



Future Colliders:

ELC-Ansatz

Vladimir SHILTSEV (Fermilab)

Physics Limits of Ultimate Beams - III

January 22, 2021 – Snowmass'21 AF1



Content:

- **Part I**
 - Ultimate colliders: *Scope and Approach*
 - Ultimate colliders: *ELC-Ansatz, Units*
 - Ultimate colliders: *Limits of E*
 - Ultimate colliders: *Limits of L*
 - Ultimate colliders: *Limits of C*
 - Other considerations: *T*
- **Part II**
 - Circular *pp / ee / $\mu\mu$*
 - Linear and Plasma *ee / $\gamma\gamma$ / $\mu\mu$*
 - Exotic (crystal) *$\mu\mu$ / $\mu\mu$*
- **Conclusions / Q&A / Discussion**

*In search of uniform approach to discuss
far future/ultimate machines*

- **BASED ON EXISTING TECHNOLOGIES**

- Circular ee
- Linear $ee/\gamma\gamma$
- Circular pp
- Circular $\mu\mu$

- **BASED ON EMERGING TECHNOLOGIES**

- ERL $ee/\gamma\gamma$
- Plasma $ee/\gamma\gamma$
- Linear $\mu\mu$ / Plasma $\mu\mu$

- **EXOTIC SCHEMES**

- Crystal linear $\mu\mu/\tau\tau$
- Crystal linear $\tau\tau$
- Crystal circular pp

“*ELC – Ansatz*”

- We will evaluate possible (ultimate) future colliders on base of
 - Feasibility of *Energy*
 - Feasibility of *Luminosity*
 - Feasibility of *Cost*
- For each machine type / technology we will start with what is the state-of-the-art now and attempt to make “*1-2-several*” orders of magnitude steps in *Energy*
 - see how it affects *Luminosity*
 - see how it affects *Cost*
- Leave it to others to judge where the lower limit on *L* and upper limit on *C* are... other limits may appear

“ELC – Ansatz” : Choice of Units

- Units of Energy will be **TeV**
 - most often $cme = 2 \times E_{beam}$, sometimes - per beam
- Units of Luminosity will be **ab⁻¹/yr**
 - e.g., $1e35$ over $1e7$ sec/yr... HL-LHC will have $0.3 \text{ ab}^{-1}/\text{yr}$
 - factor of ~ 2 uncertainty in peak lumi / machine availability
- Units of power(total facility) will be **TWh/yr**
 - Eg CERN/LHC $\sim 200\text{MW}$ and $1.1\text{-}1.3 \text{ TWh/yr}$
- Units of Cost will be **LHCU**
 - cost of the LHC construction, approx. $10\text{B}\$$ - see below
 - for other machines the cost will be estimated using **$\alpha\beta\gamma$ model** with uncertainty $O(2)$ - see below
 - the **$\alpha\beta\gamma$ model** needs to be extended for novel approaches

Limits on *Energy* (1)

- Linear vs Circular

$$\Delta U_{SR} = \frac{90 \text{ keV} \cdot E_e^4 (\text{GeV})}{R [\text{m}]}$$

$$\Delta U_{SR} < E_e$$
$$E_e < 500 \text{ GeV} \cdot \left(\frac{R}{10 \text{ km}}\right)^{1/3}$$

- *Circular does not make sense beyond these energies*

$$\text{for } \mu\text{ons: } \times \left(\frac{m_\mu}{m_e}\right)^{4/3}$$
$$E_\mu < 600 \text{ TeV} \cdot \left(\frac{R}{10 \text{ km}}\right)^{1/3}$$

$$\text{for protons: } \times \left(\frac{m_p}{m_e}\right)^{4/3}$$
$$E_p < 10 \text{ PeV} \cdot \left(\frac{R}{10 \text{ km}}\right)^{1/3}$$

Limits on *Energy* (2)

- Particles don't survive acceleration

$$dN/dt = -N/\gamma\tau_0$$

$$\frac{N}{N_0} \approx \left(\frac{m_\mu c^2}{E} \right)^\kappa, \quad \kappa = (m_\mu c/\tau_0 G)$$

– *Unstable particles*

for muons $G \gg 3 \text{ MeV m}^{-1}$

for τ -leptons $G \gg 0.3 \text{ TeV m}^{-1}$

– *Lossy transport from cell to cell (loss in plasma material, c-t-c efficiency)*

$$\left(1 - \frac{\Delta N}{N}\right)^M \lesssim 1$$

$$M = \frac{E}{\Delta E_{\text{cell}}} = \frac{5 \text{ TeV}}{5 \text{ GeV}} = 10^3$$

$$M \cdot \frac{\Delta N}{N} \lesssim 1 \rightarrow \frac{\Delta N}{N} < 10^{-3} \text{ lab}$$

Limits on *Energy* (3)

- Corollary limits

For example:

- *Space/area available*

Circumference 100 km , $B < 16$ T , $E < 50$ TeV

Circumference 40,000 km, $B = 1$ T, $E < 1.3$ PeV

Length 50 km , $G < 0.1$ GV/m, $E < 5$ TeV

Length 10 km, $G < 1$ TV/m, $E < 10$ PeV

- *Power available*

- *Money available*

Limits on *Luminosity* (1)

- General Equation

$$\mathcal{L} = f_0 \cdot n_b \cdot \frac{N_p^2}{4\pi\sigma_{SP}^2}$$

- rewrite with norm.emm.

$$\mathcal{L} \sim f_0 \cdot n_b \cdot \gamma \cdot \frac{N_p^2}{4\pi\epsilon_0 \beta^2}$$

- HEP demand

$$\mathcal{L} \sim S \sim E^{-2}$$

- limits, eg, *beam power*

$$P = f_0 \cdot n_b \cdot N_p \cdot \gamma \cdot mc^2$$

$$\mathcal{L} \sim \frac{P^2}{f_0 \cdot n_b \cdot \gamma \cdot 4\pi\epsilon_0 \cdot m^2 c^4}$$



$$\mathcal{L} \sim \frac{P^2}{E}$$

Limits on *Luminosity* (2)

- Another example

σ_{IP} is limited (e.g. 1Å)

$$\mathcal{L} \sim \frac{p^2}{f_0 n_b E^2 \cdot 4\pi \sigma_{IP}^2}$$

- *beam-beam limit*
- *space-charge limit*
- *beam loading*
- *event pile-up*

$$\xi = \frac{r_p N_p}{4\pi \epsilon_1}$$

$$\Delta Q_{sc} = \frac{r_p N_p}{4\pi \epsilon_1 \beta \gamma^2}$$

$V_L \sim N_p \cdot \text{impedance}$

$$PU \sim \frac{\mathcal{L}}{f_0 n_b} \sigma_{incl}$$

Limits on *Luminosity* (3)

- *particle production*
- *beamstrahlung*
- *synchrotron radiation*
- *SR/meter*
- *IR rad damage*
- *ν -radiation dose*
- *instabilities*
- *jitter/emittance growth*

$$\frac{dN}{dt} (\mu, e^+)$$

$$\sigma_E \sim \frac{\gamma^2 N_p}{\sigma_z \sigma_x^2}$$

$$\sim \frac{\gamma^4}{R^2}$$

$$P_{SR} \sim \frac{\gamma^4}{R}$$

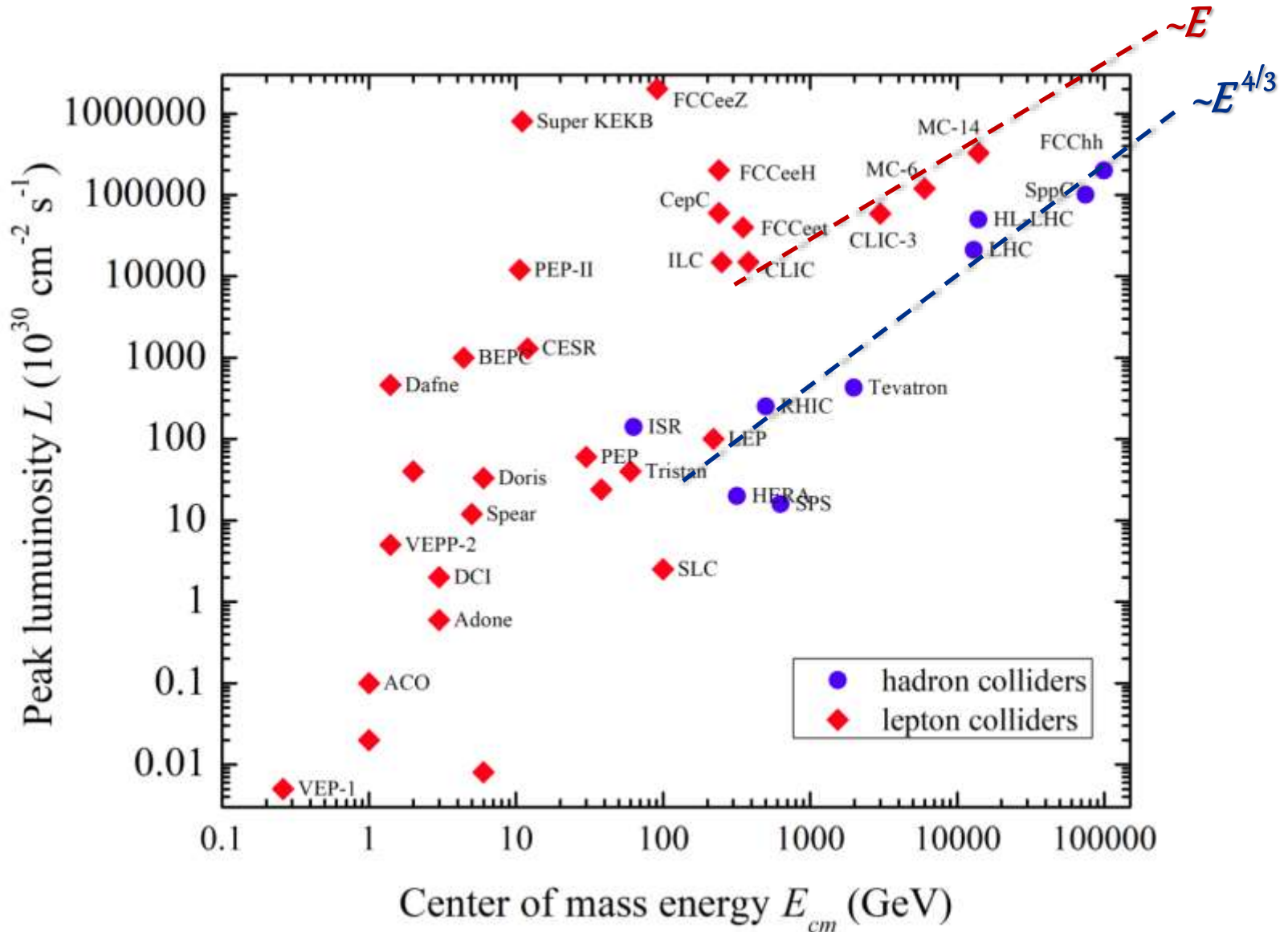
$$\sim PU \cdot E \cdot f \cdot n_b$$

$$D \sim \frac{N_p \gamma^3}{R^2}$$

$$TMci, RW, e-cloud \quad N \sim \frac{E}{\sigma_T}$$

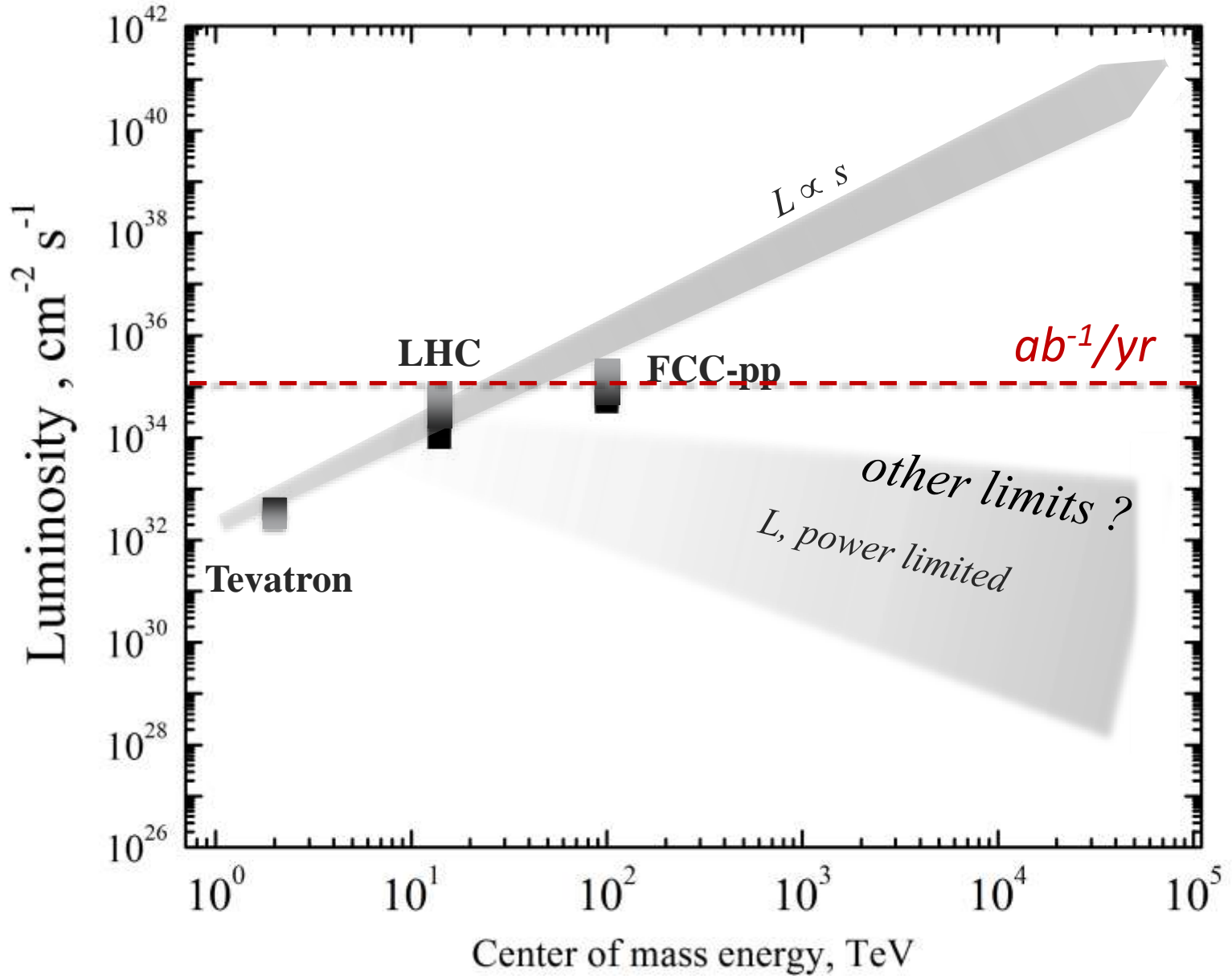
$$\sim \gamma$$

All Colliders: Past, Existing, under Discussion



On base of Shiltsev&Zimmermann, Rev.Mod.Phys. (2021)

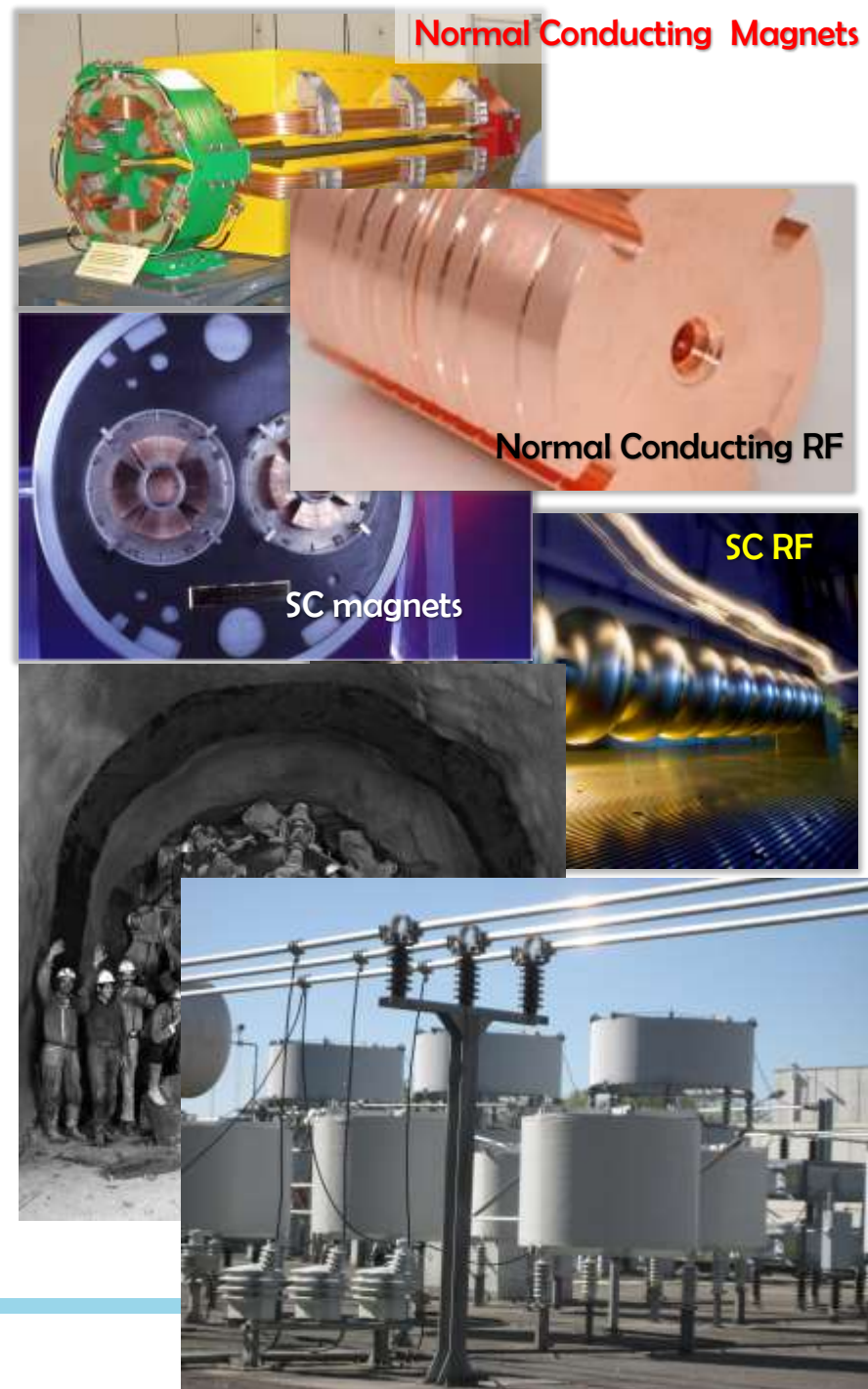
Paradigm Shift looming for $> 0.1-1$ PeV...



... to be discussed below...

Limits on Cost (1)

- Cost is set by technology
 - *Accelerator technology*
 - *Civil construction technology*
 - *Power production, delivery and distribution technology*



2014 Cost analysis:

2014 JINST 9 T07002

17 “Data Points” - Costs of Big Accelerators:

- Actually built:
 - RHIC, MI, SNS, LHC
- Under construction:
 - XFEL, FAIR, ESS
- Not built but costed:
 - SSC, VLHC, NLC
 - ILC, TESLA, CLIC, Project-X, Beta-Beam, SPL, v-Factory

Wide range :

- 4 orders in Energy, >1 order in Power, >2 orders in Length
- Almost 2 orders in cost
 - (normalized to US TPC)

	Cost (B\$) Year	Energy (TeV)	Accelerator technology	Comments	Length (km)	Site power (MW)	TPC range (Y14 B\$)
SSC	11.8 B\$ (1993)	40	SC Mag	Estimates changed many times [6–8]	87	~ 100	19–25
FNAL MI	260M\$ (1994)	0.12	NC Mag	“old rules”, no OH, existing injector [9]	3.3	~ 20	0.4–0.54
RHIC	660M\$ (1999)	0.5	SC Mag	Tunnel, some infrastructure, injector re-used [10]	3.8	~ 40	0.8–1.2
TESLA	3.14 B€ (2000)	0.5	SC RF	“European accounting” [11]	39	~ 130	11–14
VLHC-I	4.1 B\$ (2001)	40	SC Mag	“European accounting”, existing injector [12]	233	~ 60	10–18
NLC	~ 7.5 B\$ (2001)	1	NC RF	~ 6 B\$ for 0.5 TeV collider. [13]	30	250	9–15
SNS	1.4 B\$ (2006)	0.001	SC RF	[14]	0.4	20	1.6–1.7
LHC	6.5 BCHF (2009)	14	SC Mag	collider only — existing injector, tunnel & infrstr., no OH, R&D [15]	27	~ 40	7–11
CLIC	7.4–8.3B CHF(2012)	0.5	NC RF	“European accounting” [16]	18	250	12–18
Project X	1.5 B\$ (2009)	0.008	SC RF	[17]	0.4	37	1.2–1.8
XFEL	1.2 B€ (2012)	0.014	SC RF	in 2005 prices, “European accounting” [18]	3.4	~ 10	2.9–4.0
NuFactory	4.7–6.5 B€ (2012)	0.012	NC RF	Mixed accounting, w. contingency [19]	6	~ 90	7–11
Beta-Beam	1.4–2.3 B€ (2012)	0.1	SC RF	Mixed accounting, w. contingency [19]	9.5	~ 30	3.7–5.4
SPL	1.2–1.6 B€ (2012)	0.005	SC RF	Mixed accounting, w. contingency [19]	0.6	~ 70	2.6–4.6
FAIR	1.2 B€ (2012)	0.003–0.08	SC Mag	“European accounting” [20], 6 rings, existing injector	~ 3	~ 30	1.8–3.0
ILC	7.8 B\$ (2013)	0.5	SC RF	“European accounting” [21]	34	230	13–19
ESS	1.84 B€ (2013)	0.0025	SC RF	“European accounting” [22, 23]	0.4	37	2.5–3.8

! WARNING !

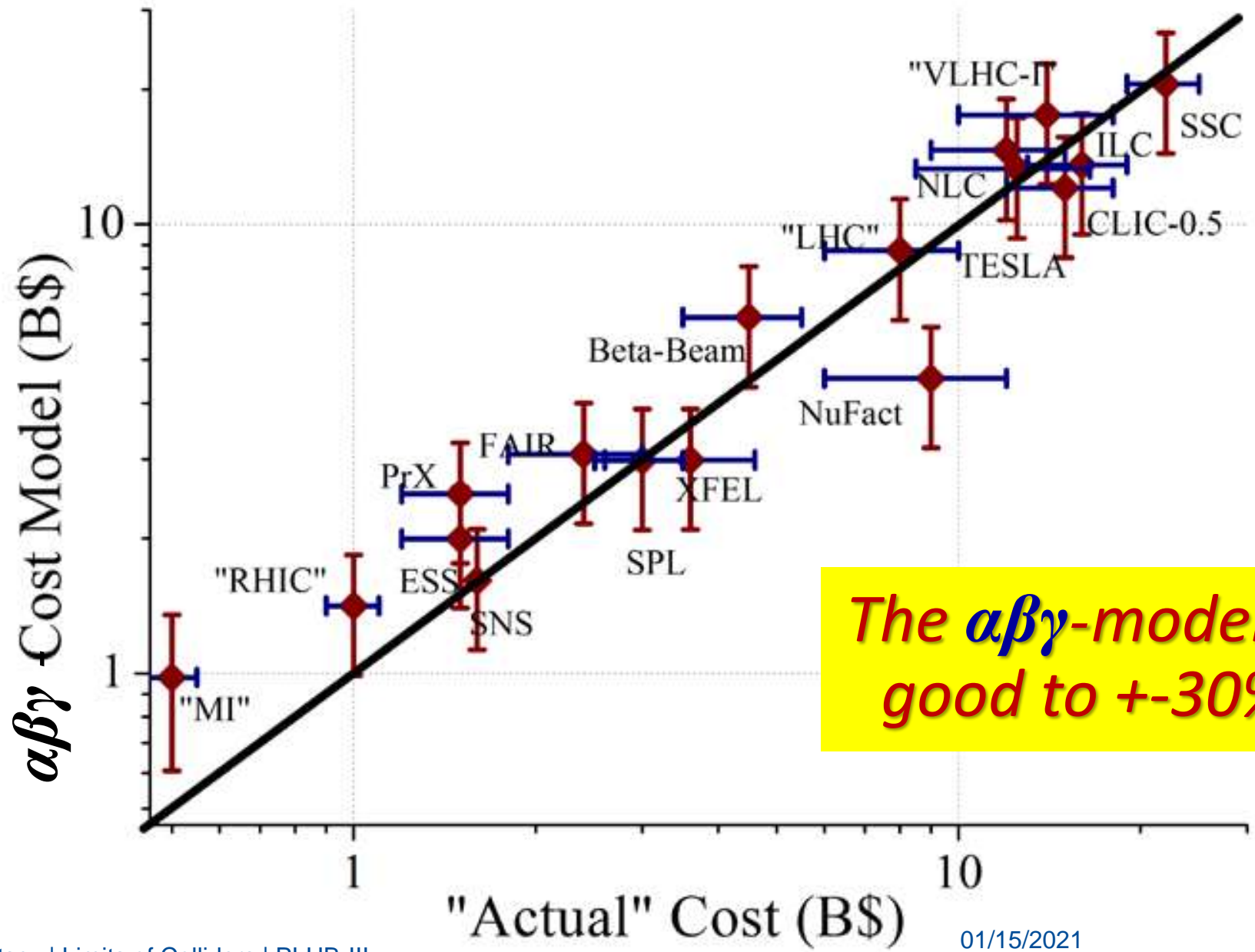
The $\alpha\beta\gamma$ cost model:

$$\text{Cost(TPC)} = \alpha L^{1/2} + \beta E^{1/2} + \gamma P^{1/2}$$

- a) Is for a “green field” facility !
- b) US-Accounting !
- c) There is hidden correlation btw E and technology progress
- d) Pay attention to units (10 km for L , 1 TeV for E , 100 MW for P)
 - $\alpha \approx 2\text{B}\$/\text{sqrt}(L/10 \text{ km})$
 - $\beta \approx 10\text{B}\$/\text{sqrt}(E/\text{TeV})$ for SC/NC RF
 - $\beta \approx 2\text{B}\$ /\text{sqrt}(E/\text{TeV})$ for SC magnets
 - $\beta \approx 1\text{B}\$ /\text{sqrt}(E/\text{TeV})$ for NC magnets
 - $\gamma \approx 2\text{B}\$/\text{sqrt}(P/100 \text{ MW})$

USE AT YOUR OWN RISK!

Total Cost vs $\alpha\beta\gamma$ -Model (Log-Log)



The $\alpha\beta\gamma$ -model is good to +/-30%

Illustrations

Comment:

Sqrt-functions are quite accurate over wide range because such dependence well approximates the “initial cost” – effect :

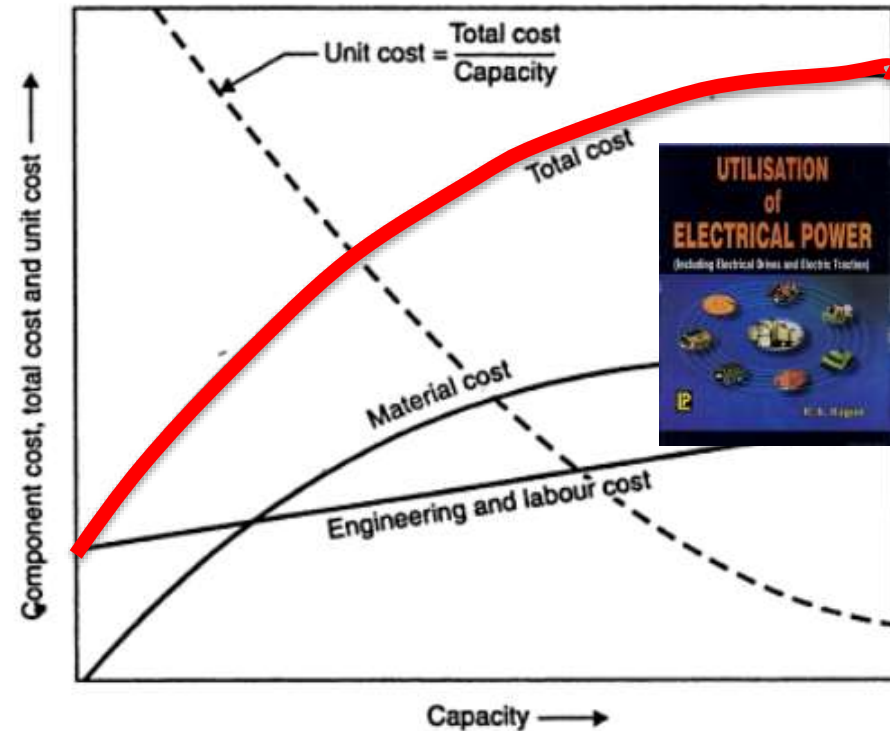
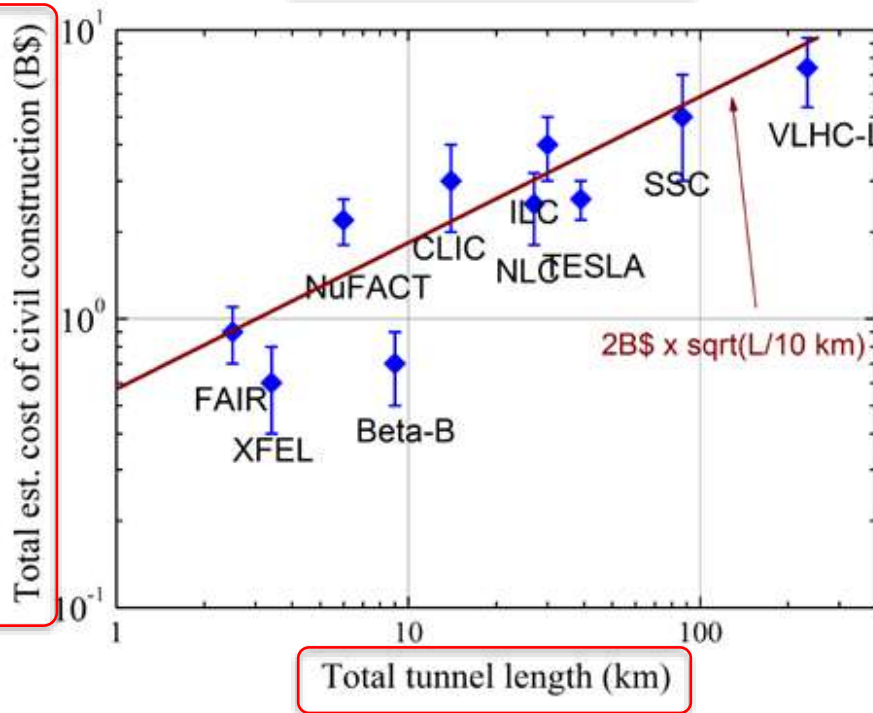
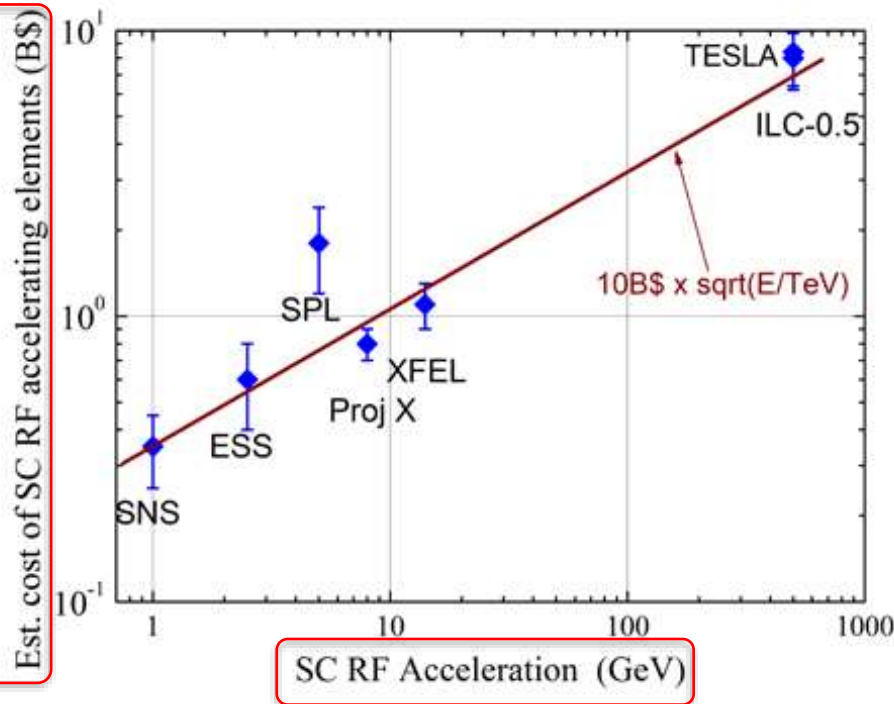


Fig. 9.5. Variation of costs of power plant versus its capacity.

Take LHC as an Example:

- **$\alpha\beta\gamma$ – Model:**

- 40 km of tunnels
- 14 TeV c.o.m SC magnets
- ~150 MW of site power

$$2\sqrt{40/10} = 4$$

$$2\sqrt{14} = 7.5$$

$$2\sqrt{150/100} = 2.5$$

TOTAL PROJECT COST : **14B\$ ± 4.5B\$**

- **ITF T.Roser talk @ PLUB-II (USD 2021):**

- existing injector complex **4.6 B\$**
- new accelerator systems **4.06 B\$**
- new infrastructure and civil **2.75 B\$**
- explicit labor **~1.4 B\$**

Total: 12.8B\$

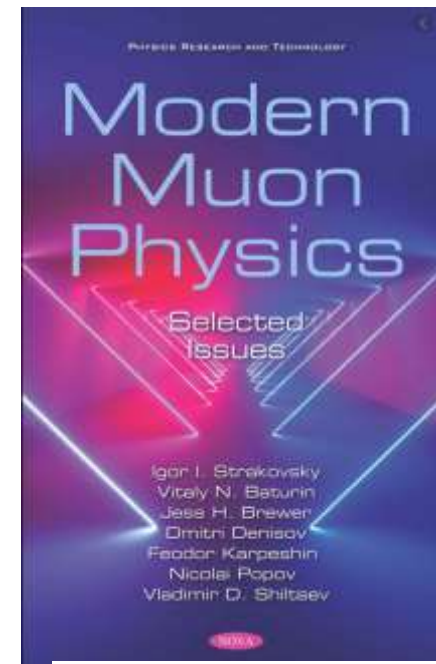
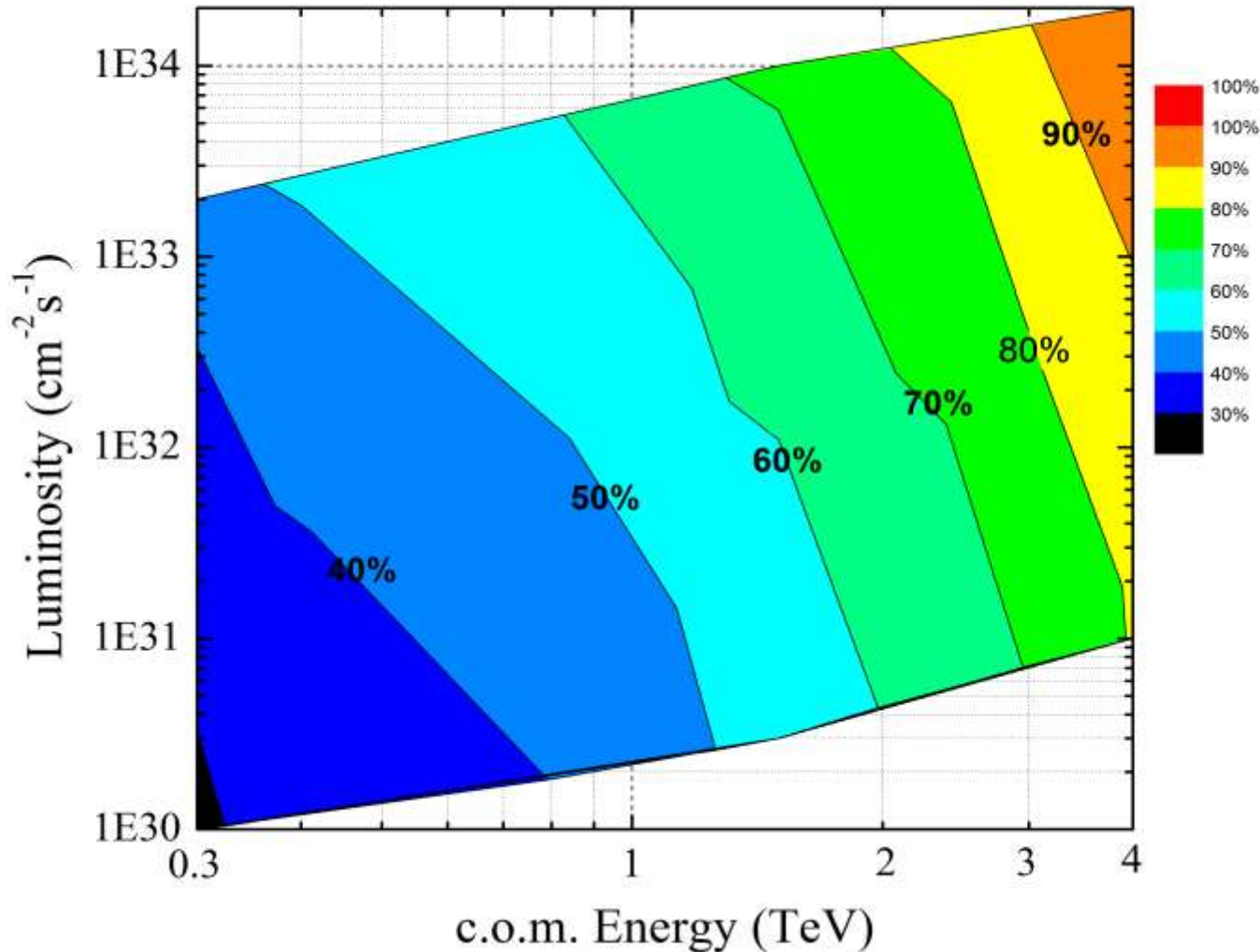
“ $\alpha\beta\gamma$ – Model” : Caveats

- (once again) note three warning signs:
 - “...+- 30% ...green field... US accounting...”
 - rounded powers and coefficients, e.g., $\sqrt{x} \approx x^{0.4...0.6}$
- Analysis was done in 2013:
 - inflation 7yrs x 3% = 21%
 - many more projects have been costed since then, others updated
- “Not-yet-built” machine costs estim’d by proponents
- “One person study” – limited research on the subject
- That’s why:
 - **a) ITF work is very important**
 - **b) I’ll use LHCU for rough estimates/analysis here**

“ $\alpha\beta\gamma$ – Model” : Notes

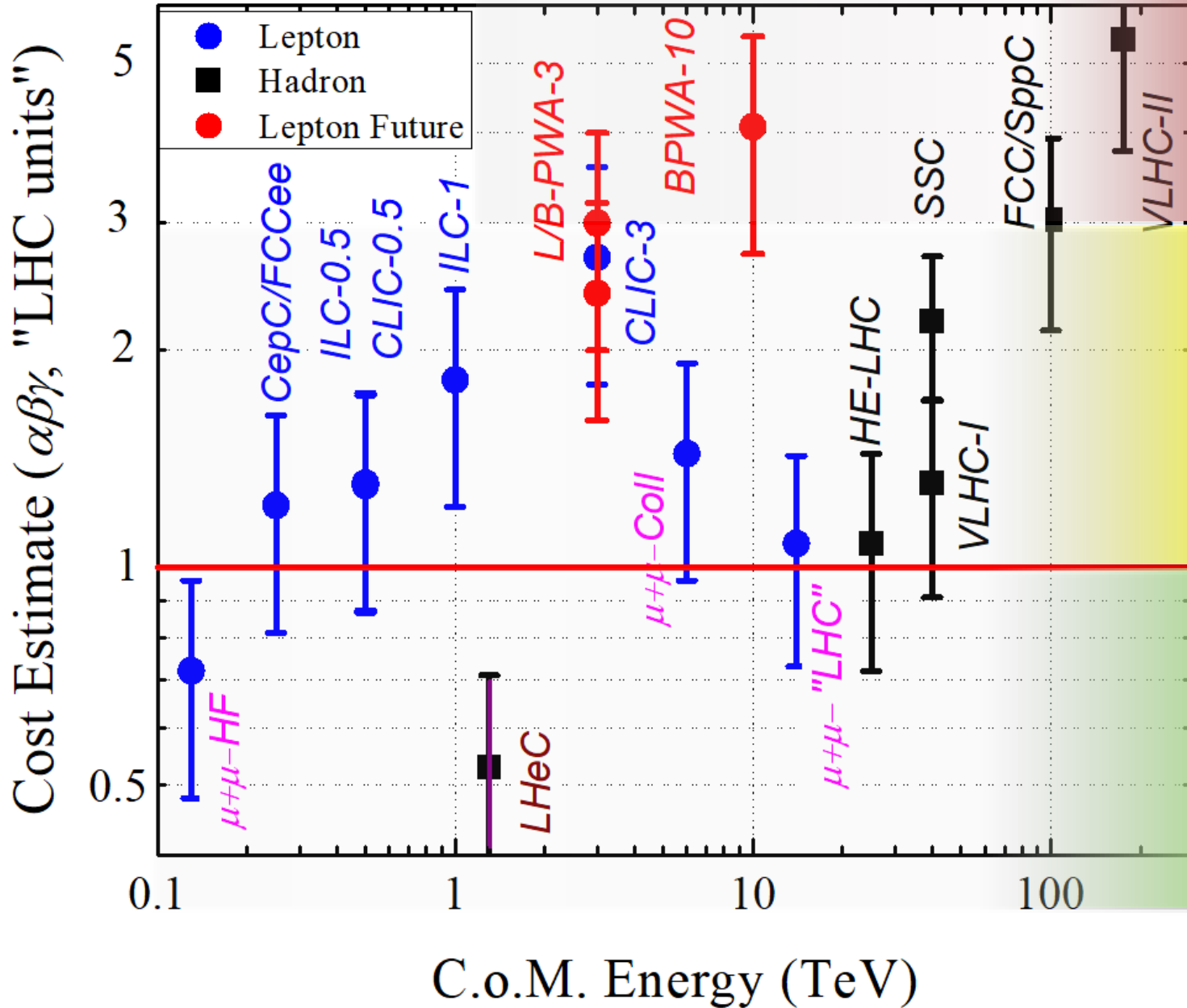
- Costs of future technologies are not well known:
 - plasma, lasers, crystals, “magic cheap” magnets, tunnels, HTS, etc
- Costs of civil construction and power systems are driven by larger economy (not by us)... “stable”
- Having injector ($\sim 1/3$ of cost) \rightarrow factor of 2 in energy reach
- Follows from the model:
 - Cost is weak function of luminosity (see next slide)
 - Also, LHC 10B\$, HL-LHC 1B\$ with x5 increase in luminosity
 - It’s OK to start high E , low L ...CESR, Tevatron increased $L > 100x$, LHC $> 10x$
 - Cost is moderate function of length/circumference
 - Cost is strong function of E nergy and technology
- Of course, the model does not tell us “what’s affordable”
 - but at least allows approximately sort proposals in categories
 - E.g., “Less than LHCU”, “1-2 LHCU”, “More than 3 LHCU”, etc

Example: Muon Colliders cost(color) vs E vs $Lumi$

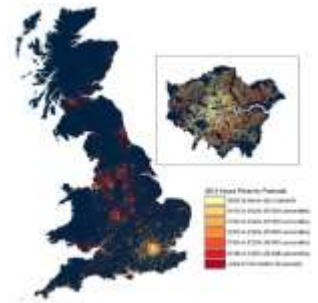


Modern Muon Physics:
Selected Issues,
I. Strakovsky, et al (Nova,
2020)

Some projects discussed @ *EPPSU'19* and *Snowmass'21*



Colliders: Probability to Be Built



$\sim 1/ \text{Cost}^2$ (is it true?)

$1/(1 \times \text{LHC})^2 = 100\%$

$1/(2 \times \text{LHC})^2 = 25\%$

$1/(3 \times \text{LHC})^2 = 10\%$

...Tao HAN : *calibration is function of community size, budget and time*

...Mike KORATZINOS : *lower cost?*

$\rightarrow 1/(1+\text{Cost}^2)$...

Fig 3 – Distribution of House Prices, 2015



Source: HM Land Registry

Distribution of Home Sales Prices in San Francisco



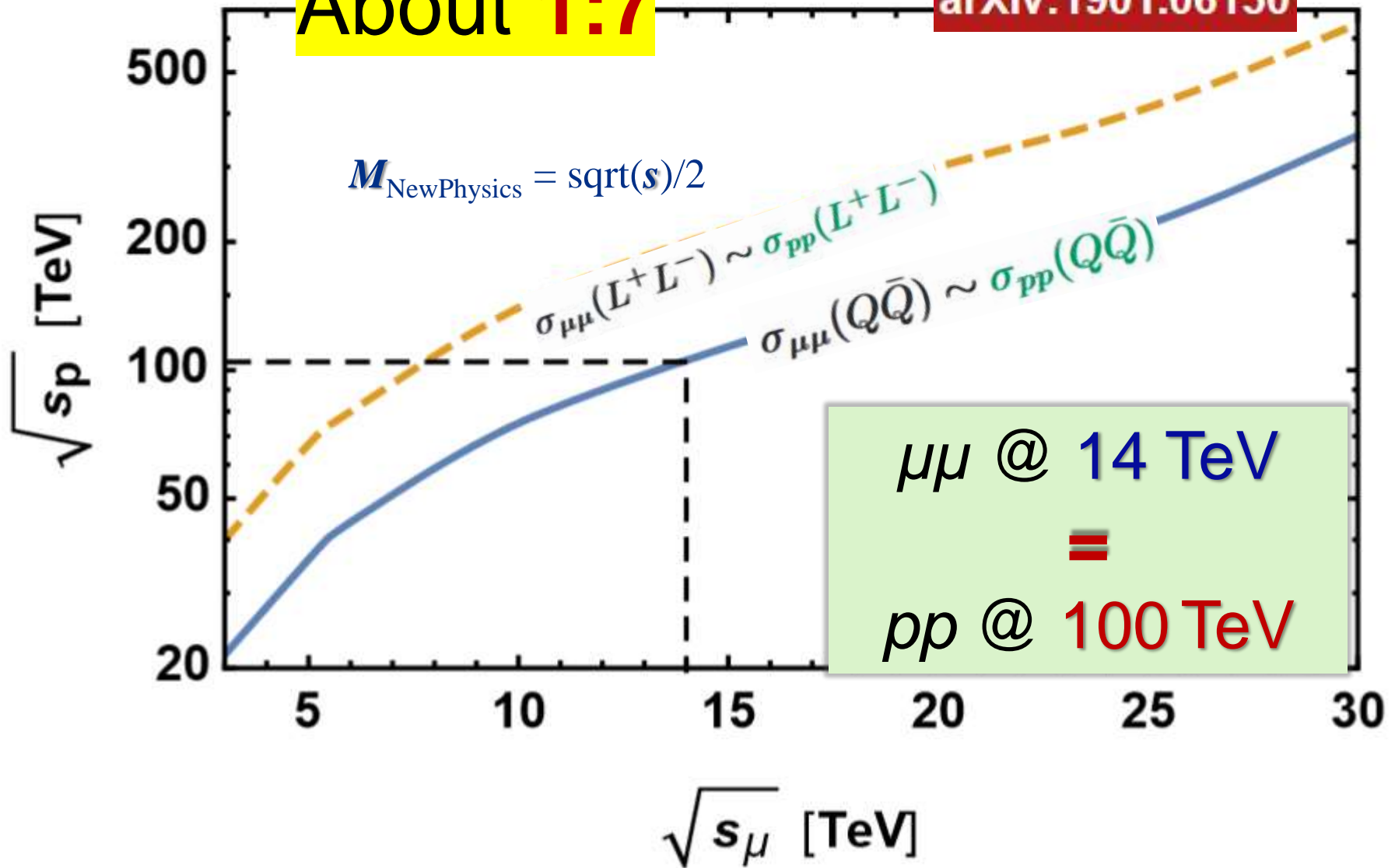
Source: Property records data.

URBAN INSTITUTE

Energy Ranges and Reference Points : *leptons vs hadrons*

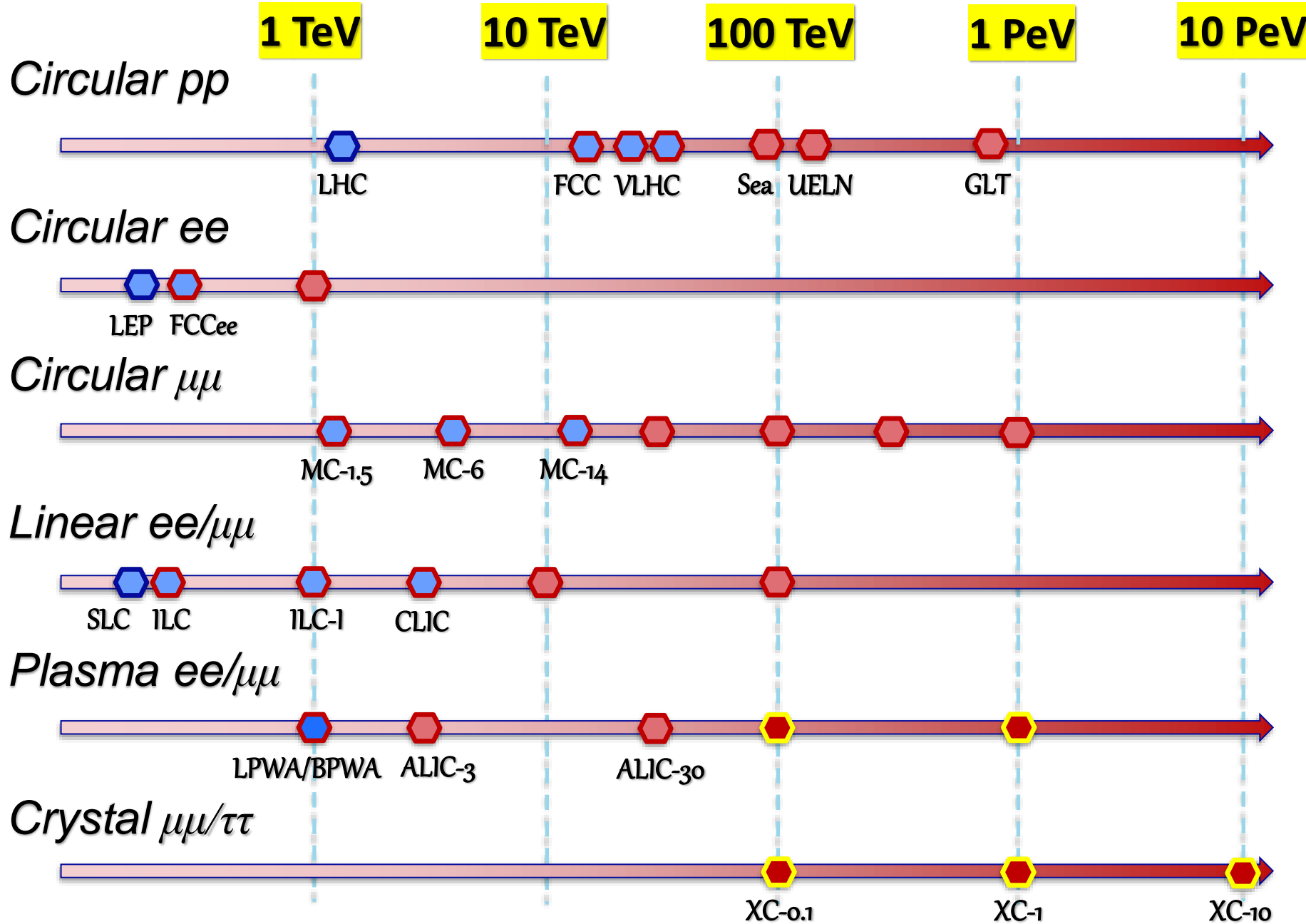
About **1:7**

arXiv:1901.06150

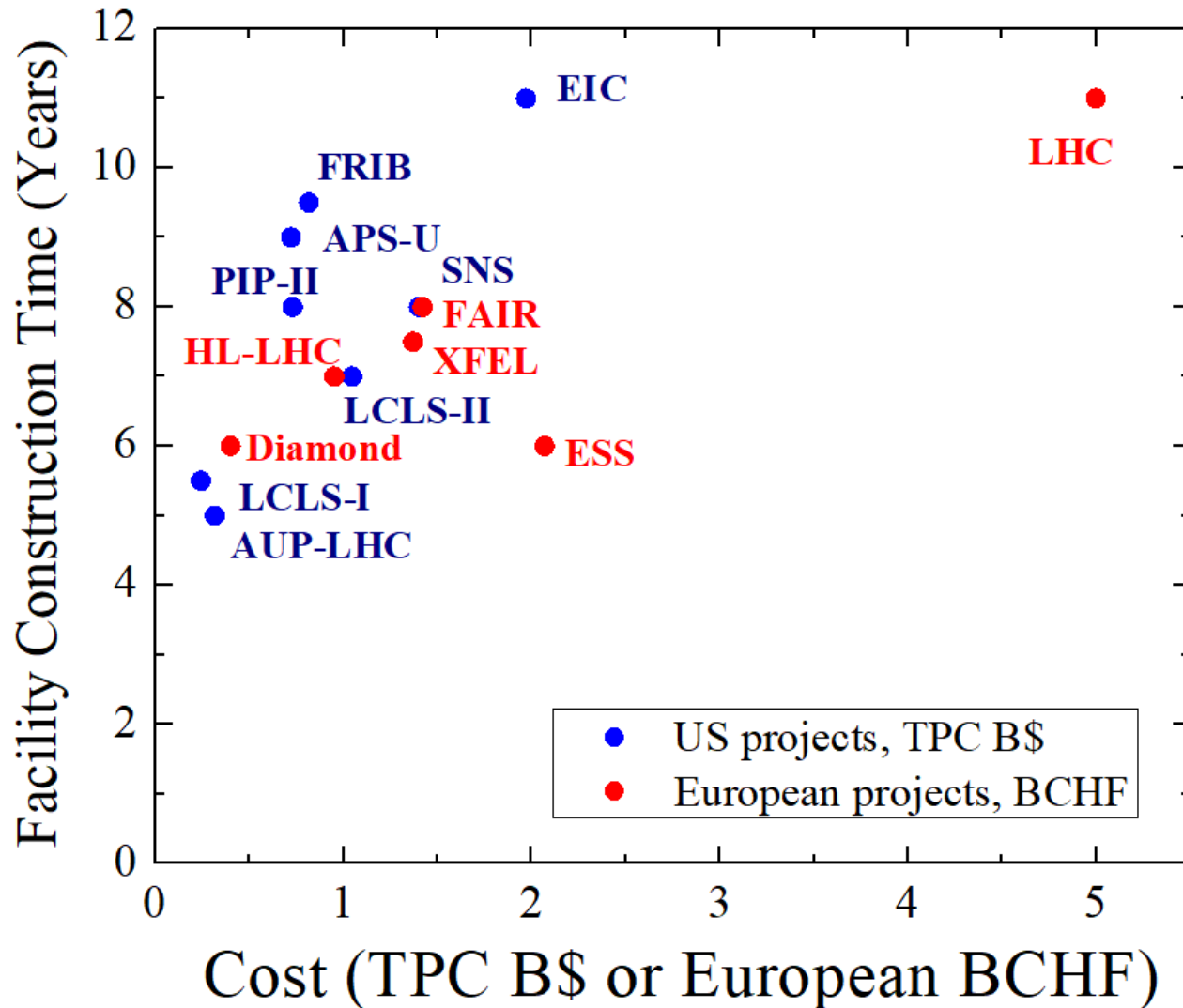


~ **Equivalent** reach in *pp* after rescaling for *pdf*'s

Reference Points and (Far) Future



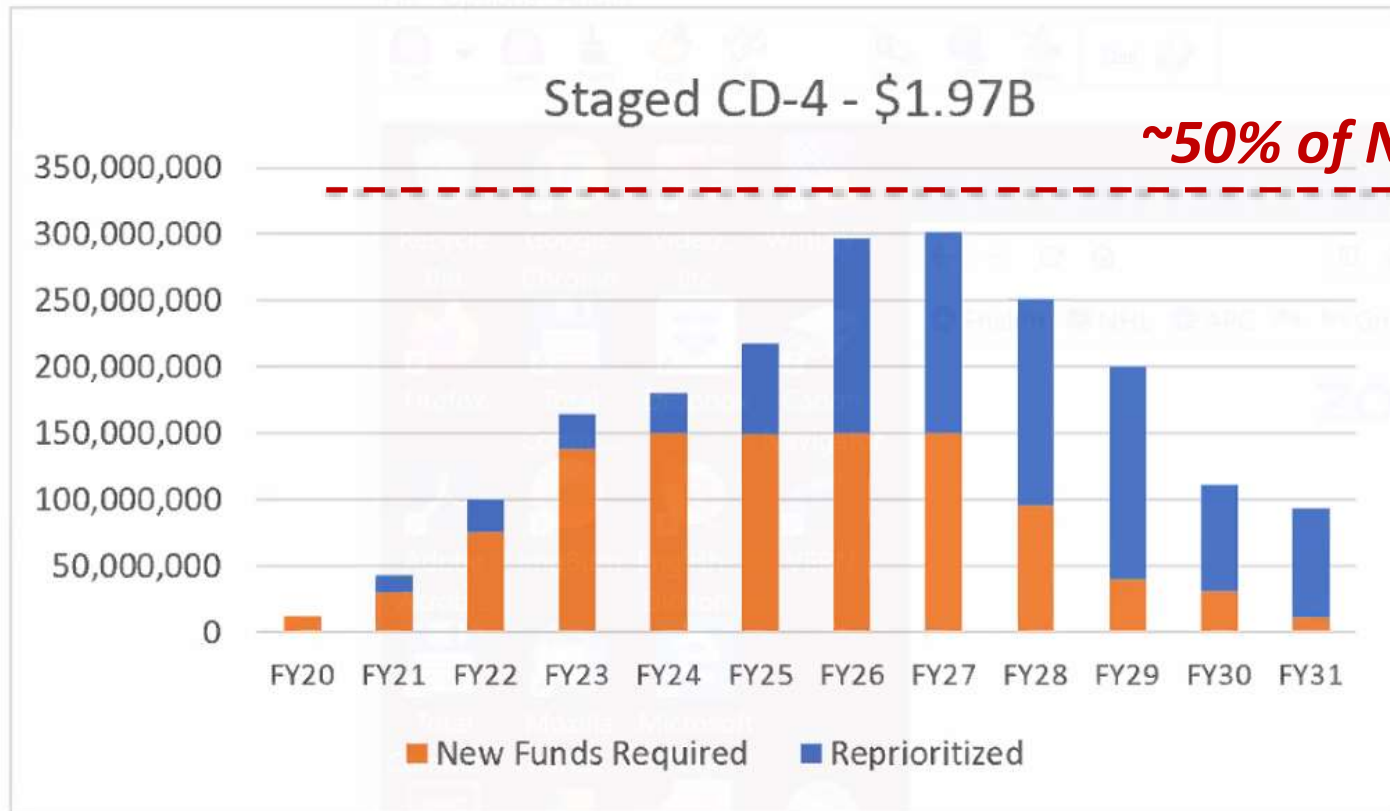
Construction Time... $\sim \text{SQRT}(\text{Cost})$?



Peak spending rate depends on \$\$/yr limit and on # of available experts ...currently, btw 0.2 to 0.5 B\$/yr (total World's HEP $\sim 4\text{B}\$$)

The latest: *EIC at BNL*

Reference Funding Profile



- Reprioritized and New Funding
- FY2021 Budget of \$30M supports schedule for CD-1
- Funding Profile Set prior to CD-2
- \$100M Investment by New York State for Conventional Construction

“Social Cost” and Social Limits

- There is probably a limit on cost of ultimate accelerators
 - *how much society (national, regional, global) wants/can afford spending on HEP...slowly varies in time (grows?)*
 - *current estimate for global big collider ~ **2-3 LHCU ?***
- Since recently – awareness of the “carbon footprint”/“ecology” limit for large facilities
 - *current estimate for global big collider ~ **1(2) TWH/yr ?***
 - *disturbed environment (land use, radiation, pollutants, etc)*
- Scarcity of materials
 - *Helium, Nb, W, etc ?*

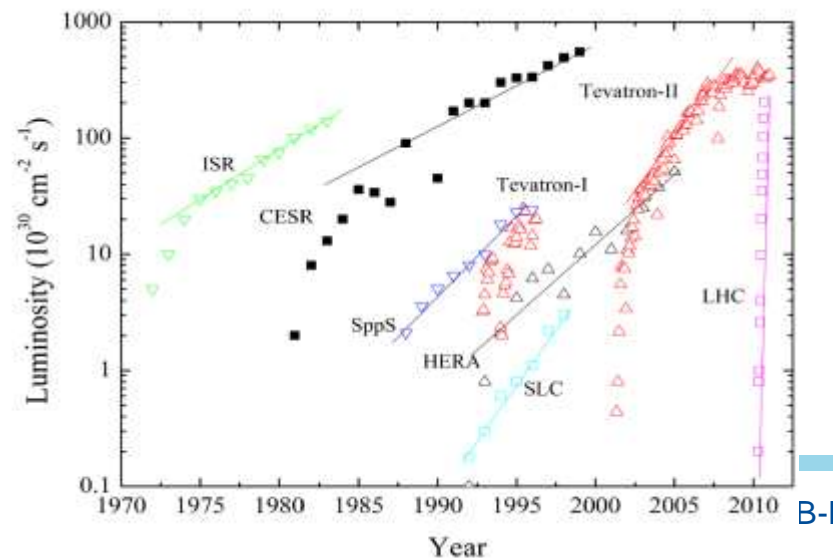
Commissioning Time : $T \sim \text{Complexity}$

CPT-theorem – V.Shiltsev *Mod. Phys. Lett. A*, vol. 26, No. 11 (2011) pp. 761-772

The evolution of the performance of continuously improving facilities where every next step brings x -fold improvement on top of previous improvement can be further simplified in an approximate formulas:

$$C \cdot P = T, \quad (3)$$

where the factor $P = \ln(\text{luminosity})$ is the “performance” gain over time interval T , and C is a machine-dependent coefficient equal to average time needed to increase the performance (in the case of colliders — luminosity) by $e = 2.71 \dots$ times, or boost the “performance” P by 1 unit. Both, T and C have the dimension of time,



- Get the energy (“one particle”):
 $C \sim O(1)$ yr – for known technologies, longer for new, $\sim \#$ of elements
- Get the (ultimate) luminosity:
depends on luminosity risk – eg for $P=4.5$ (risk ~ 100 in L) and $C \sim 2 \rightarrow T$
can be as long as $T=4.5 \times 2 = 9$ yrs

Content:

- **Part I**

- Ultimate colliders: *Scope and Approach*
- Ultimate colliders: *ELC-Ansatz, Units*
- Ultimate colliders: *Limits of E*
- Ultimate colliders: *Limits of L*
- Ultimate colliders: *Limits of C*
- Other considerations: *T*

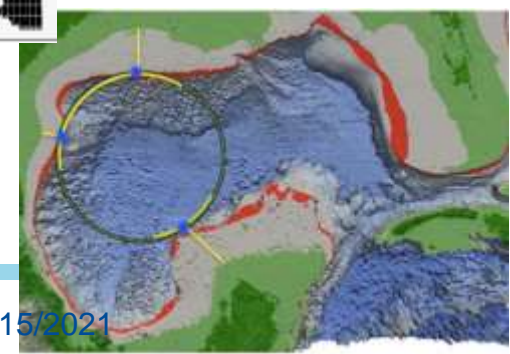
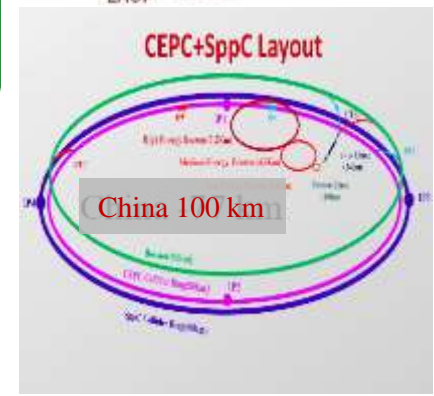
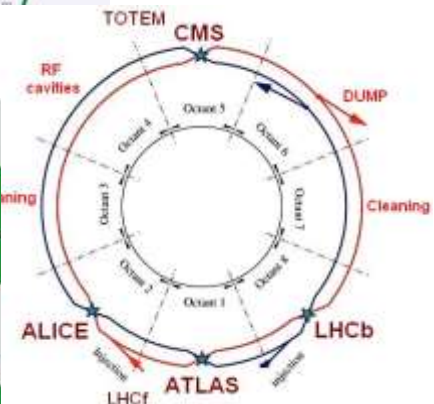
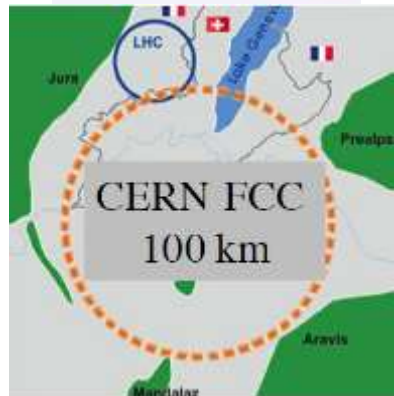
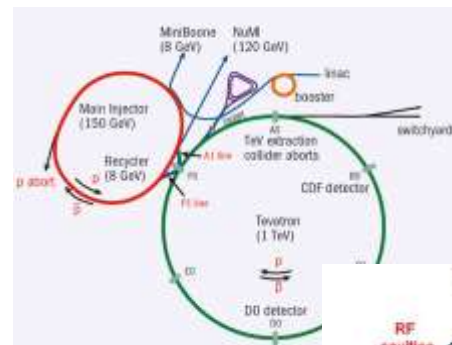
- **Part II**

- **Circular pp / ee / $\mu\mu$**
- **Linear and Plasma ee / $\gamma\gamma$ / $\mu\mu$**
- **Exotic (crystal) $\mu\mu$ / $\mu\mu$**

- **Conclusions / Q&A / Discussion**

Circular pp Colliders

- Can use Tevatron and LHC as reference points
- Parameter sets exist for SCC, FCC-hh, SppC, VLHC, Eloisatron
- Major advantages:
 - known technology and physics
 - good power efficiency ab^{-1}/TWh
- Major limitations:
 - Size (magnetic field B)
 - Power
 - Beam-beam, burn-off, instabilities
 - Synchrotron radiation
 - Cost



pp Luminosity

- Beam-beam limit #1

$$\xi = \frac{r_p N}{4\pi\epsilon_0 \beta^{**}}$$

$$\mathcal{L} \sim f_0 \gamma n_b \frac{N_0^2}{4\pi\epsilon_0 \beta^{**}}$$

$$\mathcal{L} \sim \xi \cdot f_0 \gamma n_b N_0$$

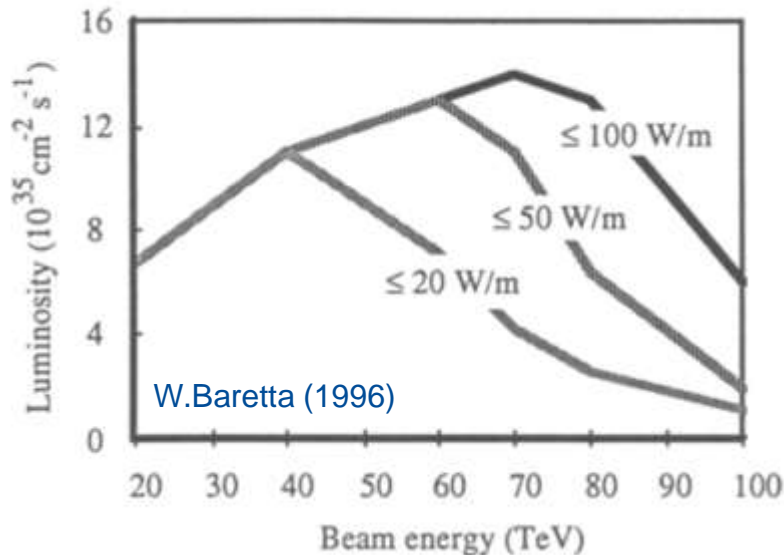
- Synchrotron radiation :

– Total power

– or SR/meter

$$P_{SR} \approx n_b N_0 \frac{\gamma^4}{R} \cdot f_0$$

$$\mathcal{L} \sim \frac{\xi}{\beta^{**}} \cdot \frac{P_{SR} \cdot R}{\gamma^3} \sim \frac{\xi}{\beta^{**}} P_{SR} \frac{1}{\gamma^2}$$



$$\mathcal{L} \sim \frac{\xi}{\beta^{**}} \left(\frac{P_{SR}}{2\pi R} \right) \cdot \frac{R^2}{\gamma^3} \sim \frac{\xi (P_{SR}/m)}{\beta^{**} \gamma^2}$$

Other limits

- Pile up

- IR radiation damage

- Resistive wall instability

- TMCI

- e-cloud

- Turn around time vs
Luminosity evolution

$$PU = \mathcal{L} \cdot \sigma_{in}$$

$$\mathcal{L} = f_0 n_b \frac{PU}{\sigma_{in}} \sim \frac{PU}{\tau_{BE} \cdot \log E}$$

$$Rad = \mathcal{L} \cdot E$$

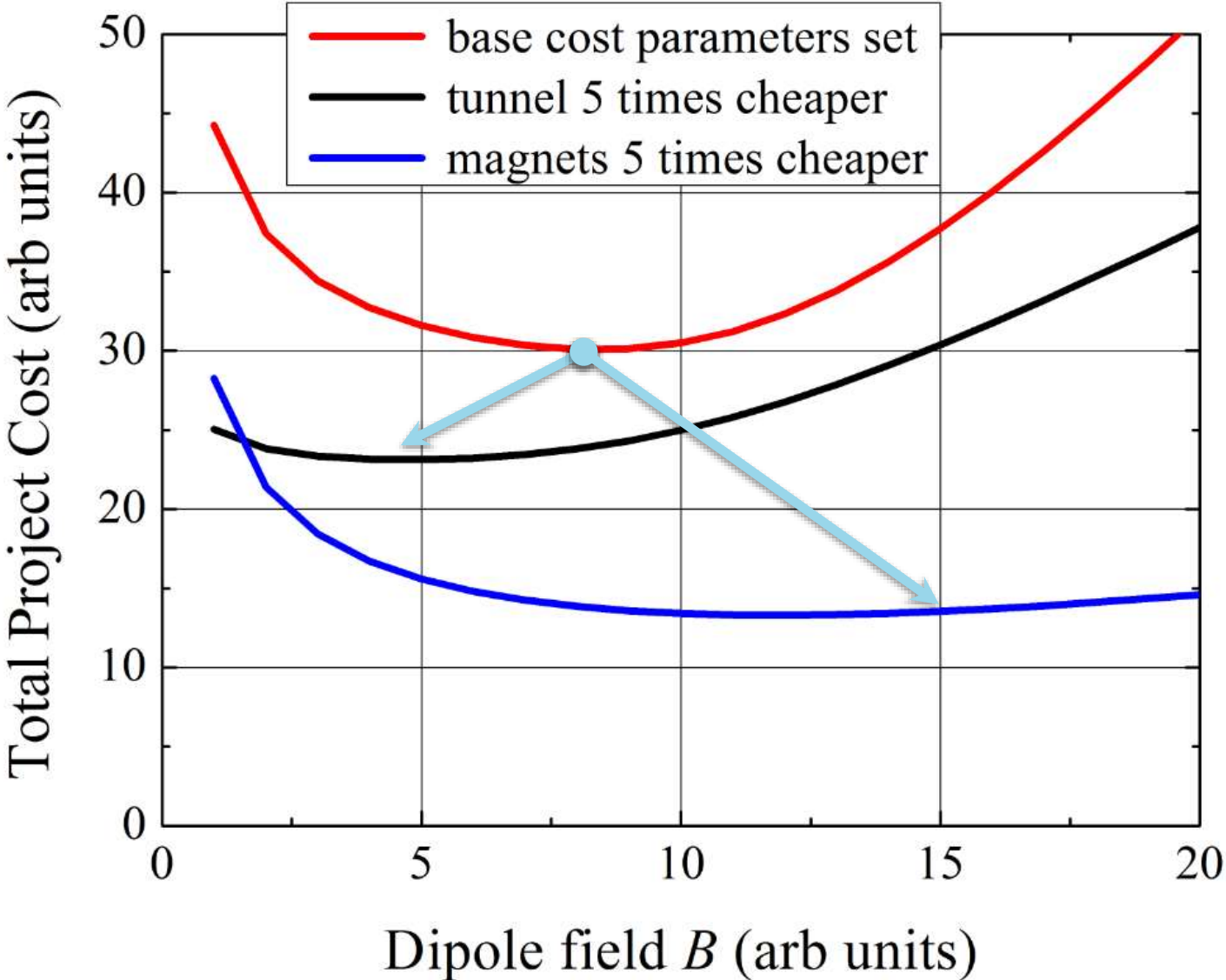
$$\rightarrow \mathcal{L} \sim \frac{Rad}{E}$$

$$N_{RW} \equiv \tau_{RW} f_0 = \frac{\sqrt{2\pi}(E_p/e)a^3}{I_B Z_0 \langle \beta \rangle} \sqrt{\frac{(1 - \Delta v)\sigma_W}{cR^3}}$$

$$N_{thr} = 1.24 \times 10^{10} \times \sqrt{\frac{\sigma_s}{0.1 \text{ m}} \frac{E}{3 \text{ TeV}} \frac{v_s}{0.005}}$$

$$\times \left(\frac{a}{0.9 \text{ cm}} \right)^3 \frac{520 \text{ km}}{c} \times \frac{250 \text{ m}}{\langle \beta \rangle}$$

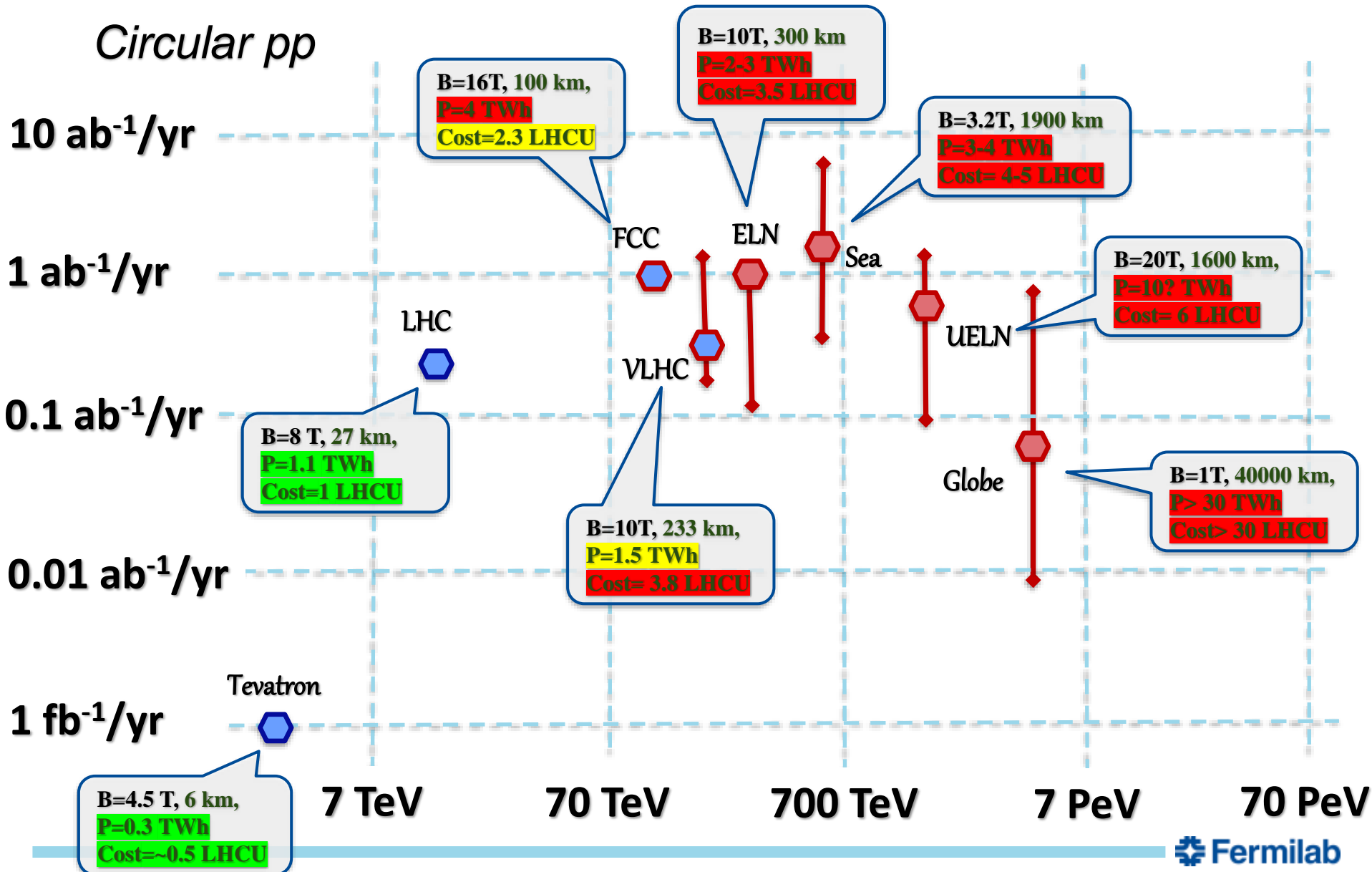
Qualitative Cost Dependencies - 100 TeV pp



* for illustration purposes only

pp Colliders: Lumi and Cost vs Energy

Circular pp



“Globaltron” and other ideas

- Cost saving magnets
 - superferric
 - permanent
- Better/cheaper conductors
 - Iron-based SC, graphene?
- Can they give factor of ~ 5 in $\text{\$/}(Tm)$?
 - (doubts so far)... leave it to AF7

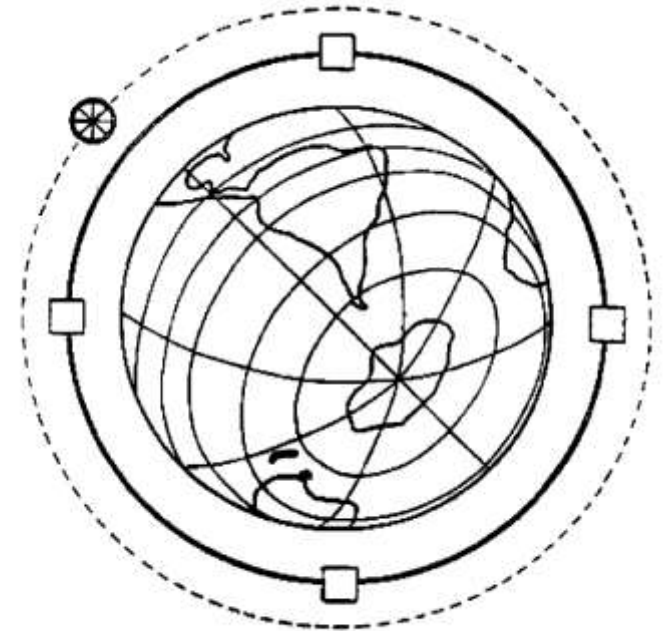
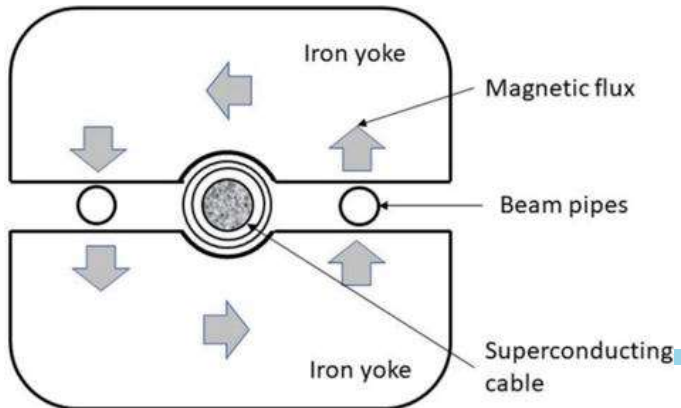
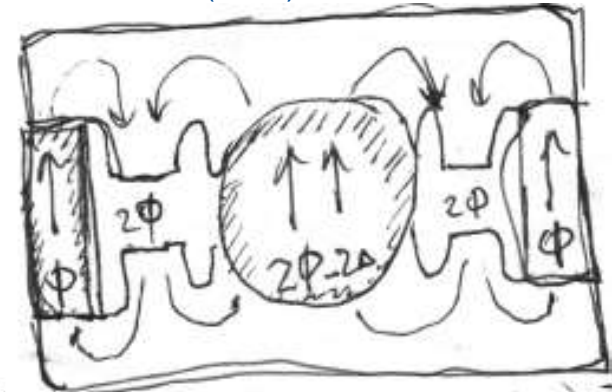
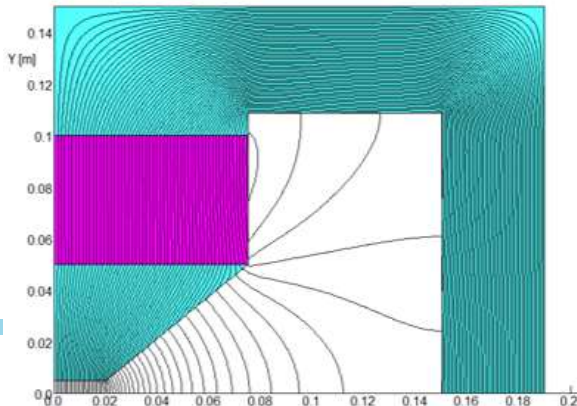


Figure 6. Enrico Fermi’s “ultimate accelerator” encircling Earth.

as Enrico Fermi’s ultimate accelerator or “globaltron” [46] (see Fig. 6), whose cost would exceed \$20,000B even under a modest estimate of \$0.5B per kilometer of a high-tech accelerator.



V.Kashikhin, FNAL beams-doc-8948 (2020)



Circular e+e- Colliders

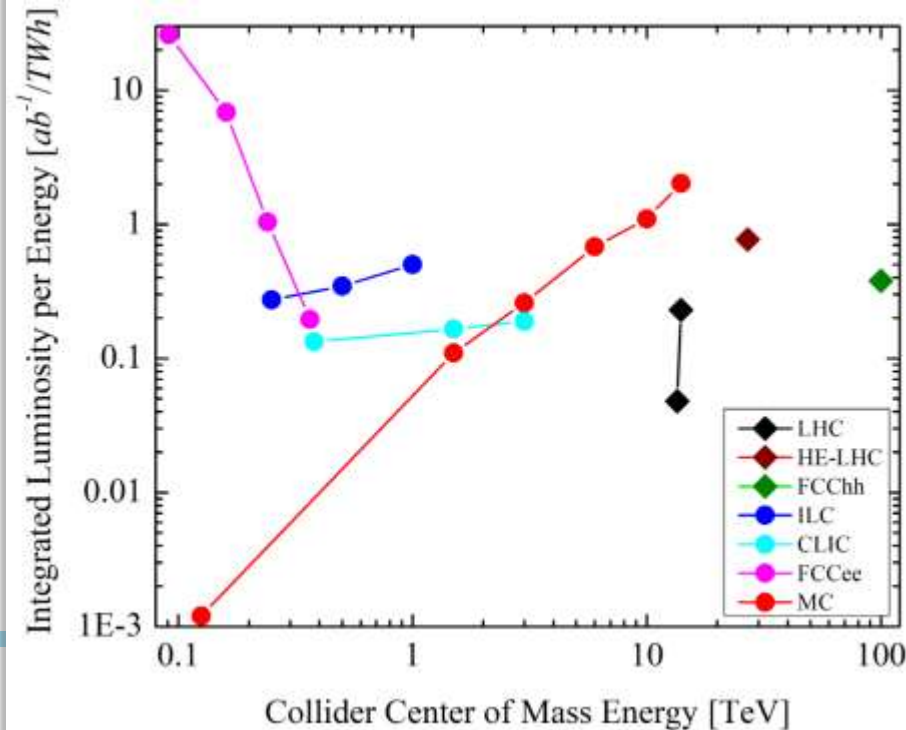
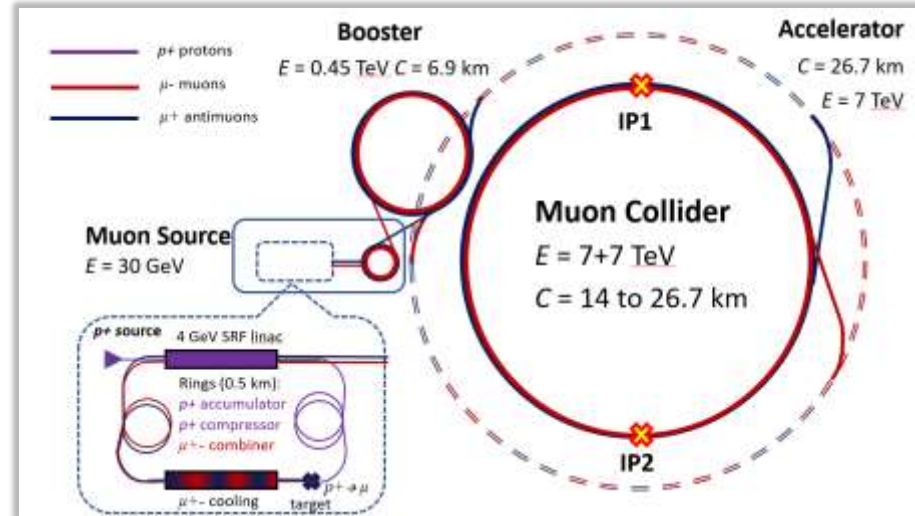
- Let's skip them... dead end... SR power

$$L = \frac{3}{16\pi r_e^2 (m_e c^2)} \frac{\xi_y P_T}{\beta_y^*} \rho \gamma^{-3}$$

- E.g. >0.5 TeV ring will be
 - Big (>200-300 km?)
 - Low luminosity O(10 fb-1/yr)
 - A lot of RF → expensive **>1.5-2 LHCU**

Circular Muon Colliders

- Parameter sets exist for 1.5, 3, 6, 10, 14 TeV
- Major advantages:
 - factor of x7 in E_{reach}
 - best power efficiency $\text{ab}^{-1}/\text{TWh}$
 - Traditional core technologies
- Major limitations:
 - Muon production
 - Muon cooling
 - Neutrino radiation



NATURE PHYSICS | www.nature.com/naturephysics

arXiv:2007.15684

Muon colliders to expand frontiers of particle physics

Jan 28, 2021

Muon colliders offer enormous potential for the exploration of the particle physics frontier but are challenging to realize. A new international collaboration is forming to make such a muon collider a reality.

K. R. Long, D. Lucchesi, M. A. Palmer, N. Pastrone, D. Schulte and V. Shiltsev

MC Luminosity

- $L \sim B$ field
- Assuming :
 - Enough muons can be produced
 - $L \sim \text{Power} \times \text{Energy}$
 - At some energy, neutrino radiation sets the limit
 - Ultimate lumi depends on suppression factor Φ

$$L = f_c \gamma n_b \cdot \frac{N_0^2}{4\pi\epsilon\beta^2}$$

\uparrow
 $\sim f_{\text{trap}} \cdot 300 \cdot B$

$$\dot{N} = N_0 \cdot n_b \cdot f_{\text{trap}} \sim 2 \cdot 10^9 \cdot 5 \sim 10^{12} / \text{s}$$

$$L \sim B \cdot P \cdot \gamma \cdot \frac{N_0}{\epsilon}$$

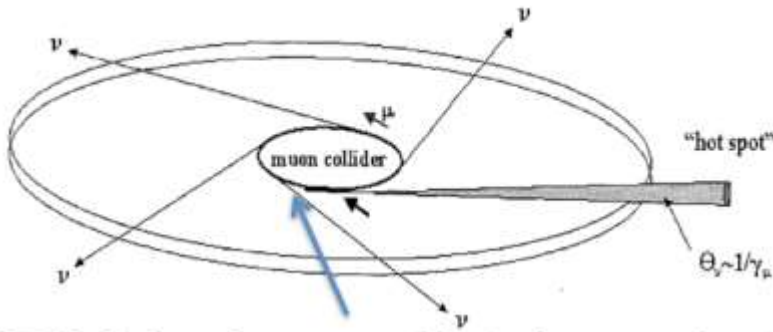
$$D(\text{dose}) \sim f_{\text{trap}} \cdot N_0 \cdot n_b \cdot \frac{\gamma^3}{\Phi} \quad D \sim \frac{P\gamma^2}{\Phi}$$

$$\text{Power} \sim \frac{D\Phi}{\gamma^2} \leq P_0$$

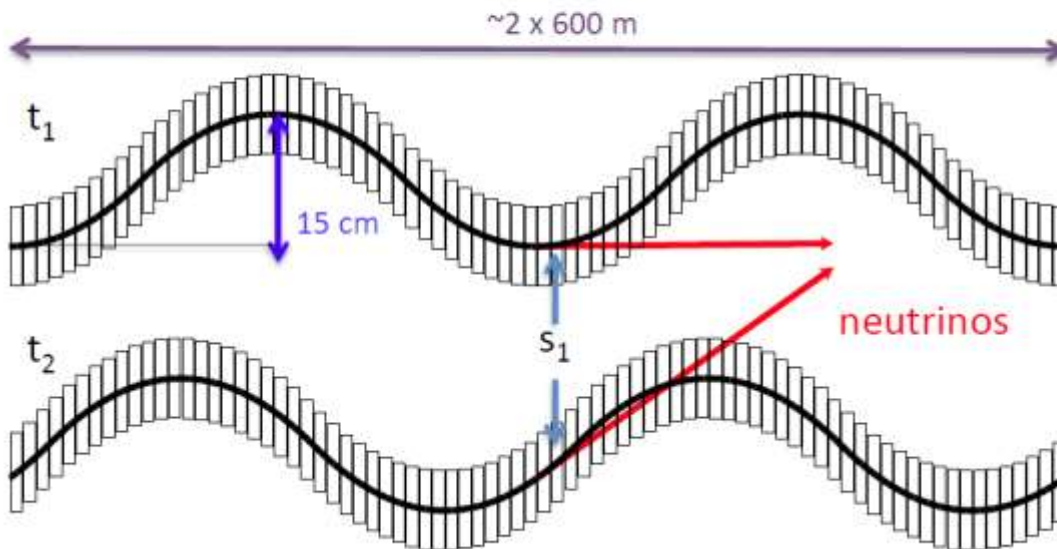
$$L \sim \frac{B}{f_{\text{trap}}} \cdot \frac{(D\Phi)^2}{\epsilon\gamma^4}$$

Neutrino Radiation Mitigation $\Phi \sim 100$ possible

disk width $\cong 4$ m at 30 km



Move collider ring components, e.g. vertical bending with 1% of main field



Opening angle ± 1 mradian

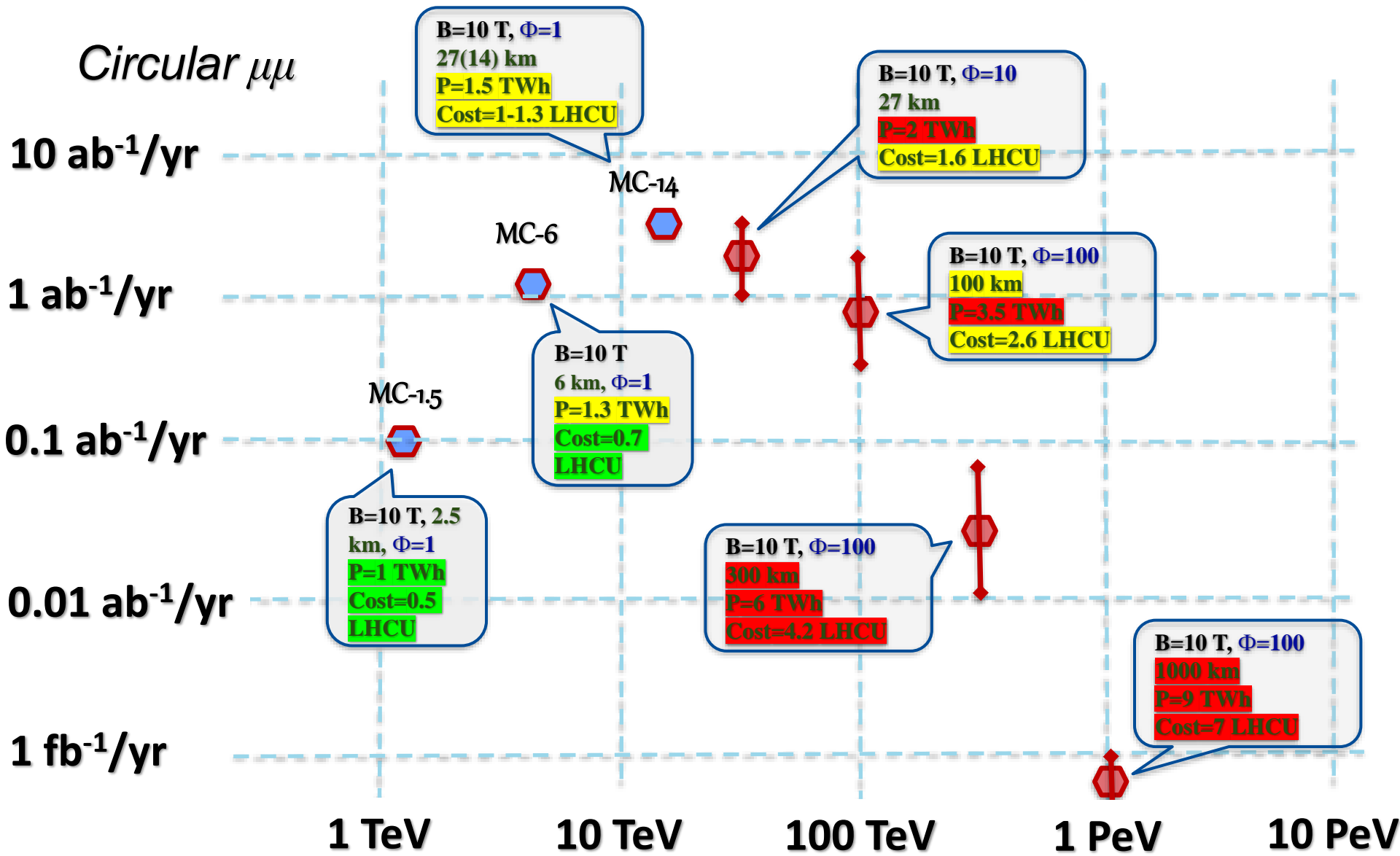
$O(100)$ larger than decay cone
 \Rightarrow gain $O(100)$ in radiation

In straights, additional improvement in horizontal

Need to study impact on beam and operation, e.g. dispersion control

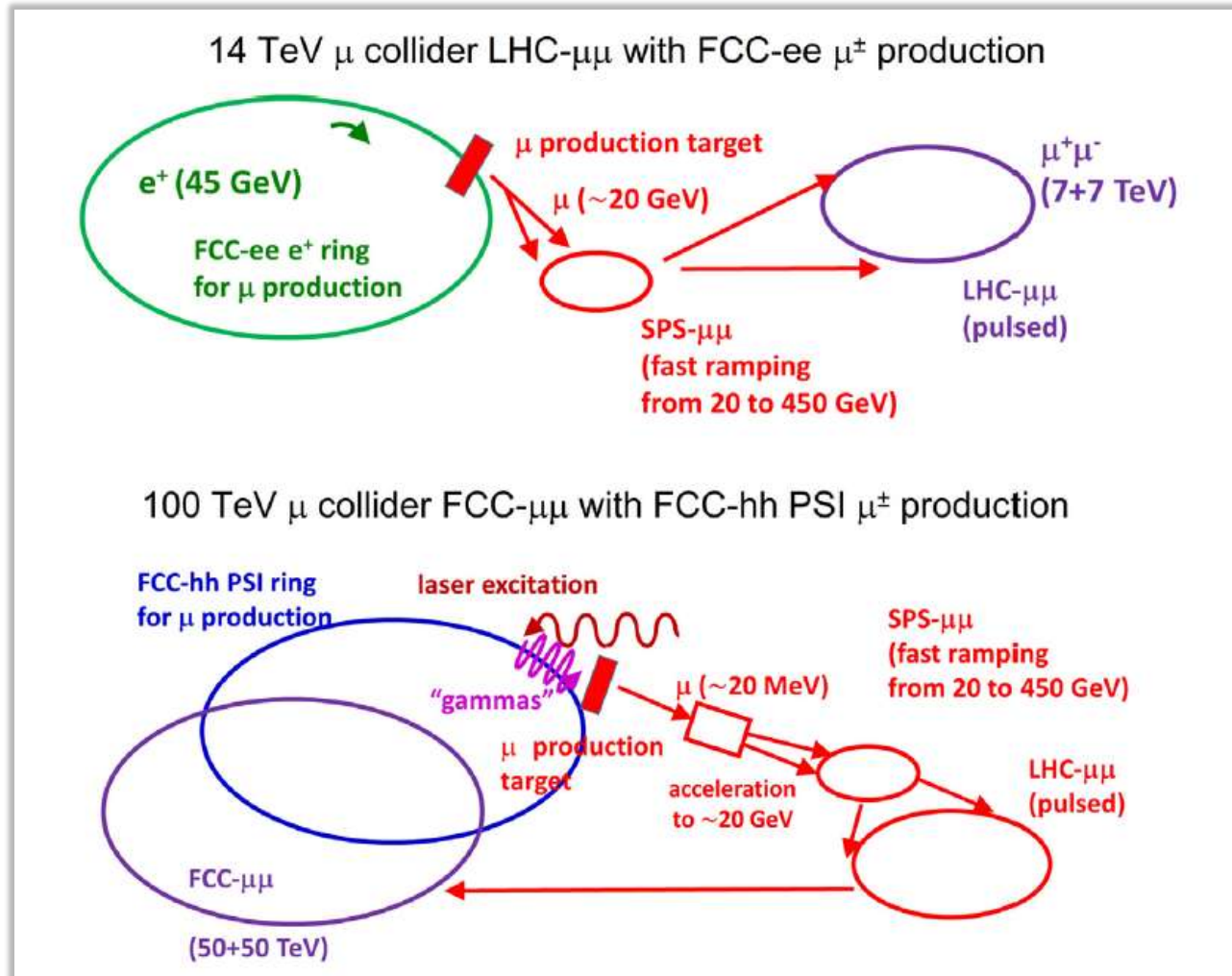
MC: *Lumi* and *Cost vs Energy*

Circular $\mu\mu$



New muon production schemes

- *LEMMA*
and
Gamma-Factory
 - small emittance
 - Intensity N/emm?
 - beam-beam
- Both require
(expensive?) aux.
 e^+ or p^+ machines



F. Zimmermann

Nuclear Inst. and Methods in Physics Research, A 909 (2018) 33–37

Linear *lepton* Colliders

- Mostly $e+e-/e-e-/γγ$
 - Muons possible, but μ -sources are expensive (and limited prod'n dN/dt)
 - Protons possible, but lose factor of 7 in effective cme energy reach in hh
 - *NC RF, SC RF, plasma, wakefields*

$$E_b = eGL$$

- Major advantages:

- No SR losses
- RF acceleration well developed

$$\mathcal{L} = (N_e n_b f_r) \left(\frac{1}{\sigma_y^*} \right) \left(\frac{N_e}{\sigma_x^*} \right) \frac{H_D}{4\pi}$$

- Major limitations:

- L scales with power, jitter/size and beamstrahlung
- plasma/wakefield acceleration is not fully matured yet (many unknowns - energy staging, $e+$, power, cost, etc)

$$\eta \equiv P_b / P_{\text{wall}}$$

$$N_e n_b f_r = \eta P_{\text{wall}} / e E_{\text{c.m.e.}}$$

$$L \propto \frac{\eta_{\text{linac}} P_{\text{wall}} N_\gamma}{E \sigma_y}$$

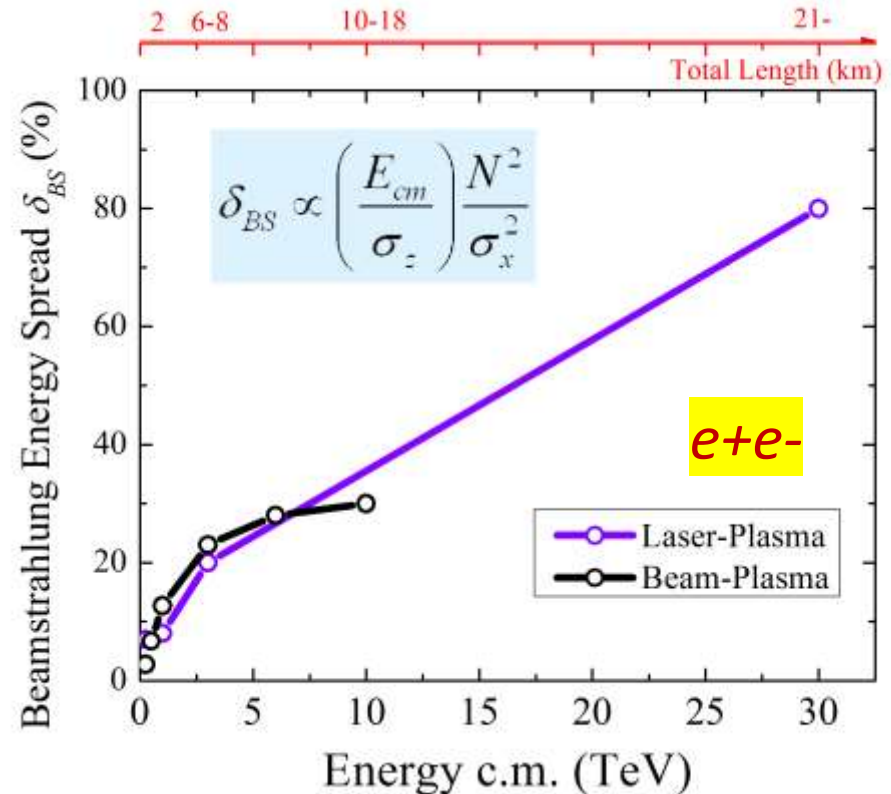
(luminosity spectrum)

$$N_\gamma \simeq \frac{2\alpha r_e N}{\sigma_x}$$

$ee/\gamma\gamma$ or $\mu\mu$ Linear Collider Luminosity

see detail analysis in eg D.Schulte, *Rev.Accel.Sci.Tech.* 9 (2016): 209-233.

- Other considerations :
 - Positron production and acceleration in plasma
 - Can be solved by switching to $ee/\gamma\gamma$
 - Beamstrahlung
 - Can be solved by ultrashort bunches or switching to $ee/\gamma\gamma$ or $\mu\mu$
(see M.Peskin @ PLUB-II and Swapan C. talk today)
 - Instabilities in RF structures or plasma
 - Jitter/emittance control
 - Problems grow with more elements and smaller beams at IP \rightarrow limit at 1A

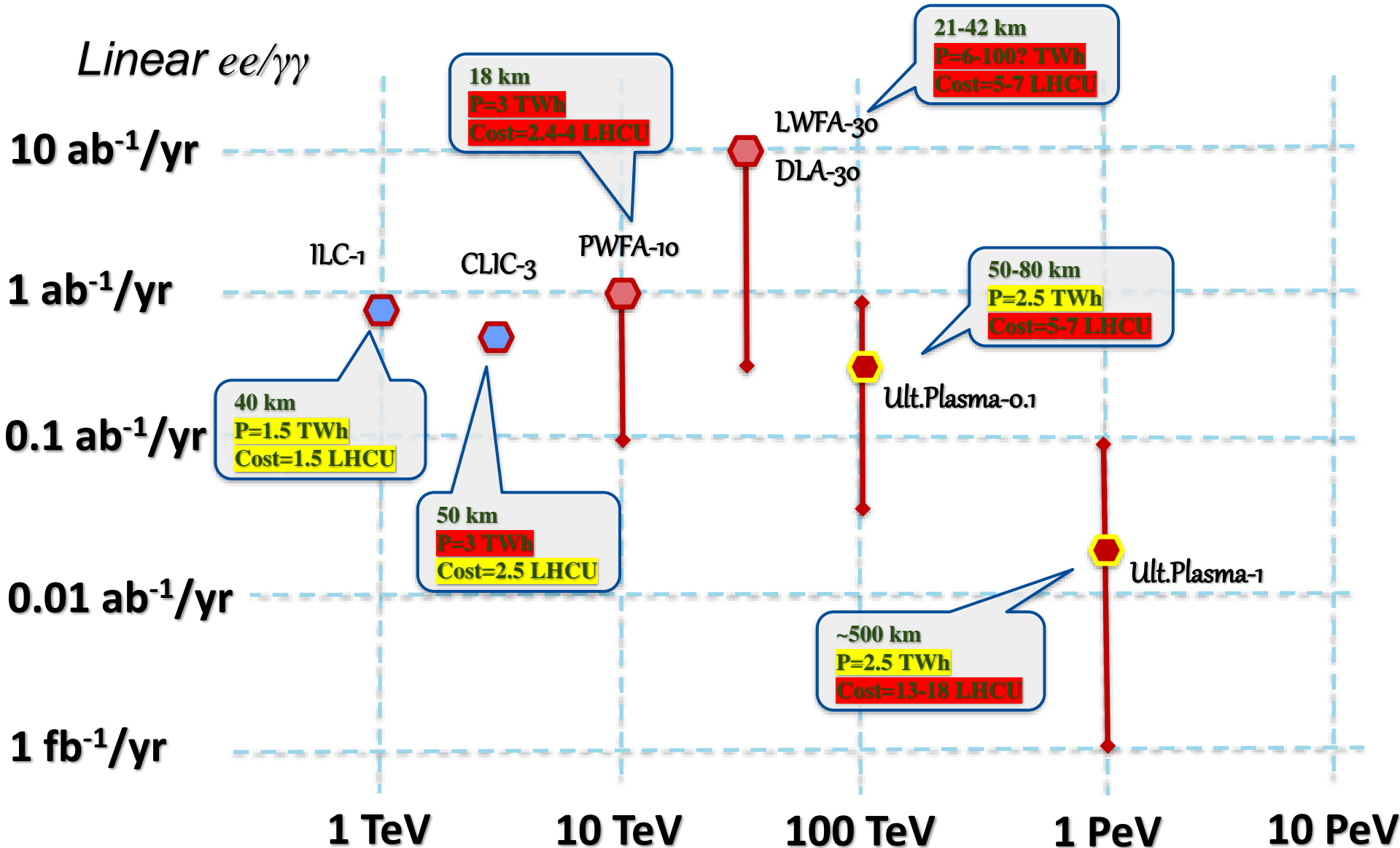


$$\delta_B \approx \frac{24}{3\sqrt{3}\pi^{3/2}} \frac{r_e^3 \gamma N_b^2}{\sigma_z (\sigma_x^* + \sigma_y^*)^2} \approx \frac{24}{3\sqrt{3}\pi^{3/2}} \frac{r_e^3 \gamma N_b^2}{\sigma_z \sigma_x^{*2}}$$

$$\mathcal{L} \propto \frac{n_\gamma^{3/2}}{\sqrt{\sigma_z}} \frac{1}{\sigma_y} N n_b f r. \quad \text{milab}$$

(T.Raubenheimer, PRSTAB 2000)

Linear RF and Plasma: *Lumi* and *Cost vs Energy*



Exotic Colliders

- Acceleration in structured media, eg CNTs or crystals (***only muons!!!***)
- Major advantages:
 - solid density \rightarrow 1-10 TV/m gradients
 - continuous focusing and acceleration (no cells, one long channel, particles get strongly cooled *betatron radiation*)
 - small size promises low cost
- Major limitations:
 - “blue sky”, O(10) papers, plans for proof-of-principle experiment *E336* @FACET-II (S.Corde, T.Tajima, et al)
 - how to drive Xtals? lasers, beams?
 - Cost is unknown, power is unknown, luminosity - (how low?)

$$E [\text{GV/m}] \approx 100 \sqrt{n_0 [10^{18} \text{ cm}^{-3}]}$$

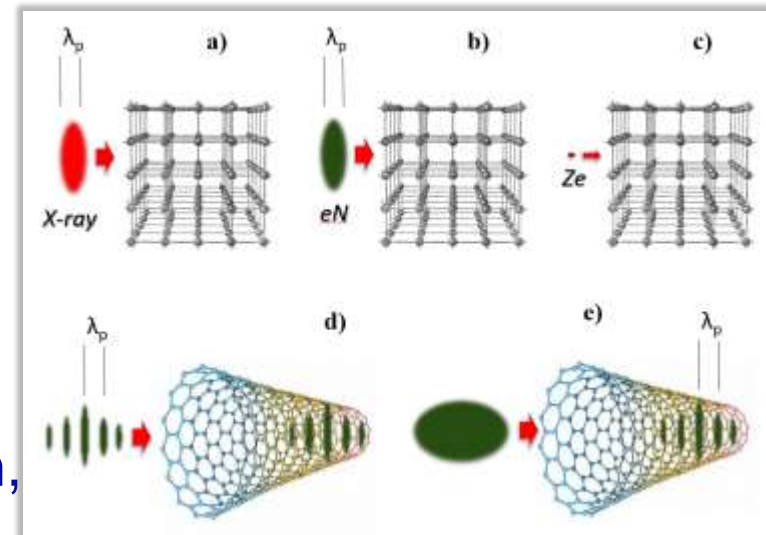
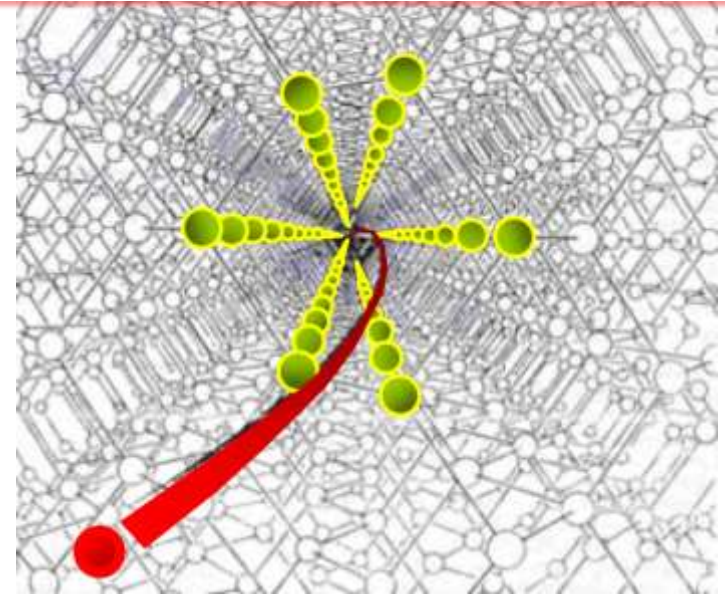


Fig. 2. Possible ways to excite plasma wakefields in crystals or/and nanostructures: (a) by short X-ray laser pulses; (b) by short high density bunches of charged particles; (c) by heavy high-Z ions; (d) by modulated high current beams; (e) by longer bunches experiencing self modulation instability in the media.

Exotic Colliders: Line of Thinking

E_{cm} Size is limited <10 km \rightarrow calls for the highest gradients \rightarrow crystals \rightarrow muons

$L = f \frac{N_1 N_2}{A}$ Luminosity calls for more particles in the smallest beam size

$A \sim 1 \text{ \AA}^2 = 10^{-16} \text{ cm}^{-2}$ This is the smallest beam size at IP

$P = f n_{ch} \cdot NE$ The power is limited <10 MW $\rightarrow N$ is small at high $E \rightarrow$ low L

XC Luminosity

- Considerations :

- Muons/bunch < Xtal electrons excited

- Employ many channels

- Limit beam power O(10MW)

- Combine $n_channels$ to gain L
via *crystal funnel* (? Is it possible)

$$L = f N^2 / A$$

$$100 \lambda_p \times \lambda_p^2$$

$$N_0 \sim 10^3$$

$$n_{ch} \sim 100$$

gain a factor of n_{ch}

$$P = f n_{ch} N E$$

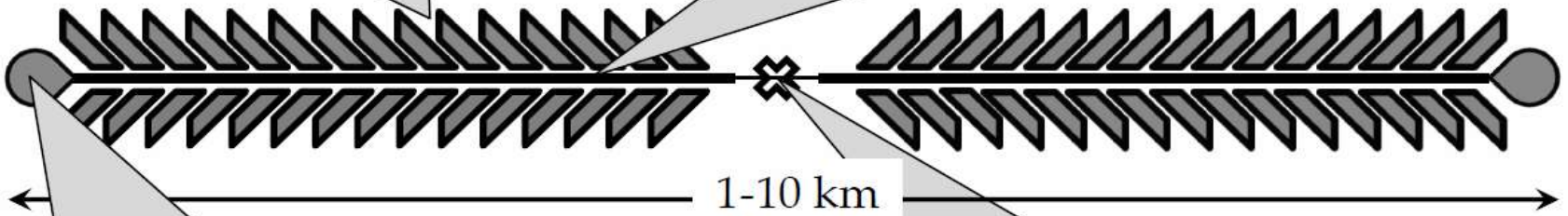
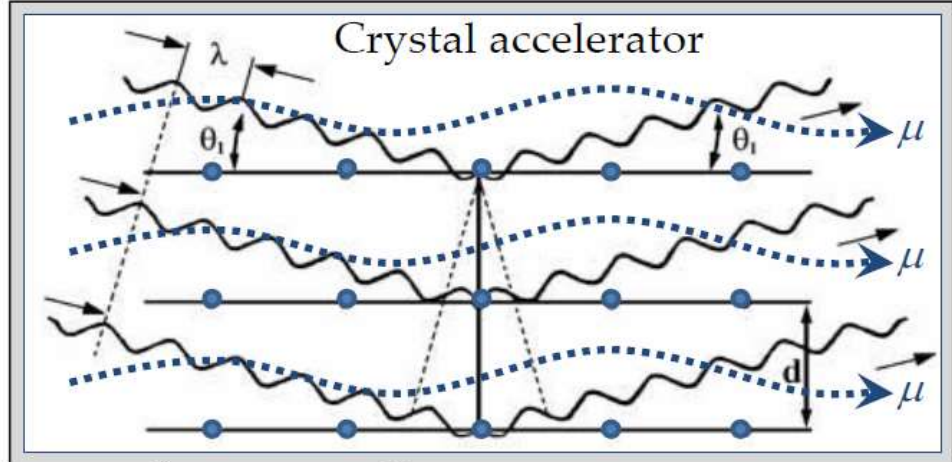
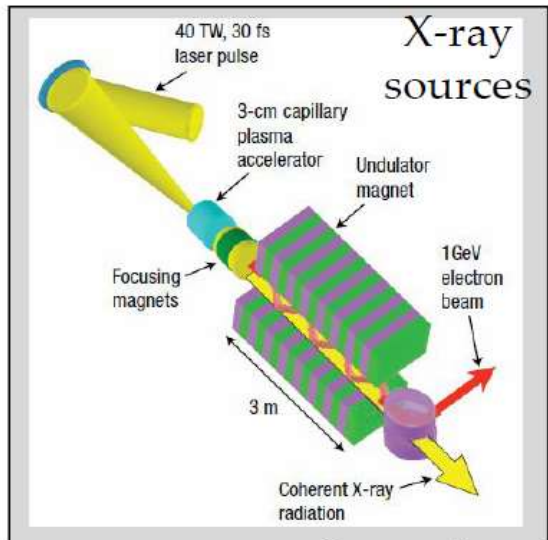
$$f = 10^6 \text{ Hz}$$

$$L [\text{sm}^{-2} \text{s}^{-1}] \approx 4 \times 10^{33-35} \frac{P^2 [\text{MW}]}{E^2 [\text{TeV}] f n_{ch} [10^8 \text{ Hz}]}$$

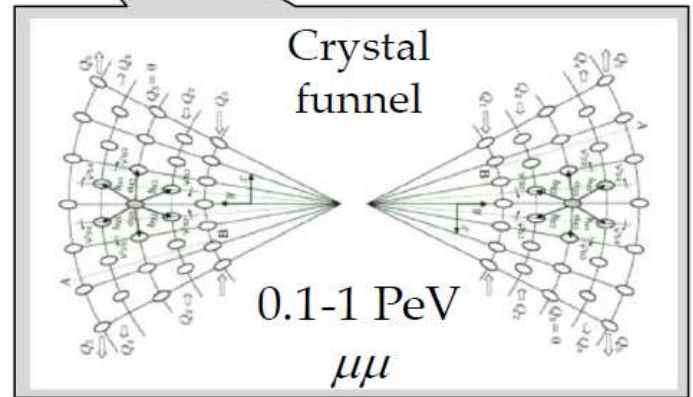
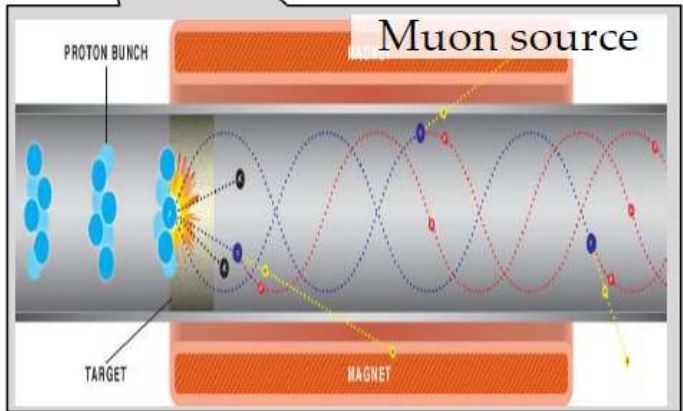
Xtal Collider

$n \sim 10^{22} \text{ cm}^{-3}$, $10 \text{ TeV/m} \rightarrow 1 \text{ PeV} = 1000 \text{ TeV}$

$n_{\mu} \sim 1000$, $n_B \sim 100$, $f_{rep} \sim 10^6$, $L \sim 10^{30-32}$

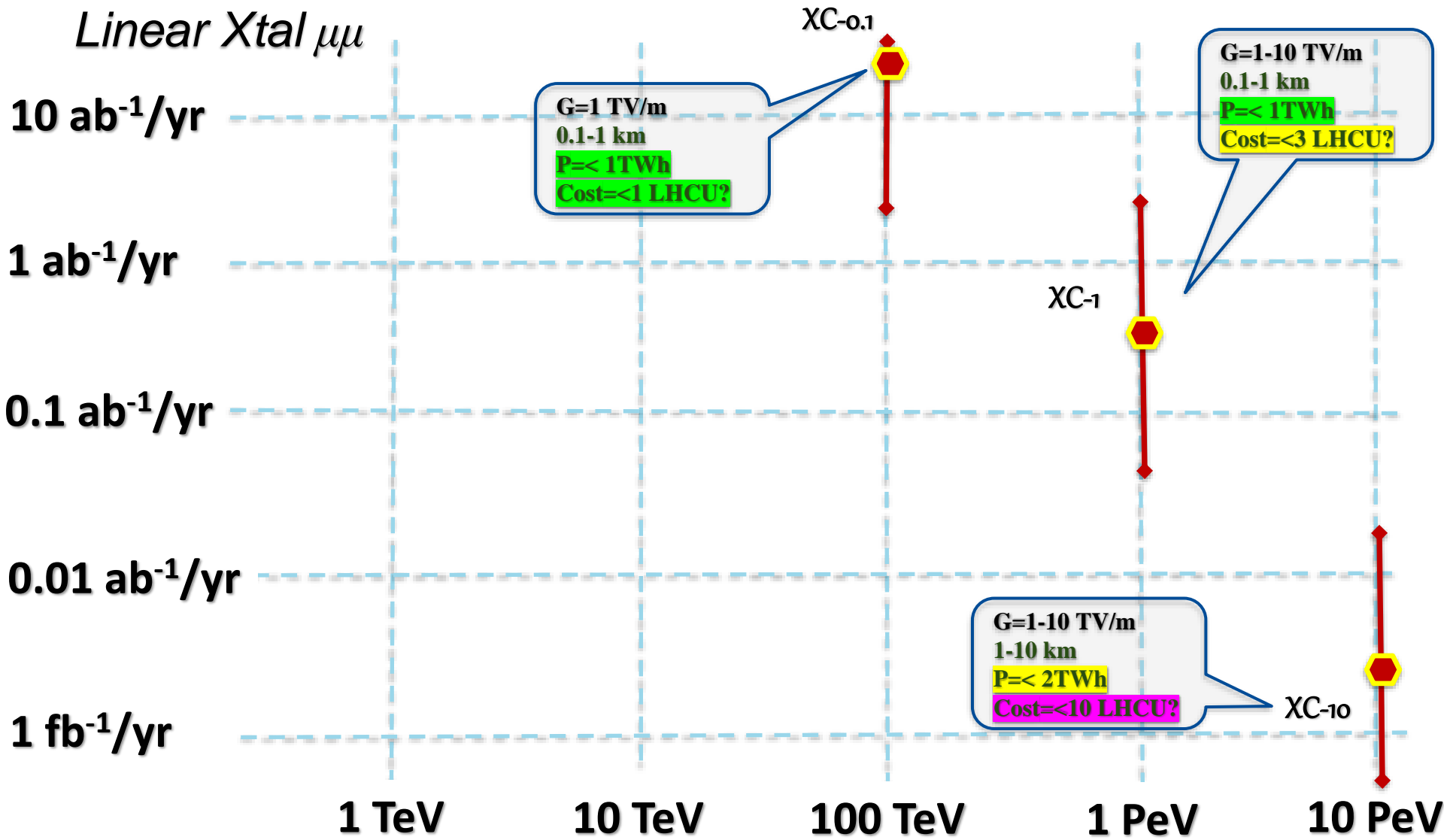


V.Shiltsev, Phys. Uspekhy 55 965 (2012)



Xtal Colliders: *Lumi* and *Cost vs Energy*

Linear Xtal $\mu\mu$



Main Conclusions:

- **For ultimate high energy colliders:**
 - Major thrust is *Energy*
 - Major concern/limit *is Cost*
 - Main focus is *Luminosity* and *Power*
- **Cost:**
 - Critically dependent on core acceleration technology
 - Existing injectors and infrastructure greatly help
- **High *Energy* means low *Luminosity* :**
 - Don't expect more than 0.1-1 ab^{-1}/yr at 30TeV-1 PeV
 - Assume *Power* limited to 1-3 TWh/yr

Main Conclusions (2):

- **For considered collider types:**
 - Circular pp – limit is close or below 100 TeV (14 TeV cm)
 - Circular ee – limit is $\sim 0.4-0.5$ TeV
 - Circular $\mu\mu$ – limit is between 30 and 100 TeV
 - Linear RF $ee/\gamma\gamma$ } – limit is between 3 and 10 TeV
 - Plasma $ee/\gamma\gamma$ }
 - Exotic crystal $\mu\mu$ – promise of 0.1-1 PeV, low Luminosity
- **Muons are particles of the future**

Helpful/cited references (next slide)

(Some) References:

1. $\alpha\beta\gamma$ model – V.Shiltsev, *JINST* 9 T07002 (2014).
2. RMP Colliders – V.Shiltsev, F.Zimmermann, *Rev.Mod.Phys.* (2021); see also arxiv
3. NatPhys MC – K.Long, et al, *Nature Physics* (2021), see also arxiv
4. Eloisatron – W.Barletta, in *AIP Conference Proceedings*, vol. 351, no. 1, pp. 56-67(1996).
5. Xtal collider – V.Shiltsev, *Physics Uspekhi*, v.55 (10), p.1033 (2012)
6. F.Zimmermann – *NIMA* 909 (2018): 33-37; see also ARIES Workshops summary
7. T.Raubenheimer - *Phys. Rev. ST Accel. Beams* 3, 121002 (2000)
8. D.Schulte Plasma Colliders – *Rev.Accel.Sci.Tech.* 9 (2016): 209-233.
9. Granada ALEGRO – Input to *EPPSU*, #007a (Granada, 2019)
10. *Modern Muon Physics: Selected Issues*, I.Strakovsky, et al (Nova, 2020)
11. 2019 Crystal Workshop - eds. T.Tajima et al *Beam Acceleration in Crystals and Nanostructures* (World Scientific, 2020)
12. *CPT*-theorem – V.Shiltsev *Mod. Phys. Lett. A*, vol. 26, No. 11 (2011) pp. 761-772
13. Cheap magnets – V.Kashikhin, Fermilab beams-doc-8948 (2021)

*Thank You for Your
Attention!*