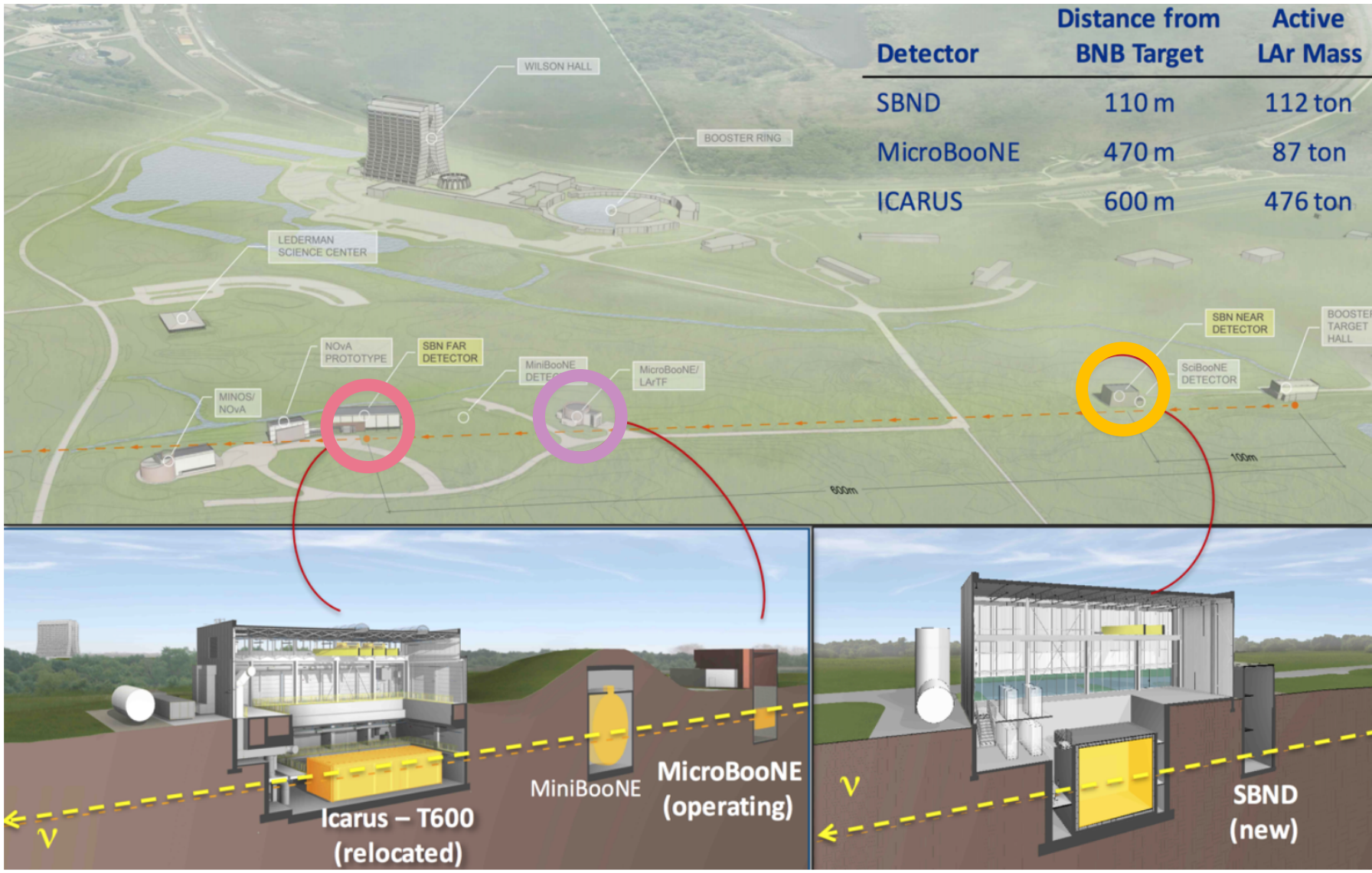


# SBNfit FC Update

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# SBN Program



- **SBN: 3 liquid argon detectors** located in the **Fermilab Booster Neutrino Beamline** with main goal to search for short baseline anomaly:
  - **ICARUS**
  - **MicroBooNE**
  - **SBND**
- Each detector shares the **same neutrinos source** and **same detector material/technology**-> measurement is **highly correlated** -> **reduce systematics**

# Extra Neutrinos

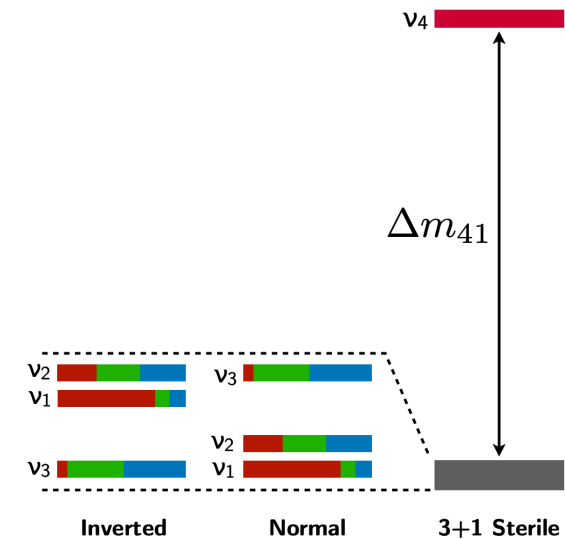
Minimal extension to the Three-Neutrino Paradigm is if there is an additional sterile neutrino.

This is referred to as the **3+1 paradigm** and currently what the current project is benchmarking against.

$$U = \begin{array}{c} \begin{array}{c} \nu_e \\ \nu_\mu \\ \nu_\tau \\ \nu_s \end{array} \begin{array}{c} \begin{array}{c} \nu_1 \quad \nu_2 \quad \nu_3 \end{array} \quad \begin{array}{c} \nu_4 \end{array} \end{array} \begin{bmatrix} \text{[Green Box]} & \text{[Green Box]} & \text{[Green Box]} & \text{[Red Box ?]} \\ \text{[Green Box]} & \text{[Green Box]} & \text{[Green Box]} & \text{[Red Box ?]} \\ \text{[Green Box]} & \text{[Green Box]} & \text{[Green Box]} & \text{[Red Box ?]} \\ \text{[Red Box ?]} & \text{[Red Box ?]} & \text{[Red Box ?]} & \text{[Red Box ?]} \end{bmatrix}$$

Oscillation probability via this mixing:

$$P_{\alpha\beta} = 4|U_{\alpha 4}|^2|U_{\beta 4}|^2 \sin^2 \left( 1.27 \frac{\Delta m_{41}^2 L}{E} \right)$$



$$P_{\alpha \rightarrow \beta} = \sin^2(2\theta)^2 \sin^2 \left( \frac{\Delta m^2 L}{4E} \right)^2$$

$\Delta m^2$ : frequency of oscillation

$\sin^2(2\theta)$ : amplitude of oscillation

**Only depends on 2 parameters!**

# More Neutrinos?

We will have to expand the U matrix seen previously to account these additional sterile neutrinos (3+x).

$$U = \begin{array}{c} \begin{array}{c} \nu_e \\ \nu_\mu \\ \nu_\tau \\ \nu_s \\ \nu_s \end{array} \begin{array}{c} \begin{array}{ccccc} \nu_1 & \nu_2 & \nu_3 & \nu_4 & \nu_4 \\ \begin{array}{ccc|c|c} \hline \text{[Green Block]} & & & ? & ? \\ \hline \end{array} & & & ? & ? \\ \hline \end{array} \end{array} \begin{array}{c} \text{.....X} \end{array}$$

..... X

depends on  
more  
parameters!

**3N+2: 7 parameters**  
**3N+3: 12 parameters**

Oscillation probability via this mixing will need to be expanded as well:

$$P_{\alpha\beta} = 4|U_{\alpha 4}|^2|U_{\beta 4}|^2 \sin^2 \left( 1.27 \frac{\Delta m_{41}^2 L}{E} \right)$$

Motivates improvement  
to the grid-based  
scanning method

# Objective: Provide FC correction to the Sensitivity Curves

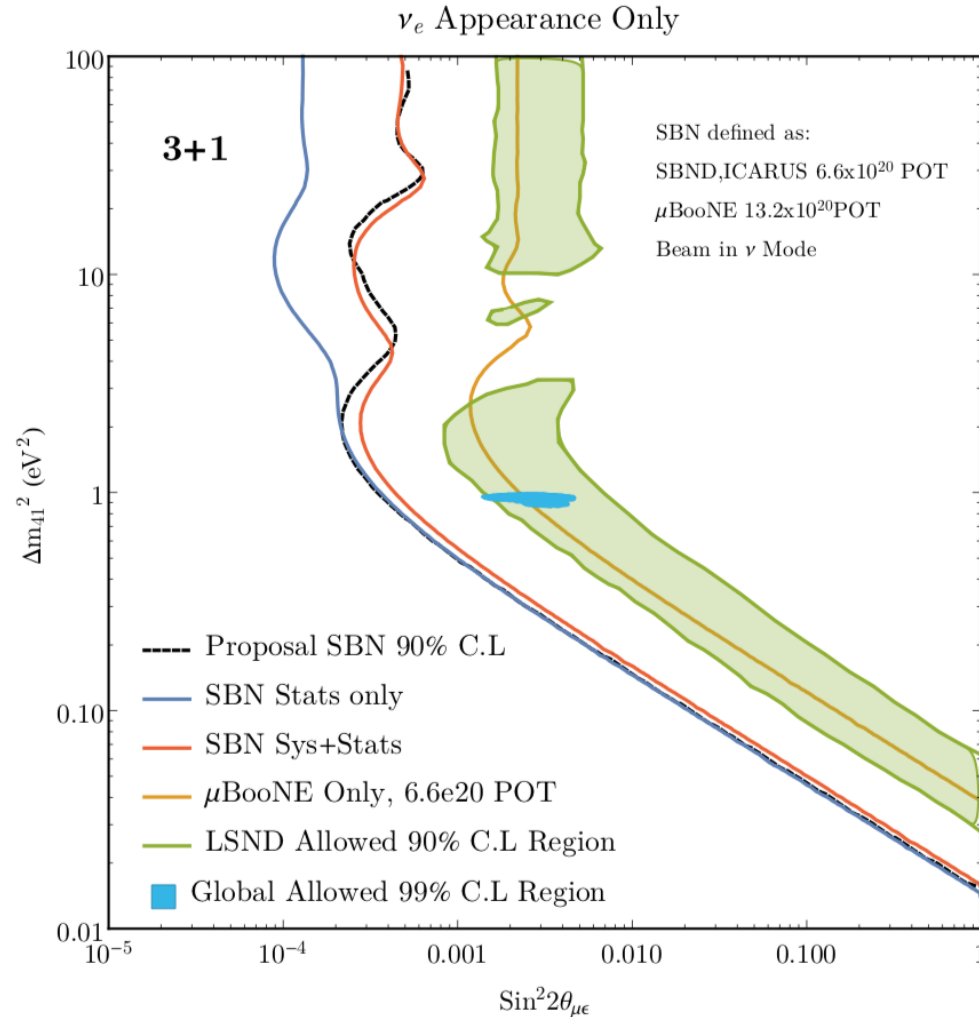
This is the (3+1) paradigm:

$$P_{\alpha \rightarrow \beta} = \sin(2\theta)^2 \sin\left(\frac{\Delta m^2 L}{4E}\right)^2$$

$\Delta m^2$ : frequency of oscillation

$\sin^2(2\theta)$ : amplitude of oscillation

Only depends on 2 parameters!



FC curves from this study will be added into this plot to increase the precision of the fits

# $\chi^2$ Calculation for $\nu$ Oscillation Sensitivity

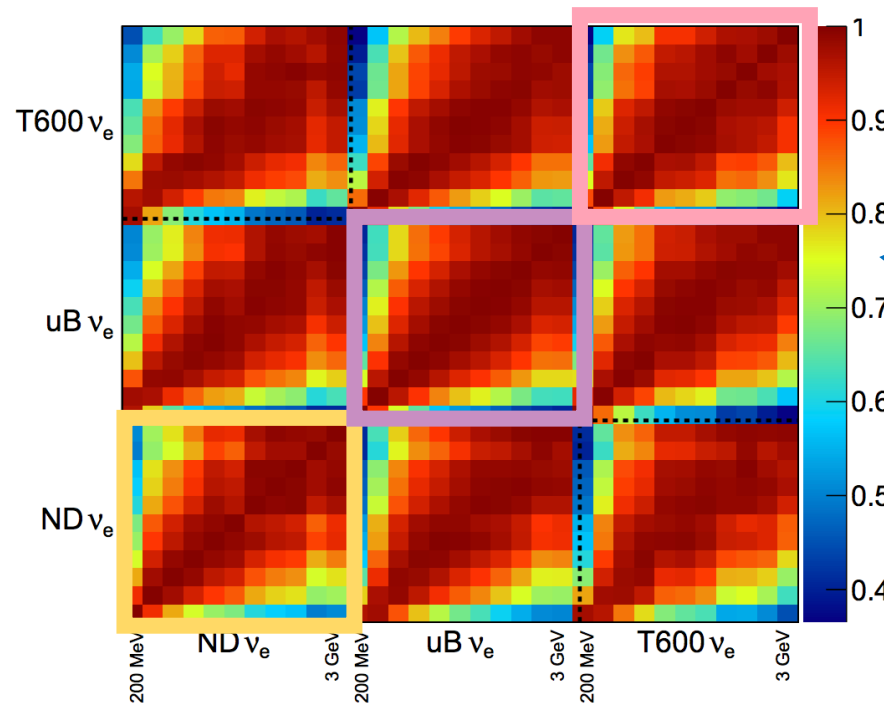
- Benchmarking:
  - SBNfit framework: one of the fitting framework used by SBN collaboration (Physics Group at Nevis Lab at Columbia University)
- The core of this procedure is to calculate a  $\chi^2$  surface in the  $(\Delta m_{41}^2, \sin^2(2\theta))$  oscillation parameter plane:

$$\chi^2(\Delta m_{41}^2, \sin^2 2\theta) = \sum_{i,j} [N_i^{null} - N_i^{osc}(\Delta m_{41}^2, \sin^2 2\theta)] (E_{ij})^{-1} [N_j^{null} - N_j^{osc}(\Delta m_{41}^2, \sin^2 2\theta)]$$

# Covariance Matrix

Sensitivity is calculated by computing a  $\chi^2$  surface in the  $(\Delta m_{41}^2, \sin^2(2\theta))$  oscillation parameter plane:

$$\chi^2(\Delta m_{41}^2, \sin^2 2\theta) = \sum_{i,j} [N_i^{null} - N_i^{osc}(\Delta m_{41}^2, \sin^2 2\theta)] (E_{ij})^{-1} [N_j^{null} - N_j^{osc}(\Delta m_{41}^2, \sin^2 2\theta)]$$



Systematics uncertainties are computed in form of combined covariance matrix of the 3 detectors **(56x56 matrix)**:  
**SBND**, **MicroBooNE**, **ICARUS**

[arXiv:1503.01520v1]

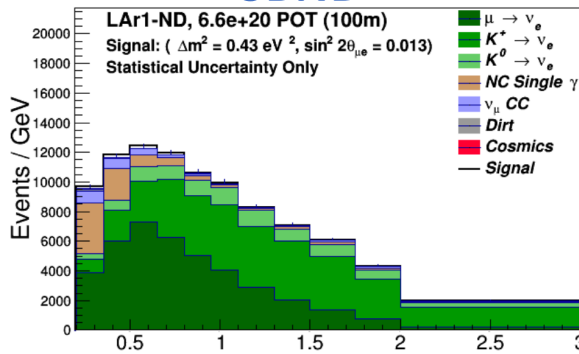
# Spectrum/Input Data

Sensitivity is calculated by computing a  $\chi^2$  surface in the  $(\Delta m_{41}^2, \sin^2(2\theta))$  oscillation parameter plane:

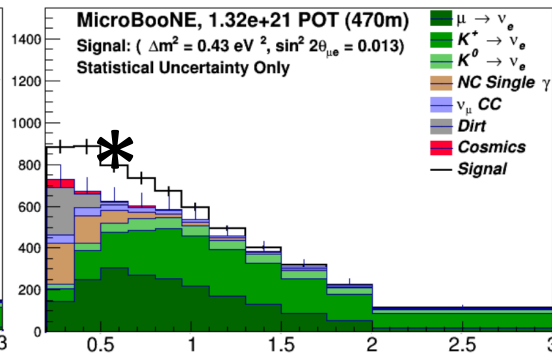
$$\chi^2(\Delta m_{41}^2, \sin^2 2\theta) = \sum_{i,j} [N_i^{null} - N_i^{osc} * (\Delta m_{41}^2, \sin^2 2\theta)] (E_{ij})^{-1} [N_j^{null} - N_j^{osc}(\Delta m_{41}^2, \sin^2 2\theta)]$$

$$P_{\alpha \rightarrow \beta}^* = \sin(2\theta)^2 \sin\left(\frac{\Delta m^2 L}{4E}\right)^2$$

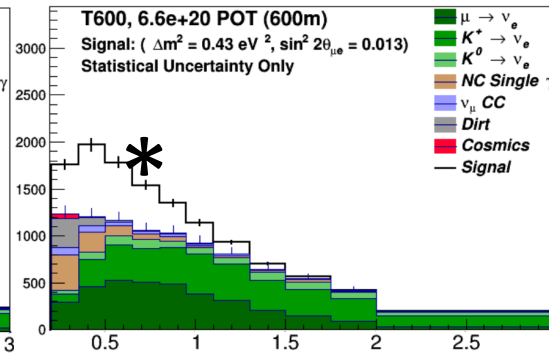
## SBND



## MICROBOONE



## ICARUS



Reconstructed Neutrino Energy (GeV)

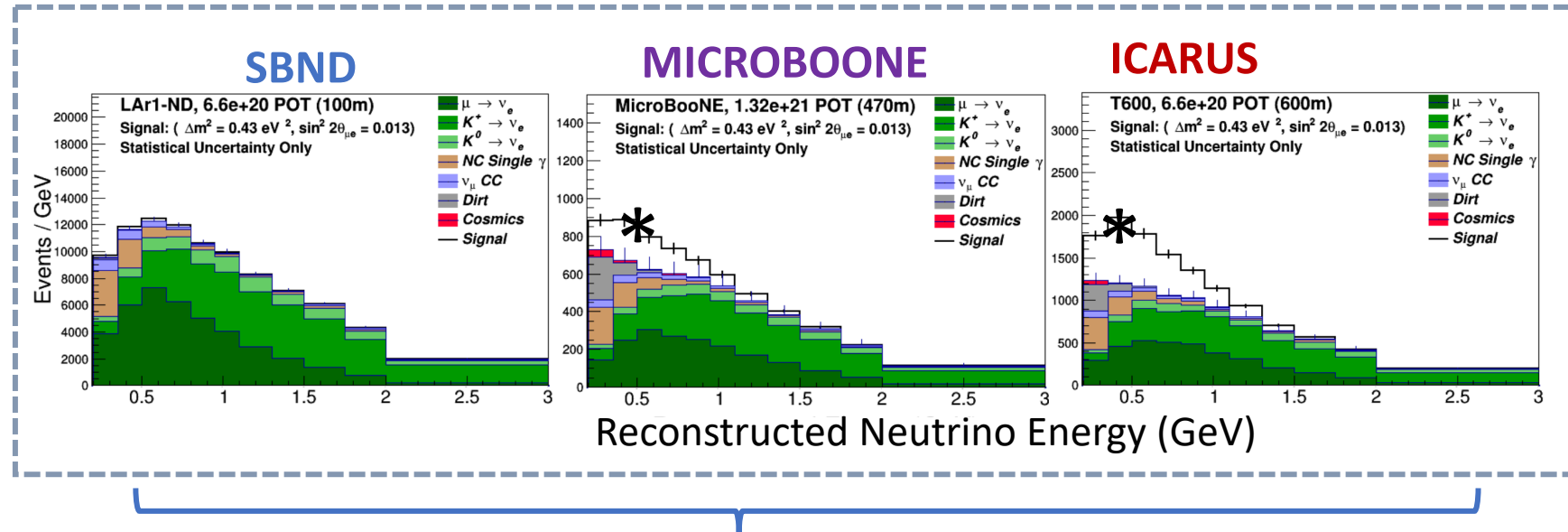
$\Delta m^2$ : frequency of oscillation  
 $\sin^2(2\theta)$ : amplitude of oscillation

\*Oscillation spectrum  
at Best Fit Point

[arXiv:1503.01520v1]



# Bringing in MFA Model (Tom, David)



We calculate the oscillated spectrum (\*) at each grid point that depends on the frequency (mass) and the amplitude (angle)

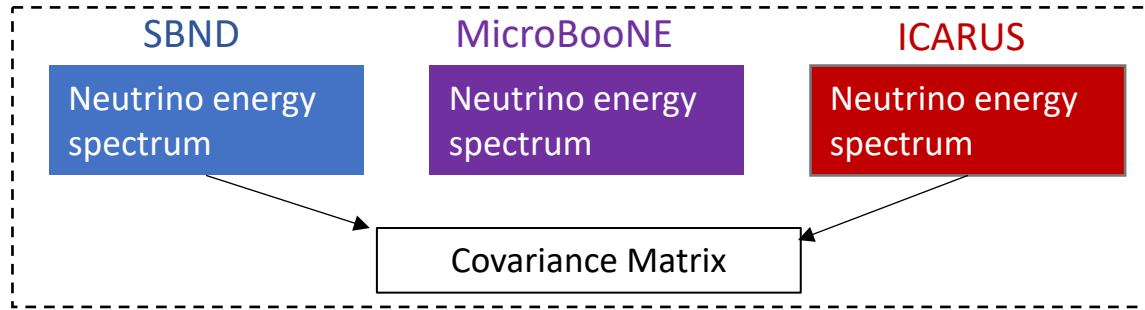
Bin contents of these oscillated spectrum at each grid point are concatenated into a 56 length size vector

Create MFA model which field-geometry dimension depends on the grid size (Ngridpoints).

Bin content represents the science variable -> 56 science variables.

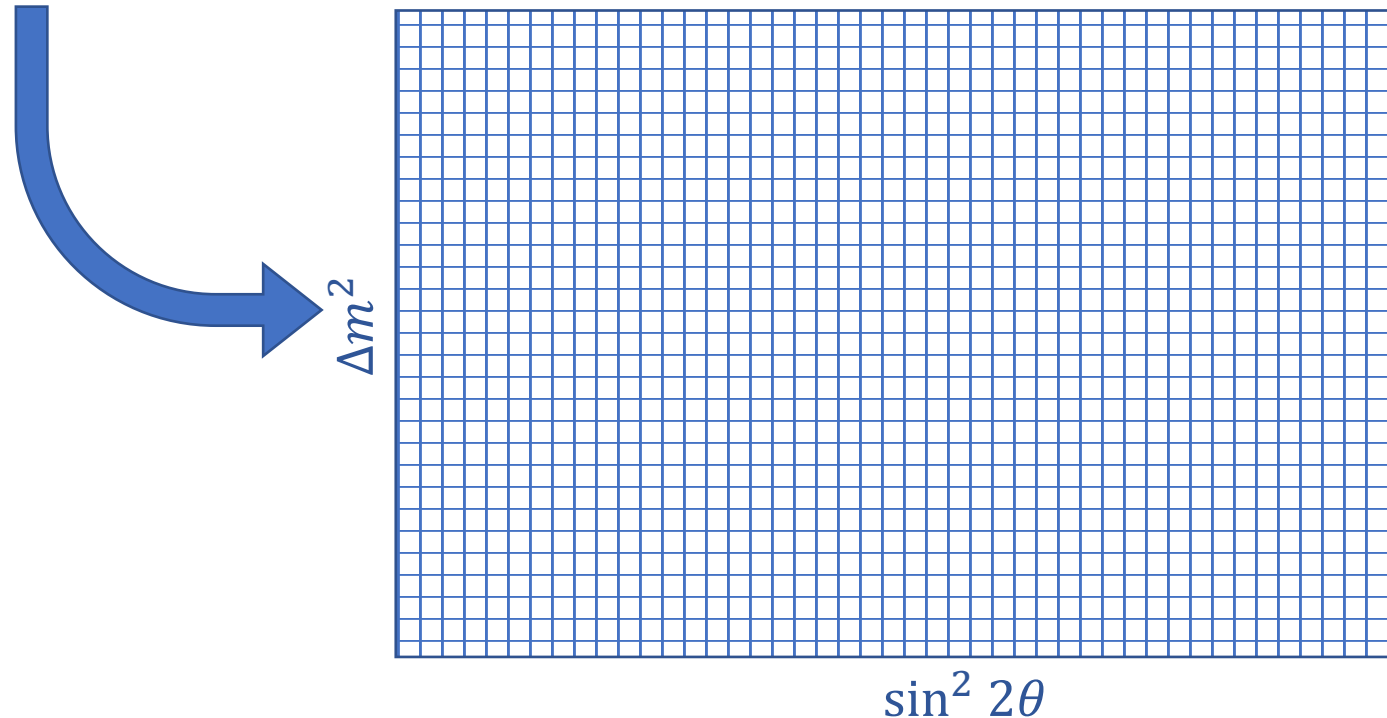
Still ongoing: validating the model. Accuracy of the MFA model not as good as previous implementation

# $\chi^2$ Calculation for $\nu$ Oscillation Sensitivity

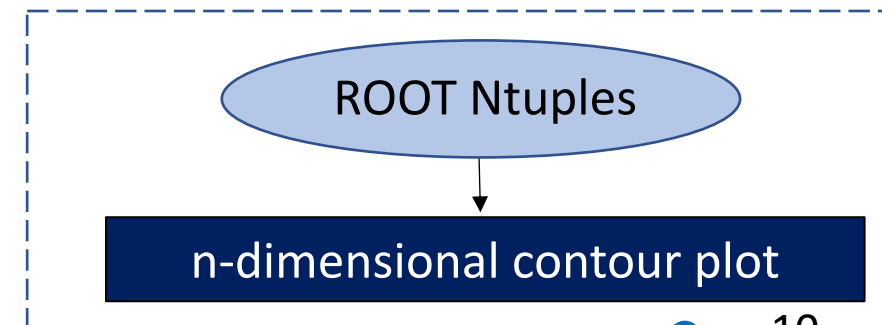


Perform  $\chi^2$  calculation at each **oscillation parameter space point** where we generate  $N$  number of toy experiments (Nuniv) – Feldman Cousins procedure

Input



Output



# FC Procedure Pseudo Code (old implementation)

Given number of universes  $N_{\text{univ}} > 0$ , discretized grid  $\mathcal{G} = \{\mathbf{p}_k : k = 1, \dots, N_{\text{gridpoints}}\}$ , and given fixed covariance  $\mathbf{M}$ .

**for**  $\mathbf{p}_k \in \mathcal{G}$  **do**

**for**  $i = 1, \dots, N_{\text{univ}}$  **do**

Fluctuate:  $\mathbf{d}_i \leftarrow \mathcal{P}(\mathbf{c}_k)$  psweudo-experiment sample of central data  $\mathbf{c}_k := \vec{\mathcal{S}}(\mathbf{p}_k)$

Initialize:  $\chi^2_{\min} \leftarrow \infty$ , and  $\mathbf{q}_{\min} \leftarrow \mathbf{p}_k$

**for**  $\mathbf{q}_l \in \mathcal{G}$  **do**

Evaluate:  $\chi^2(\mathbf{q}_l) := \chi^2(\mathbf{d}_i, \vec{\mathcal{S}}(\mathbf{q}_l), \mathbf{M})$

**if**  $\chi^2(\mathbf{q}_l) < \chi^2_{\min}$  **then**

                | Update:  $\chi^2_{\min} \leftarrow \chi^2(\mathbf{q}_l)$  and  $\mathbf{q}_{\min} \leftarrow \mathbf{q}_l$

**end**

**end**

Record:  $\Delta\chi^2(\mathbf{p}_k) \leftarrow \chi^2(\mathbf{d}_i, \mathbf{c}_k, \mathbf{M}) - \chi^2(\mathbf{d}_i, \vec{\mathcal{S}}(\mathbf{q}_{\min}), \mathbf{M})$  distance to mean.

**end**

**end**

From: Sven's overleaf document  
<https://www.overleaf.com/project/5f7205a341ace1000189420d>

- calculate the chi2 at each grid point for  $N_{\text{univ}}$
- find which grid point will give the minimum chi2 and assign that grid point as the best fit point.
- This best fit grid point and the chi2 minimum will then be used to build the sensitivity curves

**BF point is limited to the input grid point**

Algorithm 1: Classical Feldman-Cousins Algorithm.

# FC Procedure Pseudo Code (new implementation)

Given number of universes  $N_{\text{univ}} > 0$ , discretized grid  $\mathcal{G} = \{\mathbf{p}_k : k = 1, \dots, N_{\text{gridpoints}}\}$ , and given fixed covariance  $\mathbf{M}$ .

**for**  $\mathbf{p}_k \in \mathcal{G}$  **do**

**for**  $i = 1, \dots, N_{\text{univ}}$  **do**

Fluctuate:  $\mathbf{d}_i \leftarrow \mathcal{P}(\mathbf{c}_k)$  sample of central data  $\mathbf{c}_k := \vec{\mathcal{S}}(\mathbf{p}_k)$

Optimize: Find the (global) minimizer over  $\mathbf{q} \in \mathbb{R}^D$  of:

$$\mathbf{q}_{\min} \leftarrow \min_{\mathbf{q}} F(\mathbf{q}) \equiv \chi^2(\mathbf{d}_i, \vec{\mathcal{M}}(\mathbf{q}), \mathbf{M}) = \left( \mathbf{d}_i - \vec{\mathcal{M}}(\mathbf{q}) \right)^T \mathbf{M} \left( \mathbf{d}_i - \vec{\mathcal{M}}(\mathbf{q}) \right)$$

Record:  $\Delta\chi^2(\mathbf{p}_k) \leftarrow \chi^2(\mathbf{d}_i, \mathbf{c}_k, \mathbf{M}) - \chi^2(\mathbf{d}_i, \vec{\mathcal{M}}(\mathbf{q}_{\min}), \mathbf{M})$  distance to mean.

**end**

**end**

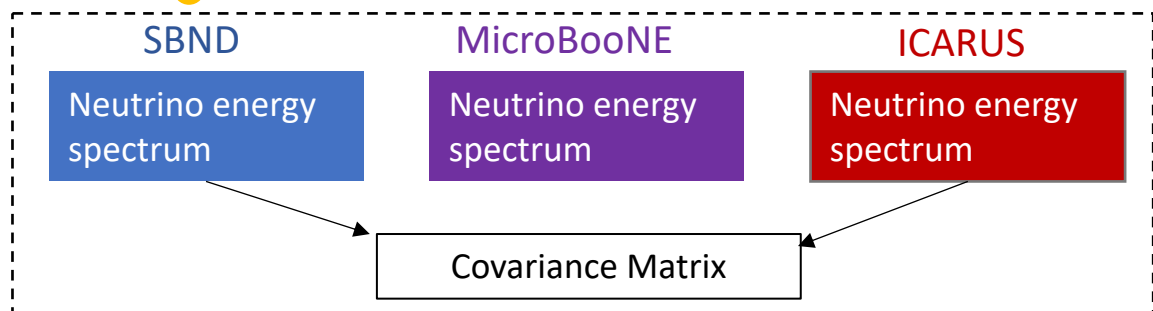
**Algorithm 2:** Optimization-Based Feldman-Cousins Algorithm.

**BF point is not limited to the input grid point!**

From: Sven's overleaf document  
<https://www.overleaf.com/project/5f7205a341ace1000189420d>

- In new procedure, use optimization to find the chi2 minimum and BF point
- The data is now encoded as MFA model
- Currently using cppoptlib libraries for the optimizer
- **Exploring the LBfgsbSolver to set the constraint for the minimization point**

# Complete Workflow



Encoded in MFA model

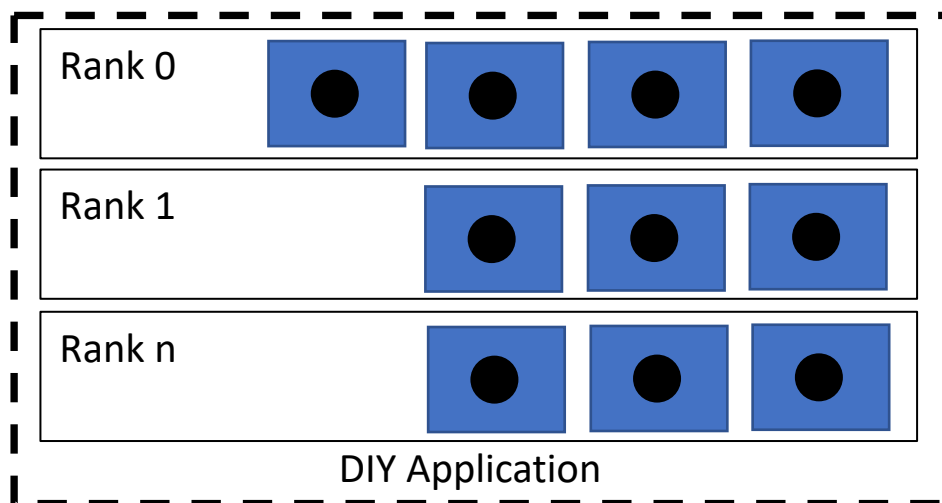
Perform  $\chi^2$  calculation at each oscillation parameter space point per toy experiments per rank in a node – Optimization-based Feldman Cousins procedure

Input

Read once

HPC tools: MPI to distribute the work load to all ranks through memory

\*MPI: Message Passing Interface



HPC tools: MPI to merge

Output

Convert to HDF5

n-dimensional contour plot

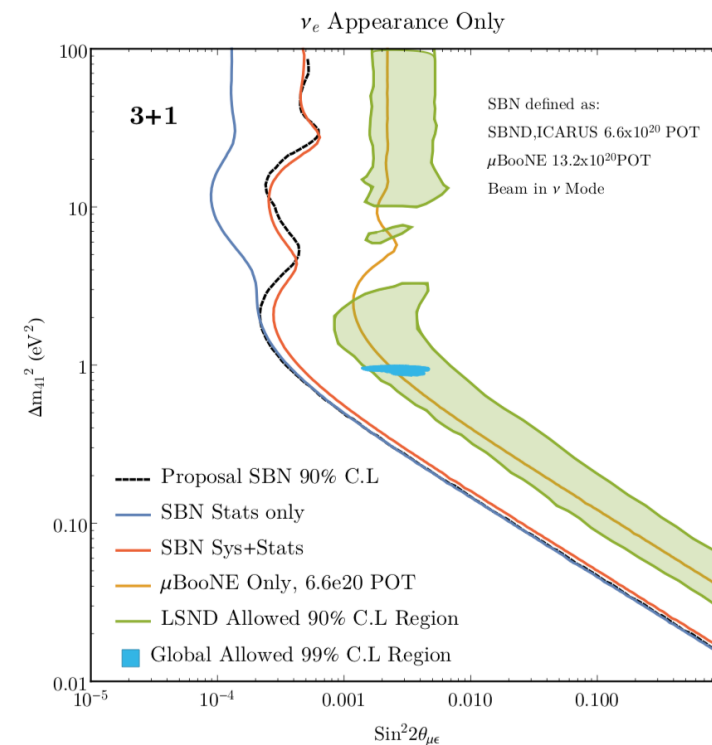
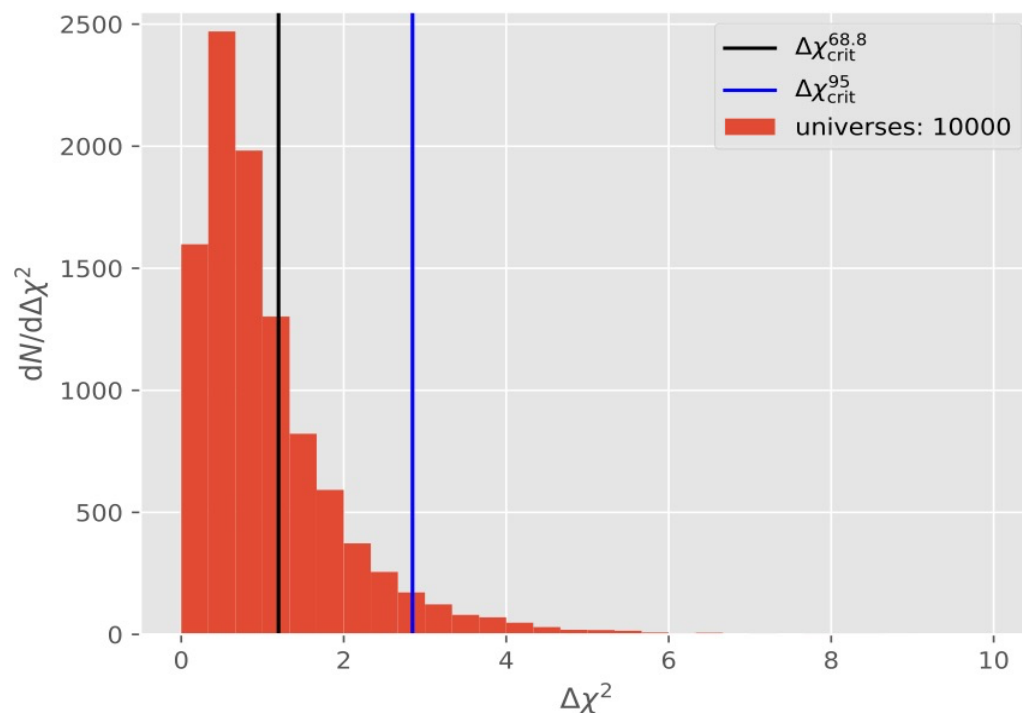
Machine	Cori phase 1 (Haswell)	Cori phase 2 (KNL)
CPU	Intel Xeon E5-2698 v3	Intel Xeon Phi 7250
Clockspeed	2.3 GHz	1.4 GHz
Cores per node	32	68

# Adding the FC curves to the Sensitivity Plot

Output

Convert to HDF5

n-dimensional contour plot



Phys. Rev. D 96, 055001 (2017)

FC calculation

# Summary

- A lot of progress made since last All Hands Meeting.
- In the process of implementing alternate approach to the grid scanning for higher dimensionality (7 parameters for  $3N+2 \rightarrow 3.2$  mil grid points! ).
  - Implementation of **MFA model**
  - Replacing grid scanning method with optimization using **libraries** from **cppoptlib**
  - Validation work for the MFA modeling and minimization are ongoing