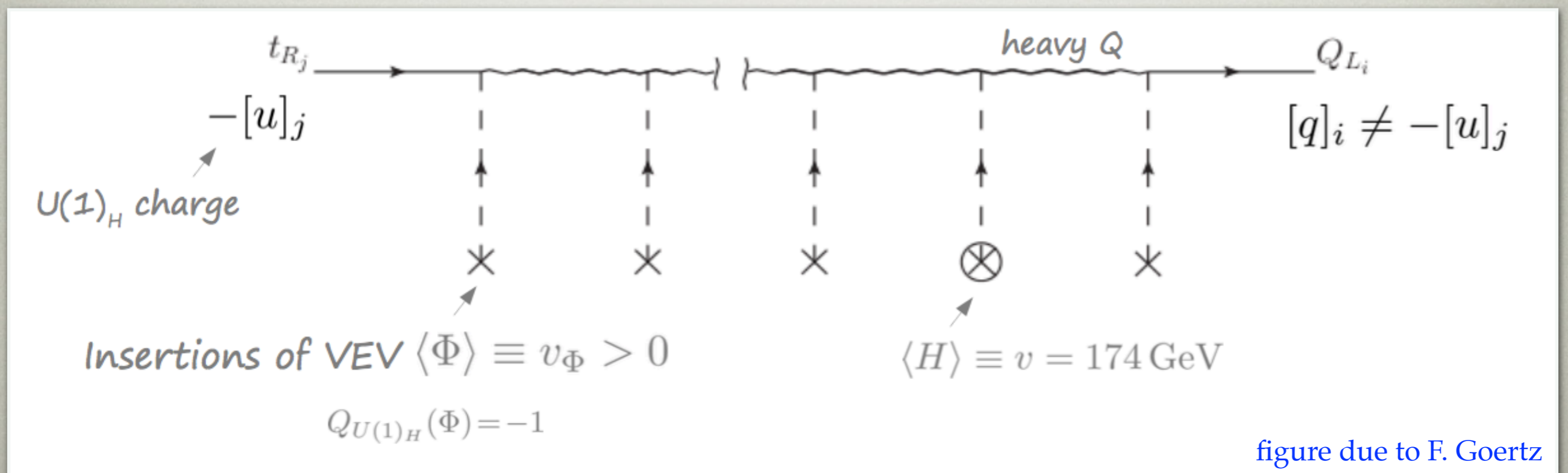


figure due to F. Goertz

# AXIFLAVON

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- ingredients for axion mechanism
  - need a global PQ symmetry that is spontaneously broken  
 $\Rightarrow$  Goldstone boson is the axion
  - global symmetry needs to be anomalous under QCD
- flavor symmetries that explain Yukawa hierarchies have a QCD anomaly
- axiflavor mechanism: identify PQ symmetry with FN  $U(1)_H$ 
  - the phase of the flavon is the QCD axion = axiflavor

$$\Phi = \frac{f + \phi(x)}{\sqrt{2}} e^{ia(x)/f}$$

Wilczek, PRL 49, 1549 (1982)

Calibbi, Goertz, Redigolo, Ziegler, JZ, 1612.08040

Ema, Hamaguchi, Moroi, Nakayama, 1612.05492

# ALPs IN TAU DECAYS

- for  $\tau \rightarrow \ell a$  the challenge is the extra missing energy
  - $e^+e^- \rightarrow \tau^+(\rightarrow \ell^+a)\tau^-(\rightarrow \rho^0\pi^-\nu_\tau)$
- can only boost to pseudo-rest frame of tau
- current bound from ARGUS 1995

$$\text{BR}(\tau \rightarrow \mu a) < 4.5 \times 10^{-3} \quad (95\% \text{ C.L.}) \quad \Rightarrow \quad F_{\tau\mu} \gtrsim 3.3 \times 10^6 \text{ GeV} .$$

ARGUS, 1995

$$\text{Belle (1/ab) prospect: } \text{BR}(\tau \rightarrow \mu a) < 1.1 \times 10^{-4} \quad \Rightarrow \quad F_{\tau\mu} \gtrsim 2.1 \times 10^7 \text{ GeV} .$$

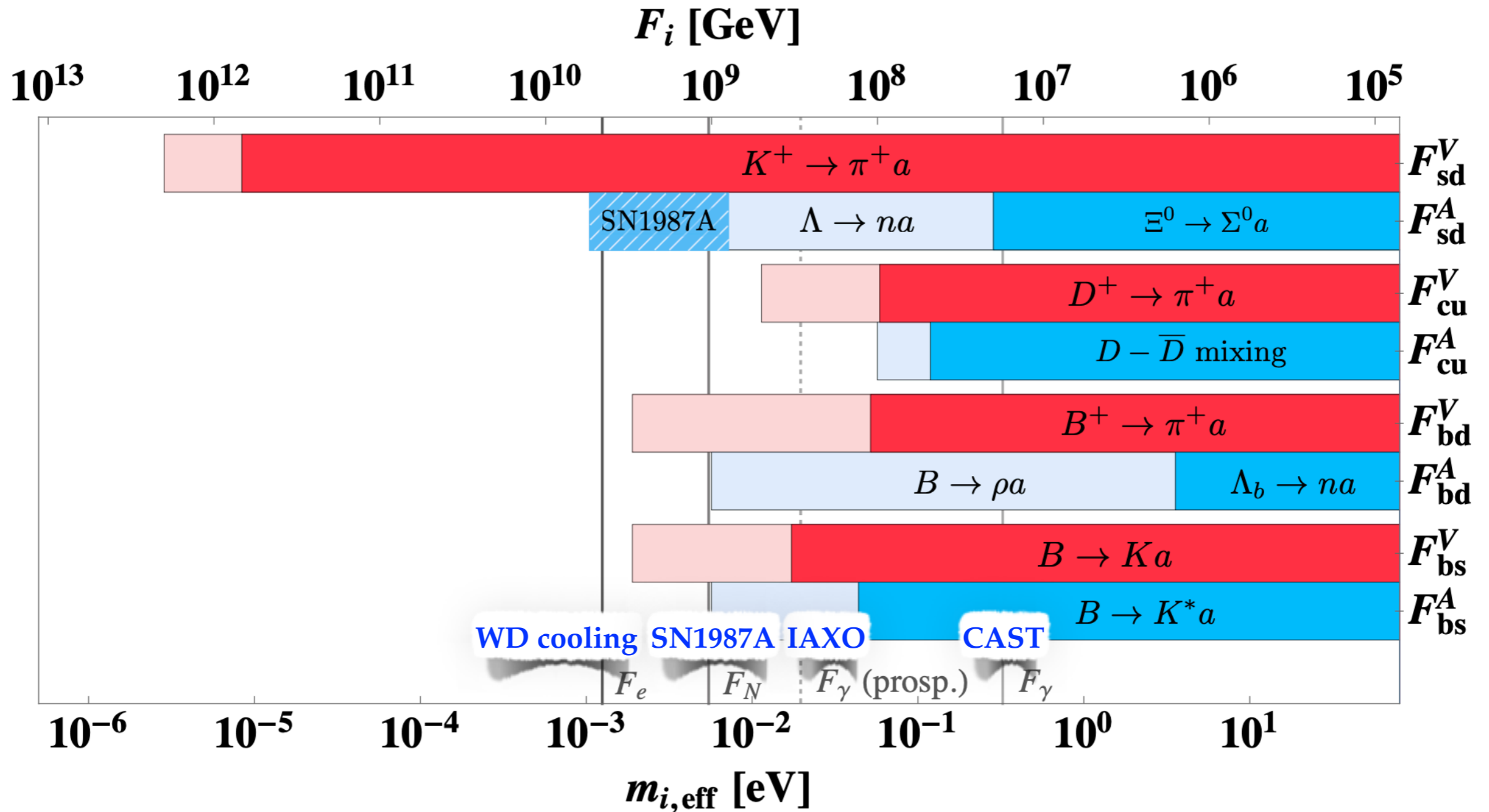
Belle, 2017

$$\text{Belle-II (50/ab) prospect: } \text{BR}(\tau \rightarrow \mu a) < 1.4 \times 10^{-5} \quad \Rightarrow \quad F_{\tau\mu} \gtrsim 5.6 \times 10^7 \text{ GeV} .$$

our naive rescaling

# THE STRONGEST FV CONSTRAINTS

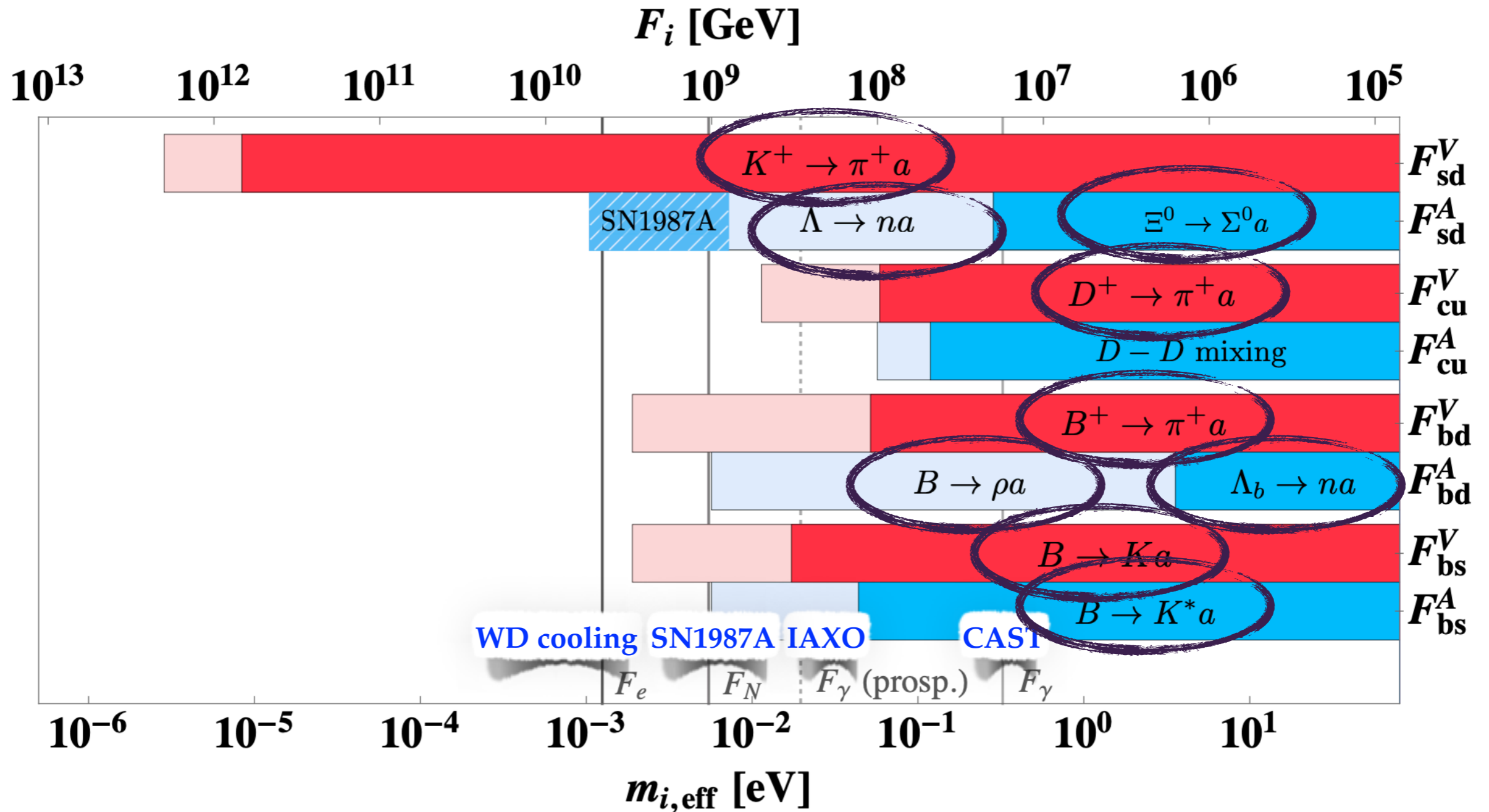
Martin Camalich, Pospelov, Vuong, Ziegler, JZ, 2002.04623



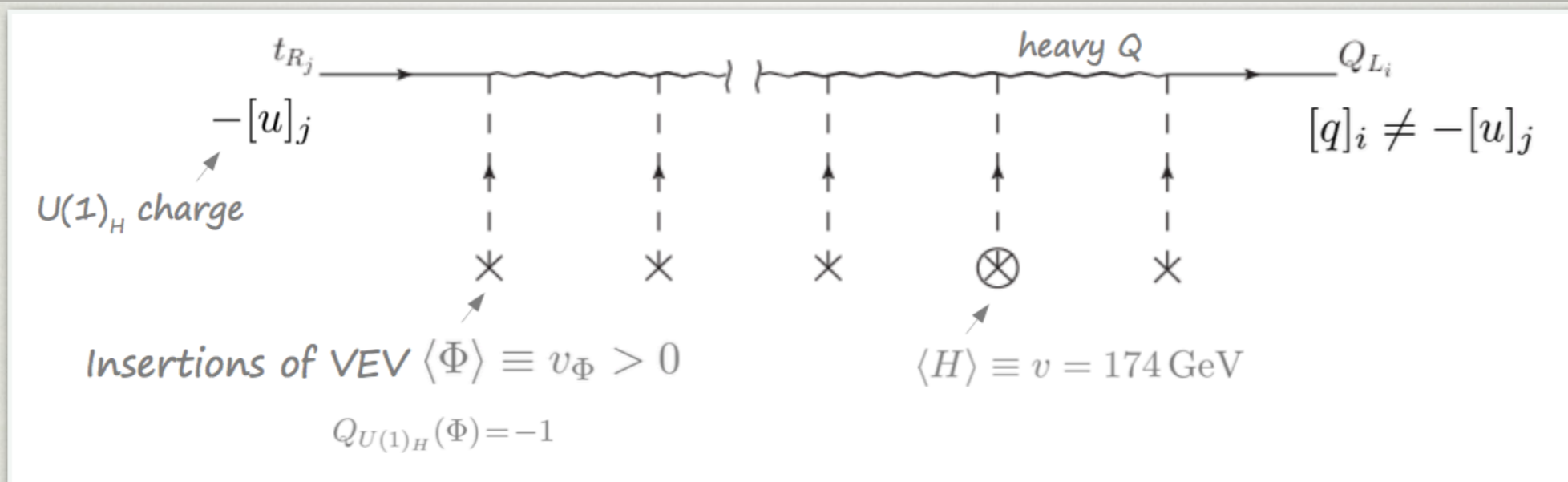


# THE STRONGEST FV CONSTRAINTS

Martin Camalich, Pospelov, Vuong, Ziegler, JZ, 2002.04623



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- effective Yukawas governed by flavon insertions (so that invariant under flavor symm.)

$$\mathcal{L}_{eff} \sim \left( \frac{\phi}{\Lambda_F} \right)^{x_{ij}} h \bar{q}_i u_j$$

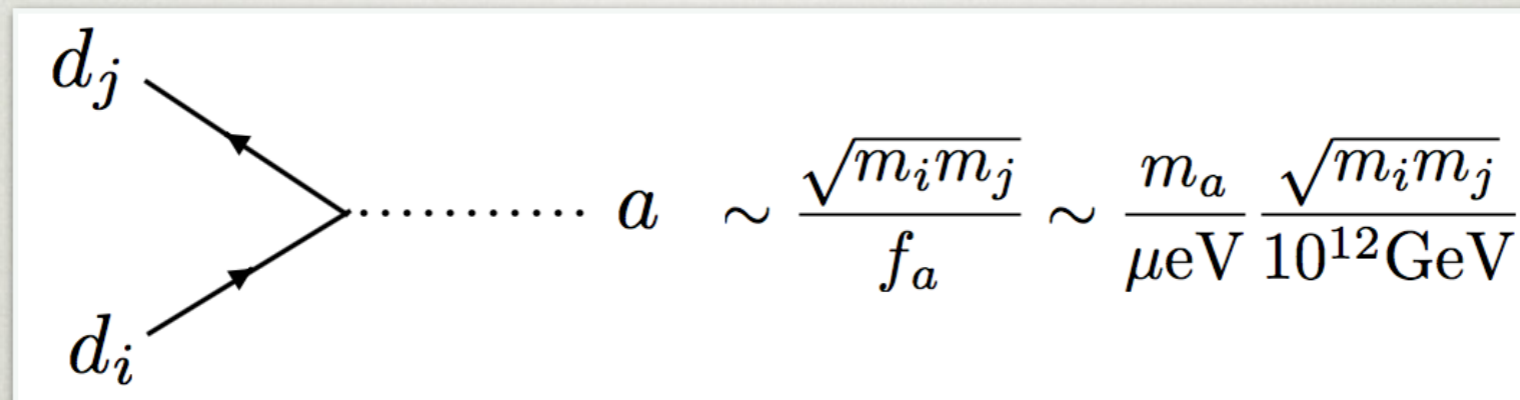
$$\epsilon \equiv \frac{\phi}{\Lambda_F}$$

- hierarchy from powers of small parameter  $\epsilon$

# SEARCHING FOR AXIFLAVON

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- axiflavor
- flavor violating couplings to fermions
  - in the minimal FN axiflavor model


$$d_j \quad d_i \quad \dots \quad a \quad \sim \frac{\sqrt{m_i m_j}}{f_a} \sim \frac{m_a}{\mu\text{eV}} \frac{\sqrt{m_i m_j}}{10^{12}\text{GeV}}$$

- in addition to flavor diagonal couplings to electrons, nucleons, couplings to photons, gluons

# SEARCHING FOR AXIFLAVON

## minimal axiflavoron

Calibbi, Goertz, Redigolo, Ziegler, JZ, 1612.08040

