Experimental overview and prospects of $|V_{ub}|$ and $|V_{cb}|$ at LHCb

Snowmass mini-workshop on |Vub| and |Vcb|

Patrick Owen, on behalf of the LHCb collaboration





01/11/21



How are we doing

- LHCb has collected 9fb⁻¹ of data.
- We are currently commissioning the first upgrade.





Hope to take another ~15fb⁻¹ in run III without the limitations of a hardware trigger.



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Plans for upgrade II strongly supported by european strategy for particle physics.

been developed. The successful completion of the high-luminosity upgrade of the machine and detectors should remain the focal point of European particle physics, together with continued innovation in experimental techniques. The full physics potential of the LHC and the HL-LHC, including the study of flavour

ESPP 2020 update

2 physics and the quark-gluon plasma, should be exploited.

Semileptonic decays at LHCb

- Do not have direct access to absolute branching fractions.
- Do have access to all b-hadron species.
- Have very large signal yields.

B-fractions analysis, Phys.Rev. D100 (2019) no.3, 031102







Measurements of $|V_{ub}|/|V_{cb}|$ at LHCb

- Select b—>u decay and fit corrected mass.
- Normalise to convenient b—>c transition
 - same b-hadron
 - well known FF

- e.g. $\frac{\mathcal{B}(\Lambda_b \to p \mu^- \overline{\nu}_\mu)_{q^2 > 15 \,\mathrm{GeV}^2/c^4}}{\mathcal{B}(\Lambda_b \to \Lambda_c \mu \nu)_{q^2 > 7 \,\mathrm{GeV}^2/c^4}}$
- charm hadron BF
- Convert ratio of branching fractions using LQCD and/or LCSR.

Measurement with $\Lambda_b^0 \rightarrow p \mu \nu$ decays

• Measure ratio:

 $\frac{\mathcal{B}(\Lambda_b \to p \mu^- \overline{\nu}_\mu)_{q^2 > 15 \,\mathrm{GeV}^2/c^4}}{\mathcal{B}(\Lambda_b \to \Lambda_c \mu \nu)_{q^2 > 7 \,\mathrm{GeV}^2/c^4}}$

- Uncertainty split equally between experiment and lattice.
 - The former benefits from updates to $\mathcal{B}(\Lambda_c \to pK\pi)$

$$\frac{|V_{ub}|}{|V_{cb}|} = 0.083 \pm 0.004 \pm 0.004$$

LHCb, Nature Physics 10 (2015) 1038





2.0

 $\frac{{\rm d}\Gamma/{\rm d}q^2}{|V_{ub}|^2}~({\rm ps}^{-1}~{\rm GeV}^{-2})$

- Measure ratio $\frac{\mathcal{B}(B_s^0 \to K^- \mu^+ \nu_{\mu})}{\mathcal{B}(B_s^0 \to D_s^- \mu^+ \nu_{\mu})} \text{ for new } |V_{ub}|/|V_{cb}| \text{ measurement with } B_s \text{ decays.}$
- Do it to two q² regions, to exploit both LCSR and LQCD calculations.

$$\frac{\mathcal{B}(B^0_s \to K^- \mu^+ \nu_\mu)_{q^2 < 7}}{\mathcal{B}(B^0_s \to D^-_s \mu^+ \nu_\mu)_{Full q^2}}$$

- is sub-dominant.
- D_s mesons reconstructed with the D_s —>KK π decay mode.

 $|V_{ub}|/|V_{cb}|$ from $B^0_s \to K^+ \mu^- \nu$

$$\frac{\mathcal{B}(B^0_s \to K^- \mu^+ \nu_\mu)_{q^2 > 7}}{\mathcal{B}(B^0_s \to D^-_s \mu^+ \nu_\mu)_{Full q^2}}$$

In both cases LQCD is used to determine the denominator, but the uncertainty





- X_c branching fraction uncertainties scaled up the PDG. Important to get more measurements on these.
 - Both Belle-II and BES-III very important here.



• Shapes for sign 3×50000 + Data 3×50000 + Data LHCb 2 fb⁻¹ Backgrounds n 2 40000 $-B_s^{o} \rightarrow D_s$ $B_s^0 \rightarrow D_s^{**-} \mu^+ \nu_{\mu} / D_s^{**} DX_{\bullet}$ ndidates / $-B_{s}^{0} \rightarrow D_{s}^{(*(*))} \tau^{+} \nu_{\tau} / B_{u,d} \rightarrow D_{s} DX$

to form factors.

predictions for e.g. $B_s - K^{(*)}$ welcome.

Branching fraction results

- Relative efficiency is between two-track and four-track final state.
 - Resulting systematic uncertainties due to effects such as tracking and trigger.
- Branching fraction ratios determined to be

$$\frac{\mathcal{B}(B_{s}^{0} \to K^{-} \mu^{+} \nu_{\mu})_{q^{2} < 7}}{\mathcal{B}(B_{s}^{0} \to D_{s}^{-} \mu^{+} \nu_{\mu})_{Full q^{2}}} = (1.66)$$

$$\frac{\mathcal{B}(B_{s}^{0} \to K^{-} \mu^{+} \nu_{\mu})_{q^{2} > 7}}{\mathcal{B}(B_{s}^{0} \to D_{s}^{-} \mu^{+} \nu_{\mu})_{Full q^{2}}} = (3.25)$$

The branching fractions are less limited by the external input c.f. Λ_b^0 case. 2 d Γ/dq^{2} [ps⁻¹ Ge 9 <u>∼_</u>qn0.4

- $\pm 0.08(\text{stat}) \pm 0.07(\text{syst}) \pm 0.05(D_s)) \times 10^{-3}$
- $\pm 0.21(\text{stat}) \stackrel{+ 0.16}{_{- 0.17}}(\text{syst}) \pm 0.09(D_s)) \times 10^{-3}$



$B_s^0 \rightarrow D_s^+ \mu v$ inputs

- For both B K measurements, we use lattice QCD for the $B_s^0 D_s^+\mu\nu$ form factors in full range. Use most precise calculation from HPQCD.
- - Would be interesting to see a LCSR calculation to be consistent at low q².

McLean, Davies, Koponen, Lytle [HPQCD]: Phys. Rev. D 101, 074513 (2020)



- Uncertainties that affect efficiencies and fit shapes included as small systematics in the measurements.

- Many precise $B_{s^0} K$ lattice calculations available [1-4].
- In the end, we chose the one which minimised the uncertainty on $|V_{ub}|/|V_{cb}|$.
 - Of course the best now would be to use the recent FLAG average.

We use the MILC/FNAL calculation [4].





[4] Bazanov et al [MILC/Fermilab], Phys. Rev. D 100, 034501 (2019)





Correlated form factor uncertainties

matrix of simultaneous fit to $B - X_u$ and $B - X_c$ form factors.

Detmold, Lehner, Meinel, Phys. Rev. D 92, 034503 (2015)

$\Lambda_b \to p$	$a_0^{f_+}$	$a_1^{f_+}$	$a_{2}^{f_{+}}$	$a_0^{f_0}$	$a_1^{f_0}$	$a_{2}^{f_{0}}$	$a_0^{f_\perp}$	$a_1^{f_\perp}$	$a_2^{f_\perp}$	$a_0^{g_\perp,g_+}$	$a_1^{g_+}$	$a_2^{g_+}$	$a_0^{g_0}$	$a_1^{g_0}$	$a_{2}^{g_{0}}$	$a_1^{g_\perp}$	$a_2^{g_\perp}$
$a_0^{f_+}$	1	-0.7671	0.2482	0.5337	-0.2670	-0.0922	0.5121	-0.2469	-0.0180	0.3774	-0.2148	-0.0472	0.4420	-0.2680	0.0018	-0.2284	-0.0231
$a_1^{f_+}$	-0.7671	1	-0.6611	-0.2486	0.1617	0.0653	-0.2526	0.1671	0.0056	-0.2177	0.1480	0.0287	-0.2496	0.1849	-0.0169	0.1534	0.0147
$a_{2}^{f_{+}}$	0.2482	-0.6611	1	-0.0792	0.0267	0.2795	-0.0035	-0.0120	0.0425	-0.0562	0.0382	0.0559	-0.0279	-0.0074	0.0870	0.0370	0.0469
$a_0^{f_0}$	0.5337	-0.2486	-0.0792	1	-0.7202	0.2599	0.4581	-0.2052	-0.0146	0.4734	-0.2798	-0.0031	0.3860	-0.2266	-0.0115	-0.2781	0.0048
$a_{1}^{f_{0}}$	-0.2670	0.1617	0.0267	-0.7202	1	-0.6947	-0.2404	0.1415	0.0128	-0.2964	0.2603	-0.0377	-0.2410	0.1694	0.0090	0.2610	-0.0279
$a_{2}^{f_{0}}$	-0.0922	0.0653	0.2795	0.2599	-0.6947	1	0.0190	-0.0056	0.0297	-0.0019	-0.0529	0.1086	-0.0081	-0.0097	0.0664	-0.0568	0.0874
$a_0^{f_\perp}$	0.5121	-0.2526	-0.0035	0.4581	-0.2404	0.0190	1	-0.7672	0.1031	0.3418	-0.1831	-0.0539	0.4313	-0.2713	0.0163	-0.1994	-0.0127
$a_1^{f_\perp}$	-0.2469	0.1671	-0.0120	-0.2052	0.1415	-0.0056	-0.7672	1	-0.5040	-0.1983	0.1259	0.0378	-0.2429	0.1907	-0.0274	0.1347	0.0083
$a_2^{f_\perp}$	-0.0180	0.0056	0.0425	-0.0146	0.0128	0.0297	0.1031	-0.5040	1	-0.0271	0.0045	0.0524	-0.0286	0.0090	0.0530	0.0120	0.0187
$a_0^{g_\perp,g_+}$	0.3774	-0.2177	-0.0562	0.4734	-0.2964	-0.0019	0.3418	-0.1983	-0.0271	1	-0.6751	0.2299	0.5903	-0.2849	-0.0084	-0.6325	0.1314
$a_1^{g_+}$	-0.2148	0.1480	0.0382	-0.2798	0.2603	-0.0529	-0.1831	0.1259	0.0045	-0.6751	1	-0.6972	-0.2576	0.1666	-0.0268	0.6832	-0.1976
$a_2^{g_+}$	-0.0472	0.0287	0.0559	-0.0031	-0.0377	0.1086	-0.0539	0.0378	0.0524	0.2299	-0.6972	1	-0.0760	0.0463	0.2693	-0.3207	0.2419
$a_0^{g_0}$	0.4420	-0.2496	-0.0279	0.3860	-0.2410	-0.0081	0.4313	-0.2429	-0.0286	0.5903	-0.2576	-0.0760	1	-0.7868	0.3673	-0.2892	-0.0105
$a_1^{g_0}$	-0.2680	0.1849	-0.0074	-0.2266	0.1694	-0.0097	-0.2713	0.1907	0.0090	-0.2849	0.1666	0.0463	-0.7868	1	-0.7393	0.1798	0.0107
$a_{2}^{g_{0}}$	0.0018	-0.0169	0.0870	-0.0115	0.0090	0.0664	0.0163	-0.0274	0.0530	-0.0084	-0.0268	0.2693	0.3673	-0.7393	1	0.0302	0.0637
$a_1^{g_\perp}$	-0.2284	0.1534	0.0370	-0.2781	0.2610	-0.0568	-0.1994	0.1347	0.0120	-0.6325	0.6832	-0.3207	-0.2892	0.1798	0.0302	1	-0.6223
$a_2^{g_{\perp}}$	-0.0231	0.0147	0.0469	0.0048	-0.0279	0.0874	-0.0127	0.0083	0.0187	0.1314	-0.1976	0.2419	-0.0105	0.0107	0.0637	-0.6223	1
$\Lambda_b \to \Lambda_c$	$a_0^{f_+}$	$a_1^{f_+}$	$a_{2}^{f_{+}}$	$a_0^{f_0}$	$a_1^{f_0}$	$a_{2}^{f_{0}}$	$a_0^{f_\perp}$	$a_1^{f_\perp}$	$a_2^{f_\perp}$	$a_0^{g_\perp,g_+}$	$a_1^{g_+}$	$a_2^{g_+}$	$a_0^{g_0}$	$a_1^{g_0}$	$a_2^{g_0}$	$a_1^{g_\perp}$	$a_2^{g_\perp}$
$\frac{\frac{1}{\Lambda_b \to \Lambda_c}}{a_0^{f_+}}$	$a_0^{f_+}$ 1	$a_1^{f_+}$ -0.5220	$a_2^{f_+}$ 0.1623	$a_0^{f_0}$ 0.7106	$a_1^{f_0} - 0.2661$	$a_2^{f_0} - 0.0293$	$a_0^{f_{\perp}} 0.6259$	$a_1^{f_{\perp}} - 0.2683$	$a_2^{f_{\perp}} 0.0077$	$a_0^{g_{\perp},g_+}$ 0.1992	$a_1^{g_+}$ -0.1307	$a_2^{g_+}$ -0.0277	$a_0^{g_0}$ 0.2833	$a_1^{g_0} - 0.1838$	$a_2^{g_0}$ 0.0436	$\frac{a_1^{g_\perp}}{-0.1611}$	$\frac{a_2^{g_\perp}}{0.0088}$
$\frac{\overline{\Lambda_b \to \Lambda_c}}{a_0^{f_+}}$	$a_0^{f_+}$ 1 -0.5220	$a_1^{f_+}$ -0.5220 1	$a_2^{f_+}$ 0.1623 -0.6595	$a_0^{f_0}$ 0.7106 -0.3199	$a_1^{f_0}$ -0.2661 0.4277	$a_2^{f_0}$ -0.0293 0.0649	$a_0^{f_\perp}$ 0.6259 -0.2548	$a_1^{f_\perp}$ -0.2683 0.2618	$\begin{array}{c} a_2^{f_\perp} \\ 0.0077 \\ -0.0102 \end{array}$	$\begin{array}{c} a_0^{g_{\perp},g_{+}} \\ 0.1992 \\ -0.1403 \end{array}$	$a_1^{g_+}$ -0.1307 0.1878	$a_2^{g_+}$ -0.0277 0.0413	$a_0^{g_0}$ 0.2833 -0.1575	$a_1^{g_0}$ -0.1838 0.1932	$a_2^{g_0}$ 0.0436 -0.0364	$\begin{array}{c} a_1^{g_\perp} \\ -0.1611 \\ 0.1703 \end{array}$	$ \begin{array}{r} a_2^{g_{\perp}} \\ \hline 0.0088 \\ 0.0030 \end{array} $
$\frac{\overline{\Lambda_b \to \Lambda_c}}{a_0^{f_+}}$ $a_1^{f_+}$ $a_2^{f_+}$	$a_0^{f_+}$ 1 -0.5220 0.1623	$\begin{array}{c} a_1^{f_+} \\ -0.5220 \\ 1 \\ -0.6595 \end{array}$	$a_2^{f_+}$ 0.1623 -0.6595 1	$\begin{array}{c} a_0^{f_0} \\ 0.7106 \\ -0.3199 \\ -0.0350 \end{array}$	$\begin{array}{c} a_1^{f_0} \\ -0.2661 \\ 0.4277 \\ 0.1309 \end{array}$	$\begin{array}{c} a_2^{f_0} \\ -0.0293 \\ 0.0649 \\ 0.0939 \end{array}$	$\begin{array}{c} a_0^{f_\perp} \\ 0.6259 \\ -0.2548 \\ 0.0181 \end{array}$	$\begin{array}{c} a_1^{f_\perp} \\ -0.2683 \\ 0.2618 \\ -0.0149 \end{array}$	$\begin{array}{c} a_2^{f_\perp} \\ 0.0077 \\ -0.0102 \\ 0.0300 \end{array}$	$\begin{array}{c} a_0^{g_{\perp},g_{+}} \\ 0.1992 \\ -0.1403 \\ -0.0111 \end{array}$	$\begin{array}{r} a_1^{g_+} \\ -0.1307 \\ 0.1878 \\ 0.0190 \end{array}$	$\begin{array}{r} a_2^{g_+} \\ -0.0277 \\ 0.0413 \\ 0.0007 \end{array}$	$\begin{array}{r} a_0^{g_0} \\ 0.2833 \\ -0.1575 \\ 0.0005 \end{array}$	$a_1^{g_0}$ -0.1838 0.1932 -0.0041	$\begin{array}{r} a_2^{g_0} \\ 0.0436 \\ -0.0364 \\ 0.0186 \end{array}$	$\begin{array}{r} a_1^{g_\perp} \\ -0.1611 \\ 0.1703 \\ 0.0246 \end{array}$	$\begin{array}{c} a_2^{g_\perp} \\ 0.0088 \\ 0.0030 \\ 0.0088 \end{array}$
$ \begin{array}{c} \hline \frac{\lambda_b \to \Lambda_c}{a_0^{f_+}} \\ a_1^{f_+} \\ a_2^{f_+} \\ a_0^{f_0} \end{array} $	$\begin{array}{c} a_0^{f_+} \\ 1 \\ -0.5220 \\ 0.1623 \\ 0.7106 \end{array}$	$\begin{array}{c} a_1^{f_+} \\ -0.5220 \\ 1 \\ -0.6595 \\ -0.3199 \end{array}$	$\begin{array}{r} a_2^{f_+} \\ 0.1623 \\ -0.6595 \\ 1 \\ -0.0350 \end{array}$	$\begin{array}{r} a_0^{f_0} \\ 0.7106 \\ -0.3199 \\ -0.0350 \\ 1 \end{array}$	$\begin{array}{r} a_1^{f_0} \\ -0.2661 \\ 0.4277 \\ 0.1309 \\ -0.5132 \end{array}$	$\begin{array}{r} a_2^{f_0} \\ -0.0293 \\ 0.0649 \\ 0.0939 \\ 0.1123 \end{array}$	$\begin{array}{c} a_0^{f_\perp} \\ 0.6259 \\ -0.2548 \\ 0.0181 \\ 0.5190 \end{array}$	$\begin{array}{c} a_1^{f_\perp} \\ -0.2683 \\ 0.2618 \\ -0.0149 \\ -0.2037 \end{array}$	$\begin{array}{c} a_2^{f_\perp} \\ 0.0077 \\ -0.0102 \\ 0.0300 \\ -0.0014 \end{array}$	$\begin{array}{c} a_0^{g_{\perp},g_+} \\ 0.1992 \\ -0.1403 \\ -0.0111 \\ 0.2531 \end{array}$	$\begin{array}{r} a_1^{g_+} \\ -0.1307 \\ 0.1878 \\ 0.0190 \\ -0.2100 \end{array}$	$\begin{array}{r} a_2^{g_+} \\ -0.0277 \\ 0.0413 \\ 0.0007 \\ 0.0128 \end{array}$	$\begin{array}{r} a_0^{g_0} \\ 0.2833 \\ -0.1575 \\ 0.0005 \\ 0.2012 \end{array}$	$\begin{array}{r} a_1^{g_0} \\ -0.1838 \\ 0.1932 \\ -0.0041 \\ -0.1481 \end{array}$	$\begin{array}{r} a_2^{g_0} \\ 0.0436 \\ -0.0364 \\ 0.0186 \\ 0.0096 \end{array}$	$\begin{array}{r} a_1^{g_\perp} \\ -0.1611 \\ 0.1703 \\ 0.0246 \\ -0.2057 \end{array}$	$\begin{array}{c} a_2^{g_\perp} \\ 0.0088 \\ 0.0030 \\ 0.0088 \\ -0.0079 \end{array}$
$ \begin{array}{c} \underline{\lambda_b \to \Lambda_c} \\ \hline \underline{\Lambda_b \to \Lambda_c} \\ a_0^{f_+} \\ a_1^{f_+} \\ a_2^{f_+} \\ a_0^{f_0} \\ a_1^{f_0} \end{array} $	$\begin{array}{r} a_0^{f_+} \\ 1 \\ -0.5220 \\ 0.1623 \\ 0.7106 \\ -0.2661 \end{array}$	$\begin{array}{r} a_1^{f+} \\ -0.5220 \\ 1 \\ -0.6595 \\ -0.3199 \\ 0.4277 \end{array}$	$\begin{array}{c} a_2^{f_+} \\ 0.1623 \\ -0.6595 \\ 1 \\ -0.0350 \\ 0.1309 \end{array}$	$\begin{array}{r} a_0^{f_0} \\ 0.7106 \\ -0.3199 \\ -0.0350 \\ 1 \\ -0.5132 \end{array}$	$\begin{array}{r} a_1^{f_0} \\ -0.2661 \\ 0.4277 \\ 0.1309 \\ -0.5132 \\ 1 \end{array}$	$\begin{array}{r} a_2^{f_0} \\ -0.0293 \\ 0.0649 \\ 0.0939 \\ 0.1123 \\ -0.5243 \end{array}$	$\begin{array}{c} a_0^{f_\perp} \\ 0.6259 \\ -0.2548 \\ 0.0181 \\ 0.5190 \\ -0.1791 \end{array}$	$\begin{array}{c} a_1^{f_\perp} \\ -0.2683 \\ 0.2618 \\ -0.0149 \\ -0.2037 \\ 0.2285 \end{array}$	$\begin{array}{c} a_2^{f\perp} \\ 0.0077 \\ -0.0102 \\ 0.0300 \\ -0.0014 \\ 0.0094 \end{array}$	$\begin{array}{c} a_0^{g_{\perp},g_{+}} \\ 0.1992 \\ -0.1403 \\ -0.0111 \\ 0.2531 \\ -0.1770 \end{array}$	$\begin{array}{r} a_1^{g_+} \\ -0.1307 \\ 0.1878 \\ 0.0190 \\ -0.2100 \\ 0.2589 \end{array}$	$\begin{array}{r} a_2^{g_+} \\ -0.0277 \\ 0.0413 \\ 0.0007 \\ 0.0128 \\ 0.0134 \end{array}$	$\begin{array}{r} a_0^{g_0} \\ 0.2833 \\ -0.1575 \\ 0.0005 \\ 0.2012 \\ -0.1266 \end{array}$	$\begin{array}{r} a_1^{g_0} \\ -0.1838 \\ 0.1932 \\ -0.0041 \\ -0.1481 \\ 0.1854 \end{array}$	$\begin{array}{r} a_2^{g_0} \\ 0.0436 \\ -0.0364 \\ 0.0186 \\ 0.0096 \\ -0.0086 \end{array}$	$\begin{array}{r} a_1^{g_\perp} \\ \hline -0.1611 \\ 0.1703 \\ 0.0246 \\ -0.2057 \\ 0.2339 \end{array}$	$\begin{array}{r} a_2^{g_\perp} \\ \hline 0.0088 \\ 0.0030 \\ 0.0088 \\ -0.0079 \\ 0.0127 \end{array}$
$ \begin{array}{c} \hline \hline \lambda_b \to \Lambda_c \\ \hline a_0^{f_+} \\ a_1^{f_+} \\ a_2^{f_+} \\ a_0^{f_0} \\ a_1^{f_0} \\ a_2^{f_0} \\ a_2^{f_0} \end{array} $	$\begin{array}{c} a_0^{f+} \\ 1 \\ -0.5220 \\ 0.1623 \\ 0.7106 \\ -0.2661 \\ -0.0293 \end{array}$	$\begin{array}{c} a_1^{f+} \\ -0.5220 \\ 1 \\ -0.6595 \\ -0.3199 \\ 0.4277 \\ 0.0649 \end{array}$	$\begin{array}{r} a_2^{f+} \\ 0.1623 \\ -0.6595 \\ 1 \\ -0.0350 \\ 0.1309 \\ 0.0939 \end{array}$	$\begin{array}{r} a_0^{f_0} \\ 0.7106 \\ -0.3199 \\ -0.0350 \\ 1 \\ -0.5132 \\ 0.1123 \end{array}$	$\begin{array}{r} a_1^{f_0} \\ -0.2661 \\ 0.4277 \\ 0.1309 \\ -0.5132 \\ 1 \\ -0.5243 \end{array}$	$\begin{array}{r} a_2^{f_0} \\ -0.0293 \\ 0.0649 \\ 0.0939 \\ 0.1123 \\ -0.5243 \\ 1 \end{array}$	$\begin{array}{c} a_0^{f_\perp} \\ 0.6259 \\ -0.2548 \\ 0.0181 \\ 0.5190 \\ -0.1791 \\ -0.0222 \end{array}$	$\begin{array}{c} a_1^{f_\perp} \\ -0.2683 \\ 0.2618 \\ -0.0149 \\ -0.2037 \\ 0.2285 \\ 0.0275 \end{array}$	$\begin{array}{c} a_2^{f_\perp} \\ 0.0077 \\ -0.0102 \\ 0.0300 \\ -0.0014 \\ 0.0094 \\ 0.0138 \end{array}$	$\begin{array}{c} a_0^{g_{\perp},g_{+}} \\ 0.1992 \\ -0.1403 \\ -0.0111 \\ 0.2531 \\ -0.1770 \\ 0.0044 \end{array}$	$\begin{array}{r} a_1^{g_+} \\ -0.1307 \\ 0.1878 \\ 0.0190 \\ -0.2100 \\ 0.2589 \\ -0.0148 \end{array}$	$\begin{array}{c} a_2^{g+} \\ -0.0277 \\ 0.0413 \\ 0.0007 \\ 0.0128 \\ 0.0134 \\ 0.0300 \end{array}$	$\begin{array}{r} a_0^{g_0} \\ 0.2833 \\ -0.1575 \\ 0.0005 \\ 0.2012 \\ -0.1266 \\ -0.0074 \end{array}$	$\begin{array}{r} a_1^{g_0} \\ -0.1838 \\ 0.1932 \\ -0.0041 \\ -0.1481 \\ 0.1854 \\ 0.0112 \end{array}$	$\begin{array}{r} a_2^{g_0} \\ 0.0436 \\ -0.0364 \\ 0.0186 \\ 0.0096 \\ -0.0086 \\ -0.0034 \end{array}$	$\begin{array}{c} a_1^{g_\perp} \\ \hline -0.1611 \\ 0.1703 \\ 0.0246 \\ -0.2057 \\ 0.2339 \\ -0.0218 \end{array}$	$\begin{array}{c} a_2^{g_\perp} \\ 0.0088 \\ 0.0030 \\ 0.0088 \\ -0.0079 \\ 0.0127 \\ 0.0075 \end{array}$
$ \begin{array}{c} \hline \underline{A_b \to \Lambda_c} \\ \hline a_0^{f_+} \\ a_1^{f_+} \\ a_2^{f_2} \\ a_0^{f_0} \\ a_1^{f_0} \\ a_2^{f_0} \\ a_0^{f_1} \\ a_0^{f_{\perp}} \\ a_0^{f_{\perp}} \end{array} $	$\begin{array}{c} a_0^{f_+} \\ 1 \\ -0.5220 \\ 0.1623 \\ 0.7106 \\ -0.2661 \\ -0.0293 \\ 0.6259 \end{array}$	$\begin{array}{c} a_1^{f_+} \\ -0.5220 \\ 1 \\ -0.6595 \\ -0.3199 \\ 0.4277 \\ 0.0649 \\ -0.2548 \end{array}$	$\begin{array}{c} a_2^{f+} \\ 0.1623 \\ -0.6595 \\ 1 \\ -0.0350 \\ 0.1309 \\ 0.0939 \\ 0.0181 \end{array}$	$\begin{array}{r} a_0^{f_0} \\ 0.7106 \\ -0.3199 \\ -0.0350 \\ 1 \\ -0.5132 \\ 0.1123 \\ 0.5190 \end{array}$	$\begin{array}{r} a_1^{f_0} \\ -0.2661 \\ 0.4277 \\ 0.1309 \\ -0.5132 \\ 1 \\ -0.5243 \\ -0.1791 \end{array}$	$\begin{array}{r} a_2^{f_0} \\ -0.0293 \\ 0.0649 \\ 0.0939 \\ 0.1123 \\ -0.5243 \\ 1 \\ -0.0222 \end{array}$	$\begin{array}{c} a_0^{f_\perp} \\ 0.6259 \\ -0.2548 \\ 0.0181 \\ 0.5190 \\ -0.1791 \\ -0.0222 \\ 1 \end{array}$	$\begin{array}{c} a_1^{f_\perp} \\ -0.2683 \\ 0.2618 \\ -0.0149 \\ -0.2037 \\ 0.2285 \\ 0.0275 \\ -0.5829 \end{array}$	$\begin{array}{c} a_2^{f_\perp} \\ 0.0077 \\ -0.0102 \\ 0.0300 \\ -0.0014 \\ 0.0094 \\ 0.0138 \\ 0.1142 \end{array}$	$\begin{array}{c} a_0^{g_{\perp},g_{+}} \\ 0.1992 \\ -0.1403 \\ -0.0111 \\ 0.2531 \\ -0.1770 \\ 0.0044 \\ 0.1754 \end{array}$	$\begin{array}{r} a_1^{g_+} \\ -0.1307 \\ 0.1878 \\ 0.0190 \\ -0.2100 \\ 0.2589 \\ -0.0148 \\ -0.1255 \end{array}$	$\begin{array}{r} a_2^{g_+} \\ -0.0277 \\ 0.0413 \\ 0.0007 \\ 0.0128 \\ 0.0134 \\ 0.0300 \\ -0.0168 \end{array}$	$\begin{array}{r} a_0^{g_0} \\ 0.2833 \\ -0.1575 \\ 0.0005 \\ 0.2012 \\ -0.1266 \\ -0.0074 \\ 0.2874 \end{array}$	$\begin{array}{r} a_1^{g_0} \\ -0.1838 \\ 0.1932 \\ -0.0041 \\ -0.1481 \\ 0.1854 \\ 0.0112 \\ -0.1811 \end{array}$	$\begin{array}{r} a_2^{g_0} \\ 0.0436 \\ -0.0364 \\ 0.0186 \\ 0.0096 \\ -0.0086 \\ -0.0034 \\ 0.0416 \end{array}$	$\begin{array}{c} a_1^{g_\perp} \\ -0.1611 \\ 0.1703 \\ 0.0246 \\ -0.2057 \\ 0.2339 \\ -0.0218 \\ -0.1320 \end{array}$	$\begin{array}{c} a_2^{g_\perp} \\ 0.0088 \\ 0.0030 \\ 0.0088 \\ -0.0079 \\ 0.0127 \\ 0.0075 \\ -0.0086 \end{array}$
$ \begin{array}{c} \hline \underline{A_b \to \Lambda_c} \\ \hline a_0^{f_+} \\ a_1^{f_+} \\ a_1^{f_+} \\ a_2^{f_+} \\ a_0^{f_0} \\ a_1^{f_0} \\ a_0^{f} \\ a_0^{f_\perp} \\ a_1^{f_\perp} \end{array} $	$\begin{array}{r} a_0^{f_+} \\ 1 \\ -0.5220 \\ 0.1623 \\ 0.7106 \\ -0.2661 \\ -0.0293 \\ 0.6259 \\ -0.2683 \end{array}$	$\begin{array}{c} a_1^{f_+} \\ -0.5220 \\ 1 \\ -0.6595 \\ -0.3199 \\ 0.4277 \\ 0.0649 \\ -0.2548 \\ 0.2618 \end{array}$	$\begin{array}{r} a_2^{f+} \\ 0.1623 \\ -0.6595 \\ 1 \\ -0.0350 \\ 0.1309 \\ 0.0939 \\ 0.0181 \\ -0.0149 \end{array}$	$\begin{array}{c} a_0^{f_0} \\ 0.7106 \\ -0.3199 \\ -0.0350 \\ 1 \\ -0.5132 \\ 0.1123 \\ 0.5190 \\ -0.2037 \end{array}$	$\begin{array}{r} a_1^{f_0} \\ -0.2661 \\ 0.4277 \\ 0.1309 \\ -0.5132 \\ 1 \\ -0.5243 \\ -0.1791 \\ 0.2285 \end{array}$	$\begin{array}{r} a_2^{f_0} \\ -0.0293 \\ 0.0649 \\ 0.0939 \\ 0.1123 \\ -0.5243 \\ 1 \\ -0.0222 \\ 0.0275 \end{array}$	$\begin{array}{c} a_0^{f_\perp} \\ 0.6259 \\ -0.2548 \\ 0.0181 \\ 0.5190 \\ -0.1791 \\ -0.0222 \\ 1 \\ -0.5829 \end{array}$	$\begin{array}{c} a_1^{f_\perp} \\ -0.2683 \\ 0.2618 \\ -0.0149 \\ -0.2037 \\ 0.2285 \\ 0.0275 \\ -0.5829 \\ 1 \end{array}$	$\begin{array}{c} a_2^{f_\perp} \\ 0.0077 \\ -0.0102 \\ 0.0300 \\ -0.0014 \\ 0.0094 \\ 0.0138 \\ 0.1142 \\ -0.4656 \end{array}$	$\begin{array}{c} a_0^{g_{\perp},g_{+}} \\ 0.1992 \\ -0.1403 \\ -0.0111 \\ 0.2531 \\ -0.1770 \\ 0.0044 \\ 0.1754 \\ -0.1154 \end{array}$	$\begin{array}{r} a_1^{g_+} \\ -0.1307 \\ 0.1878 \\ 0.0190 \\ -0.2100 \\ 0.2589 \\ -0.0148 \\ -0.1255 \\ 0.1472 \end{array}$	$\begin{array}{r} a_2^{g+} \\ -0.0277 \\ 0.0413 \\ 0.0007 \\ 0.0128 \\ 0.0134 \\ 0.0300 \\ -0.0168 \\ 0.0360 \end{array}$	$\begin{array}{r} a_0^{g_0} \\ 0.2833 \\ -0.1575 \\ 0.0005 \\ 0.2012 \\ -0.1266 \\ -0.0074 \\ 0.2874 \\ -0.1487 \end{array}$	$\begin{array}{c} a_1^{g_0} \\ -0.1838 \\ 0.1932 \\ -0.0041 \\ -0.1481 \\ 0.1854 \\ 0.0112 \\ -0.1811 \\ 0.1650 \end{array}$	$\begin{array}{c} a_2^{g_0} \\ 0.0436 \\ -0.0364 \\ 0.0186 \\ 0.0096 \\ -0.0086 \\ -0.0034 \\ 0.0416 \\ -0.0341 \end{array}$	$\begin{array}{c} a_1^{g_\perp} \\ -0.1611 \\ 0.1703 \\ 0.0246 \\ -0.2057 \\ 0.2339 \\ -0.0218 \\ -0.1320 \\ 0.1319 \end{array}$	$\begin{array}{c} a_2^{g_\perp} \\ 0.0088 \\ 0.0030 \\ 0.0088 \\ -0.0079 \\ 0.0127 \\ 0.0075 \\ -0.0086 \\ 0.0096 \end{array}$
$ \begin{array}{c} \hline \underline{\Lambda_b \to \Lambda_c} \\ a_0^{f_+} \\ a_1^{f_+} \\ a_2^{f_0} \\ a_1^{f_0} \\ a_1^{f_0} \\ a_1^{f_0} \\ a_1^{f_1} \\ a_2^{f_{\perp}} \\ a_0^{f_{\perp}} \\ a_1^{f_{\perp}} \\ a_2^{f_{\perp}} \end{array} $	$\begin{array}{c} a_0^{f_+} \\ 1 \\ -0.5220 \\ 0.1623 \\ 0.7106 \\ -0.2661 \\ -0.0293 \\ 0.6259 \\ -0.2683 \\ 0.0077 \end{array}$	$\begin{array}{c} a_1^{f_+} \\ -0.5220 \\ 1 \\ -0.6595 \\ -0.3199 \\ 0.4277 \\ 0.0649 \\ -0.2548 \\ 0.2618 \\ -0.0102 \end{array}$	$\begin{array}{c} a_2^{f_+} \\ 0.1623 \\ -0.6595 \\ 1 \\ -0.0350 \\ 0.1309 \\ 0.0939 \\ 0.0181 \\ -0.0149 \\ 0.0300 \end{array}$	$\begin{array}{r} a_0^{f_0} \\ 0.7106 \\ -0.3199 \\ -0.0350 \\ 1 \\ -0.5132 \\ 0.1123 \\ 0.5190 \\ -0.2037 \\ -0.0014 \end{array}$	$\begin{array}{r} a_1^{f_0} \\ -0.2661 \\ 0.4277 \\ 0.1309 \\ -0.5132 \\ 1 \\ -0.5243 \\ -0.1791 \\ 0.2285 \\ 0.0094 \end{array}$	$\begin{array}{r} a_2^{f_0} \\ -0.0293 \\ 0.0649 \\ 0.0939 \\ 0.1123 \\ -0.5243 \\ 1 \\ -0.0222 \\ 0.0275 \\ 0.0138 \end{array}$	$\begin{array}{c} a_0^{f_\perp} \\ 0.6259 \\ -0.2548 \\ 0.0181 \\ 0.5190 \\ -0.1791 \\ -0.0222 \\ 1 \\ -0.5829 \\ 0.1142 \end{array}$	$\begin{array}{c} a_1^{f_\perp} \\ -0.2683 \\ 0.2618 \\ -0.0149 \\ -0.2037 \\ 0.2285 \\ 0.0275 \\ -0.5829 \\ 1 \\ -0.4656 \end{array}$	$\begin{array}{c} a_{2}^{f_{\perp}} \\ 0.0077 \\ -0.0102 \\ 0.0300 \\ -0.0014 \\ 0.0094 \\ 0.0138 \\ 0.1142 \\ -0.4656 \\ 1 \end{array}$	$\begin{array}{c} a_0^{g_{\perp},g_{+}} \\ 0.1992 \\ -0.1403 \\ -0.0111 \\ 0.2531 \\ -0.1770 \\ 0.0044 \\ 0.1754 \\ -0.1154 \\ -0.0006 \end{array}$	$\begin{array}{r} a_1^{g_+} \\ -0.1307 \\ 0.1878 \\ 0.0190 \\ -0.2100 \\ 0.2589 \\ -0.0148 \\ -0.1255 \\ 0.1472 \\ -0.0003 \end{array}$	$\begin{array}{c} a_2^{g+} \\ -0.0277 \\ 0.0413 \\ 0.0007 \\ 0.0128 \\ 0.0134 \\ 0.0300 \\ -0.0168 \\ 0.0360 \\ 0.0057 \end{array}$	$\begin{array}{r} a_0^{g_0} \\ 0.2833 \\ -0.1575 \\ 0.0005 \\ 0.2012 \\ -0.1266 \\ -0.0074 \\ 0.2874 \\ -0.1487 \\ 0.0049 \end{array}$	$\begin{array}{c} a_1^{g_0} \\ -0.1838 \\ 0.1932 \\ -0.0041 \\ -0.1481 \\ 0.1854 \\ 0.0112 \\ -0.1811 \\ 0.1650 \\ -0.0059 \end{array}$	$\begin{array}{c} a_2^{g_0} \\ 0.0436 \\ -0.0364 \\ 0.0186 \\ 0.0096 \\ -0.0086 \\ -0.0034 \\ 0.0416 \\ -0.0341 \\ 0.0087 \end{array}$	$\begin{array}{c} a_1^{g_\perp} \\ -0.1611 \\ 0.1703 \\ 0.0246 \\ -0.2057 \\ 0.2339 \\ -0.0218 \\ -0.1320 \\ 0.1319 \\ -0.0006 \end{array}$	$\begin{array}{c} a_2^{g_\perp} \\ 0.0088 \\ 0.0030 \\ 0.0088 \\ -0.0079 \\ 0.0127 \\ 0.0075 \\ -0.0086 \\ 0.0096 \\ 0.0033 \end{array}$
$\begin{array}{c} \hline \underline{\Lambda_b \to \Lambda_c} \\ \hline \underline{\Lambda_b \to \Lambda_c} \\ a_0^{f_+} \\ a_1^{f_+} \\ a_2^{f_0} \\ a_1^{f_0} \\ a_1^{f_0} \\ a_0^{f_{\perp}} \\ a_0^{f_{\perp}} \\ a_2^{f_{\perp}} \\ a_0^{f_{\perp}} \\ a_2^{f_{\perp}} \\ a_0^{f_{\perp},g_+} \end{array}$	$\begin{array}{c} a_0^{f_+} \\ 1 \\ -0.5220 \\ 0.1623 \\ 0.7106 \\ -0.2661 \\ -0.0293 \\ 0.6259 \\ -0.2683 \\ 0.0077 \\ 0.1992 \end{array}$	$\begin{array}{r} a_1^{f_+} \\ -0.5220 \\ 1 \\ -0.6595 \\ -0.3199 \\ 0.4277 \\ 0.0649 \\ -0.2548 \\ 0.2618 \\ -0.0102 \\ -0.1403 \end{array}$	$\begin{array}{c} a_2^{f_+} \\ 0.1623 \\ -0.6595 \\ 1 \\ -0.0350 \\ 0.1309 \\ 0.0939 \\ 0.0181 \\ -0.0149 \\ 0.0300 \\ -0.0111 \end{array}$	$\begin{array}{r} a_0^{f_0} \\ 0.7106 \\ -0.3199 \\ -0.0350 \\ 1 \\ -0.5132 \\ 0.1123 \\ 0.5190 \\ -0.2037 \\ -0.0014 \\ 0.2531 \end{array}$	$\begin{array}{c} a_1^{f_0} \\ -0.2661 \\ 0.4277 \\ 0.1309 \\ -0.5132 \\ 1 \\ -0.5243 \\ -0.1791 \\ 0.2285 \\ 0.0094 \\ -0.1770 \end{array}$	$\begin{array}{r} a_2^{f_0} \\ -0.0293 \\ 0.0649 \\ 0.0939 \\ 0.1123 \\ -0.5243 \\ 1 \\ -0.0222 \\ 0.0275 \\ 0.0138 \\ 0.0044 \end{array}$	$\begin{array}{c} a_0^{f_\perp} \\ 0.6259 \\ -0.2548 \\ 0.0181 \\ 0.5190 \\ -0.1791 \\ -0.0222 \\ 1 \\ -0.5829 \\ 0.1142 \\ 0.1754 \end{array}$	$\begin{array}{c} a_1^{f_\perp} \\ -0.2683 \\ 0.2618 \\ -0.0149 \\ -0.2037 \\ 0.2285 \\ 0.0275 \\ -0.5829 \\ 1 \\ -0.4656 \\ -0.1154 \end{array}$	$\begin{array}{c} a_2^{f_\perp} \\ 0.0077 \\ -0.0102 \\ 0.0300 \\ -0.0014 \\ 0.0094 \\ 0.0138 \\ 0.1142 \\ -0.4656 \\ 1 \\ -0.0006 \end{array}$	$\begin{array}{c} a_0^{g_{\perp},g_{+}} \\ 0.1992 \\ -0.1403 \\ -0.0111 \\ 0.2531 \\ -0.1770 \\ 0.0044 \\ 0.1754 \\ -0.1154 \\ -0.0006 \\ 1 \end{array}$	$\begin{array}{r} a_1^{g+} \\ -0.1307 \\ 0.1878 \\ 0.0190 \\ -0.2100 \\ 0.2589 \\ -0.0148 \\ -0.1255 \\ 0.1472 \\ -0.0003 \\ -0.4436 \end{array}$	$\begin{array}{r} a_2^{g+} \\ -0.0277 \\ 0.0413 \\ 0.0007 \\ 0.0128 \\ 0.0134 \\ 0.0300 \\ -0.0168 \\ 0.0360 \\ 0.0057 \\ 0.0876 \end{array}$	$\begin{array}{r} a_0^{g_0} \\ 0.2833 \\ -0.1575 \\ 0.0005 \\ 0.2012 \\ -0.1266 \\ -0.0074 \\ 0.2874 \\ -0.1487 \\ 0.0049 \\ 0.7054 \end{array}$	$\begin{array}{r} a_1^{g_0} \\ -0.1838 \\ 0.1932 \\ -0.0041 \\ -0.1481 \\ 0.1854 \\ 0.0112 \\ -0.1811 \\ 0.1650 \\ -0.0059 \\ -0.2594 \end{array}$	$\begin{array}{r} a_2^{g_0} \\ 0.0436 \\ -0.0364 \\ 0.0186 \\ 0.0096 \\ -0.0086 \\ -0.0034 \\ 0.0416 \\ -0.0341 \\ 0.0087 \\ 0.0128 \end{array}$	$\begin{array}{c} a_1^{g_\perp} \\ -0.1611 \\ 0.1703 \\ 0.0246 \\ -0.2057 \\ 0.2339 \\ -0.0218 \\ -0.1320 \\ 0.1319 \\ -0.0006 \\ -0.4268 \end{array}$	$\begin{array}{c} a_2^{g_\perp} \\ 0.0088 \\ 0.0030 \\ 0.0088 \\ -0.0079 \\ 0.0127 \\ 0.0075 \\ -0.0086 \\ 0.0096 \\ 0.0033 \\ 0.0479 \end{array}$
$\begin{array}{c} \hline \underline{\Lambda_b \to \Lambda_c} \\ \hline \underline{\Lambda_b \to \Lambda_c} \\ a_0^{f_+} \\ a_1^{f_+} \\ a_2^{f_0} \\ a_1^{f_0} \\ a_1^{f_0} \\ a_2^{f_0} \\ a_0^{f_{-1}} \\ a_2^{f_{-1}} \\ a_2^{f_{-1}} \\ a_2^{f_{-1}} \\ a_1^{f_{-1}} \\ a_2^{f_{-1}} \\ a_2^{f_{-1}} \\ a_1^{f_{-1}} \\ a_2^{f_{-1}} $	$\begin{array}{c} a_0^{f+} \\ 1 \\ -0.5220 \\ 0.1623 \\ 0.7106 \\ -0.2661 \\ -0.0293 \\ 0.6259 \\ -0.2683 \\ 0.0077 \\ 0.1992 \\ -0.1307 \end{array}$	$\begin{array}{c} a_1^{f+} \\ -0.5220 \\ 1 \\ -0.6595 \\ -0.3199 \\ 0.4277 \\ 0.0649 \\ -0.2548 \\ 0.2618 \\ -0.0102 \\ -0.1403 \\ 0.1878 \end{array}$	$\begin{array}{c} a_2^{f_+} \\ 0.1623 \\ -0.6595 \\ 1 \\ -0.0350 \\ 0.0390 \\ 0.0939 \\ 0.0181 \\ -0.0149 \\ 0.0300 \\ -0.0111 \\ 0.0190 \end{array}$	$\begin{array}{c} a_0^{f_0} \\ 0.7106 \\ -0.3199 \\ -0.0350 \\ 1 \\ -0.5132 \\ 0.1123 \\ 0.5190 \\ -0.2037 \\ -0.0014 \\ 0.2531 \\ -0.2100 \end{array}$	$\begin{array}{c} a_1^{f_0} \\ -0.2661 \\ 0.4277 \\ 0.1309 \\ -0.5132 \\ 1 \\ -0.5243 \\ -0.1791 \\ 0.2285 \\ 0.0094 \\ -0.1770 \\ 0.2589 \end{array}$	$\begin{array}{c} a_2^{f_0} \\ -0.0293 \\ 0.0649 \\ 0.0939 \\ 0.1123 \\ -0.5243 \\ 1 \\ -0.0222 \\ 0.0275 \\ 0.0138 \\ 0.0044 \\ -0.0148 \end{array}$	$\begin{array}{c} a_0^{f_\perp} \\ 0.6259 \\ -0.2548 \\ 0.0181 \\ 0.5190 \\ -0.1791 \\ -0.0222 \\ 1 \\ -0.5829 \\ 0.1142 \\ 0.1754 \\ -0.1255 \end{array}$	$\begin{array}{c} a_1^{f\perp} \\ -0.2683 \\ 0.2618 \\ -0.0149 \\ -0.2037 \\ 0.2285 \\ 0.0275 \\ -0.5829 \\ 1 \\ -0.4656 \\ -0.1154 \\ 0.1472 \end{array}$	$\begin{array}{c} a_2^{f_\perp} \\ 0.0077 \\ -0.0102 \\ 0.0300 \\ -0.0014 \\ 0.0094 \\ 0.0138 \\ 0.1142 \\ -0.4656 \\ 1 \\ -0.0006 \\ -0.0003 \end{array}$	$\begin{array}{c} a_0^{g_\perp,g_+} \\ 0.1992 \\ -0.1403 \\ -0.0111 \\ 0.2531 \\ -0.1770 \\ 0.0044 \\ 0.1754 \\ -0.1154 \\ -0.0006 \\ 1 \\ -0.4436 \end{array}$	$\begin{array}{c} a_1^{g+} \\ -0.1307 \\ 0.1878 \\ 0.0190 \\ -0.2100 \\ 0.2589 \\ -0.0148 \\ -0.1255 \\ 0.1472 \\ -0.0003 \\ -0.4436 \\ 1 \end{array}$	$\begin{array}{r} a_2^{g_+} \\ -0.0277 \\ 0.0413 \\ 0.0007 \\ 0.0128 \\ 0.0134 \\ 0.0300 \\ -0.0168 \\ 0.0360 \\ 0.0057 \\ 0.0876 \\ -0.5465 \end{array}$	$\begin{array}{c} a_0^{g_0} \\ 0.2833 \\ -0.1575 \\ 0.0005 \\ 0.2012 \\ -0.1266 \\ -0.0074 \\ 0.2874 \\ -0.1487 \\ 0.0049 \\ 0.7054 \\ -0.2790 \end{array}$	$\begin{array}{c} a_1^{g_0} \\ -0.1838 \\ 0.1932 \\ -0.0041 \\ -0.1481 \\ 0.1854 \\ 0.0112 \\ -0.1811 \\ 0.1650 \\ -0.0059 \\ -0.2594 \\ 0.3438 \end{array}$	$\begin{array}{c} a_2^{g_0} \\ 0.0436 \\ -0.0364 \\ 0.0186 \\ 0.0096 \\ -0.0086 \\ -0.0034 \\ 0.0416 \\ -0.0341 \\ 0.0087 \\ 0.0128 \\ 0.0541 \end{array}$	$\begin{array}{c} a_1^{g_\perp} \\ -0.1611 \\ 0.1703 \\ 0.0246 \\ -0.2057 \\ 0.2339 \\ -0.0218 \\ -0.1320 \\ 0.1319 \\ -0.0006 \\ -0.4268 \\ 0.4776 \end{array}$	$\begin{array}{c} a_2^{g_\perp} \\ 0.0088 \\ 0.0030 \\ 0.0088 \\ -0.0079 \\ 0.0127 \\ 0.0075 \\ -0.0086 \\ 0.0096 \\ 0.0033 \\ 0.0479 \\ -0.1381 \end{array}$
$\begin{array}{c} \hline \underline{\Lambda_b \to \Lambda_c} \\ \hline \underline{\Lambda_b \to \Lambda_c} \\ a_0^{f_+} \\ a_1^{f_+} \\ a_2^{f_0} \\ a_1^{f_0} \\ a_1^{f_0} \\ a_2^{f_0} \\ a_1^{f_1} \\ a_2^{f_2} \\ a_0^{f_{1+}} \\ a_2^{f_{2+}} \\ a_1^{g_{1+}} \\ a_2^{g_{1+}} \\ a_2^{g_{2+}} \end{array}$	$\begin{array}{c} a_0^{f+} \\ 1 \\ -0.5220 \\ 0.1623 \\ 0.7106 \\ -0.2661 \\ -0.0293 \\ 0.6259 \\ -0.2683 \\ 0.0077 \\ 0.1992 \\ -0.1307 \\ -0.0277 \end{array}$	$\begin{array}{c} a_1^{f+} \\ -0.5220 \\ 1 \\ -0.6595 \\ -0.3199 \\ 0.4277 \\ 0.0649 \\ -0.2548 \\ 0.2618 \\ -0.0102 \\ -0.1403 \\ 0.1878 \\ 0.0413 \end{array}$	$\begin{array}{c} a_2^{f_+} \\ 0.1623 \\ -0.6595 \\ 1 \\ -0.0350 \\ 0.0390 \\ 0.0939 \\ 0.0181 \\ -0.0149 \\ 0.0300 \\ -0.0111 \\ 0.0190 \\ 0.0007 \end{array}$	$\begin{array}{c} a_0^{f_0} \\ 0.7106 \\ -0.3199 \\ -0.0350 \\ 1 \\ -0.5132 \\ 0.1123 \\ 0.5190 \\ -0.2037 \\ -0.0014 \\ 0.2531 \\ -0.2100 \\ 0.0128 \end{array}$	$\begin{array}{c} a_1^{f_0} \\ -0.2661 \\ 0.4277 \\ 0.1309 \\ -0.5132 \\ 1 \\ -0.5243 \\ -0.1791 \\ 0.2285 \\ 0.0094 \\ -0.1770 \\ 0.2589 \\ 0.0134 \end{array}$	$\begin{array}{c} a_2^{f_0} \\ -0.0293 \\ 0.0649 \\ 0.0939 \\ 0.1123 \\ -0.5243 \\ 1 \\ -0.0222 \\ 0.0275 \\ 0.0138 \\ 0.0044 \\ -0.0148 \\ 0.0300 \end{array}$	$\begin{array}{c} a_0^{f_\perp} \\ 0.6259 \\ -0.2548 \\ 0.0181 \\ 0.5190 \\ -0.1791 \\ -0.0222 \\ 1 \\ -0.5829 \\ 0.1142 \\ 0.1754 \\ -0.1255 \\ -0.0168 \end{array}$	$\begin{array}{c} a_1^{f\perp} \\ -0.2683 \\ 0.2618 \\ -0.0149 \\ -0.2037 \\ 0.2285 \\ 0.0275 \\ -0.5829 \\ 1 \\ -0.4656 \\ -0.1154 \\ 0.1472 \\ 0.0360 \end{array}$	$\begin{array}{c} a_2^{f_\perp} \\ 0.0077 \\ -0.0102 \\ 0.0300 \\ -0.0014 \\ 0.0094 \\ 0.0138 \\ 0.1142 \\ -0.4656 \\ 1 \\ -0.0006 \\ -0.0003 \\ 0.0057 \end{array}$	$\begin{array}{c} a_0^{g_{\perp},g_{+}} \\ 0.1992 \\ -0.1403 \\ -0.0111 \\ 0.2531 \\ -0.1770 \\ 0.0044 \\ 0.1754 \\ -0.1154 \\ -0.0006 \\ 1 \\ -0.4436 \\ 0.0876 \end{array}$	$\begin{array}{c} a_1^{g+} \\ -0.1307 \\ 0.1878 \\ 0.0190 \\ -0.2100 \\ 0.2589 \\ -0.0148 \\ -0.1255 \\ 0.1472 \\ -0.0003 \\ -0.4436 \\ 1 \\ -0.5465 \end{array}$	$\begin{array}{r} a_2^{g+} \\ -0.0277 \\ 0.0413 \\ 0.0007 \\ 0.0128 \\ 0.0134 \\ 0.0300 \\ -0.0168 \\ 0.0360 \\ 0.0057 \\ 0.0876 \\ -0.5465 \\ 1 \end{array}$	$\begin{array}{c} a_0^{g_0} \\ 0.2833 \\ -0.1575 \\ 0.0005 \\ 0.2012 \\ -0.1266 \\ -0.0074 \\ 0.2874 \\ -0.1487 \\ 0.0049 \\ 0.7054 \\ -0.2790 \\ -0.0447 \end{array}$	$\begin{array}{c} a_1^{g_0} \\ -0.1838 \\ 0.1932 \\ -0.0041 \\ -0.1481 \\ 0.1854 \\ 0.0112 \\ -0.1811 \\ 0.1650 \\ -0.0059 \\ -0.2594 \\ 0.3438 \\ 0.1194 \end{array}$	$\begin{array}{c} a_2^{g_0} \\ 0.0436 \\ -0.0364 \\ 0.0186 \\ 0.0096 \\ -0.0086 \\ -0.0034 \\ 0.0416 \\ -0.0341 \\ 0.0087 \\ 0.0128 \\ 0.0541 \\ 0.0577 \end{array}$	$\begin{array}{c} a_1^{g_\perp} \\ -0.1611 \\ 0.1703 \\ 0.0246 \\ -0.2057 \\ 0.2339 \\ -0.0218 \\ -0.1320 \\ 0.1319 \\ -0.0006 \\ -0.4268 \\ 0.4776 \\ -0.1482 \end{array}$	$\begin{array}{c} a_2^{g_\perp} \\ 0.0088 \\ 0.0030 \\ 0.0088 \\ -0.0079 \\ 0.0127 \\ 0.0075 \\ -0.0086 \\ 0.0096 \\ 0.0033 \\ 0.0479 \\ -0.1381 \\ 0.2692 \end{array}$
$\begin{array}{c} \hline \underline{\Lambda_b \to \Lambda_c} \\ \hline \underline{\Lambda_b \to \Lambda_c} \\ a_0^{f_+} \\ a_1^{f_+} \\ a_2^{f_0} \\ a_1^{f_0} \\ a_1^{f_0} \\ a_1^{f_0} \\ a_1^{f_{-1}} \\ a_2^{f_{-1}} \\ a_0^{f_{-1}} \\ a_2^{f_{-1}} \\ a_1^{f_{-1}} \\ a_2^{f_{-1}} $	$\begin{array}{c} a_0^{f+} \\ 1 \\ -0.5220 \\ 0.1623 \\ 0.7106 \\ -0.2661 \\ -0.0293 \\ 0.6259 \\ -0.2683 \\ 0.0077 \\ 0.1992 \\ -0.1307 \\ -0.0277 \\ 0.2833 \end{array}$	$\begin{array}{c} a_1^{f+} \\ -0.5220 \\ 1 \\ -0.6595 \\ -0.3199 \\ 0.4277 \\ 0.0649 \\ -0.2548 \\ 0.2618 \\ -0.0102 \\ -0.1403 \\ 0.1878 \\ 0.0413 \\ -0.1575 \end{array}$	$\begin{array}{c} a_2^{f_+} \\ 0.1623 \\ -0.6595 \\ 1 \\ -0.0350 \\ 0.0939 \\ 0.0181 \\ -0.0149 \\ 0.0300 \\ -0.0111 \\ 0.0190 \\ 0.0007 \\ 0.0005 \end{array}$	$\begin{array}{c} a_0^{f_0} \\ 0.7106 \\ -0.3199 \\ -0.0350 \\ 1 \\ -0.5132 \\ 0.1123 \\ 0.5190 \\ -0.2037 \\ -0.0014 \\ 0.2531 \\ -0.2100 \\ 0.0128 \\ 0.2012 \end{array}$	$\begin{array}{c} a_1^{f_0} \\ -0.2661 \\ 0.4277 \\ 0.1309 \\ -0.5132 \\ 1 \\ -0.5243 \\ -0.1791 \\ 0.2285 \\ 0.0094 \\ -0.1770 \\ 0.2589 \\ 0.0134 \\ -0.1266 \end{array}$	$\begin{array}{c} a_2^{f_0} \\ -0.0293 \\ 0.0649 \\ 0.0939 \\ 0.1123 \\ -0.5243 \\ 1 \\ -0.0222 \\ 0.0275 \\ 0.0138 \\ 0.0044 \\ -0.0148 \\ 0.0300 \\ -0.0074 \end{array}$	$\begin{array}{c} a_0^{f_\perp} \\ 0.6259 \\ -0.2548 \\ 0.0181 \\ 0.5190 \\ -0.1791 \\ -0.0222 \\ 1 \\ -0.5829 \\ 0.1142 \\ 0.1754 \\ -0.1255 \\ -0.0168 \\ 0.2874 \end{array}$	$\begin{array}{c} a_1^{f\perp} \\ -0.2683 \\ 0.2618 \\ -0.0149 \\ -0.2037 \\ 0.2285 \\ 0.0275 \\ -0.5829 \\ 1 \\ -0.4656 \\ -0.1154 \\ 0.1472 \\ 0.0360 \\ -0.1487 \end{array}$	$\begin{array}{c} a_2^{f_\perp} \\ 0.0077 \\ -0.0102 \\ 0.0300 \\ -0.0014 \\ 0.0094 \\ 0.0138 \\ 0.1142 \\ -0.4656 \\ 1 \\ -0.0006 \\ -0.0003 \\ 0.0057 \\ 0.0049 \end{array}$	$\begin{array}{c} a_0^{g_\perp,g_+} \\ 0.1992 \\ -0.1403 \\ -0.0111 \\ 0.2531 \\ -0.1770 \\ 0.0044 \\ 0.1754 \\ -0.1154 \\ -0.0006 \\ 1 \\ -0.4436 \\ 0.0876 \\ 0.7054 \end{array}$	$\begin{array}{c} a_1^{g+} \\ -0.1307 \\ 0.1878 \\ 0.0190 \\ -0.2100 \\ 0.2589 \\ -0.0148 \\ -0.1255 \\ 0.1472 \\ -0.0003 \\ -0.4436 \\ 1 \\ -0.5465 \\ -0.2790 \end{array}$	$\begin{array}{c} a_2^{g+} \\ -0.0277 \\ 0.0413 \\ 0.0007 \\ 0.0128 \\ 0.0134 \\ 0.0300 \\ -0.0168 \\ 0.0360 \\ 0.0057 \\ 0.0876 \\ -0.5465 \\ 1 \\ -0.0447 \end{array}$	$\begin{array}{c} a_0^{g_0} \\ 0.2833 \\ -0.1575 \\ 0.0005 \\ 0.2012 \\ -0.1266 \\ -0.0074 \\ 0.2874 \\ -0.1487 \\ 0.0049 \\ 0.7054 \\ -0.2790 \\ -0.0447 \\ 1 \end{array}$	$\begin{array}{c} a_1^{g_0} \\ -0.1838 \\ 0.1932 \\ -0.0041 \\ -0.1481 \\ 0.1854 \\ 0.0112 \\ -0.1811 \\ 0.1650 \\ -0.0059 \\ -0.2594 \\ 0.3438 \\ 0.1194 \\ -0.5511 \end{array}$	$\begin{array}{c} a_2^{g_0} \\ 0.0436 \\ -0.0364 \\ 0.0186 \\ 0.0096 \\ -0.0086 \\ -0.0034 \\ 0.0416 \\ -0.0341 \\ 0.0087 \\ 0.0128 \\ 0.0541 \\ 0.0577 \\ 0.2196 \end{array}$	$\begin{array}{c} a_1^{g_\perp} \\ -0.1611 \\ 0.1703 \\ 0.0246 \\ -0.2057 \\ 0.2339 \\ -0.0218 \\ -0.1320 \\ 0.1319 \\ -0.0006 \\ -0.4268 \\ 0.4776 \\ -0.1482 \\ -0.3015 \end{array}$	$\begin{array}{c} a_2^{g_\perp} \\ 0.0088 \\ 0.0030 \\ 0.0088 \\ -0.0079 \\ 0.0127 \\ 0.0075 \\ -0.0086 \\ 0.0096 \\ 0.0033 \\ 0.0479 \\ -0.1381 \\ 0.2692 \\ 0.0059 \end{array}$
$\begin{array}{c} \hline \underline{\Lambda_b \to \Lambda_c} \\ \hline \underline{\Lambda_b \to \Lambda_c} \\ a_0^{f_+} \\ a_1^{f_+} \\ a_2^{f_0} \\ a_1^{f_0} \\ a_1^{f_0} \\ a_2^{f_{0}} \\ a_1^{f_{1}} \\ a_2^{g_{\perp},g_+} \\ a_0^{f_{\perp}} \\ a_0^{g_{\perp},g_+} \\ a_0^{g_{1}} \\ a_2^{g_{2}} \\ a_0^{g_{0}} \\ a_1^{g_{1}} \\ a_2^{g_{2}} \\ a_0^{g_{0}} \\ a_1^{g_{0}} \\ a_1^{g_{1}} \\ a_2^{g_{2}} \\ a_0^{g_{0}} \\ a_1^{g_{1}} \\ a_2^{g_{2}} \\ a_0^{g_{0}} \\ a_1^{g_{1}} \\ a_2^{g_{1}} \\ a_2^{$	$\begin{array}{c} a_0^{f+} \\ 1 \\ -0.5220 \\ 0.1623 \\ 0.7106 \\ -0.2661 \\ -0.0293 \\ 0.6259 \\ -0.2683 \\ 0.0077 \\ 0.1992 \\ -0.1307 \\ -0.0277 \\ 0.2833 \\ -0.1838 \end{array}$	$\begin{array}{c} a_1^{f+} \\ -0.5220 \\ 1 \\ -0.6595 \\ -0.3199 \\ 0.4277 \\ 0.0649 \\ -0.2548 \\ 0.2618 \\ 0.26$	$\begin{array}{c} a_2^{f_+} \\ 0.1623 \\ -0.6595 \\ 1 \\ -0.0350 \\ 0.0939 \\ 0.0181 \\ -0.0149 \\ 0.0300 \\ -0.0111 \\ 0.0190 \\ 0.0007 \\ 0.0005 \\ -0.0041 \end{array}$	$\begin{array}{c} a_0^{f_0} \\ 0.7106 \\ -0.3199 \\ -0.0350 \\ 1 \\ -0.5132 \\ 0.1123 \\ 0.5190 \\ -0.2037 \\ -0.0014 \\ 0.2531 \\ -0.2100 \\ 0.0128 \\ 0.2012 \\ -0.1481 \end{array}$	$\begin{array}{c} a_1^{f_0} \\ -0.2661 \\ 0.4277 \\ 0.1309 \\ -0.5132 \\ 1 \\ -0.5243 \\ -0.1791 \\ 0.2285 \\ 0.0094 \\ -0.1770 \\ 0.2589 \\ 0.0134 \\ -0.1266 \\ 0.1854 \end{array}$	$\begin{array}{c} a_2^{f_0} \\ -0.0293 \\ 0.0649 \\ 0.0939 \\ 0.1123 \\ -0.5243 \\ 1 \\ -0.0222 \\ 0.0275 \\ 0.0138 \\ 0.0044 \\ -0.0148 \\ 0.0300 \\ -0.0074 \\ 0.0112 \end{array}$	$\begin{array}{c} a_0^{f_\perp} \\ 0.6259 \\ -0.2548 \\ 0.0181 \\ 0.5190 \\ -0.1791 \\ -0.0222 \\ 1 \\ -0.5829 \\ 0.1142 \\ 0.1754 \\ -0.1255 \\ -0.0168 \\ 0.2874 \\ -0.1811 \end{array}$	$\begin{array}{c} a_1^{f\perp} \\ -0.2683 \\ 0.2618 \\ -0.0149 \\ -0.2037 \\ 0.2285 \\ 0.0275 \\ -0.5829 \\ 1 \\ -0.4656 \\ -0.1154 \\ 0.1472 \\ 0.0360 \\ -0.1487 \\ 0.1650 \end{array}$	$\begin{array}{c} a_2^{f_\perp} \\ 0.0077 \\ -0.0102 \\ 0.0300 \\ -0.0014 \\ 0.0094 \\ 0.0138 \\ 0.1142 \\ -0.4656 \\ 1 \\ -0.0006 \\ -0.0003 \\ 0.0057 \\ 0.0049 \\ -0.0059 \end{array}$	$\begin{array}{c} a_0^{g_\perp,g_+} \\ 0.1992 \\ -0.1403 \\ -0.0111 \\ 0.2531 \\ -0.1770 \\ 0.0044 \\ 0.1754 \\ -0.1154 \\ -0.0006 \\ 1 \\ -0.4436 \\ 0.0876 \\ 0.7054 \\ -0.2594 \end{array}$	$\begin{array}{c} a_1^{g+} \\ -0.1307 \\ 0.1878 \\ 0.0190 \\ -0.2100 \\ 0.2589 \\ -0.0148 \\ -0.1255 \\ 0.1472 \\ -0.0003 \\ -0.4436 \\ 1 \\ -0.5465 \\ -0.2790 \\ 0.3438 \end{array}$	$\begin{array}{c} a_2^{g+} \\ -0.0277 \\ 0.0413 \\ 0.0007 \\ 0.0128 \\ 0.0134 \\ 0.0300 \\ -0.0168 \\ 0.0360 \\ 0.0057 \\ 0.0876 \\ -0.5465 \\ 1 \\ -0.0447 \\ 0.1194 \end{array}$	$\begin{array}{c} a_0^{g_0} \\ 0.2833 \\ -0.1575 \\ 0.0005 \\ 0.2012 \\ -0.1266 \\ -0.0074 \\ 0.2874 \\ -0.1487 \\ 0.0049 \\ 0.7054 \\ -0.2790 \\ -0.0447 \\ 1 \\ -0.5511 \end{array}$	$\begin{array}{c} a_1^{g_0} \\ -0.1838 \\ 0.1932 \\ -0.0041 \\ -0.1481 \\ 0.1854 \\ 0.0112 \\ -0.1811 \\ 0.1650 \\ -0.0059 \\ -0.2594 \\ 0.3438 \\ 0.1194 \\ -0.5511 \\ 1 \end{array}$	$\begin{array}{c} a_2^{g_0} \\ 0.0436 \\ -0.0364 \\ 0.0186 \\ 0.0096 \\ -0.0086 \\ -0.0034 \\ 0.0416 \\ -0.0341 \\ 0.0087 \\ 0.0128 \\ 0.0541 \\ 0.0577 \\ 0.2196 \\ -0.7687 \end{array}$	$\begin{array}{c} a_1^{g_\perp} \\ -0.1611 \\ 0.1703 \\ 0.0246 \\ -0.2057 \\ 0.2339 \\ -0.0218 \\ -0.1320 \\ 0.1319 \\ -0.0006 \\ -0.4268 \\ 0.4776 \\ -0.1482 \\ -0.3015 \\ 0.2440 \end{array}$	$\begin{array}{c} a_2^{g_\perp} \\ 0.0088 \\ 0.0030 \\ 0.0088 \\ -0.0079 \\ 0.0127 \\ 0.0075 \\ -0.0086 \\ 0.0096 \\ 0.0033 \\ 0.0479 \\ -0.1381 \\ 0.2692 \\ 0.0059 \\ 0.0190 \end{array}$
$\begin{array}{c} \hline \underline{\Lambda_b \to \Lambda_c} \\ \hline \underline{\Lambda_b^{f_+}} \\ a_0^{f_+} \\ a_1^{f_+} \\ a_2^{f_0} \\ a_1^{f_0} \\ a_1^{f_0} \\ a_1^{f_0} \\ a_2^{f_{-1}} \\ a_2^{g_{-1},g_+} \\ a_0^{f_{-1}} \\ a_2^{g_{+1},g_+} \\ a_2^{g_{+1}} \\ a_2^{g_{+1}} \\ a_2^{g_{+1}} \\ a_2^{g_{-1}} \\ a_2^{$	$\begin{array}{c} a_0^{f+} \\ 1 \\ -0.5220 \\ 0.1623 \\ 0.7106 \\ -0.2661 \\ -0.0293 \\ 0.6259 \\ -0.2683 \\ 0.0077 \\ 0.1992 \\ -0.1307 \\ -0.0277 \\ 0.2833 \\ -0.1838 \\ 0.0436 \end{array}$	$\begin{array}{c} a_1^{f+} \\ -0.5220 \\ 1 \\ -0.6595 \\ -0.3199 \\ 0.4277 \\ 0.0649 \\ -0.2548 \\ 0.2618 \\ 0.2618 \\ 0.2618 \\ 0.2618 \\ 0.2618 \\ 0.2618 \\ 0.2618 \\ 0.2618 \\ 0.2618 \\ 0.1575 \\ 0.1932 \\ -0.0364 \end{array}$	$\begin{array}{c} a_2^{f_+} \\ 0.1623 \\ -0.6595 \\ 1 \\ -0.0350 \\ 0.0939 \\ 0.0181 \\ -0.0149 \\ 0.0300 \\ -0.0111 \\ 0.0190 \\ 0.0007 \\ 0.0005 \\ -0.0041 \\ 0.0186 \end{array}$	$\begin{array}{c} a_0^{f_0} \\ 0.7106 \\ -0.3199 \\ -0.0350 \\ 1 \\ -0.5132 \\ 0.1123 \\ 0.5190 \\ -0.2037 \\ -0.0014 \\ 0.2531 \\ -0.2100 \\ 0.0128 \\ 0.2012 \\ -0.1481 \\ 0.0096 \end{array}$	$\begin{array}{c} a_1^{f_0} \\ -0.2661 \\ 0.4277 \\ 0.1309 \\ -0.5132 \\ 1 \\ -0.5243 \\ -0.1791 \\ 0.2285 \\ 0.0094 \\ -0.1770 \\ 0.2589 \\ 0.0134 \\ -0.1266 \\ 0.1854 \\ -0.0086 \end{array}$	$\begin{array}{c} a_2^{f_0} \\ -0.0293 \\ 0.0649 \\ 0.0939 \\ 0.1123 \\ -0.5243 \\ 1 \\ -0.0222 \\ 0.0275 \\ 0.0138 \\ 0.0044 \\ -0.0148 \\ 0.0300 \\ -0.0074 \\ 0.0112 \\ -0.0034 \end{array}$	$\begin{array}{c} a_0^{f\perp} \\ 0.6259 \\ -0.2548 \\ 0.0181 \\ 0.5190 \\ -0.1791 \\ -0.0222 \\ 1 \\ -0.5829 \\ 0.1142 \\ 0.1754 \\ -0.1255 \\ -0.0168 \\ 0.2874 \\ -0.1811 \\ 0.0416 \end{array}$	$\begin{array}{c} a_1^{f\perp} \\ -0.2683 \\ 0.2618 \\ -0.0149 \\ -0.2037 \\ 0.2285 \\ 0.0275 \\ -0.5829 \\ 1 \\ -0.4656 \\ -0.1154 \\ 0.1472 \\ 0.0360 \\ -0.1487 \\ 0.1650 \\ -0.0341 \end{array}$	$\begin{array}{c} a_2^{f_\perp} \\ 0.0077 \\ -0.0102 \\ 0.0300 \\ -0.0014 \\ 0.0094 \\ 0.0138 \\ 0.1142 \\ -0.4656 \\ 1 \\ -0.0006 \\ -0.0003 \\ 0.0057 \\ 0.0049 \\ -0.0059 \\ 0.0087 \end{array}$	$\begin{array}{c} a_0^{g_\perp,g_+} \\ 0.1992 \\ -0.1403 \\ -0.0111 \\ 0.2531 \\ -0.1770 \\ 0.0044 \\ 0.1754 \\ -0.1154 \\ -0.0006 \\ 1 \\ -0.4436 \\ 0.0876 \\ 0.7054 \\ -0.2594 \\ 0.0128 \end{array}$	$\begin{array}{c} a_1^{g+} \\ -0.1307 \\ 0.1878 \\ 0.0190 \\ -0.2100 \\ 0.2589 \\ -0.0148 \\ -0.1255 \\ 0.1472 \\ -0.0003 \\ -0.4436 \\ 1 \\ -0.5465 \\ -0.2790 \\ 0.3438 \\ 0.0541 \end{array}$	$\begin{array}{c} a_2^{g+} \\ -0.0277 \\ 0.0413 \\ 0.0007 \\ 0.0128 \\ 0.0134 \\ 0.0300 \\ -0.0168 \\ 0.0360 \\ 0.0057 \\ 0.0876 \\ -0.5465 \\ 1 \\ -0.0447 \\ 0.1194 \\ 0.0577 \end{array}$	$\begin{array}{c} a_{0}^{g_{0}} \\ a_{0}^{g_{0}} \\ 0.2833 \\ -0.1575 \\ 0.0005 \\ 0.2012 \\ -0.1266 \\ -0.0074 \\ 0.2874 \\ -0.1487 \\ 0.0049 \\ 0.7054 \\ -0.2790 \\ -0.0447 \\ 1 \\ -0.5511 \\ 0.2196 \end{array}$	$\begin{array}{c} a_1^{g_0} \\ -0.1838 \\ 0.1932 \\ -0.0041 \\ -0.1481 \\ 0.1854 \\ 0.0112 \\ -0.1811 \\ 0.1650 \\ -0.0059 \\ -0.2594 \\ 0.3438 \\ 0.1194 \\ -0.5511 \\ 1 \\ -0.7687 \end{array}$	$\begin{array}{c} a_2^{g_0} \\ 0.0436 \\ -0.0364 \\ 0.0186 \\ 0.0096 \\ -0.0034 \\ 0.0416 \\ -0.0341 \\ 0.0087 \\ 0.0128 \\ 0.0541 \\ 0.0577 \\ 0.2196 \\ -0.7687 \\ 1 \end{array}$	$\begin{array}{c} a_1^{g_\perp} \\ -0.1611 \\ 0.1703 \\ 0.0246 \\ -0.2057 \\ 0.2339 \\ -0.0218 \\ -0.1320 \\ 0.1319 \\ -0.0006 \\ -0.4268 \\ 0.4776 \\ -0.1482 \\ -0.3015 \\ 0.2440 \\ 0.0004 \end{array}$	$\begin{array}{c} a_2^{g_\perp} \\ 0.0088 \\ 0.0030 \\ 0.0088 \\ -0.0079 \\ 0.0127 \\ 0.0075 \\ -0.0086 \\ 0.0096 \\ 0.0033 \\ 0.0479 \\ -0.1381 \\ 0.2692 \\ 0.0059 \\ 0.0190 \\ 0.0405 \end{array}$
$\begin{array}{c} \hline & \overline{\Lambda_b \to \Lambda_c} \\ \hline & \overline{\Lambda_b} \to \Lambda_c \\ a_0^{f_+} & a_1^{f_+} \\ a_1^{f_+} & a_2^{f_0} \\ a_1^{f_0} & a_1^{f_0} \\ a_2^{f_0} & a_2^{f_{-1}} \\ a_0^{f_{-1}} & a_0^{f_{-1}} \\ a_2^{g_{-1},g_+} \\ a_0^{g_{+1}} & a_2^{g_{+1}} \\ a_2^{g_0} & a_1^{g_0} \\ a_2^{g_0} & a_1^{g_0} \\ a_2^{g_0} & a_2^{g_0} \\ a_2^{g_0} & a_2^{g_0} \\ a_2^{g_0} & a_2^{g_1} \\ a_2^{g_1} & a_2^{g_1} \\ a_3^{g_1} & a_3^{g_1} \\ a_4^{g_1} & a_4^{g_1} \\$	$\begin{array}{c} a_0^{f+} \\ 1 \\ -0.5220 \\ 0.1623 \\ 0.7106 \\ -0.2661 \\ -0.0293 \\ 0.6259 \\ -0.2683 \\ 0.0077 \\ 0.1992 \\ -0.1307 \\ -0.0277 \\ 0.2833 \\ -0.1838 \\ 0.0436 \\ -0.1611 \end{array}$	$\begin{array}{c} a_1^{f+} \\ -0.5220 \\ 1 \\ -0.6595 \\ -0.3199 \\ 0.4277 \\ 0.0649 \\ -0.2548 \\ 0.2618 \\ -0.0102 \\ -0.1403 \\ 0.1878 \\ 0.0413 \\ -0.1575 \\ 0.1932 \\ -0.0364 \\ 0.1703 \end{array}$	$\begin{array}{c} a_2^{f_+} \\ 0.1623 \\ -0.6595 \\ 1 \\ -0.0350 \\ 0.0939 \\ 0.0181 \\ -0.0149 \\ 0.0300 \\ -0.0111 \\ 0.0190 \\ 0.0007 \\ 0.0005 \\ -0.0041 \\ 0.0186 \\ 0.0246 \end{array}$	$\begin{array}{c} a_0^{f_0} \\ a_0^{f_0} \\ 0.7106 \\ -0.3199 \\ -0.0350 \\ 1 \\ -0.5132 \\ 0.1123 \\ 0.5190 \\ -0.2037 \\ -0.0014 \\ 0.2531 \\ -0.2100 \\ 0.0128 \\ 0.2012 \\ -0.1481 \\ 0.0096 \\ -0.2057 \end{array}$	$\begin{array}{c} a_1^{f_0} \\ -0.2661 \\ 0.4277 \\ 0.1309 \\ -0.5132 \\ 1 \\ -0.5243 \\ -0.1791 \\ 0.2285 \\ 0.0094 \\ -0.1770 \\ 0.2589 \\ 0.0134 \\ -0.1266 \\ 0.1854 \\ -0.0086 \\ 0.2339 \end{array}$	$\begin{array}{r} a_2^{f_0} \\ -0.0293 \\ 0.0649 \\ 0.0939 \\ 0.1123 \\ -0.5243 \\ 1 \\ -0.0222 \\ 0.0275 \\ 0.0138 \\ 0.0044 \\ -0.0148 \\ 0.0300 \\ -0.0074 \\ 0.0112 \\ -0.0034 \\ -0.0218 \end{array}$	$\begin{array}{c} a_0^{f\perp} \\ 0.6259 \\ -0.2548 \\ 0.0181 \\ 0.5190 \\ -0.1791 \\ -0.0222 \\ 1 \\ -0.5829 \\ 0.1142 \\ 0.1754 \\ -0.1255 \\ -0.0168 \\ 0.2874 \\ -0.1811 \\ 0.0416 \\ -0.1320 \end{array}$	$\begin{array}{c} a_1^{f\perp} \\ -0.2683 \\ 0.2618 \\ -0.0149 \\ -0.2037 \\ 0.2285 \\ 0.0275 \\ -0.5829 \\ 1 \\ -0.4656 \\ -0.1154 \\ 0.1472 \\ 0.0360 \\ -0.1487 \\ 0.1650 \\ -0.0341 \\ 0.1319 \end{array}$	$\begin{array}{c} a_2^{f_\perp} \\ 0.0077 \\ -0.0102 \\ 0.0300 \\ -0.0014 \\ 0.0094 \\ 0.0138 \\ 0.1142 \\ -0.4656 \\ 1 \\ -0.0006 \\ -0.0003 \\ 0.0057 \\ 0.0049 \\ -0.0059 \\ 0.0087 \\ -0.0006 \end{array}$	$\begin{array}{c} a_0^{g_\perp,g_+} \\ 0.1992 \\ -0.1403 \\ -0.0111 \\ 0.2531 \\ -0.1770 \\ 0.0044 \\ 0.1754 \\ -0.1154 \\ -0.0006 \\ 1 \\ -0.4436 \\ 0.0876 \\ 0.7054 \\ -0.2594 \\ 0.0128 \\ -0.4268 \end{array}$	$\begin{array}{c} a_1^{g+} \\ -0.1307 \\ 0.1878 \\ 0.0190 \\ -0.2100 \\ 0.2589 \\ -0.0148 \\ -0.1255 \\ 0.1472 \\ -0.0003 \\ -0.4436 \\ 1 \\ -0.5465 \\ -0.2790 \\ 0.3438 \\ 0.0541 \\ 0.4776 \end{array}$	$\begin{array}{r} a_2^{g+} \\ -0.0277 \\ 0.0413 \\ 0.0007 \\ 0.0128 \\ 0.0134 \\ 0.0300 \\ -0.0168 \\ 0.0300 \\ 0.0057 \\ 0.0876 \\ -0.5465 \\ 1 \\ -0.0447 \\ 0.1194 \\ 0.0577 \\ -0.1482 \end{array}$	$\begin{array}{c} a_{0}^{g_{0}} \\ a_{0}^{g_{0}} \\ 0.2833 \\ -0.1575 \\ 0.0005 \\ 0.2012 \\ -0.1266 \\ -0.0074 \\ 0.2874 \\ -0.1487 \\ 0.0049 \\ 0.7054 \\ -0.2790 \\ -0.0447 \\ 1 \\ -0.5511 \\ 0.2196 \\ -0.3015 \end{array}$	$\begin{array}{c} a_1^{g_0} \\ -0.1838 \\ 0.1932 \\ -0.0041 \\ -0.1481 \\ 0.1854 \\ 0.0112 \\ -0.1811 \\ 0.1650 \\ -0.0059 \\ -0.2594 \\ 0.3438 \\ 0.1194 \\ -0.5511 \\ 1 \\ -0.7687 \\ 0.2440 \end{array}$	$\begin{array}{c} a_2^{g_0} \\ 0.0436 \\ -0.0364 \\ 0.0186 \\ 0.0096 \\ -0.0086 \\ -0.0034 \\ 0.0416 \\ -0.0341 \\ 0.0087 \\ 0.0128 \\ 0.0541 \\ 0.0577 \\ 0.2196 \\ -0.7687 \\ 1 \\ 0.0004 \end{array}$	$\begin{array}{c} a_1^{g_\perp} \\ -0.1611 \\ 0.1703 \\ 0.0246 \\ -0.2057 \\ 0.2339 \\ -0.0218 \\ -0.1320 \\ 0.1319 \\ -0.0006 \\ -0.4268 \\ 0.4776 \\ -0.1482 \\ -0.3015 \\ 0.2440 \\ 0.0004 \\ 1 \end{array}$	$\begin{array}{c} a_2^{g_\perp} \\ 0.0088 \\ 0.0030 \\ 0.0088 \\ -0.0079 \\ 0.0127 \\ 0.0075 \\ -0.0086 \\ 0.0096 \\ 0.0033 \\ 0.0479 \\ -0.1381 \\ 0.2692 \\ 0.0059 \\ 0.0190 \\ 0.0405 \\ -0.5028 \end{array}$

TABLE XI. Correlation matrices of the higher-order form factor parameters for $\Lambda_b \to p$ (top) and $\Lambda_b \to \Lambda_c$ (bottom).

- This should give the ultimate precision.
 - Important if uncertainty from $B X_c$ form factors is significant.

To treat correlated form factor uncertainties fully in the analysis, need full covariance

Monahan et al, Phys. Rev. D 98, 114509 (2018)

TABLE XI. Covariance matrix for the coefficients of z-expansion and the corresponding Blaschke factors for the simultaneous fit to the $B_s \to K \ell \nu$ and $B_s \to D_s \ell \nu$ decays. The rows correspond to the columns, moving from top to bottom and left to right, respectively.

$a_1^{(0),K}$	$a_2^{(0),K}$	$a_3^{(0),K}$	$P_0^{(K)}$	$a_0^{(+),K}$	$a_1^{(+),K}$
7.81655746×10 ⁻	$^{-3}$ 5.11931999×10 ⁻² 4.94505240×10 ⁻¹	$\begin{array}{c} 1.26040746\!\times\!10^{-1} \\ 1.62865239 \\ 6.51816994 \end{array}$	$-3.95599616 \times 10^{-7}$ $2.22974369 \times 10^{-6}$ $-4.88348307 \times 10^{-8}$ $9.99995307 \times 10^{-7}$	$\begin{array}{c} 6.67729571 \times 10^{-4} \\ 3.58512534 \times 10^{-3} \\ 9.03252850 \times 10^{-3} \\ -1.81816269 \times 10^{-9} \\ 3.09228616 \times 10^{-4} \end{array}$	$7.88936302 \times 10^{-3}$ $6.75709862 \times 10^{-2}$ $1.99167048 \times 10^{-1}$ $1.55891061 \times 10^{-7}$ $-5.88646696 \times 10^{-5}$ $1.46893824 \times 10^{-2}$
$a_2^{(+),K}$	$P_{+}^{(K)}$	$a_0^{(0),D_s}$	$a_1^{(0),D_s}$	$a_2^{(0),D_s}$	$a_3^{(0),D_s}$
$\begin{array}{c} 5.54055868 \times 10^{-2} \\ 5.20212224 \times 10^{-1} \\ 1.72576055 \\ 1.27709131 \times 10^{-6} \\ 5.57789886 \times 10^{-4} \\ 6.49789179 \times 10^{-2} \\ 7.40157233 \times 10^{-1} \end{array}$	$5.22263419 \times 10^{-9}$ $4.60220124 \times 10^{-8}$ $1.64613013 \times 10^{-7}$ $4.34812507 \times 10^{-15}$ $3.44350904 \times 10^{-9}$ $-1.42002142 \times 10^{-7}$ $8.20182628 \times 10^{-7}$ $5.28997606 \times 10^{-8}$	$\begin{array}{c} 4.89761879 \times 10^{-5} \\ 4.23550639 \times 10^{-4} \\ 5.32746249 \times 10^{-4} \\ -2.93868039 \times 10^{-9} \\ 1.08803466 \times 10^{-4} \\ 2.37456520 \times 10^{-4} \\ 9.33127619 \times 10^{-4} \\ -4.00252884 \times 10^{-11} \\ 1.51331616 \times 10^{-3} \end{array}$	$\begin{array}{c} 1.47978430 \times 10^{-3} \\ -1.12557927 \times 10^{-3} \\ -8.00096682 \times 10^{-3} \\ 3.60812633 \times 10^{-8} \\ 7.14515361 \times 10^{-4} \\ -7.74705909 \times 10^{-3} \\ 3.38332719 \times 10^{-4} \\ 1.55683903 \times 10^{-10} \\ -1.32946477 \times 10^{-3} \\ 1.14391084 \times 10^{-1} \end{array}$	$\begin{array}{c} 1.61294090 \times 10^{-4} \\ -4.15916006 \times 10^{-4} \\ -1.57760368 \times 10^{-3} \\ 3.12552274 \times 10^{-9} \\ 1.46191770 \times 10^{-4} \\ -1.63296714 \times 10^{-3} \\ -1.12948406 \times 10^{-5} \\ 8.25859041 \times 10^{-11} \\ -2.95921529 \times 10^{-3} \\ 3.77594136 \times 10^{-1} \\ 8.04802477 \end{array}$	$\begin{array}{c} -1.50864482 \times 10^{-5} \\ 6.86722615 \times 10^{-6} \\ 6.07028861 \times 10^{-5} \\ -2.93053824 \times 10^{-10} \\ -9.57576314 \times 10^{-6} \\ 9.27876845 \times 10^{-5} \\ -1.17310027 \times 10^{-5} \\ 4.62131689 \times 10^{-12} \\ -1.18940865 \times 10^{-4} \\ -1.47064962 \times 10^{-2} \\ 6.00685427 \times 10^{-2} \\ \end{array}$



• New for B_{s^0} –>K measurement was to also provide a measurement at low q².



Low q² measurement





- Need to start making
 - In the B_s⁰ case this
 - to be good agreement in our 2017 measurement).

Ciezarek, Lupato, Rotondo, Vesterinen: JHEP02 (2017)021



• In the Λ_b^0 it would serve as a powerful validation of the lattice calculations ($\Lambda_b^0 - > \Lambda_c$ already shown



LHCb-PAPER-2017-016, Phys. Rev. D 96, 112005 (2017)

Bin purity [%]



Long term prospects

- Official goal is to determine $|V_{ub}|/|V_{cb}|$ at 1% level with full upgrade II dataset (300fb⁻¹)
- This requires D_s and/or Λ_c branching fractions to be measured at 1% level.
- Lattice assumed to be at 1% as well, seems doable particularly if we can make very high q² bin.

Uncertainty	All q^2	low q^2	high q^2
Tracking	2.0	2.0	2.0
Trigger	1.4	1.2	1.6
Particle identification	1.0	1.0	1.0
$\sigma(m_{ m corr})$	0.5	0.5	0.5
Isolation	0.2	0.2	0.2
Charged BDT	0.6	0.6	0.6
Neutral BDT	1.1	1.1	1.1
q^2 migration	—	2.0	2.0
Efficiency	1.2	1.6	1.6
Fit template	$+2.3 \\ -2.9$	$+1.8 \\ -2.4$	$+3.0 \\ -3.4$
Total	$+4.0 \\ -4.3$	$+4.3 \\ -4.5$	$+5.0 \\ -5.3$

 B_{s^0} —>K systematics

- The systematics most likely to saturate are those related to the efficiency.
 - Trigger calibration expected to be greatly simplified in run III and beyond.
 - Tracking efficiency is more challenging, need to measure the material in the detector.
 - The rest should go down to small levels.



$|V_{cb}|$ measurement from B_s decays

- Recently measured $|V_{cb}|$ with B_s decays.
- Normalise B_{s^0} signal to corresponding B^0 decays.

$$\mathcal{R} \equiv \frac{\mathcal{B}(B_s^0 \to D_s^- \mu^+ \nu_\mu)}{\mathcal{B}(B^0 \to D^- \mu^+ \nu_\mu)},$$
$$\mathcal{R}^* \equiv \frac{\mathcal{B}(B_s^0 \to D_s^{*-} \mu^+ \nu_\mu)}{\mathcal{B}(B^0 \to D^{*-} \mu^+ \nu_\mu)}$$

- Use B⁰->D^(*)µv branching fractions to determine normalisation with 4(3)% uncertainty from PDG.
- Measurement of f_s/f_d used to control production fractions
- Also limited by current knowledge on D_(s) branching fractions.

LHCb, Phys. Rev. D101 (2020) 072004

Fit to determine form factors and signal yield.



LHCb, arXiv:2003.08453

- Performed analysis with CLN and BGL parameterisations.
 - Parameters have constraints from 2:39.0.8 (stat) = $1.2(ext) \times 10^{-3}$

 $|V_{cb}|_{\rm CLN} = (41.4 \pm 0.6 \,({\rm stat}) \pm 0.9 \,({\rm syst}) \pm 1.2$ $|V_{cb}|_{BGL} = (42.3 \pm 0.8 \,(\text{stat}) \pm 0.9 \,(\text{syst}) \pm 1.2$

 Both results compatible with each other and existing measurements.

[1] McLean, Davies, Koponen, Lytle [HPQCD]: Phys. Rev. D 101, 074513 (2020)

V_{cb} results

$|V_{cb}|_{\text{CLN}} = (41.4 \pm 0.6(\text{stat}) \pm 0.9(\text{syst}) \pm 1.2(\text{ext})) \times 10^{-3}$

$$2 (\text{ext}) \times 10^{-3}$$

 $2 (\text{ext}) \times 10^{-3}$



Yes, it really is a $|V_{cb}|$ measurement

- If both numerator and denominator depend on $|V_{cb}|$, how can one be sensitive to $|V_{cb}|$?
- The point is that the denominator is measured, we do not use a prediction which depends on $|V_{cb}|$.
 - The $B^0 D^{(*)}$ branching fraction measurements could be correlated to the exclusive $|V_{cb}|$ B-factory measurements, but I understand this is a small effect(?).
- We do, however, rely on the equally of semileptonic widths. Bigi, Mannel, Uraltsev, JHEP09(2011)012
 - We are heavily dependent on this in LHCb, so might be useful to provide precise validations in data. More lifetime measurements?







Planned measurements • Plan to perform a similar measurement with Λ_b^0 decays.

• Here the normalisation is a bit different, we instead normalise to inclusive Λ_b^0 semileptonic decays and employ equally of partial widths.

$$\Gamma(\Lambda_b^0 \to \Lambda_c^+ \mu^- \overline{\nu}_\mu) = \frac{n_{\rm corr}(\Lambda_b^0 \to n_{\rm corr}(\Lambda_b^0 \to X_c \, \mu^-))}{n_{\rm corr}(\Lambda_b^0 \to X_c \, \mu^-)}$$

- Plan is to use the differential measurement as a function of q² to control form factor uncertainties a la LHCb-PAPER-2017-016
- Also plan to perform a measurement with $B^0 D^*\mu\nu$ decays using a similar method:

$$\frac{\mathcal{B}(B^0 \to D^{*-} \mu^+ \nu_{\mu})}{\mathcal{B}(B \to \bar{X}_c \mu^+ \nu_{\mu} X)} = \frac{2n_{corr} (B^0 \to D^{*-} \mu^+ \nu_{\mu})}{n_{corr} (\bar{D}^0 \mu^+ X) + n_{corr} (D^- \mu^+ X)}$$

 $\stackrel{\rightarrow}{\times} \frac{\Lambda_c^+ \mu^- \overline{\nu}_{\mu}}{\times \Gamma(\Lambda_b^0 \to X_c \mu^- \overline{\nu}_{\mu})}$



Summary and prospects

- LHCb is still relatively new to performing precise $|V_{xb}|$ measurements.
- More dependent on external inputs, but can make precise measurements in the future which are largely uncorrelated to B-factory ones.
- Expect to stay competitive with Belle-II but will take a lot of work.
- Eventually we will perform full angular analyses of these modes, which will also help determinations indirectly.
 - Expect shape information from e.g. $B^0 D^* \mu v$ decays to be complimentary to those obtained at e⁺e⁻ machines.



