

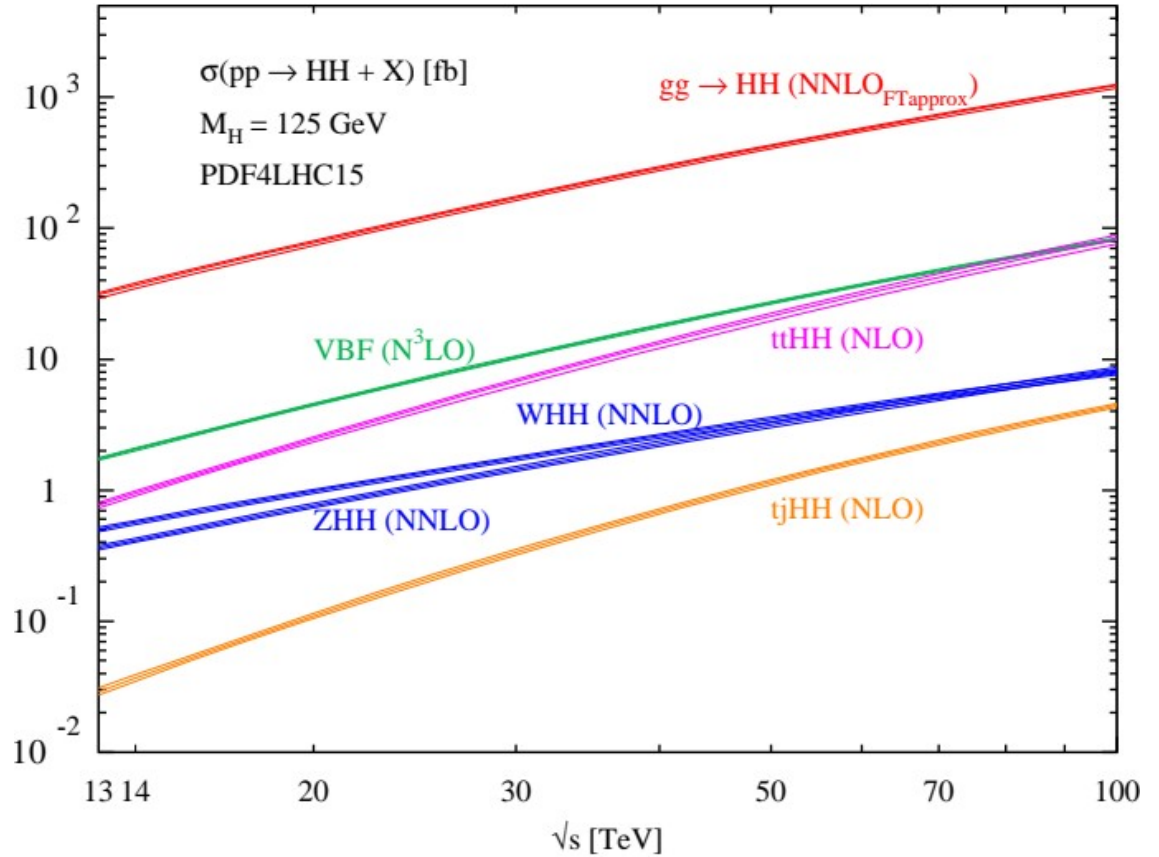
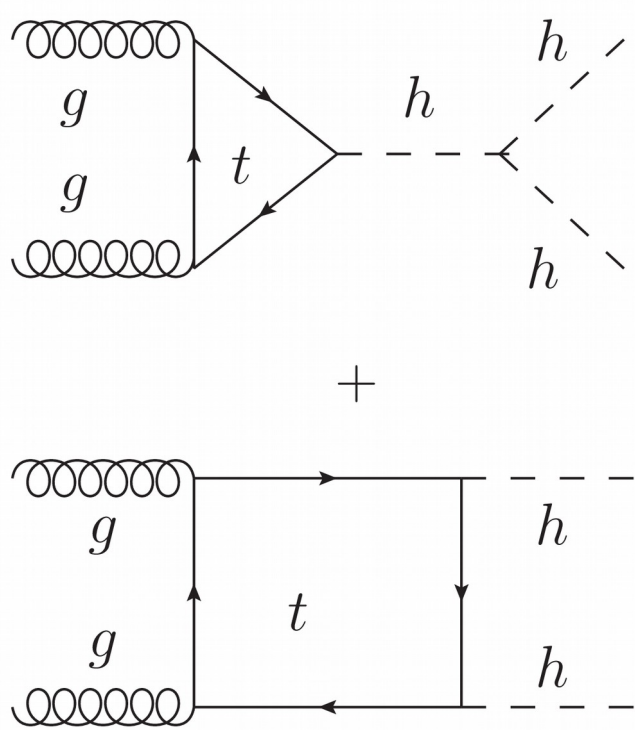
HH Theory Status

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EF01 Jan. 12, 2022

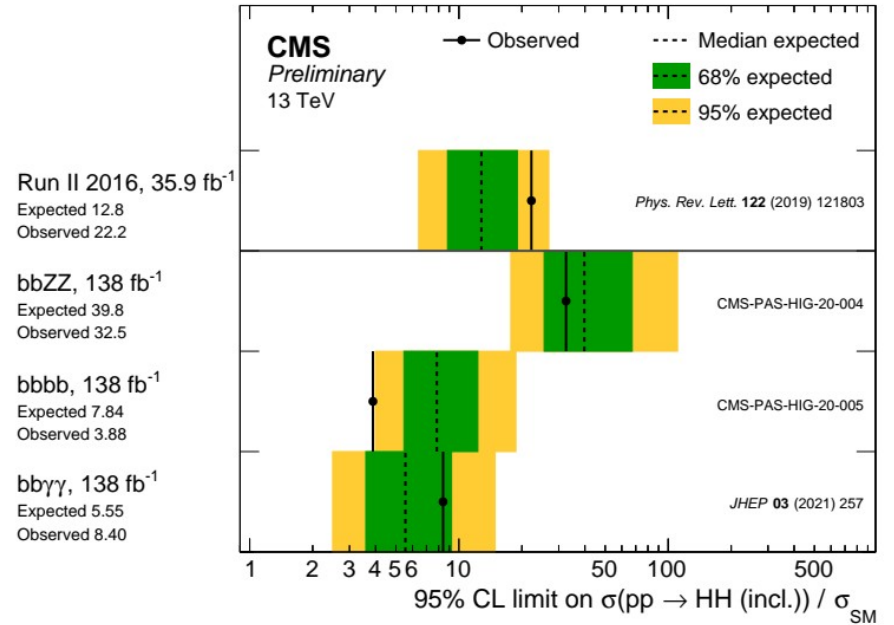
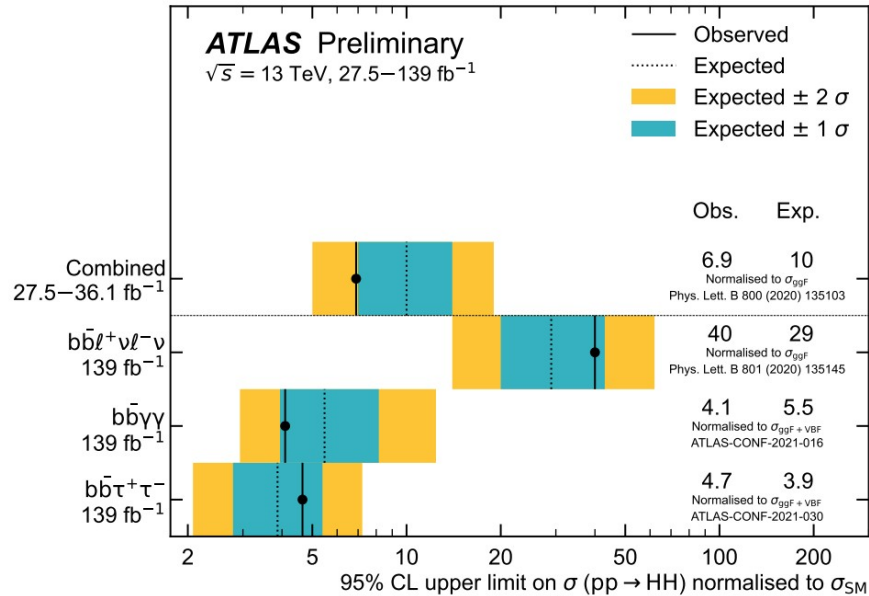
Di-Higgs in SM



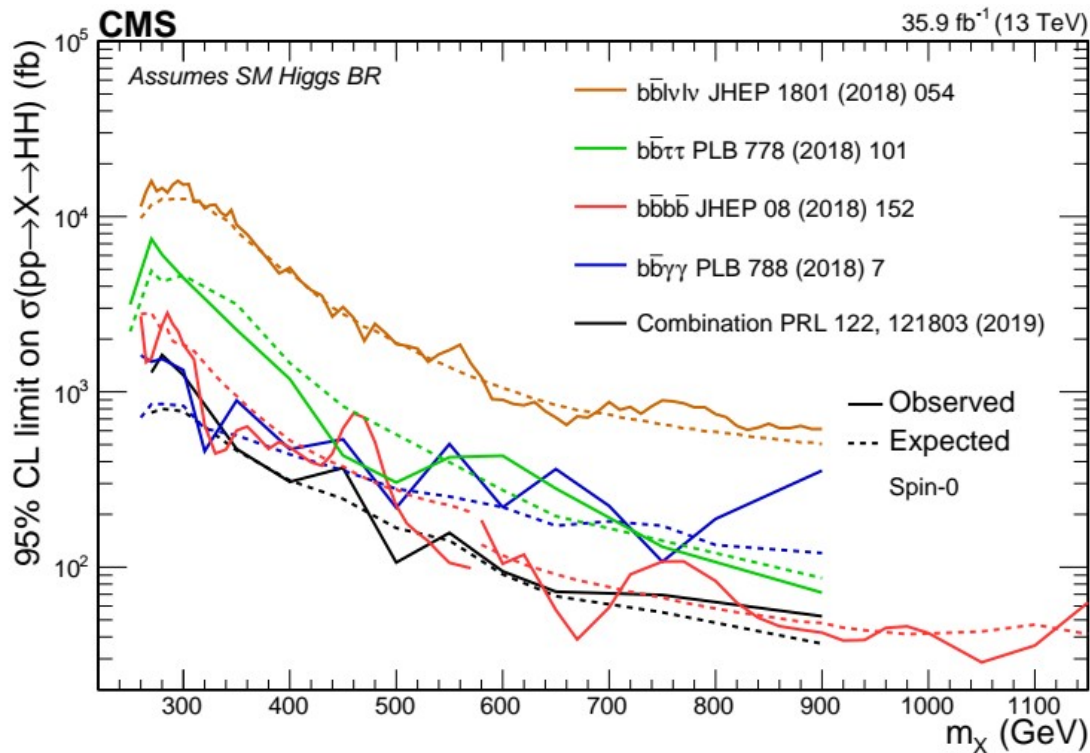
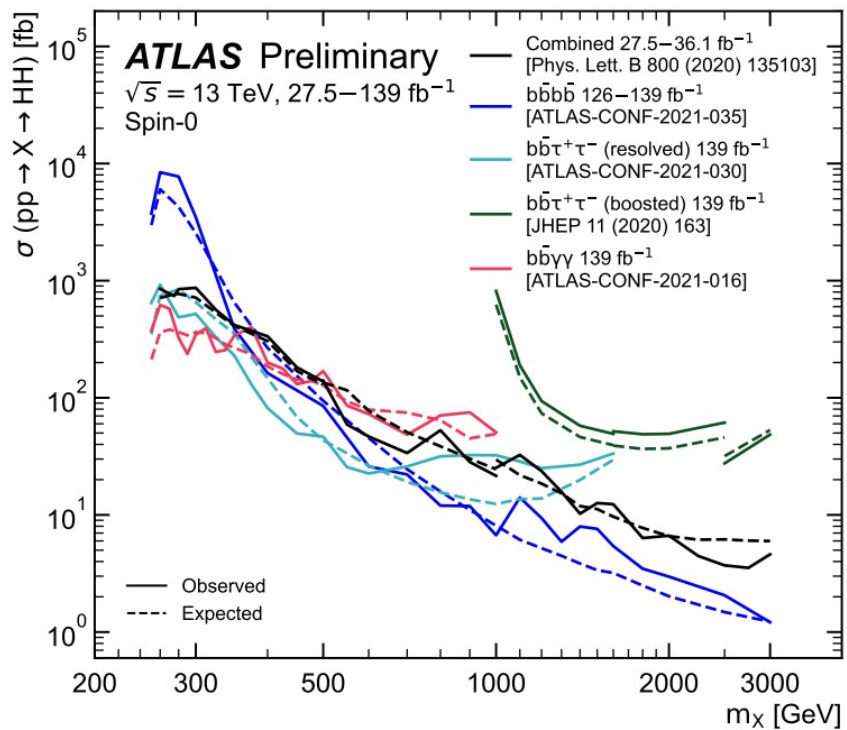
Higgs boson potential at colliders: Status and perspectives, Rev. Phys. 5 (2020) 100045

- From now on, will concentrate on $gg \rightarrow hh$.

Current Searches: Non-Resonant



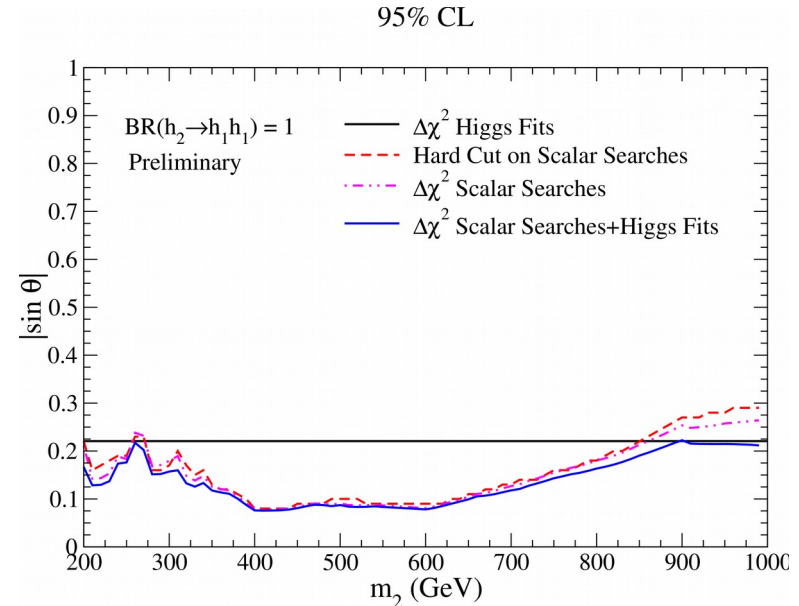
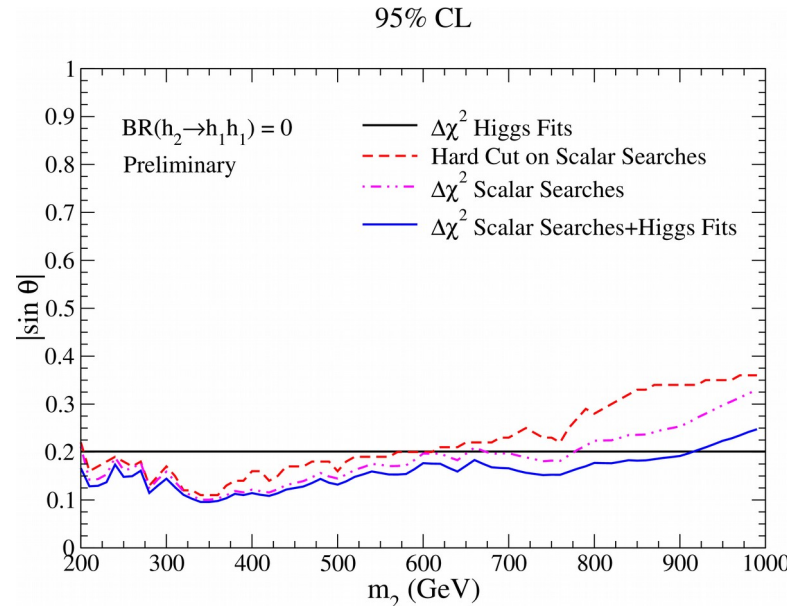
Current Searches: Resonance



Precision vs. Direct Searches

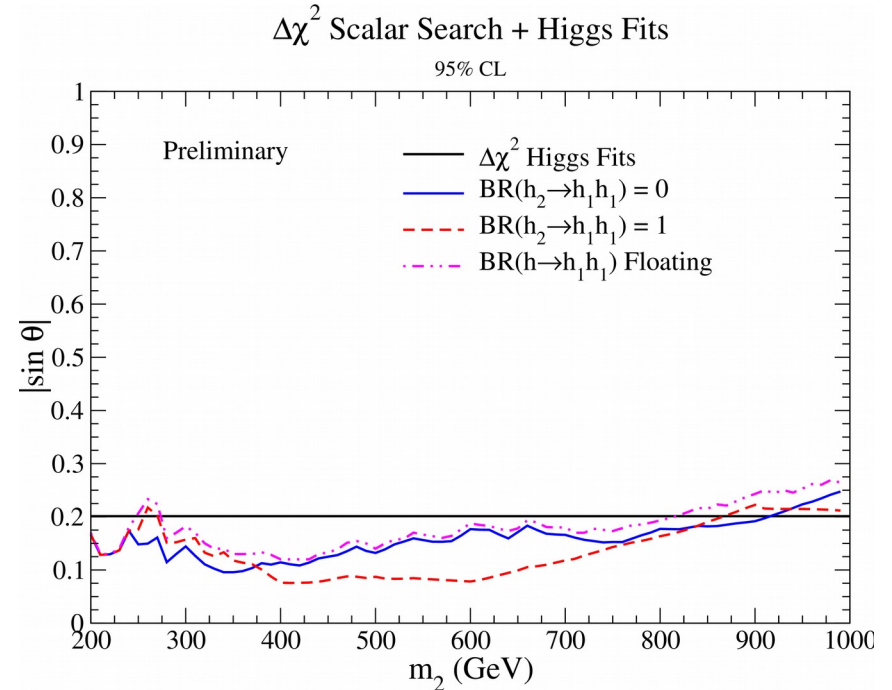
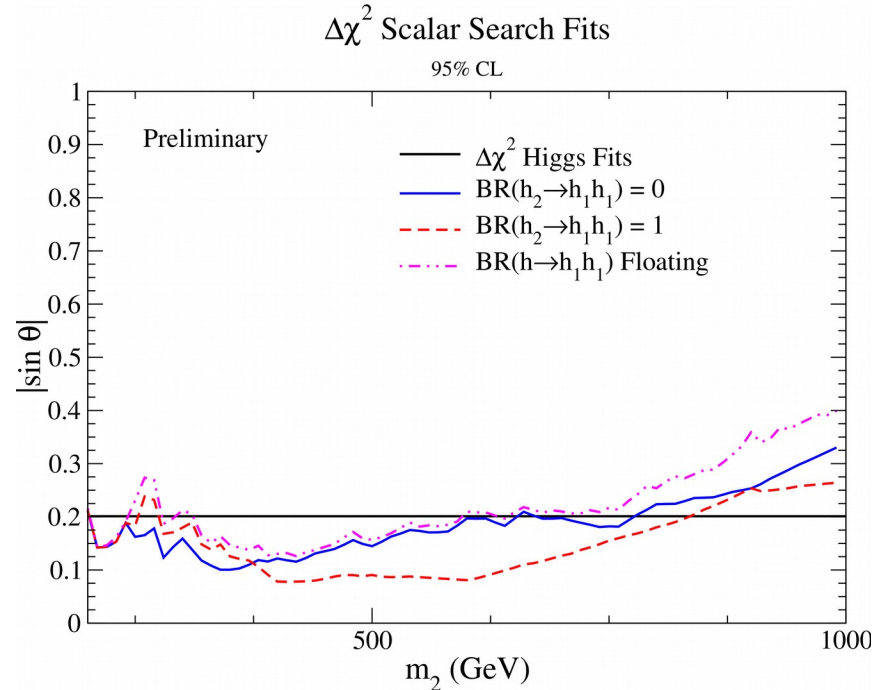
Singlet Model (No Z_2): Fits to data

- Compare fits including and not including Di-Higgs resonance searches.
- Including WW/ZZ/hh resonant searches.
- Hard cut: usual method of rejecting a point if it is excluded by any search.
- $\Delta\chi^2$: our proposed method for including searches in a χ^2 fit, see [Adhikari, IML, Sullivan, PRD 103 \(2021\) 075027](#)



Adhikari, Lane, IML, Sullivan, PRELIMINARY

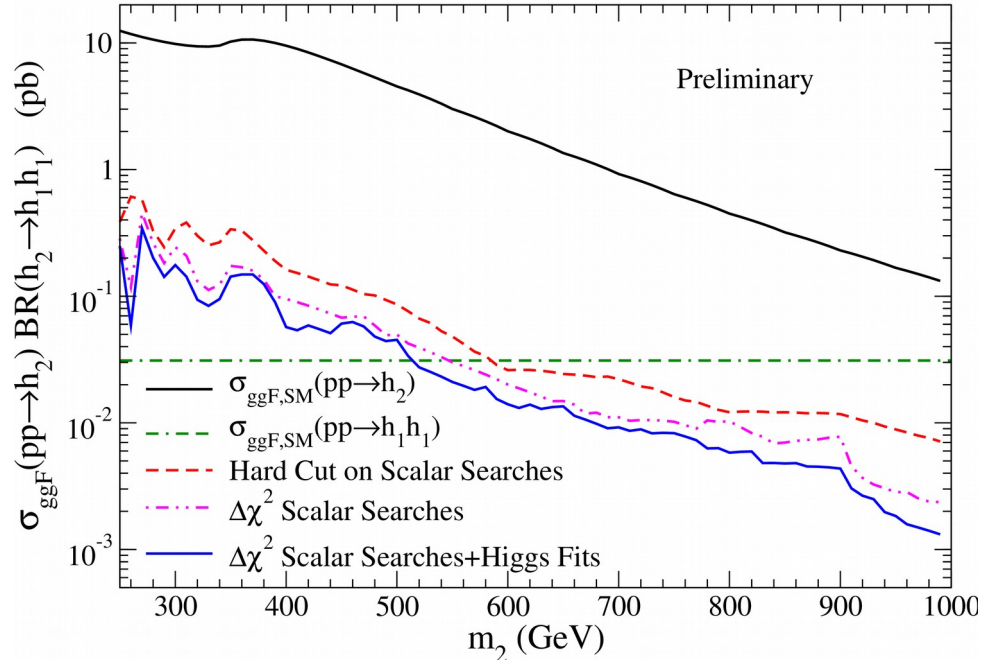
Singlet Model (No Z_2): Fits to data



- Comparing 0%, 100%, and floating Di-Higgs branching ratios.

Max Rates in Singlet Model

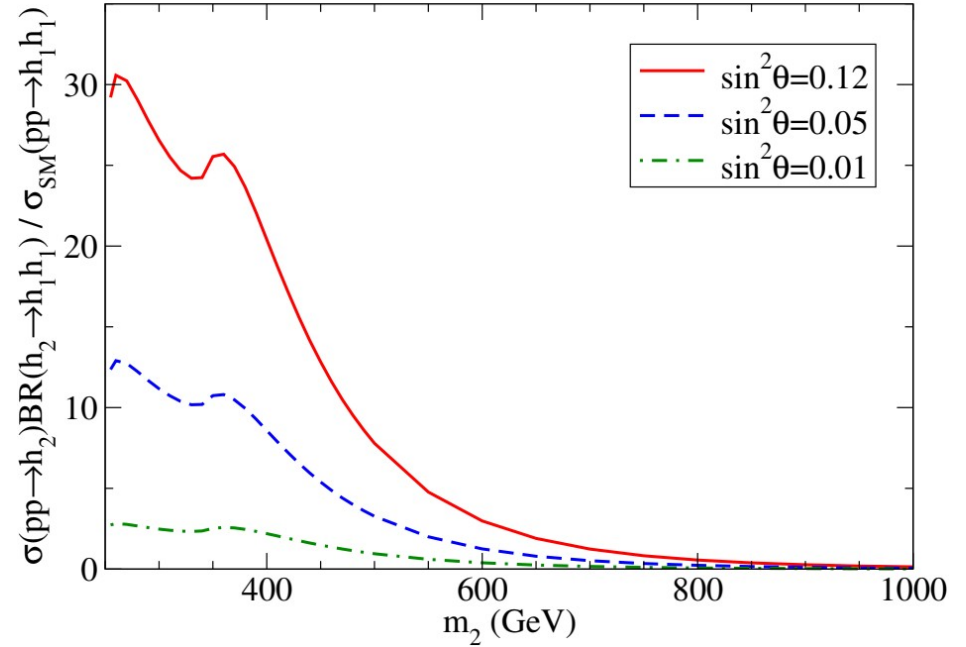
95% CL



Adhikari, Lane, IML, Sullivan, PRELIMINARY

- Current constraints

Double Higgs Production $\sin\theta$ Dependence at 13 TeV, $b_4=4.2$

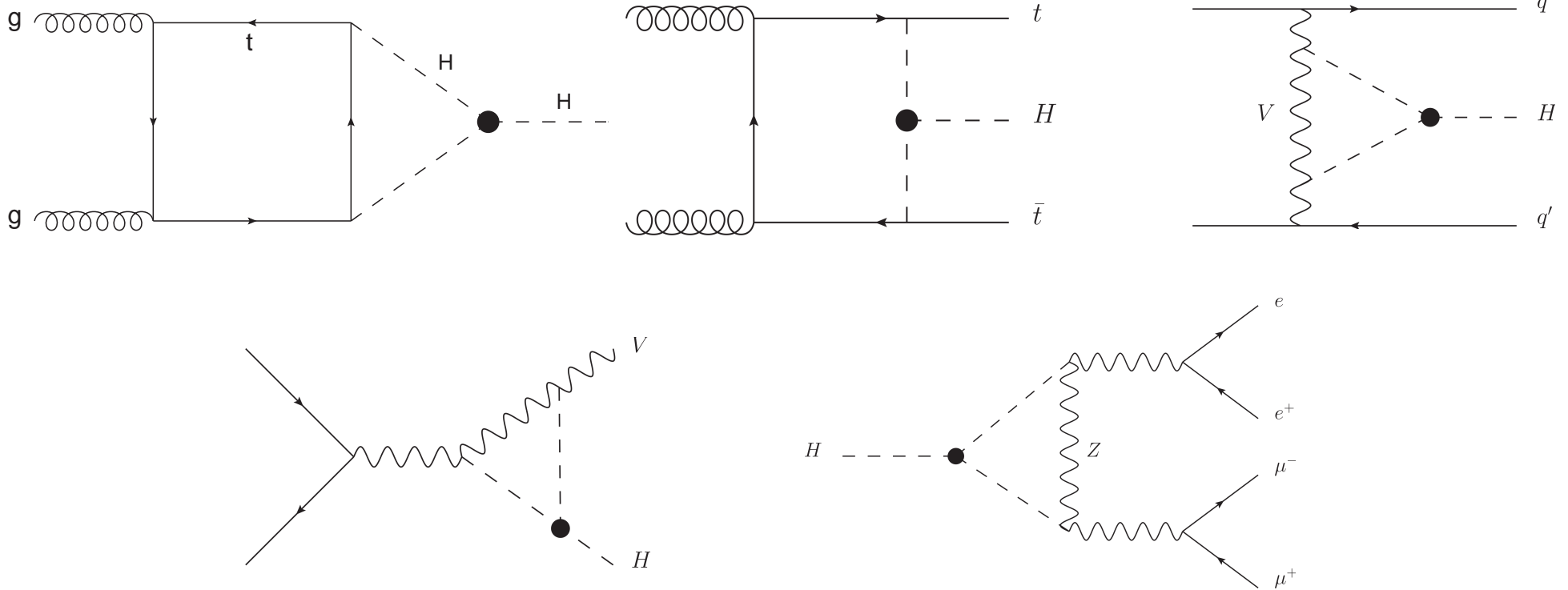


IML, Sullivan, PRD 96 (2017) 035037

See also Robens, Stefaniak, EPJC 76 (2016) 268

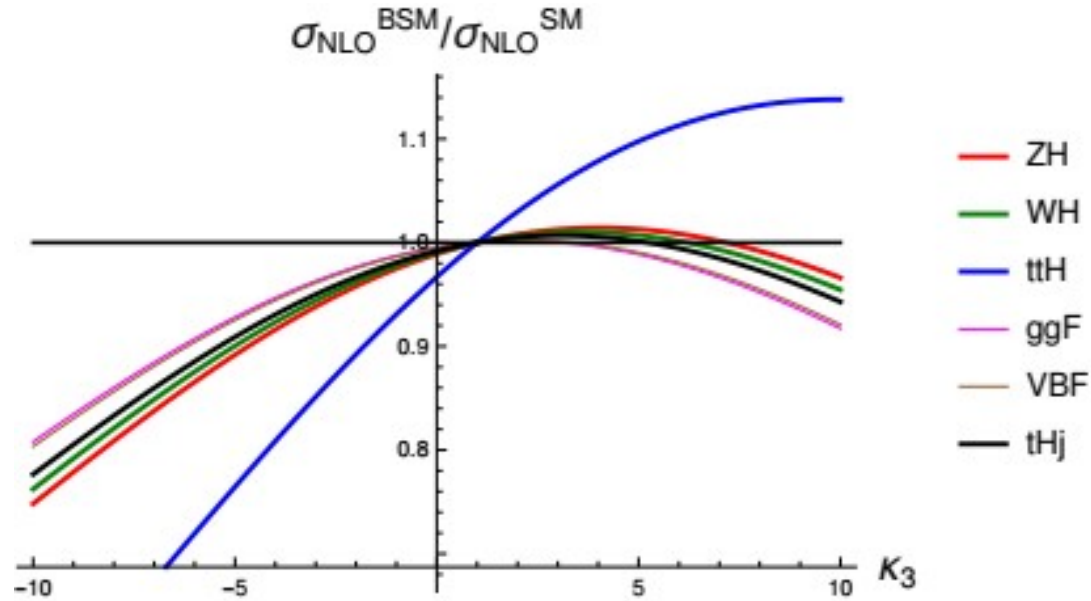
- Maximum allowed rates

Trilinear: Indirect



- Trilinear Higgs boson coupling can also appear in single Higgs production and decay at loop level. [McCullough 2014](#); [Gorbah, Haisch, 2016](#); [Degrassi Guardinio, Maltoni, Pagain, 2016](#); [Bizon, Gorbahn, Haisch, Zanderighi, 2016](#); [Di Vita, Grojean, Panico, Rimbau, Vantalón, 2017](#); [Maltoni, Pagani, Shivaji, Zhao, 2018](#)

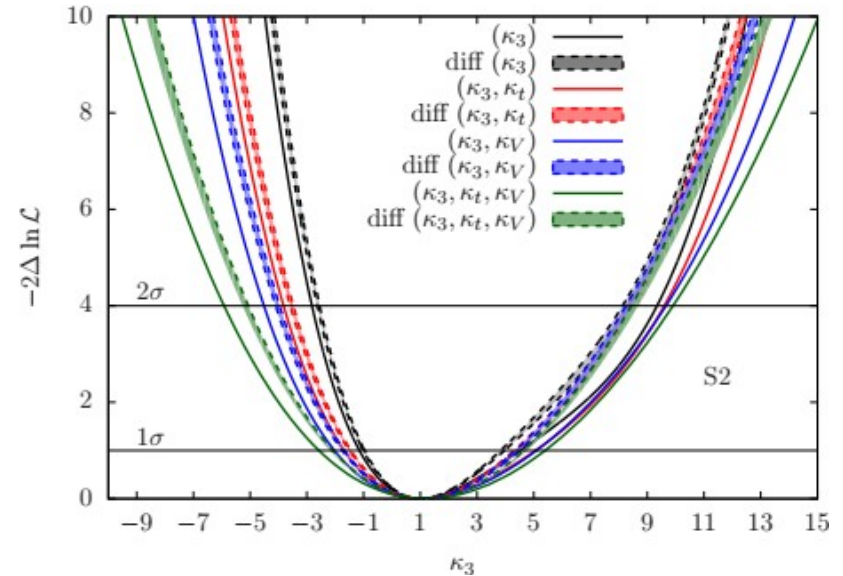
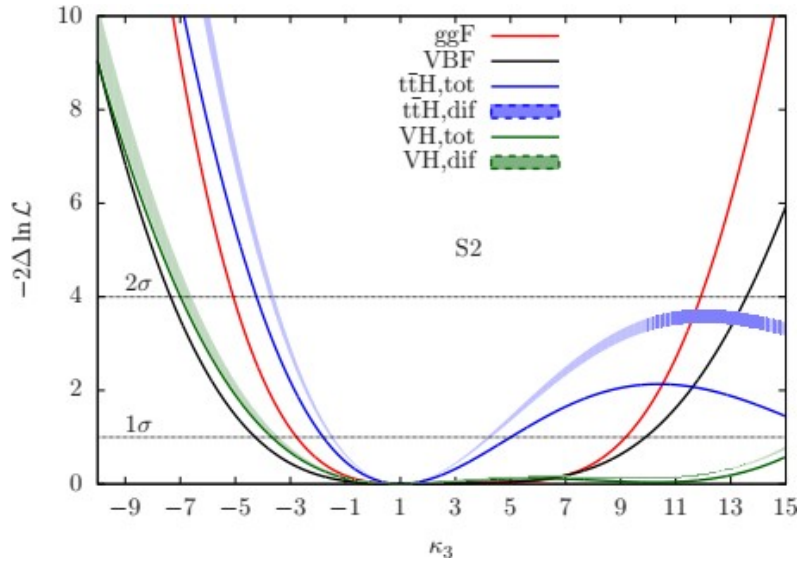
Trilinear in Loops



Maltoni, Pagani, Shivaji, Zhao, EPJC 77 (2017) 887

- Effects of anomalous trilinear Higgs couplings in production and decay.

Loop Level Trilinear



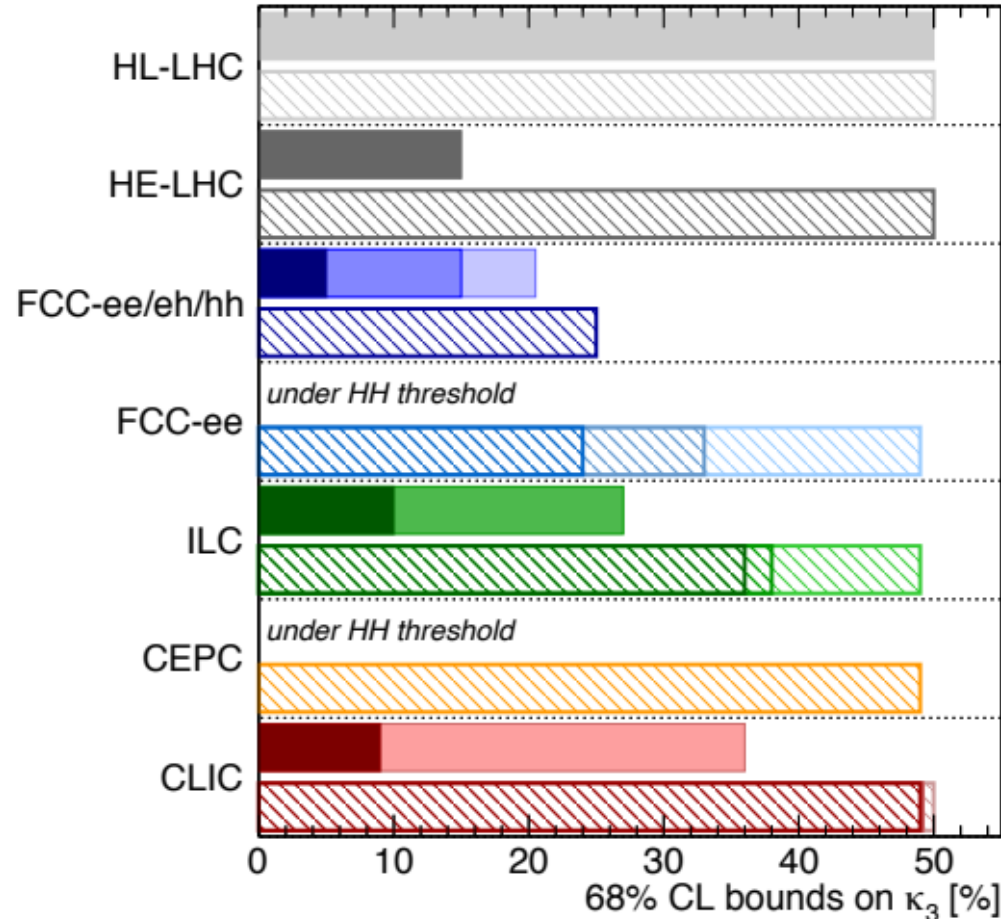
Maltoni, Pagani, Shivaji, Zhao, EPJC 77 (2017) 887

- HL-LHC projections
- Including systematic and theory uncertainties
- κ_3 expectations from direct searches at HL-LHC:
 - 1σ : 0.5-1.4

Single Production vs. Double Production: Future Colliders

- Direct: Solid
- Indirect: hashed
- Paranthesis: one parameter fit

Higgs boson potential at colliders:
 Status and perspectives,
 Rev. Phys. 5 (2020) 100045



Higgs@FC WG November 2019

di-Higgs	single-Higgs
HL-LHC 50%	HL-LHC 50% (47%)
HE-LHC [10-20]%	HE-LHC 50% (40%)
FCC-ee/eh/hh 5%	FCC-ee/eh/hh 25% (18%)
LE-FCC 15%	LE-FCC n.a.
FCC-eh ₃₅₀₀ -17+24%	FCC-eh ₃₅₀₀ n.a.
	FCC-ee ₃₆₅ ^{4IP} 24% (14%)
	FCC-ee ₃₆₅ 33% (19%)
	FCC-ee ₂₄₀ 49% (19%)
ILC ₁₀₀₀ 10%	ILC ₁₀₀₀ 36% (25%)
ILC ₅₀₀ 27%	ILC ₅₀₀ 38% (27%)
	ILC ₂₅₀ 49% (29%)
	CEPC 49% (17%)
CLIC ₃₀₀₀ -7%+11%	CLIC ₃₀₀₀ 49% (35%)
CLIC ₁₅₀₀ 36%	CLIC ₁₅₀₀ 49% (41%)
	CLIC ₃₈₀ 50% (46%)

All future colliders combined with HL-LHC

Trilinear from Models

- In SMEFT, have operators $\frac{C_{\square}}{\Lambda^2}(\Phi^\dagger\Phi)\square(\Phi^\dagger\Phi) + \frac{C_{\phi}}{\Lambda^2}(\Phi^\dagger\Phi)^3$
- This give an anomalous trilinear Higgs coupling:

$$\kappa_3 = \frac{\lambda_3}{\lambda_3^{\text{SM}}} = 1 - \frac{v^2}{\Lambda^2} (C_{\phi} - 3 C_{\square})$$

- If we integrate out heavy fields, can match onto that operator (small mixing limit)

Dawson, Murphy, PRD 96 (2017) 015041; Dawson, Homiller, Lane, PRD 102 (2020) 055012

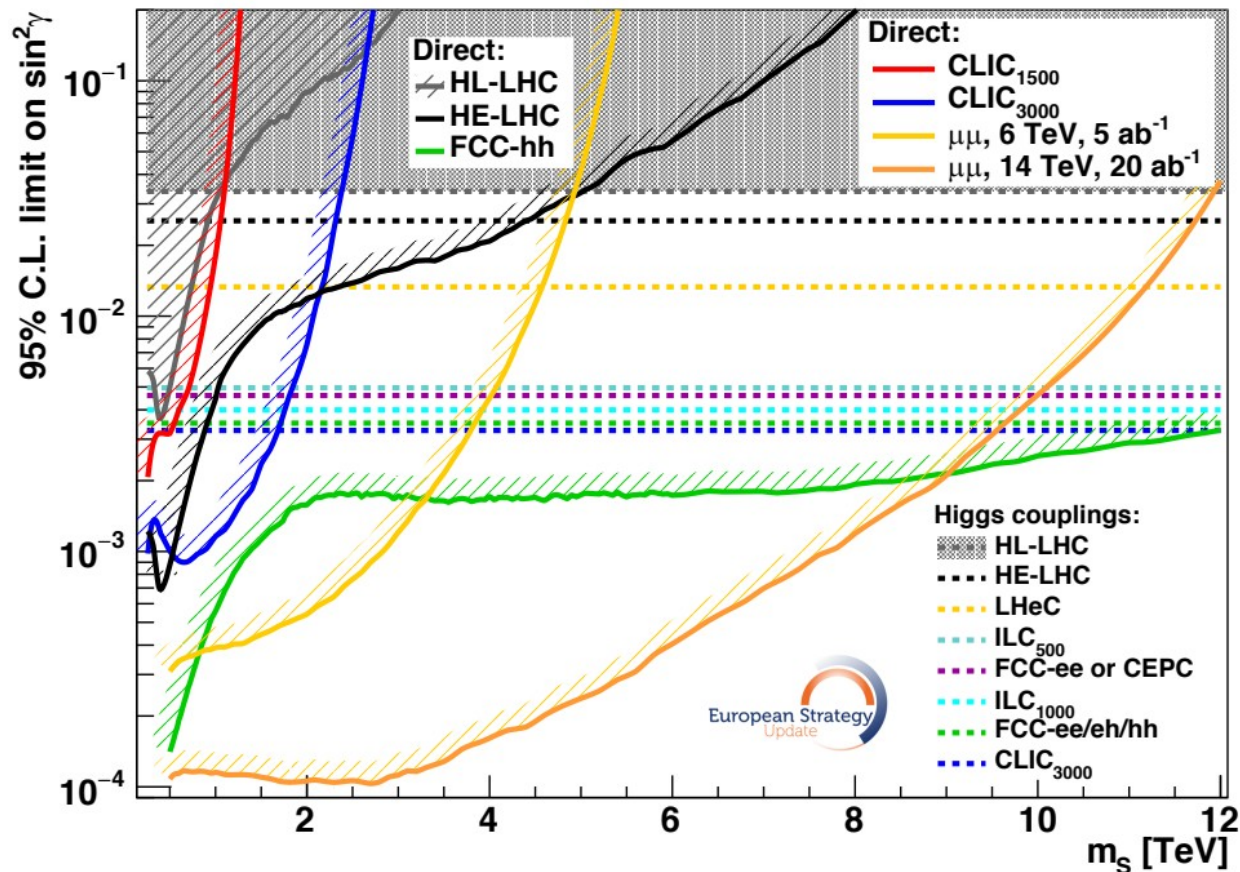
- Singlet model: $\frac{v^2}{\Lambda^2} C_{\square} = -\frac{1}{2} \tan^2 \theta$ $C_{\phi} = -C_{\square} \left(\tan \theta \frac{m}{2v} - \kappa \right)$

- 2HDM: $\frac{v^2}{\Lambda^2} C_{\phi} = \frac{\cos^2(\beta - \alpha) M^2}{v^2}$

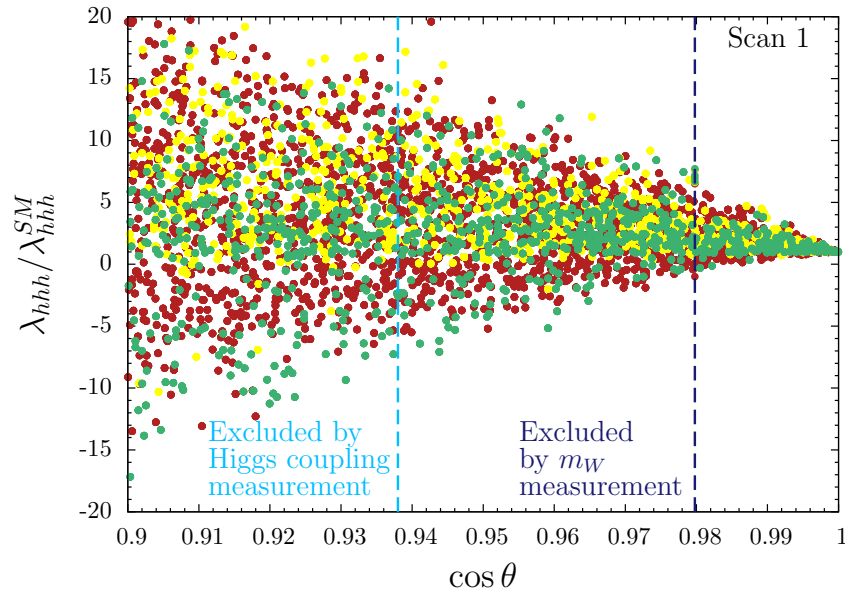
- M is the common mass of the heavy Higgs doublet, m is a Lagrangian mass parameter, κ depends on quartics and mass parameters.

Singlet Constraints from single parameter Trilinear fits

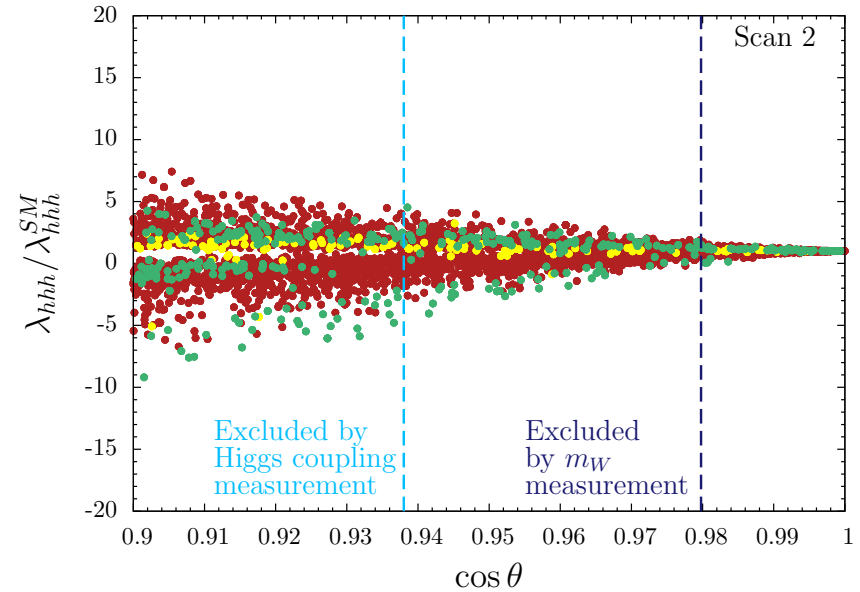
- ILC 240:
 - Single H: $\sin^2 \theta \lesssim 0.2 - 0.25$
- ILC-500:
 - Single/Double H: $\sin^2 \theta \lesssim 0.19 - 0.24$
- FCC-ee 250:
 - Single H: $\sin^2 \theta \lesssim 0.14 - 0.18$
- FCC-ee/eh/hh:
 - Single H: $\sin^2 \theta \lesssim 0.14 - 0.17$
 - Double H: $\sin^2 \theta \lesssim 0.04 - 0.05$
- Current precision Higgs:
 - $\sin^2 \theta \lesssim 0.04$



How big can trilinear get in Singlet Model?



Strongly Coupled



Weakly Coupled

Di Luzio, Grober, Spannowsky EPJC 77 (2017) 788

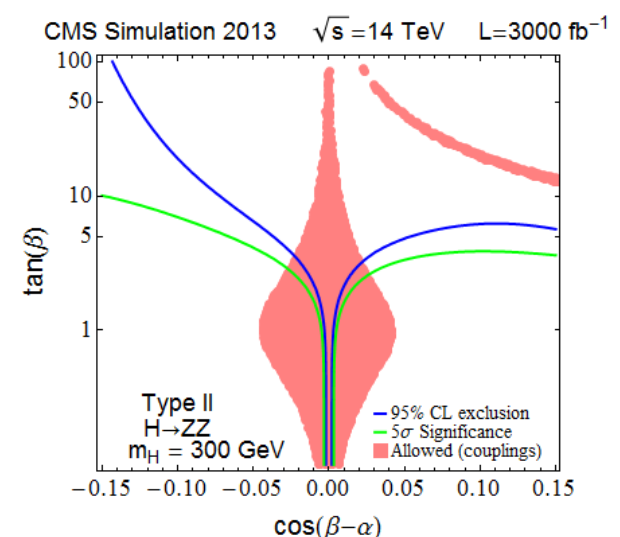
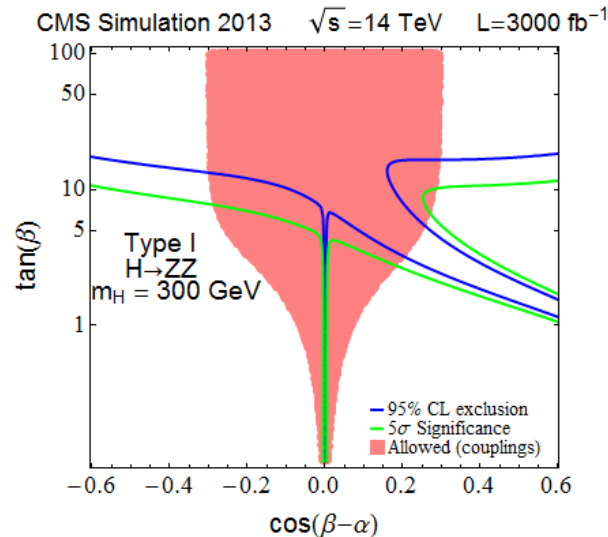
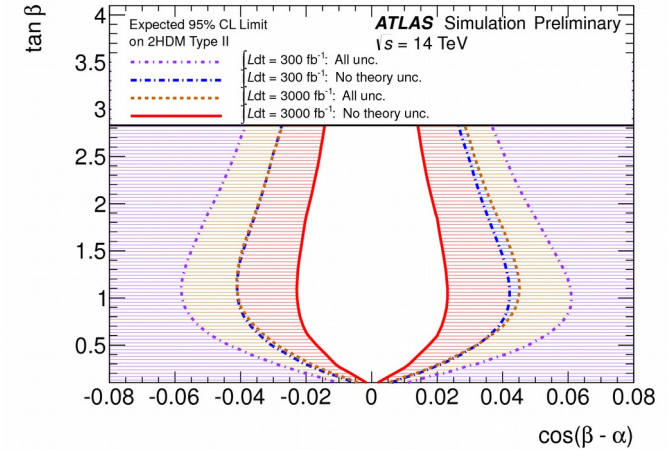
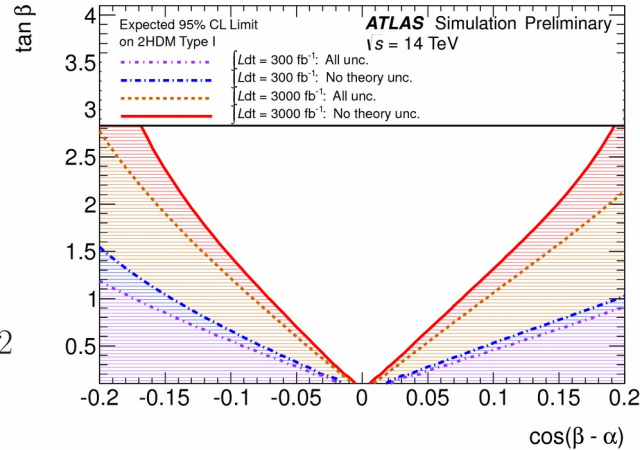
- Current Higgs precision limit: $\cos \theta > 0.98$
- Assumed mass about 800 GeV.
- Can still have a variation by a factor of two.

2HDM: HL-LHC Precision Measurements

- Variation of trilinear is small unless there are large decoupling effects.
- Due to mixing angle being small from precision measurements.

$$\kappa_3 = 1 + 0.17 \left(\frac{\cos(\beta - \alpha)}{0.1} \right)^2 \left(\frac{M}{\text{TeV}} \right)^2$$

- Would expect HL-LHC to see resonance before variation in trilinear gauge coupling.
- HL-LHC expected to have ~50% measurement of trilinear coupling.
- CEPC and FCC-ee can put 95% CL limit on the variation up to 17-19%

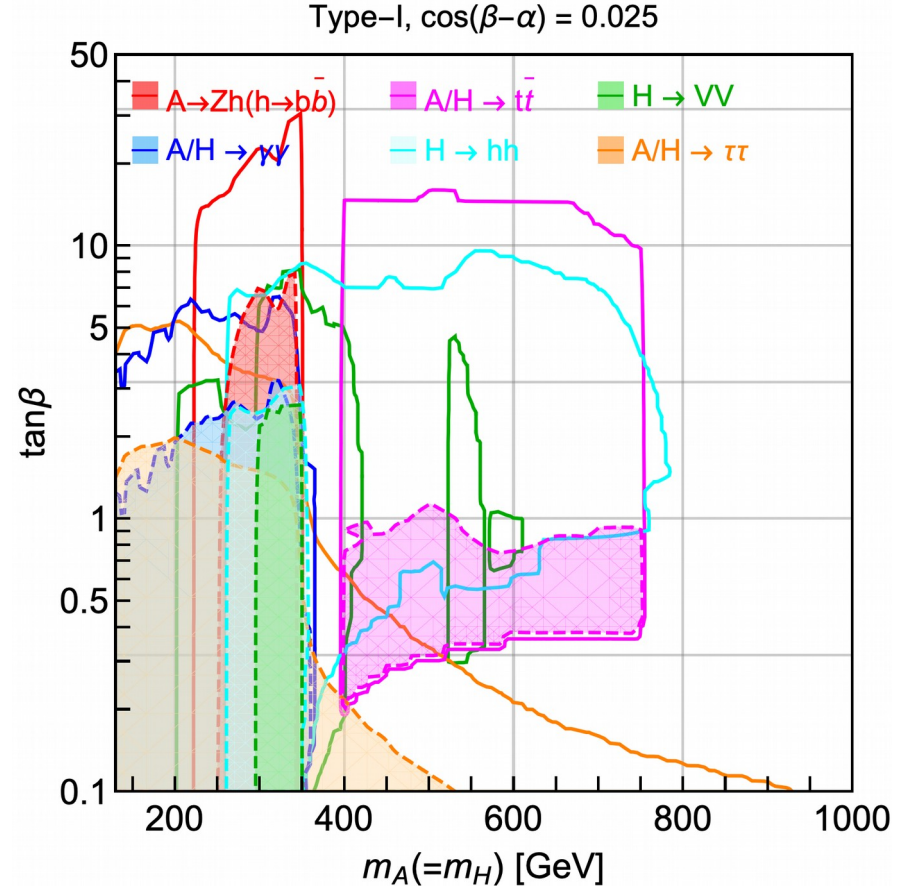


2HDM Type I: HL-LHC

- Solid: HL-LHC
- At $\cos(\beta - \alpha) = 0.025$ the trilinear variation is

$$\kappa_3 = 1 - 0.01 \left(\frac{M}{\text{TeV}} \right)^2$$

- Sensitive to direct detection before variations in anomalous trilinear Higgs coupling.

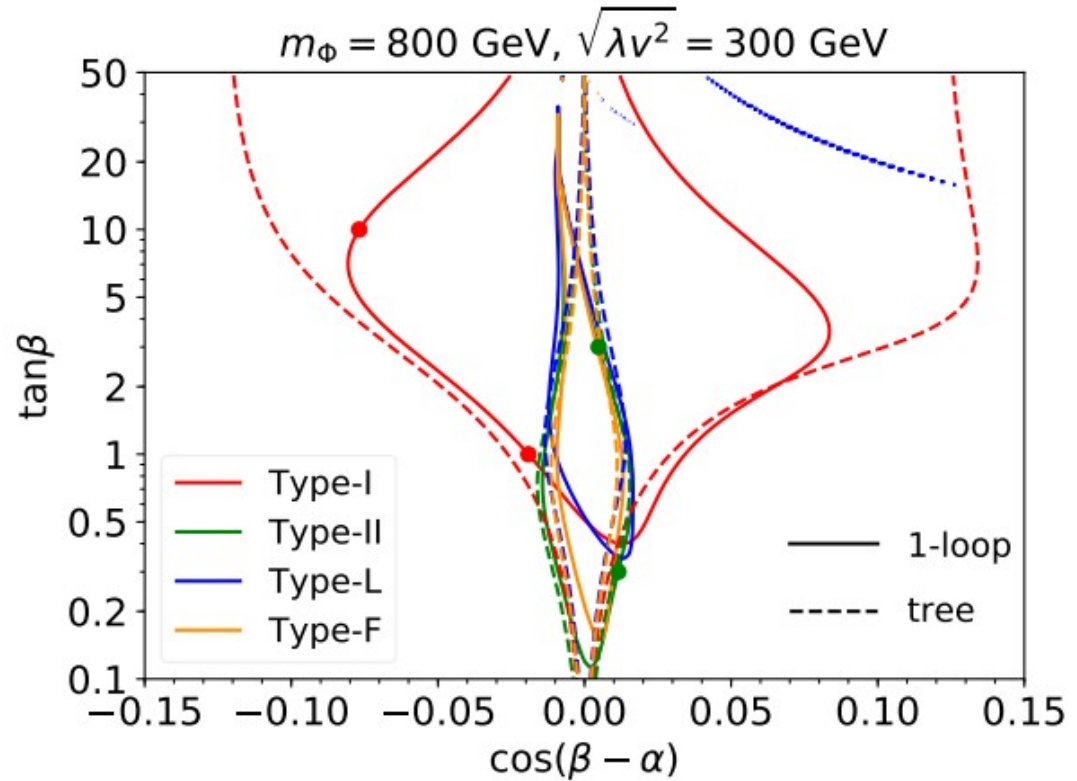


2HDM: CEPC Precision Measurements

- 5 sigma discovery regions
- Can measure triple Higgs coupling indirectly to 17% at CEPC.
- At a mass of 800 GeV, this translates to

$$|\cos(\beta - \alpha)| \lesssim 0.13$$

- Precision Higgs measurements more sensitive.
- Note: parameter point on previous slide is just discoverable at CEPC, depending on $\tan \beta$



2HDM Benchmarks for Resonant Di-Higgs

- Type-I
- $\text{Cos}(\beta-\alpha)=0.11$

m_{H_1} [GeV]	m_{H_2} [GeV]	m_A [GeV]	m_{H^\pm} [GeV]	α	$\tan\beta$	m_{12}^2 [GeV ²]
125.09	263	622	626	-0.285	2.371	25922
$\lambda_{3H_1}/\lambda_{3H}$	$y_{t,H_1}/y_{t,H}$	$\sigma_{H_1}^{\text{NNLO}}$ [pb]	$\sigma_{H_2}^{\text{NNLO}}$ [pb]	σ_A^{NNLO} [pb]		
0.909	1.042	53.45	1.26	0.55		

$$\begin{aligned} \text{BR}(H_2 \rightarrow H_1 H_1) &= 0.504, & \text{BR}(H_2 \rightarrow WW) &= 0.342, & \text{BR}(H_2 \rightarrow ZZ) &= 0.147 \\ \text{BR}(A \rightarrow ZH_2) &= 0.865, & \text{BR}(A \rightarrow t\bar{t}) &= 0.116, & & \\ \text{BR}(H^\pm \rightarrow W^\pm H_2) &= 0.874, & \text{BR}(H^+ \rightarrow t\bar{b}) &= 0.107, & & \\ & & \sigma_{H_2}^{\text{NNLO}} \times \text{BR}(H_2 \rightarrow H_1 H_1) &= 635 \text{ fb} & & \end{aligned}$$

- Type-II
- $\text{Cos}(\beta-\alpha)=-0.027$

m_{H_1} [GeV]	m_{H_2} [GeV]	m_A [GeV]	m_{H^\pm} [GeV]	α	$\tan\beta$	m_{12}^2 [GeV ²]
125.09	528	798	809	-0.695	1.268	130388
$\lambda_{3H_1}/\lambda_{3H}$	$y_{t,H_1}/y_{t,H}$	$\sigma_{H_1}^{\text{NNLO}}$ [pb]	$\sigma_{H_2}^{\text{NNLO}}$ [pb]	σ_A^{NNLO} [pb]		
0.974	0.978	47.02	2.84	0.47		

$$\begin{aligned} \text{BR}(H_2 \rightarrow H_1 H_1) &= 0.012, & \text{BR}(H_2 \rightarrow t\bar{t}) &= 0.979, \\ \text{BR}(A \rightarrow ZH_2) &= 0.514, & \text{BR}(A \rightarrow t\bar{t}) &= 0.482, \\ \text{BR}(H^\pm \rightarrow W^\pm H_2) &= 0.560, & \text{BR}(H^+ \rightarrow t\bar{b}) &= 0.437. \\ & & \sigma_{H_2}^{\text{NNLO}} \times \text{BR}(H_2 \rightarrow H_1 H_1) &= 34 \text{ fb} \end{aligned}$$

Maximize resonant production rate

“Nightmare Scenario”

Resonant vs. Non-Resonant

- Immense amount of work on Di-Higgs resonances.
 - Pair production of SM Higgs and mixed states via resonance: hh, hS, SS
- What about non-resonant production?
 - Case study: singlet model with no Z_2
 - Indeed, there is a diagram that can produce SS that does not decouple in the zero mixing limit.
 - So-called “nightmare-scenario” [Curtin, Meade, Yu, JHEP 11 \(2014\) 127](#)
 - However, if Z_2 is broken or no Z_2 , mixing angle does not have to be precisely zero.
 - Then new heavy scalars can decay and give visible signatures.
 - Will have little to no evidence in SM Higgs decays or double SM Higgs production.

Zero Mixing Limit

- Couplings between scalar and Higgs:

$$V(h, S) = \frac{a_1}{4}(h + v)^2 S + \frac{a_2}{4}(h + v)^2 S^2$$

- Source of Higgs-scalar mixing is:

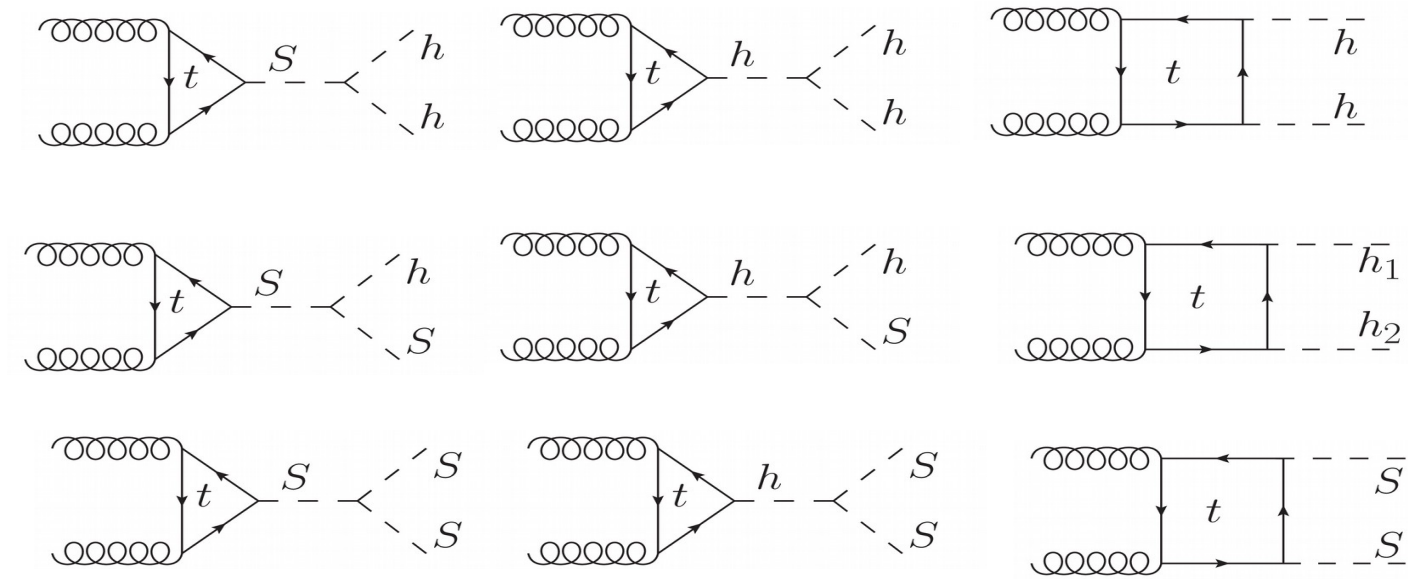
$$V(h, S) \supset \frac{a_1 v}{2} h S$$

- In the limit of zero mixing $a_1 \rightarrow 0$ and only a_2 survives

$$V(h, S) \rightarrow \frac{a_2}{4}(h + v)^2 S^2 = \frac{a_2 v^2}{4} S^2 + \frac{a_2 v}{2} h S^2 + \frac{a_2}{4} h^2 S^2$$

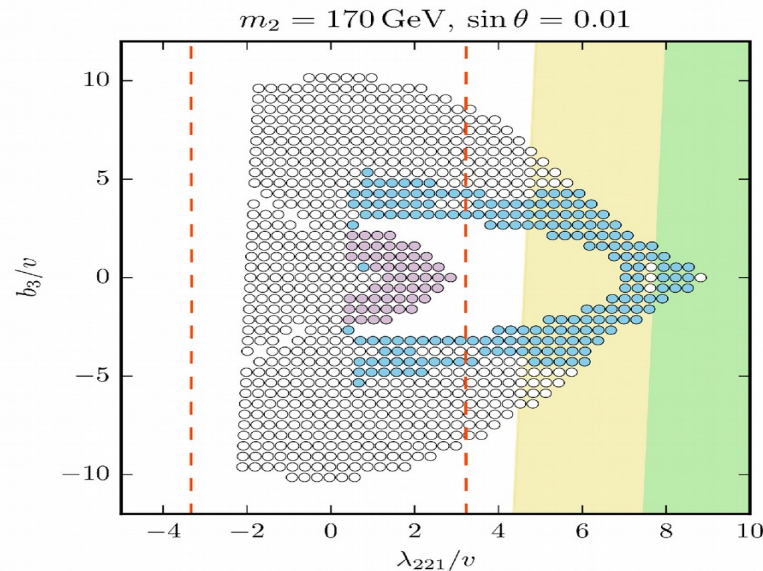
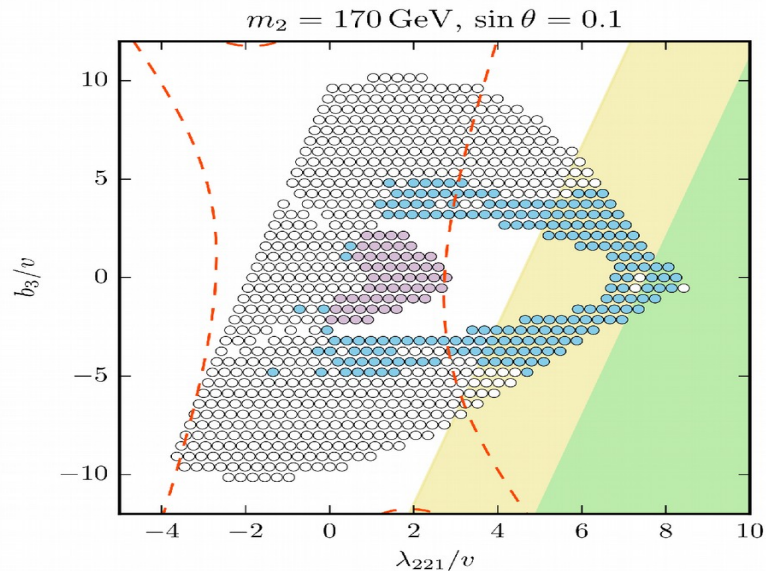
- If the scalar S does not mix with the Standard Model Higgs, it only couples to the Higgs. Very difficult to produce and can be stable.
- a_2 is the only term to drive the first order phase transition.
 - Lower limit on how large it can be.
 - Gives h-h-S-S and h-S-S couplings, and so we have a lower bound on these.

Non-Zero Mixing



- Many di-boson production modes, all with different information about the potential.
 - Can have resonant di-Higgs if allowed.
- SS production depends on h-S-S coupling.
 - This is the coupling that must stay non-zero to have a strong first order electroweak phase transition.

High Luminosity LHC

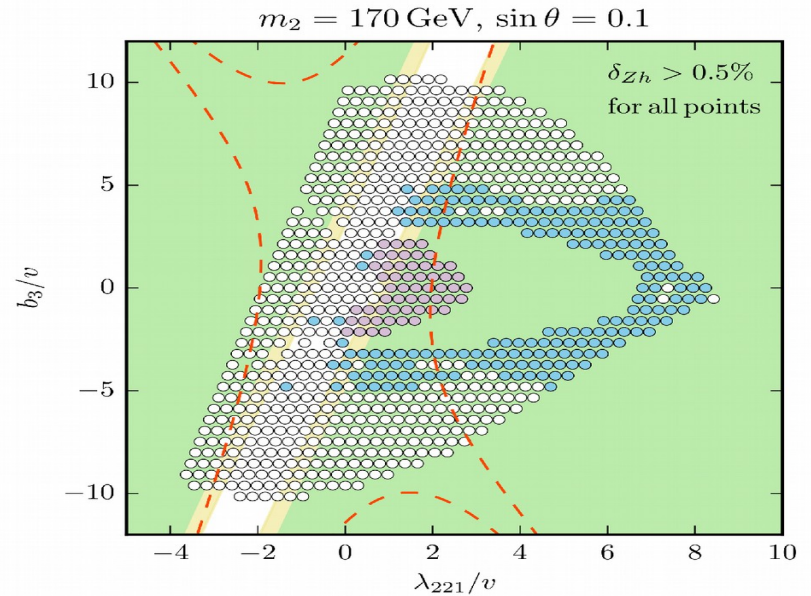
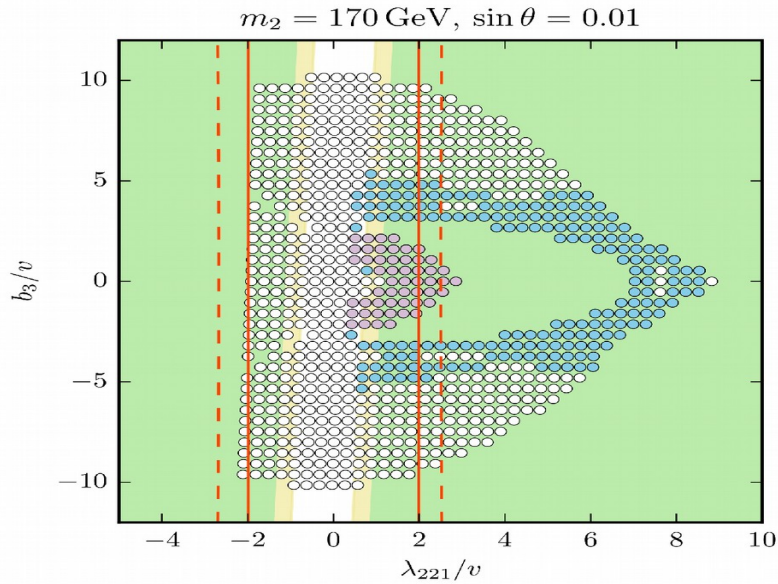


Chen, Kozaczuk, IML JHEP 1708 (2017) 096

- 3 ab^{-1} at 14 TeV LHC.
- Comparison of different methods of searching.
- Colored Dots: Compatible with strong first order electroweak phase transition.
- Searches for $h_2 h_2$ production: **Yellow: Exclusion**, **Green: Discovery**
- **Red dashed curves: Higgs self-coupling limits at 30%.**

$$pp \rightarrow h_2 h_2 \rightarrow 4W \rightarrow 2j2\ell^\pm \ell'^\mp 3\nu, \quad \ell \neq \ell'.$$

100 TeV



Chen, Kozaczuk, IML JHEP 1708 (2017) 096

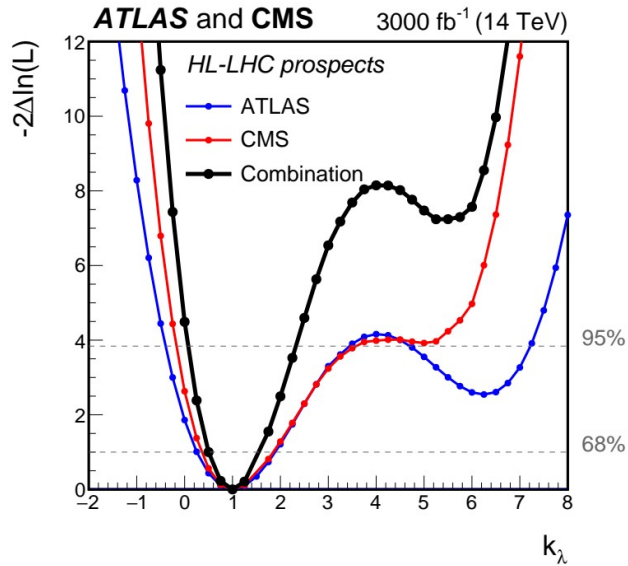
- 30 ab^{-1} at 100 TeV, can probe much of the parameter space.
- Colored Dots: Compatible with strong first order electroweak phase transition.
- Searches for $h_2 h_2$ production: Yellow: Exclusion, Green: Discovery
- Red dashed curves: Higgs self-coupling limits to 15%. Solid lines: Higgs-Z-boson coupling limits to 0.5%

$$pp \rightarrow h_2 h_2 \rightarrow 4W \rightarrow 2j2\ell^\pm \ell'^\mp 3\nu, \quad \ell \neq \ell'.$$

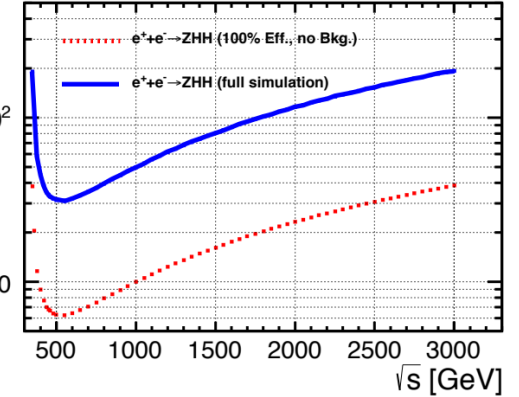
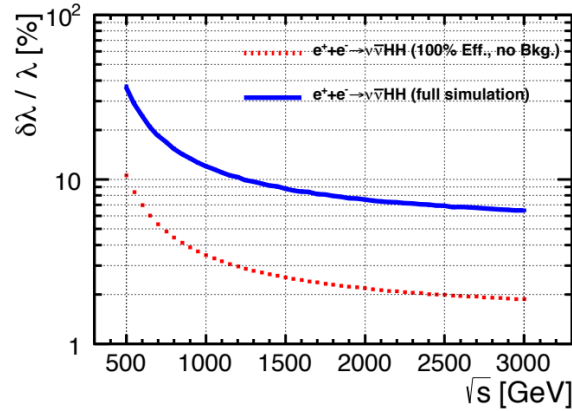
Conclusions

- Complementarity between precision Higgs and direct searches.
- Current double Higgs resonance searches do put meaningful constraints on models.
- Direct searches can be sensitive to regions precision Higgs is not.
 - Some production modes of double scalar do not decouple.
- Many topics not covered:
 - The aforementioned double scalar resonances: hS , SS
 - New particles in the loop.
 - Light quark Yukawas in double Higgs production. [Alasfar, Lopez, Grober JHEP 11 \(2019\) 088](#)

Di-Higgs Projections: Future Colliders



HL-LHC



ILC

	$b\bar{b}\gamma\gamma$	$b\bar{b}\tau^+\tau^-$	$b\bar{b}ZZ^* (4\ell)$	$b\bar{b}WW^* (2j\ell\nu)$	$b\bar{b}b\bar{b} + \text{jet}$
$\delta\kappa_\lambda$	6%	8%	14%	40%	30%

Table 10.4: Precision of the direct Higgs self-coupling measurement in $gg \rightarrow HH$ production at $\sqrt{s} = 100$ TeV with $\mathcal{L} = 30$ ab⁻¹ for various decay modes.

100 TeV pp

Thank You