

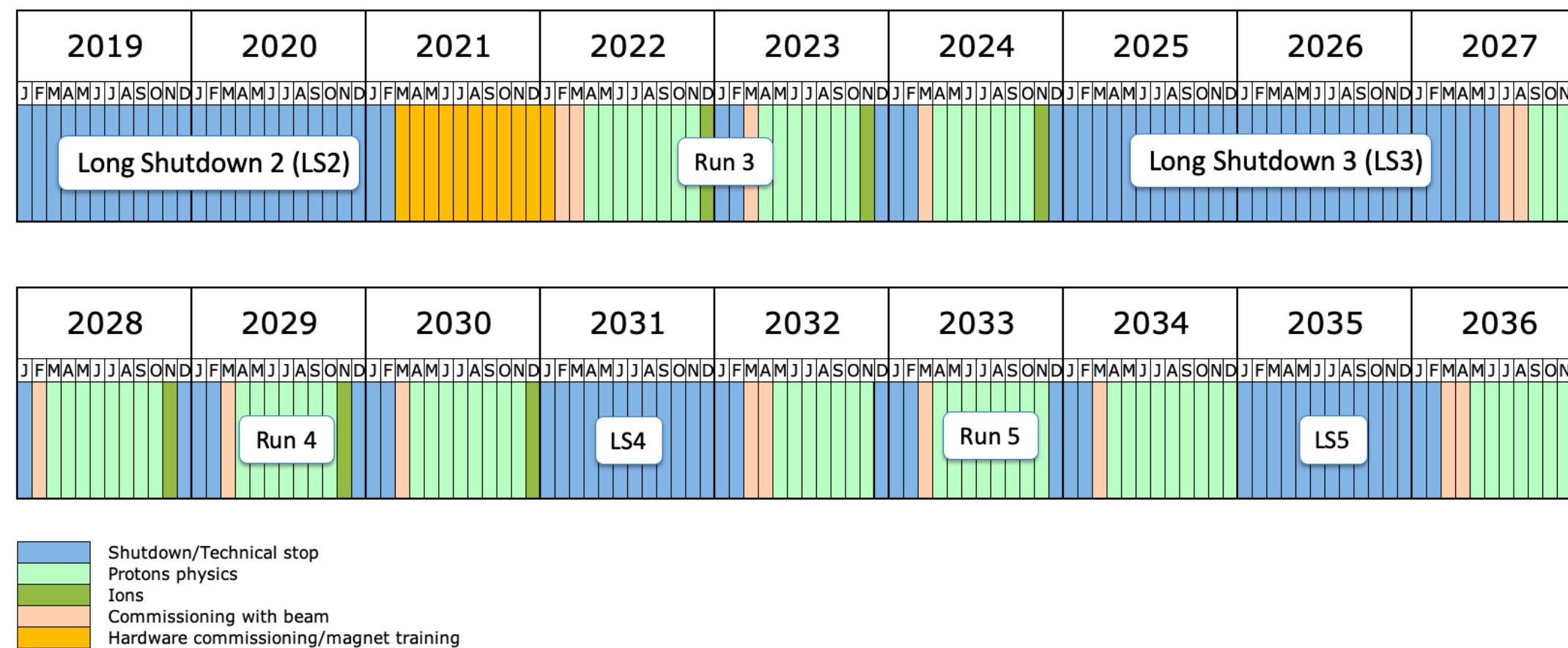
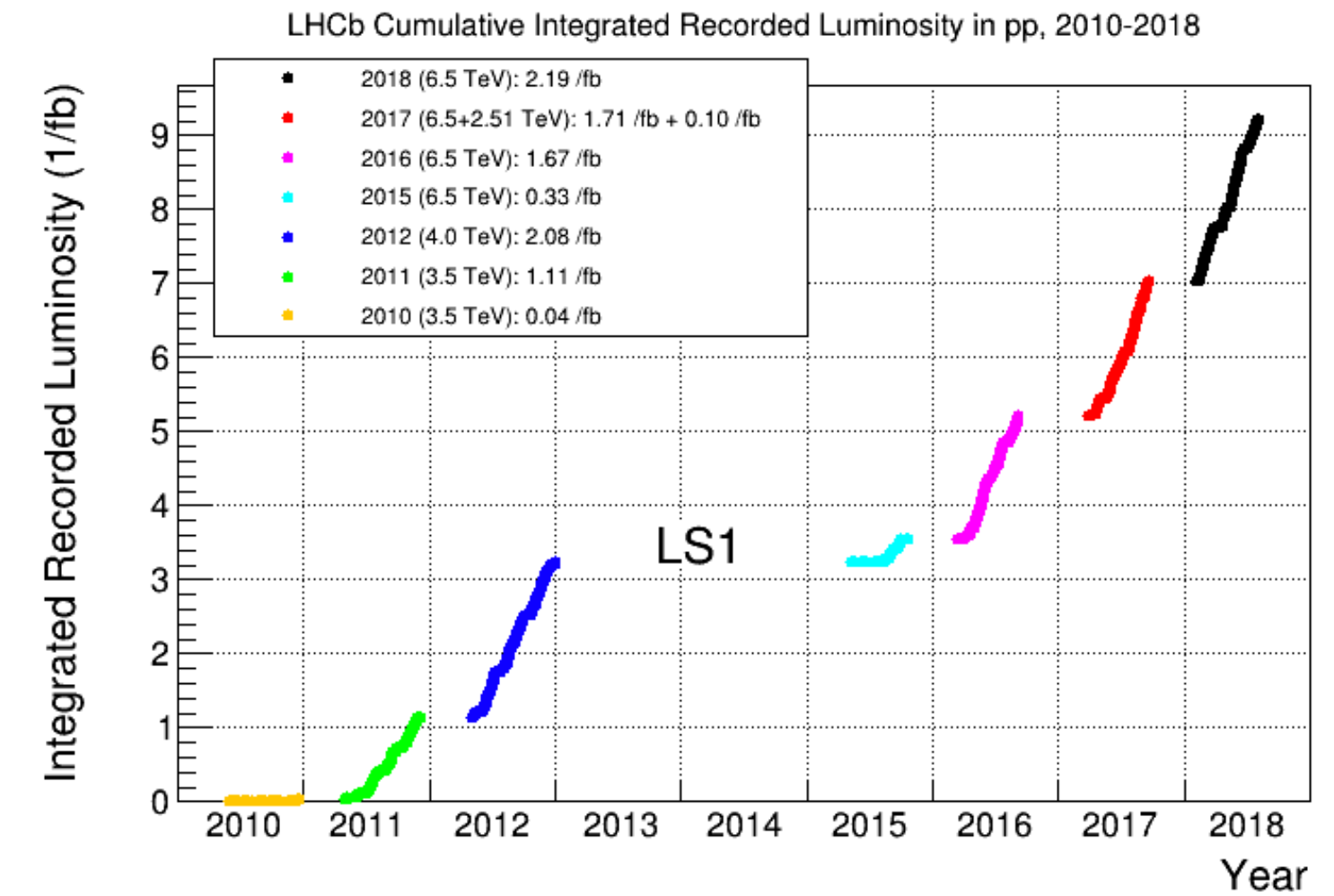


# Experimental overview and prospects of $|V_{ub}|$ and $|V_{cb}|$ at LHCb

**Snowmass mini-workshop on  $|V_{ub}|$  and  $|V_{cb}|$**

# How are we doing

- LHCb has collected  $9\text{fb}^{-1}$  of data.
- We are currently commissioning the first upgrade.
- Hope to take another  $\sim 15\text{fb}^{-1}$  in run III without the limitations of a hardware trigger.



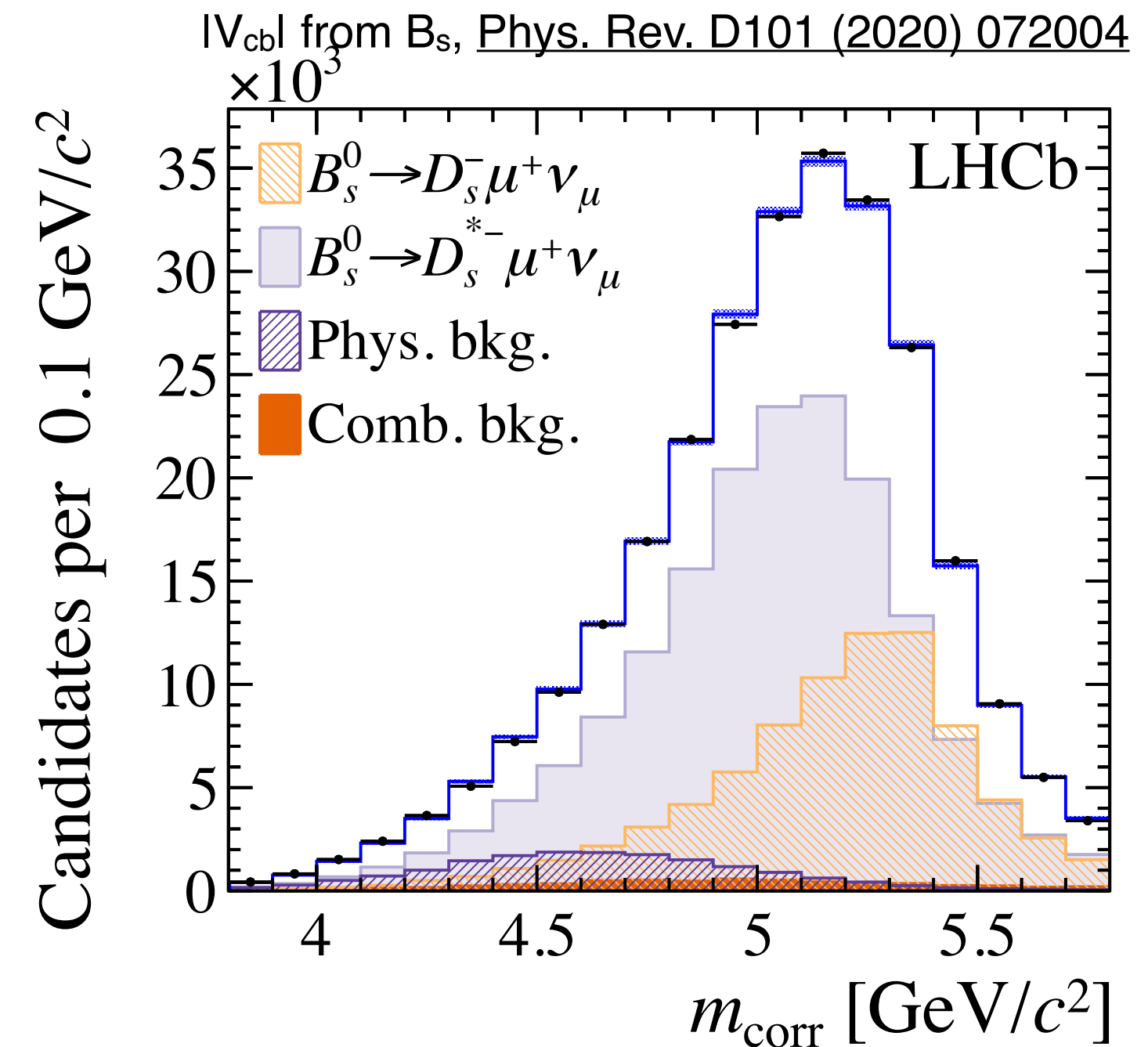
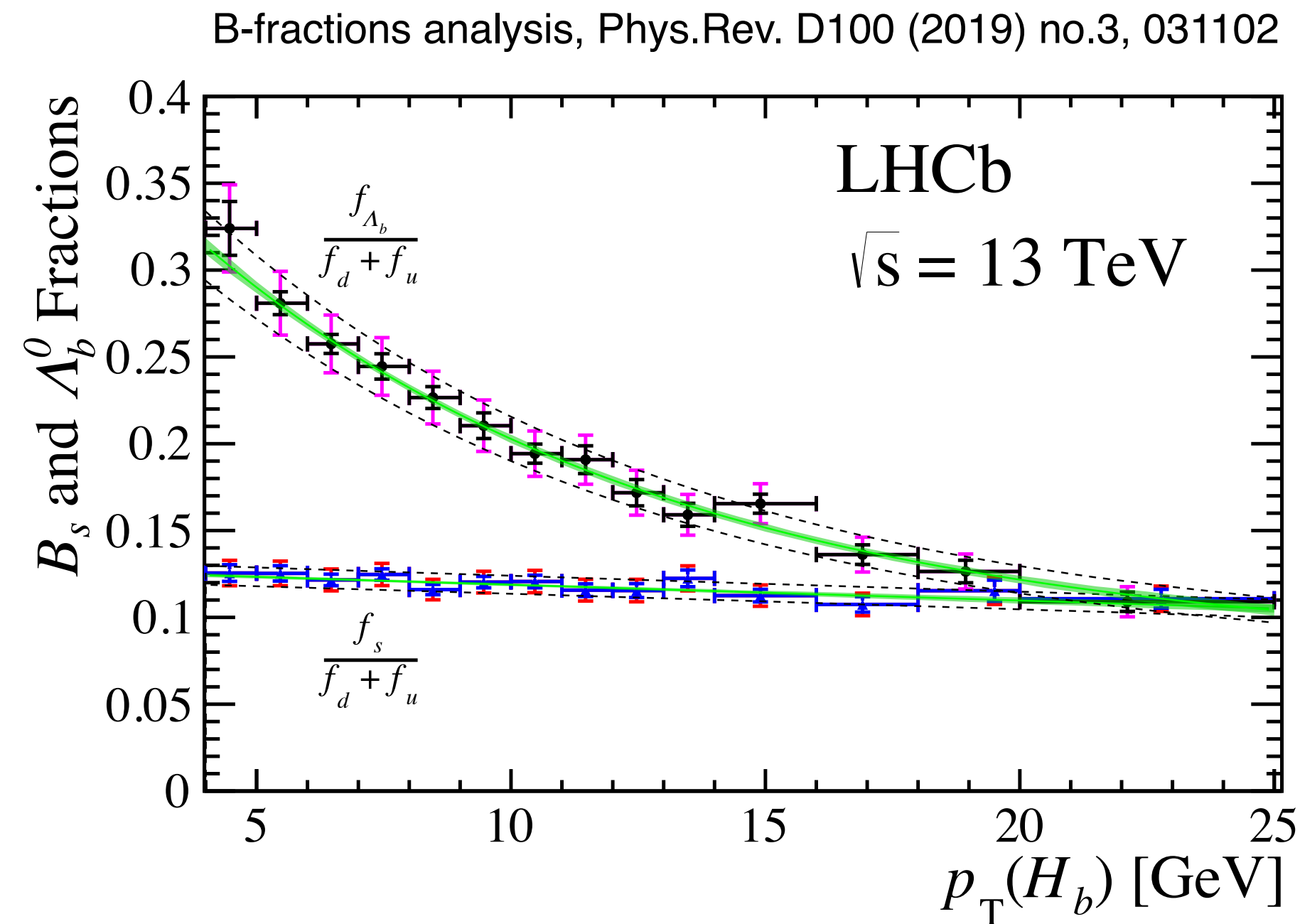
- Due to the pandemic, run III was delayed until 2022.

- Plans for upgrade II strongly supported by european strategy for particle physics.

been developed. *The successful completion of the high-luminosity upgrade of the machine and detectors should remain the focal point of European particle physics, together with continued innovation in experimental techniques. The full physics potential of the LHC and the HL-LHC, including the study of flavour physics and the quark-gluon plasma, should be exploited.*

# Semileptonic decays at LHCb

- Do not have direct access to absolute branching fractions.
- Do have access to all b-hadron species.
- Have very large signal yields.



# Measurements of $|V_{ub}|/|V_{cb}|$ at LHCb

- Select  $b \rightarrow u$  decay and fit corrected mass.
- Normalise to convenient  $b \rightarrow c$  transition
  - same b-hadron
  - well known FF
  - charm hadron BF
- Convert ratio of branching fractions using LQCD and/or LCSR.

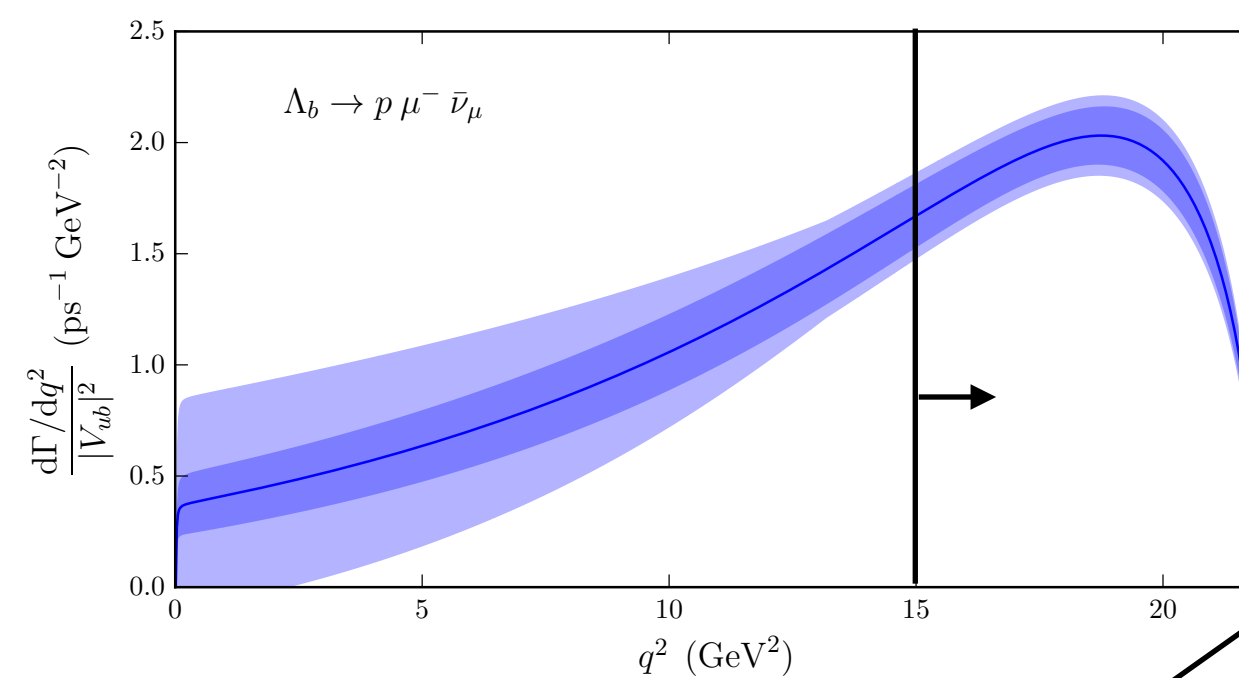
e.g. 
$$\frac{\mathcal{B}(\Lambda_b \rightarrow p \mu^- \bar{\nu}_\mu)_{q^2 > 15 \text{ GeV}^2/c^4}}{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c \mu \nu)_{q^2 > 7 \text{ GeV}^2/c^4}}$$



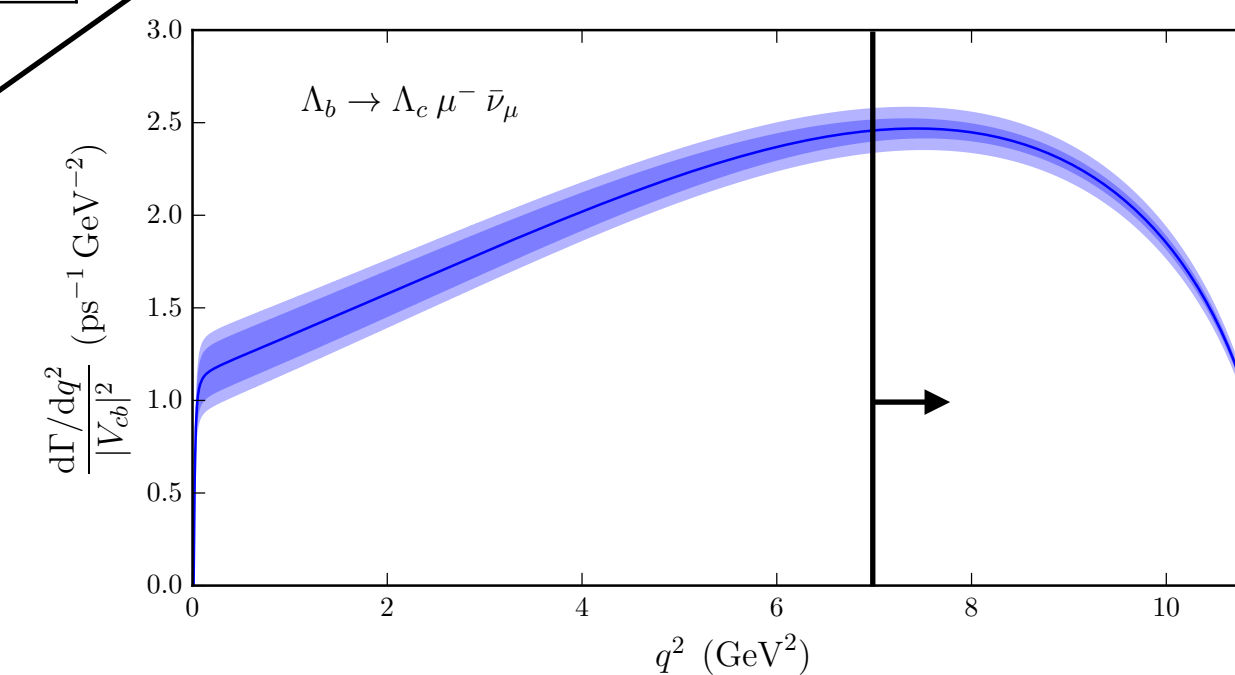
# Measurement with $\Lambda_b^0 \rightarrow p\mu\nu$ decays

- Measure ratio:

$$\frac{\mathcal{B}(\Lambda_b \rightarrow p\mu^- \bar{\nu}_\mu)_{q^2 > 15 \text{ GeV}^2/c^4}}{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c \mu \nu)_{q^2 > 7 \text{ GeV}^2/c^4}}$$



Detmold, Lehner, Meinel, Phys. Rev. D 92, 034503 (2015)



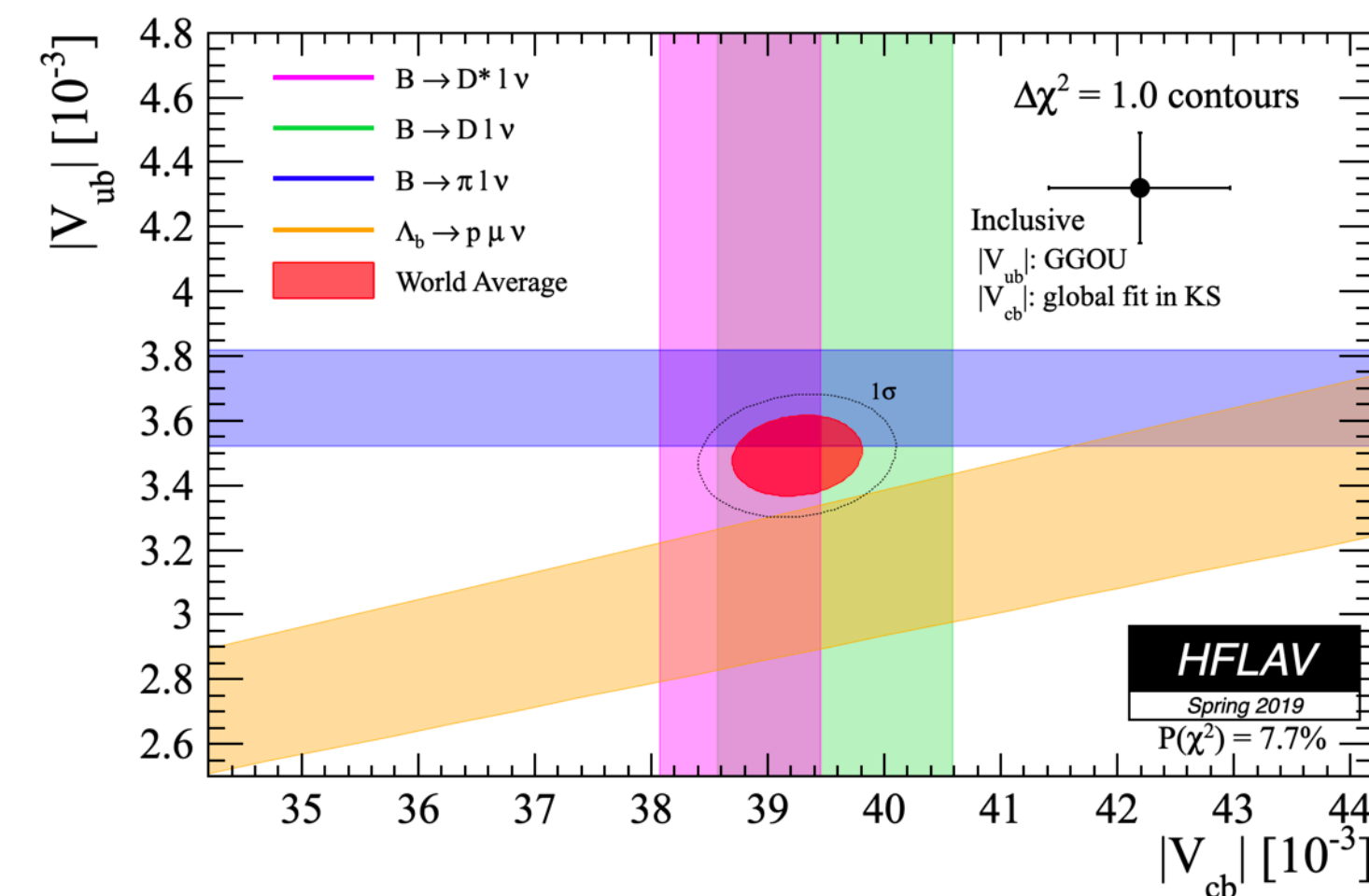
- Uncertainty split equally between experiment and lattice.

- The former benefits from updates to  $\mathcal{B}(\Lambda_c \rightarrow pK\pi)$

$$\frac{|V_{ub}|}{|V_{cb}|} = 0.083 \pm 0.004 \pm 0.004$$

↑  
Expt

↑  
Lattice



$|V_{ub}|/|V_{cb}|$  from  $B_s^0 \rightarrow K^+ \mu^- \nu$

LHCb, [arXiv:2012.05143](https://arxiv.org/abs/2012.05143)

- Measure ratio  $\frac{\mathcal{B}(B_s^0 \rightarrow K^- \mu^+ \nu_\mu)}{\mathcal{B}(B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu)}$  for new  $|V_{ub}|/|V_{cb}|$  measurement with  $B_s$  decays.
- Do it to two  $q^2$  regions, to exploit both LCSR and LQCD calculations.

$$\frac{\mathcal{B}(B_s^0 \rightarrow K^- \mu^+ \nu_\mu)_{q^2 < 7}}{\mathcal{B}(B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu)_{\text{Full } q^2}}$$

$$\frac{\mathcal{B}(B_s^0 \rightarrow K^- \mu^+ \nu_\mu)_{q^2 > 7}}{\mathcal{B}(B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu)_{\text{Full } q^2}}$$

- In both cases LQCD is used to determine the denominator, but the uncertainty is sub-dominant.
- $D_s$  mesons reconstructed with the  $D_s \rightarrow KK\pi$  decay mode.

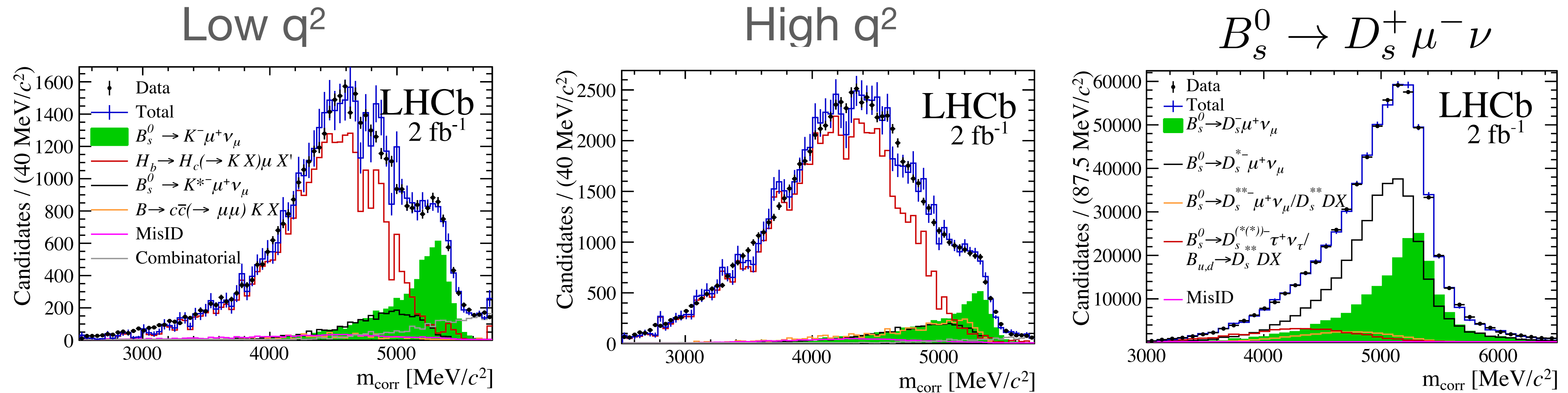
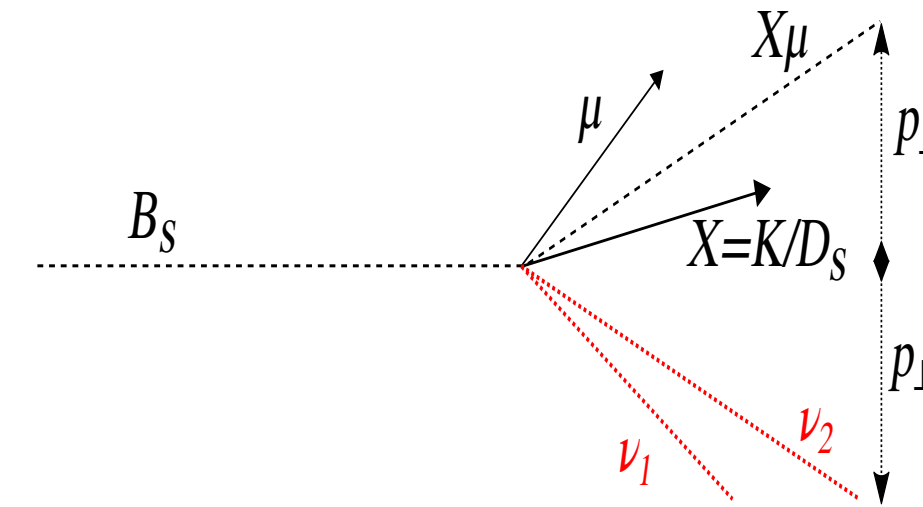
$$B_s^0 \rightarrow K^+ \mu^- \nu \quad \text{vs} \quad \Lambda_b^0 \rightarrow p \mu \nu$$

Decay	$\Lambda_b^0$	$B_s^0$
theory error	5%	$\sim 5\%$
prod frac	20%	10%
BF	$4 \times 10^{-4}$	$1 \times 10^{-4}$
$\mathcal{B}(X_c)$ error	$\pm 5\%$	$\pm 2.8\%$
background	$\Lambda_c^+$	$\Lambda_c^+, D_s, D^+, D^0$

- $X_c$  branching fraction uncertainties scaled up the PDG. Important to get more measurements on these.
- Both Belle-II and BES-III very important here.

# $B_s^0 \rightarrow K^+ \mu^- \nu$ and $B_s^0 \rightarrow D_s^+ \mu^- \nu$ fits LHCb, [arXiv:2012.05143](https://arxiv.org/abs/2012.05143)

- Fit corrected mass  $M_{corr} = \sqrt{M_{X\mu}^2 + p_{\perp}^2} + p_{\perp}$



- Shapes for signal reasonably insensitive to form factors.
- Backgrounds more affected. Form factor predictions for e.g.  $B_s \rightarrow K^{(*)}$  welcome.

# Branching fraction results

- Relative efficiency is between two-track and four-track final state.
  - Resulting systematic uncertainties due to effects such as tracking and trigger.
- Branching fraction ratios determined to be

$$\frac{\mathcal{B}(B_s^0 \rightarrow K^- \mu^+ \nu_\mu)_{q^2 < 7}}{\mathcal{B}(B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu)_{\text{Full } q^2}} = (1.66 \pm 0.08(\text{stat}) \pm 0.07(\text{syst}) \pm 0.05(D_s)) \times 10^{-3}$$

$$\frac{\mathcal{B}(B_s^0 \rightarrow K^- \mu^+ \nu_\mu)_{q^2 > 7}}{\mathcal{B}(B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu)_{\text{Full } q^2}} = (3.25 \pm 0.21(\text{stat}) \pm_{-0.17}^{+0.16}(\text{syst}) \pm 0.09(D_s)) \times 10^{-3}$$

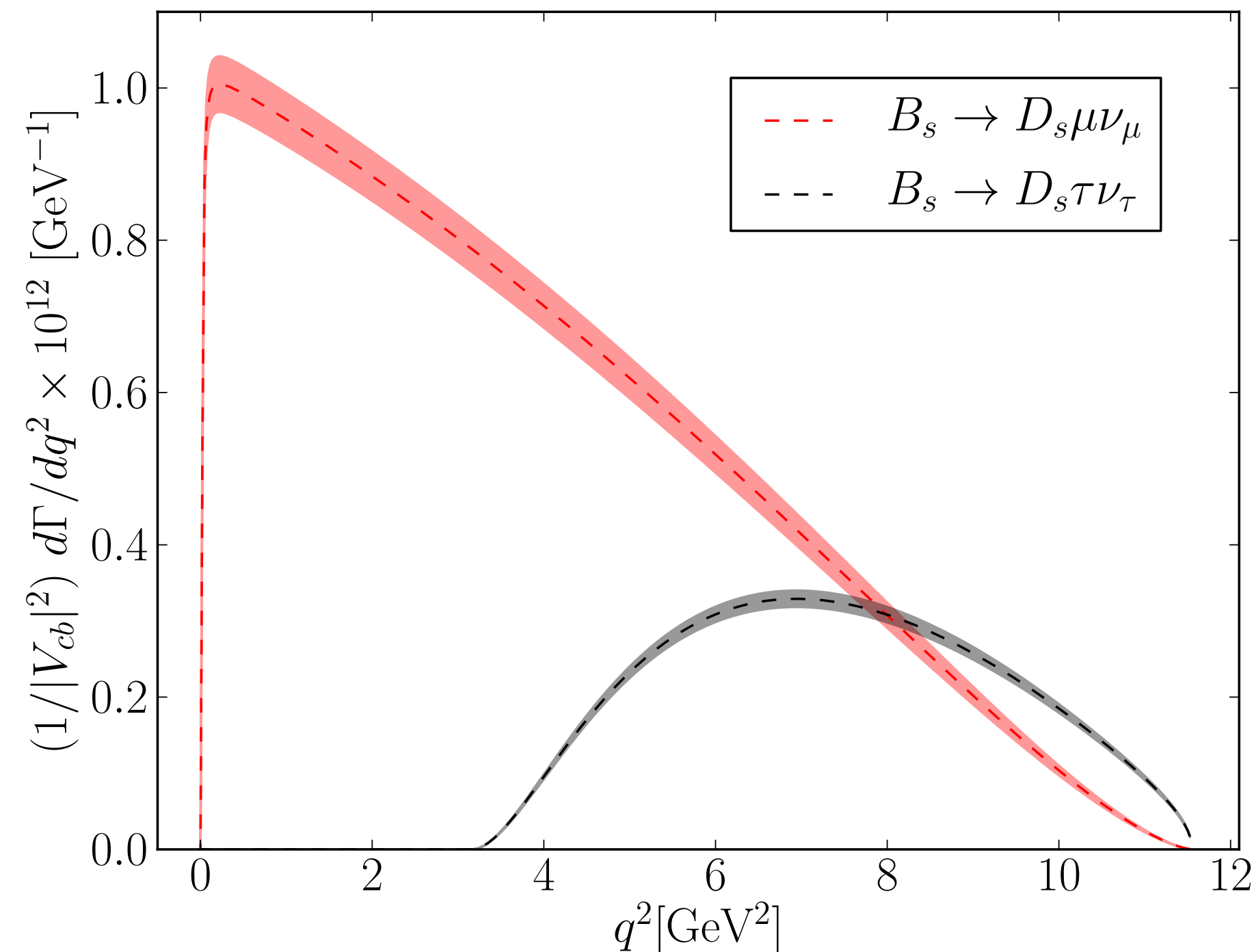
- The branching fractions are less limited by the external input c.f.  $\Lambda_b^0$  case.



# $B_s^0 \rightarrow D_s^+ \mu \nu$ inputs

- For both  $B \rightarrow K$  measurements, we use lattice QCD for the  $B_s^0 \rightarrow D_s^+ \mu \nu$  form factors in full range.
- Use most precise calculation from HPQCD.
- Would be interesting to see a LCSR calculation to be consistent at low  $q^2$ .

McLean, Davies, Koponen, Lytle [HPQCD]: Phys. Rev. D 101, 074513 (2020)

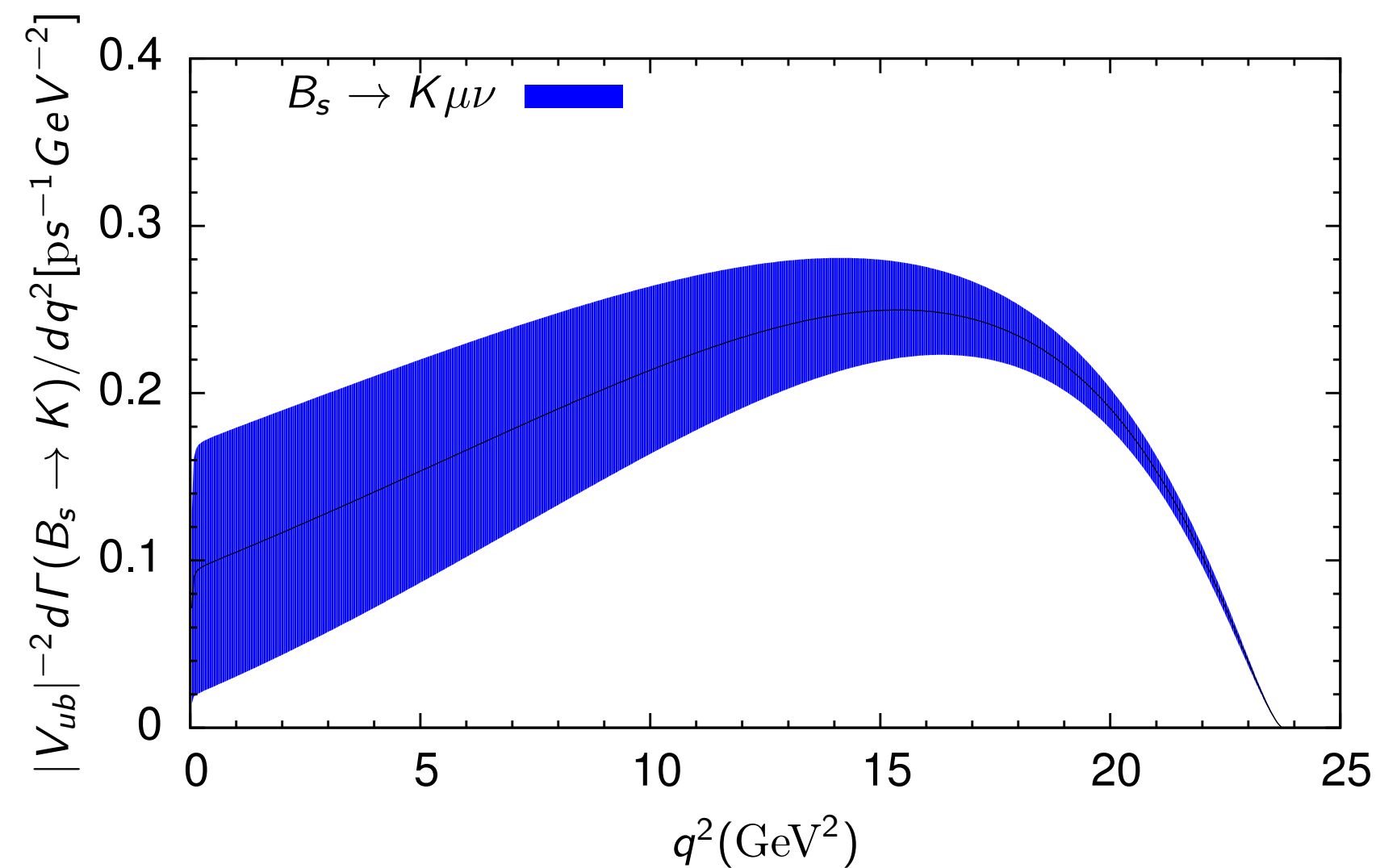


- Uncertainties that affect efficiencies and fit shapes included as small systematics in the measurements.

# High $q^2$ inputs

- Many precise  $B_s^0 \rightarrow K$  lattice calculations available [1-4].
- In the end, we chose the one which minimised the uncertainty on  $|V_{ub}|/|V_{cb}|$ .
  - Of course the best now would be to use the recent [FLAG average](#).

We use the MILC/FNAL calculation [4].



and get:

$$|V_{ub}|/|V_{cb}|(\text{high}) = 0.0946 \pm 0.0030 (\text{stat})_{-0.0025}^{+0.0024} (\text{syst}) \pm 0.0013 (D_s) \pm 0.0068 (\text{FF})$$

Large contribution to uncertainty from extrapolation.

[1] Bouchard et al [MILC], Phys. Rev. D 90, 054506 (2014)

[2] Flynn et al [RBC-UKQCD], Phys. Rev. D 91, 074510 (2015)

[3] Monahan et al [HPQCD], Phys. Rev. D 98, 114509 (2018)

[4] Bazanov et al [MILC/Fermilab], Phys. Rev. D 100, 034501 (2019)

# Correlated form factor uncertainties

- To treat correlated form factor uncertainties fully in the analysis, need full covariance matrix of simultaneous fit to  $B \rightarrow X_u$  and  $B \rightarrow X_c$  form factors.

Detmold, Lehner, Meinel, Phys. Rev. D 92, 034503 (2015)

$\Lambda_b \rightarrow p$	$a_0^{f^+}$	$a_1^{f^+}$	$a_2^{f^+}$	$a_0^{f^0}$	$a_1^{f^0}$	$a_2^{f^0}$	$a_0^{f^-}$	$a_1^{f^-}$	$a_2^{f^-}$	$a_0^{g^+}$	$a_1^{g^+}$	$a_2^{g^+}$	$a_0^{g^0}$	$a_1^{g^0}$	$a_2^{g^0}$	$a_0^{g^-}$	$a_1^{g^-}$	$a_2^{g^-}$	
$a_0^{f^+}$	1	-0.7671	0.2482	0.5337	-0.2670	-0.0922	0.5121	-0.2469	-0.0180	0.3774	-0.2148	-0.0472	0.4420	-0.2680	0.0018	-0.2284	-0.0231		
$a_1^{f^+}$	-0.7671	1	-0.6611	-0.2486	0.1617	0.0653	-0.2526	0.1671	0.0056	-0.2177	0.1480	0.0287	-0.2496	0.1849	-0.0169	0.1534	0.0147		
$a_2^{f^+}$	0.2482	-0.6611	1	-0.0792	0.0267	0.2795	-0.0035	-0.0120	0.0425	-0.0562	0.0382	0.0559	-0.0279	-0.0074	0.0870	0.0370	0.0469		
$a_0^{f^0}$	0.5337	-0.2486	-0.0792	1	-0.7202	0.2599	0.4581	-0.2052	-0.0146	0.4734	-0.2798	-0.0031	0.3860	-0.2266	-0.0115	-0.2781	0.0048		
$a_1^{f^0}$	-0.2670	0.1617	0.0267	-0.7202	1	-0.6947	-0.2404	0.1415	0.0128	-0.2964	0.2603	-0.0377	-0.2410	0.1694	0.0090	0.2610	-0.0279		
$a_2^{f^0}$	-0.0922	0.0653	0.2795	0.2599	-0.6947	1	0.0190	-0.0056	0.0297	-0.0019	-0.0529	0.1086	-0.0081	-0.0097	0.0664	-0.0568	0.0874		
$a_0^{f^-}$	0.5121	-0.2526	-0.0035	0.4581	-0.2404	0.0190	1	-0.7672	0.1031	0.3418	-0.1831	-0.0539	0.4313	-0.2713	0.0163	-0.1994	-0.0127		
$a_1^{f^-}$	-0.2469	0.1671	-0.0120	-0.2052	0.1415	-0.0056	-0.7672	1	-0.5040	-0.1983	0.1259	0.0378	-0.2429	0.1907	-0.0274	0.1347	0.0083		
$a_2^{f^-}$	-0.0180	0.0056	0.0425	-0.0146	0.0128	0.0297	0.1031	-0.5040	1	-0.0271	0.0045	0.0524	-0.0286	0.0090	0.0530	0.0120	0.0187		
$a_0^{g^+}$	0.3774	-0.2177	-0.0562	0.4734	-0.2964	-0.0019	0.3418	-0.1983	-0.0271	1	-0.6751	0.2299	0.5903	-0.2849	-0.0084	-0.6325	0.1314		
$a_1^{g^+}$	-0.2148	0.1480	0.0382	-0.2798	0.2603	-0.0529	-0.1831	0.1259	0.0045	-0.6751	1	-0.6972	-0.2576	0.1666	-0.0268	0.6832	-0.1976		
$a_2^{g^+}$	-0.0472	0.0287	0.0559	-0.0031	-0.0377	0.1086	-0.0539	0.0378	0.0524	0.2299	-0.6972	1	-0.0760	0.0463	0.2693	-0.3207	0.2419		
$a_0^{g^0}$	0.4420	-0.2496	-0.0279	0.3860	-0.2410	-0.0081	0.4313	-0.2429	-0.0286	0.5903	-0.2576	-0.0760	1	-0.7868	0.3673	-0.2892	-0.0105		
$a_1^{g^0}$	-0.2680	0.1849	-0.0074	-0.2266	0.1694	-0.0097	-0.2713	0.1907	0.0090	-0.2849	0.1666	0.0463	-0.7868	1	-0.7393	0.1798	0.0107		
$a_2^{g^0}$	0.0018	-0.0169	0.0870	-0.0115	0.0090	0.0664	0.0163	-0.0274	0.0530	-0.0084	-0.0268	0.2693	0.3673	-0.7393	1	0.0302	0.0637		
$a_0^{g^-}$	-0.2284	0.1534	0.0370	-0.2781	0.2610	-0.0568	-0.1994	0.1347	0.0120	-0.6325	0.6832	-0.3207	-0.2892	0.1798	0.0302	1	-0.6223		
$a_1^{g^-}$	-0.0231	0.0147	0.0469	0.0048	-0.0279	0.0874	-0.0127	0.0083	0.0187	0.1314	-0.1976	0.2419	-0.0105	0.0107	0.0637	-0.6223	1		
$a_2^{g^-}$																			1

TABLE XI. Correlation matrices of the higher-order form factor parameters for  $\Lambda_b \rightarrow p$  (top) and  $\Lambda_b \rightarrow \Lambda_c$  (bottom).

Monahan et al, Phys. Rev. D 98, 114509 (2018)

TABLE XI. Covariance matrix for the coefficients of  $z$ -expansion and the corresponding Blaschke factors for the simultaneous fit to the  $B_s \rightarrow K\ell\nu$  and  $B_s \rightarrow D_s\ell\nu$  decays. The rows correspond to the columns, moving from top to bottom and left to right, respectively.

$a_1^{(0),K}$	$a_2^{(0),K}$	$a_3^{(0),K}$	$P_0^{(K)}$	$a_0^{(+),K}$	$a_1^{(+),K}$
$7.81655746 \times 10^{-3}$	$5.11931999 \times 10^{-2}$	$1.26040746 \times 10^{-1}$	$-3.95599616 \times 10^{-7}$	$6.67729571 \times 10^{-4}$	$7.88936302 \times 10^{-3}$
	$4.94505240 \times 10^{-1}$	$1.62865239$	$2.22974369 \times 10^{-6}$	$3.58512534 \times 10^{-3}$	$6.75709862 \times 10^{-2}$
		$6.51816994$	$-4.88348307 \times 10^{-8}$	$9.03252850 \times 10^{-3}$	$1.99167048 \times 10^{-1}$
			$9.99995307 \times 10^{-7}$	$-1.81816269 \times 10^{-9}$	$1.55891061 \times 10^{-7}$
				$3.09228616 \times 10^{-4}$	$-5.88646696 \times 10^{-5}$
					$1.46893824 \times 10^{-2}$

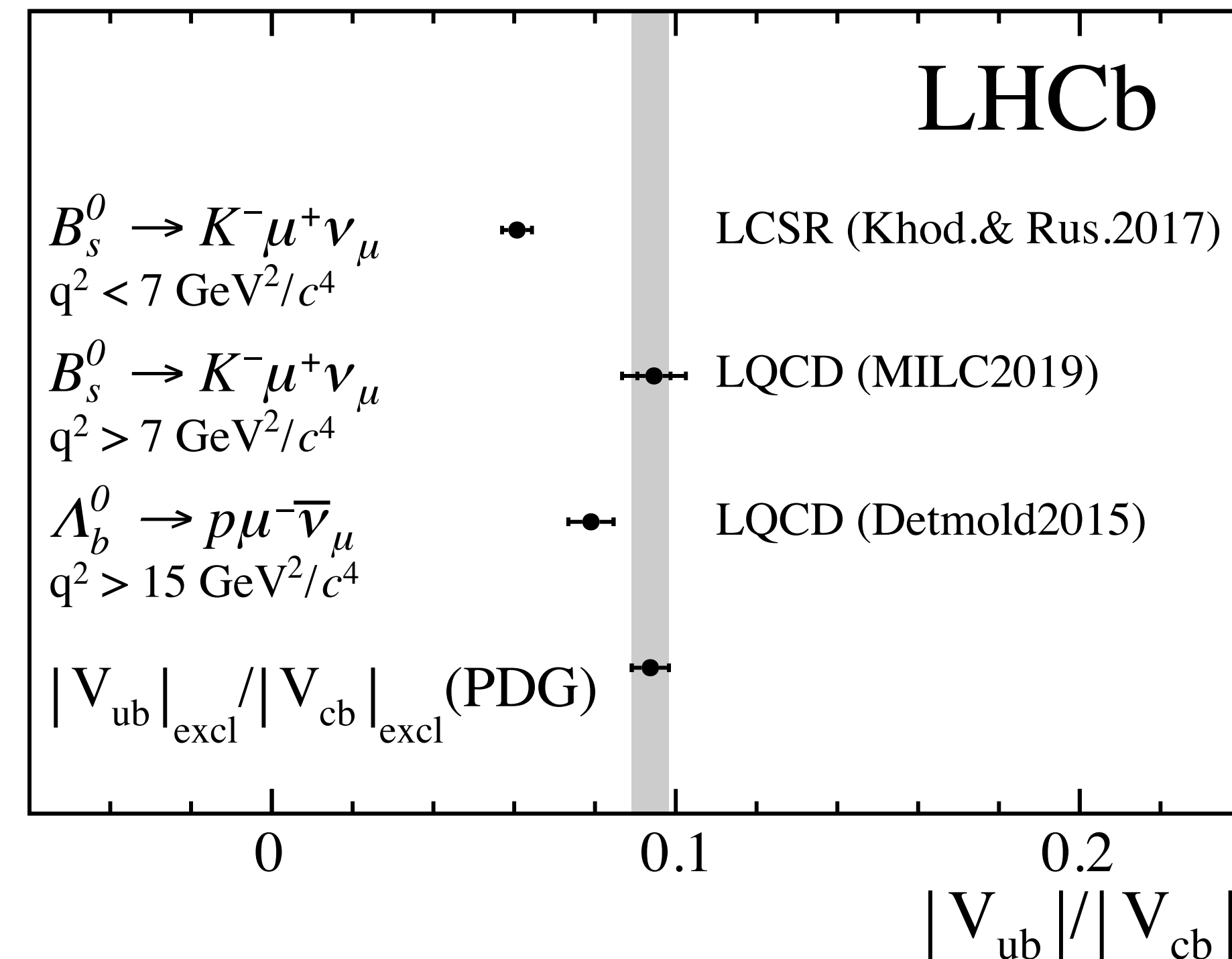
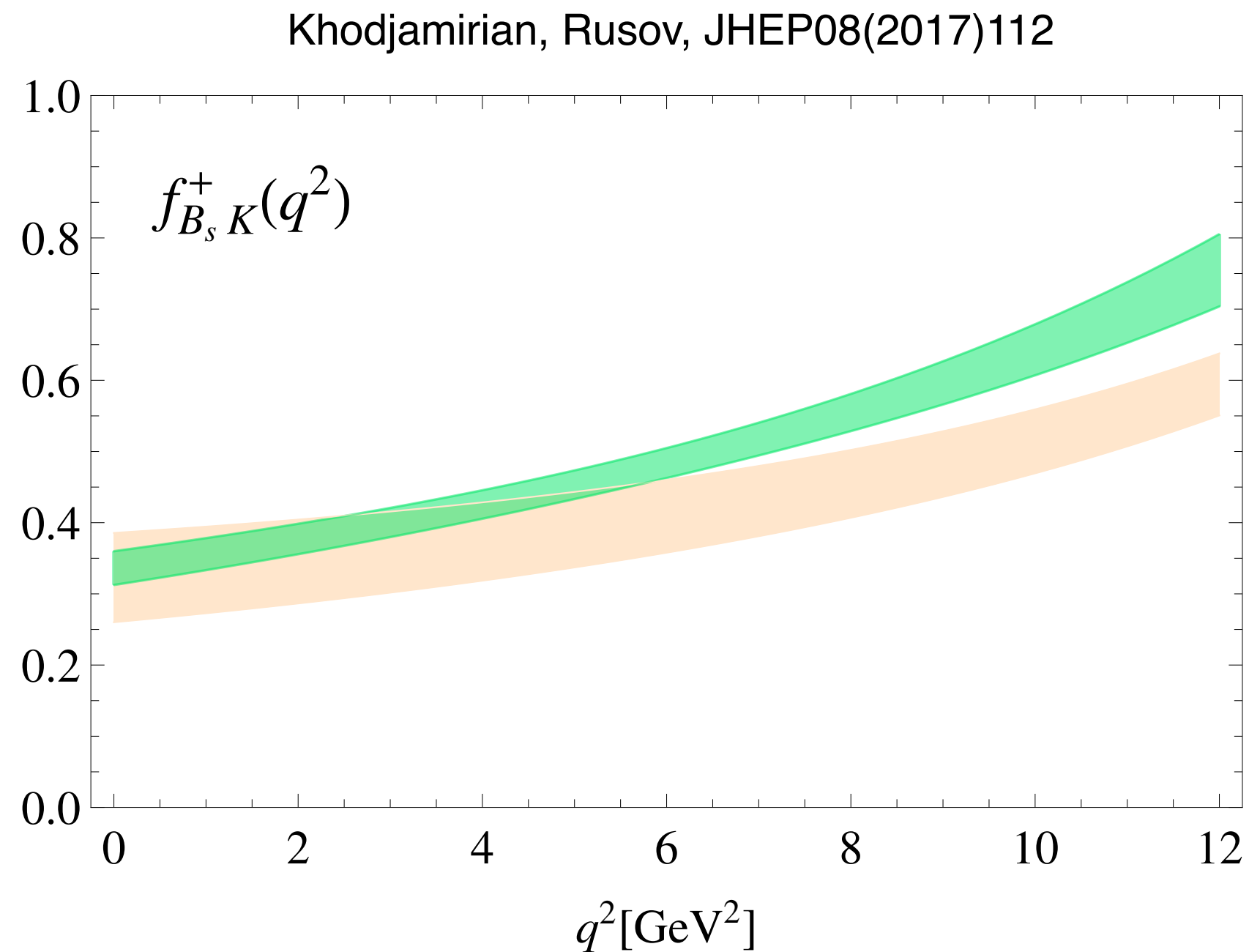
  

$a_2^{(+),K}$	$P_+^{(K)}$	$a_0^{(0),D_s}$	$a_1^{(0),D_s}$	$a_2^{(0),D_s}$	$a_3^{(0),D_s}$
$5.54055868 \times 10^{-2}$	$5.22263419 \times 10^{-9}$	$4.89761879 \times 10^{-5}$	$1.47978430 \times 10^{-3}$	$1.61294090 \times 10^{-4}$	$-1.50864482 \times 10^{-5}$
$5.20212224 \times 10^{-1}$	$4.60220124 \times 10^{-8}$	$4.23550639 \times 10^{-4}$	$-1.12557927 \times 10^{-3}$	$-4.15916006 \times 10^{-4}$	$6.86722615 \times 10^{-6}$
	$1.72576055$	$1.64613013 \times 10^{-7}$	$5.32746249 \times 10^{-4}$	$-8.00096682 \times 10^{-3}$	$-1.57760368 \times 10^{-3}$
		$1.27709131 \times 10^{-6}$	$4.34812507 \times 10^{-15}$	$-2.93868039 \times 10^{-9}$	$3.60812633 \times 10^{-8}$
			$3.44350904 \times 10^{-9}$	$1.08803466 \times 10^{-4}$	$7.14515361 \times 10^{-4}$
				$1.46191770 \times 10^{-4}$	$1.46191770 \times 10^{-4}$
					$-9.57576314 \times 10^{-6}$
					$6.49789179 \times 10^{-2}$
					$-1.42002142 \times 10^{-7}$
					$2.37456520 \times 10^{-4}$
					$-7.74705909 \times 10^{-3}$
					$-1.63296714 \times 10^{-3}$
					$9.27876845 \times 10^{-5}$
					$7.40157233 \times 10^{-1}$
					$8.20182628 \times 10^{-7}$
					$9.33127619 \times 10^{-4}$
					$3.38332719 \times 10^{-4}$
					$-1.12948406 \times 10^{-5}$
					$-1.17310027 \times 10^{-5}$
					$-1.30771878 \times 10^{-10}$
					$5.28997606 \times 10^{-8}$
					$4.00252884 \times 10^{-11}$
					$1.55683903 \times 10^{-10}$
					$8.25859041 \times 10^{-11}$
					$4.62131689 \times 10^{-12}$
					$-1.32946477 \times 10^{-3}$
					$-2.95921529 \times 10^{-3}$
					$-1.18940865 \times 10^{-4}$
					$1.14391084 \times 10^{-1}$
					$3.77594136 \times 10^{-1}$
					$-1.47064962 \times 10^{-2}$
					$8.04802477$
					$6.00685427 \times 10^{-2}$
					$8.99580234$

- This should give the ultimate precision.
  - Important if uncertainty from  $B \rightarrow X_c$  form factors is significant.

# Low $q^2$ measurement

- New for  $B_s^0 \rightarrow K$  measurement was to also provide a measurement at low  $q^2$ .

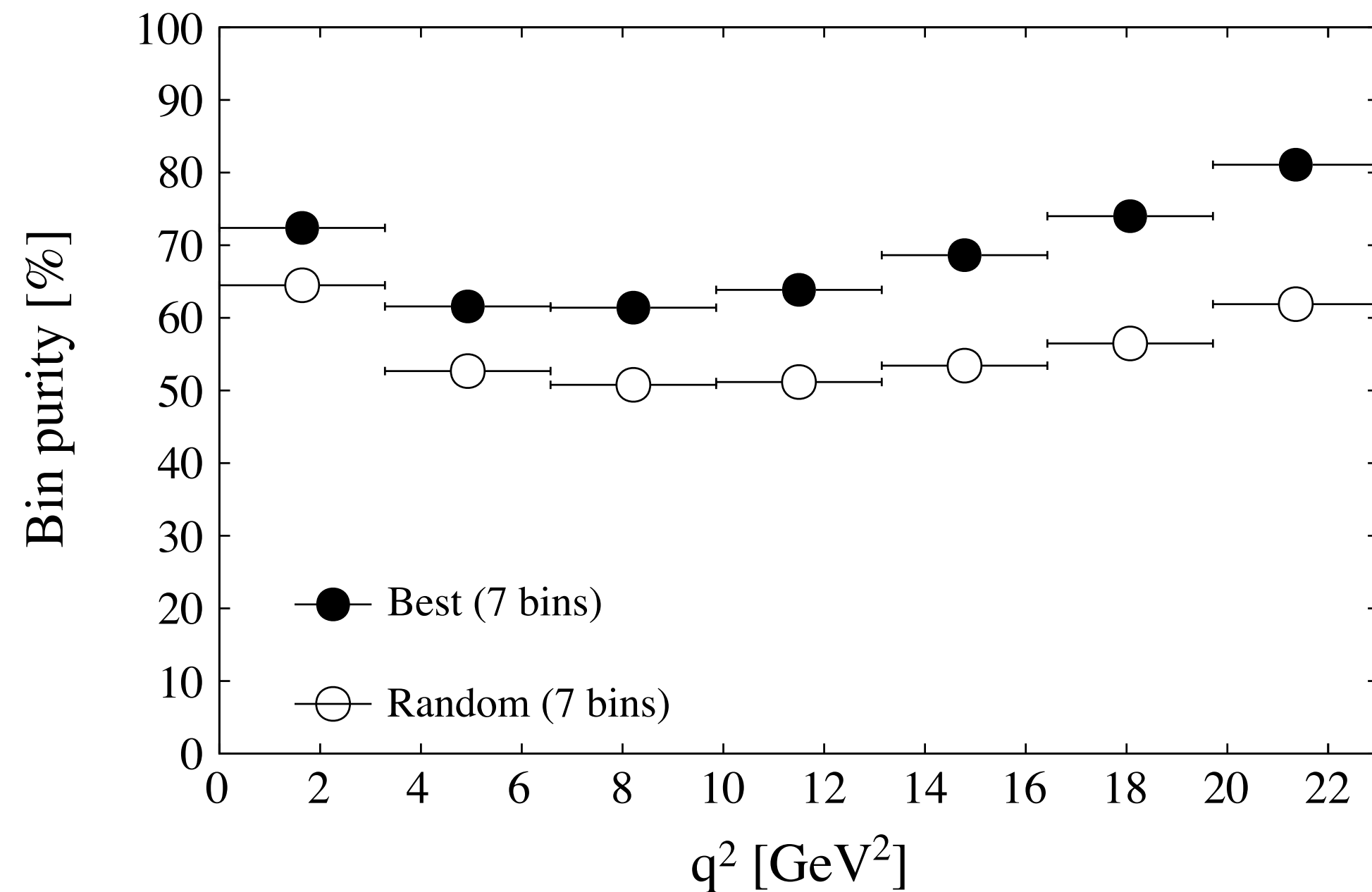


- Measurements do not agree.
  - Would be interesting to see a full LQCD fit including both BF measurements.
  - Also interesting to see a LCSR  $B_s^0 \rightarrow D_s$  calculation.

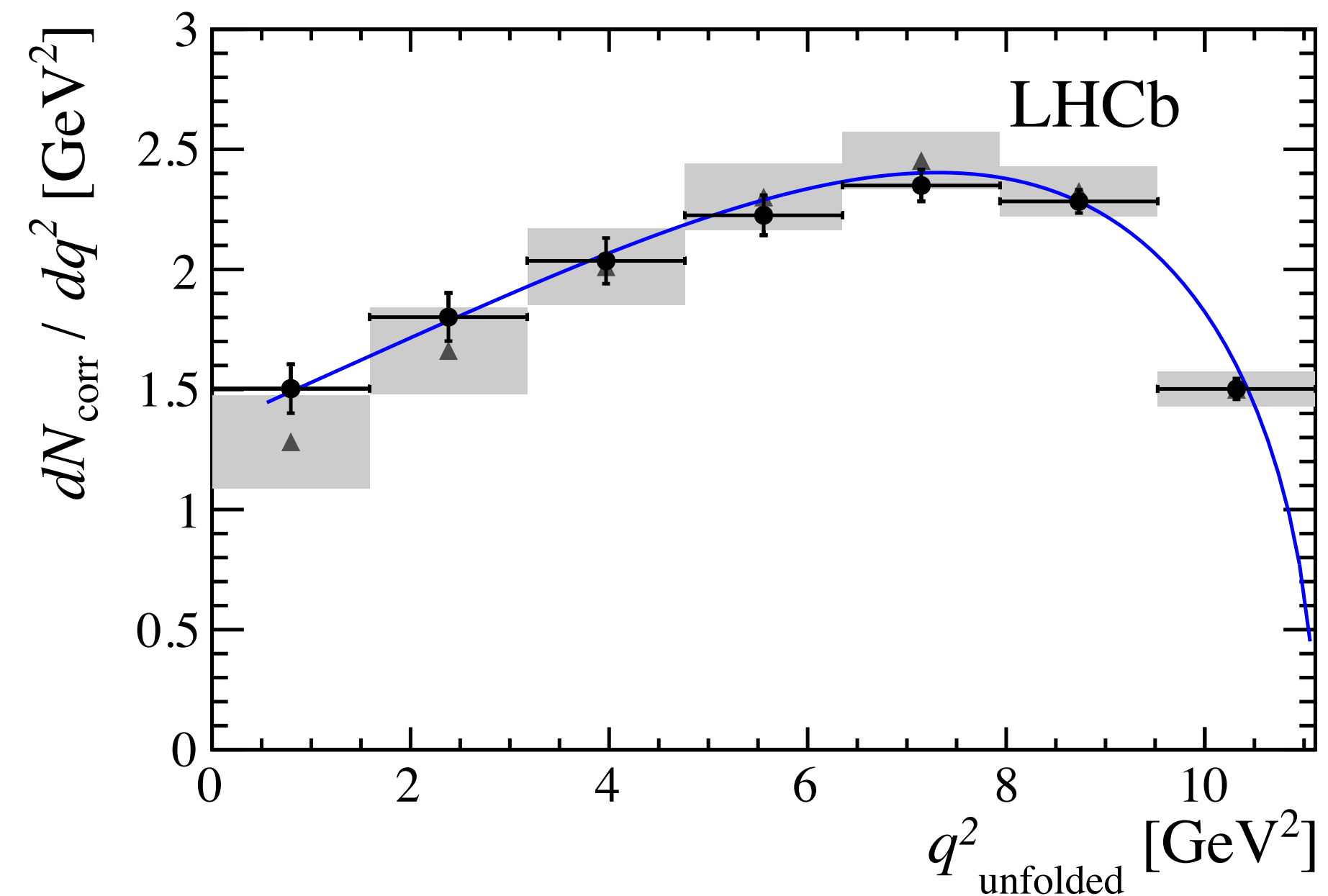
# Medium term prospects

- Need to start making differential measurements as fine as possible.
  - In the  $B_s^0$  case this would massively improve the sensitivity.
  - In the  $\Lambda_b^0$  it would serve as a powerful validation of the lattice calculations ( $\Lambda_b^0 \rightarrow \Lambda_c$  already shown to be good agreement in our 2017 measurement).

Ciezarek, Lupato, Rotondo, Vesterinen: JHEP02 (2017)021



LHCb-PAPER-2017-016, Phys. Rev. D 96, 112005 (2017)





# Long term prospects

- Official goal is to determine  $|V_{ub}|/|V_{cb}|$  at 1% level with full upgrade II dataset (300fb<sup>-1</sup>)
- This requires  $D_s$  and/or  $\Lambda_c$  branching fractions to be measured at 1% level.
- Lattice assumed to be at 1% as well, seems doable particularly if we can make very high  $q^2$  bin.

$B_s^0 \rightarrow K$  systematics

Uncertainty	All $q^2$	low $q^2$	high $q^2$
Tracking	2.0	2.0	2.0
Trigger	1.4	1.2	1.6
Particle identification	1.0	1.0	1.0
$\sigma(m_{\text{corr}})$	0.5	0.5	0.5
Isolation	0.2	0.2	0.2
Charged BDT	0.6	0.6	0.6
Neutral BDT	1.1	1.1	1.1
$q^2$ migration	–	2.0	2.0
Efficiency	1.2	1.6	1.6
Fit template	+2.3 –2.9	+1.8 –2.4	+3.0 –3.4
Total	+4.0 –4.3	+4.3 –4.5	+5.0 –5.3

- The systematics most likely to saturate are those related to the efficiency.
  - Trigger calibration expected to be greatly simplified in run III and beyond.
  - Tracking efficiency is more challenging, need to measure the material in the detector.
  - The rest should go down to small levels.

# $|V_{cb}|$ measurement from $B_s$ decays

LHCb, [Phys. Rev. D101 \(2020\) 072004](#)

- Recently measured  $|V_{cb}|$  with  $B_s$  decays.
- Normalise  $B_s^0$  signal to corresponding  $B^0$  decays.

$$\mathcal{R} \equiv \frac{\mathcal{B}(B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu)}{\mathcal{B}(B^0 \rightarrow D^- \mu^+ \nu_\mu)},$$

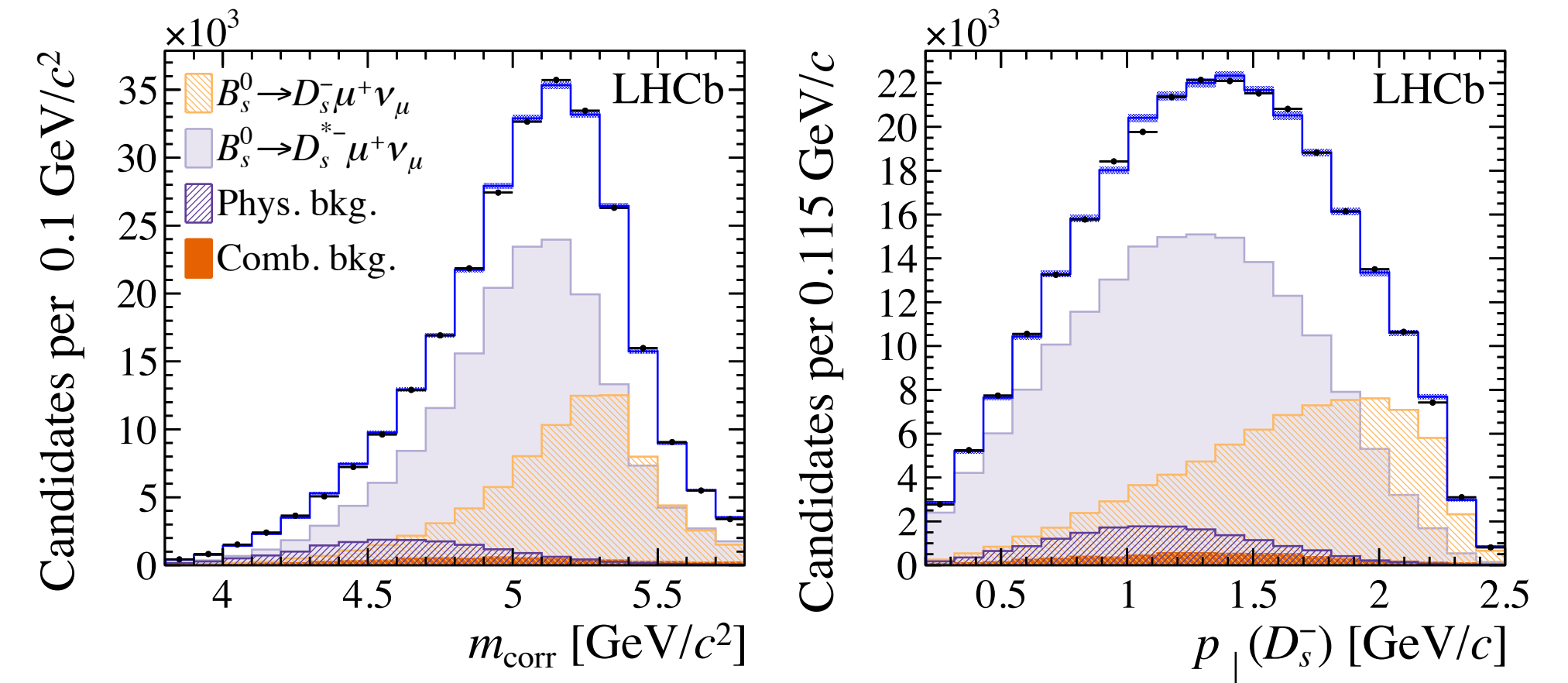
$$\mathcal{R}^* \equiv \frac{\mathcal{B}(B_s^0 \rightarrow D_s^{*-} \mu^+ \nu_\mu)}{\mathcal{B}(B^0 \rightarrow D^{*-} \mu^+ \nu_\mu)}$$

- Fit to determine form factors and signal yield.

- Use  $B^0 \rightarrow D^{(*)} \mu \nu$  branching fractions to determine normalisation with 4(3)% uncertainty from PDG.

- Measurement of  $f_s/f_d$  used to control production fractions.

- Also limited by current knowledge on  $D_{(s)}$  branching fractions.



- Also measured  $B_s \rightarrow D_s^{(*)}$  form factors:

LHCb, [arXiv:2003.08453](#)

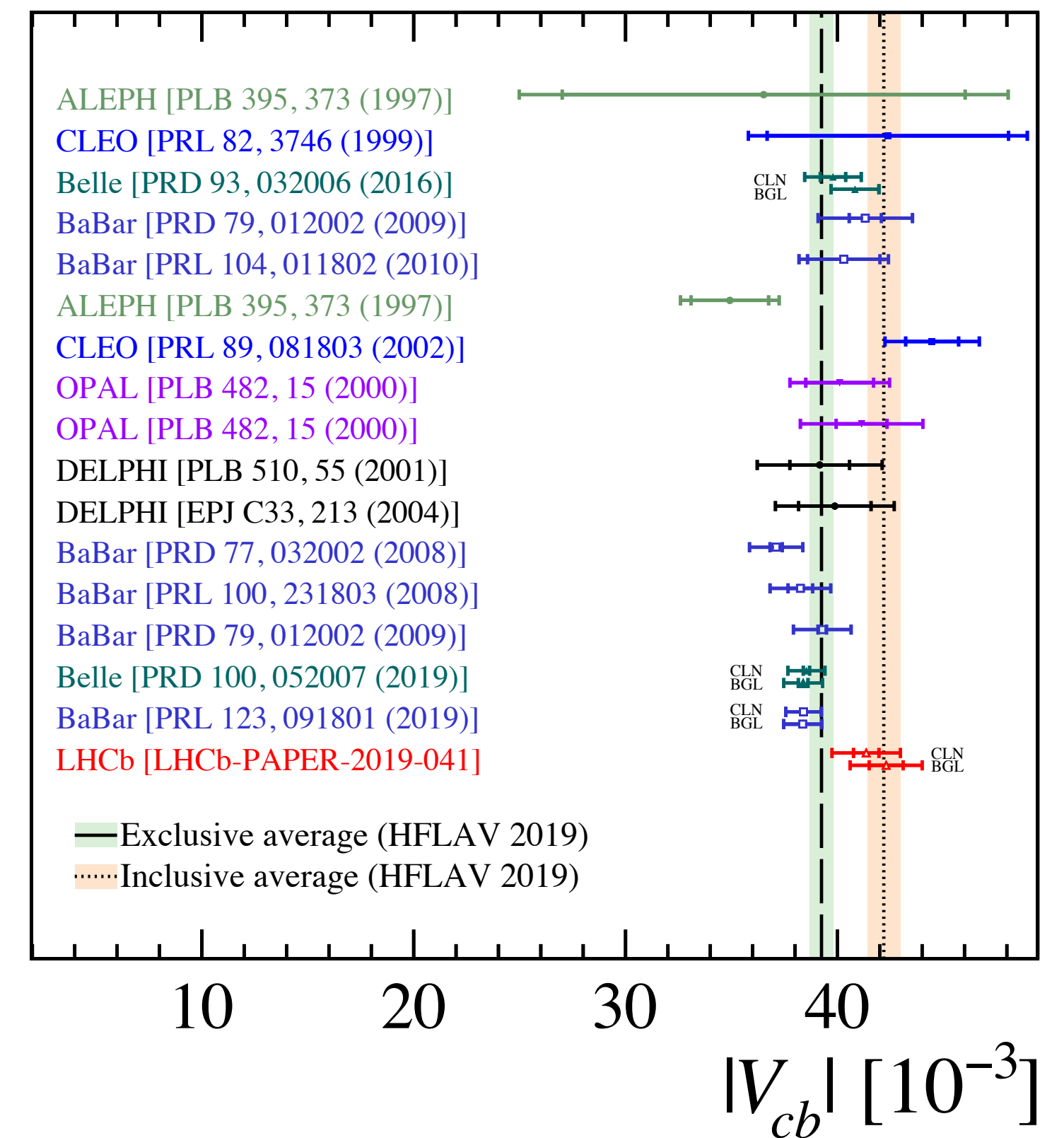
# $|V_{cb}|$ results

- Performed analysis with CLN and BGL parameterisations.
- Parameters have constraints from e.g. HPQCD [1].

$$|V_{cb}|_{\text{CLN}} = (41.4 \pm 0.6 (\text{stat}) \pm 0.9 (\text{syst}) \pm 1.2 (\text{ext})) \times 10^{-3}$$

$$|V_{cb}|_{\text{BGL}} = (42.3 \pm 0.8 (\text{stat}) \pm 0.9 (\text{syst}) \pm 1.2 (\text{ext})) \times 10^{-3}$$

- Both results compatible with each other and existing measurements.



[1] McLean, Davies, Koponen, Lytle [HPQCD]: Phys. Rev. D 101, 074513 (2020)

# Yes, it really is a $|V_{cb}|$ measurement

- If both numerator and denominator depend on  $|V_{cb}|$ , how can one be sensitive to  $|V_{cb}|$ ?
- The point is that the denominator is measured, we do not use a prediction which depends on  $|V_{cb}|$ .
  - The  $B^0 \rightarrow D^{(*)}$  branching fraction measurements could be correlated to the exclusive  $|V_{cb}|$  B-factory measurements, but I understand this is a small effect(?).
- We do, however, rely on the equality of semileptonic widths. Bigi, Mannel, Uraltsev, [JHEP09\(2011\)012](#)
  - We are heavily dependent on this in LHCb, so might be useful to provide precise validations in data. More lifetime measurements?

# Planned measurements

- Plan to perform a similar measurement with  $\Lambda_b^0$  decays.
- Here the normalisation is a bit different, we instead normalise to inclusive  $\Lambda_b^0$  semileptonic decays and employ equality of partial widths.

$$\Gamma(\Lambda_b^0 \rightarrow \Lambda_c^+ \mu^- \bar{\nu}_\mu) = \frac{n_{\text{corr}}(\Lambda_b^0 \rightarrow \Lambda_c^+ \mu^- \bar{\nu}_\mu)}{n_{\text{corr}}(\Lambda_b^0 \rightarrow X_c \mu^-) \times \Gamma(\Lambda_b^0 \rightarrow X_c \mu^- \bar{\nu}_\mu)}$$

- Plan is to use the differential measurement as a function of  $q^2$  to control form factor uncertainties a la LHCb-PAPER-2017-016
- Also plan to perform a measurement with  $B^0 \rightarrow D^* \mu \nu$  decays using a similar method:

$$\frac{\mathcal{B}(B^0 \rightarrow D^{*-} \mu^+ \nu_\mu)}{\mathcal{B}(B \rightarrow \bar{X}_c \mu^+ \nu_\mu X)} = \frac{2n_{\text{corr}}(B^0 \rightarrow D^{*-} \mu^+ \nu_\mu)}{n_{\text{corr}}(\bar{D}^0 \mu^+ X) + n_{\text{corr}}(D^- \mu^+ X)}$$



# Summary and prospects

- LHCb is still relatively new to performing precise  $|V_{xb}|$  measurements.
- More dependent on external inputs, but can make precise measurements in the future which are largely uncorrelated to B-factory ones.
- Expect to stay competitive with Belle-II but will take a lot of work.
- Eventually we will perform full angular analyses of these modes, which will also help determinations indirectly.
- Expect shape information from e.g.  $B^0 \rightarrow D^* \mu \nu$  decays to be complimentary to those obtained at  $e^+e^-$  machines.