

# Nuclear matrix elements for neutrino-nucleus scattering from lattice QCD

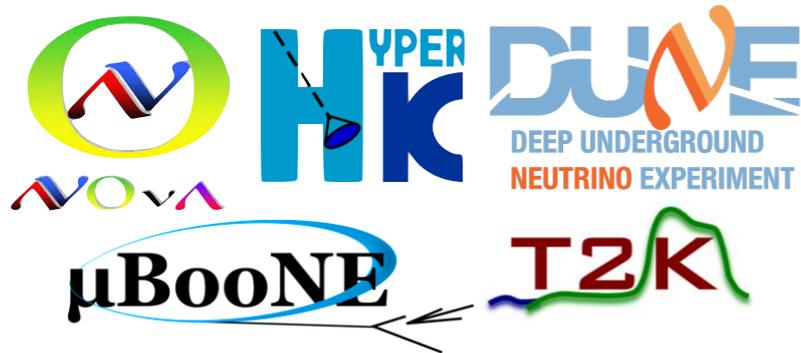
Phiala Shanahan, MIT

Image Credit: 2018 EIC User's Group Meeting



Massachusetts  
Institute of  
Technology

# Neutrino oscillation experiments

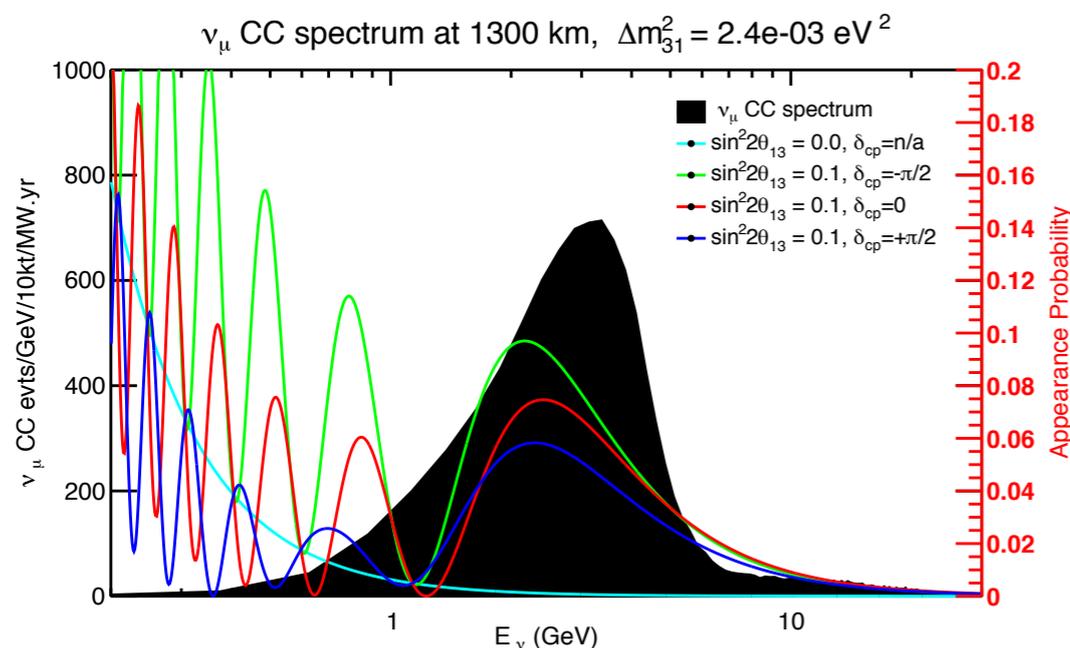


Seek to determine neutrino mass hierarchy, mixing parameters, CP violating phase

To differentiate between mixing & CP parameter scenarios



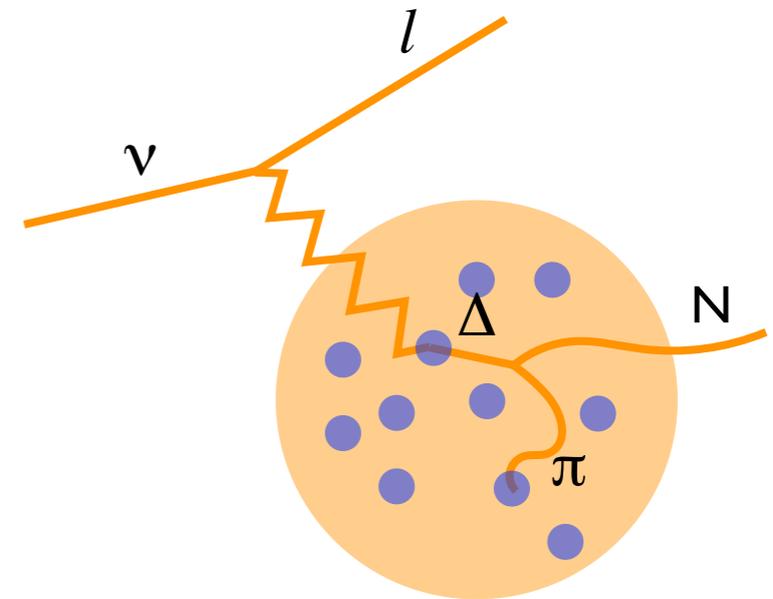
Need neutrino energy reconstruction from final state to better than 100 MeV



Lattice QCD: direct non-perturbative QCD predictions for nucleon and nuclear matrix elements  
e.g., axial and pseudo-scalar form factors important in **quasi-elastic** region

# Nuclear effects

- Targets are nuclei (C, Fe, Ar, Pb, H<sub>2</sub>O) so how relevant are nucleon FFs, PDFs?
  - EMC effect
  - Suppression of  $g_A$  in Gamow-Teller transitions
- Experimental investigations: MINERvA



Calculate matrix elements in light nuclei from lattice QCD

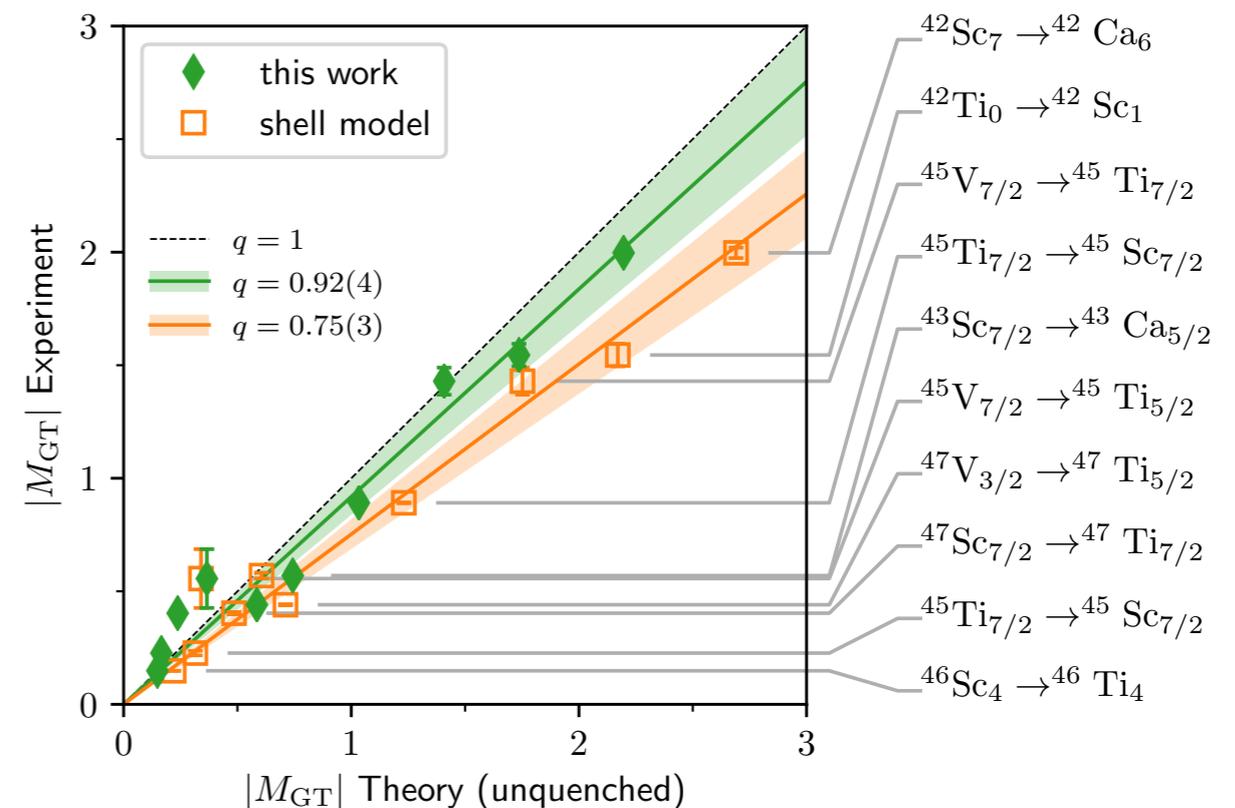
➔ EFT to reach heavy nuclear targets relevant to experiment

e.g., First calculations of axial charge of light nuclei, EMC effect in light nuclei

# Nuclear effects

How well do we know nuclear matrix elements?

- Gamow-Teller transitions in nuclei are a stark example of importance of nuclear effects
  - Well-measured for large range of nuclei where the spectrum is well described ( $30 < A < 60$ )
  - Historically nuclear structure calculations were systematically off by 20–30%
  - Correct using two-body currents where they are known

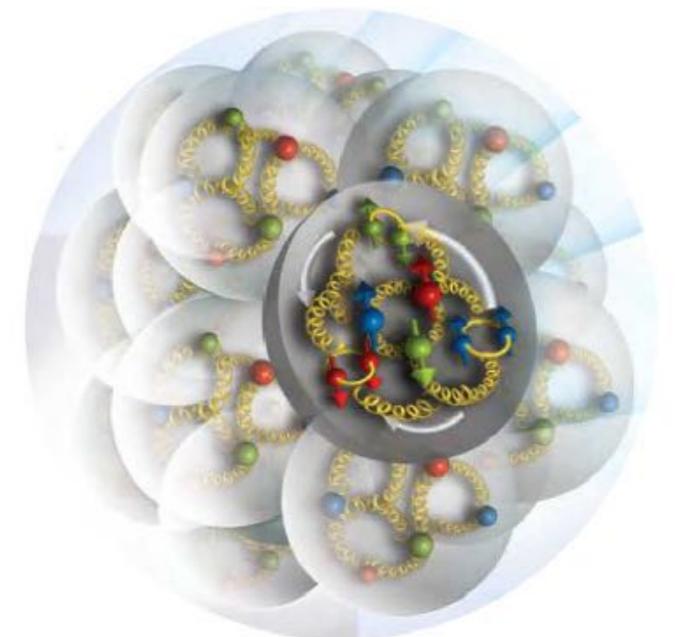


[Gysbers et al, Nature Phys. 15 (2019) no. 5 428-431]

# Nuclear physics from lattice QCD

## Nuclei on the lattice are HARD

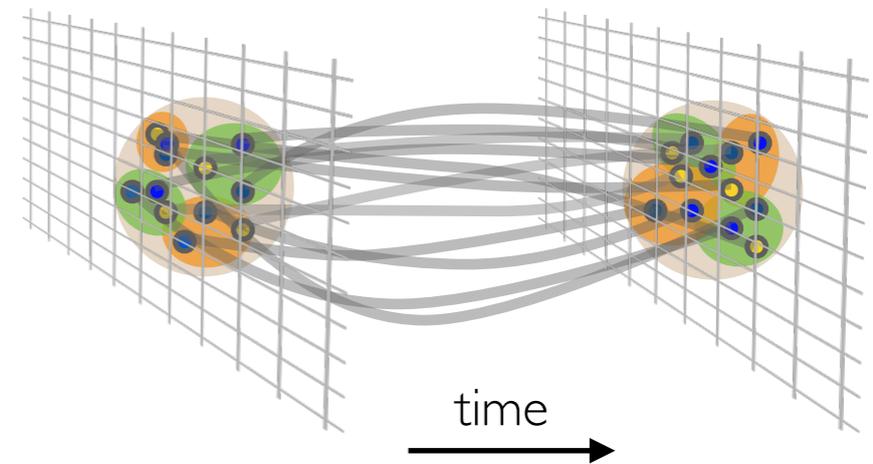
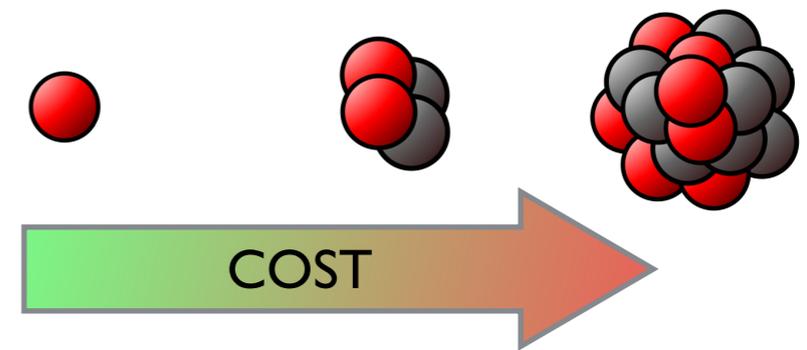
- Calculations of matrix elements of currents in light nuclei just beginning:
  - Controlled calculations of spectrum of light nuclei yet to be achieved
  - First exploratory calculations of matrix elements taking place now
- With sufficient computing resources, calculations are in principle possible:
  - Deeply bound nuclei: same techniques as for single hadron matrix elements
  - Near threshold states: need to be careful with volume effects



# Nuclear physics from lattice QCD

## Nuclei on the lattice are HARD

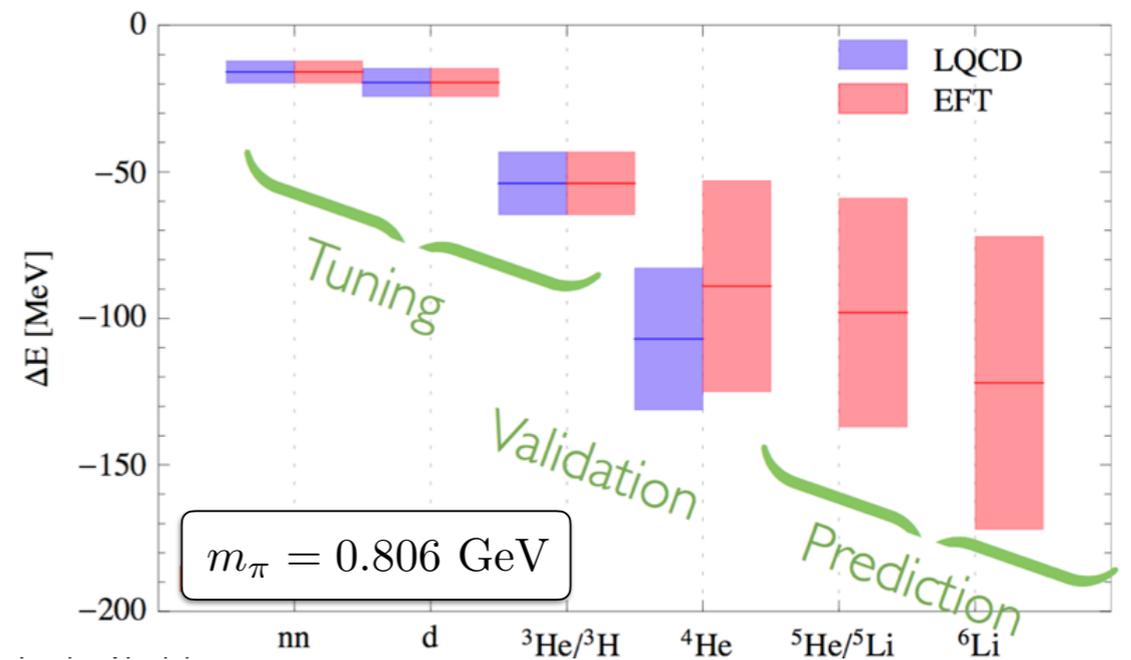
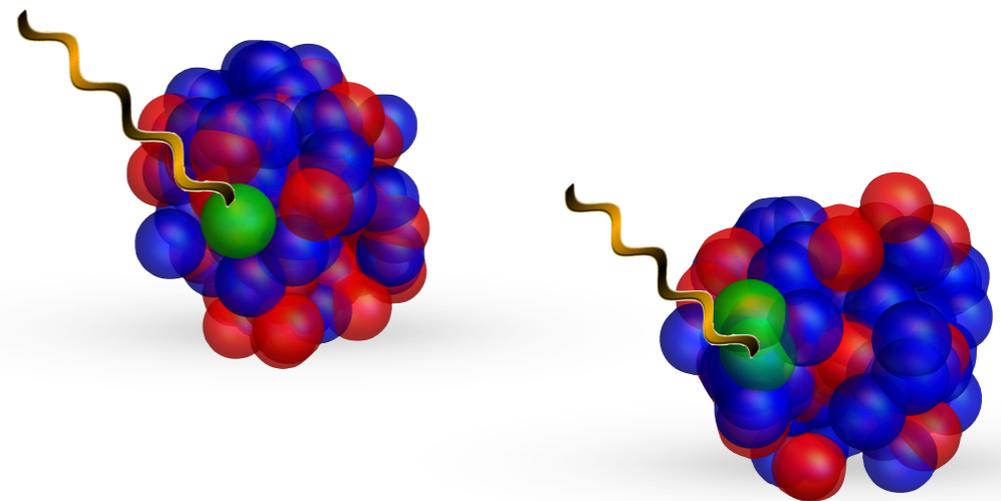
- **Noise:**  
Statistical uncertainty grows exponentially with number of nucleons
- **Complexity:**  
Number of contractions grows factorially



Calculations possible for  $A < 5$

# Larger nuclei

- What about larger (phenomenologically-relevant) nuclei?
- Nuclear effective field theory:
  - 1-body currents are dominant
  - 2-body currents are sub-leading but non-negligible
- Determine one body contributions from single nucleon
- Determine few-body contributions from  $A=2,3,4\dots$
- Match EFT and many body methods to LQCD to make predictions for larger nuclei



[Barnea et al., PRL 2015]

# Nuclear physics from lattice QCD

Nuclear matrix elements from lattice QCD studied only by the NPLQCD Collaboration to date

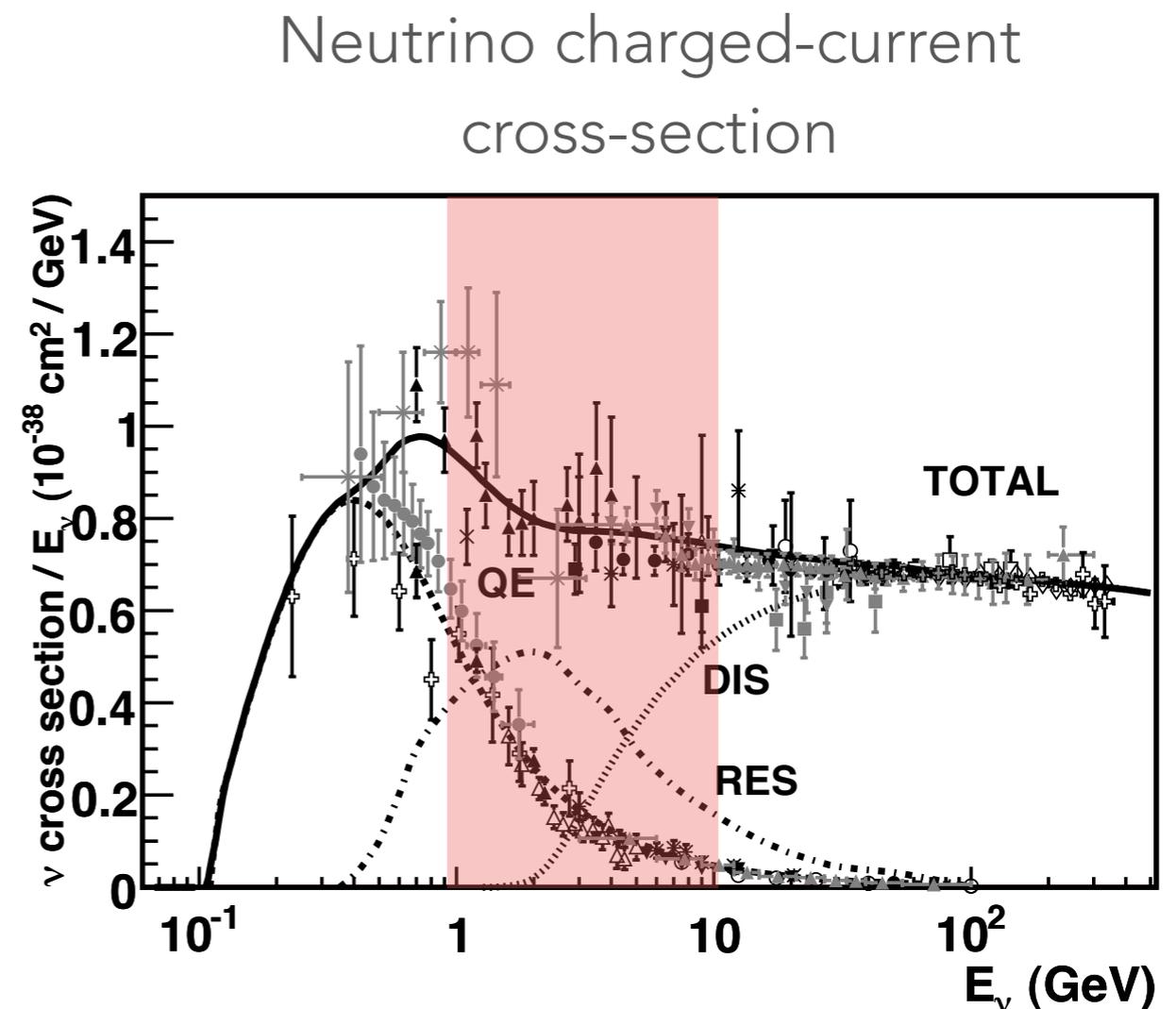
- Proton-proton fusion and tritium  $\beta$ -decay [PRL 119, 062002 (2017)]
- Double  $\beta$ -decay [PRL 119, 062003 (2017), PRD 96, 054505 (2017)]
- Gluon structure of light nuclei [PRD 96 094512 (2017)]
- Scalar, axial, tensor MEs [PRL 120 152002 (2018), PRD 103, 074511 (2021)]
- Baryon-baryon interactions, including QED [PRD 103, 054504 (2021), PRD 103, 054508 (2021)]
- EMC-type effects in light nuclei [PRD 96 094512 (2017), PRL 126, 202001 (2021)]

Many other collaborations are studying nuclei from lattice QCD

- **PACS-CS**  
e.g., Yamazaki et al, PRD 92 (2015);
- **Callatt**  
e.g., E Berkowitz et al, PLB 765 (2017); Hörz et al, PRC 103 (2021)
- **Mainz**  
e.g., A. Francis et al, PRD 99 (2019); Green et al, [2103.01054]
- **HALQCD**  
e.g., Ishii et al, PRL 99 (2007)  
(potential approach)

# Constraining $\nu$ -nucleus interactions

- For DUNE neutrino energy distributions peak at 1-10 GeV
- Challenging region: several processes contribute
  - Quasielastic lepton scattering
  - Deep inelastic scattering
  - Resonances
- Lattice QCD can provide direct non-perturbative QCD predictions of nucleon and **nuclear** matrix elements



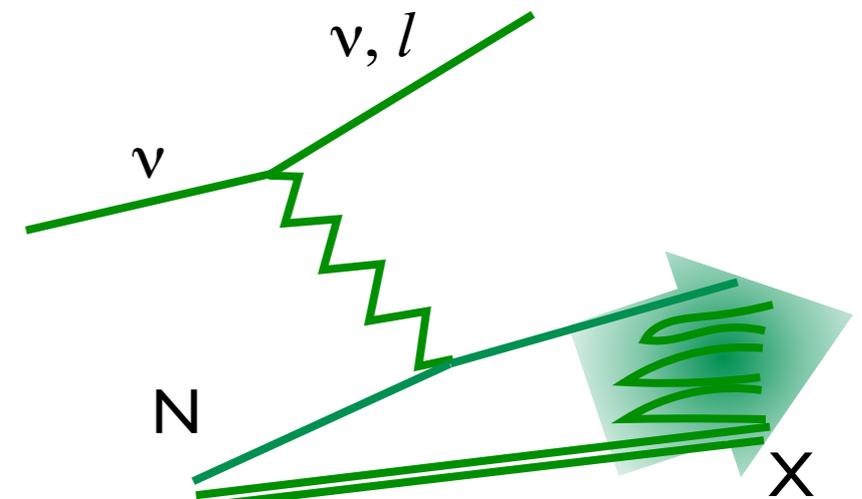
J.A. Formaggio, G.P. Zeller, Rev. Mod. Phys. 84 (2012) 1307

# Inelastic region

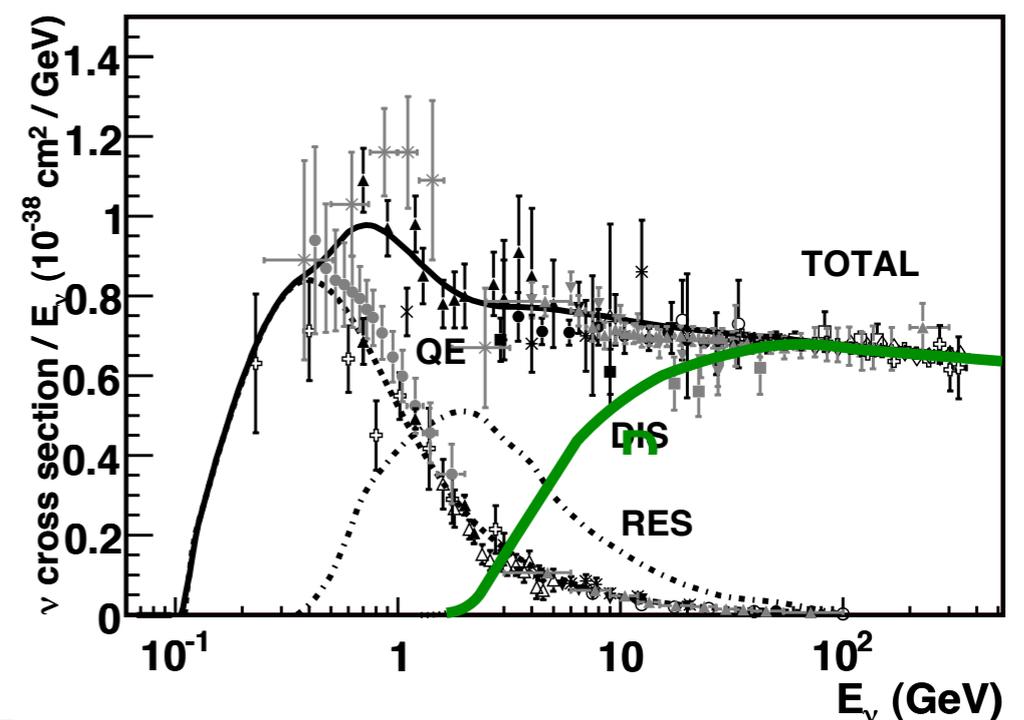
- In inelastic regime, quark PDFs of the nucleon control scattering cross-section
- Both resonances and DIS are important
- Multi-meson channels may become important
- Nuclear effects are different in  $\nu A$  vs.  $eA$
- DIS structure functions accessible in LQCD
  - Low moments of structure functions controlled

$$M_n = \int_{-1}^1 x^n f(x) dx, \quad n \lesssim 4$$

- x-dependence: systematics challenging, but rapid and exciting progress!



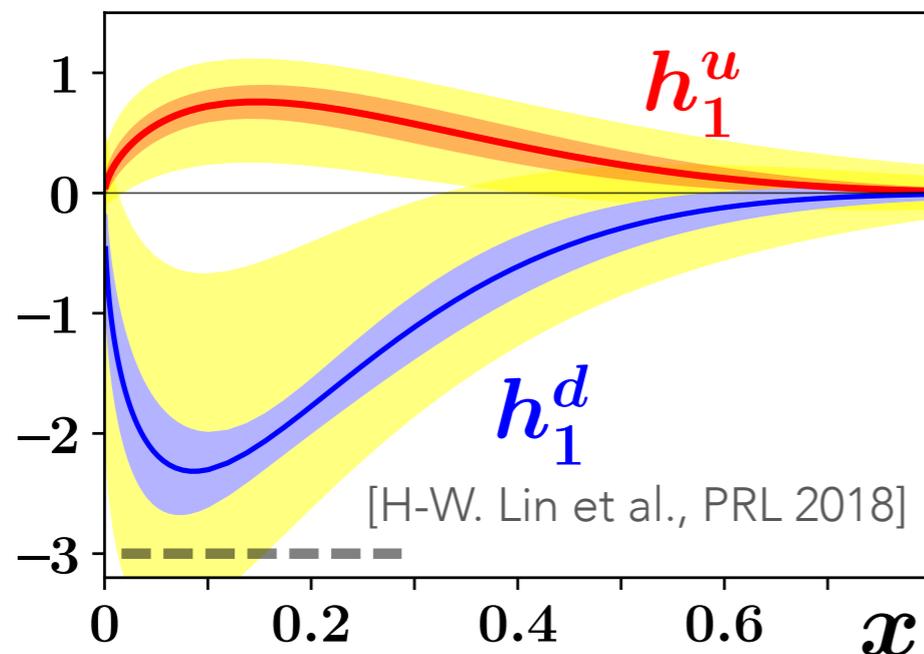
$\nu$  charged-current cross-section



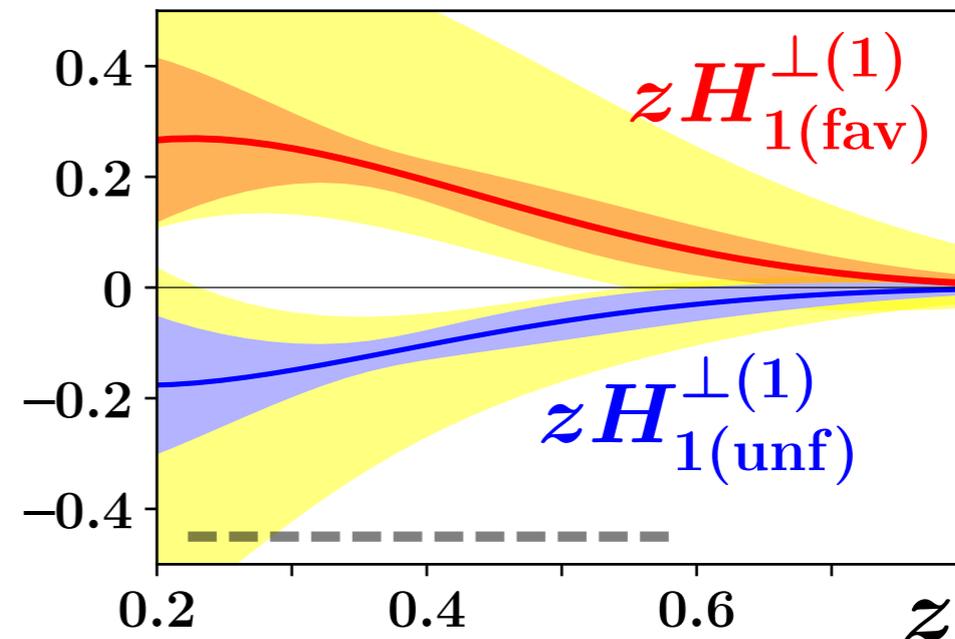
# Constraints on global PDF fits

- Including lattice QCD results for moments in global PDF fits can yield significant improvements
- Community white paper (LQCD + phenomenologists) assessed potential impacts [Lin et al., Prog. Part. Nucl. Phys 100 (2018), 107]

Transversity PDFs



Collins fragmentation functions

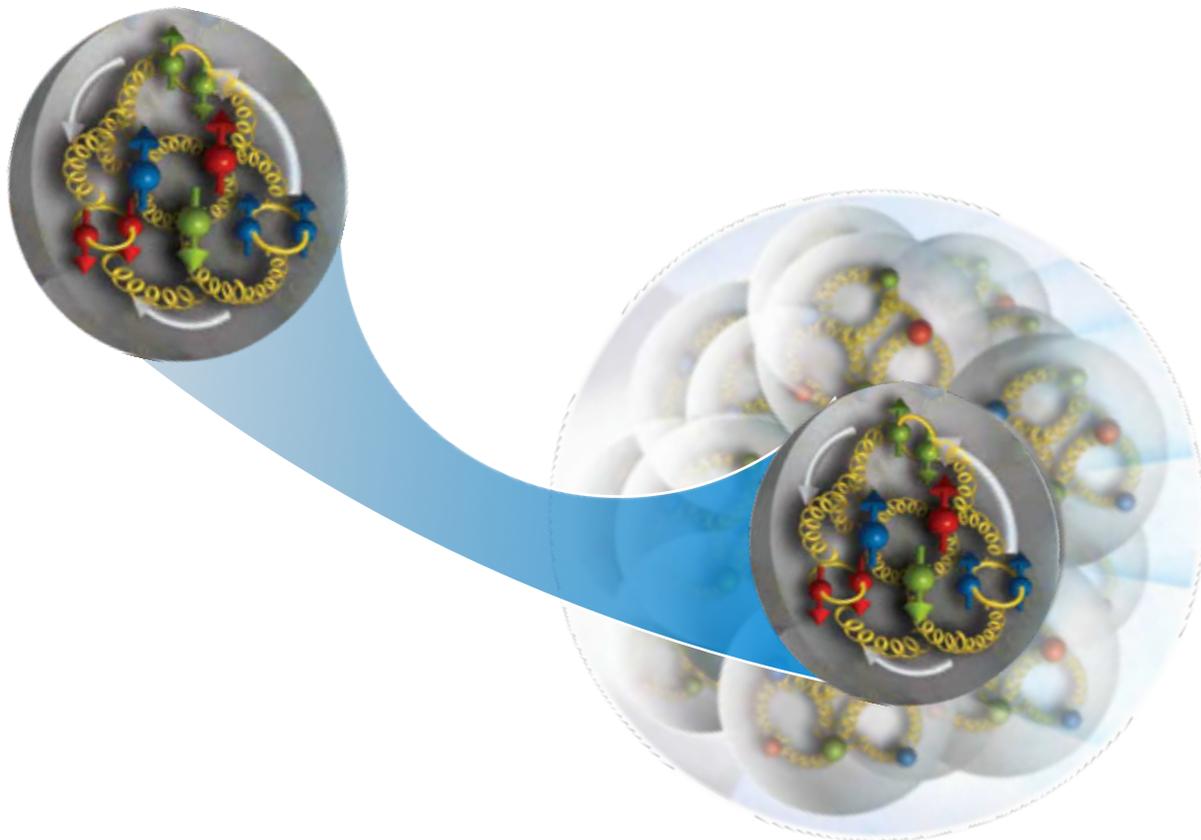


Yellow: SIDIS data only: direct constraints in region indicated by dashes  
 Blue/Red: SIDIS + lattice QCD for tensor charge (zeroth moment)

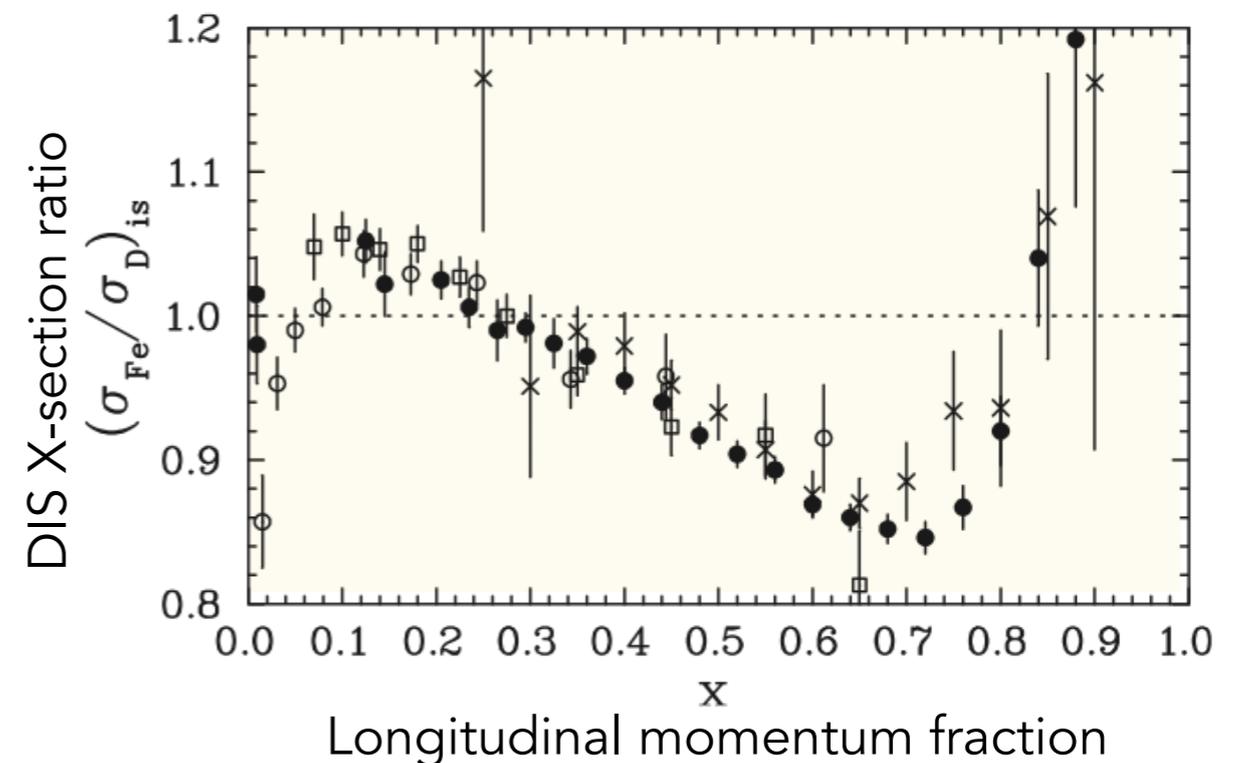
# EMC-type effects from Lattice QCD

Understanding the quark and gluon structure of matter

How is the partonic structure of nuclei different from that of nucleons?



Encoded in EMC-type effects

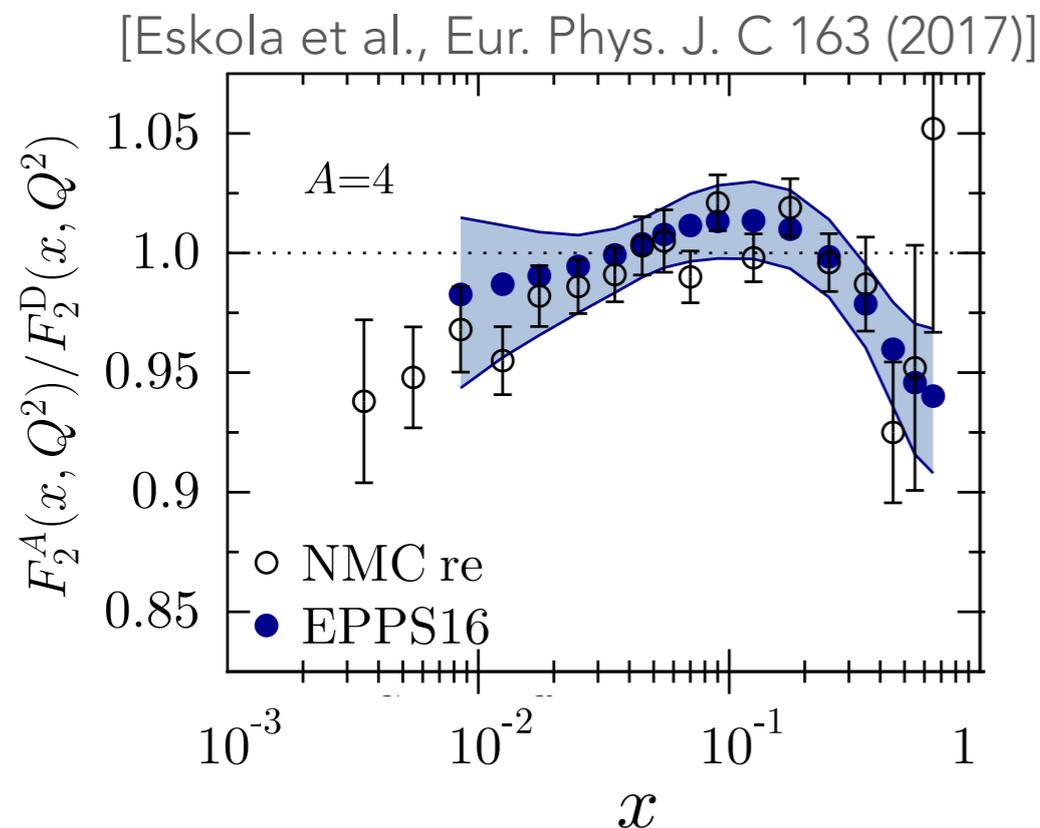


(EMC: Aubert et al., 1983)

# EMC effects in Mellin moments

First investigation of EMC-type effects from LQCD:  
Nuclear effects in Mellin moments of PDFs

- Calculable from local operators
- **BUT** EMC effects in moments are very small



Classic EMC effect is defined in  $F_2$ :

$$F_2(x, Q^2) = \sum_{q=u,d,s,\dots} x e_q^2 [q(x, Q^2) + \bar{q}(x, Q^2)]$$

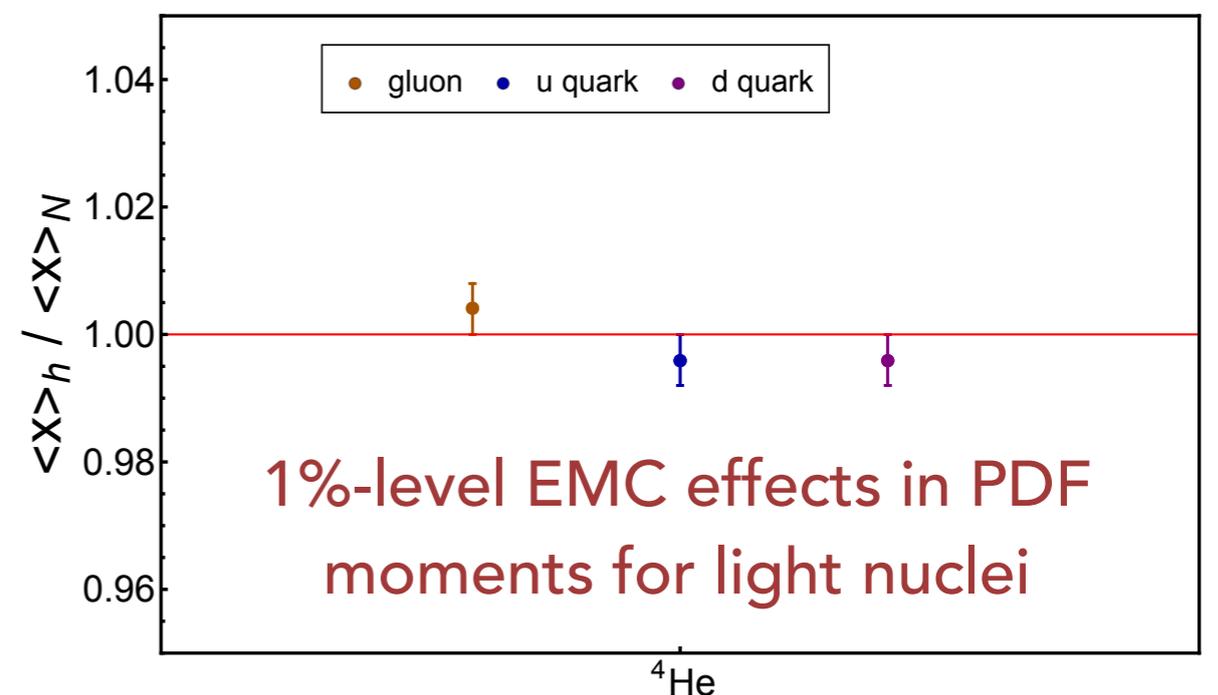
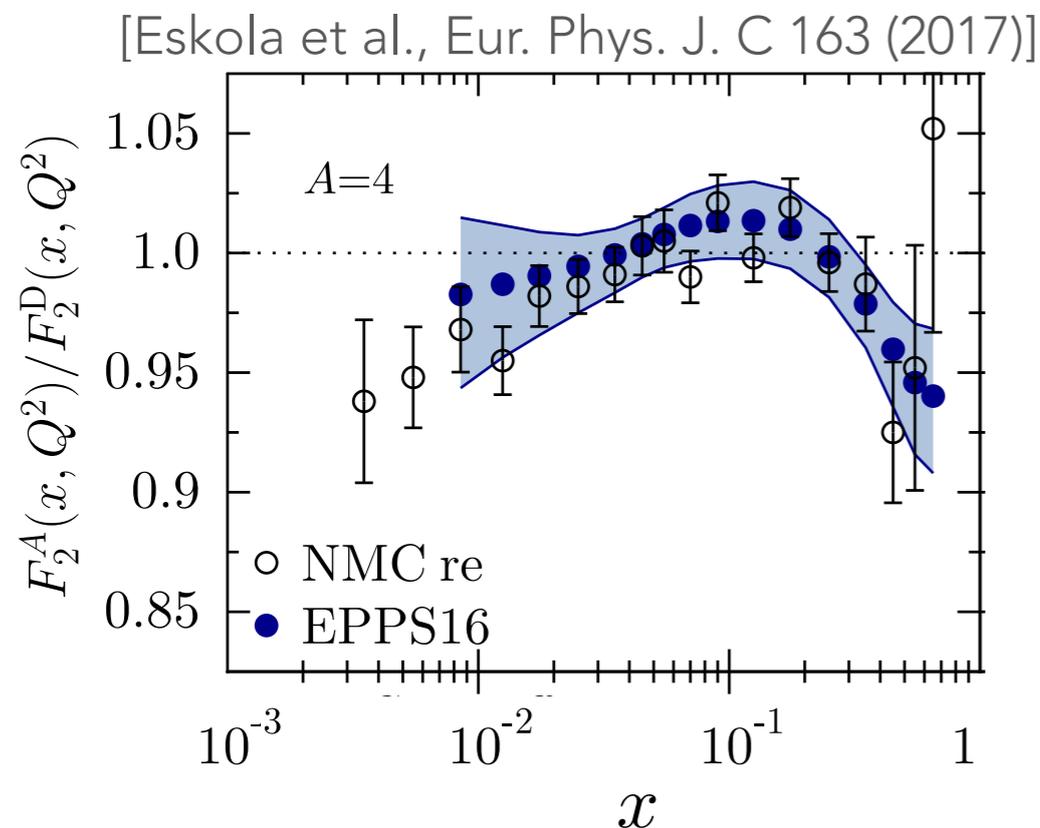
Number density of partons of flavour  $q$

→ x-integrals of numerator and denominator  $\int_0^1 dx x^n q(x, Q^2)$

# EMC effects in Mellin moments

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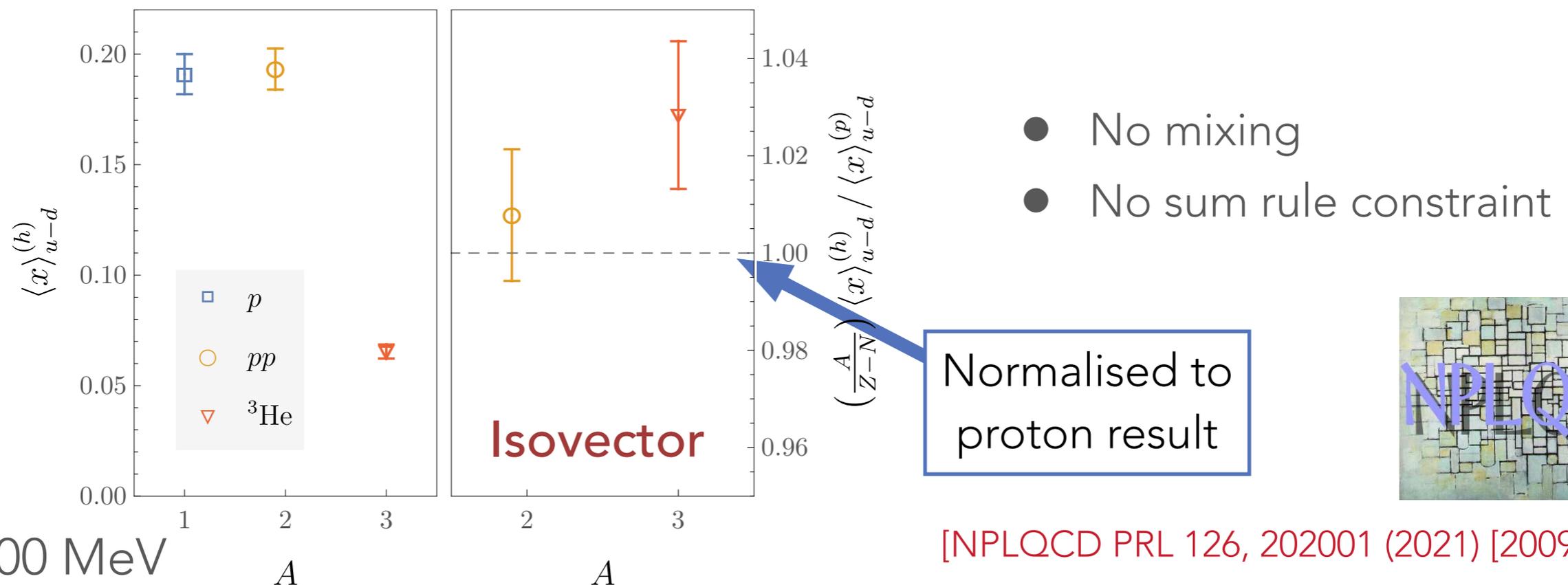
# Momentum fraction of nuclei

Matrix elements of the Energy-Momentum Tensor in light nuclei

→ first QCD determination of momentum fraction of nuclei

- Bounds on EMC effect in moments at ~few percent level, consistent with phenomenology [2009.05522 [hep-lat] (2021)]

## Ratio of quark momentum fraction in nucleus to nucleon



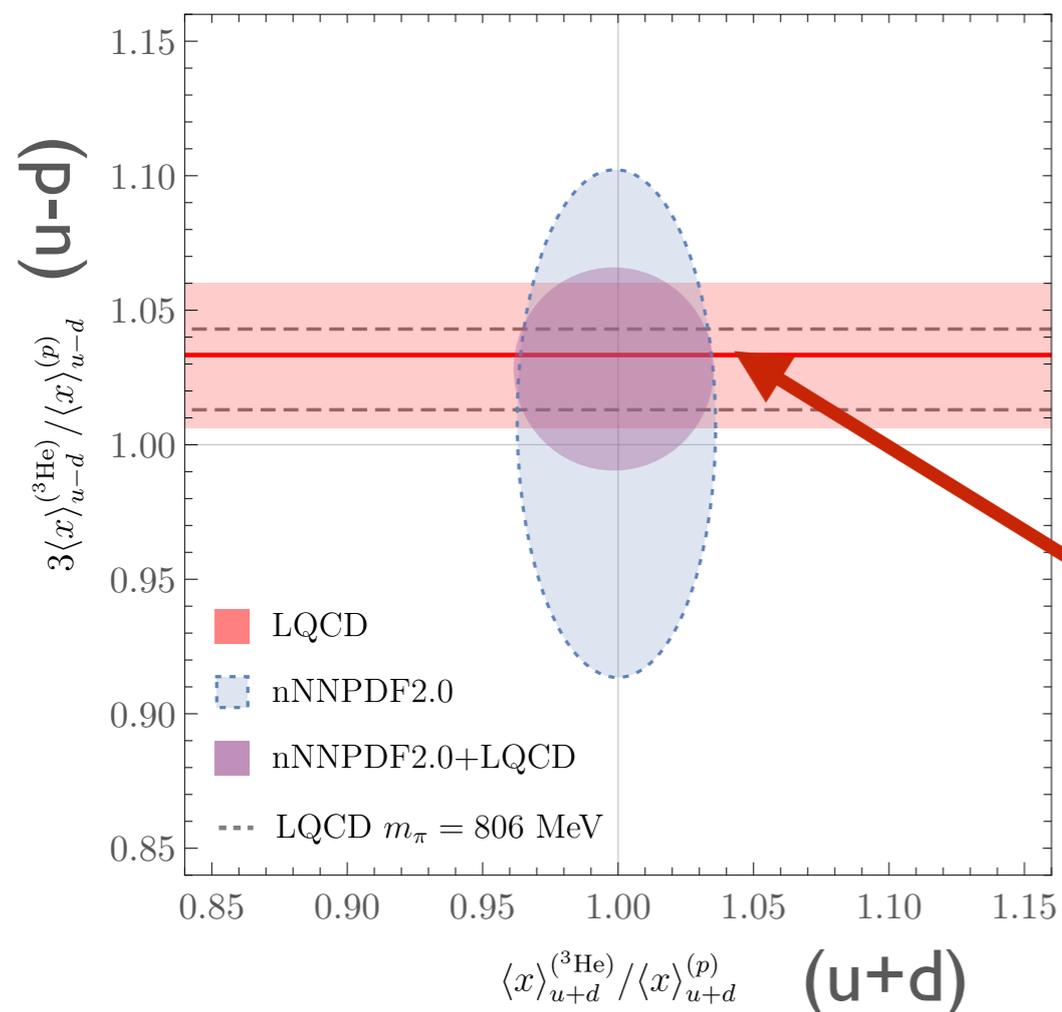
$m_\pi \sim 800$  MeV

# Momentum fraction of ${}^3\text{He}$

Matrix elements of the Energy-Momentum Tensor in light nuclei

→ first QCD determination of momentum fraction of nuclei

Ratio of  ${}^3\text{He}$  to proton momentum fractions



- Match isovector (u-d quark combination) momentum fraction to low-energy constants of effective field theory, extrapolate to physical quark masses
- Include into nNNPDF global fits of experimental lepton-nucleus scattering data

Blue → Purple:  
Improvement using theory constraints

[NPLQCD PRL 126, 202001 (2021) [2009.05522]]

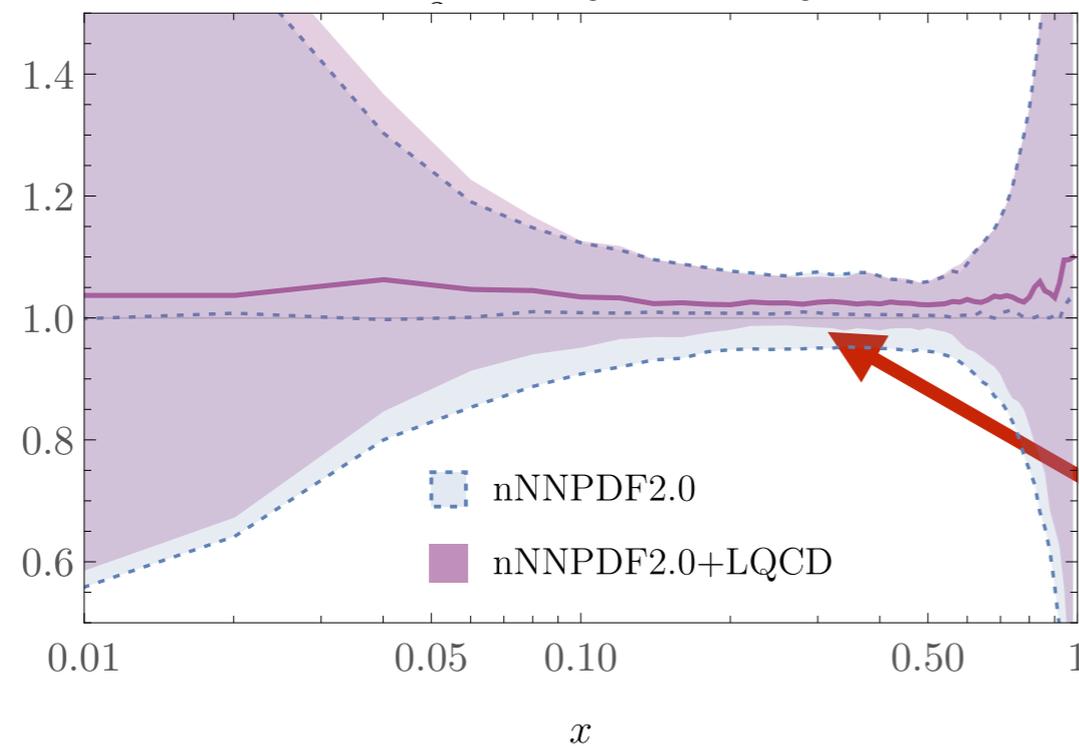
# Momentum fraction of $^3\text{He}$

Matrix elements of the Energy-Momentum Tensor in light nuclei

→ first QCD determination of momentum fraction of nuclei

Ratio of  $^3\text{He}$  to proton  
parton distributions

$$R^{(^3\text{He})}(x) = 3q_3^{(^3\text{He})}(x)/q_3^{(p)}(x)$$



- Match isovector (u-d quark combination) momentum fraction to low-energy constants of effective field theory, extrapolate to physical quark masses
- Include into nNNPDF global fits of experimental lepton-nucleus scattering data

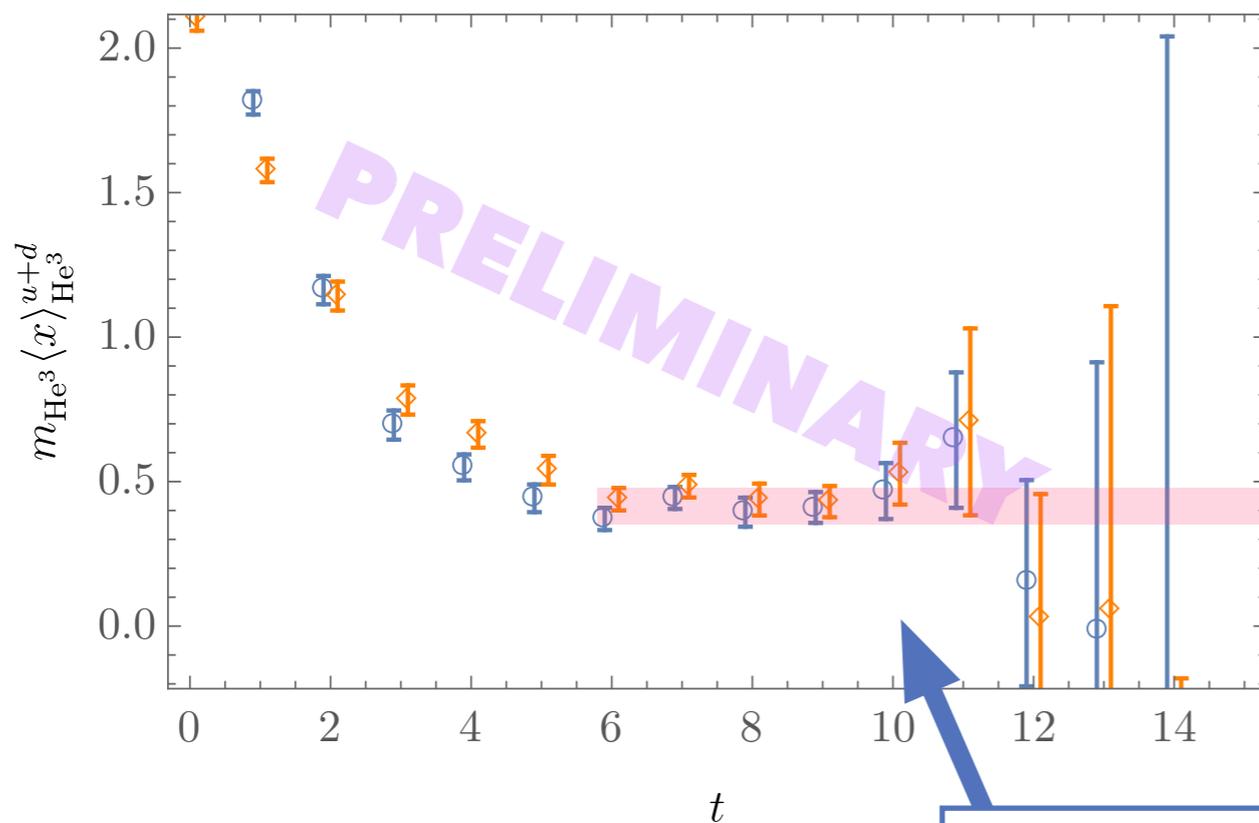
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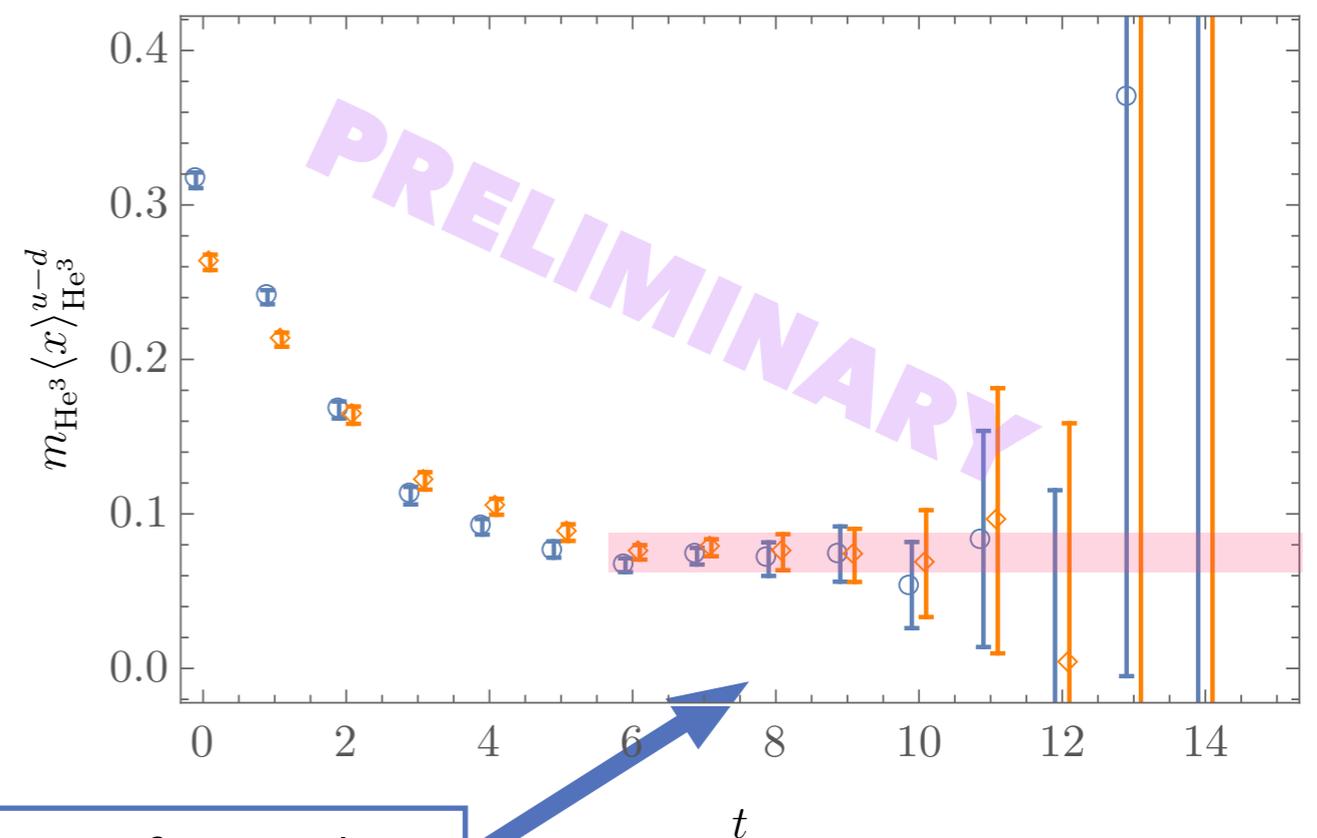
# Momentum fractions of nuclei

- Work in progress at close-to-physical values of the quark masses

Isoscalar



Isovector



First evidence of signals in physical-point data

- Polarised PDFs also accessible from moments



# Quasi-elastic scattering

Cross-section for quasi-elastic neutrino-nucleon scattering

$$\frac{d\sigma}{dQ^2} = \frac{G_f^2 M^2 \cos^2 \theta_C}{8\pi E_\nu^2} \left[ A \mp \frac{(s-u)}{M^2} B + \frac{(s-u)^2}{M^4} C \right]$$

$$A = \frac{(m^2 + Q^2)}{M^2} \left[ (1 + \tau) G_A^2 - (1 - \tau) F_1^2 + \tau(1 - \tau) F_2^2 + 4\tau F_1 F_2 - \frac{m^2}{4M^2} \left( (F_1 + F_2)^2 + (G_A + 2G_P)^2 - \left( \frac{Q^2}{M^2} + 4 \right) G_P^2 \right) \right]$$

$$B = \frac{Q^2}{M^2} G_A (F_1 + F_2)$$

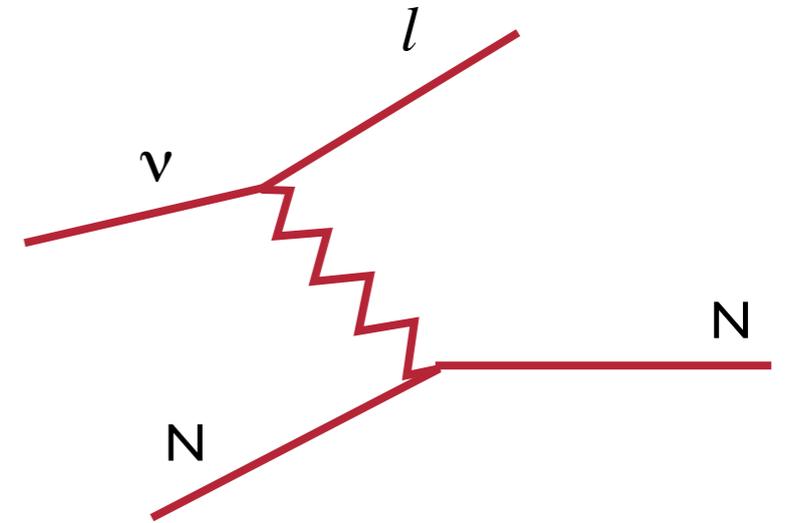
$$C = \frac{1}{4} (G_A^2 + F_1^2 + \tau F_2^2)$$

$G_A$

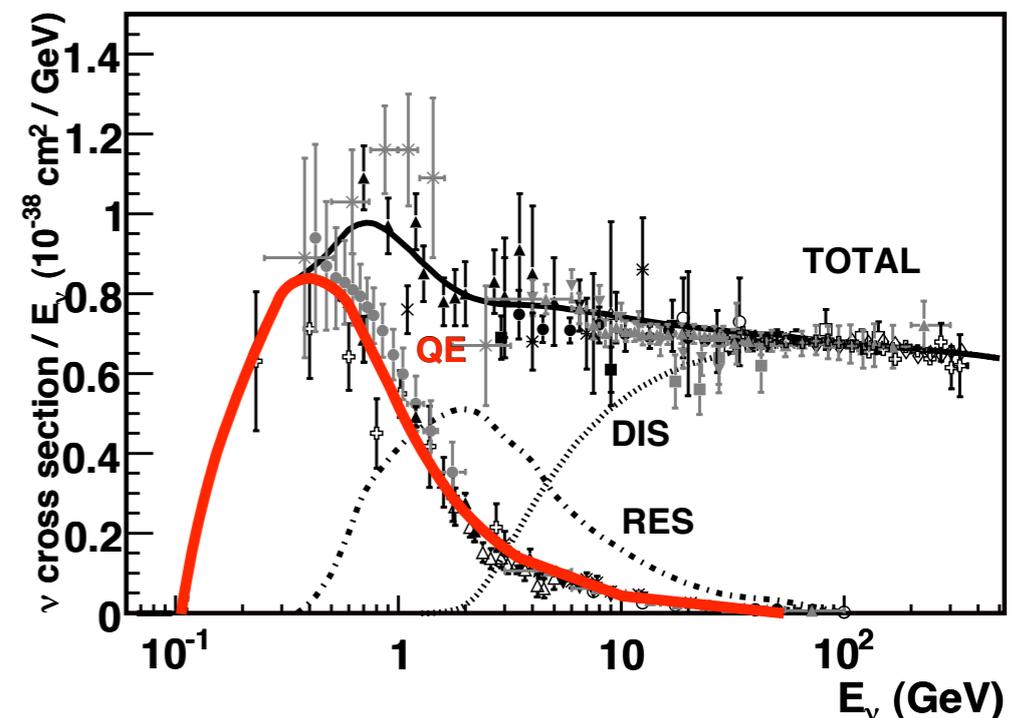
- dominant contribution
- largest uncertainty

$F_{1,2}$  Well-determined from electron scattering expts

$G_P$  can be related to  $G_A$  by pion pole dominance

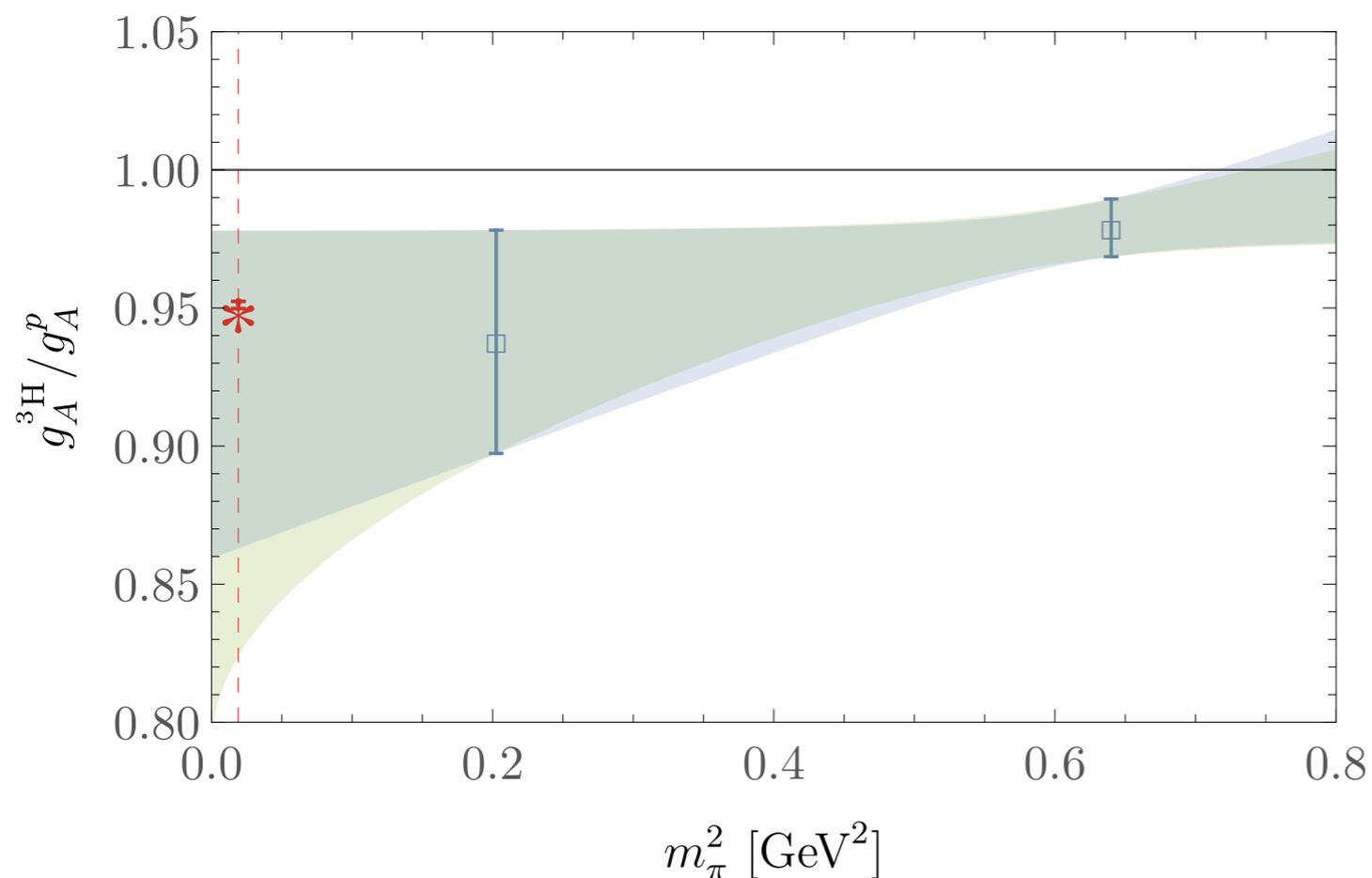


$\nu$  charged-current cross-section



# Axial charge of the triton

- No axial form factors of nuclei from lattice QCD yet
- Axial charge of He: first extrapolation to the physical quark masses this year

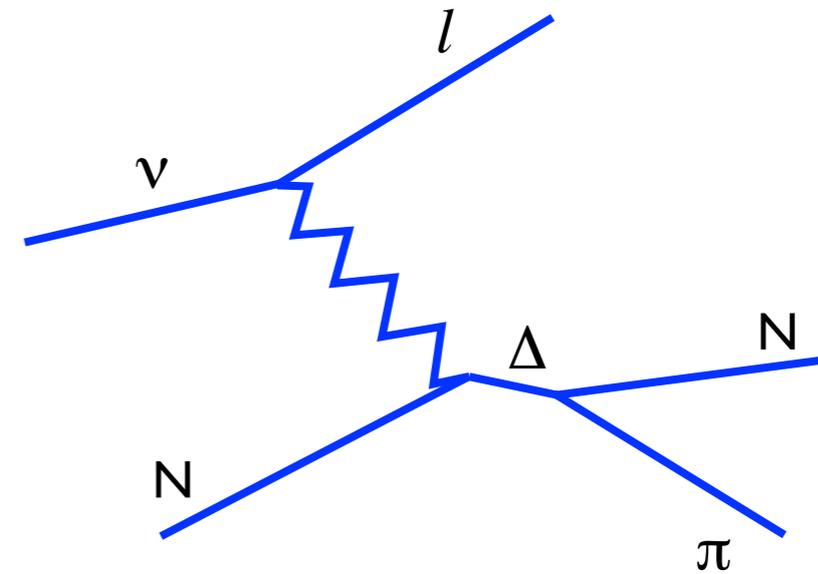


Development of finite-volume effective field theory for nuclear matrix elements allows connection to larger nuclei

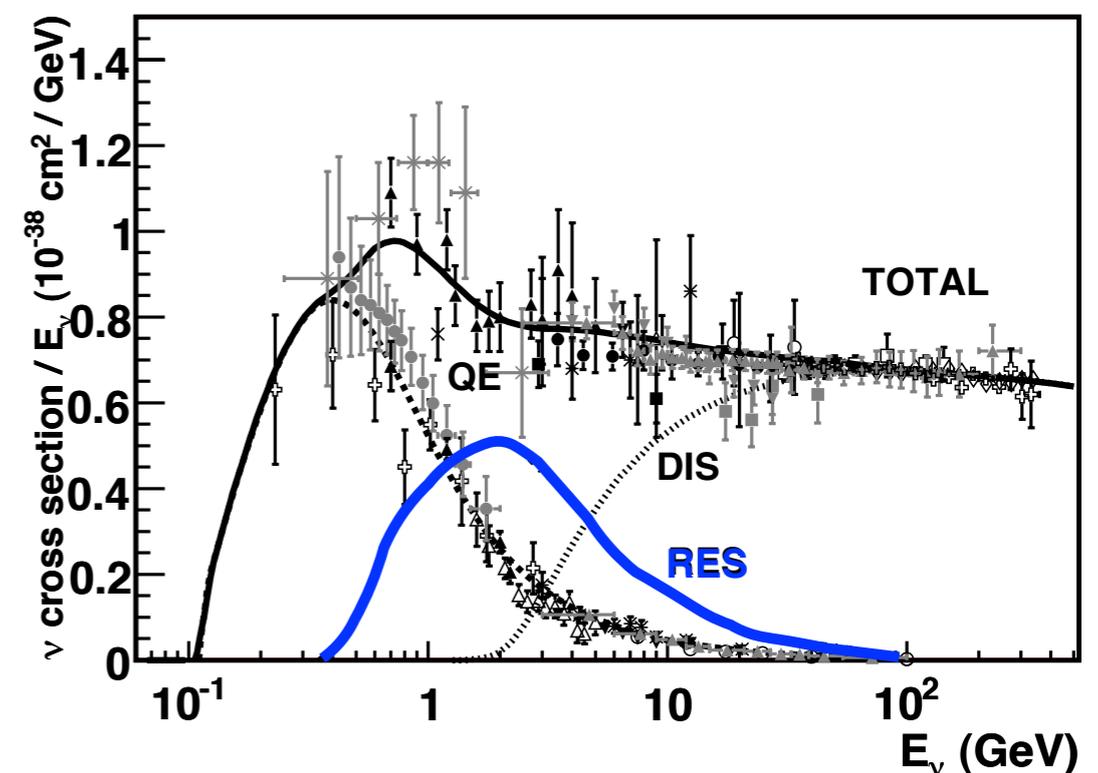
[Detmold & Shanahan, Phys.Rev.D 103, 074503 (2021) ]

# Resonance region

- Energies above  $\sim 200$  MeV, inelastic excitations from pion production:  $\Delta$  resonance dominant
- Very difficult to access experimentally  
Constrained only from PCAC
- QCD calculations possible:  
Need to account for unstable nature of resonance, extract  $N \rightarrow N\pi$  transition FFs
- Nuclear effects in transition FFs are beyond the scope of even exploratory lattice QCD calculations at this stage



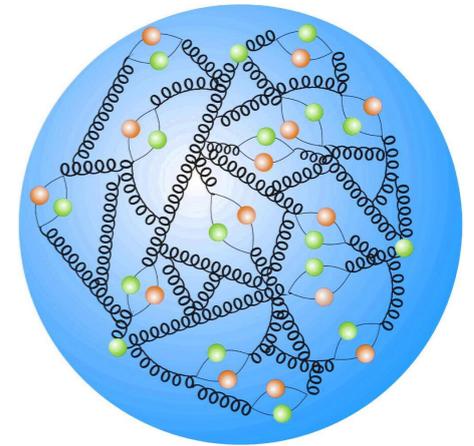
$\nu$  charged-current cross-section



# LQCD input for $\nu$ -nucleus interactions

1. Directly access QCD single-nucleon form factors without nuclear corrections

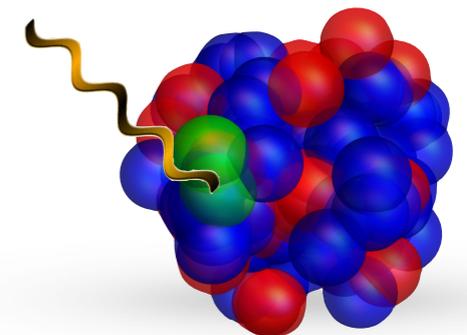
Reliable calculations with fully-controlled uncertainties



2. Calculate matrix elements in light nuclei from first principles

➔ EFT to reach heavy nuclear targets relevant to experiment

e.g., First calculations of axial charge of light nuclei, EMC effect in light nuclei



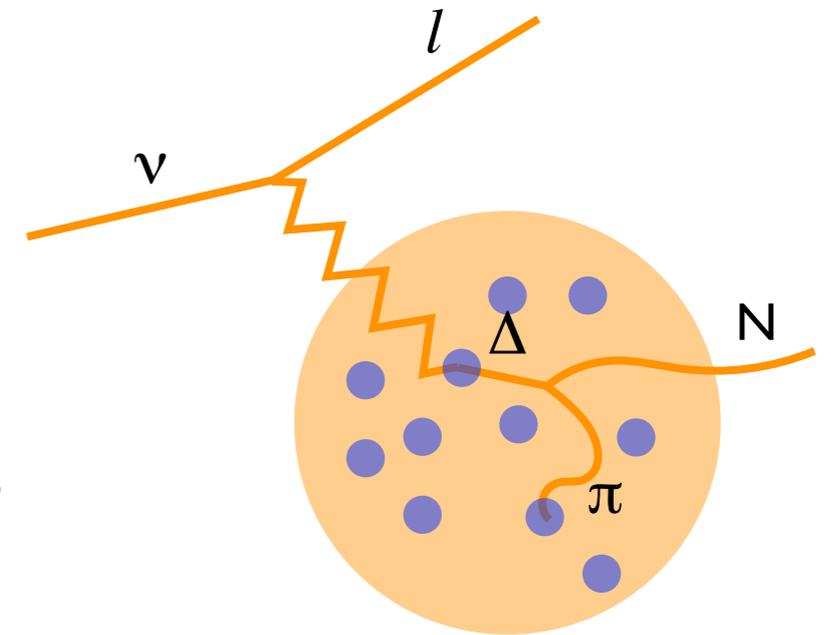
# LQCD input for $\nu$ -nucleus interactions

Constraints on nuclear matrix elements are possible:

- Pipeline well-defined and tested
- Still quite far from controlled calculations

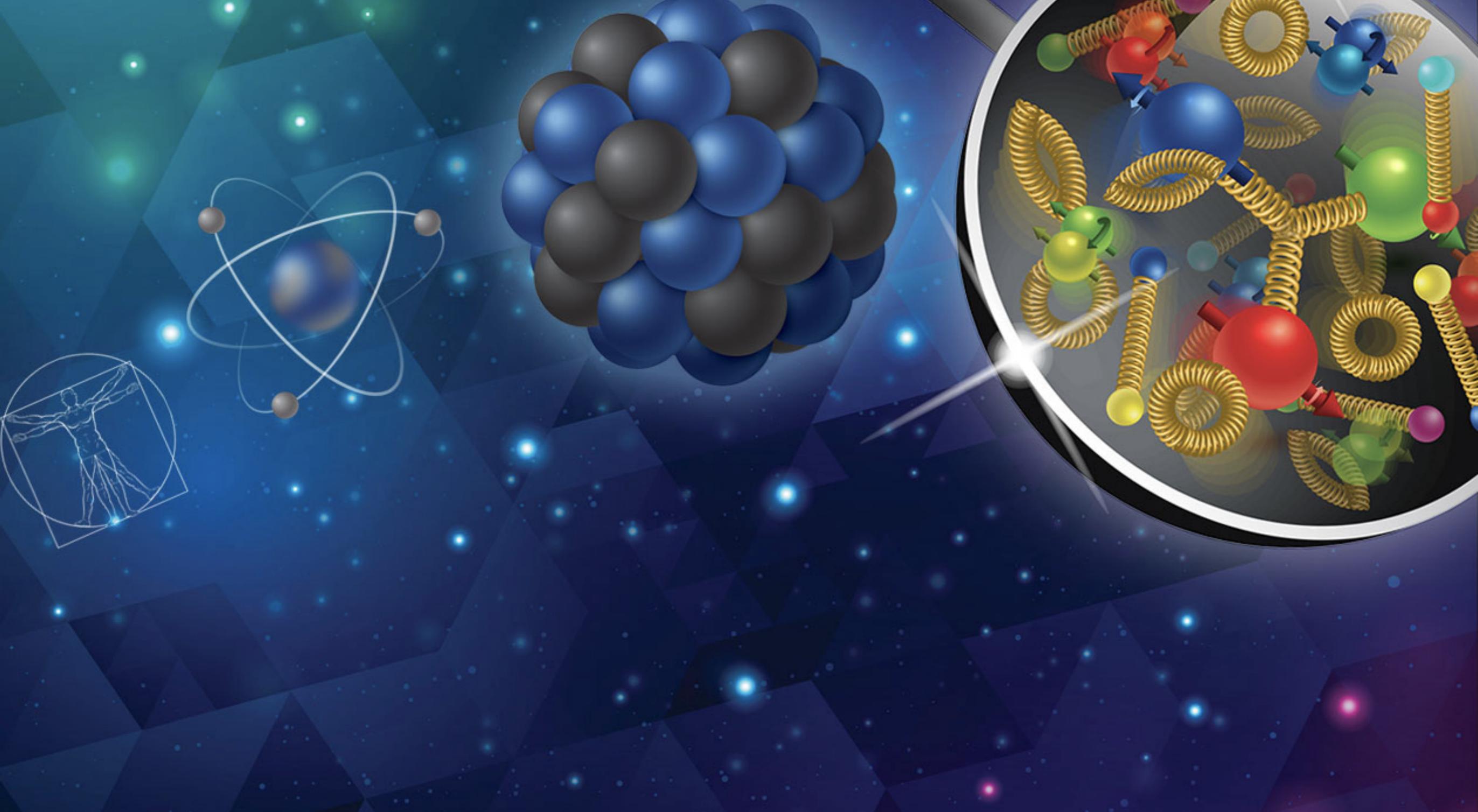
Controlled calculations achievable with  $\sim 10\text{-}20\%$  uncertainty in 10-year timeframe:

- Axial MEs of nuclei with  $A < 5$ , including form factors
- Constraints on nuclear PDFs of nuclei with  $A < 5$  via moments



Would require substantial investment of computing resources

What are community priorities?



Massachusetts  
Institute of  
Technology

