

Motivation

The **Standard Model** (SM) of particle physics describes electroweak interactions at low energies with remarkable precision but cannot provide an explanation for:

- **neutrino flavour oscillations** which imply nonvanishing neutrino masses and lepton mixing;
- the observed **Baryon Asymmetry of the Universe** (BAU).

These two limitations may be overcome by adding to the SM **two heavy right-handed (RH) neutrinos**, which:

- act as light-neutrino mass mediators at the classical level, via **type-I seesaw mechanism** and,
- Play a crucial role in generating the BAU via **leptogenesis**.

Occam's Razor approach

Consider the **most economical seesaw framework** with the **most economical texture zeros** in the lepton Yukawa and mass matrices of the model

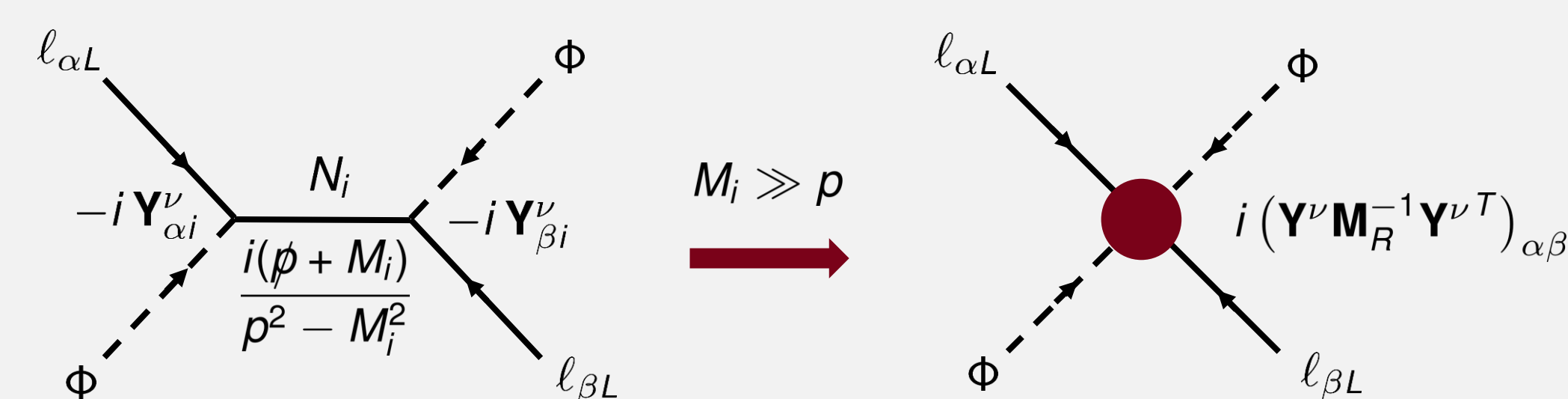
Previous studies [1] have shown that the two RH neutrino extension of the SM (2RHvSM) with maximally-restrictive texture-zero Yukawa and mass matrices **is not compatible with data** for a normally-ordered (NO) neutrino mass spectrum (currently preferred by data at 3σ [2]), when **the lepton mixing originates solely from the neutrino sector**. Also, the lightest RH neutrino mass required to generate the observed BAU via leptogenesis ($M_1 \sim 10^{14}$ GeV) is in **conflict with vanilla scenarios for axion dark matter** where the reheating temperature of the Universe is typically below 10^{12} GeV.

Can we get compatibility with NO and a lower leptogenesis scale by including two-flavour charged-lepton mixing in our model?

Minimal type-I seesaw mechanism

In the neutrino sector: $\mathcal{L}_\nu = -\bar{\ell}_L \mathbf{Y}_\nu^* \tilde{\Phi} \nu_R - \frac{1}{2} \bar{\nu}_R \mathbf{M}_R \nu_R + \text{H.c.}$

Type-I seesaw mechanism



After EWSB: $\mathbf{M}_\nu = -v^2 \mathbf{Y}_\nu \mathbf{M}_R^{-1} \mathbf{Y}_\nu^T$ with $\mathbf{U}_\nu^T \mathbf{M}_\nu \mathbf{U}_\nu = \text{diag}(m_1, m_2, m_3)$

In the charged-lepton sector: $\mathcal{L}_\ell = -\bar{\ell}_L \mathbf{Y}_\ell \Phi e_R + \text{H.c.}$

After EWSB: $\mathbf{M}_\ell = v \mathbf{Y}_\ell$ with $\mathbf{U}_\ell^T \mathbf{M}_\ell \mathbf{U}_\ell = \text{diag}(m_e^2, m_\mu^2, m_\tau^2)$

Low-energy constraints

Effective neutrino mass matrices \mathbf{M}_ν generated from the most restrictive \mathbf{Y}_ν and \mathbf{M}_R texture-zero matrices:

$$A: \begin{pmatrix} 0 & \times & \times \\ \cdot & \times & \times \\ \cdot & \cdot & \times \end{pmatrix} B: \begin{pmatrix} \times & 0 & \times \\ \cdot & \times & \times \\ \cdot & \cdot & \times \end{pmatrix} C: \begin{pmatrix} \times & \times & 0 \\ \cdot & \times & \times \\ \cdot & \cdot & \times \end{pmatrix} D: \begin{pmatrix} \times & \times & \times \\ \cdot & 0 & \times \\ \cdot & \cdot & \times \end{pmatrix} E: \begin{pmatrix} \times & \times & \times \\ \cdot & \times & 0 \\ \cdot & \cdot & \times \end{pmatrix} F: \begin{pmatrix} \times & \times & \times \\ \cdot & \times & \times \\ \cdot & \cdot & \times \end{pmatrix}$$

which feature the condition $(\mathbf{M}_\nu)_{ij} = 0$, resulting in two low-energy constraints. For NO:

$$\frac{m_2}{m_3} = -\frac{(\mathbf{U}_\ell^* \mathbf{U}^*)_{i3} (\mathbf{U}_\ell^* \mathbf{U}^*)_{j3}}{(\mathbf{U}_\ell^* \mathbf{U}^*)_{i2} (\mathbf{U}_\ell^* \mathbf{U}^*)_{j2}}$$

$$\alpha = -\arg \left[\frac{(\mathbf{U}_\ell^* \mathbf{V}_\delta^*)_{i3} (\mathbf{U}_\ell^* \mathbf{V}_\delta^*)_{j3}}{(\mathbf{U}_\ell^* \mathbf{V}_\delta^*)_{i2} (\mathbf{U}_\ell^* \mathbf{V}_\delta^*)_{j2}} \right]$$

being the **lepton mixing matrix** in the standard parametrization given by:

$$\mathbf{U} = \mathbf{U}_\ell^i \mathbf{U}_\nu = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha/2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Most restrictive two-flavour mixing **charged-lepton mass matrices** \mathbf{M}_ℓ :

$$L_1^k: \begin{pmatrix} m_k & 0 & 0 \\ 0 & 0 & \epsilon \\ 0 & \epsilon & m \end{pmatrix} L_2^k: \begin{pmatrix} 0 & 0 & \epsilon \\ 0 & m_k & 0 \\ \epsilon & 0 & m \end{pmatrix} L_3^k: \begin{pmatrix} 0 & \epsilon & 0 \\ \epsilon & m & 0 \\ 0 & 0 & m_k \end{pmatrix}$$

which are diagonalized by a matrix \mathbf{U}_ℓ parametrized by a single angle:

$$\theta_\ell^k = \pm \frac{1}{2} \arctan \left(\frac{2\sqrt{m_i m_j}}{m_j - m_i} \right) \simeq \pm \sqrt{m_i/m_j} \text{ with } i \neq j \neq k = e, \mu, \tau \text{ and } m_j > m_i$$

δ , θ_{23} and $m_{\beta\beta}$ predictions

After verifying the compatibility of all possible combinations $(\mathbf{M}_\nu, \mathbf{M}_\ell, \theta_\ell^k) = (A-F, L_{1,2,3}^k, \pm)$ with a NO neutrino mass spectrum, we conclude that the **best-fit case corresponds to $(C, L_1^e, +)$** . This case selects the **second octant for θ_{23}** and predicts $m_{\beta\beta} \in [1.2, 3.8]$ meV.

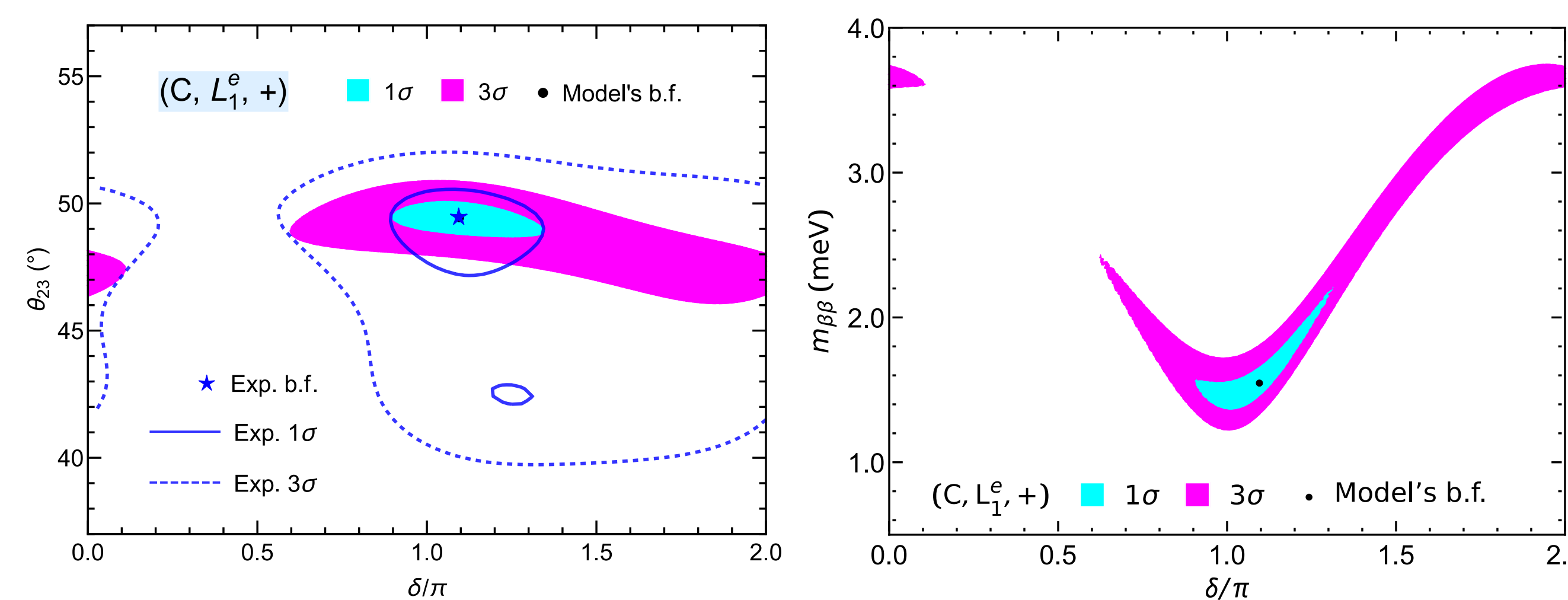
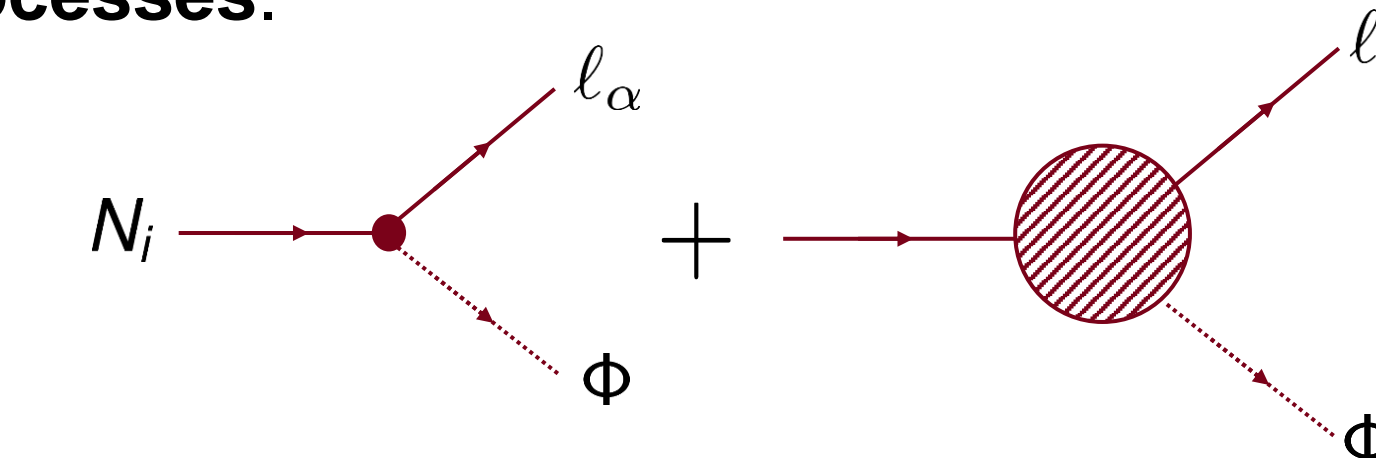


Fig. 1. 1σ and 3σ allowed regions (in cyan and magenta, respectively) in the (δ, θ_{23}) and $(\delta, m_{\beta\beta})$ planes, for the \mathbf{M}_ν and \mathbf{M}_ℓ texture zero patterns, C and L_1^e , respectively, with $\theta_\ell^e \simeq +0.24$. For comparison, the lines delimiting the regions allowed by experimental data are also shown (solid and dashed for 1σ and 3σ , respectively).

Leptogenesis predictions

A lepton asymmetry is dynamically generated via the **CP-violating out-of-equilibrium decay** of the heavy neutrinos N_1 and N_2 added to the SM, and later transformed into a baryon asymmetry via **(B-L)-conserving sphaleron processes**.



In the **two-flavoured regime** where only electron and muon Yukawa interactions are out of equilibrium (for $10^9 \lesssim M_1, M_2 \lesssim 10^{12}$ GeV), the baryon-to-photon ratio is approximately given by [3]:

$$\eta_B \simeq -9.6 \times 10^{-3} (-\kappa_1^\tau \epsilon_1^\tau - \kappa_1^\mu \epsilon_1^\mu)$$

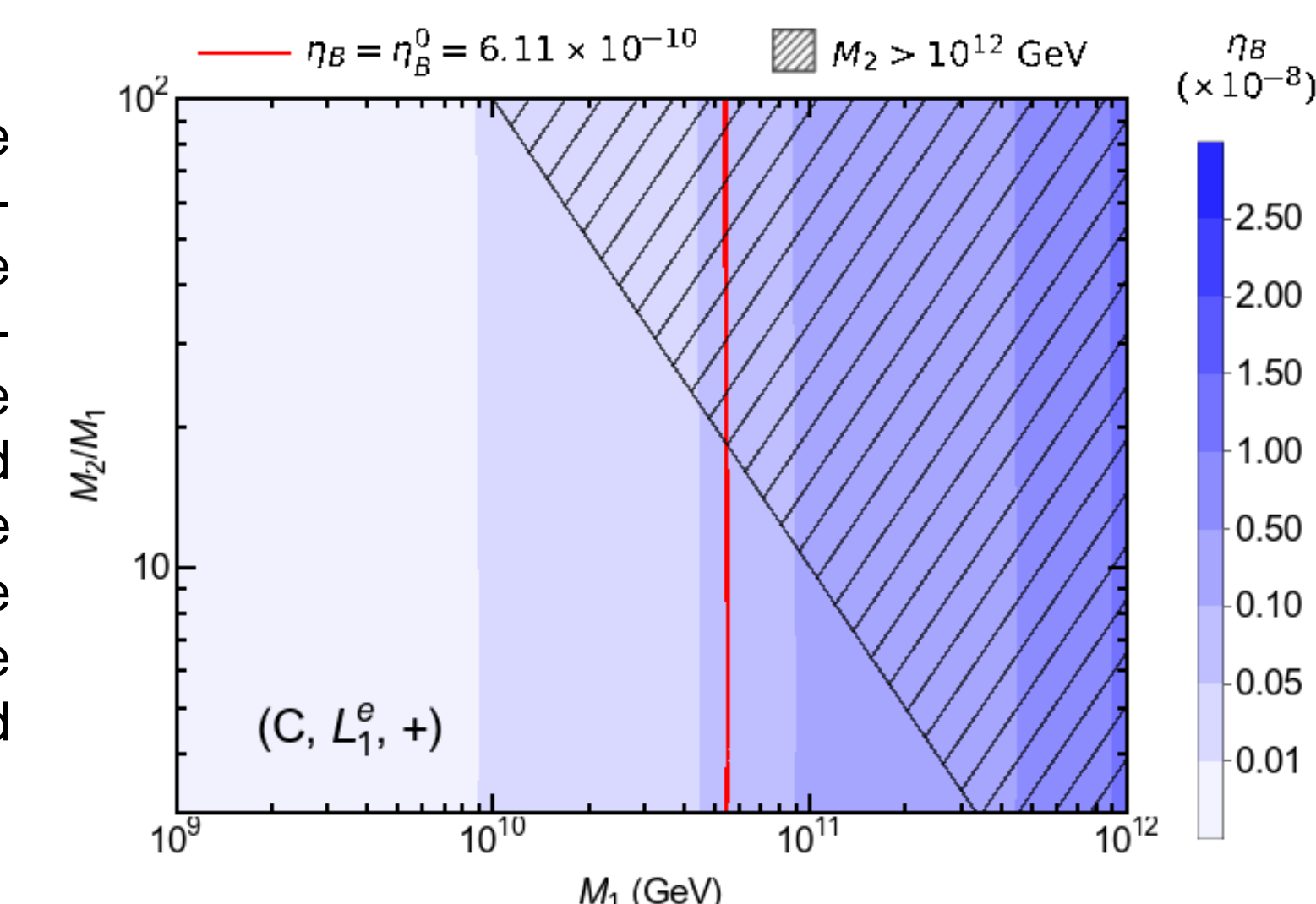
In the specific case of $(C, L_1^e, +)$, the obtained **CP asymmetries** read:

$$\epsilon_1^\mu = \epsilon_1^\tau \simeq \frac{3M_1 \sqrt{\Delta m_{31}^2} s_\delta s_{13} s_{23} c_{23}}{16\pi v^2 r_\nu \tan \theta_{12}}, \quad \epsilon_1^\tau \simeq \frac{3M_1 \sqrt{\Delta m_{31}^2} s_\delta s_{13} (s_{13} c_{23}^2 - r_\nu s_{12} c_{12} s_{23} c_{23})}{16\pi v^2 (r_\nu^2 s_{12}^2 + s_{13}^2)}$$

and the **efficiency factors** are $\kappa_1^\tau \simeq 1.7 \times 10^{-1}$ and $\kappa_1^\mu \simeq 5.6 \times 10^{-3}$.

The **observed BAU is obtained for $M_1 \sim 5.5 \times 10^{10}$ GeV**, being consistent with axion dark matter.

Fig. 2. η_B contour regions in the $(M_1, M_2/M_1)$ plane, taking the low-energy parameters that best fit the combination $(C, L_1^e, +)$. The blue-scale contour regions represent the obtained η_B values, while the red contour line corresponds to the observed value η_B^0 [4]. In the hatched region, M_2 is out of the mass interval for the flavored leptogenesis regime ($M_2 \gtrsim 3 M_1$).



Conclusions

- New Occam's razor scenario for texture-zero Yukawa and mass matrices with $(\mathbf{M}_\nu, \mathbf{M}_\ell, \theta_\ell^k) = (C, L_1^e, +)$ is **compatible with NO**, and **predicts θ_{23} belonging to the second octant**.
- Lightest RH neutrino mass required for leptogenesis to work is substantially **lowered to 5.5×10^{10} GeV** (comparing with previous works where only mixing in the neutrino sector was considered [1]).

References

- [1] Barreiros *et al.*, Phys. Rev. D 97, 115016 (2018)
- [2] Capozzi *et al.*, Phys. Rev. D 101, 116013 (2020); Salas *et al.*, J. High Energy. Phys. 2021, 71 (2021); Esteban *et al.*, J. High Energy. Phys. 2020, 178 (2020)
- [3] Antusch *et al.*, Phys. Rev. D 86, 023516 (2012)
- [4] Ade *et al.* (Planck Collaboration), Astron. Astrophys. 594, A13 (2016)