

Electroweak Heavy Flavor physics at FCC-ee (LoI #152)

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Electroweak Heavy Flavour (bottom, charm, tau) at the FCC-ee

Letter of Interest submitted to Snowmass 2021

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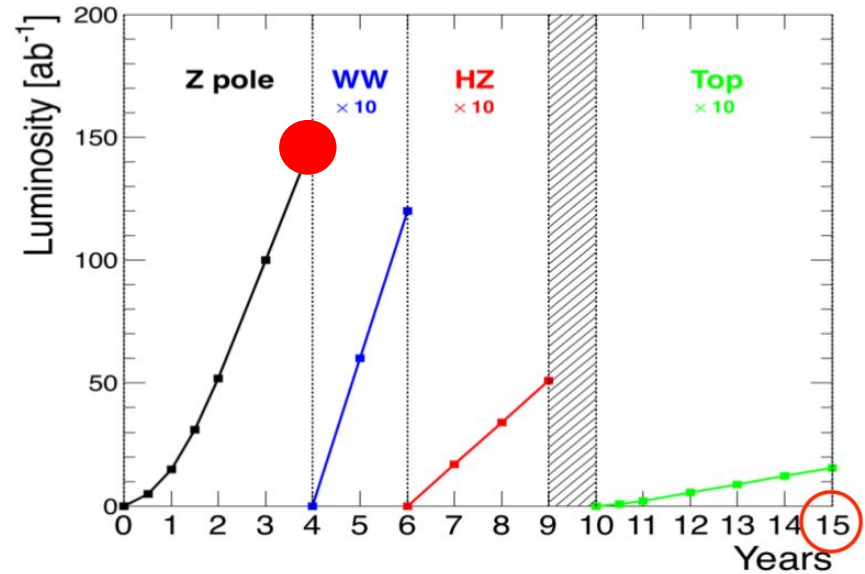
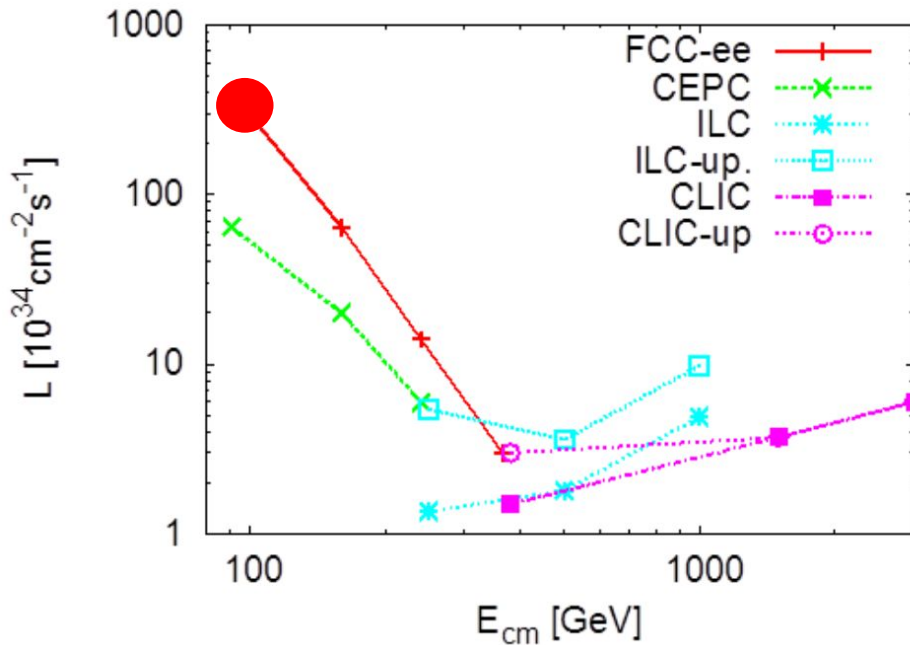
Lol #152

Abstract

The FCC-ee is a frontier Higgs, Top, Electroweak, and Flavour factory. It will be operated in a 100km circular tunnel built in the CERN area, and will serve as the first step of the FCC integrated programme towards ≥ 100 TeV proton-proton collisions in the same infrastructure [1]. In addition to an essential and unique Higgs program, it offers powerful opportunities for discovery of direct or indirect evidence for BSM physics, via a combination of high precision measurements and searches for forbidden or rare processes, and feebly coupled particles.

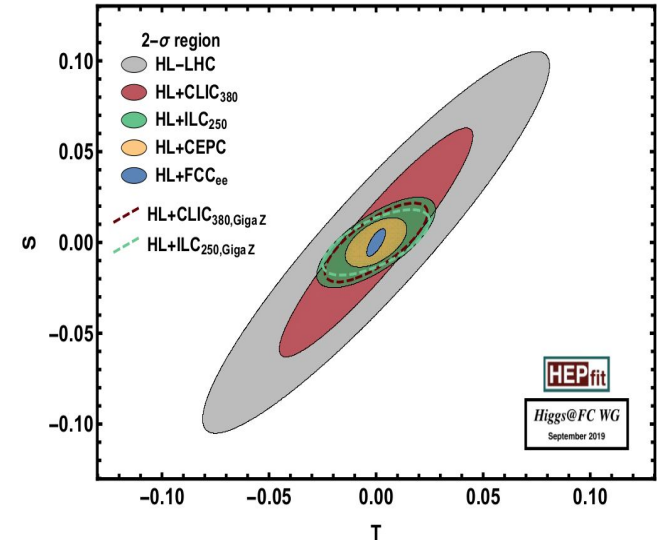
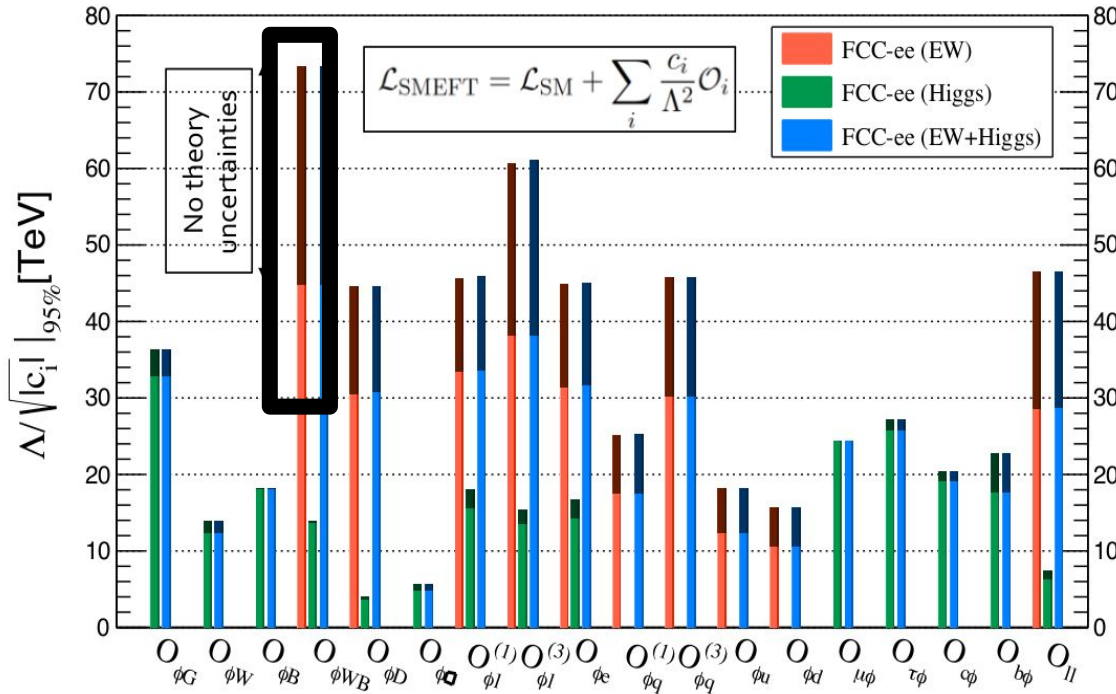
A key element of the FCC-ee physics program is, thanks to the huge Z statistics, the ability to provide a complete determination of the chiral couplings of the Z to fermions via a combination of total widths, decay rates and forward-backward or polarization asymmetries, with a leap in precision of up to two orders of magnitude. In this LOI we focus on some of the heavy flavour observables (b , c , τ). The ultimate goal, that experimental and theory systematic errors match the statistical accuracy, leads to highly demanding requirements on detector design and on theoretical calculations. This letter of interest describes some of the many challenges presented by these benchmark measurements.

FCC-ee context



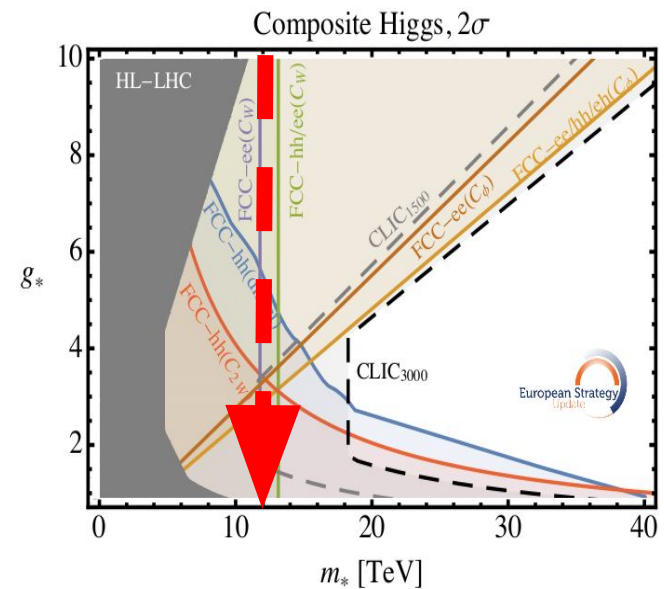
- FCC-ee: 150 ab⁻¹, 5 × 10¹² Z decays in ≈ 4 years of running at the Z pole
- Extraordinary √s precision: 100 keV at the Z, 300 keV at WW threshold → exquisite control of beam uncertainties (average, width, systematics)
- Aiming for up to 20-100 times better precision than LEP/SLD on most electroweak precision observables (EWPO)
- **Current challenges: reduce uncertainties, establish theory / detector / machine requirements to reach the ultimate precision**

Physics potential of EWPO



- Probing the 10-TeV scale for universal new-physics effects with just a few years of FCC-ee EW running:

- Strong constraints on the S parameter ($O_{\phi WB}$, $O_W + O_B$ in Higgs compositeness, ...)
- and on the T parameter (violations of custodial symmetry)



This Lol: HF EW precision observables

Observable	present value \pm error	FCC-ee Stat.	FCC-ee Syst.	Comment and leading exp. error
$A_{\text{FB}}^b, 0 (\times 10^4)$	992 ± 16	0.02	1-3	b-quark asymmetry at Z pole from jet charge
$A_{\text{FB}}^{\text{pol}, \tau} (\times 10^4)$	1498 ± 49	0.15	< 2	τ polarization asymmetry τ decay physics
$R_b (\times 10^6)$	216290 ± 660	0.3	< 60	ratio of bb to hadrons stat. extrapol. from SLD

- **Current projections: ≥ 20 times better than current precision**

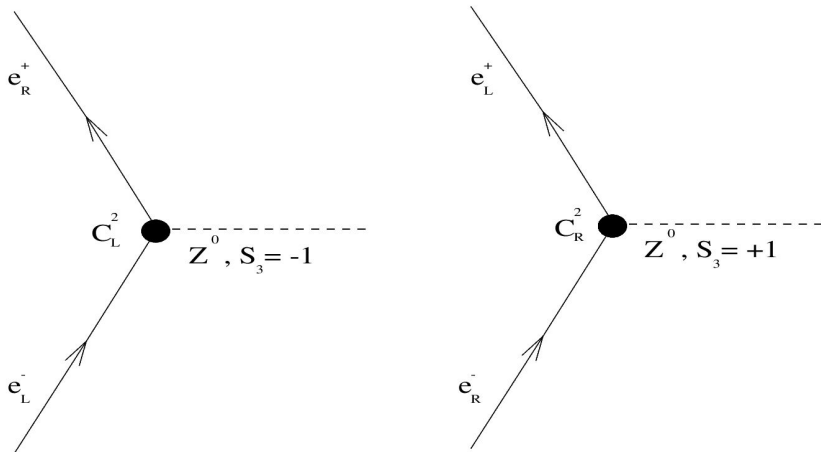
τ polarization, \mathcal{P}_τ

$\mathcal{P}_\tau \rightarrow$ access to $\frac{v_e}{a_e}, \frac{v_\tau}{a_\tau} :$

$$\frac{v_l}{a_l} = (1 - 4 \sin^2 \theta_l^{\text{eff}})$$

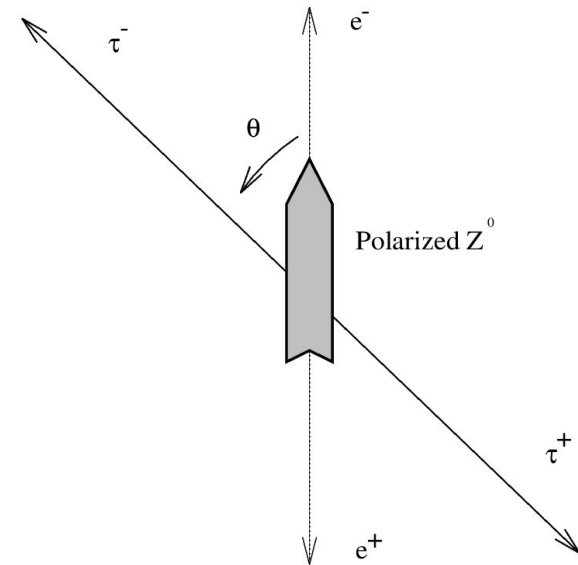
Tau polarization: A_τ , A_e

Z: naturally polarized



$$\mathcal{P}_{Z^0} = \frac{C_R^2 - C_L^2}{C_R^2 + C_L^2} = -\frac{2v_e a_e}{v_e^2 + a_e^2} \equiv -\mathcal{A}_e$$

τ decay: excellent polarimeter



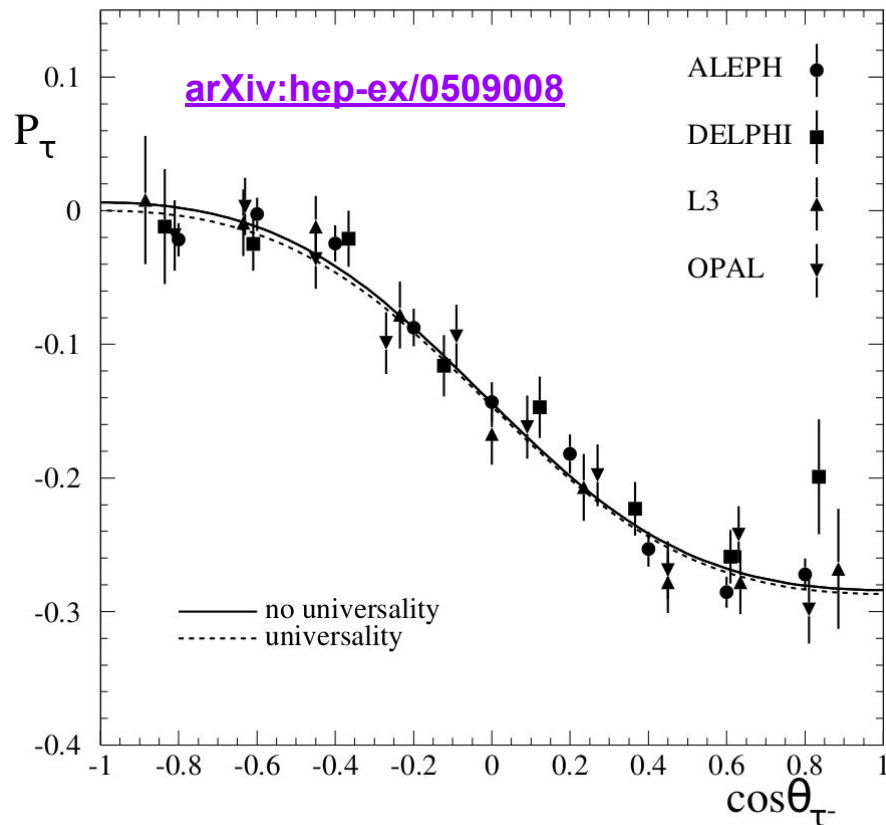
$$\mathcal{P}_\tau(\cos \theta) = -\frac{\mathcal{A}_\tau(1 + \cos^2 \theta) + 2\mathcal{A}_e \cos \theta}{(1 + \cos^2 \theta) + 2\mathcal{A}_e \mathcal{A}_\tau \cos \theta}$$

$$\langle \mathcal{P}_\tau \rangle = -\mathcal{A}_\tau$$

$$\mathcal{P}_\tau^{\text{FB}} = -\frac{3}{4} \mathcal{A}_e$$

Tau polarization: A_τ , A_e

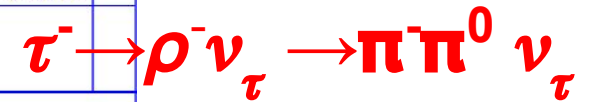
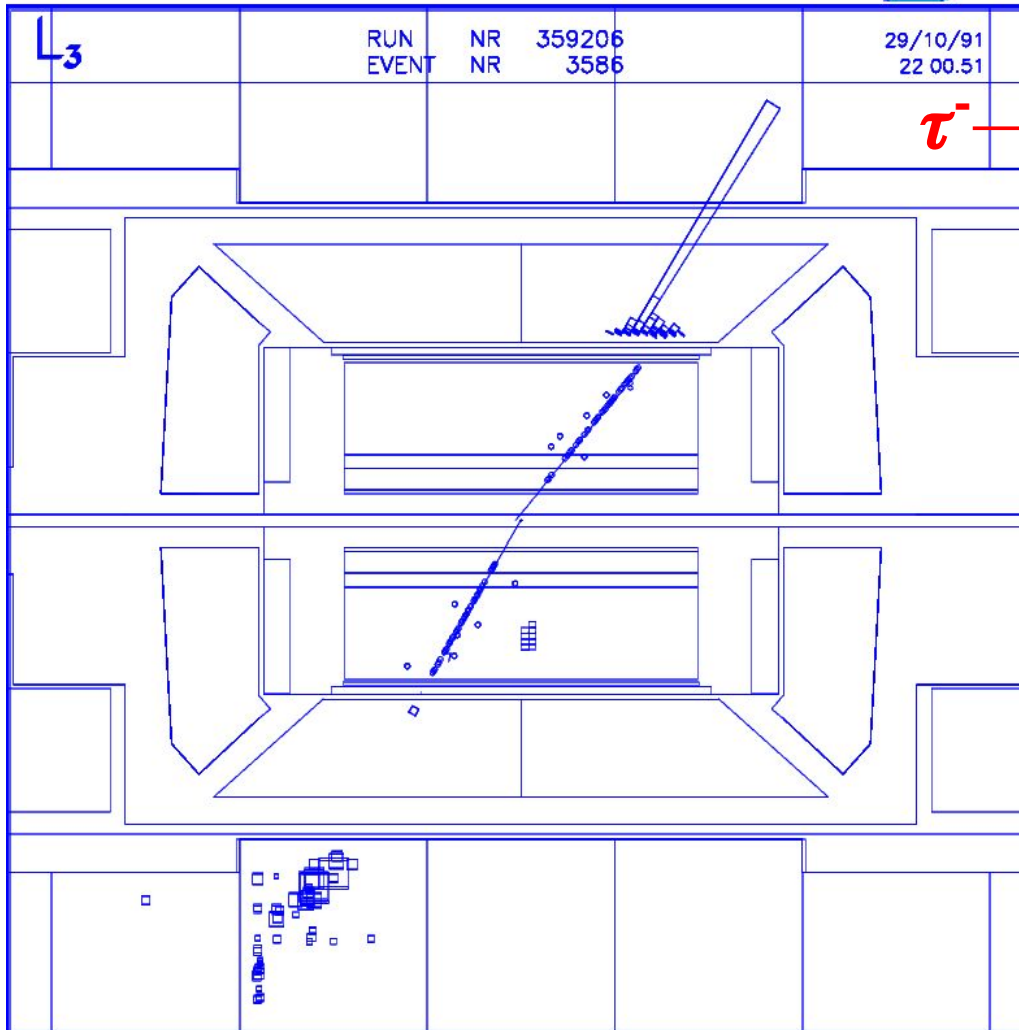
Measured P_τ vs $\cos\theta_\tau$



- **The FCC-ee baseline does not use longitudinal beam polarization:**
 - Although feasible, it would reduce too much the available luminosity
 - Not needed: tau polarization input is enough to facilitate precise measurements of the L-R asymmetry parameters for all fermions: $A_e, A_\mu, A_\tau, A_b, A_c$

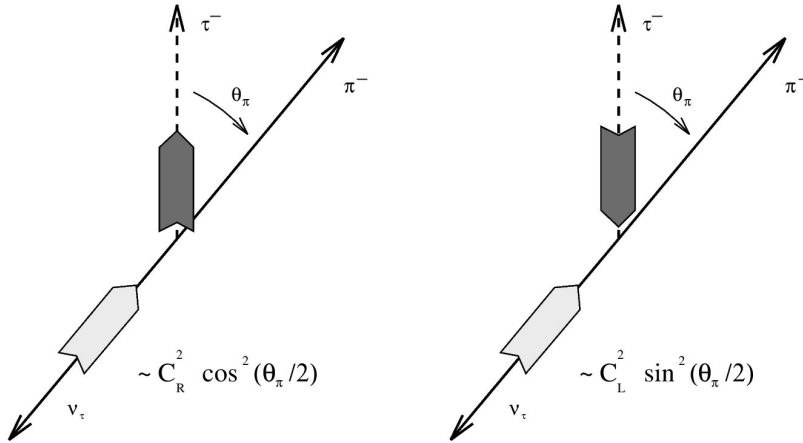
$$P(\cos\theta) = \frac{\mathcal{A}_\tau(1 + \cos^2\theta) + 2\mathcal{A}_e \cos\theta}{(1 + \cos^2\theta) + 2\mathcal{A}_e \mathcal{A}_\tau \cos\theta}$$

Most sensitive channels



Most sensitive channels

Pseudo-scalar: $\tau^- \rightarrow \pi^- \nu_\tau$
(π, K 1-prong decays $\approx 13\%$)

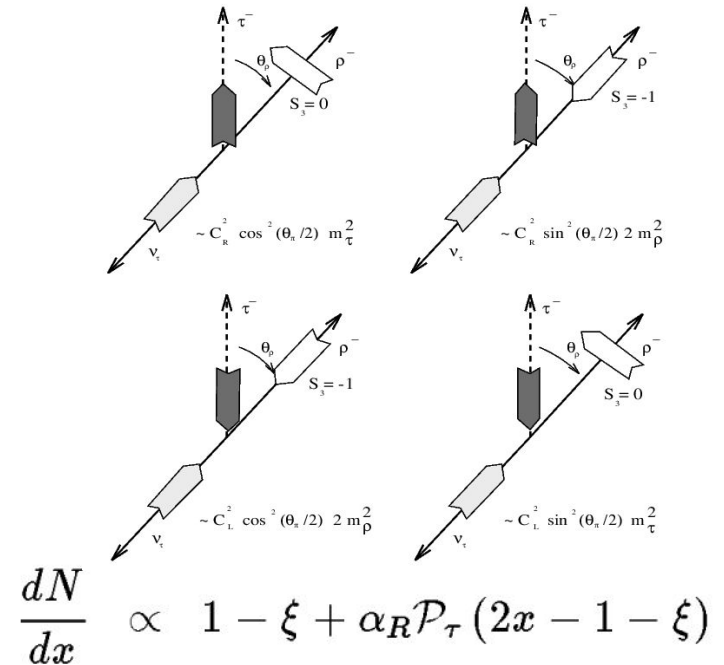


More $\cos\theta_\pi \Rightarrow$ more E_π^{LAB}

$$\frac{dN}{dx} \propto 1 - \xi + \mathcal{P}_\tau (2x - 1 - \xi)$$

$$\left(x = E_\pi^{\text{LAB}}/E_B, \xi = m_\pi^2 / (2m_\tau^2) \right)$$

Vector: $\tau^- \rightarrow \rho^- \nu_\tau \rightarrow \pi^- \pi^0 \nu_\tau$
(ρ, K^* 1-prong decays $\approx 25\%$)



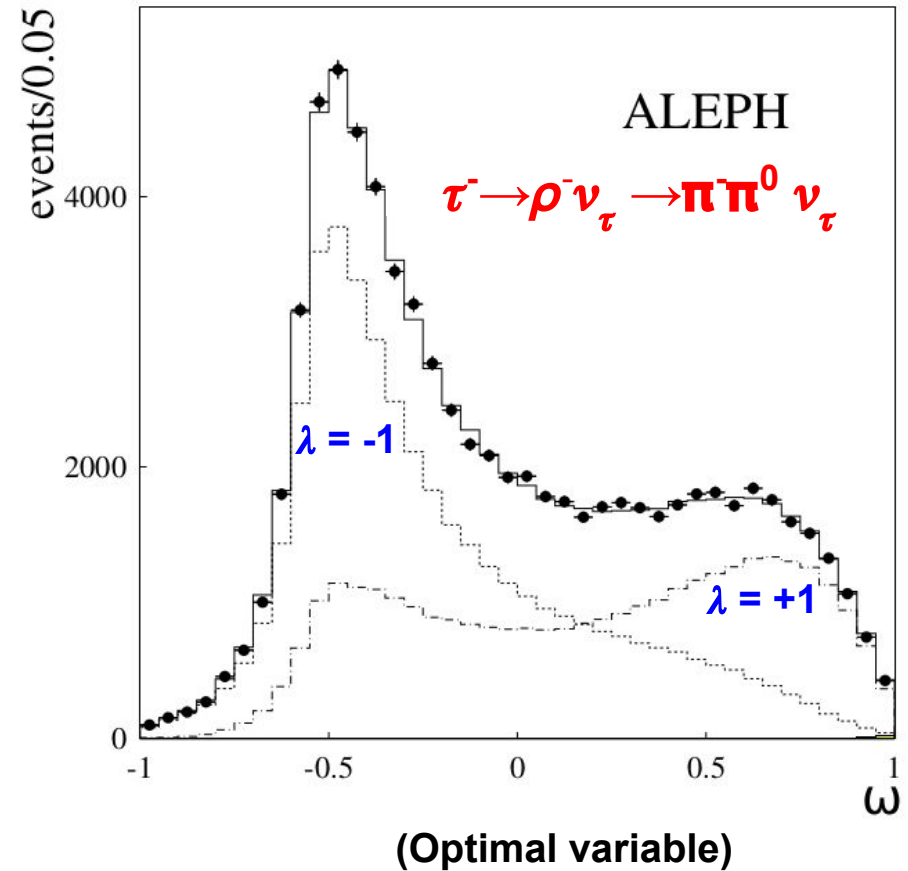
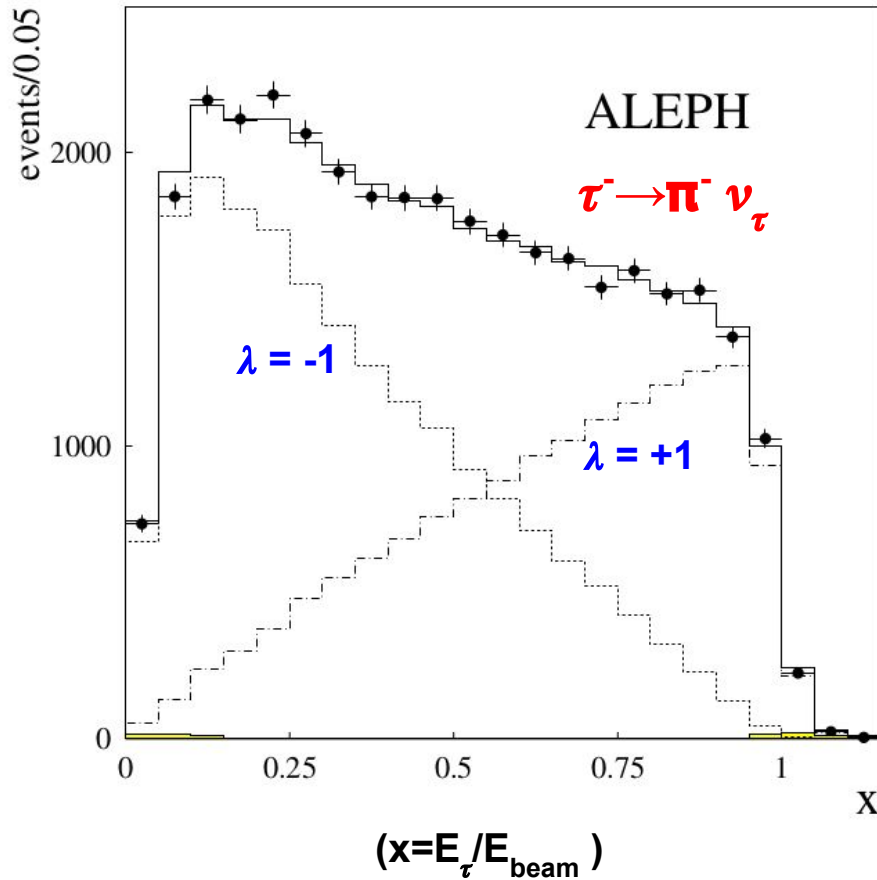
$$\left(\alpha_R = (m_\tau^2 - 2m_\rho^2) / (m_\tau^2 + 2m_\rho^2) \right)$$

Loss of sensitivity due to dilution almost recovered using just 1 optimal variable ω :

$\hat{\xi} \equiv$ phase space variables \rightarrow

$$\frac{1}{N} \frac{dN}{d\hat{\xi}} = f(\hat{\xi}) (1 + \mathcal{P} \omega)$$

Analysis at LEP



- **Cross-talk between τ decay channels and the precise understanding of the helicity shape are main items to study to reduce systematics:**
 - $\approx 11\%$ τ background from other decay channels in these plots
 - the tiny yellow shaded area is the non- τ background

A_τ to do: optimize channel separation

Table 2: Summary of the systematic uncertainties (%) on A_τ and A_e in the single- τ analysis.

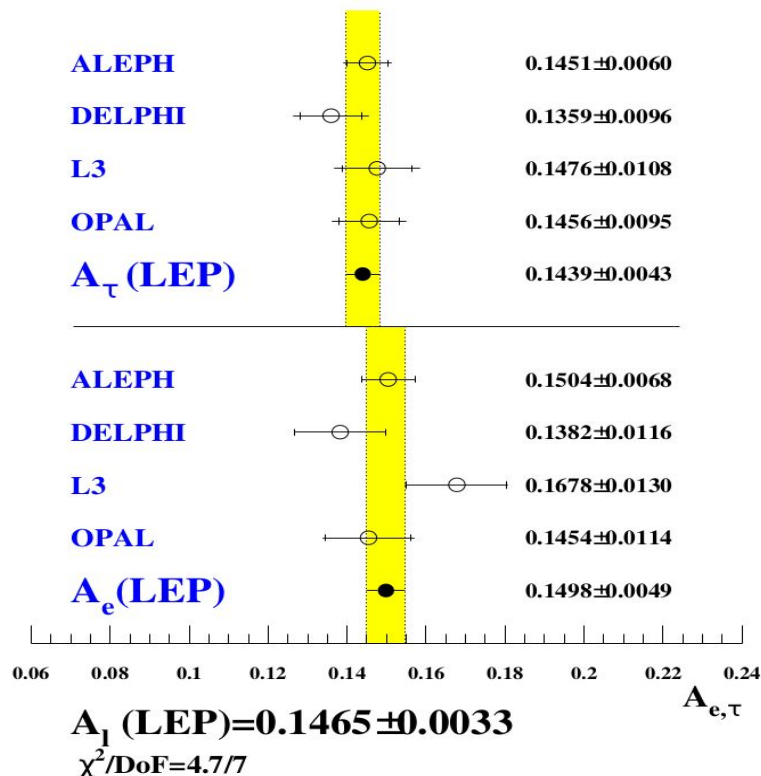
Source	A_τ							Incl. h
	h	ρ	$3h$	$h2\pi^0$	e	μ		
selection	-	0.01	-	-	0.14	0.02	0.08	
tracking	0.06	-	0.22	-	-	0.10	-	
ECAL scale	0.15	0.11	0.21	1.10	0.47	-	-	
PID	0.15	0.06	0.04	0.01	0.07	0.07	0.18	
misid.	0.05	-	-	-	0.08	0.03	0.05	
photon	0.22	0.24	0.37	0.22	-	-	-	
non- τ back.	0.19	0.08	0.05	0.18	0.54	0.67	0.15	
τ BR	0.09	0.04	0.10	0.26	0.03	0.03	0.78	
modelling	-	-	0.70	0.70	-	-	0.09	
MC stat	0.30	0.26	0.49	0.63	0.61	0.63	0.26	
TOTAL	0.49	0.38	1.00	1.52	0.96	0.93	0.87	

ALEPH

- **ALEPH was the best detector for this: large tracking volume for separation, large magnetic field for bending, high granularity for $\pi^0 \rightarrow \gamma\gamma$ identification**
- **Photon separation / π^0 identification was still the dominant systematics**

A_e is slightly different...

Experiment	A_τ	A_e
ALEPH	$0.1451 \pm 0.0052 \pm 0.0029$	$0.1504 \pm 0.0068 \pm 0.0008$
DELPHI	$0.1359 \pm 0.0079 \pm 0.0055$	$0.1382 \pm 0.0116 \pm 0.0005$
L3	$0.1476 \pm 0.0088 \pm 0.0062$	$0.1678 \pm 0.0127 \pm 0.0030$
OPAL	$0.1456 \pm 0.0076 \pm 0.0057$	$0.1454 \pm 0.0108 \pm 0.0036$
LEP	$0.1439 \pm 0.0035 \pm 0.0026$	$0.1498 \pm 0.0048 \pm 0.0009$



- Note that A_e ($\equiv -P_\tau^{\text{FB}}$) is much less affected by systematic uncertainties, because forward-backward asymmetry measurements are largely independent of (charge symmetric) acceptance uncertainties

$A_{FB}(Q), Q=b,c$

Assuming $\frac{v_e}{a_e}$ precisely known :

$$\mathcal{A}_{FB}(b) \rightarrow \frac{v_b}{a_b} = \left(1 - \frac{4}{3} \sin^2 \theta_b^{\text{eff}}\right)$$

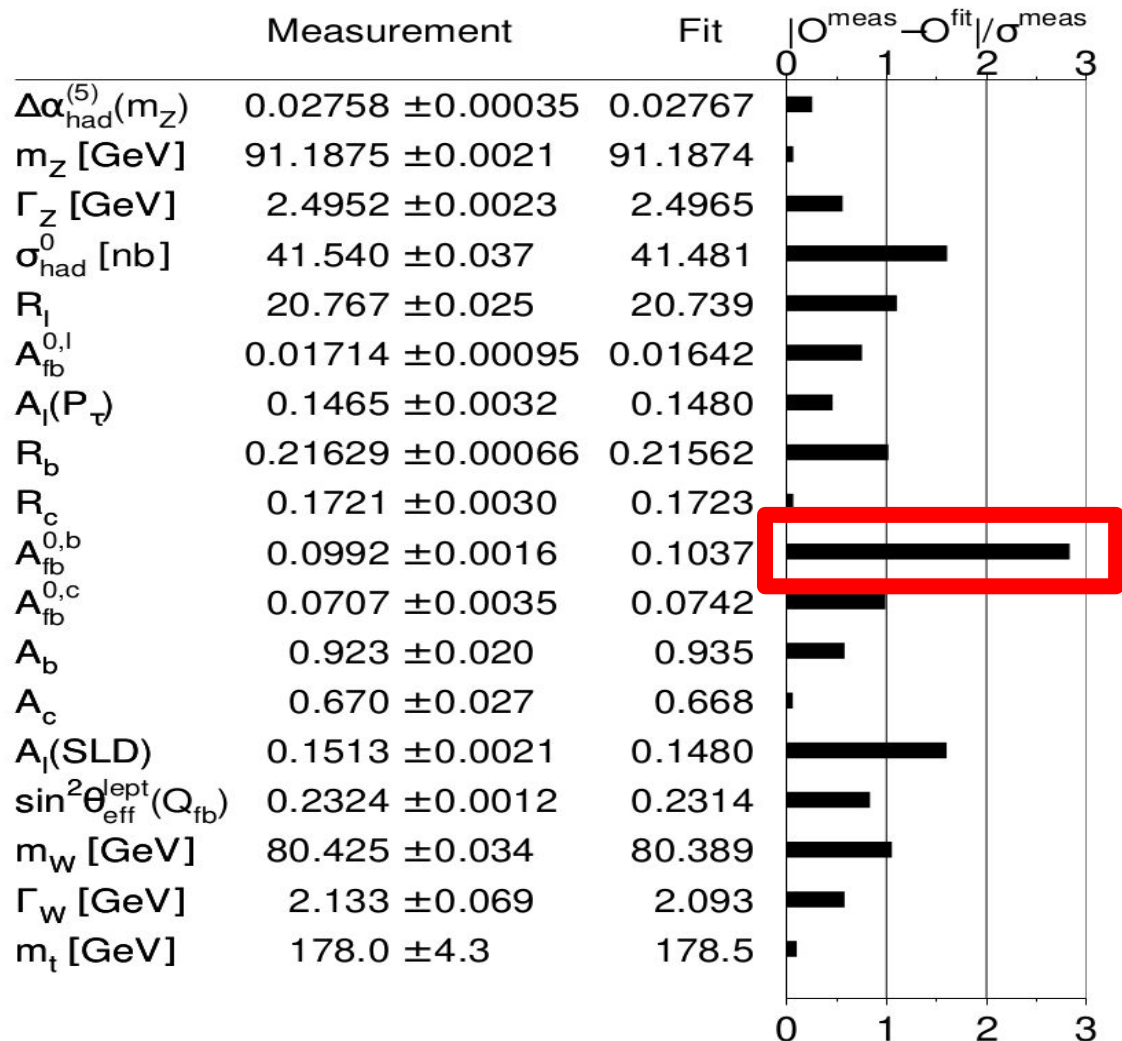
$$\mathcal{A}_{FB}(c) \rightarrow \frac{v_c}{a_c} = \left(1 - \frac{8}{3} \sin^2 \theta_c^{\text{eff}}\right)$$

Present status of $A_{FB}(Q)$

- Electroweak measurement presenting the largest deviations in the global SM fit ([final LEPWWG paper \(2005\)](#))

$$A_{FB}(Q) = \frac{\sigma_F^Q - \sigma_B^Q}{\sigma_F^Q + \sigma_B^Q}$$

- New physics explanations require a substantial modification of Zbb right-hand couplings ([arxiv:0610173](#))



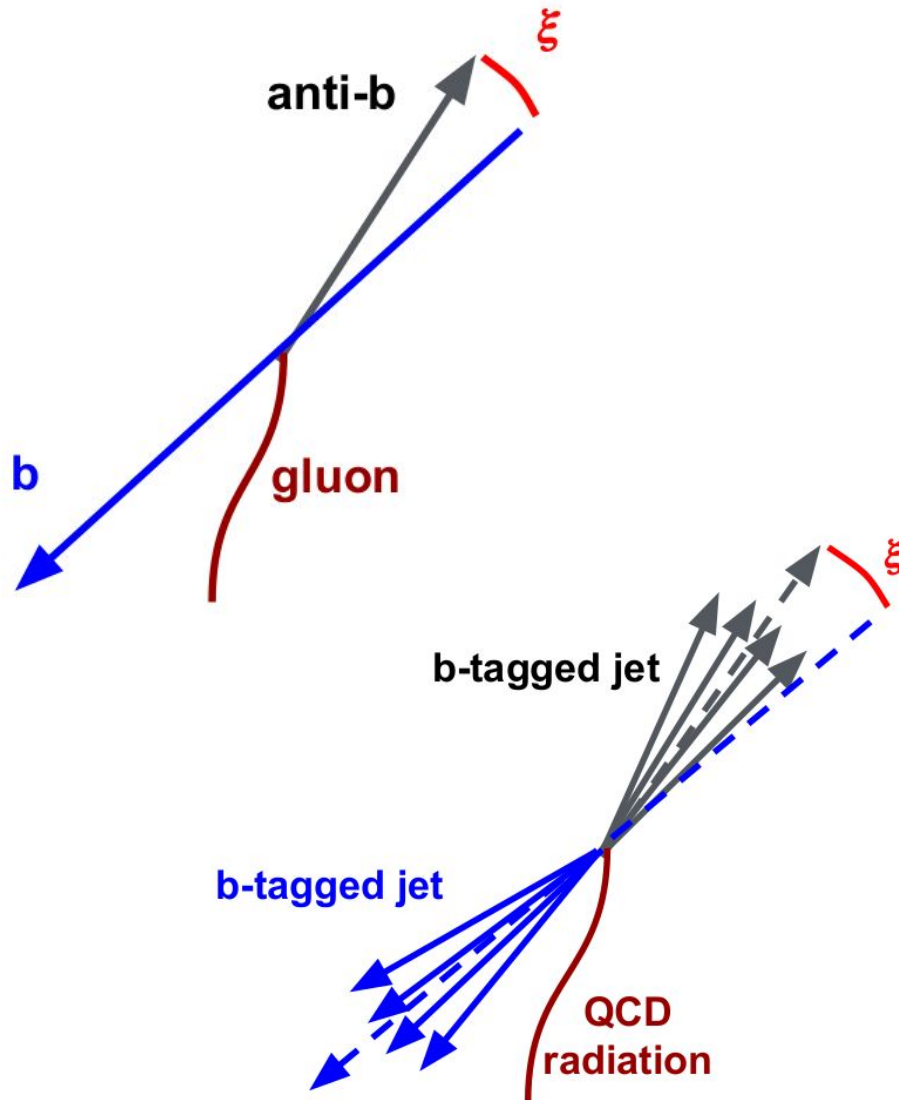
Present status of $A_{FB}(Q)$

- QCD corrections are the dominant source of correlated systematics between measurements
- Measurement ([LEPEWWG reference](#)):
 0.0992
 ± 0.0015 (stat.)
 ± 0.0007 (syst.)
- 1/2 syst. uncertainty using today's knowledge ([arXiv:2011.00530](#))
- Aiming for a $\approx \pm 0.0001$ precision measurement at FCC-ee: one order of magnitude improvement !!**

Source	R_b^0 [10^{-3}]	R_c^0 [10^{-3}]	$A_{FB}^{0,b}$ [10^{-3}]	$A_{FB}^{0,c}$ [10^{-3}]	\mathcal{A}_b [10^{-2}]	\mathcal{A}_c [10^{-2}]
statistics	0.44	2.4	1.5	3.0	1.5	2.2
internal systematics	0.28	1.2	0.6	1.4	1.2	1.5
QCD effects	0.18	0	0.4	0.1	0.3	0.2
<i>B</i> (<i>D</i> → neut.)	0.14	0.3	0	0	0	0
<i>D</i> decay multiplicity	0.13	0.6	0	0.2	0	0
<i>B</i> decay multiplicity	0.11	0.1	0	0.2	0	0
<i>B</i> (<i>D</i> ⁺ → <i>K</i> ⁻ <i>π</i> ⁺ <i>π</i> ⁺)	0.09	0.2	0	0.1	0	0
<i>B</i> (<i>D</i> _s → <i>φπ</i> ⁺)	0.02	0.5	0	0.1	0	0
<i>B</i> (<i>Λ</i> _c → <i>p K</i> ⁻ <i>π</i> ⁺)	0.05	0.5	0	0.1	0	0
<i>D</i> lifetimes	0.07	0.6	0	0.2	0	0
<i>B</i> decays	0	0	0.1	0.4	0	0.1
decay models	0	0.1	0.1	0.5	0.1	0.1
non incl. mixing	0	0.1	0.1	0.4	0	0
gluon splitting	0.23	0.9	0.1	0.2	0.1	0.1
<i>c</i> fragmentation	0.11	0.3	0.1	0.1	0.1	0.1
light quarks	0.07	0.1	0	0	0	0
beam polarisation	0	0	0	0	0.5	0.3
total correlated	0.42	1.5	0.4	0.9	0.6	0.4
total error	0.66	3.0	1.6	3.5	2.0	2.7

$A_{FB}(b/c)$

[arXiv:2010.08604](https://arxiv.org/abs/2010.08604)




- New developments for $A_{FB}(b/c)$: QCD corrections and uncertainties can be reduced significantly using acollinearity (ξ) cuts \Rightarrow not a limiting factor anymore to reach the $\lesssim 0.1\%$ precision level
- Further improvements expected from better heavy flavor tagging capabilities and a more accurate measurement of the heavy quark flight direction
- **Performing a realistic measurement with more sophisticated b/c tagging techniques \rightarrow define detector requirements**
- Note that all these measurements can be done with exclusive decays. Certainly for the charm case. For instance, a Tera-Z facility will provide $\approx 10^8$ B^+ exclusive decays

Reduction of QCD uncertainties

- Detailed table of central values and uncertainties:

**stat. unc. for 7×10^7
 $Z \rightarrow b\bar{b}$ events**



ξ_0 cut	Measured A_{FB}	$\Delta A_{FB}(\text{stat})$	$\Delta A_{FB}(\text{tune})$	$\Delta A_{FB}(\text{theo. QCD corr})$
No cut	0.0998 ± 0.0004	0.00008	0.00014	0.00033
1.50	0.1003 ± 0.0003	0.00011	0.00014	0.00023
1.00	0.1011 ± 0.0002	0.00011	0.00010	0.00016
0.50	0.1023 ± 0.0002	0.00011	0.00010	0.00007
0.30	0.1030 ± 0.0002	0.00011	0.00010	0.00003
0.20	0.1033 ± 0.0001	0.00011	0.00005	0.00002
0.10	0.1035 ± 0.0002	0.00016	0.00005	0.00001

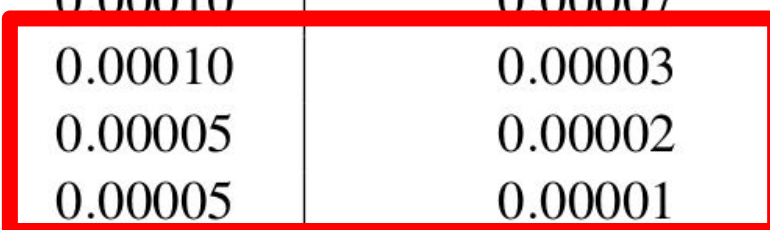


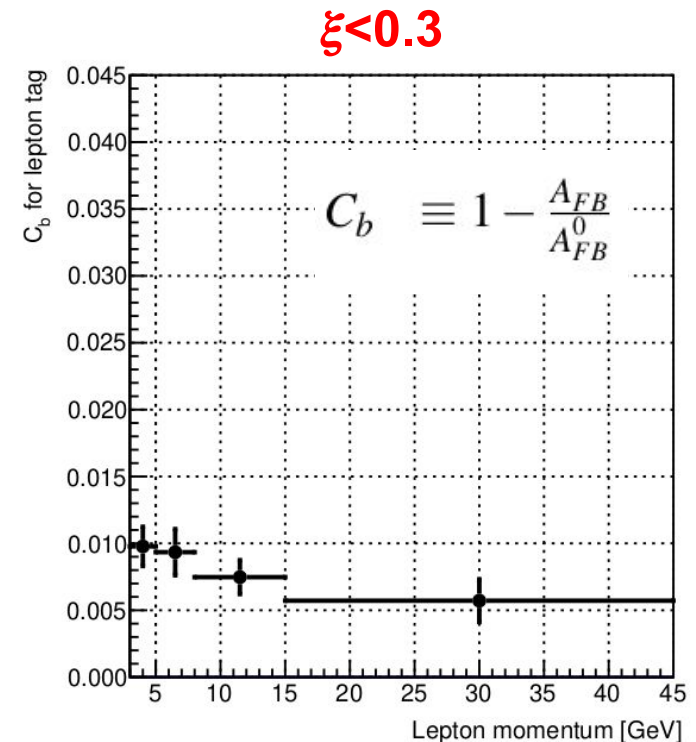
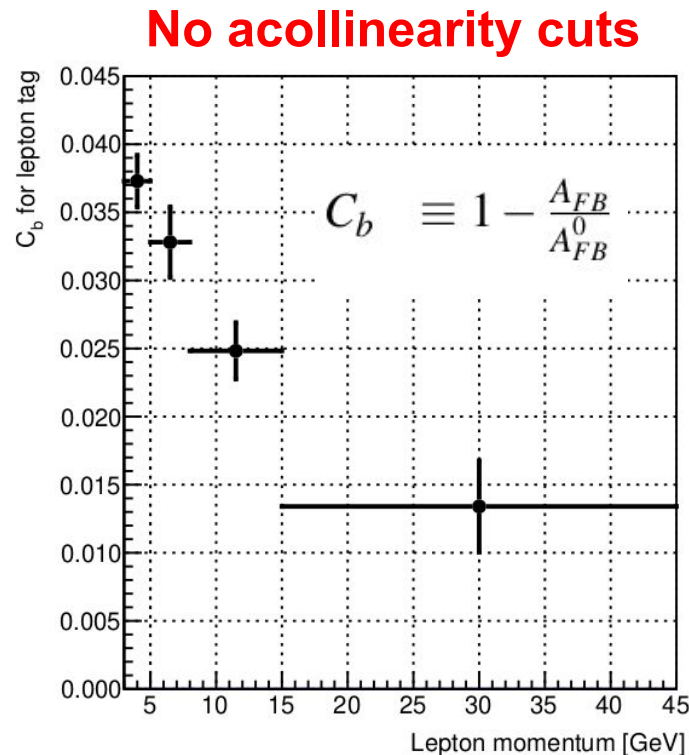
Table 9: Central values and components of the uncertainty in the measurement of the A_{FB} asymmetry with $7 \times 10^7 e^+e^- \rightarrow b\bar{b}(g)$ events at the Z pole, for different $\xi < \xi_0$ cuts at the reconstructed level.

**$\lesssim 0.1\%$ relative systematic
uncertainties for $\xi \lesssim 0.3$**



... also in semi-leptonic decays

- Evaluating the QCD corrections as a function of the momentum in semi-leptonic b decays, now with acollinearity cuts (generator level):



- Significant reduction (note: $p_l > 3$ GeV cut in preselection)
- Full realistic analysis still to be done

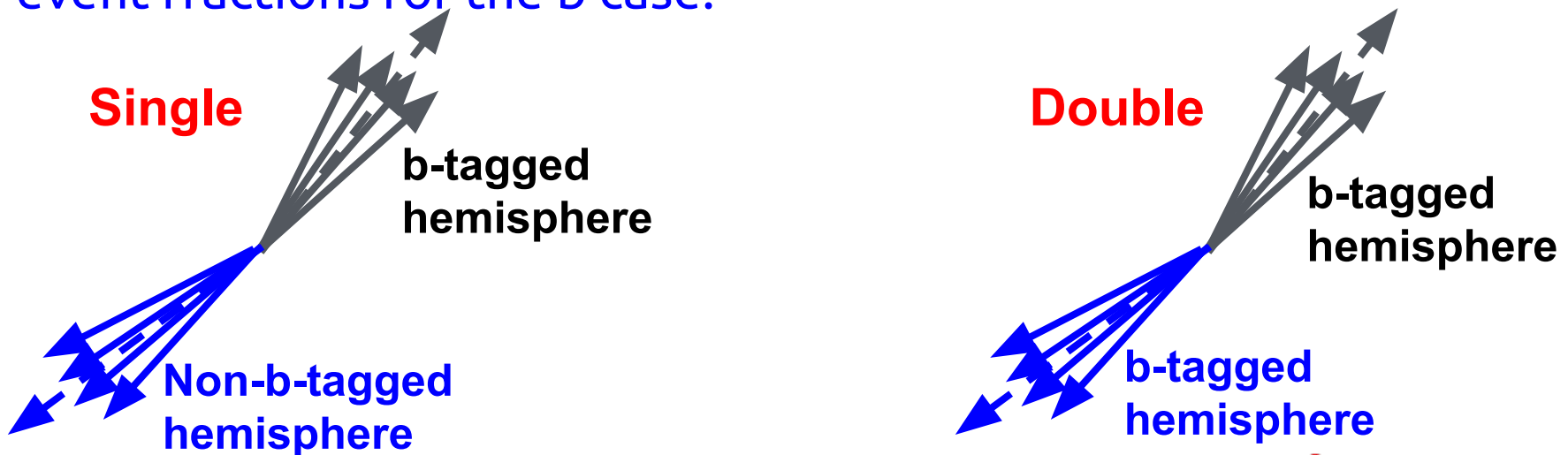
R_b, R_c

$$R_b = \frac{\Gamma_{b\bar{b}}}{\Gamma_{had}}, \quad R_c = \frac{\Gamma_{c\bar{c}}}{\Gamma_{had}}$$

R_b, R_c

$$R_b = \frac{\Gamma_{b\bar{b}}}{\Gamma_{had}}, \quad R_c = \frac{\Gamma_{c\bar{c}}}{\Gamma_{had}}$$

- Measured at LEP/SLC very precisely using single and double-tag event fractions for the b case:



No Bckgd, no hemisphere correlations $\Rightarrow R_b = \frac{f_{single}^2}{f_{double}}$

$$f_{single} = R_b \epsilon_b + R_c \epsilon_c + (1 - R_b - R_c) \epsilon_{uds}$$

Real life:

$$f_{double} = c_b R_b \epsilon_b^2 + c_c R_c \epsilon_c^2 + c_{uds} (1 - R_b - R_c) \epsilon_{uds}^2$$

$$c_b = c_c = c_{uds} = 1 \text{ if no hemisphere correlations}$$

Present status of R_b , R_c

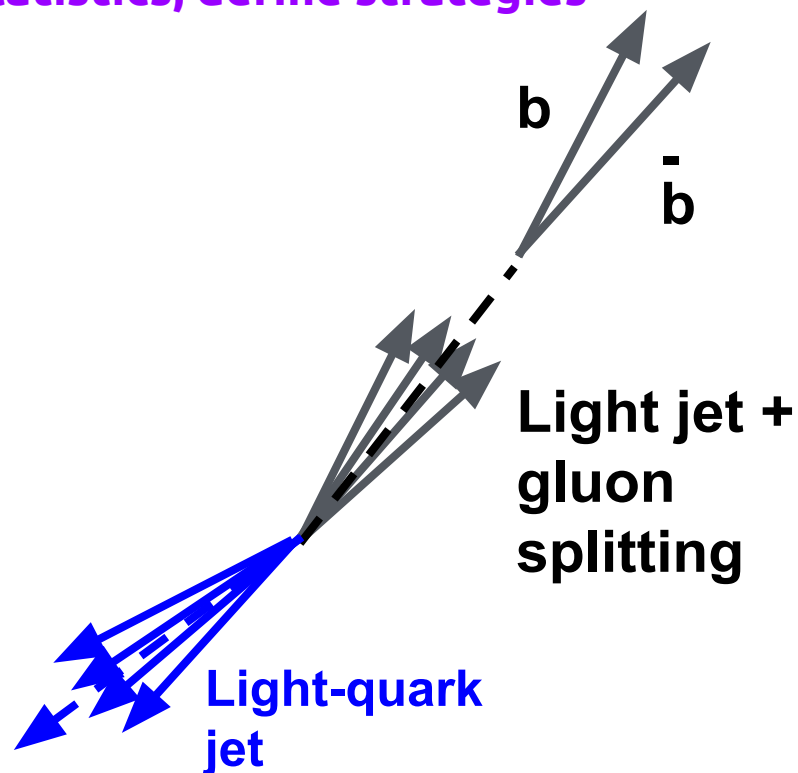
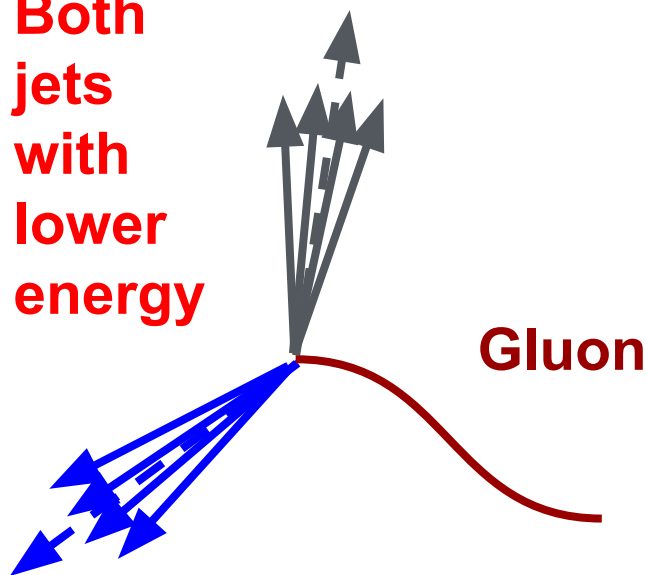
- Hemisphere correlation effects (QCD) and gluon splitting are large sources of correlated uncertainty among experiments
- LEPEWWG result:
 $R_b = 0.21629 \pm 0.00066$
- Aiming for a $\lesssim 3 \times 10^{-4}$ precision measurement on R_b at FCC-ee: one order of magnitude improvement
- R_c to be re-studied for a Tera-Z factory via exclusive / inclusive single+double-tag methods (SLD way, not LEP main way)

Source	R_b^0 [10^{-3}]	R_c^0 [10^{-3}]	$A_{\text{FB}}^{0,b}$ [10^{-3}]	$A_{\text{FB}}^{0,c}$ [10^{-3}]	\mathcal{A}_b [10^{-2}]	\mathcal{A}_c [10^{-2}]
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QCD effects	0.18	0	0.4	0.1	0.3	0.2
$B(D \rightarrow \text{neut.})$	0.14	0.3	0	0	0	0
D decay multiplicity	0.13	0.6	0	0.2	0	0
B decay multiplicity	0.11	0.1	0	0.2	0	0
$B(D^+ \rightarrow K^- \pi^+ \pi^+)$	0.09	0.2	0	0.1	0	0
$B(D_s \rightarrow \phi \pi^+)$	0.02	0.5	0	0.1	0	0
$B(\Lambda_c \rightarrow p K^- \pi^+)$	0.05	0.5	0	0.1	0	0
D lifetimes	0.07	0.6	0	0.2	0	0
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total error	0.66	3.0	1.6	3.5	2.0	2.7

R_b, R_c

- Important elements of the study:
 - Improvement of the b (and c) purity → better detectors
 - Reduction of hemisphere correlations and syst. uncertainties:
 - Common vertex correlations (smaller in future detectors)
 - QCD effects (reduction with acollinearity cuts like in $A_{FB}(Q)$?)
 - Gluon splitting → huge available statistics, define strategies

Both jets with lower energy



Summary/Outlook

- A few years of Tera-Z running should provide EWPO measurements in the heavy flavor sector with $\gtrsim 20$ times the current precision, thus giving early access to 3rd generation universal and flavor-dependent new physics effects at the ≈ 10 TeV scale:
 - $P_\tau, A_{FB}(b/c), R_b, R_c$
- Systematics will be the limiting factor in all these measurements \Rightarrow more detailed studies needed to estimate the ultimate precision. Reducing associated uncertainties via:
 - theory developments
 - new analysis strategies
 - optimized detector design
- Significant amount of work still to be done...