

# Measurements of the top quark mass at the ILC

**Snowmass EF04 meeting November 20th 2020**

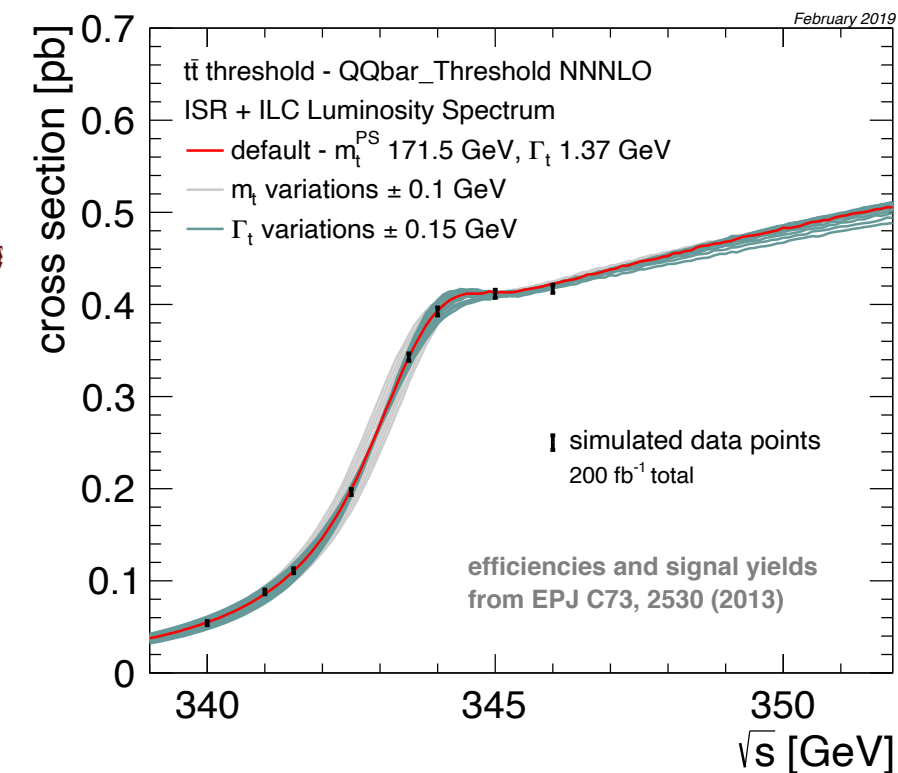
# Top Mass Measurements in $e^+e^-$ Colliders

## Overview

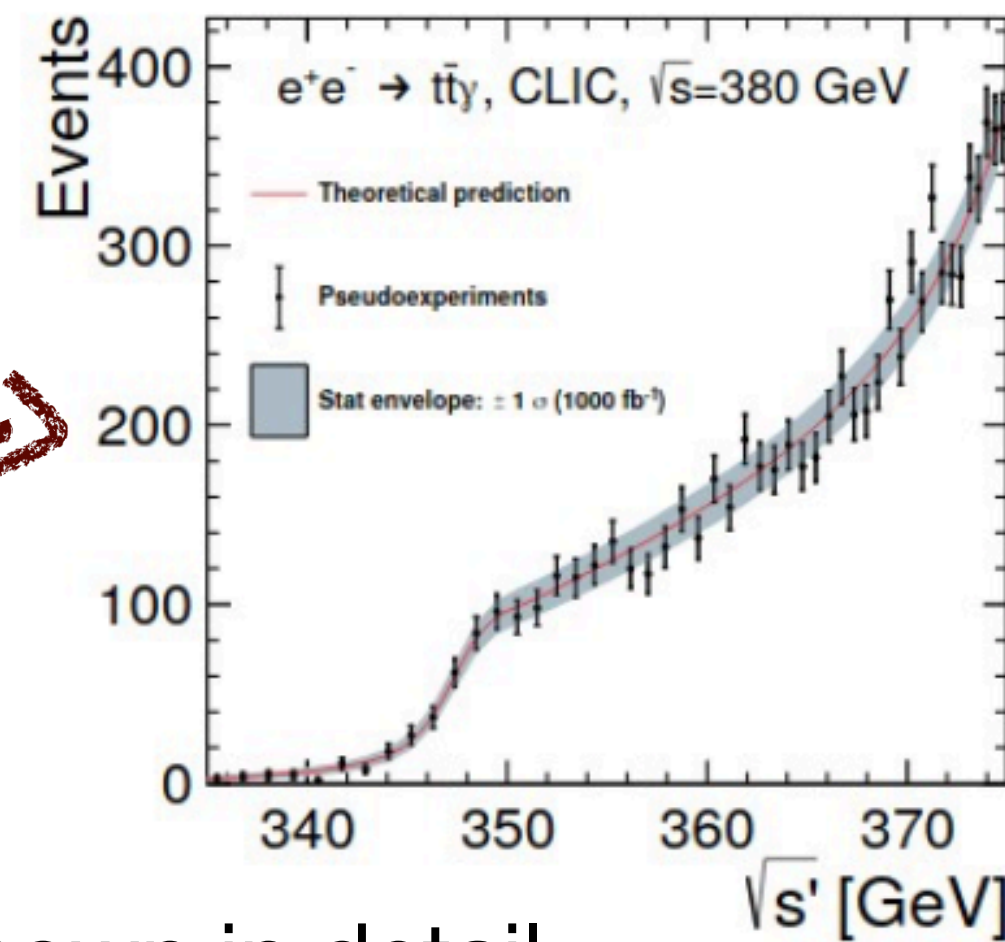
- The accelerator side: Requires sufficient collision energy for top pair production
  - So far thoroughly studied for ILC, CLIC, some derivative studies for FCCee

Three approaches to the top mass

The threshold scan around 350 GeV

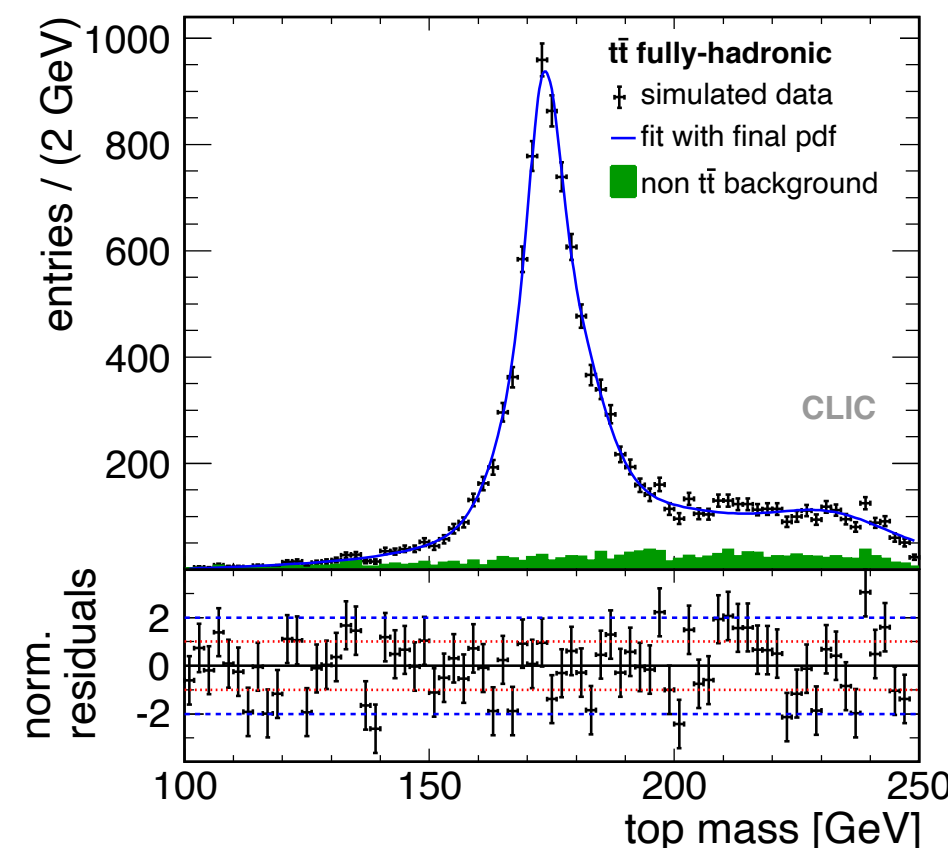


The top mass from radiative events



not shown in detail,  
stat:  $\sim 20 - 40$  MeV

Direct kinematic reconstruction



Key references:

EPJ C73, 2530 (2013)  
(CLIC, (ILC): Threshold, direct)

JHEP 11, 003 (2019)  
(CLIC: Threshold, radiative, direct)

PLB 804, 135353 (2020)  
(ILC, CLIC: radiative)

+ a rich set of reports and conference proceedings on arXiv



This talk includes material from the following people:

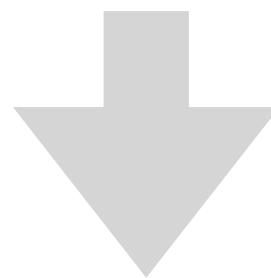
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## Top Mass from Radiative Events

PhD Thesis of M. Boronat and P. Gomis

Together with J.Fuster, M. Perello, M. Vos, E. Fullana from Valencia group

Theoretical framework: A. H. Hoang, V. Mateu, A. Widl,



Physics Letters B 804 (2020) 135353

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Physics Letters B

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### Top quark mass measurement in radiative events at electron-positron colliders

M. Boronat<sup>a</sup>, E. Fullana<sup>a</sup>, J. Fuster<sup>a</sup>, P. Gomis<sup>a,\*</sup>, A.H. Hoang<sup>b,c</sup>, A. Widl<sup>b</sup>, V. Mateu<sup>d,e</sup>, M. Vos<sup>a</sup>

<sup>a</sup> Institut de Física Corpuscular (Universitat de València/CSIC), c/ Catedrático J. Beltrán, 46980 Paterna, Valencia, Spain  
<sup>b</sup> University of Vienna, Faculty of Physics, Boltzmanngasse 5, 1090 Vienna, Austria  
<sup>c</sup> Erwin Schrödinger International Institute for Mathematical Physics, Austria  
<sup>d</sup> Departamento de Física Fundamental e IUFFyM, Universidad de Salamanca, Plaza de la Merced s/n, 37008 Salamanca, Spain  
<sup>e</sup> Instituto de Física Teórica UAM-CSIC, Spain

arXiv:1902.07246v2 [hep-ex] 22 May 2020

## Scanning Strategies at the Top Threshold at ILC

Frank Simon

Max-Planck-Institut für Physik, Munich, Germany

E-mail: [fsimon@mpp.mpg.de](mailto:fsimon@mpp.mpg.de)

ABSTRACT: A scan of the top quark pair production threshold at a future electron-positron collider provides the possibility for high-precision measurements of the top quark mass, and, when using two dimensional fits of the measured cross sections, also of other properties such as the width and the Yukawa coupling. The energy range of the scan and the distribution of the integrated luminosity can be optimized depending on the main goals of the threshold program. This contribution examines the possibility to determine the top quark mass in fast exploratory measurements with an adequate precision to enable such an optimization, and studies a scanning program with a reduced energy range of 6 GeV for the measurement of the mass, width and the Yukawa coupling, taking theoretical uncertainties from QCD scale variations and parametric uncertainties from the strong coupling constant into account.



Eur. Phys. J. C (2013) 73:2530  
DOI 10.1140/epjc/s10052-013-2530-7

Special Article - Tools for Experiment and Theory

THE EUROPEAN  
PHYSICAL JOURNAL C

## Top quark mass measurements at and above threshold at CLIC

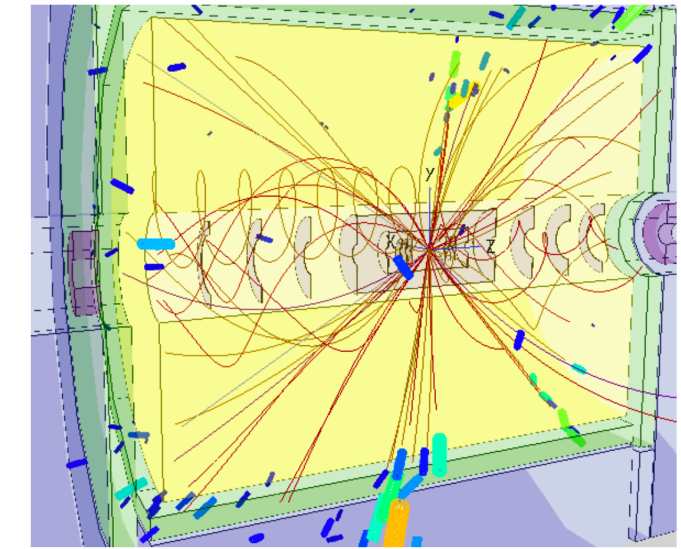
Katja Seidel<sup>1</sup>, Frank Simon<sup>1,a</sup>, Michal Tesař<sup>1</sup>, Stephane Poss<sup>2</sup>

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<sup>2</sup>CERN, 1211 Geneva, Switzerland

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Optimising top-quark pair-production threshold scan at future e+e- colliders



ILD Top/HF group meeting, November 13, 2020




Kacper Nowak, Aleksander Filip Żarnecki

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Plus the following papers :

(<https://arxiv.org/pdf/hep-ph/0207315>, <https://arxiv.org/pdf/1310.0563>, <https://arxiv.org/pdf/1604.08122>)

Let's start with:

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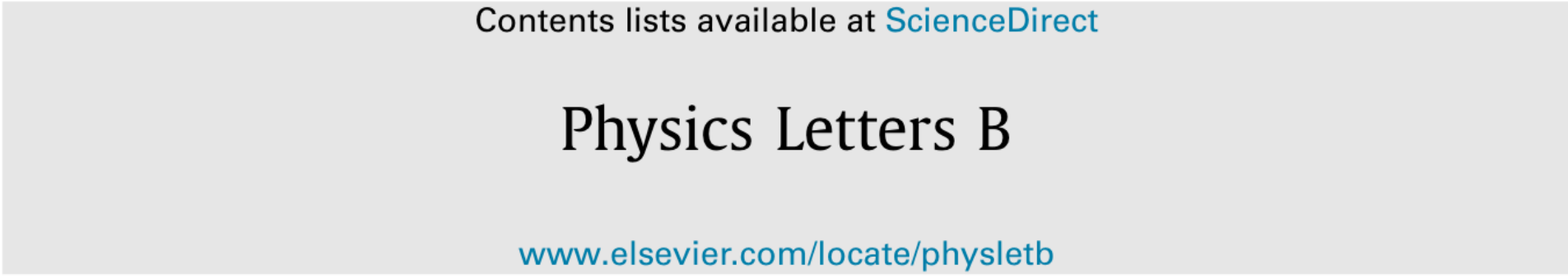

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PLB 804,135353 (2020)

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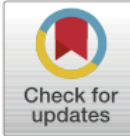
  

Physics Letters B

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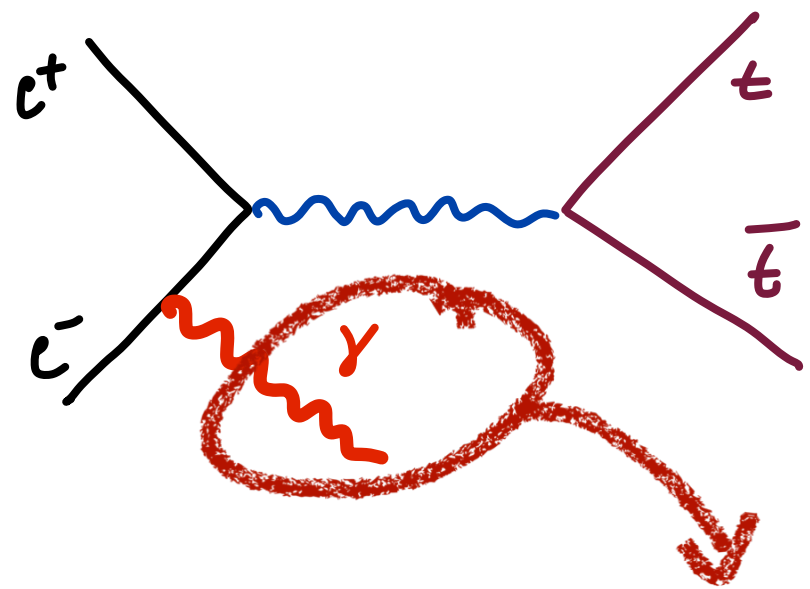
...because also in the lifetime of the ILC would be convenient to start with this measurement of the top-quark mass



# Mass from Radiative Events

At CLIC, ILC - 380 and 500 GeV

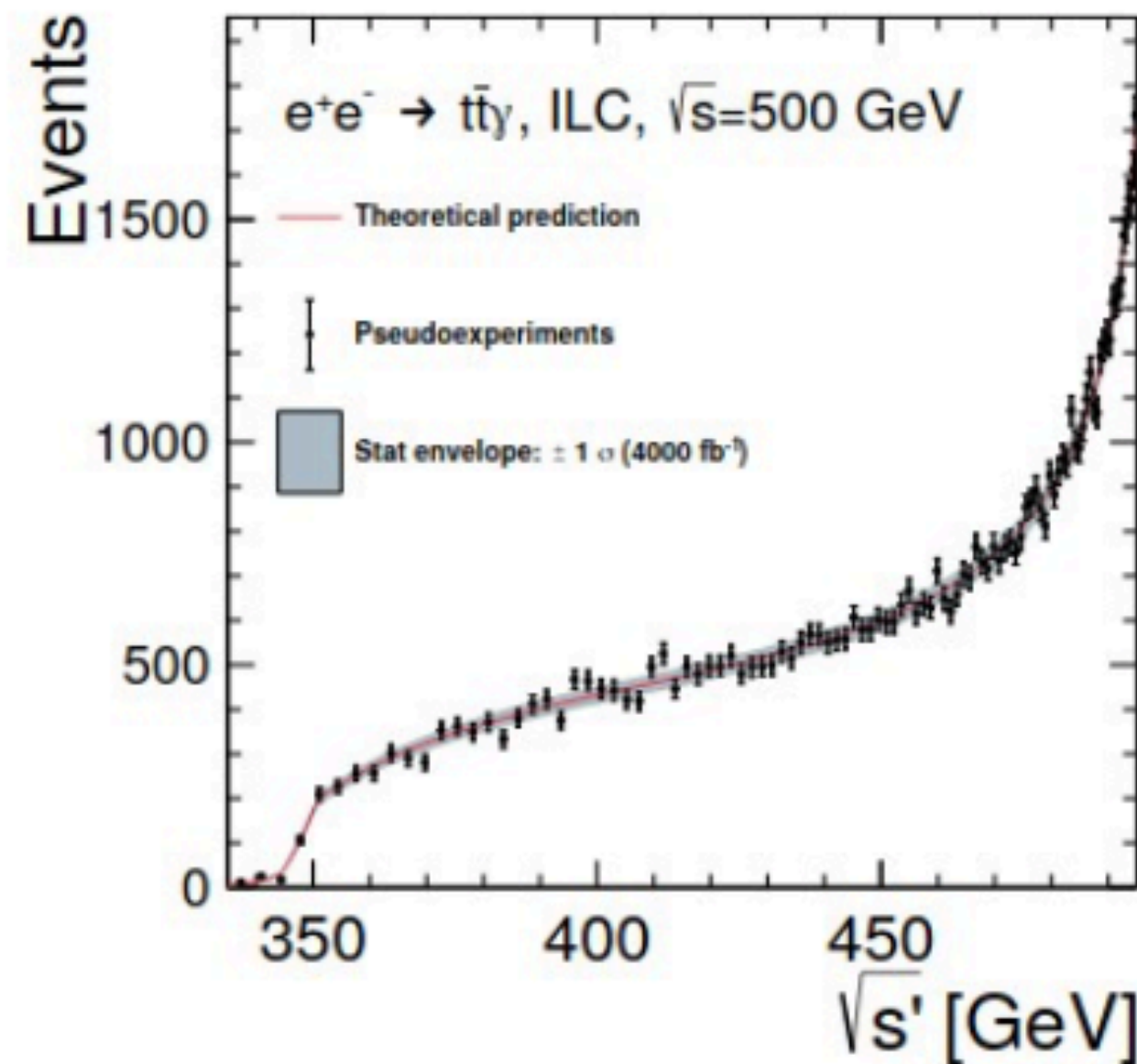
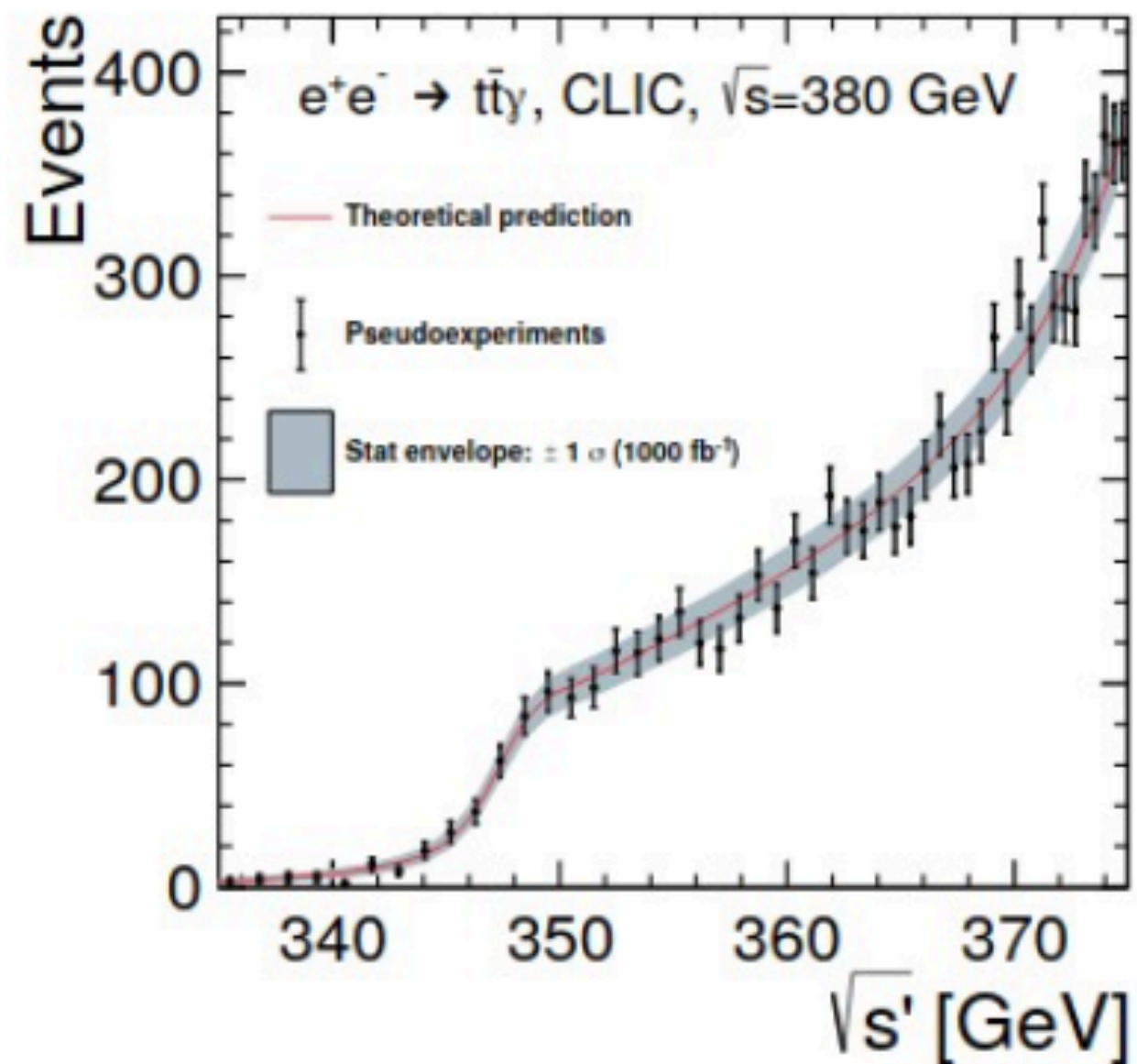
- A new(er) idea to measure the top mass in a theoretically well-defined scheme in high-energy running above the threshold



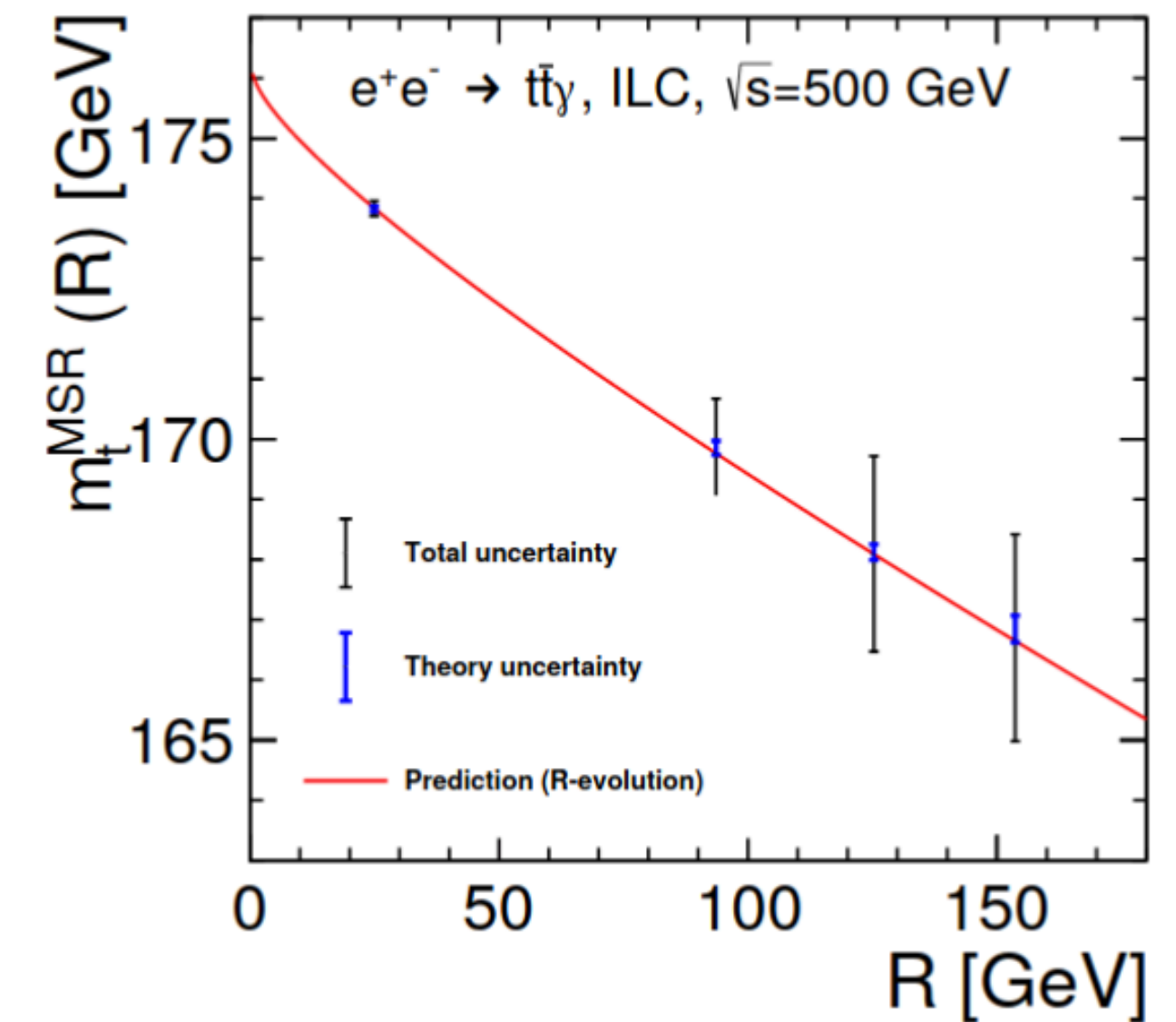
matched NNLO + NNLL calculation,  
luminosity spectrum folded in explicitly;  
Extraction of short distance MSR mass

The expected uncertainty on the top  $\overline{MS}$  mass

cms energy	CLIC, $\sqrt{s} = 380$ GeV		ILC, $\sqrt{s} = 500$ GeV	
	500	1000	500	4000
statistical	140 MeV	90 MeV	350 MeV	110 MeV
theory	46 MeV		55 MeV	
lum. spectrum	20 MeV		20 MeV	
photon response	16 MeV		85 MeV	
total	150 MeV	110 MeV	360 MeV	150 MeV



can provide  $5\sigma$  evidence for scale evolution (“running”) of the top quark MSR mass from ILC500 data alone



... and now that we have the top-quark mass in the  
~100MeV ballpark we can move to

## Scanning Strategies at the Top Threshold at ILC

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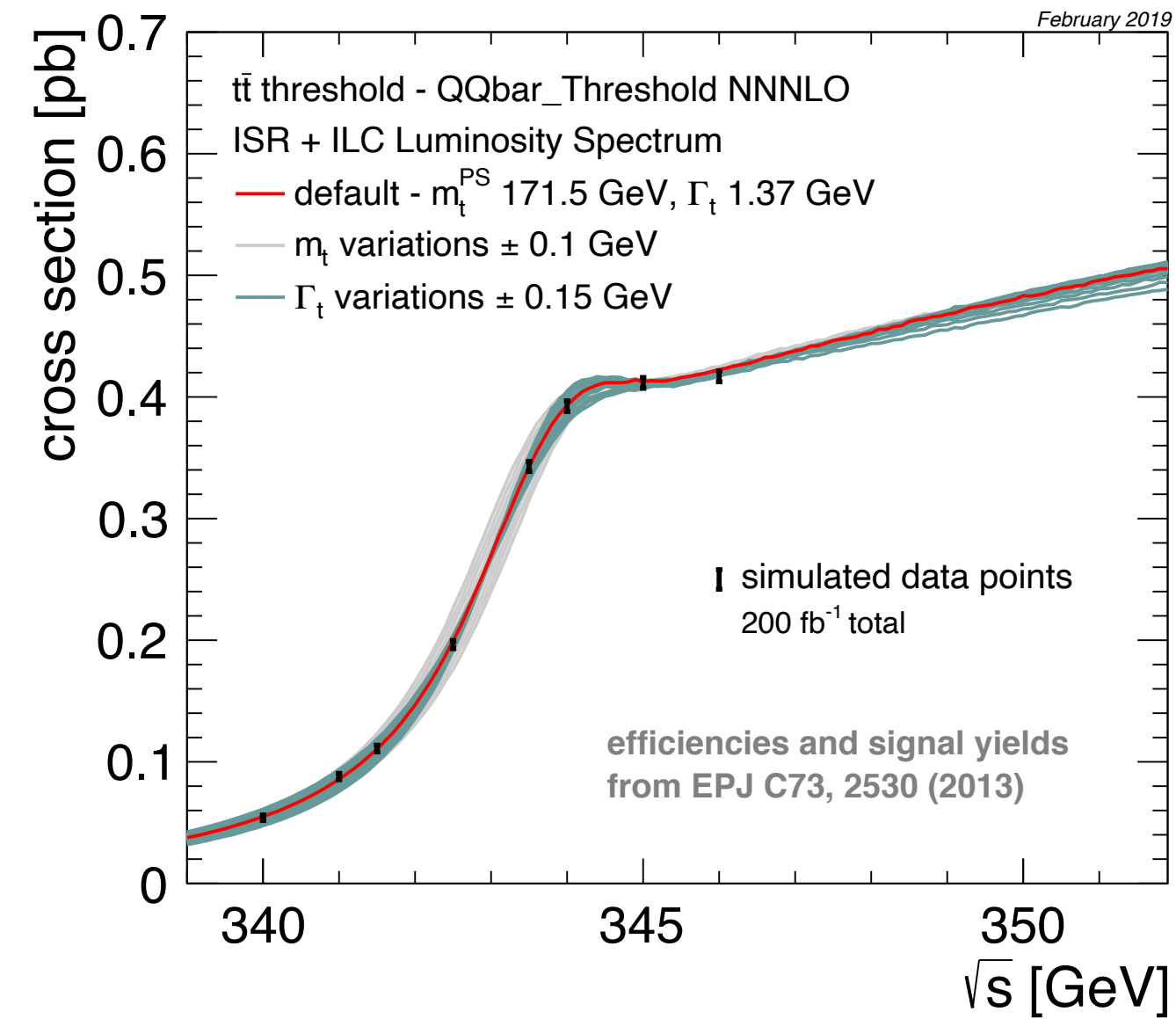
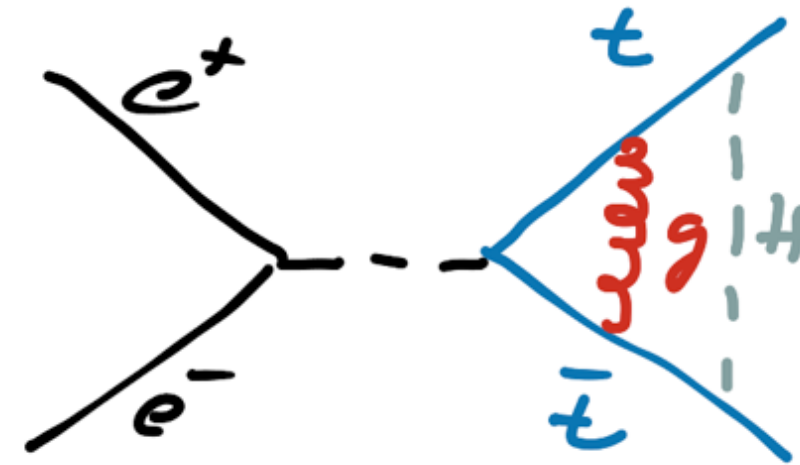
+ a rich set of reports and  
conference proceedings on arXiv



# Mass at the Threshold

At CLIC, ILC, FCCee

- The top threshold provides excellent sensitivity to the mass and other top quark properties
- Measurement of the top quark mass in theoretically well-defined mass schemes



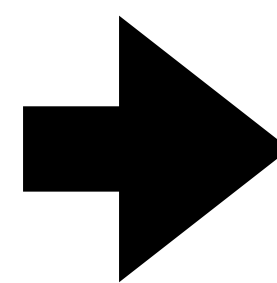
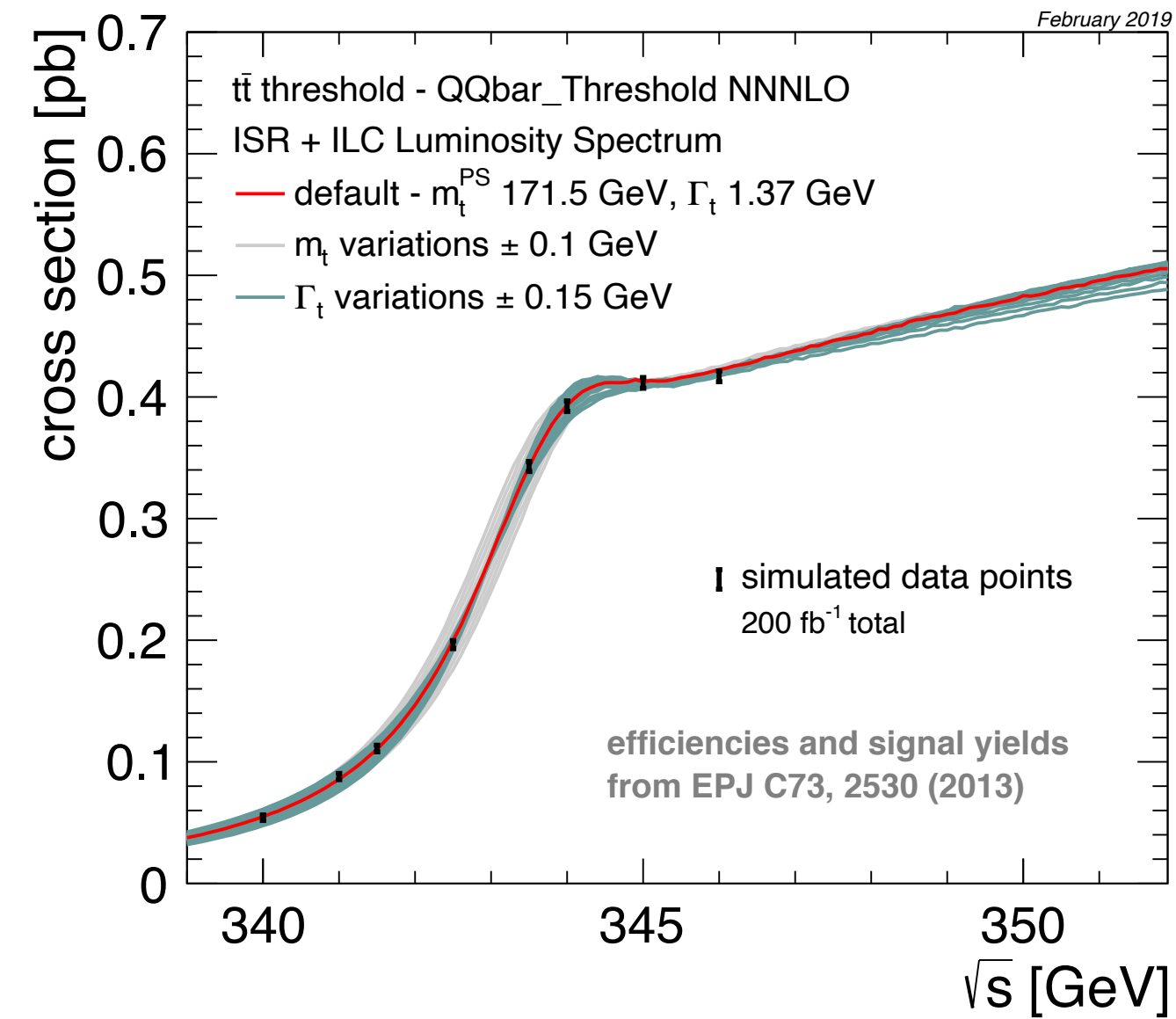
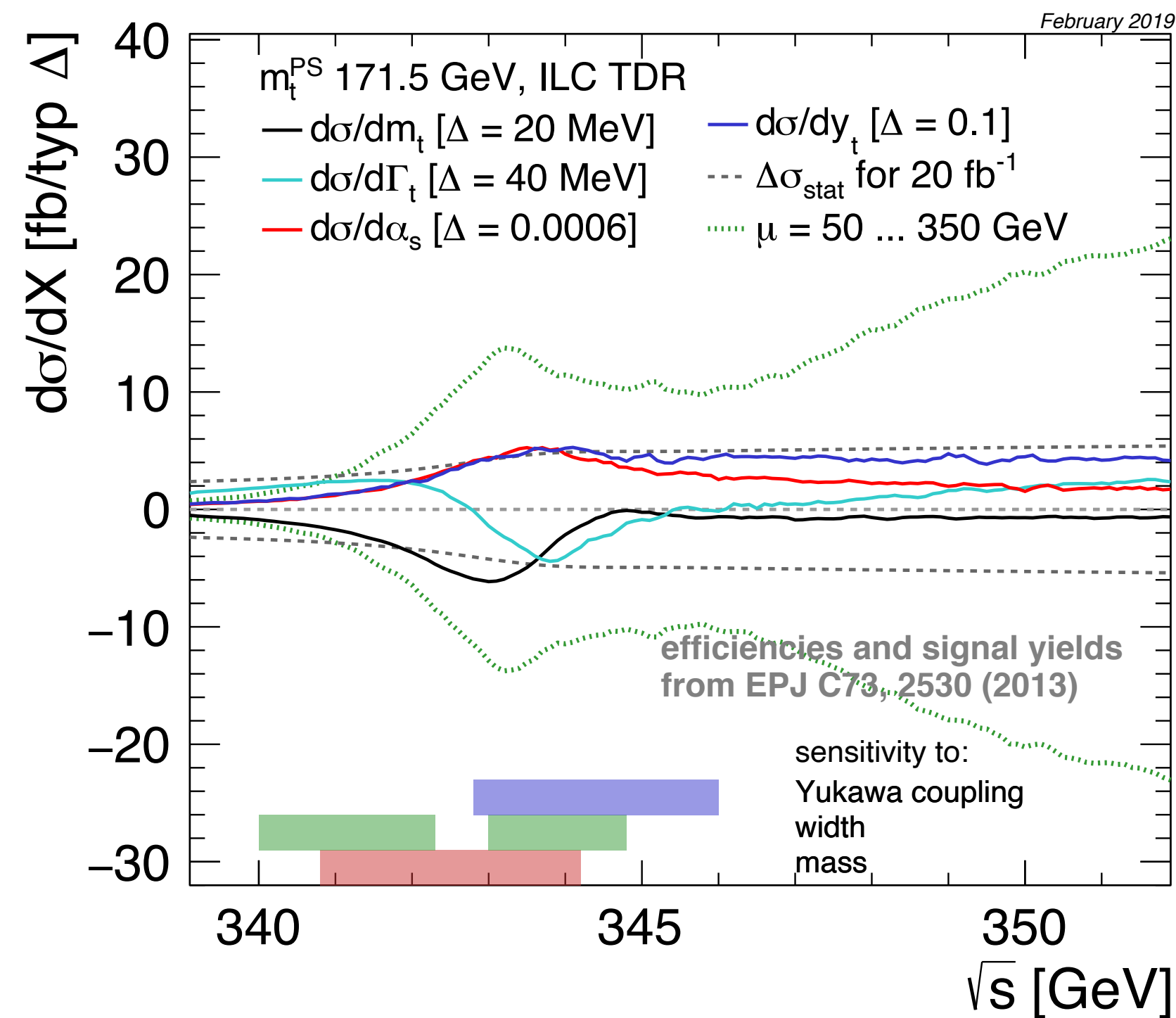
- Assuming an integrated luminosity of  $200 \text{ fb}^{-1}$  (default for ILC, FCCee, x2 of CLIC standard scenario - 10 points spaced by 1 GeV)

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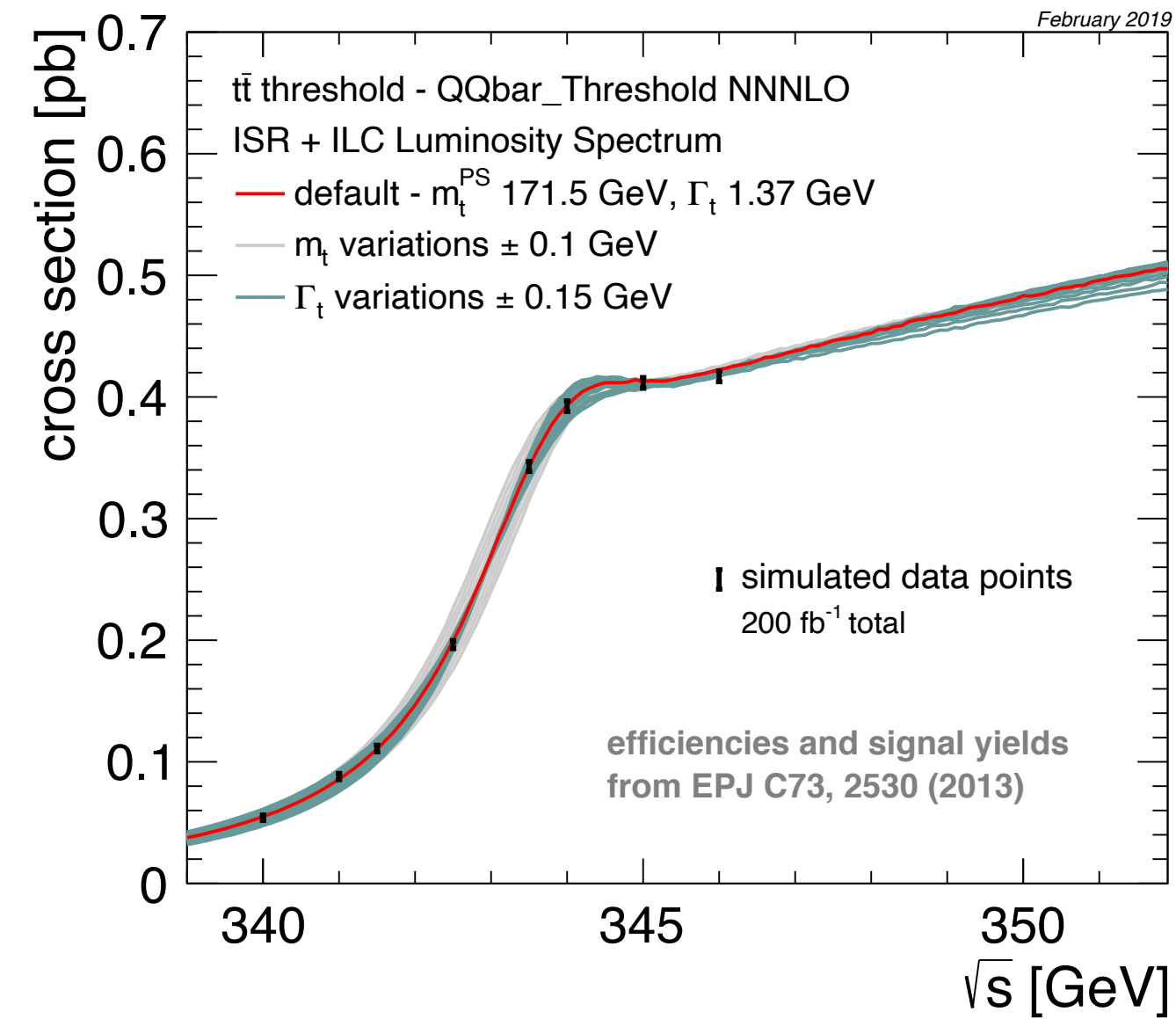
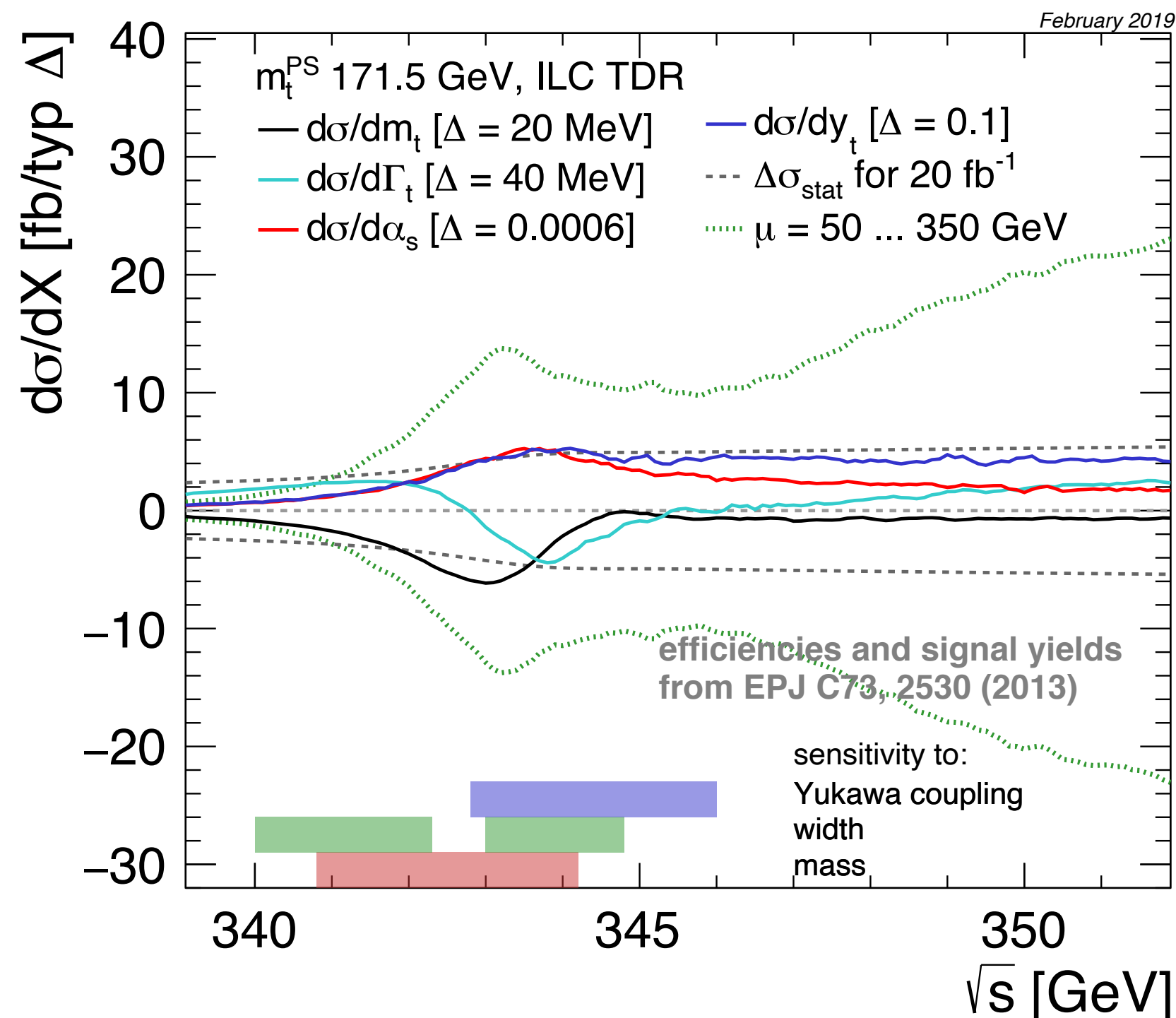
- Sensitivity to :
  - Top-quark mass
  - Top-quark width
  - Yukawa coupling
  - Strong coupling constant



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- Sensitivity to :
  - Top-quark mass
  - Top-quark width
  - Yukawa coupling
  - Strong coupling constant

So we are going to assume three scenarios

# Scenario 1 : We fit all

## float top quark mass, width, Yukawa coupling and alpha\_s

arXiv:hep-ph/0207315v2 23 Oct 2002

Multi-parameter fits to the  $t\bar{t}$  threshold observables at a future  $e^+e^-$  linear collider

Manel Martinez<sup>a</sup>, Ramon Miquel<sup>b</sup>

<sup>a</sup> *Institut de Física d'Altes Energies, Univ. Aut. de Barcelona  
E-08390 Bellaterra (Barcelona) Spain*

<sup>b</sup> *Lawrence Berkeley National Laboratory, Physics Division  
1 Cyclotron Road, Berkeley, CA 94720, USA*

November 1, 2018

- Assumes an integrated luminosity of  $300 \text{ fb}^{-1}$  (10 points)
- Assumes  $M(\text{Higgs}) = 120 \text{ GeV}$
- TESLA beam conditions
- Theoretical error normalisation  $\sim 1\%$
- 3 observables : XS, momentum distribution and F-B asym.
- But XS is dominant

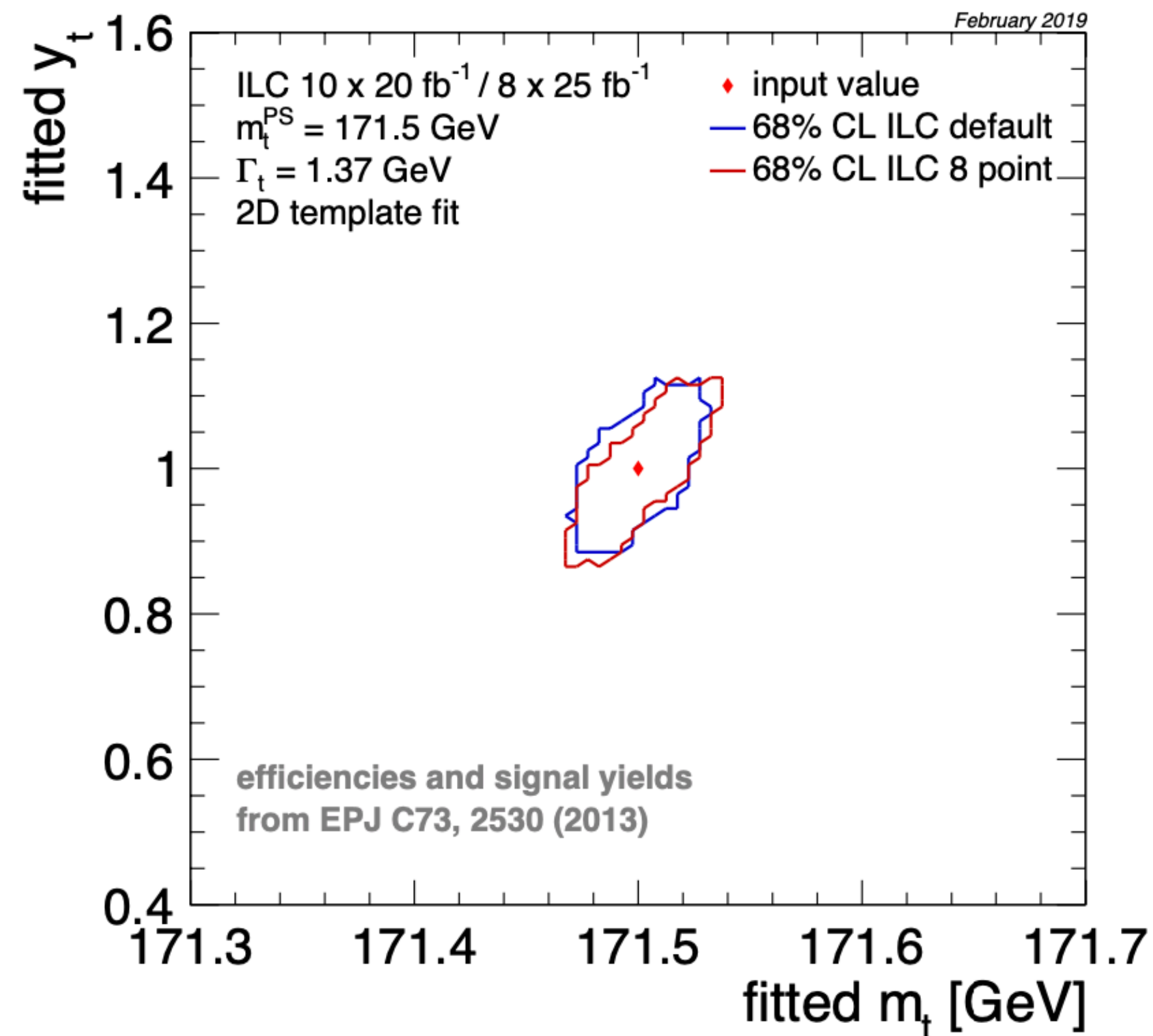
$$\begin{aligned} \Delta m_t &= 31 \text{ MeV} & \Delta \alpha_s &= 0.001 \text{ (constraint)} \\ \Delta \Gamma_t &= 34 \text{ MeV} & \frac{\Delta \lambda_t}{\lambda_t} &= \begin{matrix} +0.35 \\ -0.65 \end{matrix} . \end{aligned}$$

This scenario will be revisited in the last part of the talk



# Scenario 2 : We fit the mass and the coupling

fit the Yukawa coupling, floating the mass, but not the width. Vary  $\alpha_s$  within some uncertainty.



parameter	8 point scan		10 point scan	
2D fit $m_t$ and $y_t$			marg.	marg.
$m_t$	$(\pm 35_{(\text{stat})} \pm 45_{(\text{theo})}) \text{ MeV}$		17.0 MeV	$(^{+34}_{-31}_{(\text{stat})} \pm 42_{(\text{theo})}) \text{ MeV}$
$y_t$	$^{+0.120}_{-0.140}_{(\text{stat})} \pm 0.09_{(\text{theo})}$		0.055	$^{+0.128}_{-0.112}_{(\text{stat})} \pm 0.132_{(\text{theo})}$

Yukawa coupling current (pdg) value(\*) :  $1.07^{+0.34}_{-0.43}$

Prospects after the ILC@500GeV run ( $1\text{ab}^{-1}$ ) set at the 10% ballpark.

(\*) ratio wrt the SM predicted value

# Scenario 3 : We fit only the mass

extraction of the top mass assuming the SM: fix width to SM prediction, fix  $y_t = 1$ . Vary  $\alpha_s$  within some uncertainty.

error source	$\Delta m_t^{\text{PS}}$ [MeV]
stat. error (200 fb <sup>-1</sup> )	13
theory (NNNLO scale variations, PS scheme)	40
parametric ( $\alpha_s$ , current WA)	35
non-resonant contributions (such as single top)	< 40
residual background / selection efficiency	10 – 20
luminosity spectrum uncertainty	< 10
beam energy uncertainty	< 17
combined theory & parametric	30 – 50
combined experimental & backgrounds	25 - 50
total (stat. + syst.)	40 – 75

- Detailed evaluation of systematic uncertainties
- 8 points configuration for this uncertainty
- Theory dominated (~40MeV vs ~10MeV); assuming a N4LO available for 2040 expect further reductions

For other configurations of the scan points :

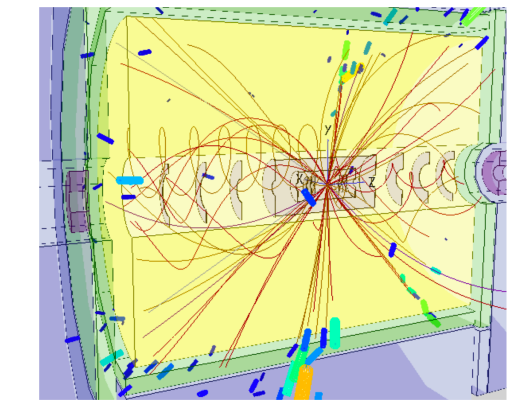
parameter	8 point scan	10 point scan
1D fit		
$m_t$	$(\pm 10.3_{\text{(stat)}} \pm 44_{\text{(theo)}})$ MeV	$(12.2_{\text{(stat)}} \pm 40_{\text{(theo)}})$ MeV



# Scenario 1 revisited

## Studies done by Kacper Nowak and Filip Zarnecki

Optimising top-quark pair-production threshold scan at future e+e- colliders



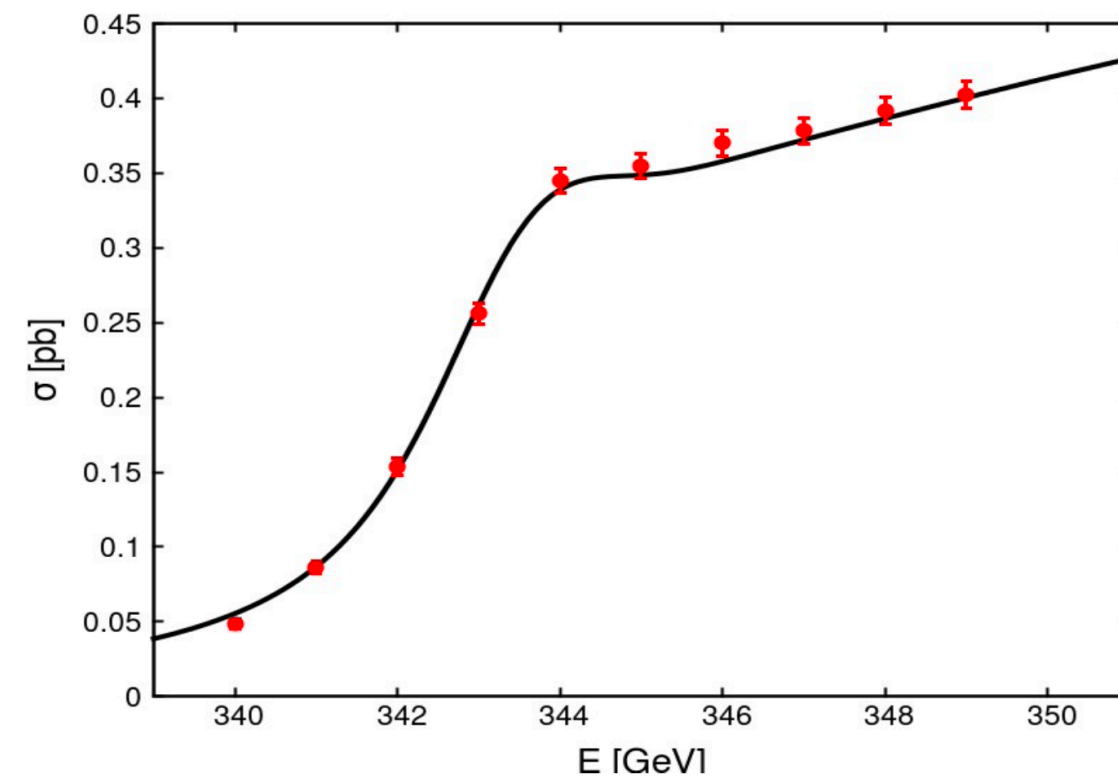
ILD Top/HF group meeting, November 13, 2020

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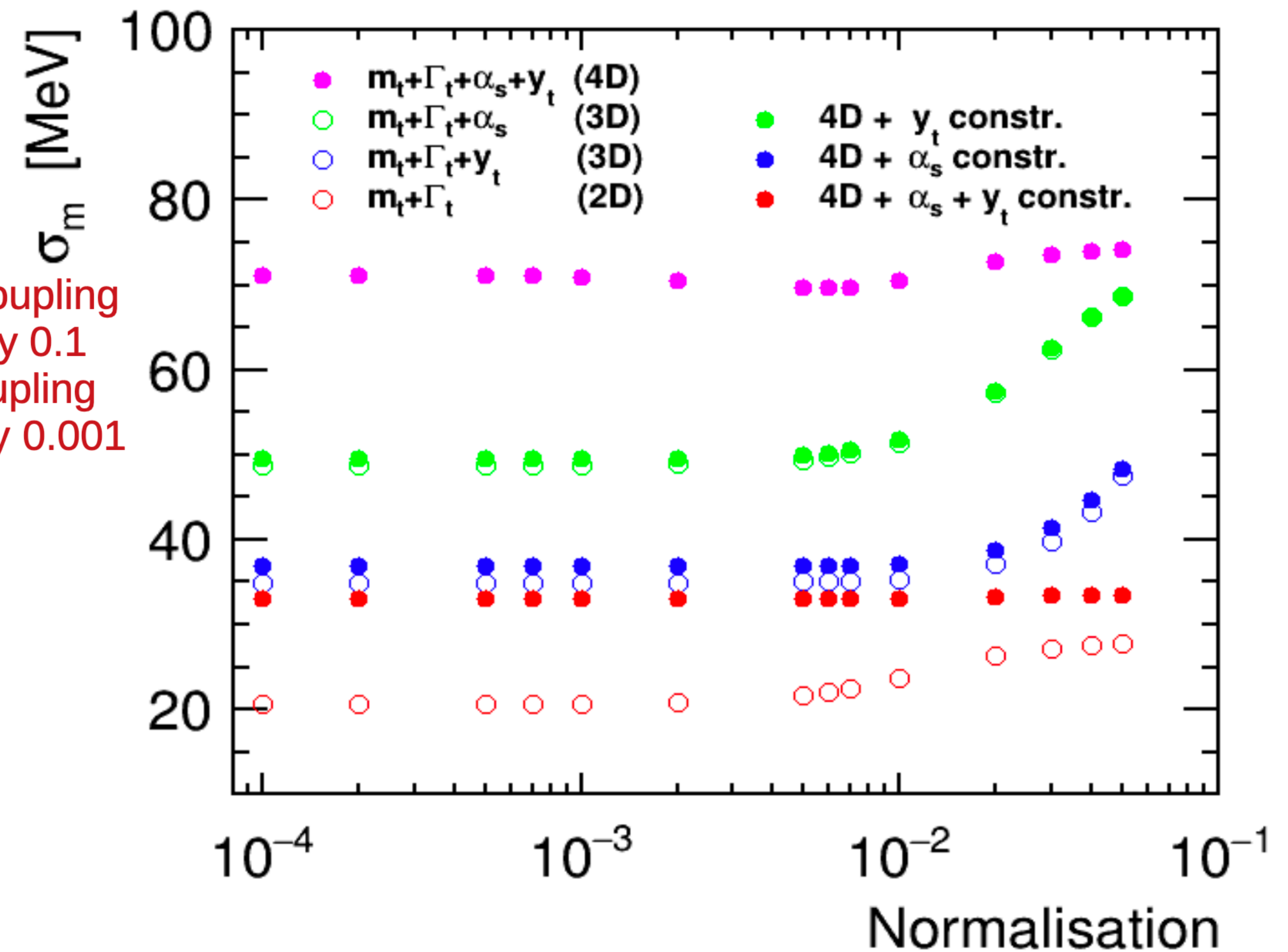
results for the benchmark scenario

Assume 10 measurements at the threshold, with 1 GeV step in energy, with  $10 \text{ fb}^{-1}$  taken at each energy point ( $100 \text{ fb}^{-1}$  total).



Generate statistical fluctuation assuming 70.2% event reconstruction efficiency and background level (remaining after cuts) corresponding to the 73 fb

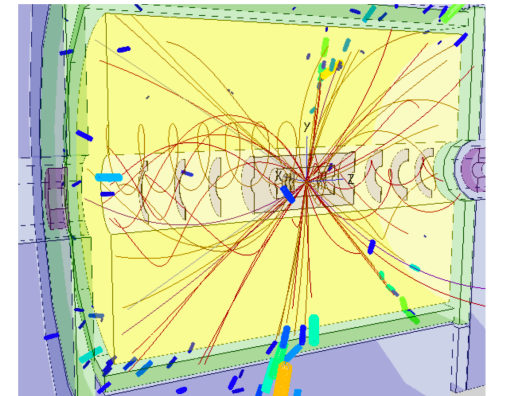
Yukawa coupling  
Uncertainty 0.1  
Strong coupling  
uncertainty 0.001



# Optimisations (based on the genetic algorithm)

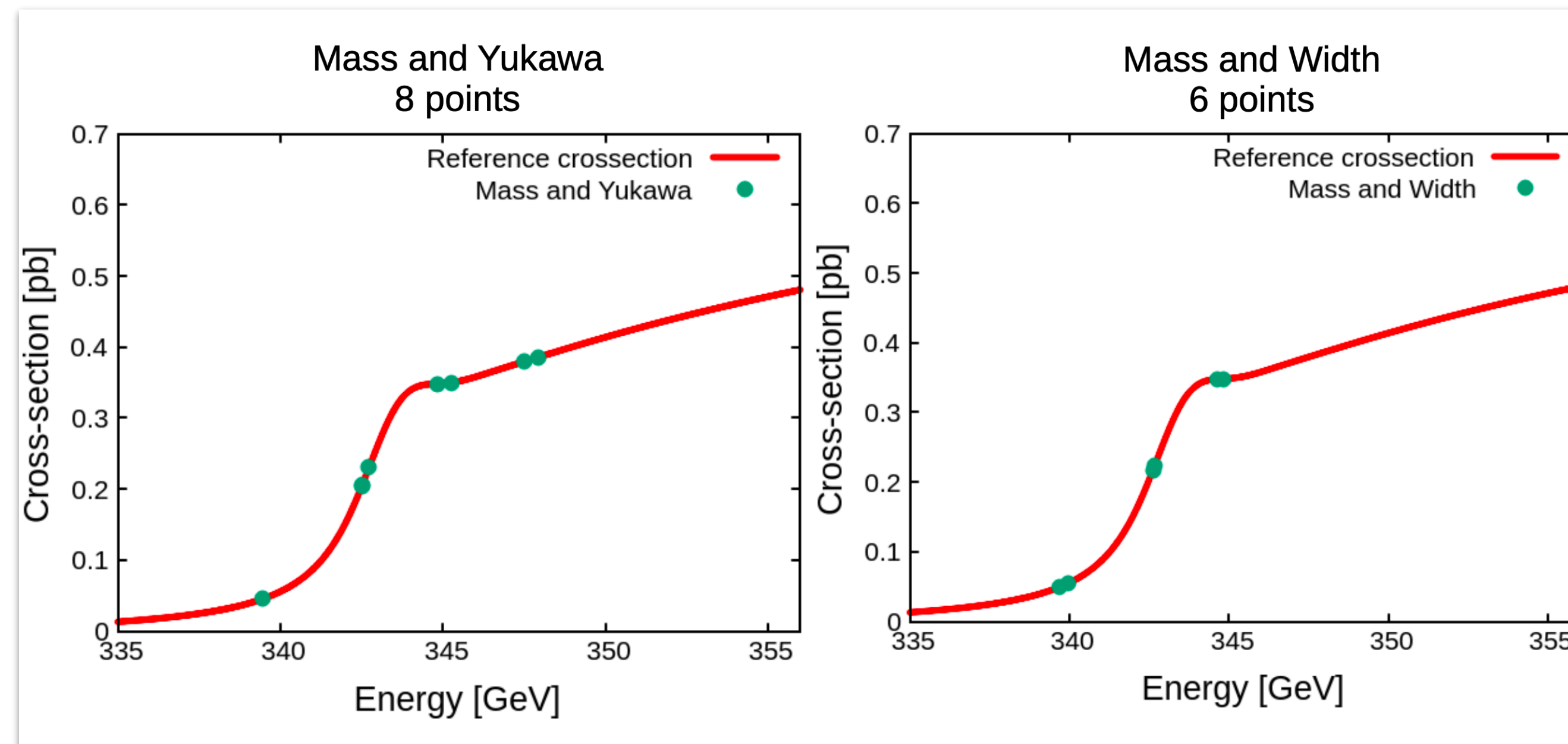
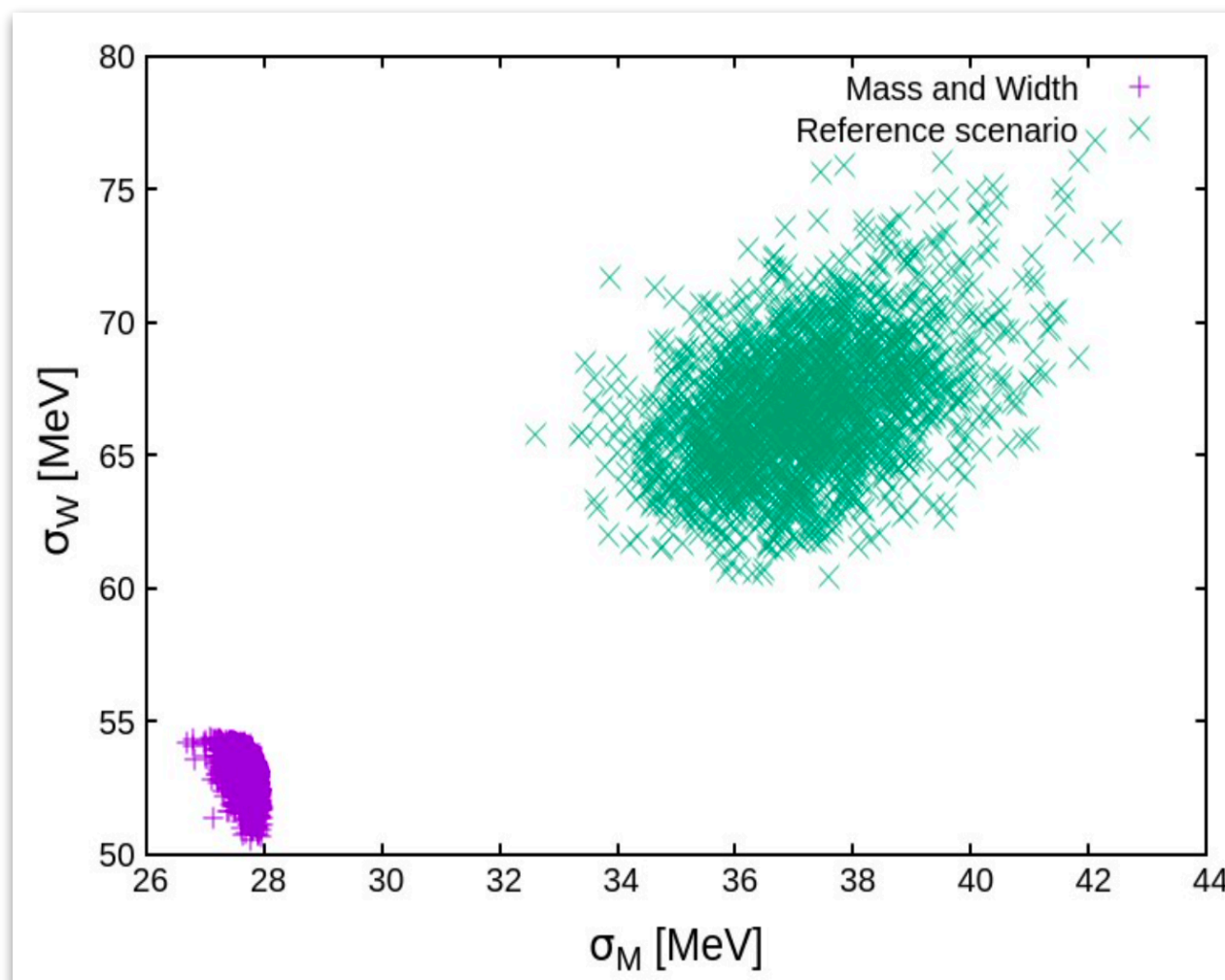
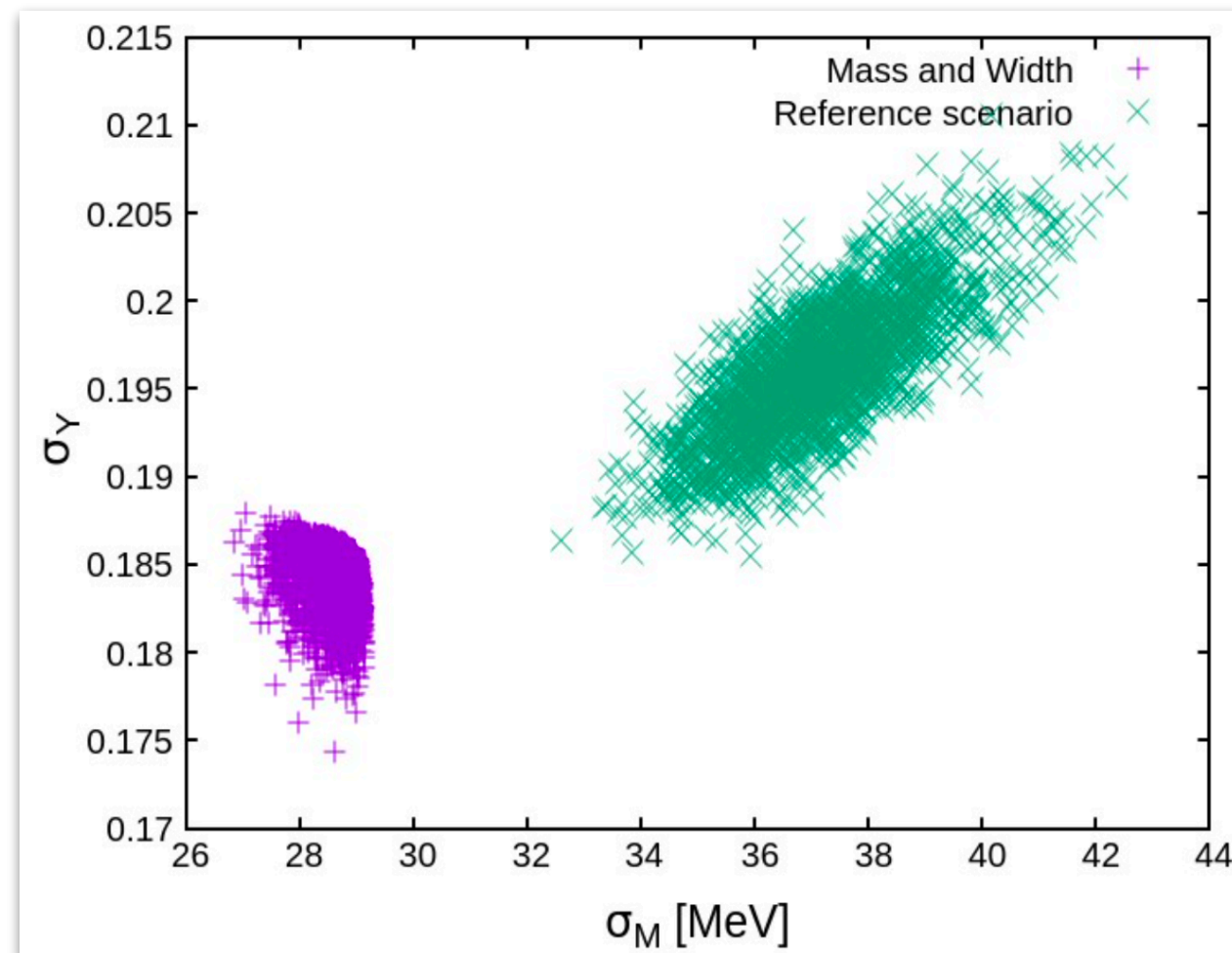
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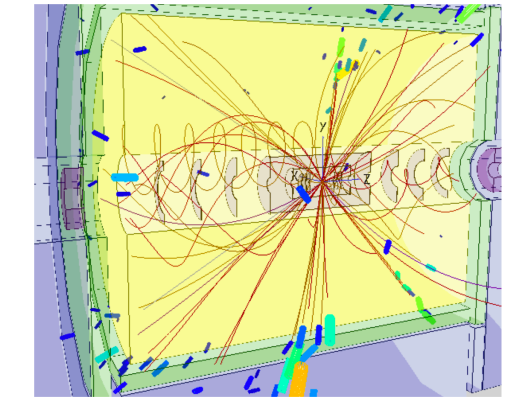




# Optimisations (based on the genetic algorithm)

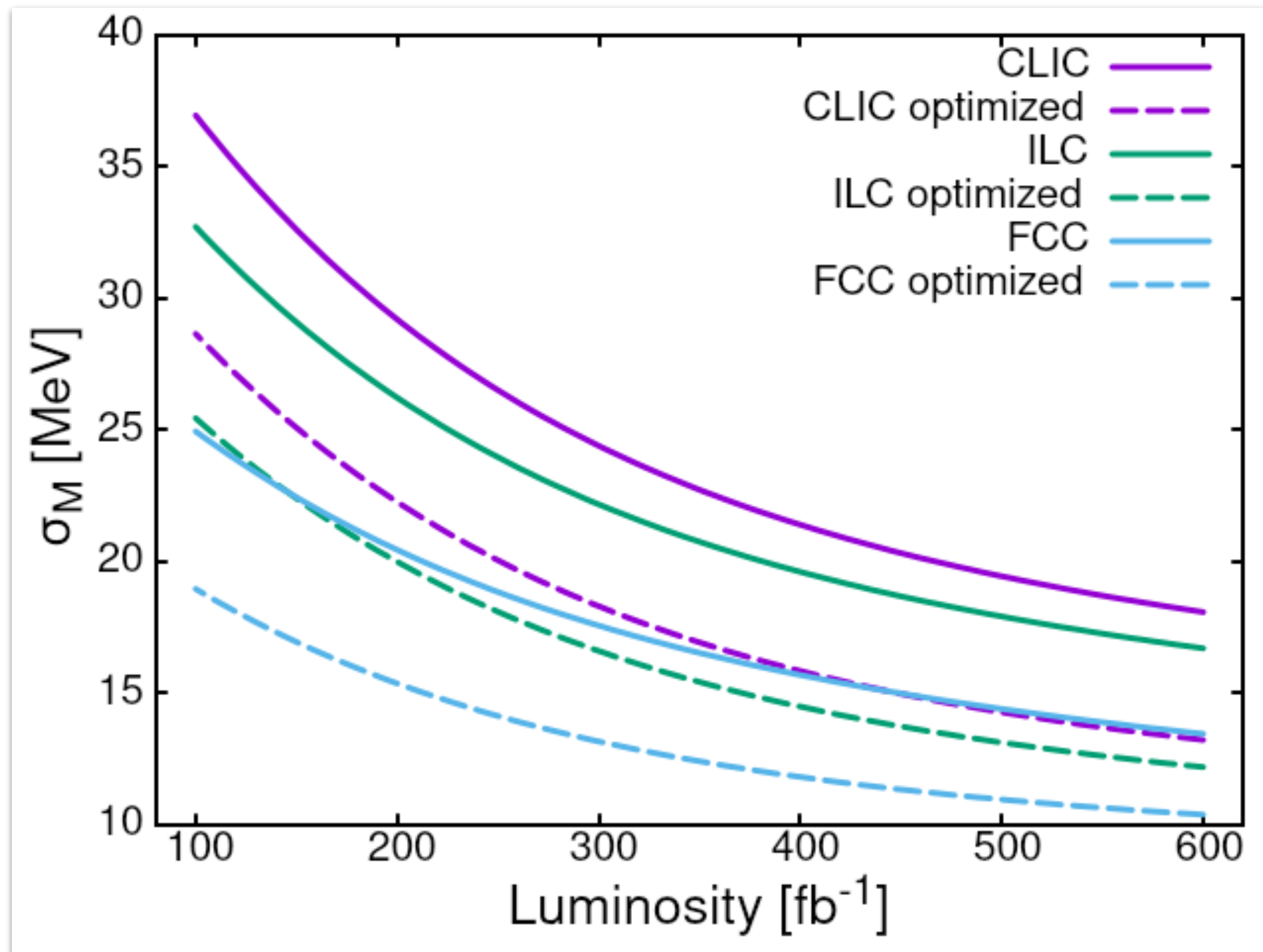
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Statistical uncertainty of the extracted top-quark mass can be reduced by ~25%, without losing precision in width or Yukawa determination

# Summary

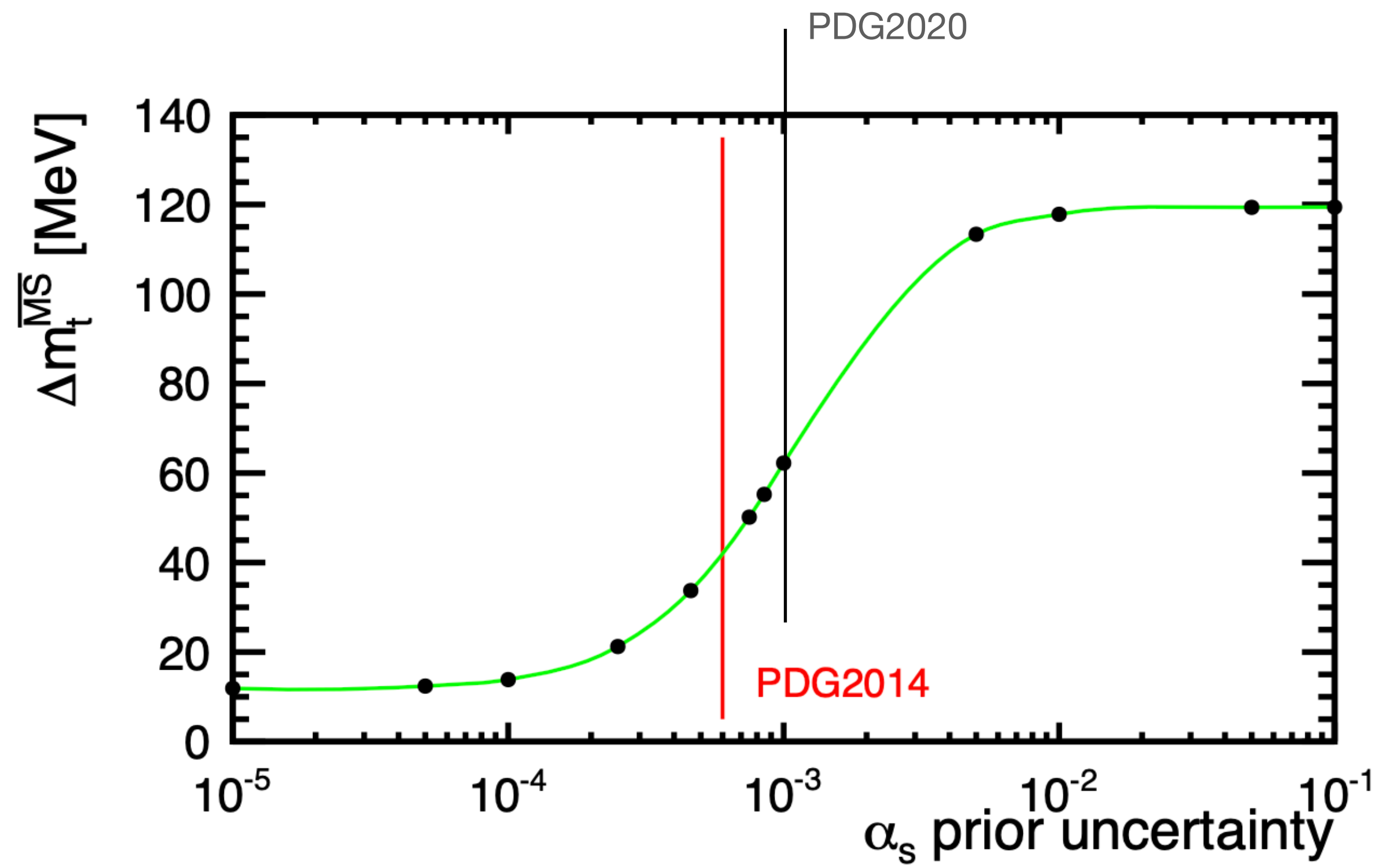
- Current precision  $\sim 50\text{MeV}$  dominated by theoretical uncertainty
- Possibility to measure other parameters : width, strong coupling and Yukawa
  - To be decided after the ILC@500GeV run
- Room for optimisation and the optimisation depends on the parameters we want to aim



**the end**

# Dependency with Alpha\_s

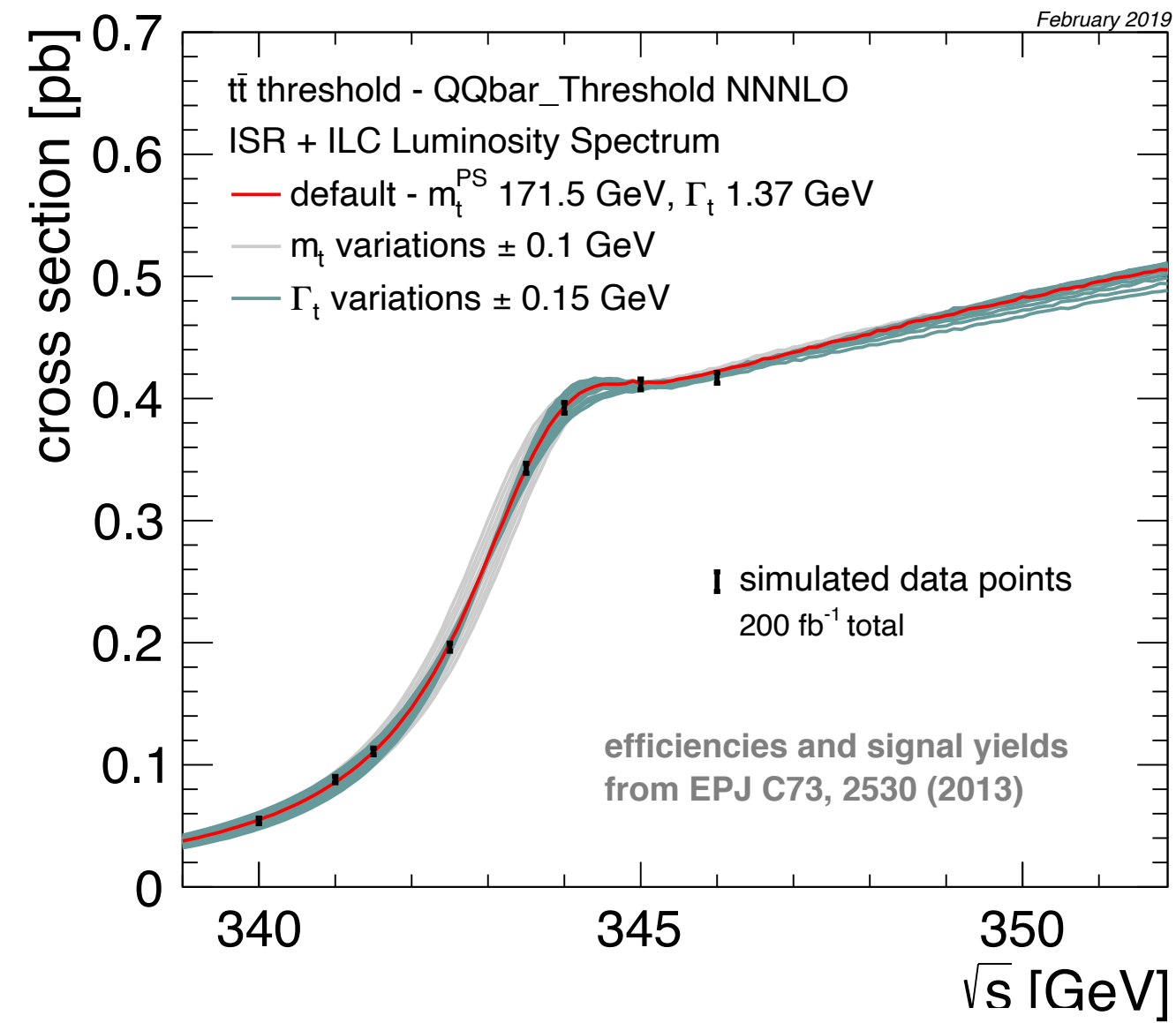
Taken from [arXiv:1604.08122v1 \[hep-ex\]](https://arxiv.org/abs/1604.08122v1)



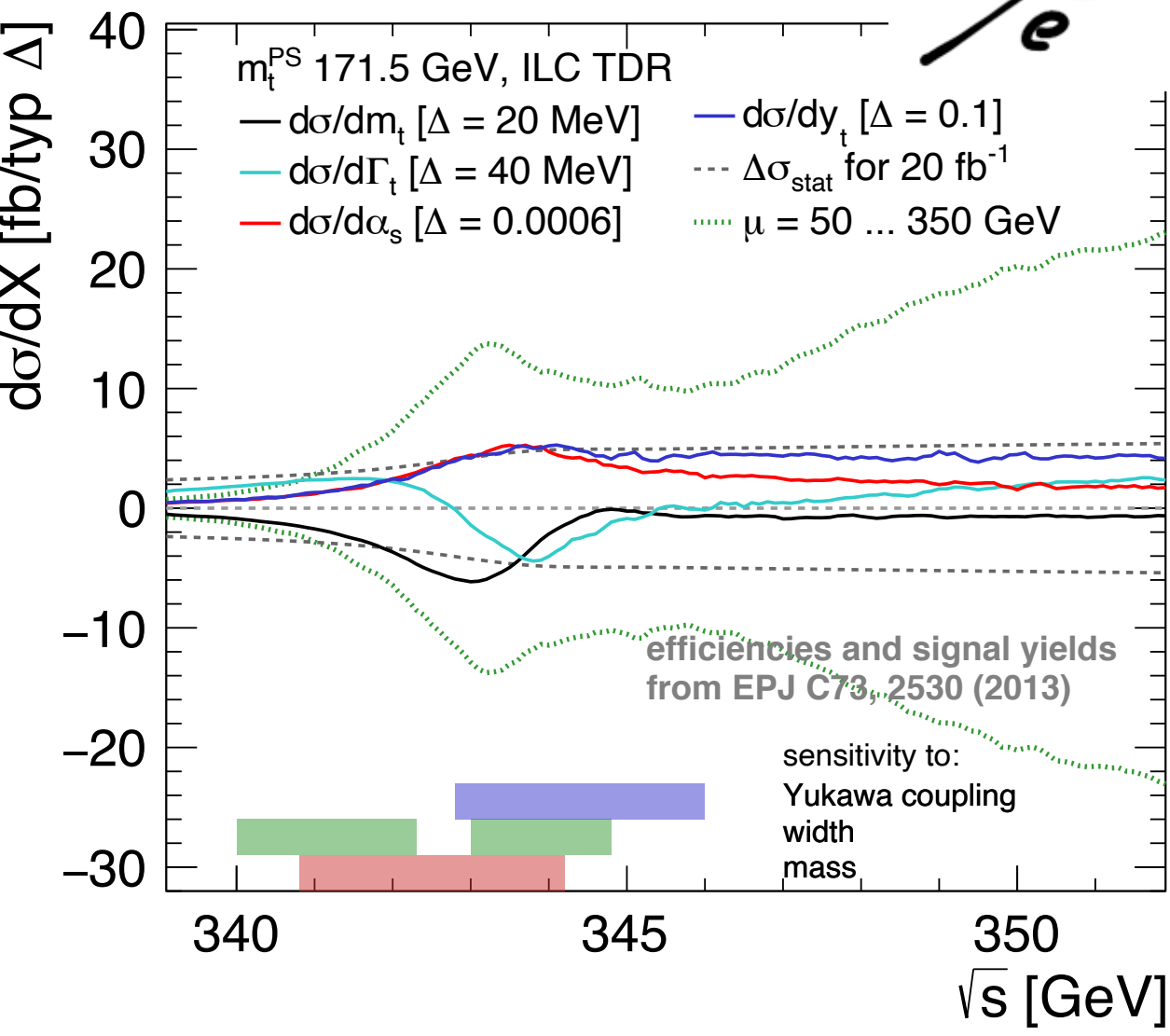
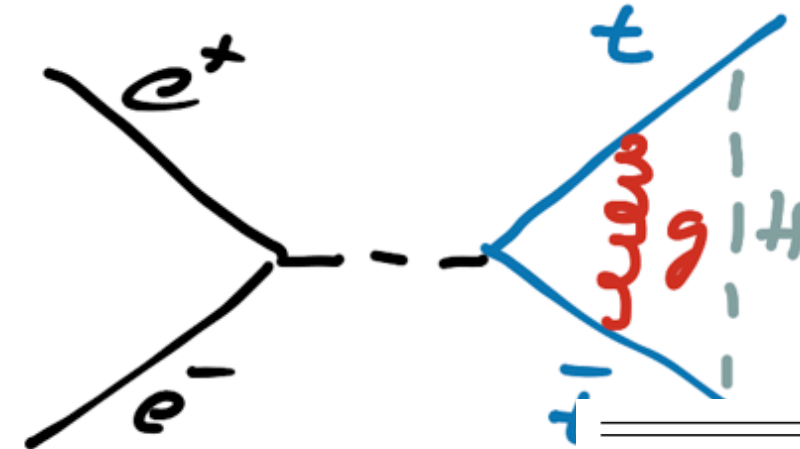
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- Assuming an integrated luminosity of 200 fb<sup>-1</sup> (default for ILC, FCCee, x2 of CLIC standard scenario - 10 points spaced by 1 GeV)
- Standard fit of mass only:  
 ILC 12.2 MeV [stat]  
 CLIC 13.3 MeV [stat]  
 FCCee 10.0 MeV [stat]



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stat. error (200 fb <sup>-1</sup> )	13
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combined theory & parametric	30 – 50
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total (stat. + syst.)	40 – 75

- Detailed evaluation of systematic uncertainties
- Multi-parameter fits (mass, width,  $\alpha_s$ ,  $y_t$ ), scan optimization...