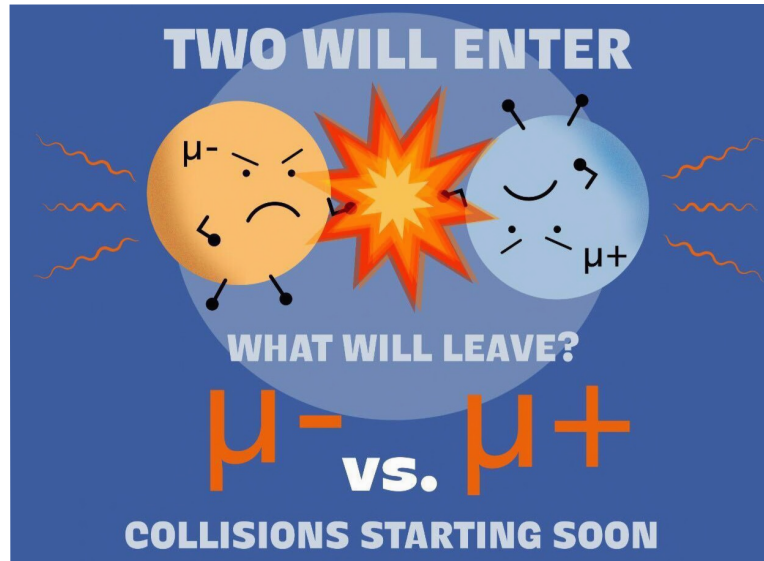


# Some Guidance for Muon Smashers



Tim Cohen (U Oregon)

Snowmass Muon Collider Forum, April 14

# How do we find BSM physics?



What experiment should we build?

Assume  
we have  
one of  
these...



What experiment should we build?

and as  
many ideas  
as we need...





What experiment should we build?

So we  
can focus  
on...

Show me the  
physics case!



# The Muon Smasher's Guide

Hind Al Ali<sup>1</sup>, Nima Arkani-Hamed<sup>2</sup>, Ian Banta<sup>1</sup>, Sean Benevedes<sup>1</sup>, Dario Buttazzo<sup>3</sup>, Tianji Cai<sup>1</sup>, Junyi Cheng<sup>1</sup>, Timothy Cohen<sup>4</sup>, Nathaniel Craig<sup>1</sup>, Majid Ekhterachian<sup>5</sup>, JiJi Fan<sup>6</sup>, Matthew Forslund<sup>7</sup>, Isabel Garcia Garcia<sup>8</sup>, Samuel Homiller<sup>9</sup>, Seth Koren<sup>10</sup>, Giacomo Koszegi<sup>1</sup>, Zhen Liu<sup>5,11</sup>, Qianshu Lu<sup>9</sup>, Kun-Feng Lyu<sup>12</sup>, Alberto Mariotti<sup>13</sup>, Amara McCune<sup>1</sup>, Patrick Meade<sup>7</sup>, Isobel Ojalvo<sup>14</sup>, Umut Oktem<sup>1</sup>, Diego Redigolo<sup>15,16</sup>, Matthew Reece<sup>9</sup>, Filippo Sala<sup>17</sup>, Raman Sundrum<sup>5</sup>, Dave Sutherland<sup>18</sup>, Andrea Tesi<sup>16,19</sup>, Timothy Trott<sup>1</sup>, Chris Tully<sup>14</sup>, Lian-Tao Wang<sup>10</sup>, and Menghang Wang<sup>1</sup>

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## Outline

I. Why Collide Muons?

II. Physics

III. Outlook

arXiv: 2103.14043

# The Muon Smasher's Guide

Hind Al Ali<sup>1</sup>, Nima Arkani-Hamed<sup>2</sup>, Ian Banta<sup>1</sup>, Sean Benevedes<sup>1</sup>, Dario Buttazzo<sup>3</sup>, Tianji Cai<sup>1</sup>, Junyi Cheng<sup>1</sup>, Timothy Cohen<sup>4</sup>, Nathaniel Craig<sup>1</sup>, Majid Ekhterachian<sup>5</sup>, JiJi Fan<sup>6</sup>, Matthew Forsslund<sup>7</sup>, Isabel Garcia Garcia<sup>8</sup>, Samuel Homiller<sup>9</sup>, Seth Koren<sup>10</sup>, Giacomo Koszegi<sup>1</sup>, Zhen Liu<sup>5,11</sup>, Qianshu Lu<sup>9</sup>, Kun-Feng Lyu<sup>12</sup>, Alberto Mariotti<sup>13</sup>, Amara McCune<sup>1</sup>, Patrick Meade<sup>7</sup>, Isobel Ojalvo<sup>14</sup>, Umut Oktem<sup>1</sup>, Diego Redigolo<sup>15,16</sup>, Matthew Reece<sup>9</sup>, Filippo Sala<sup>17</sup>, Raman Sundrum<sup>5</sup>, Dave Sutherland<sup>18</sup>, Andrea Tesi<sup>16,19</sup>, Timothy Trott<sup>1</sup>, Chris Tully<sup>14</sup>, Lian-Tao Wang<sup>10</sup>, and Menghang Wang<sup>1</sup>

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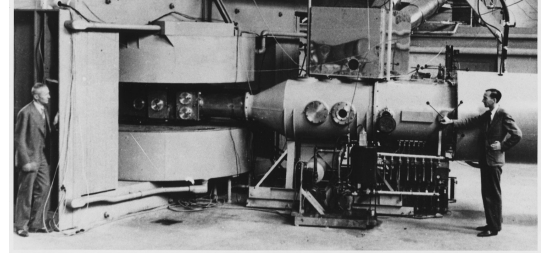
arXiv: 2103.14043

## Contents

<b>1</b>	<b>Introduction</b>	<b>3</b>
<b>2</b>	<b>Muons vs. Protons</b>	<b>6</b>
2.1	Muon annihilation . . . . .	6
2.2	Vector boson fusion . . . . .	9
2.3	Annihilation vs. VBF . . . . .	10
2.4	Signal vs. background . . . . .	12
<b>3</b>	<b>Muon Colliders Are Gauge Boson Colliders</b>	<b>13</b>
3.1	From the effective vector approximation to PDFs . . . . .	15
3.2	PDFs with broken electroweak symmetry . . . . .	16
3.3	Impact of subleading logs . . . . .	19
3.4	Finite mass effects . . . . .	22
<b>4</b>	<b>Physics</b>	<b>23</b>
4.1	Electroweak symmetry breaking . . . . .	24
4.2	Dark matter . . . . .	38
4.3	Naturalness . . . . .	44
<b>5</b>	<b>Complementarity</b>	<b>58</b>
5.1	EDMs . . . . .	58
5.2	Flavor . . . . .	60
5.3	Gravitational waves . . . . .	67
<b>6</b>	<b>Summary and Future Directions</b>	<b>69</b>
	<b>Appendix</b>	<b>72</b>
<b>A</b>	<b>Simplified Models</b>	<b>72</b>
A.1	Standard Model . . . . .	73
A.2	Supersymmetry . . . . .	74
A.3	Vector-like quarks . . . . .	79
A.4	Higgs portal . . . . .	80
A.5	Hidden valleys . . . . .	88
A.6	Axion-like particles . . . . .	89
	<b>References</b>	<b>90</b>

I. Why Collide Moons?

# Evolution of the microscope



Muon  
collider??



# What to collide?

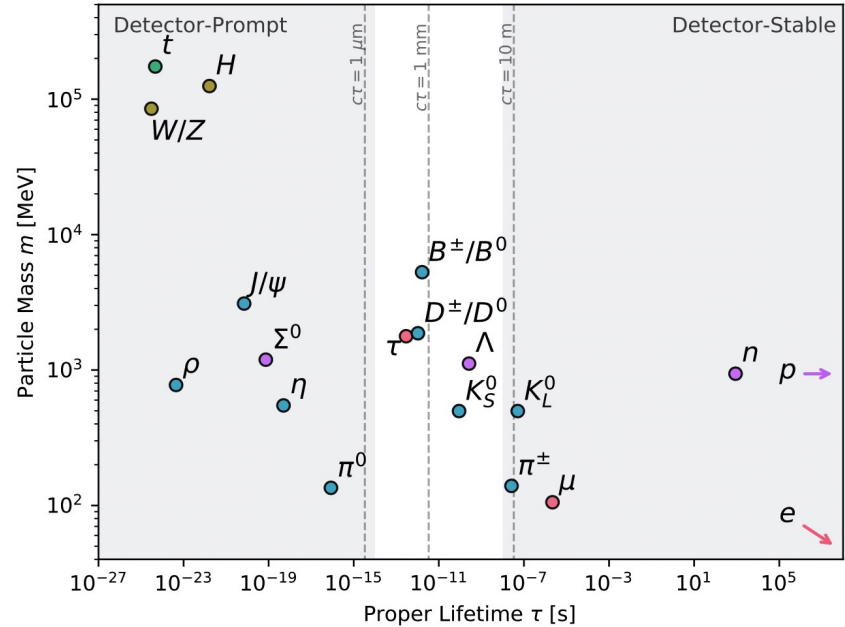
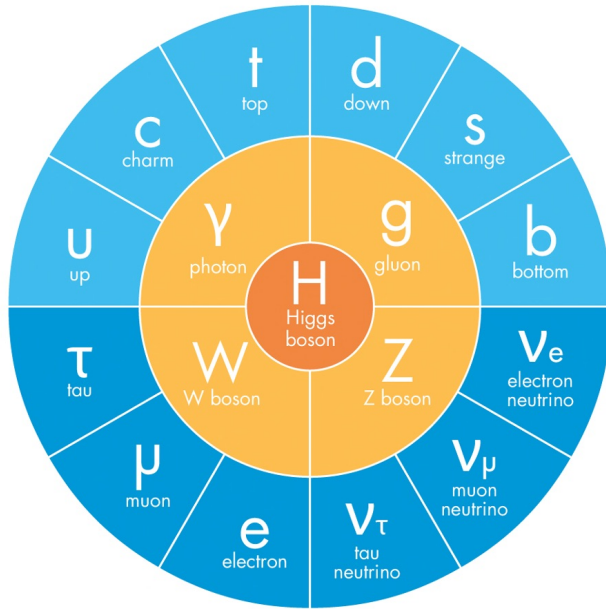
## THE STANDARD MODEL

FERMIONS (matter)

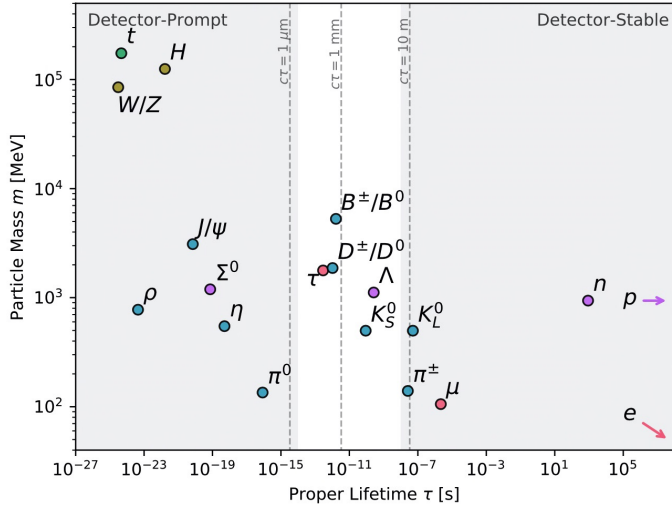
● Quarks ● Leptons

BOSONS (force carriers)

● Gauge bosons ● Higgs boson



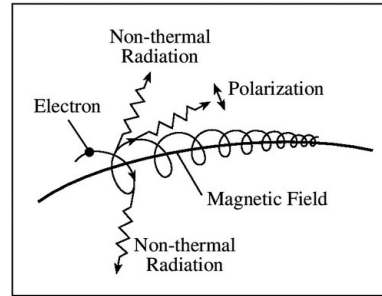
# What to collide?



- Charged



- Heavier is better

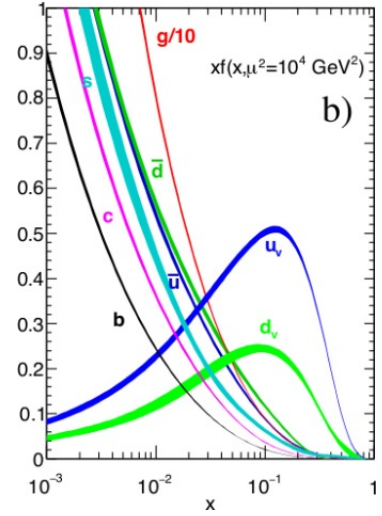
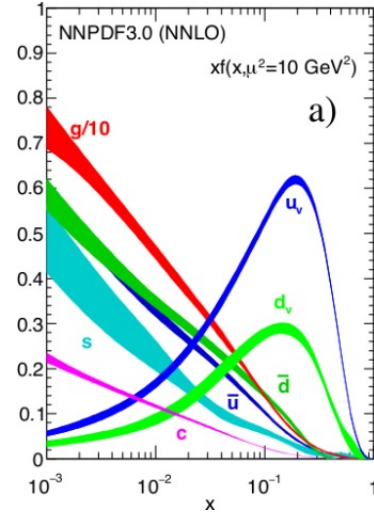
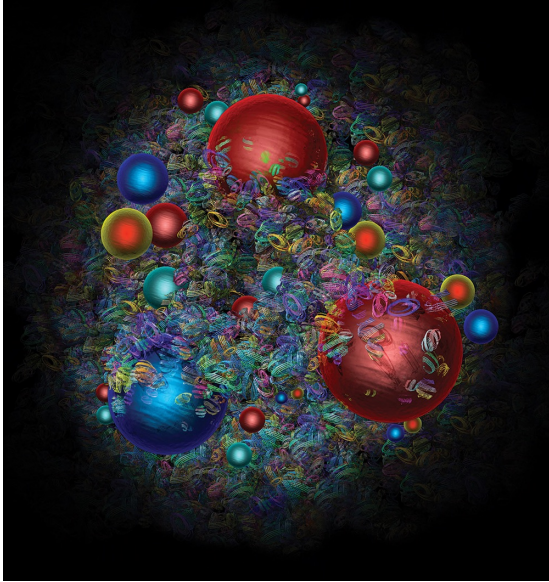


$$P_{\text{sync}} \sim \frac{1}{M^4}$$

- Stable(ish)



But fundamental is nice too...



Their ~~deadly~~ mission: to crack the forbidden island of ~~Honk!~~

Physics

BSM!



# Enter The Dragon

The ultimate Martial Arts masterpiece! Lavishly filmed by Warner Bros. in Hong Kong and the China Sea!

Mhon



STARRING  
**BRUCE LEE · JOHN SAXON · AHNA CAPRI** in "ENTER THE DRAGON" **BOB WALL · SHIH KIEN** and Introducing **JIM KELLY**

Music: Labo Schifrin - Written by Michael Allin - Produced by Fred Weintraub and Paul Heller in association with Raymond Chow - Directed by Robert Clouse

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# The muon is trending

SCIENCE

The New York Times

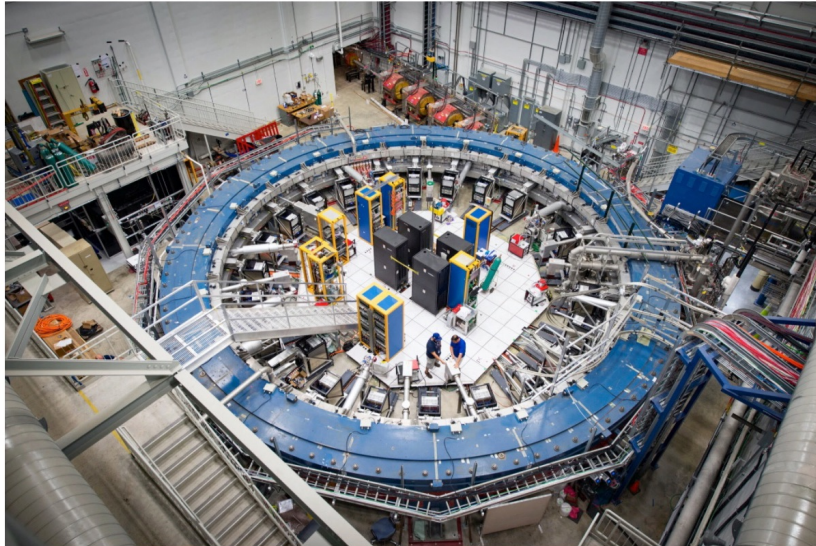
PLAY THE CROSSWORD

Account

## A Tiny Particle's Wobble Could Upend the Known Laws of Physics

Experiments with particles known as muons suggest that there are forms of matter and energy vital to the nature and evolution of the cosmos that are not yet known to science.

f 📷 🐦 📺 ↻ 📄 536



The Muon g-2 ring, at the Fermi National Accelerator Laboratory in Batavia, Ill., operates at minus 450 degrees Fahrenheit and studies the wobble of muons as they travel through the magnetic field. Reidar Hahn/Fermilab, via U.S. Department of Energy

But muons decay...

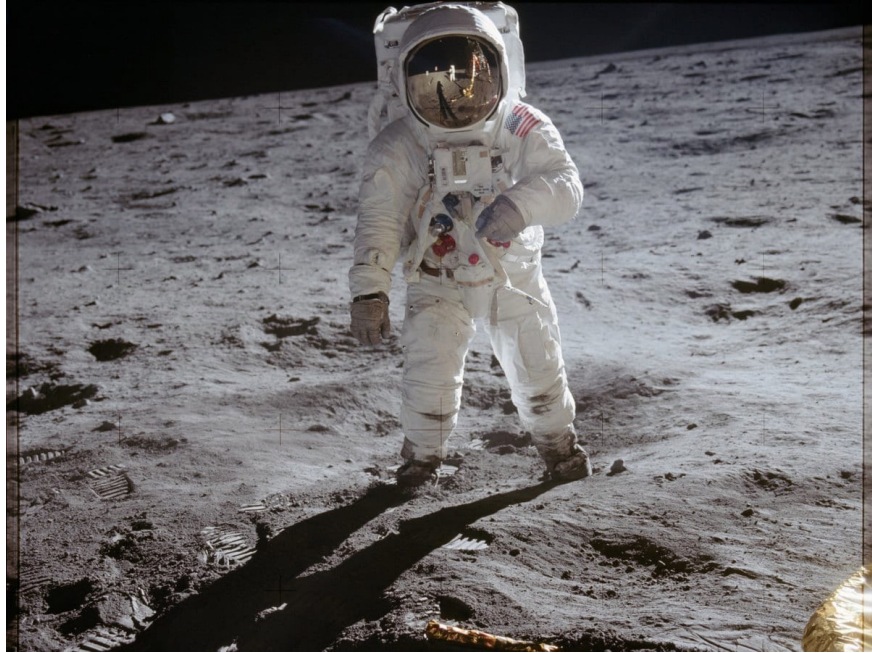
Poses many experimental challenges



Beam induced background  $\Rightarrow \eta \lesssim 2.5$



Let's be "reasonable"



Next generation  
experiment at

 **Fermilab**

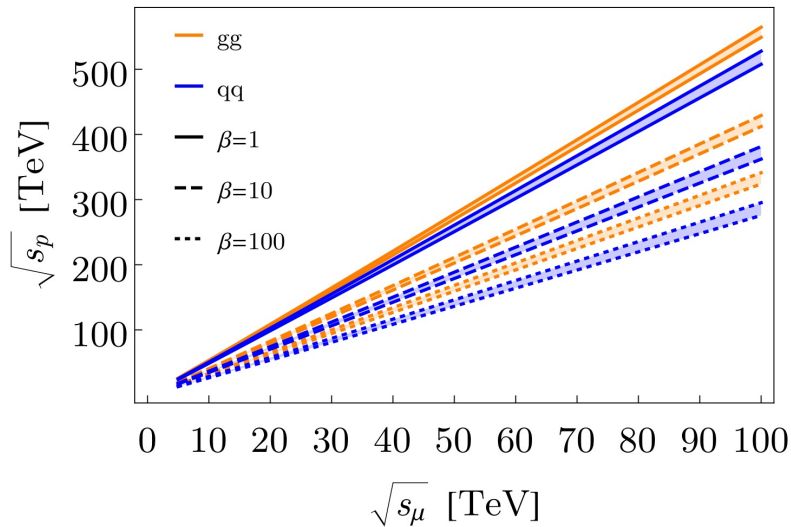
and before  
we retire

$$\Rightarrow \sqrt{s} \lesssim 10 \text{ TeV}$$

What is the physics case?

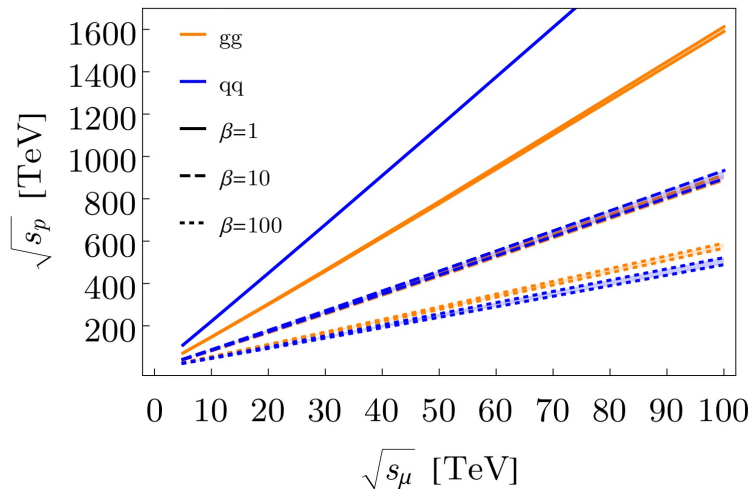
# Muons vs. Protons

$Z \rightarrow 1$



Curves of equivalent  $\sigma$

$Z \rightarrow Z$

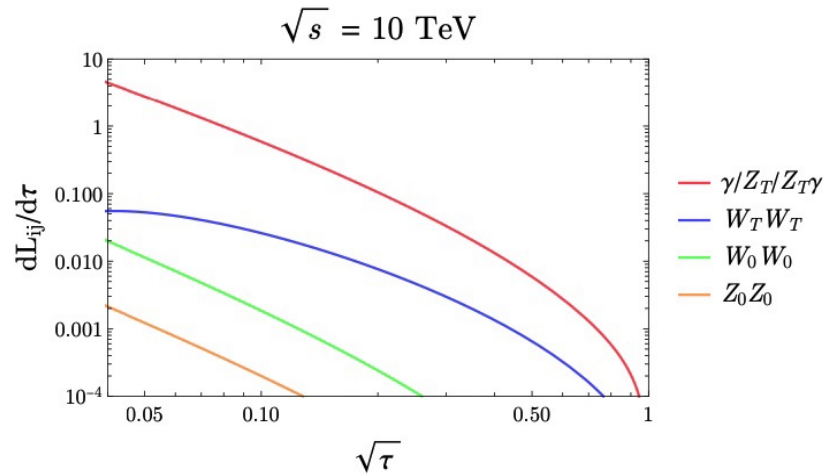
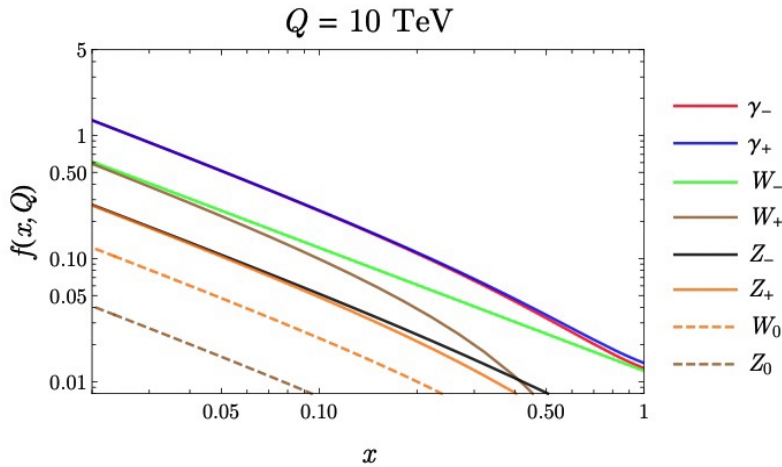


$$\beta = \frac{[\hat{\sigma}_p]}{[\hat{\sigma}_\mu]}$$

$$\frac{\text{QCD}}{\text{EW}} \Rightarrow \beta \sim 10$$

# Muons have PDFs too!

$$\sqrt{s} \gg m_W \gg m_\mu$$

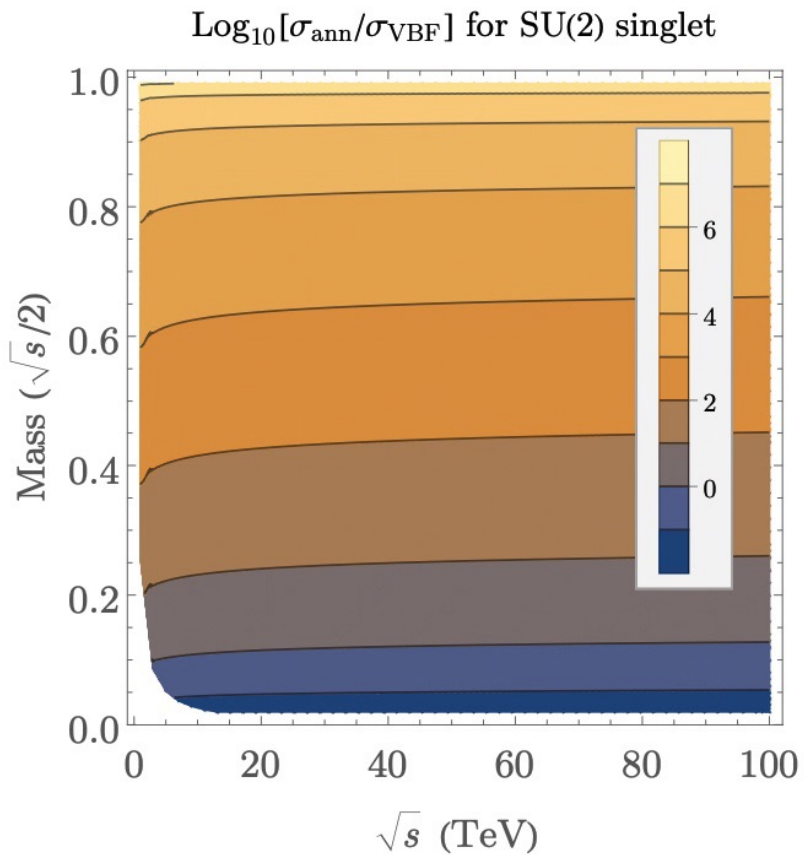


Parton  
luminosity

$$\frac{d\mathcal{L}_{ij}}{d\tau} = \frac{1}{1+\delta_{ij}} \int_{\tau}^1 \frac{dx}{x} \left[ f_i(x) f_j\left(\frac{\tau}{x}\right) + (i \leftrightarrow j) \right]$$



# Annihilation vs. VBF

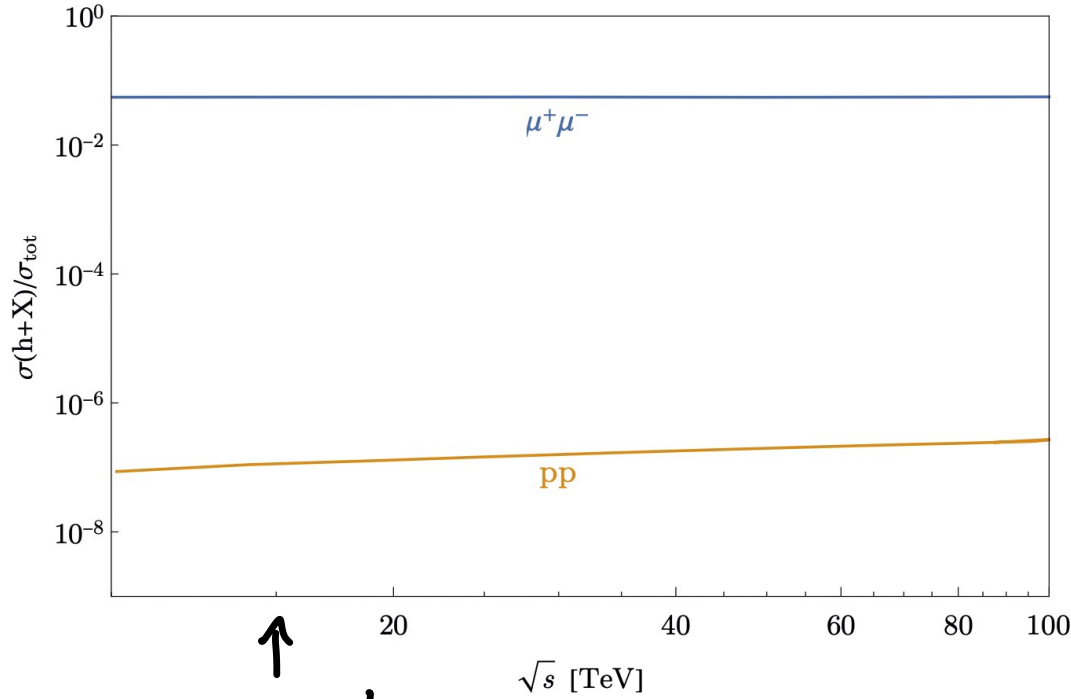


↑ Ann  
↓ VBF

## II. Physics

- Higgs/EW
- Dark Matter
- SUSY

# Higgs production



↑  
10 TeV

Muon

$$\sigma_h : \mu^+\mu^- \rightarrow h\nu\bar{\nu}$$

$$\sigma_{\text{tot}} : \mu^+\mu^- \rightarrow \nu\bar{\nu}$$

Proton

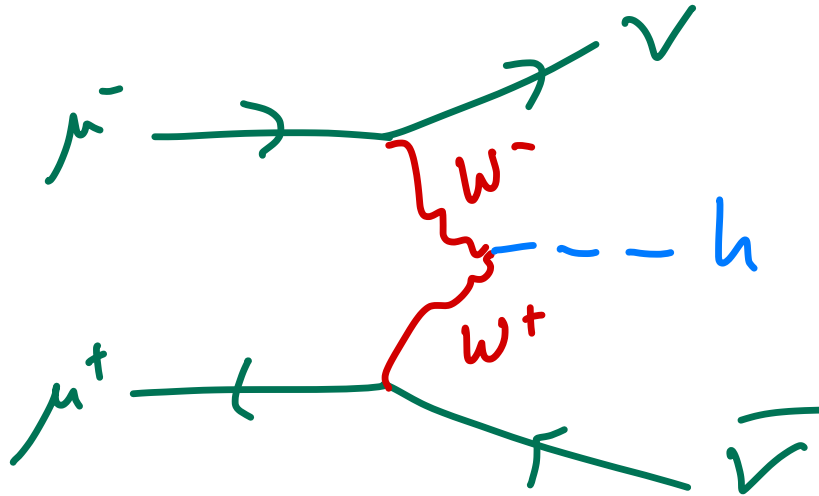
$$\sigma_h : gg \rightarrow h$$

$$\sigma_{\text{tot}} : pp \rightarrow b\bar{b}$$

# Higgs Production

$\sqrt{s} = 10 \text{ TeV} \Rightarrow \mathcal{O}(10^7)$  single Higgs events

$\mathcal{L} = 10 \text{ ab}^{-1} \Rightarrow \mathcal{O}(10^4)$  di-Higgs events



# Higgs Production

10 TeV @ 10 ab<sup>-1</sup>

Production	Decay	Rate [fb]	$A \cdot \epsilon$ [%]	$\Delta\sigma/\sigma$ [%]
W-fusion	$bb$	490	7.4	0.17
	$cc$	24	1.4	1.7
	$jj$	72	37	0.19
	$\tau^+\tau^-$	53	6.5	0.54
	$WW^*(jj\ell\nu)$	53	21	0.30
	$WW^*(4j)$	86	4.9	0.49
	$ZZ^*(4\ell)$	0.1	6.6	12
	$ZZ^*(jj\ell^+\ell^-)$	2.1	8.9	2.3
	$ZZ^*(4j)$	11	4.6	1.4
	$\gamma\gamma$	1.9	33	1.3
	$Z(jj)\gamma$	0.9	27	2.0
	$\mu^+\mu^-$	0.2	37	0.37
Z-fusion	$bb$	51	8.1	0.49
	$WW^*(4j)$	8.9	6.2	1.3
W-fusion $tth$	$bb$	0.06	12	12

Signal only selection

# Higgs Production

	Fit Result [%]		
	10 TeV Muon Collider	with HL-LHC	with HL-LHC + 250 GeV $e^+e^-$
$\kappa_W$	0.06	0.06	0.06
$\kappa_Z$	0.23	0.22	0.10
$\kappa_g$	0.15	0.15	0.15
$\kappa_\gamma$	0.64	0.57	0.57
$\kappa_{Z\gamma}$	1.0	1.0	0.97
$\kappa_c$	0.89	0.89	0.79
$\kappa_t$	6.0	2.8	2.8
$\kappa_b$	0.16	0.16	0.15
$\kappa_\mu$	2.0	1.8	1.8
$\kappa_\tau$	0.31	0.30	0.27

2d framework  
signal only

# Higgs Production

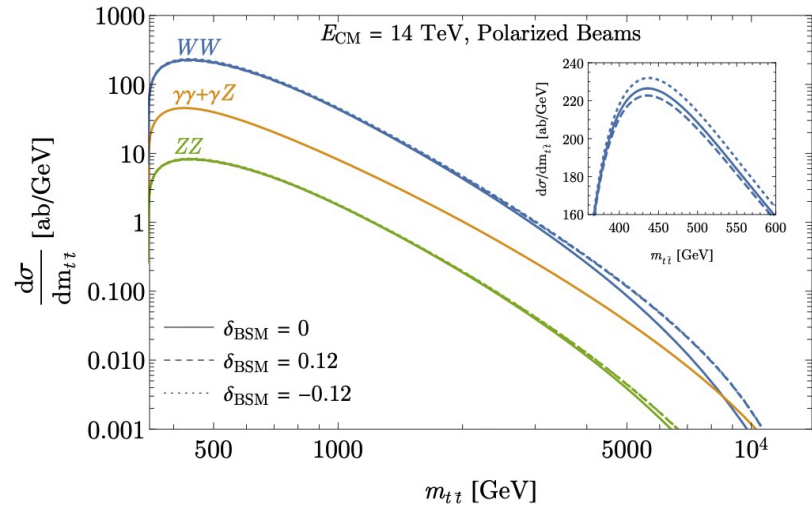
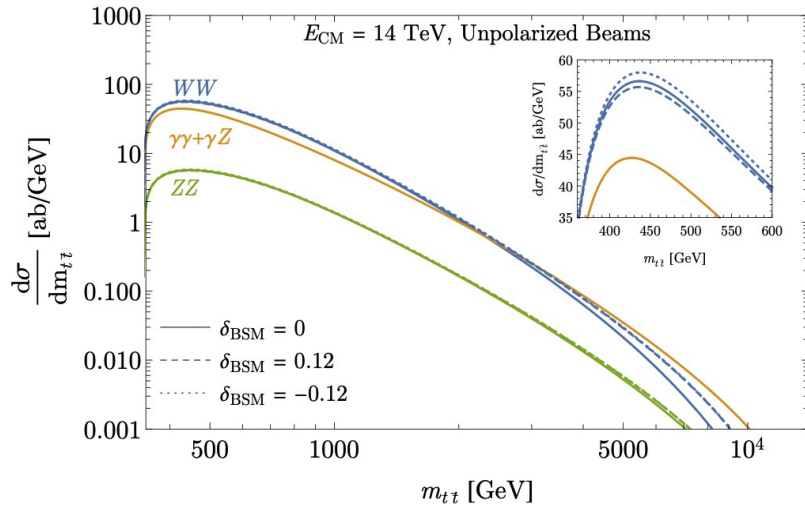
$\kappa$ -0 fit	HL-LHC	LHeC	HE-LHC		ILC			CLIC			CEPC	FCC-ee		FCC-ee/ eh/hh	$\mu^+\mu^-$ <b>10000</b>
			S2	S2'	250	500	1000	380	1500	3000		240	365		
$\kappa_W$ [%]	1.7	0.75	1.4	0.98	1.8	0.29	0.24	0.86	0.16	0.11	1.3	1.3	0.43	0.14	0.06
$\kappa_Z$ [%]	1.5	1.2	1.3	0.9	0.29	0.23	0.22	0.5	0.26	0.23	0.14	0.20	0.17	0.12	0.23
$\kappa_g$ [%]	2.3	3.6	1.9	1.2	2.3	0.97	0.66	2.5	1.3	0.9	1.5	1.7	1.0	0.49	0.15
$\kappa_\gamma$ [%]	1.9	7.6	1.6	1.2	6.7	3.4	1.9	98*	5.0	2.2	3.7	4.7	3.9	0.29	0.64
$\kappa_{Z\gamma}$ [%]	10.	—	5.7	3.8	99*	86*	85*	120*	15	6.9	8.2	81*	75*	0.69	1.0
$\kappa_c$ [%]	—	4.1	—	—	2.5	1.3	0.9	4.3	1.8	1.4	2.2	1.8	1.3	0.95	0.89
$\kappa_t$ [%]	3.3	—	2.8	1.7	—	6.9	1.6	—	—	2.7	—	—	—	1.0	6.0
$\kappa_b$ [%]	3.6	2.1	3.2	2.3	1.8	0.58	0.48	1.9	0.46	0.37	1.2	1.3	0.67	0.43	0.16
$\kappa_\mu$ [%]	4.6	—	2.5	1.7	15	9.4	6.2	320*	13	5.8	8.9	10	8.9	0.41	2.0
$\kappa_\tau$ [%]	1.9	3.3	1.5	1.1	1.9	0.70	0.57	3.0	1.3	0.88	1.3	1.4	0.73	0.44	0.31

(Not fair to compare with our signal only analysis)



# Modified Top Yukawa

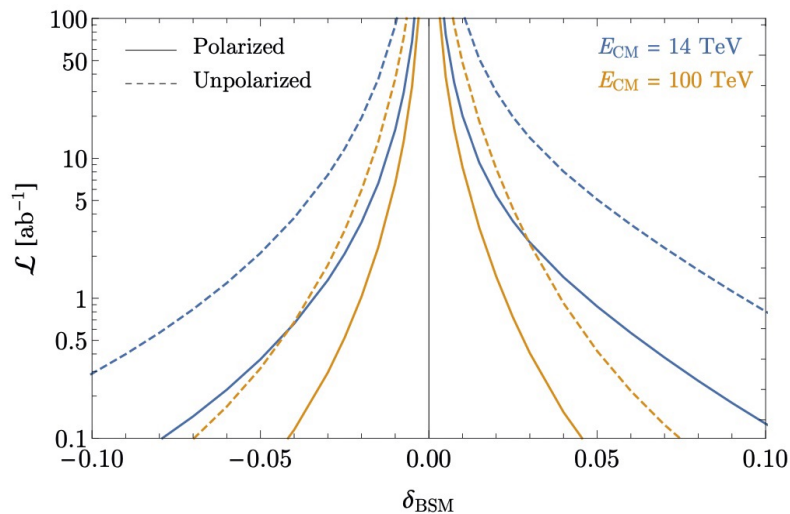
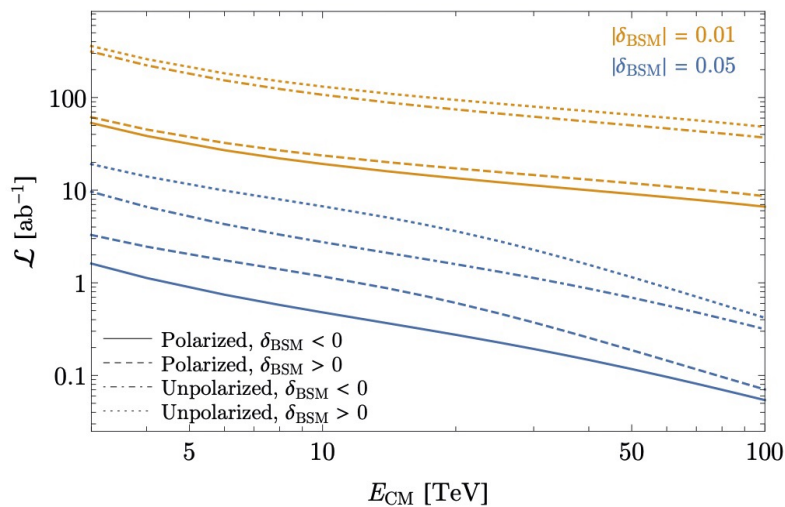
$$Y_t \rightarrow Y_t (1 + \delta_{\text{BSM}})$$



$$\mathcal{M}(W_L^+ W_L^- \rightarrow t\bar{t}) \simeq -\frac{m_t}{v^2} \delta_{\text{BSM}} \sqrt{\hat{s}} \quad \text{w/ } \hat{s} \gg m_t^2$$

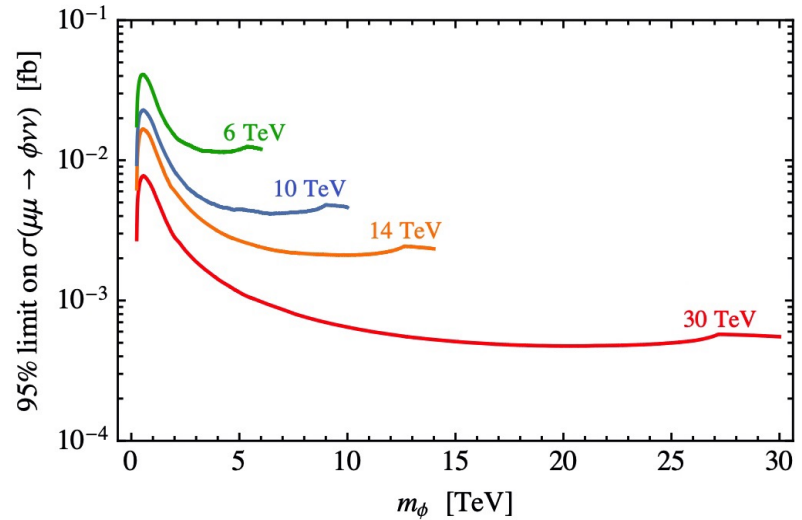
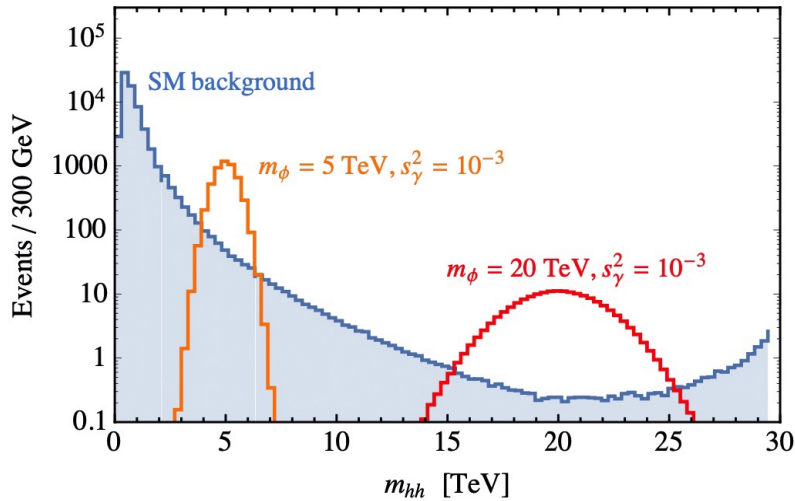
# Modified Top Yukawa

$$Y_t \rightarrow Y_t (1 + \delta_{\text{BSM}})$$



# Extra Higgs Bosons

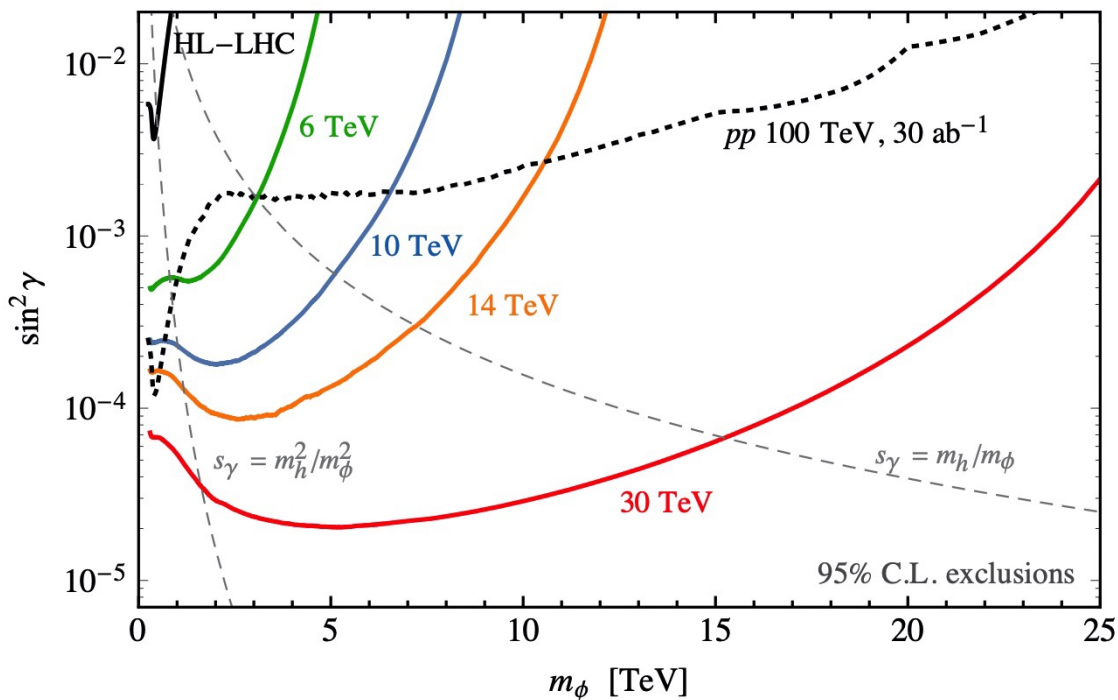
$$\mu^+ \mu^- \rightarrow \phi \nu \bar{\nu} \rightarrow hh \nu \bar{\nu}$$



For di-Higgs ZHDM study, see arXiv: 2102.08386

# Extra Higgs Bosons

$$\mu^+ \mu^- \rightarrow \phi \nu \bar{\nu} \rightarrow hh \nu \bar{\nu}$$



# WIMP Dark Matter Models considered

Model (color, $n$ , $Y$ )		Thermal target	5 $\sigma$ discovery coverage (TeV)			
			mono- $\gamma$	mono- $\mu$	di- $\mu$ 's	disp. tracks
(1,2, $\frac{1}{2}$ )	Dirac	1.1 TeV	—	2.8	—	1.8 - 3.7
(1,3,0)	Majorana	2.8 TeV	—	3.7	—	13 - 14
(1,3, $\epsilon$ )	Dirac	2.0 TeV	0.9	4.6	—	13 - 14
(1,5,0)	Majorana	14 TeV	3.1	7.0	3.1	10 - 14
(1,5, $\epsilon$ )	Dirac	6.6 TeV	6.9	7.8	4.2	11 - 14
(1,7,0)	Majorana	23 TeV	14	8.6	6.1	8.1 - 12
(1,7, $\epsilon$ )	Dirac	16 TeV	13	9.2	7.4	8.6 - 13

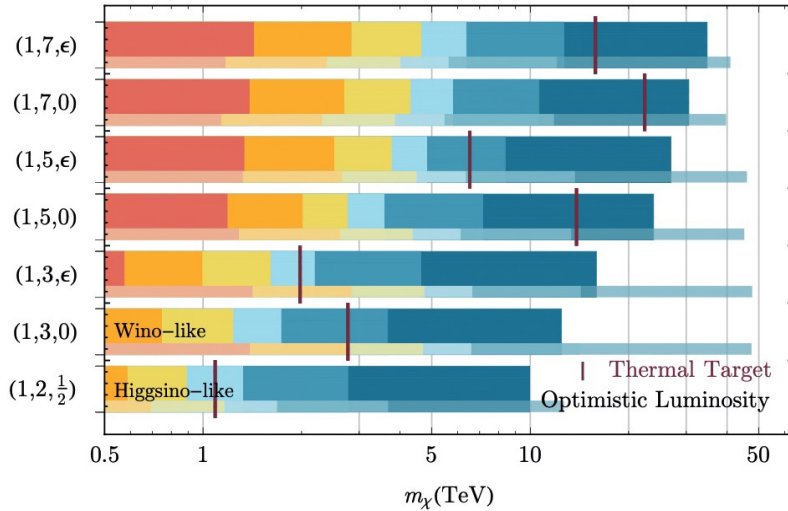
see arXiv: 2009.11287

# WIMP Dark Matter Strategies

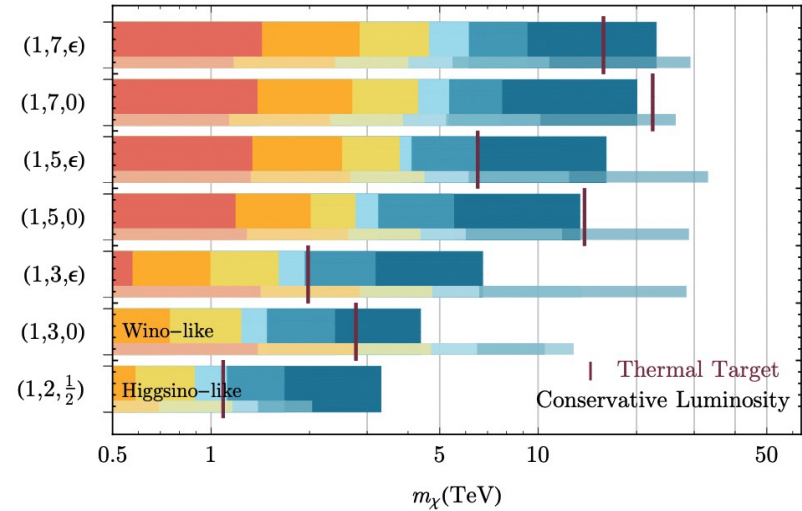
- Mono-muon
- Mono-photon
- Di-muon
- Disappearing tracks

# WIMP Dark Matter

Muon Collider  $5\sigma$  Reach ( $\sqrt{s} = 3, 6, 10, 14, 30, 100$  TeV)



Muon Collider  $5\sigma$  Reach ( $\sqrt{s} = 3, 6, 10, 14, 30, 100$  TeV)



Narrow bars include disappearing tracks

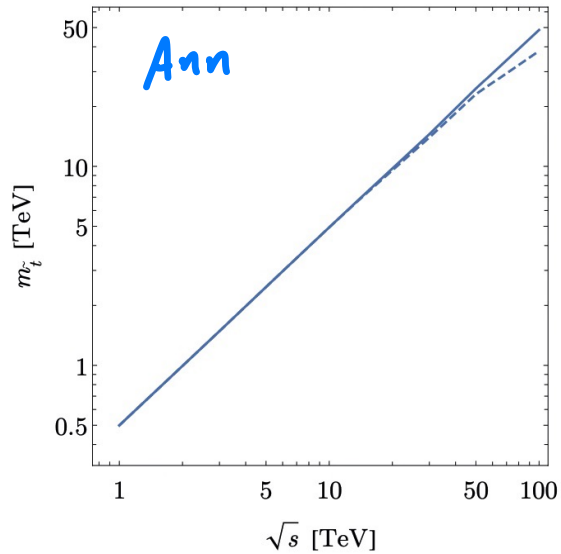


# SUSY

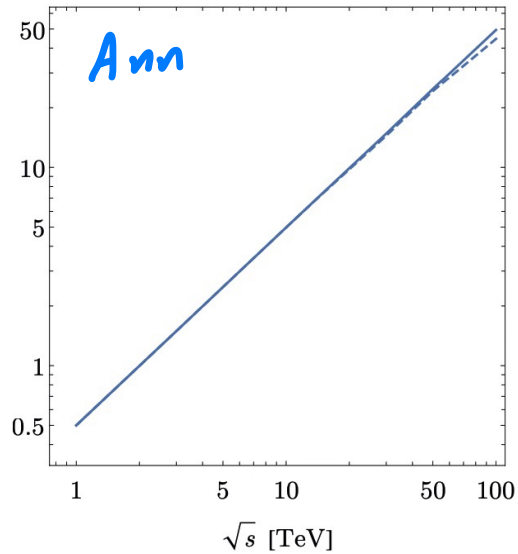
## Stop-neutralino simplified model

### Exclusions

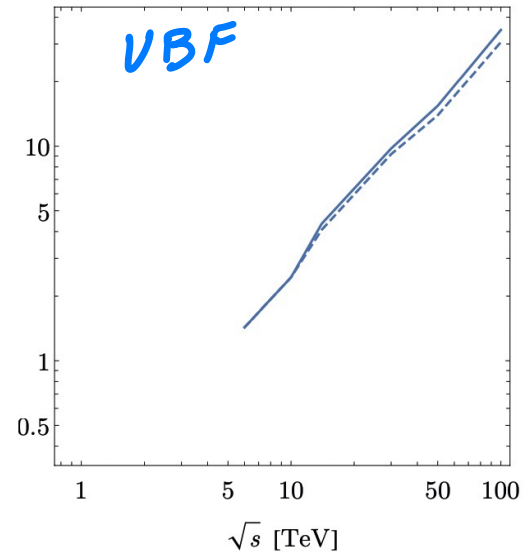
$$\mu^+\mu^- \rightarrow \tilde{t}_R \tilde{t}_R \rightarrow t\bar{t} + \chi\chi$$



$$\mu^+\mu^- \rightarrow \tilde{t}_L \tilde{t}_L \rightarrow t\bar{t} + \chi\chi$$



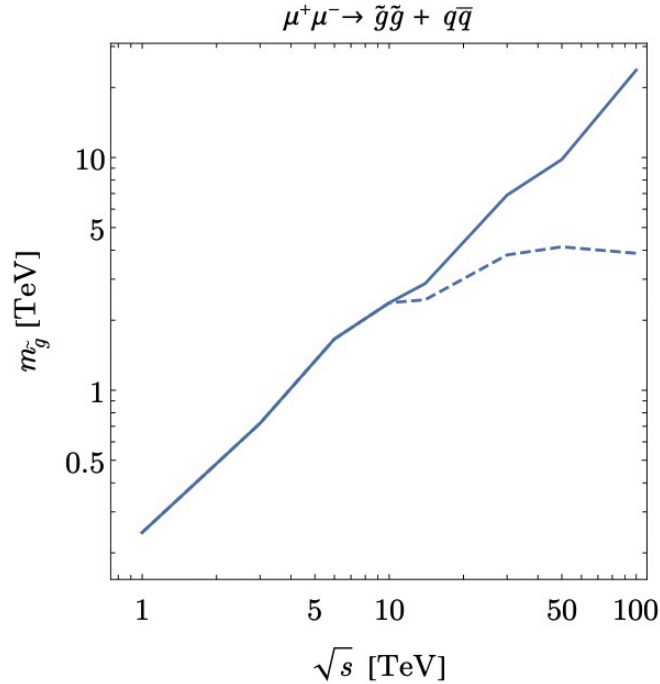
$$\mu^+\mu^- \rightarrow \tilde{t}_L \tilde{t}_L + \nu\bar{\nu} \rightarrow t\bar{t} + \chi\chi + \nu\bar{\nu}$$



$$m_\chi = 1 \text{ GeV}$$

# SUSY

## Gluino - neutralino simplified model



$$m_{\tilde{\chi}} = 1 \text{ GeV}$$

### III. Outlook

# Outlook

10 TeV muon collider would  
qualitatively impact Higgs and  
WIMP dark matter pheno.

Would provide incremental  
progress for SUSY (heavy BSM)  
unless we get more  $\sqrt{s}$ .

# Outlook

A naive comparison for  
single Higgs production

- Polarization  $\Rightarrow$  factor of 2
- Log growth of rate from  
 $3\text{ TeV} \Rightarrow 10\text{ TeV} \Rightarrow$  factor of 2

$\Rightarrow$  3 TeV CLIC w/ pol  $\sim$  10 TeV  $\mu^+\mu^-$   
and muon collider has more hh production

# Outlook

Many fascinating accelerator  
and detector design questions!!

- Timing and tagging
- Polarization vs Luminosity
- $|\eta| < 2.5$  improved?
- What  $\sqrt{s}$ ?

# Outlook

A  $10^7$  TeV muon collider is  
viable and exciting opportunity  
for future US HEP program!!