

# Straightness evaluation for the 206-m-long part of the KEK electron/positron linac using inclinometers

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# Target

Evaluate aligning straightness of linear particle accelerators (Linacs) for distance of **several 100 m** with accuracy of **better than 1 mm**

## Contents

### 1. Introduction

- Straightness evaluation using an inclinometer

### 2. Demonstration

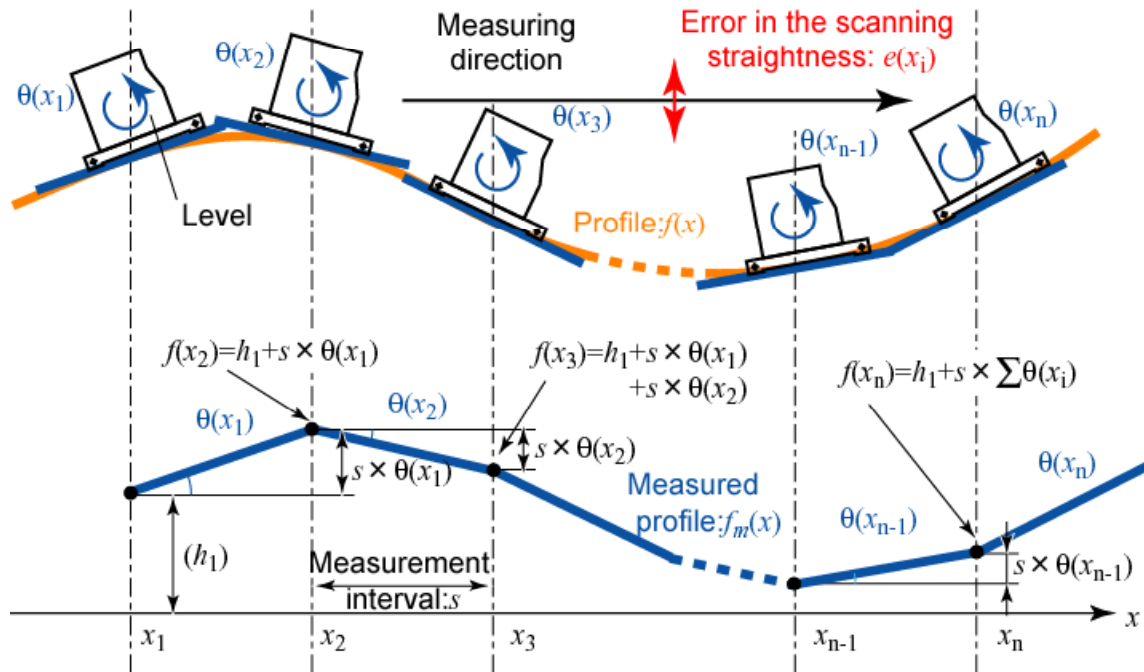
- 71-m-long (single accelerator sector) straightness evaluation with a straight bar
- 206-m-long (multi accelerator sectors) straightness evaluation with a straight bar and offset bars

### 3. Conclusion

# Straightness evaluation using an inclinometer

Not affected by transferring locus (= error in the scanning straightness)

⇒ Advantageous for long distance evaluation



Straightness:

$$f(x_n) = h_1 + s \times \sum_{i=1}^{n-1} \theta(x_i)$$

$h_1$ : Arbitrary straightness of the start point,

$s_i$ : Sampling interval, ( $s_i = s$ )

$\theta(x_i)$ : Measured tangential angle,

$n$ : Number of measurements

Error propagated to the straightness: 
$$\sigma_f = \sqrt{\sigma_s^2 \cdot \sum_{i=1}^n \{\theta(x_i)\}^2 + \sigma_\theta^2 \cdot \sum_{i=1}^n s_i^2}$$

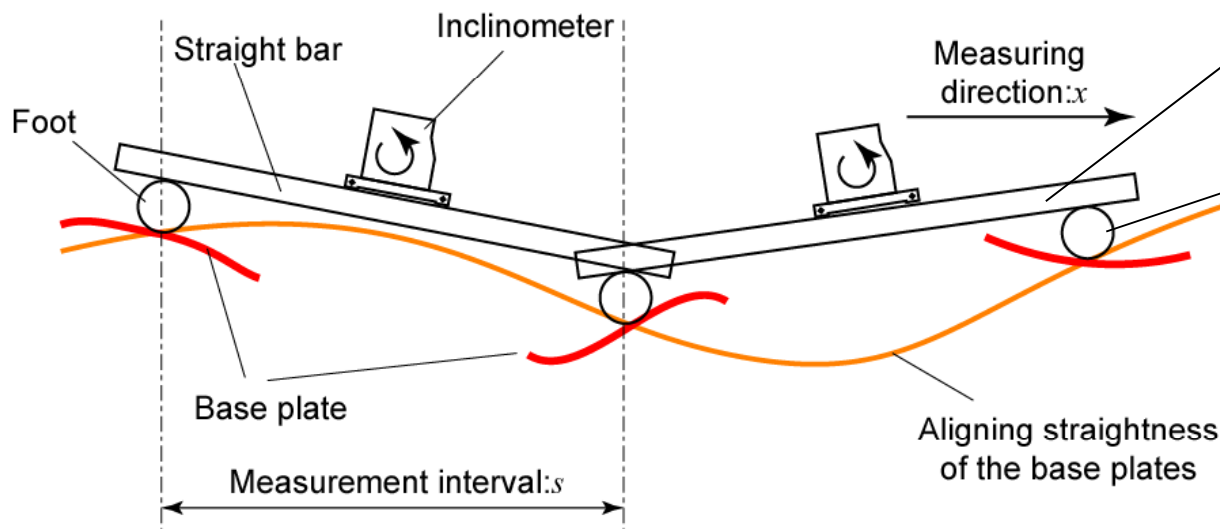
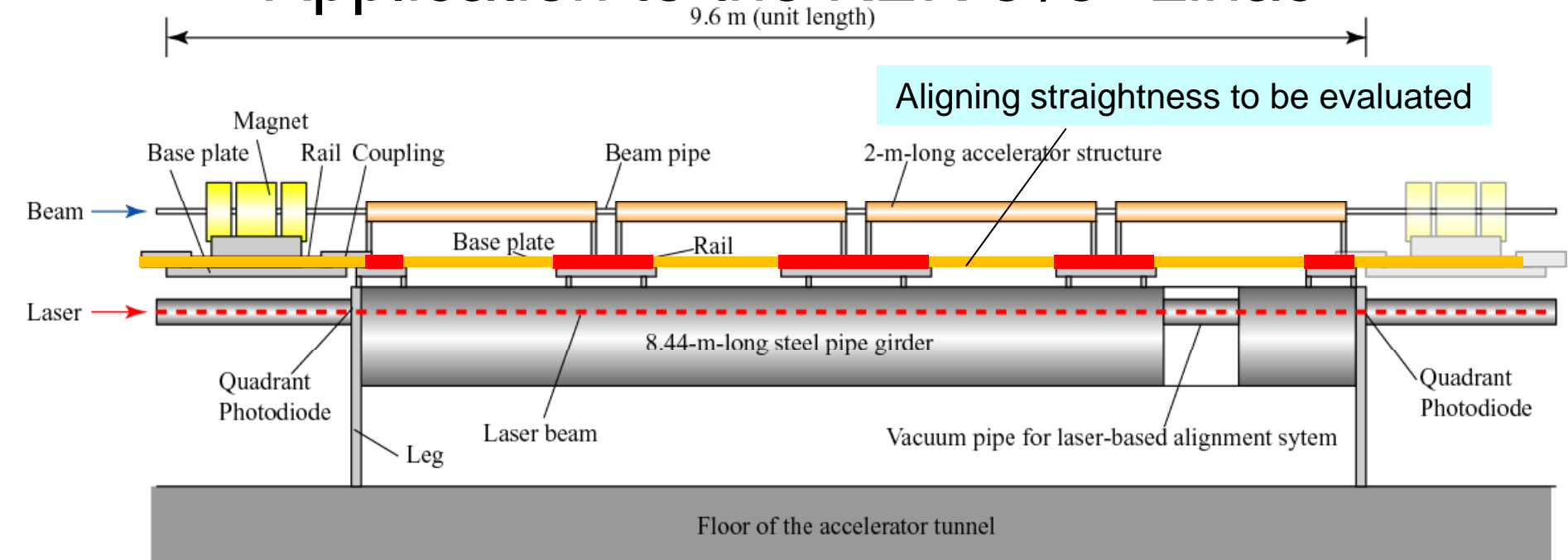
$\sigma_s$ : Error in the sampling interval:  $s_i$ ,

$\sigma_\theta$ : Error in the measured tangential angle,

$l$ : Measurement distance, ( $l = s \times n$ )

$$\approx \sqrt{s \cdot l} \cdot \sigma_\theta \quad (\text{In case } \theta(x_i) \doteq 0 \\ \Rightarrow \text{quasi-straight object})$$

# Application to the KEK e-/e<sup>+</sup> Linac

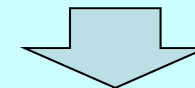


**Straight bar**

⇒ Ensures continuity of aligning straightness

**Contact foot**

⇒ Reduces affect of plate shape and roughness



• Spatial low pass filter

• Reduce affects of **positioning error** in evaluation

# Gravity referenced precise electric inclinometer (Talyvel 4)



Angle detector

- Range:  $\pm 3$  mrad ( $\pm 600$  sec ),
- Resolution:  $0.5 \mu\text{rad}$  ( $0.1$  sec ),
- Accuracy:  $0.2 \text{ sec} \pm 3\%$ -definition

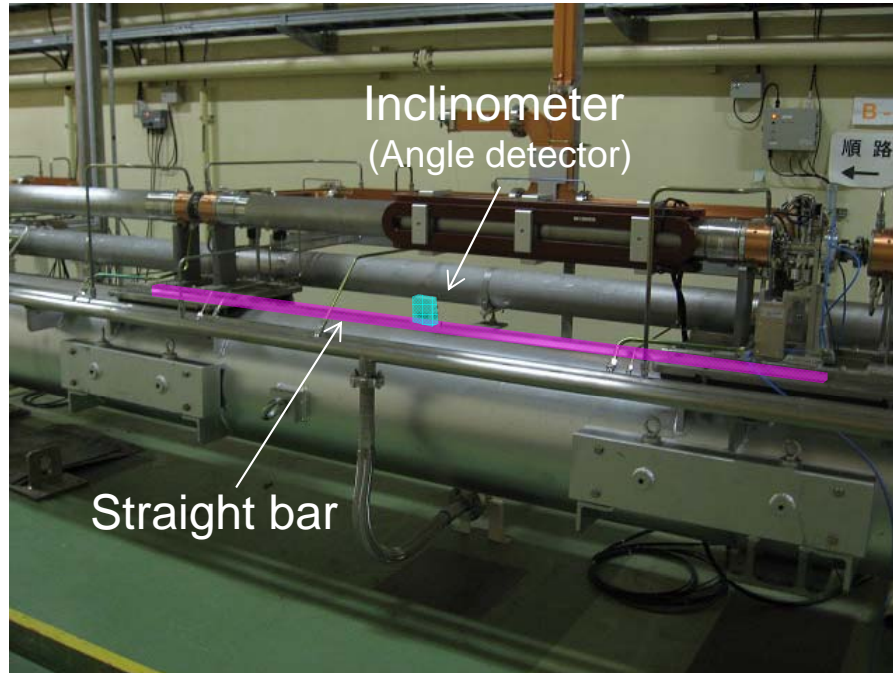


Controller

## 【 Acknowledgement 】

Authors thank Yukinori Kobayashi and members of the Accelerator Division 7 in Accelerator Laboratory in KEK and Masahiro Katoh of Institute of Molecular Science for providing us Talyvel 4.

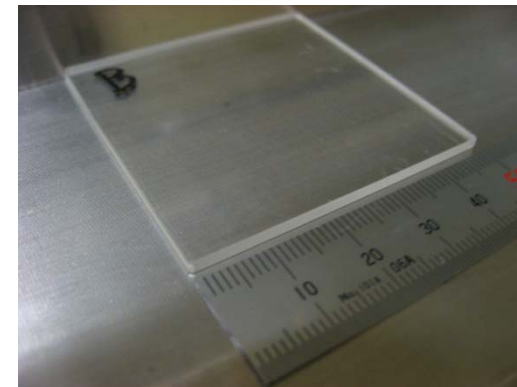
# Straightness evaluation for the KEK e-/e<sup>+</sup> Linac using an inclinometer and a straight bar



Straight bar made of 3-mm-thick Al rectangular pipe (1990~2306-mm-long, 50-mm-wide, and 25-mm-high)



Cross-section of the straight bar



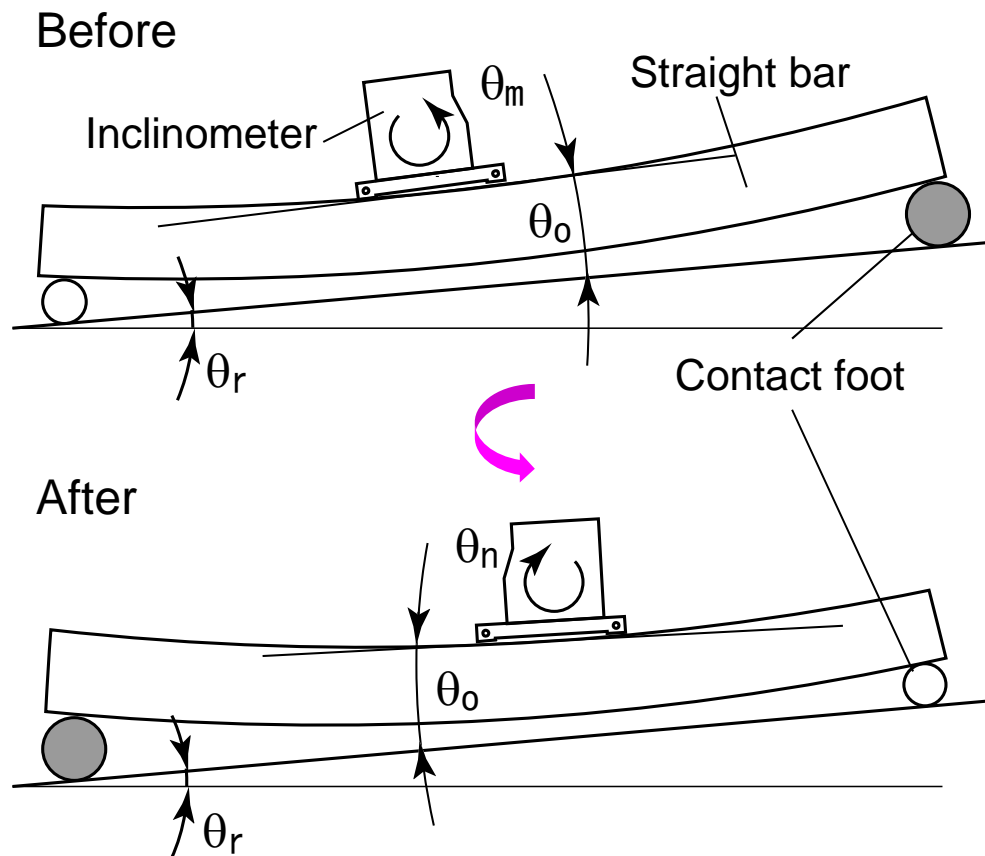
Foot made of 2-mm-thick glass plate  
(=optical parallel-  $\lambda = 633 \text{ nm}$ )  
with area of  $50 \times 50 \text{ mm}$



# Reversal measurement

Eliminate offset of the angle measurement system

(= Inclinator + Straight bar + Pair of contact feet)



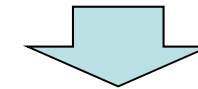
Offset of the system:  $\theta_o$  caused by

**Offset** of the inclinometer,

**Shape** error of the bar

(including the height difference between the pair of the contact feet),

**Deformation** of the bar



can be eliminated by

$$\theta_r = (\theta_m - \theta_n) / 2$$

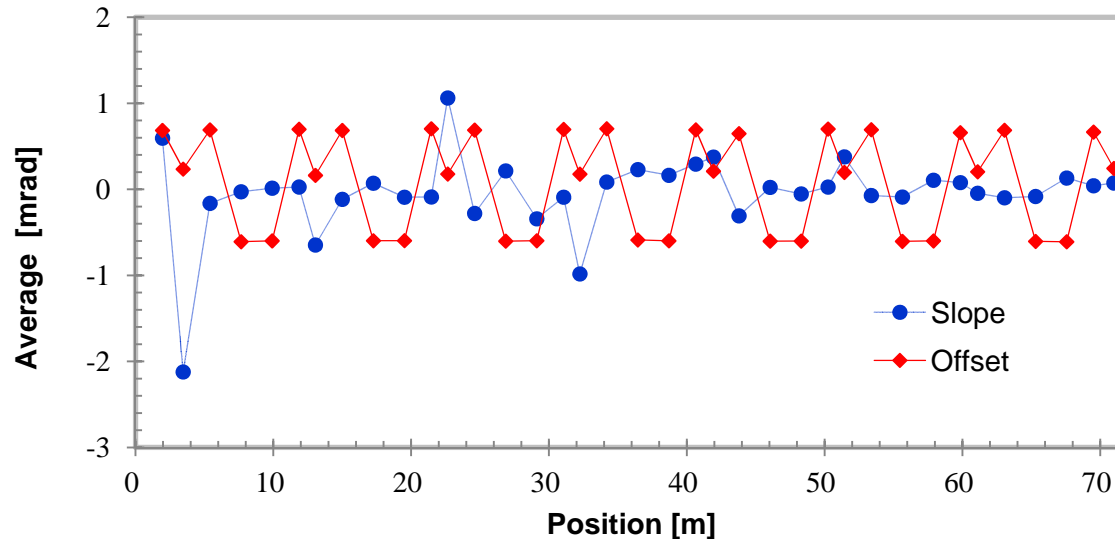
$\theta_r$  : Angle to be measured,

$\theta_o$  : Offset of the system,

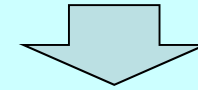
$\theta_m = \theta_r + \theta_o$  : Measurement before reverse,

$\theta_n = -\theta_r + \theta_o$  : Measurement after reverse

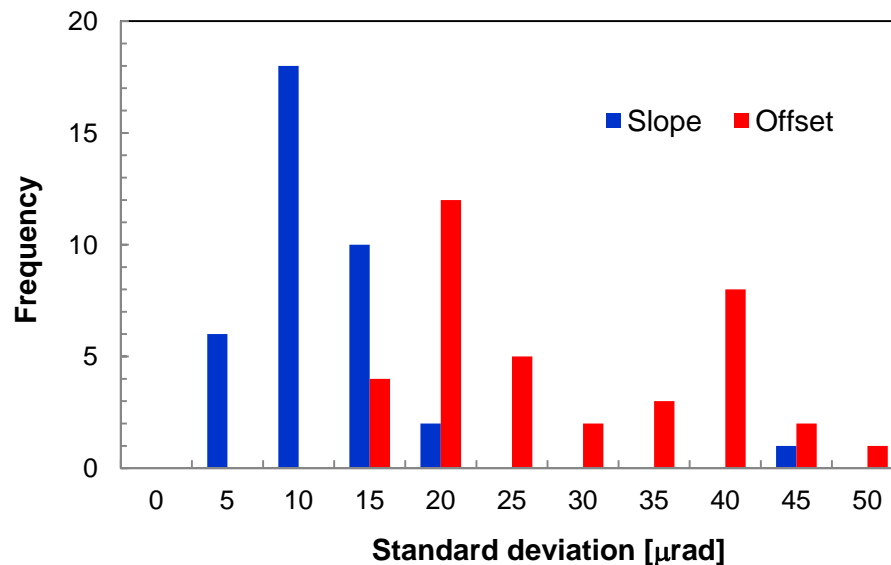
# Effect of the reversal measurements



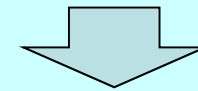
The offset angles:  $\theta_0$   
is comparable to  
the slope angles:  $\theta_r$ .



Offsets must be  
eliminated



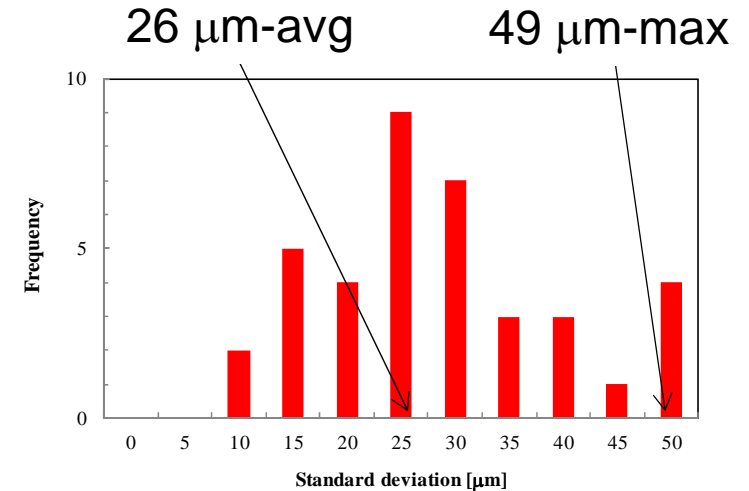
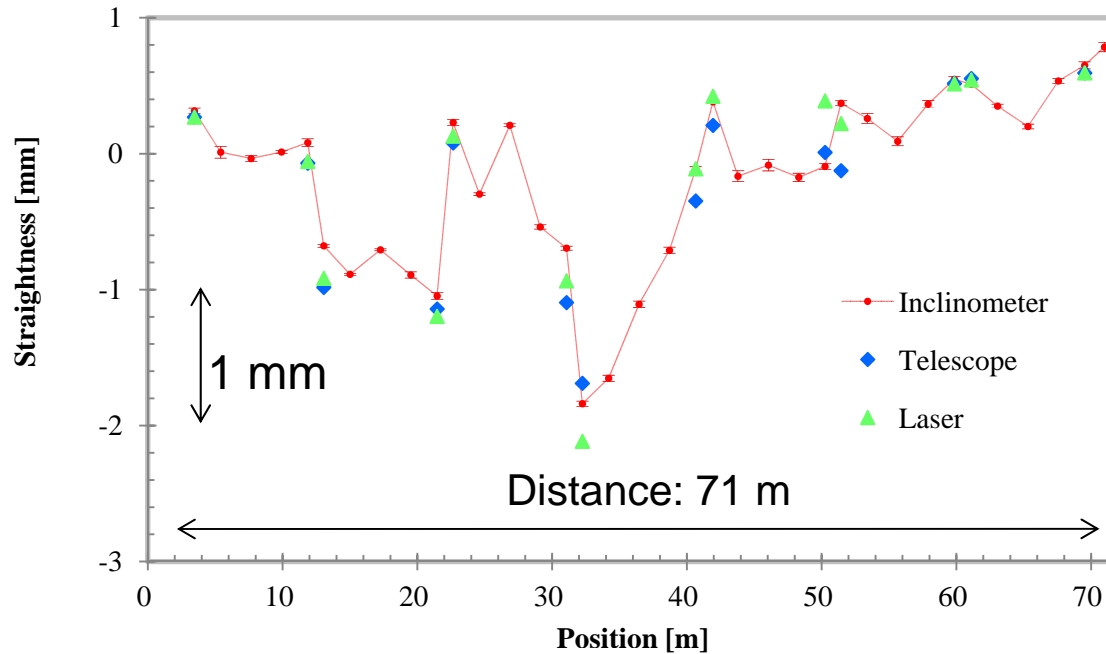
Standard deviations of the  
slope angles  
are smaller than those of the  
offset angles



Fluctuations of the  
offset angles ( $\Rightarrow$  drift)  
are also reduced.



# Evaluation results for the 71-m-long part of the sector C



Histogram of the standard deviations for each position

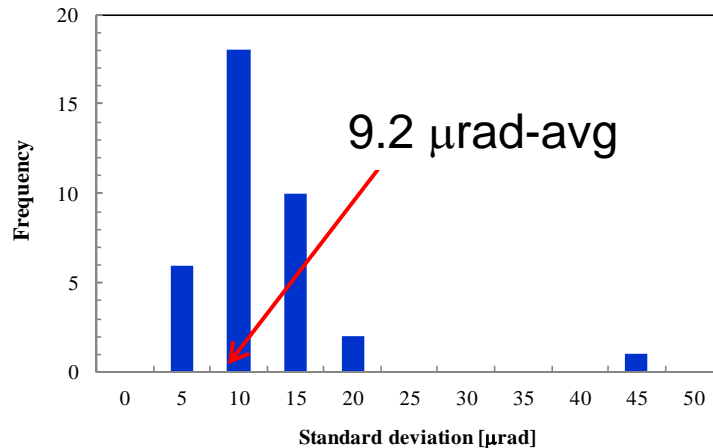
Comparison between the other methods,  
“Laser” stands for the results by our laser alignment system

- Agreed with the two results within **sub-mm**.
- Straightness can be evaluated with standard deviations of **26 μm-avg**, and **49 μm-max**.

\*The earth curvature was compensated considering the earth as a sphere with a radius of 6371 km for the result by the inclinometer.

# Error estimation

- **0.6 mm- $2\sigma$  for 500 m**  $\Rightarrow$  Can be adopted for evaluating the KEK linac

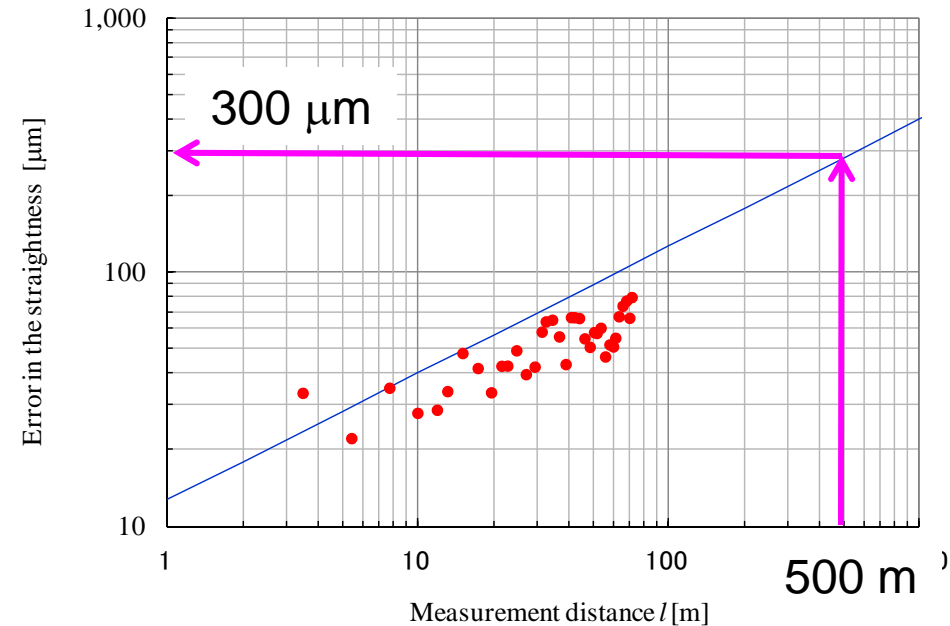


Histogram of the standard deviations for the derived slope angles

Error propagated to the straightness:

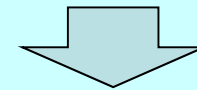
$$\sigma_f = \sqrt{s \cdot l} \cdot \sigma_\theta$$

$l$ : Measurement distance,  
 $s$ : Sampling interval  $\Rightarrow$  1.9 m-avg,  
 $\sigma_\theta$ : Error in the obtained angle  
 $\Rightarrow$  9.2  $\mu\text{rad}$ -avg



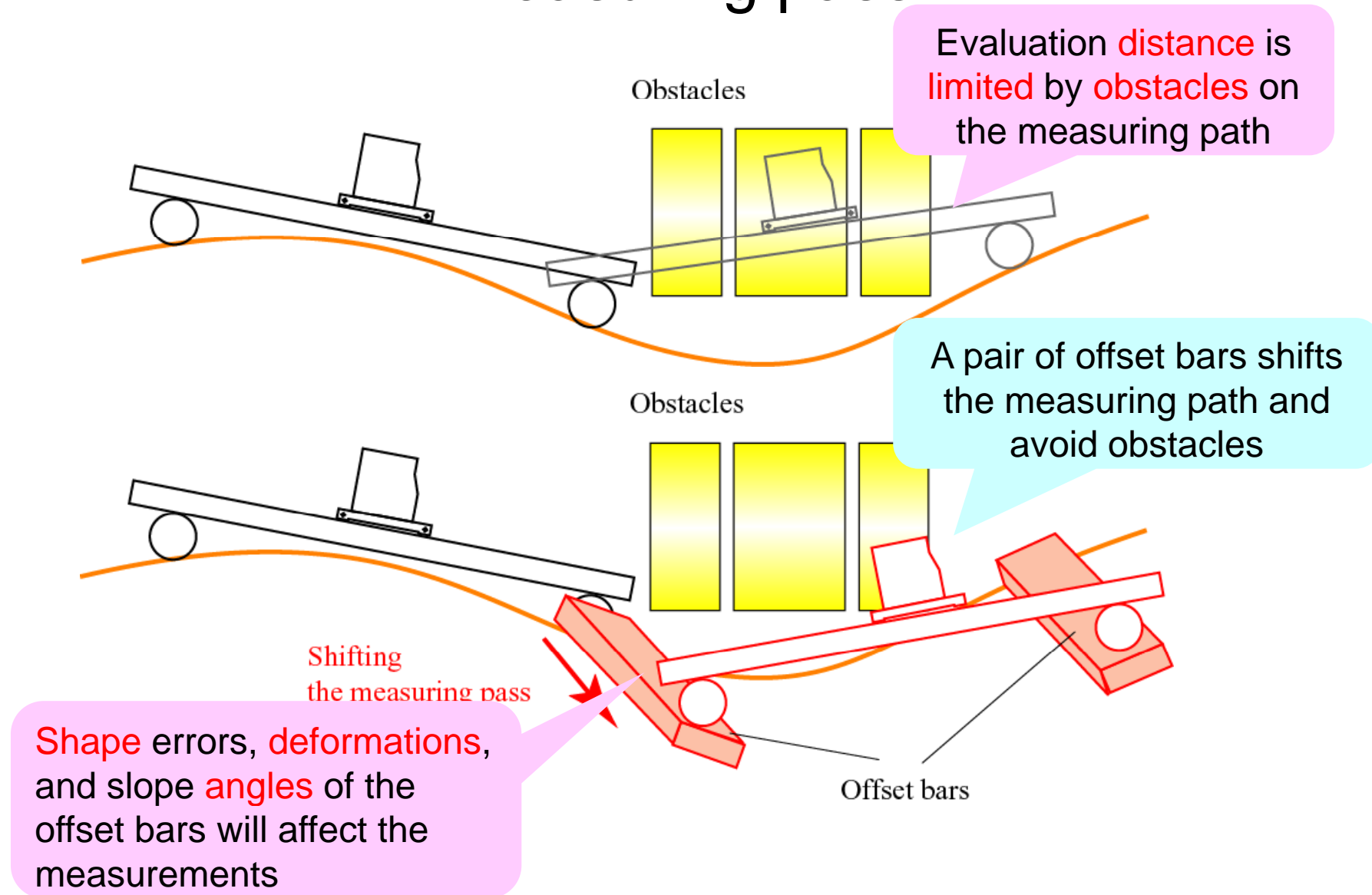
Error propagated to the straightness -experimental and estimated value.

- The experimental value agrees well with the estimated one.

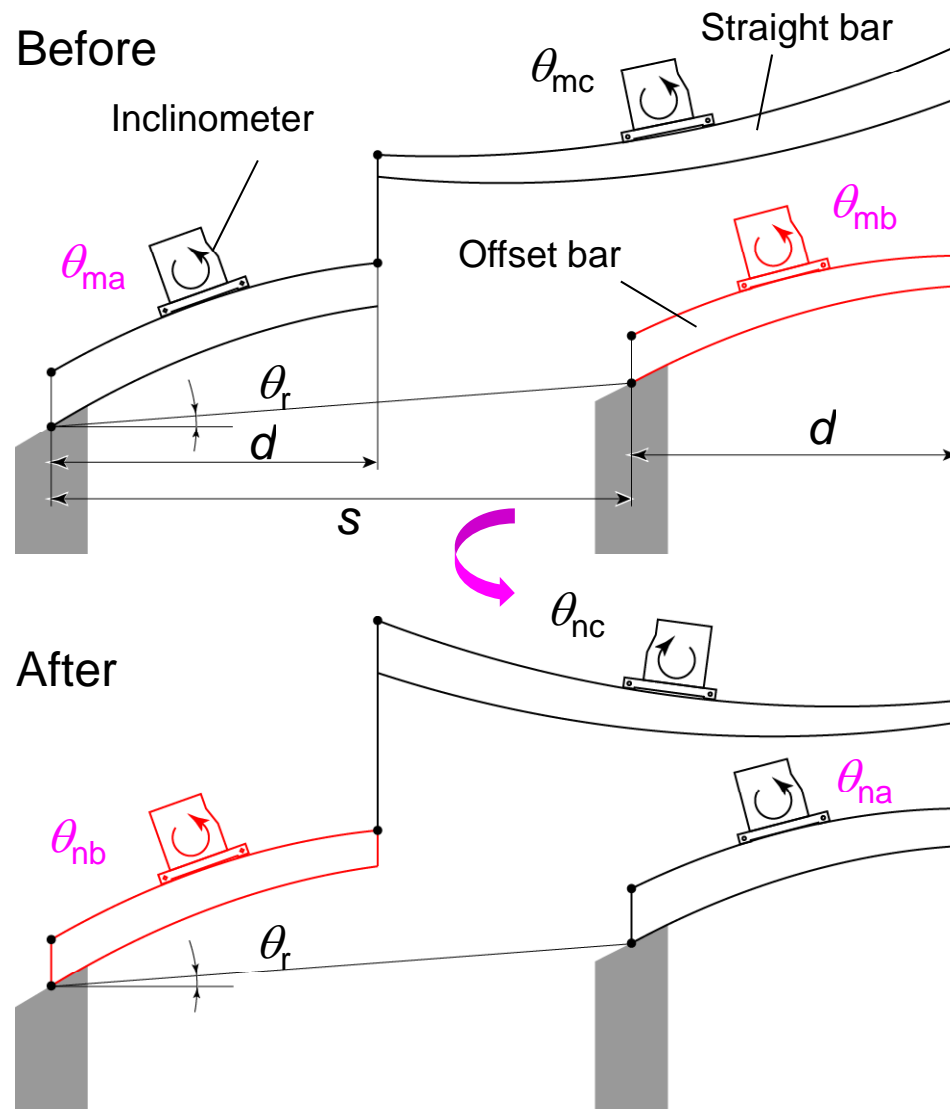


The estimated value is **reliable**.

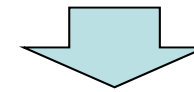
# Offset bars for avoiding obstacles on the measuring pass



# Reversal measurement considering slope angles of the offset bars



Offset of the system caused by  
Offsets of the inclinometers,  
**Shape** errors of the bars,  
**Deformations** and **slopes** of the bars

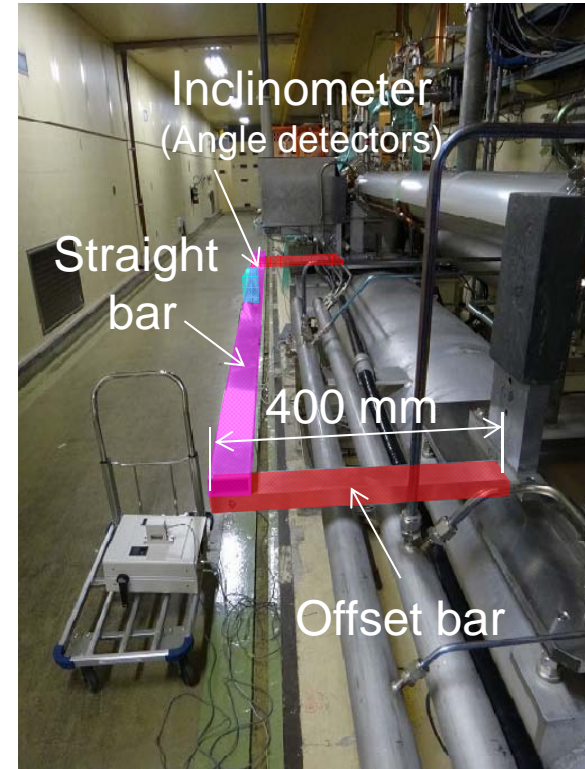
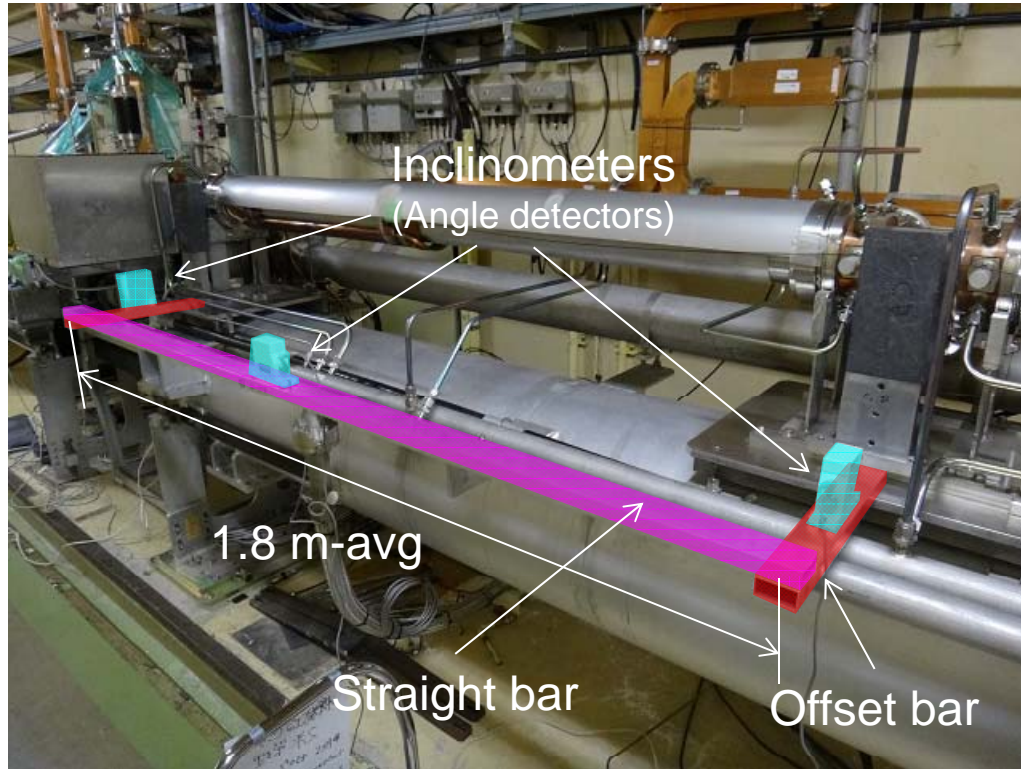


can be eliminated by

$$\theta_r = \frac{\theta_{mc} - \theta_{nc}}{2} - \frac{d \{ (\theta_{mb} - \theta_{ma}) + (\theta_{na} - \theta_{nb}) \}}{2s}$$

$\theta_r$ : Slope angle (angle to be measured),  
 $\theta_{ma}$ ,  $\theta_{mb}$ ,  $\theta_{mc}$ : Measurements before reverse,  
 $\theta_{na}$ ,  $\theta_{nb}$ ,  $\theta_{nc}$ : Measurement after reverse,  
 $d$ : Length of the offset bars,  
 $s$ : Length of the straight bar

# Straightness evaluation for the KEK $e^-/e^+$ Linac using a pair of offset bars



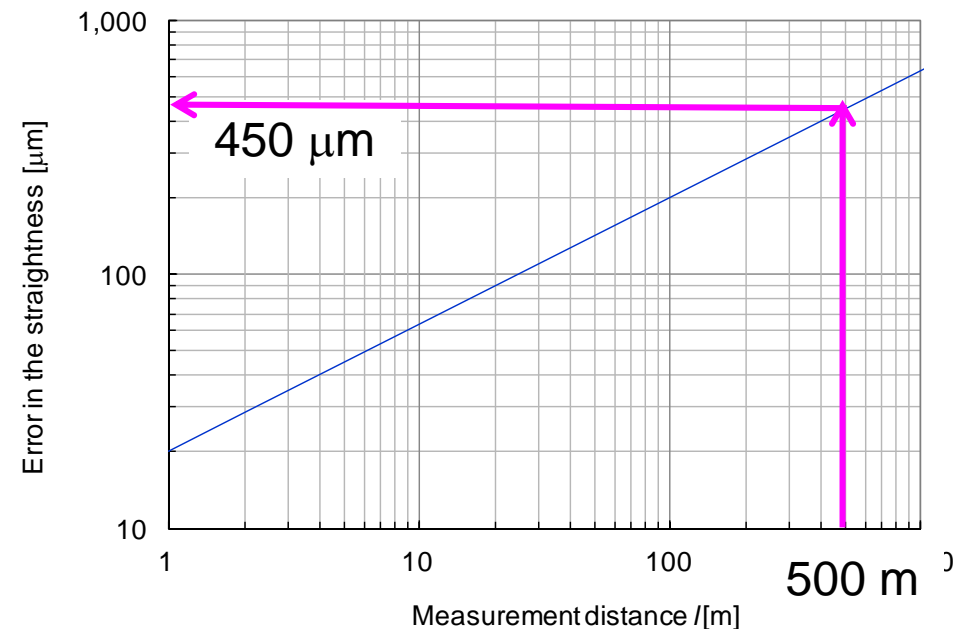
# Deviation of the derived slope angle and Error estimation

- 0.9 mm-2 $\sigma$  for 500 m  $\Rightarrow$  Can be adopted for evaluating the KEK linac

Error propagated to the straightness:

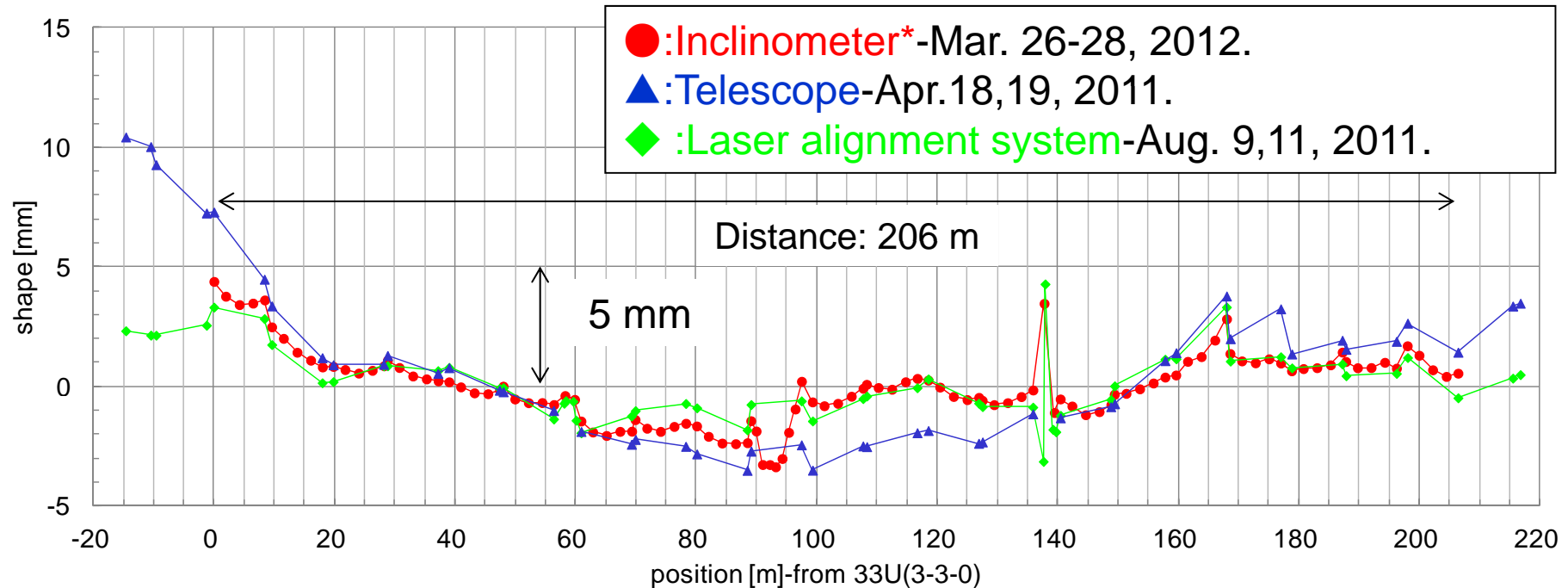
$$\sigma_f = \sqrt{s \cdot l} \cdot \sigma_\theta$$

$l$ : Measurement distance,  
 $s$ : Sampling interval  $\Rightarrow$  1.8 m-avg,  
 $\sigma_\theta$ : Error in the obtained angle  
 $\Rightarrow$  15  $\mu$ rad for single measurement point



Error propagated to the straightness  
-estimated value.

# Straightness evaluation for the 206-m-long part of the KEK e-/e<sup>+</sup> linac



- Similar trend.
- Partly agreed within sub-mm range.



Fairly **reliable** with each other

\*The earth curvature was compensated considering the earth as a sphere with a radius of 6371 km.



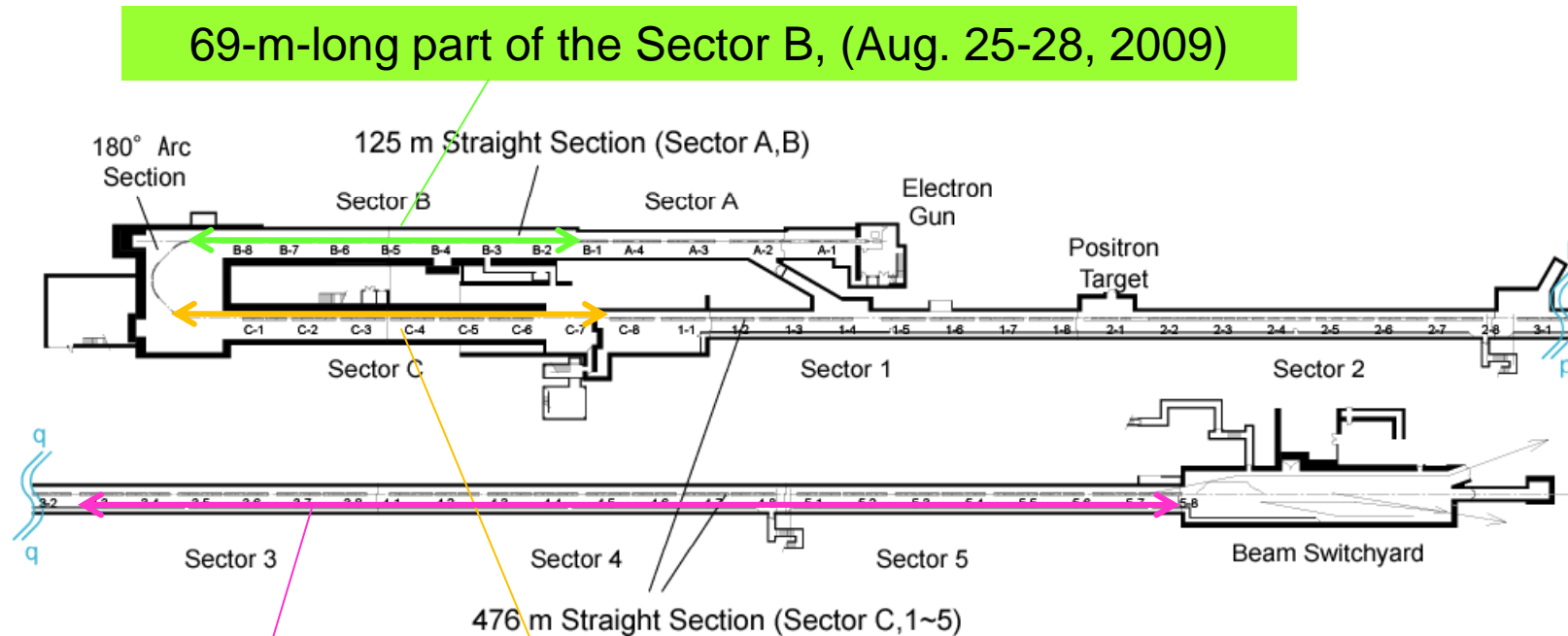
# Conclusion

1. Reversal measurement is effective for **eliminating offset** and **reducing drift** of the angle measurement system.
2. Obstacles on the measuring path can be avoided by pair of **offset bars**. It can extend evaluation distance of the system.
3. By considering **slope angles** of the offset bars, affects of the shape errors, deformations, and slopes of the offset bars can be eliminated.
4. **206-m-long** straightness evaluation of the KEK e<sup>-</sup>/e<sup>+</sup> Linac was demonstrated with standard deviation of **15 μrad** for the derived slope angles.
5. It is **applicable** for evaluating the whole 500-m-long KEK e<sup>-</sup>/e<sup>+</sup> Linac with  $2\sigma$  of better than 1 mm.

# Issues

1. Demonstrate **longer** (500 m or longer) straightness measurement
2. Estimate/evaluate the system's performance **precisely** for longer measurement distance.
3. Consider/realize **horizontal** straightness evaluation method  
(Straightness in the horizontal plane)

# Straightness measurement using inclinometers adopted for the KEK e<sup>-</sup>/e<sup>+</sup> linac



71-m-long part of the Sector C, (Mar. 29-31, 2010)

206-m-long part for the longer straight section (Mar. 26-8, 2012)