

Forward Jet Production within small-x/TMD factorization framework

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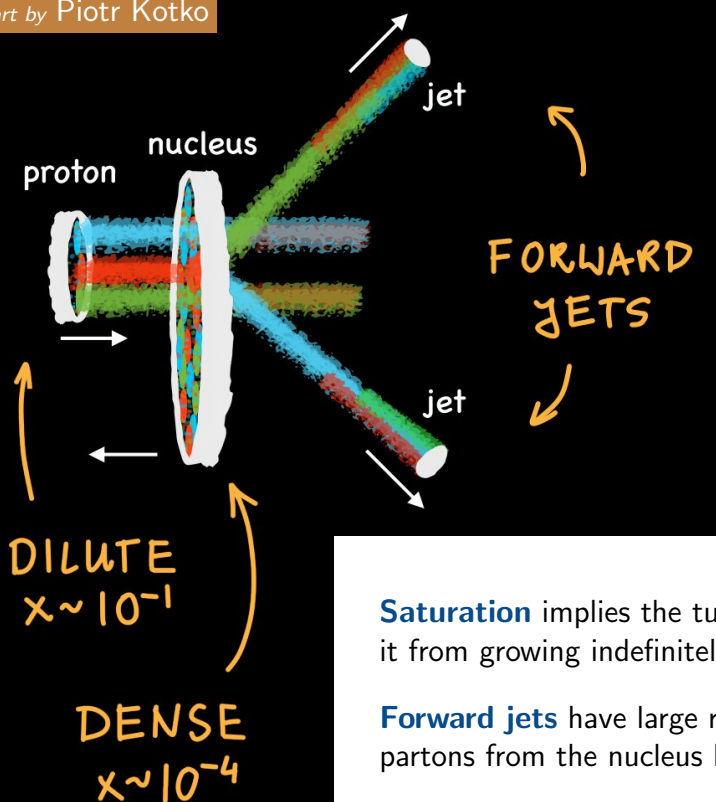
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QCD evolution, dilute vs. dense, forward jets

art by Piotr Kotko



A **dilute** system carries a few **high- x** partons contributing to the hard scattering.

A **dense** system carries many **low- x** partons.

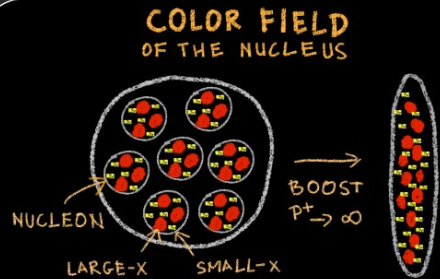
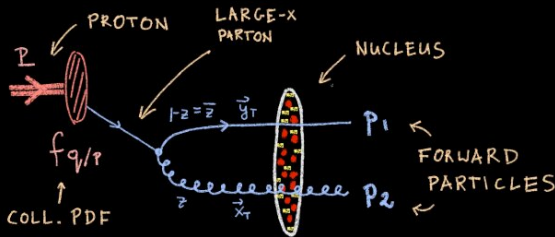
At high density, gluons are imagined to undergo recombination, and to saturate.

This is modeled with non-linear evolution equations, involving explicit **non-vanishing k_T** .

Saturation implies the turnover of the gluon density, stopping it from growing indefinitely for small x .

Forward jets have large rapidities, and trigger events in which partons from the nucleus have small x .

pA (dilute-dense) collisions within CGC

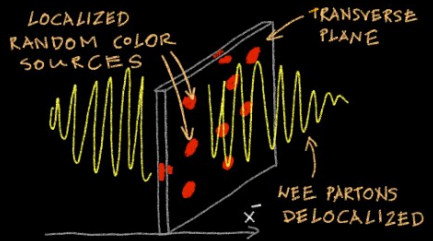


[L. McLerran, R. Venugopalan, 1993]

$$\frac{d\sigma_{qA \rightarrow 2j}}{d^3p_1 d^3p_2} \sim \int \frac{d^2x}{(2\pi)^2} \frac{d^2x'}{(2\pi)^2} \frac{d^2y}{(2\pi)^2} \frac{d^2y'}{(2\pi)^2} e^{-i\vec{p}_T \cdot (\vec{x}_T - \vec{x}'_T)} e^{-i\vec{p}'_T \cdot (\vec{y}_T - \vec{y}'_T)}$$

$\times \psi_z^*(\vec{x}'_T - \vec{y}'_T) \psi_z(\vec{x}_T - \vec{y}_T)$ ← QUARK WAVE FUNCTION
 $\times \left\{ S_x^{(6)}(\vec{y}_T, \vec{x}_T, \vec{y}'_T, \vec{x}'_T) - S_x^{(4)}(\vec{y}_T, \vec{x}_T, \vec{z}\vec{y}'_T + \vec{z}\vec{x}'_T) \right.$
 $\left. - S_x^{(4)}(\vec{z}\vec{y}_T + \vec{z}\vec{x}_T, \vec{y}'_T, \vec{x}'_T) - S_x^{(2)}(\vec{z}\vec{y}_T + \vec{z}\vec{x}_T, \vec{z}\vec{y}'_T + \vec{z}\vec{x}'_T) \right\}$

← CORRELATORS OF WILSON LINES
 $S_x^{(2)}(\vec{y}_T, \vec{x}_T) = \frac{1}{N_c} \langle \text{Tr} U(\vec{y}_T) U^\dagger(\vec{x}_T) \rangle_x$
 $S_x^{(4)}(\vec{z}\vec{y}_T, \vec{x}_T) = \frac{1}{2C_F N_c} \langle \text{Tr} [U(\vec{z}\vec{y}_T) U^\dagger(\vec{y}_T)] \text{Tr} [U(\vec{y}_T) U^\dagger(\vec{x}_T)] \rangle_x$
 etc...



Large-x partons — the color source for wee partons:
 $(D_\mu F^{\mu\nu})_a(x^-, \vec{x}_T) = \delta^{\nu+} \rho_a(\vec{x}_T) \delta(x^-)$
 RANDOM DISTRIBUTION OF COLOR SOURCES

AVERAGE OVER COLOR SOURCES
 GAUSSIAN FUNCTIONAL → $\mathcal{W}_x[\rho]$
 B-JIMWLK EVOLUTION IN X

$$U(\vec{x}_T) = \mathcal{P} \exp \left\{ ig \int_{-\infty}^{+\infty} dx^+ A_a^-(x^+, \vec{x}_T) t^a \right\}$$

[C. Marquet, 2007]

[Balitsky-Jalilian-Marian-Iancu-McLerran-Weigert-Leonidov-Kovner, 1996-2002]

Small-x Improved TMD Factorization (ITMD)

Factorization formula for forward dijets in p-p and p-A collisions

[PK, K. Kutak, C. Marquet, E. Petreska, S. Sapeta, A. van Hameren, 2015]

$$\frac{d\sigma_{pA \rightarrow 2j+X}}{dy_1 dy_2 d^2p_{T1} d^2p_{T2}} \sim \sum_{a,c,d} f_{alp}(x_1, \mu) \sum_{i=1,2} K_{ag \rightarrow cd}^{(i)}(k_T) \Phi_{ag \rightarrow cd}^{(i)}(x_2, k_T)$$

RAPIDITY

TRANSVERSE
MOMENTA

COLLINEAR
PROTON PDF

GAUGE
INVARIANT
OFF-SHELL
HARD FACTORS

TMD GLUON
DISTRIBUTIONS
AT SMALL-X

$$x_2 \ll x_1 \quad |\vec{p}_{T1} + \vec{p}_{T2}| = k_T$$

TWO PER CHANNEL
($g^*q \rightarrow qg, g^*g \rightarrow gg, g^*g \rightarrow q\bar{q}$)

ITMD factorization formula has been proven from the Color Glass Condensate (CGC) theory.

⇒ RESUMMATION OF KINEMATIC TWISTS AND NEGLECTING GENUINE TWISTS.

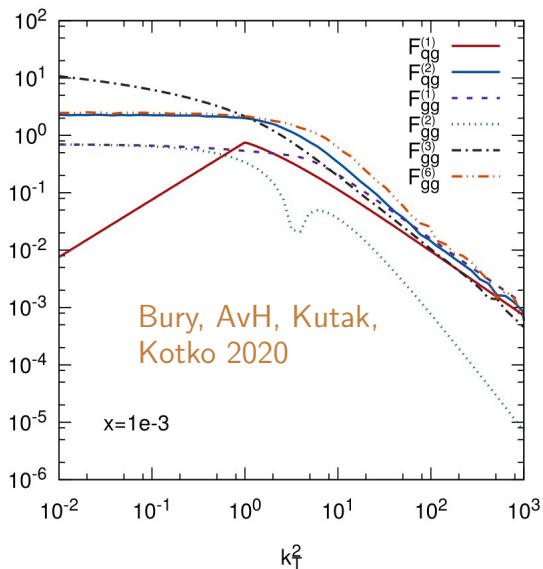
$$\Lambda_{\text{QCD}} \ll Q_s \ll P_T$$

SATURATION SCALE

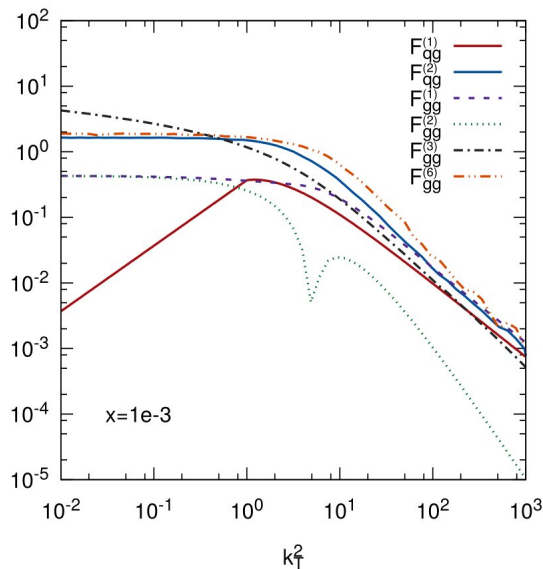
[T. Altinoluk, R. Boussarie, PK, 2019]

ITMD gluons

KS gluon TMDs in proton



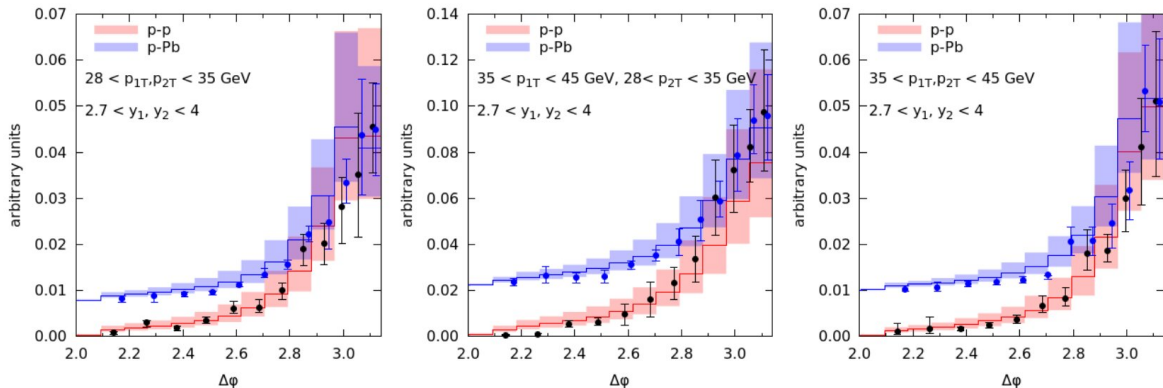
KS gluon TMDs in lead



- KS gluon (Kutak, Sapeta 2012) is the dipole-distribution as a solution to the BK equation (Balitsky 1996, Kovchegov 1999) formulated in the momentum space with corrections of higher order, and fitted to F_2 data.
- ITMD gluons follow from the KS gluon

Study of saturation using dijet production in p-p and p-Pb collisions.
Angle $\Delta\phi$ between the jets is particularly sensitive to saturation effects.

Data points from **ATLAS 2019**. Arbitrary normalization and relative shift to to accentuate the difference in shape between p-p and p-Pb.



Calculations were performed within ITMD factorization.

Besides saturation, the inclusion of resummed Sudakov logarithms is essential to reach this accuracy, included here via event-reweighting.

Independent cross-checks with KATIE (<http://bitbucket.org/hameren/katie>) and LxJet (<http://nz42.ifj.edu.pl/~pkotko/LxJet.html>).

Outlook

- Improvement of the Sudakov resummation (starting from eg. [Mueller, Xiao, Yuan 2013](#)).
- Inclusion of linearly dependent gluon distributions in higher jet-multiplicity calculations, i.e. extending ITMD* ([Bury, AvH, Kotko, Kutak 2020](#)) to complete ITMD.
- Increasing the perturbative order to NLO.

Thank you for your attention.