

LOI entry: SNOWMASS21-RF1\_RF0-063

# $CP$ -violation study in $b$ -baryon hadronic decays using $SU(3)$ symmetry

Shibasis Roy <sup>1,2</sup>   Rahul Sinha <sup>1,2</sup>   N.G. Deshpande <sup>3</sup>

<sup>1</sup>The Institute of Mathematical Sciences, <sup>2</sup>Homi Bhabha National Institute

<sup>3</sup>Institute for Fundamental Science, University of Oregon

October 1, 2020



SnowMass2021



# Motivations

- $CP$  violation (CPV) in  $B$ -meson decays: **well established**.
- Promising evidence of CPV in  $b$ -baryon decays:
  - ✓  $CP$  asymmetry measurement ( $A_{CP}$ ) in  $\Lambda_b^0 \rightarrow p^+ K^-$ ,  $\Lambda_b^0 \rightarrow p^+ \pi^-$  first at CDF and subsequently at LHCb.  
PRL 113 (2014) 24, 242001, PLB 787 (2018) 124-133
  - ✓ **Results consistent with  $CP$  symmetry**.
- Theory predicts sizable direct  $CP$ -asymmetry in bottom baryon decays.  
PRD 80 (2009) 034011, PRD 80 (2009) 094016, PRD 91 (2015) 11, 116007
- LHCb have also observed several multibody decays of  $b$ -baryons
  - ✓ Rich resonant structure leading to a common final state.
  - ✓ Analyze  $T$ -odd observables to look for CPV.  
Nature Physics 13 (2017) 391, JHEP 08 (2018) 039, EPJC 79 (2019) 745, PRD 102 (2020) 051101
- Large  $b$ -baryon production fraction at LHCb
- Provides an opportunity to measure the CKM parameters, complimentary to analogous  $B$ -meson decays.

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# Overview

- Charmless  $b$ -baryon decays: Ideal place to look for CPV in  $b$ -baryons
- Two body decays of  $b$ -baryons:
  - ✓ Octet baryon and octet(singlet) meson.
  - ✓ Decuplet baryon and octet(singlet) meson.
- Several strangeness-changing ( $\Delta S = -1$ ) and strangeness-conserving ( $\Delta S = 0$ ) decays of  $b$ -baryons are possible.
- Similar studies in  $B \rightarrow PP$ ,  $B \rightarrow PV$  and  $B \rightarrow VV$  decays have been well explored using various approaches.

Zeppenfeld (Z.Phys.C (1981)), Savage et al. (PRD (1989)), Gronau et al.(PRD (1994)), Grinstein et al.(PRD (1996)), Deshpande et al.(PRD (2000)), Hai-Yang Cheng et al. (PRD (2015)), Grossman et al. (JHEP (2014)), He et al. (EPJC(2020)) . . .



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## Goal:

Identify amplitude relations and  $CP$ -asymmetry relations using  $SU(3)$ -symmetry.

# Formalism

- Effective Hamiltonian( $\mathcal{H}_{\text{eff}}$ )= $\mathcal{H}_{\text{eff}}^{\text{T}} + \mathcal{H}_{\text{eff}}^{\text{QCDP}} + \mathcal{H}_{\text{eff}}^{\text{EWP}}$

# Formalism

•  $\mathcal{H}_{\text{eff}}^{\text{T}}$

$\in \mathbf{15} \oplus \bar{\mathbf{6}} \oplus \mathbf{3}^{(6)} \oplus \mathbf{3}^{(\bar{3})}$

Tree operators

$$O_1^{(q=d, s)} = (\bar{u}_L^i \gamma^\mu b_L^j)(\bar{q}_L^j \gamma_\mu u_L^i), \quad O_2^{(q=d, s)} = (\bar{u}_L^i \gamma^\mu b_L^i)(\bar{q}_L^j \gamma_\mu u_L^j)$$

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- $\mathcal{H}_{eff}^{QCDP}$   
 $\in \mathbf{3}^{(6)} \oplus \mathbf{3}^{(\bar{3})}$

## QCD penguin operators

$$O_3^{(q_1=d, s)} = (\bar{q}_{1L}^i \gamma^\mu b_L^i) \sum_{q=u, d, s} (\bar{q}_L^j \gamma_\mu q_L^j), \quad O_4^{(q_1=d, s)} = (\bar{q}_{1L}^i \gamma^\mu b_L^j) \sum_{q=u, d, s} (\bar{q}_L^j \gamma_\mu q_L^i)$$
$$O_5^{(q_1=d, s)} = (\bar{q}_{1L}^i \gamma^\mu b_L^i) \sum_{q=u, d, s} (\bar{q}_R^j \gamma_\mu q_R^j), \quad O_6^{(q_1=d, s)} = (\bar{q}_{1L}^i \gamma^\mu b_L^j) \sum_{q=u, d, s} (\bar{q}_R^j \gamma_\mu q_R^i).$$

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- $\mathcal{H}_{eff}^{EWP}$

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## Electroweak penguin operators


$$O_7^{(q_1=d, s)} = \frac{3}{2} (\bar{q}_{1L}^i \gamma^\mu b_L^i) \sum_{q=u, d, s} e_q (\bar{q}_R^j \gamma_\mu q_R^j), \quad O_8^{(q_1=d, s)} = \frac{3}{2} (\bar{q}_{1L}^i \gamma^\mu b_L^i) \sum_{q=u, d, s} e_q (\bar{q}_R^j \gamma_\mu q_R^j)$$

$$O_9^{(q_1=d, s)} = \frac{3}{2} (\bar{q}_{1L}^i \gamma^\mu b_L^i) \sum_{q=u, d, s} e_q (\bar{q}_L^j \gamma_\mu q_L^j), \quad O_{10}^{(q_1=d, s)} = \frac{3}{2} (\bar{q}_{1L}^i \gamma^\mu b_L^i) \sum_{q=u, d, s} e_q (\bar{q}_L^j \gamma_\mu q_L^j).$$



# Formalism

- Effective Hamiltonian ( $\mathcal{H}_{\text{eff}}$ ) =  $\mathcal{H}_{\text{eff}}^{\text{T}}$  +  $\mathcal{H}_{\text{eff}}^{\text{QCDP}}$  +  $\mathcal{H}_{\text{eff}}^{\text{EWP}}$


$$\mathcal{H}_{\text{eff}} = \frac{4G_F}{\sqrt{2}} \left[ \lambda_u^{(s)} \left( C_1(O_1^{(u)} - O_1^{(c)}) + C_2(O_2^{(u)} - O_2^{(c)}) \right) - \lambda_t^{(s)} \sum_{i=1,2} C_i O_i^{(c)} \right. \\ \left. - \lambda_t^{(s)} \sum_{i=3}^{10} C_i O_i^{(s)} + \lambda_u^{(d)} \left( C_1(O_1^{(u)} - O_1^{(c)}) + C_2(O_2^{(u)} - O_2^{(c)}) \right) \right. \\ \left. - \lambda_t^{(d)} \sum_{i=1,2} C_i O_i^{(c)} - \lambda_t^{(d)} \sum_{i=3}^{10} C_i O_i^{(d)} \right],$$

Rev. Mod. Phys. **68** (1996) 1125

$V_{ub} V_{us}^* = \lambda_u^s$ ,  $V_{ub} V_{ud}^* = \lambda_u^d$ ,  $V_{tb} V_{ts}^* = \lambda_t^s$ ,  $V_{tb} V_{td}^* = \lambda_t^d$  are the CKM elements and  $C_i$  s are the Wilson coefficients.

- Decompose the decay amplitude in terms of  $SU(3)$ -reduced amplitudes.

$$B_b(\bar{3}) \rightarrow \mathcal{O}(8)\mathcal{M}(8)$$

- Final state:  $1 \oplus 8_1 \oplus 8_2 \oplus 10 \oplus \bar{10} \oplus 27$
- Number of independent  $SU(3)$ -reduced amplitudes: 10
- $SU(3)$ -reduced amplitudes:

$$\langle 10 \parallel \mathbf{15} \parallel \bar{3} \rangle, \langle \bar{10} \parallel \bar{\mathbf{6}} \parallel \bar{3} \rangle, \langle 8_1 \parallel \mathbf{15} \parallel \bar{3} \rangle, \\ \langle 8_1 \parallel \bar{\mathbf{6}} \parallel \bar{3} \rangle, \langle 1 \parallel \mathbf{3} \parallel \bar{3} \rangle, \langle 27 \parallel \mathbf{15} \parallel \bar{3} \rangle, \\ \langle 8_1 \parallel \mathbf{3} \parallel \bar{3} \rangle, \langle 8_2 \parallel \mathbf{15} \parallel \bar{3} \rangle, \\ \langle 8_2 \parallel \bar{\mathbf{6}} \parallel \bar{3} \rangle, \langle 8_2 \parallel \mathbf{3} \parallel \bar{3} \rangle.$$

R Sinha, N.G. Deshpande, SR (Phys.Rev.D 101 (2020) 3, 036018)

$$B_b(\bar{3}) \rightarrow \mathcal{D}(10)\mathcal{M}(8)$$

- Final state:  $8 \oplus 10 \oplus 27 \oplus 35$
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- Assuming an unbroken  $SU(3)$  symmetry,

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# Amplitude and $CP$ relations

- Tree and penguin parts of a decay amplitude follow the same amplitude relation.
- Decay amplitude is decomposed as,

$$\mathcal{A}^l = \lambda_u^q \mathcal{A}_{\text{tree}}^l + \lambda_t^q \mathcal{A}_{\text{penguin}}^l.$$

where  $l = 0, 1, 2$  denote contributions from particular partial waves.

$$\delta_{CP}^l(\mathcal{B}_b \rightarrow \mathcal{B} \mathcal{M}) = -4\mathbf{J} \times \text{Im} \left[ \mathcal{A}_{\text{tree}}^{l*}(\mathcal{B}_b \rightarrow \mathcal{B} \mathcal{M}) \mathcal{A}_{\text{penguin}}^l(\mathcal{B}_b \rightarrow \mathcal{B} \mathcal{M}) \right],$$

where  $\mathbf{J}$  is the Jarlskog Invariant and  $\mathcal{B}$  is a final state octet( $\mathcal{O}$ ) or decuplet( $\mathcal{D}$ ) baryon.

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$$\delta_{CP}^l(\mathcal{B}_b \rightarrow \mathcal{B} \mathcal{M}) = -4\mathbf{J} \times \text{Im} \left[ \mathcal{A}_{\text{tree}}^{l*}(\mathcal{B}_b \rightarrow \mathcal{B} \mathcal{M}) \mathcal{A}_{\text{penguin}}^l(\mathcal{B}_b \rightarrow \mathcal{B} \mathcal{M}) \right],$$

where  $\mathbf{J}$  is the Jarlskog Invariant and  $\mathcal{B}$  is a final state octet( $\mathcal{O}$ ) or decuplet( $\mathcal{D}$ ) baryon.

- $\mathcal{A}_{CP}$  relations are obtained by multiplying appropriate phase space factor corresponding to each partial wave contributing to the decay.

# Amplitude and $CP$ relations

- Tree and penguin parts of a decay amplitude follow the same amplitude relation.
- Decay amplitude is decomposed as,

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# Selected results

## $B_b(\bar{3}) \rightarrow \mathcal{D}(10)\mathcal{M}(8)$

$$\begin{aligned} \delta_{\text{CP}}^I(\Lambda_b^0 \rightarrow \Delta^+ K^-) &= \delta_{\text{CP}}^I(\Lambda_b^0 \rightarrow \Delta^0 \bar{K}^0) \\ \delta_{\text{CP}}^I(\Lambda_b^0 \rightarrow \Sigma'^- \pi^+) &= \delta_{\text{CP}}^I(\Lambda_b^0 \rightarrow \Xi'^- K^+) \\ &= -\frac{1}{3} \delta_{\text{CP}}^I(\Lambda_b^0 \rightarrow \Delta^+ \pi^-) = -\delta_{\text{CP}}^I(\Lambda_b^0 \rightarrow \Sigma'^- K^+) \end{aligned}$$

- Several other relations possible, see [Phys.Rev.D 102 \(2020\) 5, 053007](#)
- All the relations in case of  $B_b(\bar{3}) \rightarrow \mathcal{O}(8)\mathcal{M}(8)$  transition can be derived using  $U$ -spin symmetry.

## $B_b(\bar{3}) \rightarrow \mathcal{O}(8)\mathcal{M}(8)$

$$\begin{aligned} \delta_{\text{CP}}^I(\Lambda_b^0 \rightarrow \Sigma^- K^+) &= -\delta_{\text{CP}}^I(\Xi_b^0 \rightarrow \Xi^- \pi^+), \\ \delta_{\text{CP}}^I(\Lambda_b^0 \rightarrow \rho^+ \pi^-) &= -\delta_{\text{CP}}^I(\Xi_b^0 \rightarrow \Sigma^+ K^-), \\ \delta_{\text{CP}}^I(\Xi_b^- \rightarrow n K^-) &= -\delta_{\text{CP}}^I(\Xi_b^- \rightarrow \Xi^0 \pi^-), \\ \delta_{\text{CP}}^I(\Xi_b^- \rightarrow \Xi^- K^0) &= -\delta_{\text{CP}}^I(\Xi_b^- \rightarrow \Sigma^- \bar{K}^0), \\ \delta_{\text{CP}}^I(\Xi_b^0 \rightarrow \Xi^- K^+) &= -\delta_{\text{CP}}^I(\Lambda_b^0 \rightarrow \Sigma^- \pi^+), \\ \delta_{\text{CP}}^I(\Xi_b^0 \rightarrow \Sigma^- \pi^+) &= -\delta_{\text{CP}}^I(\Lambda_b^0 \rightarrow \Xi^- K^+), \\ \delta_{\text{CP}}^I(\Xi_b^0 \rightarrow \Sigma^+ \pi^-) &= -\delta_{\text{CP}}^I(\Lambda_b^0 \rightarrow \rho^+ K^-), \\ \delta_{\text{CP}}^I(\Xi_b^0 \rightarrow n \bar{K}^0) &= -\delta_{\text{CP}}^I(\Lambda_b^0 \rightarrow \Xi^0 K^0), \\ \delta_{\text{CP}}^I(\Xi_b^0 \rightarrow \rho^+ K^-) &= -\delta_{\text{CP}}^I(\Lambda_b^0 \rightarrow \Sigma^+ \pi^-), \\ \delta_{\text{CP}}^I(\Xi_b^0 \rightarrow \Xi^0 K^0) &= -\delta_{\text{CP}}^I(\Lambda_b^0 \rightarrow n \bar{K}^0), \end{aligned}$$

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# Future directions

- Conclusive measurement of  $CP$ -violation in  $b$ -baryon decays.
- Study  $SU(3)$ -breaking effects in two body decays of  $b$ -baryons.
- Identify the intermediate charmless states that lead to common multibody electrically charged final states.
- Analyze the angular distribution of final states to isolate individual partial wave contributions to the total  $CP$  asymmetry.



Stay tuned for updated results from LHCb

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