

# Light Singlino Dark Matter at Future Colliders

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Snowmass21: Letter of interest

**Future collider reach for light DM in the NMSSM via light Higgs searches and direct electroweakino searches\***

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Thematic areas:

- EF08: BSM: Model specific explorations
- EF10: BSM: Dark Matter at colliders

arXiv : 2006.07854



# THE SALES PITCH

- NMSSM light neutralino sector is different from MSSM
- An expanded Higgs and neutralino sector.
- Phenomenologically richer and well motivated.
- Offers scope for exploration in complementary experiments
- The light neutralino DM in NMSSM will largely remain unexplored without future colliders and next generation DD experiments
- A pitch for measuring the Invisible decay of the Higgs



# NMSSM Higgses

$$W_{MSSM} = y_u^{ij} \hat{u}_i \hat{Q}_j \cdot \hat{H}_u - y_d^{ij} \hat{d}_i \hat{Q}_j \cdot \hat{H}_d - y_e^{ij} \hat{E}_i \hat{L}_j \cdot \hat{H}_d + \mu \hat{H}_u \cdot \hat{H}_d$$

An accidental weak scale parameter

$$W_{NMSSM} = W_{MSSM}(\mu = 0) + \lambda \hat{S} \hat{H}_u \cdot \hat{H}_d + \frac{\kappa}{3} \hat{S}^3$$

- Instead generate a weak scale parameter by a SUSY breaking term
- Additional quartic Higgs doublet with self coupling  $\lambda^2$
- Additional contribution to SM Higgs
- Lower fine tuning

A phenomenologically richer Higgs sector compared to MSSM:

7 Higgs bosons: 3 CP-even states ( $h_1$ ,  $h_2$  and  $h_3$ ), 2 CP-odd states ( $a_1$  and  $a_2$ ) and 2 charged Higgses ( $H^\pm$ ).

Possible to have singlet dominated light pseudoscalar or light CP even state

The tree level Higgs sector is driven by:

$$\lambda, \kappa, A_\lambda, A_\kappa, \tan \beta, \mu$$

$A_\lambda$  and  $A_\kappa$  are the trilinear soft-breaking parameters.

$$M_A^2 = \frac{\mu}{\sin \beta \cos \beta} \left( A_\lambda + \frac{\kappa \mu}{\lambda} \right)$$

$$M_{H^\pm}^2 = M_A^2 + M_W^2 - \frac{1}{2} \lambda^2 v^2$$



# NMSSM Higgses

The neutralino mass matrix:

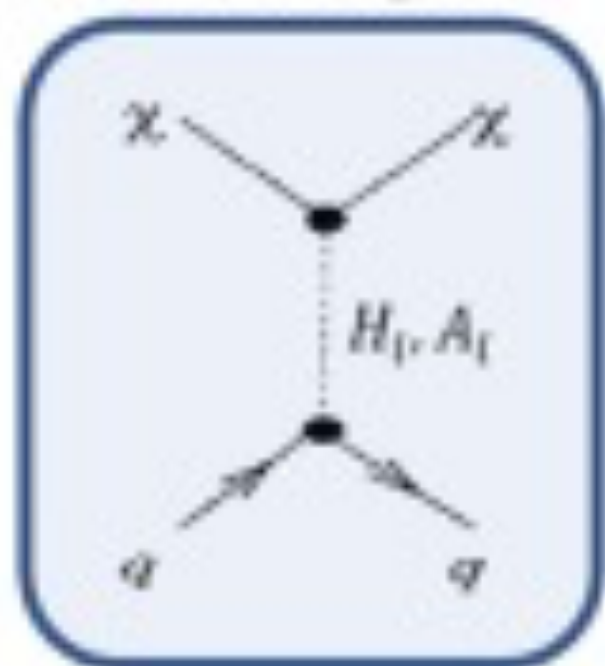
$$M_{\chi_i^0} = \begin{pmatrix} M_1 & 0 & -M_Z \sin \theta_W \cos \beta & M_Z \sin \theta_W \sin \beta & 0 \\ 0 & M_2 & M_Z \cos \theta_W \cos \beta & -M_Z \cos \theta_W \sin \beta & 0 \\ -M_Z \sin \theta_W \cos \beta & M_Z \cos \theta_W \cos \beta & 0 & -\mu & -\lambda v \sin \beta \\ M_Z \sin \theta_W \sin \beta & -M_Z \cos \theta_W \sin \beta & -\mu & 0 & -\lambda v \cos \beta \\ 0 & 0 & -\lambda v \sin \beta & -\lambda v \cos \beta & 2\kappa v_s \end{pmatrix}$$

The neutralinos can be admixtures of *singlino*, bino, wino and higgsinos.

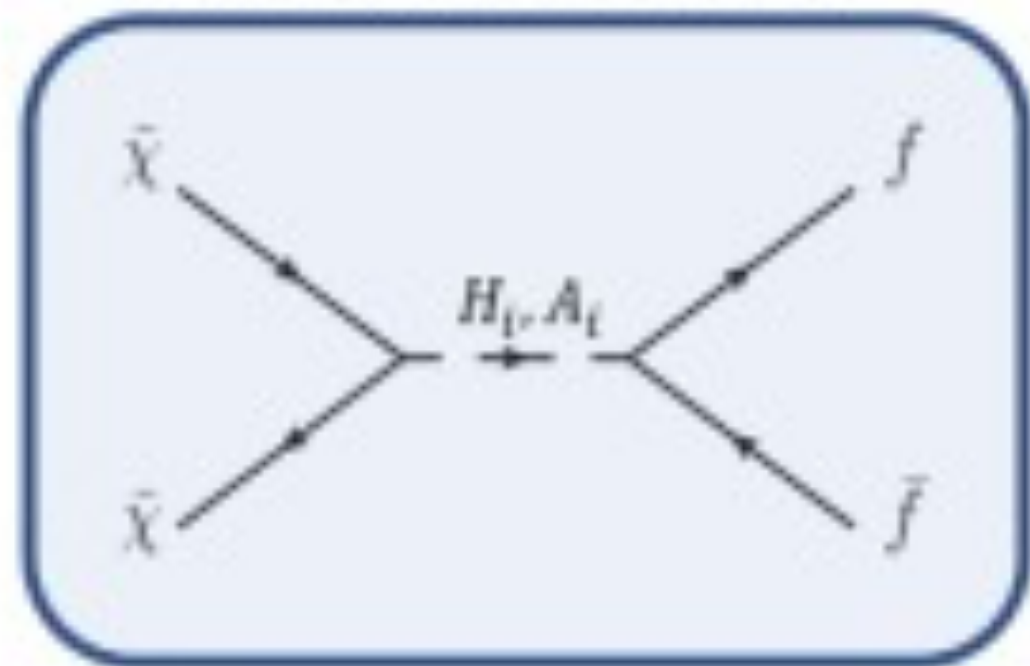
At the tree level, the EW ino sector is controlled by:  $M_1$ ,  $M_2$ ,  $\mu$ ,  $\tan \beta$ ,  $\lambda$ ,  $\kappa$

- Light neutralino can be dominantly singlet, as light as a few GeV
- Small direct detection cross section
- Relic via s channel pseudo-scalar and CP even scalar

Scattering XS



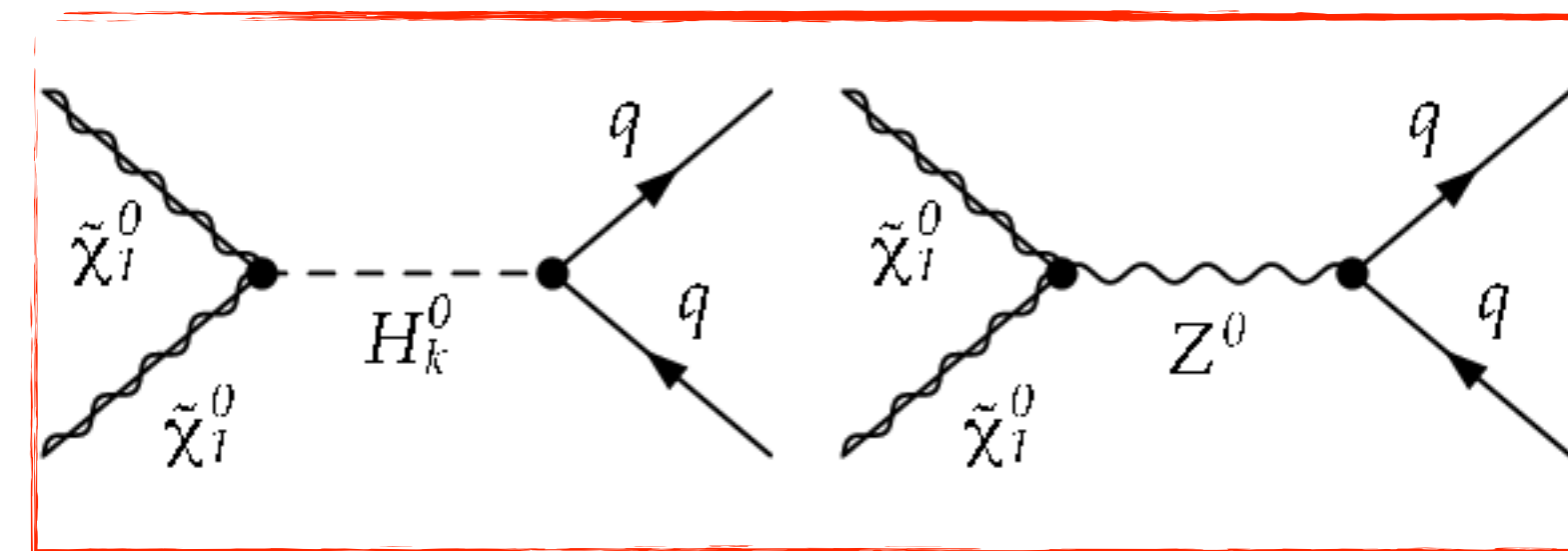
Annihilation XS



## MSSM light neutralinos

Light Neutralinos mostly Bino, some admixture with Higgsinos

Constrained by a combination of DD, relic and and chargino constraints

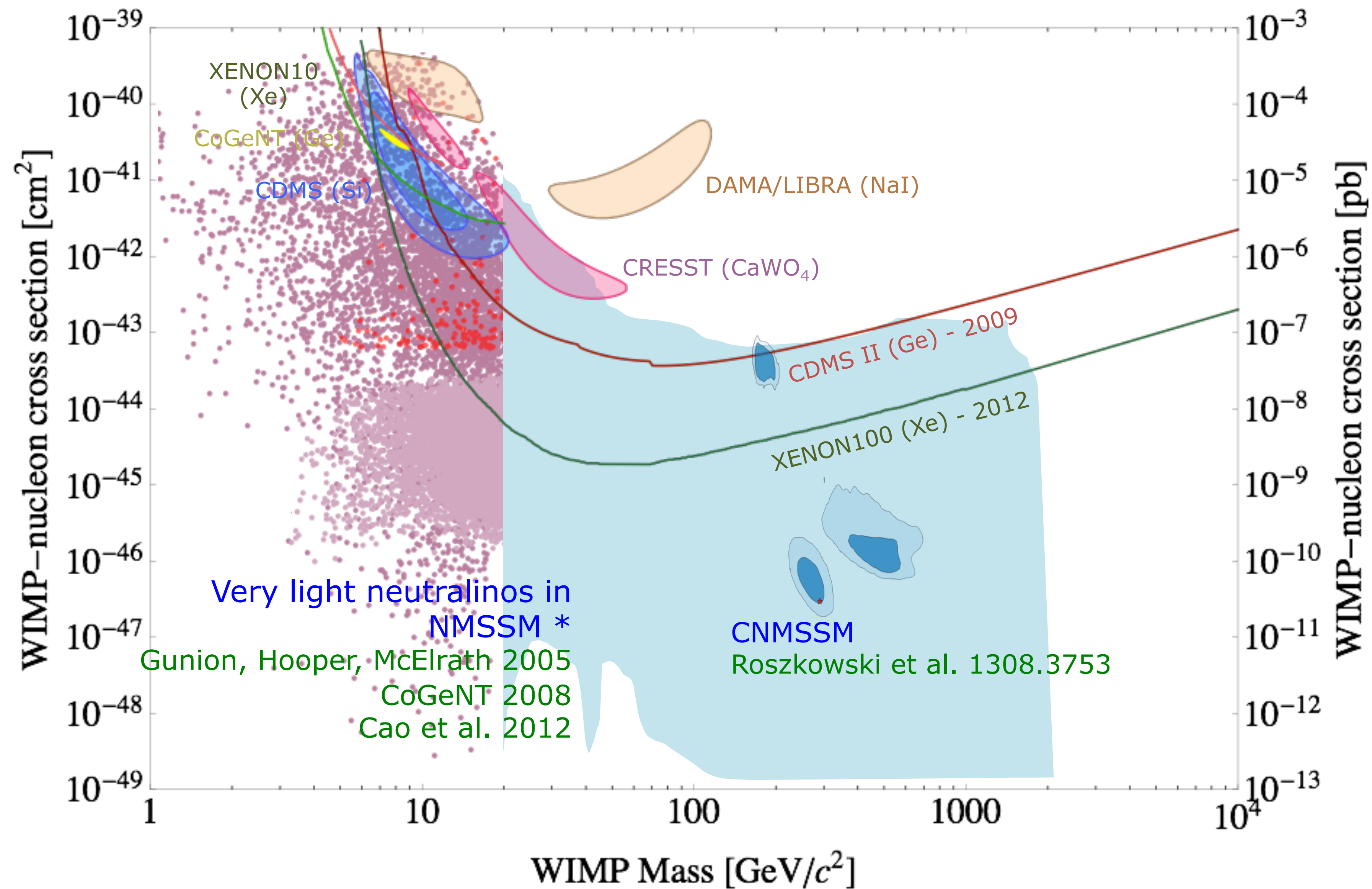


$$M_{\tilde{\chi}_1^0} \gtrsim 34 \text{ GeV}$$

arXiv: 1703.03838  
G. Belanger, R. K. Barman, B. Bhattacharjee,  
R. Godbole, D. Sengupta



# NMSSM vs others



\* without constrains on the Higgs sector

# Analyzing the space

- Standard Cosmology with  $\Omega h^2 \leq 0.120$  and focus on the  $M_{\tilde{\chi}_1^0} \leq 62.5 \text{ GeV}$
- Constraints and prospects from Invisible Higgs decays
- Collider, astrophysical and cosmological constraints.

- ① future multi-ton direct detection experiments.
- ② invisible Higgs decay width measurement at the future LHC, FCC, ILC and CEPC.
- ③ direct light Higgs searches and direct electroweakino searches at the HL-LHC and the HE-LHC.

# Light States in NMSSM

Analyzing current constraints for light DM in NMSSM

$$0.01 < \lambda < 0.7, 10^{-5} < \kappa < 0.05 \quad 3 < \tan \beta < 40$$

$$100 \text{ GeV} < \mu < 1 \text{ TeV}, 1.5 \text{ TeV} < M_3 < 10 \text{ TeV}$$

$$2 \text{ TeV} < A_\lambda < 10.5 \text{ TeV}, -150 \text{ GeV} < A_\kappa < 100 \text{ GeV}$$

$$M_1 = 2 \text{ TeV}, 70 \text{ GeV} < M_2 < 2 \text{ TeV}$$

$$A_t = 2 \text{ TeV}, A_{b,\tilde{\tau}} = 0, M_{U_R^3}, M_{D_R^3}, M_{Q_L^3} = 2 \text{ TeV}, M_{e_L^3}, M_{e_R^3} = 3 \text{ TeV}$$

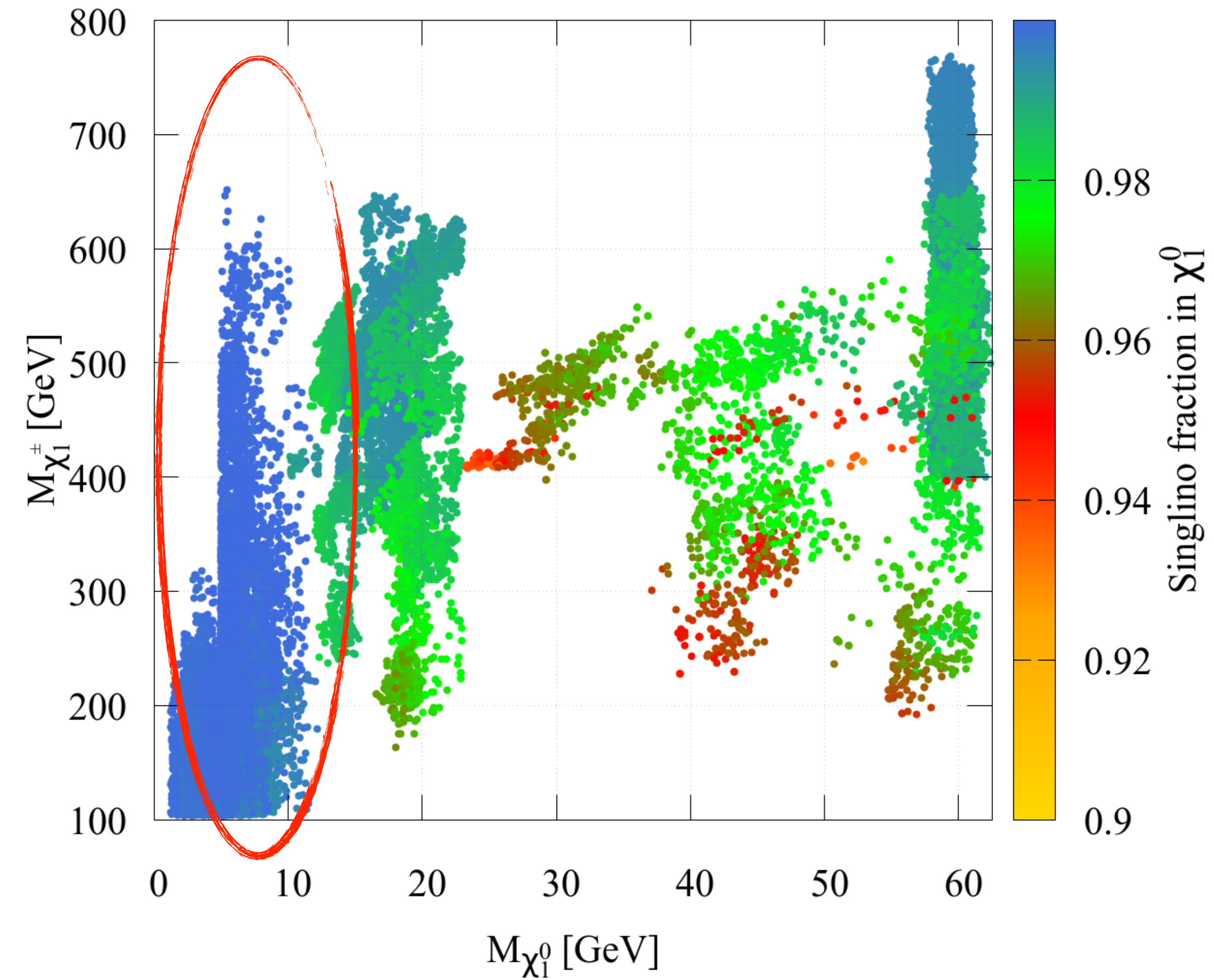
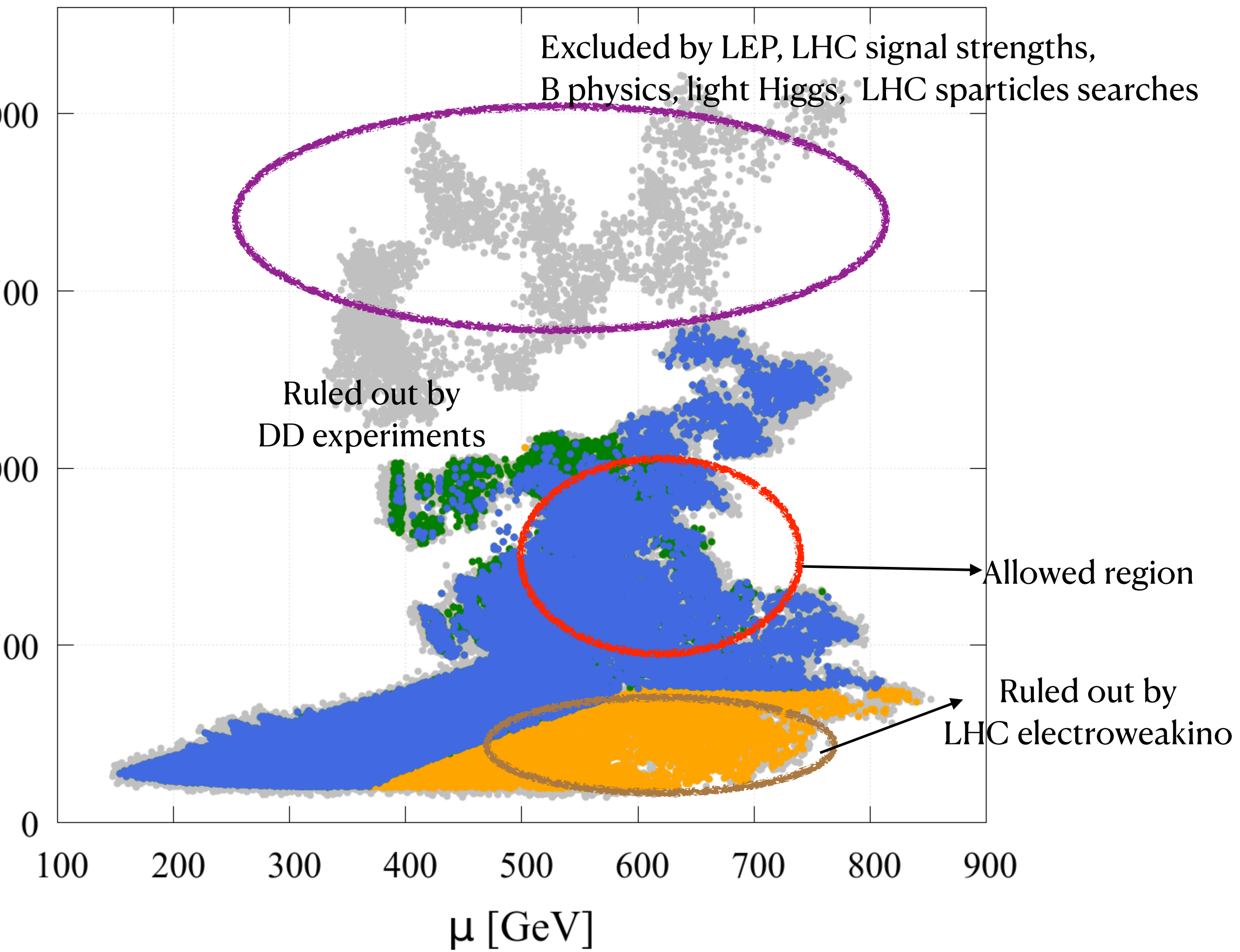
→ Scan Parameters



# Light States in NMSSM : constraints

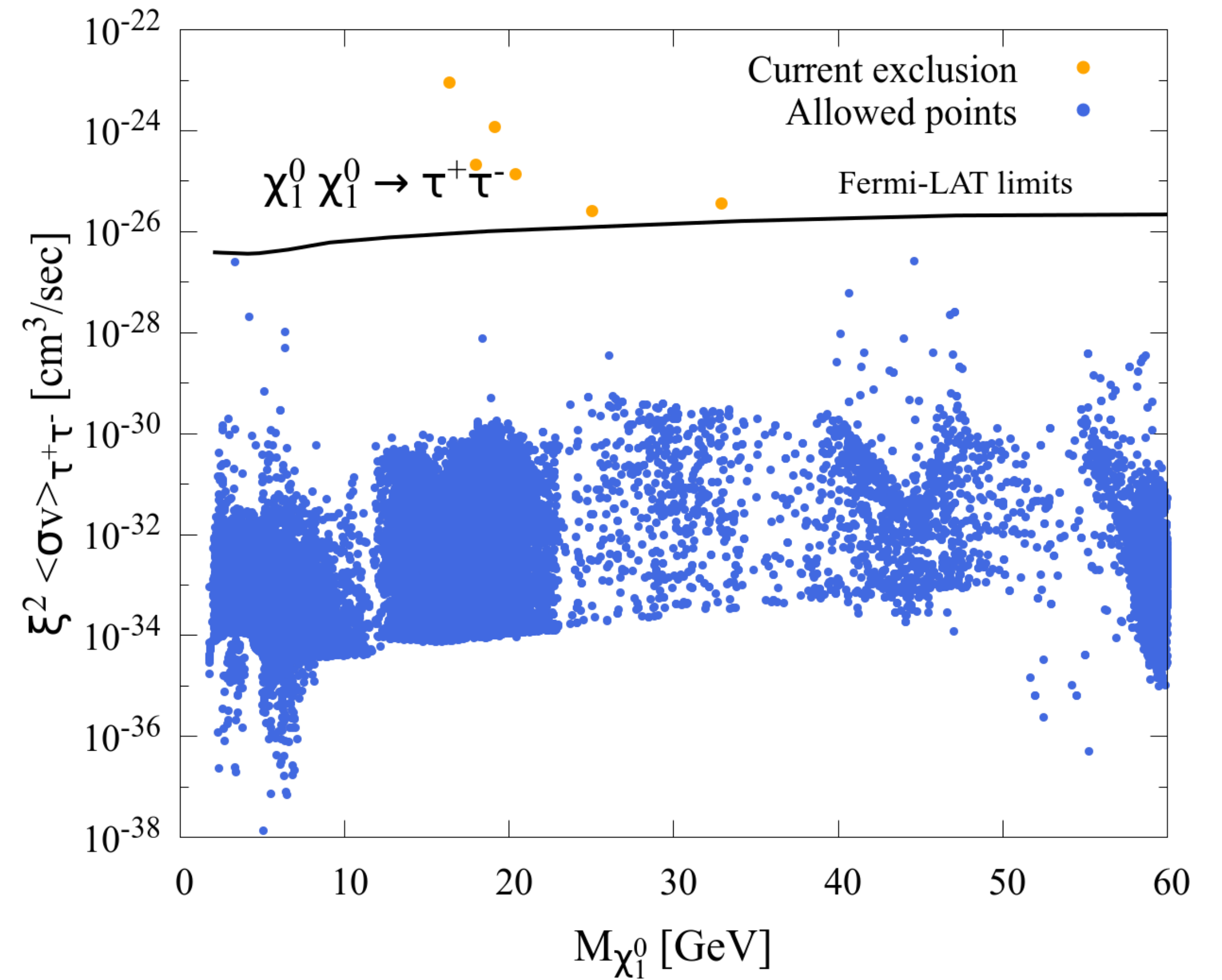
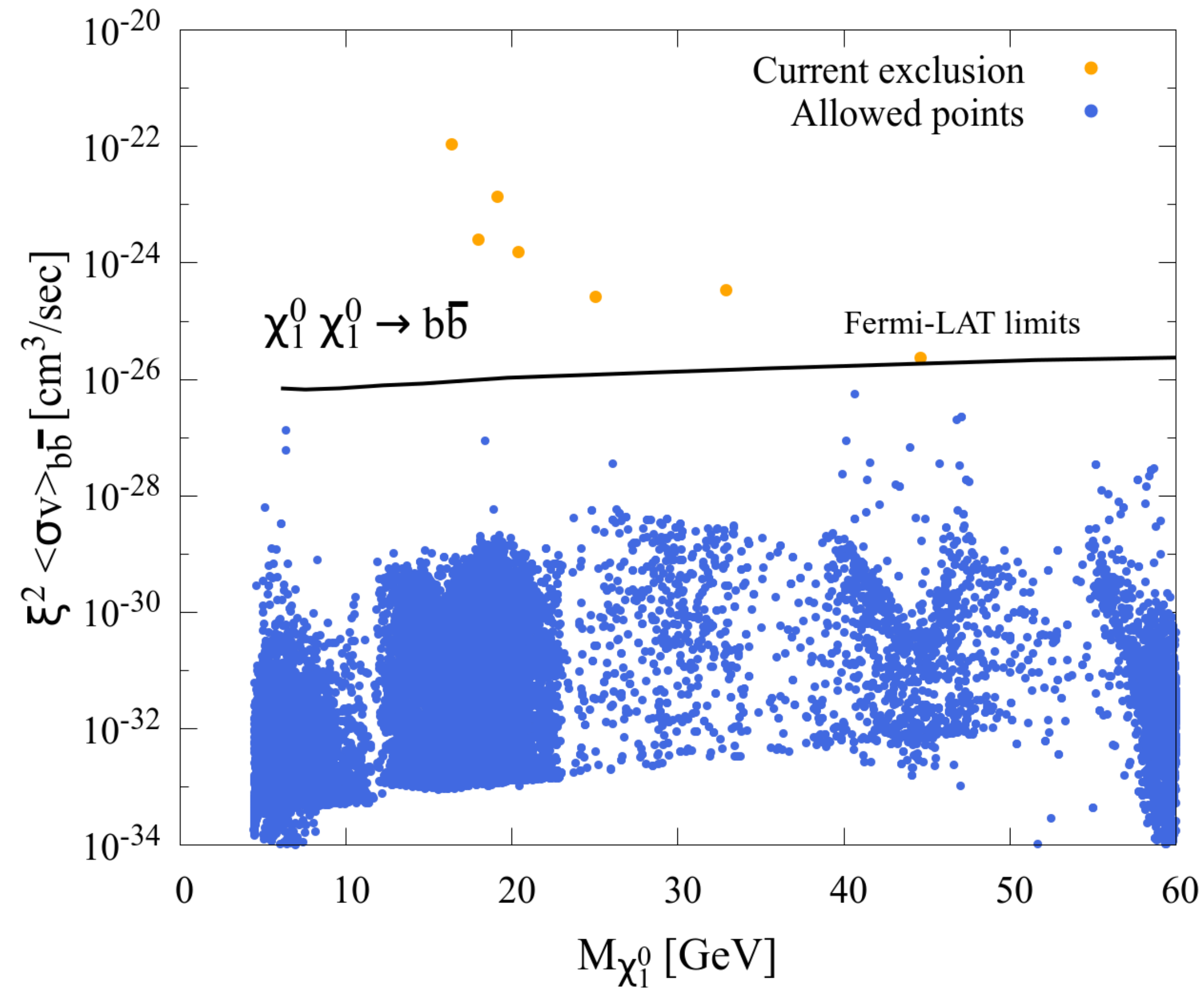
- An SM like Higgs, the heavier CP even, a lighter CP odd.
- LEP limit on chargino  $< 103.5$  GeV
- LEP limit :  $\sigma_{\tilde{\chi}_1^0 \tilde{\chi}_2^0} \lesssim 0.1$  pb
- Upper bound on relic  $\Omega_{DM(\tilde{\chi}_1^0)}^{obs.} h^2 \leq 0.122$
- Flavor constraints :  $Br(B_s \rightarrow \mu^+ \mu^-) = (3.0 \pm 0.6_{-0.2}^{+0.3}) \times 10^{-9}$   $Br(B^+ \rightarrow \tau^+ \nu_\tau) = (1.06 \pm 0.19) \times 10^{-4}$   $Br(B \rightarrow X_s \gamma) = (3.32 \pm 0.16) \times 10^{-4}$
- Higgs signal strengths  $b\bar{b}$ ,  $\tau^+ \tau^-$ ,  $ZZ$ ,  $W^+ W^-$  and  $\gamma\gamma$
- Invisible decays of the Higgs : VBF  $< 13$  %  $\Gamma_{H_{125}} < 22$  MeV
- Light Higgs searches at the LHC  $\sigma_{H_{125}} / \sigma_{H_{SM}} \times Br(H_{125} \rightarrow A_1 A_1 \rightarrow 2b2\mu)$
- Electroweakino searches at the LHC.  $pp \rightarrow (\tilde{\chi}_i^0 \rightarrow Z/H_{125} \tilde{\chi}_1^0)(\tilde{\chi}_1^\pm \rightarrow W^\pm \tilde{\chi}_1^0) 3l + \cancel{E}_T$
- Direct Detection bounds from Xenon 1T

# Light States in NMSSM : constraints





# Light States in NMSSM : Indirect detection



$$\xi = \Omega_{\tilde{\chi}_1^0}^{\text{thermal}} / 0.12$$



# Light States in NMSSM : Relic

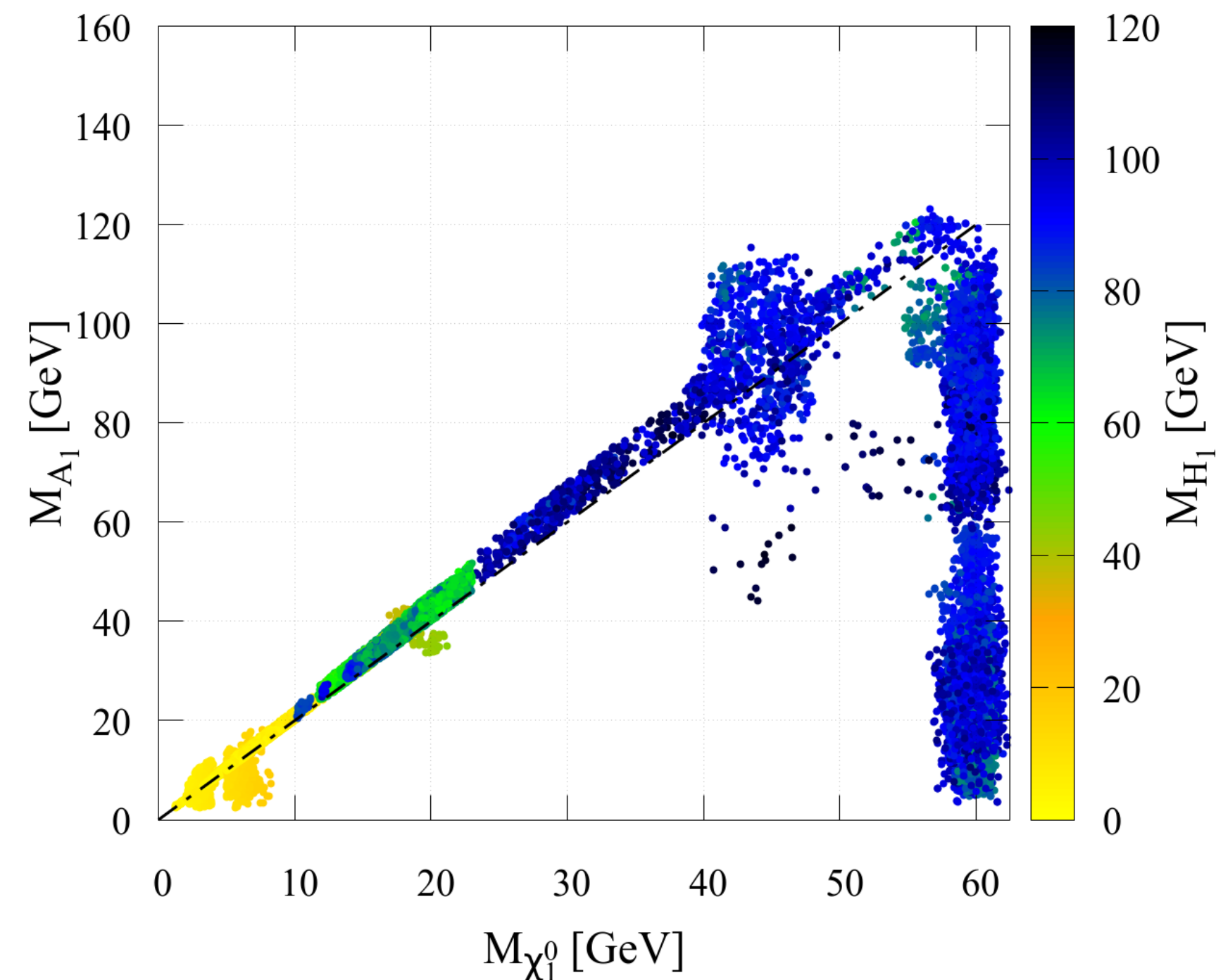
MSSM light neutralinos

Lower bound  $M_{\tilde{\chi}_1^0} \gtrsim 34 \text{ GeV}$   $Z$  funnel ( $\sim M_Z/2$ ) Higgs-funnel ( $M_{H_{125}}/2$ )

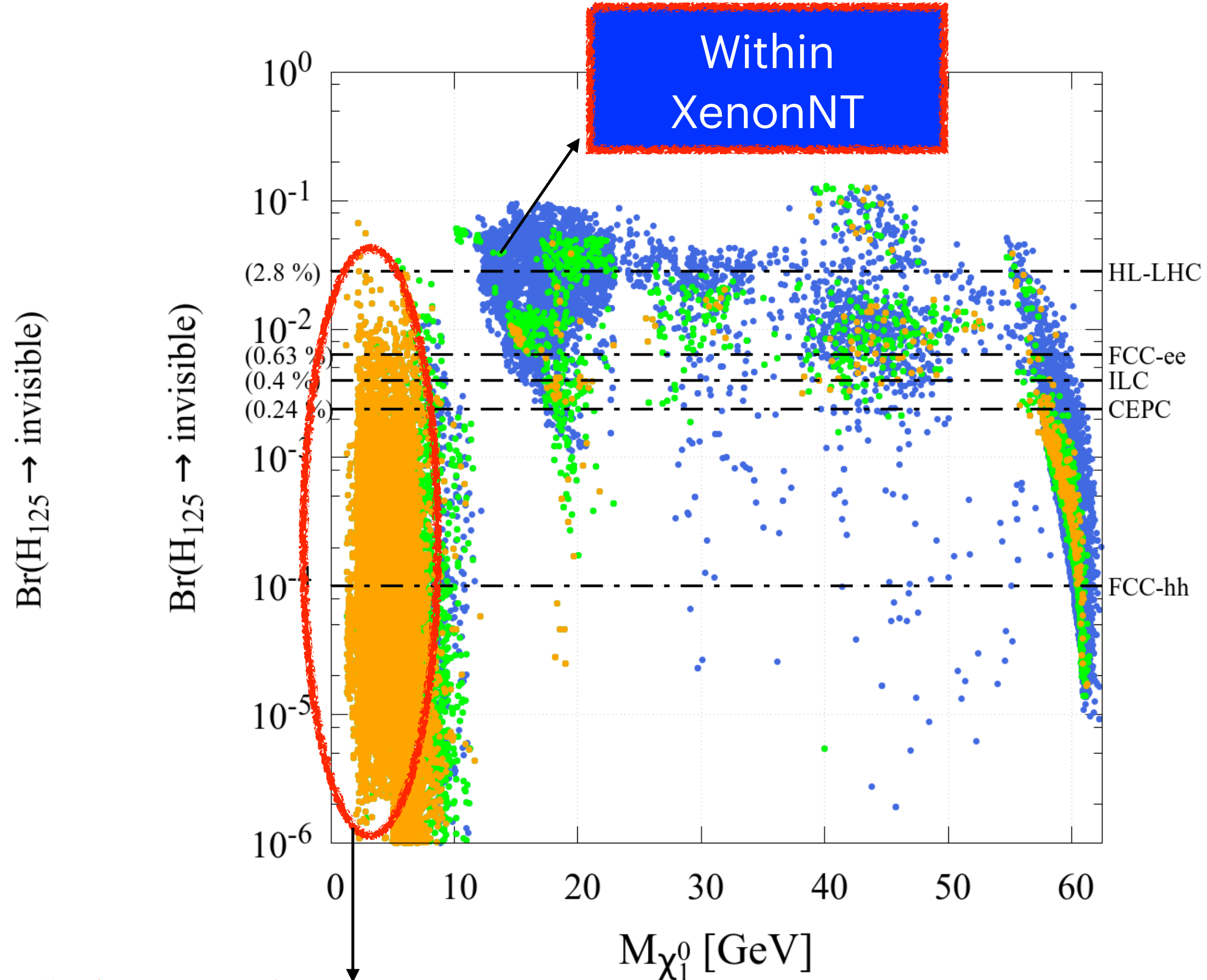
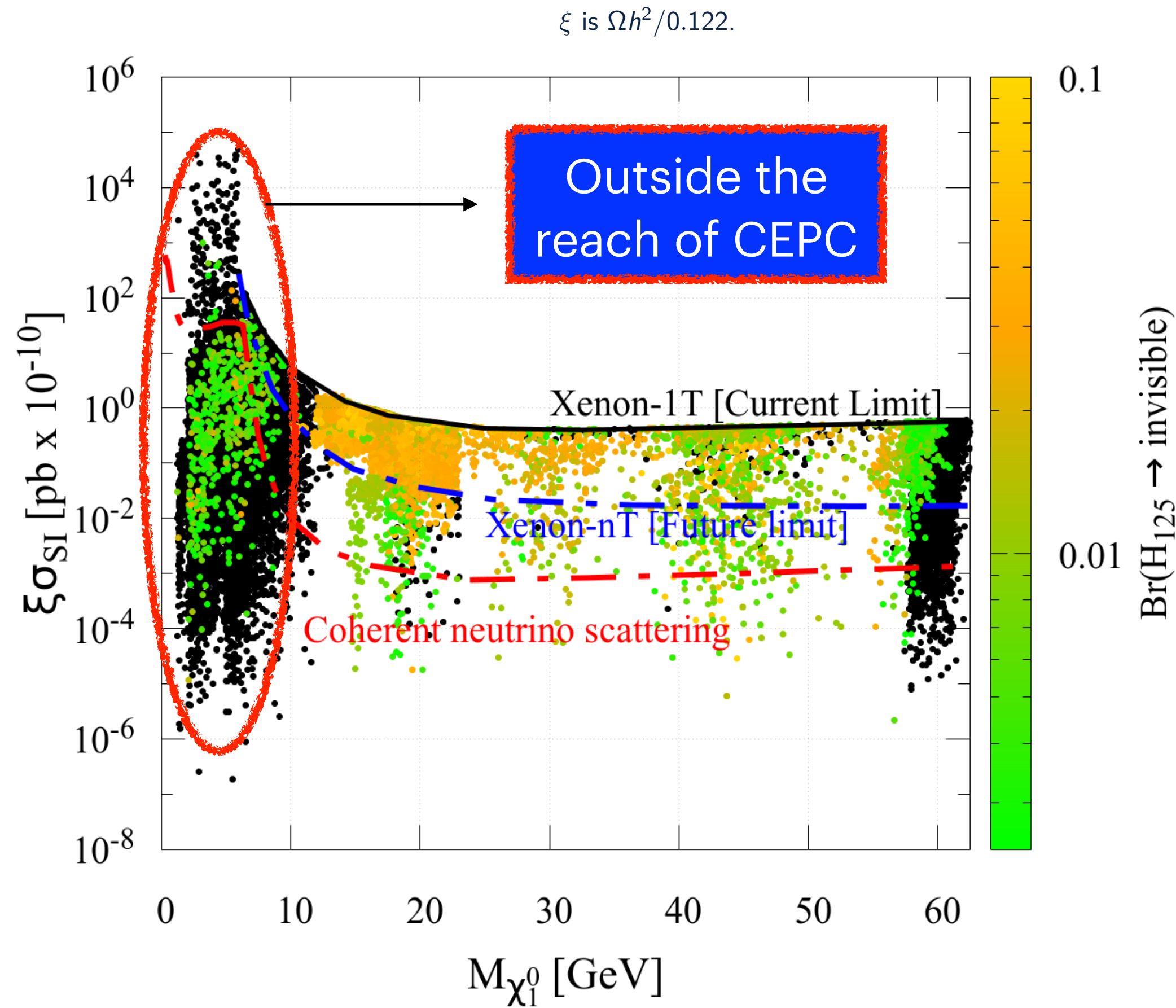
- The  $\tilde{\chi}_1^0$  has to be bino or singlino dominated.
- In such cases,  $\Omega h^2 \leq 0.122$  can be satisfied only through co-annihilation or annihilation via resonance.
- For our parameter space, **co-annihilation**  $\rightarrow$  **not feasible**
- **Only possibility**  $\rightarrow$  annihilation via resonance.
- We fix  $M_1$  at 2 TeV  $\rightarrow \tilde{\chi}_1^0$  is always **singlino dominated**.
- $a_1$  and  $h_1$  is always singlet dominated.

- Below the  $Z$  funnel region:

- 1 the allowed points are mostly populated along  $M_{a_1} \sim 2M_{\tilde{\chi}_1^0}$ .
- 2 points away from the above correlation have  $M_{h_1} \sim 2M_{\tilde{\chi}_1^0}$ .



# Light States in NMSSM : Invisible Higgs constraints



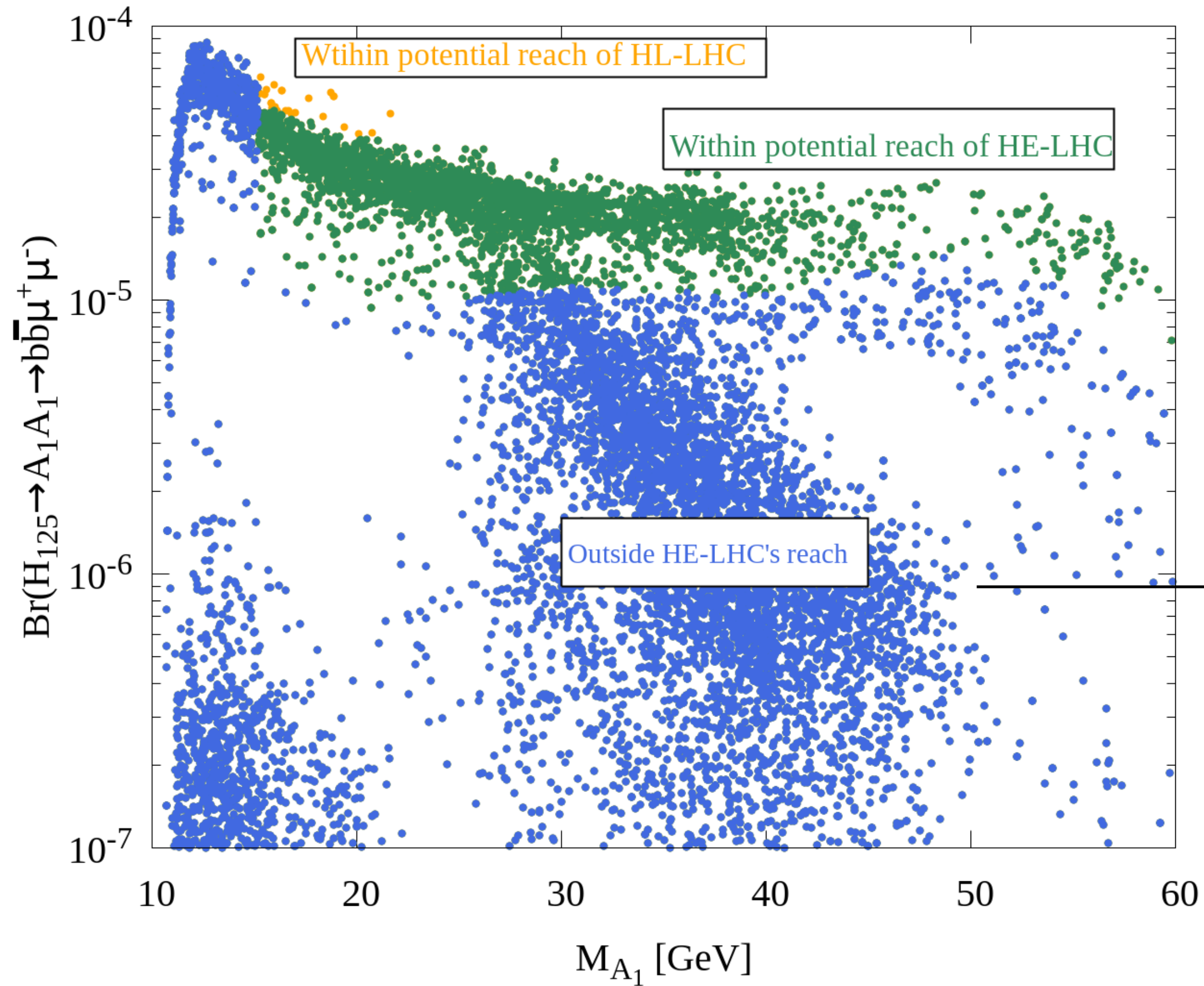
- $H_{125} \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0$
- $H_{125} \rightarrow A_1 A_1 \rightarrow 4 \tilde{\chi}_1^0$
- $H_{125} \rightarrow H_1 H_1 \rightarrow 4 \tilde{\chi}_1^0$
- $H_{125} \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^0 \rightarrow (\tilde{\chi}_2^0 \rightarrow H_1 \tilde{\chi}_1^0) \tilde{\chi}_1^0 \rightarrow (H_1 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0) 2 \tilde{\chi}_1^0 \rightarrow 4 \tilde{\chi}_1^0$
- $H_{125} \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^0 \rightarrow (\tilde{\chi}_2^0 \rightarrow A_1 \tilde{\chi}_1^0) \tilde{\chi}_1^0 \rightarrow (A_1 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0) 2 \tilde{\chi}_1^0 \rightarrow 4 \tilde{\chi}_1^0$

Projected capability of future experiments to probe invisibly decaying Higgs boson:

- HL-LHC ( $\gtrsim 2.8\%$ ) [CMS-PAS-FTR-16-002],
- FCC-ee ( $\gtrsim 0.63\%$ ) [1605.00100],
- ILC ( $\gtrsim 0.4\%$ ) [1310.0763],
- CEPC ( $\gtrsim 0.24\%$ ) [1811.10545],
- FCC-hh ( $\gtrsim 0.01\%$ ) [CERN-ACC-2018-045].



# Light States in NMSSM : constraints



Not optimized, room for improvement  
Dedicated simulation required

The future projections have been taken from 1902.00134 (Report from WG 2: Higgs Physics at the HL-LHC and HE-LHC, M. Cepeda et. al.) and translated to our allowed parameter space.



# Light States in NMSSM : Projections

Collider reach of HE-LHC and HL-LHC

- Simple cut based optimized analysis
- Target WZ and WH mediated  $3l + \text{MET}$  channel for Higgsino production
- Projections translated to allowed NMSSM parameter space
- Map out Efficiency grids in the Higgsino-LSP mass plane

# WZ-mediated $3l + \cancel{E}_T$ at the HL-LHC

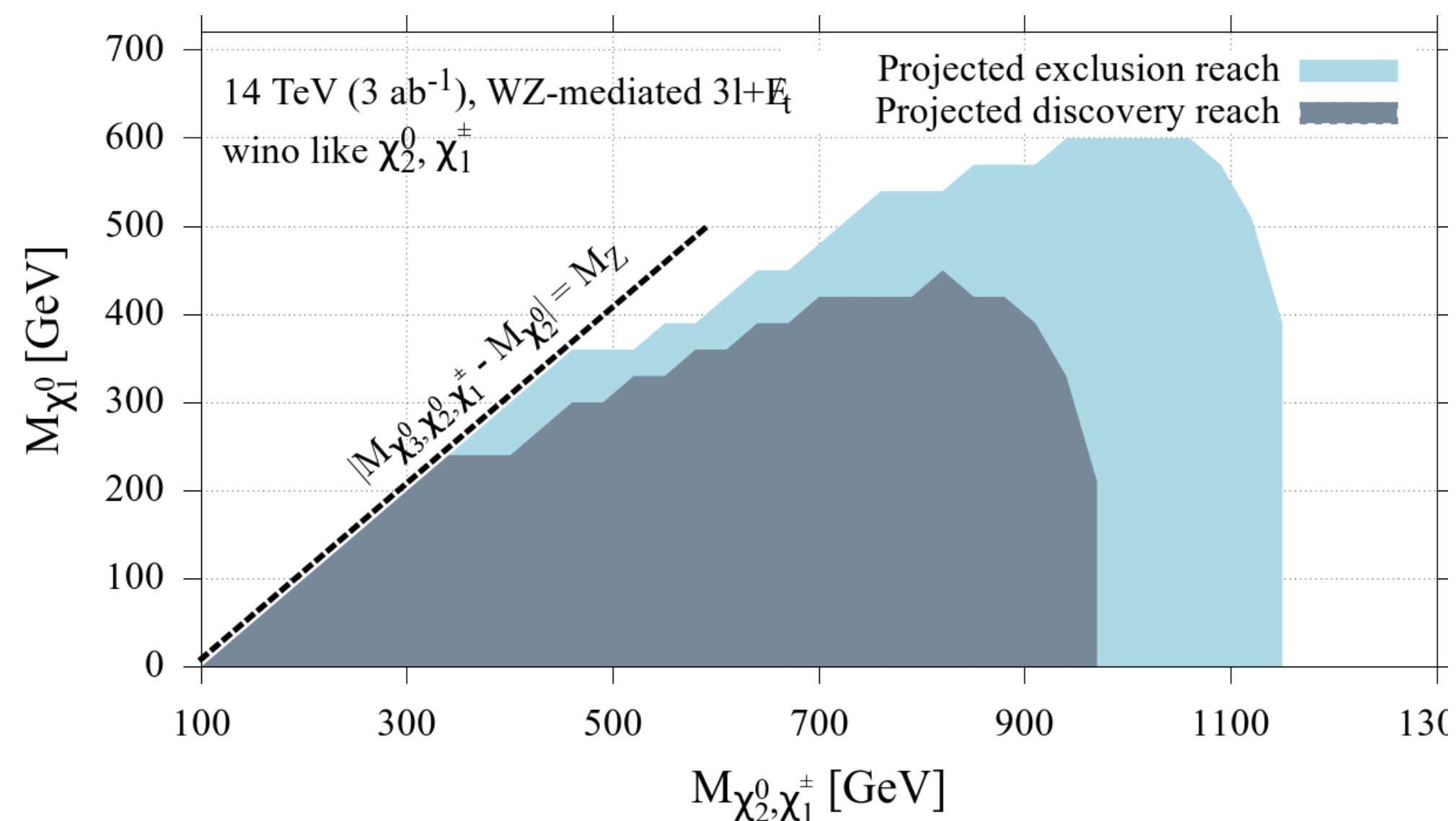
The following signal regions (SR) are used. We choose SRs optimized for large (BPB1, BPD1, BPG1), intermediate (BPE1, BPF1, BPH1) and small (BPA1, BPC1, BPF1) mass difference between NLSPs and the LSP.

	Benchmark points							
	BPA1	BPB1	BPC1	BPD1	BPE1	BPF1	BPG1	BPH1
$M_{\tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_1^\pm}$ [GeV]	130	310	310	610	610	610	1000	1000
$M_{\tilde{\chi}_1^0}$ [GeV]	30	0	210	0	300	510	0	420
Kinematic variables	Signal regions							
	SRA1	SRB1	SRC1	SRD1	SRE1	SRF1	SRG1	SRH1
$\Delta\Phi_{lW\cancel{E}_T}$	$\leq 0.2$	-	$\leq 1.5$	-	-	-	-	-
$\Delta\Phi_{SFOS-\cancel{E}_T}$	-	$[2.7 : \pi]$	$[1.8 : \pi]$	$[1.5 : \pi]$	$[1.8 : \pi]$	-	$[1.6 : \pi]$	$[1.5 : \pi]$
$\Delta R_{SFOS}$	$[1.4 : 3.8]$	$[0.3 : 2.1]$	-	$[0.1 : 1.3]$	$[0.1 : 1.3]$	$[1.6 : 4.0]$	$[0.1 : 1.0]$	$[0.1 : 1.3]$
$\cancel{E}_T$ [GeV]	$[50 : 290]$	$\geq 220$	$[100 : 380]$	$\geq 200$	$\geq 250$	-	$\geq 200$	$\geq 200$
$M_T^{lW}$ [GeV]	-	$\geq 100$	$[100 : 225]$	$\geq 300$	$\geq 150$	$[150 : 350]$	$\geq 150$	$\geq 200$
$M_{CT}^{lW}$ [GeV]	-	$\geq 100$	-	$\geq 100$	$\geq 150$	$[100 : 400]$	$\geq 200$	$\geq 200$
$p_T^{l_1}$ [GeV]	$[50 : 150]$	$\geq 120$	$[60 : 110]$	$\geq 150$	$\geq 150$	$[60 : 150]$	$\geq 210$	$\geq 200$
$p_T^{l_2}$ [GeV]	$[50 : 110]$	$\geq 60$	$\geq 30$	$\geq 100$	$\geq 100$	$[50 : 80]$	$\geq 150$	$\geq 100$
$p_T^{l_3}$ [GeV]	$\geq 30$	$\geq 30$	$\geq 30$	$\geq 50$	$\geq 50$	$[30 : 60]$	$\geq 50$	$\geq 50$

Background generation (at LO) done using [MadGraph5\\_aMC@NLO](#). Signal generated using [Pythia-6](#) and detector effects simulated with [Delphes-3.4.2](#).

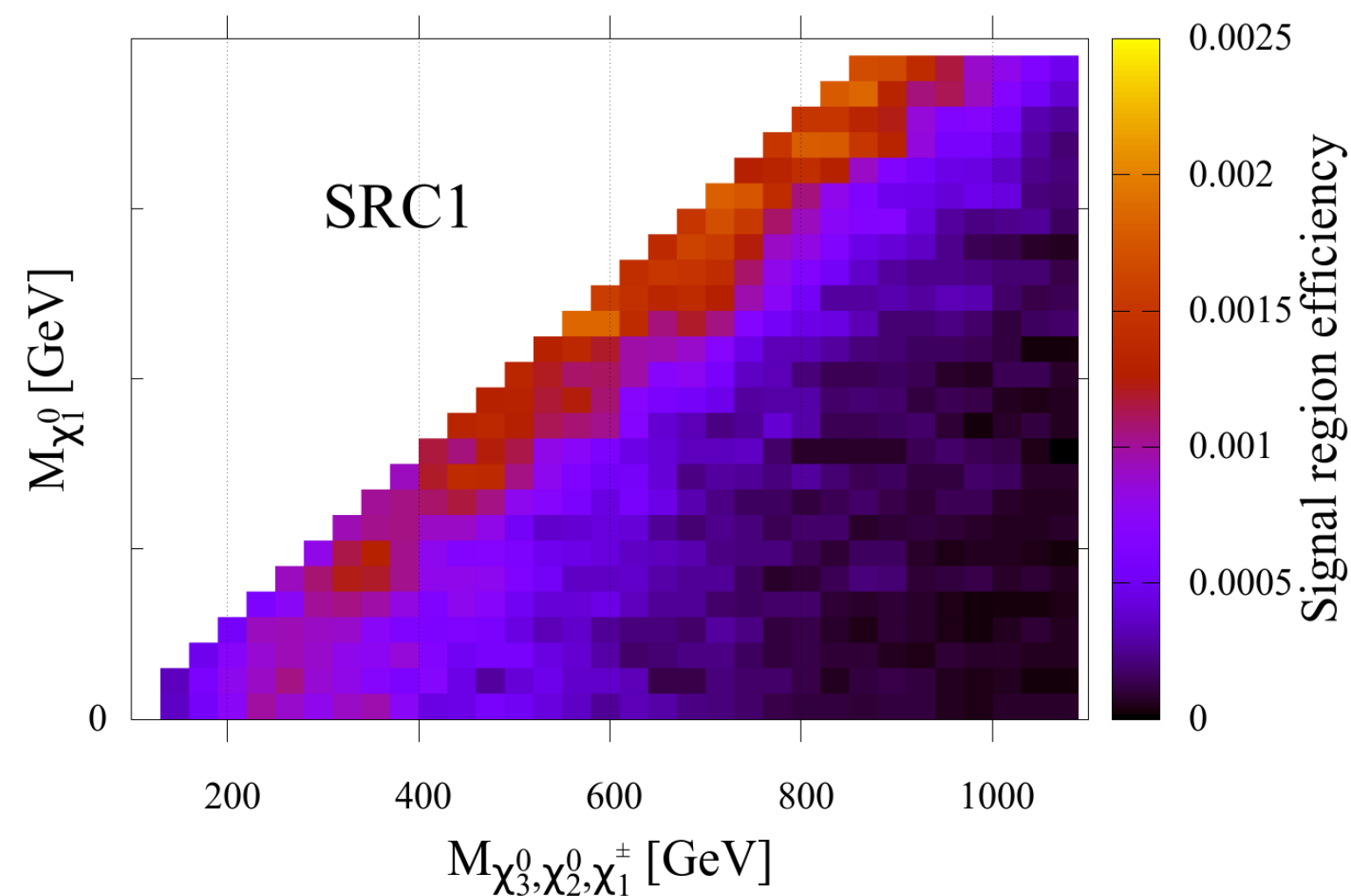
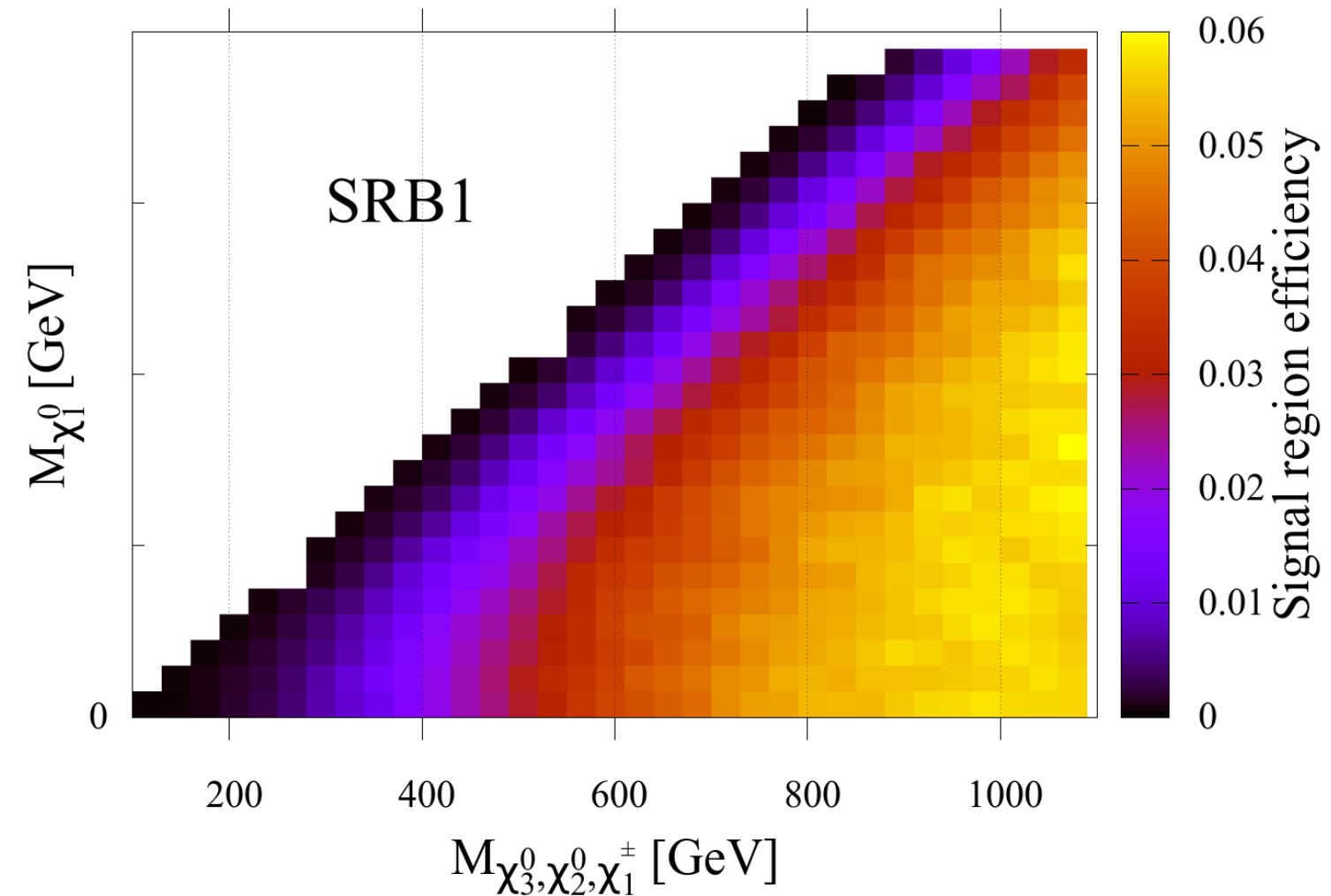
# WZ-mediated $3l + \cancel{E}_T$ at the HL-LHC

Projected reach of wino searches in the WZ mediated  $3l + \cancel{E}_T$  final state at the HL-LHC.



Our projection results are comparable with the ATLAS projections in ATLAS-PHYS-PUB-2018-048 (discovery (exclusion) upto  $\sim 950$  ( $\sim 1110$ ) GeV for massless LSP at 95% C.L.).

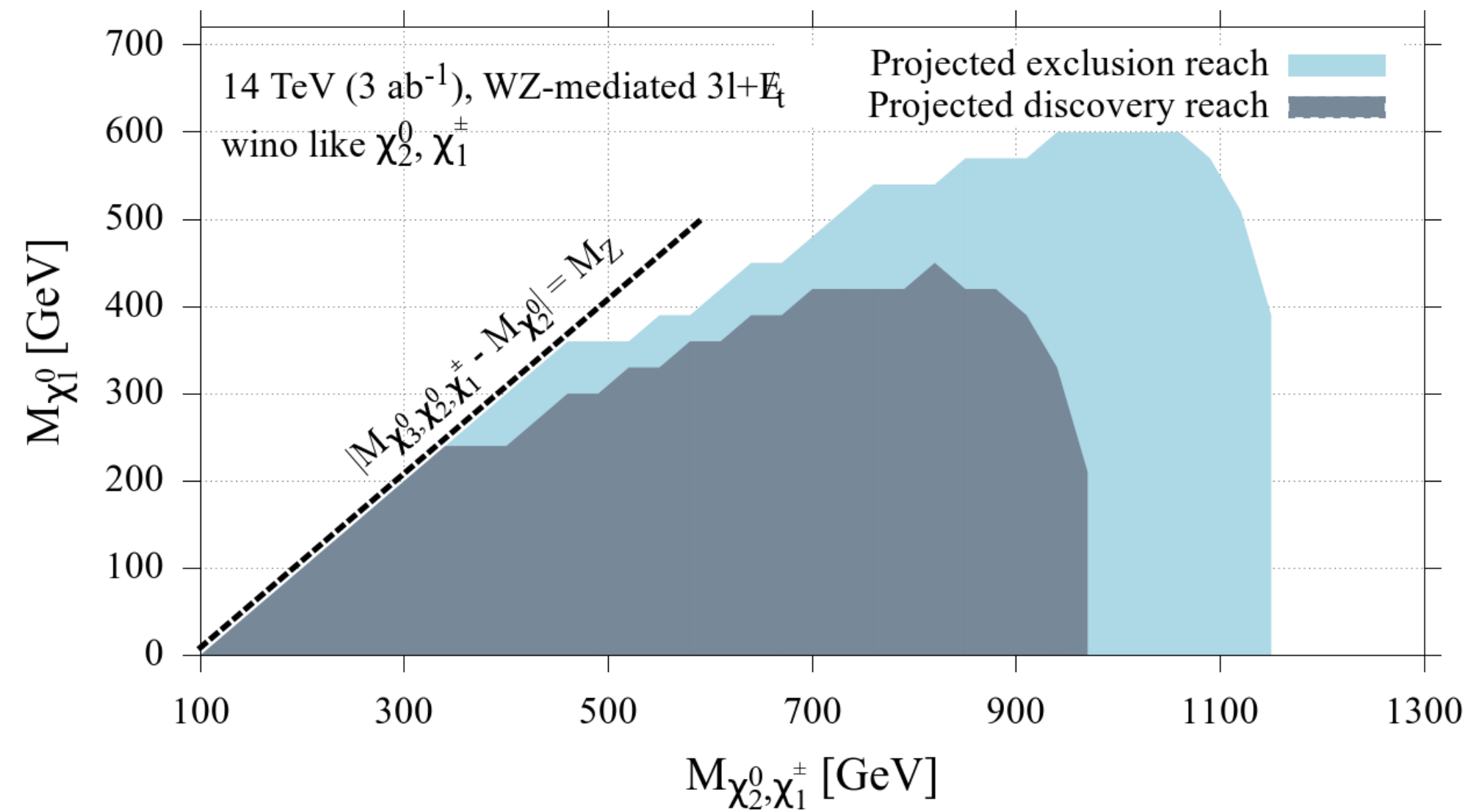
Efficiency maps:





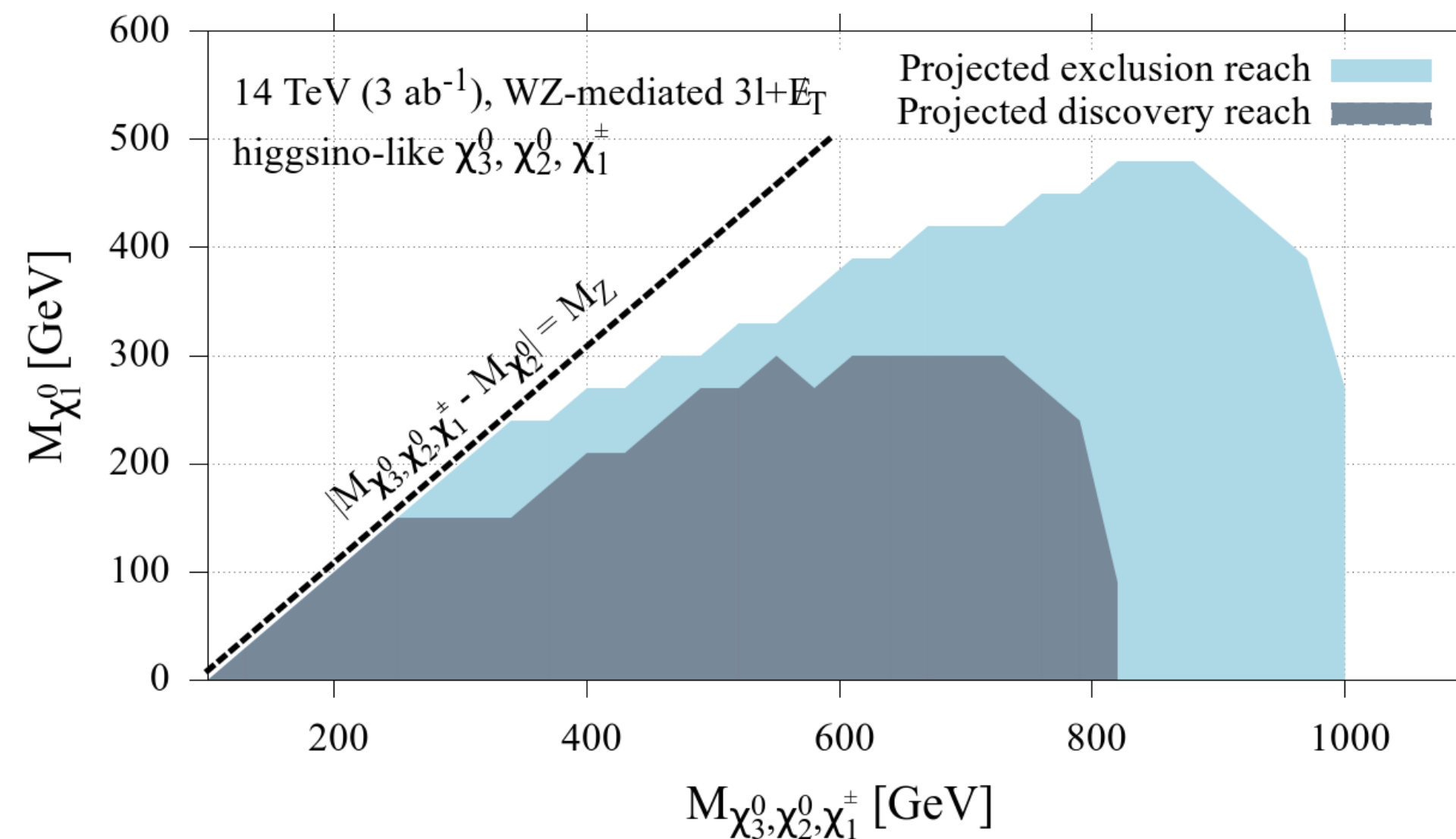
# WZ-mediated $3l + \cancel{E}_T$ at the HL-LHC

Projected reach of **wino** searches in the WZ mediated  $3l + \cancel{E}_T$  final state at the HL-LHC.



Our projection results are comparable with the ATLAS projections in ATLAS-PHYS-PUB-2018-048 (discovery (exclusion) upto  $\sim 950$  ( $\sim 1110$ ) GeV for massless LSP at 95% C.L.).

Projected reach of **higgsino** searches in the WZ mediated  $3l + \cancel{E}_T$  final state at the HL-LHC.



A systematic uncertainty of 5% has been assumed in these analyses.

# Impact on allowed NMSSM parameter space

- In our allowed parameter region,  $\tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_4^0, \tilde{\chi}_1^\pm, \tilde{\chi}_2^\pm$  are either higgsino-like, wino-like or wino-higgsino admixtures.
- Direct chargino-neutralino pair production modes which can potentially contribute to  $WZ$  mediated  $3l + \cancel{E}_T$ :  $\tilde{\chi}_2^0\tilde{\chi}_1^\pm, \tilde{\chi}_2^0\tilde{\chi}_2^\pm, \tilde{\chi}_3^0\tilde{\chi}_1^\pm, \tilde{\chi}_3^0\tilde{\chi}_2^\pm, \tilde{\chi}_4^0\tilde{\chi}_1^\pm$  and  $\tilde{\chi}_4^0\tilde{\chi}_2^\pm$
- The direct production cross-section ( $\sigma_{\tilde{\chi}_i^0\tilde{\chi}_j^\pm}$ ) is computed by scaling the pure higgsino cross-section with the respective reduced squared  $W\tilde{\chi}_i^0\tilde{\chi}_j^\pm$  couplings:

$$C_{W\tilde{\chi}_i^0\tilde{\chi}_j^\pm}^2 = \left\{ \left( N_{i3} V_{j2} - N_{i2} V_{j1}\sqrt{2} \right)^2 + \left( N_{i4} U_{j2} + N_{i2} U_{j1}\sqrt{2} \right)^2 \right\}$$

$U/V$  are the chargino mixing matrices while  $N$  represents the neutralino mixing matrix.

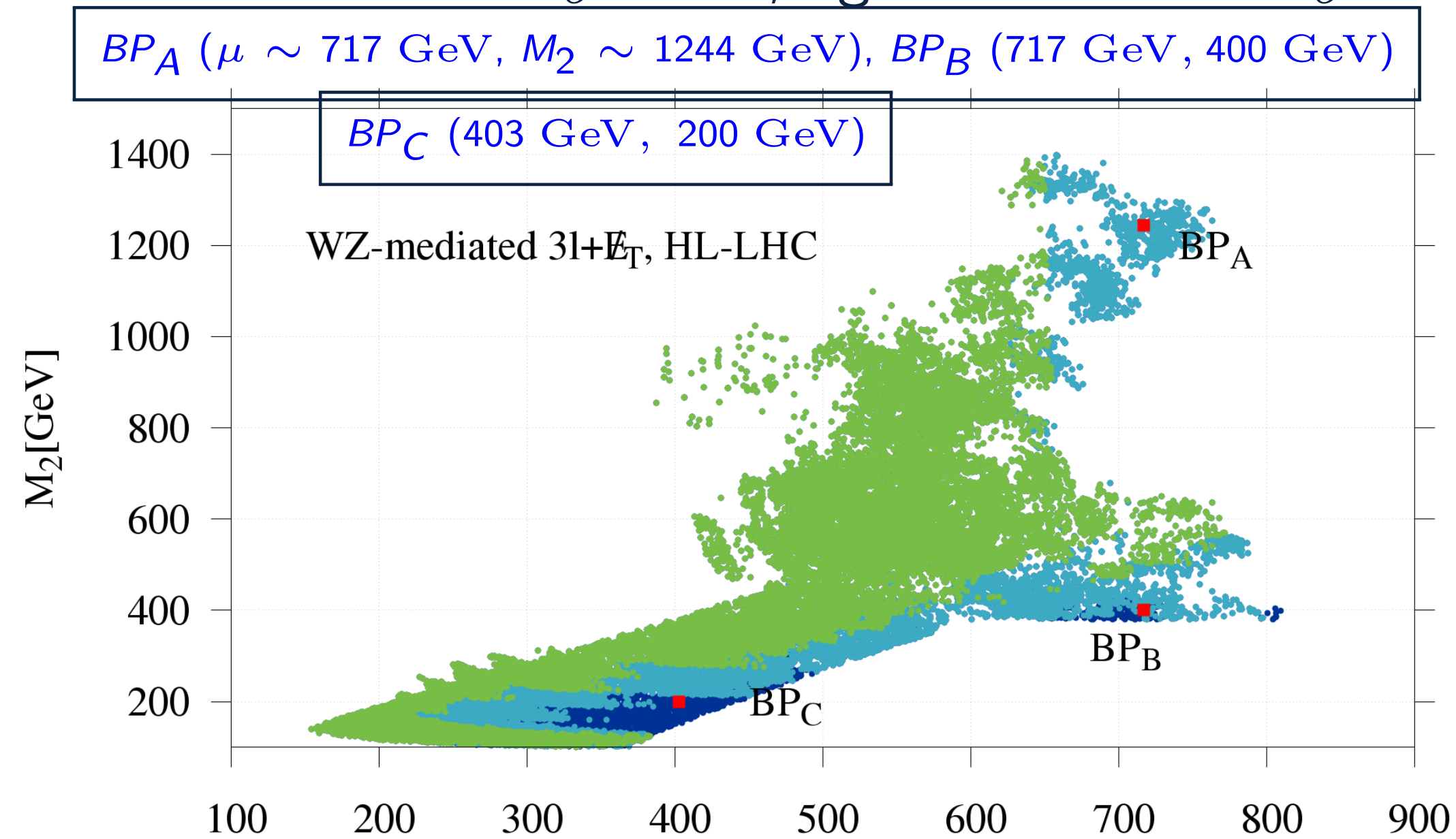
- The signal yield for a particular parameter space point is computed for all the signal regions through:

$$S = \sigma_{\tilde{\chi}_i^0\tilde{\chi}_j^\pm} \times (\text{Relevant } Br \text{ ratios}) \times (\mathcal{L} = 3000 \text{ fb}^{-1}) \times \text{Signal efficiency} \quad (1)$$

- The signal efficiency is obtained from the efficiency maps shown earlier.
- The signal significance ( $S_\sigma$ ) is computed as:  $S/\sqrt{B + (B \cdot \text{sys\_un})^2}$ , by adopting the signal region that yields the highest  $S_\sigma$ . Here,  $B$  stands for background.

# Impact on allowed NMSSM parameter space

**Color code:** Green:  $S_\sigma > 5$ , light blue:  $2 < S_\sigma < 5$ , dark blue:  $S_\sigma < 2$

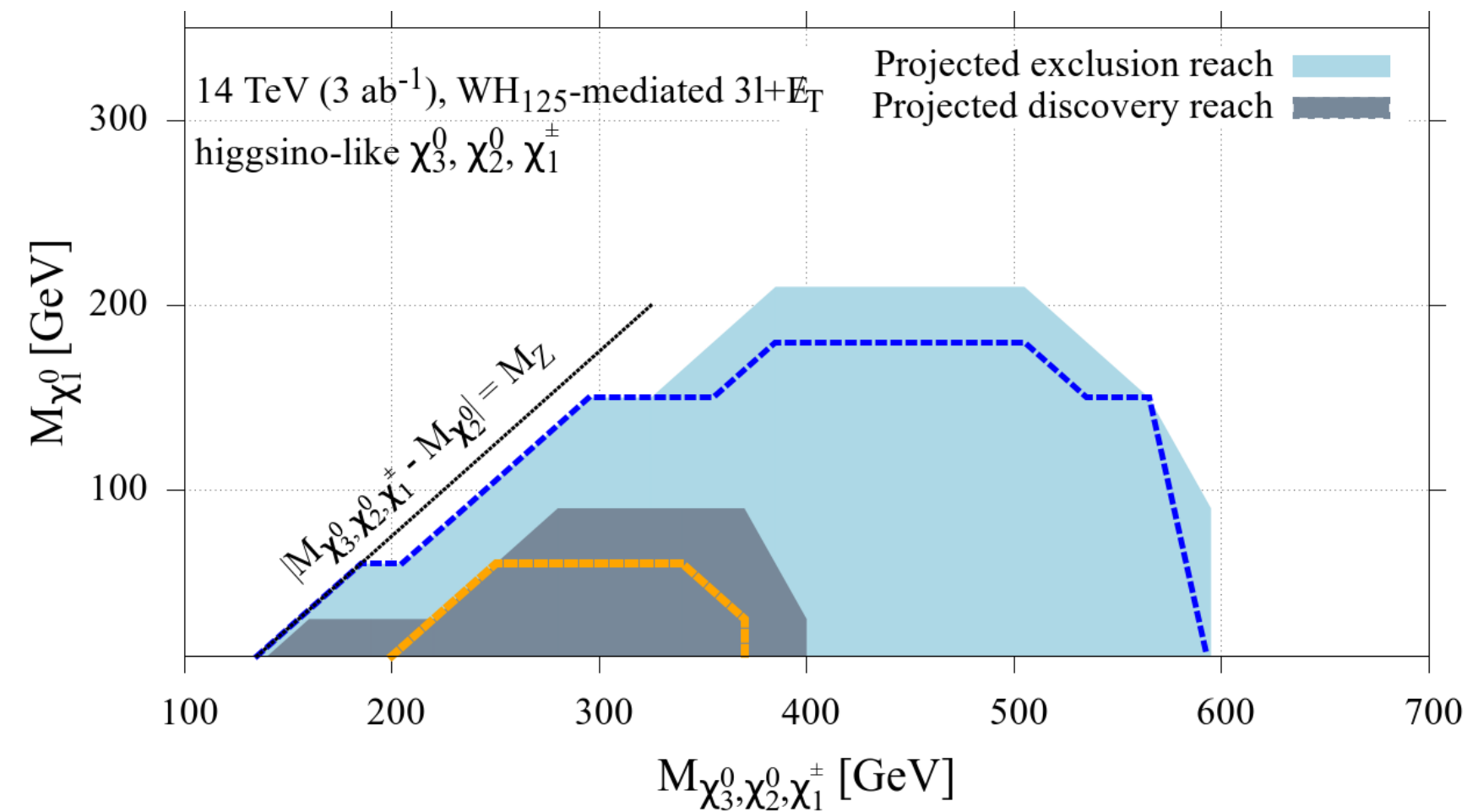


- The observation of a signal is an interplay between the production cross-section and signal efficiency.
- At large values of  $M_2, \mu$  (near  $BP_A$ )  $\rightarrow$  large efficiency but smaller production cross-section  $\rightarrow$  kinematically suppressed signal.

- At smaller values of  $M_2, \mu$ ,  $\rightarrow$  larger production cross-section but signal efficiencies reduce.
- The dark blue points near  $BP_C$  have  $S_\sigma$  marginally less than  $2\sigma$  on account of smaller efficiency from SRB1 and suppressed  $\tilde{\chi}_2^0 \rightarrow Z\tilde{\chi}_1^0$ .
- In  $BP_B$  and  $BP_C$ , the dominant production mode is  $\tilde{\chi}_2^0\tilde{\chi}_1^\pm$ , and  $\tilde{\chi}_2^0$  dominantly decays into  $H_{125} + \tilde{\chi}_1^0$  with branching rates of 82% and 92%, respectively  $\rightarrow$  reduced sensitivity in  $WZ$  mediated channels.
- Direct searches in  $WH_{125}$  mediated channels could be more effective for these benchmarks.



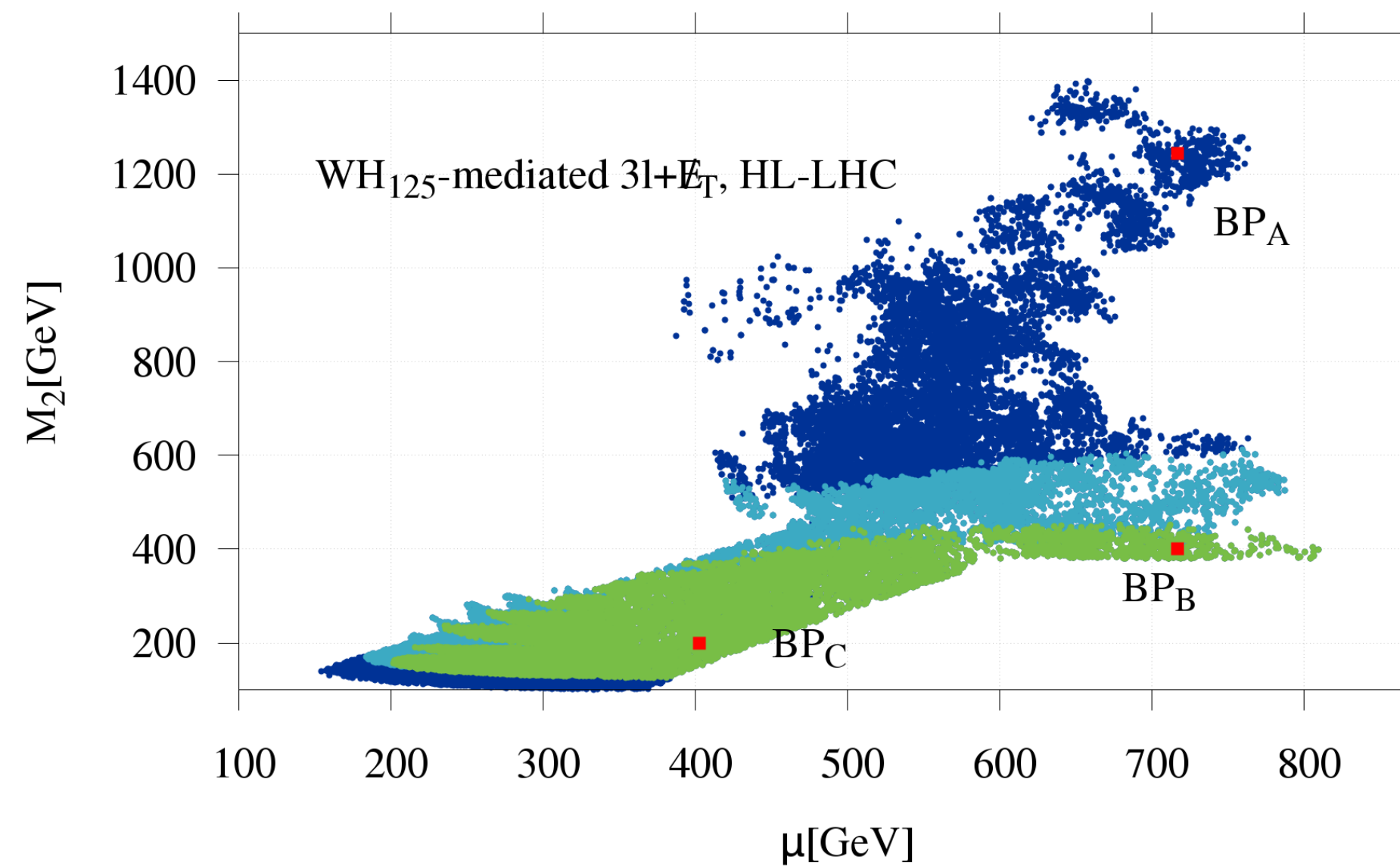
# $WH_{125}$ -mediated $3l + \cancel{E}_T$ at the HL-LHC



- Here, we use the optimized signal region cuts from ATL-PHYS-PUB-2014-010.

The figure at the bottom shows the projected reach on the currently allowed region  $\rightarrow$  direct searches in the  $WH_{125}$  mediated  $3l + \cancel{E}_T$  channel are more effective in probing the  $M_2 \lesssim \mu$  region of parameter space.

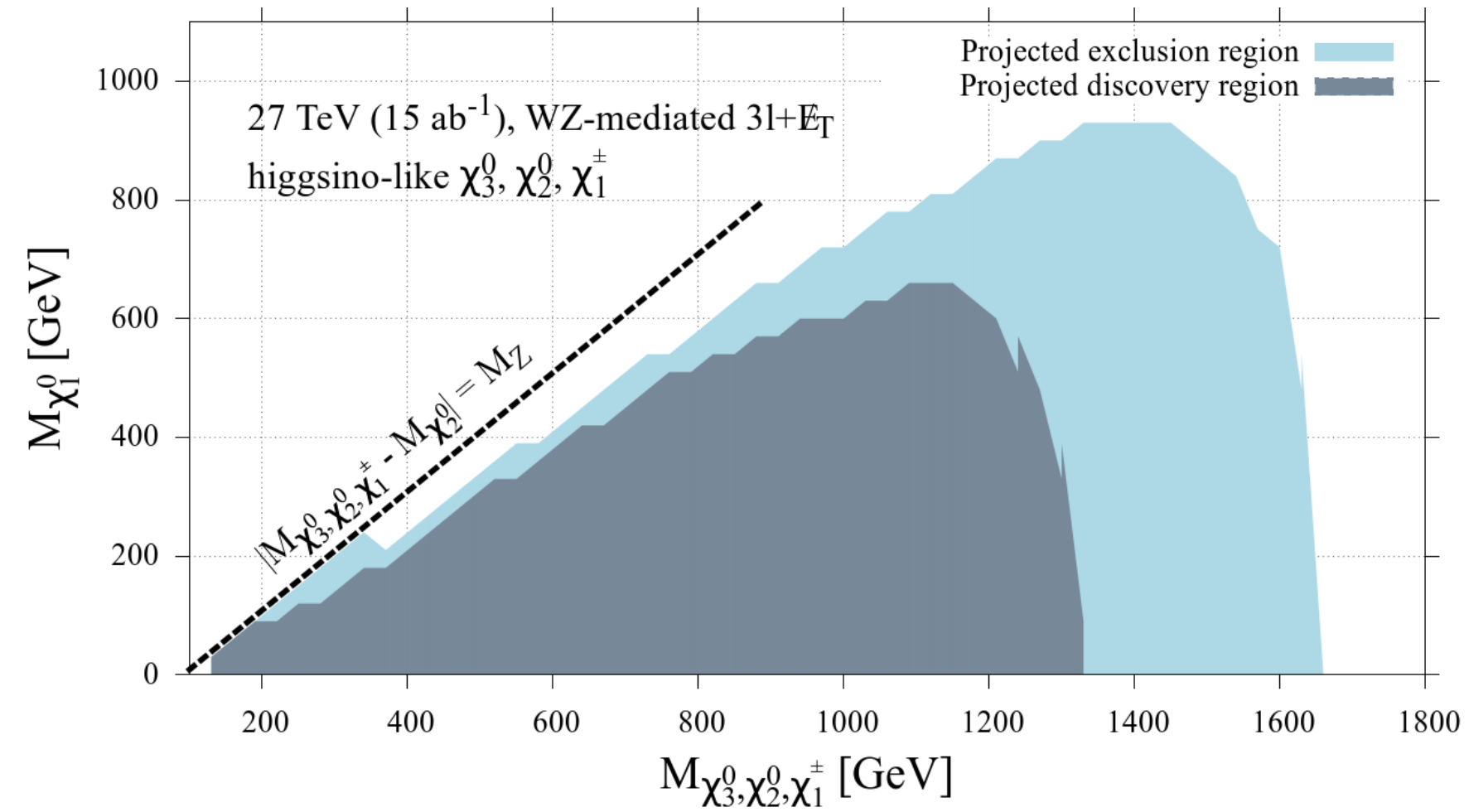
- $BP_B$  and  $BP_C$ : outside the reach of direct searches in  $WZ$  mediated  $3l + \cancel{E}_T$ , but fall within the discovery reach of direct searches in the  $WH_{125}$  mediated channel.
- Similarly, the  $M_2 \lesssim 150$  GeV region in this figure shows  $5\sigma$  sensitivity via the  $WZ$  mediated  $3l + \cancel{E}_T$  search channel.
- We observe a striking complementarity in the search power via  $WZ$  and  $WH_{125}$  mediated  $3l + \cancel{E}_T$  search channels..



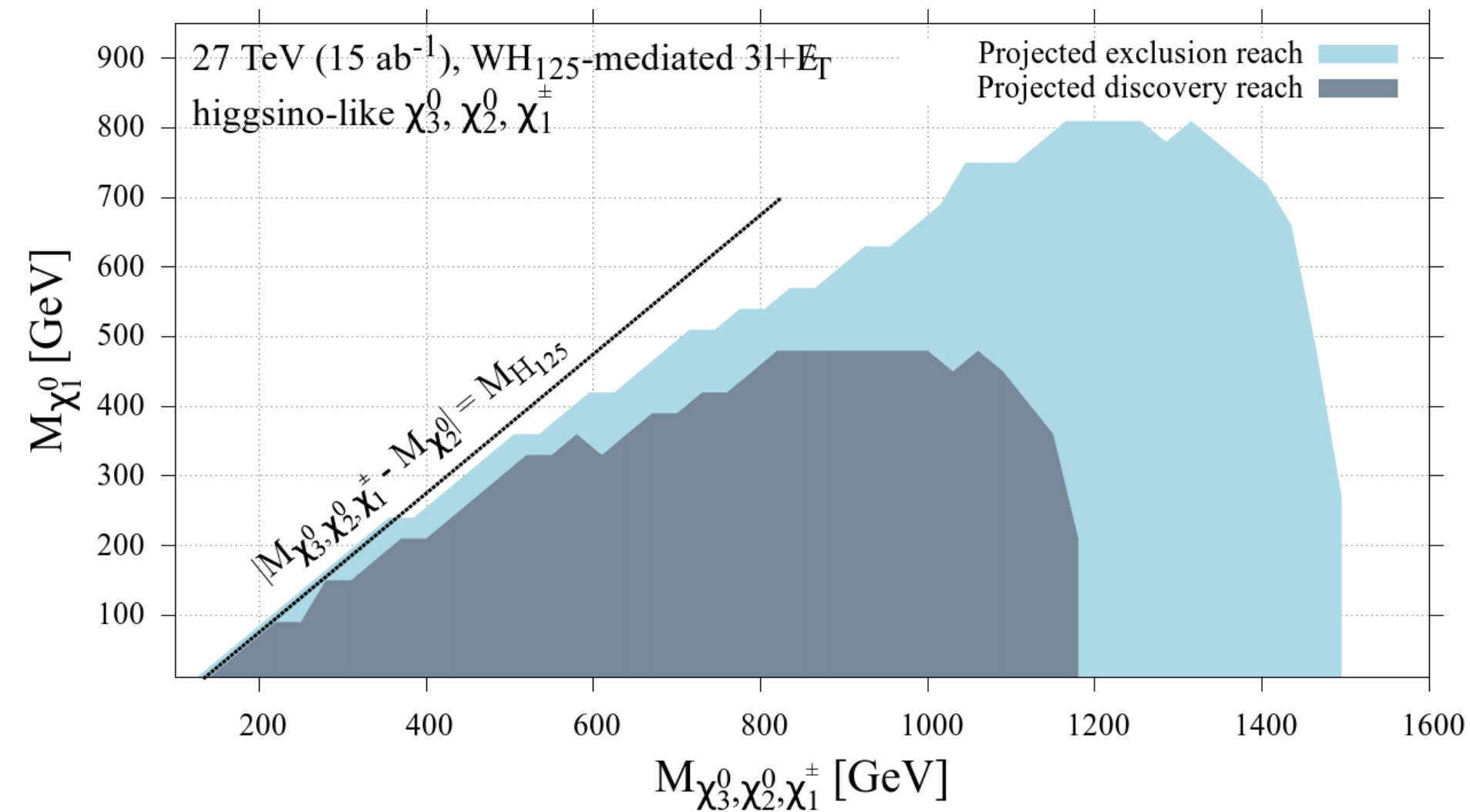
# Projected reach of doublet higgsino searches at the HE-LHC

**Color code:** Grey: projected discovery region, light blue: projected exclusion region

- We perform our own collider analysis and 10 optimized signal regions are considered.
- Considerable improvement over its HL-LHC counterpart. **Projected exclusion reach at the HL-LHC was only up to  $\sim 1000$  GeV for massless  $\tilde{\chi}_1^0$ .**



- We optimize 7 different signal regions to perform this search.
- Projected exclusion reach at the HL-LHC was only up to  $\sim 600$  GeV.



# Scope of other complementary search channels in $BP_B$

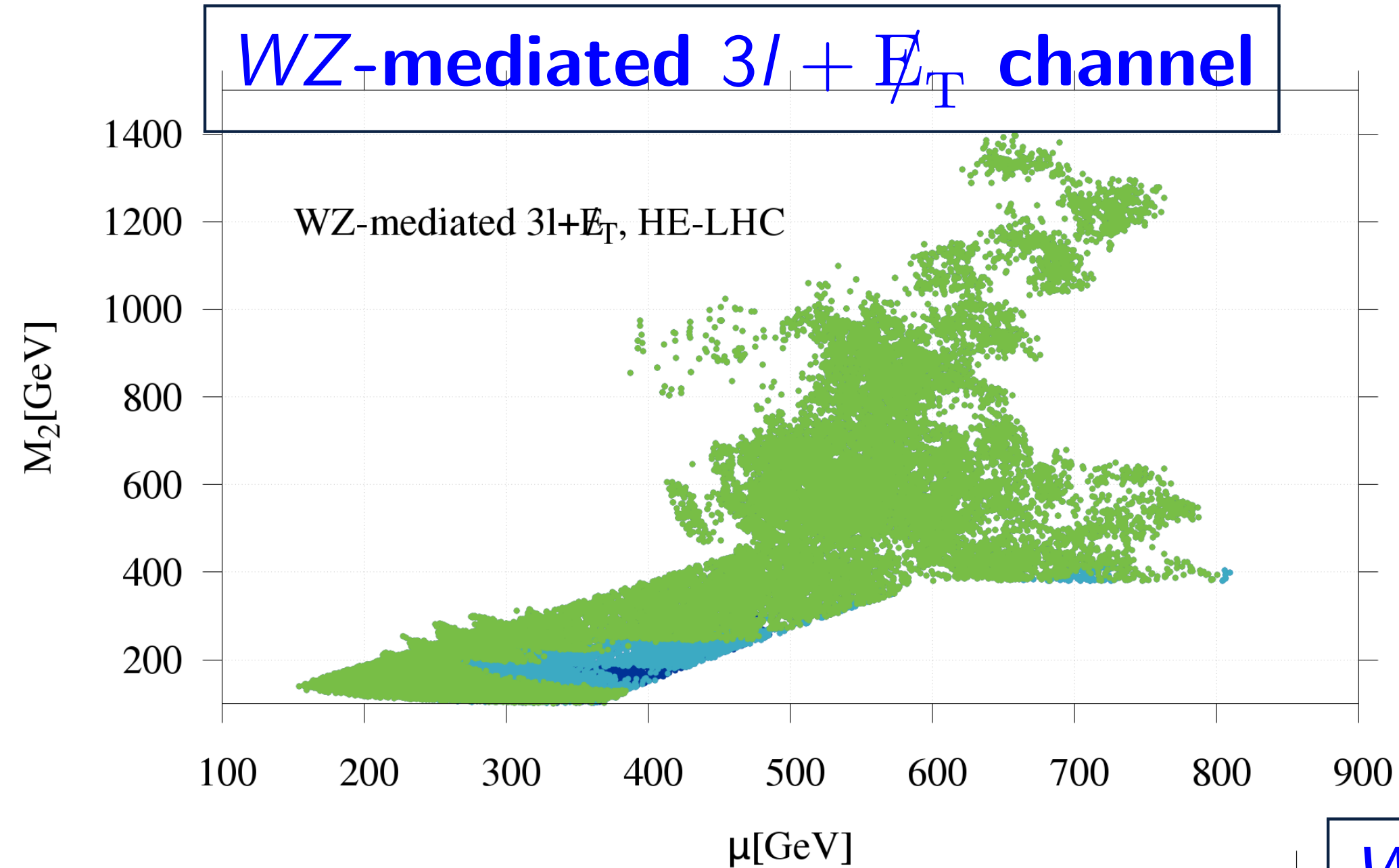
	$\tilde{\chi}_1^0$	$\tilde{\chi}_2^0$	$\tilde{\chi}_3^0$	$\tilde{\chi}_4^0$	$\tilde{\chi}_1^\pm$	$\tilde{\chi}_2^\pm$
Mass [GeV]	60.4	421	734	742	421	741
wino %	$10^{-5}$	0.96	$2 \times 10^{-3}$	0.04	0.94	0.06
higgsino %	$10^{-4}$	0.04	0.99	0.96	0.06	0.94
Singlino fraction in $\tilde{\chi}_1^0$ : 0.99			$M_{H_1} = 97.2$ GeV, $M_{A_1} = 99$ GeV			
Cross-section (fb)	$\tilde{\chi}_2^0 \tilde{\chi}_1^\pm$	$\tilde{\chi}_2^0 \tilde{\chi}_2^\pm$	$\tilde{\chi}_3^0 \tilde{\chi}_1^\pm$	$\tilde{\chi}_3^0 \tilde{\chi}_2^\pm$	$\tilde{\chi}_4^0 \tilde{\chi}_1^\pm$	$\tilde{\chi}_4^0 \tilde{\chi}_2^\pm$
$\sqrt{s} = 14$ TeV	104	0.27	0.28	2.1	0.25	2.3
$\sqrt{s} = 27$ TeV	363	1.1	1.1	10.2	1.0	11.2
Branching ratio	$\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 Z$ (0.04), $\tilde{\chi}_1^0 H_{125}$ (0.82), $\tilde{\chi}_1^0 H_1$ (0.14)					
	$\tilde{\chi}_3^0 \rightarrow \tilde{\chi}_1^0 Z$ (0.13), $\tilde{\chi}_1^0 H_{125}$ (0.10), $\tilde{\chi}_1^0 H_1$ (0.01), $\tilde{\chi}_1^\pm W^\mp$ (0.51), $\tilde{\chi}_2^0 Z$ (0.23), $\tilde{\chi}_2^0 H_{125}$ (0.01)					
	$\tilde{\chi}_4^0 \rightarrow \tilde{\chi}_1^0 Z$ (0.12), $\tilde{\chi}_1^0 H_{125}$ (0.11), $\tilde{\chi}_1^\pm W^\mp$ (0.53) $\tilde{\chi}_4^0 \rightarrow \tilde{\chi}_2^0 Z$ (0.02), $\tilde{\chi}_2^0 H_{125}$ (0.21)					
Significance at HL-LHC: $WZ$ mediated $3l + \cancel{E}_T$ : 1.5, $WH_{125}$ mediated $3l + \cancel{E}_T$ : 5.3						
Significance at HE-LHC: $WZ$ mediated $3l + \cancel{E}_T$ : 4.4, $WH_{125}$ mediated $3l + \cancel{E}_T$ : 34						

- Notice the presence of other cascade decay modes:
  - ①  $\tilde{\chi}_3^0$  can decay into  $\tilde{\chi}_2^0 Z$ , while  $\tilde{\chi}_2^0$  can decay into  $\tilde{\chi}_1^0 H_1$  or  $\tilde{\chi}_1^0 H_{125}$ .
  - ②  $\tilde{\chi}_3^0$  is dominantly produced in association with  $\tilde{\chi}_2^\pm$ , which can decay into  $Z/H_{125} + \tilde{\chi}_1^\pm$  or  $W^\pm + \tilde{\chi}_2^0/\tilde{\chi}_1^0$  with appreciable rates.
  - ③  $\tilde{\chi}_3^0 \tilde{\chi}_2^\pm$  can eventually lead to rich final states including  $VV + \cancel{E}_T$  or  $V/Z/H_1 + \cancel{E}_T$ . Although,  $\sigma(\tilde{\chi}_3^0 \tilde{\chi}_2^\pm)$  is small for  $BP_B$ , but one obtain points with relatively larger  $\sigma(\tilde{\chi}_3^0 \tilde{\chi}_2^\pm)$ , for. eg.  $BP_C$  with  $\sigma(\tilde{\chi}_3^0 \tilde{\chi}_2^\pm) \sim 24.8$  fb.
- $3l + \cancel{E}_T$  channels might not be most the efficient ones in the presence of these cascade decay channels.
- **Dedicated searches beyond the scope of this work will be needed to explore these novel signals.**

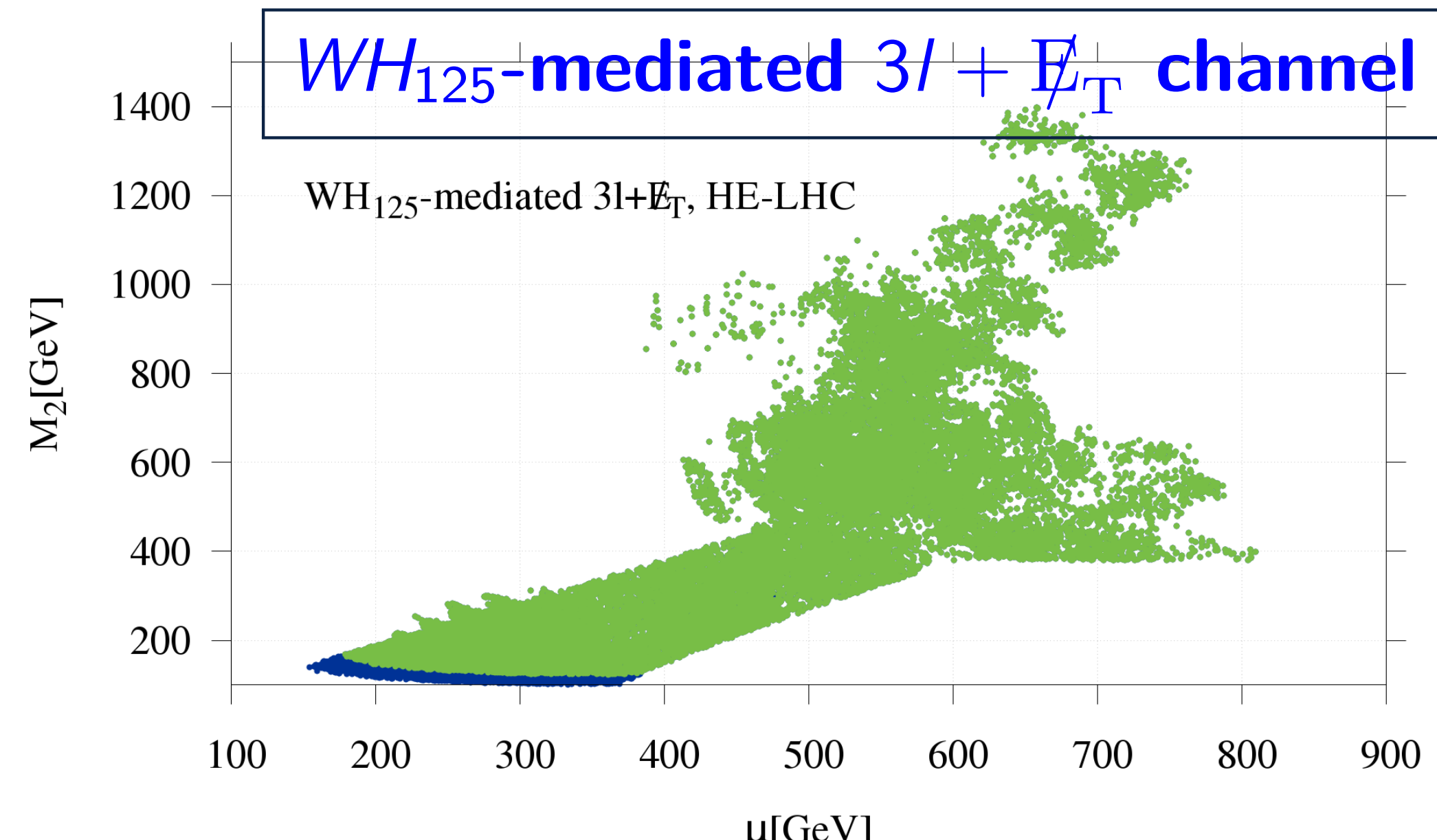


# Projected reach of EW ino searches at the HE-LHC on the allowed parameter space

Color code: Green:  $S_\sigma > 5$ , light blue:  $2 < S_\sigma < 5$ , dark blue:  $S_\sigma < 2$



The HE-LHC provides a larger discovery opportunity than the HL-LHC for the detection of NMSSM inos with light LSP.



Combination of EW ino searches in the WZ and WH<sub>125</sub> mediated  $3l + \cancel{E}_T$  channel will probe all the currently allowed parameter space points at discovery potential.

# Future directions

## Light Higgs phenomenology

- Benchmark studies focused on exploring the parameter region with light  $H_1/A_1$  at the future high-energy colliders through dedicated searches in various final states, viz. the  $4\tau$  final state.
- Study of complementarity between the direct light Higgs search projections and the invisible Higgs width measurement capability of the linear colliders.

## The alternate probes for electroweakino searches

- Benchmark points  $BP_B$  and  $BP_C$  indicated towards the possibility of having cascade decays which culminate in final states which are different from the traditional search channels.
- These novel search modes might provide complementary probes for benchmark points with cascade decays and could increase the discovery reach at the future colliders.

## A comprehensive study of the light singlino region of parameter space

- We find light singlino-like LSPs with mass as small as  $\sim 1$  GeV compatible with the current collider, astrophysical and cosmological constraints.
- Despite having a pseudoscalar Higgs as the mediator, the annihilation cross-section of these light singlinos is found to be small enough to avoid any implications from the current indirect constraints while also generating an under-abundant relic.
- This sector would require a more careful study.

# Benchmark points

Benchmark points	Input parameters
$BP_A$	$\lambda = 0.3, \kappa = 0.01, \tan \beta = 9.5, A_\lambda = 6687 \text{ GeV}, A_\kappa = 5.2 \text{ GeV},$ $\mu = 717 \text{ GeV}, M_2 = 1244 \text{ GeV}, M_3 = 2301 \text{ GeV}$
$BP_B$	$\lambda = 0.44, \kappa = 0.02, \tan \beta = 11.8, A_\lambda = 8894 \text{ GeV}, A_\kappa = -57 \text{ GeV},$ $\mu = 717 \text{ GeV}, M_2 = 400 \text{ GeV}, M_3 = 4323 \text{ GeV}$
$BP_C$	$\lambda = 0.08, \kappa = 3 \times 10^{-4}, \tan \beta = 18, A_\lambda = 6563 \text{ GeV}, A_\kappa = -7.9 \text{ GeV},$ $\mu = 403 \text{ GeV}, M_2 = 200 \text{ GeV}, M_3 = 3080 \text{ GeV}$
$BP_D$	$\lambda = 0.44, \kappa = 0.02, \tan \beta = 15.6, A_\lambda = 585 \text{ GeV}, A_\kappa = 9501 \text{ GeV},$ $\mu = 585 \text{ GeV}, M_2 = 952 \text{ GeV}, M_3 = 4457 \text{ GeV}$
$BP_E$	$\lambda = 0.27, \kappa = 0.02, \tan \beta = 11.6, A_\lambda = 5875 \text{ GeV}, A_\kappa = 12 \text{ GeV},$ $\mu = 518 \text{ GeV}, M_2 = 696 \text{ GeV}, M_3 = 3634 \text{ GeV}$
$BP_F$	$\lambda = 0.30, \kappa = 0.01, \tan \beta = 11.2, A_\lambda = 6319 \text{ GeV}, A_\kappa = 17 \text{ GeV},$ $\mu = 571 \text{ GeV}, M_2 = 555 \text{ GeV}, M_3 = 2687 \text{ GeV}$
$BP_G$	$\lambda = 0.42, \kappa = 0.02, \tan \beta = 15.9, A_\lambda = 8638 \text{ GeV}, A_\kappa = 43.4 \text{ GeV},$ $\mu = 515 \text{ GeV}, M_2 = 396 \text{ GeV}, M_3 = 2903 \text{ GeV}$
$BP_H$	$\lambda = 0.02, \kappa = 7 \times 10^{-5}, \tan \beta = 25.5, A_\lambda = 7348 \text{ GeV}, A_\kappa = -7.3 \text{ GeV},$ $\mu = 302 \text{ GeV}, M_2 = 204 \text{ GeV}, M_3 = 2239 \text{ GeV}$
$BP_I$	$\lambda = 0.02, \kappa = 6 \times 10^{-5}, \tan \beta = 27.6, A_\lambda = 6924 \text{ GeV}, A_\kappa = -5.7 \text{ GeV},$ $\mu = 262 \text{ GeV}, M_2 = 210 \text{ GeV}, M_3 = 2217 \text{ GeV}$