

Exotic B and L Violating Processes

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How exotic?

A) $\Delta B > 1, \Delta L > 1, \dots$ in EFT (heavy new physics). [Weinberg, '80]

- E.g. $pp \rightarrow e^+e^+$ or $p \rightarrow e^+\bar{\nu\nu}$.

B) Flavored ΔB & ΔL .

- E.g. $p \rightarrow e^-\mu^+\mu^+$ or $t \rightarrow \bar{c}b \tau^+$ ($\rightsquigarrow n \rightarrow \pi^0 \bar{\nu}_\tau$).

[Hambye, JH, PRL '18]

[Marciano '95; Hou, Nagashima, Soddu, '05]

C) ΔB & ΔL with *light* new particles.

- E.g. $n \rightarrow \pi^0 \chi$ or $p \rightarrow e^+ \chi$. See talks by Fornal and McKeen.

D) Dark matter induced ΔB & ΔL .

- E.g. $DM p \rightarrow n e^+, DM p \rightarrow DM' e^+, DM n \rightarrow DM' \pi^0$.

[Kile, Soni, '09; Davoudiasl, Morrissey, Sigurdson, Tulin, PRL '10 & PRD '11; ...]

Homework: everything together.

Standard Model effective field theory

- EFT with Majorana neutrinos: [Weinberg, '79 & '80]

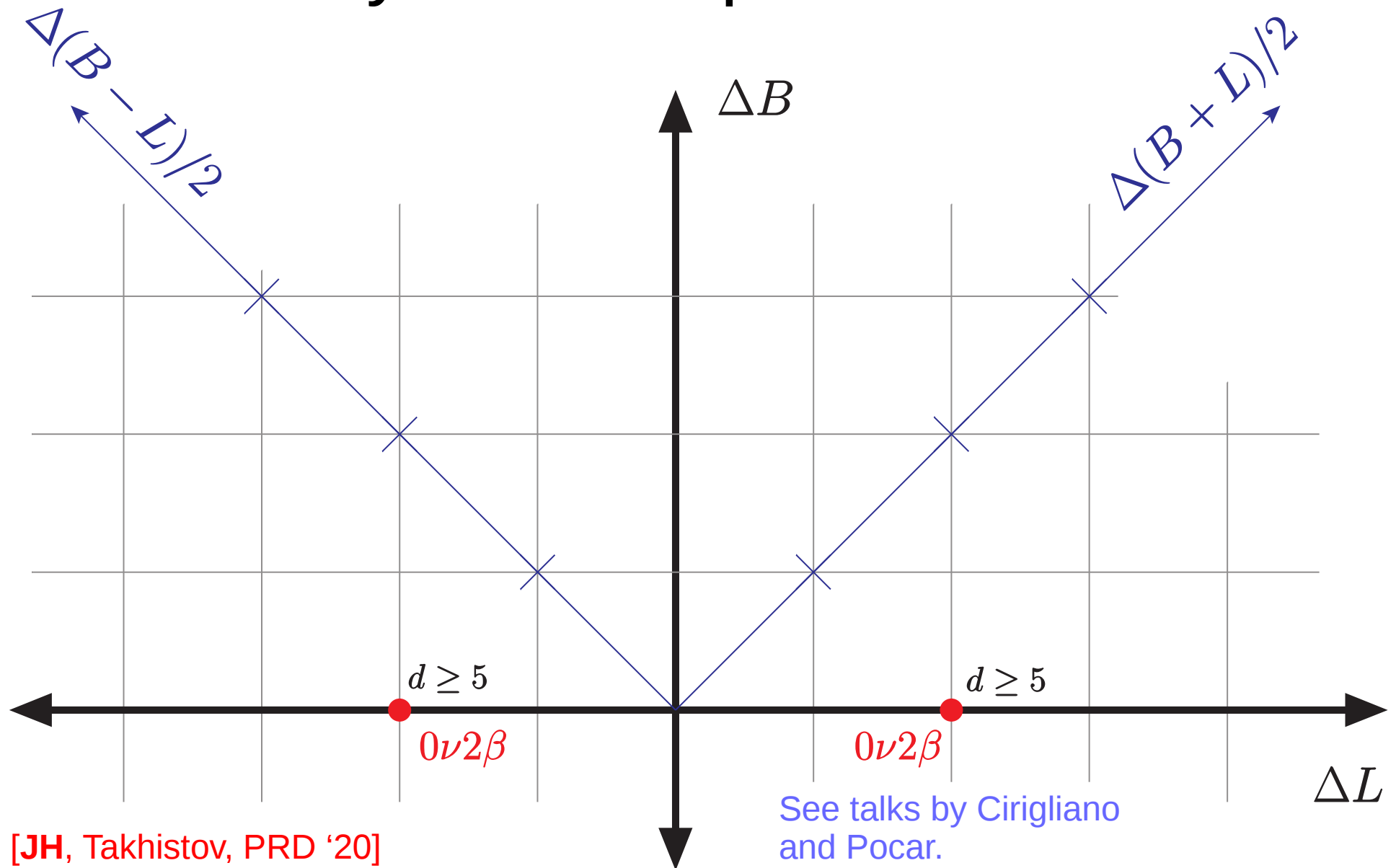
$$L = L_{\text{SM}} + \frac{LLHH}{\Lambda} + \sum_j \frac{\mathcal{O}_j}{\Lambda^2} + \sum_j \frac{\mathcal{O}'_j}{\Lambda^3} + \sum_j \frac{\mathcal{O}''_j}{\Lambda^4} + \dots$$

$\Delta L = 2$ $\Delta B = \Delta L = 1$ $\Delta B = -\Delta L = 1$

- $d_{\min} \geq \frac{9}{2}|\Delta B| + \frac{3}{2}|\Delta L|$. [Kobach '16; Helset, Kobach, '19]
- ΔB dominated by $d = 6$, unless forbidden by **symmetry!**
[Weinberg, '80]

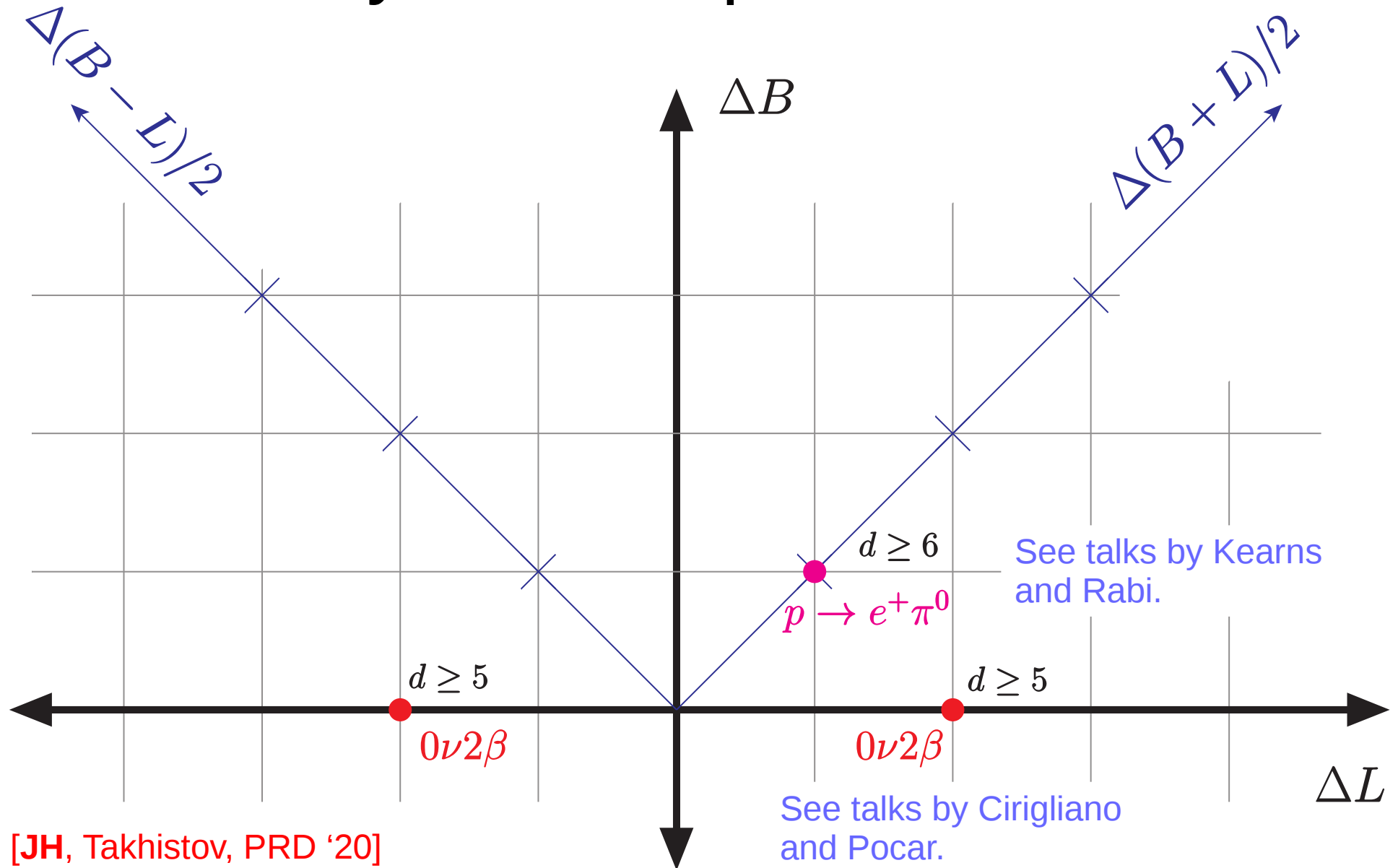
Get global view on ΔB and ΔL .

Baryon and lepton number



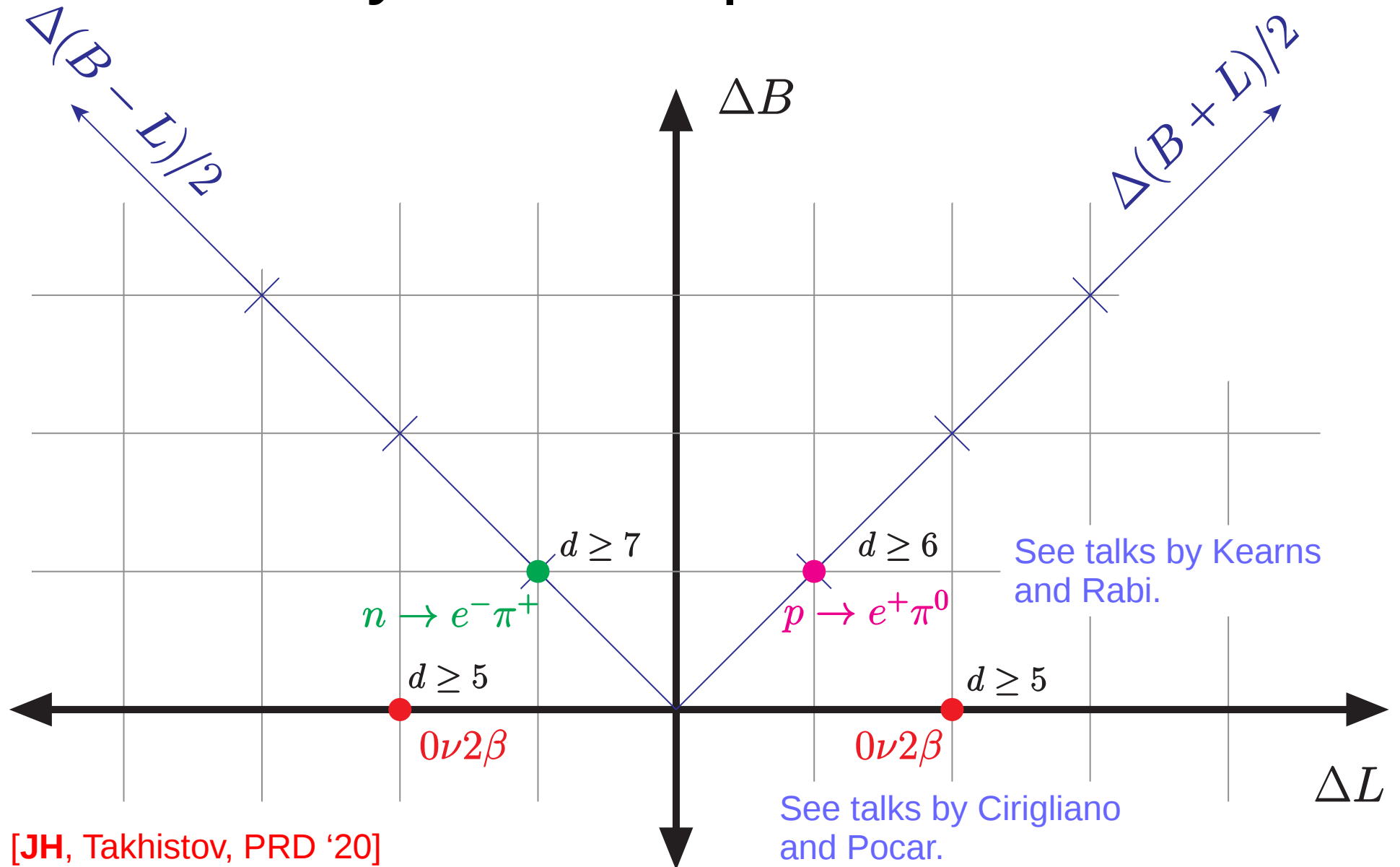
[JH, Takhistov, PRD '20]

Baryon and lepton number



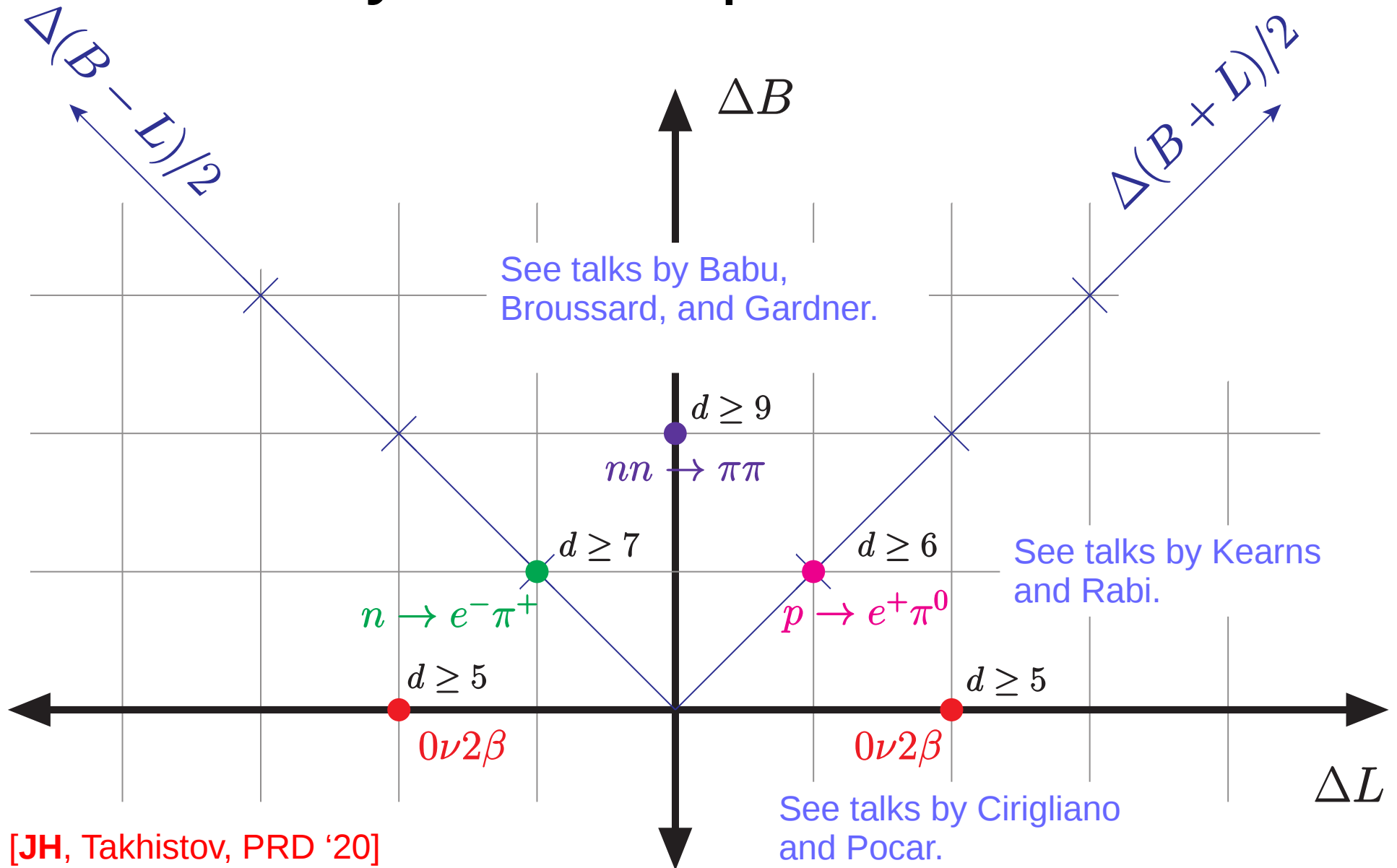
[JH, Takhistov, PRD '20]

Baryon and lepton number

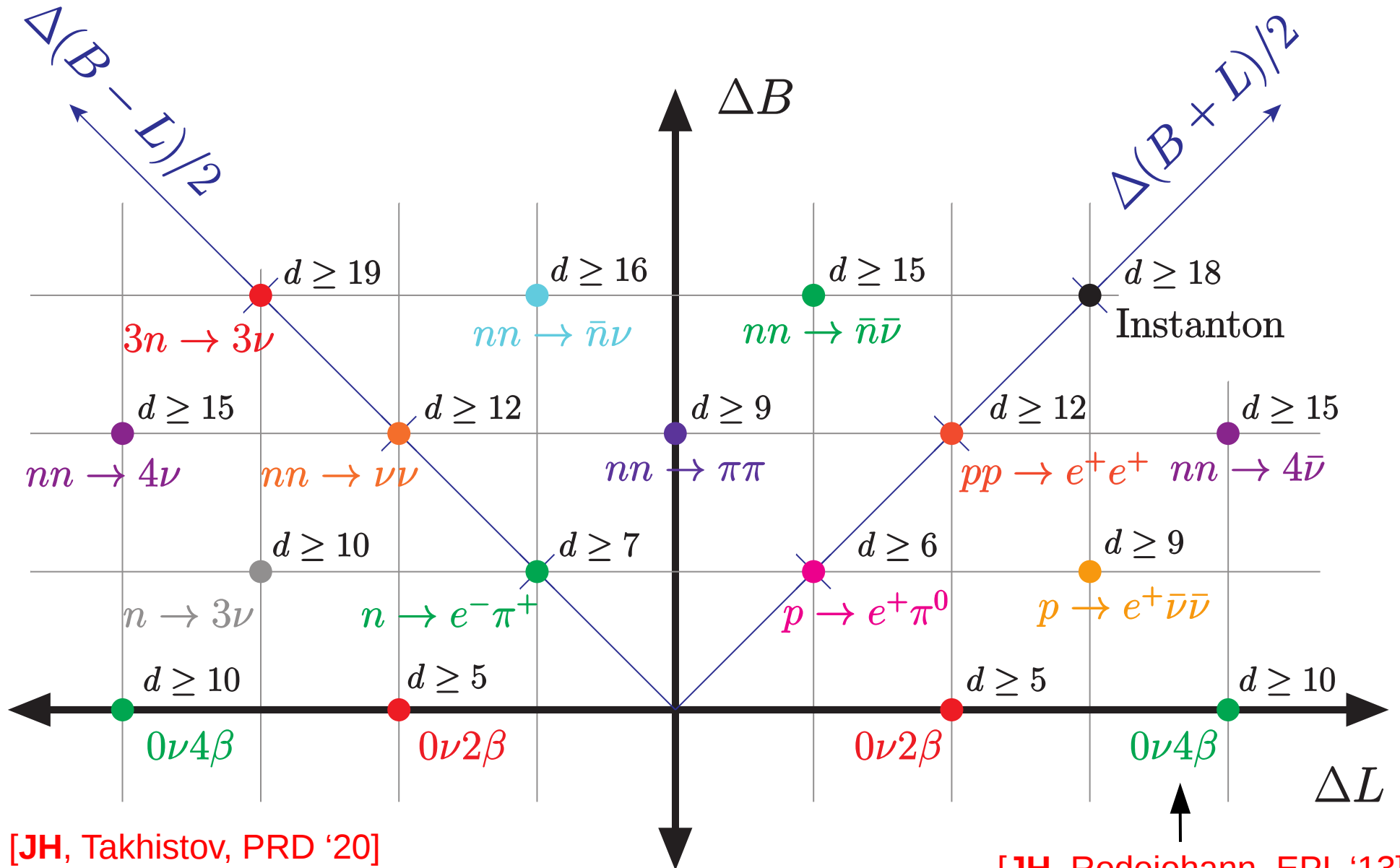


[JH, Takhistov, PRD '20]

Baryon and lepton number



Exotic B and L

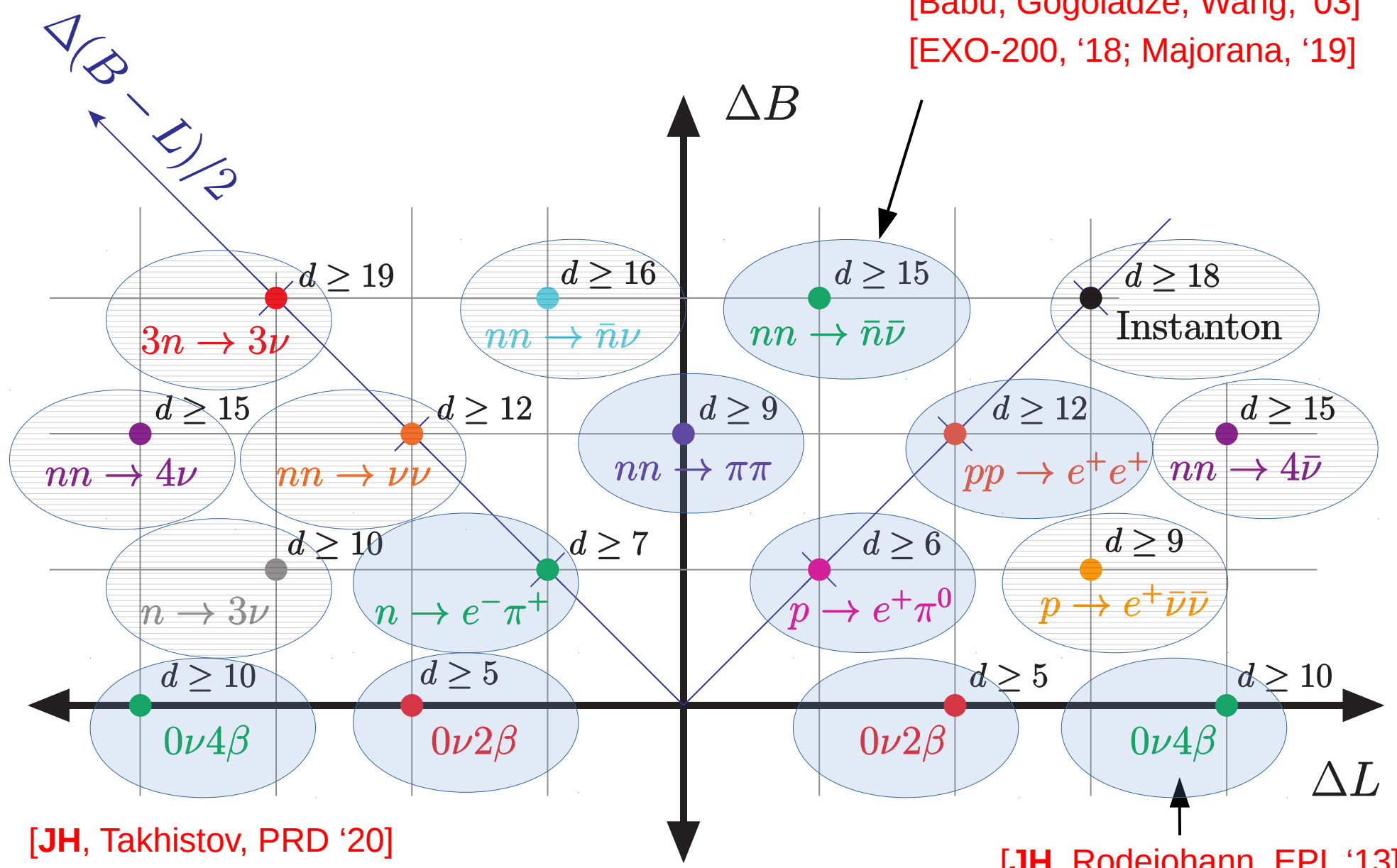


[JH, Takhistov, PRD '20]

[JH, Rodejohann, EPL '13]
[NEMO-3, PRL '17]

Recent limits:  Older than 5 yr: 

$ppp \rightarrow e^+ \pi^+ \pi^+$
 [Babu, Gogoladze, Wang, '03]
 [EXO-200, '18; Majorana, '19]



[JH, Takhistov, PRD '20]

[JH, Rodejohann, EPL '13]
 [NEMO-3, PRL '17]

ppp \rightarrow $e^+ \pi^+ \pi^+$

- Symmetry

	Q	u^c	d^c	ℓ	e^c	ν^c	H
Z_6	6	5	1	2	5	3	1

$$\mathbb{Z}_6 \subset U(1)_{2Y-B+3L}$$

[Babu, Gogoladze, Wang, '03]

allows for $d = 15$ $\Delta B = 3\Delta L = 3$ operators $\frac{1}{\Lambda^{11}} Q^5 d^4 \bar{\ell}, \dots$

- $ppp \rightarrow e^+ \pi^+ \pi^+$, $ppn \rightarrow e^+ \pi^+$, $pnn \rightarrow e^+ \pi^0$, $nn \rightarrow \bar{n} \bar{\nu}, \dots$

- $\tau(pnn \rightarrow e^+ \pi^0) \simeq 3 \times 10^{33} \text{ yr} \left(\frac{\Lambda}{100 \text{ GeV}} \right)^{22}$.

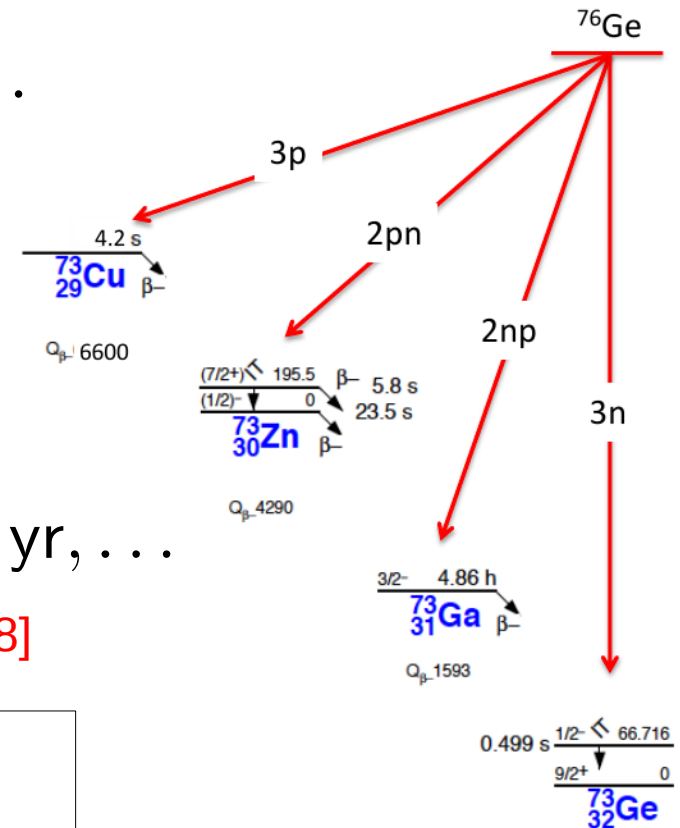
- Limits:

$$\tau(^{73}\text{Ge}(pnn) \rightarrow ^{70}\text{Ga} e^+ \pi^0) > 7 \times 10^{23} \text{ yr},$$

$$\tau(^{76}\text{Ge}(ppn) \rightarrow ^{73}\text{Zn} e^+ \pi^+) > 5 \times 10^{25} \text{ yr},$$

$$\tau(^{76}\text{Ge}(ppp) \rightarrow ^{73}\text{Cu} e^+ \pi^+ \pi^+) > 5 \times 10^{25} \text{ yr}, \dots$$

[Majorana Demonstrator, PRD '19; see also EXO-200, '18]



SK, JUNO, DUNE, HK?

ppp \rightarrow $e^+ \pi^+ \pi^+$

- Symmetry

	Q	u^c	d^c	ℓ	e^c	ν^c	H
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- ppp $\rightarrow e^+ \pi^+ \pi^+$, ppn $\rightarrow e^+ \pi^+$, pnn $\rightarrow e^+ \pi^0$, nn $\rightarrow \bar{n} \bar{\nu}, \dots$

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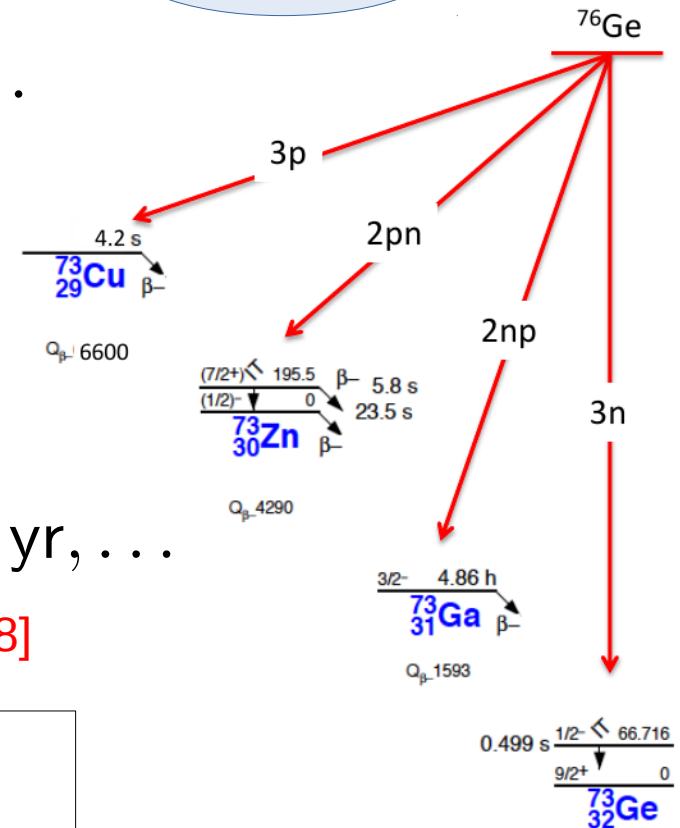
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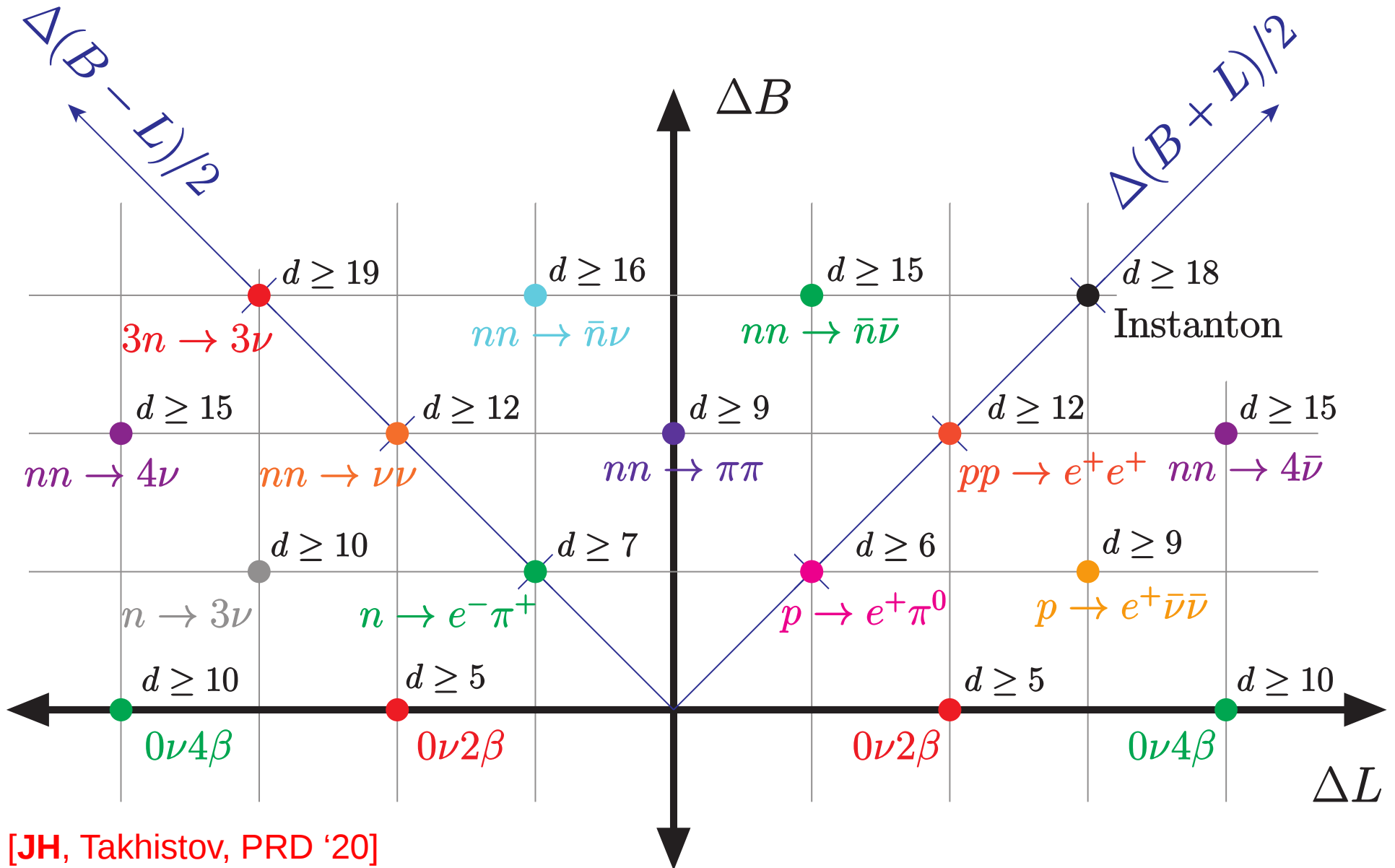
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[Majorana Demonstrator, PRD '19; see also EXO-200, '18]



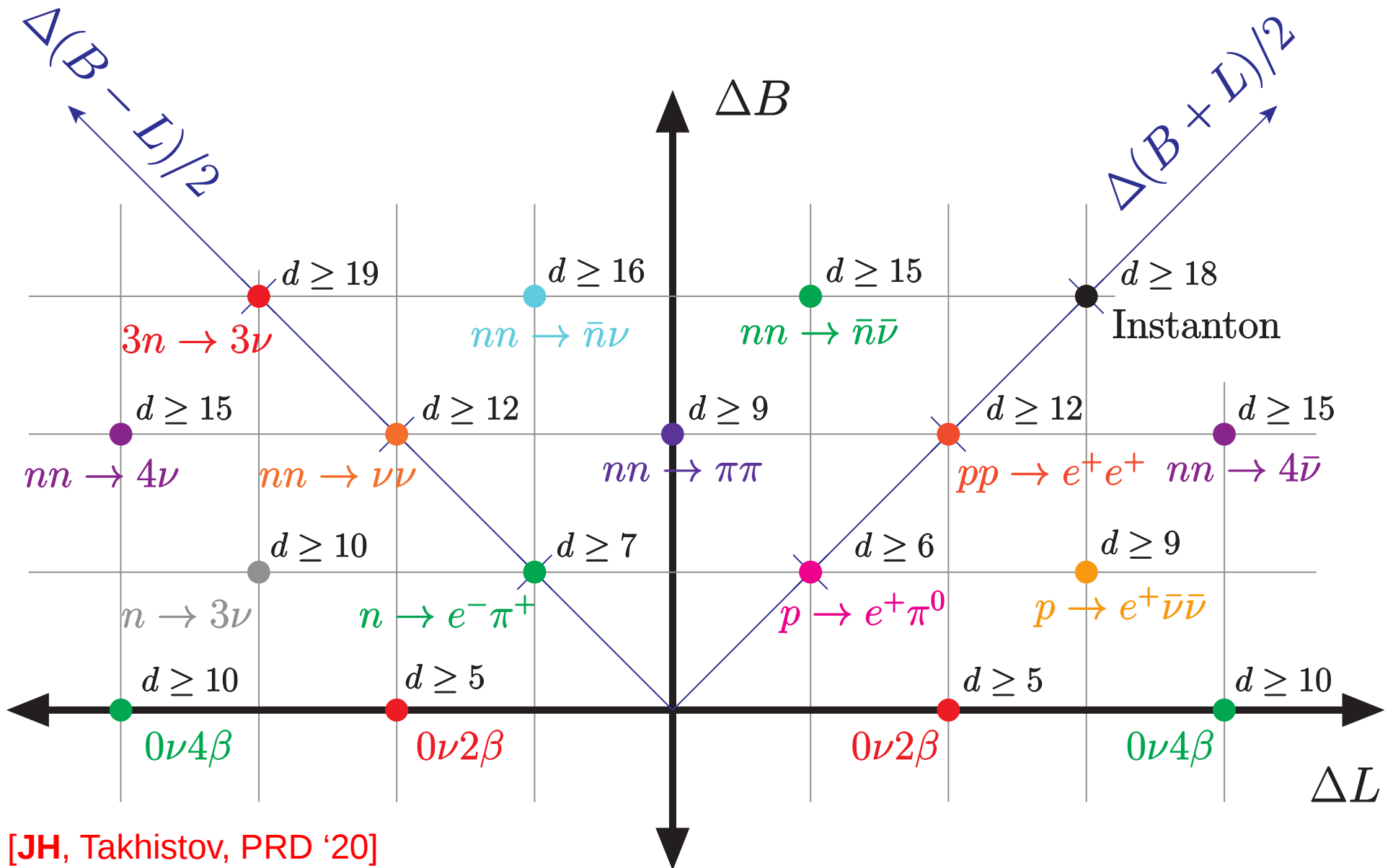
SK, JUNO, DUNE, HK?

Exotic B and L

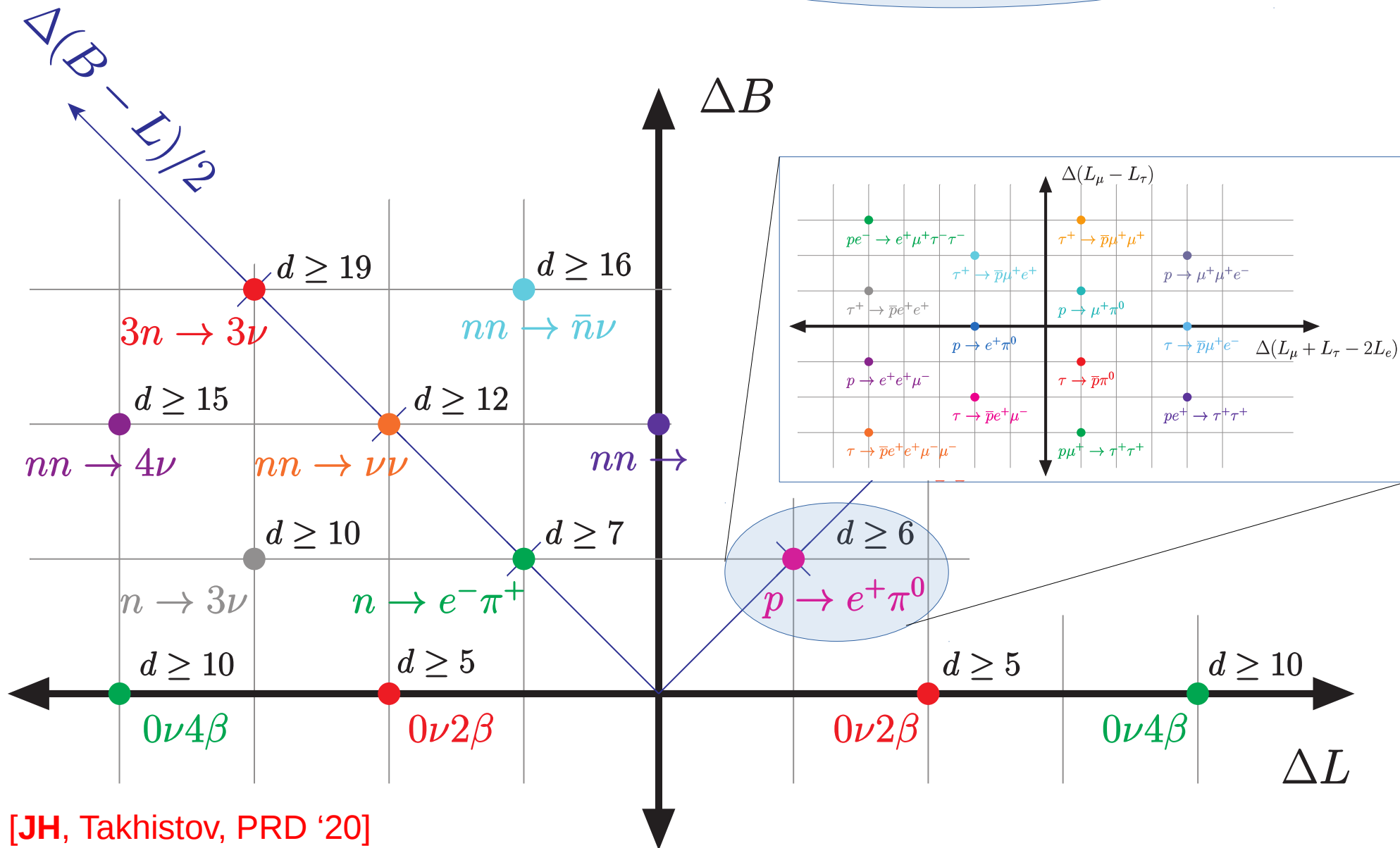


[JH, Takhistov, PRD '20]

$$\mathbb{Z}_3^{(B+L)/2} \times U(1)_{B-L} \times U(1)_{L_\mu - L_\tau} \times U(1)_{L_\mu + L_\tau - 2L_e}$$



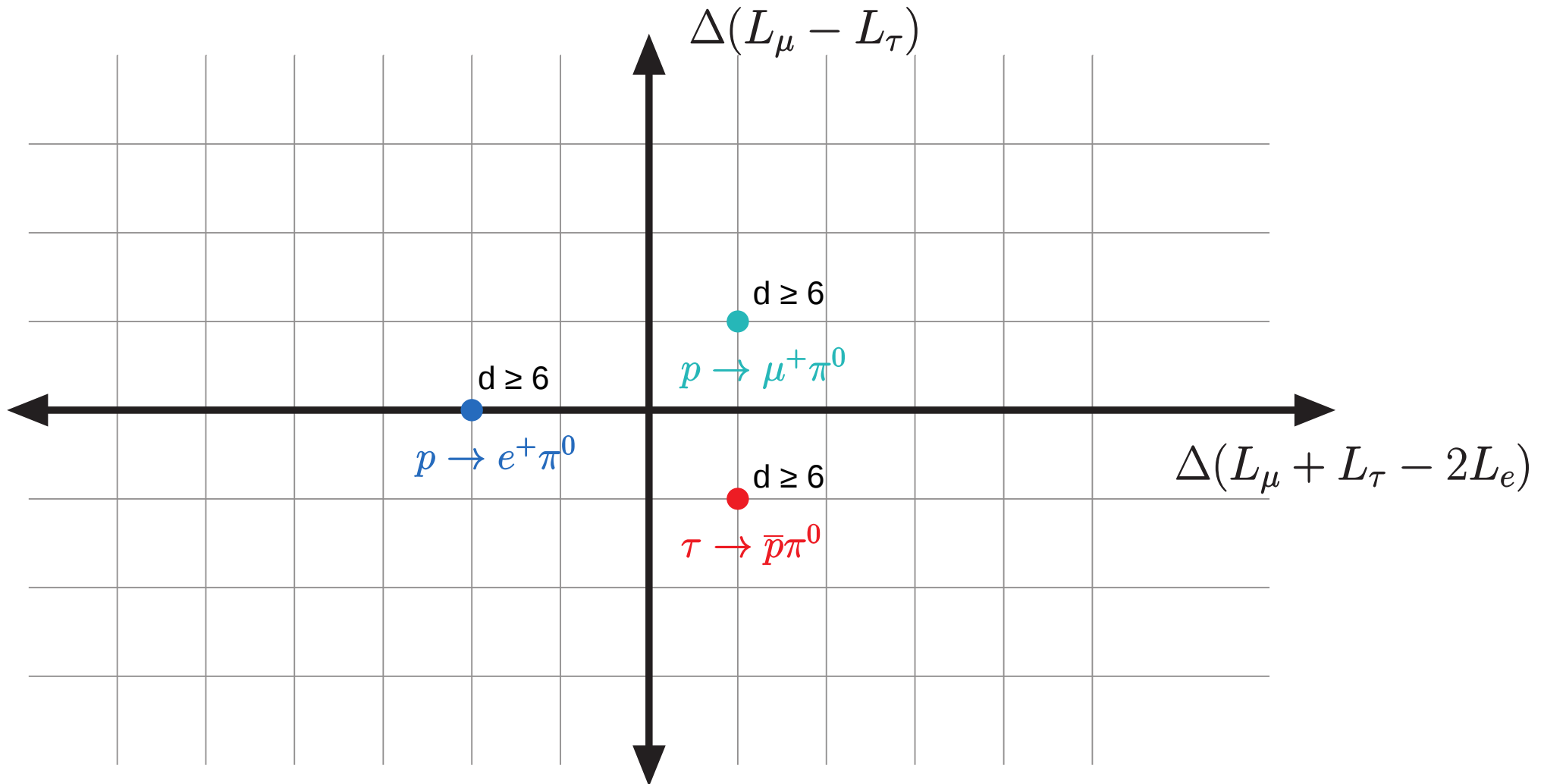
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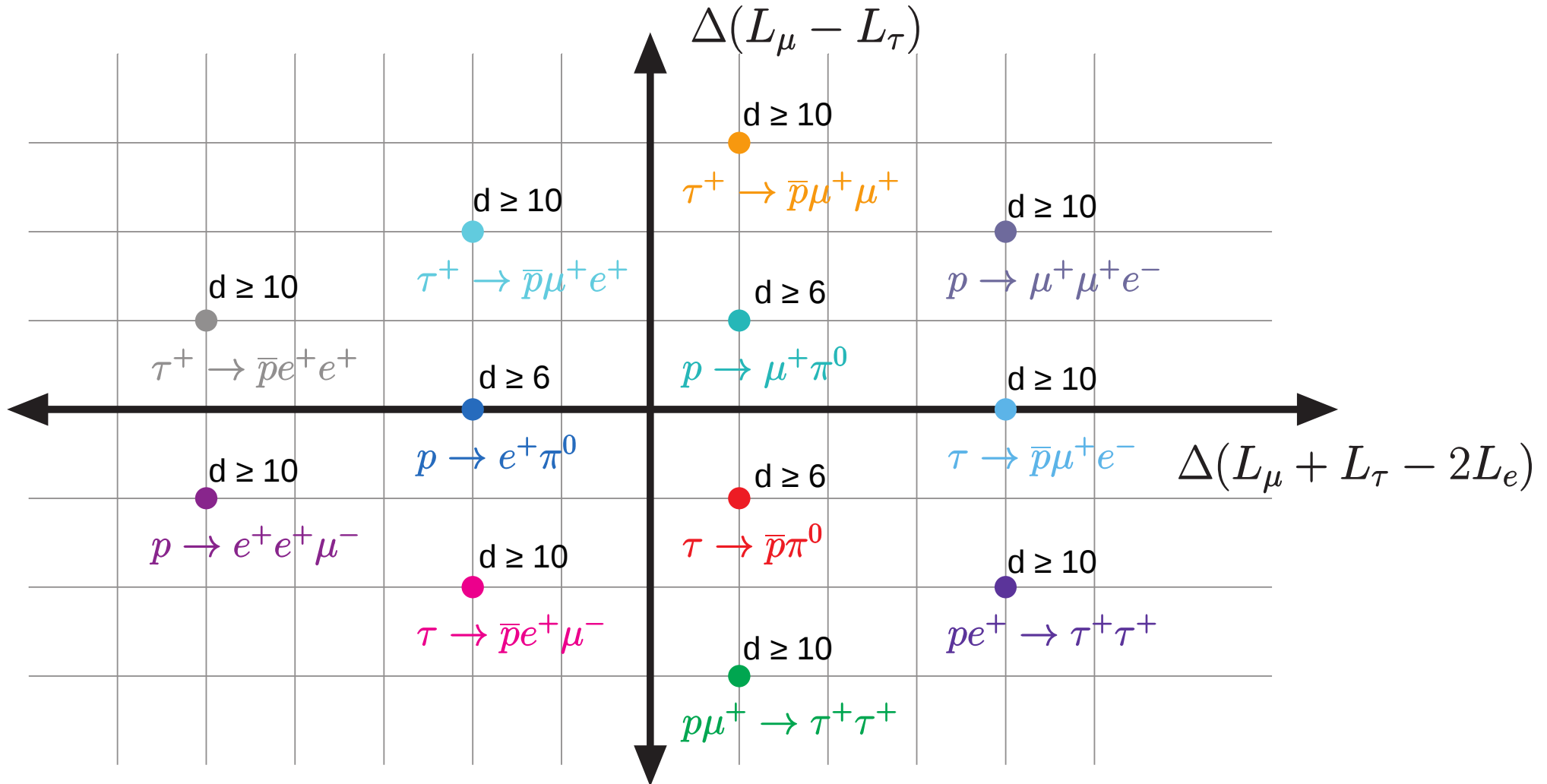
Proton decay = lepton flavor violation

$$\Delta B = \Delta L = 1$$



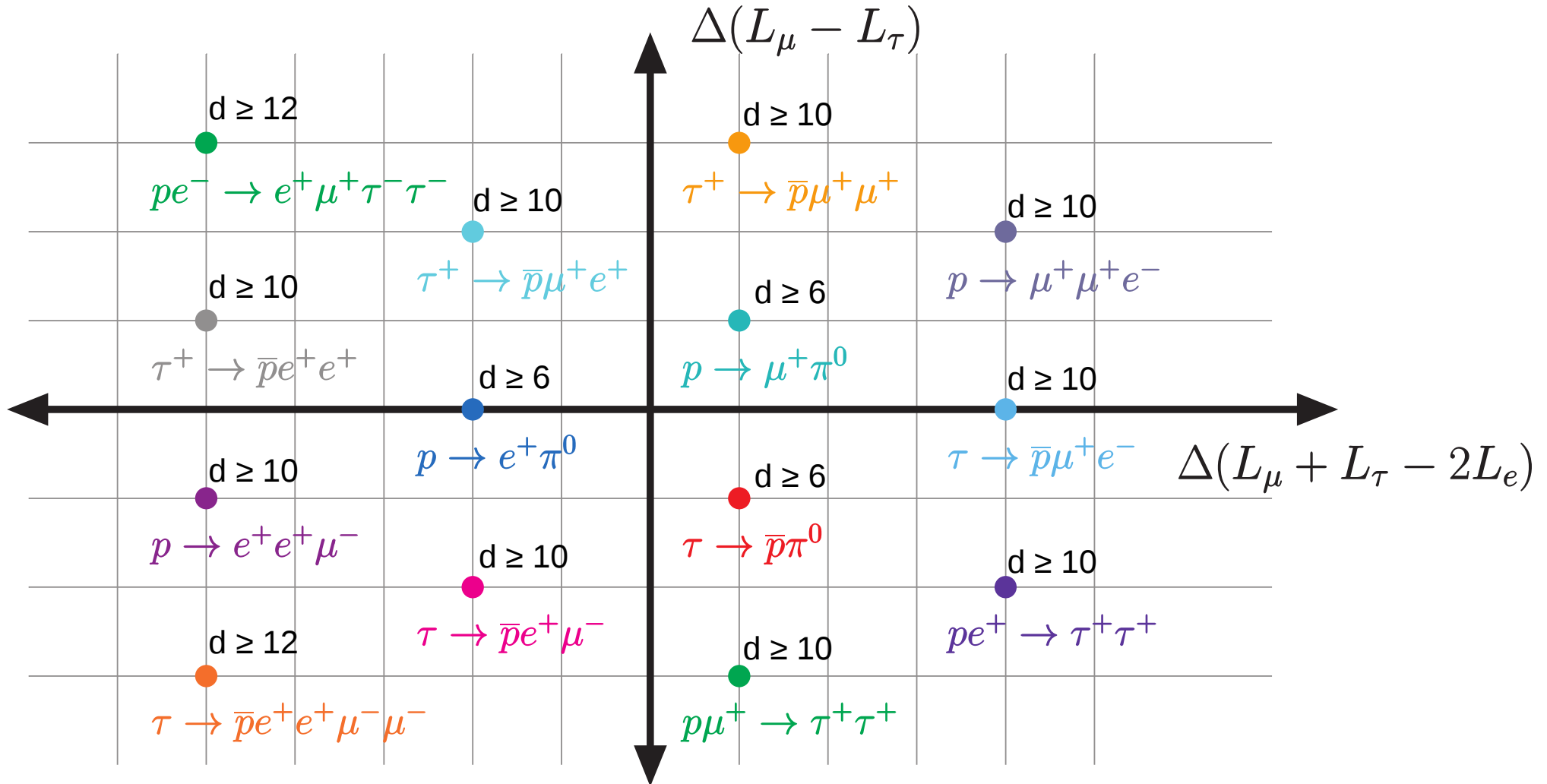
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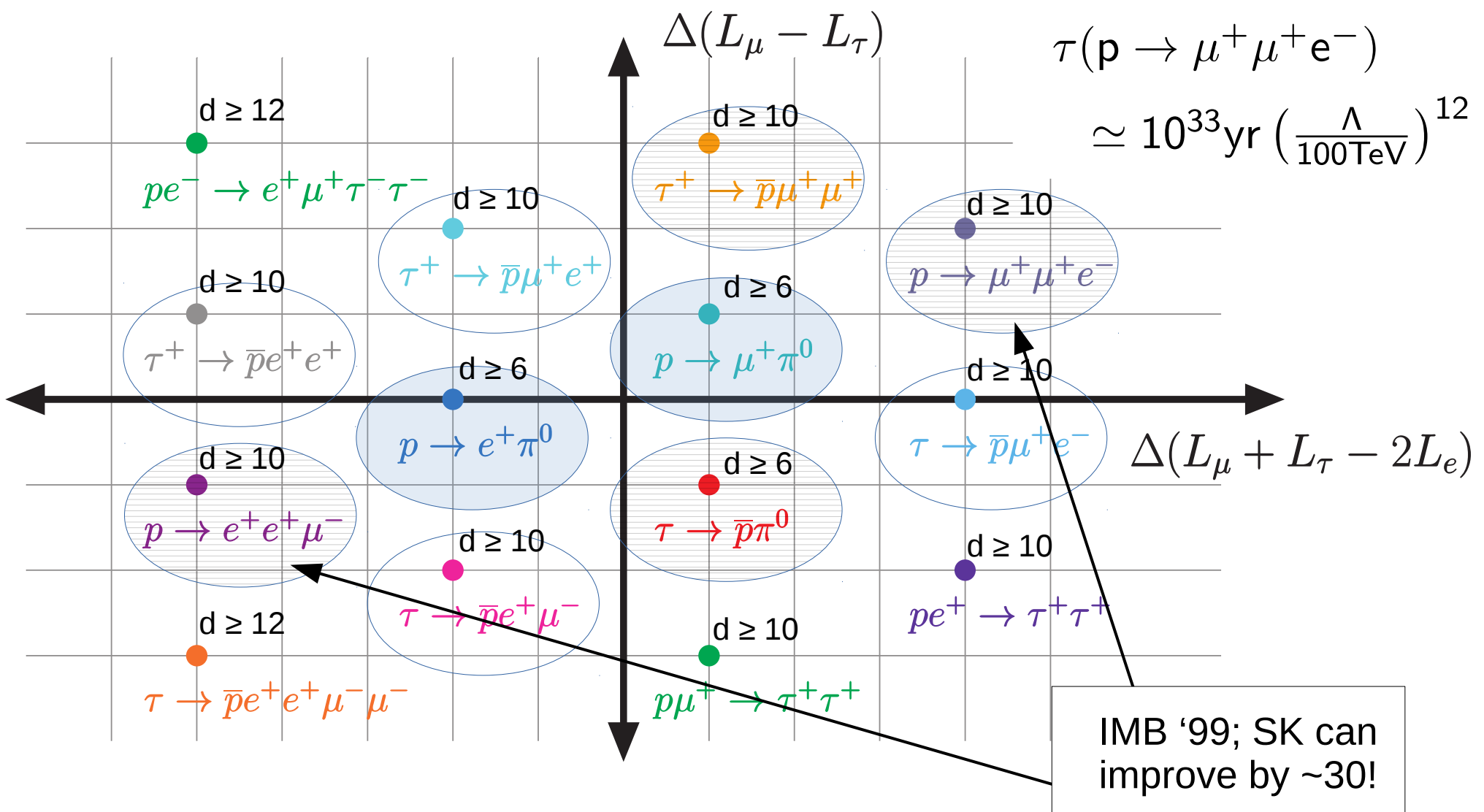
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Currently being probed: Old results: Doable:

$\Delta B = \Delta L = 1$



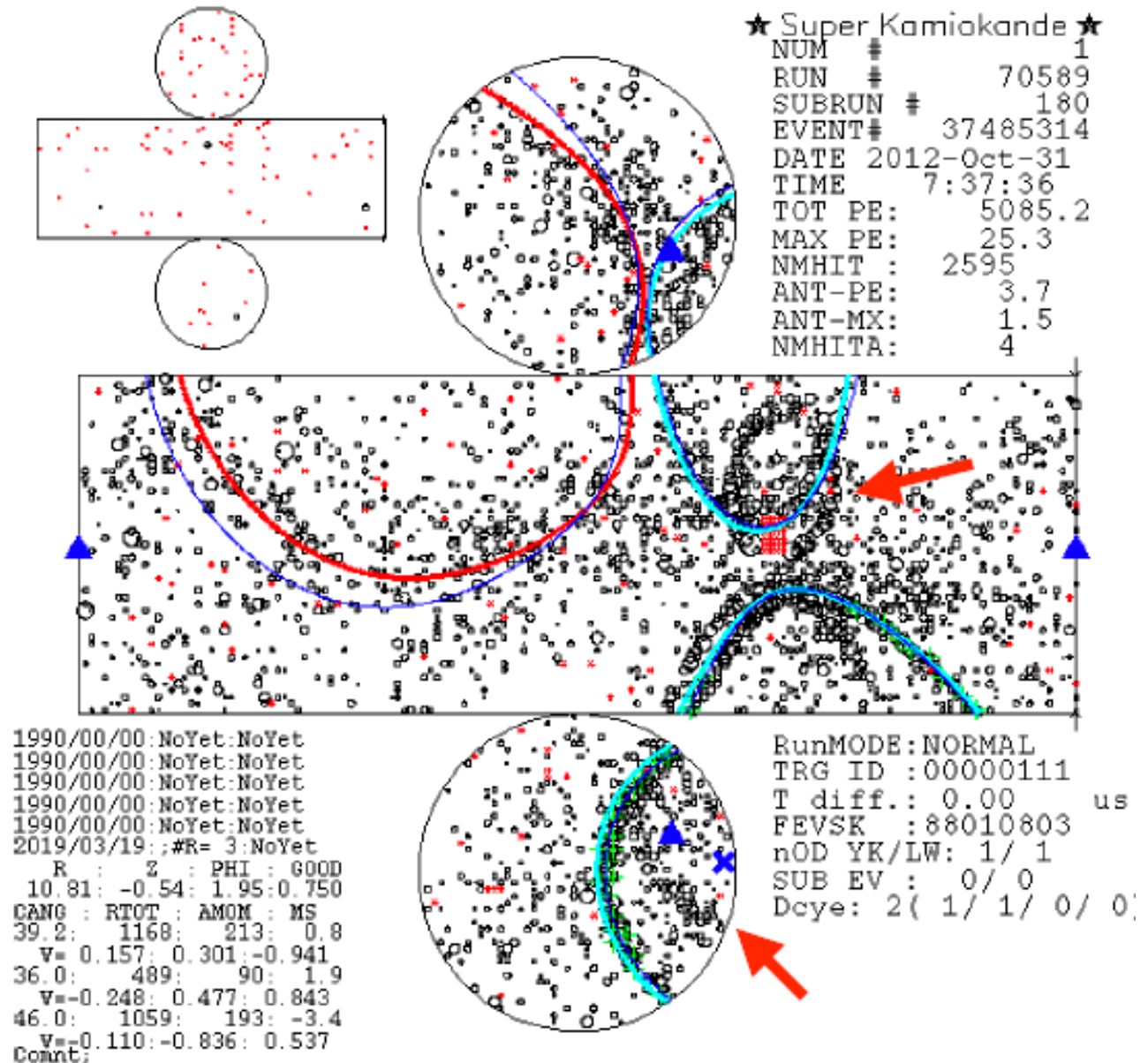
[Hambye, JH, PRL '18]

Done!

$$p \rightarrow e\mu\mu$$

- Super-K searched for $p \rightarrow e\mu\mu$!
- Presented by Makoto Miura at BLV 2019 in Madrid.

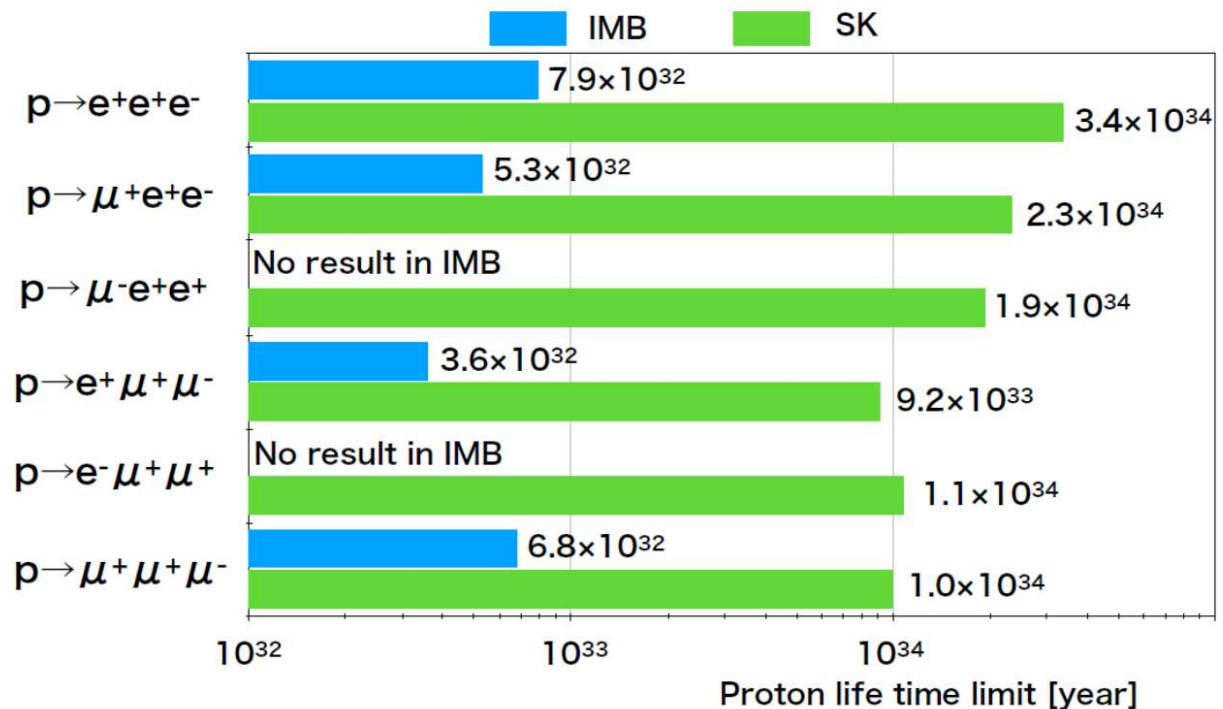
[full paper: PRD '20]



Done!

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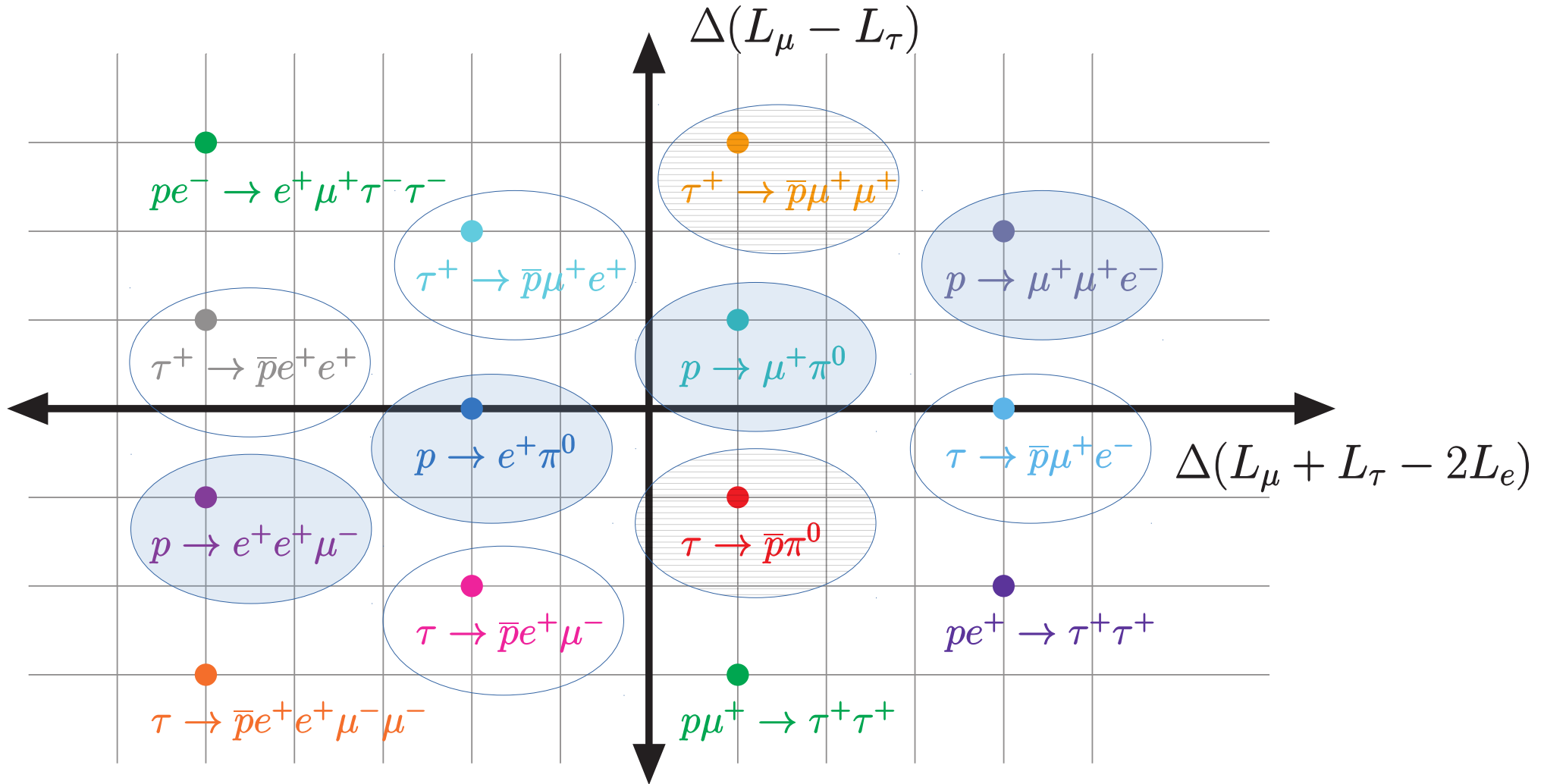
[full paper: PRD '20]



Compatible with background, limits around 10^{34} yr.

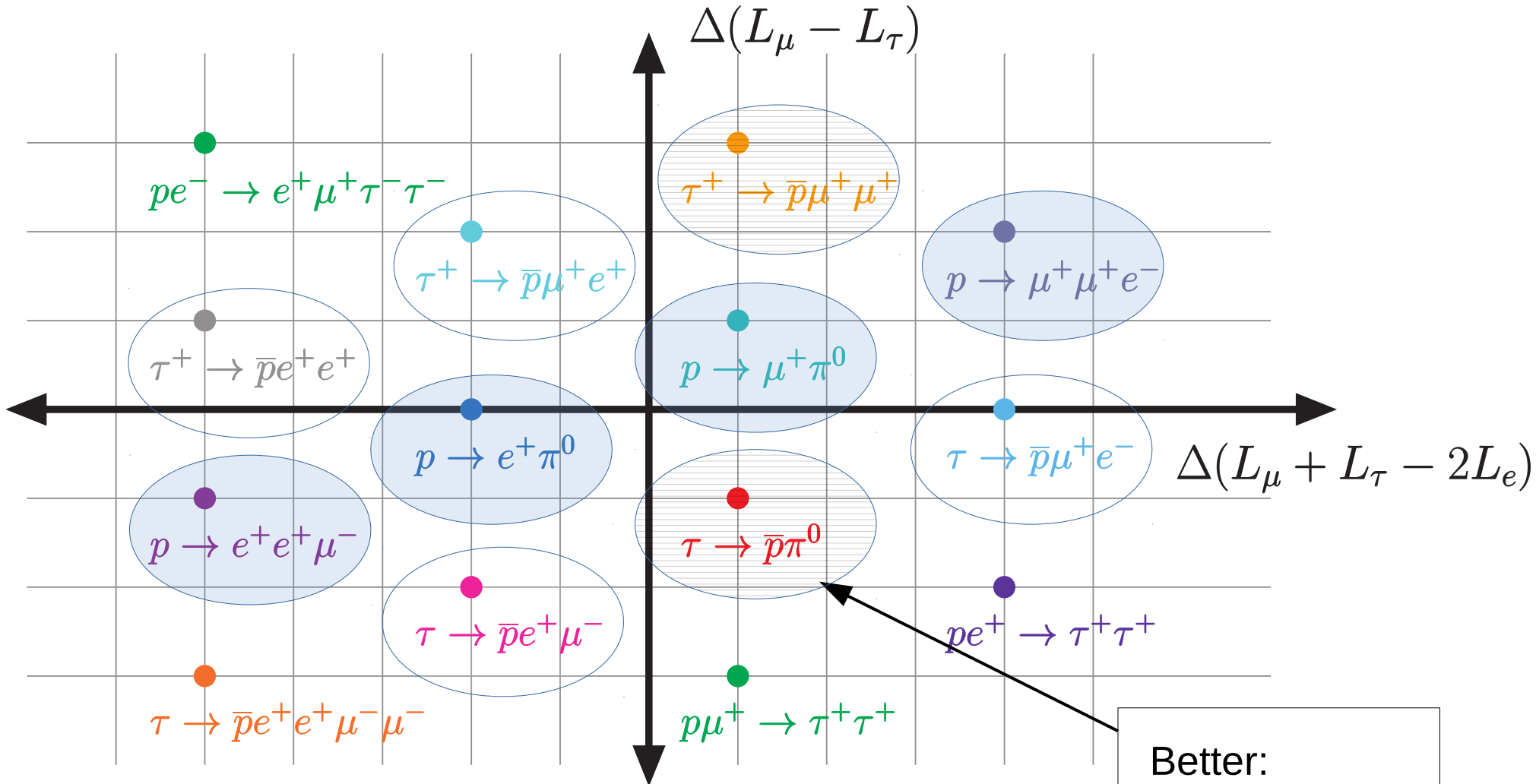
Currently being probed:  Old results:  Doable: 

$$\Delta B = \Delta L = 1$$



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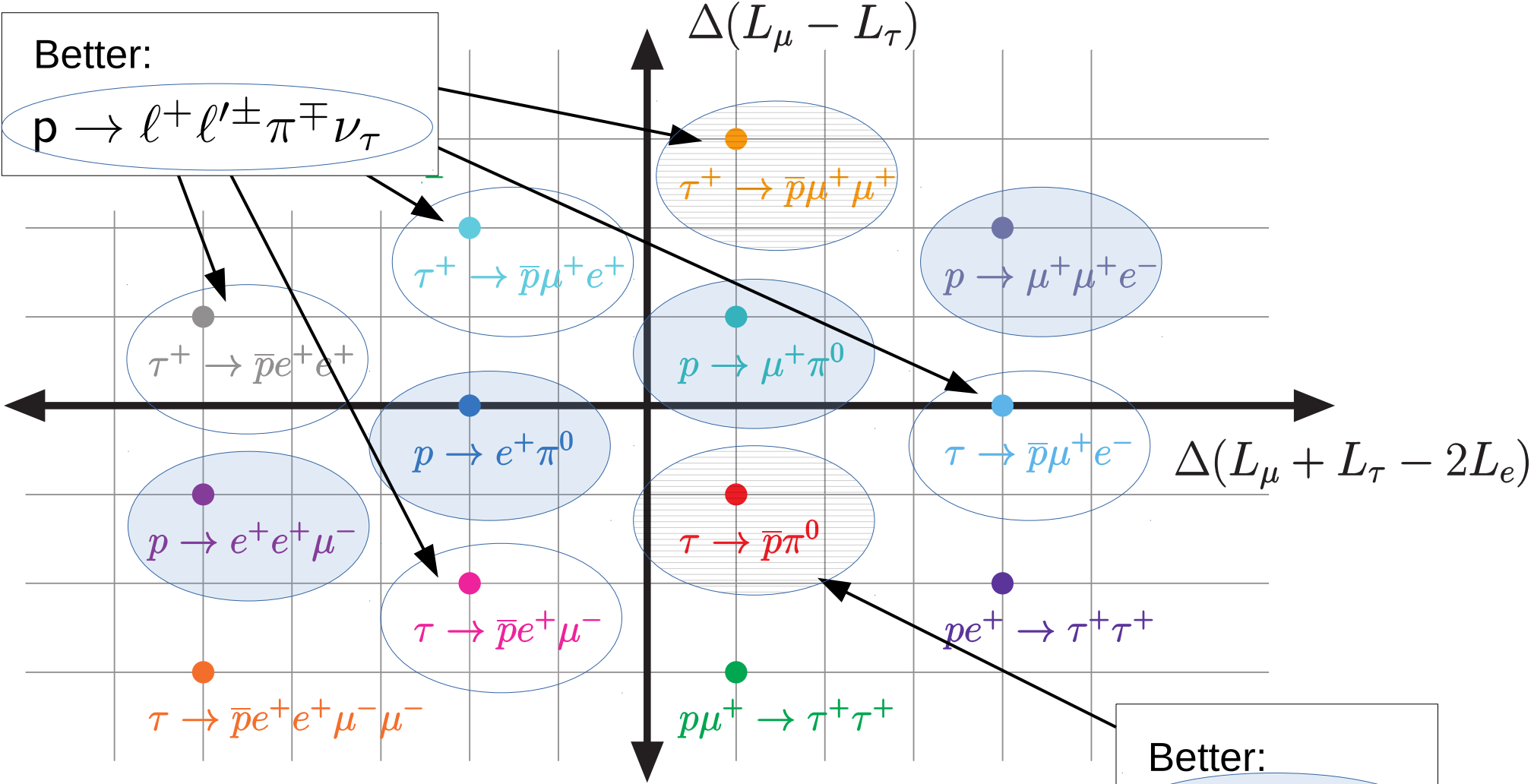
Better:
 $p \rightarrow \pi^+ \bar{\nu}_\tau$

[Marciano, NPB '95]

Currently being probed: Old results: Doable:

$\Delta B = \Delta L = 1$

Better:
 $p \rightarrow l^+ l'^{\pm} \pi^{\mp} \nu_{\tau}$



Better:
 $p \rightarrow \pi^+ \bar{\nu}_{\tau}$

[Marciano, NPB '95]

Full ΔB coverage possible?

- Cannot to go through all $\Delta B > 0$ decays:
 - 38 two-body $\Delta B = 1$ modes: $N \rightarrow AB$. 36 limits.
 - 76 three-body $\Delta B = 1$ modes: $N \rightarrow ABC$. 33 limits.
 - 300 four-body $\Delta B = 1$ modes: $N \rightarrow ABCD$. 0 limits.
 - 118 two-body $\Delta B = 2$ modes: $NN \rightarrow AB$. 18 limits.
 - 500 three-body $\Delta B = 2$ modes: $NN \rightarrow ABC$. 0 limits.
 - ...
- *Exclusive* searches can reach $t \sim 10^{34}$ yr in SK.

Inclusive searches to the rescue!

Inclusive searches

- Current limits:

$$\Gamma^{-1}(N \rightarrow e + \text{anything}) > 0.6 \times 10^{30} \text{ yr}, \quad [\text{Learned, Reines, Soni, '79}]$$

$$\Gamma^{-1}(N \rightarrow \mu + \text{anything}) > 12 \times 10^{30} \text{ yr}. \quad [\text{Cherry, Deakyne, Lande, Lee, Steinberg, Cleveland, '81}]$$

- **40 years old**, improve with new tech!
- $p \rightarrow e^+ + \text{anything}$ in SK could reach **10^{32} yr**, judging by

$$\Gamma^{-1}(p \rightarrow e^+ \nu \nu) > 1.7 \times 10^{32} \text{ yr}. \quad [\text{Super-K, PRL '14}]$$

- Do inclusive searches for $N \rightarrow \ell/\text{meson} + \text{anything}$.
- Also probes $\Delta B > 1$, light new physics, and dark matter!

[**JH**, Takhistov, PRD '20]

Invisible neutron decay

- Special case of inclusive searches:

$$\Gamma^{-1}(n \rightarrow \text{neutrinos}) > 0.58 \times 10^{30} \text{ yr},$$

$$\Gamma^{-1}(nn \rightarrow \text{neutrinos}) > 1.4 \times 10^{30} \text{ yr},$$

$$\Gamma^{-1}(nnn \rightarrow \text{neutrinos}) > 1.8 \times 10^{23} \text{ yr},$$

$$\Gamma^{-1}(nnnn \rightarrow \text{neutrinos}) > 1.4 \times 10^{23} \text{ yr}.$$

[KamLAND, PRL '06; see also SNO+, PRD '19]

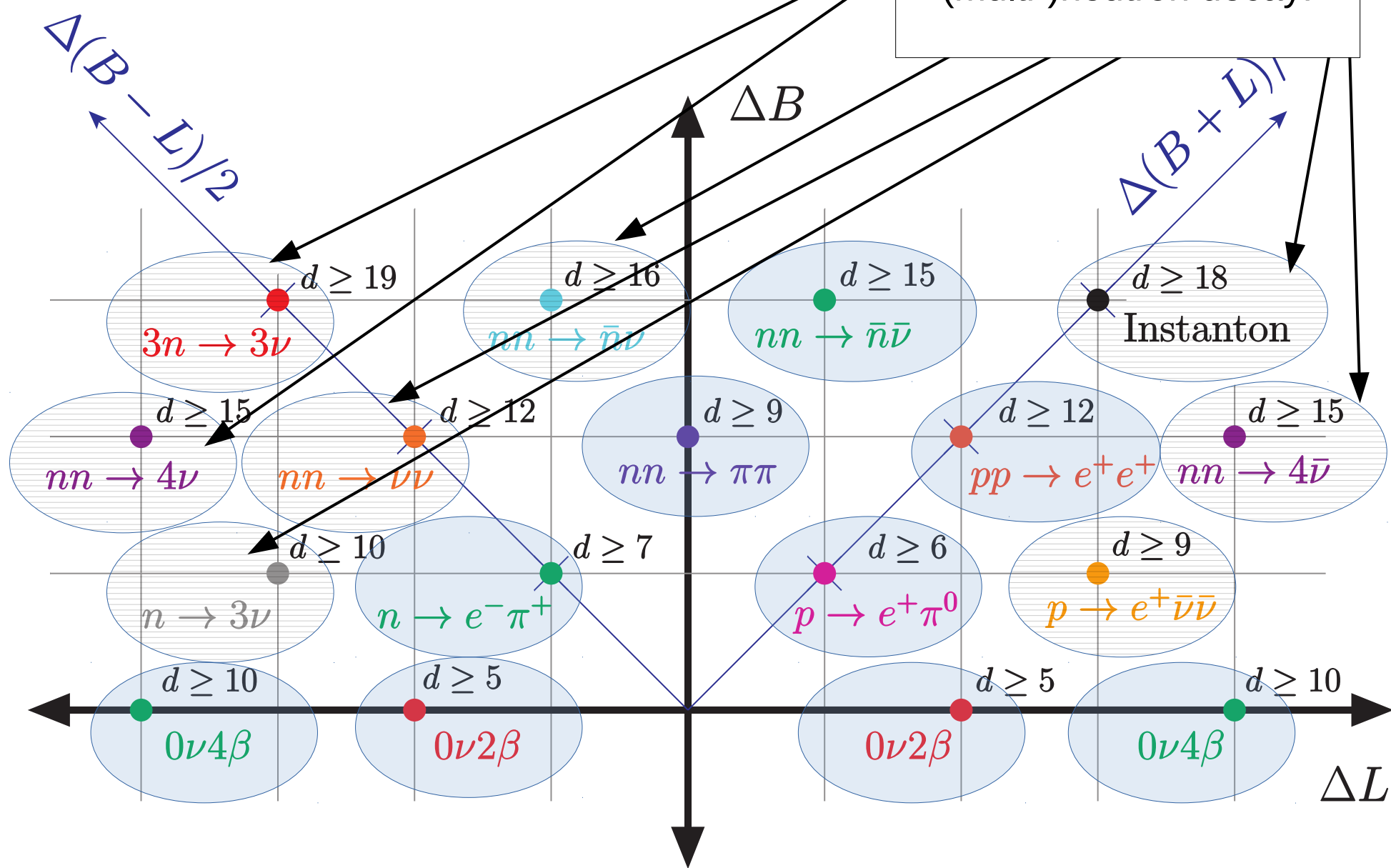
[Hazama, Ejiri, Fushimi, Ohsumi, PRC '94]

- Only signature is **de-excitation** of daughter nucleus. [Ejiri, '93]
- **Every** $\Delta B = k$ operator gives rise to **k neutrons \rightarrow neutrinos.**
- Neutrinos carry away arbitrary lepton number & flavor!
- Also probes light new physics and dark matter.
- Can JUNO improve KamLAND limit? DUNE?

[JH, Takhistov, PRD '20]

Recent limits:  Older than 5 yr: 

Limits from invisible (multi-)neutron decay!



Summary

- SM: $\mathbb{Z}_3^{(B+L)/2} \times U(1)_{B-L} \times U(1)_{L_\mu - L_\tau} \times U(1)_{L_\mu + L_\tau - 2L_e}$.
- **Violated?** **New particles!** **How?** **New structure!**
- ΔB (& ΔL) probe
 - high scales (10^{15} GeV) or
 - high *multiplicities* ($N \rightarrow 15$ particles) or
 - high operator *dimensions* ($d \sim 15$)!
- Go beyond two-body proton decay, do **inclusive** searches!
- Still untapped areas:
 - Light new physics ($p \rightarrow \ell^+ + X$, $X \rightarrow \text{SM?}$).
 - Dark matter induced ΔB & ΔL .

SK/HK,
DUNE,
JUNO,
 $0\nu\beta\beta$ exp.?

Exotic = new normal!

Backup

Symmetries of the Standard Model

- Rephasing lepton and quark fields:

$$\begin{aligned}
 & U(1)_B \times U(1)_{L_e} \times U(1)_{L_\mu} \times U(1)_{L_\tau} \\
 &= U(1)_{B+L} \times U(1)_{B-L} \times U(1)_{L_\mu-L_\tau} \times U(1)_{L_\mu+L_\tau-2L_e} .
 \end{aligned}$$

- $U(1)_{B+L}$ broken non-perturbatively to \mathbb{Z}_3 ,

$$\Delta B = 3 \quad \wedge \quad \Delta L_e = \Delta L_\mu = \Delta L_\tau = 1 ,$$

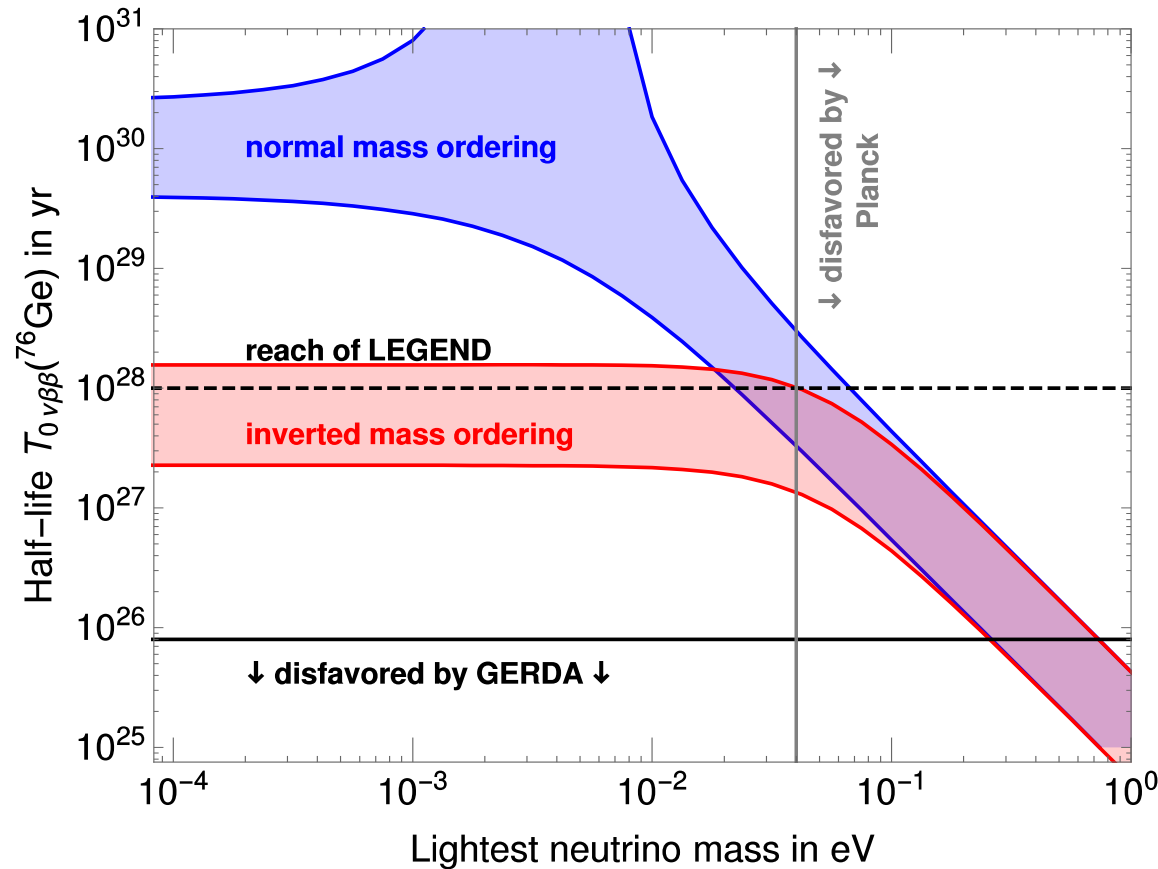
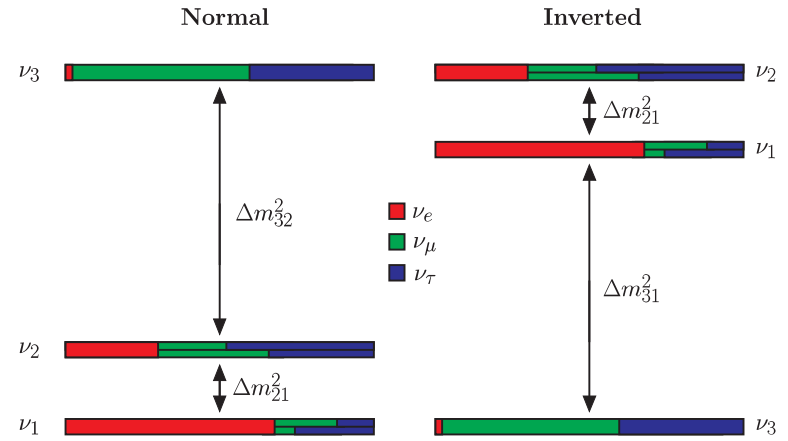
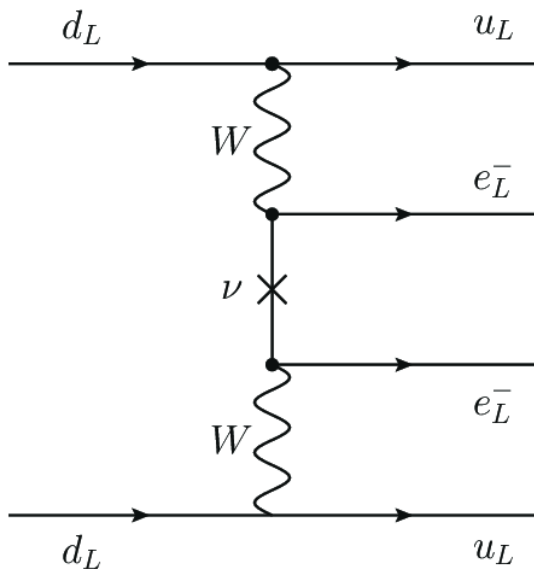
but unobservable at low temperatures. [['t Hooft, PRL '76](#)]

- True accidental global symmetry:

$$\mathbb{Z}_3^{(B+L)/2} \times U(1)_{B-L} \times U(1)_{L_\mu-L_\tau} \times U(1)_{L_\mu+L_\tau-2L_e} .$$

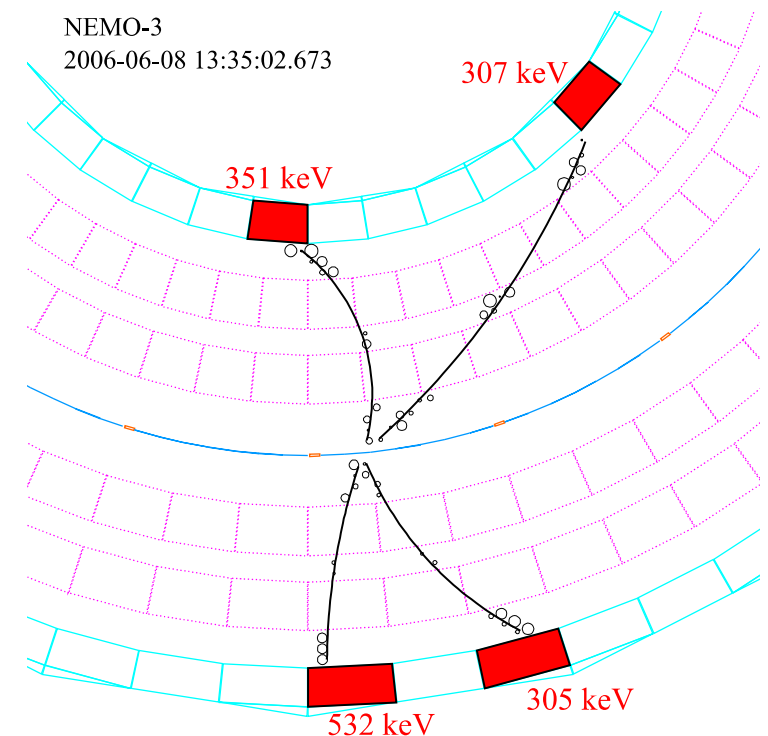
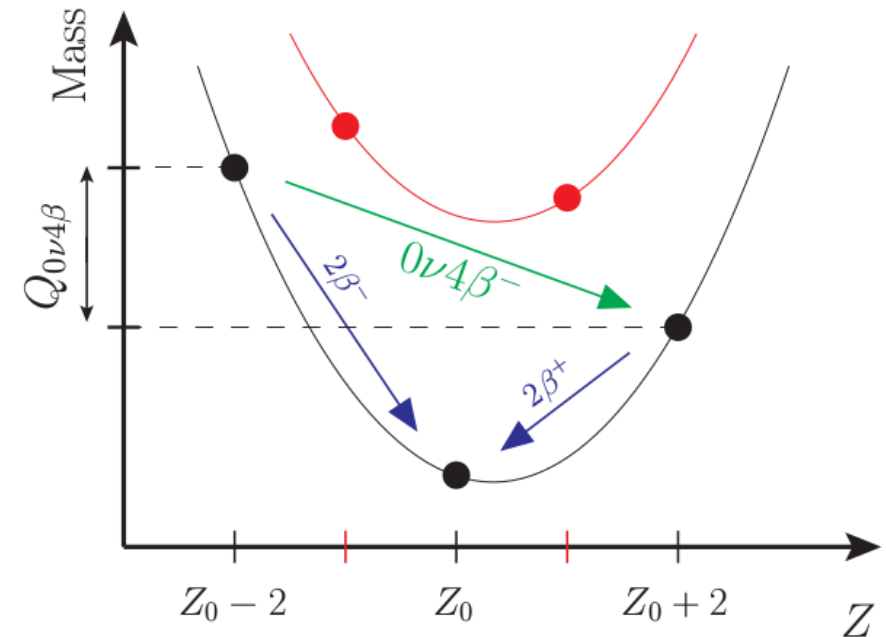
$$\Delta L = 2$$

- Neutrinoless double β decay:
 $(A, Z) \rightarrow (A, Z+2) + 2 e^-$
 in β stable isotopes.
- Current limits $\sim 10^{26}$ yr.
- $0\nu 2\beta \Leftrightarrow$ Majorana ν .



$$\Delta L = 4$$

- $\Delta L = 4$ in rare decays?
 $(A, Z) \rightarrow (A, Z+4) + 4 e^-!$
- 3 candidates: ^{96}Zr , ^{136}Xe , ^{150}Nd .
 [JH, Rodejohann, EPL '13]
- First limit: $\tau_{0\nu 4\beta}(^{150}\text{Nd}) > 10^{21}\text{yr}$.
 [NEMO-3, PRL '17]
- Hard to find testable models.
 [Fonseca, Hirsch, PRD '18; see however Dasgupta, Kang, Popov, PRD '19]
- Could still explain matter-antimatter asymmetry.
 [JH, PRD '13]



$$p \rightarrow \mu^+ \mu^+ e^-$$

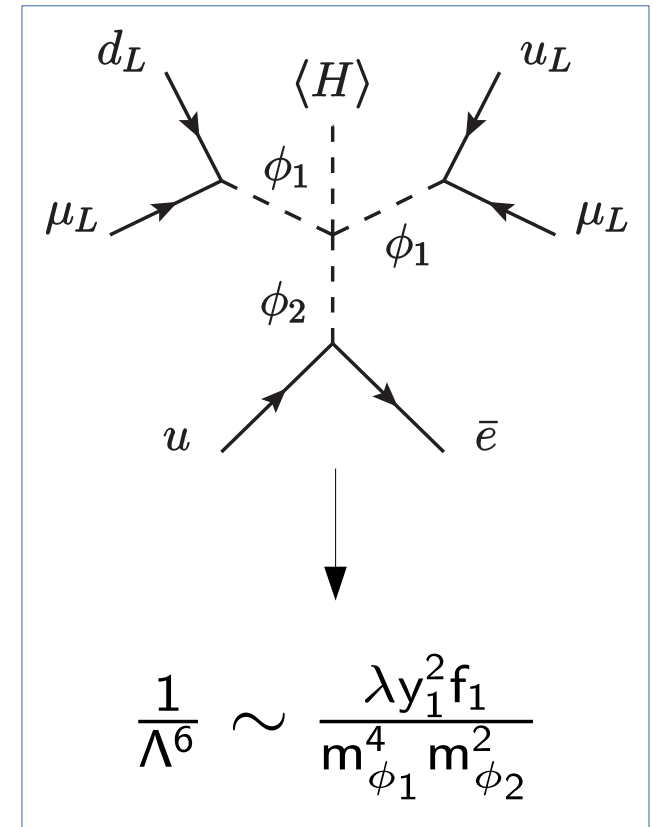
- Minimal **leptoquark** example:

$$\phi_1 \sim (\mathbf{3}, \mathbf{3}, -2/3), \phi_2 \sim (\mathbf{3}, \mathbf{2}, 7/3).$$

- $L_\mu + 2L_e - 3L_\tau$ ensures simple structure

$$y_j \bar{L}_\mu \phi_1 Q_j^c + f_j \bar{u}_j \phi_2 L_e + \lambda \phi_1^2 \phi_2 H.$$

- Final **$\Delta B=1$** operator: $\frac{1}{\Lambda^6} Q Q u L_\mu L_\mu \bar{L}_e H.$
- Lattice QCD input: $\langle 0 | u u d | p \rangle.$



[Hambye, JH, PRL '18]

$$\Gamma(p \rightarrow \mu^+ \mu^+ e^-) \simeq \frac{\langle H \rangle^2 \beta^2 m_p^5}{6144 \pi^3 \Lambda^{12}} \simeq \frac{(100 \text{ TeV} / \Lambda)^{12}}{10^{33} \text{ yr}}$$

Lepton universality in $b \rightarrow s \mu^- \mu^+$

- $\frac{y_j \bar{y}_i}{m_{\phi_1}^2} (\bar{L}_\mu Q_j^c)(Q_i L_\mu)$.

- Modifies $b \rightarrow s \mu^- \mu^+$:

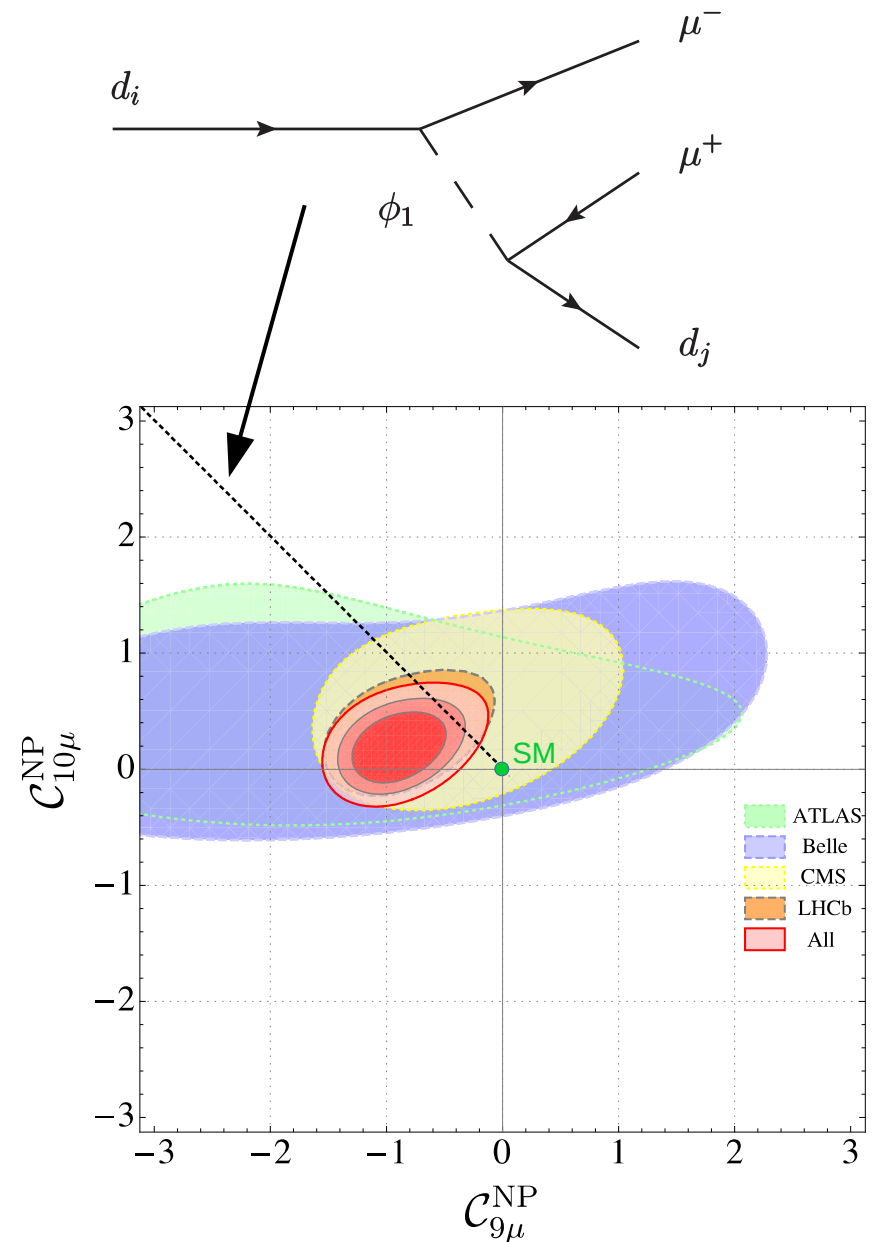
$$R(K^{(*)}) = \frac{B \rightarrow K^{(*)} \mu^+ \mu^-}{B \rightarrow K^{(*)} e^+ e^-}.$$

- LHCb: $R(K) \sim 0.85$,
 $R(K^*) \sim 0.67$.

- Improve fit with

$$m_{\phi_1} \simeq 30 \text{ TeV} \sqrt{y_2 y_3}.$$

[Alok+, PRD '17; Dorsner+, JHEP '17;
Capdevila+, JHEP '18, Algueró+, EPJC '19]



[Algueró+, EPJC '19]

Two-body nucleon decays

Channel	$ \Delta(B - L) $	$\frac{\Gamma^{-1}}{10^{30} \text{ yr}}$	
$p \rightarrow e^+ + \gamma$	0	41000	[72]
$p \rightarrow e^+ + \pi^0$	0	16000	[24]
$p \rightarrow e^+ + \eta$	0	10000	[73]
$p \rightarrow e^+ + \rho^0$	0	720	[73]
$p \rightarrow e^+ + \omega$	0	1600	[73]
$p \rightarrow e^+ + K^0$	0	1000	[74]
$p \rightarrow e^+ + K^{*,0}$	0	84	[65]
$p \rightarrow \mu^+ + \gamma$	0	21000	[72]
$p \rightarrow \mu^+ + \pi^0$	0	7700	[24]
$p \rightarrow \mu^+ + \eta$	0	4700	[73]
$p \rightarrow \mu^+ + \rho^0$	0	570	[73]
$p \rightarrow \mu^+ + \omega$	0	2800	[73]
$p \rightarrow \mu^+ + K^0$	0	1600	[75]
$p \rightarrow \nu + \pi^+$	0,2	390	[76]
$p \rightarrow \nu + \rho^+$	0,2	162	[65]
$p \rightarrow \nu + K^+$	0,2	5900	[77]
$p \rightarrow \nu + K^{*,+}$	0,2	130	[78]
$n \rightarrow e^- + \pi^+$	2	65	[79] (5300* [73])
$n \rightarrow e^- + \rho^+$	2	62	[79] (217* [65])
$n \rightarrow e^- + K^+$	2		32 [62]
$n \rightarrow e^- + K^{*,+}$	2		
$n \rightarrow e^+ + \pi^-$	0		5300 [73]
$n \rightarrow e^+ + \rho^-$	0		217 [65]
$n \rightarrow e^+ + K^-$	0		17 [65]
$n \rightarrow e^+ + K^{*,-}$	0		
$n \rightarrow \mu^- + \pi^+$	2	49	[79] (3500* [73])
$n \rightarrow \mu^- + \rho^+$	2	7	[79] (228* [65])
$n \rightarrow \mu^- + K^+$	2		57 [62]
$n \rightarrow \mu^+ + \pi^-$	0		3500 [73]
$n \rightarrow \mu^+ + \rho^-$	0		228 [65]
$n \rightarrow \mu^+ + K^-$	0		26 [65]
$n \rightarrow \nu + \gamma$	0,2		550 [28]
$n \rightarrow \nu + \pi^0$	0,2		1100 [76]
$n \rightarrow \nu + \eta$	0,2		158 [65]
$n \rightarrow \nu + \rho^0$	0,2		19 [79]
$n \rightarrow \nu + \omega$	0,2		108 [65]
$n \rightarrow \nu + K^0$	0,2		130 [74]
$n \rightarrow \nu + K^{*,0}$	0,2		78 [65]

[JH, Takhistov, PRD '20]

Three-body nucleon decays

Channel	$ \Delta(B-L) $	$\frac{\Gamma^{-1}}{10^{30} \text{ yr}}$
$p \rightarrow e^- + e^+ + e^+$	0	793 [65]
$p \rightarrow e^- + e^+ + \mu^+$	0	529 [65]
$p \rightarrow e^+ + e^+ + \mu^-$	0	529* [65]
$p \rightarrow e^- + \mu^+ + \mu^+$	0	6 [64] (359* [65])
$p \rightarrow e^+ + \mu^- + \mu^+$	0	359 [65]
$p \rightarrow \mu^- + \mu^+ + \mu^+$	0	675 [65]
$p \rightarrow e^+ + 2\nu$	0,2	170 [81]
$p \rightarrow \mu^+ + 2\nu$	0,2	220 [81]
$p \rightarrow e^- + 2\pi^+$	2	30 [62] (82* [65])
$p \rightarrow e^- + \pi^+ + \rho^+$	2	
$p \rightarrow e^- + K^+ + \pi^+$	2	75 [65]
$p \rightarrow e^+ + 2\gamma$	0	100 [82] (793* [65])
$p \rightarrow e^+ + \pi^- + \pi^+$	0	82 [65]
$p \rightarrow e^+ + \rho^- + \pi^+$	0	
$p \rightarrow e^+ + K^- + \pi^+$	0	75* [65]
$p \rightarrow e^+ + \pi^- + \rho^+$	0	
$p \rightarrow e^+ + \pi^- + K^+$	0	75* [65]
$p \rightarrow e^+ + 2\pi^0$	0	147 [65]
$p \rightarrow e^+ + \pi^0 + \eta$	0	
$p \rightarrow e^+ + \pi^0 + \rho^0$	0	
$p \rightarrow e^+ + \pi^0 + \omega$	0	
$p \rightarrow e^+ + \pi^0 + K^0$	0	
$p \rightarrow \mu^- + 2\pi^+$	2	17 [62] (133* [65])
$p \rightarrow \mu^- + K^+ + \pi^+$	2	245 [65]
$p \rightarrow \mu^+ + 2\gamma$	0	529* [65]
$p \rightarrow \mu^+ + \pi^- + \pi^+$	0	133 [65]
$p \rightarrow \mu^+ + K^- + \pi^+$	0	245* [65]
$p \rightarrow \mu^+ + \pi^- + K^+$	0	245* [65]
$p \rightarrow \mu^+ + 2\pi^0$	0	101 [65]
$p \rightarrow \mu^+ + \pi^0 + \eta$	0	
$p \rightarrow \mu^+ + \pi^0 + K^0$	0	
$p \rightarrow \nu + \pi^+ + \pi^0$	0,2	
$p \rightarrow \nu + \pi^+ + \eta$	0,2	
$p \rightarrow \nu + \pi^+ + \rho^0$	0,2	
$p \rightarrow \nu + \pi^+ + \omega$	0,2	
$p \rightarrow \nu + \pi^+ + K^0$	0,2	
$p \rightarrow \nu + \rho^+ + \pi^0$	0,2	
$p \rightarrow \nu + K^+ + \pi^0$	0,2	

Channel	$ \Delta(B-L) $	$\frac{\Gamma^{-1}}{10^{30} \text{ yr}}$
$n \rightarrow \nu + e^- + e^+$	0,2	257 [65]
$n \rightarrow \nu + e^- + \mu^+$	0,2	83 [65]
$n \rightarrow \nu + e^+ + \mu^-$	0,2	83* [65]
$n \rightarrow \nu + \mu^- + \mu^+$	0,2	79 [65]
$n \rightarrow 3\nu$	0,2,4	0.58 [83]
$n \rightarrow e^- + \pi^+ + \pi^0$	2	29 [62] (52* [65])
$n \rightarrow e^- + \pi^+ + \eta$	2	
$n \rightarrow e^- + \pi^+ + \rho^0$	2	
$n \rightarrow e^- + \pi^+ + \omega$	2	
$n \rightarrow e^- + \pi^+ + K^0$	2	
$n \rightarrow e^- + \rho^+ + \pi^0$	2	
$n \rightarrow e^- + K^+ + \pi^0$	2	
$n \rightarrow e^+ + \pi^- + \pi^0$	0	52 [65]
$n \rightarrow e^+ + \pi^- + \eta$	0	
$n \rightarrow e^+ + \pi^- + \rho^0$	0	
$n \rightarrow e^+ + \pi^- + \omega$	0	
$n \rightarrow e^+ + \pi^- + K^0$	0	18 [82]
$n \rightarrow e^+ + \rho^- + \pi^0$	0	
$n \rightarrow e^+ + K^- + \pi^0$	0	
$n \rightarrow \mu^- + \pi^+ + \pi^0$	2	34 [62] (74* [65])
$n \rightarrow \mu^- + \pi^+ + \eta$	2	
$n \rightarrow \mu^- + \pi^+ + K^0$	2	
$n \rightarrow \mu^- + K^+ + \pi^0$	2	
$n \rightarrow \mu^+ + \pi^- + \pi^0$	0	74 [65]
$n \rightarrow \mu^+ + \pi^- + \eta$	0	
$n \rightarrow \mu^+ + \pi^- + K^0$	0	
$n \rightarrow \mu^+ + K^- + \pi^0$	0	
$n \rightarrow \nu + 2\gamma$	0,2	219 [65]
$n \rightarrow \nu + \pi^- + \pi^+$	0,2	
$n \rightarrow \nu + \rho^- + \pi^+$	0,2	
$n \rightarrow \nu + K^- + \pi^+$	0,2	
$n \rightarrow \nu + \pi^- + \rho^+$	0,2	
$n \rightarrow \nu + \pi^- + K^+$	0,2	
$n \rightarrow \nu + 2\pi^0$	0,2	
$n \rightarrow \nu + \pi^0 + \eta$	0,2	
$n \rightarrow \nu + \pi^0 + \rho^0$	0,2	
$n \rightarrow \nu + \pi^0 + \omega$	0,2	
$n \rightarrow \nu + \pi^0 + K^0$	0,2	

[JH, Takhistov, PRD '20]
Does not include SK's 2020
limits on $p \rightarrow \ell\ell\ell$.

Two-body di-nucleon decays

Channel	$ \Delta(B-L) $	$\frac{\Gamma^{-1}}{10^{30} \text{ yr}}$
$pp \rightarrow e^+ + e^+$	0	4200 [72]
$pp \rightarrow \mu^+ + \mu^+$	0	4400 [72]
$pp \rightarrow e^+ + \mu^+$	0	4400 [72]
$pp \rightarrow e^+ + \tau^+$	0	
$pp \rightarrow \pi^+ + \pi^+$	2	72 [115]
$pp \rightarrow \pi^+ + \rho^+$	2	
$pp \rightarrow \pi^+ + K^+$	2	
$pp \rightarrow \pi^+ + K^{*,+}$	2	
$pp \rightarrow \rho^+ + \rho^+$	2	
$pp \rightarrow \rho^+ + K^+$	2	
$pp \rightarrow \rho^+ + K^{*,+}$	2	
$pp \rightarrow K^+ + K^+$	2	170 [116]
$pp \rightarrow K^+ + K^{*,+}$	2	
$pp \rightarrow K^{*,+} + K^{*,+}$	2	

$nn \rightarrow e^+ + e^-$	2	4200 [72]
$nn \rightarrow e^+ + \mu^-$	2	4400 [72]
$nn \rightarrow \mu^+ + e^-$	2	4400 [72]
$nn \rightarrow \mu^+ + \mu^-$	2	4400 [72]
$nn \rightarrow e^+ + \tau^-$	2	
$nn \rightarrow \tau^+ + e^-$	2	
$nn \rightarrow 2\nu$	0,2,4	1.4 [83]
$nn \rightarrow 2\gamma$	2	4100 [72]
$nn \rightarrow \gamma + \pi^0$	2	
$nn \rightarrow \gamma + \eta$	2	
$nn \rightarrow \gamma + \rho^0$	2	
$nn \rightarrow \gamma + \omega$	2	
$nn \rightarrow \gamma + \eta'$	2	
$nn \rightarrow \gamma + K^0$	2	
$nn \rightarrow \gamma + K^{*,0}$	2	
$nn \rightarrow \gamma + D^0$	2	
$nn \rightarrow \gamma + \phi$	2	
$nn \rightarrow \pi^- + \pi^+$	2	0.7 [62] (72* [115])
$nn \rightarrow \pi^+ + \rho^-$	2	
$nn \rightarrow K^- + \pi^+$	2	
$nn \rightarrow K^{*,-} + \pi^+$	2	
$nn \rightarrow \pi^- + \rho^+$	2	
$nn \rightarrow K^+ + \pi^-$	2	
$nn \rightarrow K^{*,+} + \pi^-$	2	
$nn \rightarrow 2\pi^0$	2	404 [115]
$nn \rightarrow \eta + \pi^0$	2	
$nn \rightarrow \pi^0 + \rho^0$	2	
$nn \rightarrow \pi^0 + \omega$	2	
$nn \rightarrow \eta' + \pi^0$	2	
$nn \rightarrow K^0 + \pi^0$	2	
$nn \rightarrow K^{*,0} + \pi^0$	2	

Channel	$ \Delta(B-L) $	$\frac{\Gamma^{-1}}{10^{30} \text{ yr}}$
$nn \rightarrow \pi^0 + \phi$	2	
$nn \rightarrow 2\eta$	2	
$nn \rightarrow \eta + \rho^0$	2	
$nn \rightarrow \eta + \omega$	2	
$nn \rightarrow \eta + \eta'$	2	
$nn \rightarrow \eta + K^0$	2	
$nn \rightarrow \eta + K^{*,0}$	2	
$nn \rightarrow \eta + \phi$	2	
$nn \rightarrow 2\rho^0$	2	
$nn \rightarrow \rho^0 + \omega$	2	
$nn \rightarrow \eta' + \rho^0$	2	
$nn \rightarrow K^0 + \rho^0$	2	
$nn \rightarrow K^{*,0} + \rho^0$	2	
$nn \rightarrow \rho^0 + \phi$	2	
$nn \rightarrow \rho^- + \rho^+$	2	
$nn \rightarrow K^+ + \rho^-$	2	
$nn \rightarrow K^{*,+} + \rho^-$	2	
$nn \rightarrow K^- + \rho^+$	2	
$nn \rightarrow K^{*,-} + \rho^+$	2	
$nn \rightarrow 2\omega$	2	
$nn \rightarrow \eta' + \omega$	2	
$nn \rightarrow K^0 + \omega$	2	
$nn \rightarrow K^{*,0} + \omega$	2	
$nn \rightarrow \omega + \phi$	2	
$nn \rightarrow \eta' + K^0$	2	
$nn \rightarrow \eta' + K^{*,0}$	2	
$nn \rightarrow K^- + K^+$	2	170* [116]
$nn \rightarrow K^+ + K^{*,-}$	2	
$nn \rightarrow K^- + K^{*,+}$	2	
$nn \rightarrow 2K^0$	2	
$nn \rightarrow K^{*,0} + K^0$	2	
$nn \rightarrow K^0 + \phi$	2	
$nn \rightarrow 2K^{*,0}$	2	
$nn \rightarrow K^{*,-} + K^{*,+}$	2	

Channel	$ \Delta(B-L) $	$\frac{\Gamma^{-1}}{10^{30} \text{ yr}}$
$pn \rightarrow e^+ + \nu$	0,2	260 [28]
$pn \rightarrow \mu^+ + \nu$	0,2	200 [28]
$pn \rightarrow \tau^+ + \nu$	0,2	29 [28]
$pn \rightarrow \gamma + \pi^+$	2	
$pn \rightarrow \gamma + \rho^+$	2	
$pn \rightarrow \gamma + K^+$	2	
$pn \rightarrow \gamma + K^{*,+}$	2	
$pn \rightarrow \gamma + D^+$	2	
$pn \rightarrow \pi^+ + \pi^0$	2	170 [115]
$pn \rightarrow \eta + \pi^+$	2	
$pn \rightarrow \pi^+ + \rho^0$	2	
$pn \rightarrow \pi^+ + \omega$	2	
$pn \rightarrow \eta' + \pi^+$	2	
$pn \rightarrow K^0 + \pi^+$	2	
$pn \rightarrow K^{*,0} + \pi^+$	2	
$pn \rightarrow \pi^+ + \phi$	2	
$pn \rightarrow \pi^0 + \rho^+$	2	
$pn \rightarrow K^+ + \pi^0$	2	
$pn \rightarrow K^{*,+} + \pi^0$	2	
$pn \rightarrow \eta + \rho^+$	2	
$pn \rightarrow \eta + K^+$	2	
$pn \rightarrow \eta + K^{*,+}$	2	
$pn \rightarrow \rho^+ + \rho^0$	2	
$pn \rightarrow K^+ + \rho^0$	2	
$pn \rightarrow K^{*,+} + \rho^0$	2	
$pn \rightarrow \rho^+ + \omega$	2	
$pn \rightarrow \eta' + \rho^+$	2	
$pn \rightarrow K^0 + \rho^+$	2	
$pn \rightarrow K^{*,0} + \rho^+$	2	
$pn \rightarrow \rho^+ + \phi$	2	
$pn \rightarrow K^+ + \omega$	2	
$pn \rightarrow K^{*,+} + \omega$	2	
$pn \rightarrow \eta' + K^+$	2	
$pn \rightarrow \eta' + K^{*,+}$	2	
$pn \rightarrow K^+ + K^0$	2	
$pn \rightarrow K^+ + K^{*,0}$	2	
$pn \rightarrow K^+ + \phi$	2	
$pn \rightarrow K^{*,+} + K^0$	2	
$pn \rightarrow K^{*,+} + K^{*,0}$	2	

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