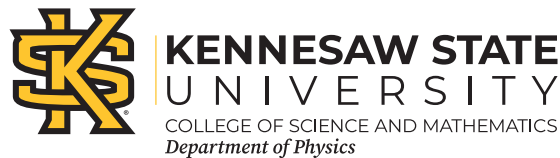


# Soft gluons in $t\bar{t}$ and $tW$ processes at high energies

Nikolaos Kidonakis

- Higher-order soft-gluon corrections
- Top-antitop pair production
- $tW$  production



**Snowmass 2021**  
**Energy Frontier Workshop**



## Soft-gluon corrections

partonic processes (in general  $2 \rightarrow n$ )

$$f_1(p_1) + f_2(p_2) \rightarrow t(p_t) + X$$

define  $s = (p_1 + p_2)^2$ ,  $t = (p_1 - p_t)^2$ ,  $u = (p_2 - p_t)^2$  and  $s_4 = s + t + u - p_t^2 - p_X^2$

At partonic threshold  $s_4 \rightarrow 0$

Soft corrections  $\left[ \frac{\ln^k(s_4/m_t^2)}{s_4} \right]_+$  with  $k \leq 2n - 1$  for the order  $\alpha_s^n$  corrections

Resum these soft corrections  $\rightarrow$  finite-order expansions-no prescription needed

Approximate NNLO (aNNLO) and N<sup>3</sup>LO (aN<sup>3</sup>LO) predictions  
for cross sections and differential distributions (single and double)

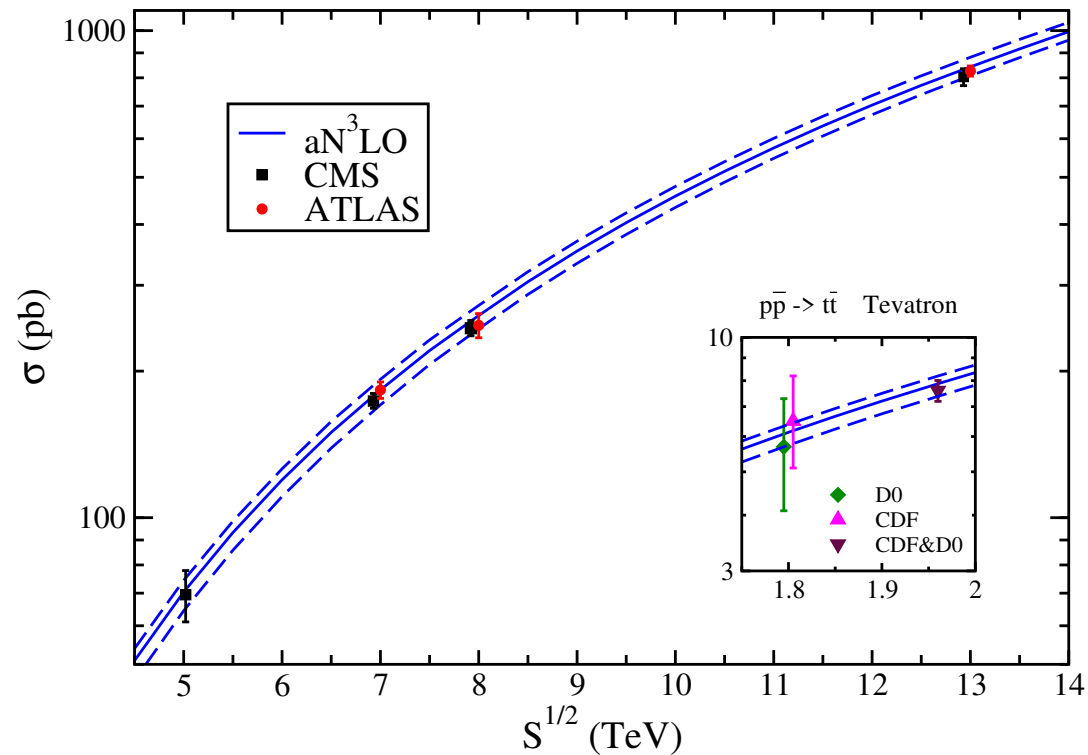
Soft anomalous dimension  $\Gamma_S^{f_1 f_2 \rightarrow t X}$  controls the evolution of the soft function

At NLL, NNLL, and N<sup>3</sup>LL accuracy we need, respectively,  
one-loop, two-loop, three-loop soft anomalous dimensions

# Top-antitop pair production

$pp \rightarrow t\bar{t}$  at LHC energies  $aN^3LO$   $m_t=172.5$  GeV

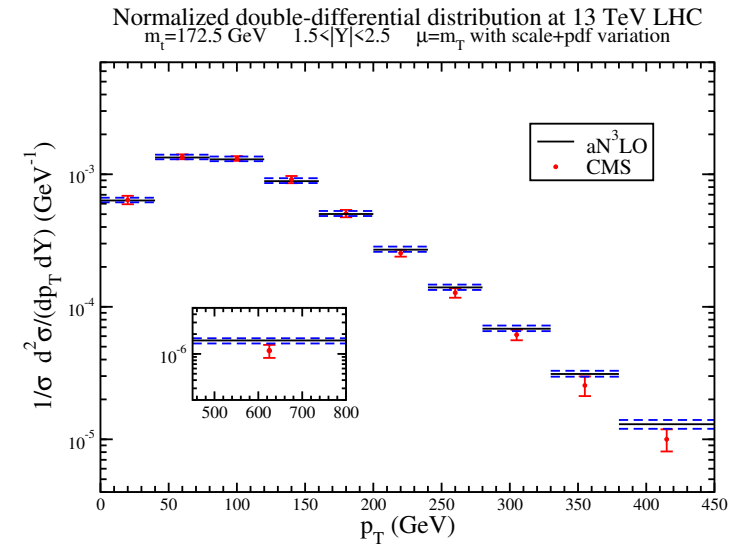
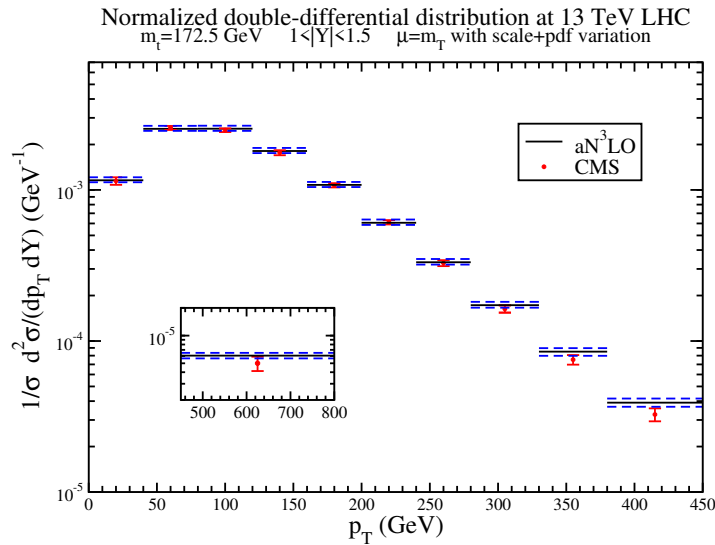
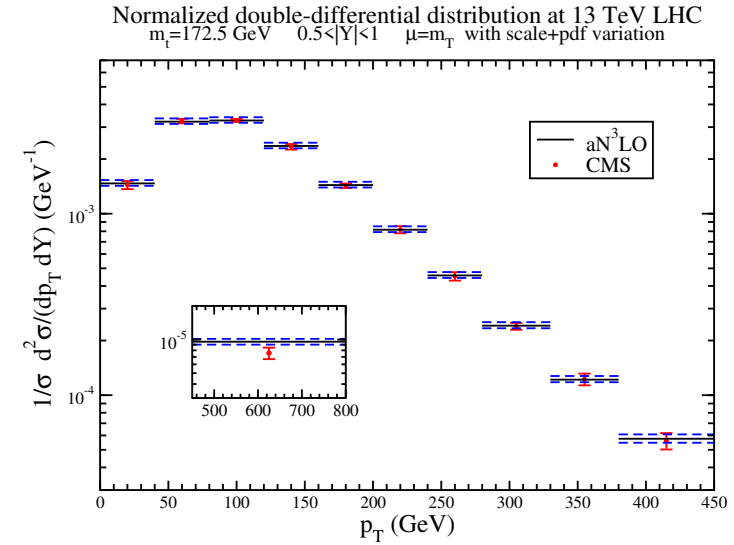
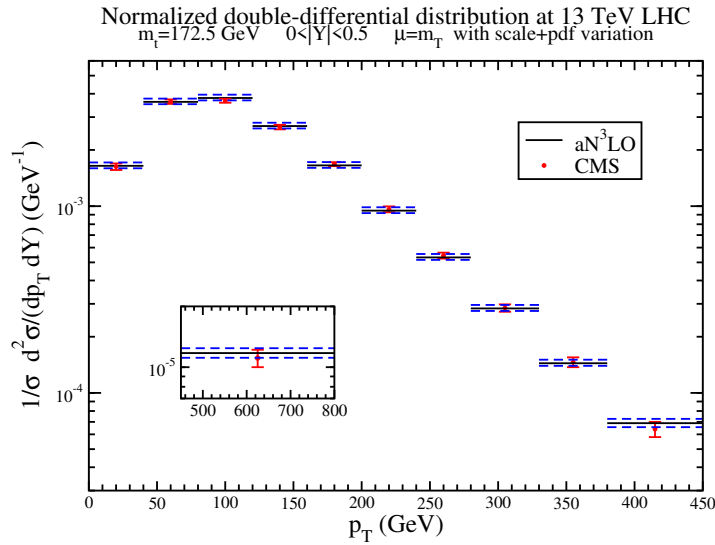
MMHT2014 NNLO pdf



soft-gluon corrections dominant at LHC for total & differential cross sections

also dominant at higher energies at future colliders  $\rightarrow$  more studies

# Top double-differential distributions in $t\bar{t}$ production



$t\bar{t}$  at high energies - preliminary results ( $\mu = m_t$ , same pdf)

	14 TeV	20 TeV	30 TeV	40 TeV	50 TeV	100 TeV
NLO/LO	1.50	1.51	1.52	1.53	1.54	1.58
aNLO/NLO	0.99	0.98	0.97	0.96	0.95	0.92
NNLO/NLO	1.11	1.11	1.11	1.11	1.11	1.10
aNNLO/NNLO	1.00	1.00	0.99	0.99	0.99	0.98
aN <sup>3</sup> LO/NNLO	1.03					

where

aNLO = LO + soft-gluon NLO corrections

aNNLO = NLO + soft-gluon NNLO corrections

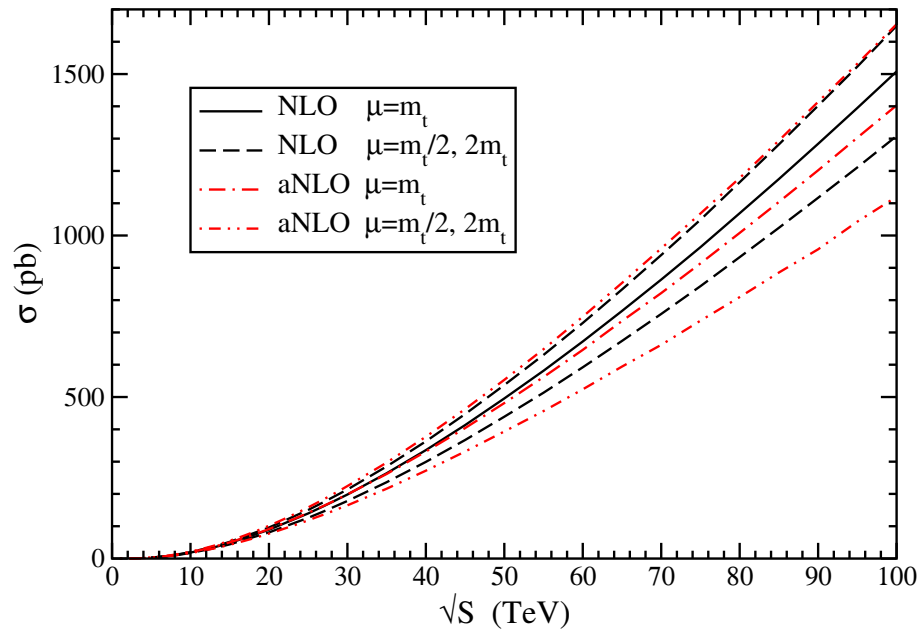
aN<sup>3</sup>LO = NNLO + soft-gluon N<sup>3</sup>LO corrections

# $tW$ production at high-energy colliders

(with Nodoka Yamanaka, JHEP 05, 278 (2021) )

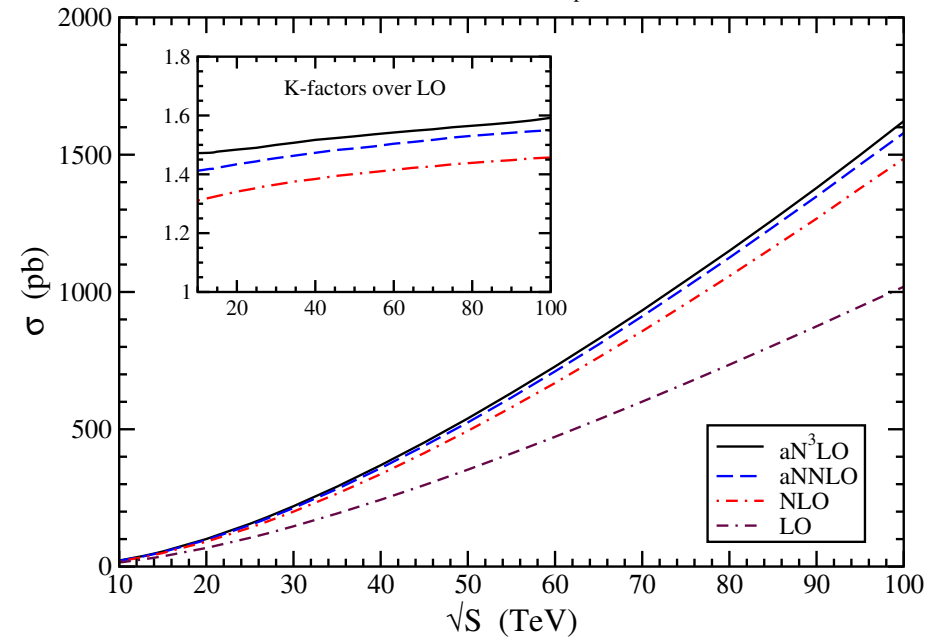
pp  $\rightarrow$   $tW^-$  NLO and aNLO cross sections  $m_t=172.5$  GeV

MSHT20 NLO pdf



pp  $\rightarrow$   $tW^-$  cross section  $\mu=m_t=172.5$  GeV

MSHT20 NNLO pdf



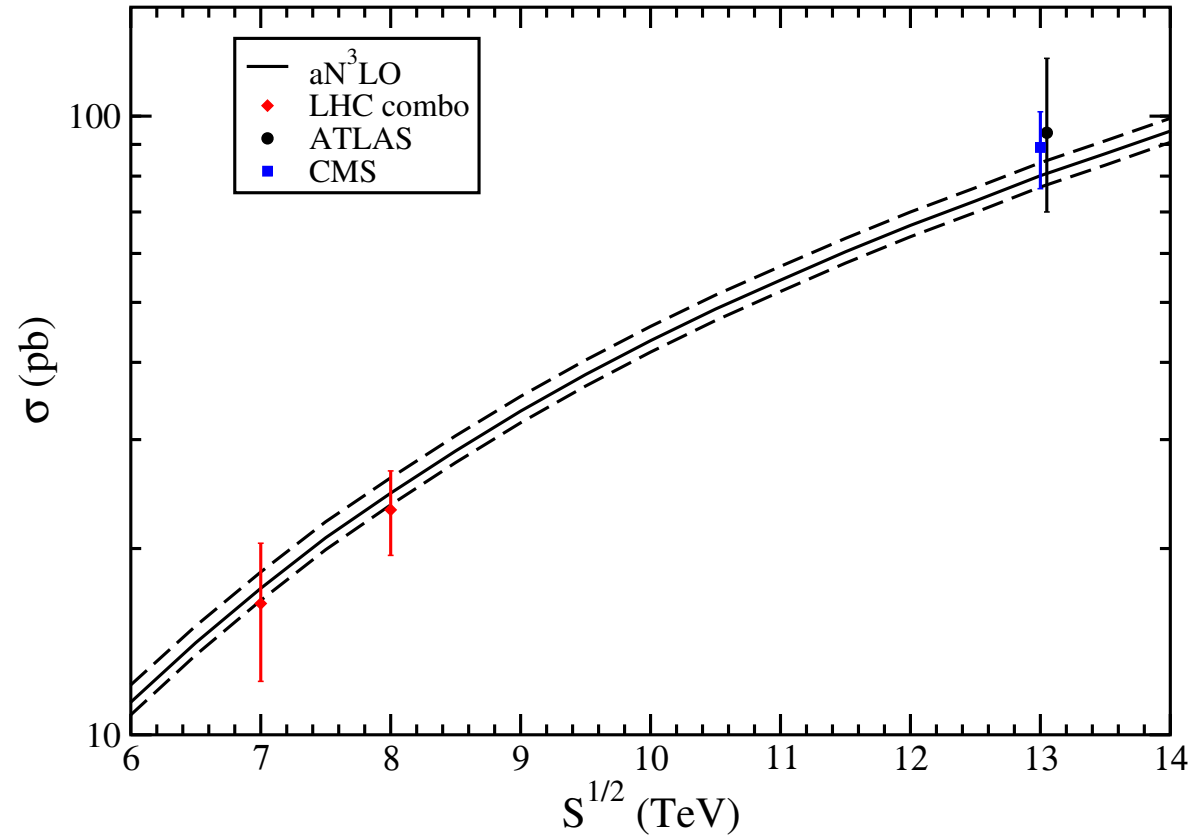
The aNLO cross section is a very good approximation to the complete NLO result for all foreseeable collider energies

$\rightarrow$  the soft-gluon corrections are dominant

The aNNLO and aN<sup>3</sup>LO corrections (at NNLL) are also significant

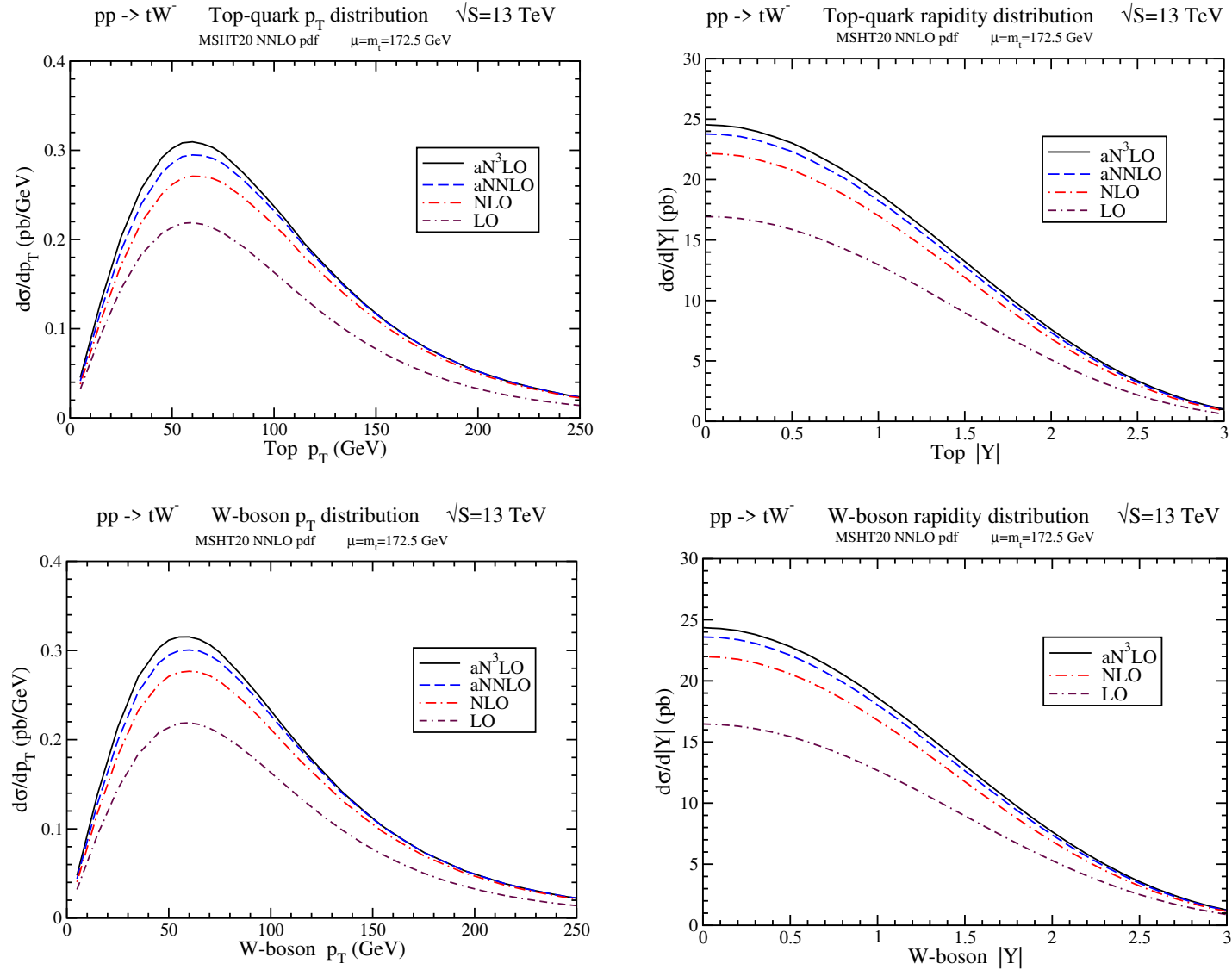
$tW^- + \bar{t}W^+$  aN<sup>3</sup>LO cross section  $m_t=172.5$  GeV

MSHT20 NNLO pdf with scale+pdf uncertainties



The aN<sup>3</sup>LO cross section with scale and pdf (MSHT20) uncertainty is  
 at 13 TeV:  $79.5^{+1.9+2.0}_{-1.8-1.4}$  pb      at 14 TeV  $94.0^{+2.2+2.2}_{-2.1-1.6}$  pb

# Top-quark and $W$ -boson distributions in $tW$ production





## Summary

- quality of soft-gluon approximation at high energies
- top-antitop pair production
- top-quark double-differential distributions in  $t\bar{t}$  production
- $tW$  cross sections and top-quark,  $W$ -boson distributions
- soft-gluon corrections are dominant and they are significant through aN<sup>3</sup>LO