

Determination of the argon spectral function from $(e,e'p)$ data

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for the E12-14-012 experiment

based on L. Jiang *et al.*, arXiv:2203.01748

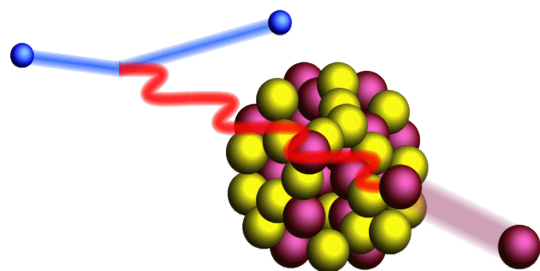
NuSTEC Workshop on Electron Scattering, March 29–31, 2022

E12-14-012 in JLab: (e,e') and $(e,e'p)$ on Ar and Ti

Aim: Obtaining the experimental input indispensable to construct the argon spectral function, thus paving the way for a reliable estimate of the neutrino cross sections in DUNE. In addition, stimulating a number of theoretical developments, such as the description of final-state interactions.

[Benhar *et al.*, arXiv:1406.4080]

$$E_e = 2.222 \text{ GeV}$$

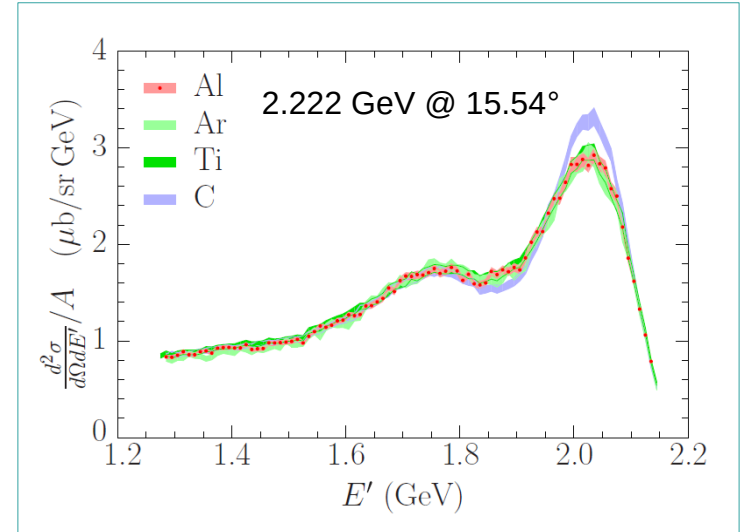


	E'_e (GeV)	θ_e (deg)	$ \mathbf{p}' $ (MeV)	$\theta_{p'}$ (deg)	$ \mathbf{q} $ (MeV)	p_m (MeV)	E_m (MeV)
kin1	1.777	21.5	915	-50.0	865	50	73
kin2	1.716	20.0	1030	-44.0	846	184	50
kin3	1.799	17.5	915	-47.0	741	174	50
kin4	1.799	15.5	915	-44.5	685	230	50
kin5	1.716	15.5	1030	-39.0	730	300	50

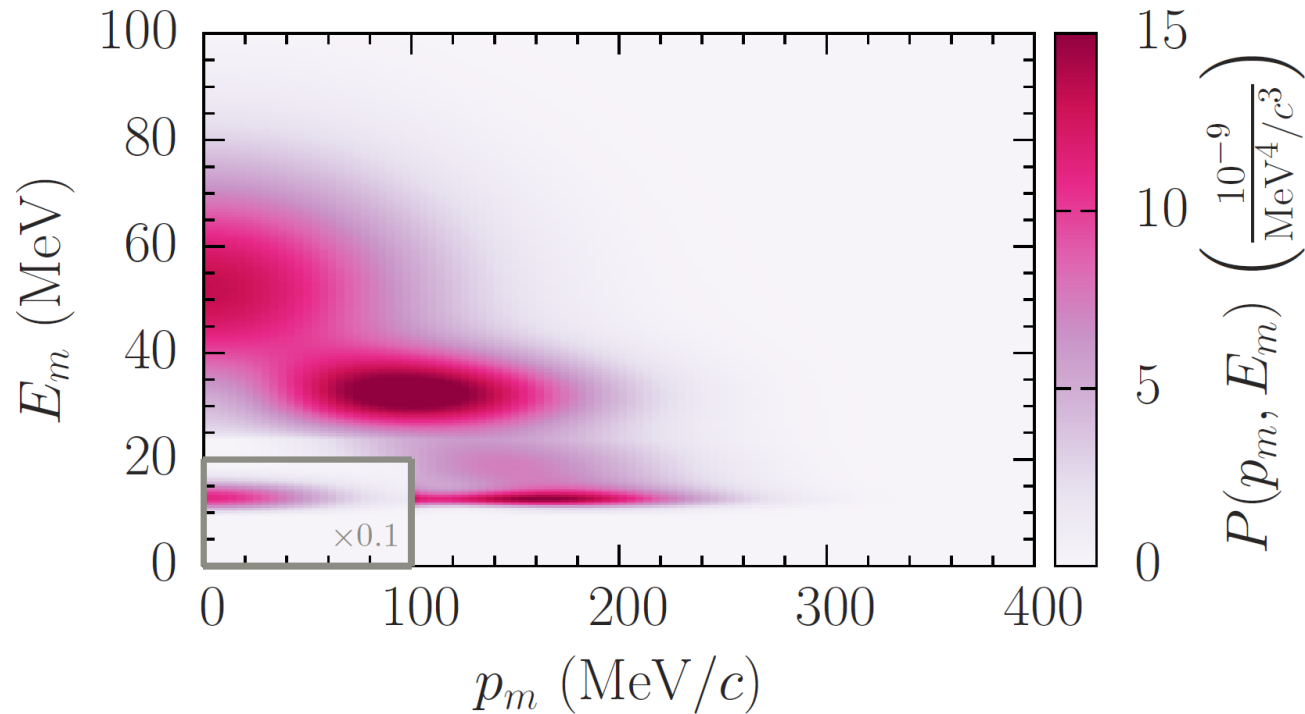
First, exploratory analysis of the full dataset

Previous results

- Inclusive cross sections for C and Ti [Dai *et al.*, PRC 98, 014617 (2018)]
- Inclusive cross section for Ar [Dai *et al.*, PRC 99, 054608 (2019)]
- Inclusive cross section for Al-7075, A -, y -, ψ -scaling of all (e, e') data [Murphy *et al.*, PRC 100, 054606 (2019)]
- Exclusive Ar & Ti cross sections for a single kinematics, $p_m \sim 50\text{--}60$ MeV, $E_m \sim 50\text{--}70$ MeV [Gu *et al.*, PRC 103, 034604 (2021)]

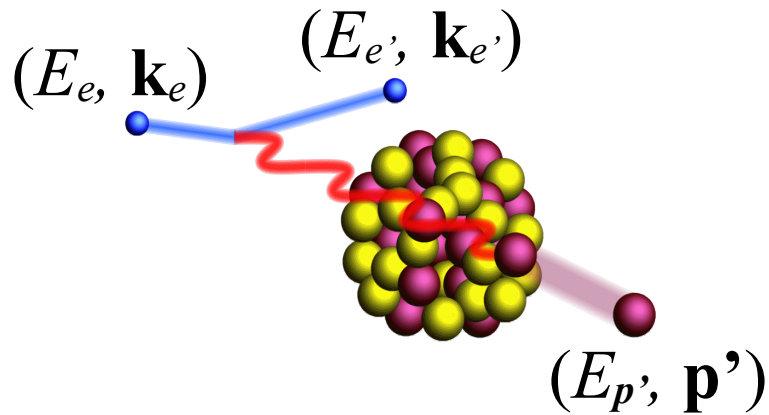


This analysis: extraction of the spectral function



Universal property of the nucleus, independent of the interaction.

Missing momentum \mathbf{p}_m and missing energy E_m



Without final-state interactions,

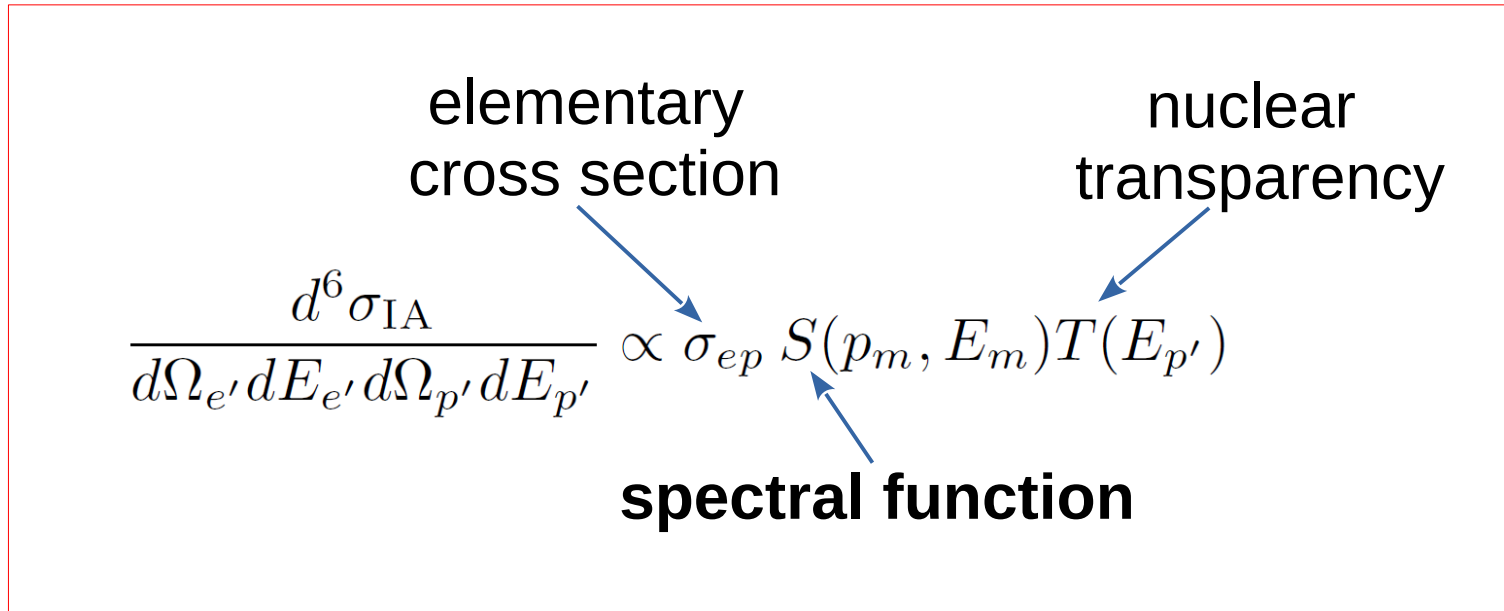
$$E_e + M - \underline{E_m} = E_{e'} + E_p$$

known

$$\mathbf{k}_e + \underline{\mathbf{p}_m} = \mathbf{k}_{e'} + \mathbf{p}'$$

$E_m - E_{\text{thr}}$ is the excitation energy of ^{39}Cl
 $p_m \equiv |\mathbf{p}_m|$ is the initial proton momentum

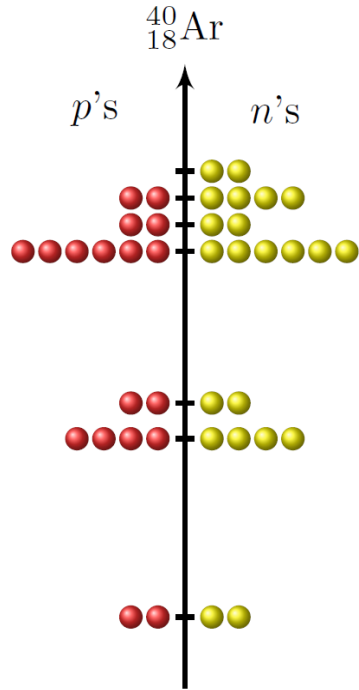
(e,e'p) cross section



Analysis procedure

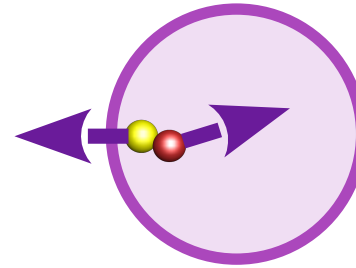
- 1) Extract of the $(e,e'p)$ cross section
- 2) Using σ_{cc1} of de Forest and nuclear transparency, obtain the reduced cross sections as a function of (a) p_m and (b) E_m .
- 3) Find the parameters of the spectral function (*i.e.*, spectroscopic factors) from the fits to the reduced cross sections as a function of p_m .
- 4) Using the priors from Step 3), find the parameters of the spectral function (*i.e.*, spectroscopic factors, peak positions, distribution widths) from the fits to the reduced cross sections as a function of E_m .

Test spectral function: 80% mean-field + 20% *NN* correlations



Independent-particle shell model

+



Convolution model
of the correlated spectral function

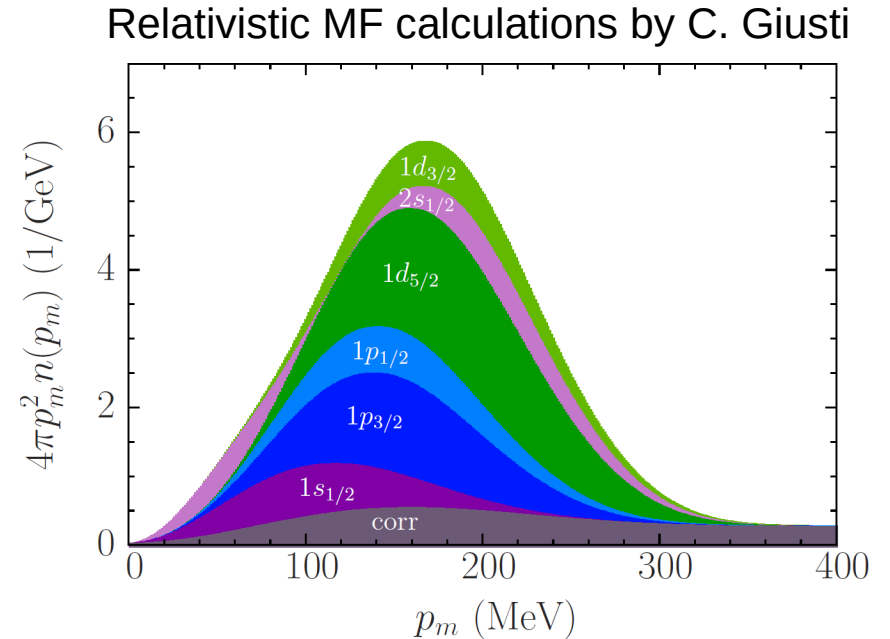
Mean-field part of the spectral function

spectroscopic factor

energy distribution

$$P_{\text{MF}}(p_m, E_m) = \sum_{\alpha} S_{\alpha} |\phi_{\alpha}(p_m)|^2 f_{\alpha}(E_m)$$

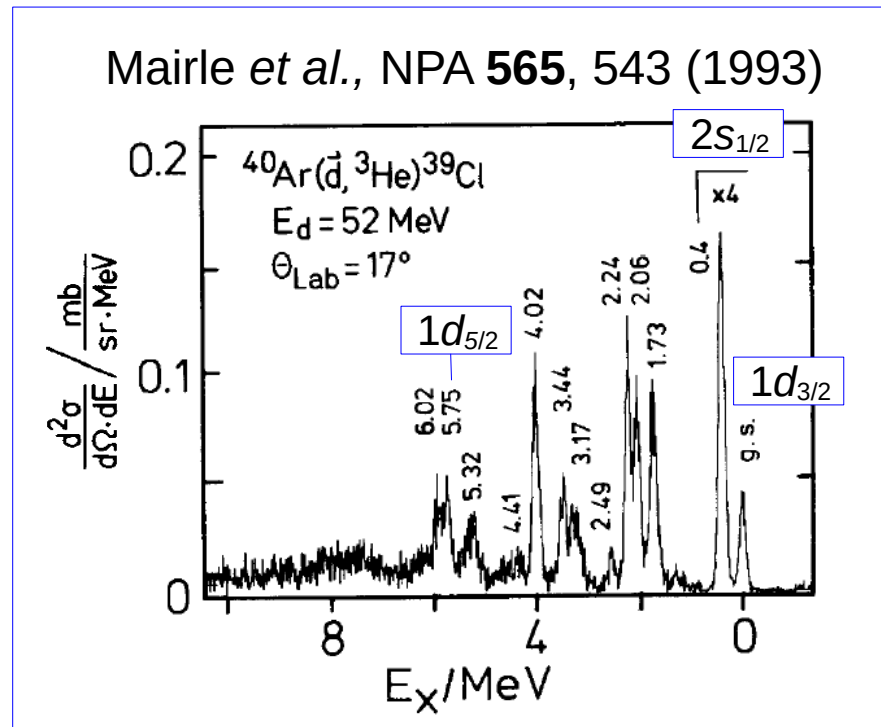
wave function in momentum space



Mean-field part of the spectral function

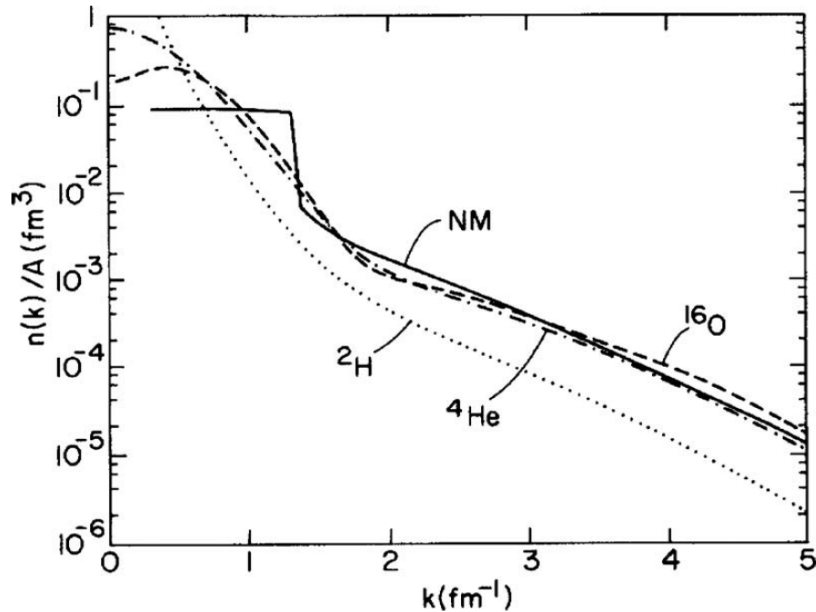
α	S_α	E_α (MeV)
$1d_{3/2}$	1.6	12.53
$2s_{1/2}$	1.6	12.93
$1d_{5/2}$	4.8	18.23
$1p_{1/2}$	1.6	28.0
$1p_{3/2}$	3.2	33.0
$1s_{1/2}$	1.6	52.0

- $1d_{3/2}$: from the mass difference between ^{40}Ar and $^{39}\text{Cl} + p + e$
- $2s_{1/2}$ and $1d_{5/2}$: from the dominant contribs. in the past $^{40}\text{Ar}(d, ^3\text{He})^{39}\text{Cl}$ measurements
- Lower levels were not probed with deuteron
- Assumed Gaussian distribution



Correlated part of the spectral function

Benhar *et al.*, RMP **80**, 189 (2008)



Ciofi degli Atti and Simula, PRC **53**, 1689 (1996)

- Correlated nucleons form quasi-deuteron pairs, with the relative momentum distributed as in deuteron.
- NN pairs undergo CM motion (Gaussian distrib.)
- Excitation energy of the $(A - 1)$ -nucleons is their kinetic energy plus the pn knockout threshold

p_m fit results

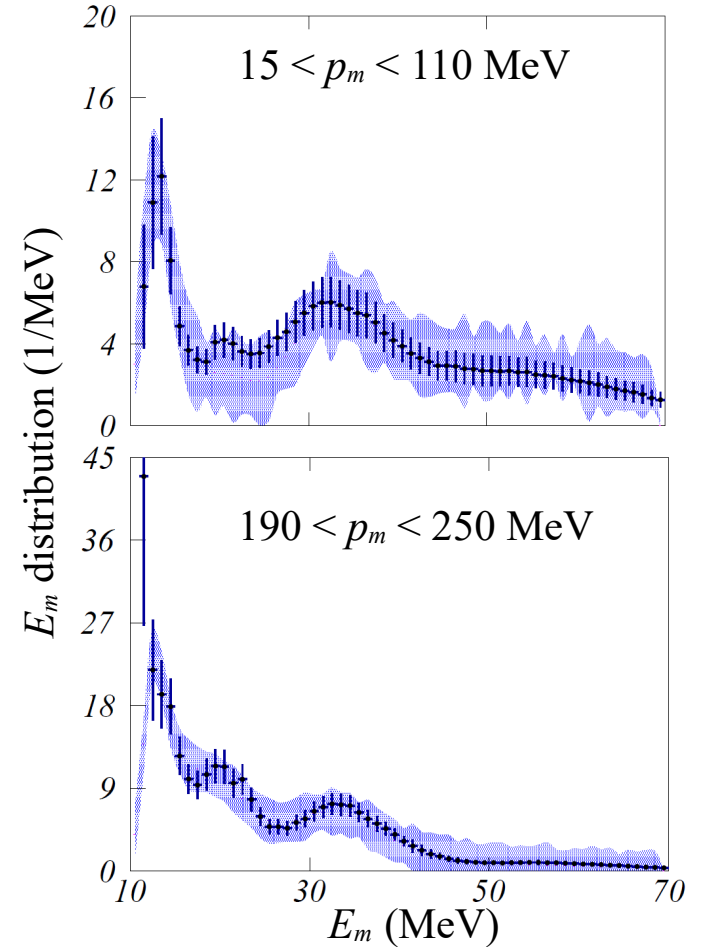
α	N_α	w/ corr.	S_α	w/o corr.
$1d_{3/2}$	2	0.78 ± 0.05		0.78 ± 0.09
$2s_{1/2}$	2	2.07 ± 0.07		2.10 ± 0.10
$1d_{5/2}$	6	2.27 ± 0.04		2.27 ± 0.08
$1p_{1/2}$	2	2.72 ± 1.23		2.72 ± 0.34
$1p_{3/2}$	4	3.36 ± 0.04		3.53 ± 0.06
$1s_{1/2}$	2	2.54 ± 0.04		2.65 ± 0.02
corr.	0	0.48 ± 0.01		excluded
$\sum_\alpha S_\alpha$		14.48 ± 1.24		14.05 ± 0.38
d.o.f.		1,132		1,133
$\chi^2/\text{d.o.f.}$		1.9		3.2

In the p_m fit, only deeply bound states are sensitive to the correlated spectral function.

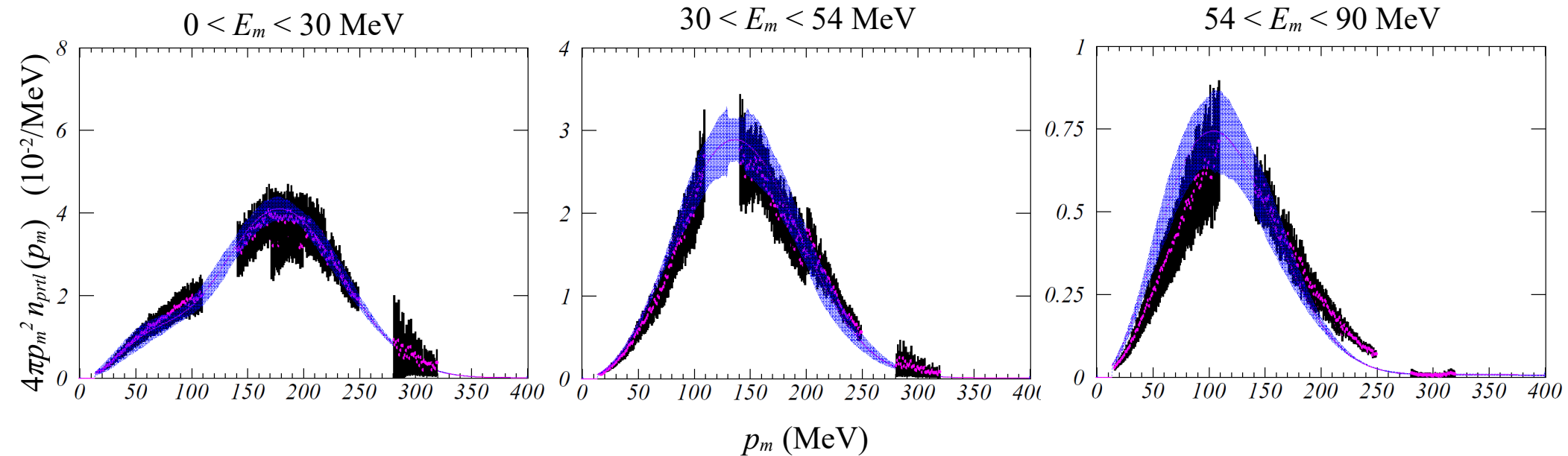
E_m fit results

α	N_α	all priors	w/o p_m	w/o corr.
			S_α	
$1d_{3/2}$	2	0.89 ± 0.11	1.42 ± 0.20	0.95 ± 0.11
$2s_{1/2}$	2	1.72 ± 0.15	1.22 ± 0.12	1.80 ± 0.16
$1d_{5/2}$	6	3.52 ± 0.26	3.83 ± 0.30	3.89 ± 0.30
$1p_{1/2}$	2	1.53 ± 0.21	2.01 ± 0.22	1.83 ± 0.21
$1p_{3/2}$	4	3.07 ± 0.05	2.23 ± 0.12	3.12 ± 0.05
$1s_{1/2}$	2	2.51 ± 0.05	2.05 ± 0.23	2.52 ± 0.05
corr.	0	3.77 ± 0.28	3.85 ± 0.25	excluded
$\sum_\alpha S_\alpha$		17.02 ± 0.48	16.61 ± 0.57	14.12 ± 0.42
d.o.f		206	231	232
$\chi^2/\text{d.o.f.}$		1.9	1.4	2.0

α	E_α (MeV)		σ_α (MeV)	
	w/ priors	w/o priors	w/ priors	w/o priors
$1d_{3/2}$	12.53 ± 0.02	10.90 ± 0.12	1.9 ± 0.4	1.6 ± 0.4
$2s_{1/2}$	12.92 ± 0.02	12.57 ± 0.38	3.8 ± 0.8	3.0 ± 1.8
$1d_{5/2}$	18.23 ± 0.02	17.77 ± 0.80	9.2 ± 0.9	9.6 ± 1.3
$1p_{1/2}$	28.8 ± 0.7	28.7 ± 0.7	12.1 ± 1.0	12.0 ± 3.6
$1p_{3/2}$	33.0 ± 0.3	33.0 ± 0.3	9.3 ± 0.5	9.3 ± 0.5
$1s_{1/2}$	53.4 ± 1.1	53.4 ± 1.0	28.3 ± 2.2	28.1 ± 2.3
corr.	24.1 ± 2.7	24.1 ± 1.7	—	—

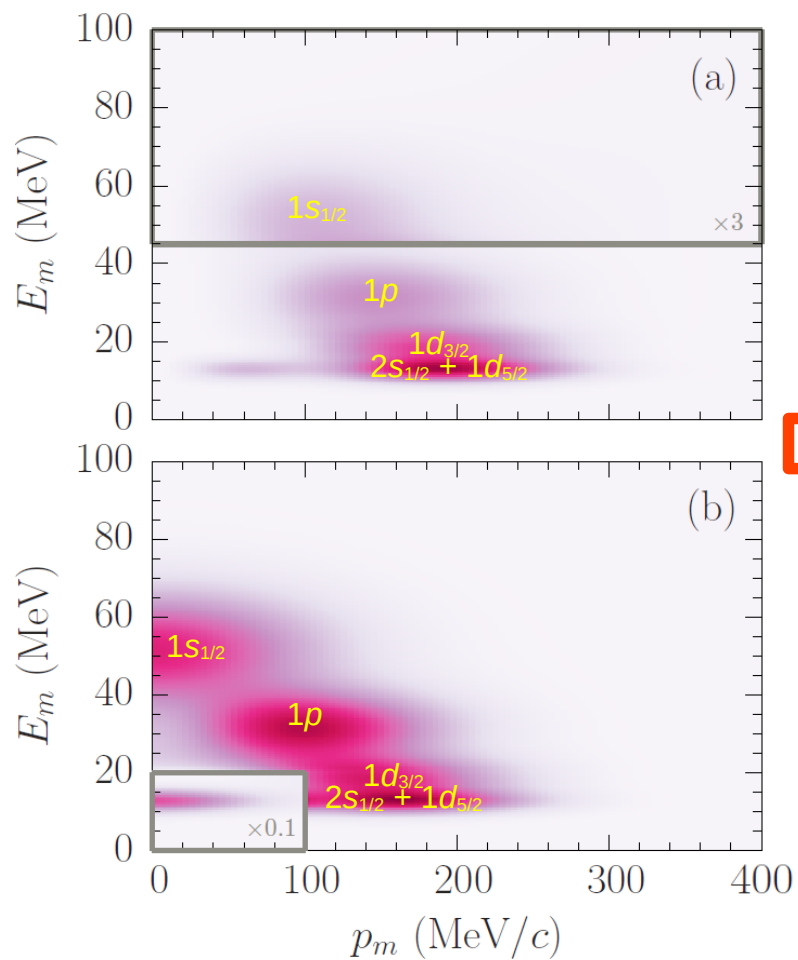


E_m fit results

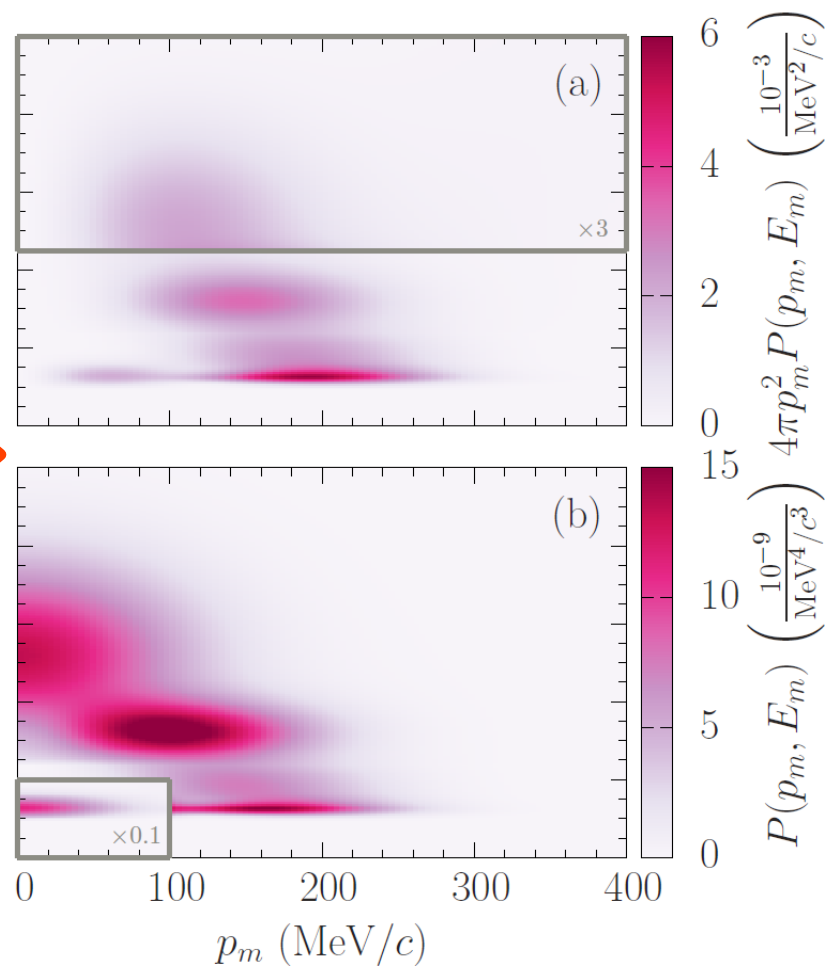


Data from different kinematics are consistent within uncertainties.

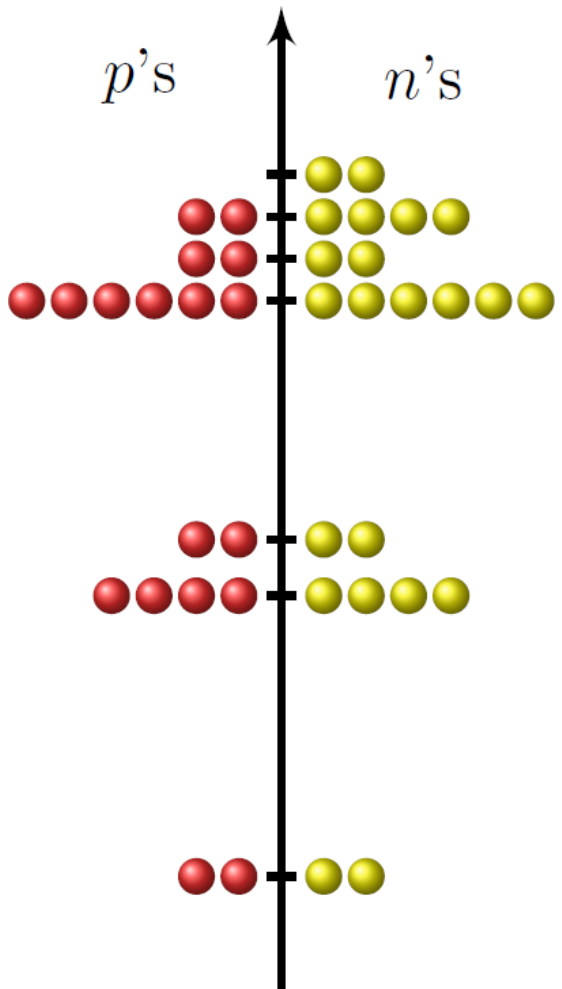
Test spectral function



Extracted spectral function



$^{40}_{18}\text{Ar}$



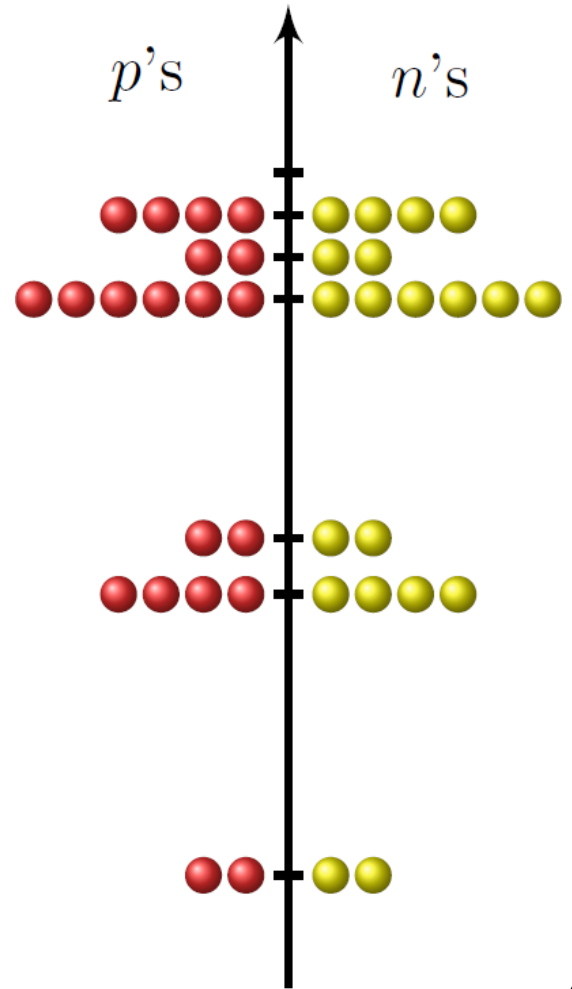
proton energy levels

Ar		Ca
12.53	1d3/2	8.5
12.92	2s1/2	11.0
18.23	1d5/2	15.7
28.8	1p1/2	29.8
33.0	1p3/2	34.7
53.3	1s1/2	53.6

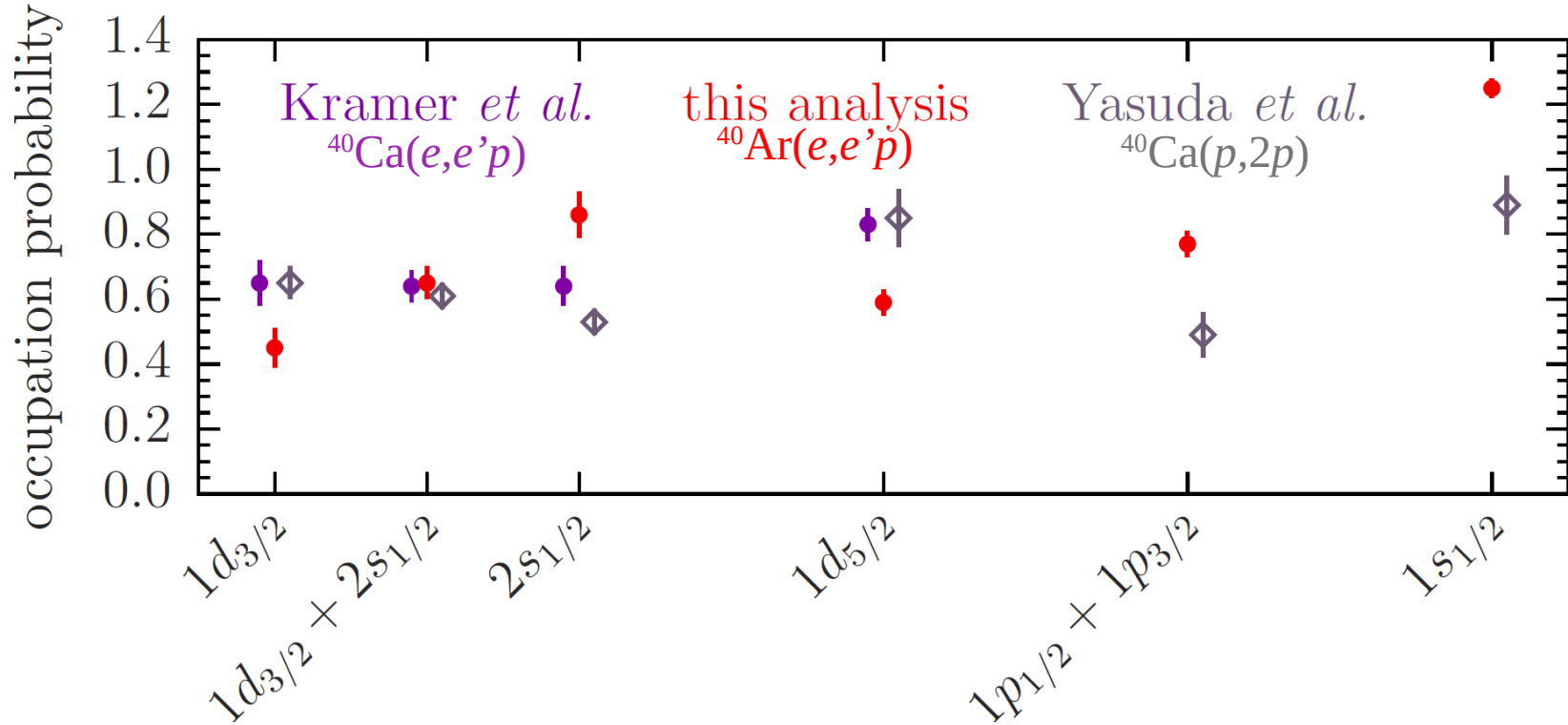
This analysis

Volkov *et al.*
SJNP 52, 848 (1990)

$^{40}_{20}\text{Ca}$



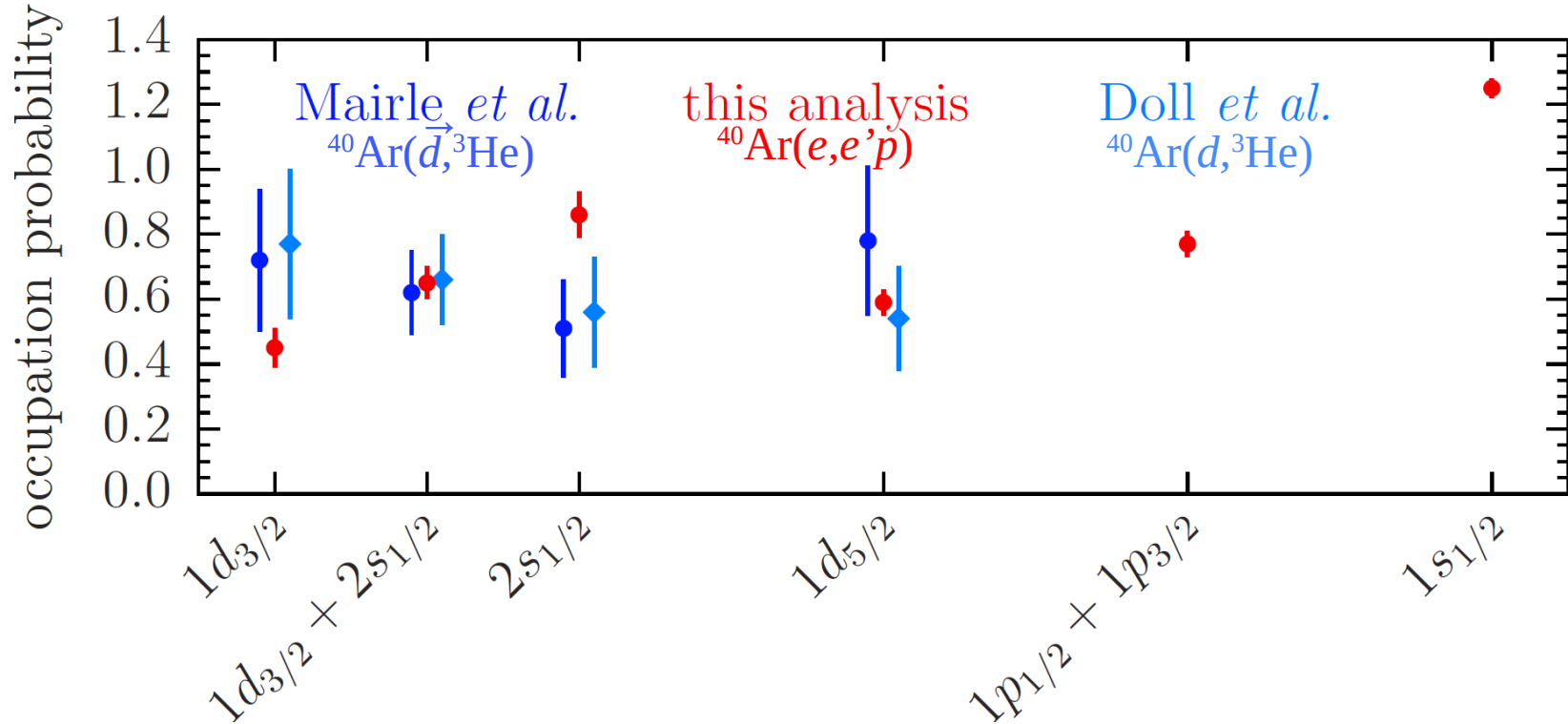
Occupation probability



Kramer *et al.* [Ph.D. thesis (1990)]: ~340–440-MeV electron beam at NIKHEF-K

Yasuda *et al.* [Ph.D. thesis (2012)]: 392-MeV polarized proton beam at RCNP

Occupation probability



52-MeV **polarized** [Mairle *et al.*, NPA **565**, 543 (1993); $E_x < 9$ MeV] and **unpolarized** [Doll *et al.*, NPA **230**, 329 (1974); **129**, 469 (1969); $E_x < 7$ MeV] deuteron beam at Karlsruhe

Kramer *et al.* [NPA **679**, 267 (2001)]: reanalysis of $(d, ^3\text{He})$ experiments, $S_\alpha \rightarrow S_\alpha/1.5$

Summary

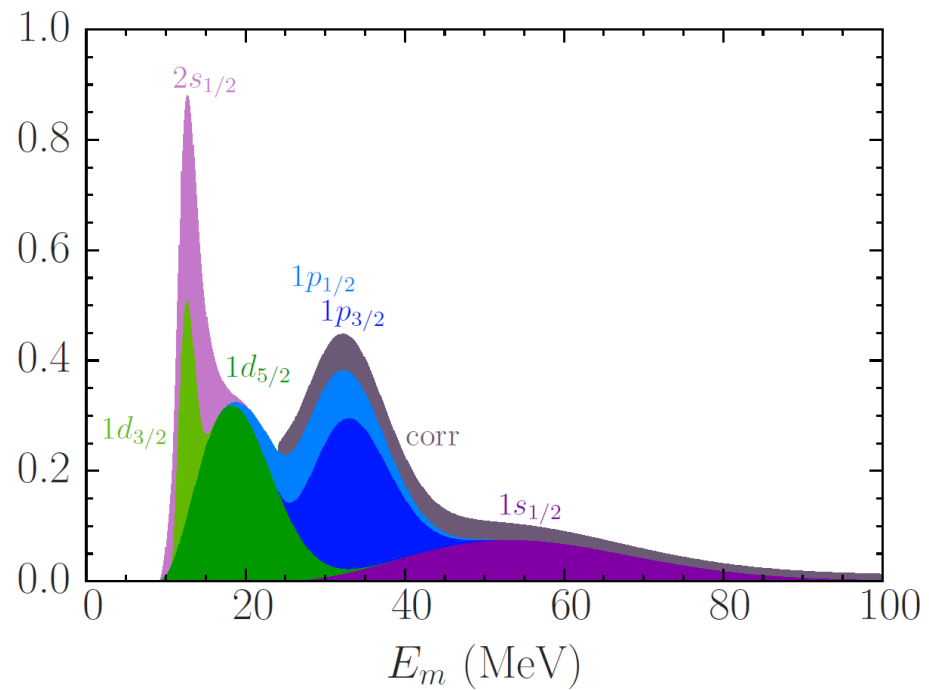
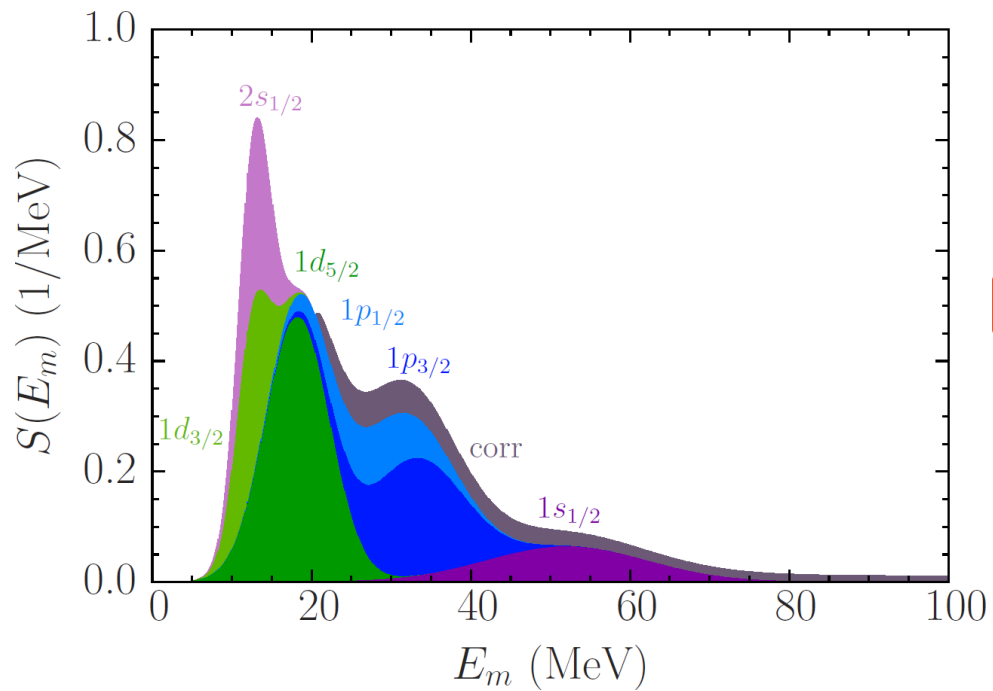
- The first, exploratory analysis of the full dataset.
- Reasonable parametrization of the spectral function of ^{40}Ar is found.
- Comparison with past results shows strengths and limitations.
- Separation of individual contributions requires improved analysis. Numerous theoretical developments are necessary.



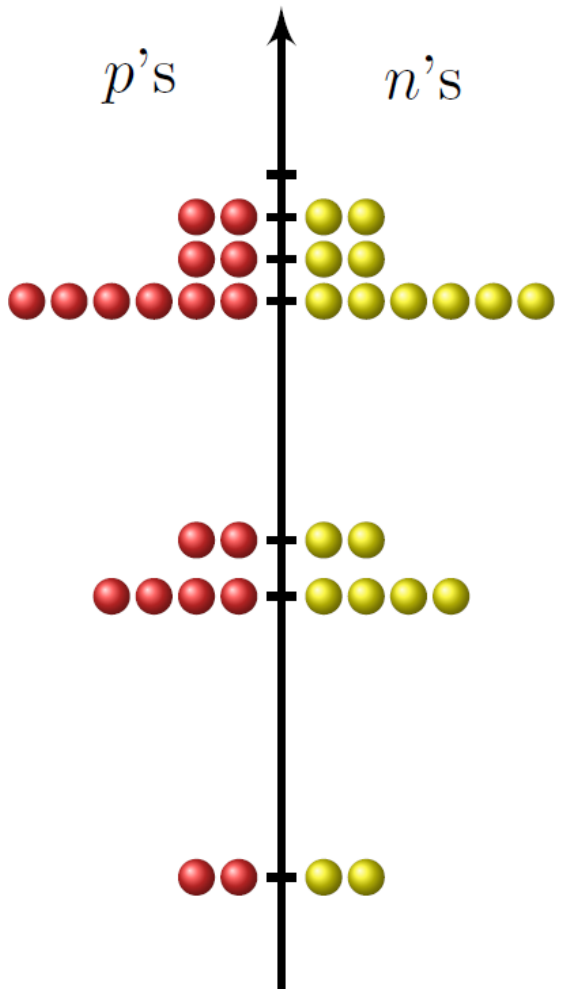
Backup

Directions for future improvements

- 2D analysis
- Final-state interactions
- Wave functions
- Correlated part of the spectral function



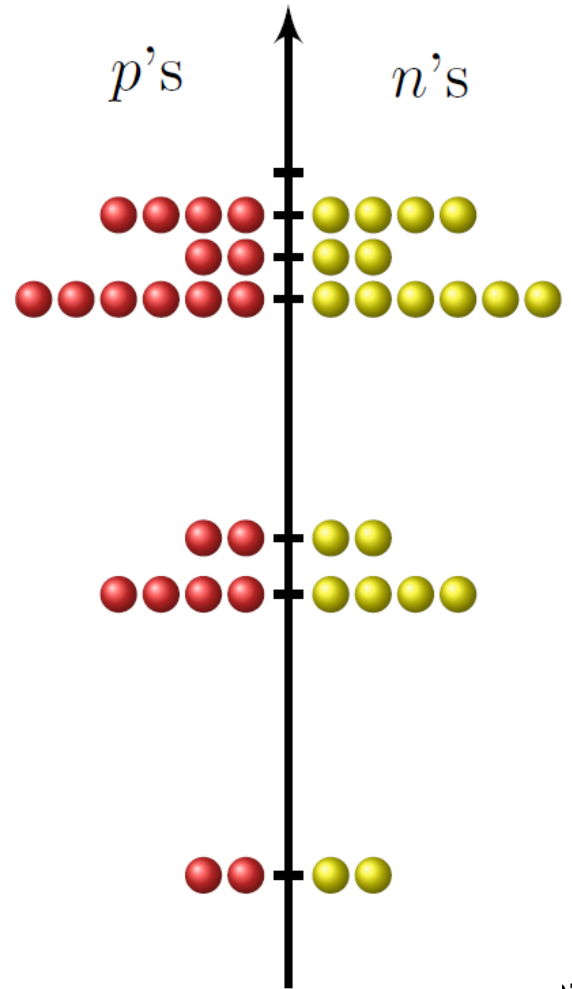
$^{36}_{18}\text{Ar}$



proton energy levels

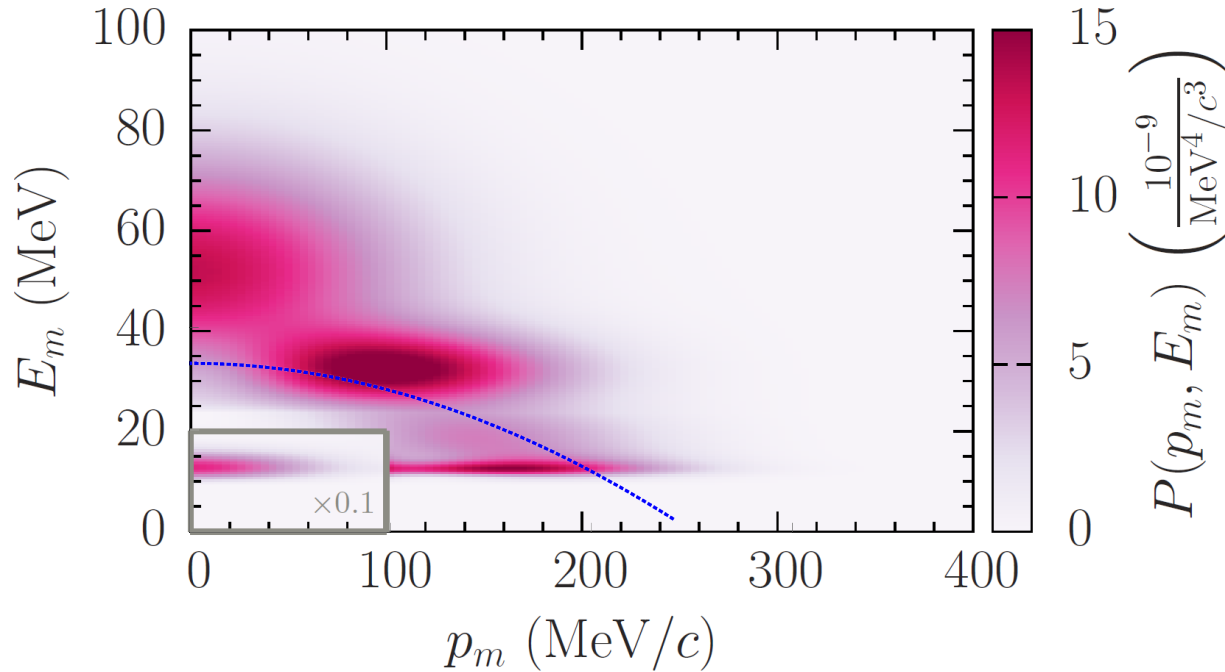
Ar		Ca
8.51	1d3/2	8.33
9.73	2s1/2	10.85
	1d5/2	
	1p1/2	
	1p3/2	
	1s1/2	

$^{40}_{20}\text{Ca}$



Realistic description of the nucleus

Fermi gas vs. spectral function



see e.g. L. Gu et al., PRC 103, 034604 (2021)

Realistic description of the nucleus

