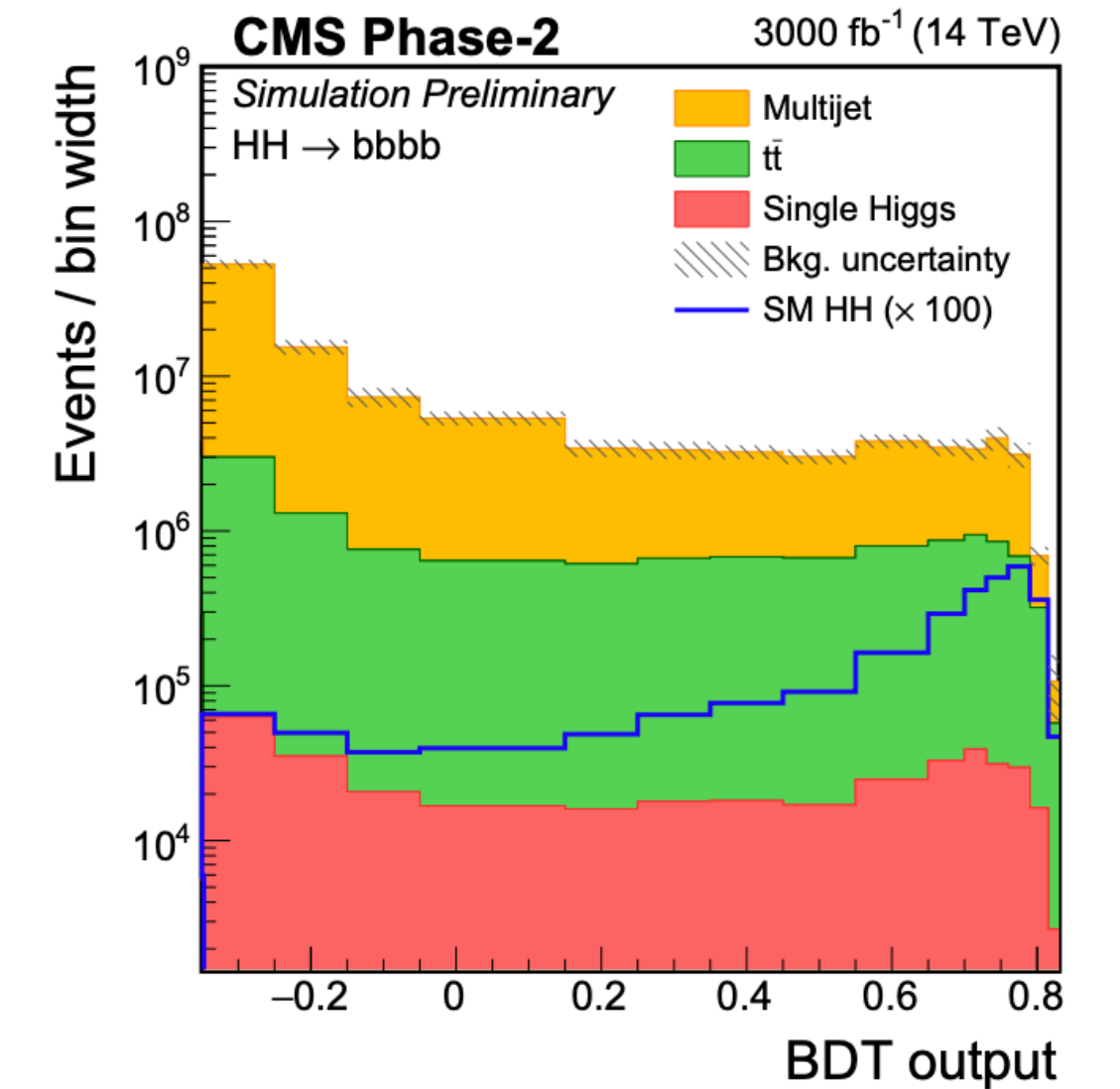
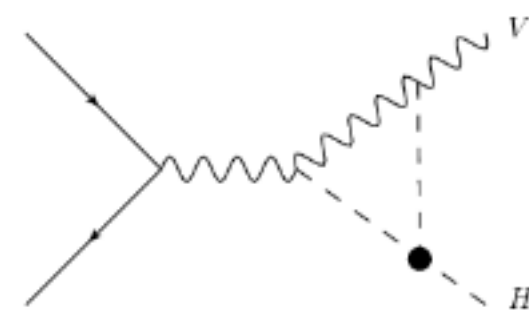
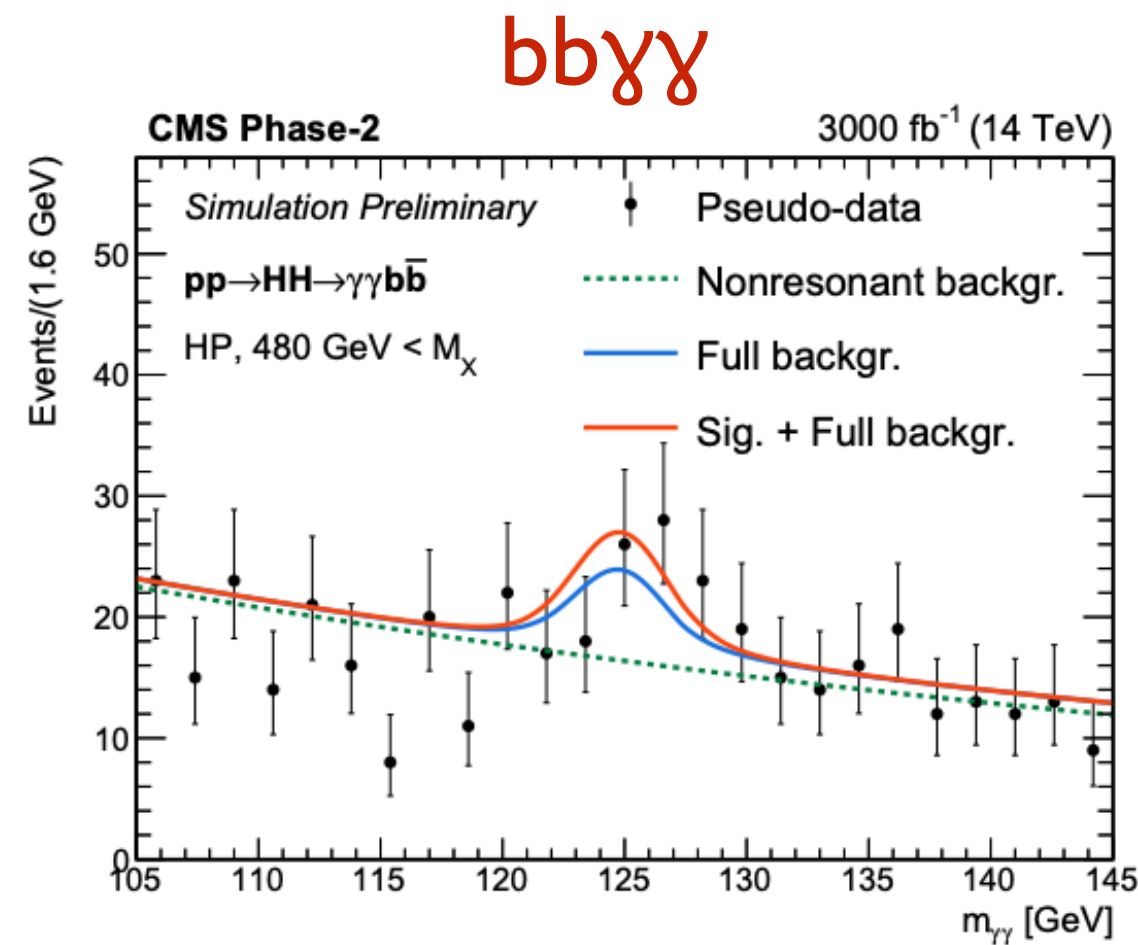
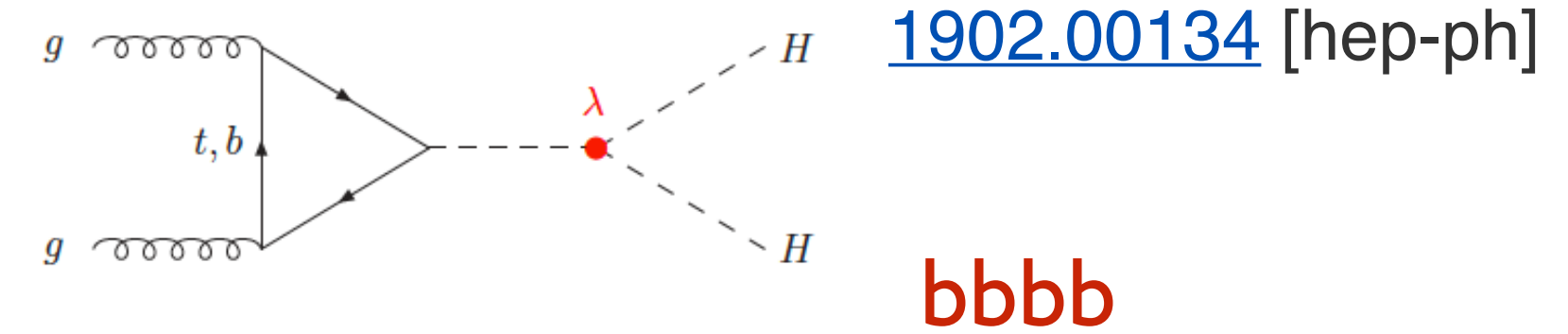


# The Higgs Potential at future colliders

Michele Selvaggi (CERN)

Snowmass '20 - 06/10/2020

# Self coupling @ HL-LHC measurements



- At the (HL-)LHC the self-coupling can be measured via both:

- Higgs pair production
- single Higgs production

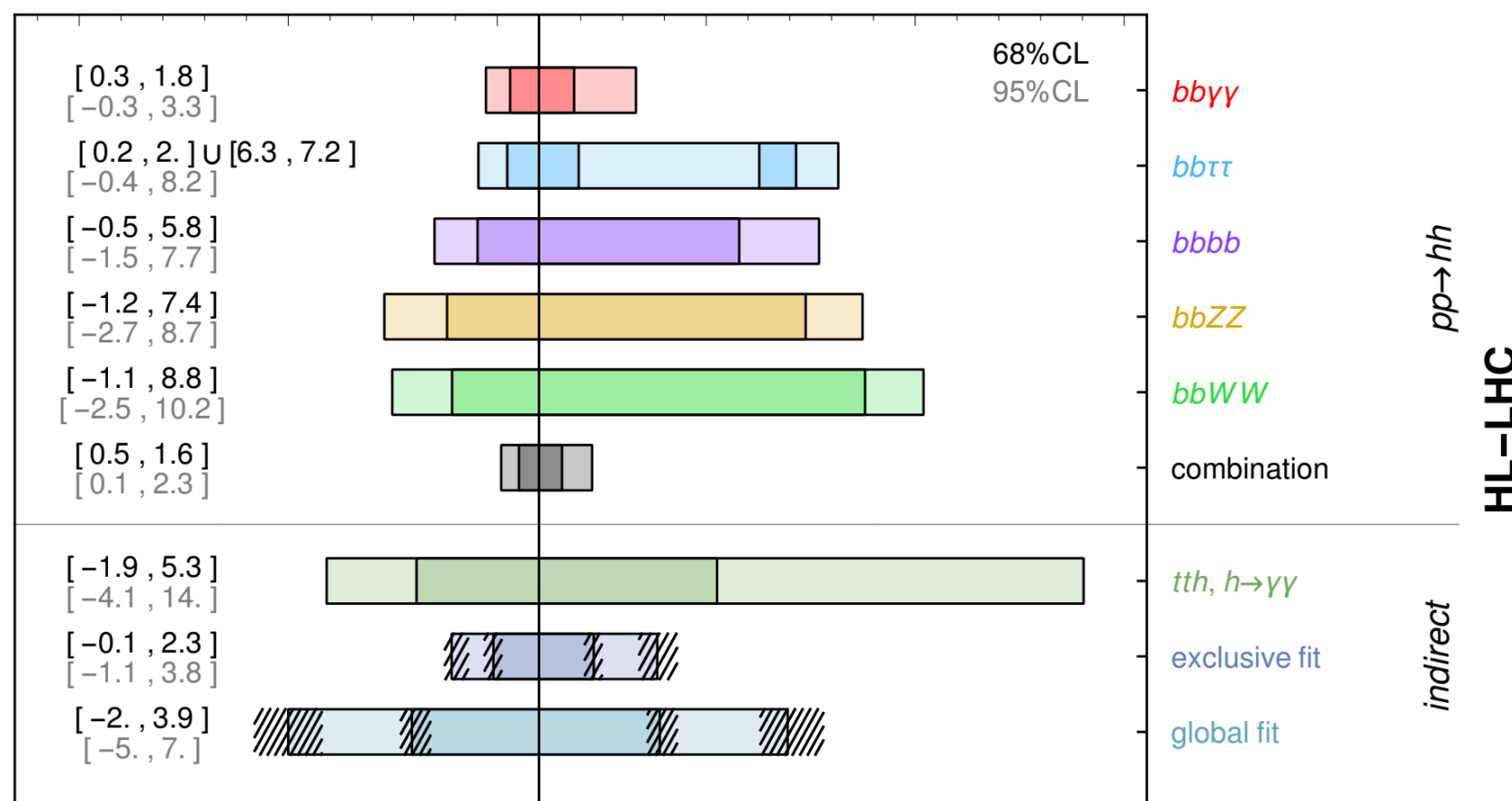
- Indirect constraint from ggH and ttH:

- $\delta\kappa_\lambda \approx 100\%$  (exclusive)
- $\delta\kappa_\lambda \approx 200\%$  (global)

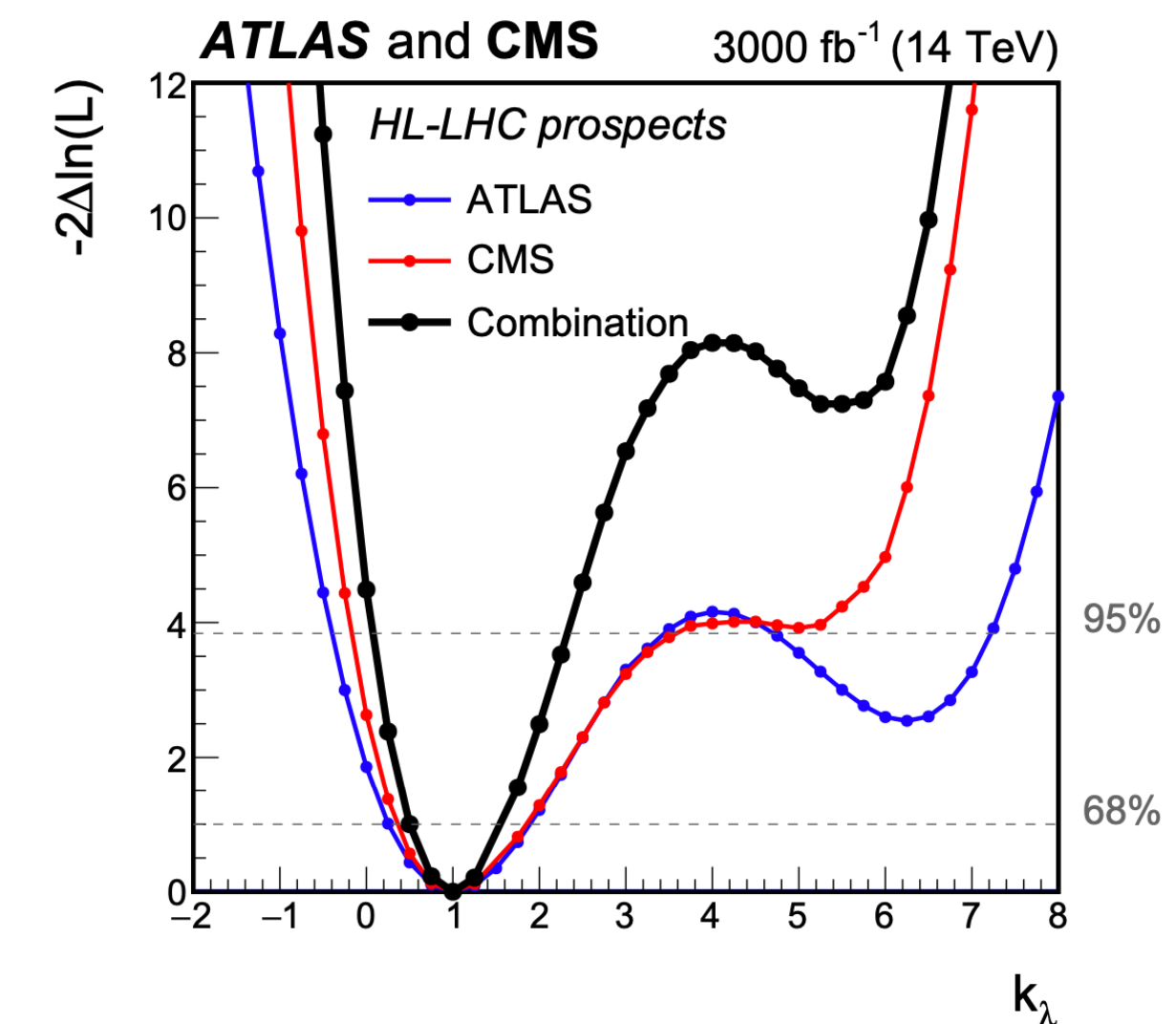
- Direct measurement:

- $\delta\kappa_\lambda \approx 50\%$

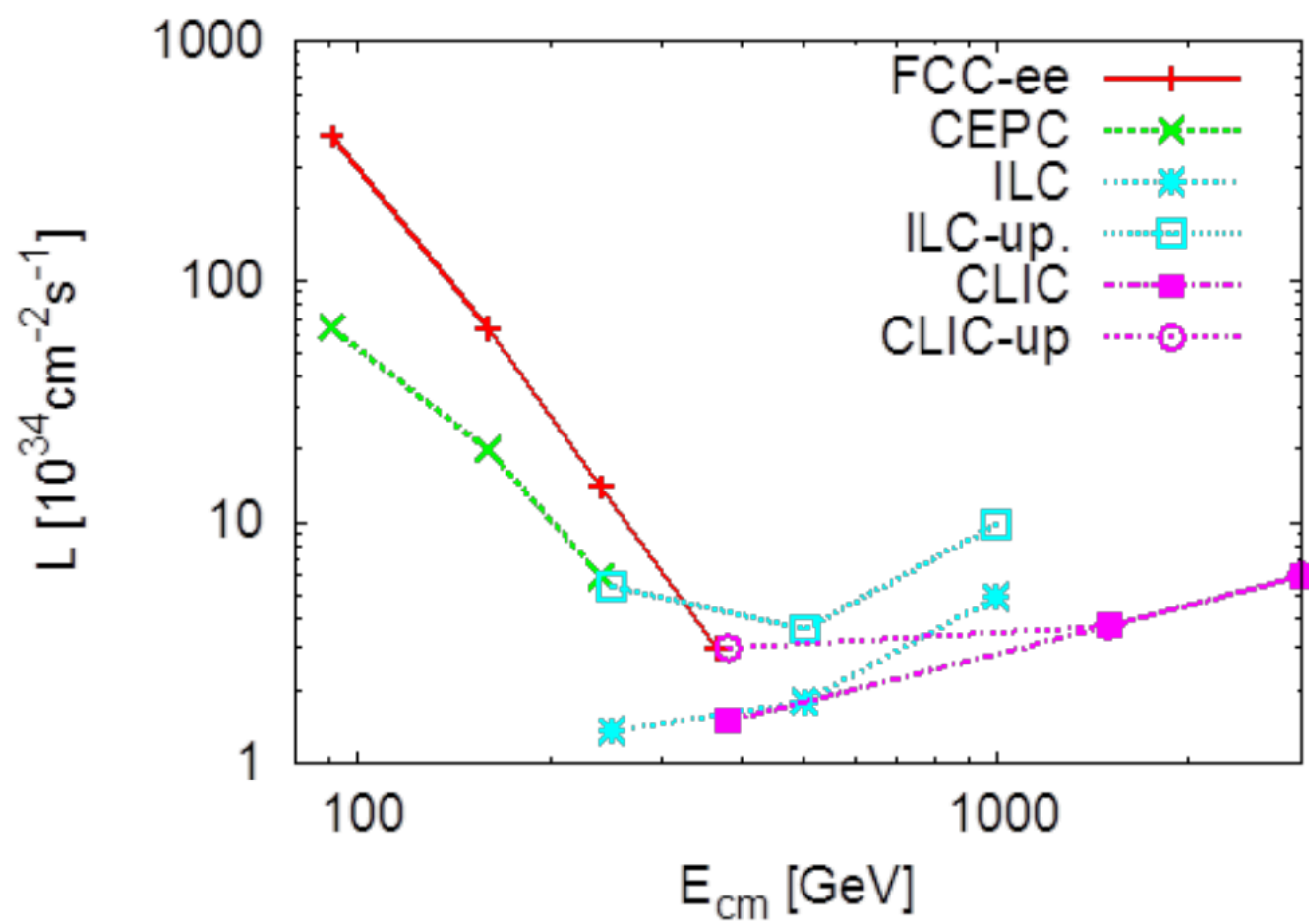
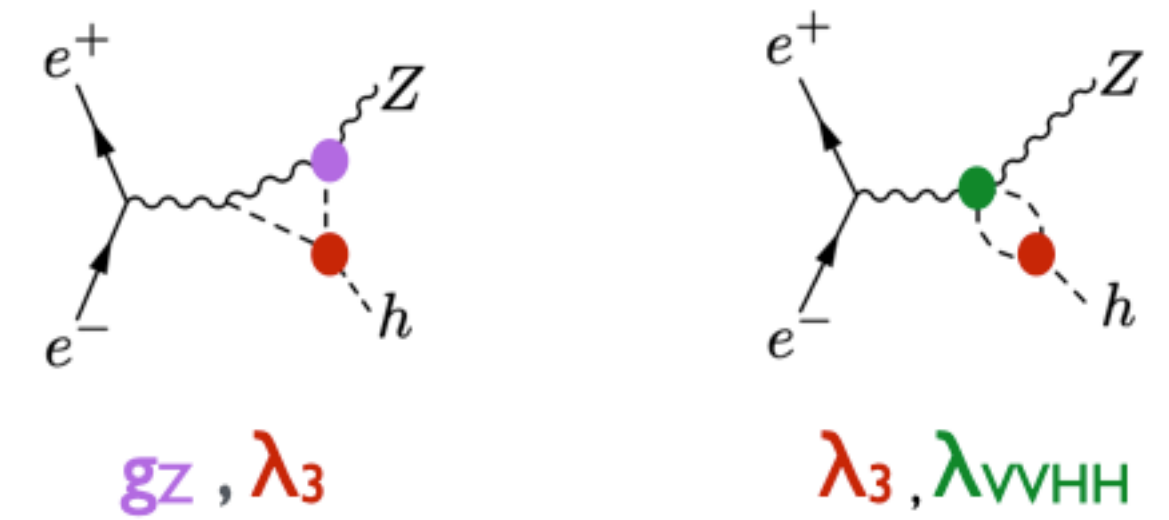
## combination HL-LHC



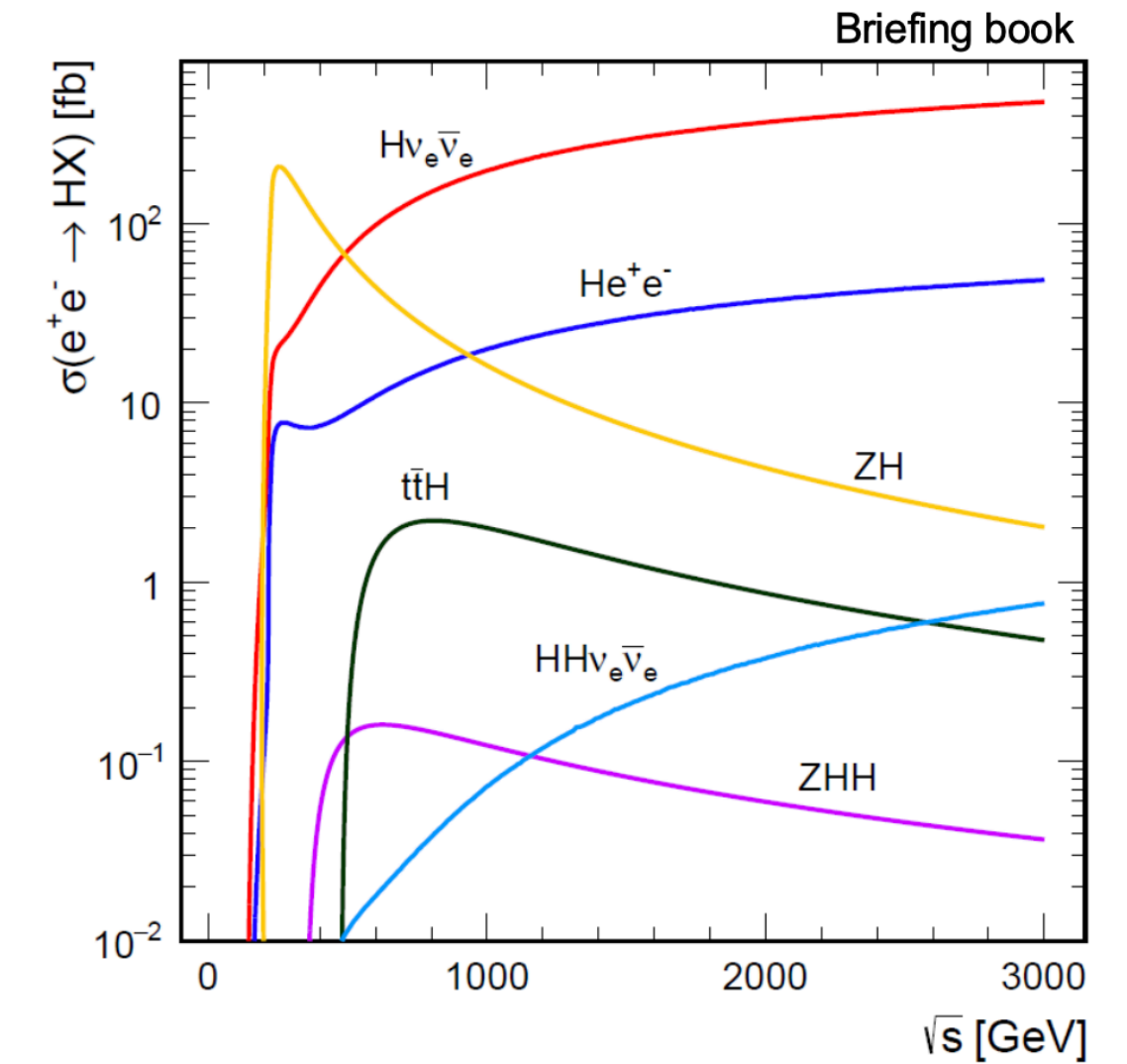
## combination HL-LHC



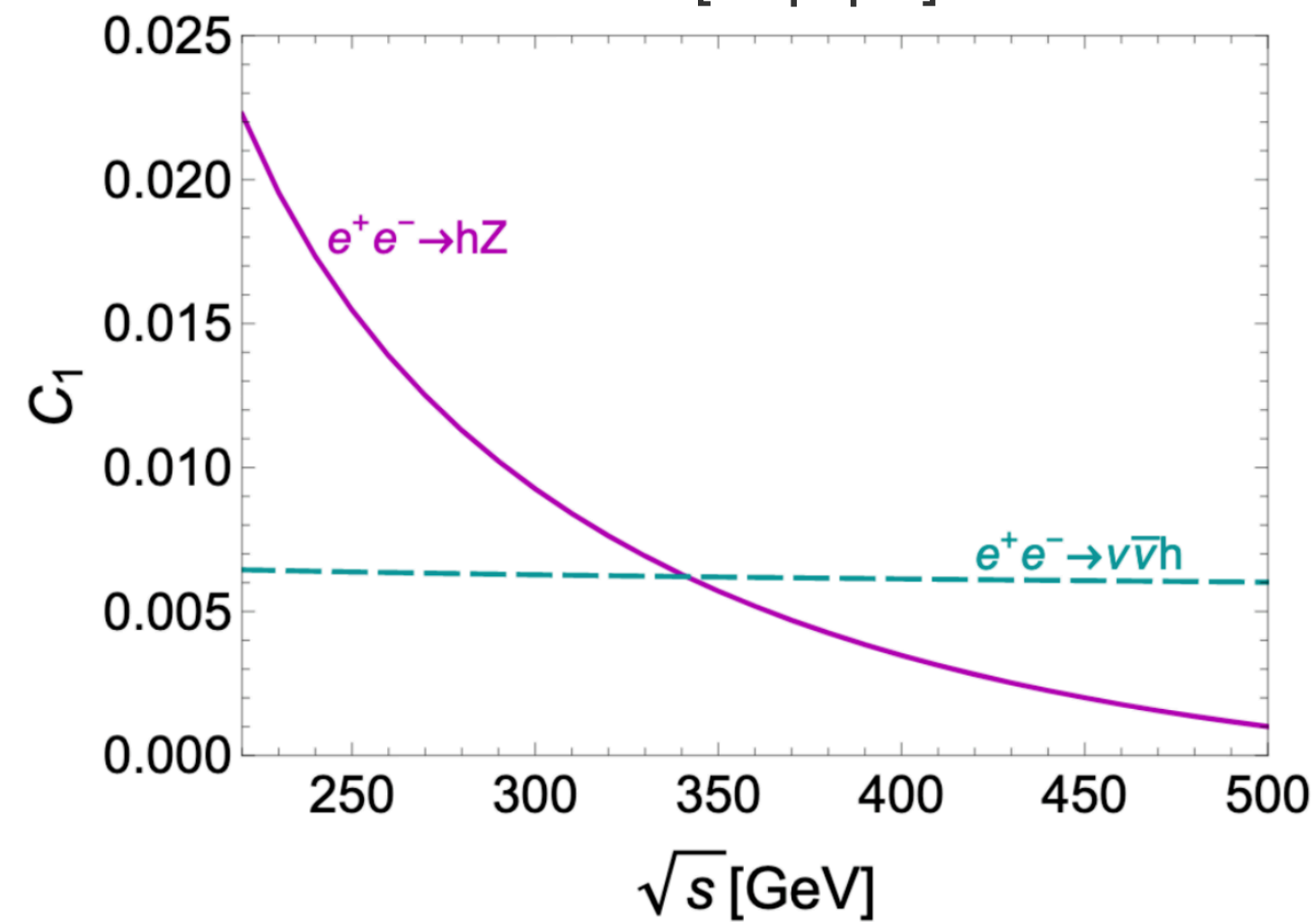
# Self-coupling at circular $e^+e^-$ colliders



- At low energy  $\sqrt{s} < 500$  GeV the self-coupling is measured via **single Higgs production (FCC-ee)**
- Precise ZH cross-section measurement at various energies can resolve  $\lambda_3, \lambda_{VVHH}$
- **FCC-ee gives the best indirect measurement:**



[1312.3322 \[hep-ph\]](https://arxiv.org/abs/1312.3322)

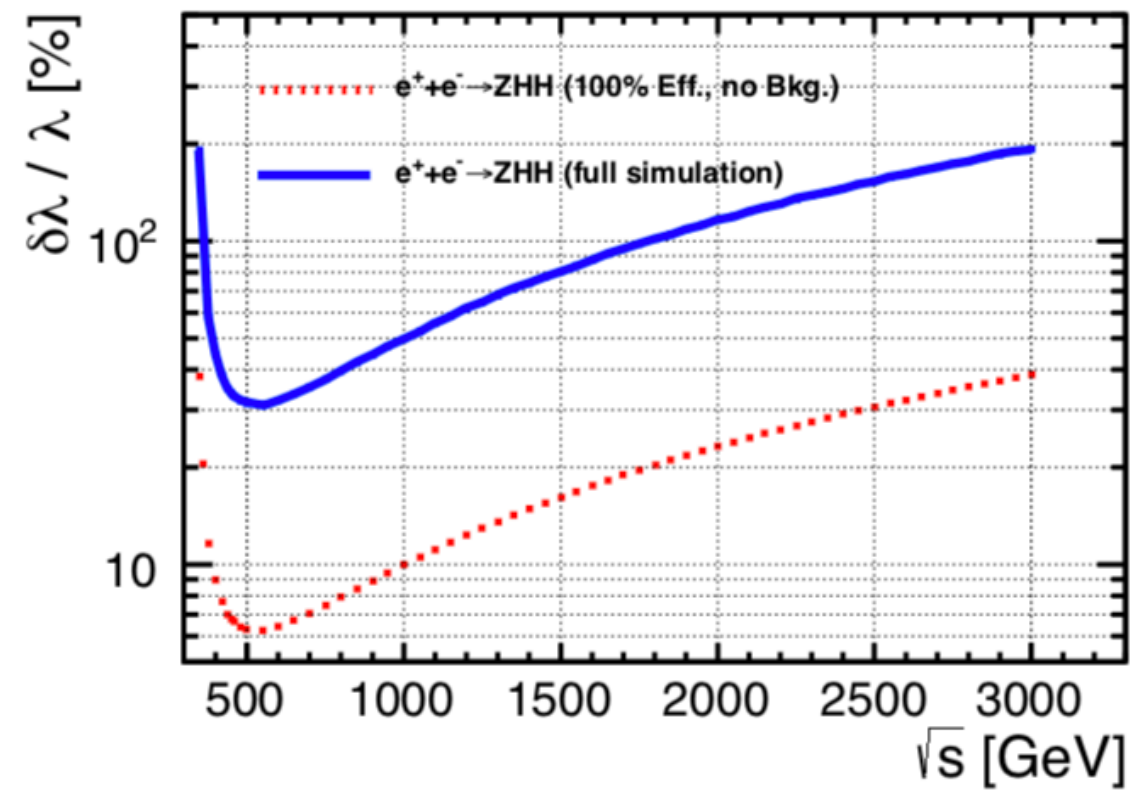
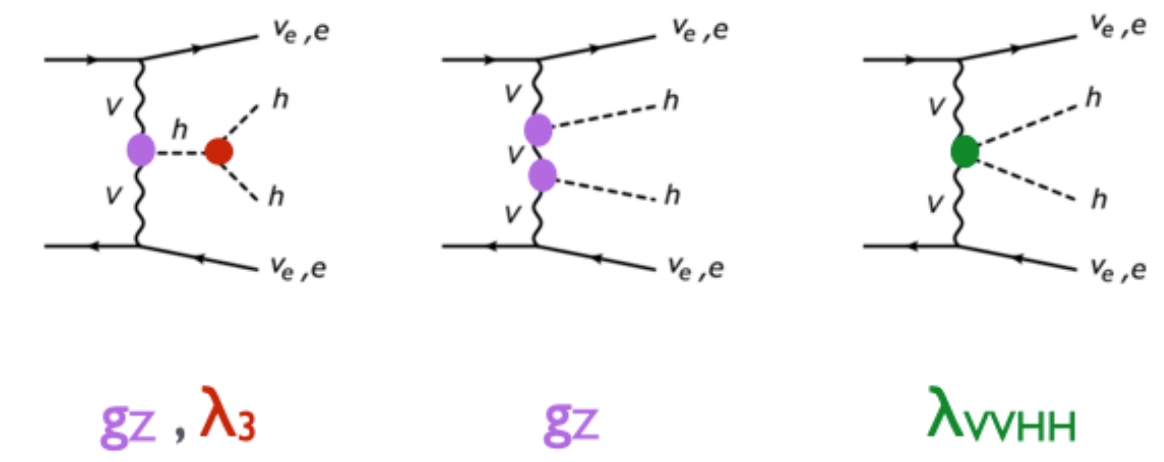


- $\delta_{K\lambda} = 33\%$  (2 IPs)
- $\delta_{K\lambda} = 24\%$  (4 IPs)

Collider	HL-LHC	ILC <sub>250</sub>	CLIC <sub>380</sub>	CEPC <sub>240</sub>	FCC-ee <sub>240→365</sub>
Lumi (ab <sup>-1</sup> )	3	2	1	5.6	5 + 0.2 + 1.5
Years	10	11.5	8	7	3 + 1 + 4
$g_{HHH}$ (%)	50.	- / 49.	- / 50.	- / 50.	44./33. <b>2IP</b> 27./24. <b>4IP</b>

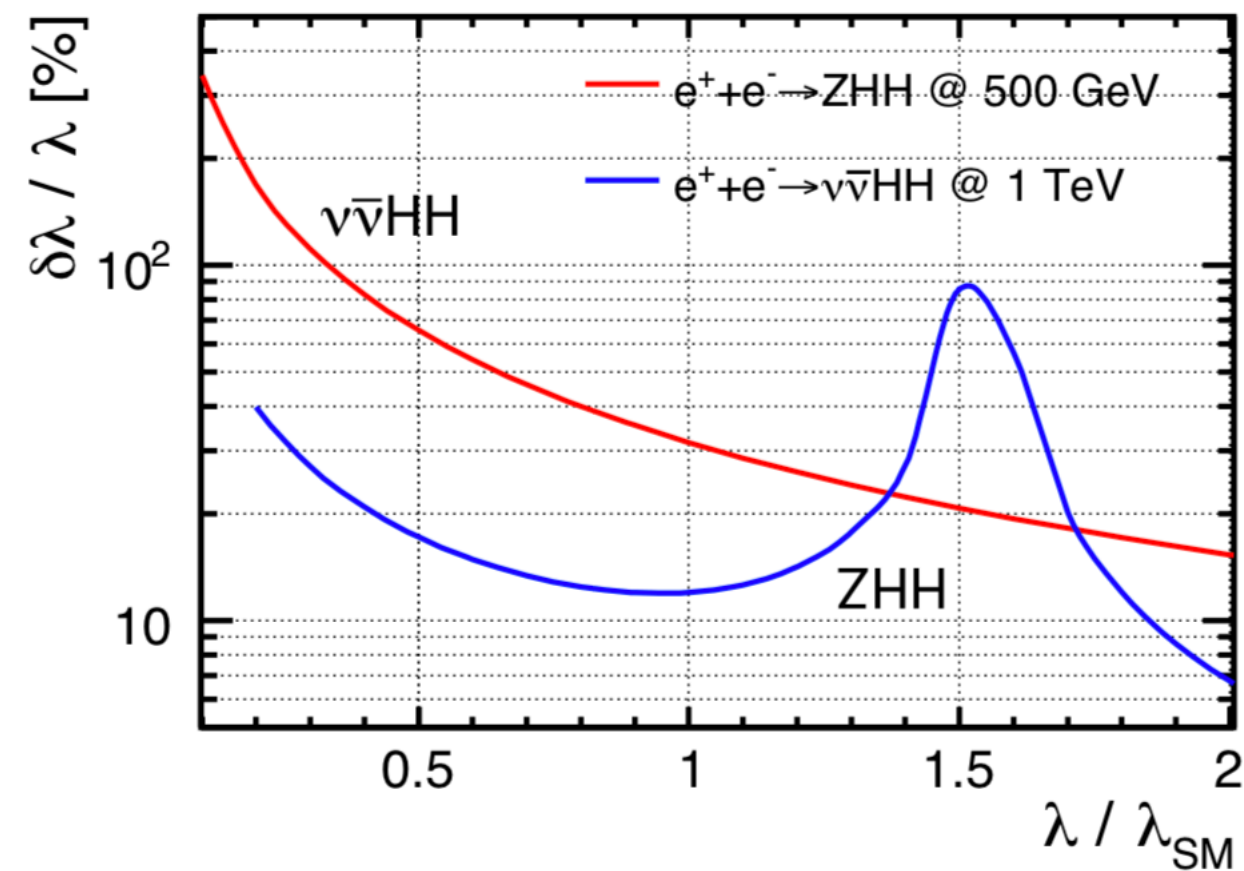
global fit, with/without HL-LHC input

# Self-coupling at linear $e^+e^-$ colliders

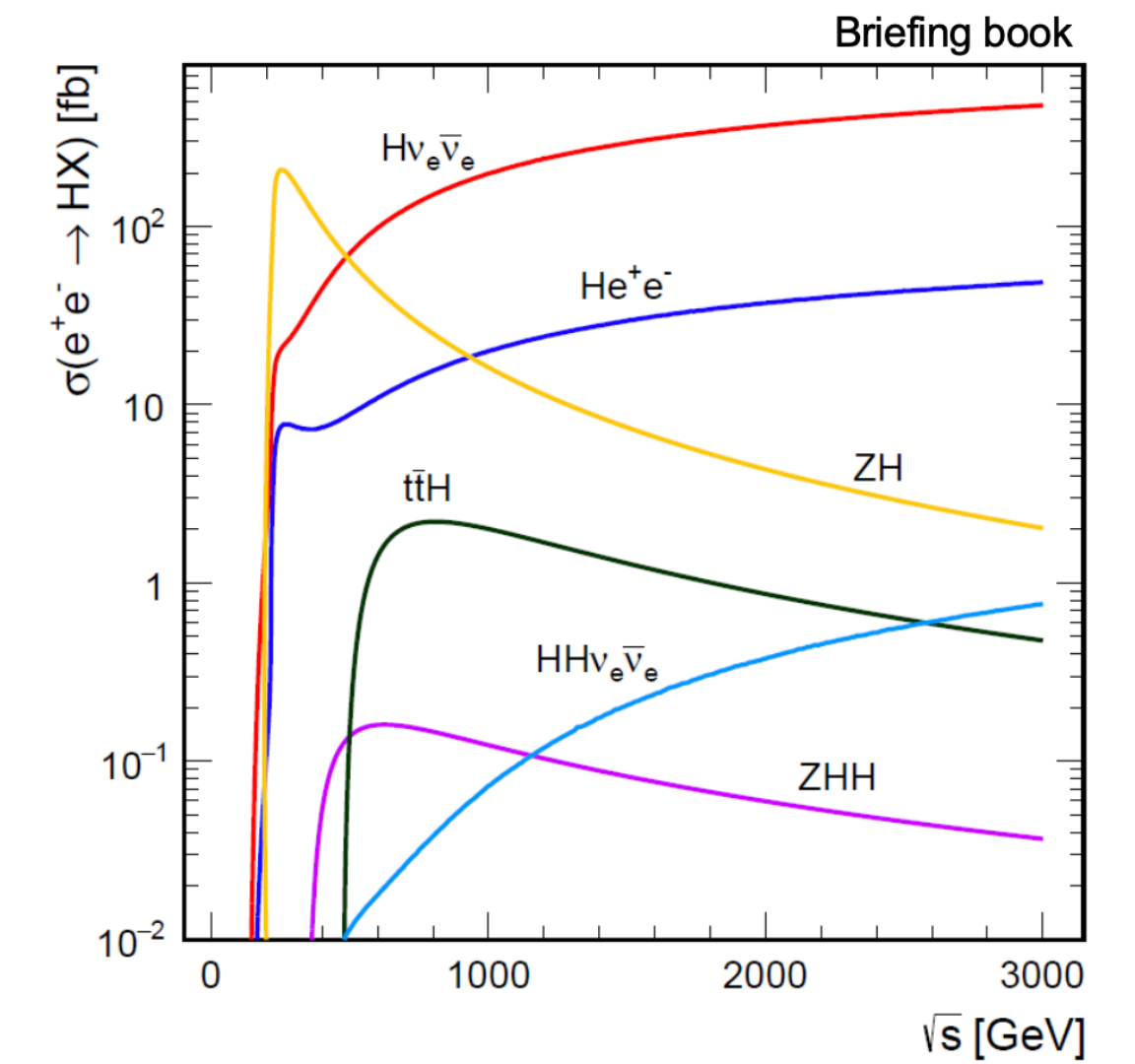


ILC - 1 TeV

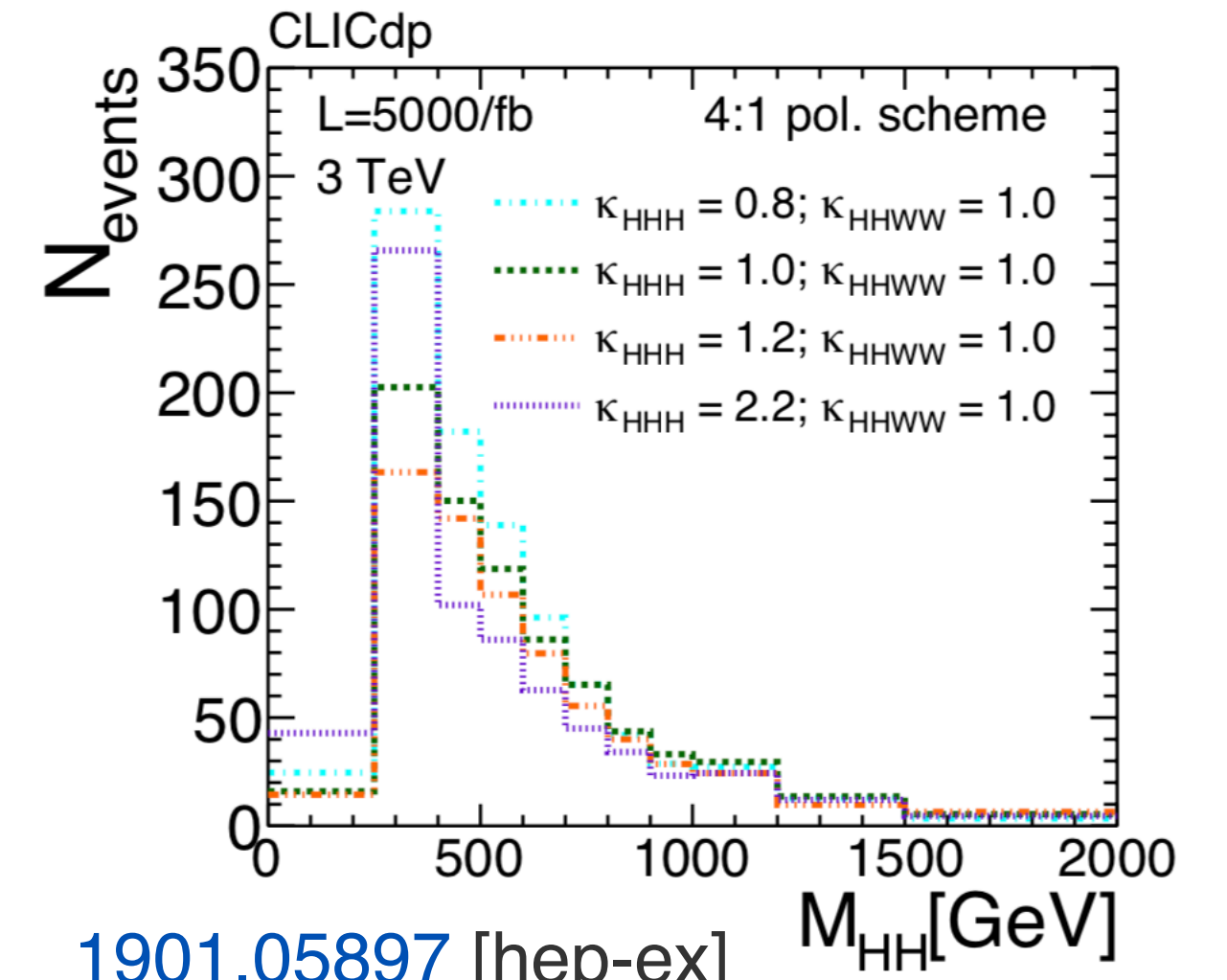
[1910.00012](#) [hep-ph]



- At high energies  $\sqrt{s} > 500$  GeV self-coupling is measured via double Higgs production (**ZHH** and  **$\nu\nu\text{HH}$** )
- Cross-section at various energies depends on  $\lambda_3$
- Measured in  $l\bar{l}b\bar{b}b\bar{b}$  (**ZHH**) and  $\nu\nu b\bar{b}b\bar{b}$ ,  $\nu\nu b\bar{b}W\bar{W}$  ( **$\nu\nu\text{HH}$** )



CLIC - 3 TeV

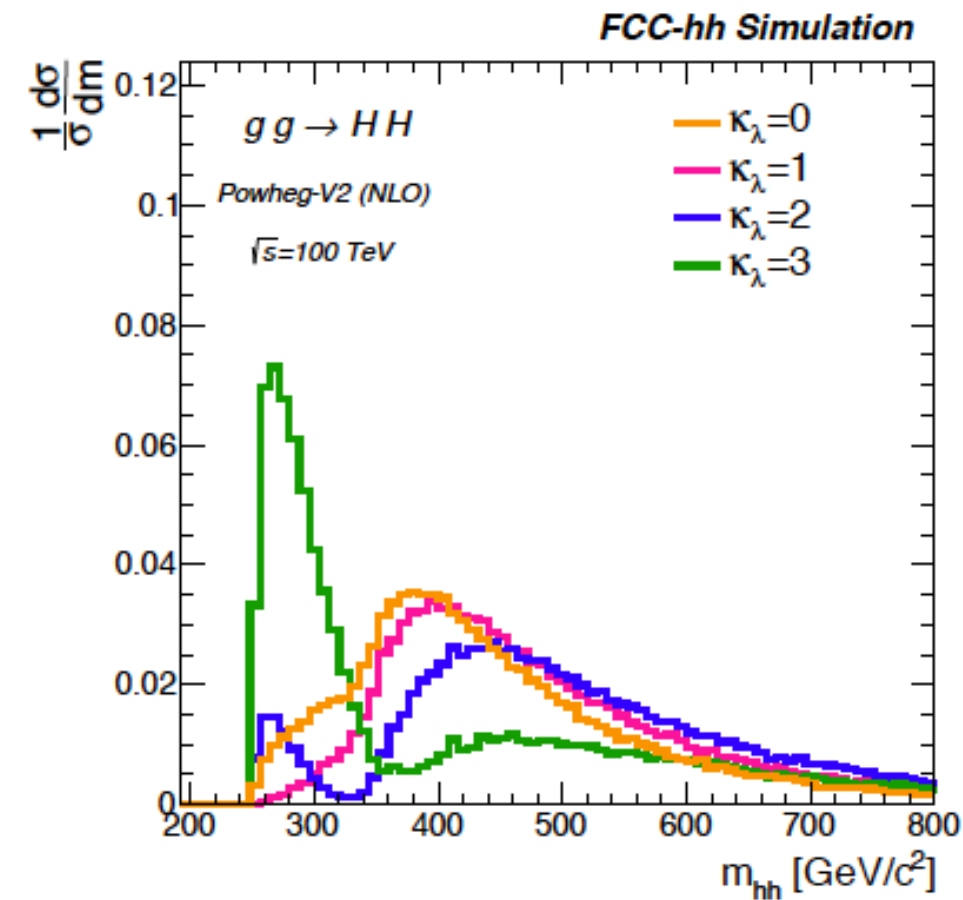
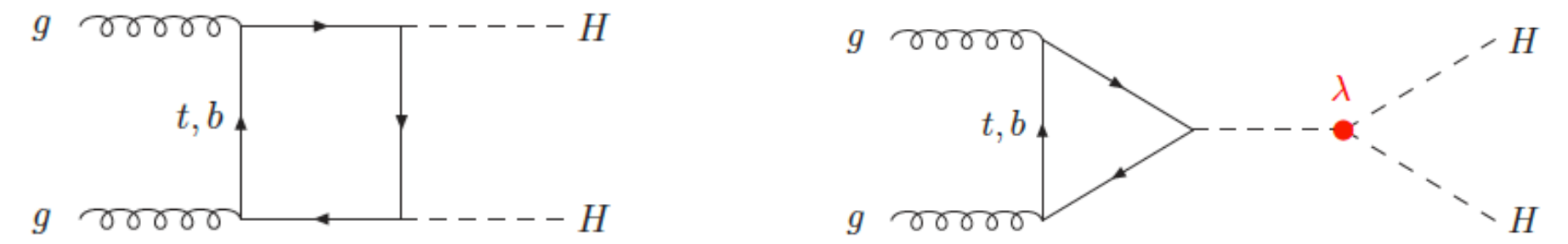


[1901.05897](#) [hep-ex]

- ILC and CLIC best direct measurement at  $e^+e^-$ :
  - $\delta\kappa_\lambda = 10\%$  (ILC<sub>1000</sub>)
  - $\delta\kappa_\lambda = 9\%$  (CLIC<sub>3000</sub>)

Collider	ILC <sub>500</sub>	ILC <sub>1000</sub>	CLIC
$g_{\text{HHH}}$ (%)	27.	10.	9.

# Self-coupling at the FCC-hh



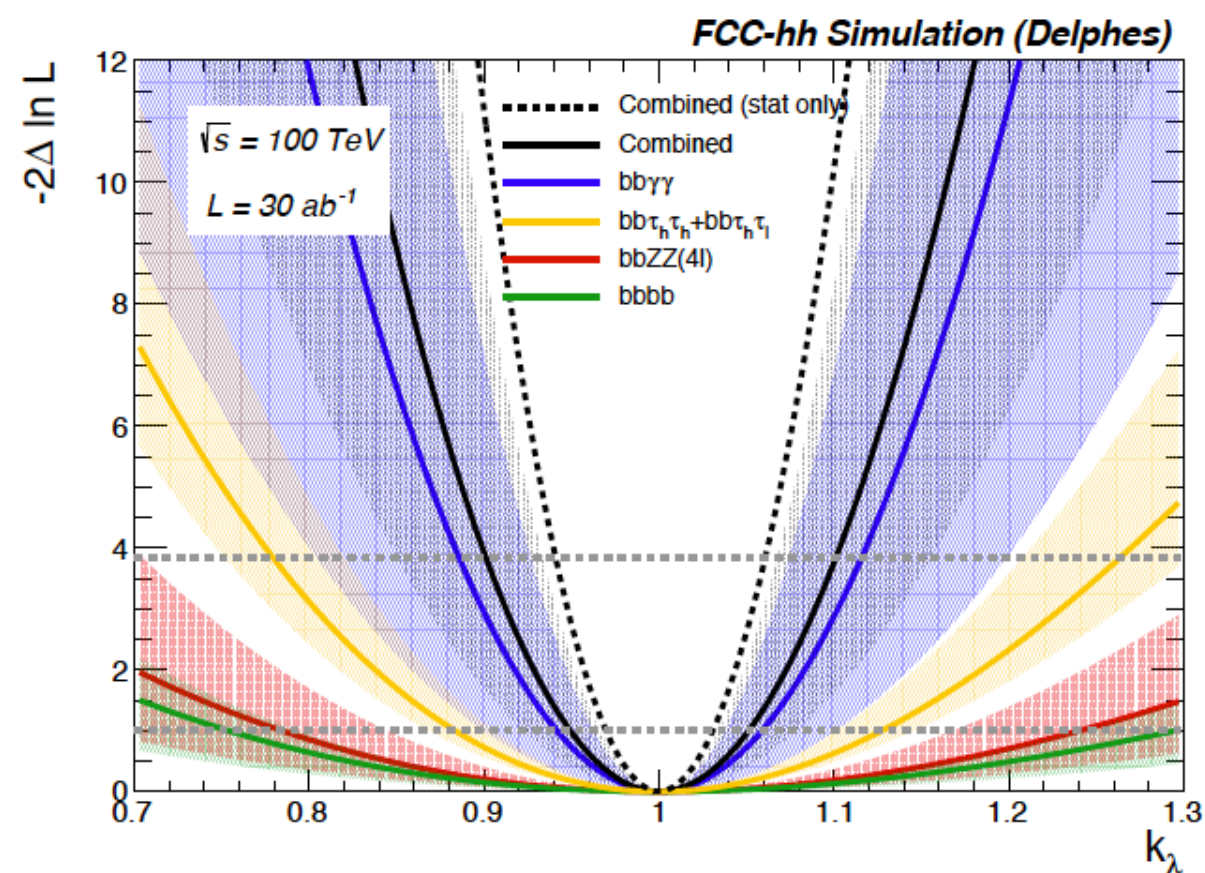
- At 100 TeV pp, Higgs pair production gives best precision on  $\lambda_3$

- Measured in:

parameterisation	scenario I	scenario II	scenario III
b-jet ID eff.	82-65%	80-63%	78-60%
b-jet c mistag	15-3%	15-3%	15-3%
b-jet l mistag	1-0.1%	1-0.1%	1-0.1%
$\tau$ -jet ID eff	80-70%	78-67%	75-65%
$\tau$ -jet mistag (jet)	2-1%	2-1%	2-1%
$\tau$ -jet mistag (ele)	0.1-0.04%	0.1-0.04%	0.1-0.04%
$\gamma$ ID eff.	90	90	90
jet $\rightarrow \gamma$ eff.	0.1	0.2	0.4
$m_{\gamma\gamma}$ resolution [GeV]	1.2	1.8	2.9
$m_{bb}$ resolution [GeV]	10	15	20

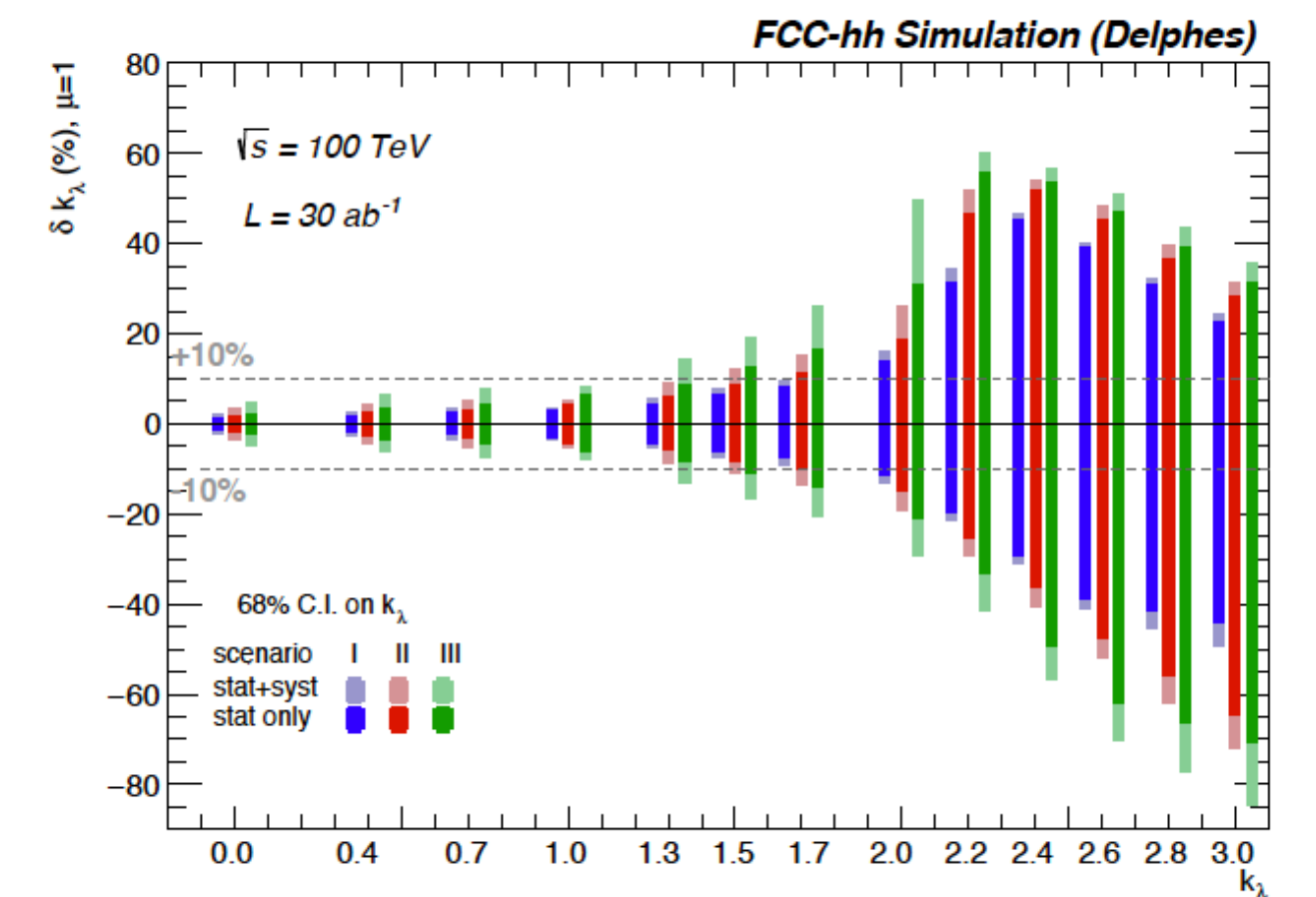
[2004.03505 \[hep-ph\]](#)

- $bb\gamma\gamma$  (golden channel),  $bb\tau\tau$ ,  $bbbb$ ,  $bbZZ(4l)$

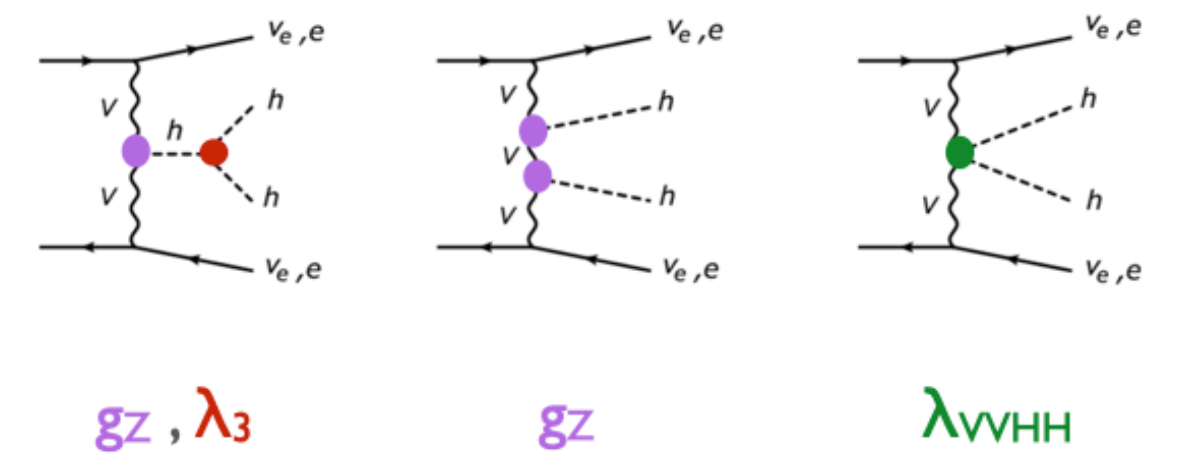


- Combined precision:

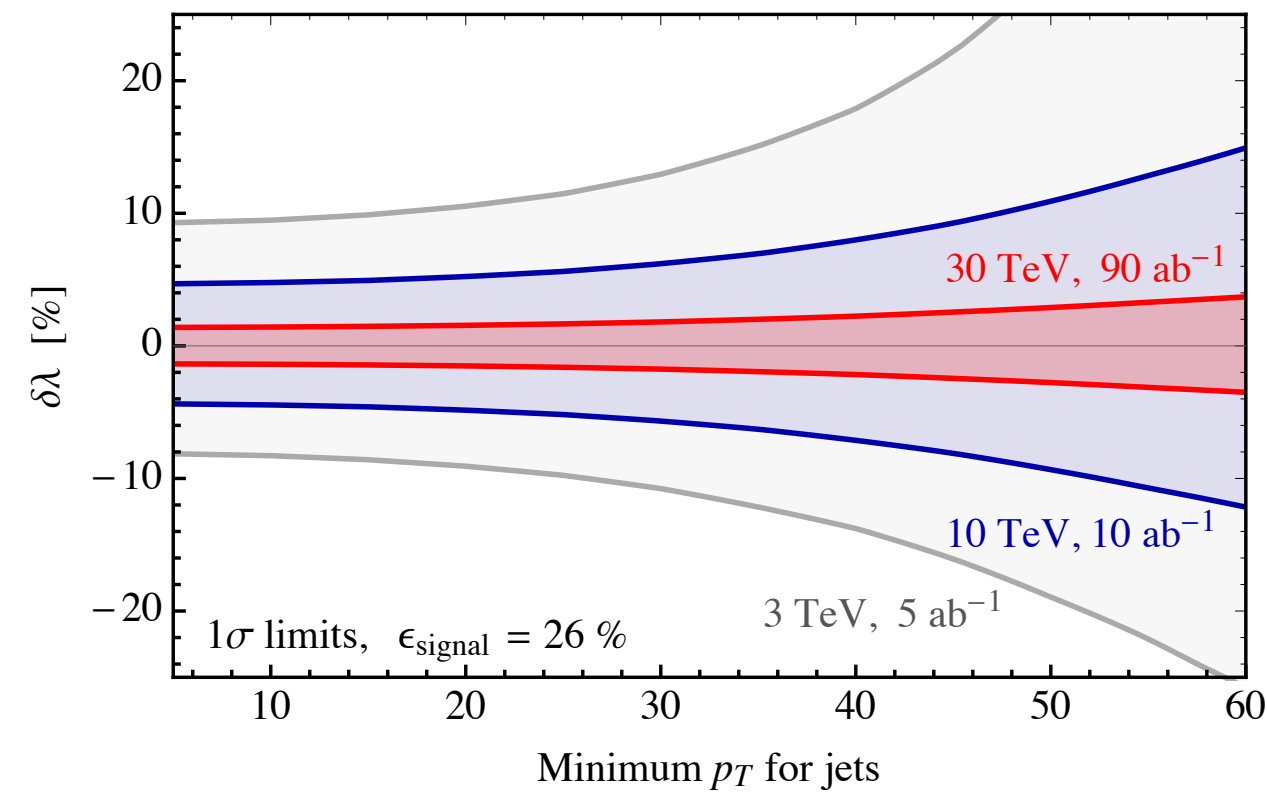
- 3.5-7% for SM (3% stat. only)
- 10-20% for  $\lambda_3 = 1.5 * \lambda_3^{\text{SM}}$



# Self-coupling at the Muon Collider

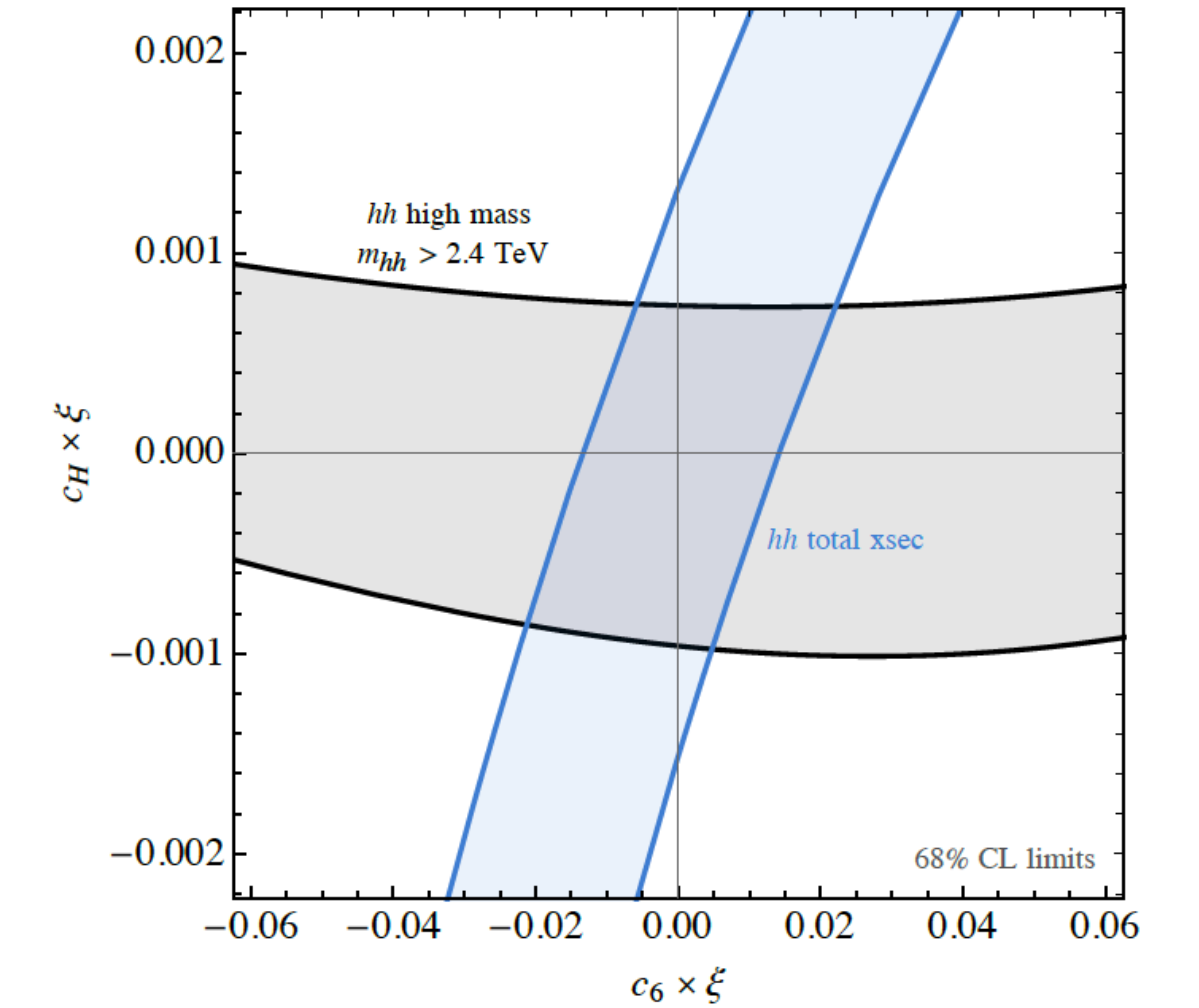


Buttazzo, Franceschini, Wulzer

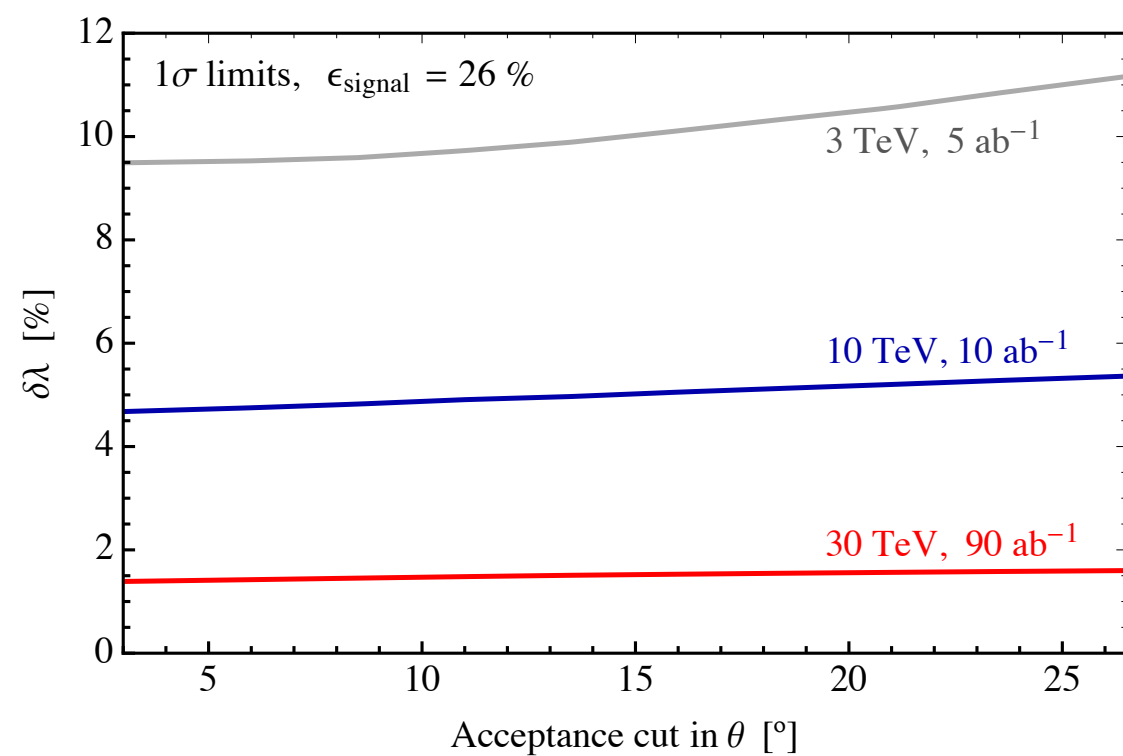


- At 10-30 TeV muon collider, the VBF pair production dominates ( $\sim$  CLIC)

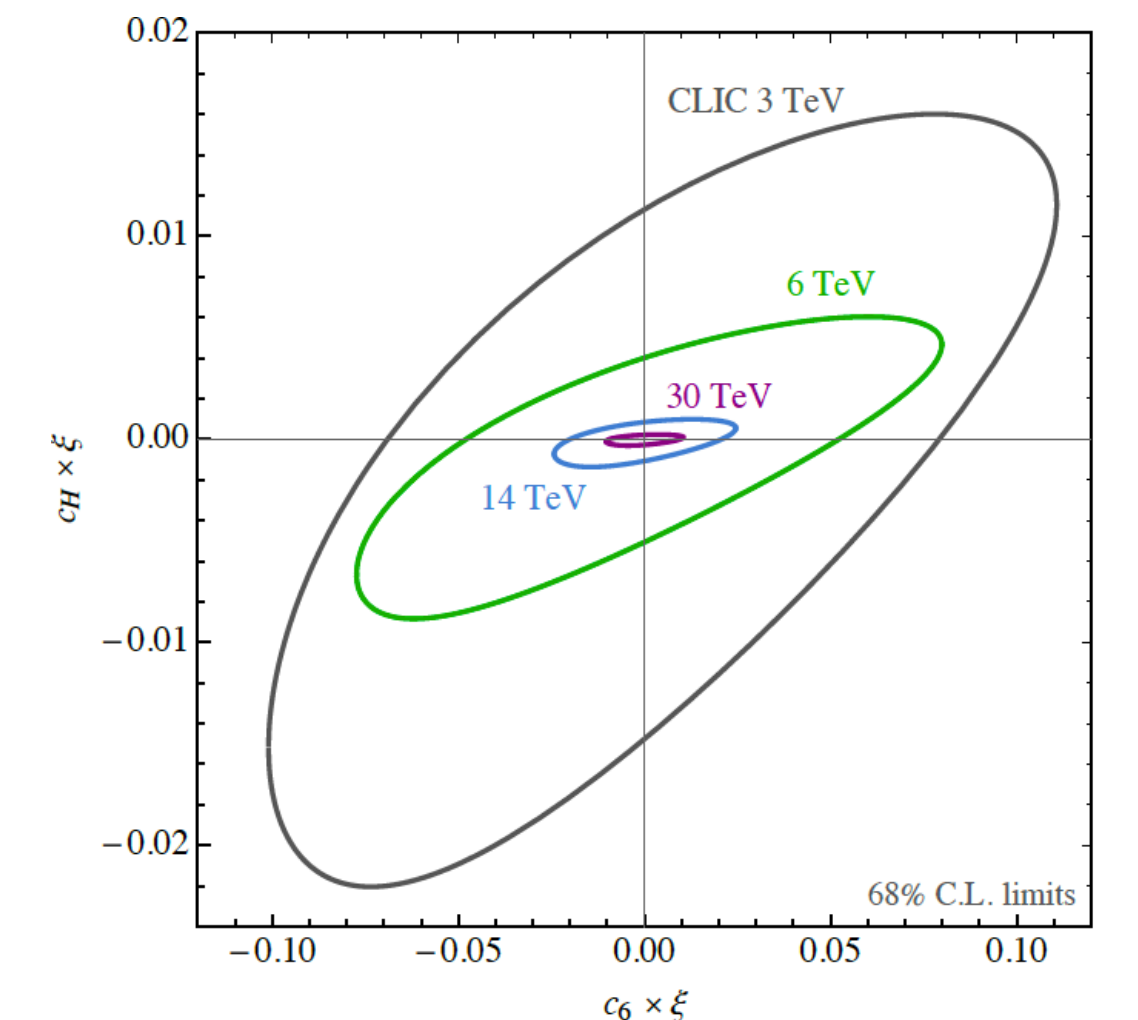
- **vvbbbb** final state (4jets + ME)



- Muon collider could potentially provide the best precision  $\sim 2\%$  (stat only) ?



- More studies needed, parton level only for now



# Open questions:

- For simplicity, most of the **benchmarking on future colliders capabilities** is made assuming  $\lambda_3^{\text{SM}}$  (allows for easy comparison), or varying  $\lambda_3$  alone.
  - desirable to investigate use of global — (SM)EFT fit from exp. community, or this exercise can be left to theorists?
  - how about indirect measurements? (e.g single Higgs production or W/Z mass)
  - how approach global fits as a community (pheno/exp)
- Various proposed future colliders present different **levels of maturity**
  - How do we deal with detector effects (Pile-up , Beam Induced Background) ?
    - Can be indirectly parameterised if full-sim is not available (very different environment) ?
  - Treatment of dominant systematic uncertainties (theory vs. exp)
  - How do we estimate **uncertainties** (performance/systematics) on future colliders?

# Open questions:

- What is the interplay between auxiliary measurements at various colliders to allow for best self-coupling precision? e.g.
  - at proton collider precise measurement of  $\lambda_3$  requires  $y_t$  (itself requiring  $g_{ttZ}$ )?
  - at lepton (and proton) colliders need both measurements of  $\lambda_{\nu\nu HH}$  and  $\lambda_3$
- How about  $\lambda_{\nu\nu HH}$  and  $\lambda_4$ ?
  - missing exp. efforts so far (see backup for pheno. work)



# Open questions

- A **strongly first-order EWPT** requires new physics coupling to the Higgs.
  - What does this imply generically for **di-Higgs rates**?
  - Does it imply a **minimum deviation** pattern in Higgs couplings?
  - How does the reach of **Higgs coupling measurements** compare to other **direct and indirect probes**?
- What can we learn about the **history of the universe** from **collider measurements** ?

**BACKUP**

# The Standard Model Higgs Potential

11

$$\begin{aligned} V &= -\mu^2 H^\dagger H + \lambda (H^\dagger H)^2 \\ &\rightarrow -\frac{\lambda}{4} v^4 + \frac{1}{2} (2\lambda v^2) h^2 + \lambda v h^3 + \frac{\lambda}{4} h^4 \\ &= V_0 + \frac{1}{2} m_h^2 h^2 + \lambda_3 v h^3 + \frac{\lambda_4}{4} h^4 \end{aligned}$$

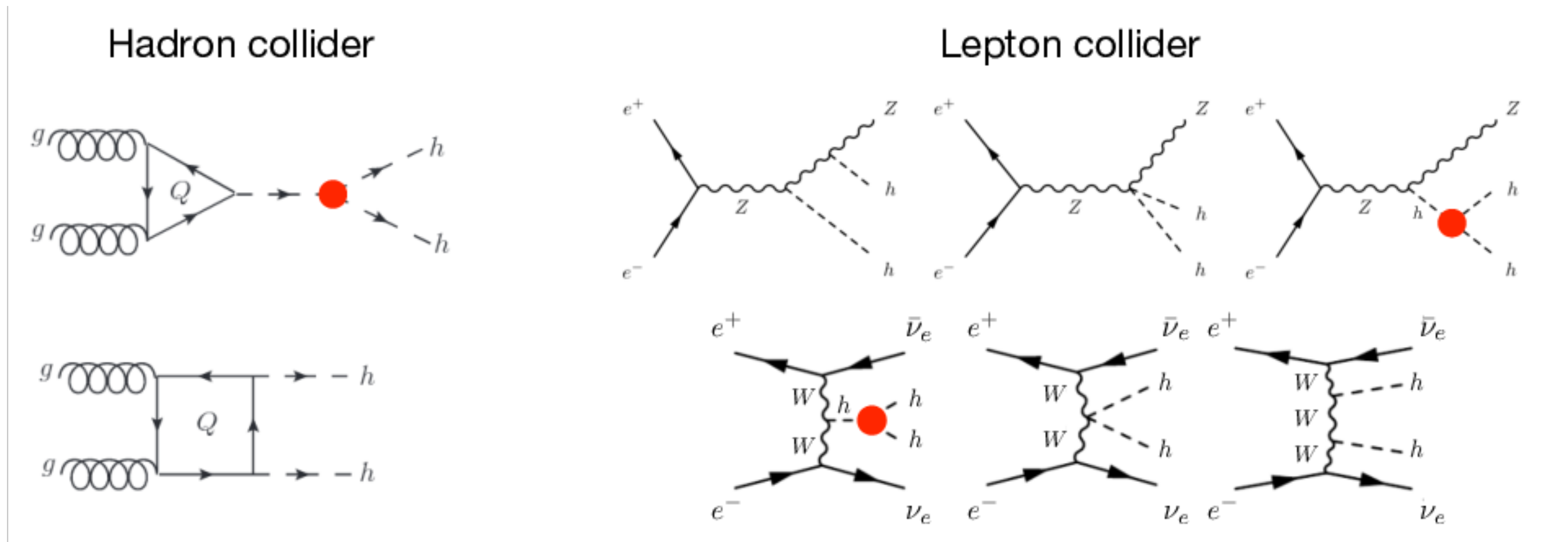
- Fix the two parameters  $(\mu^2, \lambda)$  with two observables  $(v, m_h)$ .

- Predictions:

$$\lambda_3 = \lambda_4 = \frac{m_h^2}{2v^2}$$

# Testing the SM Higgs Potential

- Measure di-Higgs (tri-Higgs?) production to probe  $\lambda_3$  ( $\lambda_4$ ): [talk by M. Selvaggi]



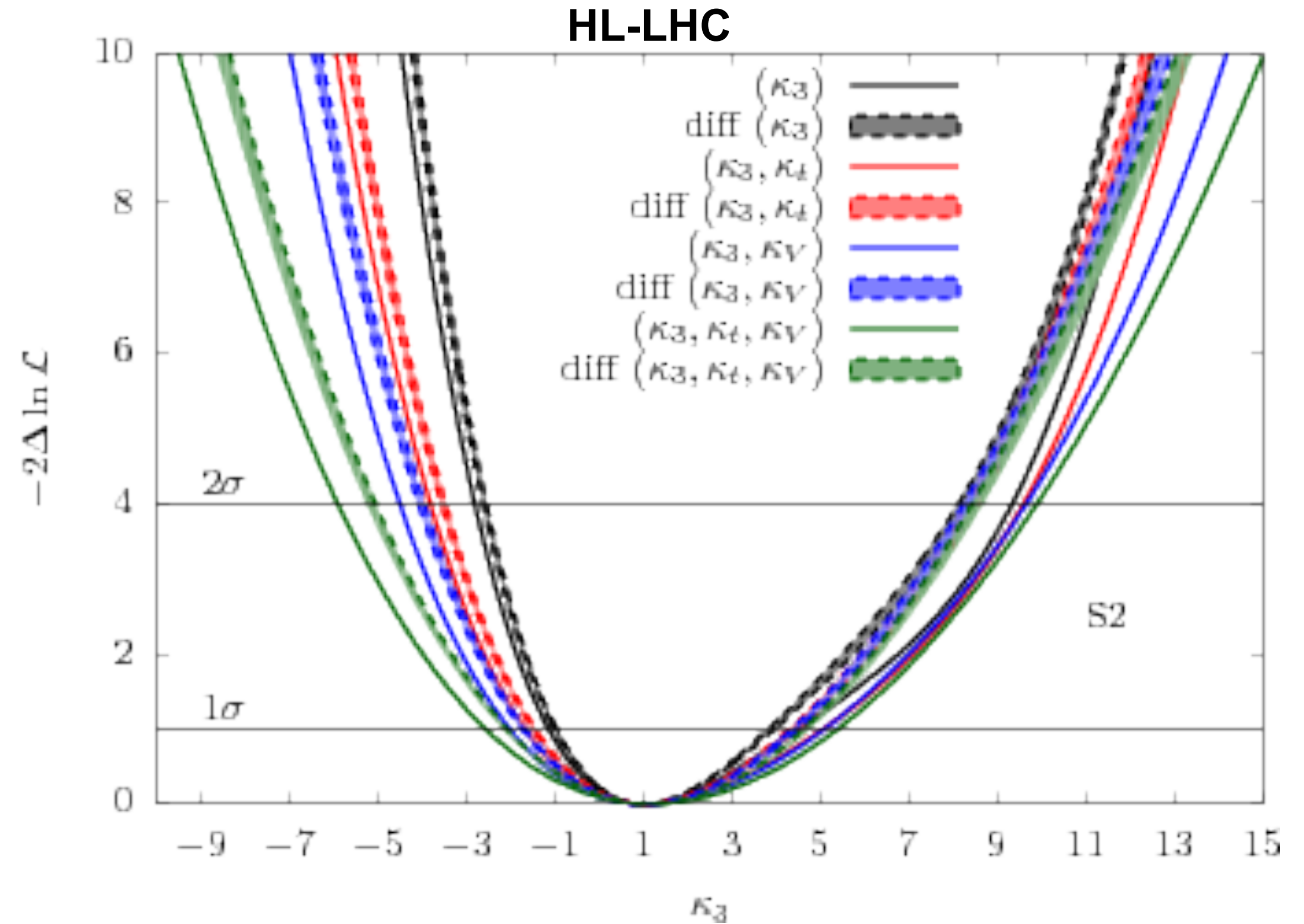
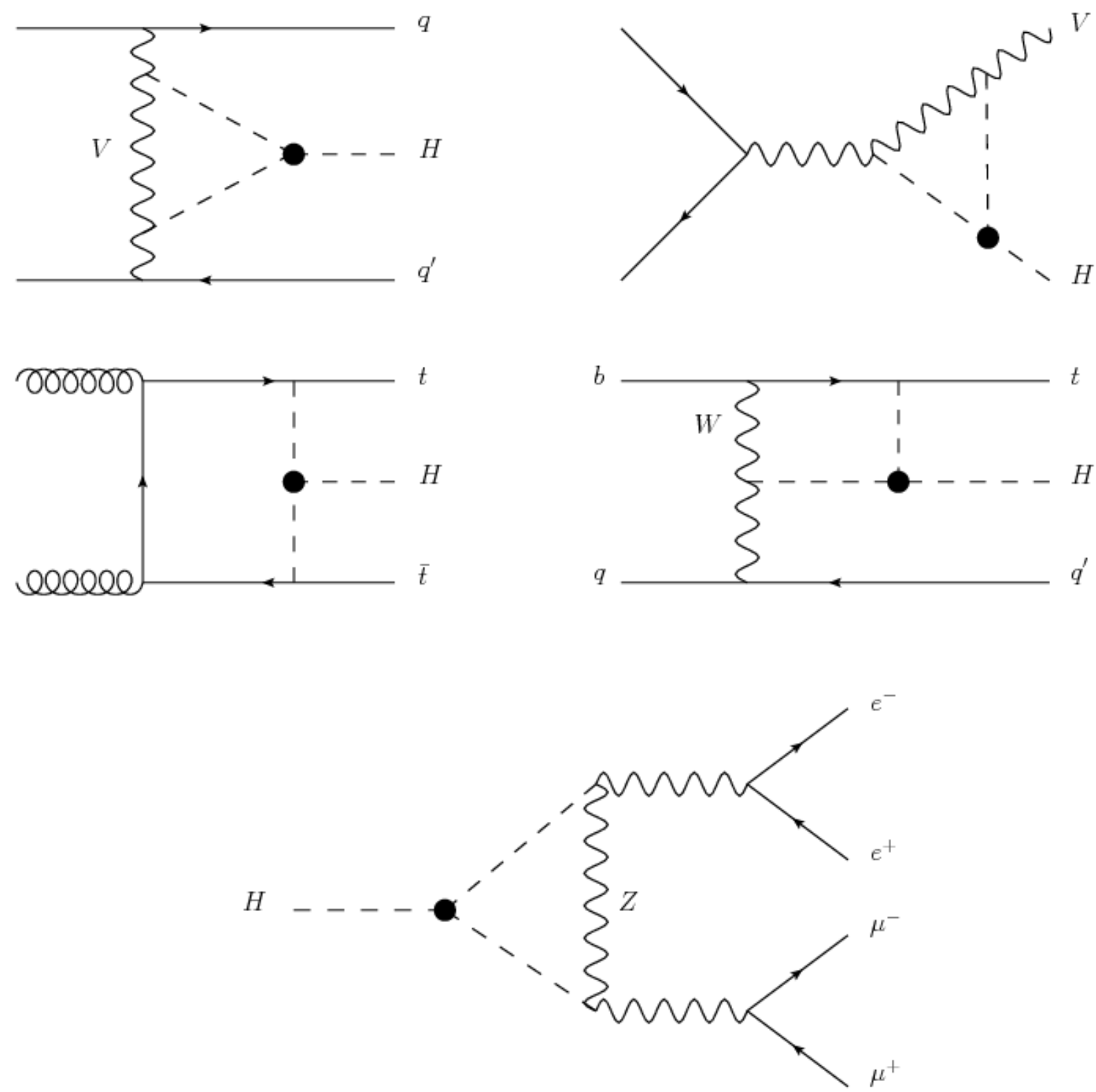
[de Blas et al. 1905.03764]

- Must be part of a global fit to Higgs couplings, requires high SM precision!

[e.g. Di Vita, Grojean, Riemann, Vantalon 1704.01953]

# Testing the SM Higgs Potential

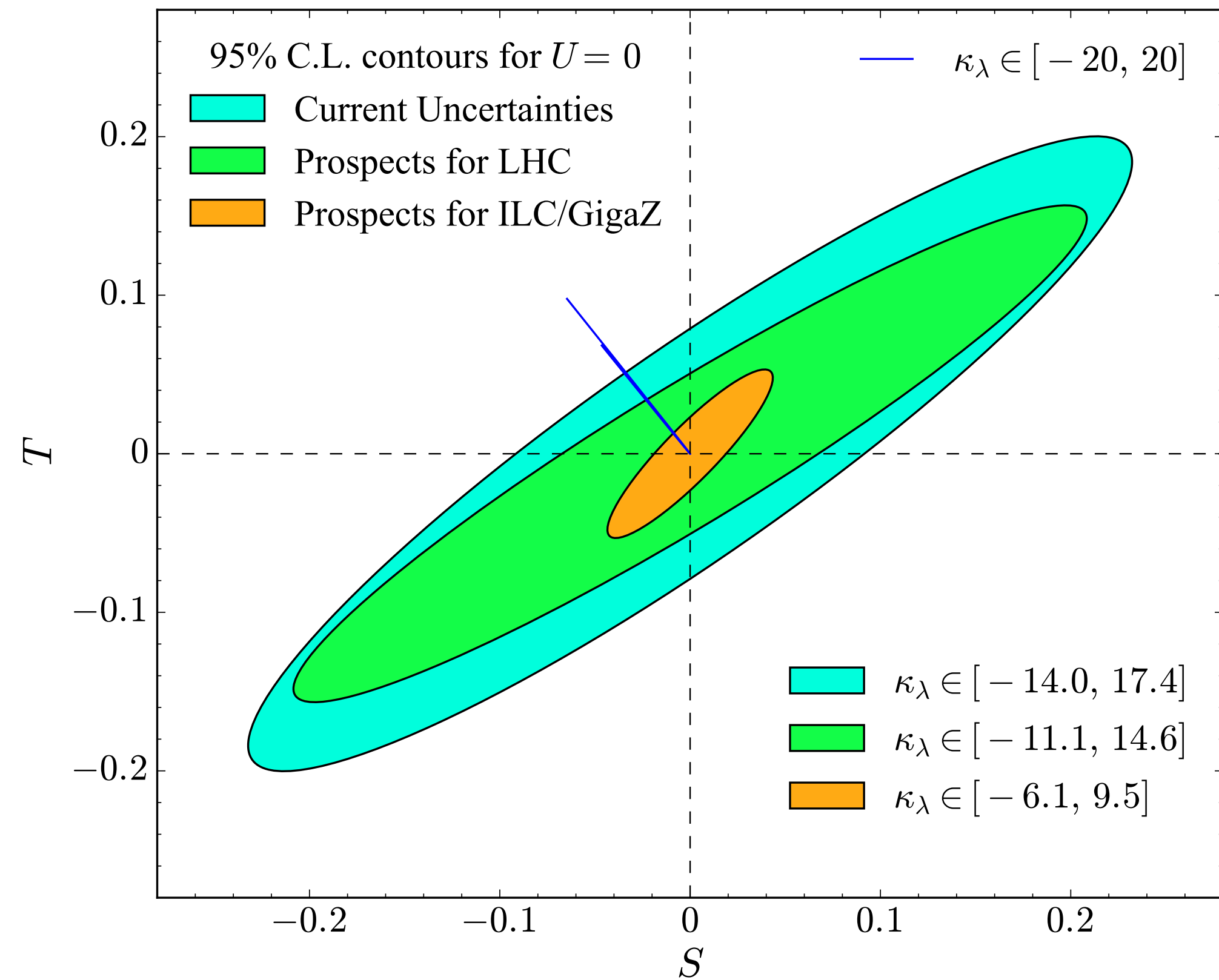
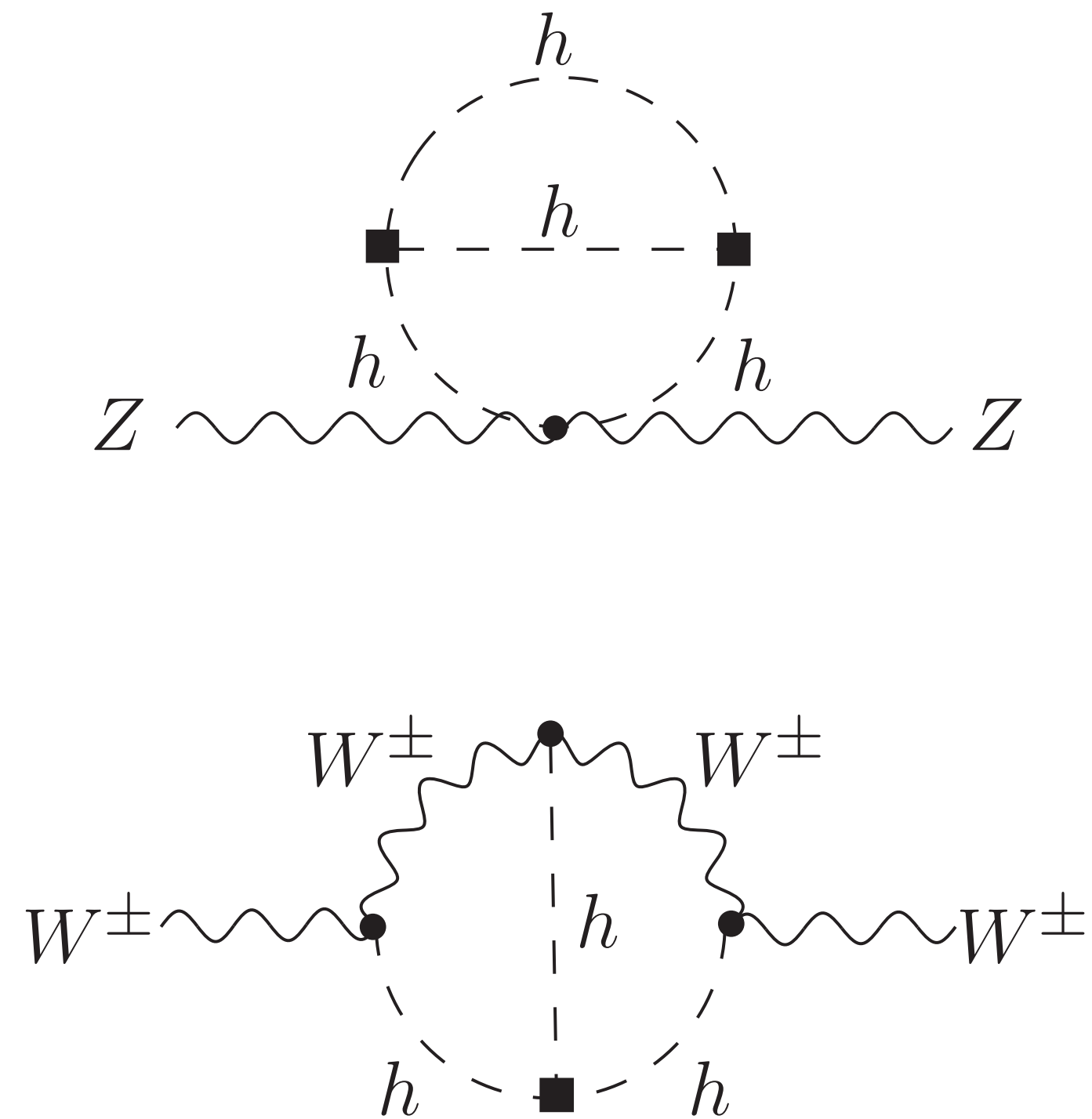
- Look for NLO effects of  $\lambda_3$  in single Higgs production:



[McCullough 1312.3322; Maltoni, Pagani, Shivaji, Zhao 1709.08649]

# Testing the SM Higgs Potential

- Look for effects of  $\lambda_3$  in precision electroweak observables:



# Higgs Potential Beyond the SM

- Heavy new physics can yield effective operators that modify the potential.

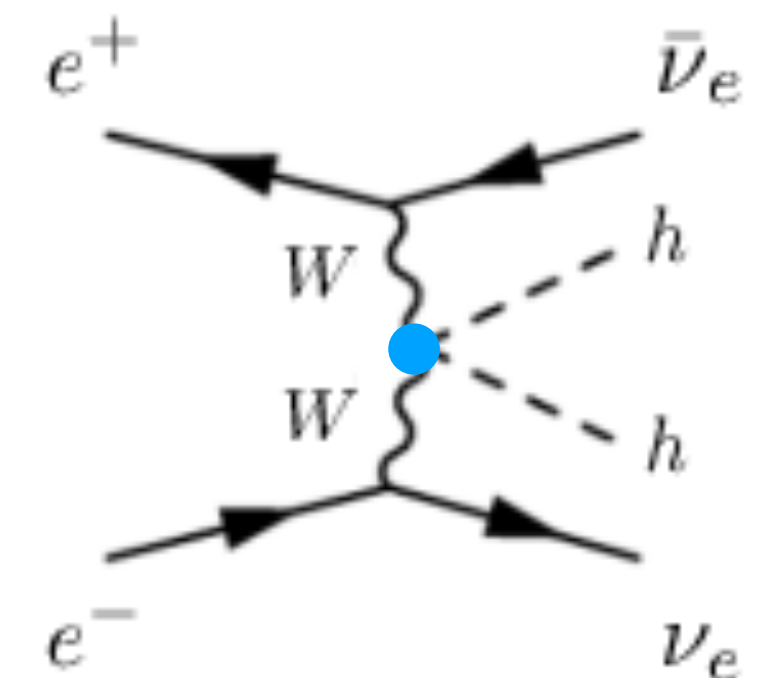
[e.g. Giudice, Grojean, Pomarol, Rattazzi hep-ph/0703164; Brivio, Trott 1706.08945]

$$\mathcal{L} \supset \frac{c_H}{2\Lambda^2} [\partial_\mu (H^\dagger H)]^2 - \frac{c_6 \lambda}{\Lambda^2} (H^\dagger H)^3$$

$$\frac{\lambda_3}{\lambda_3^{SM}} = 1 + c_6 \frac{v^2}{\Lambda^2} - \frac{3}{2} c_H \frac{v^2}{\Lambda^2}$$

$$\frac{\lambda_4}{\lambda_4^{SM}} = 1 + \left( 6c_6 - \frac{25}{3} c_H \right) \frac{v^2}{\Lambda^2}$$

- Note:  $c_H$  also modifies hhVV couplings!

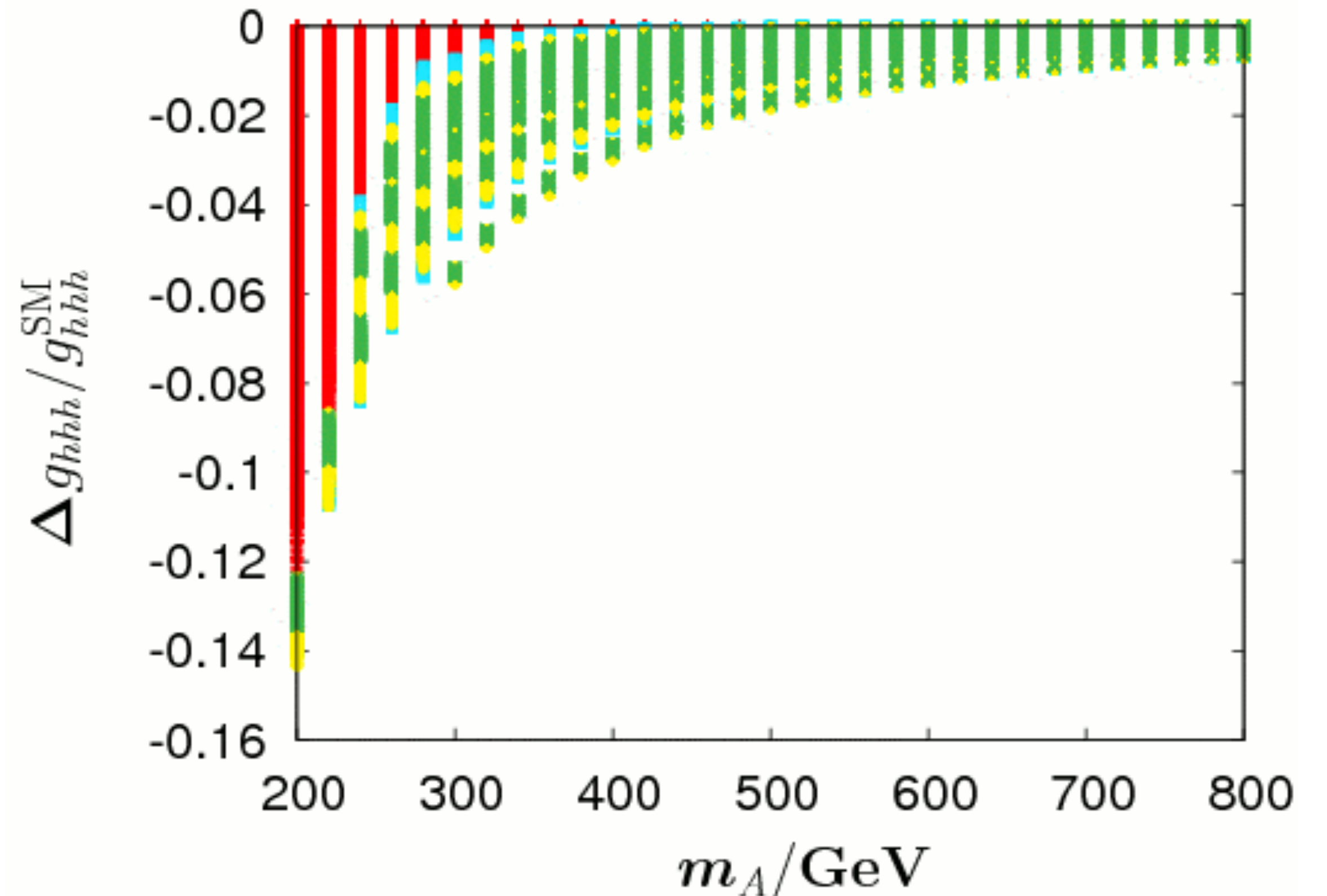


# Higgs Potential Beyond the SM

- Higgs mixing with other fields or new sources of EWSB can too.

*e.g.*

Model	$\max\left\{\frac{\lambda_3}{\lambda_3^{SM}} - 1\right\}$
Mixed-in Singlet	-18%
Composite Higgs	$\mathcal{O}(10\%)$
MSSM	-15%
NMSSM	-25

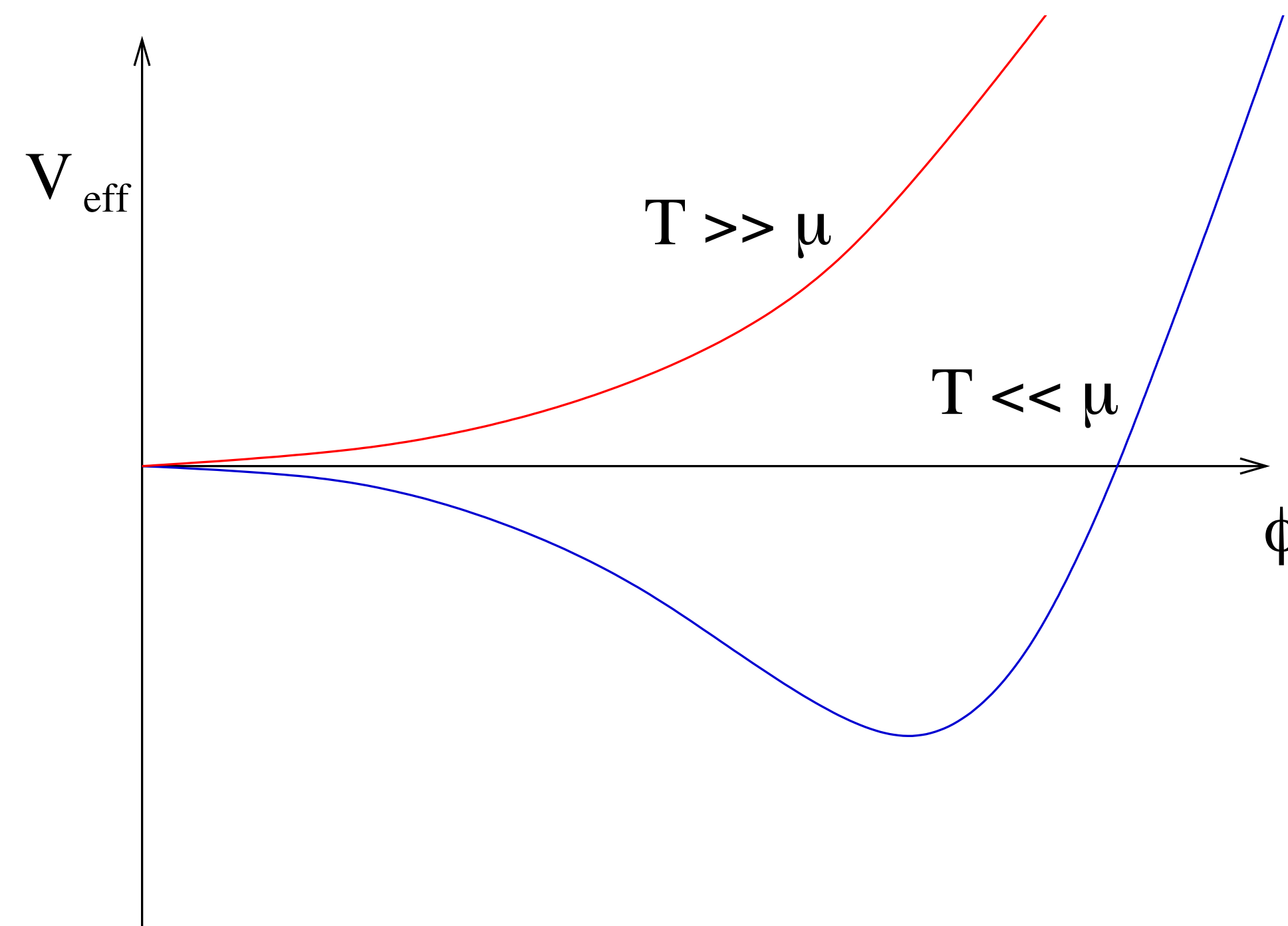




# Higgs Potential in the Early Universe

- Thermal effective potential:

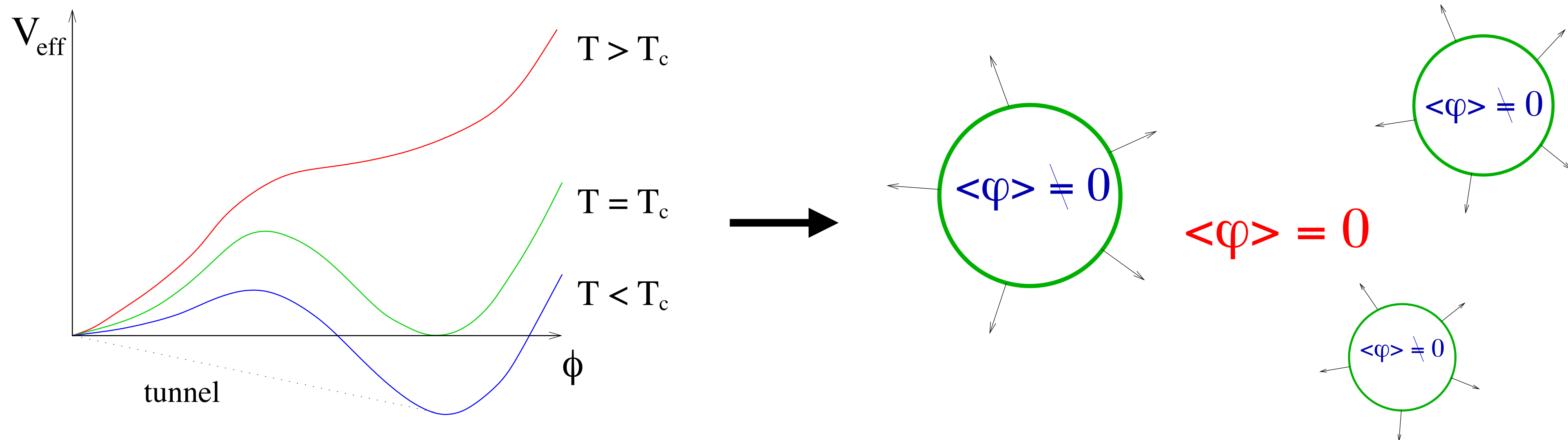
$$V(\phi, T) \simeq (\xi T^2 - \mu^2)\phi^2 - AT(\phi^2 + B)^{3/2} + \lambda\phi^4$$



→ electroweak phase transition (EWPT)

# Electroweak Phase Transition

- SM: the electroweak phase transition is a smooth crossover. [Kajantie *et al.* hep-lat/9510020]
- BSM: the EWPT can be strongly first order if new physics couples to the Higgs.



- A strong first-order EWPT can allow baryogenesis or make gravitational waves!

[e.g. Shaposhnikov NPB287, 575; Kamionkowski, Kosowsky, Turner astro-ph/9310044;

Cohen, Kaplan, Nelson hep-ph/9302210; Grojean, Servant hep-ph/0607107, LOIs by Carena *et al.*]

# A First Order EWPT

- Requires new physics that couples to the Higgs.
- SM-charged new physics  $\Rightarrow$  modified Higgs production and decay rates.  
e.g. gluon fusion rates rule out a SFO EWPT from light stops in the MSSM

[Cohen, DM, Pierce 1203.2924; Curtin, Jaiswal, Meade 1203.2932]

- SM-singlet new physics - main effect can be to alter the self-coupling  $\lambda_3$ .

[Noble, Perelstein 0711.3018;  
Profumo, Ramsey-Musolf,  
Wainwright, Winslow 1407.5342;  
Curtin, Meade, Yu 1409.0005]

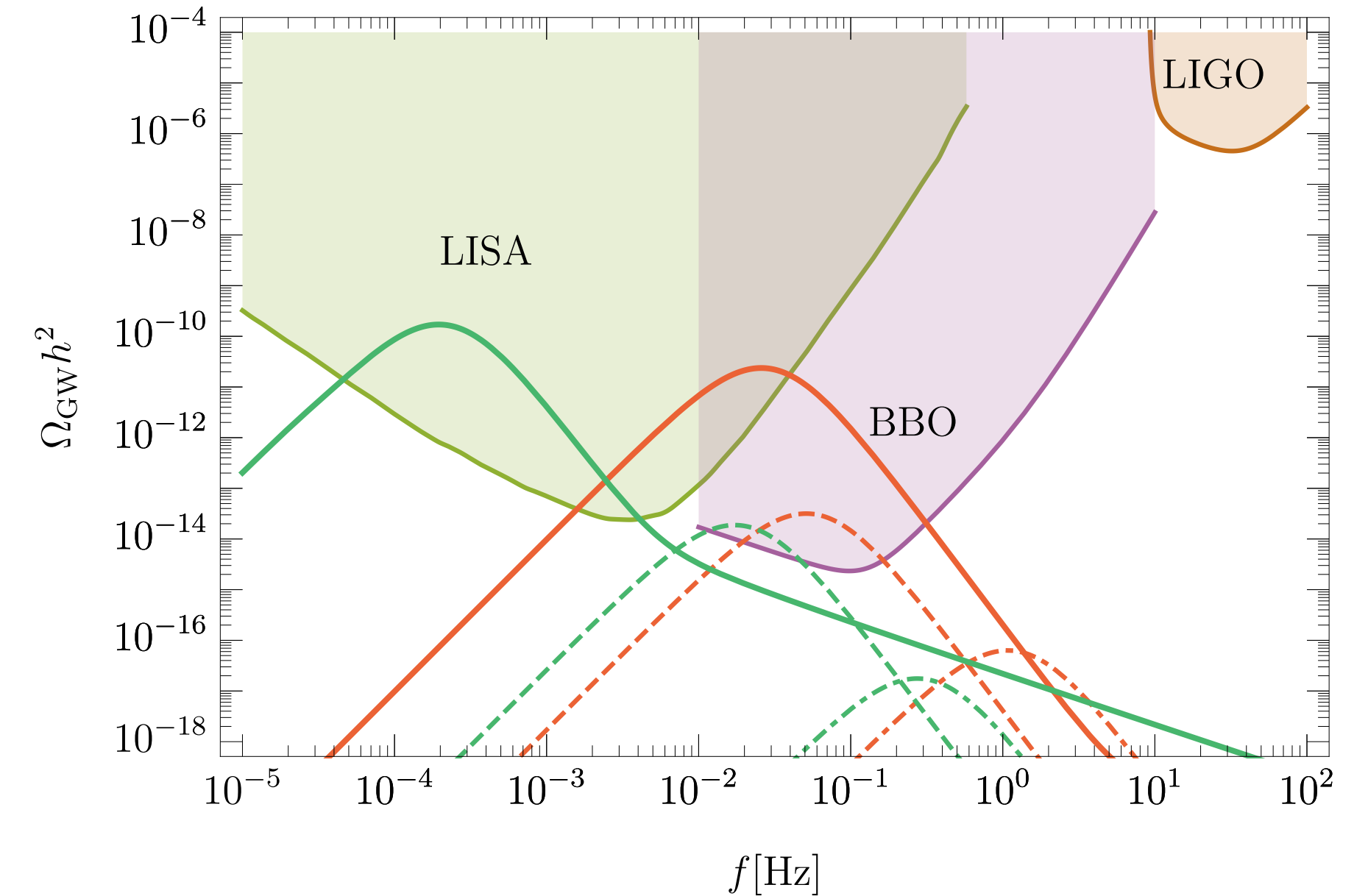
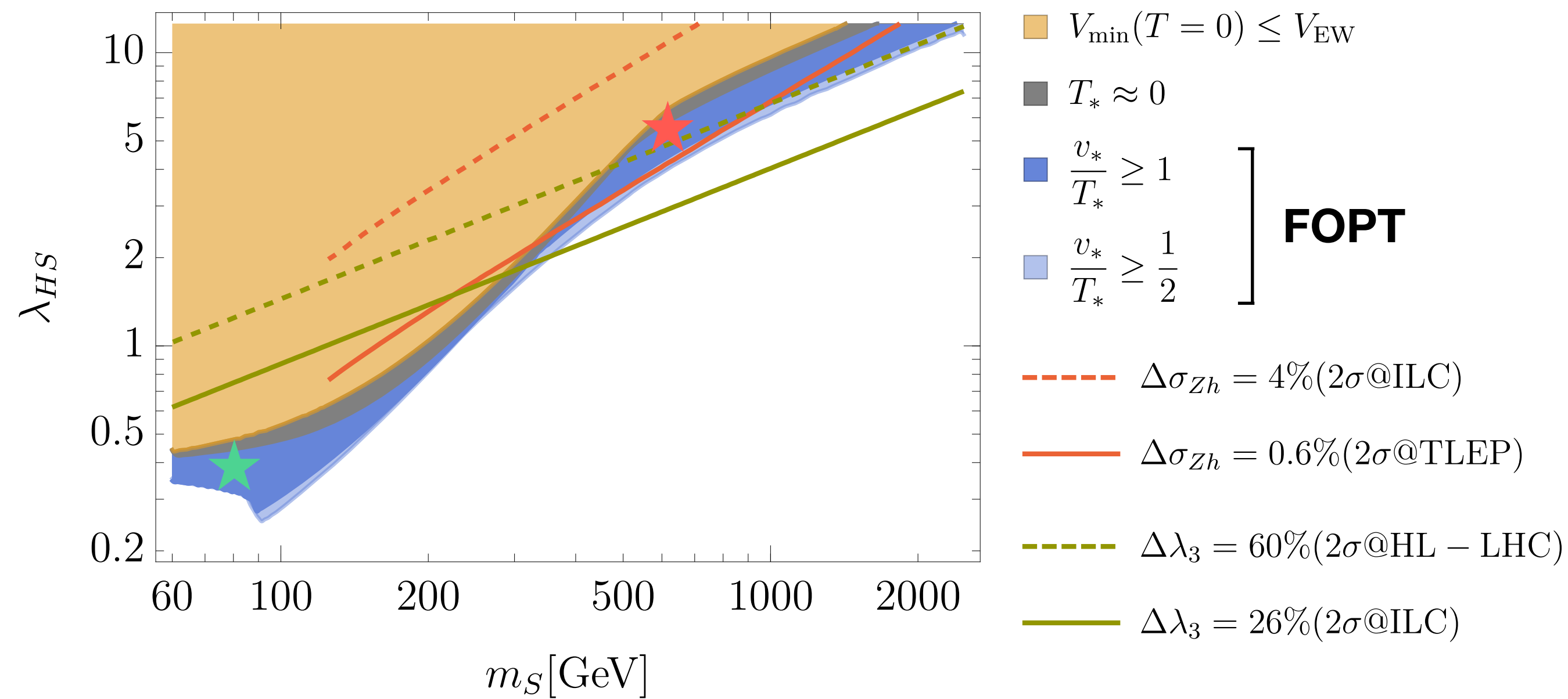
- Higgs-singlet portal:  $\lambda_{HS} S^2 H^\dagger H$

- SMEFT operator:  $\frac{c_6}{\Lambda^2} (H^\dagger H)^3$

[Grojean, Servant, Wells hep-ph/0407019;  
Noble, Perelstein 0711.3018]

# A First Order EWPT with Singlet

- For the Higgs-singlet portal:  $\lambda_{HS} S^2 H^\dagger H$



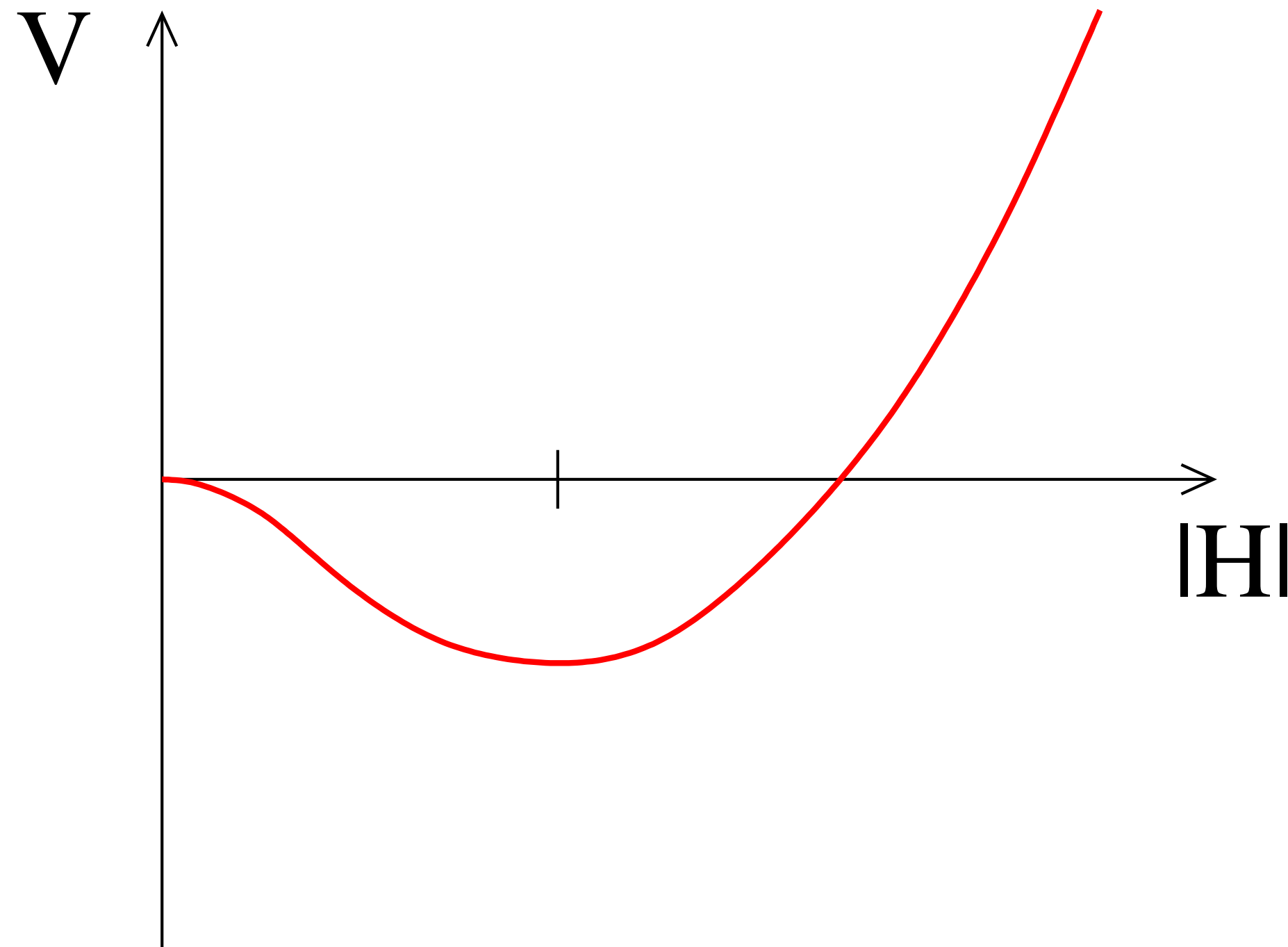
**[Curtin, Meade, Yu 1409.0005; Kotwal, Ramsey-Musolf, No, Winslow 1605.06123; Huang, Long, Wang 1608.06619; Beniwal, Lewicki, Wells, White, Williams 1702.06124]**

# The Standard Model Higgs Potential

$$V = -\mu^2 H^\dagger H + \lambda (H^\dagger H)^2$$

hierarchy  
problem

Higgs  
metastability

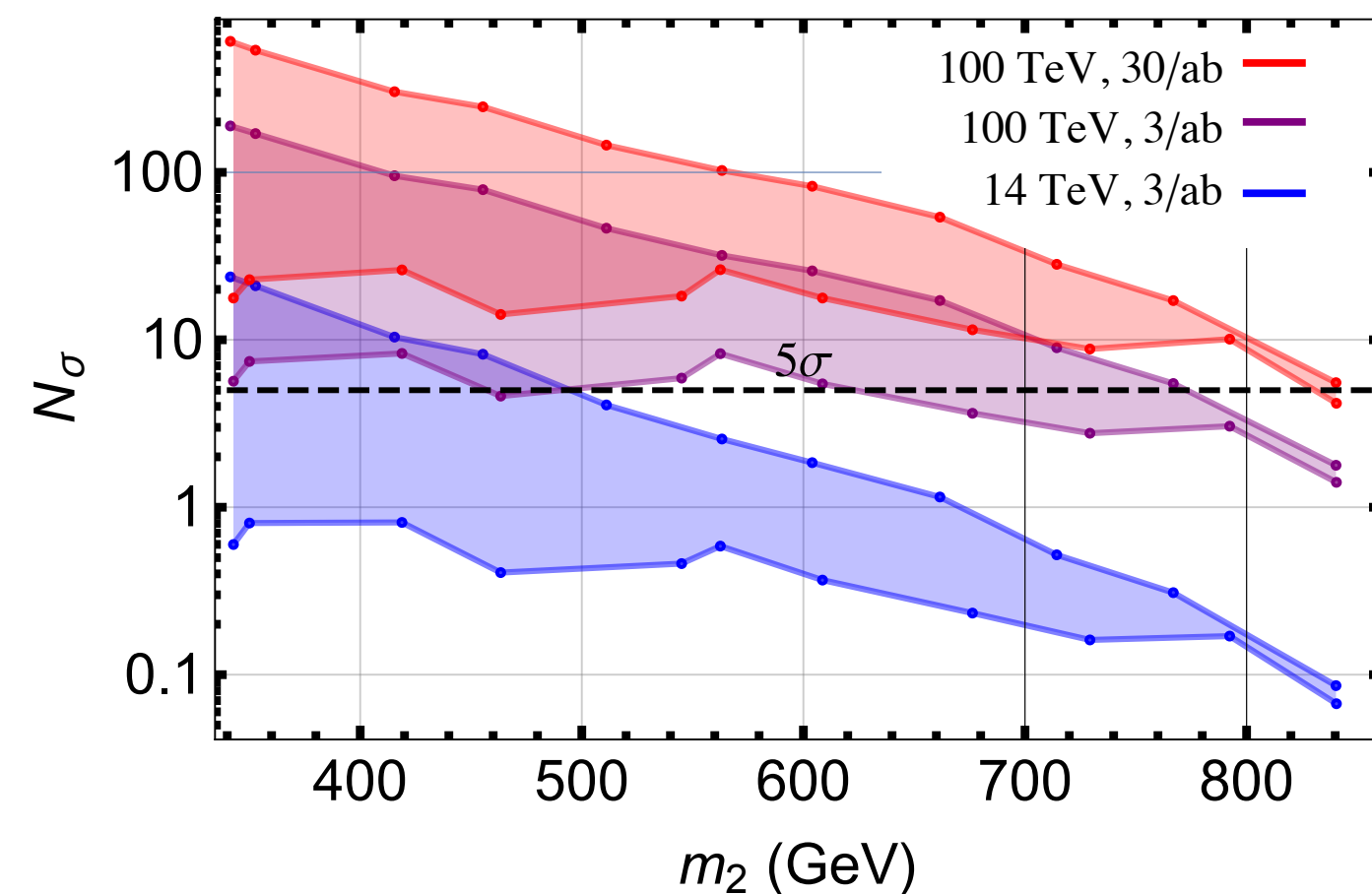


# (Higgs) Potential Questions

- What can we learn about new physics from Higgs couplings?
- A strongly first-order EWPT requires new physics coupling to the Higgs:
  - What does this imply generically for di-Higgs rates?
  - Does it imply a minimum deviation pattern in Higgs couplings?
  - How does the reach of Higgs coupling measurements compare to other direct and indirect probes?

# Higgs Potential Beyond the SM

- **Note 1:** extractions of  $\lambda_3$  are sensitive to other deviations in Higgs couplings as well as uncertainties in SM parameters.
- **Note 2:** some BSM scenarios can even interfere with the full realization of electroweak symmetry at high temperature. [e.g. Meade, Ramani 1807.07578; Baldes, Servant 1807.08770]
- **Note 3:** in Higgs-singlet scenarios with a first-order EWPT, finding the new (mostly) singlet scalar might be easier than measuring Higgs rates.



$$pp \rightarrow h_2^{(*)} \rightarrow hh$$

[Kotwal, Ramsey-Musolf, No, Winslow 1605.06123;  
Papaefstathiou, White 2010.00597]

# Summary future $\lambda_3$ measurements

## 1) LHC

- $O(10)$ - $O(2)$
- Could detect large anomalous coupling

## 2) HL-LHC

- $O(1)$
- Potential for evidence ( $3\sigma$  precision)

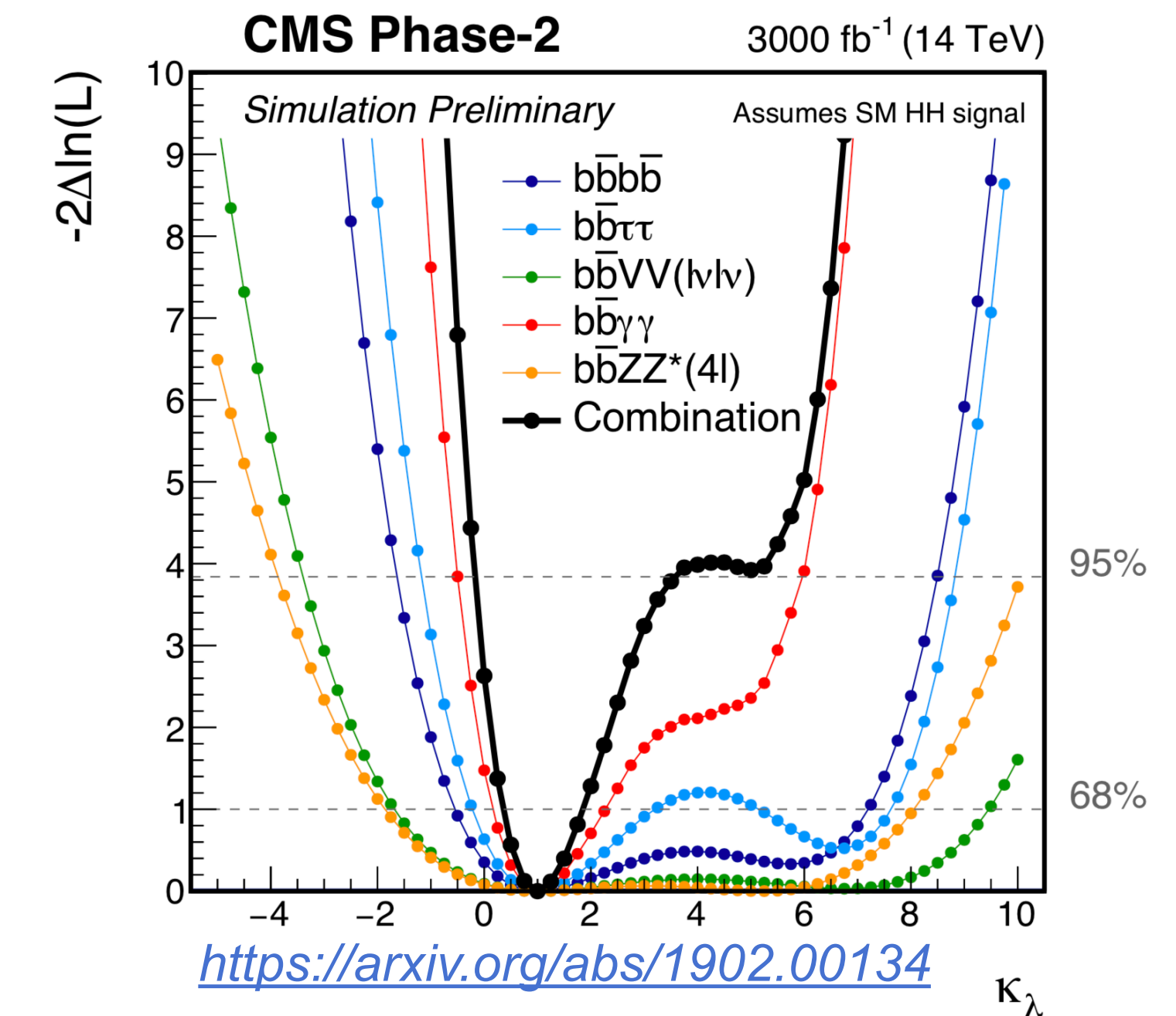
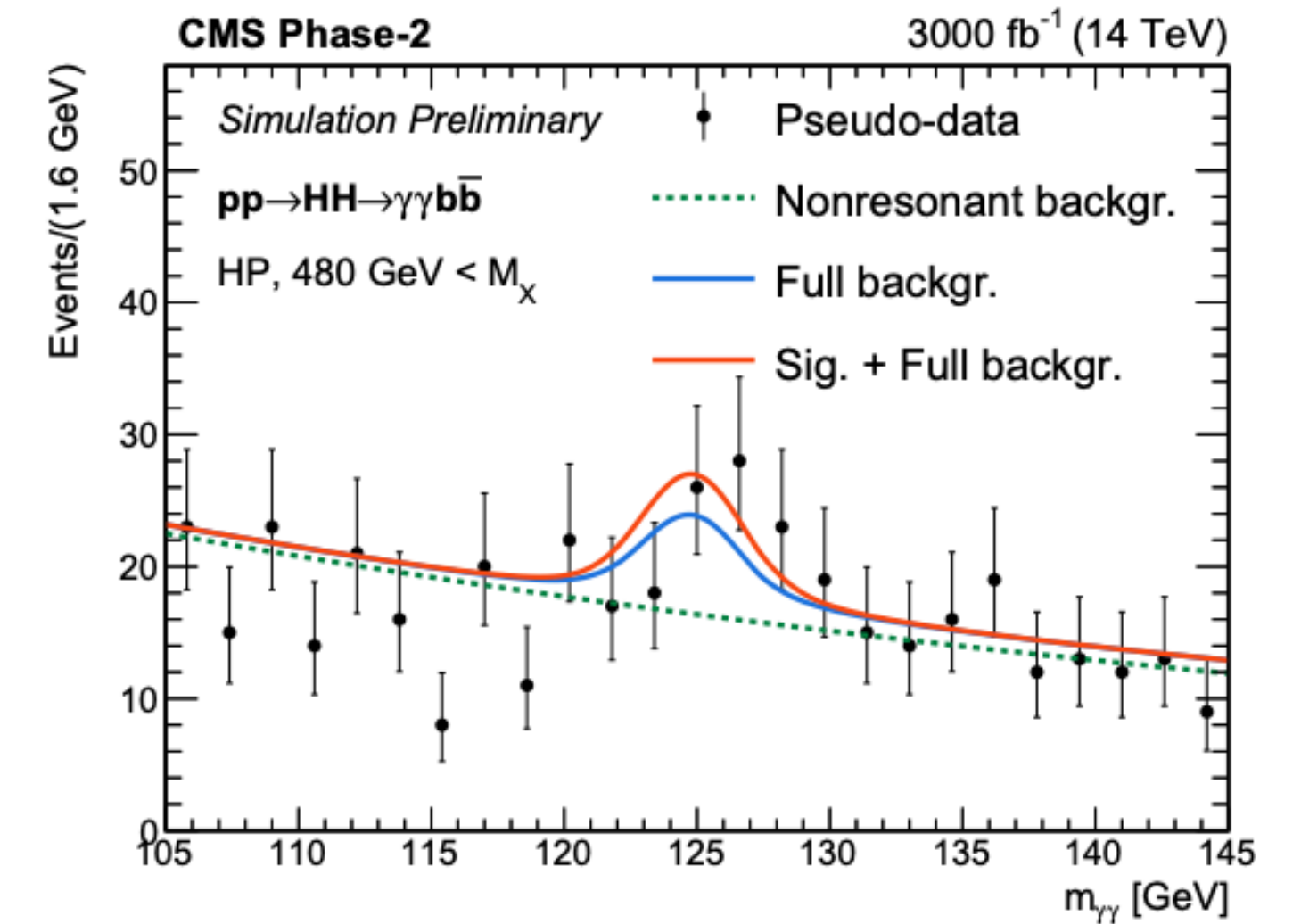
## 3) CEPC/FCC-ee : single H couplings + indirect measurement

- Potential for observation ( $5\sigma$  precision)
- $\delta g_{ttZ} \sim 1\%$ , allows for  $\delta \gamma_t \sim 1\%$  @FCC-hh

## 4) ILC/CLIC : $\sim 10\%$ precision

## 5) FCC-hh : precision measurement: 3.5-7.8%

## 6) Muon Collider: precision 2-3% (stat only) ?





# Global fit in indirect ee measurements

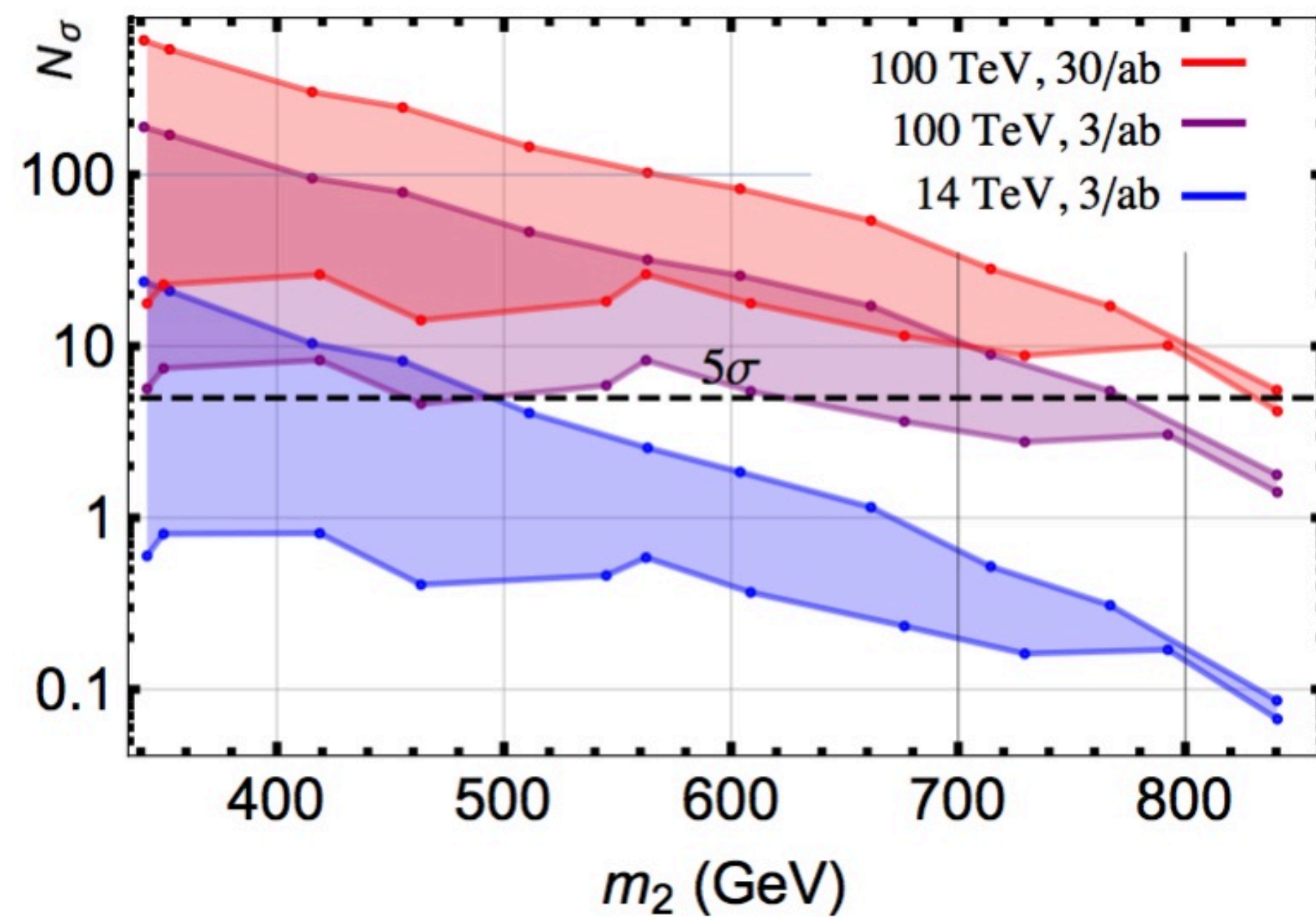
collider	1-parameter	full SMEFT
CEPC 240	18%	-
FCC-ee 240	21%	-
FCC-ee 240/365	21%	44%
FCC-ee (4IP)	15%	27%
ILC 250	36%	-
ILC 250/500	32%	58%
ILC 250/500/1000	29%	52%
CLIC 380	117%	-
CLIC 380/1500	72%	-
CLIC 380/1500/3000	49%	-

[1910.00012](#) [hep-ph]

# Higgs Self-coupling and constraints on models with 1st order EWPT

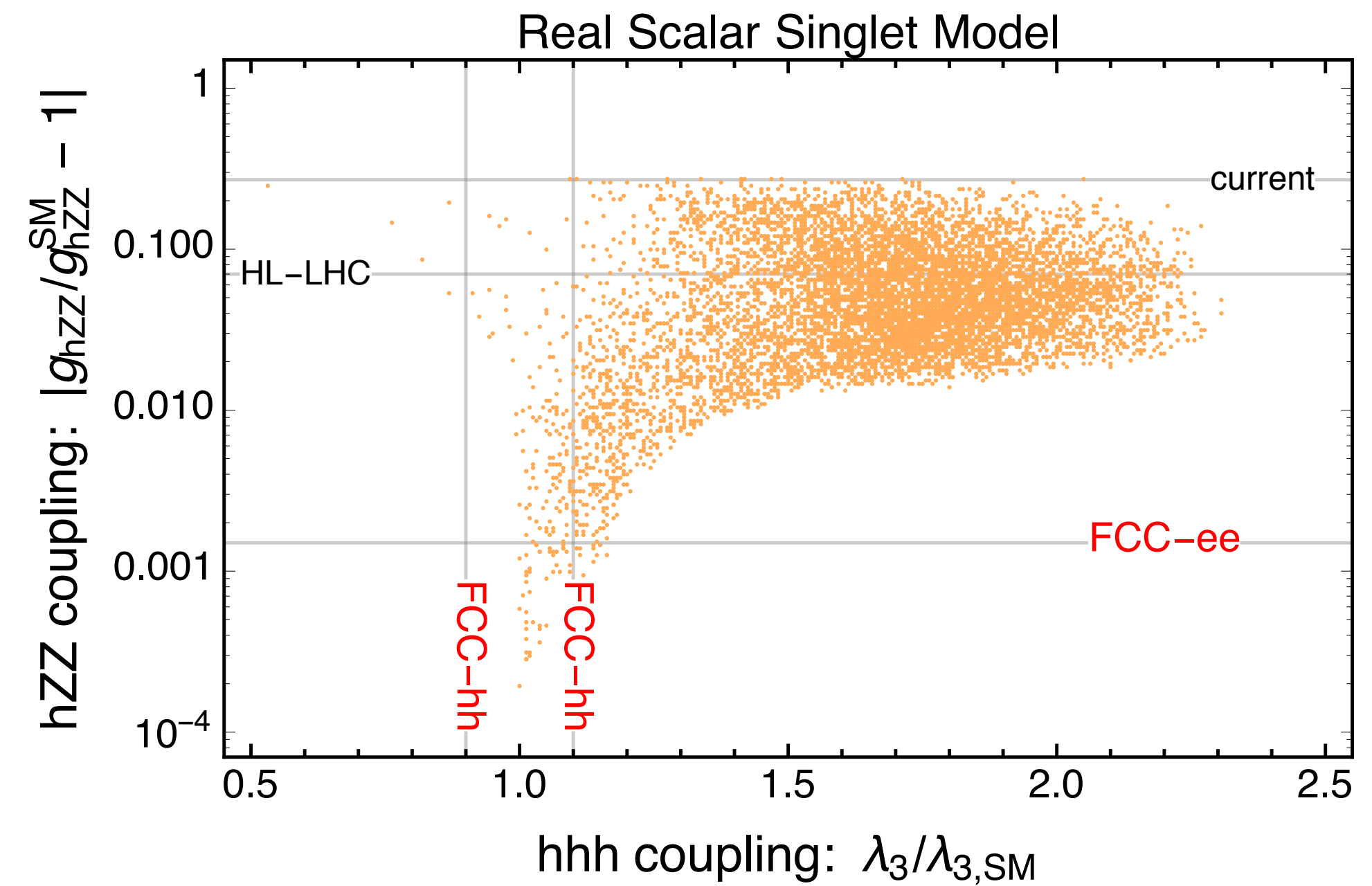
- Strong 1st order EWPT needed to explain large observed baryon asymmetry in our universe
- Can be achieved with extension of SM + singlet

Direct detection of extra Higgs states



$$h_2 \rightarrow h_1 h_1 \quad (b\bar{b}\gamma\gamma + 4\tau)$$

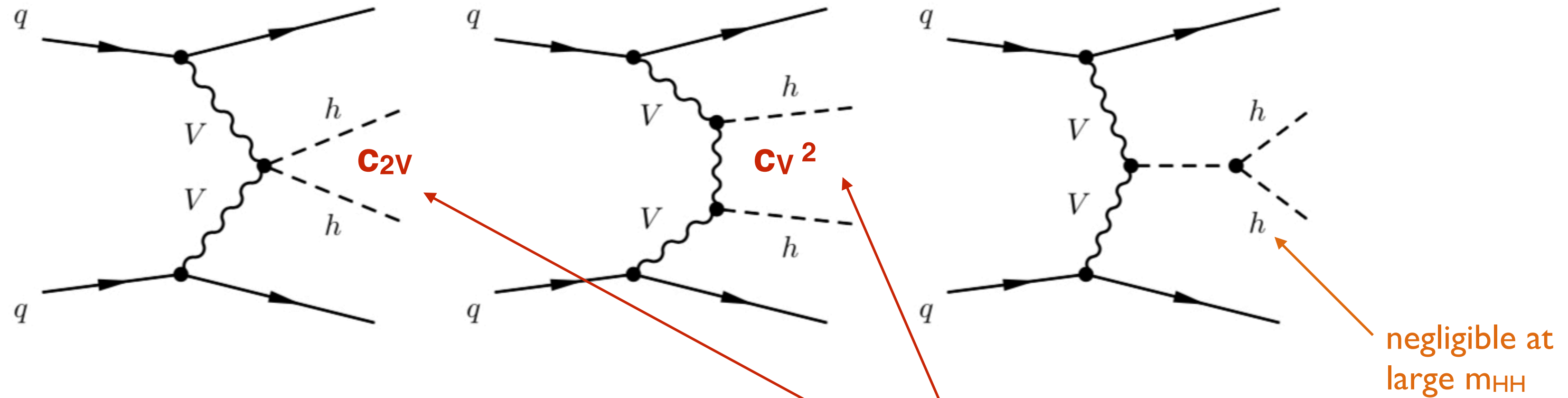
Combined constraints from precision Higgs measurements at FCC-ee and FCC-hh



Parameter space scan for a singlet model extension of the Standard Model. The points indicate a first order phase transition.

# $V_L V_L \rightarrow HH$

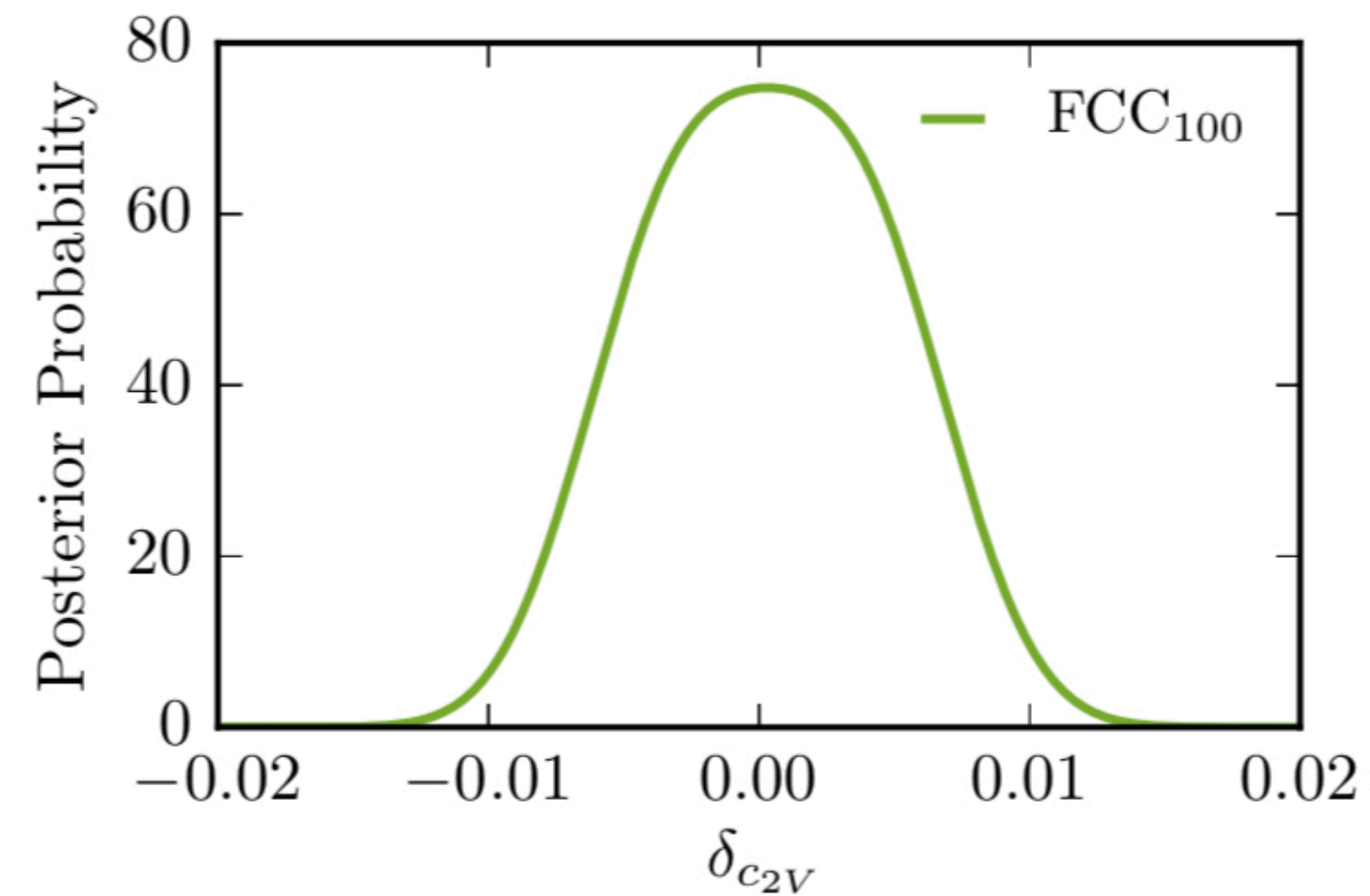
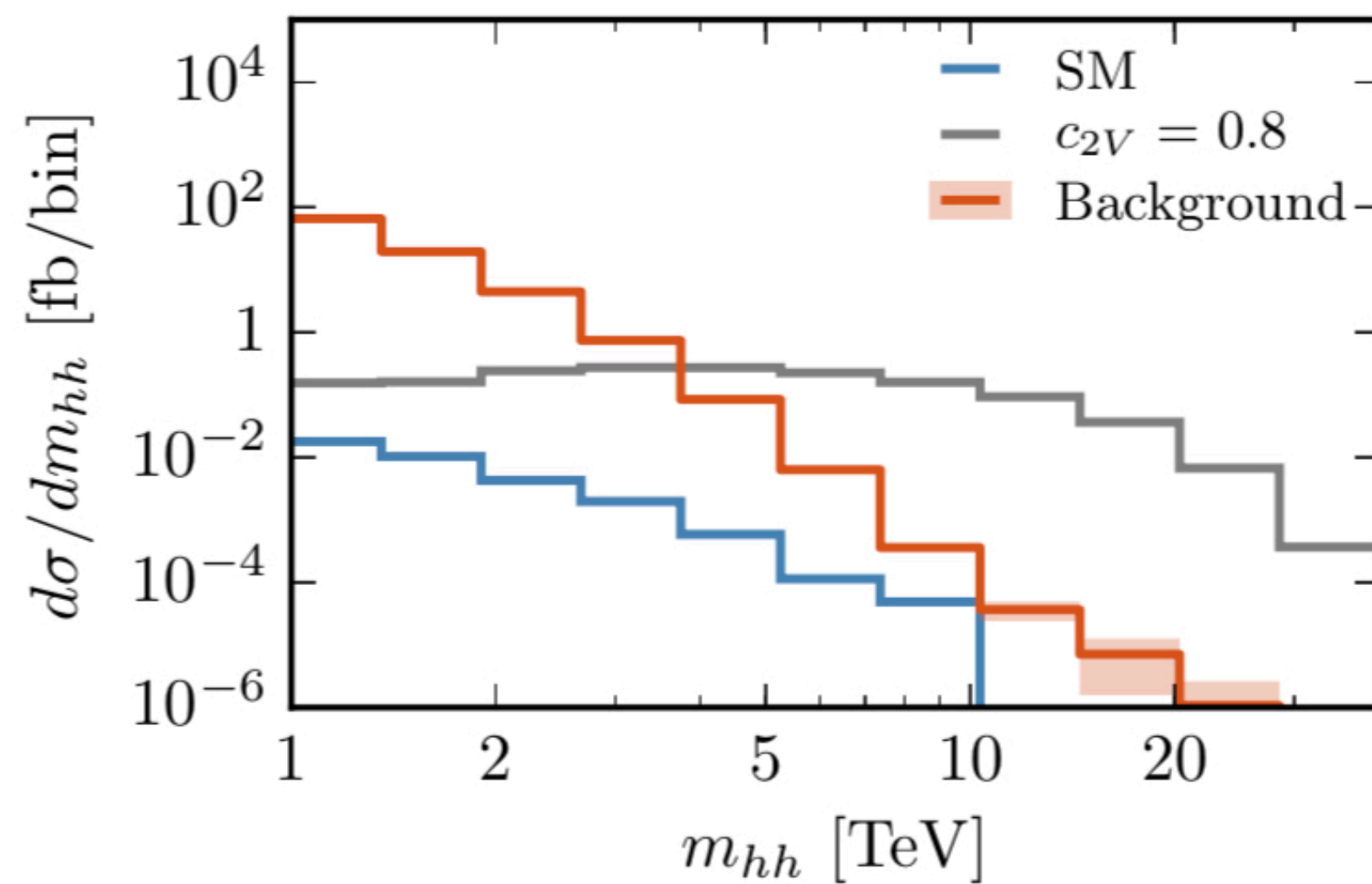
[1611.03860]



$$A(V_L V_L \rightarrow HH) \sim \frac{\hat{s}}{v^2} (c_{2V} - c_V^2) + \mathcal{O}(m_W^2/\hat{s}),$$

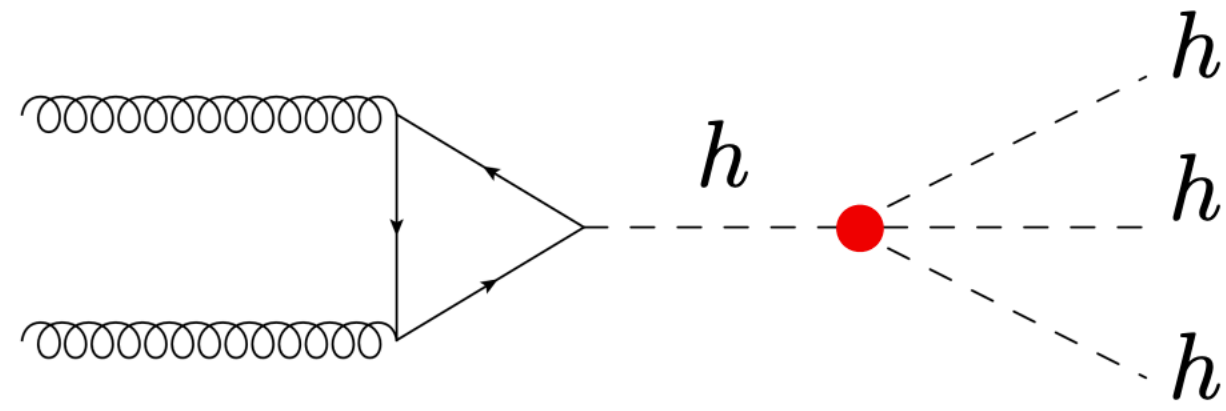
0 in the SM

high energy behaviour driven by  $C_{2V}$  and  $C_V$ , if  $\delta C_{2V} \neq 0$ , grows with  $E$

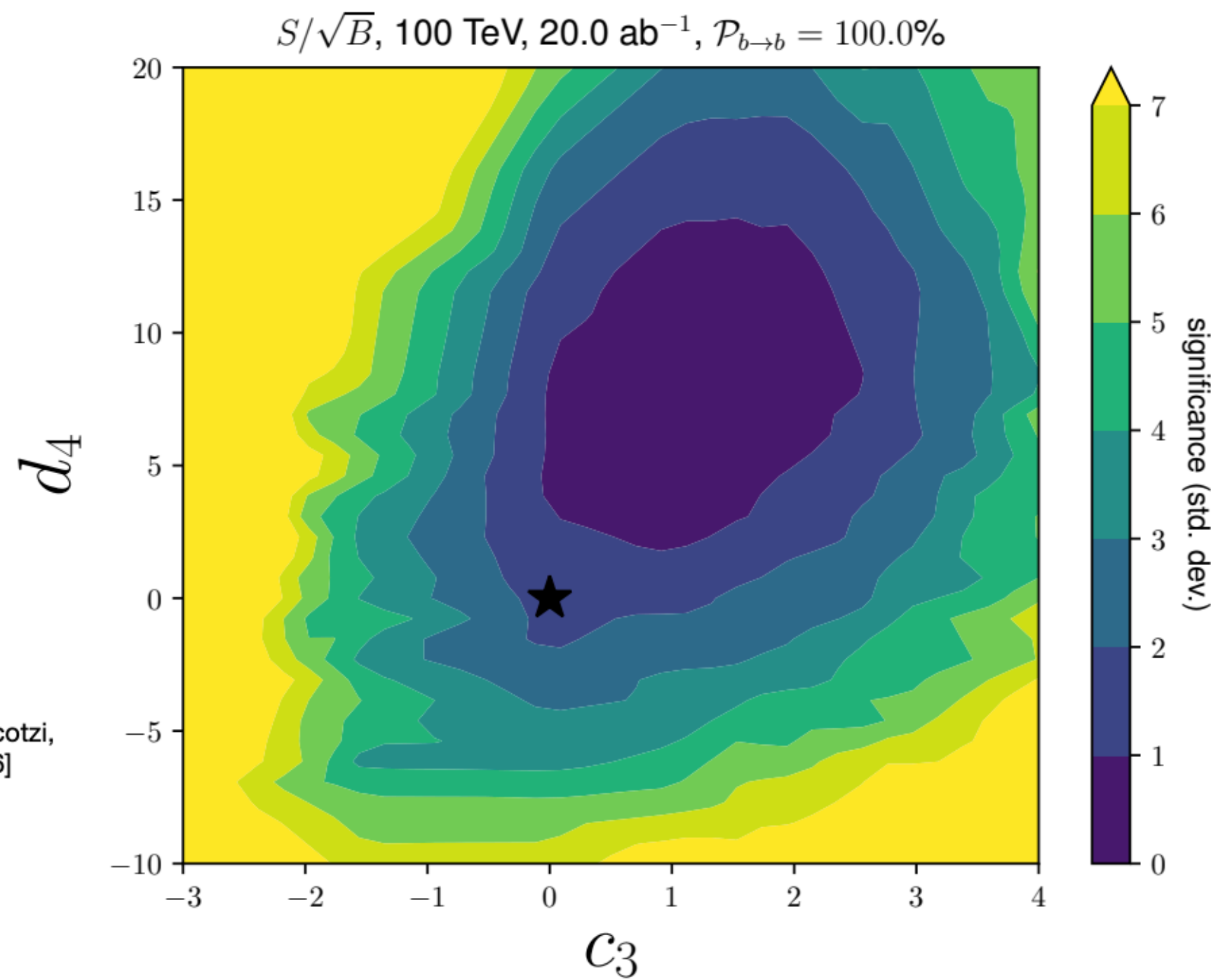
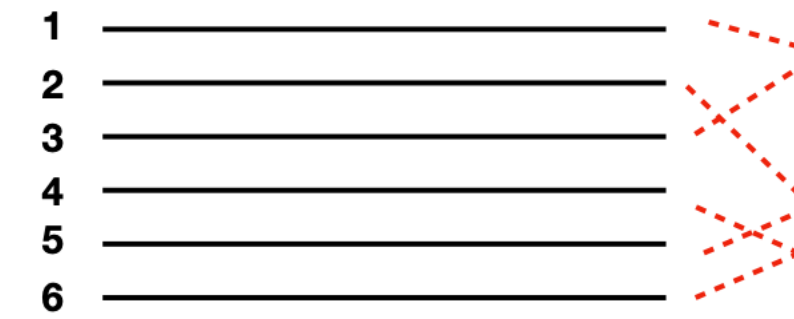


With  $c_V$  from FCC-ee,  $\delta c_{2V} < 1\%$

# HHH → bbbbbb



$$\chi^2 = \sum_{qr \in \text{pairings } I} (M_{qr} - m_h^2)^2$$



[AP, Tetlalmatzi-Xolocotzi, Zaro, 1909.09166]

**SM significance ~ 1.7σ**

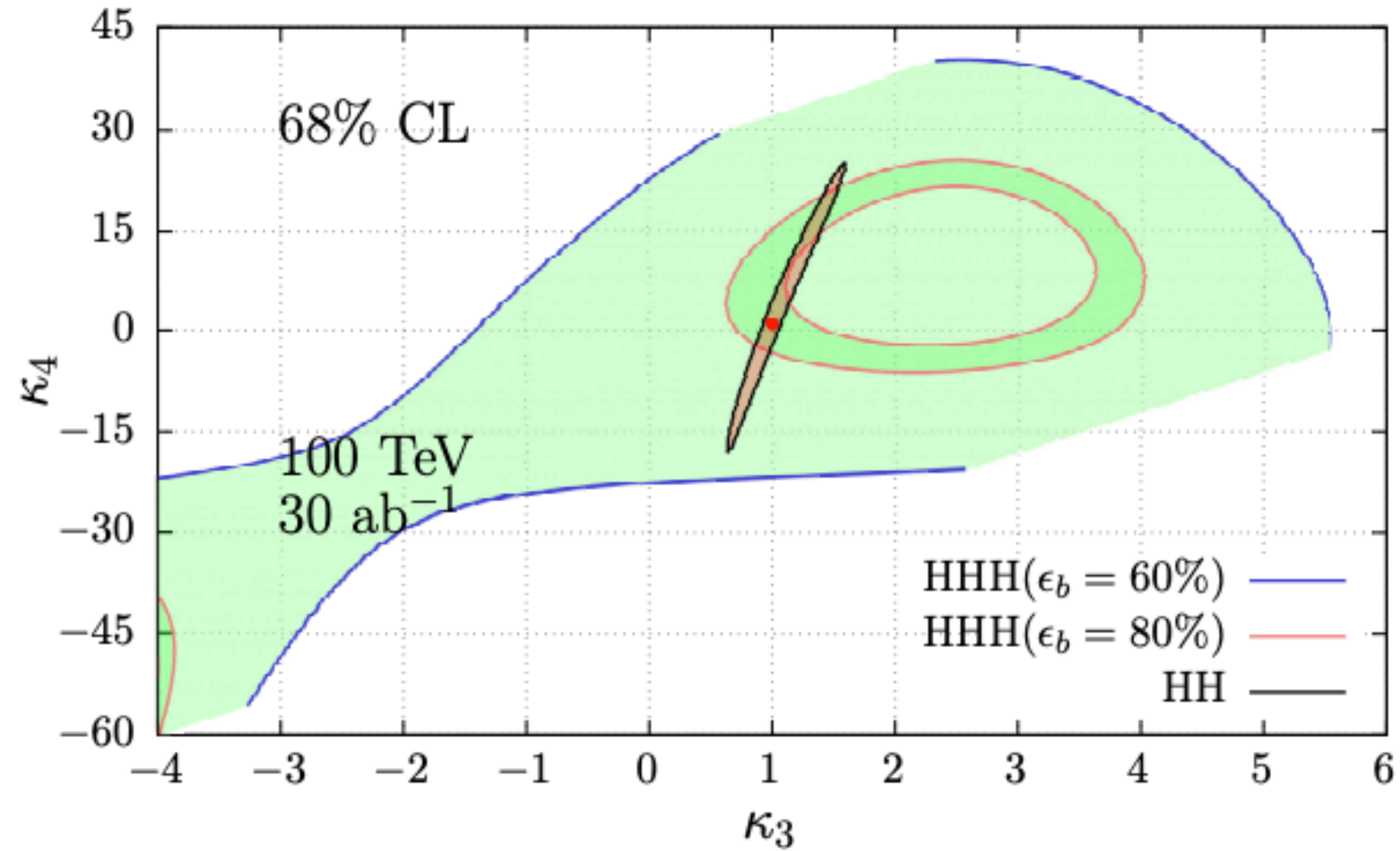
**$d_4 \in [-1.7, 13.3]$**

[Maltoni, Vryonidou]

$hhh \rightarrow$ final state	BR (%)	$N_{20\text{ab}^{-1}}$	
$(b\bar{b})(b\bar{b})(b\bar{b})$	19.21	22207	
$(b\bar{b})(b\bar{b})(WW_{1\ell})$	7.20	8328	
$(b\bar{b})(b\bar{b})(\tau\bar{\tau})$	6.31	7297	→ Fuks, Kim, Lee, 1510.07697, Fuks, Kim, Lee, 1704.04298.
$(b\bar{b})(\tau\bar{\tau})(WW_{1\ell})$	1.58	1824	
$(b\bar{b})(b\bar{b})(WW_{2\ell})$	0.98	1128	
$(b\bar{b})(WW_{1\ell})(WW_{1\ell})$	0.90	1041	→ Kilian, Sun, Yan, Zhao, Zhao, 1702.03554.
$(b\bar{b})(\tau\bar{\tau})(\tau\bar{\tau})$	0.69	799	
$(b\bar{b})(b\bar{b})(\gamma\gamma)$	0.23	263	→ AP, Sakurai, 1508.06524,

# Quartic bounds from di-Higgs

[1811.12366 \[hep-ph\]](#)



$\kappa_4 \in [-2.3, 4.3]$  at 68%CL