

A 3D rendering of a photonic crystal slab. The slab is a grey rectangular plate with a regular grid of small circular holes. A vertical waveguide, a narrow channel with a grid of larger holes, runs through the center of the slab. Red laser light is shown entering from the left, passing through a lens, and being directed into the waveguide. The light then exits the waveguide and is directed towards the right by another lens. The background is dark red, and the overall scene is illuminated with a soft red glow.

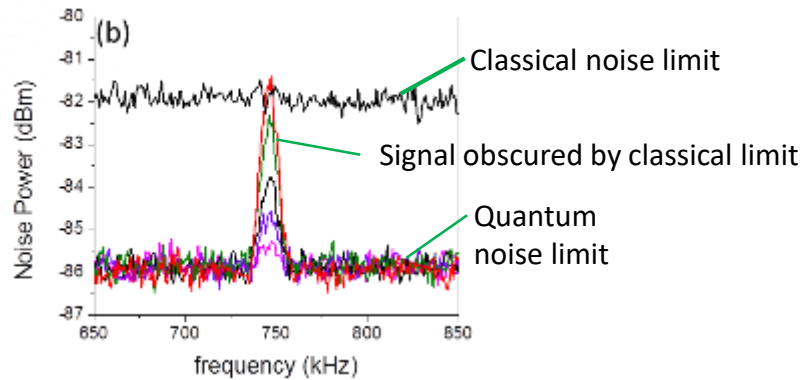
Opportunities for optical quantum noise reduction

Raphael Pooser

Snowmass
Quantum sensing workshop
8/19/2020

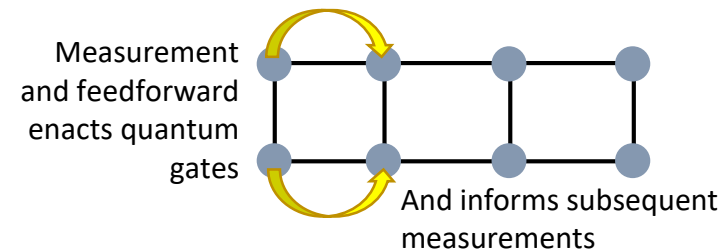
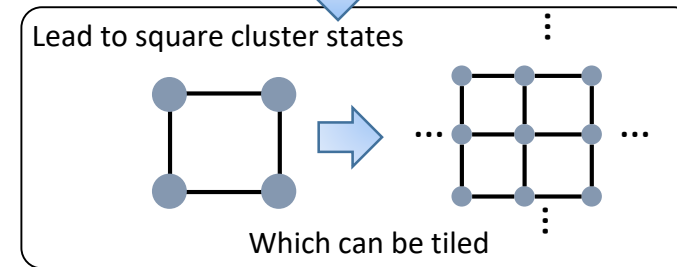
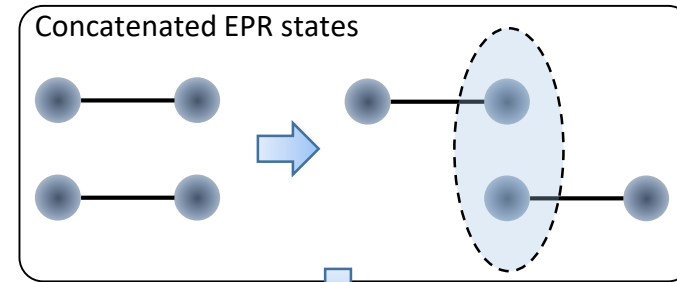
Quantum Sensing and Quantum Computing Across Quantum Networks

- Quantum networks are collections of qubits (nodes) connected by interactions, or quantum gates (edges)
- Simplest quantum network is the two qubit EPR state or Bell state, *which is a workhorse in quantum sensing*
 - The quantum correlations in EPR quantum networks can be used to *reduce the noise floor in measurements – quantum metrology*

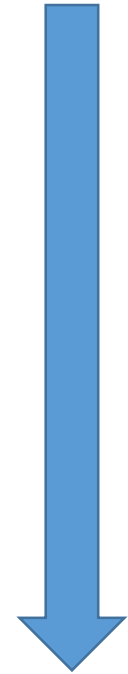


- Indefinitely large quantum networks can be built by concatenating EPR states – *the same network is a resource for measurement-based quantum computing and distributed quantum sensors*

$$|EPR\rangle = \int_{-\infty}^{\infty} |x\rangle_a \otimes |x\rangle_b dx$$



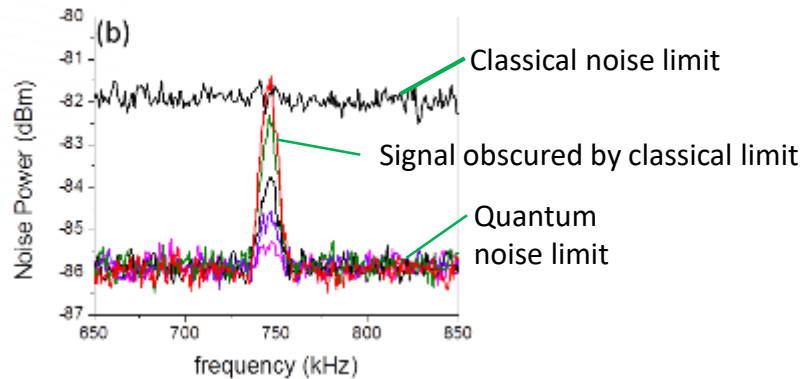
Sensing



Computing

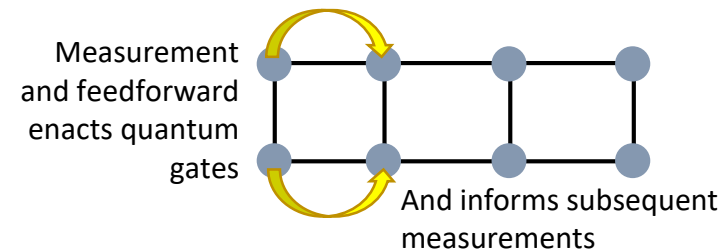
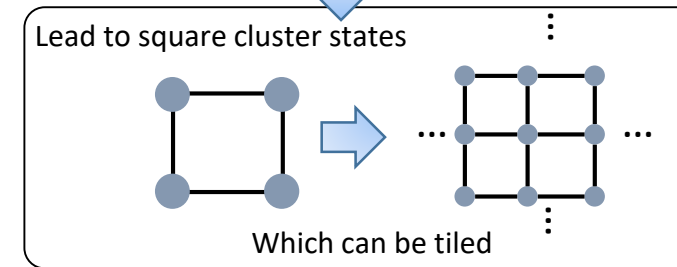
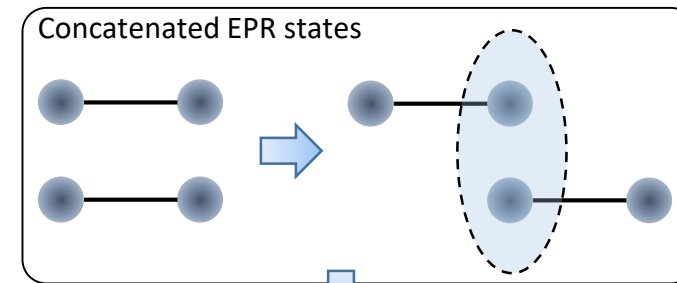
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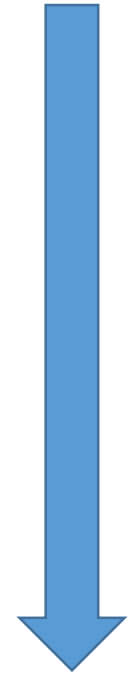


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Sensing

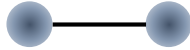


Computing

The know-how in generating long range entanglement for quantum sensing lends itself to building quantum computers. This is because in order to make these quantum sensors, one must build a *quantum network with a two qubit gate interaction between the nodes.*

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Sensing

Motivation:

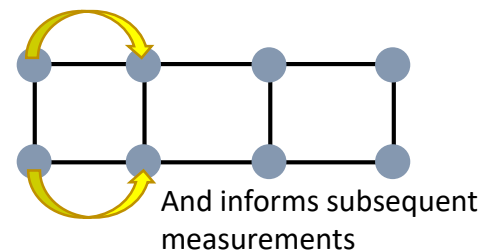
- Build quantum networks of sensors with entangled states
- Construct, e.g., stabilizer code and perform joint measurements to detect syndromes on the network
- Quantum noise reduction (QNR) is a signature of this type of entanglement
- Harness QNR and networks to obtain Heisenberg scaling across large geographically distributed networks for HEP experiments

Also see Dan Carney and Juehang Qin's talks for more motivation

frequency (kHz)

- Indefinitely large quantum networks can be built by concatenating EPR states – *the same network is a resource for measurement-based quantum computing and distributed quantum sensors*

Measurement and feedforward enacts quantum gates



Computing

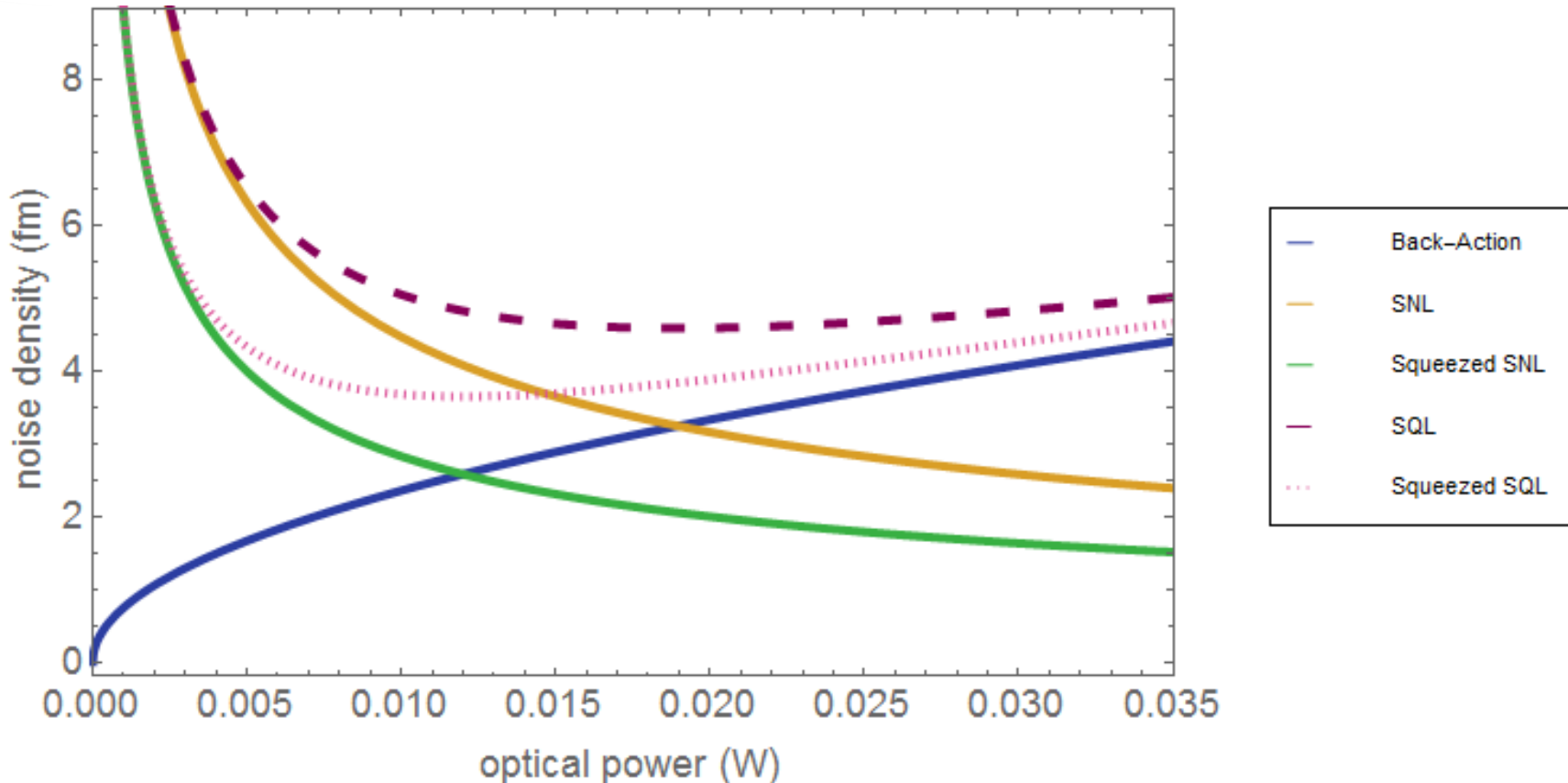
Optomechanics (MEMS) Noise

1. **Thermal noise limit** due to cantilever interactions with heat bath,
2. **Shot noise limit** due to photostatistics
3. **Back-action noise limit** due to fluctuations in radiation pressure imparted on cantilever.

On resonance, $\langle(\Delta x)^2\rangle_{th} > \langle(\Delta x)^2\rangle_{SQL} = \langle(\Delta x)^2\rangle_{shot} + \langle(\Delta x)^2\rangle_{back}$ above 1 μK .

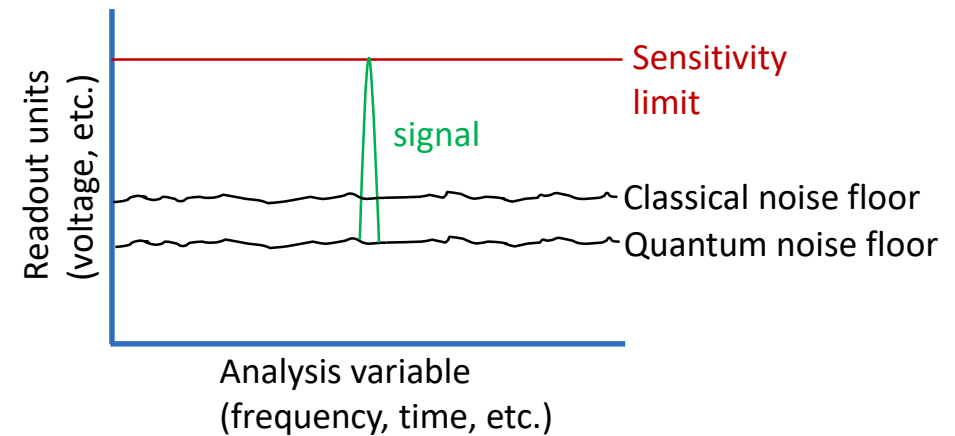
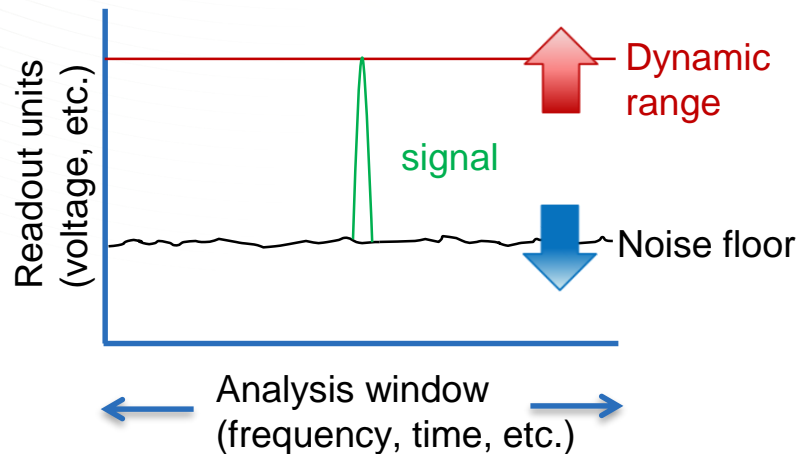
Off-resonance,

$$\langle(\Delta x)^2\rangle_{th} = \frac{2k_B T \Delta f}{k \pi f_0 Q}, \quad \langle(\Delta x)^2\rangle_{shot} = \frac{hc \lambda \Delta f}{8 \pi^2 P}, \quad \text{and} \quad \langle(\Delta x)^2\rangle_{back} = \frac{8 P h \Delta f}{c \lambda k^2}$$



Detection Limits

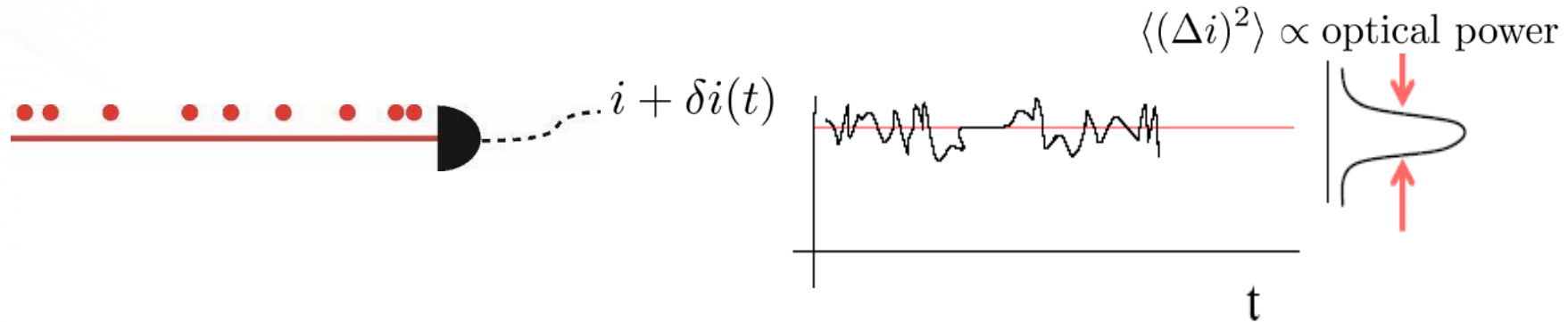
- The *fundamental detection limit* is the noise floor of the full sensor as viewed at the backend after all filters and computational analysis



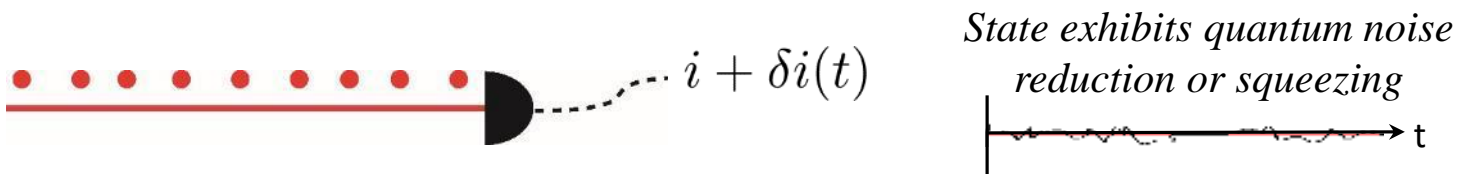
- Our approach increases the signal to noise (SNR) by decreasing the noise floor using **quantum noise reduction (QNR)** and increasing dynamic range using quantum signal modulation

Quantum Noise Reduction

- Quantum noise can be viewed as a result of light being composed of discrete photons with a random temporal distribution.



- This noise represents the shot noise limit (SNL) and is the minimum noise level for a classical state of light.
- Can generate states of light with less noise in amplitude through the use of a nonlinear process that can emit pairs of photons.

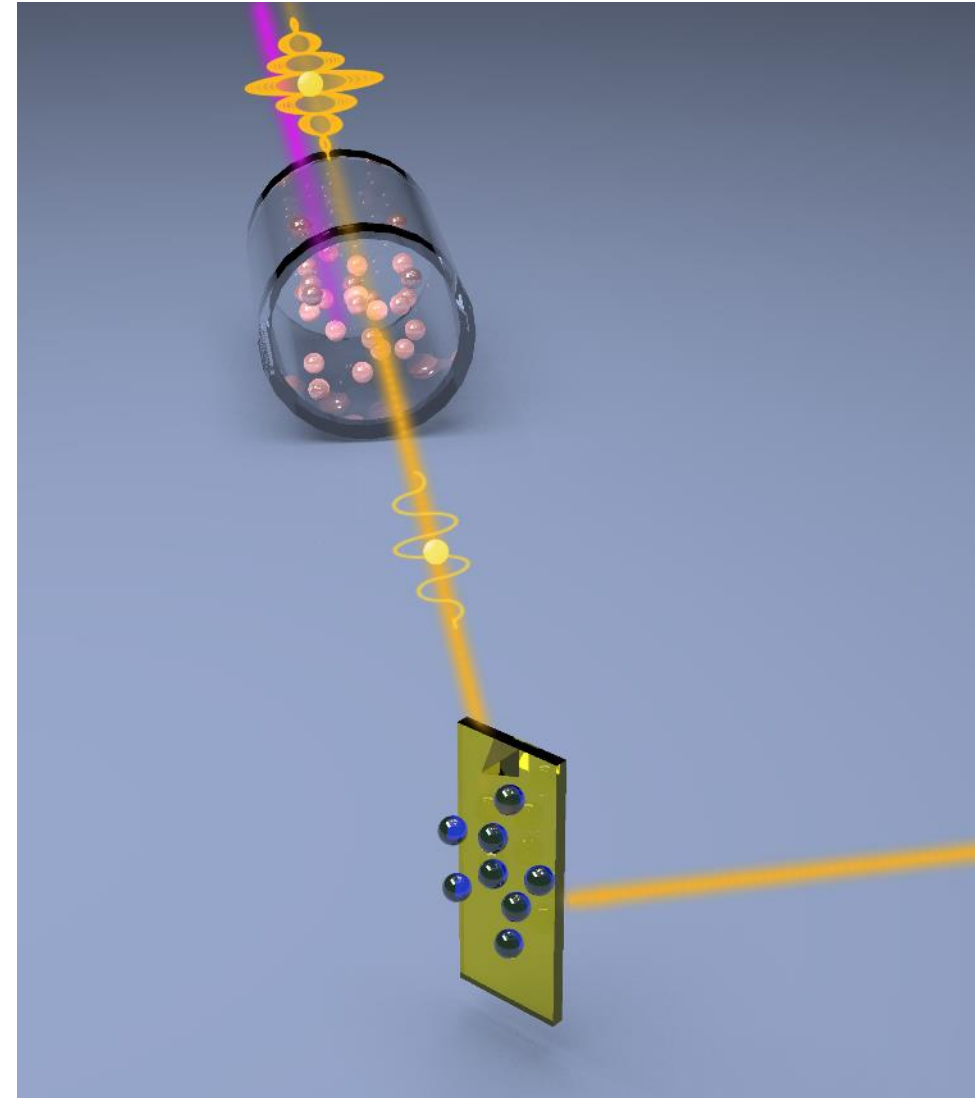
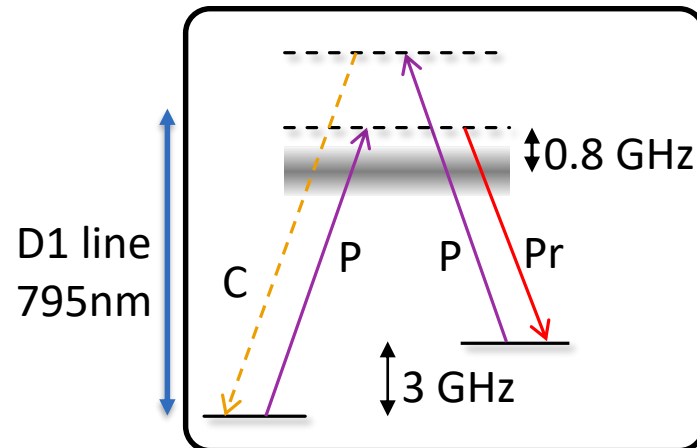


- Amount of quantum noise reduction increases with strength of nonlinearity.

Four wave mixing for CV quantum optics

Generate quantum noise reduction via nonlinear interactions:

Force light fields to interact with themselves via nonlinear optics near atomic resonance in Rb vapor. *Joint detection allows quantum noise reduction.*



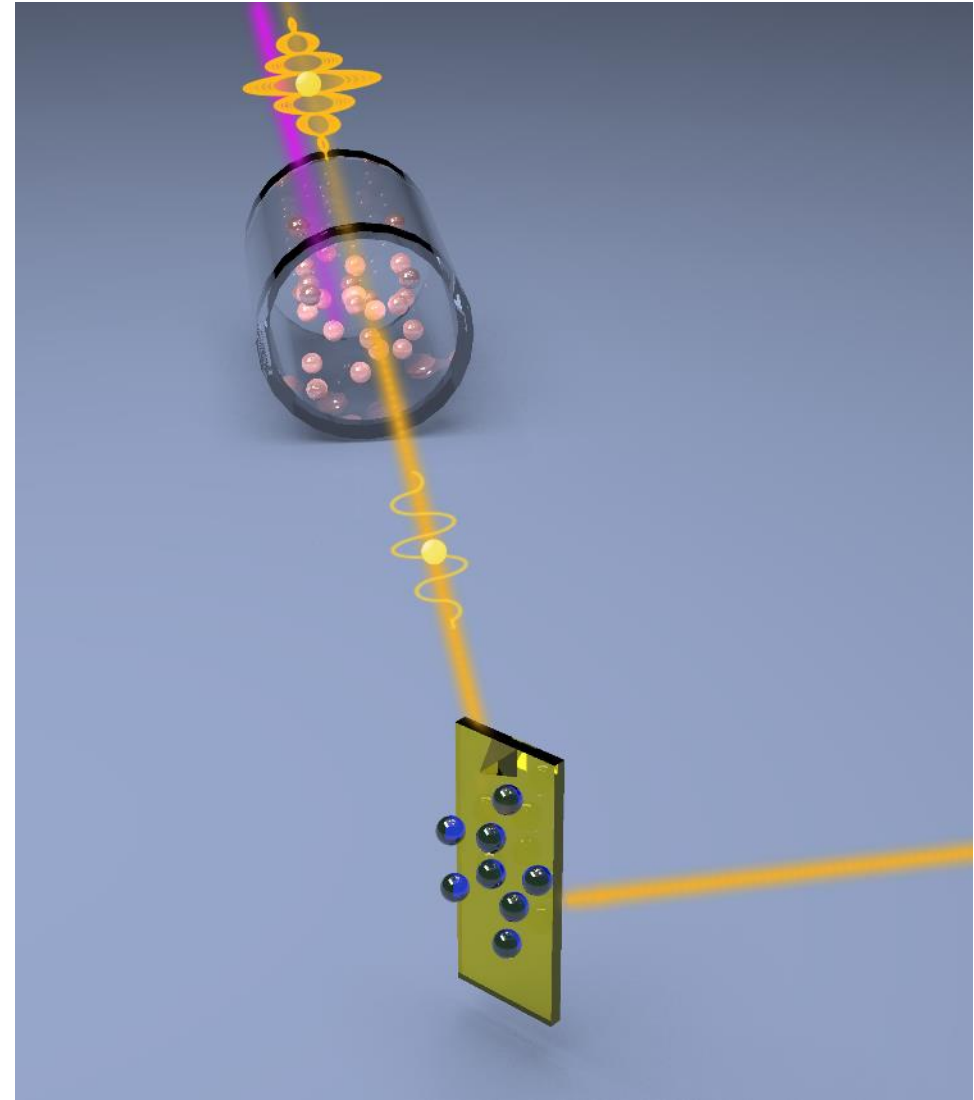
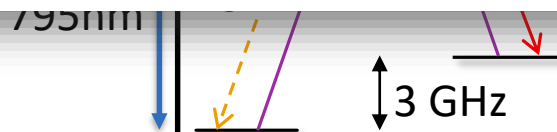
Science **321**, 544-547 (2008) *Nature* **457**, 859-862 (2009)

Four wave mixing for CV quantum optics

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$$\Delta N_{-,n}^2 = 1 + \frac{2\eta(1 - G)}{2G - 1} \text{ Hz}$$



Science **321**, 544-547 (2008) Nature **457**, 859-862 (2009)

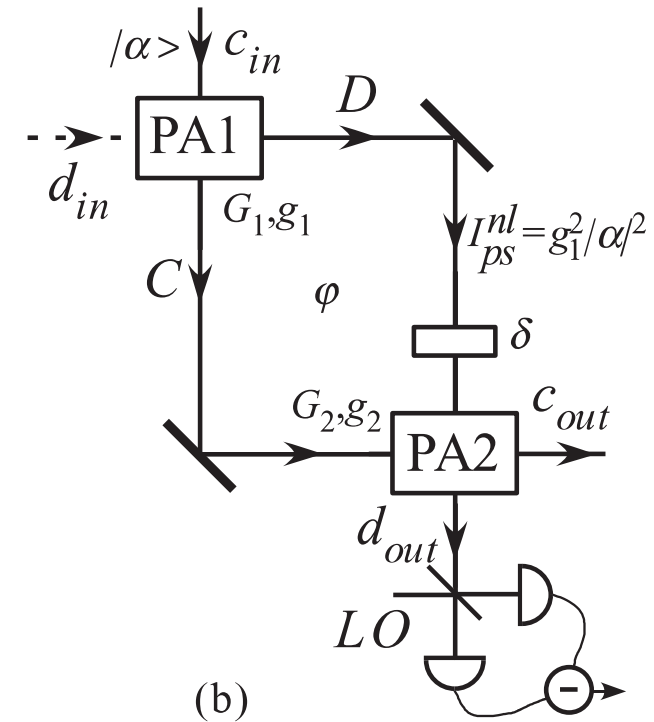
Recent Theoretical Innovation for Phase Estimation

- Non Linear Interferometry (NLI) improves sensitivity over LI:
 - Replace beam splitters with parametric amplifiers (PA)
 - Second PA becomes phase sensitive improves sensing signal
 - Does not change noise, improving SNR
 - For amplitude gain G , the SNR is:

$$G^2 g^2 (4|\alpha|^2 + 2)\delta^2 / 1 \approx 4G^2 I_{ps}^{nl} \delta^2 \quad \text{for } |\alpha|^2 \gg 1$$

- In this limit, the SNR improvement relative to LI is:

$$\text{SNR}_{\text{NLI}} / \text{SNR}_{\text{LI}} \approx 2 G^2$$



Z. Y. Ou, Phys. Rev. A **85**, 023815 (2012)

Homodyne detection

- Phase sum and amplitude difference show noise reduction for misaligned modes
- For *pure* phase, noise equivalent to two-mode-squeezed source

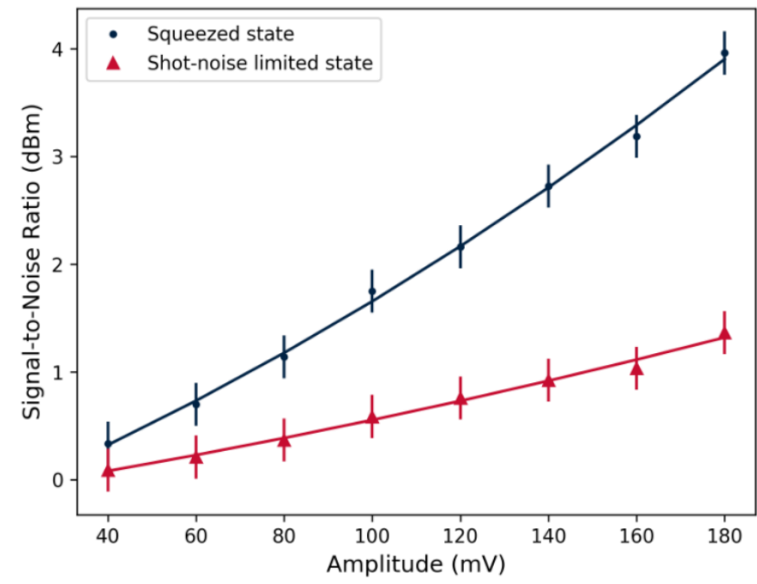
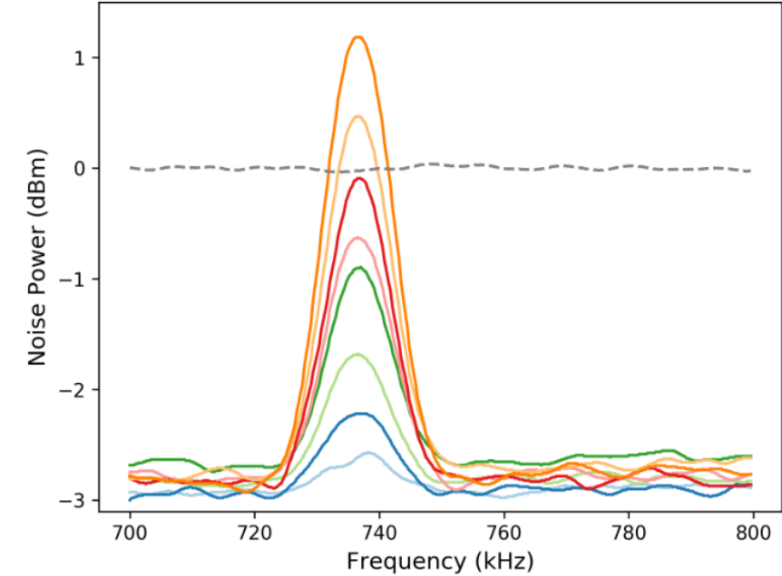
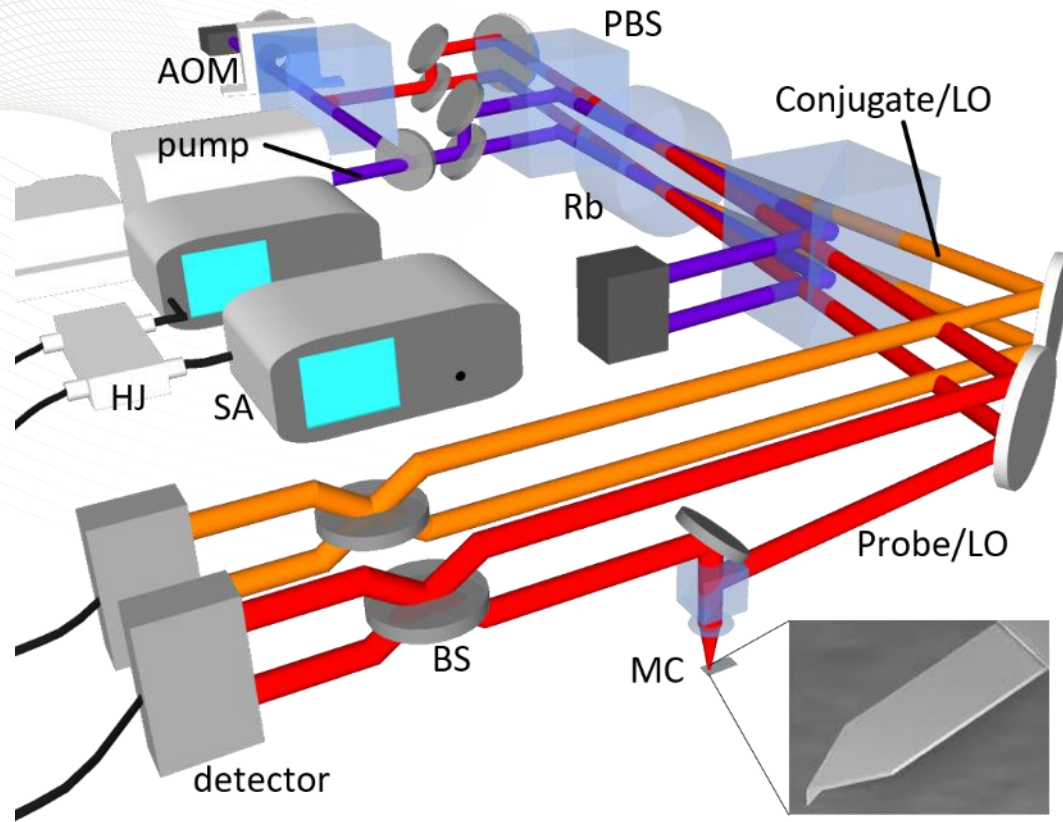
$$\begin{aligned}\Delta p_+^2 &= \frac{P_0}{P_{\text{tot}}} [1 + 2\eta_d(G - 1 - \sqrt{G(G - 1)})] \\ &+ \sum_{i=1}^N \frac{P_i}{P_{\text{tot}}} [1 + 2\eta_i(G - 1 - \sqrt{G(G - 1)})] \\ &+ \sum_{i=1}^N \frac{(P_{\text{tot}} - P_0 - P_i)}{P_{\text{tot}}} [1 + 2\eta_i(G - 1)]\end{aligned}$$

$$\Delta p_+^2 = 1 + 2\eta[G - 1 - \sqrt{G(G - 1)}]$$

$$p_+ = p_i + p_j + \Delta\varphi$$

$$\Delta\varphi = n\Delta d$$

Nonlinear Interferometric AFM imaging

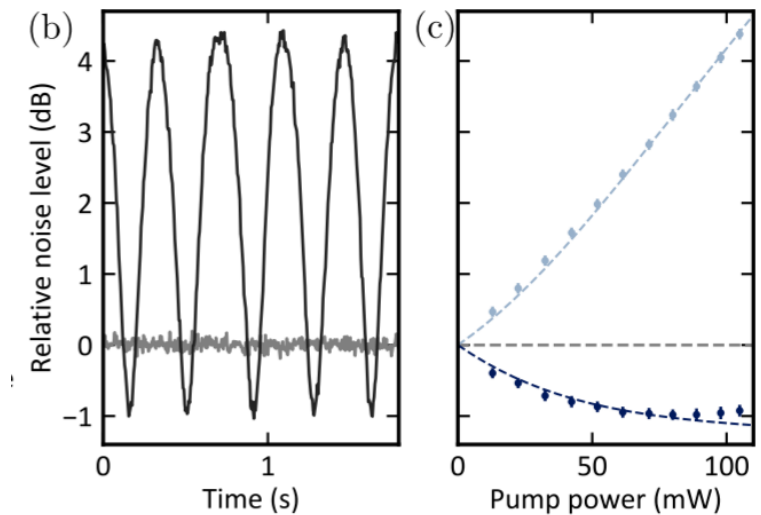
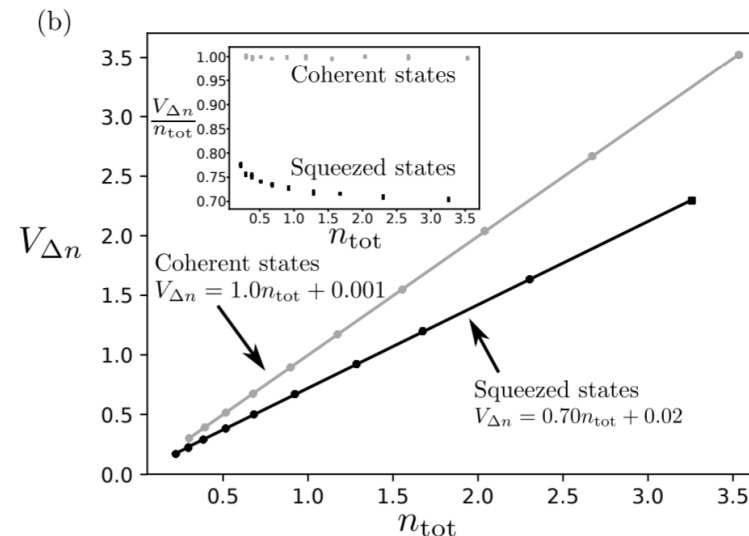
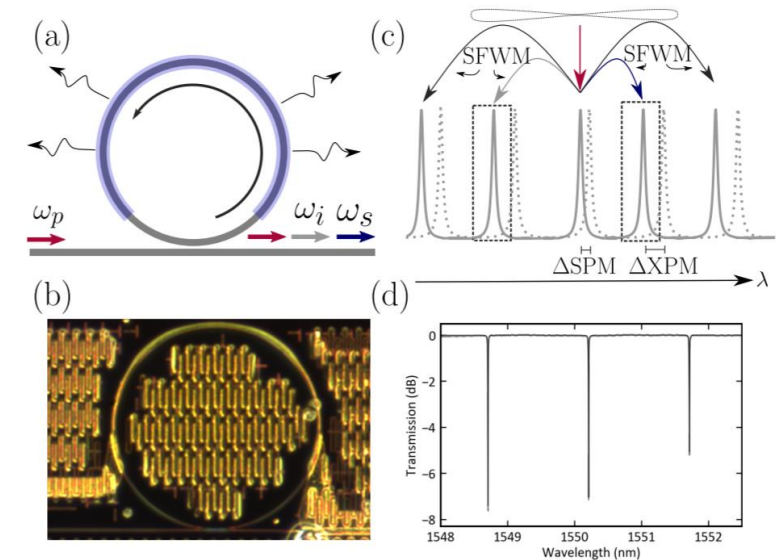


[Truncated Nonlinear Interferometry for Quantum-Enhanced Atomic Force Microscopy](#), RC Pooser, N Savino, E Batson, JL Beckey, J Garcia, BJ Lawrie
Physical Review Letters **124** (23), 230504 (2020)

But probably should go integrated

- See Dan Carney and Jeuhang Qin's talks
- Much less squeezing on chip, but
- Will be crucial for limiting losses in signal transduction outlined by others here
- Will allow for longer range quantum networks

arXiv:1904.07833v3



Thanks!

- W. M. Keck foundation
- DOE BES
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- SULI program
- Intelligence community postdoc program
- ORNL CNMS
- Office of Naval Research

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- Nick Peters
- Joe Lukens
- Nick Savino
- Emma Batson
- Nick Black
- Miller Eaton