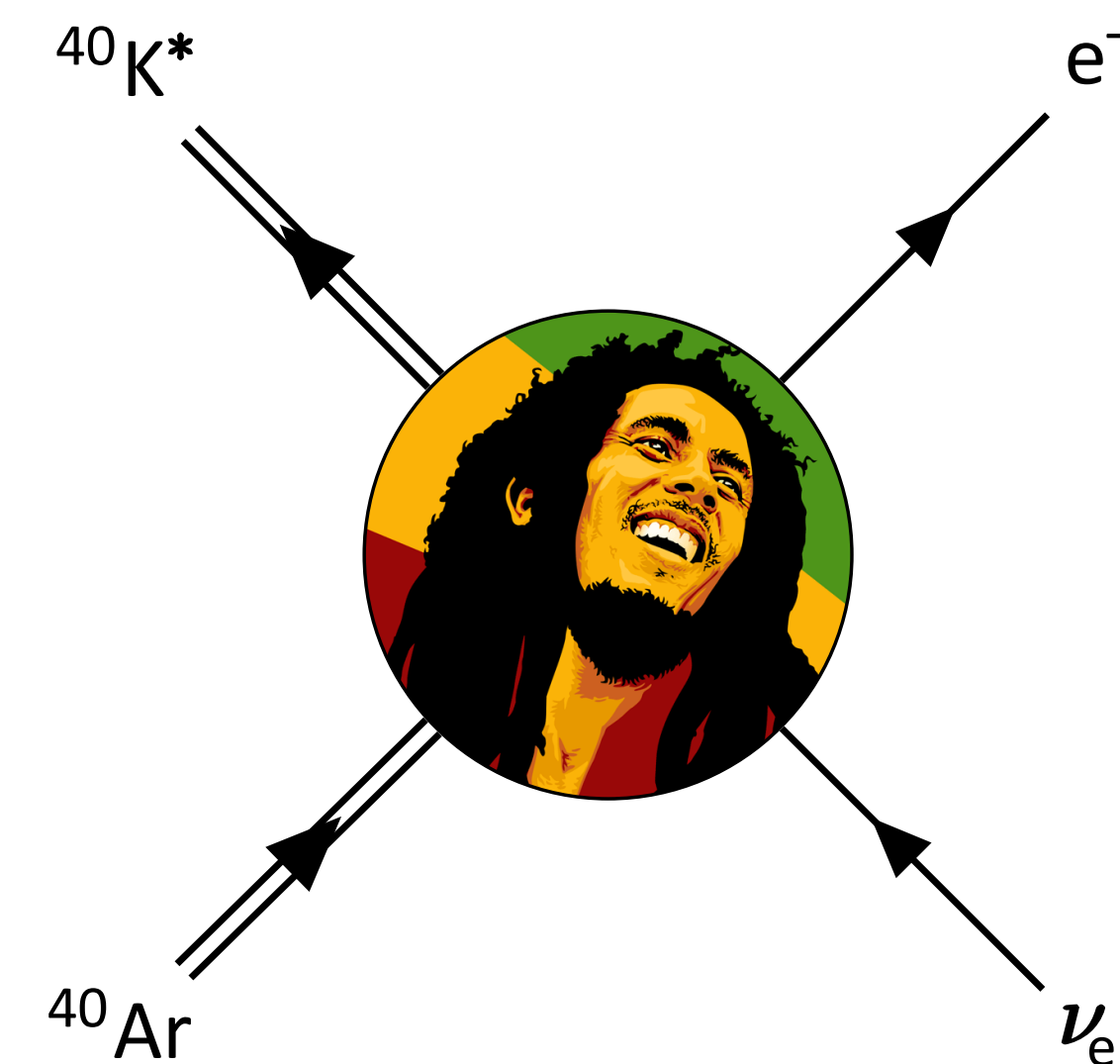
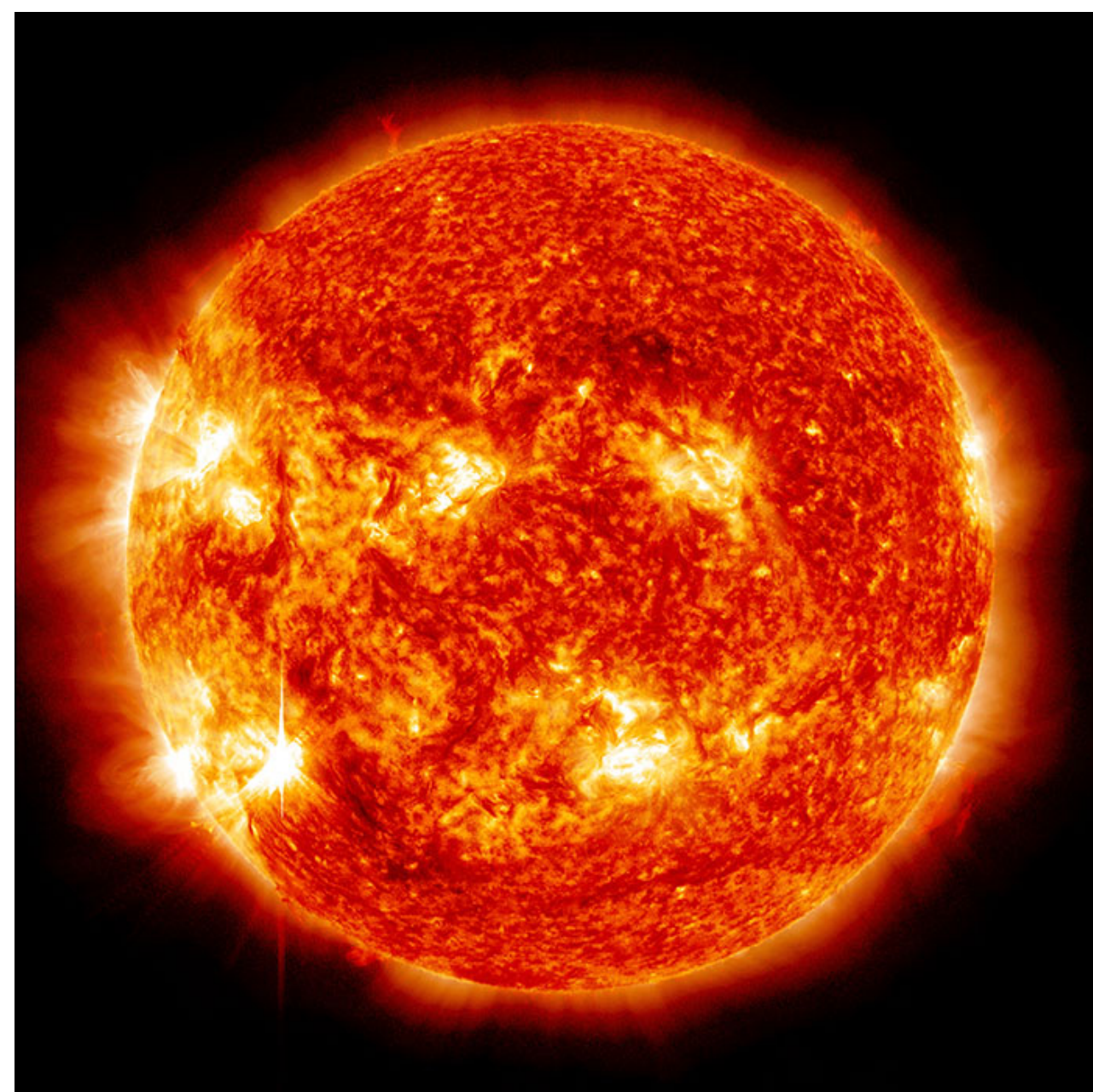
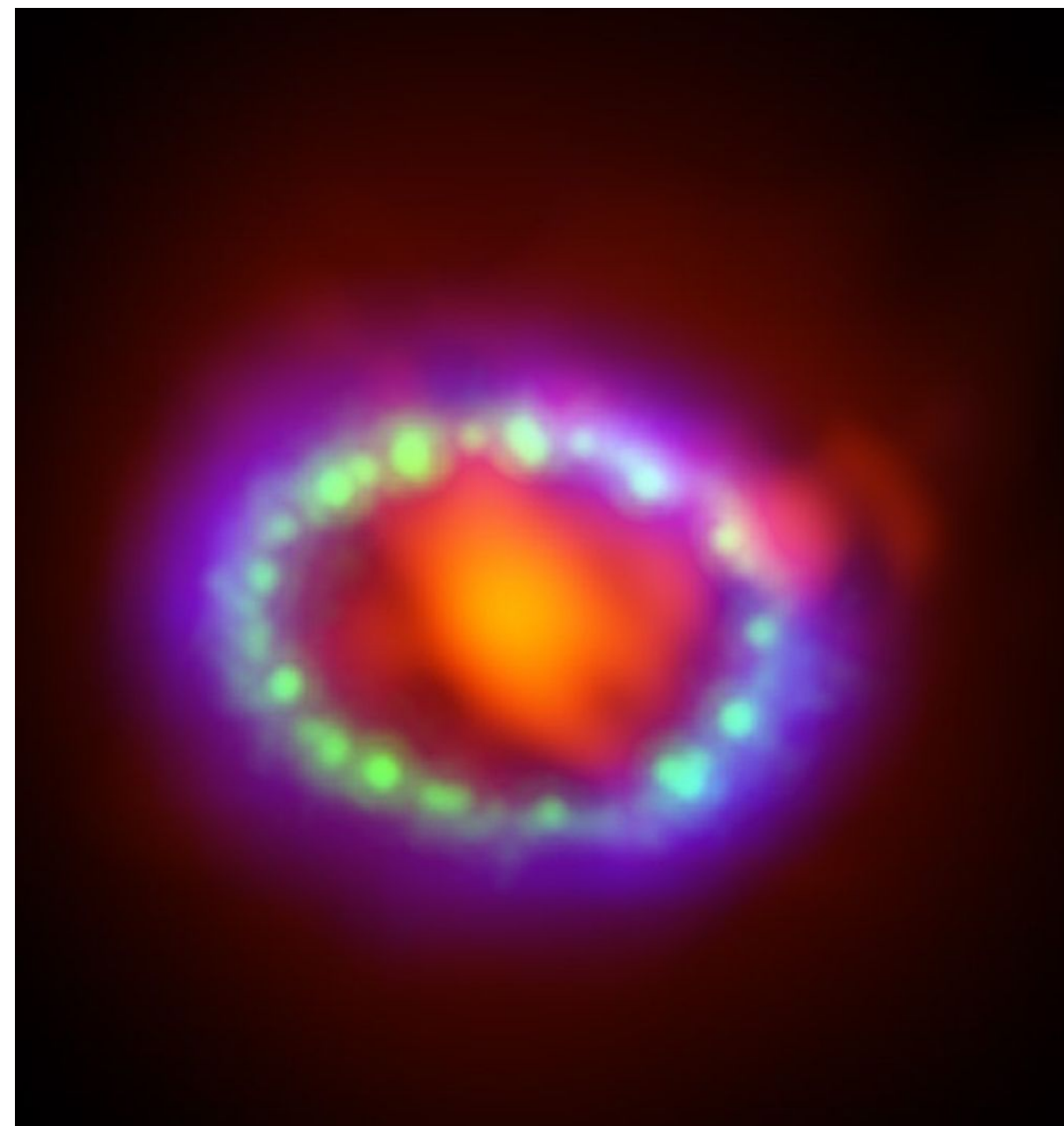


# The MARLEY low-energy neutrino event generator



Steven Gardiner  
 NuSTEC Workshop on Electron Scattering  
 29 March 2022



# MARLEY overview

- Event generator focused specifically on neutrino energies below  $\sim 100$  MeV
  - $\nu$ -A inelastic scattering, some capability for  $\nu$ -e, CEvNS
- “Model of Argon Reaction Low Energy Yields”
  - Emphasizes  $\nu_e$  CC on  $^{40}\text{Ar}$ , extensible
- Two dedicated publications so far:
  - Physics models: [Phys. Rev. C 103, 044604 \(2021\)](#)
  - Numerical implementation: [Comput. Phys. Commun. 269, 108123 \(2021\)](#)
- Written in C++14, few dependencies

Nuclear de-excitations in low-energy charged-current  $\nu_e$  scattering on  $^{40}\text{Ar}$

Steven Gardiner<sup>1,2,\*</sup>

<sup>1</sup>Fermi National Accelerator Laboratory, P.O. Box 500, Batavia, Illinois 60510 USA

<sup>2</sup>Department of Physics, University of California, Davis,

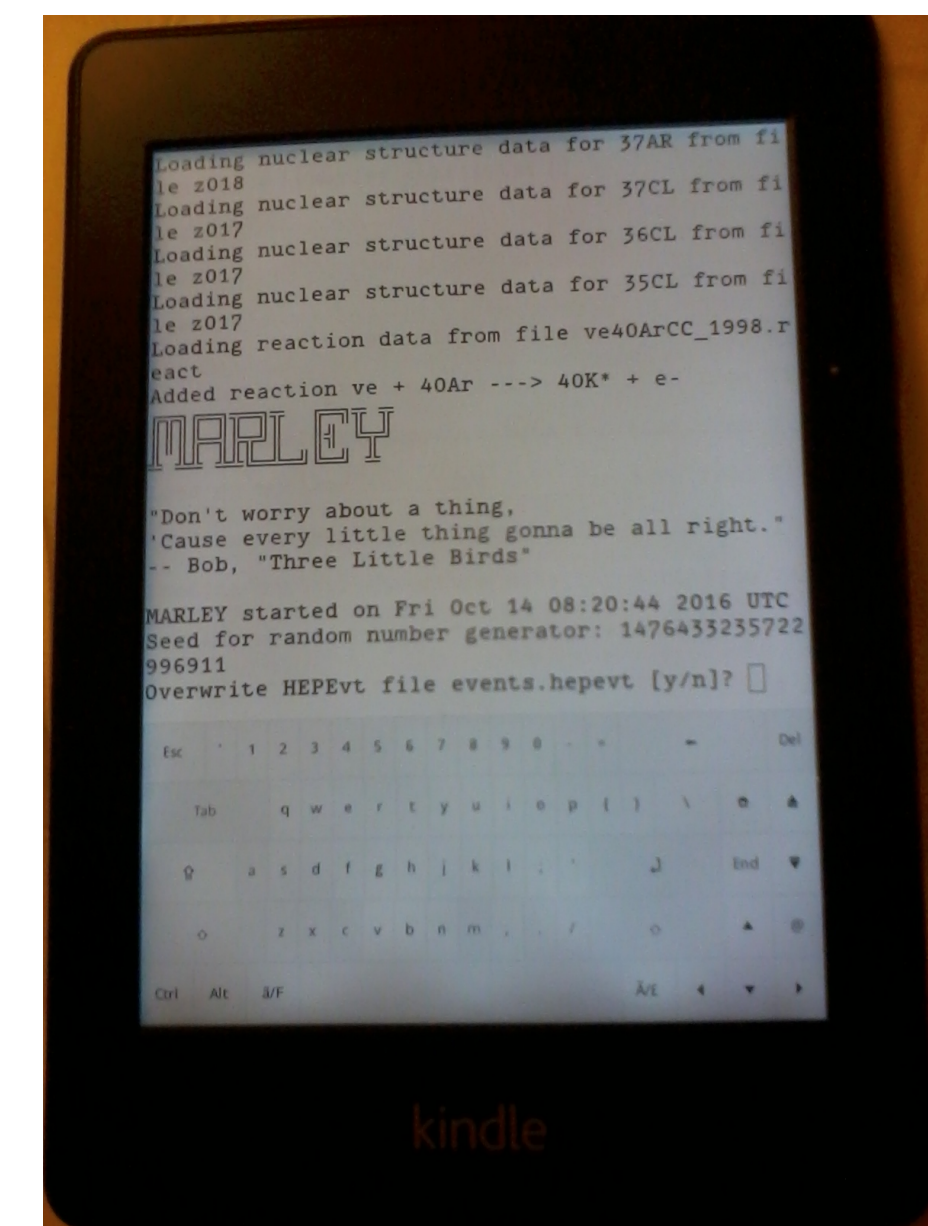
One Shields Avenue, Davis, California 95616 USA

(Dated: September 15, 2020)

**Background:** Large argon-based neutrino detectors, such as those planned for the Deep Underground Neutrino Experiment (DUNE), have the potential to provide unique sensitivity to low-energy ( $\sim 10$  MeV) electron neutrinos produced by core-collapse supernovae. Despite their importance for neutrino energy reconstruction, nuclear de-excitations following charged-current  $\nu_e$  absorption on  $^{40}\text{Ar}$  have never been studied in detail at supernova energies.

**Purpose:** I develop a model of nuclear de-excitations that occur following the  $^{40}\text{Ar}(\nu_e, e^-)^{40}\text{K}^*$  reaction. This model is applied to the calculation of exclusive cross sections.

**Methods:** A simple expression for the inclusive differential cross section is derived under the allowed approximation. Nuclear de-excitations are described using a combination of measured  $\gamma$ -ray decay schemes and the Hauser-Feshbach statistical model. All calculations are carried out using a novel Monte Carlo event generator called MARLEY (Model of Argon Reaction Low Energy Yields).



**MARLEY User Guide**

**Model of Argon Reaction Low Energy Yields**

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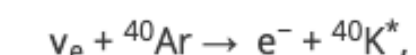
- Copyright and License
- Citing MARLEY
- Getting started
- Interpreting the output
- Bibliography
- GitHub repository
- Developer documentation
- News

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## Overview

**MARLEY** (Model of Argon Reaction Low Energy Yields) is a Monte Carlo event generator for neutrino-nucleus interactions at energies of tens-of-MeV and below. The current version computes inclusive neutrino-nucleus cross sections employing the *allowed approximation*: the nuclear matrix elements are evaluated while neglecting Fermi motion and applying the long-wavelength (zero momentum transfer) limit. De-excitations of the final-state nucleus emerging from the primary interaction are simulated using a combination of tabulated  $\gamma$ -ray decay schemes and an original implementation of the Hauser-Feshbach statistical model.

Input files are provided with the code that are suitable for simulating the charged-current process



coherent elastic neutrino-nucleus scattering (CEvNS) on spin-zero target nuclei, and neutrino-electron elastic scattering on any atomic target. Inclusion of additional reactions and targets is planned for the future.

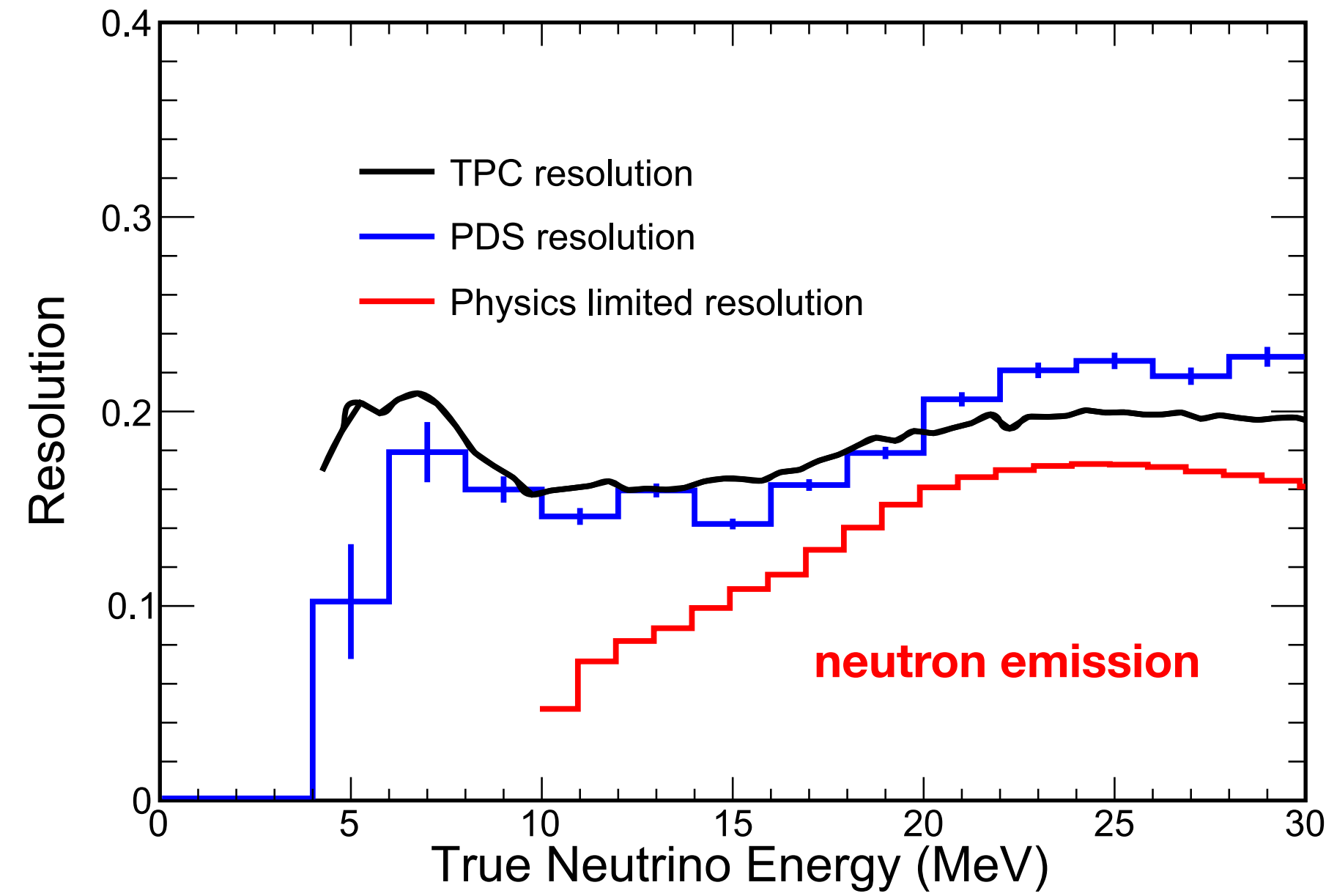
The material presented here focuses on the practical aspects of MARLEY: installing the code, configuring and running simulations, and analyzing the output events. For more details on the MARLEY physics models, please see the references in the online [bibliography](#).

MARLEY follows an open-source development model and welcomes contributions of new input files and code improvements from the community. A partial list of potential projects for future MARLEY development is available on the developer documentation [webpage](#).



# Example applications of MARLEY

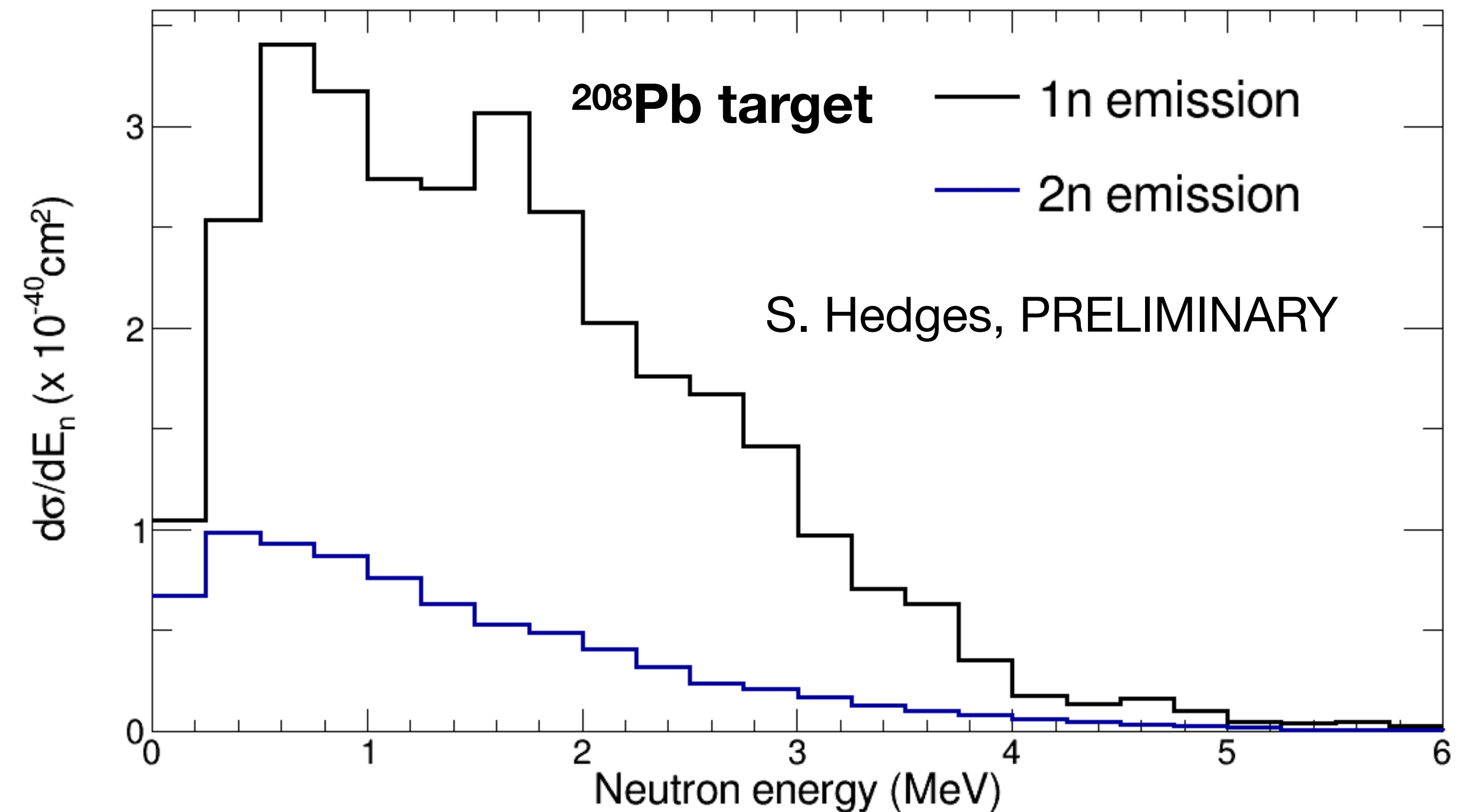
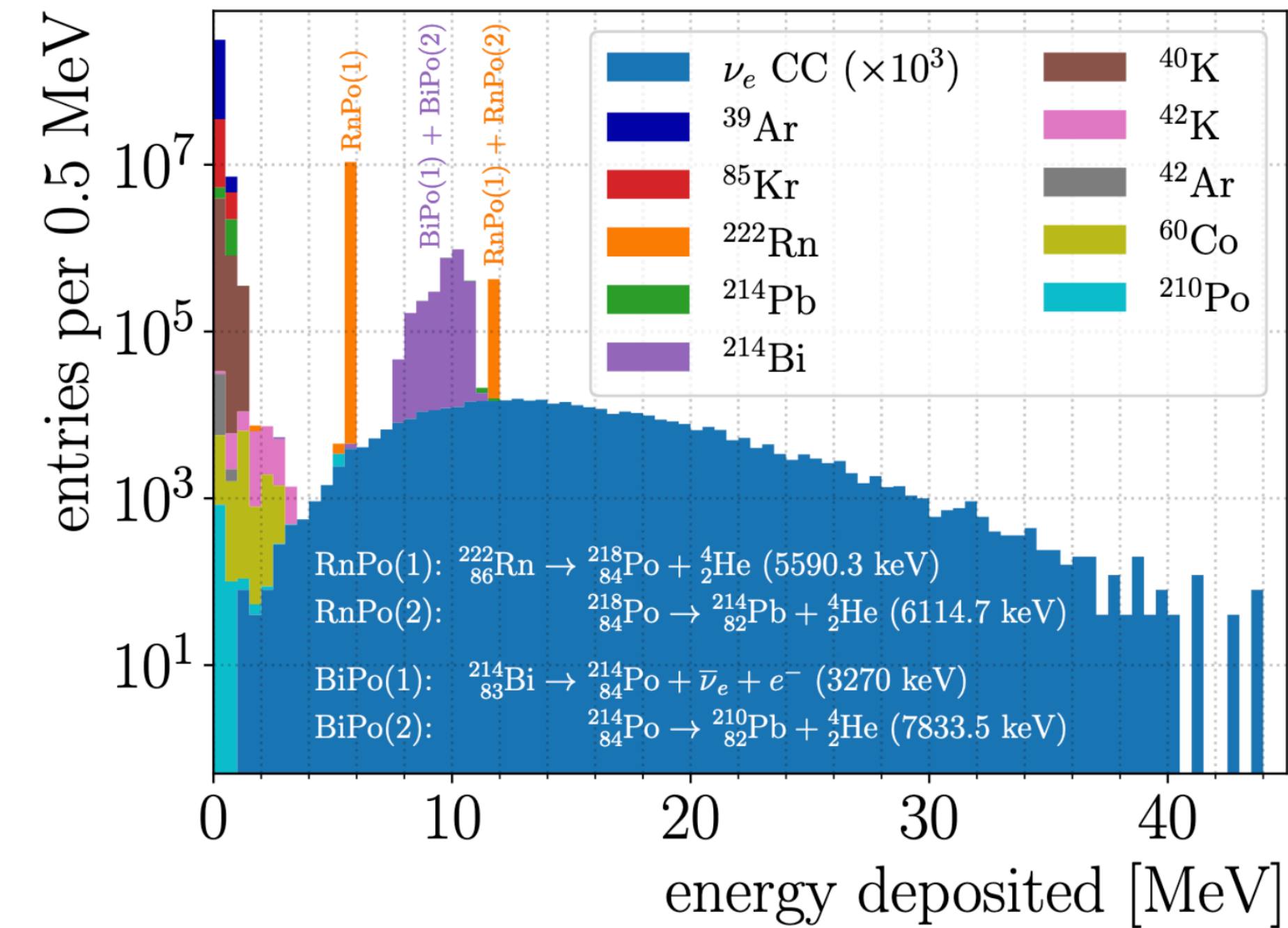
[Eur. Phys. J. C 81, 423 \(2021\)](#)



Supernova neutrino energy resolution in DUNE

Neutrino-induced neutron spectra for COHERENT (see [arXiv:2110.07730](#))

Pixelated readout (Q-Pix) performance for supernova neutrino detection in DUNE



# MARLEY inclusive cross section model

Neutrino-nucleus reaction treated as a **two-step process**. In the first step, inclusive scattering on the nucleus is simulated.

$$\frac{d\sigma}{d\cos\theta_\ell} = \frac{G_F^2}{2\pi} \mathcal{F}_{CC} \left[ \frac{E_i E_f}{s} \right] E_\ell |\mathbf{p}_\ell| \left[ (1 + \beta_\ell \cos\theta_\ell) B(F) + \left(1 - \frac{1}{3}\beta_\ell \cos\theta_\ell\right) B(GT) \right]$$

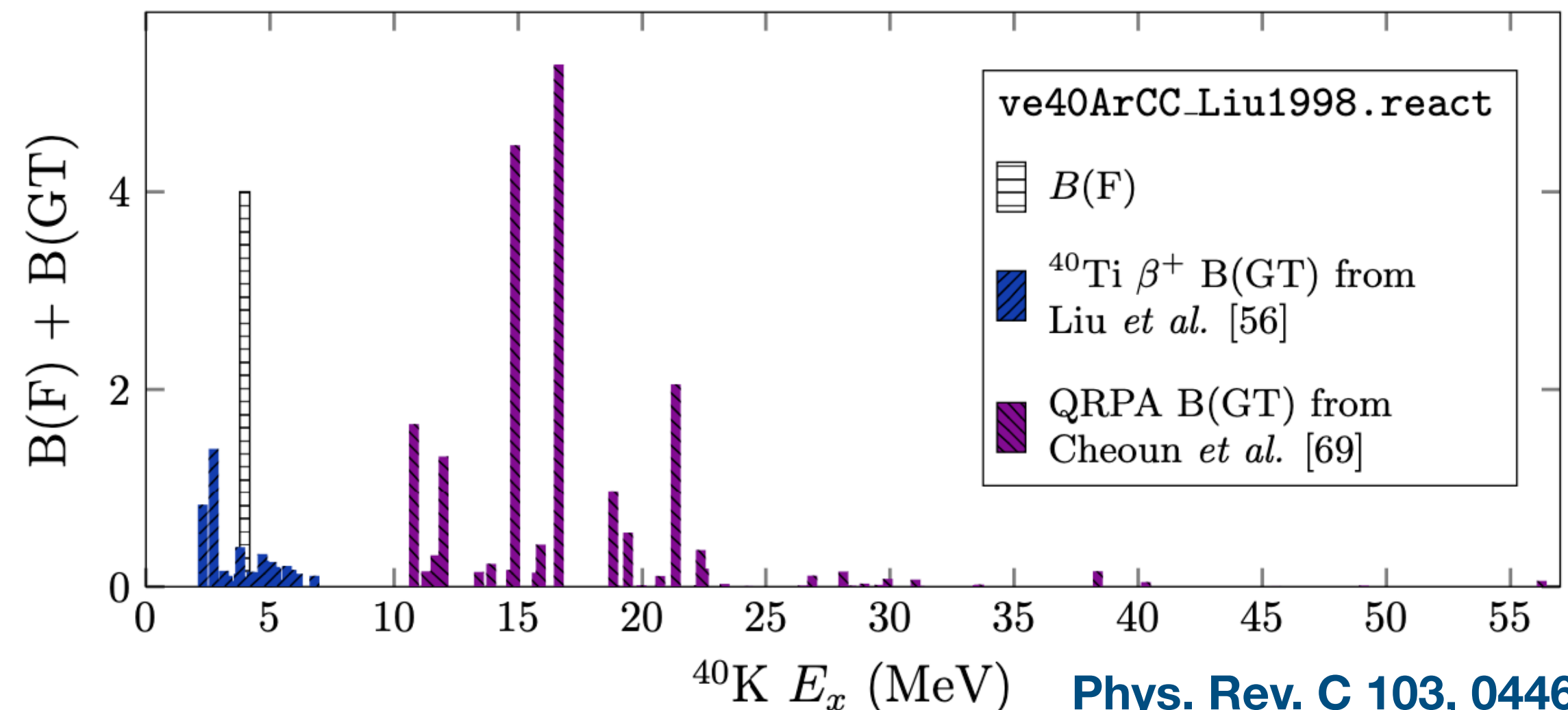
Charged current factor      Recoil factor      Allowed nuclear matrix elements

Expression above obtained under the impulse approximation (no 2p2h) and the **allowed approximation**

Long-wavelength limit:  $q \rightarrow 0$

Slow nucleon limit:  $\frac{|\mathbf{p}_{N_i}|}{m_N} \rightarrow 0$

Nuclear matrix elements must be supplied as input. For  $^{40}\text{Ar}$ , they are based on a combination of **indirect measurements** (e.g., mirror  $\beta$  decay) and a **QRPA calculation**





# MARLEY inclusive cross section model

**Charged-current factor** contains CKM matrix element and a Coulomb correction factor  $F_C$ . MARLEY handles Coulomb corrections using a combination of the Fermi function and the Modified Effective Momentum Approximation (MEMA).

$$\mathcal{F}_{CC} \equiv \begin{cases} |V_{ud}|^2 F_C & \text{CC} \\ 1 & \text{NC} \end{cases}$$

See [J. Engel, Phys. Rev. C 57, 2004 \(1998\)](#)

The code can handle **allowed matrix elements** for  $\nu_e$  CC,  $\bar{\nu}_e$  CC, and NC, but only inputs for  $\nu_e$  CC are currently provided “out of the box”

$$\mathcal{O}_F \equiv \begin{cases} \sum_{n=1}^A t_{\pm}(n) & \text{CC} \\ Q_W/2 & \text{NC} \end{cases}$$

$$B(F) \equiv \frac{g_V^2}{2J_i + 1} \left| \langle J_f \parallel \mathcal{O}_F \parallel J_i \rangle \right|^2$$

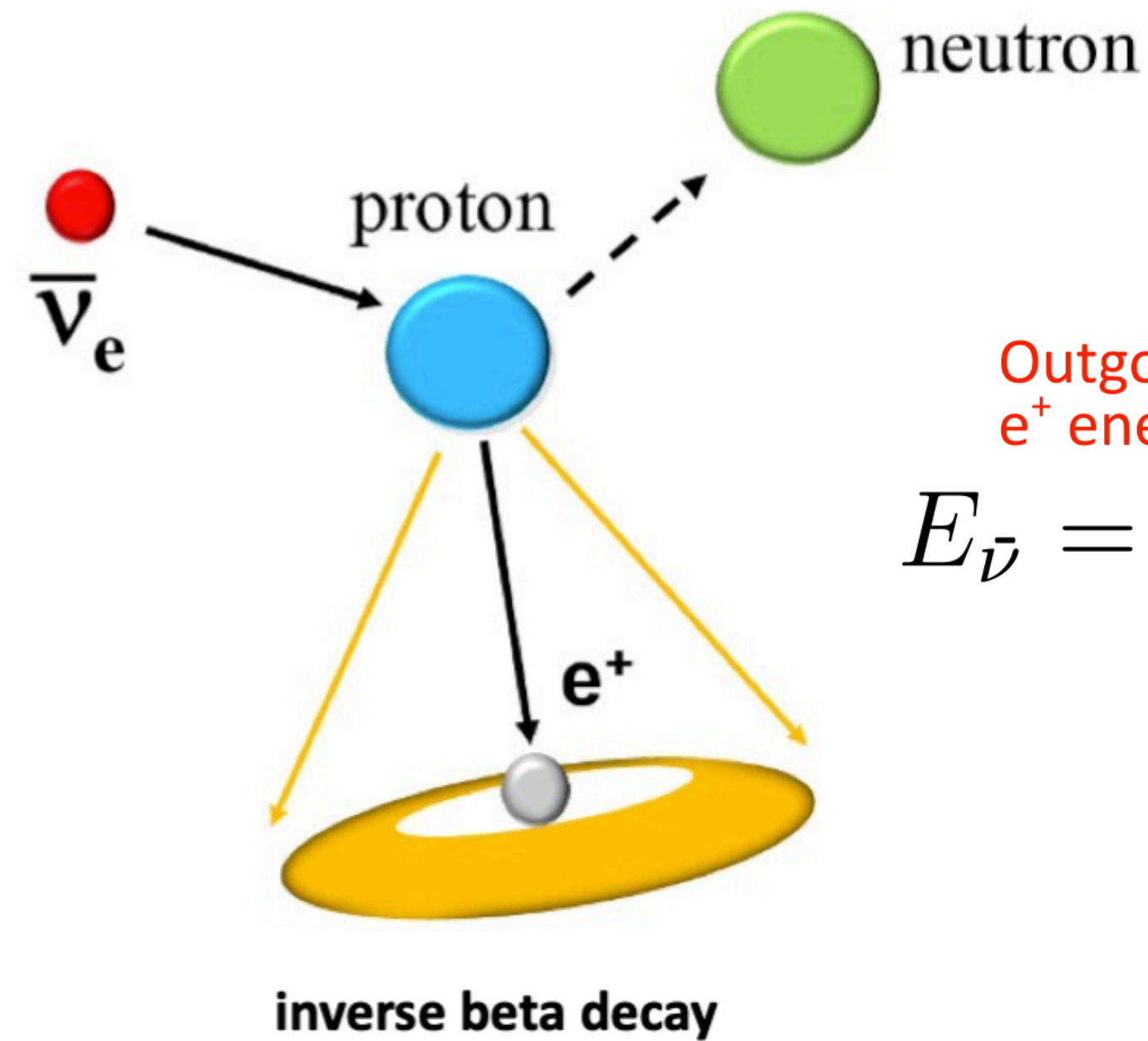
$$B(GT) \equiv \frac{g_A^2}{2J_i + 1} \left| \langle J_f \parallel \mathcal{O}_{GT} \parallel J_i \rangle \right|^2$$

$$\mathcal{O}_{GT} \equiv \begin{cases} \sum_{n=1}^A \sigma(n) t_{\pm}(n) & \text{CC} \\ \sum_{n=1}^A \sigma(n) t_3(n) & \text{NC} \end{cases}$$



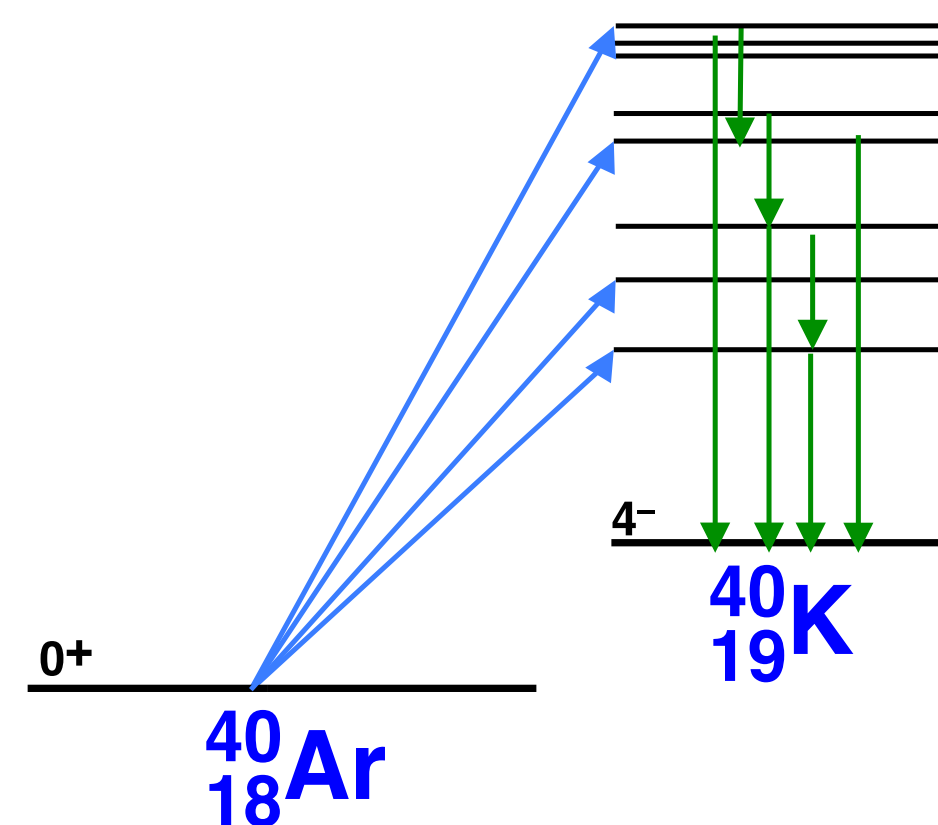
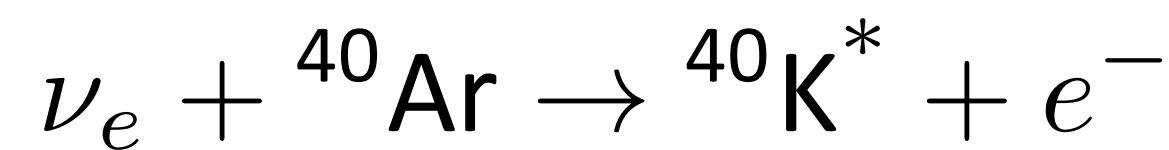
# The importance of full final-state predictions

- Needs are similar to those for GeV-scale experiments
- **Example:** supernova neutrino calorimetry
- Scintillator & water Cherenkov detectors
  - Inverse beta decay
  - Positron energy sufficient
- LArTPCs (e.g., DUNE)
  - Complex nuclear target, many transitions
  - De-excitation products must be measured
  - Correct for missing energy from neutrons, etc.



Outgoing  $e^+$  energy    Neutron proton mass difference    Recoil energy of neutron (negligible)

$$E_{\bar{\nu}} = E_e + \Delta + K_{\text{recoil}}$$



**MARLEY** seeks to provide a realistic treatment of the de-excitation physics

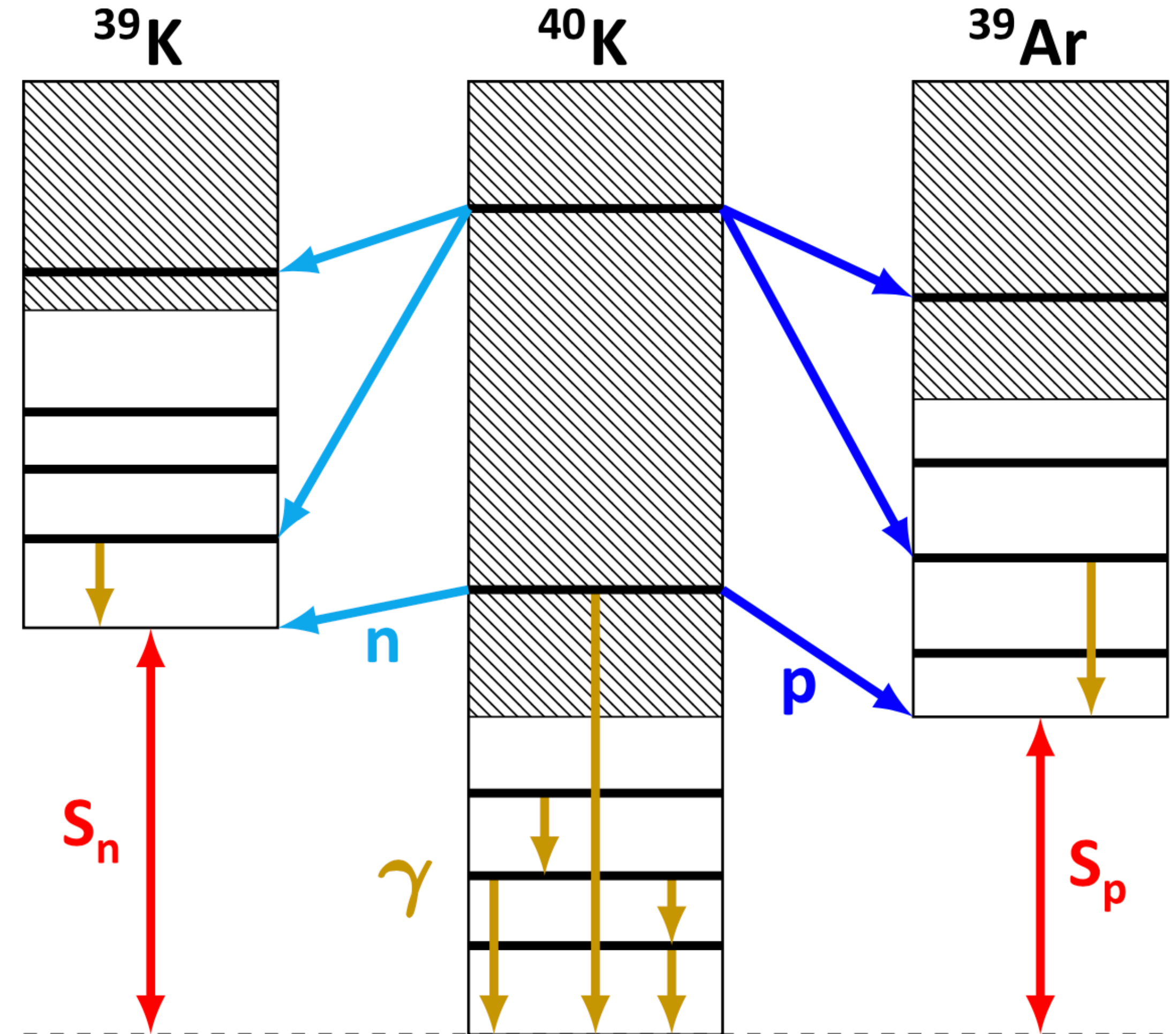
Outgoing  $e^-$  Energy    Energy donated to transition    Recoil Energy of Nucleus (negligible)

$$E_{\nu} = E_e + Q + K_{\text{recoil}}$$



# The importance of full final-state predictions

- Needs are similar to those for GeV-scale experiments
- **Example:** supernova neutrino calorimetry
- Scintillator & water Cherenkov detectors
  - Inverse beta decay
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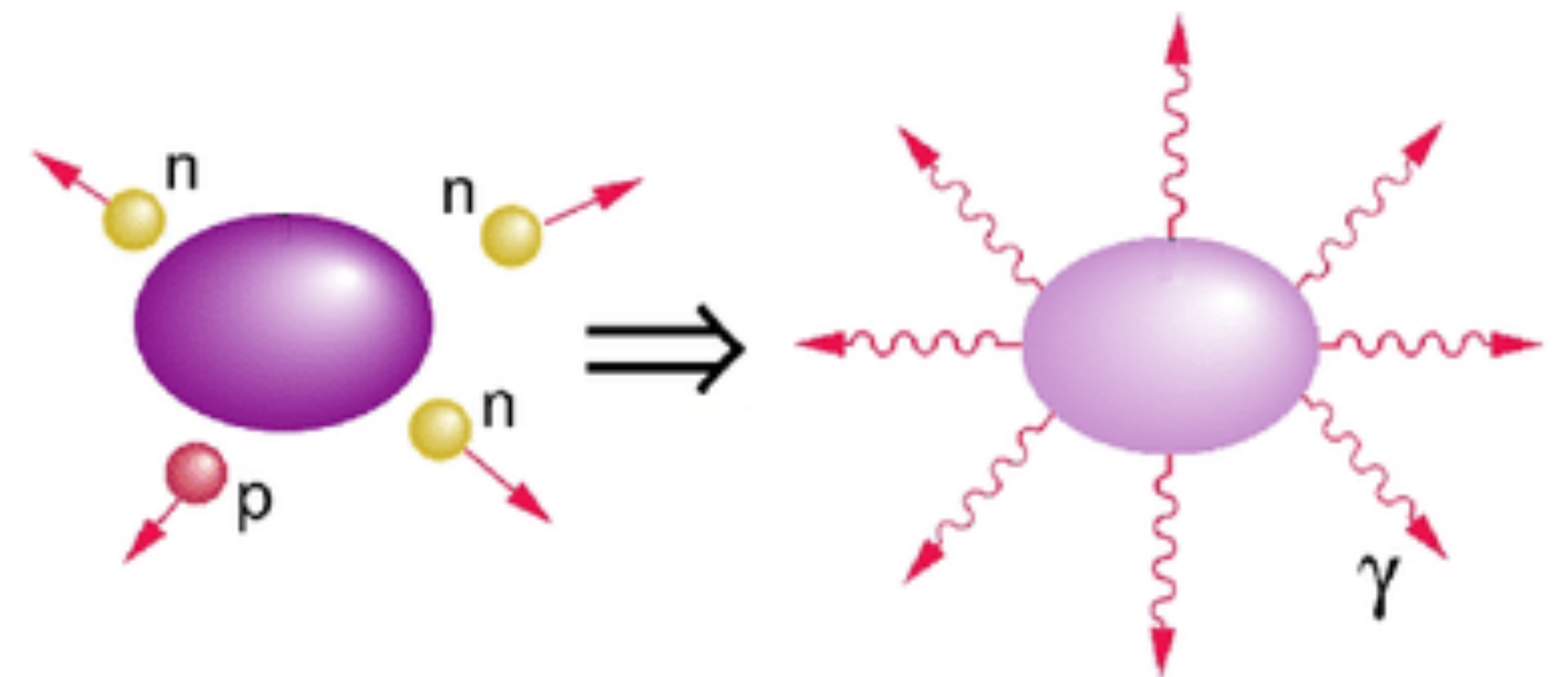
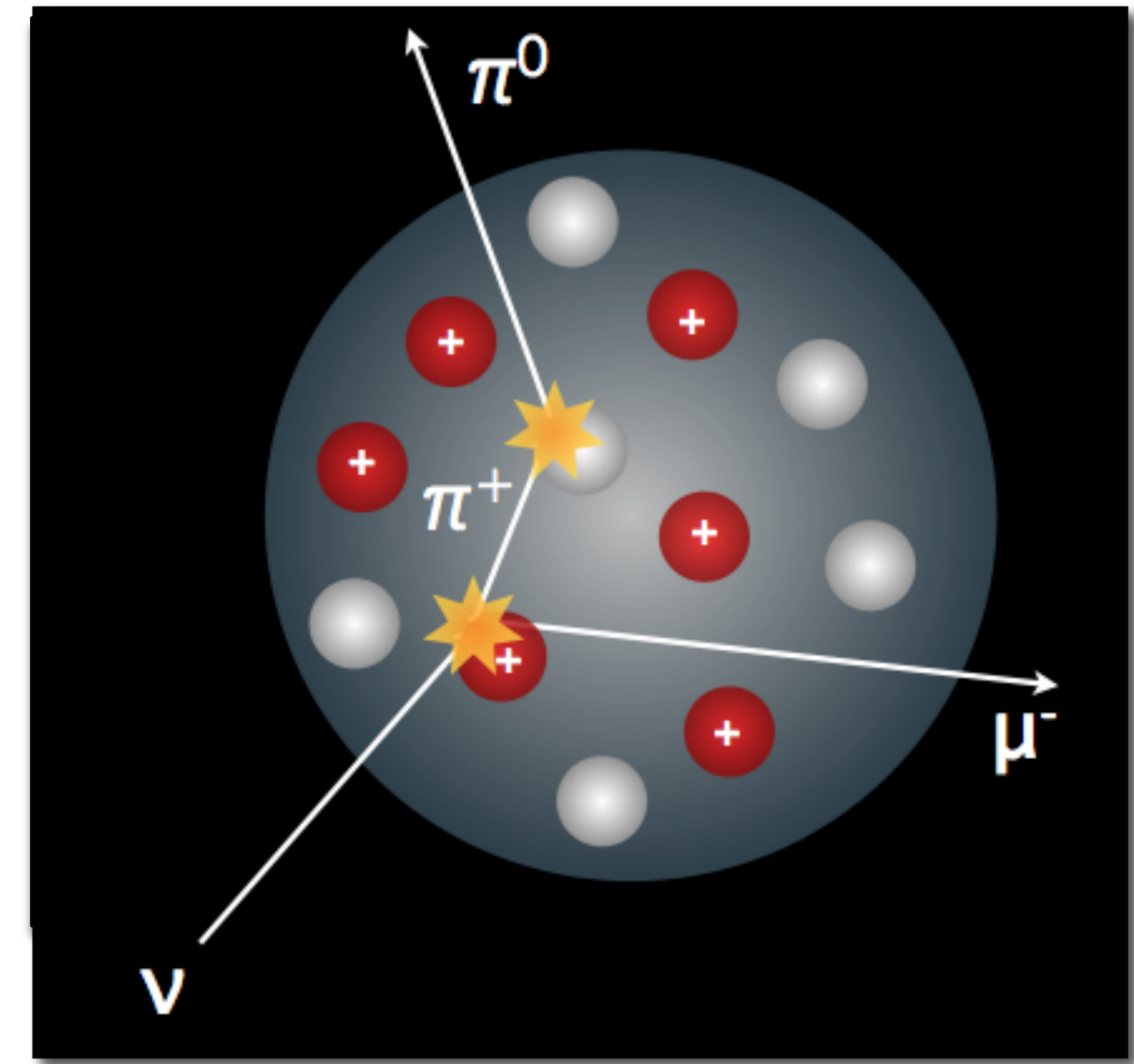


**Various de-excitation channels  
make the problem complicated**



# The compound nucleus assumption

- High-energy generators rely primarily on a **direct knockout** picture
  - Transport outgoing hadrons through the nucleus
  - Dynamical models: intranuclear cascade (GENIE, NEUT, NuWro) or BUU transport (GiBUU)
- MARLEY uses a **compound nucleus** picture standard in the low-energy literature
  - Energy transfer widely shared, leading to equilibration and “boil off” of nucleons
  - Hauser-Feshbach statistical model
- Some FSI models include both (e.g., FLUKA)
  - FLUKA and MARLEY both have realistic gamma-ray emission

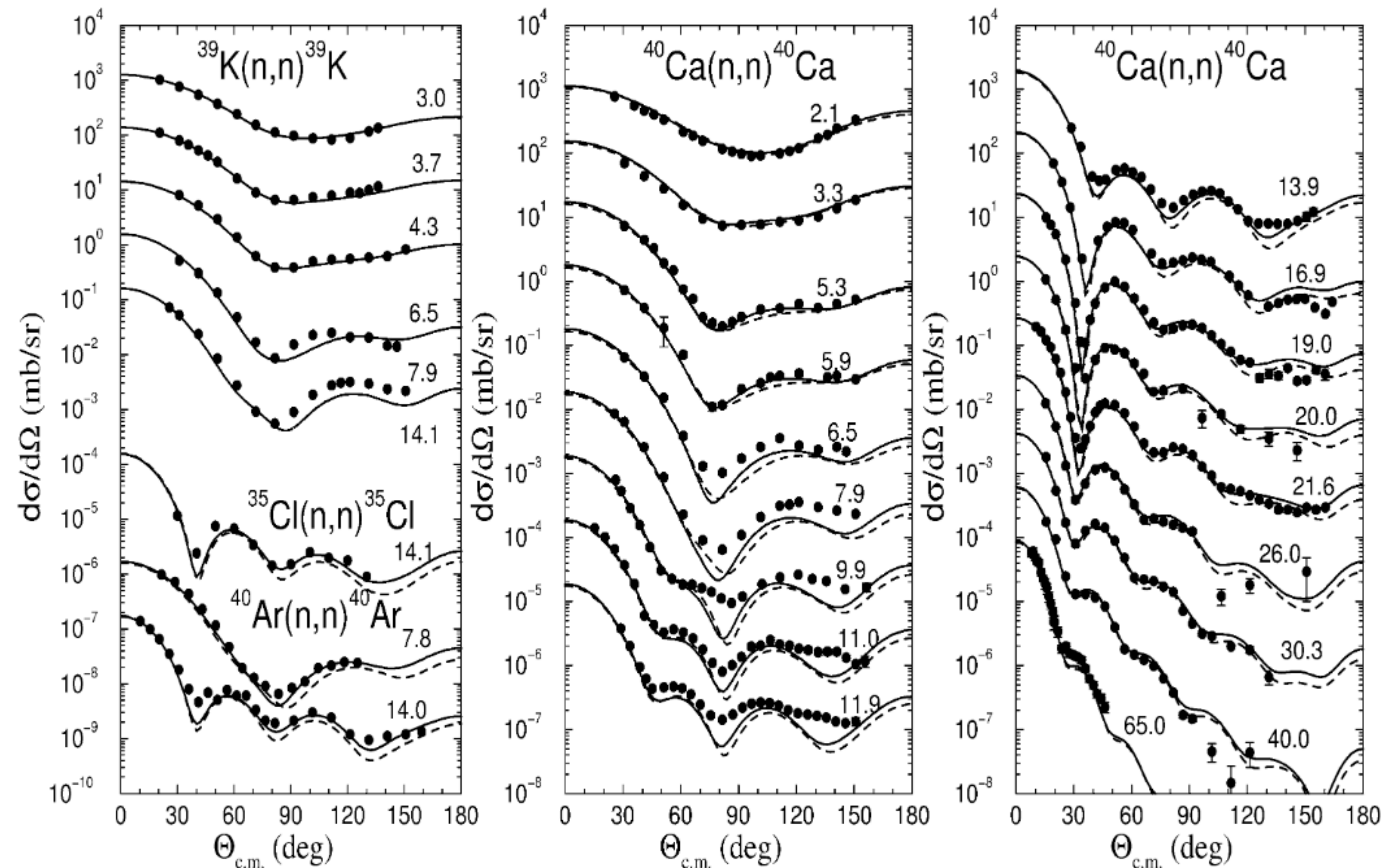




# The compound nucleus assumption

- Equilibration → “amnesia”
  - Compound nucleus de-excitations independent of creation process
- Time reversal symmetry
  - Relate decay widths to compound nucleus formation cross sections
- MARLEY ingredients taken from semi-empirical fits to low-energy nuclear reaction & structure data
  - Also tabulated nuclear levels and gamma-rays

Koning & Delaroche, *Nucl. Phys. A* 713, 231–310 (2003)



Dashed line is the global optical model fit that MARLEY currently uses. Solid lines are local fits to specific nuclei.



# MARLEY nuclear de-excitation model

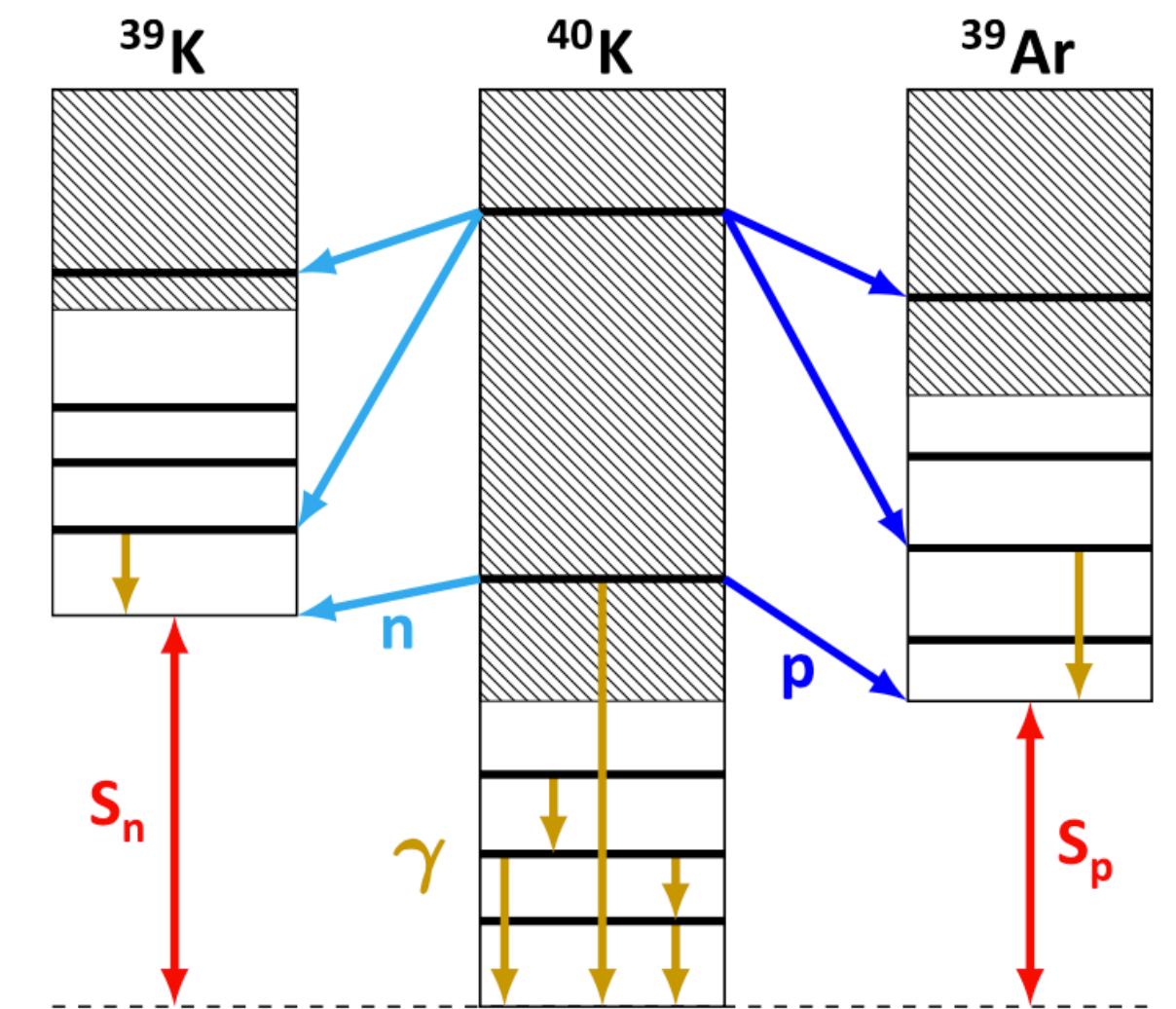
The nucleus de-excites via a series of binary decays. Decay widths for **unbound states** are computed according to the Hauser-Feshbach formalism:

Differential decay width  
for emission of a  
nuclear fragment  $\alpha$   
( $A \leq 4$  considered)

$$\frac{d\Gamma_{\alpha}}{dE'_x} = \frac{1}{2\pi} \frac{1}{\rho_i(E_x, J, \Pi)} \sum_{\ell=0}^{\ell_{\max}} \sum_{j=|\ell-s|}^{\ell+s} \sum_{J'=|J-j|}^{J+j} T_{\ell j}(\varepsilon) \rho_f(E'_x, J', \Pi')$$

Differential decay width  
for emission of a  
 $\gamma$ -ray

$$\frac{d\Gamma_{\gamma}}{dE'_x} = \frac{1}{2\pi} \frac{1}{\rho_i(E_x, J, \Pi)} \sum_{\lambda=1}^{\lambda_{\max}} \sum_{J'=|J-\lambda|}^{J+\lambda} \sum_{\Pi' \in \{-1, 1\}} T_{X\lambda}(E_{\gamma}) \rho_f(E'_x, J', \Pi')$$



**Level density model:** Back-shifted Fermi gas  
(RIPL-3), Nucl. Data Sheets 110, 3107–3214 (2009)

**Nuclear optical model:** Koning & Delaroche, Nucl. Phys. A 713, 231–310 (2003)

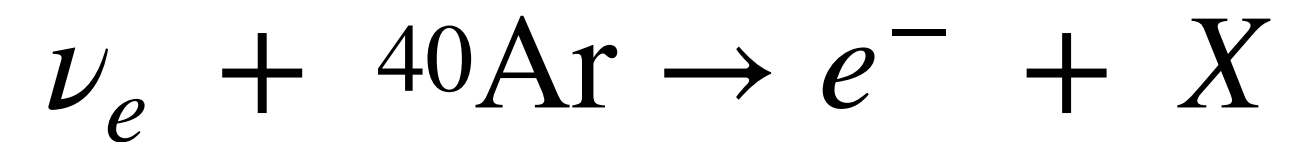
**Gamma-ray strength function model:** Standard Lorentzian (RIPL-3), Nucl. Data Sheets 110, 3107–3214 (2009)

Supplemented with tabulated discrete levels and  $\gamma$ -rays for **bound states** (taken from TALYS 1.6). Transitions from continuum to all accessible levels are explicitly treated.



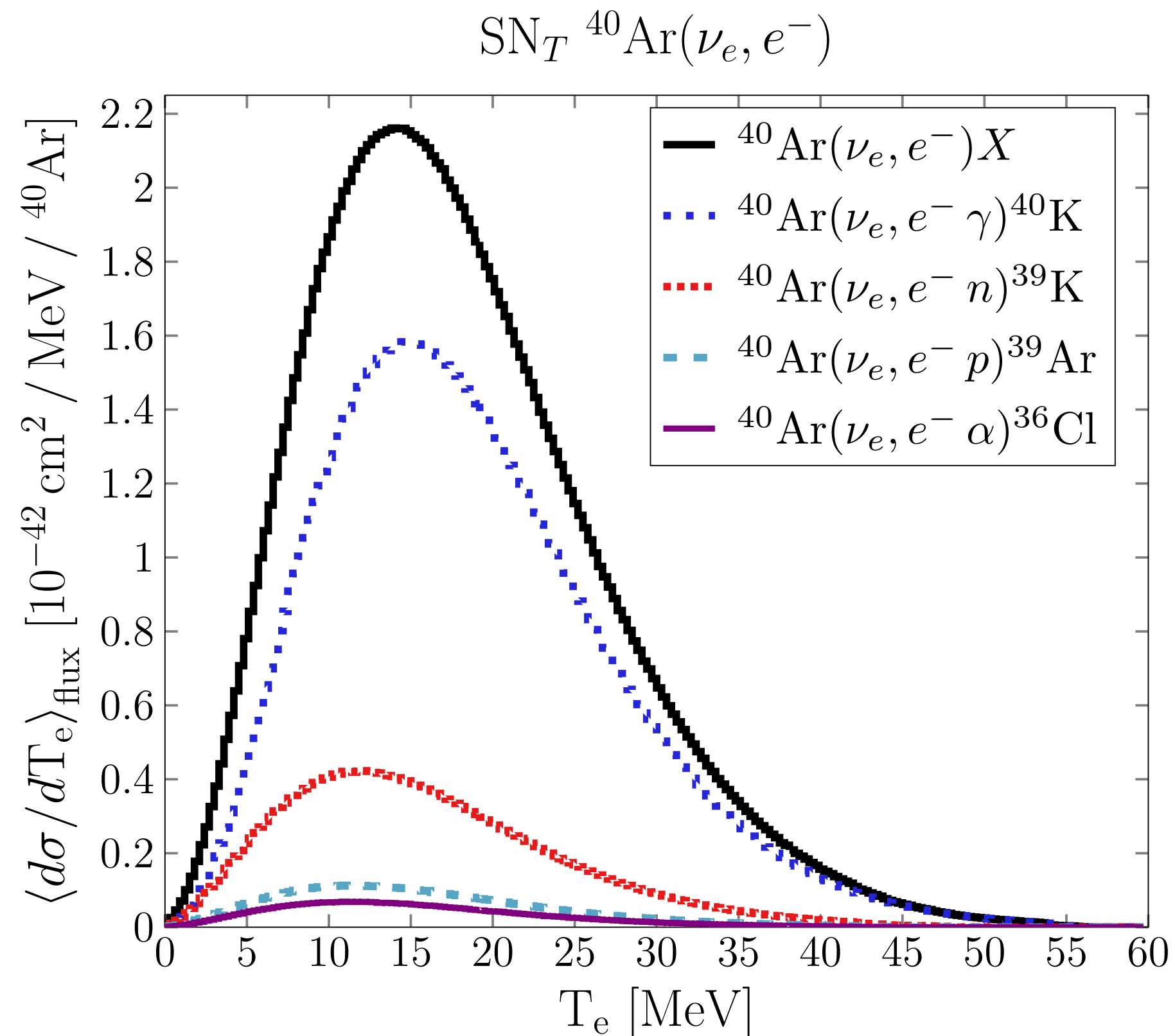
# MARLEY v1.2.0 predictions for $^{40}\text{Ar}$

- First calculation of cross sections for **exclusive final states** of the reaction

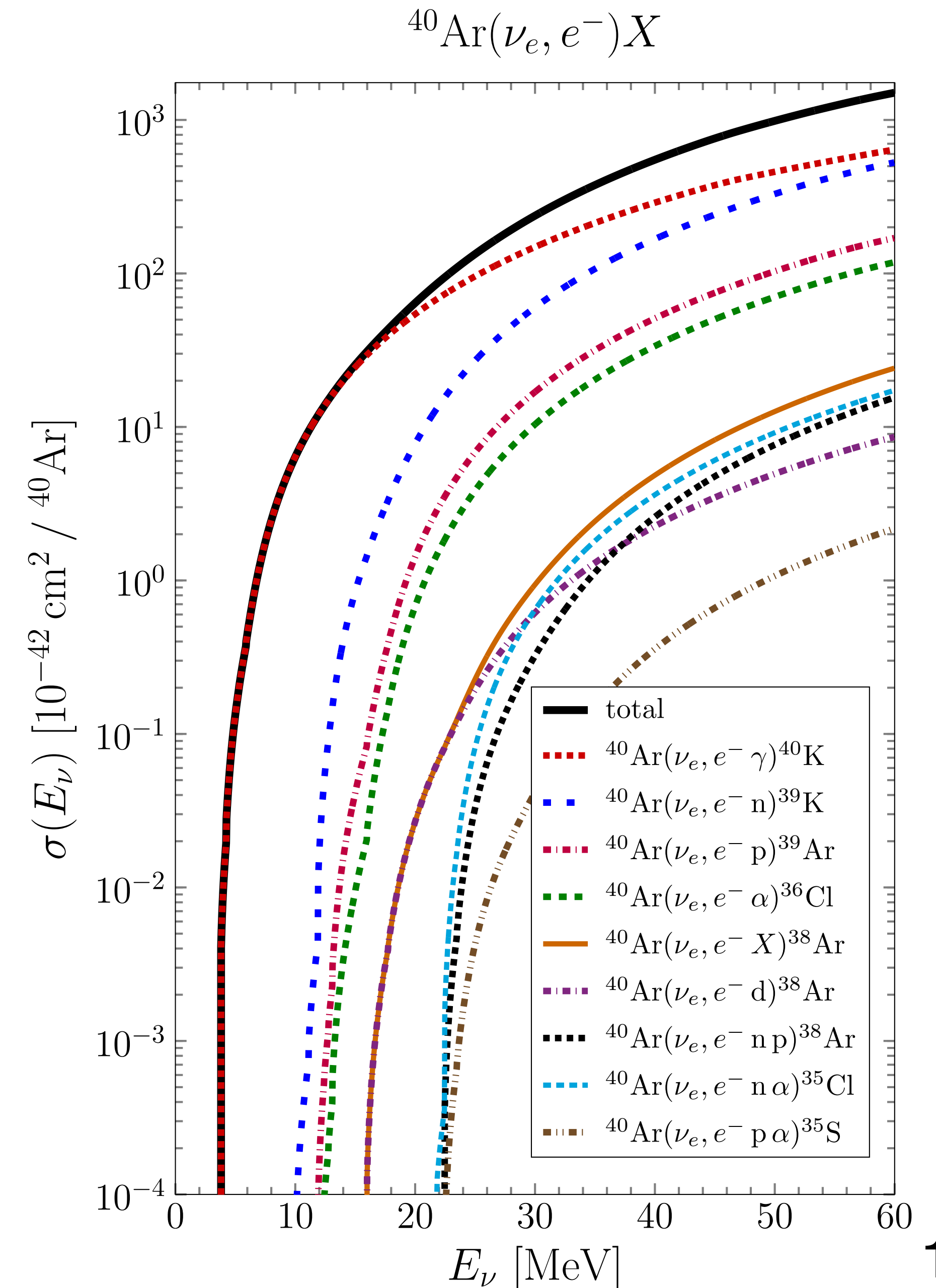


at tens-of-MeV energies.

- Flux-averaged differential cross sections shown here are for the supernova model described in [Phys. Rev. D 97, 023019 \(2018\)](#).



[Phys. Rev. C 103, 044604 \(2021\)](#)

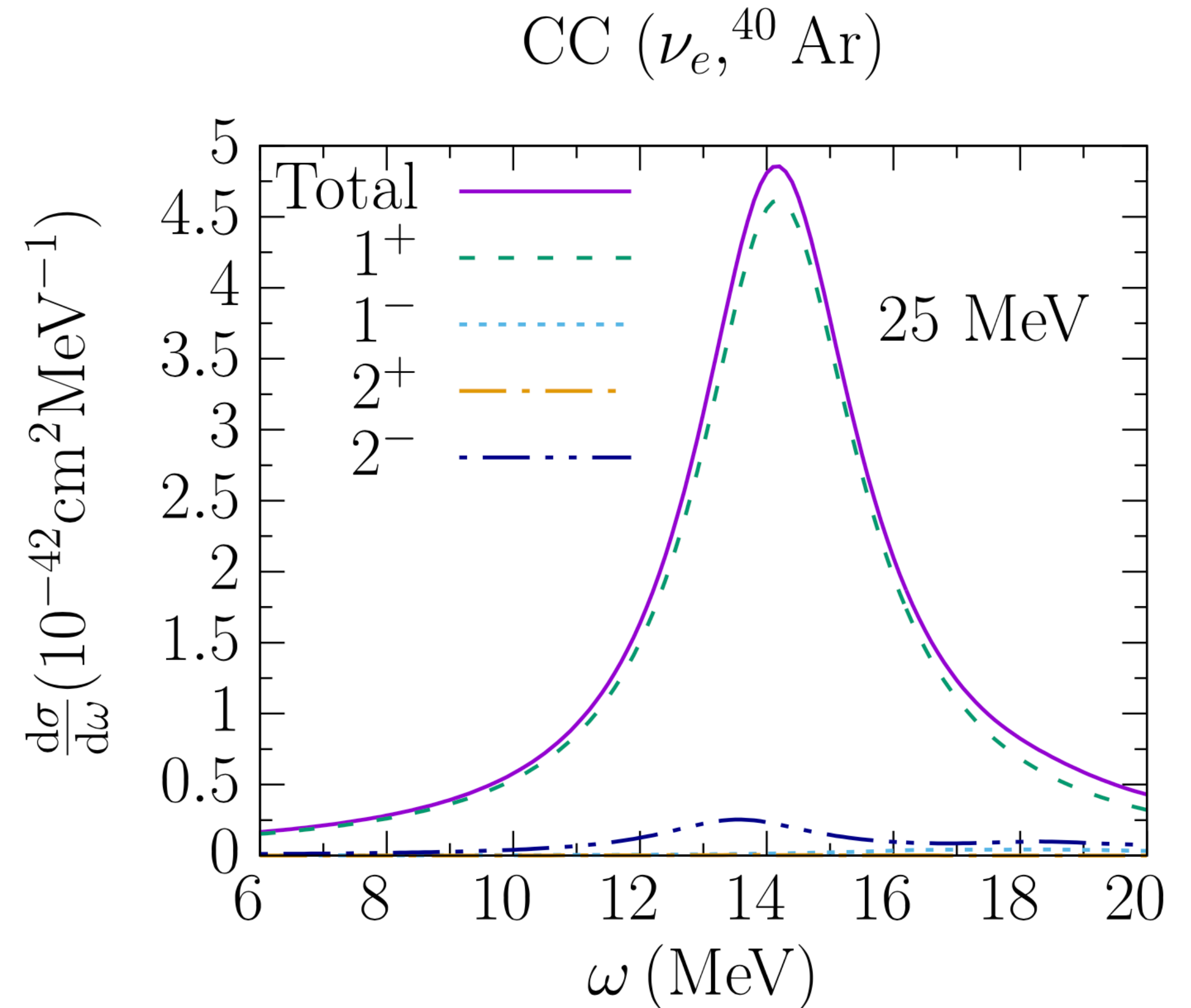




# HF-CRPA model in MARLEY

- “Allowed approximation” begins to break down at several tens of MeV
  - $q \rightarrow 0$  and  $p_N/m_N \rightarrow 0$ , only  $0^+$  and  $1^+$  multipoles survive
- HF-CRPA includes higher multipoles (“forbidden transitions”)
  - Strong impact on angular distribution
- **More strength to higher excitation energies**
  - Expected impact on neutron yield, etc.
- Implementation in progress
  - Similar to GENIE strategy ([arXiv:2110.14601](https://arxiv.org/abs/2110.14601))
  - Responses separated by multipole order:  $J^\pi$  input to de-excitation model
- Opportunity to simulate electrons consistently

N. Van Dessel *et al.*, [Phys. Rev. C 100, 055503 \(2019\)](https://doi.org/10.1103/PhysRevC.100.055503)

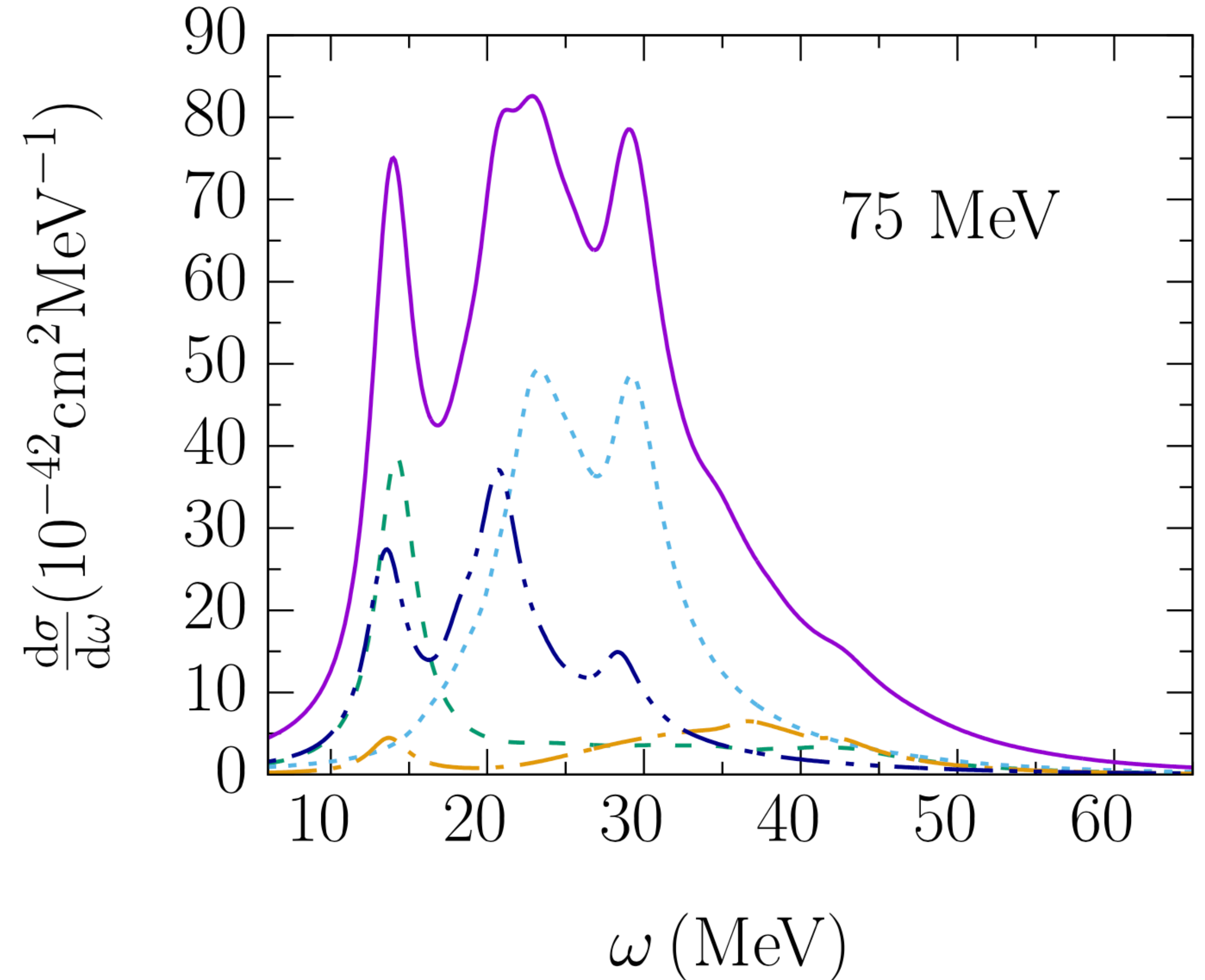


**1+ component** analogous to B(GT) strength

# HF-CRPA model in MARLEY

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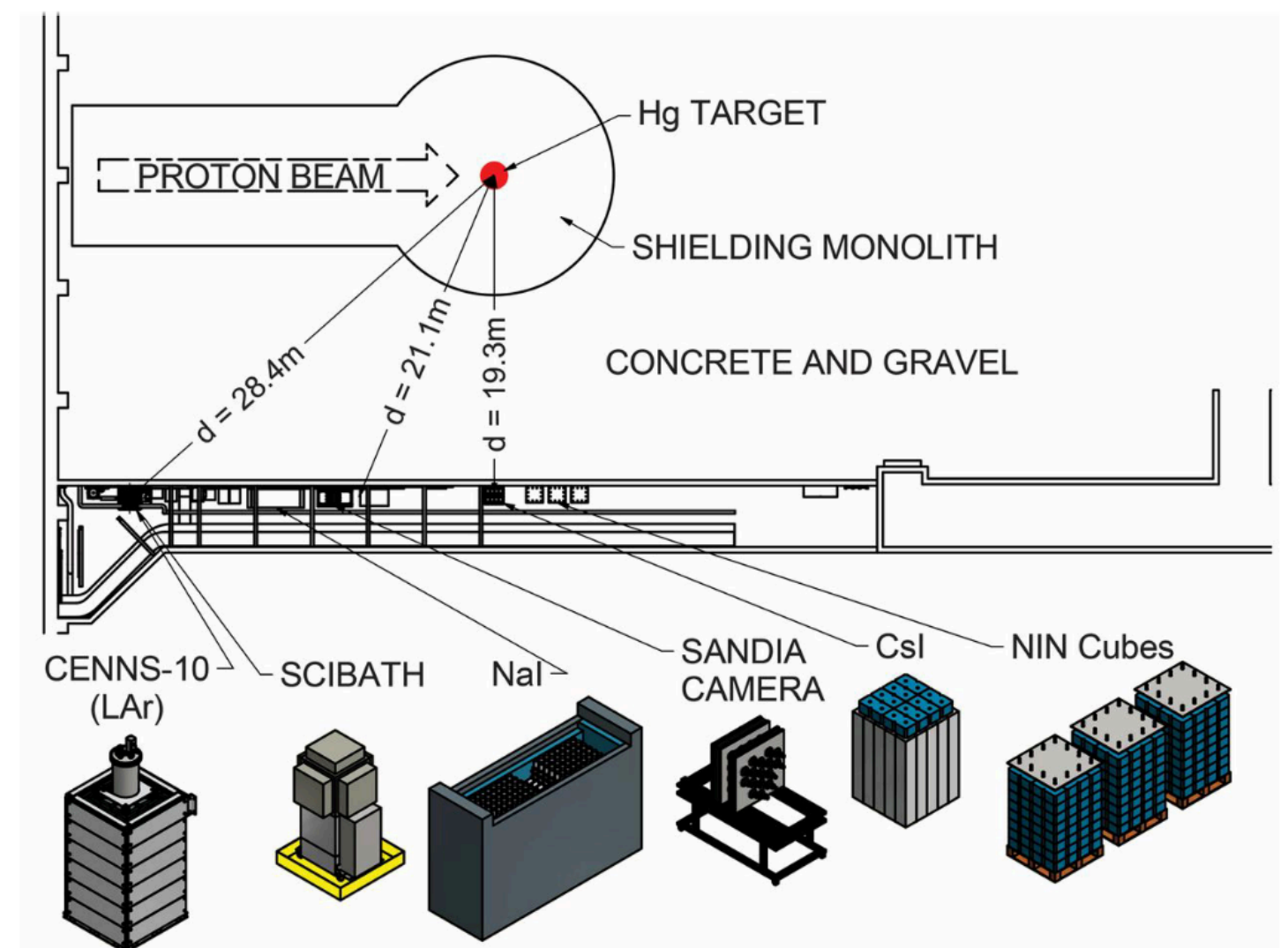
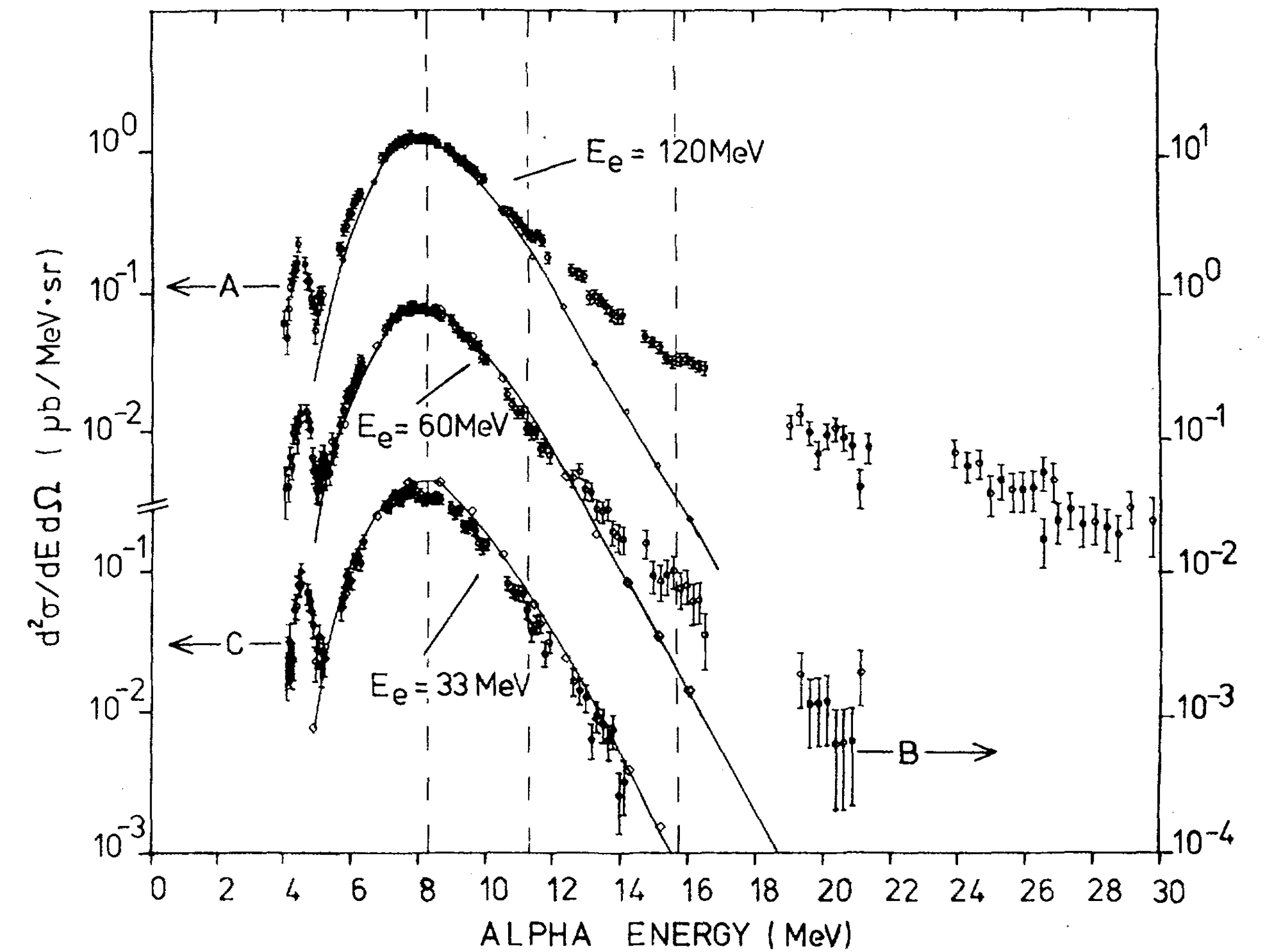
**1+ component** analogous to B(GT) strength



# Opportunities with electron data

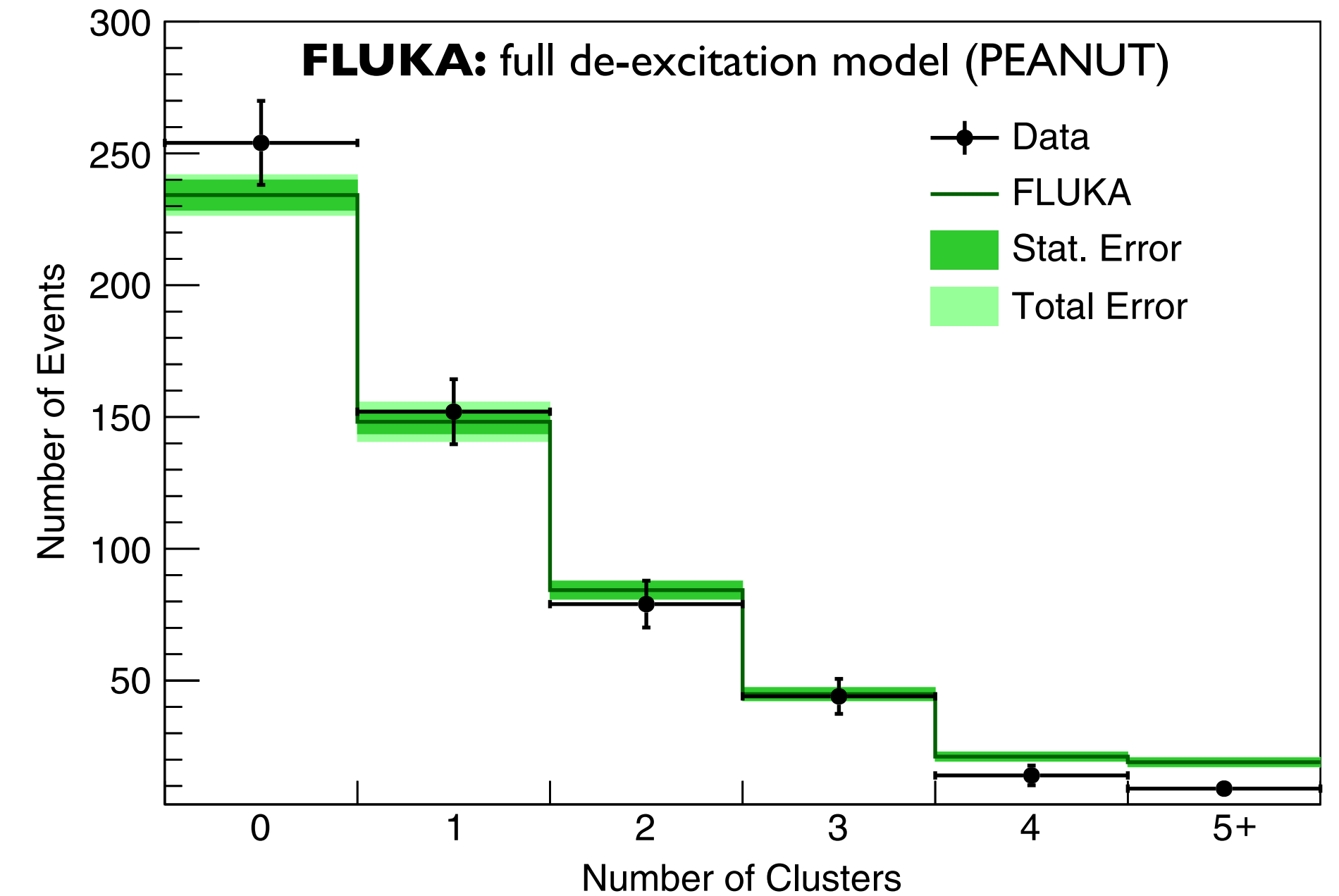
- Only elastic e-A scattering under “allowed approximation”
  - Inclusive electron data can helpfully probe forbidden contributions
- (Semi-)exclusive data very powerful
  - Little direct evidence for compound nucleus assumption with leptonic probe
  - Benchmark simulations of the full final state
- Complementary to forthcoming neutrino-induced neutron data from COHERENT
  - Is any tension in the inclusive or the de-excitation model?

Flowers et al., Phys. Rev. Lett. 40 (1978)

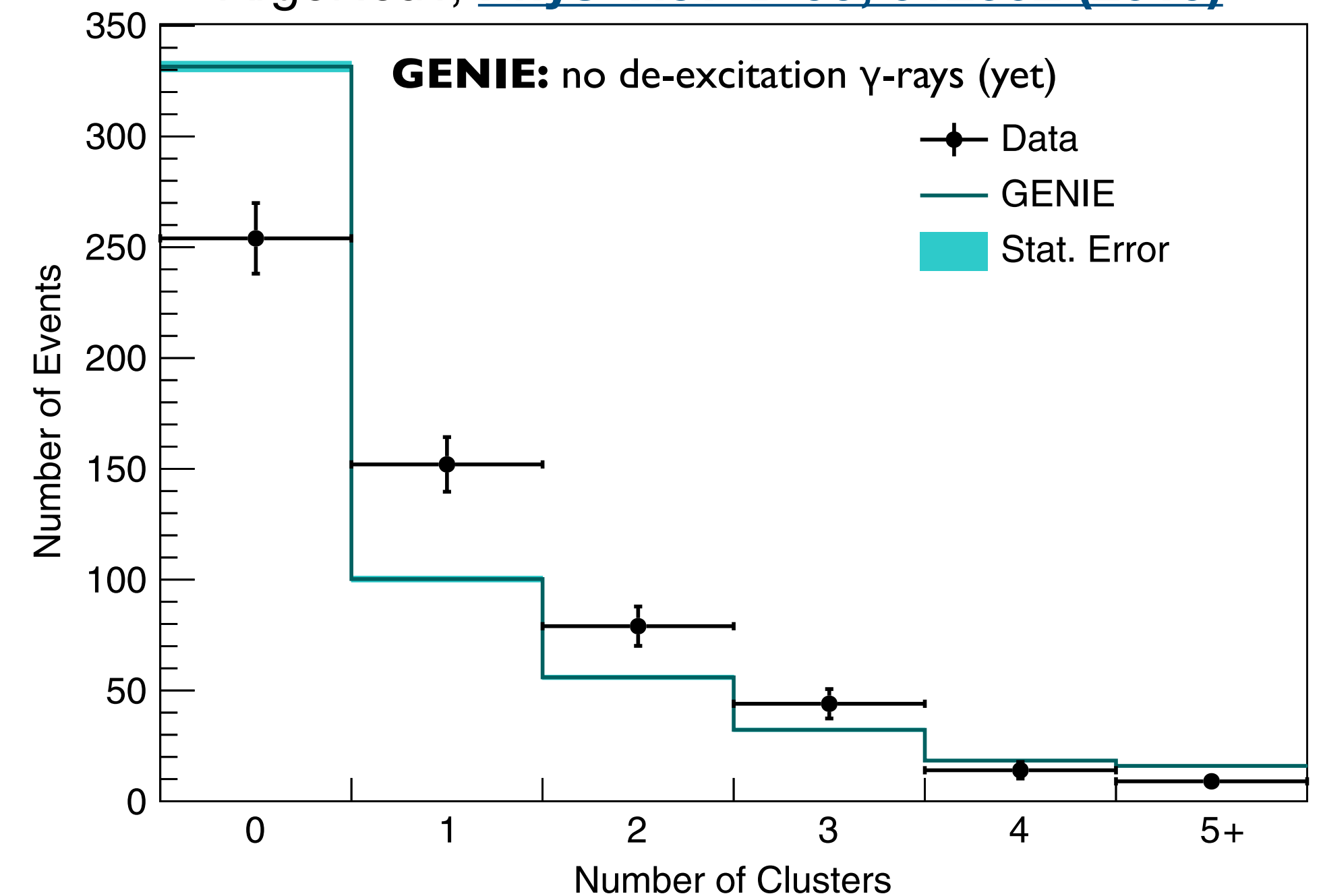


# Connections to higher energies

- MARLEY-like de-excitation physics observable in LArTPCs
  - Recently demonstrated by ArgoNeuT
  - Comparisons to FLUKA, GENIE
  - Use MARLEY as an open-source “afterburner”?
- Possible means of improving reconstruction of GeV neutrinos
  - “Blip reconstruction” under active development
- De-excitations from proton decay may provide a powerful new handle for searches (see [this Snowmass LOI](#))
- Snowmass white paper “Low-Energy Physics in Neutrino LArTPCs” ([arXiv:2203.00740](#))



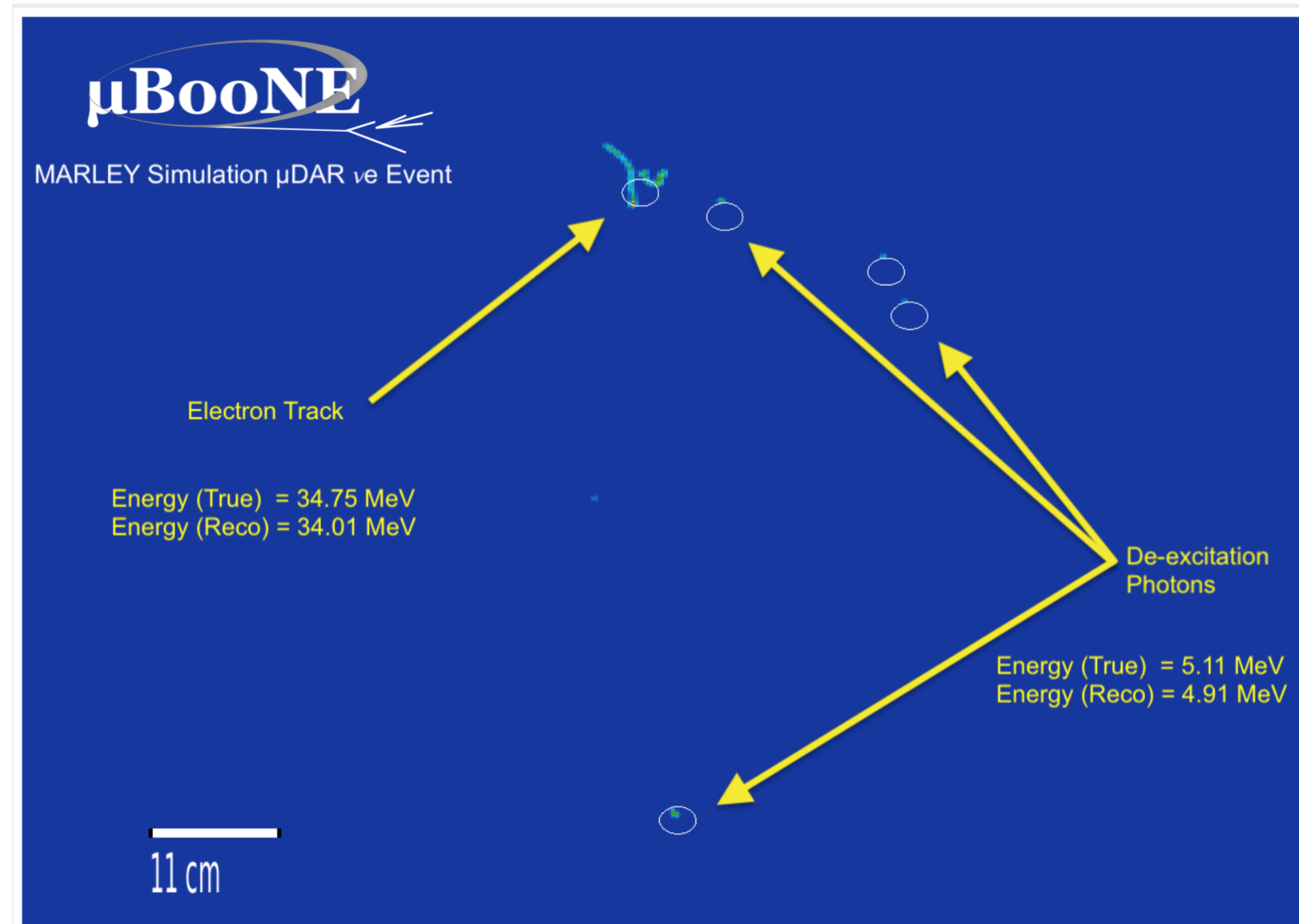
ArgoNeuT, [Phys. Rev. D 99, 012002 \(2019\)](#)





# Summary

- **MARLEY** is a dedicated neutrino event generator focused on sub-100-MeV energies
  - Emphasis on  $\nu_e$  CC on  $^{40}\text{Ar}$  for DUNE
- Nuclear de-excitation modeling is key to predicting full final states
  - Some shared challenges and overlap with topics for higher energies
- HF-CRPA implementation will provide a clear path to  $e^-$  simulations
- Electron data valuable to inform low-energy interaction modeling
  - I am excited to explore related opportunities further



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