

# Electron-Nucleus Scattering for Neutrino Interactions and Oscillations



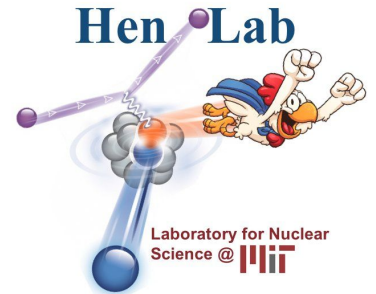
A. Papadopoulou (apapadop@mit.edu)

For the  $e4\nu$  collaboration



March 28 2022

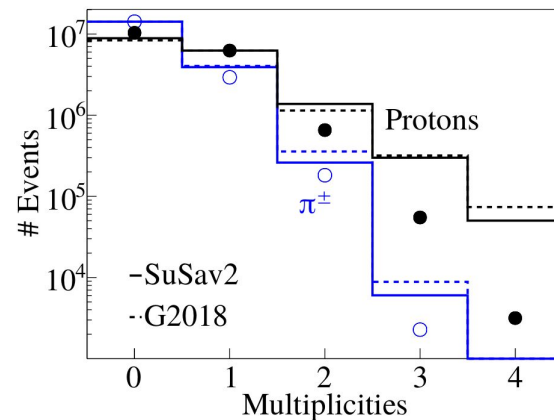
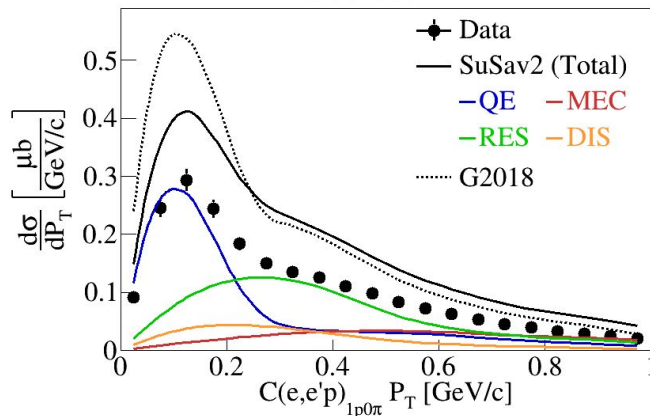
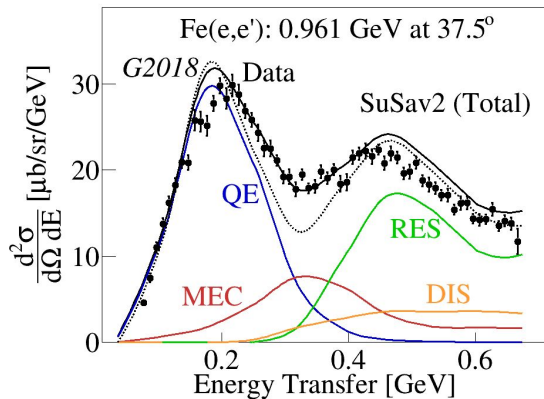
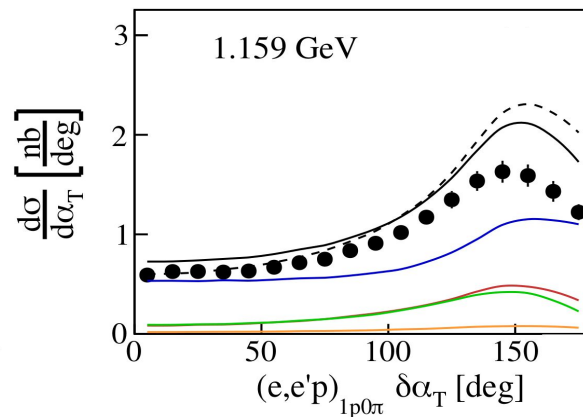
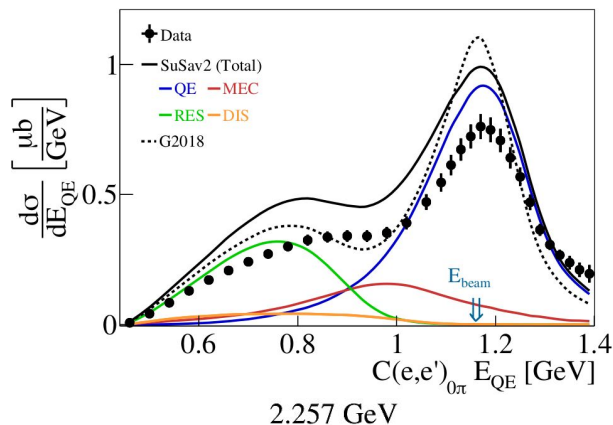
NuSTEC Workshop on Electron Scattering



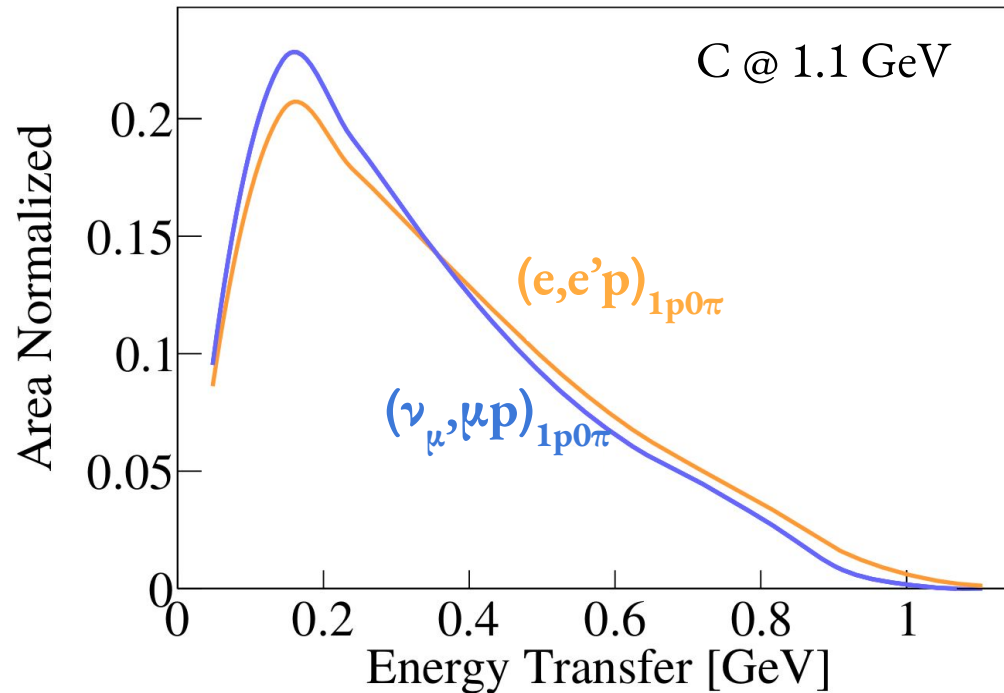
# The $e4\nu$ Result Factory

Many

- nuclei
- beam energies
- channels
- variables



# Similar $\nu$ & e Distributions

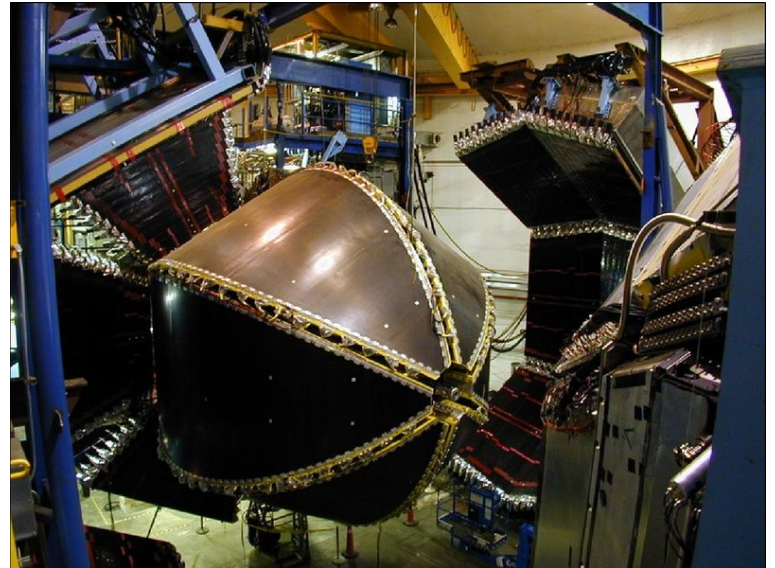


Accounting for propagator mass ( $\gamma$  vs  $W$ ) via  $Q^4$  scaling of the electron side

# Jefferson Laboratory

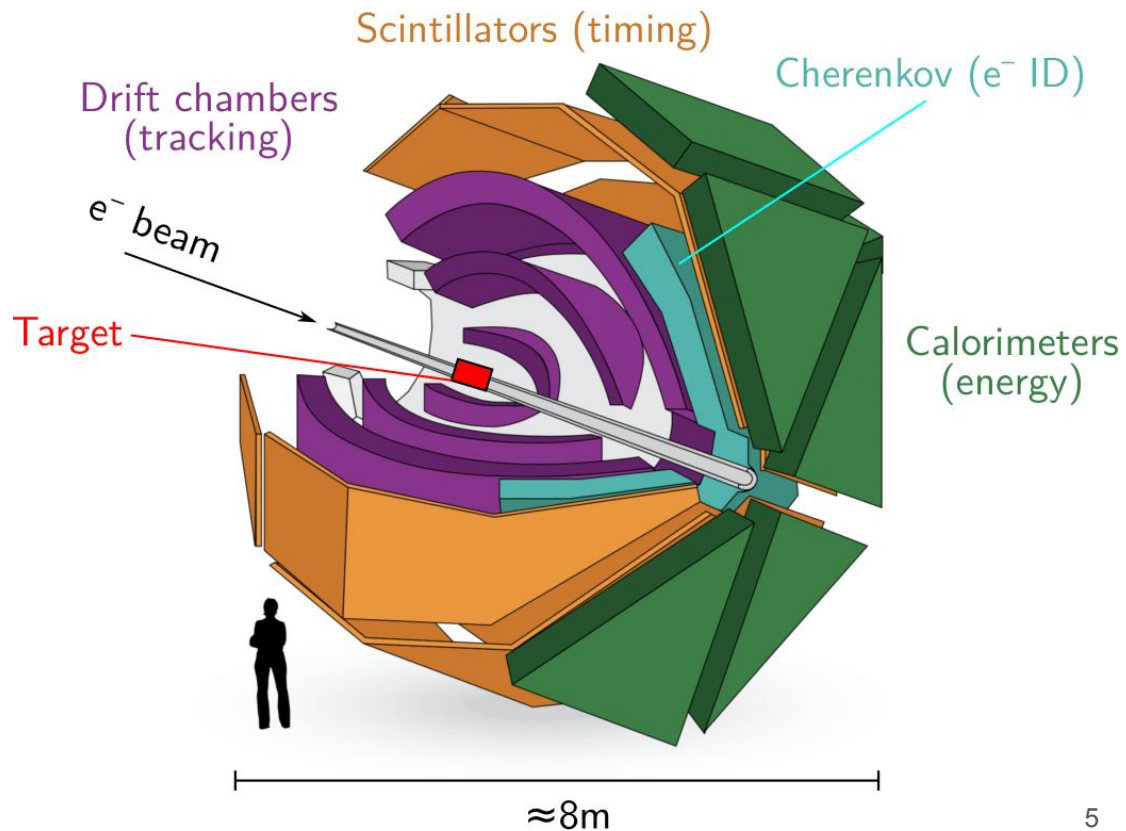


- Electron beam accelerator facility
- Energies up to 12 GeV
- Using Hall B & CLAS detector



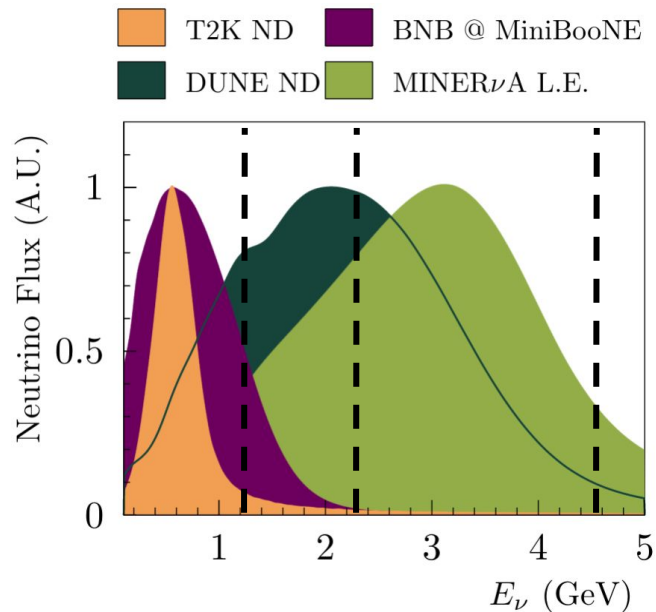
# e4ν Data-Mining W/ CLAS

- Large acceptance @  $\theta_e > 15^\circ$
- Charged particle threshold similar to  $\nu$  tracking detectors
- ~50% of “ $4\pi$ ” coverage



# e4 $\nu$ Data-Mining W/ CLAS

- Large acceptance @  $\theta_e > 15^\circ$
- Charged particle threshold  
similar to  $\nu$  tracking detectors
- ~50% of “ $4\pi$ ” coverage
- Energies: 1, 2 & 4 GeV
- Targets:  $^4\text{He}$ ,  $^{12}\text{C}$ ,  $^{56}\text{Fe}$



H<sub>2</sub>O

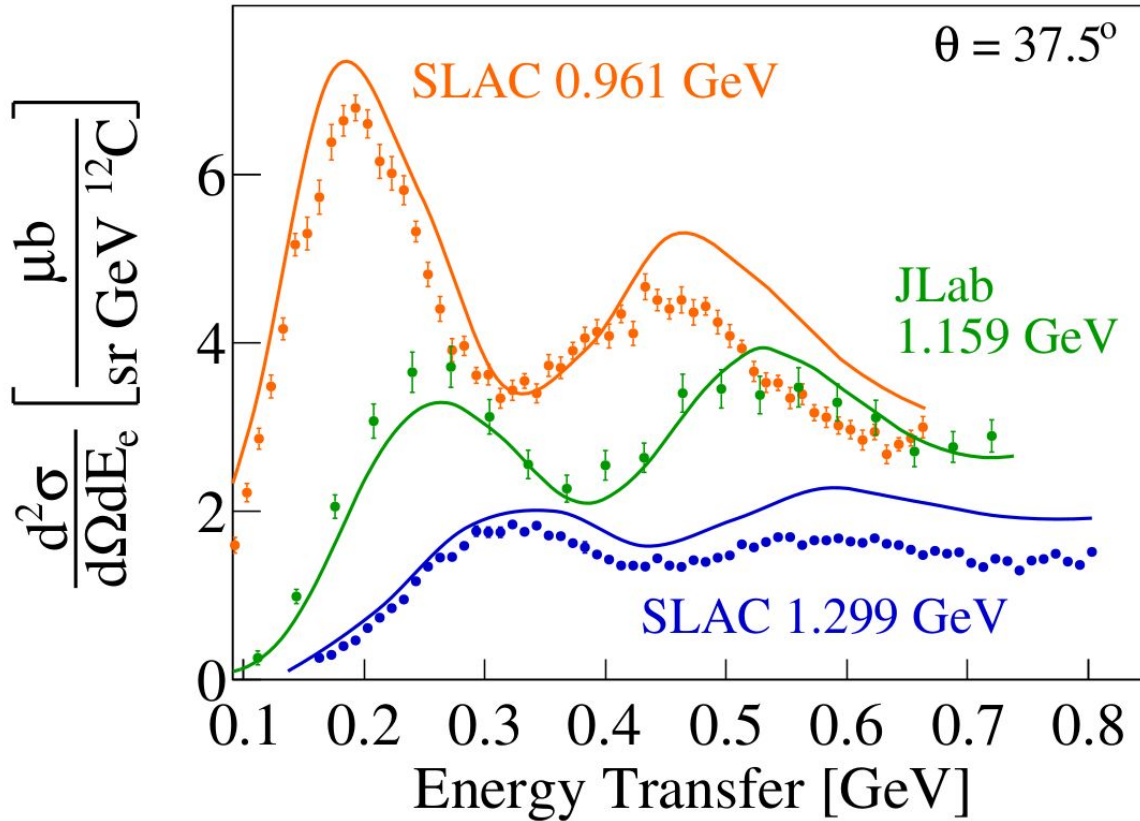


CH

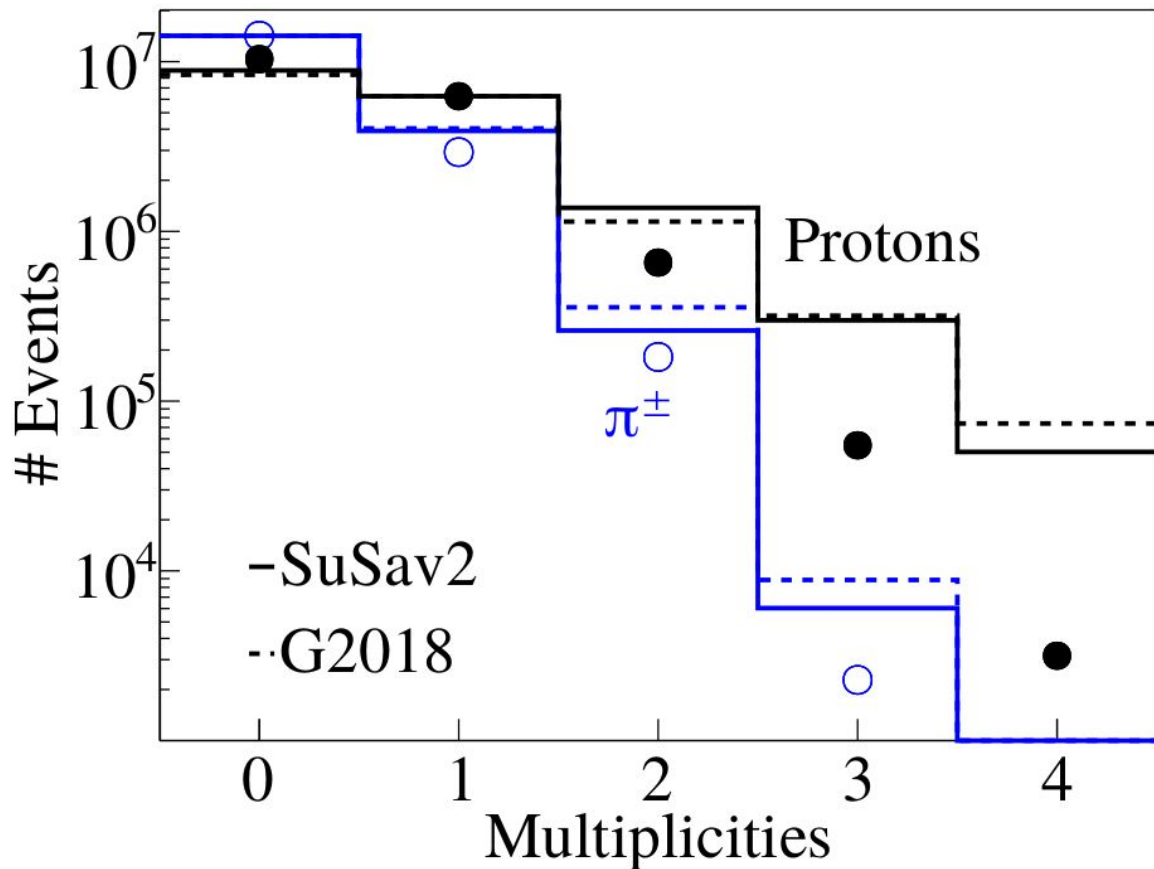


Ar

# Sanity Check With Inclusive Cross Sections



# Detected Hadron Multiplicities



$^{12}\text{C}$  @ 2.2 GeV

$P_p > 300 \text{ MeV}/c$   
 $P_\pi > 150 \text{ MeV}/c$

Simulation overpredicts  
hadron multiplicities

M.Khachatryan, A.Papadopoulou, et al.  
Nature 599, 565–570 (2021)



# Playing The QE-like Neutrino Game

---



- 1 proton ( $> 300 \text{ MeV}/c$ )
- No  $\pi^\pm$  ( $> 70 \text{ MeV}/c$ )

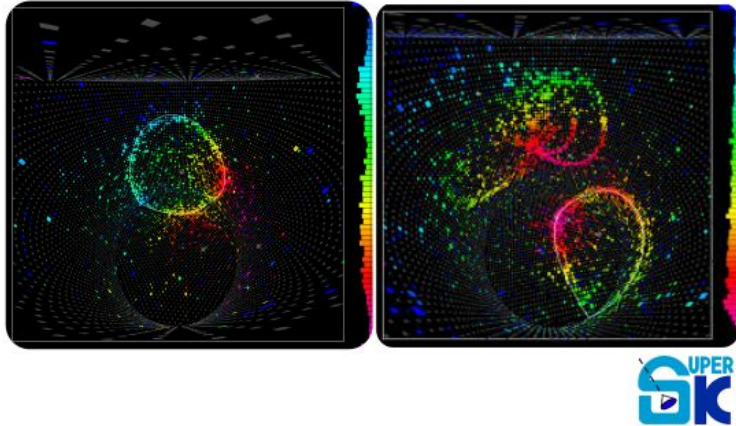


- 1 proton ( $> 300 \text{ MeV}/c$ )
- No  $\pi^\pm$  ( $> 150 \text{ MeV}/c$ )
- Scale by  $\sigma_{\nu N} / \sigma_{eN} \propto Q^4$

- Study energy reconstruction
- Test against GENIE event generator

# QE Energy Reconstruction

---

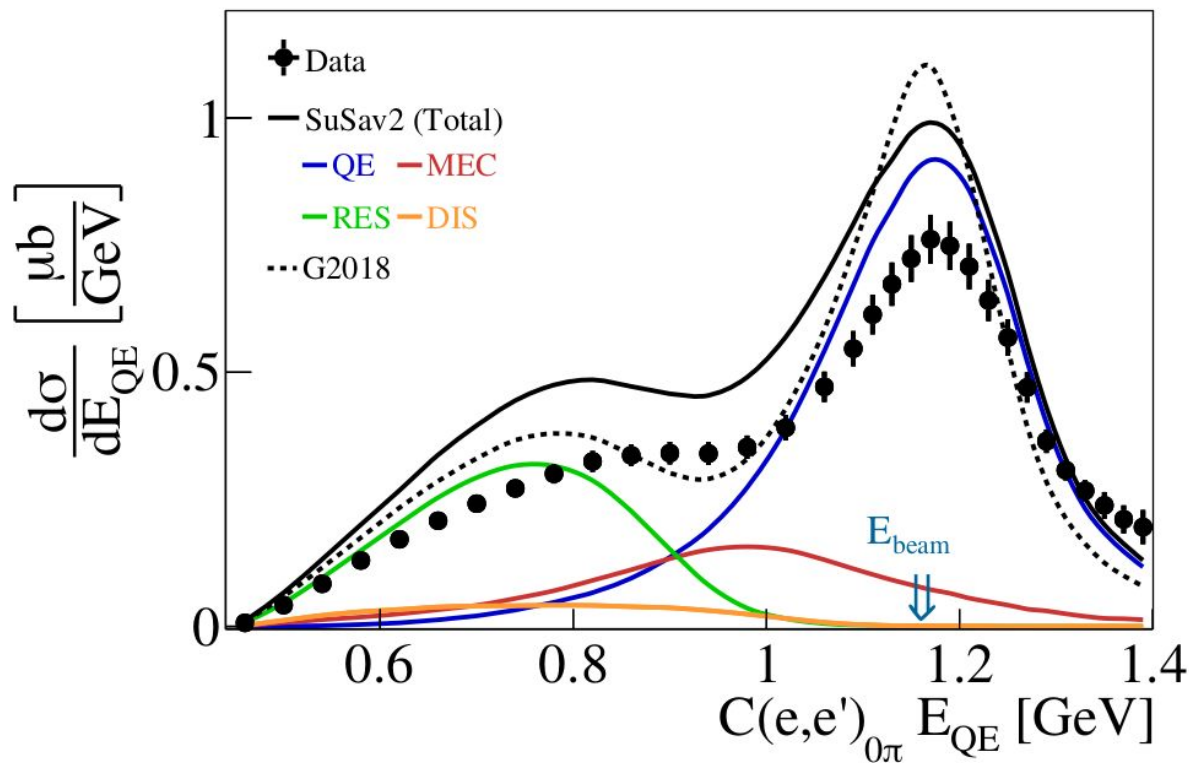


Cherenkov detectors  
Assuming QE interaction  
Using lepton kinematics

$$E_{QE} = \frac{2M\epsilon + 2ME_l - m_l^2}{2(M - E_l + |k_l|\cos\theta_l)}$$

# QE Energy Reconstruction

C @ 1.1 GeV



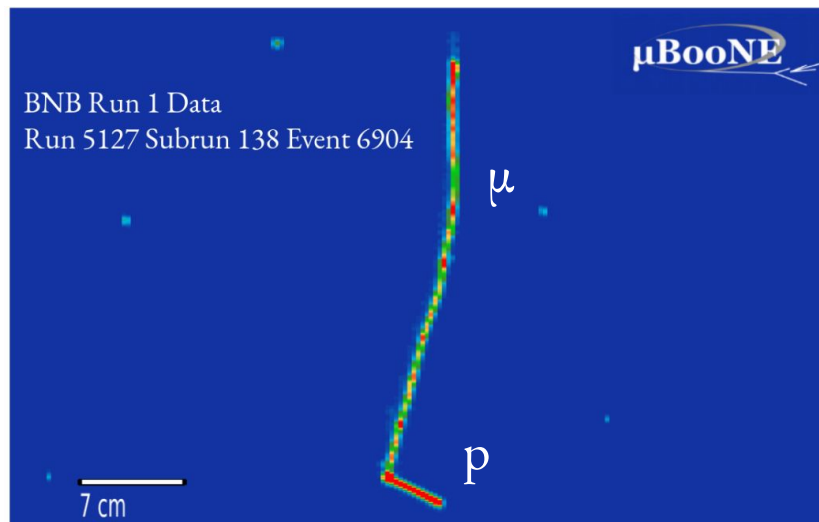
- Relevant for T2K
- Overestimation of  
QE peak & RES tail

$$E_{QE} = \frac{2M\epsilon + 2ME_l - m_l^2}{2(M - E_l + |k_l|\cos\theta_l)}$$

M.Khachatryan, A.Papadopoulou, et al.  
Nature 599, 565–570 (2021)

# Calorimetric Energy Reconstruction

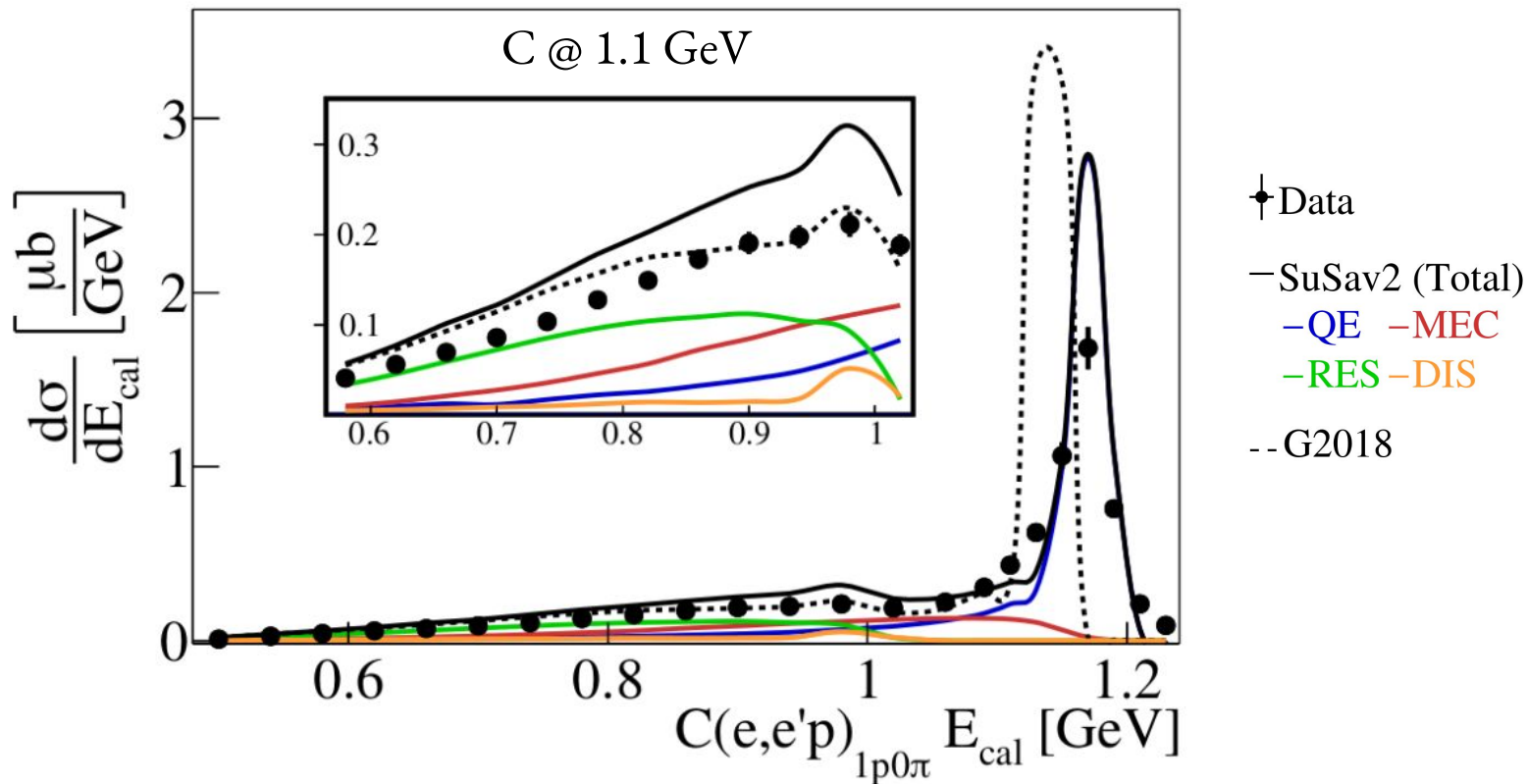
---



Tracking detectors  
Calorimetric sum  
Using all detected particles

$$E_{cal} = E_l + T_p + \epsilon_B$$

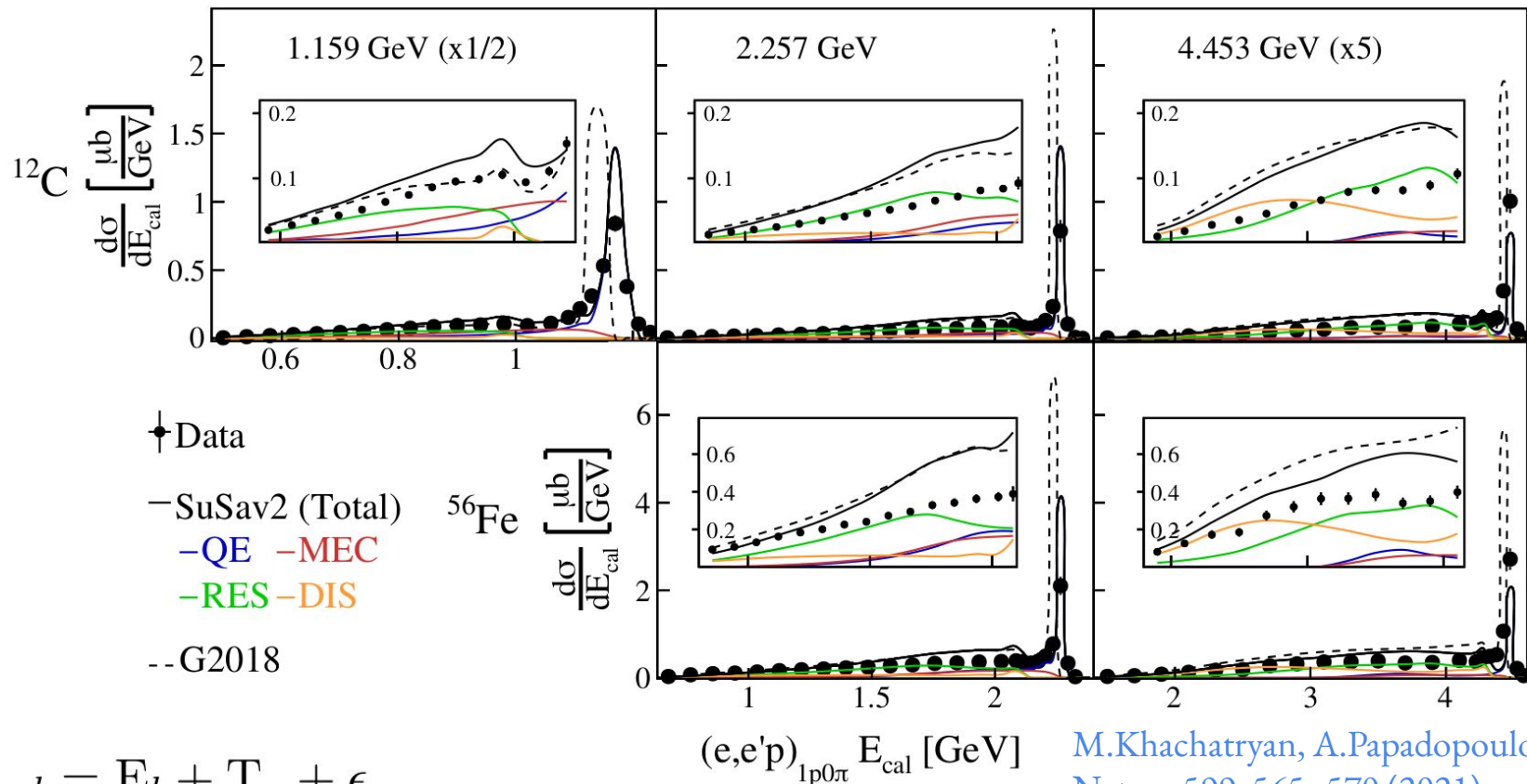
# Calorimetric Energy Reconstruction



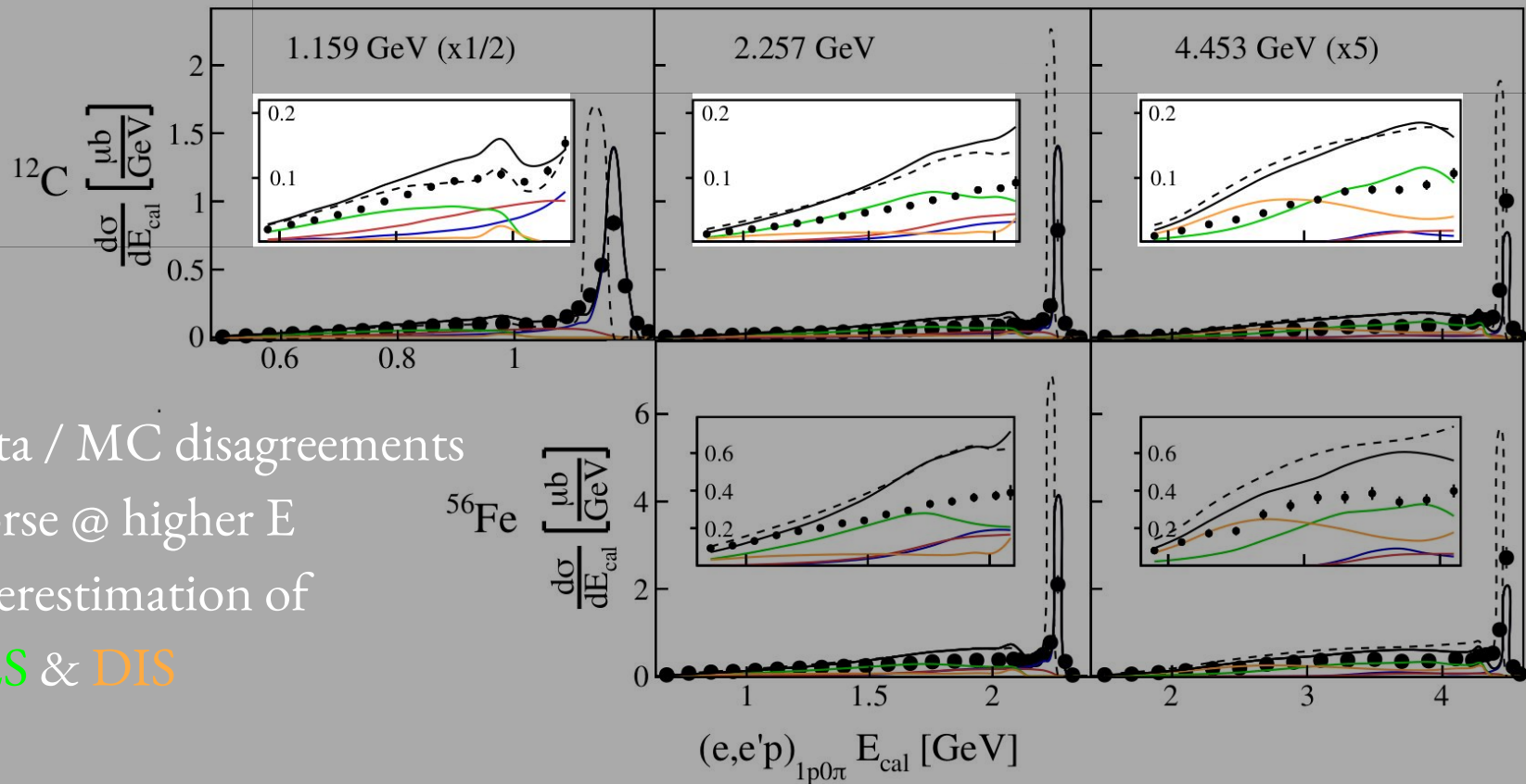
$$E_{cal} = E_l + T_p + \epsilon$$

M.Khachatryan, A.Papadopoulou, et al.  
 Nature 599, 565–570 (2021)

# $E_{cal}$ Nucleus & Energy Dependence

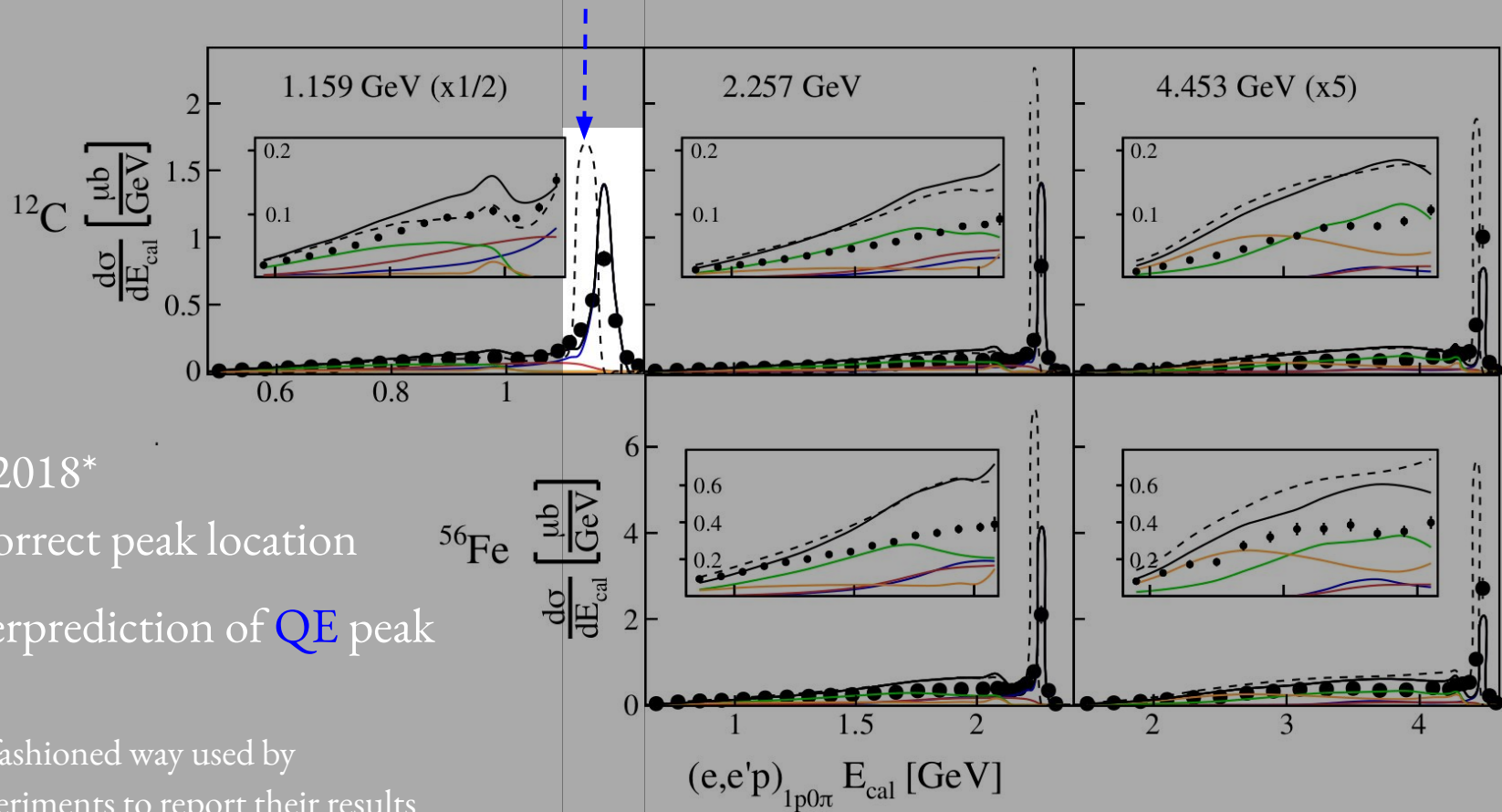


# Nucleus & Energy Dependence



- Data / MC disagreements
- Worse @ higher E
- Overestimation of  
**RES** & **DIS**

# Nucleus & Energy Dependence



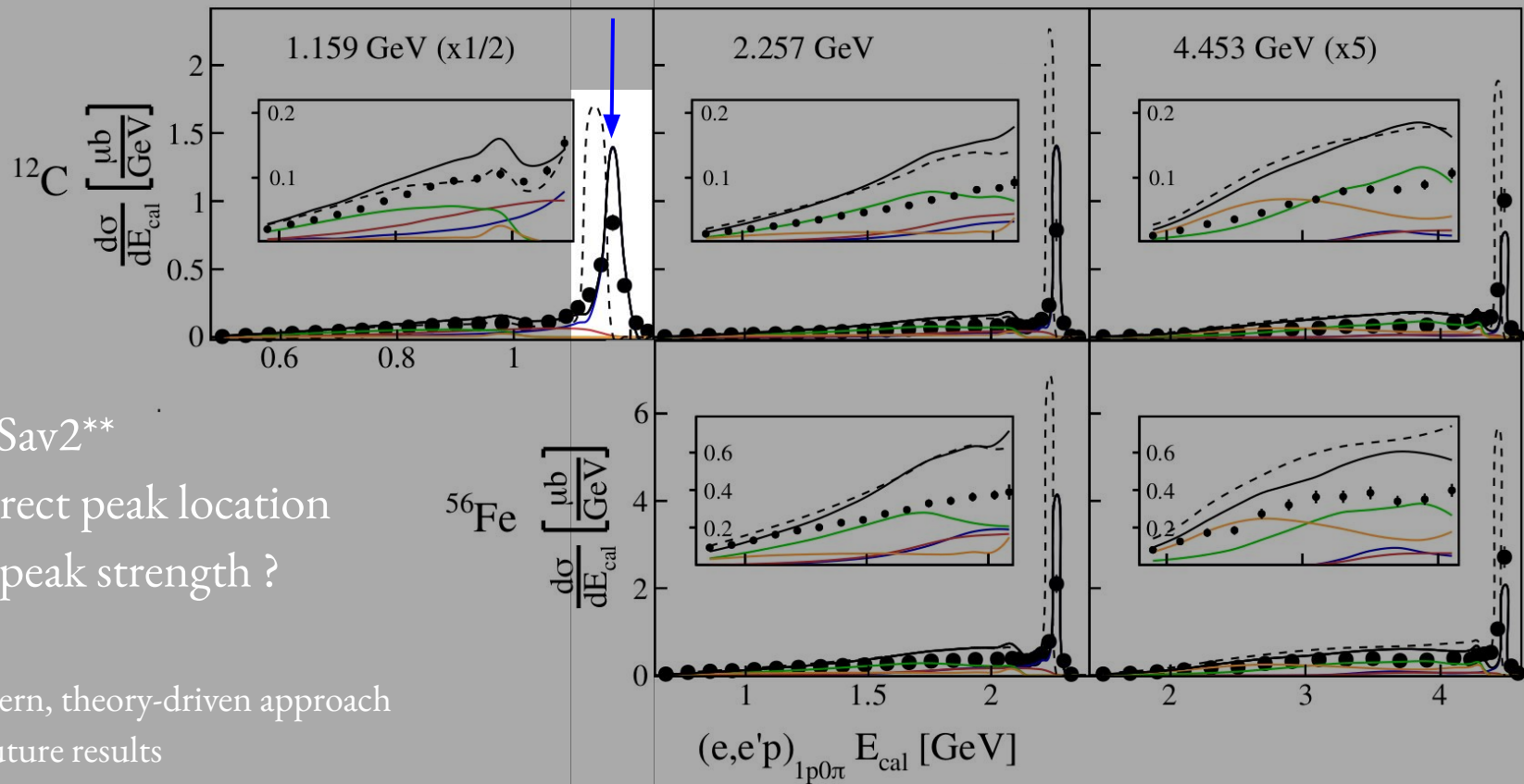
--- G2018\*

- Incorrect peak location
- Overprediction of QE peak

\* Old-fashioned way used by  $\nu$  experiments to report their results



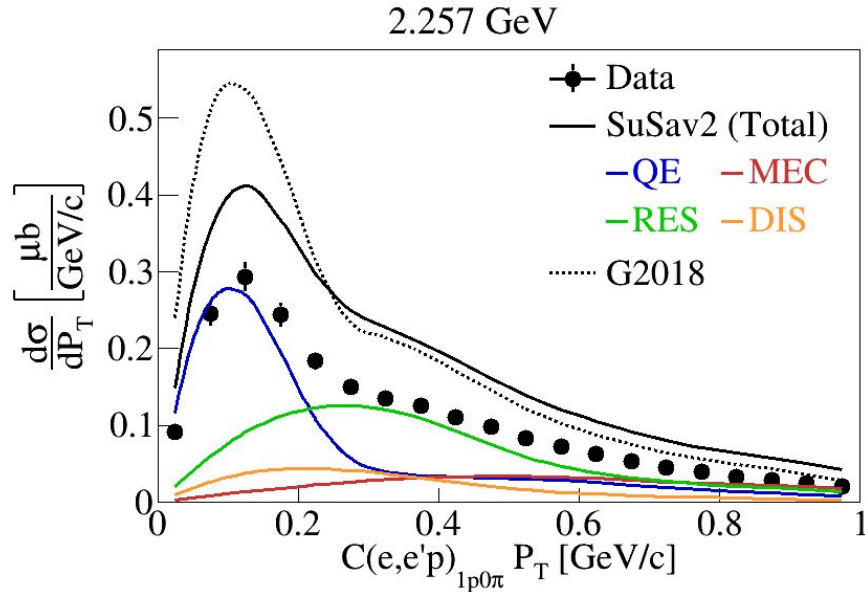
# Nucleus & Energy Dependence



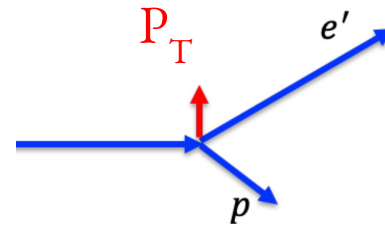
- SuSav2\*\*
- Correct peak location
- QE peak strength ?

\*\* Modern, theory-driven approach for future results

# Transverse Momentum



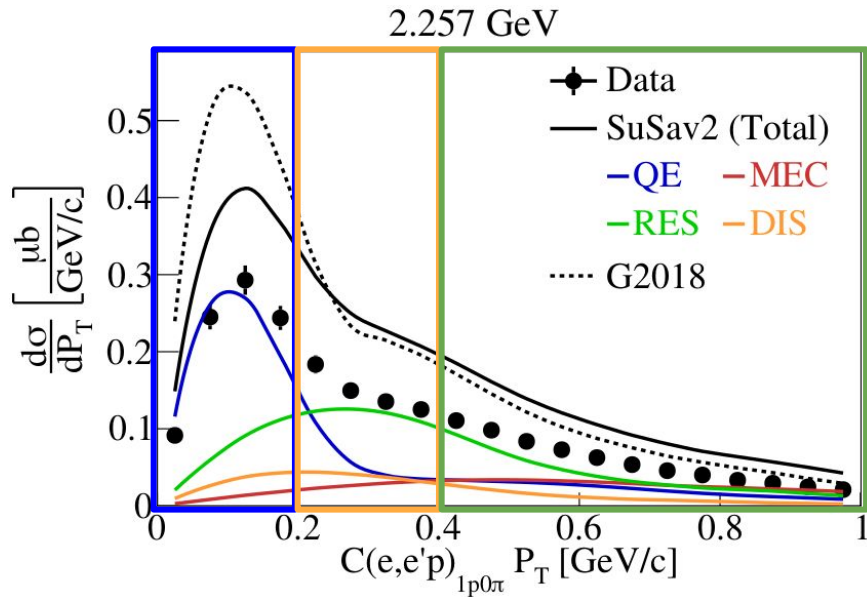
$$P_T = | \mathbf{P}_T^{e'} + \mathbf{P}_T^p |$$



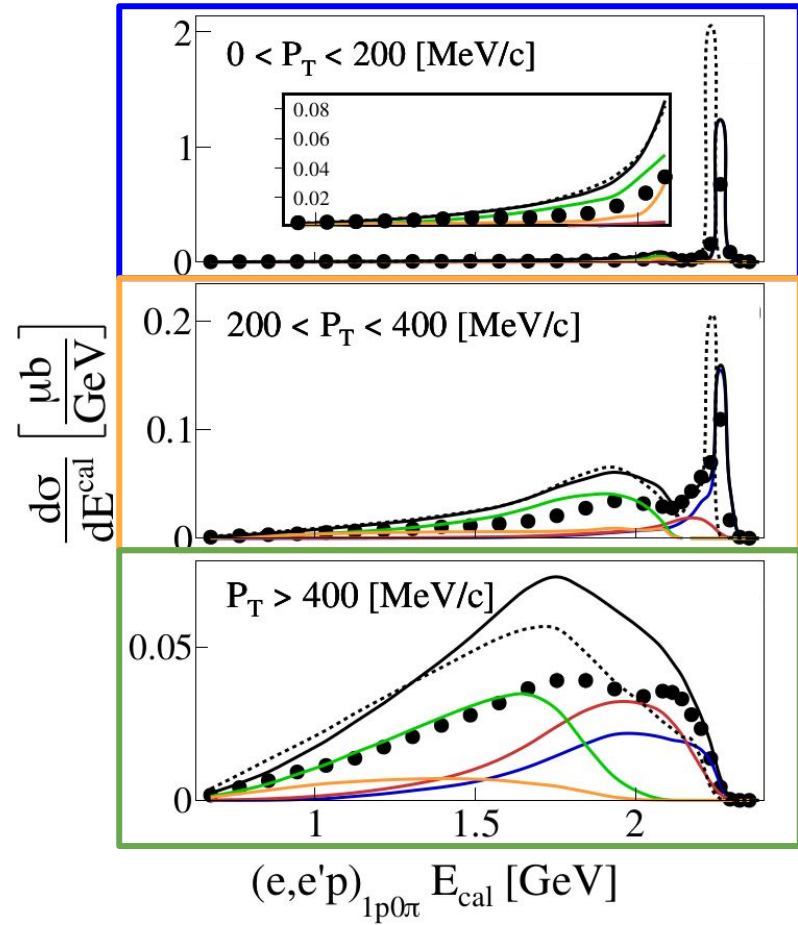
- Overestimation of  
QE peak & RES tail

M.Khachatryan, A.Papadopoulou, et al.  
Nature 599, 565–570 (2021)

# Energy Reconstruction In $P_T$ Slices



M.Khachatryan, A.Papadopoulou, et al.  
 Nature 599, 565–570 (2021)



## Leveraging electron scattering data to improve neutrino interaction modeling

The extraction of mixing parameters in accelerator-based neutrino oscillation measurement relies on detailed understanding of neutrino-nucleus interactions and the reconstruction of incident neutrino energy. With improved detection technologies and neutrino production beams, nuclear interaction uncertainties are becoming a leading and limiting systematic for the analysis of neutrino oscillation measurements.

Building on the large similarity of electron- and neutrino-nucleus interactions, the electrons-for-neutrino collaboration is leading a set of precision electron-nucleus interaction measurements at various beam energies and target nuclei to test, constrain, and validate models of neutrino-nucleus interactions.

We welcome all collaborators to join our e4ν effort.

NuSTEC hands-on [tutorial](#)

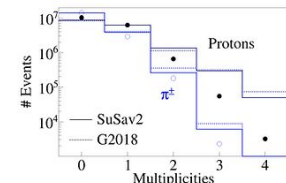
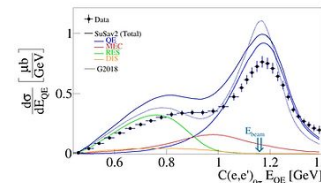
## Data releases

If you are interested in reproducing our results, please see links and brief discussion below

Some basic requirements include:

1. A build of [CERN ROOT](#)
2. Access to the [e4ν Software from GitHub](#)

To reproduce our plots, see the Results\_C/ folder within the github, and you can run each of these within a ROOT session to produce the plots; you can also directly view the bin contents of each plot. Here are a few examples:



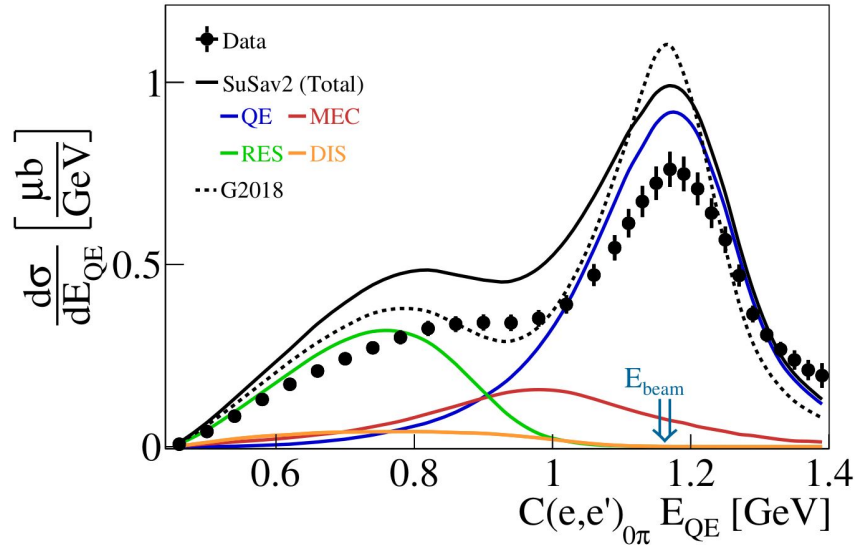
# e4ν Results

master e4nu / Results\_C /

afropapp13 Feb 14 2022: 1) adding C files

- ..
- 12C\_1\_161\_EQE.C
- 12C\_2\_261\_ECalInPTSlices\_NoxBCut.C
- 12C\_2\_261\_Multiplicities.C
- 12C\_2\_261\_PT.C
- 12C\_ECal\_Feeddown.C
- 12C\_EQE\_Feeddown.C
- 56Fe\_ECal\_Feeddown.C
- 56Fe\_EQE\_Feeddown.C
- Correction\_Panel.C
- DataXSec\_Inclusive\_Validation.C
- DeltaAlphaT\_Panel.C
- DeltaPT\_Panel.C
- DeltaPhiT.C
- ECal\_Panel.C
- Fluxes.C
- SubtractionEffect.C

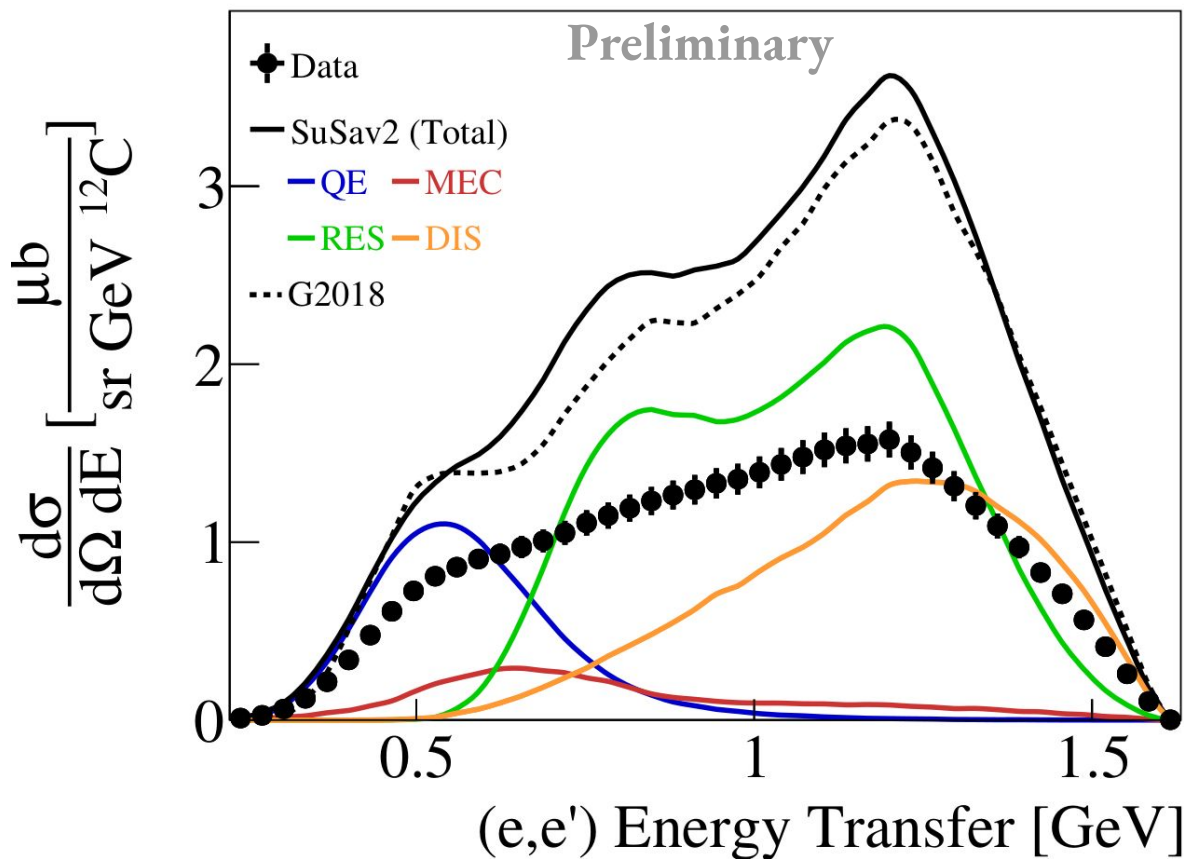
```
git clone https://github.com/adishka/e4nu.git
cd e4nu/Results_C
root -l 12C_1_161_EQE.C
```



Designated branches for truth-level studies ([e4ν truth](#))  
& fiducial cuts/acceptance maps ([e4ν multiplicity](#))

# Inclusive Results

2.261 GeV,  $\theta = 28^\circ$



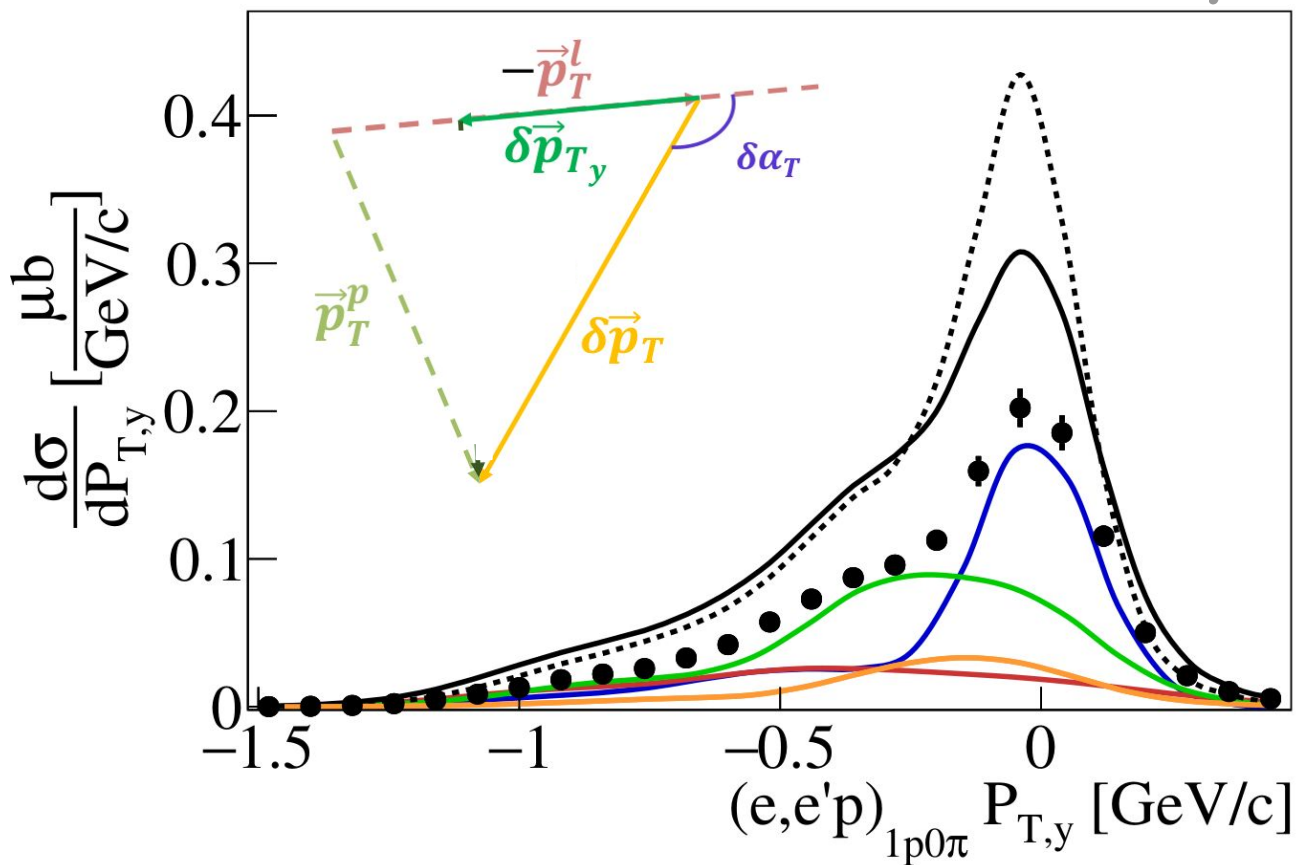
The  $e4\nu$  Result Factory  
Continued!

- Scan over multiple angles
- Results on Argon soon

$e4\nu$  Collaboration  
In preparation

# Nuclear Sensitivity Variables

12C @ 2.261 GeV Preliminary



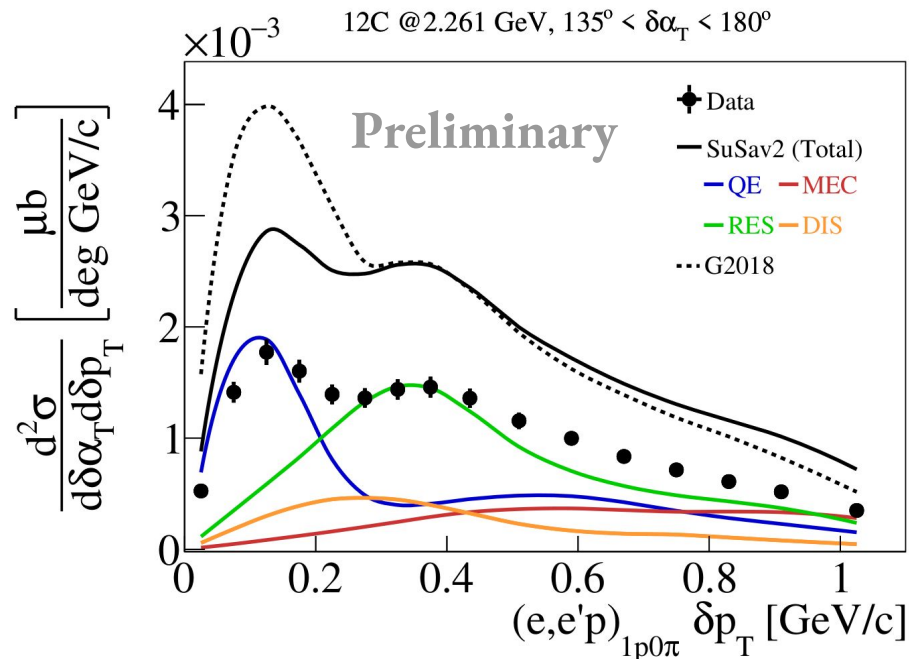
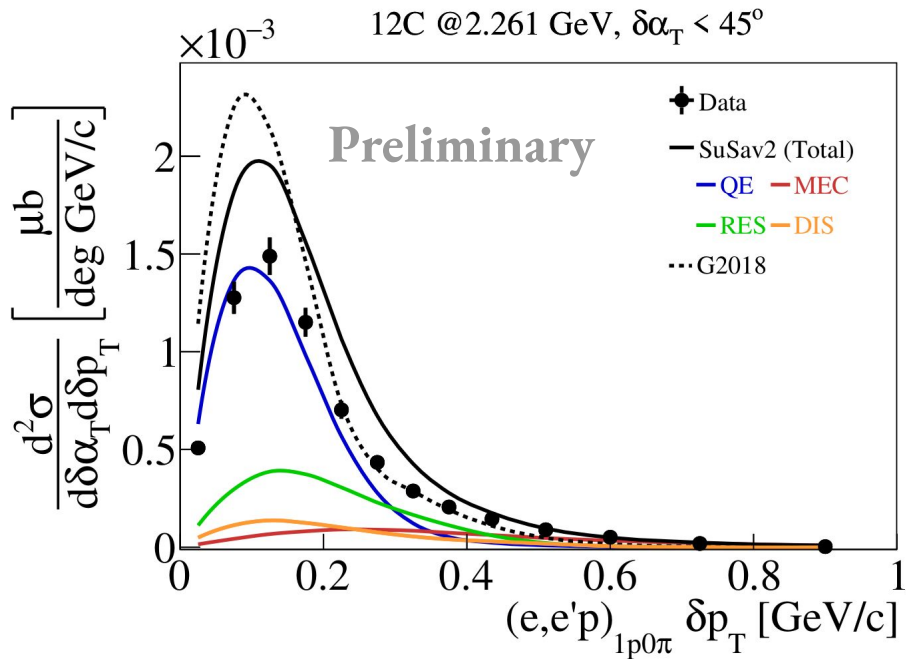
$$\delta p_{T,y} = -\hat{p}_T^l \cdot \delta \vec{p}_T = |\delta \vec{p}_T| \cos(\delta \alpha_T)$$

The  $e4\nu$  Result Factory  
Continued!

- Fermi motion
- Final state interactions (FSI)

*e4ν* Collaboration  
In preparation

# Double Differential Results



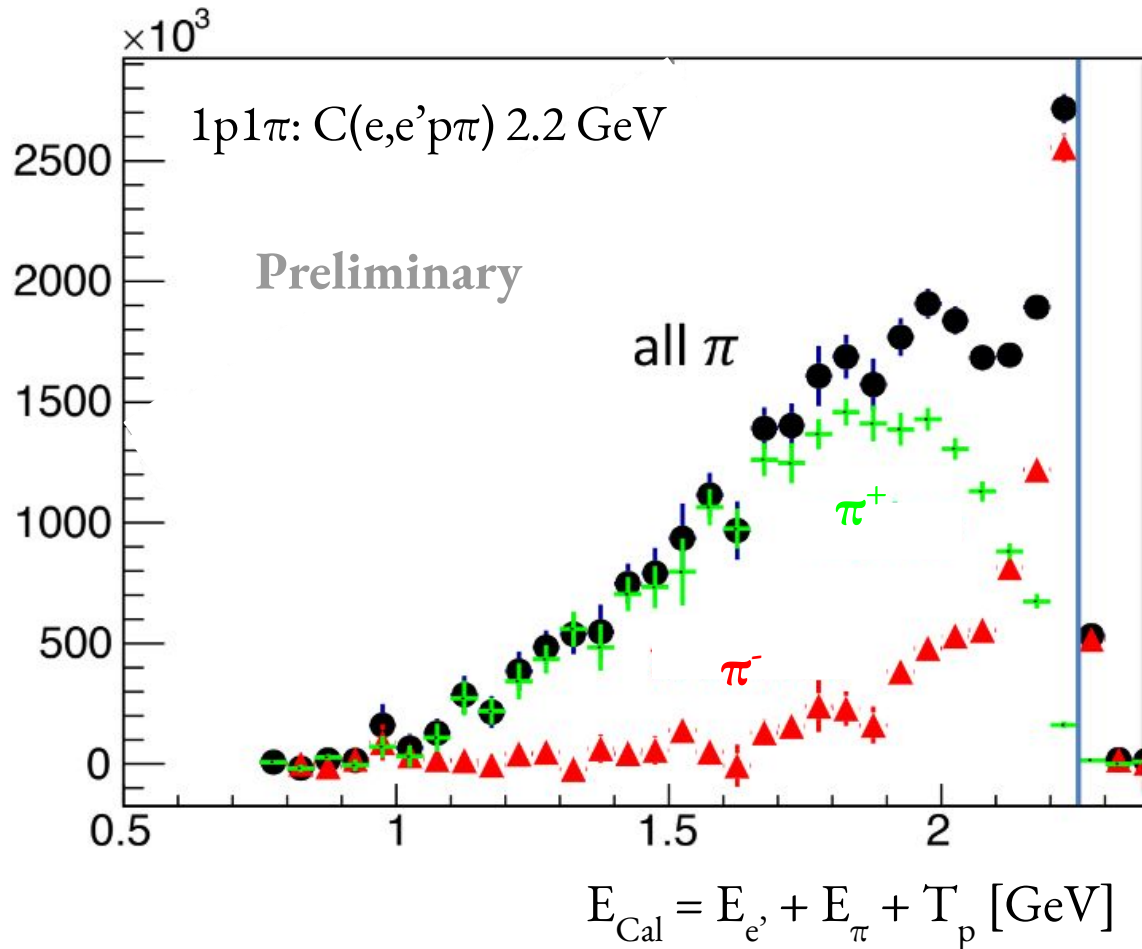
The e4ν Result Factory  
Continued!

e4ν Collaboration  
In preparation

- Handle over FSI / initial state effects
- Tuning potential



# More Complex Channels



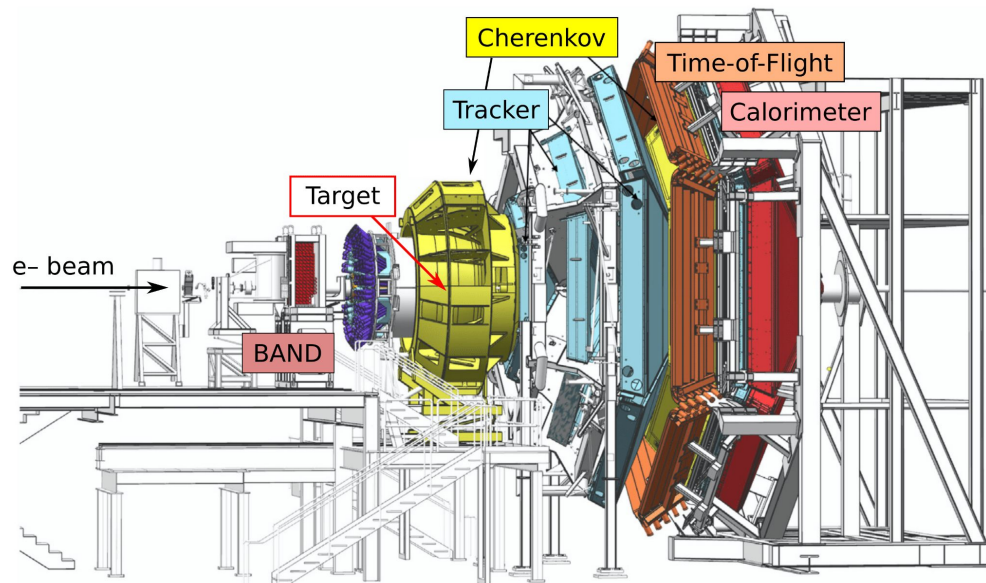
The e4 $\nu$  Result Factory  
Continued!

- Critical for DUNE
- LArTPCs cannot separate  $\pi^+/\pi^-$

e4 $\nu$  Collaboration  
In preparation

# New Data W/ CLAS12

- $\theta_e > 5^\circ$
- x10 luminosity [ $10^{35} \text{ cm}^{-2} \text{ s}^{-1}$ ]
- Targets  
 $^2\text{D}$ ,  $^4\text{He}$ ,  $^{12}\text{C}$ ,  $^{16}\text{O}$ ,  $^{40}\text{Ar}$ ,  $^{120}\text{Sn}$
- 1 - 6 GeV beam energies



Support  
Letters



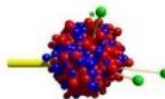
ICECUBE  
SOUTH POLE NEUTRINO OBSERVATORY



Hyper-Kamiokande



MINERVA



GiBUU

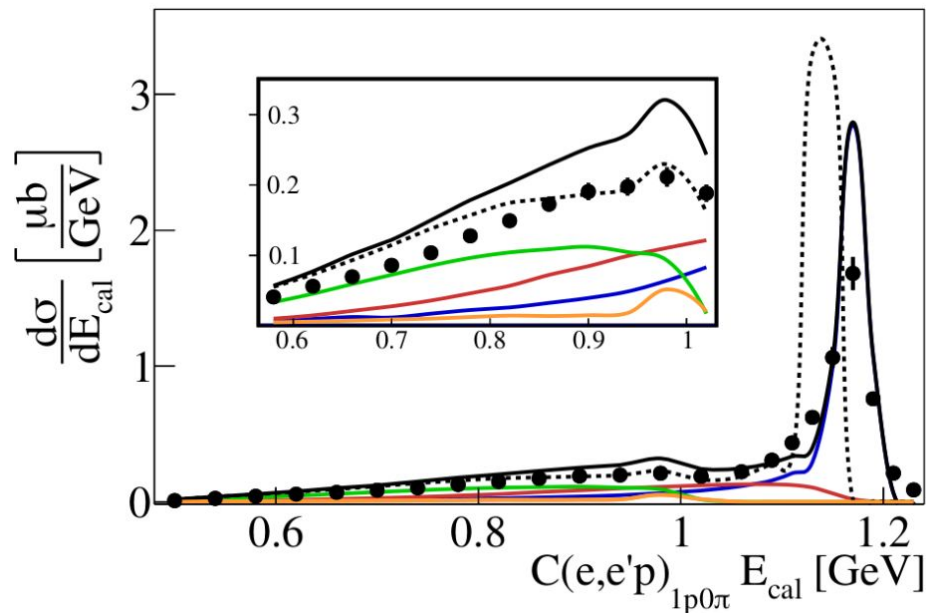
The Giessen Boltzmann-Uehling-Uhlenbeck Project



Genie



- First use of wide phase-space electron data to test  $\nu$  event generators
- Data/MC disagreement even for simple  $1p0\pi$  events
- Identified regions requiring modeling improvements
- Wealth of results to follow!



M.Khachatryan, A.Papadopoulou, et al.  
 Nature 599, 565–570 (2021)

# Growing Collaboration !



Join us!



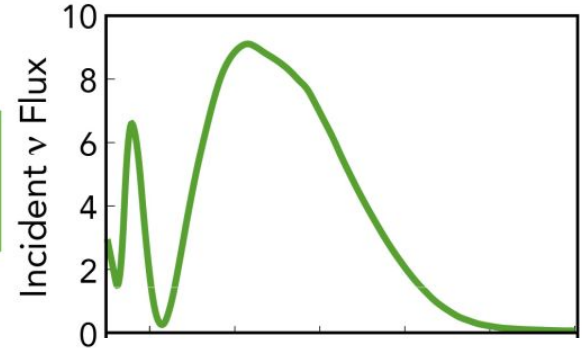
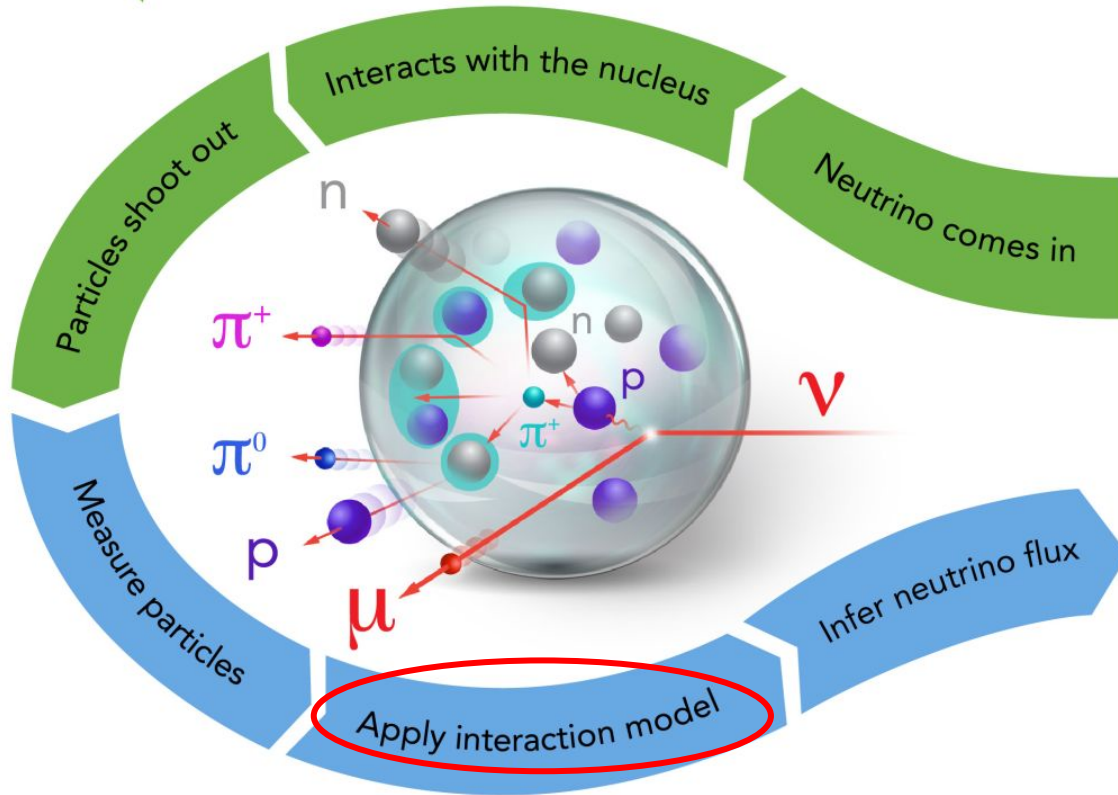
CONSEJO SUPERIOR DE INVESTIGACIONES CIENTÍFICAS

Thank you !



# Backup Slides

# PHYSICS PROCESS



Infer neutrino flux

Apply interaction model

Measure particles

# EXPERIMENTAL ANALYSIS

# Attacking The Modeling Monster

---

- $\gamma$  cross sections

- Modeling in event generators

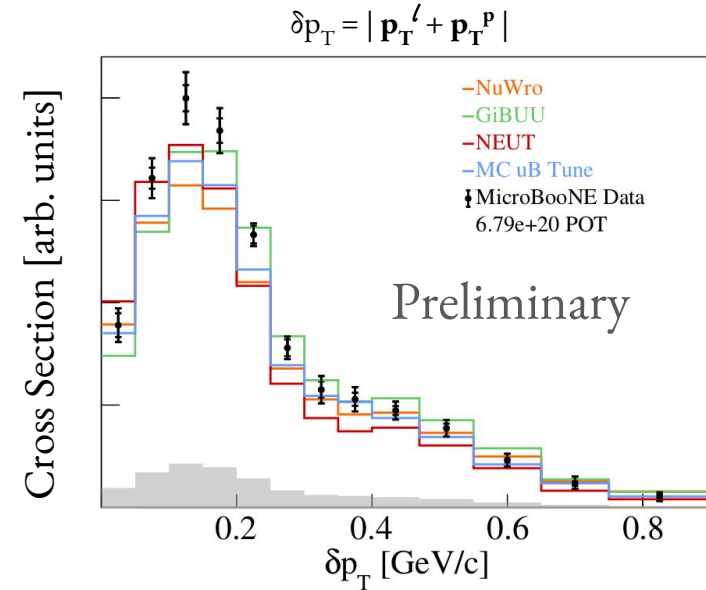
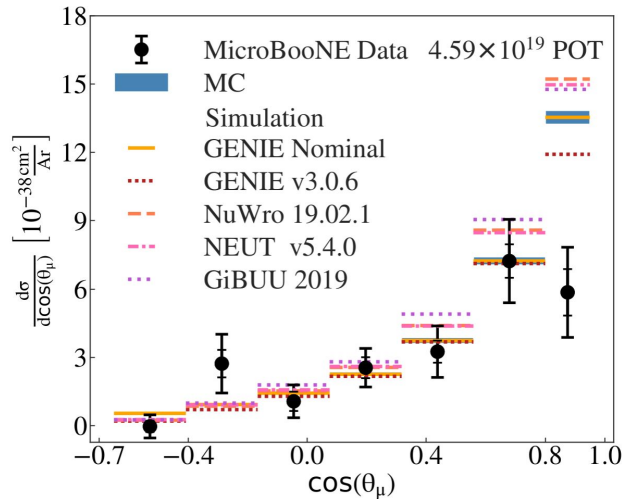


- Electron cross sections



# Attacking The Modeling Monster!

- $\nu$  cross sections



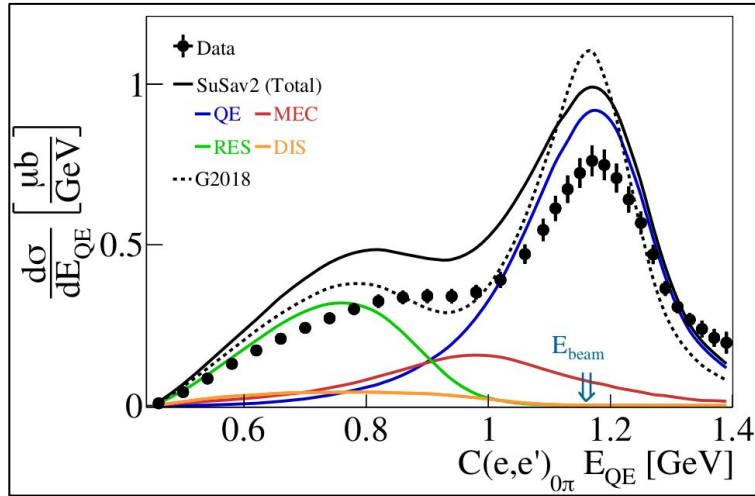
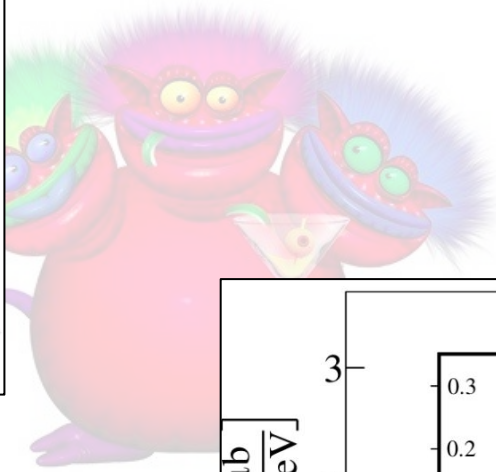
- A.Papadopoulou, et al, Phys. Rev. Lett. 125, 201803 (2020)
- E.Cohen, A.Papadopoulou, et al, Eur. Phys. J. C 79, 673 (2019)

A.Papadopoulou, et al,  
In preparation

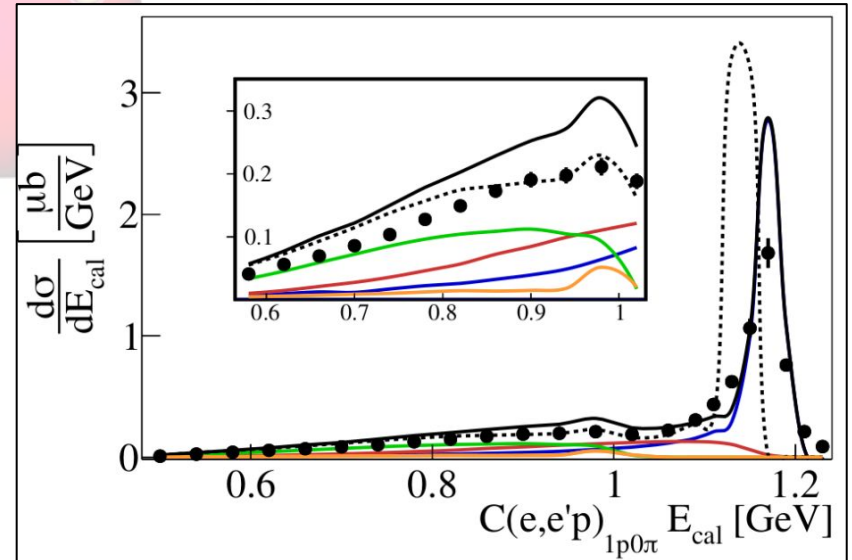
# Today



- Electron cross sections

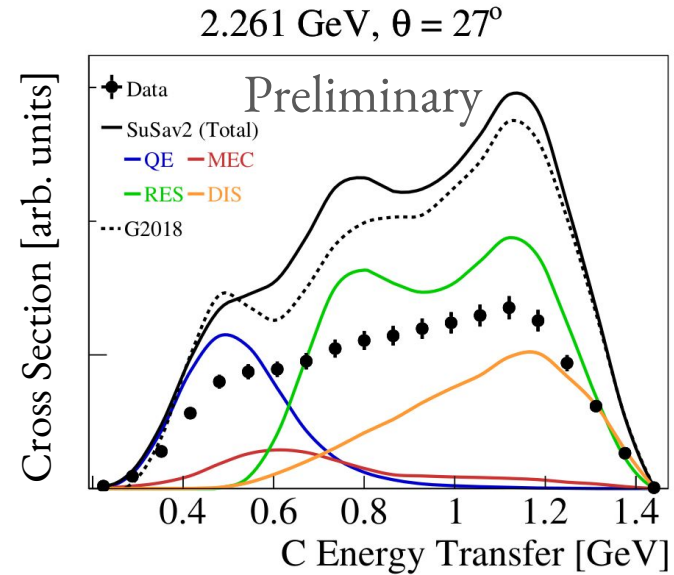
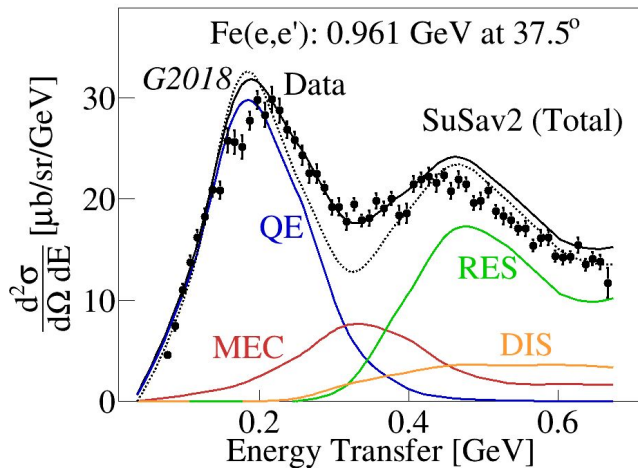
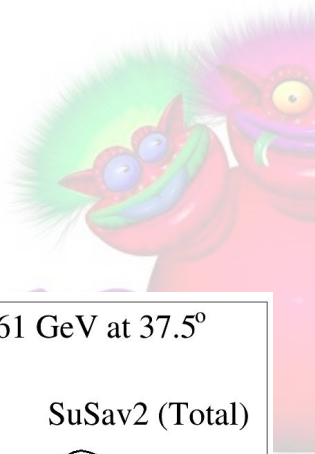


M.Khachatryan, A.Papadopoulou, et al.  
Nature 599, 565–570 (2021)



# Attacking The Modeling Monster!

- Modeling in event generators



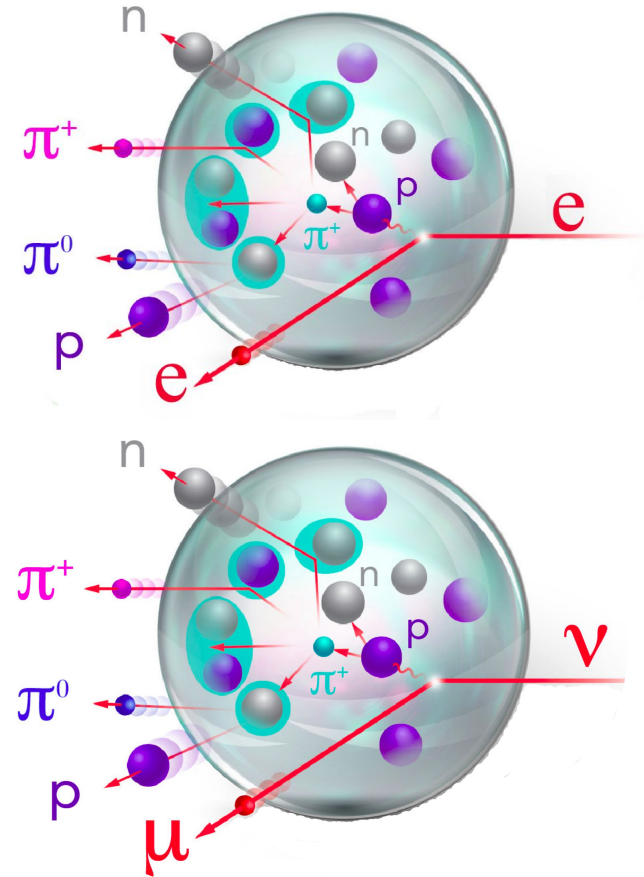
A.Papadopoulou, et al, In preparation

A.Papadopoulou, et al,  
Phys. Rev. D 103, 113003 (2021)

# Why electrons?

- Common vector current
- Identical nuclear effects
- Monoenergetic beams
- High statistics
  - Precision measurements

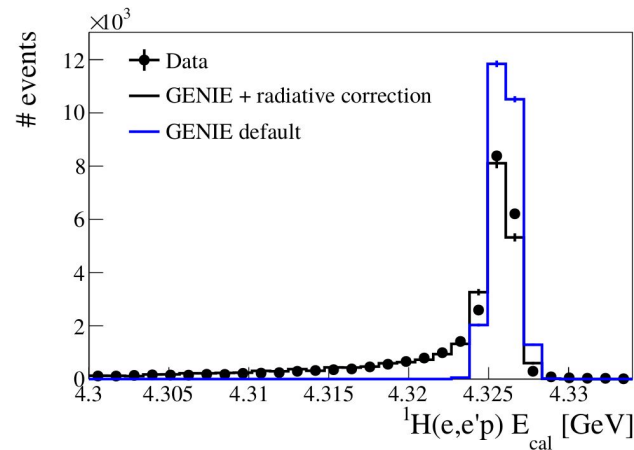
Any model must work for electrons,  
or it won't work for neutrinos !



# Cross-Section Extraction

- Subtract backgrounds
- Scale counts by luminosity
- Correct for detector acceptance & radiation

Systematic uncertainties on each correction plus variation among detector sectors

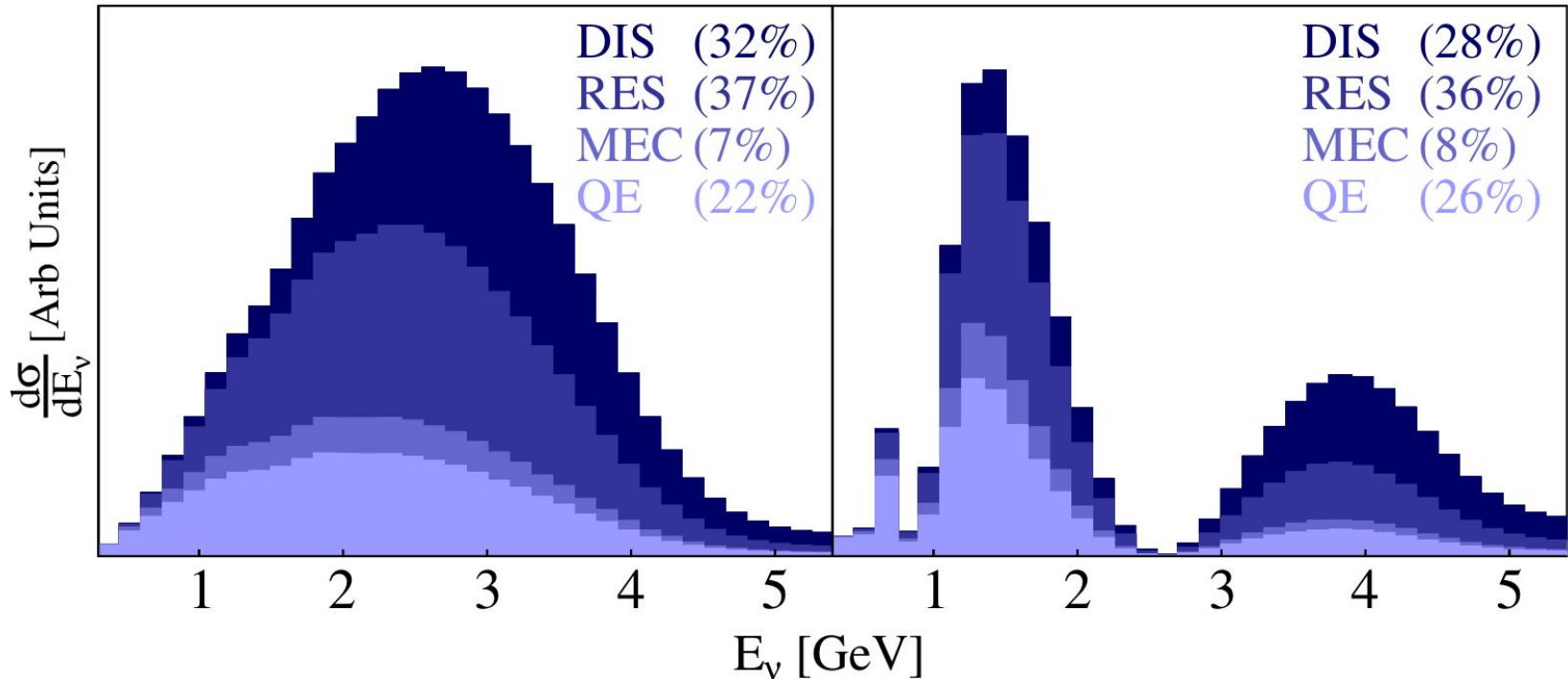


Hall A@JLab

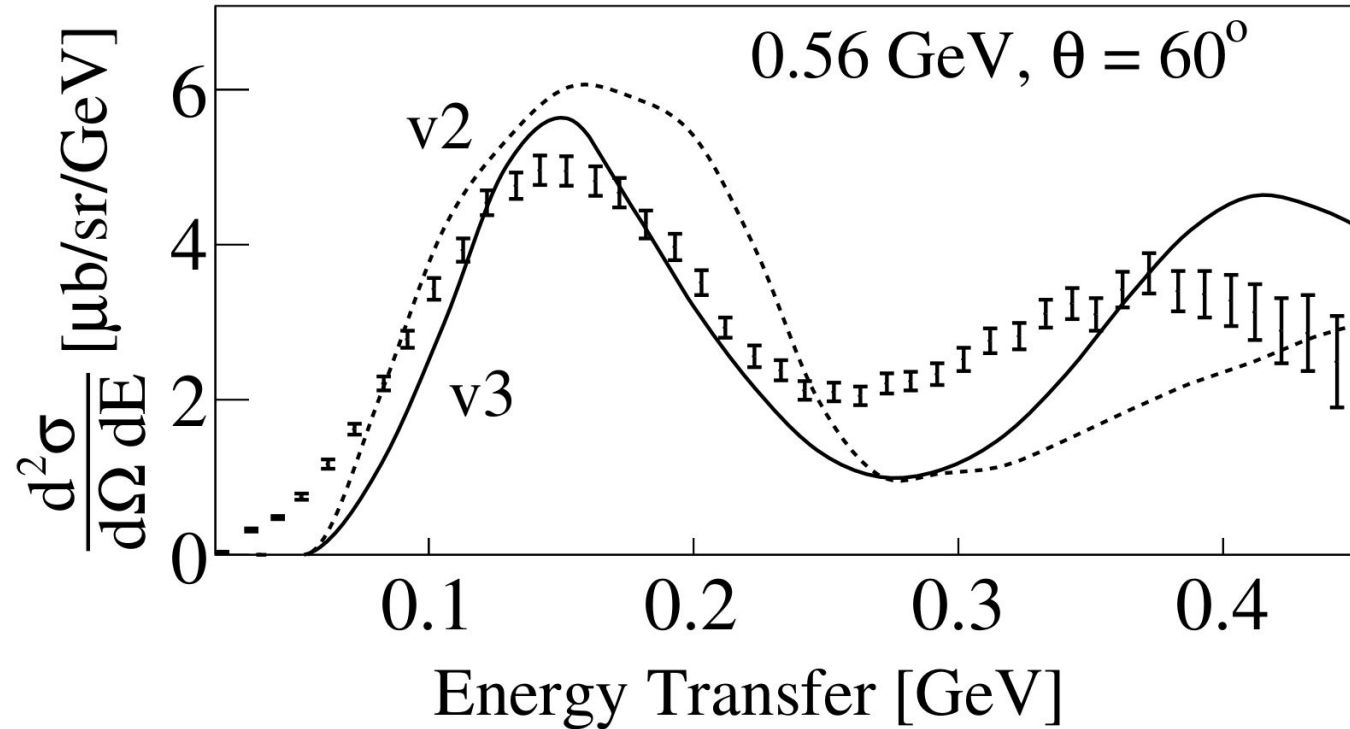
H(e,e'p) @ 4.32 GeV

# Mismodelling Impact On Mixing Parameters

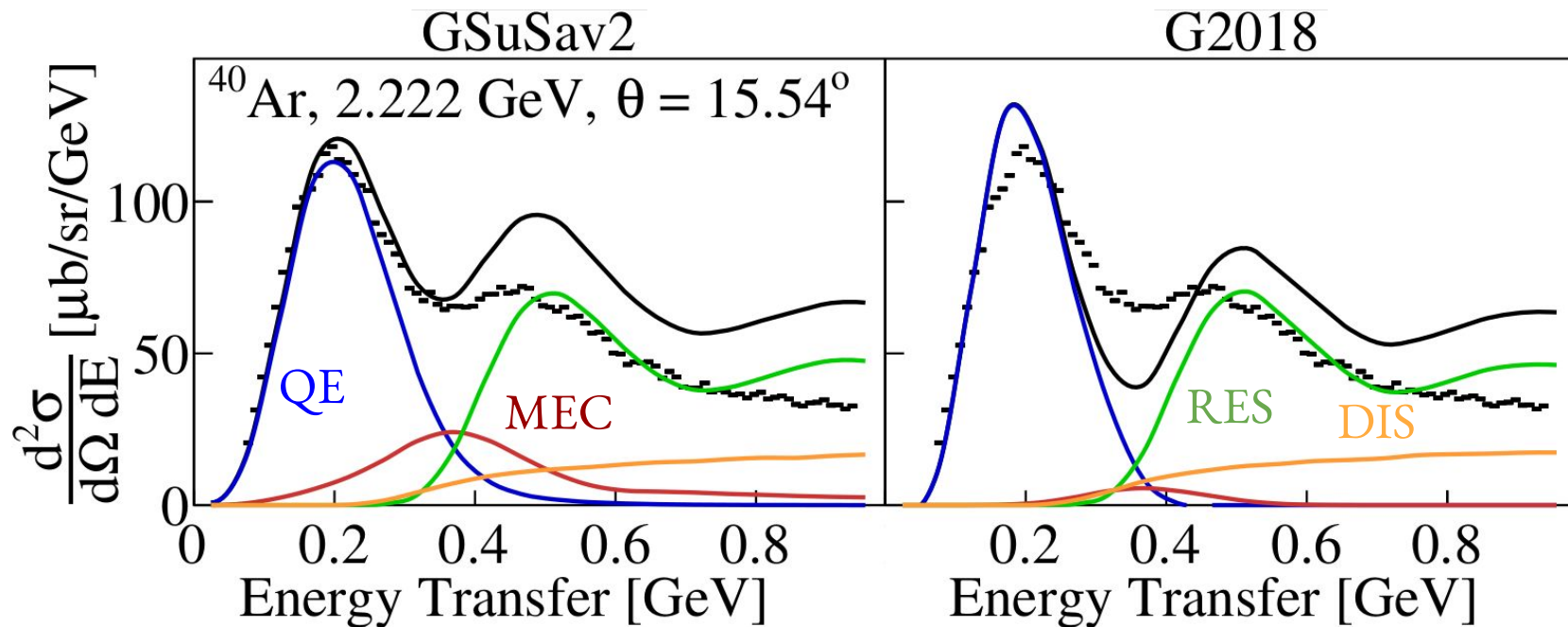
Charged current cross sections obtained using GENIE for the DUNE near detector (left) and far detector (right) oscillated fluxes



$(e,e')$   $^{12}\text{C}$  with G2018



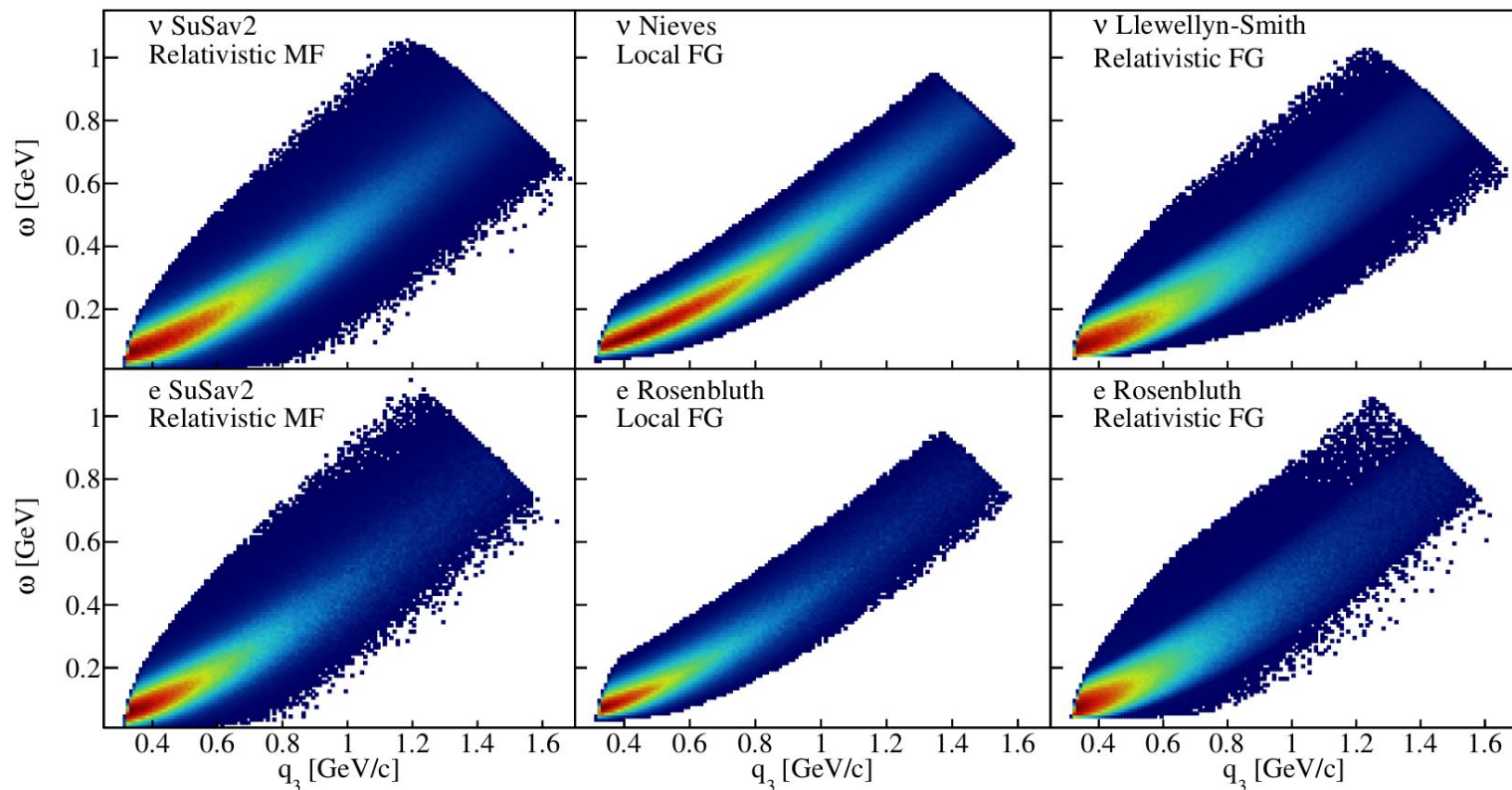
# SuSav2 Offers More Accurate Prediction





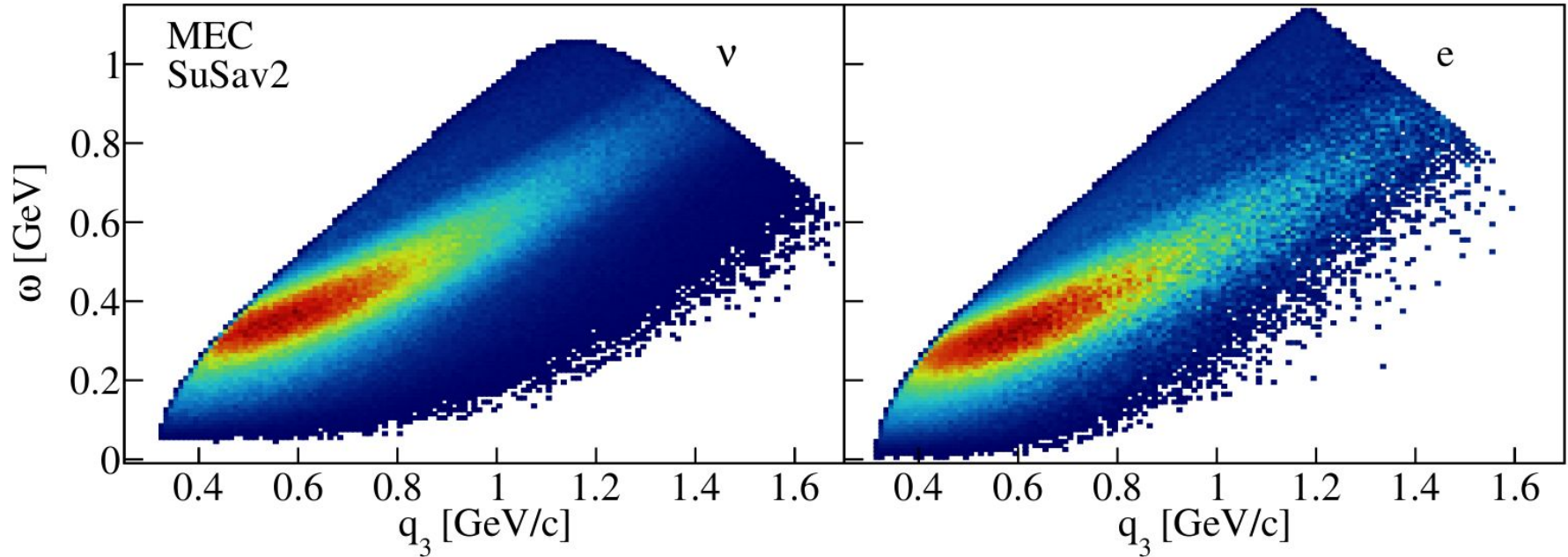
# Probing The Neutrino Phase-Space With Electrons

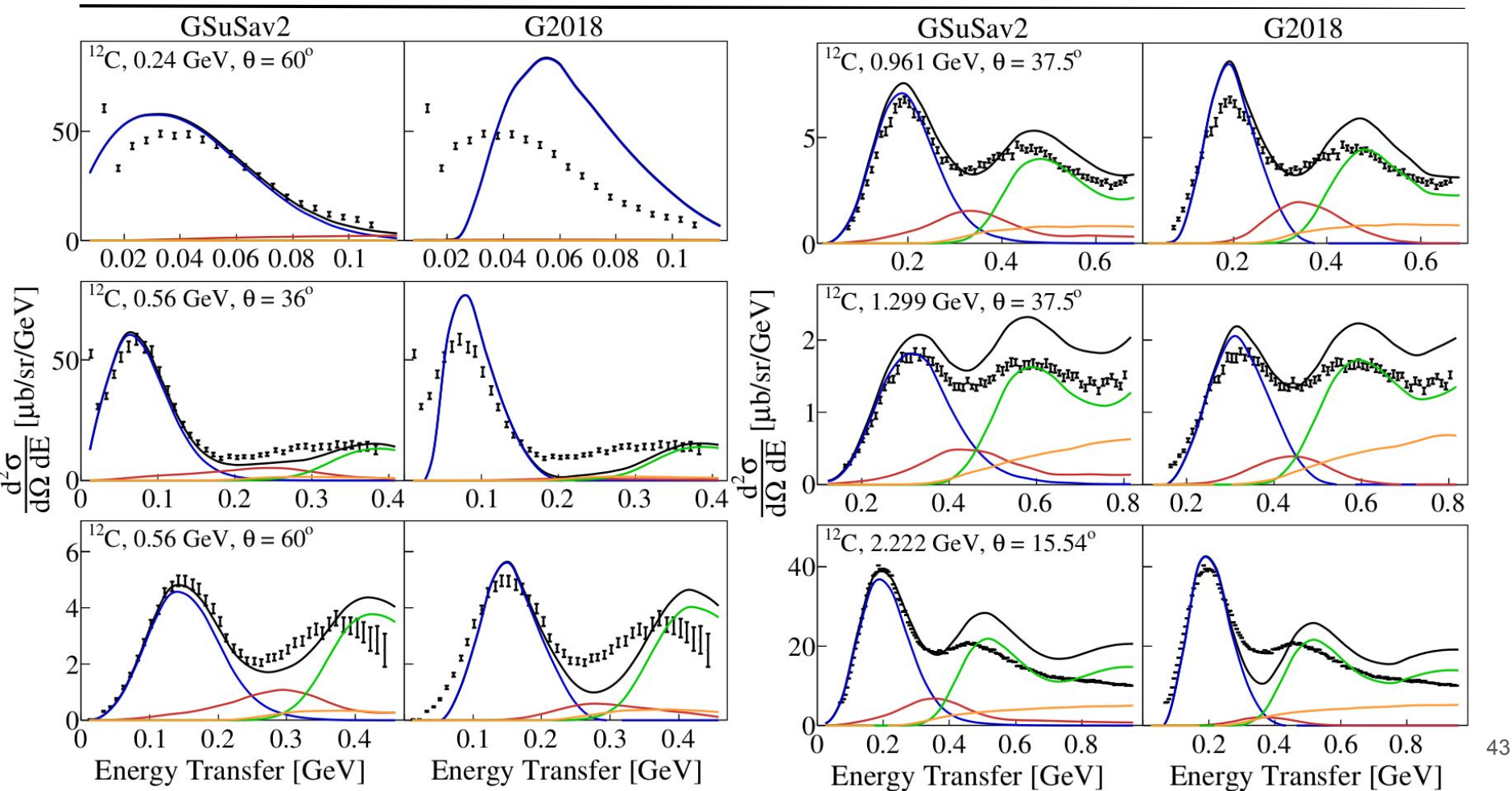
## QE Events

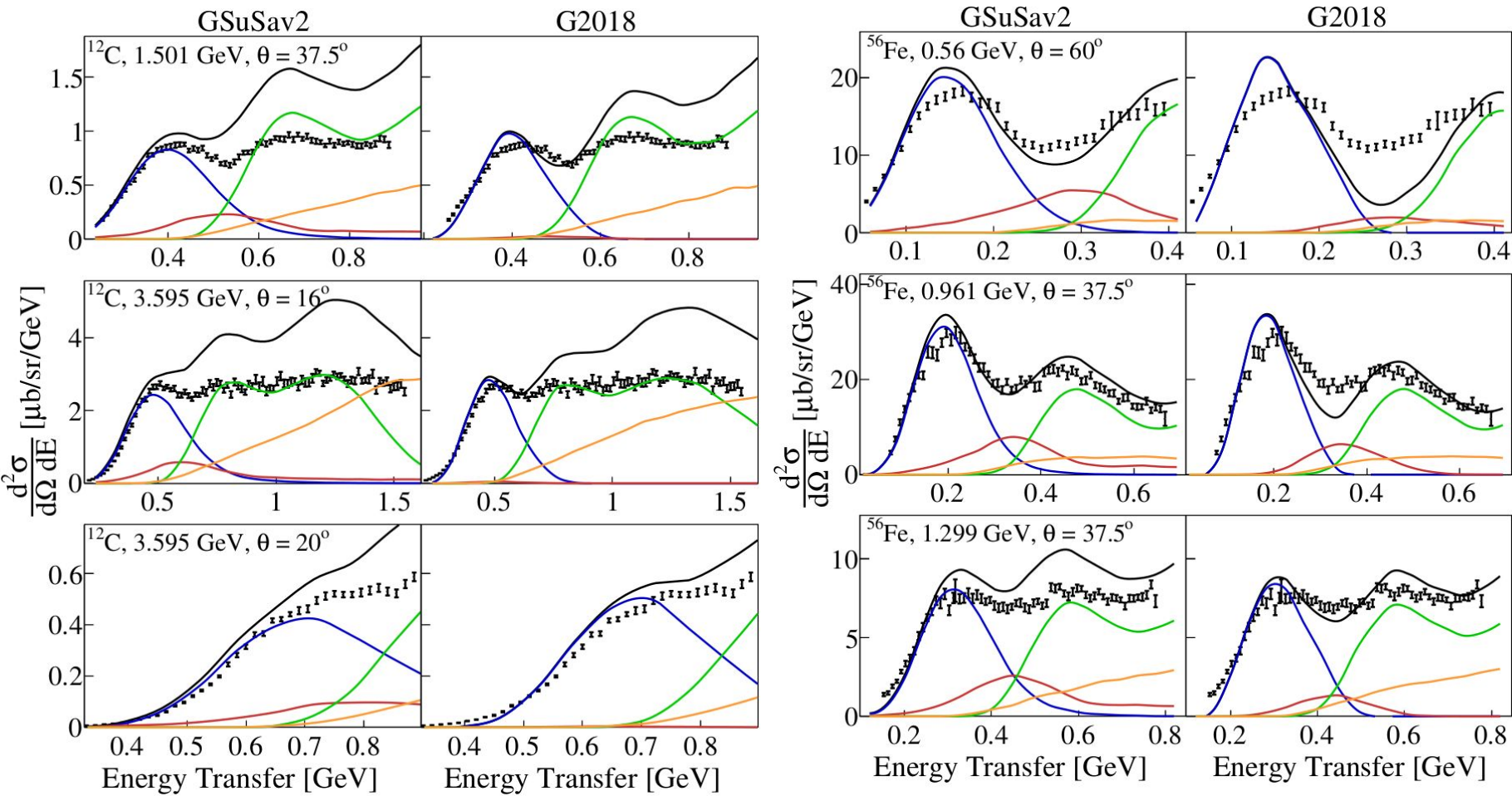


# Consistent Treatment Of MEC Events With SuSav2

Unique chance to constraint one of least understood interaction channels

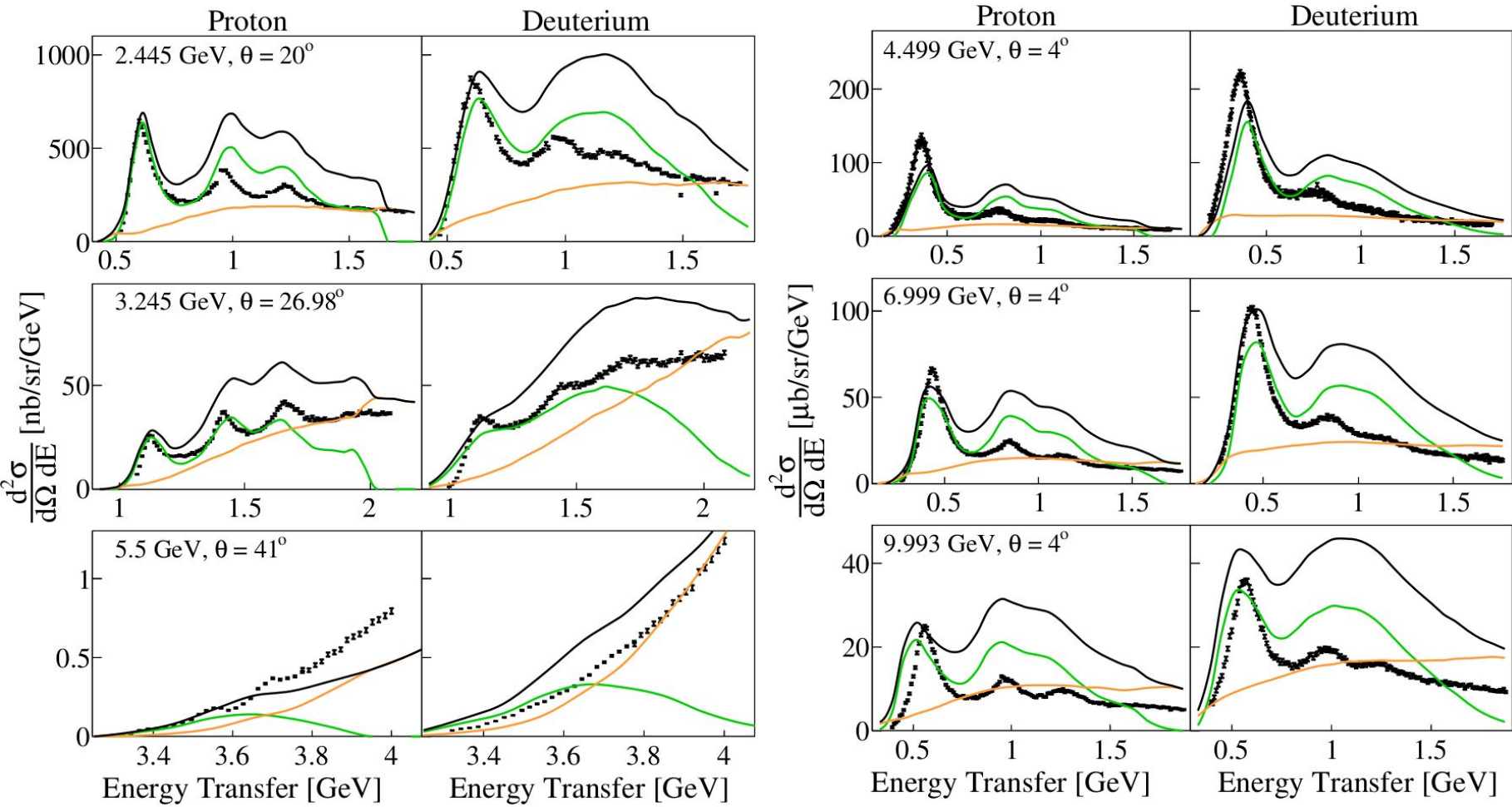




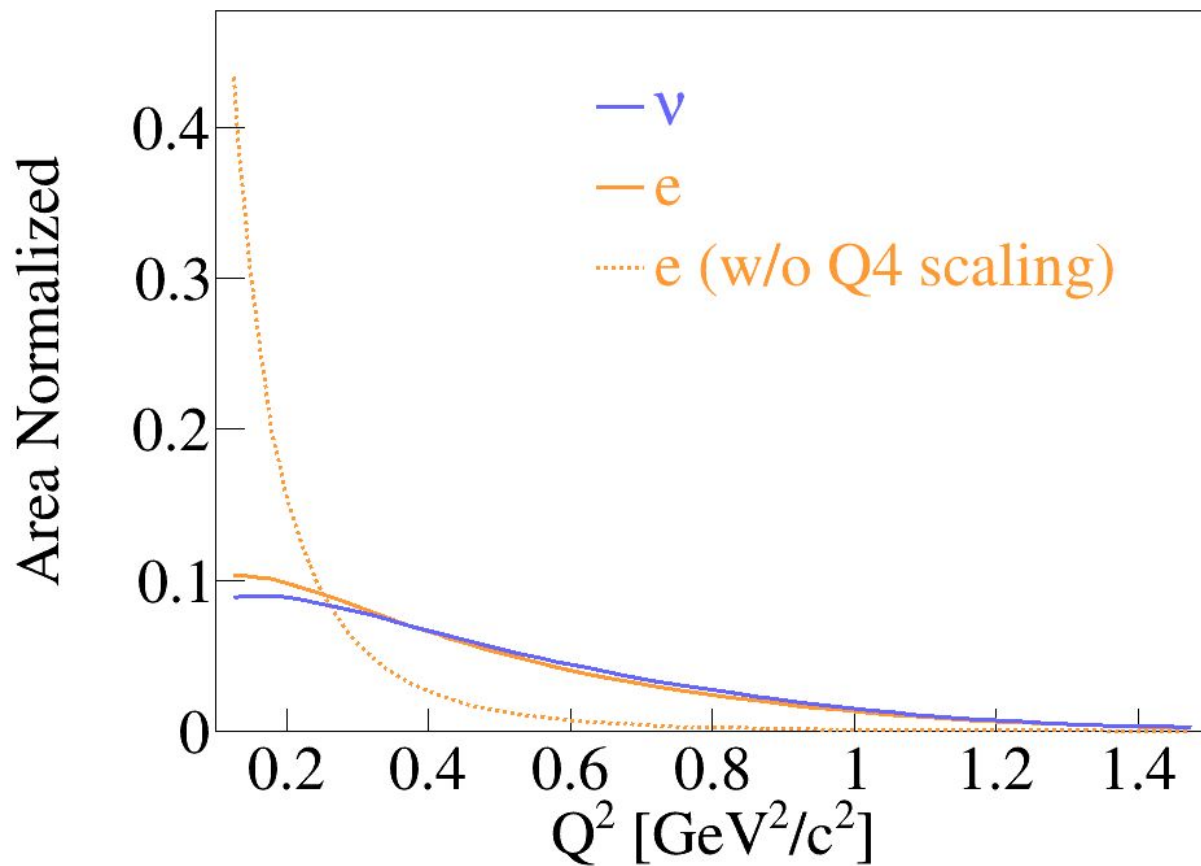


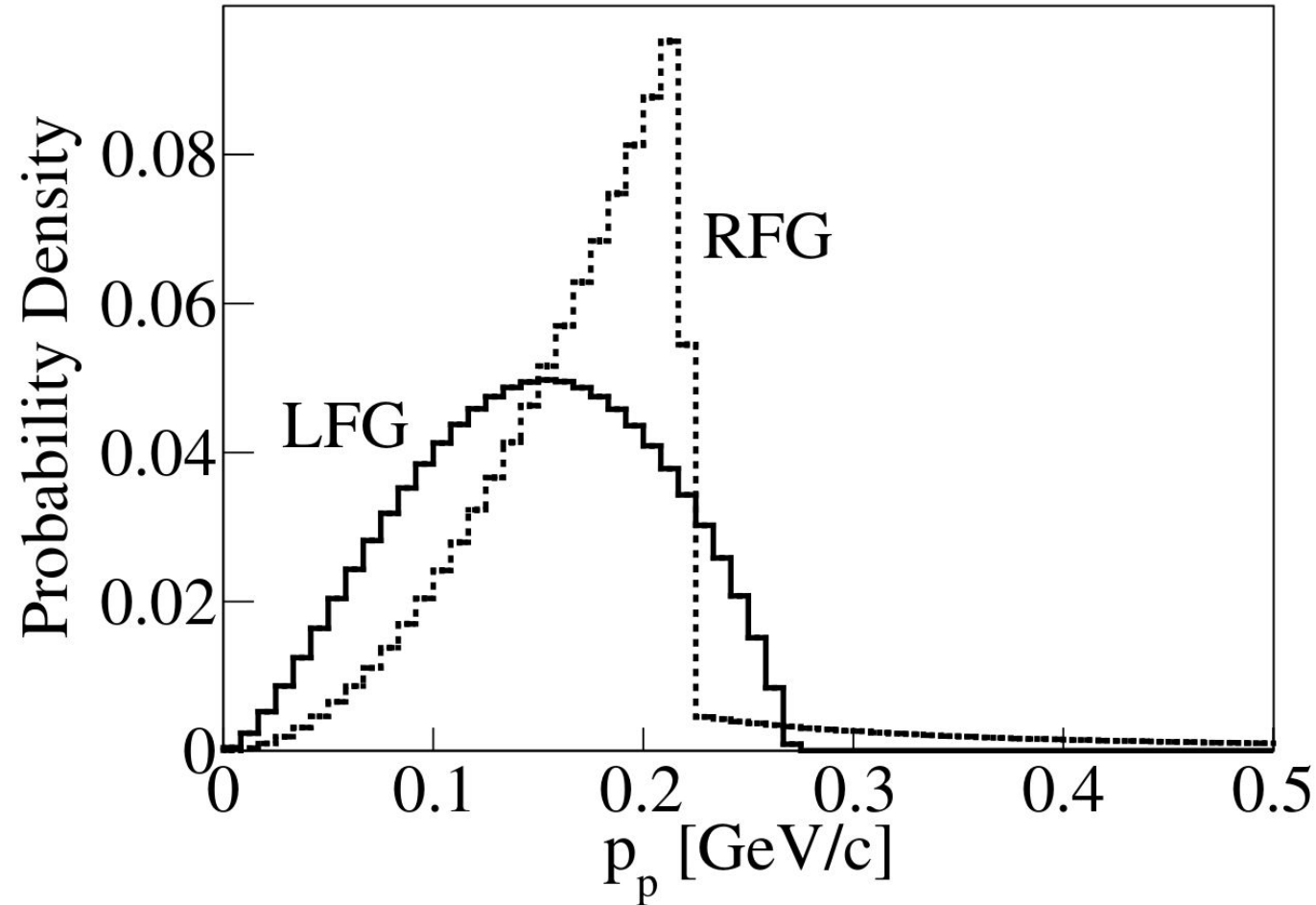
# Inclusive H cross sections

Phys. Rev. D 103, 113003 (2021)



# $Q^4$ Scaling Effect





# SuSav2 Configuration / GEM21\_11b\_00\_000

---

	<b>Electrons</b>	<b>Neutrinos</b>
<b>QE</b>	SuSav2	SuSav2
<b>MEC</b>	SuSav2	SuSav2
<b>RES</b>	Berger-Sehgal	Berger-Sehgal
<b>DIS</b>	AGKY	AGKY
<b>FSI</b>	hN2018	hN2018
<b>Nuclear Model</b>	Relativistic Mean Field	Relativistic Mean Field



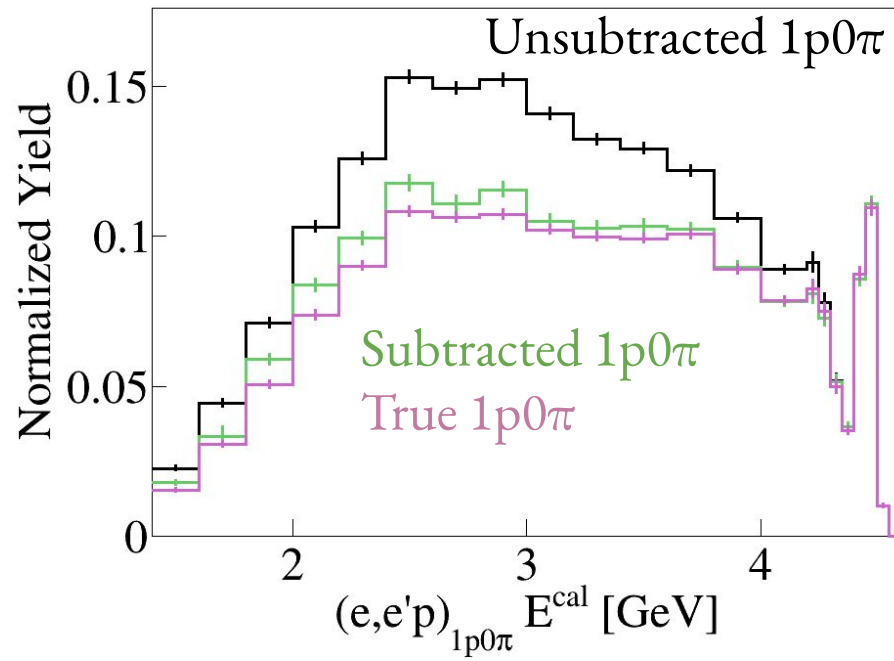
# G2018 Model Configuration

---

	<b>Electrons</b>	<b>Neutrinos</b>
<b>QE</b>	Rosenbluth	Nieves
<b>MEC</b>	Empirical	Nieves
<b>RES</b>	Berger-Sehgal	Berger-Sehgal
<b>DIS</b>	AGKY	AGKY
<b>FSI</b>	hA2018	hA2018
<b>Nuclear Model</b>	Local Fermi Gas	Local Fermi Gas

# Closure Test

- Use GENIE files
- Filter specific topologies (e.g.  $1p0\pi p + 1p1\pi$ )
- **Subtracted** & **True**  $1p0\pi$  are in good agreement



# Well defined signal definition: Min $\theta_e$ Cut

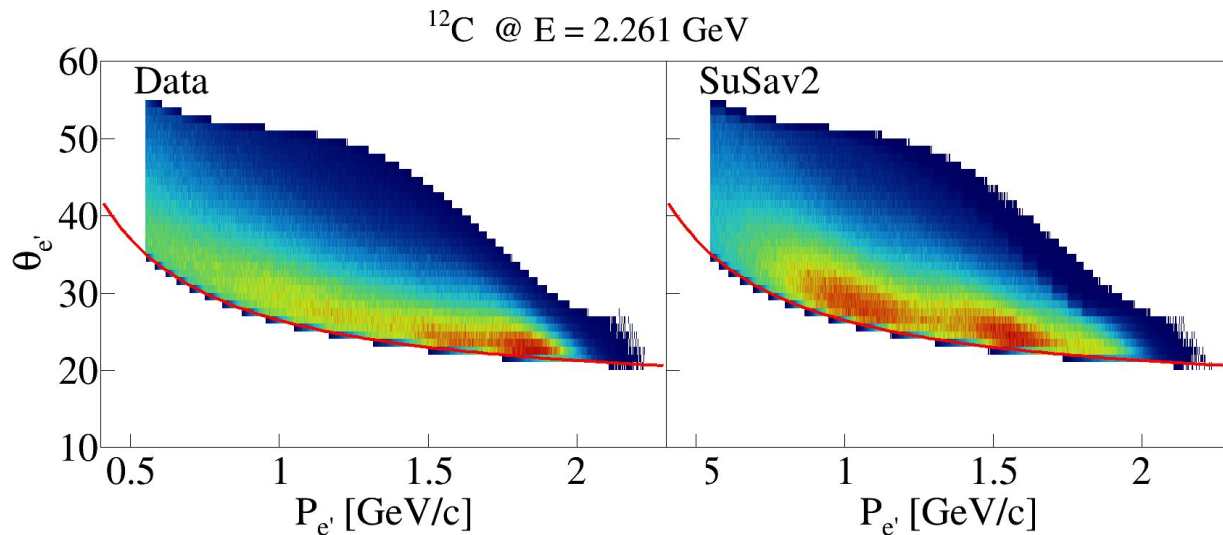
@ 1.1 GeV:  $\theta = 17 + 7 / P$

@ 2.2 GeV:  $\theta = 16 + 10.5 / P$

@ 4.4 GeV:  $\theta = 13.5 + 15 / P$

See backup for p /  $\pi^{+/-}$  definitions

- We do not acceptance correct below min  $\theta$



# Well defined signal definition: Min $\theta_e$ Cut

@ 1.1 GeV:  $\theta = 17 + 7 / P$

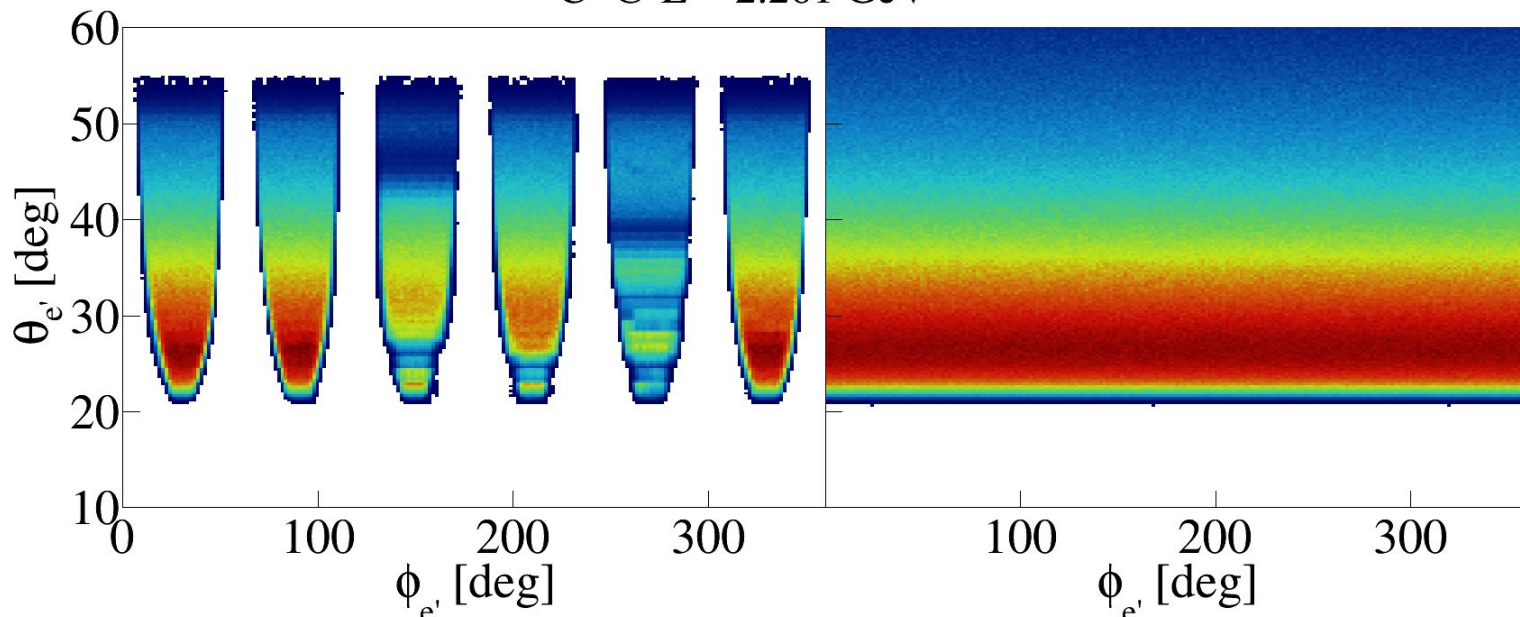
@ 2.2 GeV:  $\theta = 16 + 10.5 / P$

@ 4.4 GeV:  $\theta = 13.5 + 15 / P$

See backup for  $p / \pi^{+/-}$  definitions

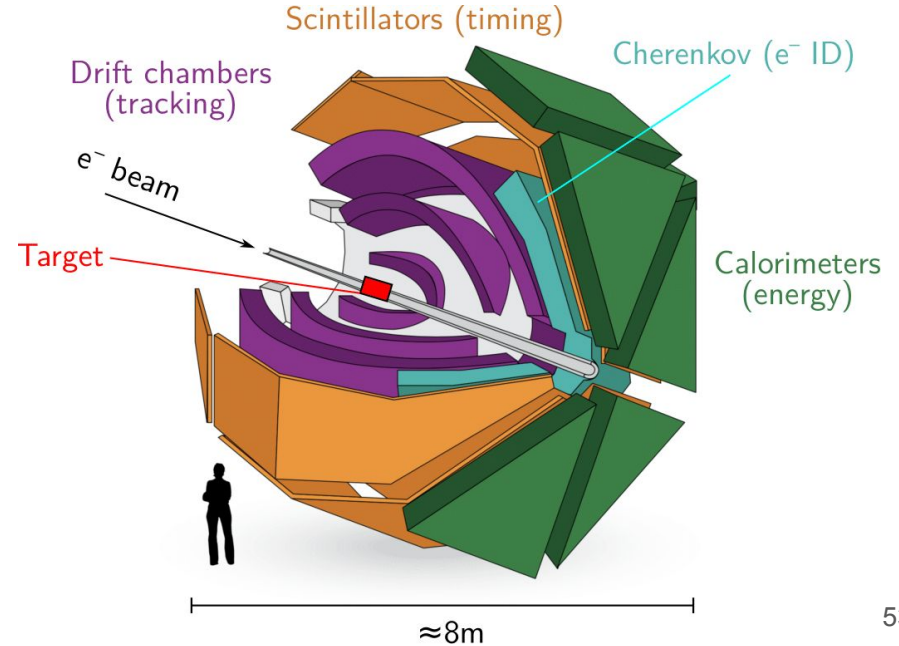
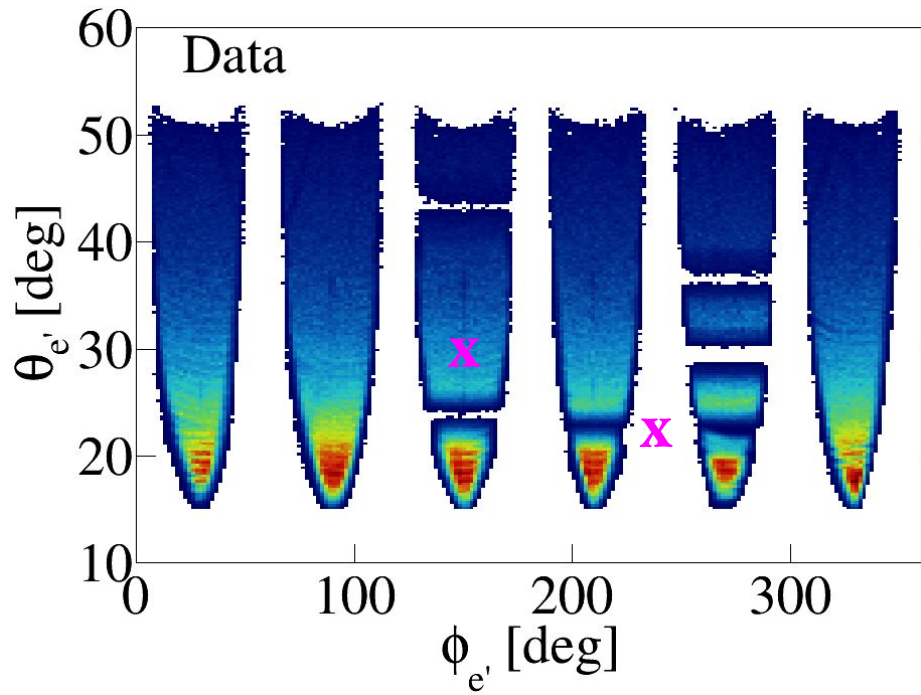
- We do not acceptance correct below min  $\theta$

$^{12}\text{C}$  @  $E = 2.261$  GeV



# Background Subtraction

Non-( $e,e'p$ ) interactions lead to multi-hadron final states  
Gaps can make them look like ( $e,e'p$ ) events

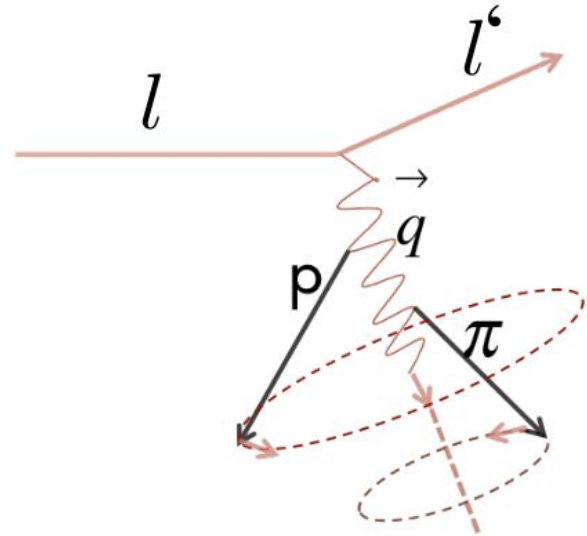


# Data Driven Correction

---

Non-( $e,e'p$ ) interactions lead to multi-hadron final states  
Gaps make them look like ( $e,e'p$ ) events

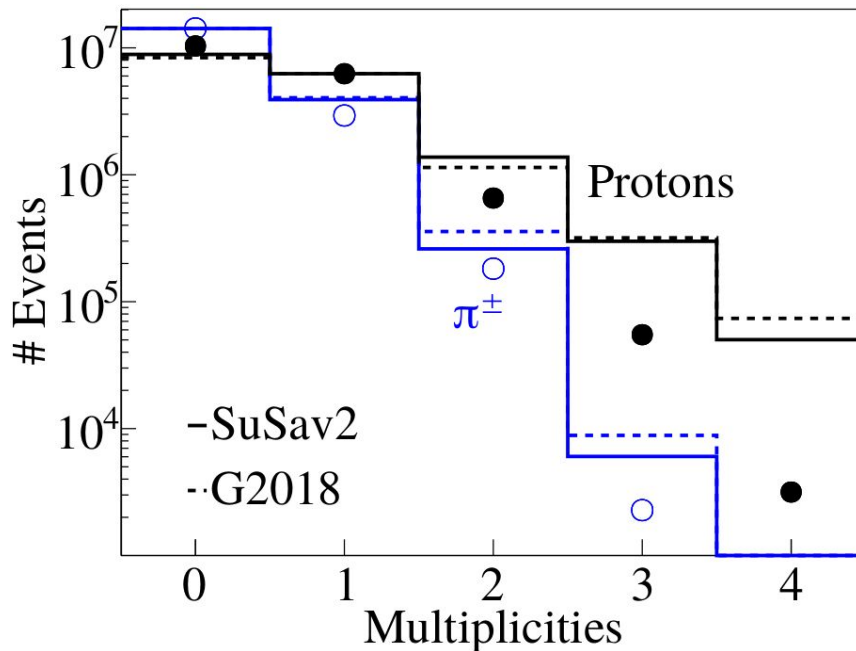
- Use measured ( $e,e'p\pi$ ) events
- Rotate  $p$ ,  $\pi$  around  $q$  to determine  $\pi$  detection efficiency
- Subtract undetected ( $e,e'p\pi$ )
- Repeat for higher hadron multiplicities



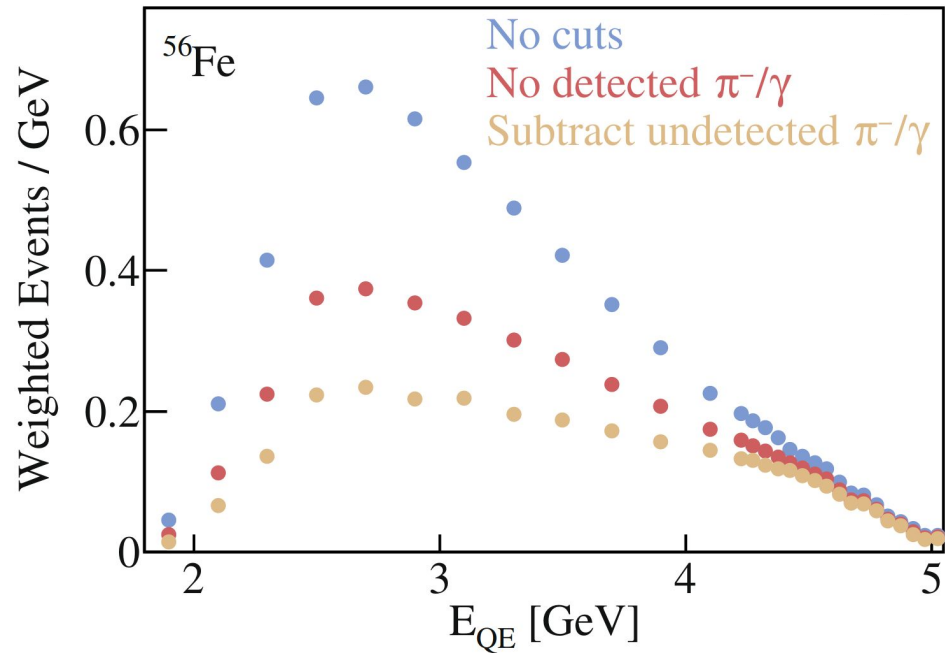
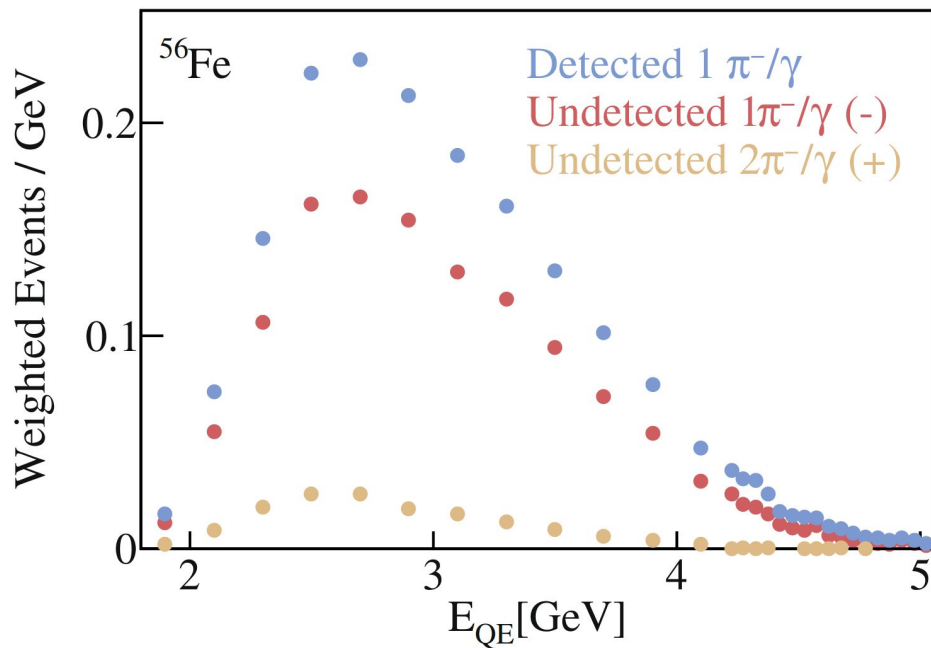
# Data Driven Correction

Non-( $e,e'p$ ) interactions lead to multi-hadron final states  
Gaps can make them look like ( $e,e'p$ ) events

- Use measured ( $e,e'p\pi$ ) events
- Rotate  $p$ ,  $\pi$  around  $q$  to determine  $\pi$  detection efficiency
- Subtract for undetected ( $e,e'p\pi$ )
- Repeat for higher hadron multiplicities  
( $2p$ ,  $3p$ ,  $2p+1\pi$ , ...)



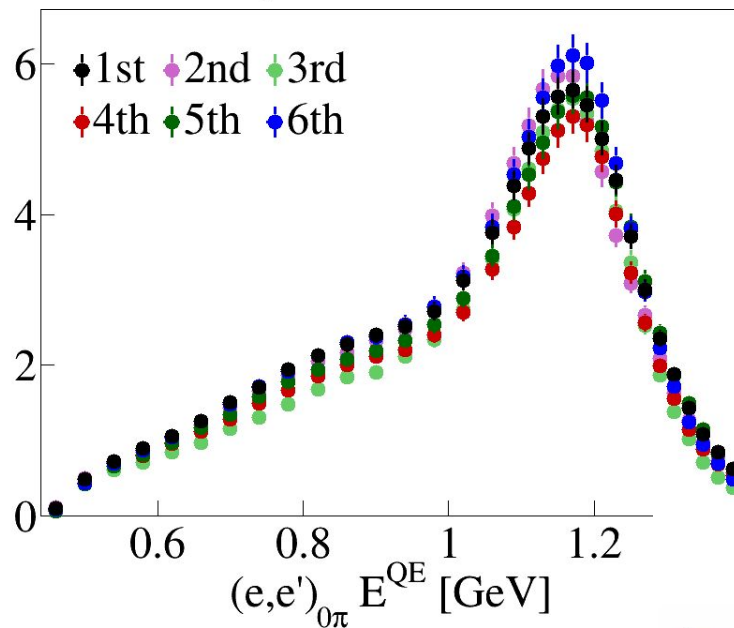
# Subtraction Effect



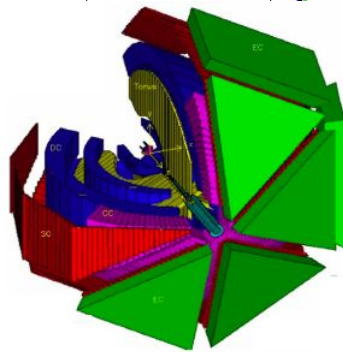
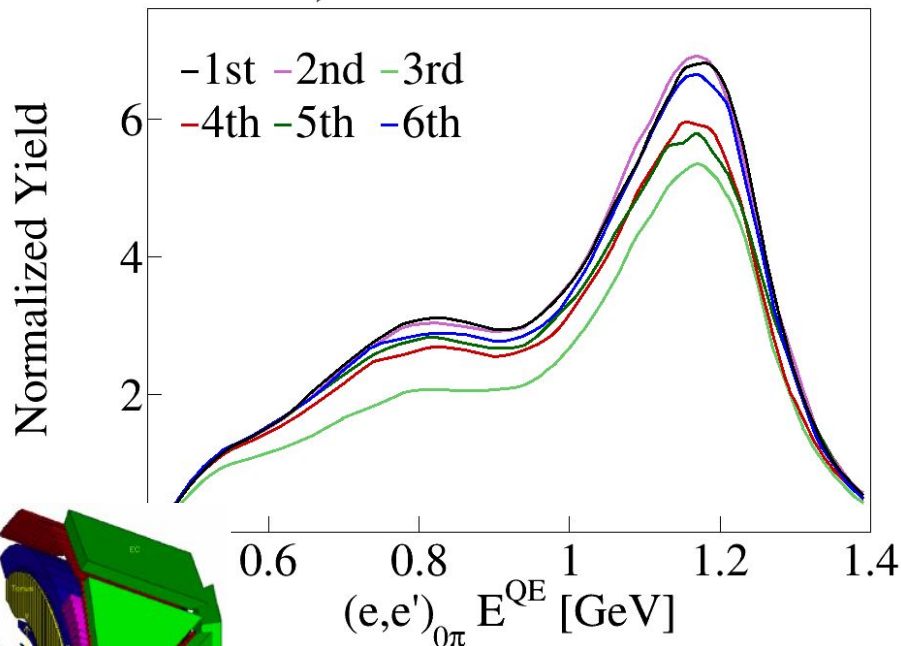


# Systematics: Sector Dependence

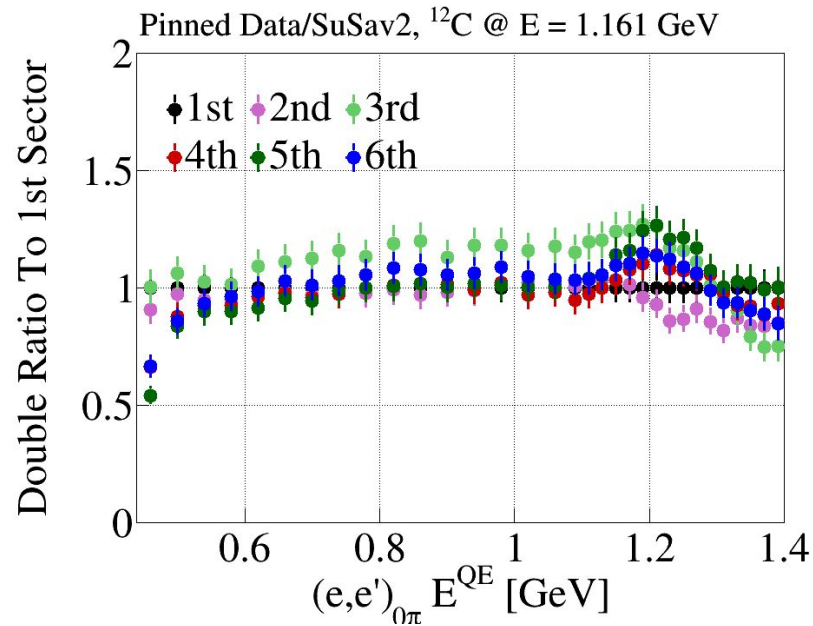
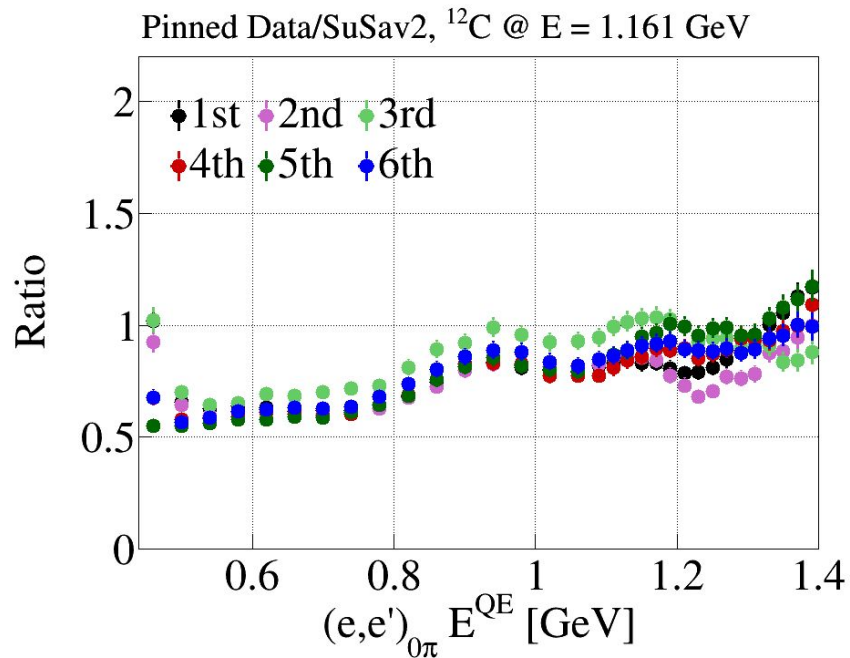
Pinned Data,  $^{12}\text{C}$  @  $E = 1.161$  GeV



SuSav2,  $^{12}\text{C}$  @  $E = 1.161$  GeV

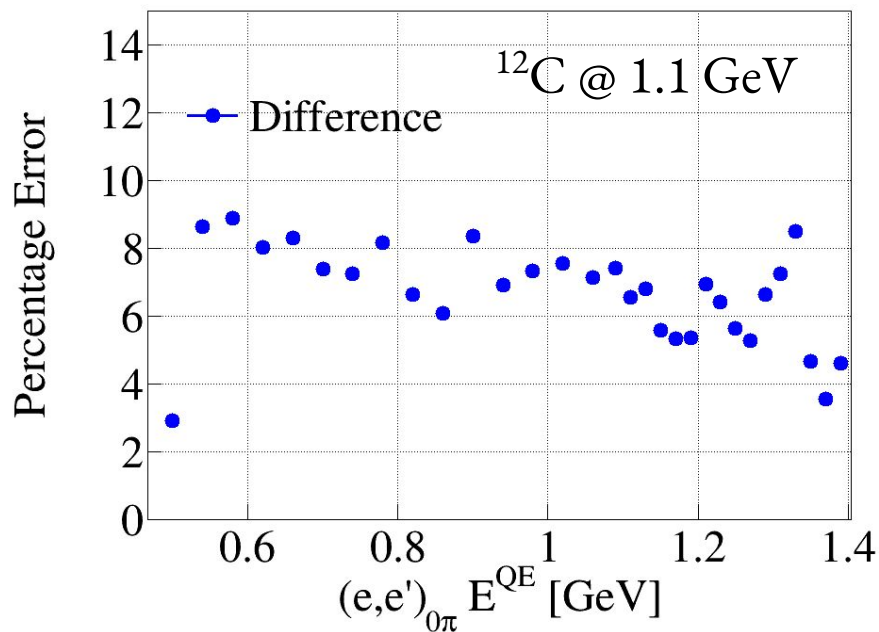


# Systematics: Sector Dependence



# Systematics: Sector Dependence

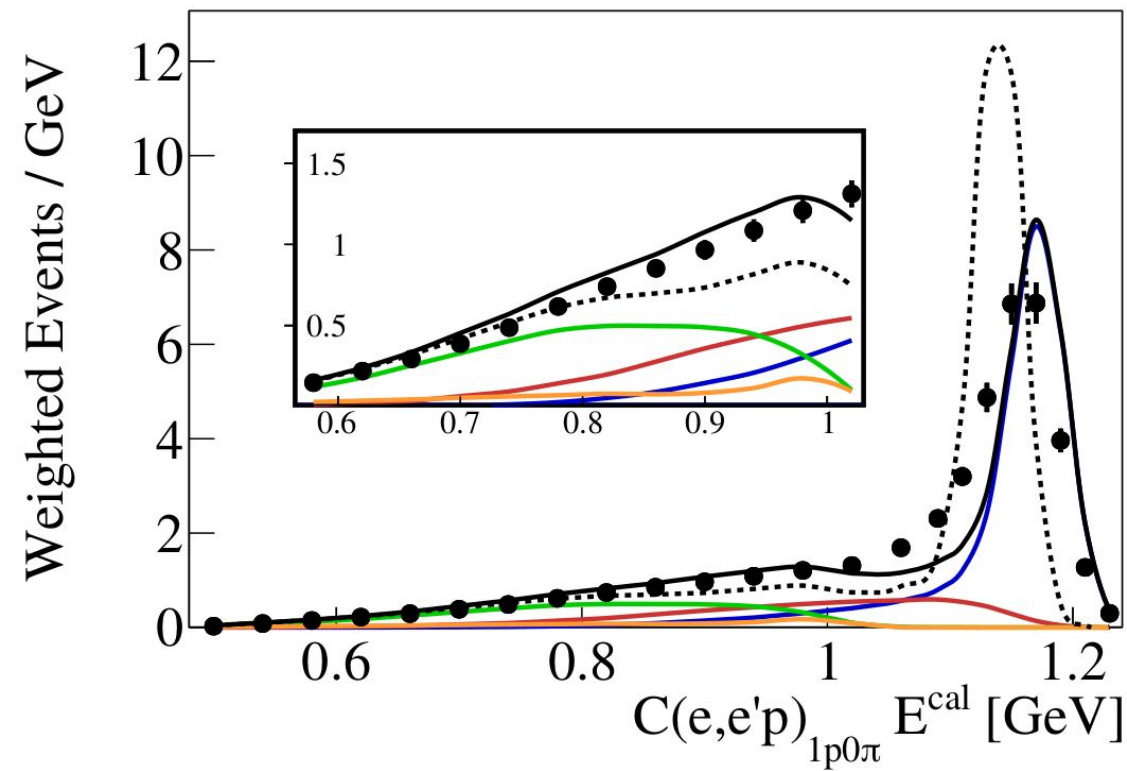
Quantifying uncertainty by using unweighted variance & by subtracting variance from statistical uncertainty



- Playing this game across all nuclei & energies
- Division by  $\sqrt{N}_{\text{sectors}}$
- Flat uncertainty of 6%

# 1st $e4\nu$ Submission

Calorimetric energy reconstruction using the  $1p0\pi$  channel



- Area normalized results
- No information with respect to absolute scale
- G2018 offset potentially due to binding energy issue

• Data

— SuSav2 (Total)

— QE — MEC

— RES — DIS

-- G2018

## Step #2: Normalized Yield

---

### Data

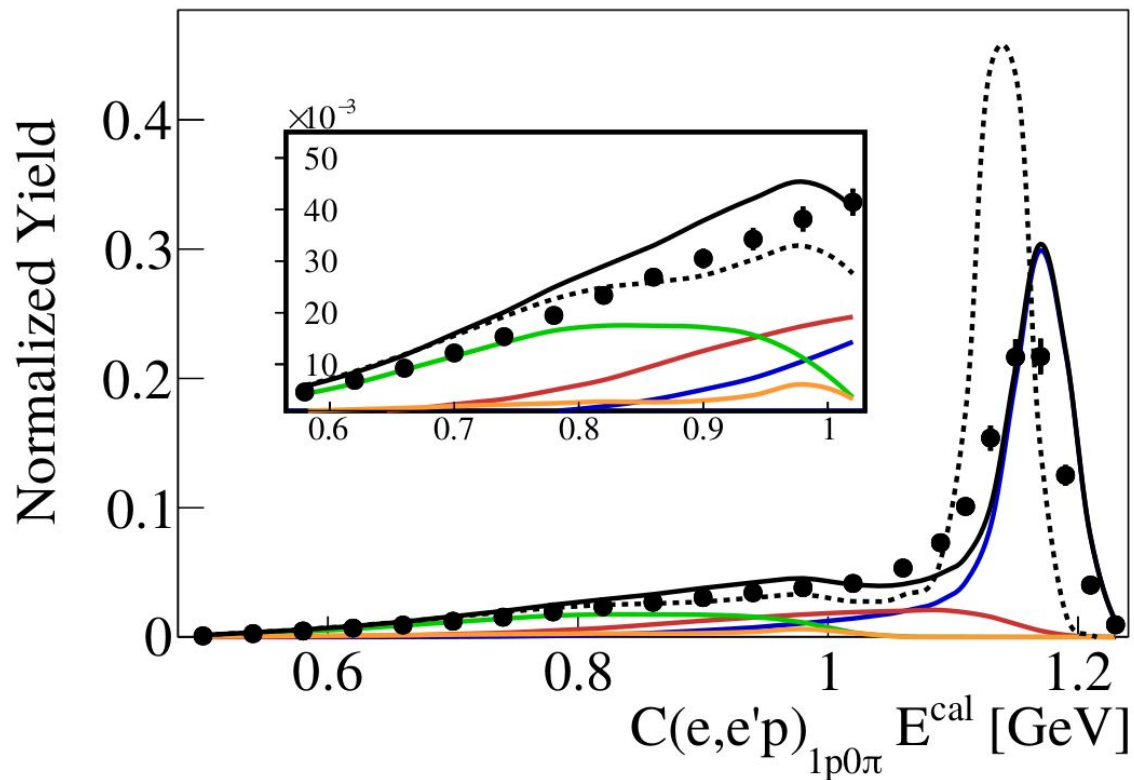
- Divide # events by integrated charge & target thickness to get xsec in  $\mu\text{b}$
- Divide by bin width to get  $\mu\text{b}/\text{GeV}$

### Simulation

- Get GENIE total cross section for  $E_e$  / target A &  $Q2 > Q2_{\text{min}}$
- $\text{xsec} = (\text{Selected detected events} / \text{all generated events}) * \text{total xsec} / \text{bin width}$

No corrections for CLAS acceptance or for bremsstrahlung radiation

## Step #2: Normalized Yield



- Absolute scale comparison
- Small effect @ 1GeV

• Data

— SuSav2 (Total)

— QE — MEC

— RES — DIS

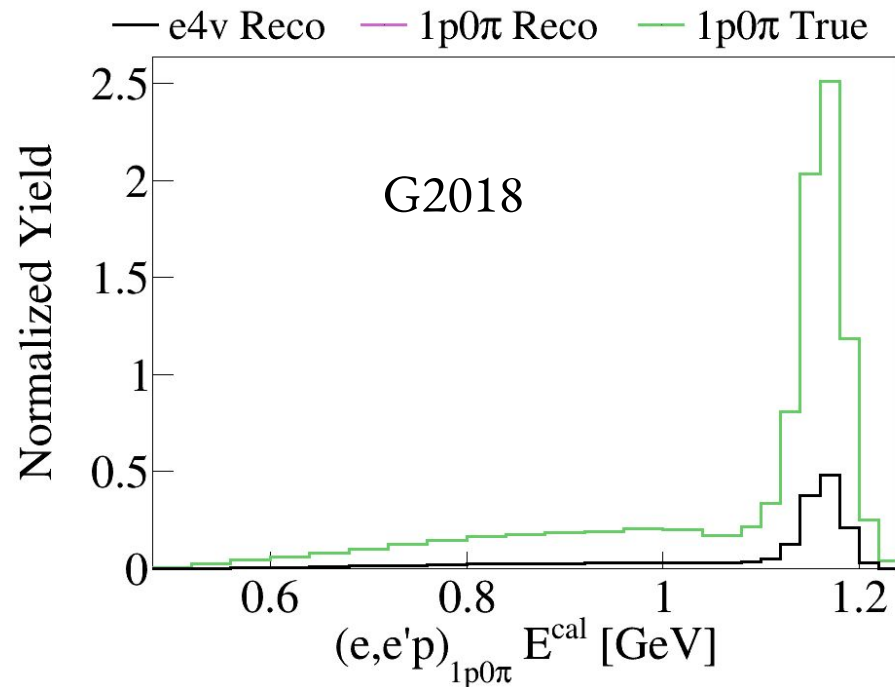
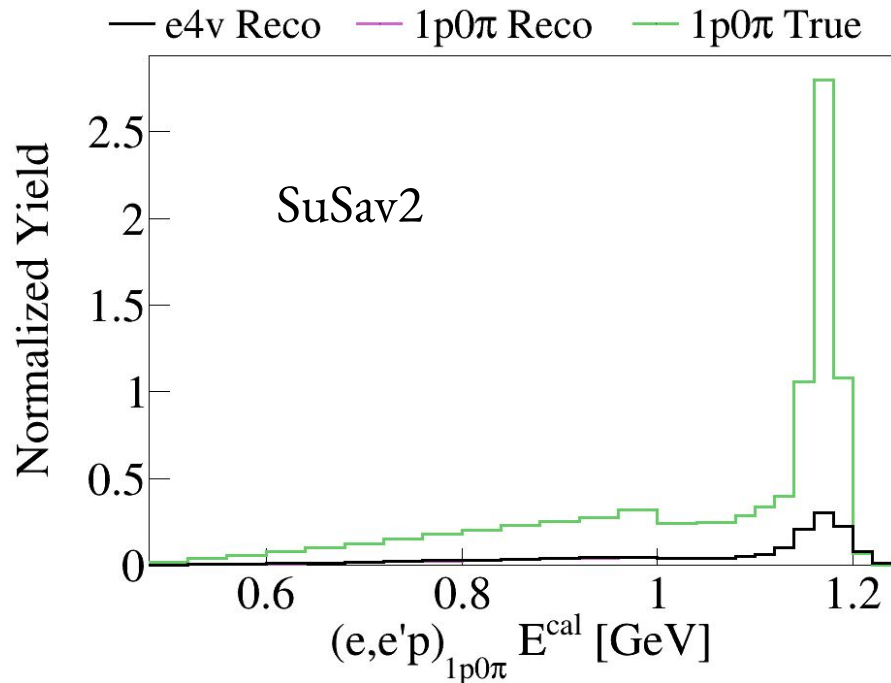
-- G2018

## Step #3a: Acceptance Correction

---

- Start from reco / true ratio w/o radiation to obtain acceptance correction
- Average on a bin-by-bin basis  $x = |\text{SuSav2} + \text{G2018}| / 2$
- Due to offset, G2018 Ecal predictions have been shifted by  
10/25/36 MeV for  $^4\text{He}/^{12}\text{C}/^{56}\text{Fe}$  respectively

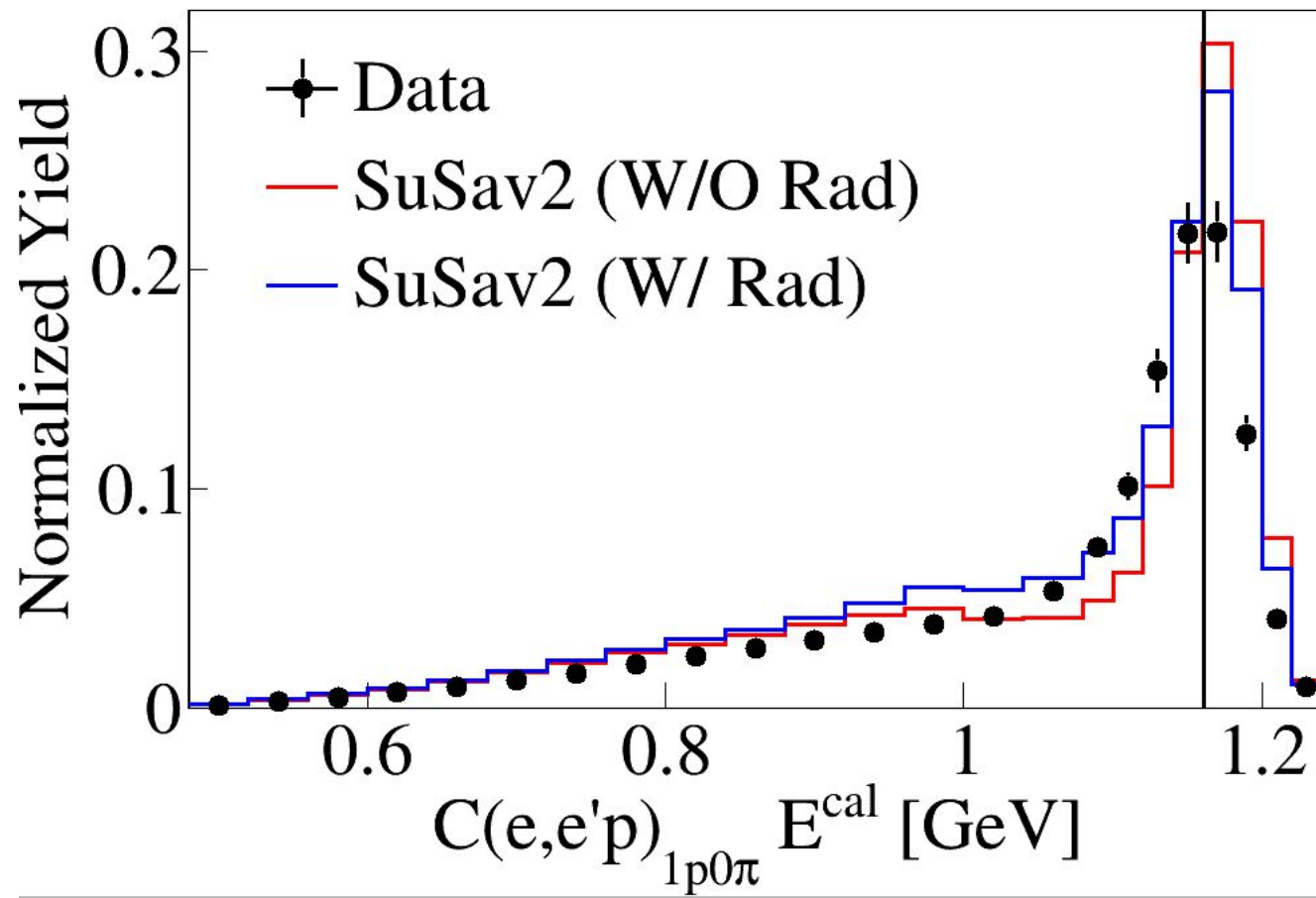
# Step #3a: Example 12C @ 1.1 GeV



Use reco / true ratio to obtain acceptance correction



## Step #3b: Radiation Correction



Use ratio of red / blue  
to correct for radiation

# Averaged Acceptance Correction Uncertainty Over True Beam Energy

---

On a bin-by-bin basis

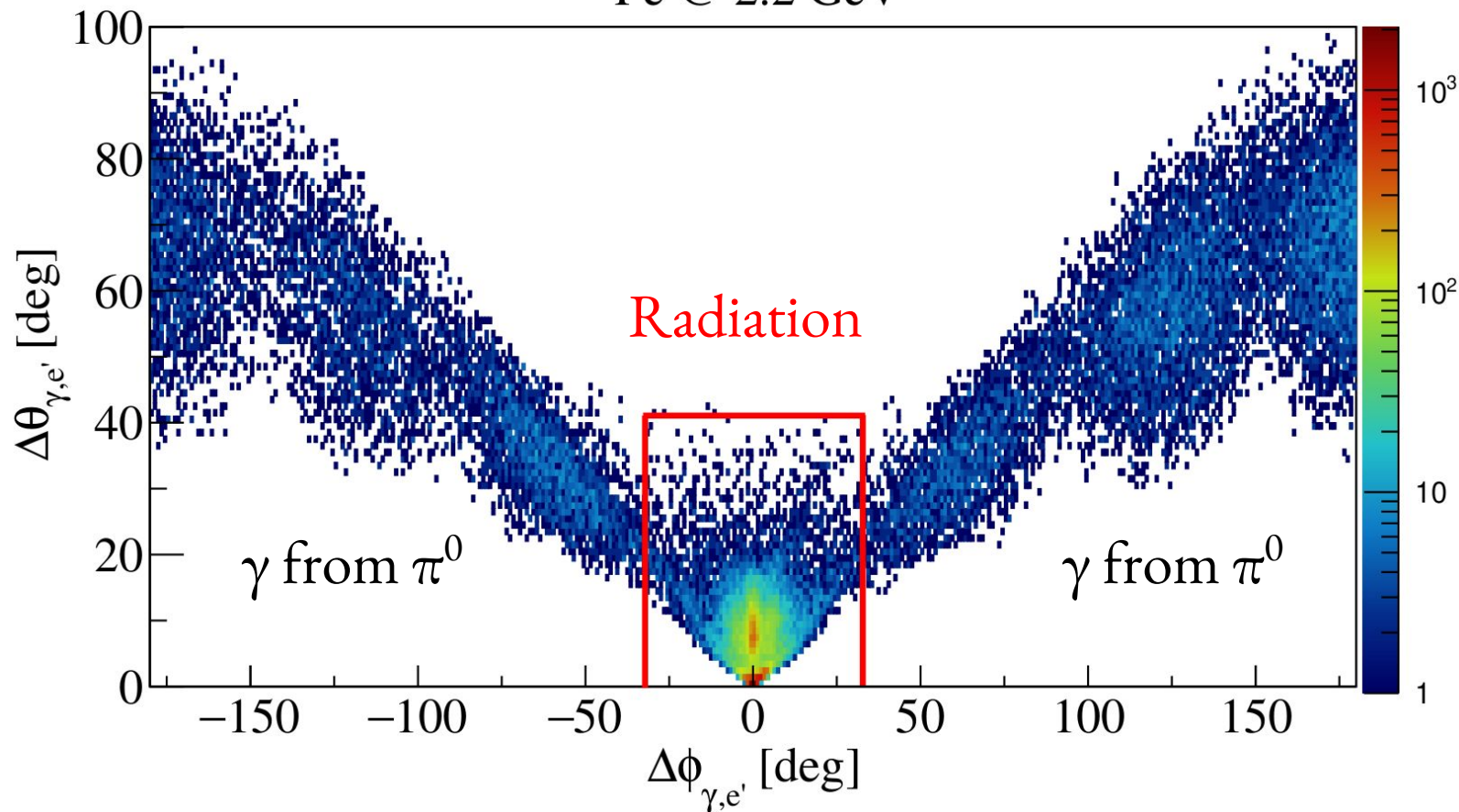
$$x = |\text{SuSav2} - \text{G2018}| / \text{Sqrt}(12)$$

$$\text{Bin Entry} = x / \text{Average} * 100 \%$$

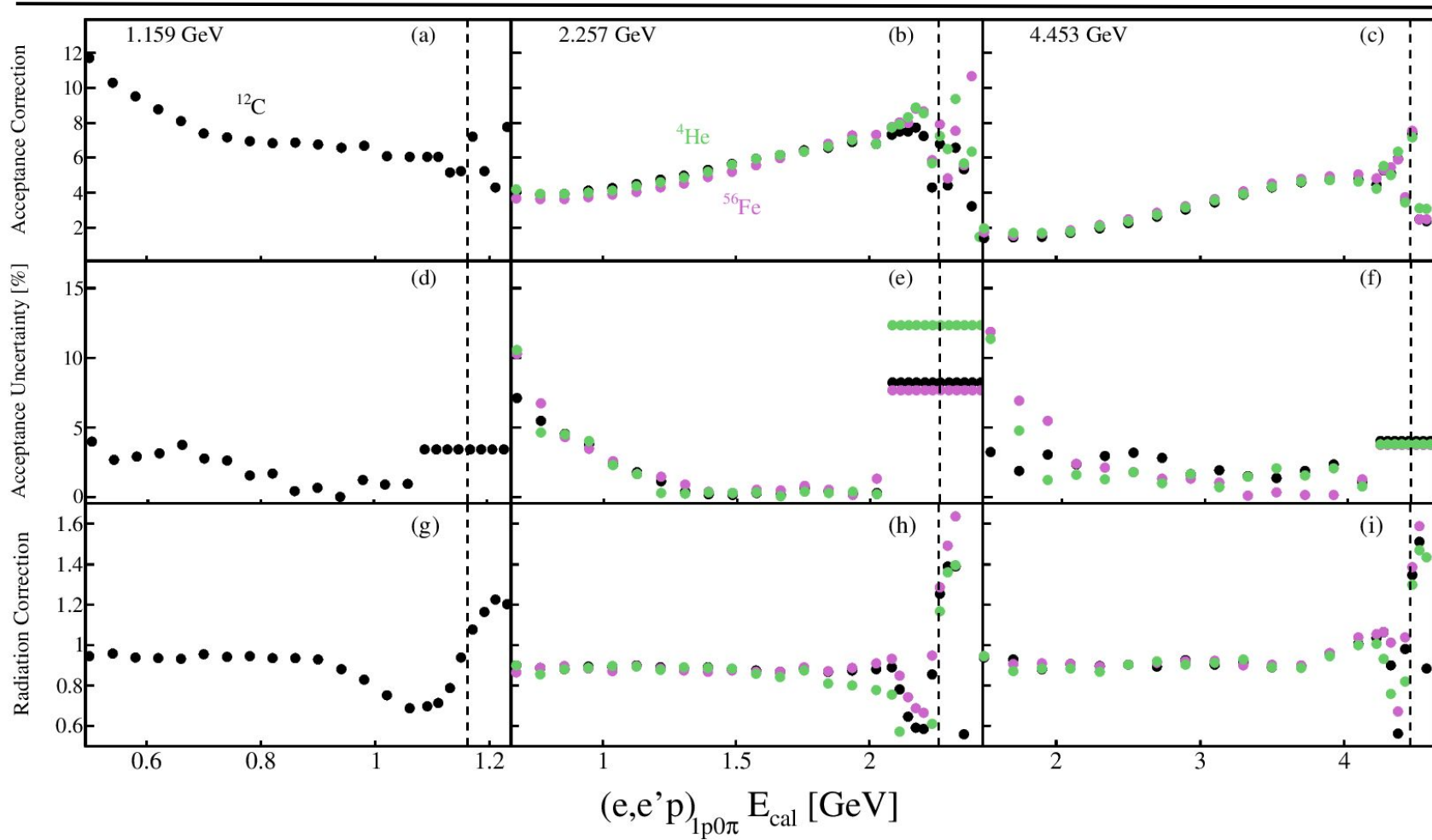
Same recipe as for acceptance correction but,  
to avoid infinities, will use average (1 bin) around the peak and  
 $\text{average}(\text{reco}) / \text{average}(\text{true})$  for correction factor

# Excluding Radiation

$^{56}\text{Fe}$  @ 2.2 GeV

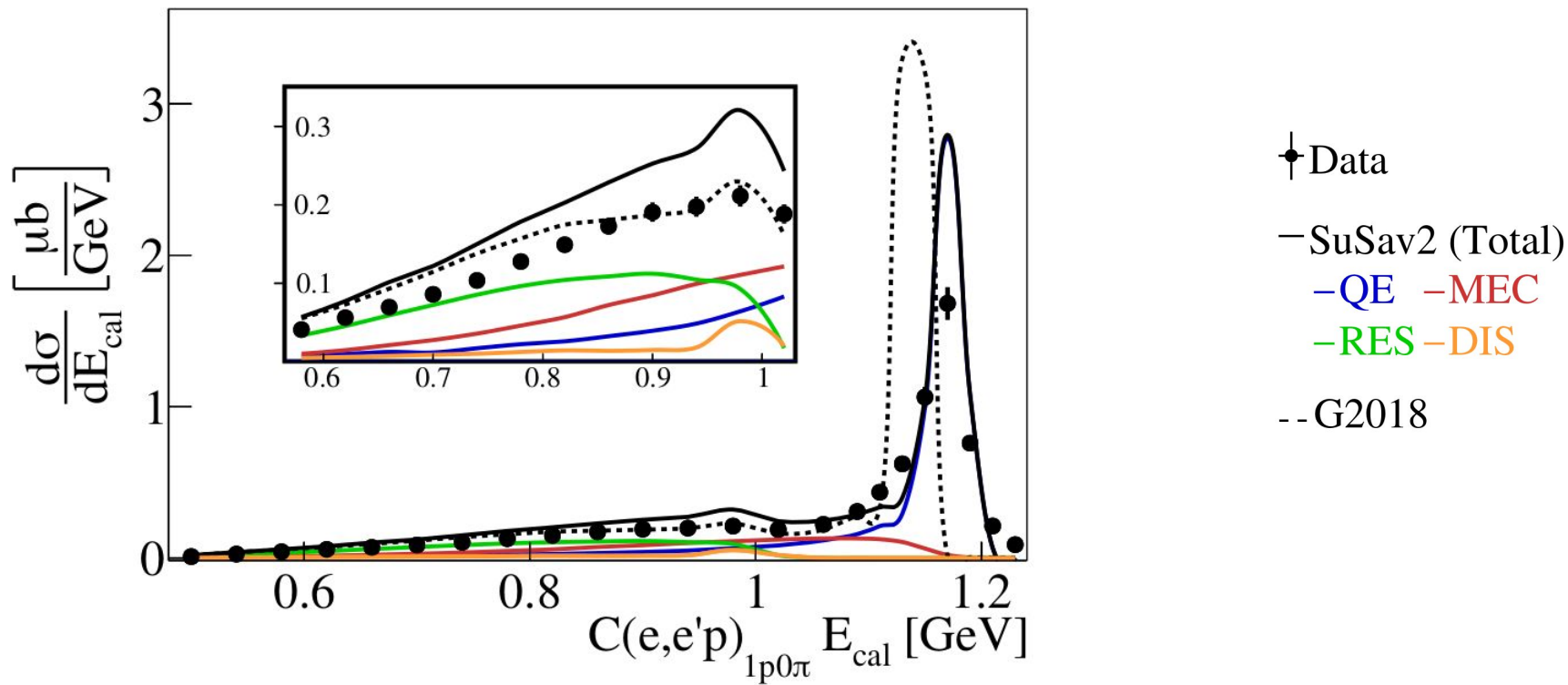


# Correction Factors



# Step #4: Absolute Cross Sections

After both acceptance & radiation corrections, without systematics yet



# Systematics

---

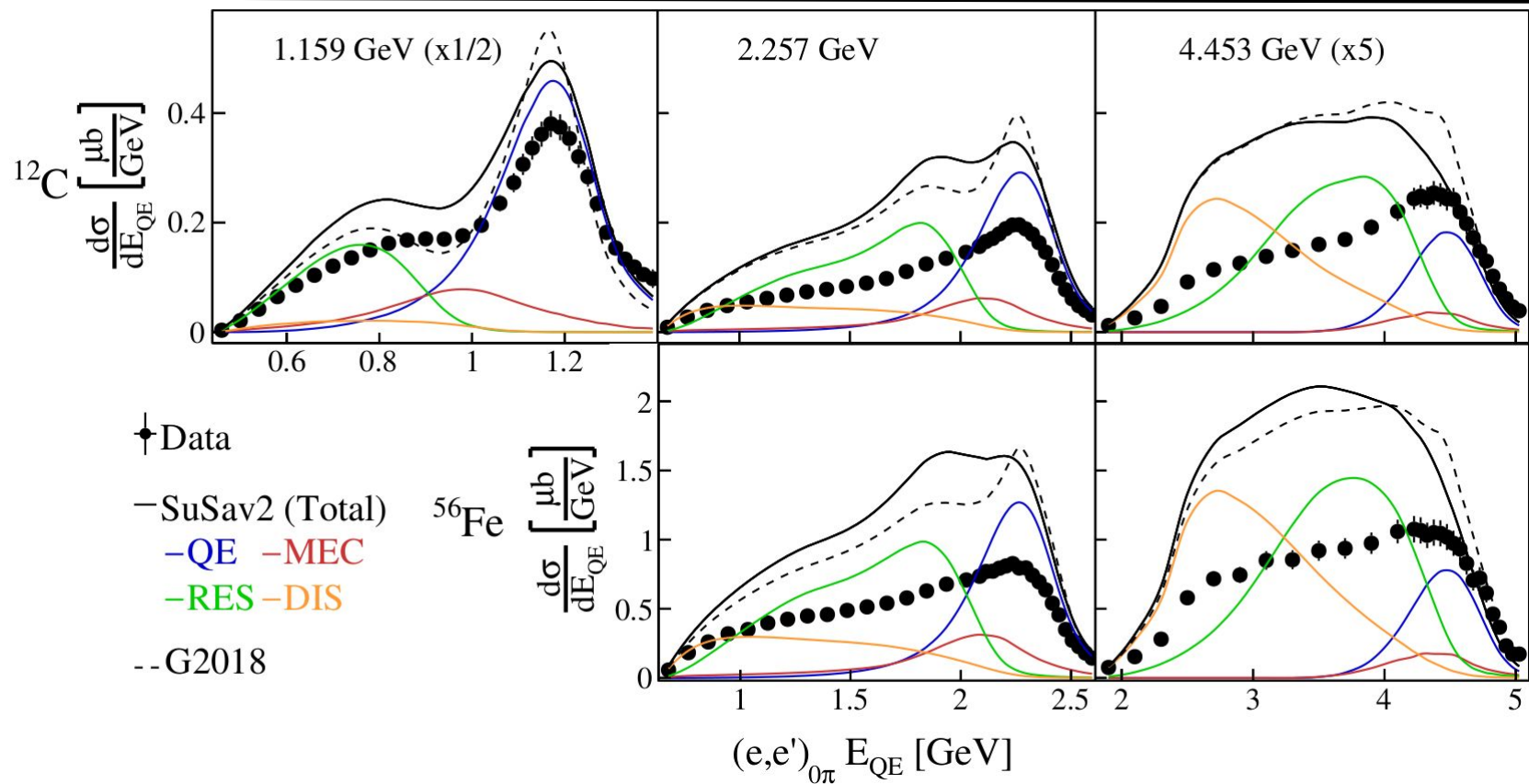
Source	Uncertainty (%)
Detector acceptance Identification cuts $\phi_{q\pi}$ cross section dependence Number of rotations	2,2.1,4.7 (@ 1.1,2.2,4.4 GeV)
Sector dependence	6
Acceptance correction	2-15
Overall normalization	3
Electron inefficiency	2

# Energy Reconstruction Accuracy

---

		1.159 GeV		2.257 GeV		4.453 GeV	
		Peak	Peak	Peak	Peak	Peak	Peak
		Fraction	Sum [ $\mu\text{b}$ ]	Fraction	Sum [ $\mu\text{b}$ ]	Fraction	Sum [ $\mu\text{b}$ ]
$^4\text{He}$	Data	-	-	41	0.48	38	0.15
	SuSAv2	-	-	45	1.31	22	0.14
	G2018	-	-	39	0.93	24	0.16
$^{12}\text{C}$	Data	39	4.13	31	1.26	32	0.34
	SuSAv2	44	5.33	27	1.76	12	0.20
	G2018	51	6.53	37	2.44	23	0.43
$^{56}\text{Fe}$	Data	-	-	20	3.73	23	1.01
	SuSAv2	-	-	21	5.28	10	0.58
	G2018	-	-	30	8.22	19	1.48

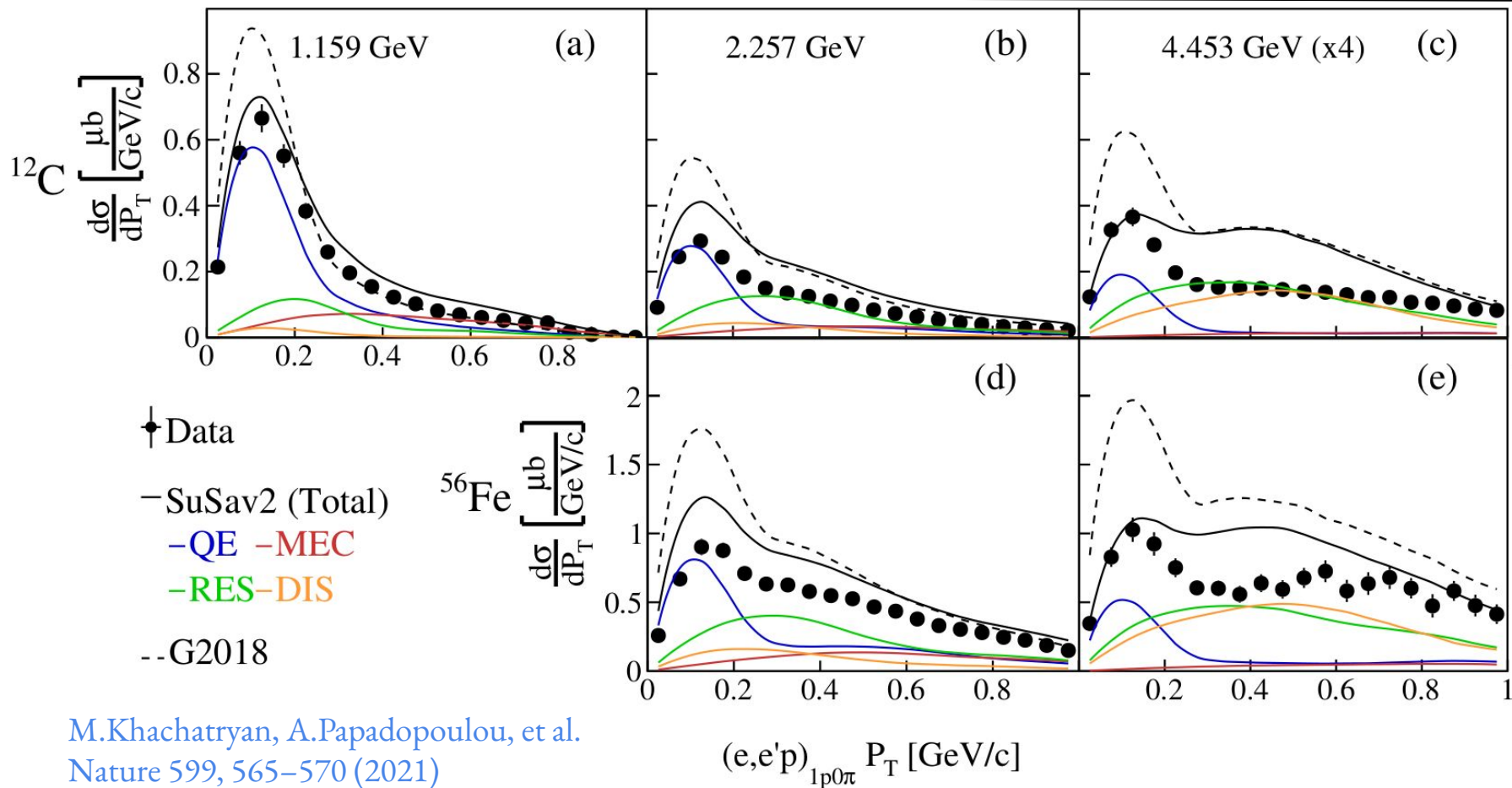
# $E_{QE}$ Nucleus & Energy Dependence



$$E_{QE} = \frac{2M\epsilon + 2ME_l - m_l^2}{2(M - E_l + |k_l|\cos\theta_l)}$$

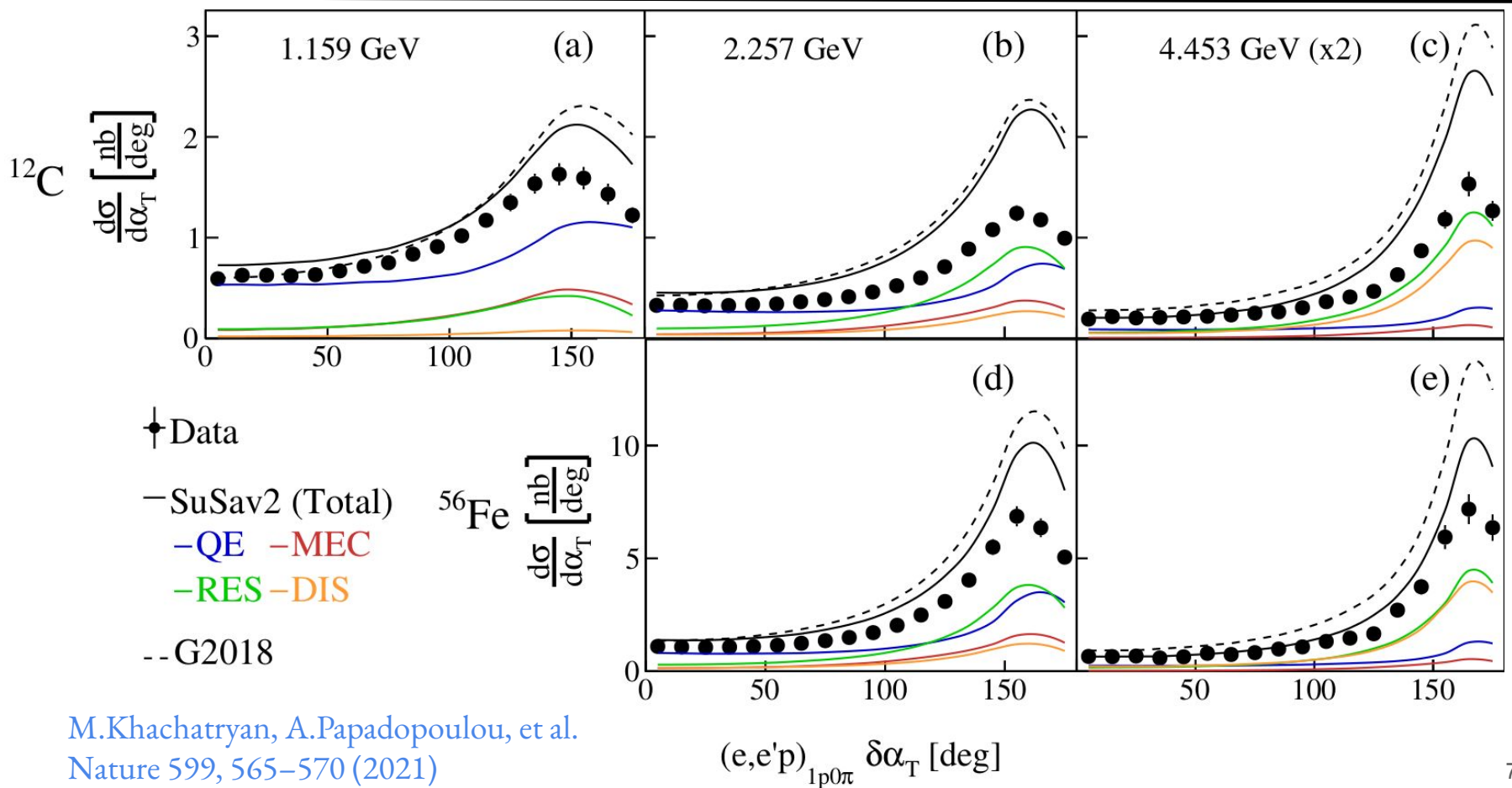


# $P_T$ Nucleus & Energy Dependence



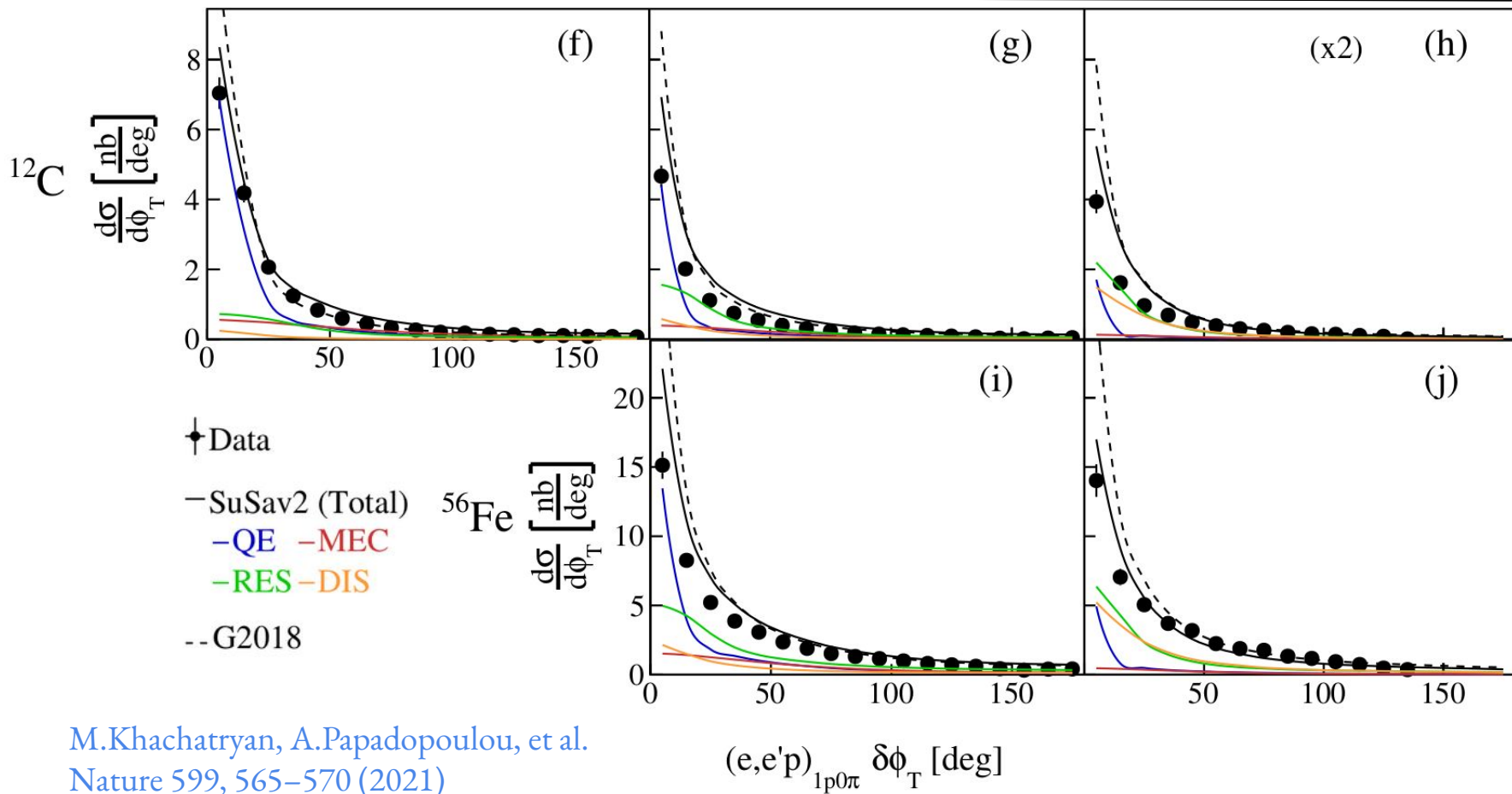
M.Khachatryan, A.Papadopoulou, et al.  
 Nature 599, 565–570 (2021)

# $\delta\alpha_T$ Nucleus & Energy Dependence



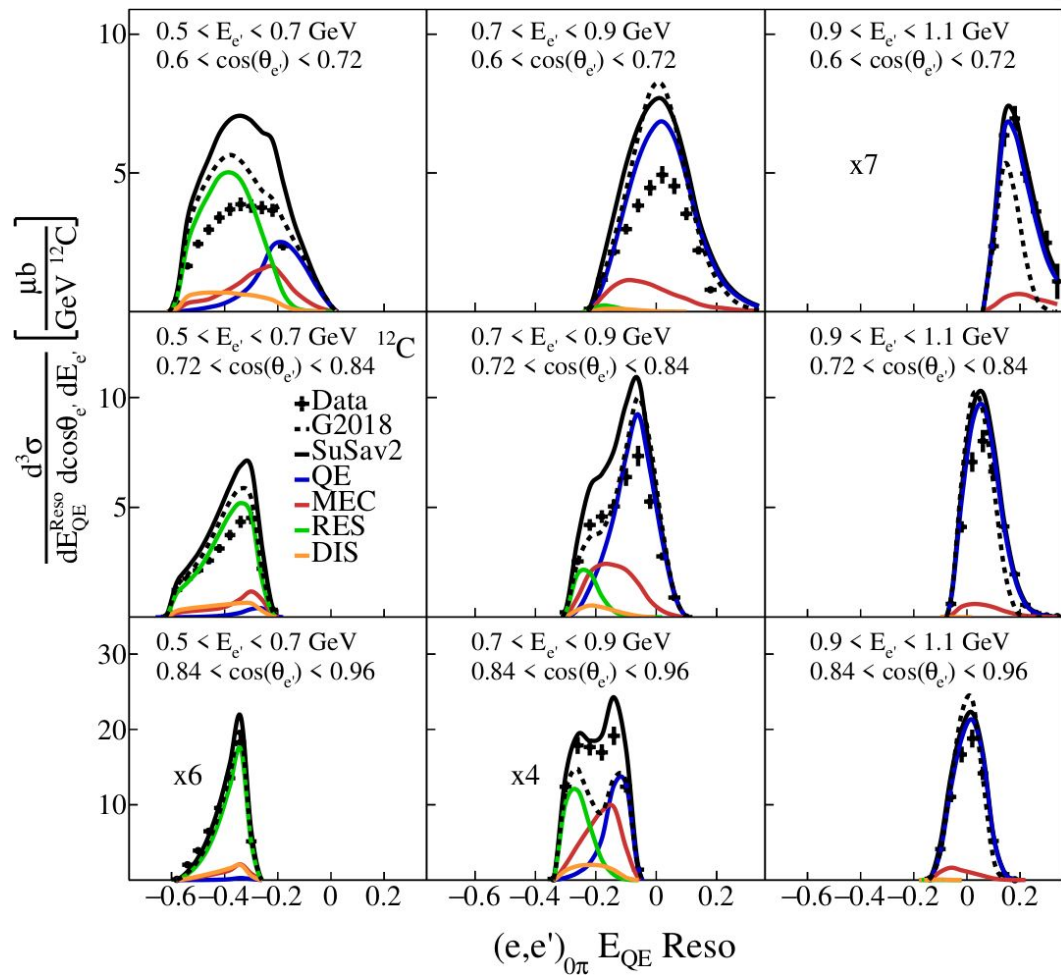
M.Khachatryan, A.Papadopoulou, et al.  
 Nature 599, 565–570 (2021)

# $\delta\phi_T$ Nucleus & Energy Dependence



M.Khachatryan, A.Papadopoulou, et al.  
 Nature 599, 565–570 (2021)

# Into The 3D $e4\nu$ Multiverse!

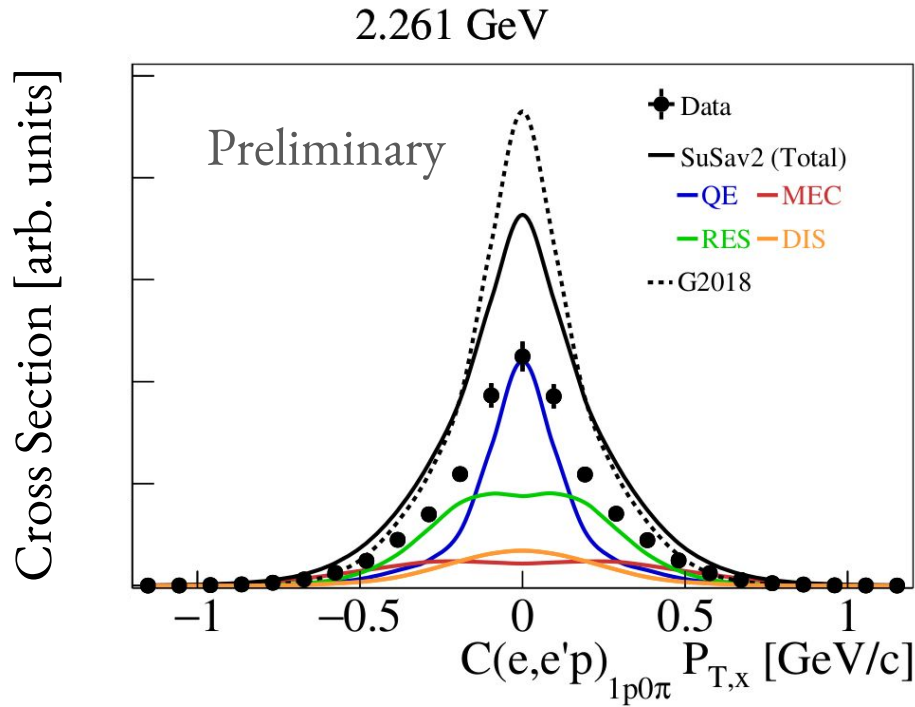


A.Papadopoulou, et al,  
In preparation

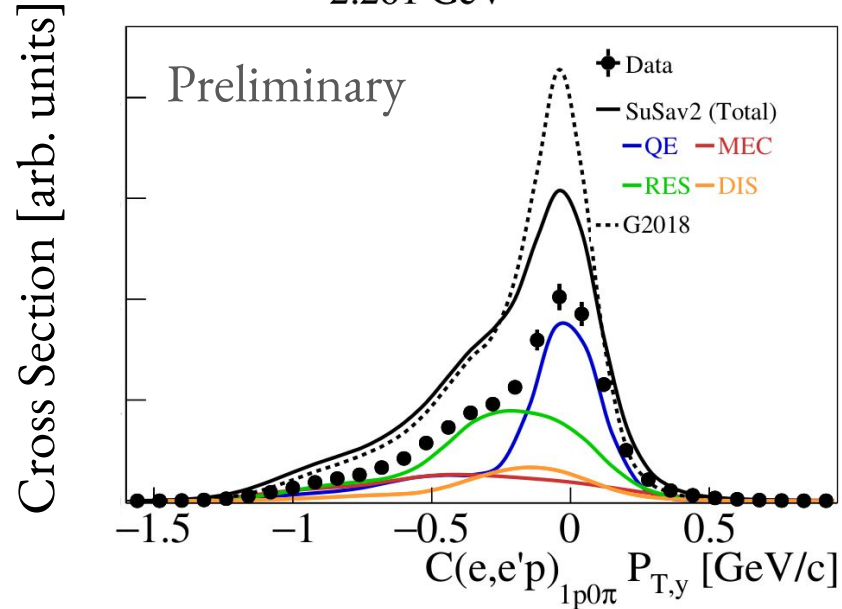
# Nuclear Sensitivity Variables

$$\delta p_{T_x} = (\hat{p}_v \times \hat{p}_T^l) \cdot \delta \vec{p}_T = |\delta \vec{p}_T| \sin(\delta \alpha_T)$$

Sensitivity to Fermi motion



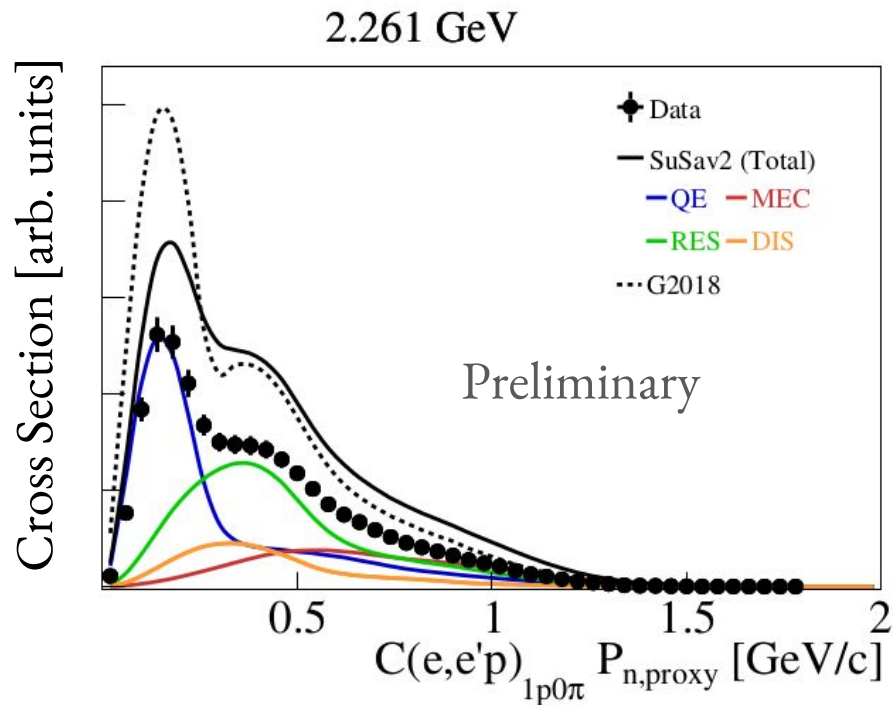
2.261 GeV



$$\delta p_{T_y} = -\hat{p}_T^l \cdot \delta \vec{p}_T = |\delta \vec{p}_T| \cos(\delta \alpha_T)$$

Sensitivity to final state interactions

# Missing Momentum Approximation



$$P_{n,proxy} = \sqrt{\delta p_L^2 + \delta p_T^2}$$

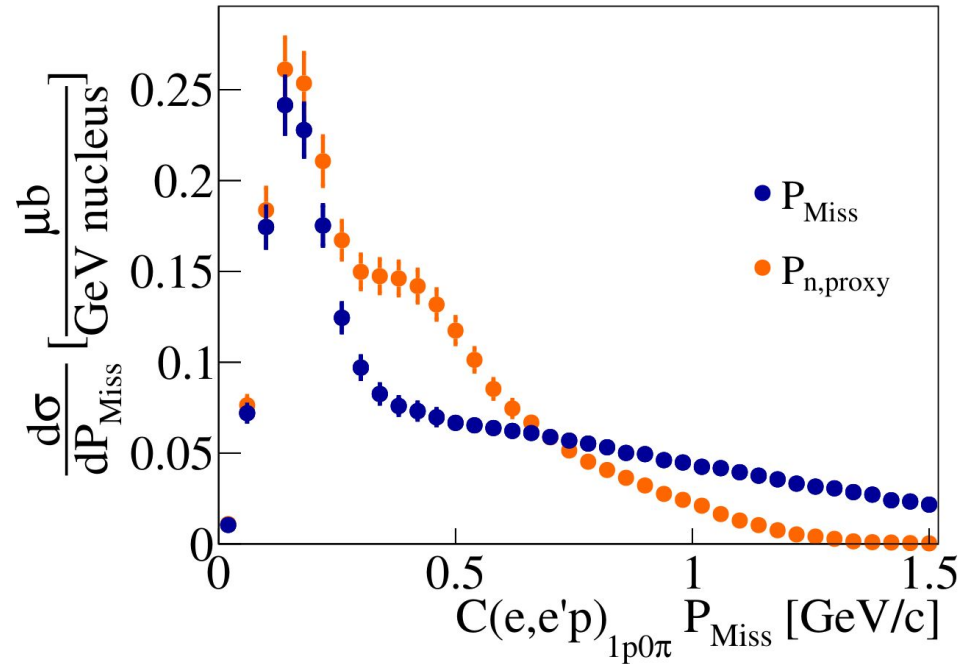
Under QE assumption

[Phys. Rev. Lett. 121, 022504 \(2018\)](#)

[A.Papadopoulou, et al, In preparation](#)

# Fails To Reproduce True Missing Momentum

2.261 GeV



A.Papadopoulou, et al, In preparation

$$P_{\text{n,proxy}} = \sqrt{\delta p_{\text{L}}^2 + \delta p_{\text{T}}^2}$$

Under QE assumption

[Phys. Rev. Lett. 121, 022504 \(2018\)](#)

True missing momentum

$$P_{\text{miss}} = |p - q|$$

$p$  = proton 3-vector

$q$  = momentum transfer

# The $e4\nu$ Result Factory Continued!

- More inclusive results
- More complex channels
- Nuclear sensitivity variables
- Multi-differential results

$e4\nu$  Collaboration, In preparation

