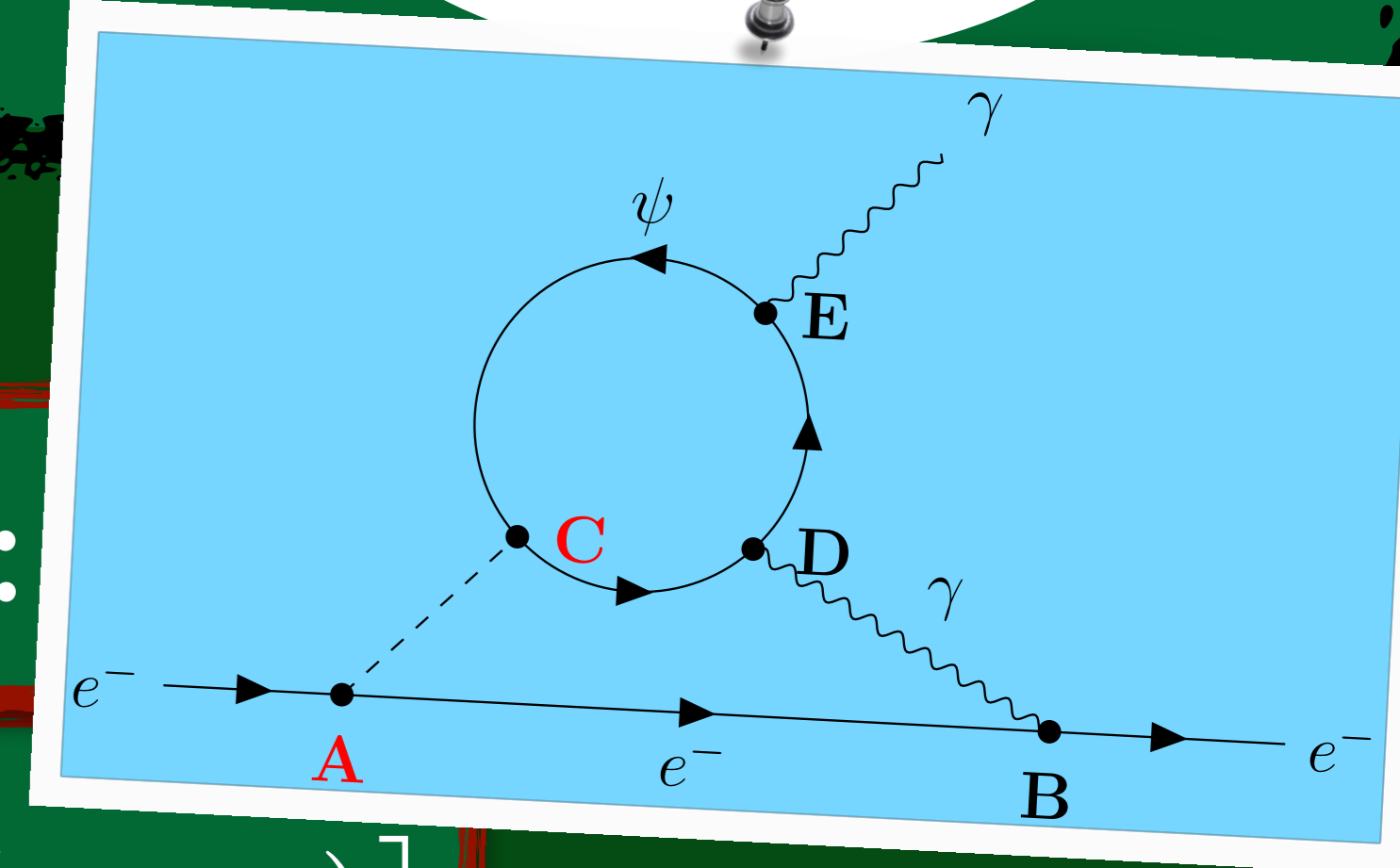


CP Violation in the τ Lepton Yukawa Coupling and Flavour Symmetries



1. \mathcal{CP} τ Yukawa Coupling

Effective Higgs- τ Lagrangian:

$$\mathcal{L}_{\text{eff}} = -\frac{y_\tau}{\sqrt{2}} (\kappa_\tau \bar{\tau}\tau + i \tilde{\kappa}_\tau \bar{\tau}\gamma_5\tau) h$$

$$\begin{aligned} y_\tau &= \sqrt{2} m_\tau / v \\ \kappa_\tau^{\text{SM}} &= 1, \tilde{\kappa}_\tau^{\text{SM}} = 0 \end{aligned}$$

$\tilde{\kappa}_\tau \neq 0$ encodes BSM \mathcal{CP} effects:

1. It sources the baryon asymmetry of the Universe (BAU) in EWBG:
With SMEFT d=6 operators to τ Yukawas, $|\tilde{\kappa}_\tau| \gtrsim 0.08$ can explain the entire BAU!!! [1]
2. It contributes to the electron EDM (eEDM)

2. eEDM Bounds

The Barr-Zee diagram contribution to eEDM [2]:

$$\frac{d_e}{e} = 4 N_C Q_\psi^2 \frac{\alpha_{\text{em}}}{(4\pi)^3} \sqrt{2} G_F m_e [\kappa_e \tilde{\kappa}_\psi f_1(x_\psi/h) + \tilde{\kappa}_e \kappa_\psi f_2(x_\psi/h)]$$

ACME II Bound

$$|d_e| < 1.1 \times 10^{-29} \text{ e cm, at 90\% C.L.}$$

Bounds assuming single NP contribution:

- ◆ $\psi = \tau$ and $\tilde{\kappa}_e = 0$ [1]: $|\tilde{\kappa}_\tau| \lesssim 0.3$
- ◆ $\psi = t$ and $\tilde{\kappa}_t = 0$: $|\tilde{\kappa}_e| \lesssim 0.0017$

Compatible with BAU!!!

3. Imposing Flavour Symmetries

Assumptions

1. Lepton Yukawas from SMEFT d=4 and d=6 operators
2. \mathcal{L} compatible with flavour symmetry

In the interaction basis:

Λ : effective NP scale

$$\mathcal{L} = -\bar{L}' H Y' e'_R - \bar{L}' H C' e'_R \frac{H^\dagger H}{\Lambda^2} + \text{h.c.}$$

Y', C' : complex 3x3 matrices in flavor space

In the mass basis, below EWSB scale:

$$\mathcal{L} = -\bar{e}_L Y e_R \frac{v}{\sqrt{2}} - \bar{e}_L \left(Y + \frac{v^2}{\Lambda^2} C \right) e_R \frac{h}{\sqrt{2}} + \text{h.c.} + \dots$$

$$C = V^\dagger C' U$$

$$\begin{aligned} \tilde{\kappa}_\tau &= \frac{v^2}{\Lambda^2} \frac{\text{Im } C_{33}}{y_\tau} \\ \tilde{\kappa}_e &= \frac{v^2}{\Lambda^2} \frac{\text{Im } C_{11}}{y_e} \end{aligned}$$

$$\begin{aligned} Y &= V^\dagger \left(Y' + \frac{v^2}{2\Lambda^2} C' \right) U = \\ &= \sqrt{2}/v \text{diag}(m_e, m_\mu, m_\tau) \end{aligned}$$

The strong bound on $\tilde{\kappa}_e$ is translated to $\tilde{\kappa}_\tau$!!

$$|\tilde{\kappa}_\tau| \lesssim 0.0017 \frac{m_e}{m_\tau} \frac{\text{Im } C_{33}}{\text{Im } C_{11}}$$

4. Two Concrete Examples

Minimal Flavour Violation

$$C' = c' Y'$$

c' : complex number

$|\tilde{\kappa}_\tau| \lesssim 0.0017$
Incompatible with BAU!!!

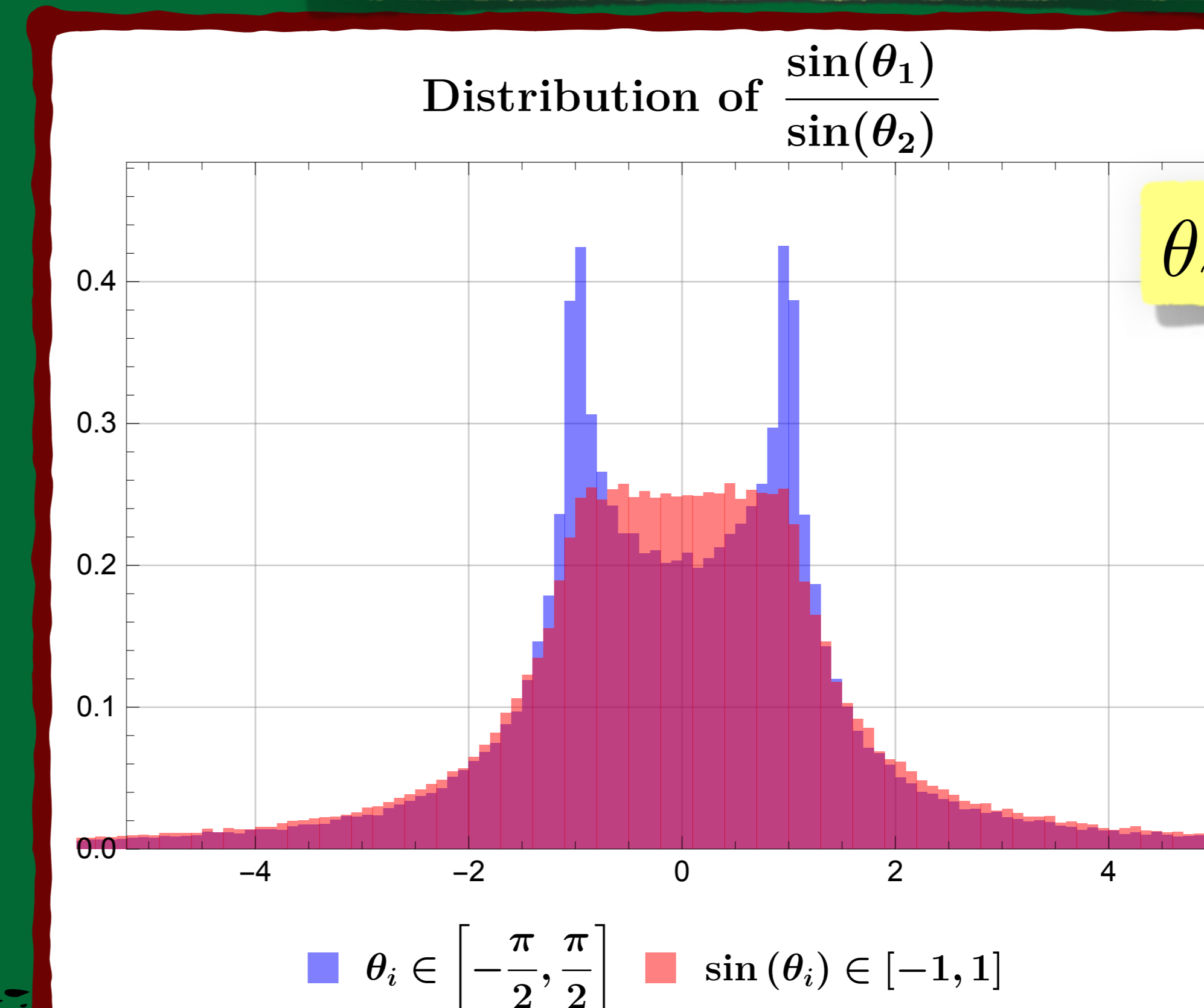
U(1) Charges

$$\begin{aligned} \text{Flavon} &: n_\phi = -1 \\ \bar{L}_i &: n_{L1} > n_{L2} > n_{L3} > 0 \\ e_{Ri} &: n_{R1} > n_{R2} > n_{R3} > 0 \end{aligned}$$

Froggatt-Nielsen Models with horizontal U(1)

$$\begin{aligned} C_{33} &\simeq \mathcal{O}(\sqrt{2} m_\tau / v) e^{i\theta_1} \\ C_{11} &\simeq \mathcal{O}(\sqrt{2} m_e / v) e^{i\theta_2} \end{aligned}$$

θ_i : effective not fixed phases



$$|\tilde{\kappa}_\tau| \lesssim 0.0017 \frac{\sin \theta_1}{\sin \theta_2} \mathcal{O}(1)$$

Incompatible with BAU!!!