

RF2: Strange and light quarks

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Snowmass Day
September 23, 2021

Outline

3 main topics:

1. Rare η and η' decays
2. Rare Kaon Physics
3. First-row CKM unitarity and lepton universality tests

1. Rare η and η' decays

From S. Tulin

Upcoming experiments:

Jefferson Eta Factory (JEF) at Jefferson Lab – Hall D (approved)

	η	η'	
Tagged mesons	6.5×10^7	4.9×10^7	per 100 days

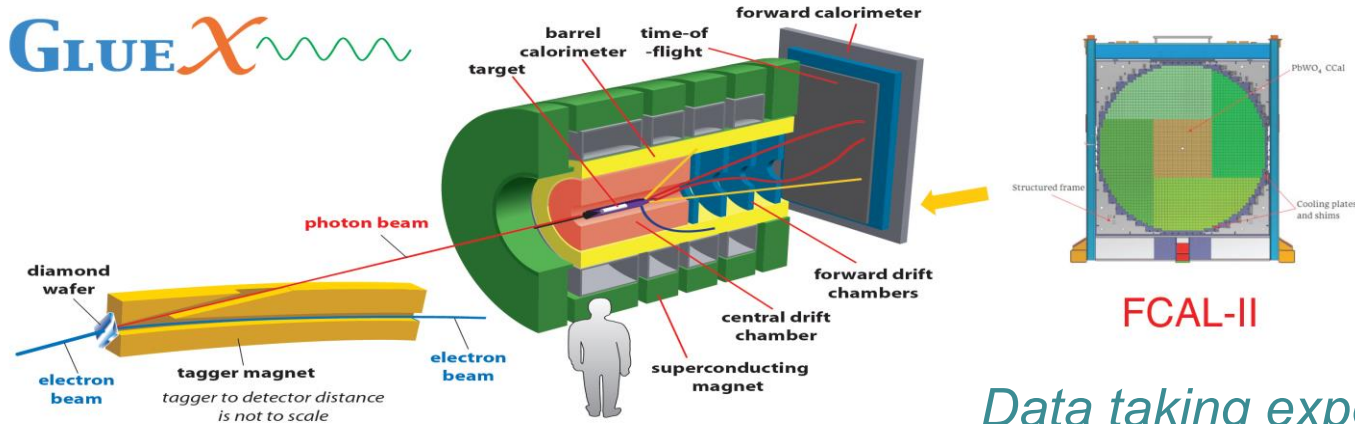
Rare Eta Decays with a TPC for Optical Photons (REDTOP) possibly at Fermilab (proposed)

Phase I (untagged mode)	2×10^{13}	10^{11}	per year
Phase II+ (tagged mode)	1×10^{13}	10^{11}	

Previous experiments:

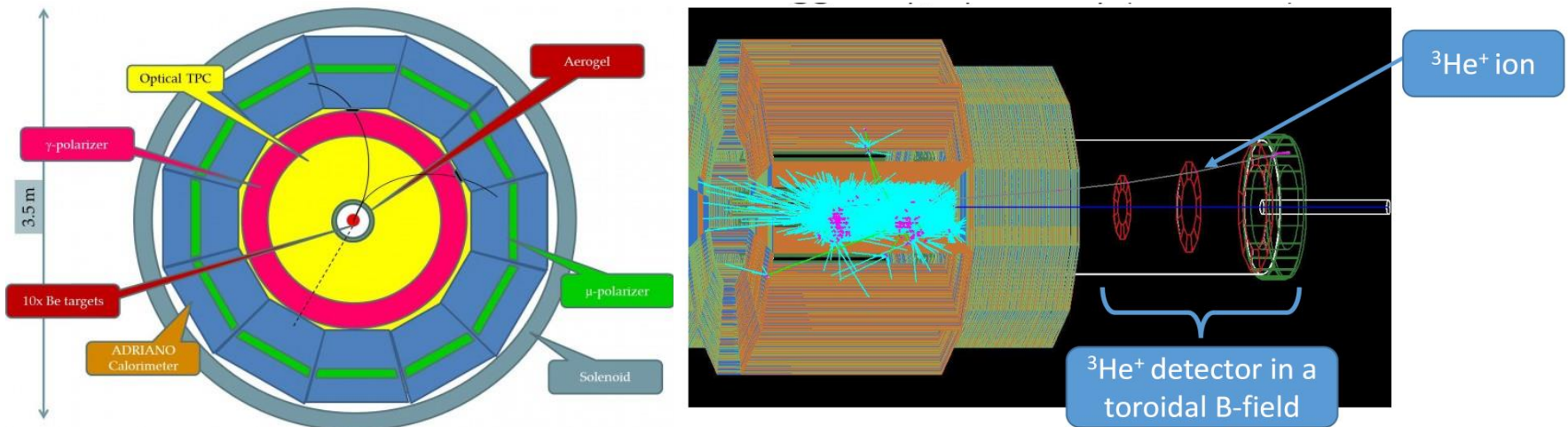
Experiment	Total η	Total η'
CB at AGS	10^7	-
CB MAMI-B	2×10^7	-
CB MAMI-C	6×10^7	10^6
WASA-COSY	$\sim 3 \times 10^7$ (p+d), $\sim 5 \times 10^8$ (p+p)	-
KLOE-II	3×10^8	5×10^5
BESIII	$\sim 10^7$	$\sim 5 \times 10^7$

Jefferson Eta Factory (JEF) experiment γ beam (10 GeV) on H target GlueX + upgraded forward calorimeter at Jefferson Lab (Hall D)



Data taking expected in 2024

Rare Eta Decays with a TPC for Optical Photons (REDTOP) Proton beam (1-3 GeV) on nuclear target (Be/D)



Very rich physics program at η and η' factories

From S. Tulin

RF/SNOWMASS21-RF6_RF2_Sean_Tulin-117.pdf

RF/SNOWMASS21-RF2_RF0_Sergi-085.pdf

Standard Model highlights

- Theory input for light-by-light scattering for $(g-2)_\mu$
- Extraction of light quark masses
- QCD scalar dynamics

Fundamental symmetry tests

- P,CP violation
- C,CP violation

[Kobzarev & Okun (1964), Prentki & Veltman (1965), Lee (1965), Lee & Wolfenstein (1965), Bernstein et al (1965)]

Dark sectors (MeV—GeV)

- Vector bosons
- Scalars
- Pseudoscalars (ALPs)

(Plus other channels that have not been searched for to date)

Channel	Expt. branching ratio	Discussion
$\eta \rightarrow 2\gamma$	39.41(20)%	chiral anomaly, η - η' mixing
$\eta \rightarrow 3\pi^0$	32.68(23)%	$m_u - m_d$
$\eta \rightarrow \pi^0\gamma\gamma$	$2.56(22) \times 10^{-4}$	χ PT at $O(p^6)$, leptophobic B boson, light Higgs scalars
$\eta \rightarrow \pi^0\pi^0\gamma\gamma$	$< 1.2 \times 10^{-3}$	χ PT, axion-like particles (ALPs)
$\eta \rightarrow 4\gamma$	$< 2.8 \times 10^{-4}$	$< 10^{-11}$ [52]
$\eta \rightarrow \pi^+\pi^-\pi^0$	22.92(28)%	$m_u - m_d$, C/CP violation, light Higgs scalars
$\eta \rightarrow \pi^+\pi^-\gamma$	4.22(8)%	chiral anomaly, theory input for singly-virtual TFF and $(g-2)_\mu$, P/CP violation
$\eta \rightarrow \pi^+\pi^-\gamma\gamma$	$< 2.1 \times 10^{-3}$	χ PT, ALPs
$\eta \rightarrow e^+e^-\gamma$	$6.9(4) \times 10^{-3}$	theory input for $(g-2)_\mu$, dark photon, protophobic X boson
$\eta \rightarrow \mu^+\mu^-\gamma$	$3.1(4) \times 10^{-4}$	theory input for $(g-2)_\mu$, dark photon
$\eta \rightarrow e^+e^-$	$< 7 \times 10^{-7}$	theory input for $(g-2)_\mu$, BSM weak decays
$\eta \rightarrow \mu^+\mu^-$	$5.8(8) \times 10^{-6}$	theory input for $(g-2)_\mu$, BSM weak decays, P/CP violation
$\eta \rightarrow \pi^0\pi^0\ell^+\ell^-$		C/CP violation, ALPs
$\eta \rightarrow \pi^+\pi^-e^+e^-$	$2.68(11) \times 10^{-4}$	theory input for doubly-virtual TFF and $(g-2)_\mu$, P/CP violation, ALPs
$\eta \rightarrow \pi^+\pi^-\mu^+\mu^-$	$< 3.6 \times 10^{-4}$	theory input for doubly-virtual TFF and $(g-2)_\mu$, P/CP violation, ALPs
$\eta \rightarrow e^+e^-e^+e^-$	$2.40(22) \times 10^{-5}$	theory input for $(g-2)_\mu$
$\eta \rightarrow e^+e^-\mu^+\mu^-$	$< 1.6 \times 10^{-4}$	theory input for $(g-2)_\mu$
$\eta \rightarrow \mu^+\mu^-\mu^+\mu^-$	$< 3.6 \times 10^{-4}$	theory input for $(g-2)_\mu$
$\eta \rightarrow \pi^+\pi^-\pi^0\gamma$	$< 5 \times 10^{-4}$	direct emission only
$\eta \rightarrow \pi^\pm e^\mp \nu_e$	$< 1.7 \times 10^{-4}$	second-class current
$\eta \rightarrow \pi^+\pi^-$	$< 4.4 \times 10^{-6}$ [53]	P/CP violation
$\eta \rightarrow 2\pi^0$	$< 3.5 \times 10^{-4}$	P/CP violation
$\eta \rightarrow 4\pi^0$	$< 6.9 \times 10^{-7}$	P/CP violation

Gan, Kubis, Passemar, ST
[arxiv:2007.00664]

2. Rare kaon decays

Situation before ICHEP 2020

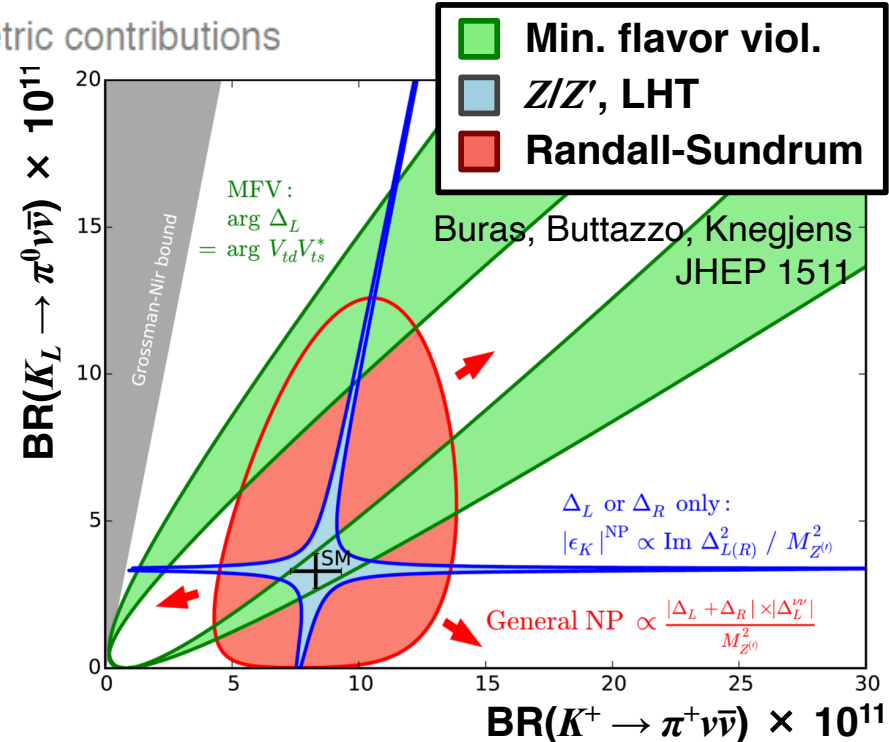
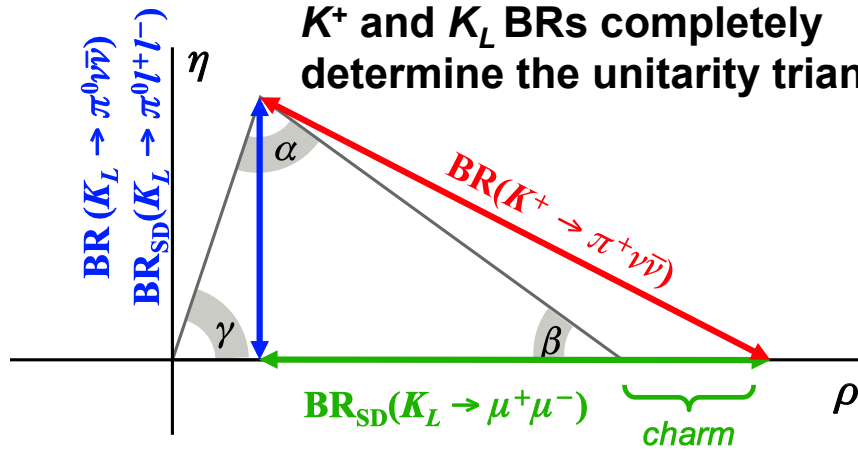
Decay	$\Gamma_{\text{SD}}/\Gamma$	Theory err.*	SM BR $\times 10^{11}$	Exp. BR $\times 10^{11}$
$K_L \rightarrow \mu^+\mu^-$	10%	30%	79 ± 12 (SD)	684 ± 11
$K_L \rightarrow \pi^0 e^+ e^-$	40%	10%	3.2 ± 1.0	< 28 (@ 90% CL)
$K_L \rightarrow \pi^0 \mu^+ \mu^-$	30%	15%	1.5 ± 0.3	< 38
$K^+ \rightarrow \pi^+ \nu \bar{\nu}$	90%	4%	8.4 ± 1.0	< 17.8
$K_L \rightarrow \pi^0 \nu \bar{\nu}$	$> 99\%$	2%	3.4 ± 0.6	< 300

Theory err.
under control
→ Plan from
lattice QCD

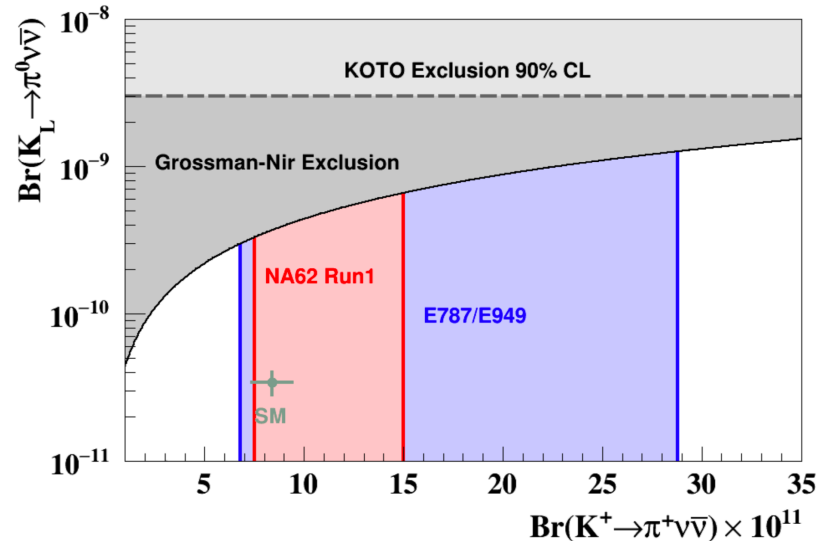
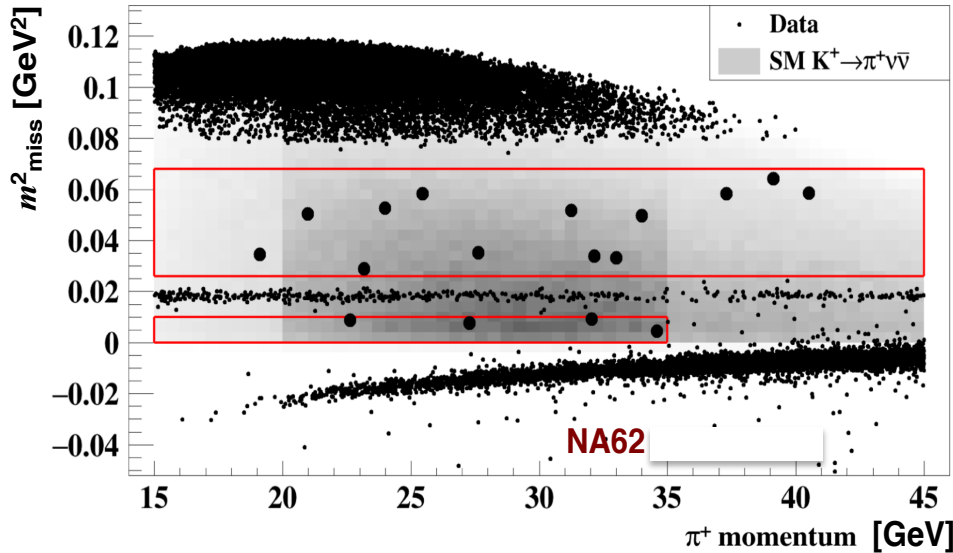
*Approx. error on LD-subtracted rate excluding parametric contributions

Golden channel: $K \rightarrow \pi \nu \bar{\nu}$

Very suppressed in the SM, through FCNC
High sensitivity to BSM : corr. K_L and K^+



With 2018 data



NA62 experiment:

$$BR(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = \left(10.6^{+4}_{-3.4} \Big|_{stat} \pm 0.9_{syst} \right) \times 10^{-11}$$

- Run 1 (2016-2018) :
Expected signal (SM): 10 events, Expected background: 7 events
Total observed: 20 events, 3.4 σ significance
- Plans for NA62 Run 2 (from LS2 to LS3): Data taking resume in July 2021 with
 - Key modifications to reduce background
 - Higher beam intensity: 70% \rightarrow 100%



Expect to measure $BR(K^+ \rightarrow \pi^+ \nu \bar{\nu})$ to better than 20%

KOTO experiment: *PRL 126, 121801'21*

- Limit based on 2016-2018 data:

$$BR(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 4.9 \times 10^{-9} \text{ (90\% C.L.)}$$

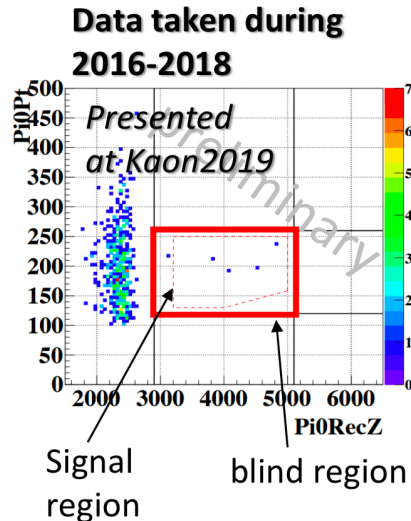
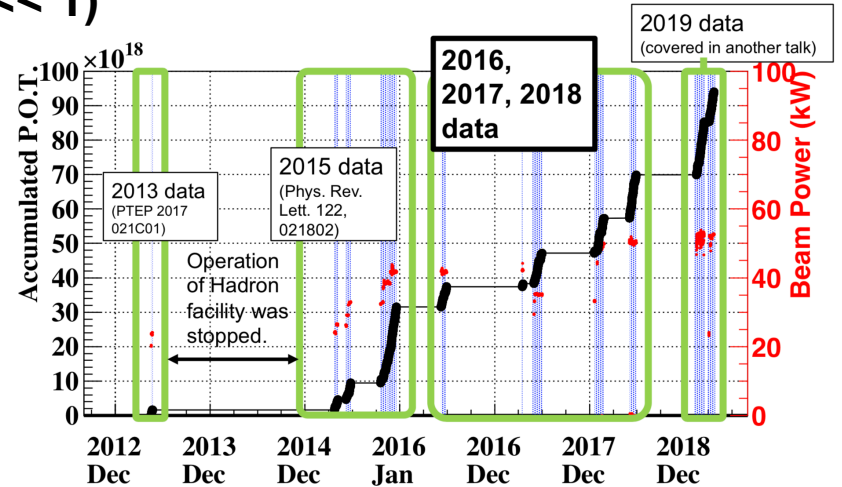
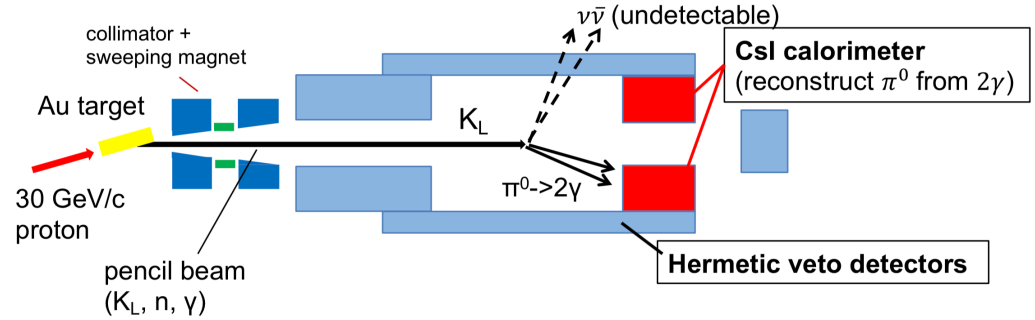
3 events observed in signal region

- Blind analysis of 2016-2018 data:

4 events in the signal region (expected $\ll 1$)

- * 1 event from mistake in cut application
- * Additional background from charged kaon decay identified
- * Upstream detector needed to veto K^+ :
 Prototype installed for 2020 run and
 Design in progress for higher efficiency UCV

$$K_L \rightarrow \pi^0 \nu \bar{\nu} : (\pi^0 \rightarrow) 2\gamma + \text{nothing}$$



KOTO Step-1 expects to reach SM single event sensitivity by 2025

Plots from Shinohara, KAON 2019 and Shimizu, ICHEP 2020

LHCb experiment:

- LHCb expanding its physics reach towards strange physics complementary to the core program

Sensitivity Studies [ArXiv:1808.03477](https://arxiv.org/abs/1808.03477)

- Encouraging Run 1-2 results on $K_S^0 \rightarrow \mu^+ \mu^-$ and $\Sigma^+ \rightarrow p \mu^+ \mu^-$

- Large samples available on tape

- Run 2 giving new results with improved trigger

- Upgrade trigger
 unprecedented sensitivities on many channels

- Complementary to K_L and K^+ dedicated experiments


LHCb major player for K_S and hyperons rare decays

Channel	\mathcal{R}	ϵ_L	ϵ_D	$\sigma_L(\text{MeV}/c^2)$	$\sigma_D(\text{MeV}/c^2)$
$K_S^0 \rightarrow \mu^+ \mu^-$	1	1.0 (1.0)	1.8 (1.8)	~ 3.0	~ 8.0
$K_S^0 \rightarrow \pi^+ \pi^-$	1	1.1 (0.30)	1.9 (0.91)	~ 2.5	~ 7.0
$K_S^0 \rightarrow \pi^0 \mu^+ \mu^-$	1	0.93 (0.93)	1.5 (1.5)	~ 35	~ 45
$K_S^0 \rightarrow \gamma \mu^+ \mu^-$	1	0.85 (0.85)	1.4 (1.4)	~ 60	~ 60
$K_S^0 \rightarrow \mu^+ \mu^- \mu^+ \mu^-$	1	0.37 (0.37)	1.1 (1.1)	~ 1.0	~ 6.0
$K_L^0 \rightarrow \mu^+ \mu^-$	~ 1	$2.7 (2.7) \times 10^{-3}$	0.014 (0.014)	~ 3.0	~ 7.0
$K^+ \rightarrow \pi^+ \pi^+ \pi^-$	~ 2	$9.0 (0.75) \times 10^{-3}$	$41 (8.6) \times 10^{-3}$	~ 1.0	~ 4.0
$K^+ \rightarrow \pi^+ \mu^+ \mu^-$	~ 2	$6.3 (2.3) \times 10^{-3}$	0.030 (0.014)	~ 1.5	~ 4.5
$\Sigma^+ \rightarrow p \mu^+ \mu^-$	~ 0.13	0.28 (0.28)	0.64 (0.64)	~ 1.0	~ 3.0
$\Lambda \rightarrow p \pi^-$	~ 0.45	0.41 (0.075)	1.3 (0.39)	~ 1.5	~ 5.0
$\Lambda \rightarrow K_S^0 \rightarrow \mu^+ \mu^-$	~ 0.45	0.32 (0.31)	0.88 (0.86)	–	–
$\Xi^- \rightarrow \Sigma^0 \mu^- \bar{\nu}_\mu$	~ 0.04	$39 (5.7) \times 10^{-3}$	0.27 (0.09)	–	–
$\Xi^- \rightarrow \Sigma^0 \mu^- \bar{\nu}_\mu$	~ 0.03	$24 (4.9) \times 10^{-3}$	0.21 (0.068)	–	–
$\Xi^- \rightarrow p \pi^- \pi^-$	~ 0.03	0.41 (0.05)	0.94 (0.20)	~ 3.0	~ 9.0
$\Xi^0 \rightarrow p \pi^-$	~ 0.03	1.0 (0.48)	2.0 (1.3)	~ 5.0	~ 10
$\Omega^- \rightarrow \Lambda \pi^-$	~ 0.001	$95 (6.7) \times 10^{-3}$	0.32 (0.10)	~ 7.0	~ 20
Channel	\mathcal{R}	ϵ_L	ϵ_D	$\sigma_L(\text{MeV}/c^2)$	$\sigma_D(\text{MeV}/c^2)$
$K_S^0 \rightarrow \pi^+ \pi^- e^+ e^-$	1	1.0 (0.18)	2.83 (1.1)	~ 2.0	~ 10
$K_S^0 \rightarrow \mu^+ \mu^- e^+ e^-$	1	1.18 (0.48)	2.93 (1.4)	~ 2.0	~ 11
$K^+ \rightarrow \pi^+ e^- e^+$	~ 2	0.04 (0.01)	0.17 (0.06)	~ 3.0	~ 13
$\Sigma^+ \rightarrow p e^+ e^-$	~ 0.13	1.76 (0.56)	3.2 (1.3)	~ 3.5	~ 11
$\Lambda \rightarrow p \pi^- e^+ e^-$	~ 0.45	$< 2.2 \times 10^{-4}$	$\sim 17 (< 2.2) \times 10^{-4}$	–	–
Channel	\mathcal{R}	ϵ_L	ϵ_D	$\sigma_L(\text{MeV}/c^2)$	$\sigma_D(\text{MeV}/c^2)$
$K_S^0 \rightarrow \mu^+ e^-$	1	1.0 (0.84)	1.5 (1.3)	~ 3.0	~ 8.0
$K_L^0 \rightarrow \mu^+ e^-$	1	$3.1 (2.6) \times 10^{-3}$	$13 (11) \times 10^{-3}$	~ 3.0	~ 7.0
$K^+ \rightarrow \pi^+ \mu^+ e^-$	~ 2	$3.1 (1.1) \times 10^{-3}$	$16 (8.5) \times 10^{-3}$	~ 2.0	~ 7.0

\mathcal{R} = ratio of production

ϵ = ratio of efficiencies

Next Generation experiments:

- Required to make a precision measurement $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ and to make a significant observation of $K_L \rightarrow \pi^0 \nu \bar{\nu}$
 - Would become a very high priority if hints of new physics from NA62 or KOTO
 - In absence of hints, more precise measurements  potential discovery
- **High intensity K^+ and K_L beams at SPS, CERN :** RF/SNOWMASS21-RF2_RF0-010.pdf
3 phases with same primary beamline and interchangeable detectors
 1. “NA62x4”: $K^+ \rightarrow \pi^+ \nu \bar{\nu}$
 2. KLEVER: $K_L \rightarrow \pi^0 \nu \bar{\nu}$
 3. Intermediate stage: K_L beam + charged-particle tracking/PID:
 $K_L \rightarrow \pi^0 \mu^+ \mu^-$; LFV and radiative K_L decays

$K \rightarrow \pi \nu \bar{\nu}$ and $K \rightarrow (\pi) \mu e$ offer complementary tests for discrepancies observed in B decays
- **KOTO Step-2**
 - construction around 2025 and ~ 100 events at SM level with $S/N \sim 1$ (3y data).
 - Two major upgrades :
 - Higher kaon flux: reduce targeting angle from 16 degrees to 5 degrees, increase target length from 60 mm to 102 mm
 - Increase detector acceptance: increase calorimeter radius from 2 m to 3 m, increase fiducial region from 2 m to ~ 15 m

Next Generation experiments:

- **Fermilab based experiment?**
 - Well-developed proposals exist
 - Could be enabled by planned upgrades to Fermilab accelerator complex

Potential Snowmass message from Rare & Precision Frontier: *design FNAL upgrades to facilitate a broad physics program*
- **Examples of opportunities for discussion and high-level cooperation:**
 - Detector ideas and R&D: Calorimeters with photon vectoring; in-beam vetoes; signal processing and readout
 - Simulation: Benchmarking for MC and event generators; techniques for generation of large samples
- **Message from US Kaon LOI:** Both out of intellectual interest and a desire to maintain breadth in the US physics program, the US kaon physics community would like to explore possibilities for expanded US participation in the current and next-generation rare kaon decay experiments at JPARC and CERN. We would also like to hold open the possibility for more major contributions to these experiments or for a complementary US-based experiment if the science points in that direction.

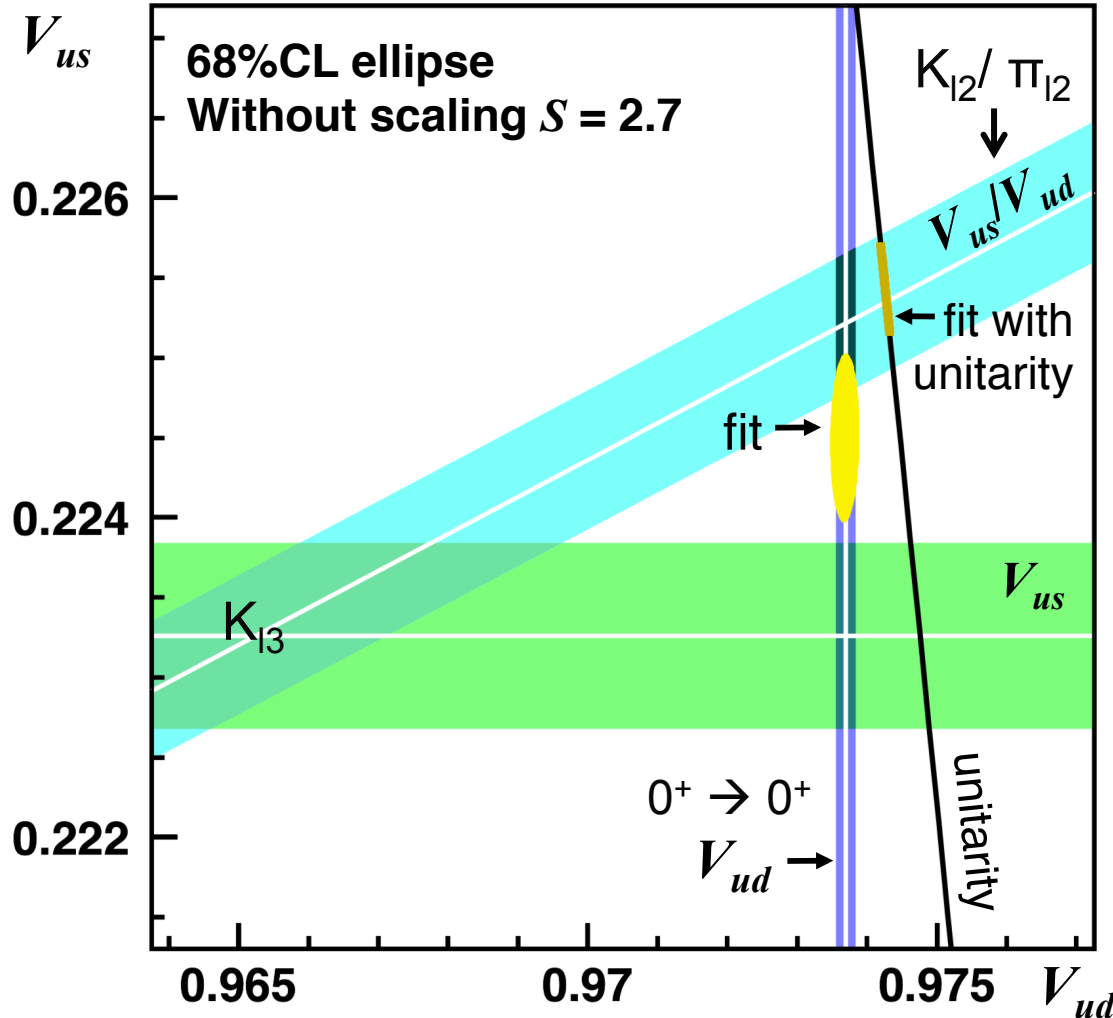
3. First-row CKM unitarity and lepton universality tests

- Recent discrepancy with CKM unitarity:

$$|V_{ud}| = 0.97370(14)$$

$$|V_{us}| = 0.2233(6)$$

$$|V_{us}|/|V_{ud}| = 0.2313(5)$$



Fit results, no constraint

$$V_{ud} = 0.97368(14)$$

$$V_{us} = 0.22450(35)$$

$$\chi^2/\text{ndf} = 7.2/1 \text{ (0.7\%)}$$

$$\Delta_{\text{CKM}} = -0.00154(32)$$

-4.8σ

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1 + \Delta_{\text{CKM}}$$

Broad sensitivity to BSM scenarios :

Discrepancy with CKM unitarity: -4.8σ due to change in theory inputs:

$f_+(0)$ from lattice QCD:

2σ inconsistency between K_{l3} and K_{l2} results for V_{us}

V_{us} from K_{l2} consistent with unitarity up to new V_{ud} evaluation

Leptonic decays of kaons and pions: V_{us}/V_{ud} from $K_{l2} (K \rightarrow \mu \nu) / \pi_{l2} (\pi \rightarrow \mu \nu)$

Full QCD+QED decay rate on the lattice

➡ Inclusion of EM and IB corrections :

- Perturbative treatment of QED on lattice established
- Formalism for K_{l2} worked out

Prospects for RBC/UKQCD: Calculation at the physical point in 2-3 years with

- continuum extrapolation
- non-perturbative renormalisation of the weak Hamiltonian in QCD+QED
- isospin breaking effects for sea quarks
- lattice calculation of real photon emission

Exploring to calculate QED corrections in infinite volume analytically to eliminate power-law finite volume errors

➡ **Aim: Per mile level within 10 years**

Application of the method for **semileptonic Kaon (K_{l3}) and Baryon decays**

V_{ud} side: new radiative corrections to $0^+ \rightarrow 0^+$ superallowed beta decays:

2.9 σ - 4.8 σ discrepancy with unitarity

$$\frac{1}{t} = \frac{G_\mu^2 |V_{ud}|^2 m_e^5}{\pi^3 \log 2} f(Q) (1 + RC) \longrightarrow ft (1 + RC) = \frac{2984.48(5) s}{|V_{ud}|^2}$$

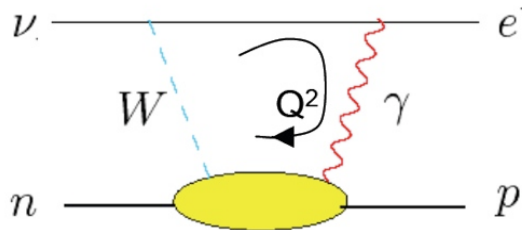
$$(1 + RC) = (1 - \delta_C) (1 + \delta_R) (1 + \Delta_R)$$

$\langle f | \tau_+ | i \rangle = \sqrt{2} (1 - \delta_C/2)$
 Coulomb distortion
 of wave-functions

Nucleus-dependent
 rad. corr.
 (Z, E^{\max} , nuclear structure)

Nucleus-independent
 short distance rad. corr.

- New calculation based on Dispersion Relations



Inputs needed: DIS of neutrino on nucleon but also quasi elastic neutrino nucleon data

$$|V_{ud}| = 0.97418(10)_{Ft} (18)_{\Delta_R}$$



$$|V_{ud}| = 0.97370(10)_{Ft} (10)_{\Delta_R}$$

~1.8 σ smaller

The quest for explaining the top-row CKM unitarity deficit:

- Revisit evaluation of RC to extract V_{us} from $0^+ \rightarrow 0^+$ superallowed beta decays:
 - Improved γW box inputs
 - Evaluation of γW box on the lattice
 - Modern ab-initio calculations of nuclear corrections δ_C , δ_{NS}
- Radiative corrections (EM+IB) in K_{l2} decays

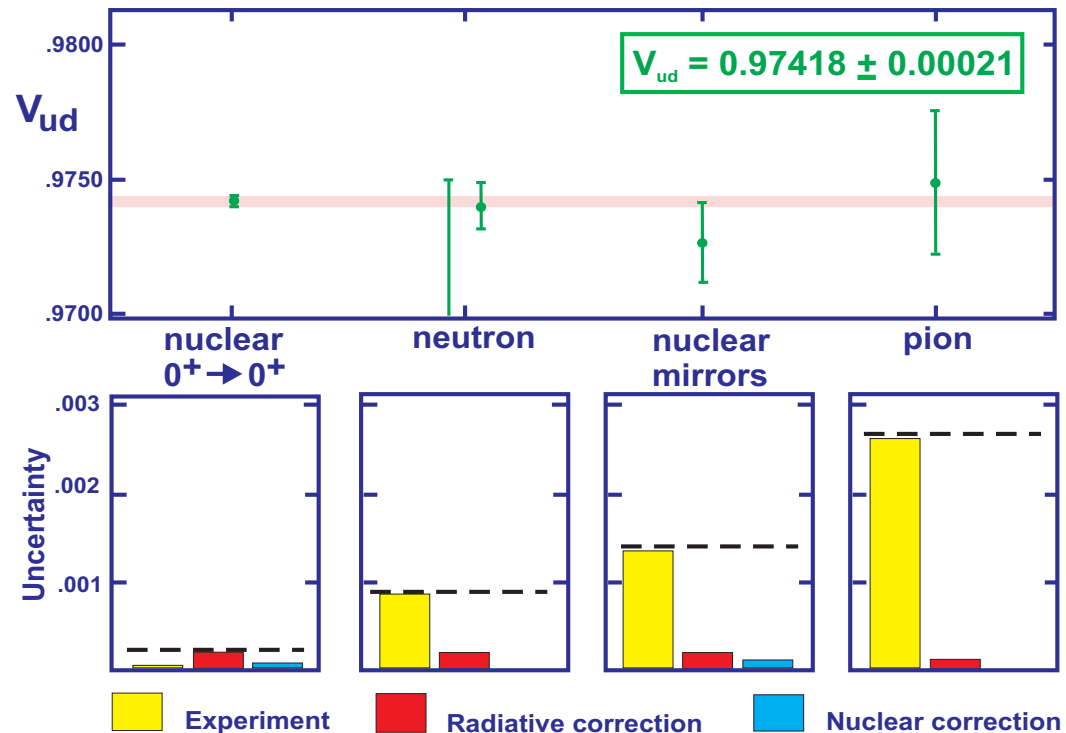
Hardy@Amherst'19

Can we extract V_{ud} differently?

- **From neutron decays**
 - *UCN $\tau \rightarrow$ UCN $\tau^+ \rightarrow$ Next Gen
 - *UCNA \rightarrow UCNA $^+ \rightarrow$ Next Gen
 - *Radiative Corrections: lattice QCD and effective field theory.

Effort undertaken at LANL

- From $\pi^+ \rightarrow \pi^0 e^+ \nu$
PIENUXE proposal



Conclusion

3 main topics with interesting proposals for the future

1. Rare η and η' decays
2. Rare Kaon Physics
3. First-row CKM unitarity and lepton universality tests

Please contact us if you are interested to contribute !

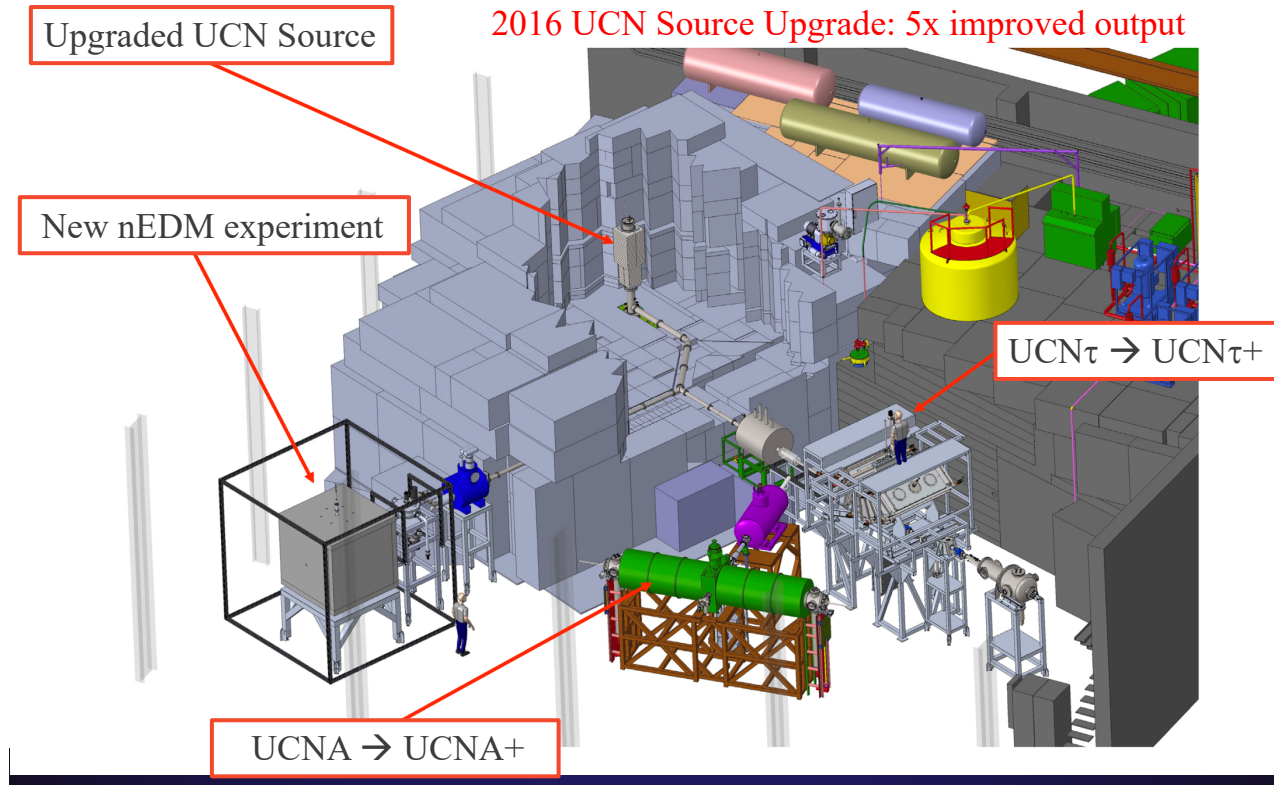
Web: <https://snowmass21.org/rare/weaksud>

Mailing list: SNOWMASS-RPF-02-LIGHT-QUARKS@FNAL.GOV

Slack channel: rpf-02-light-quarks

Back-up

V_{ud} from neutron decay



- Requires

- *UCN τ \rightarrow UCN τ^+ \rightarrow Next Gen

- *UCNA \rightarrow UCNA+ \rightarrow Next Gen

- *Radiative Corrections: lattice QCD and effective field theory.

All three efforts are underway at LANL to resolve the V_{ud} – SM discrepancy.

V_{ud} from pion β decay: $\pi^+ \rightarrow \pi^0 e^+ \nu$

- Theoretically cleanest method to extract V_{ud} : corrections computed in SU(2) ChPT
- Present result: PIBETA Experiment (2004) \rightarrow **Uncertainty: 0.64%**

$$B(\pi^+ \rightarrow \pi^0 e^+ \nu) = (1.036 \pm 0.004_{\text{stat}} \pm 0.004_{\text{syst}} \pm 0.003_{\pi e 2}) \times 10^{-8} (\pm 0.6\%)$$

$$\Rightarrow |V_{ud}| = 0.9739(28)_{\text{exp}} (1)_{\text{th}}$$

Next Generation experiment: Goal 0.06%

Opportunity to extract V_{us}/V_{ud} from $\frac{B(K \rightarrow \pi l \nu)}{B(\pi^+ \rightarrow \pi^0 e^+ \nu)}$ *Czarnecki, Marciano, Sirlin'20*

Improve precision on $B(\pi^+ \rightarrow \pi^0 e^+ \nu)$ by x3 $\Rightarrow V_{us}/V_{ud} < \pm 0.2\%$

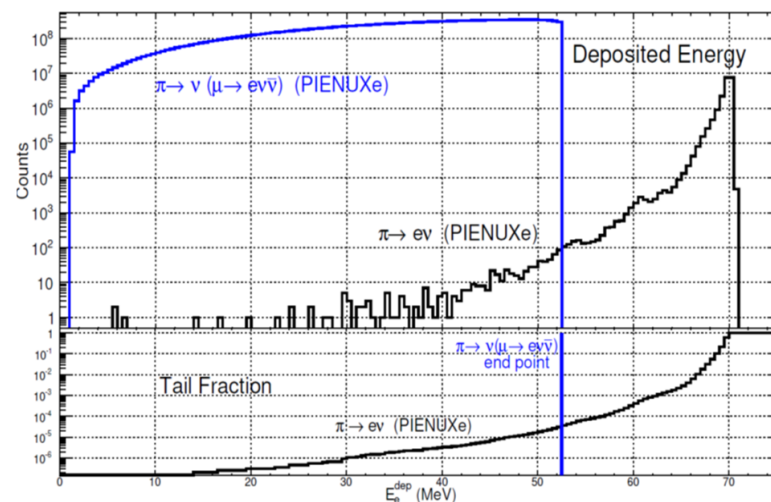
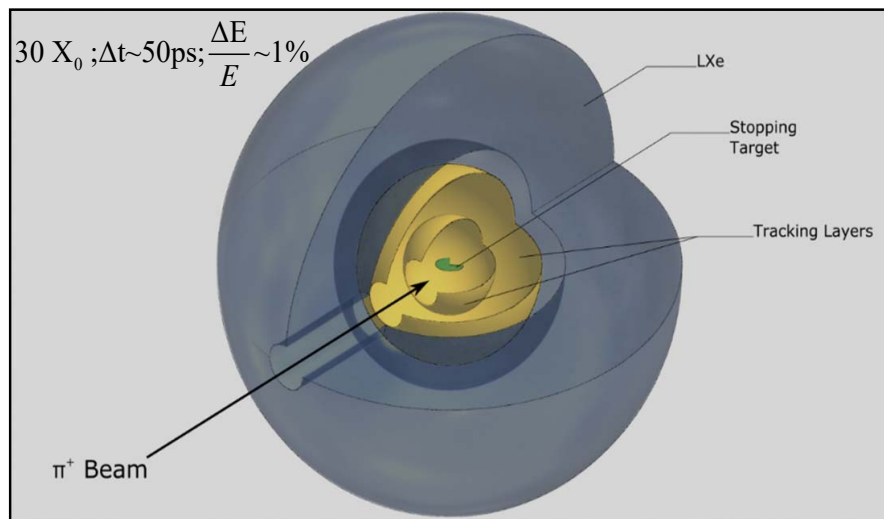
Test of LFU from $R_{e/\mu}^{\text{theory}} = \frac{\Gamma(\pi \rightarrow e \nu(\gamma))}{\Gamma(\pi \rightarrow \mu \nu(\gamma))} = (1.2353 \pm 0.0002) \times 10^{-4}$ **(0.016%)** *Marciano & Sirlin, Cirigliano*

Present Experimental result: $R_{e/\mu}^{\text{exp } \pi} = 1.2327 \pm 0.0023 \times 10^{-4}$ **(0.19%)** *PDG'20*

\Rightarrow **Goal next generation PIENUXE: 0.015%** $\rightarrow \frac{g_e}{g_\mu} \sim (\pm 0.0075\%)$

V_{ud} from pion β decay: $\pi^+ \rightarrow \pi^0 e^+ \nu$ and Lepton Flavour Universality

PIENUXE: New Rare π Decay Experiment with LXe



Faster calorimeter response time x10-100.

Low energy tail reduced x 10



- π^+ Beam: 75 MeV/c ; 2×10^5 Hz
- Tracking – SciFi-SiPM, Si pixels
- LXe calorimeter
- Sensitivity, Precision: 10^8 events $\pm 0.015\%$ in 1 yr

$$\frac{g_e}{g_\mu} \sim (\pm 0.0075\%)$$



- π^+ Beam: 75 MeV/c ; 3×10^7 Hz
- Sensitivity, Precision: 10^6 events $\pm 0.1\%$ in 1 yr

$$V_{ud} \sim (\pm 0.03\%) \quad \frac{V_{us}}{V_{ud}} \sim (\pm 0.1\%)$$