

THEORY FRONTIER AND RARE AND PRECISION MEASUREMENTS

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Snowmas2021@Cincy, May 17 2022

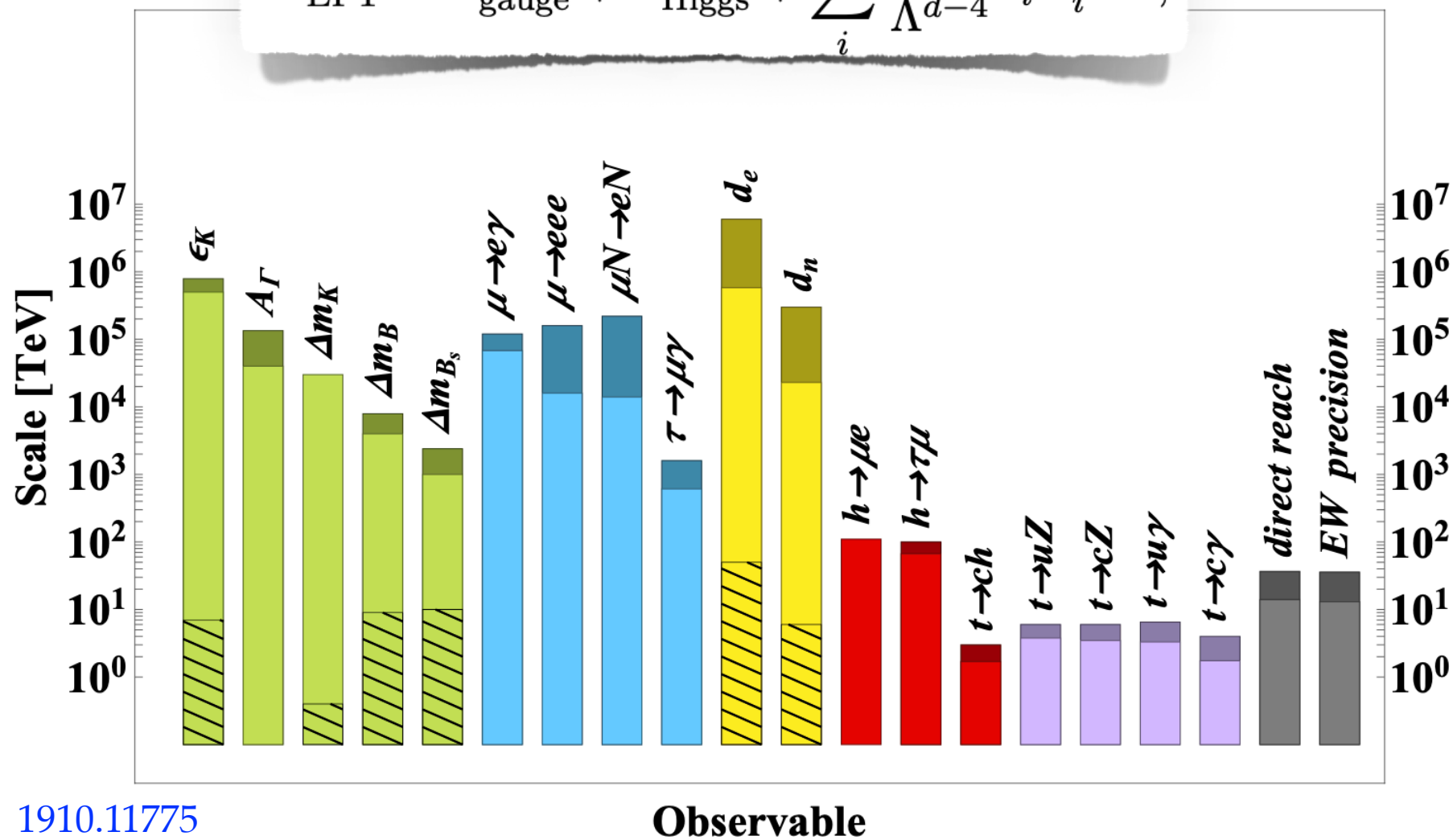
MAIN MESSAGES

- two obvious, yet important statements
 - theory is an essential input for experimental measurements
 - experimental results are essential inputs to theory considerations
- this talk: selected examples of the above interplay

FROM EXPERIMENTS TO PARADIGM SHIFTS

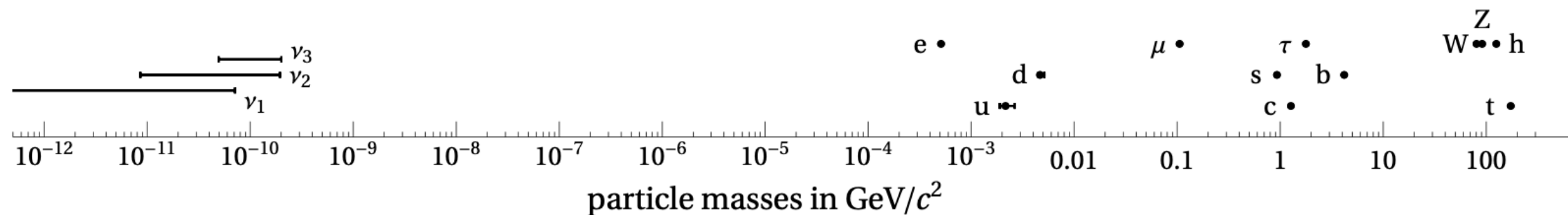
- experimental results can lead to qualitative jumps in theoretical understanding
 - $\delta_{\text{CKM}} \sim \mathcal{O}(1) \Rightarrow$ the strong CP problem, i.e., why $\bar{\theta} \lesssim 10^{-10}$, becomes even more striking
 - is the PMNS phase (and Majorana phases) also $\mathcal{O}(1)$?
- Higgs discovery \Rightarrow no hiding from the hierarchy problem
 - flavor constraints \Rightarrow NP flavor puzzle
 - even if one loop and MFV already being squeezed
 - do we simply live in a fine-tuned world?

$$\mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{gauge}}^{\text{SM}} + \mathcal{L}_{\text{Higgs}}^{\text{SM}} + \sum_i \frac{1}{\Lambda^{d-4}} c_i \mathcal{O}_i^{d>4},$$



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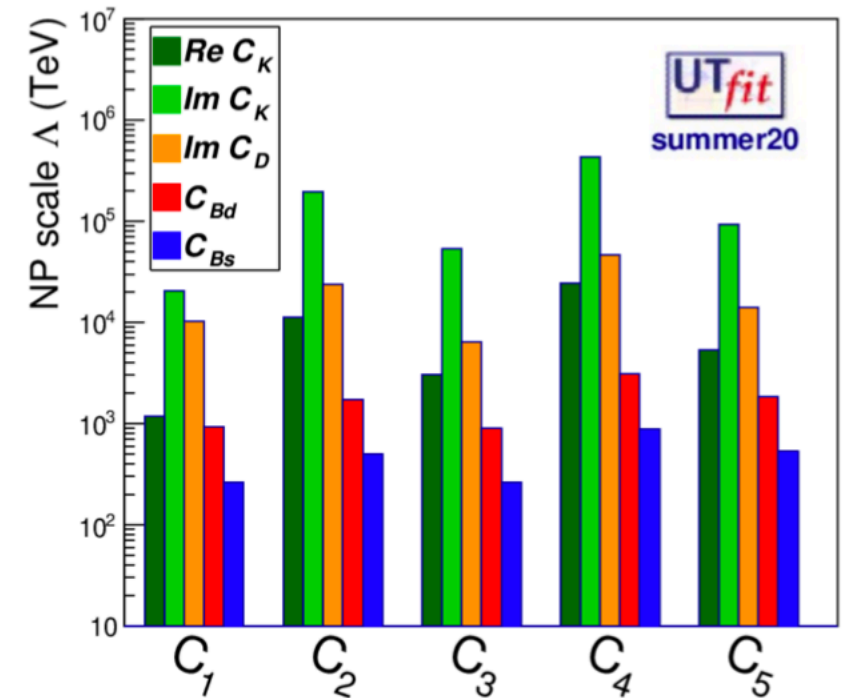
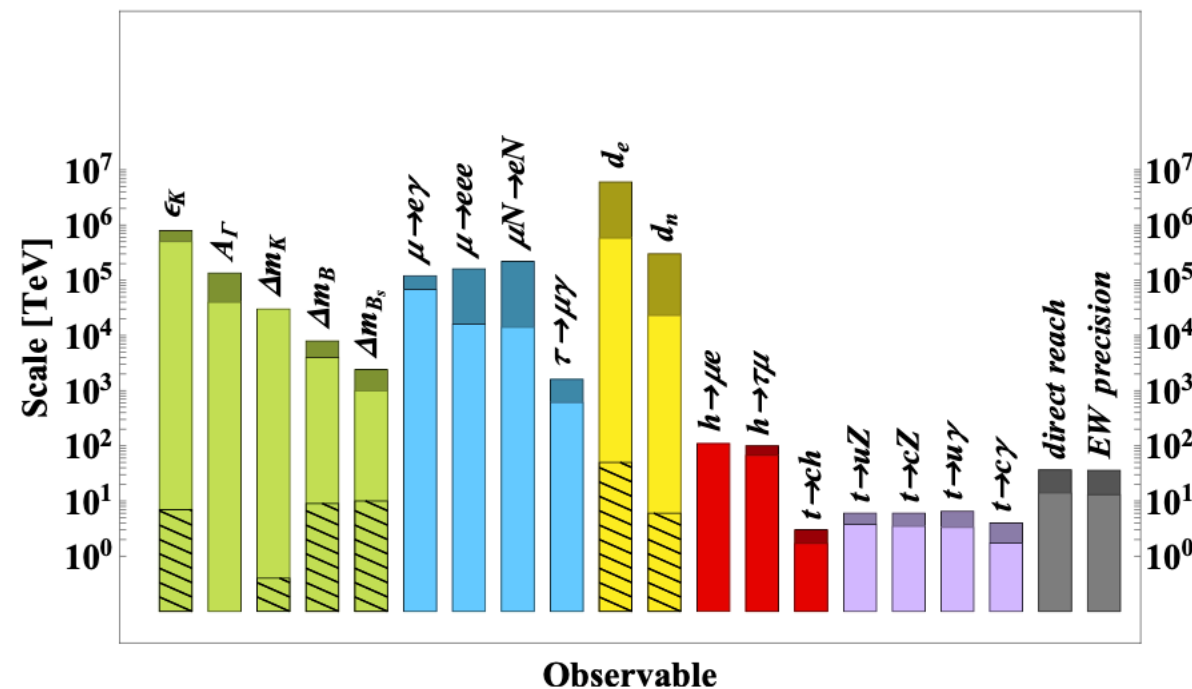
EXPLAINING THE SM HIERARCHIES



[Altmannshofer, JZ, 2203.07726](#)

- is there a dynamical explanation for the pattern of SM fermion masses and mixings?
- horizontal flavor symmetries
- warped extra dimensions
- partial compositeness

FLAVOR AS A NEW PHYSICS PROBE



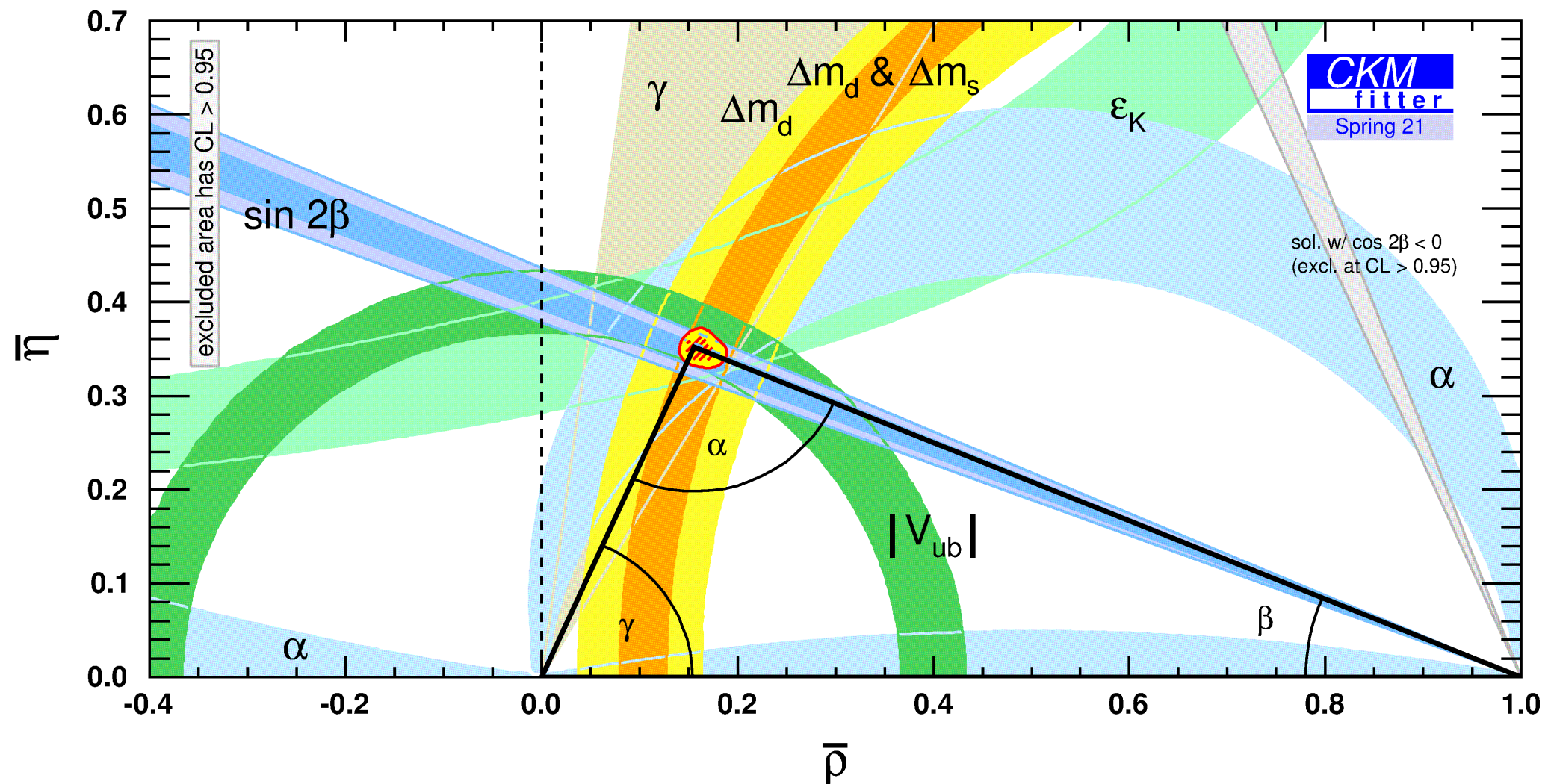
- assuming NP is heavy \Rightarrow SMEFT
- flavor observables probe very high scales
 - decoupling
 - Minimal Flavor Violation
 - hierarchical new physics flavor couplings

THEORY INPUT

- in many corners of flavor / precision physics theory input indispensable
 - quark flavor transitions involve hadrons / nonperturbative QCD
 - CKM unitarity triangle
 - prediction for $(g - 2)_\mu$ in the SM
 - $b \rightarrow c\tau\nu$ and $b \rightarrow s\mu\mu$ predictions
 - understanding the backgrounds
 - $\mu \rightarrow e$ conversion
 - interpretation of experimental results
 - flavor anomalies
 - motivating experimental searches
 - light new physics

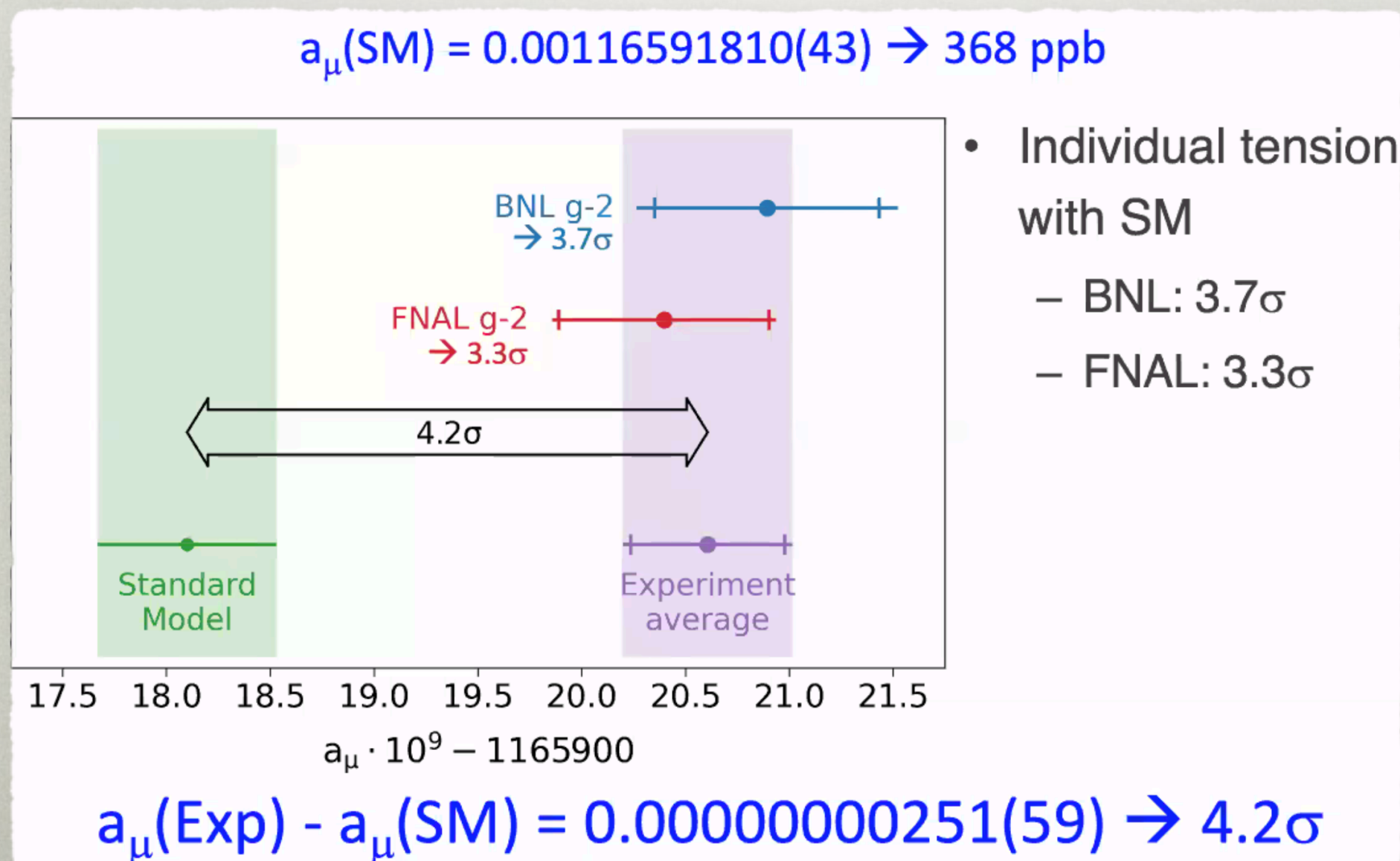
STANDARD CKM UNITARITY TRIANGLE

- every single constraint requires theory inputs or insights
 - lattice QCD, HQET, SCET, SU(2), perturbative QCD & electroweak corrections,...



PREDICTIONS FOR $(g - 2)_\mu$ IN THE SM

- searching for NP only if the SM prediction for $(g - 2)_\mu$ is understood
 - lattice QCD, dispersion relations

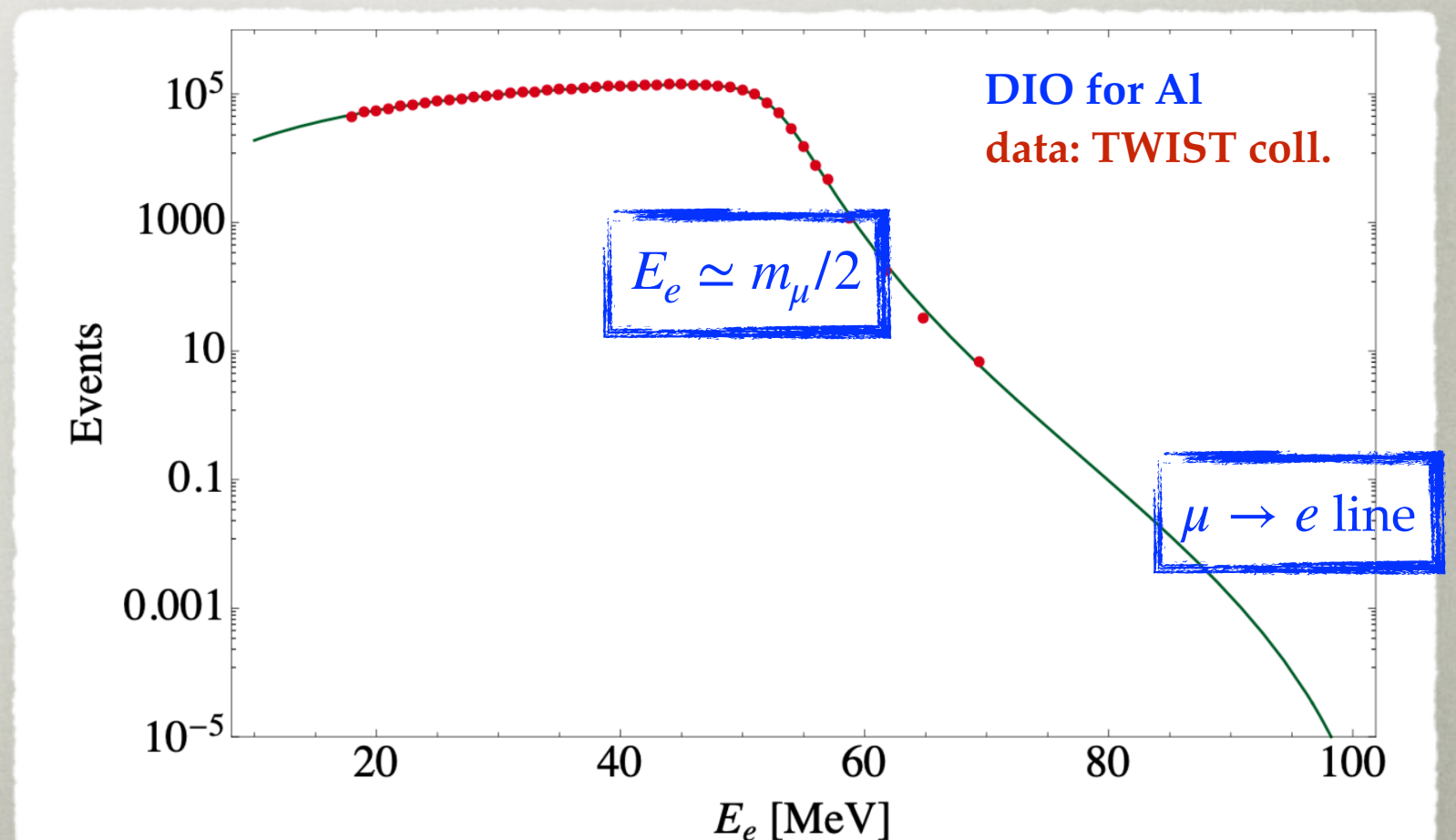
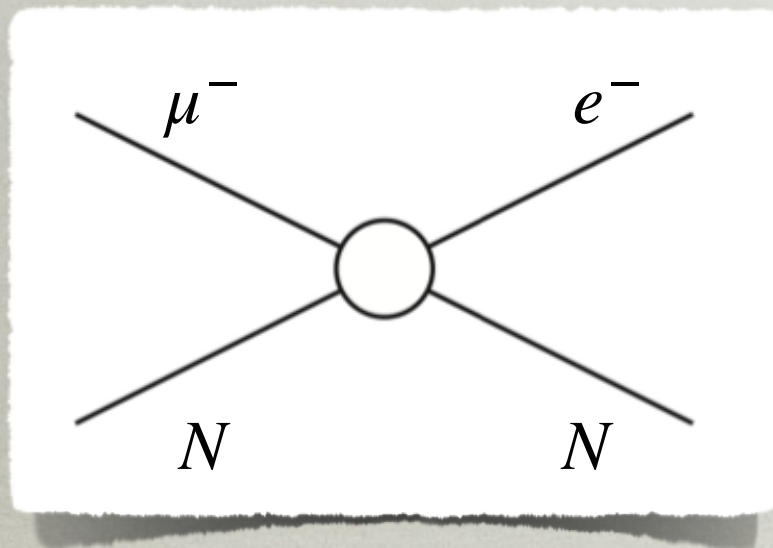


THEORY INPUTS FOR FLAVOR ANOMALIES

- $b \rightarrow c\tau\nu$ predictions: HQET, lattice QCD
- $b \rightarrow s\mu\mu$
 - the SM corrections to LFUV ratios
 - mass corrections, treatment of QED,...
 - predictions for branching ratios, angular observables

SM BACKGROUND IN $\mu \rightarrow e$ CONVERSION

- $\mu^- N \rightarrow e^- N$ conversion
 - the only intrinsic bckgd is $\mu^- \rightarrow e^- \nu_\mu \bar{\nu}_e$ decay in orbit
 - in $\mu^- N \rightarrow e^- N$ the e^- is at the kinematical edge of DIO
 - the SM prediction for it essential



INTERPRETATION OF EXPERIMENTAL RESULTS

- example: flavor anomalies point to leptoquarks
 - 3 options if a single LQ dominates in $b \rightarrow s\mu\mu$

Hiller, Nisandzic, 1704.05444

Scalar
LQ

label	representation	Wilson coefficient	Relation	$R_{K(*)}$
\tilde{S}_2	$(3, 2, 1/6)$	C_{BL}	$C'_9 = -C'_{10}$	$R_K < 1, R_{K^*} > 1$
S_3	$(\bar{3}, 3, 1/3)$	C_{LL}^{NP}	$C_9 = -C_{10}$	$R_K \simeq R_{K^*} < 1$
S_2	$(3, 2, 7/6)$	C_{LR}	$C_9 = C_{10}$	$R_K \simeq R_{K^*} \simeq 1$
\tilde{S}_1	$(\bar{3}, 1, 4/3)$	C_{RR}	$C'_9 = C'_{10}$	$R_K \simeq R_{K^*} \simeq 1$

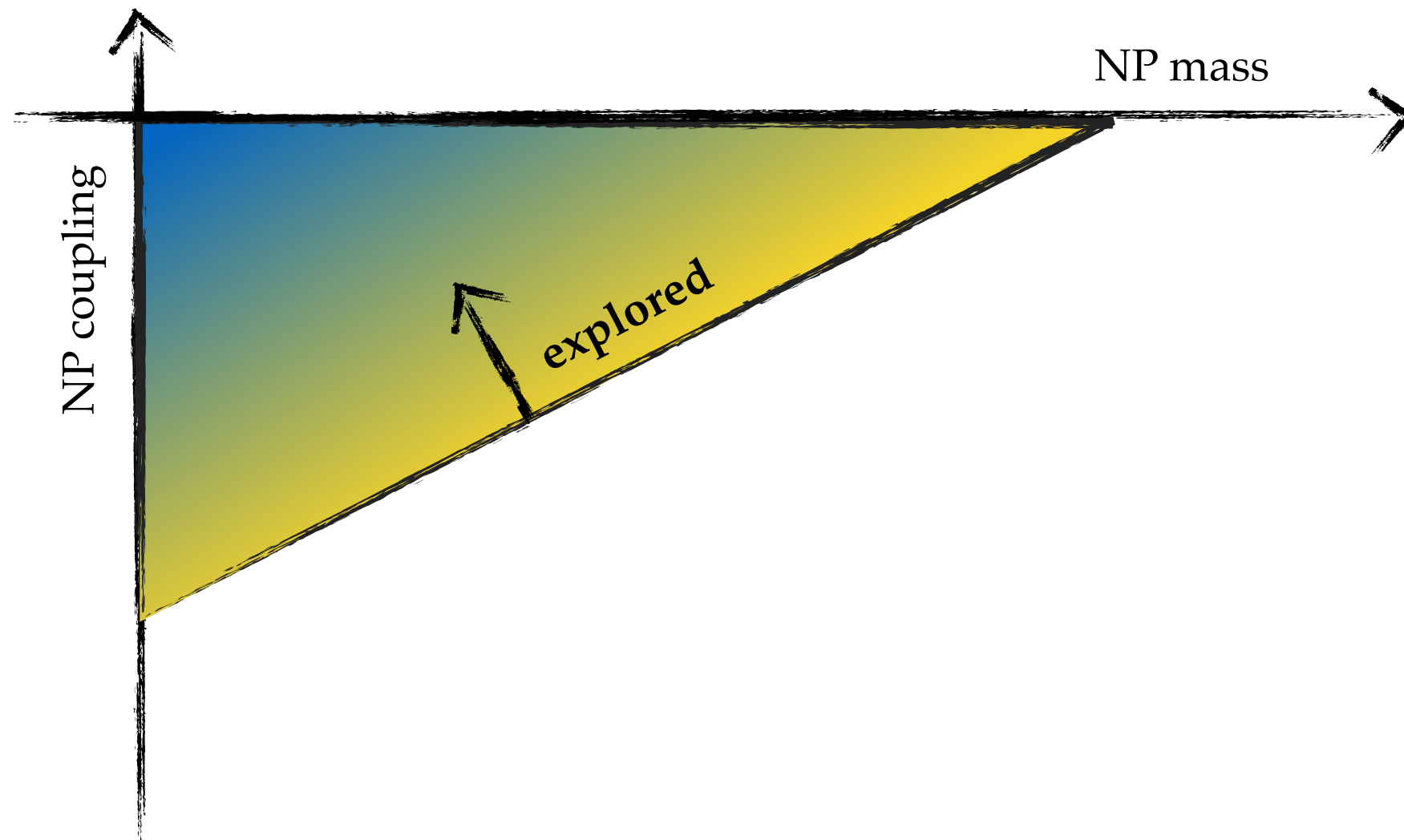
Vector
LQ

label	representation	Wilson coefficient	Relation	$R_{K(*)}$
V_1	$(3, 1, 2/3)$	C_{LL}^{NP}	$C_9 = -C_{10}$	$R_K \simeq R_{K^*} < 1$
		C_{LR}	$C_9 = +C_{10}$	$R_K \simeq R_{K^*} \simeq 1$
V_2	$(3, 2, -5/6)$	C_{RL}	$C'_9 = -C'_{10}$	$R_K < 1, R_{K^*} > 1$
		C_{RR}	$C'_9 = +C'_{10}$	$R_K \simeq R_{K^*} \simeq 1$
V_3	$(3, 3, -2/3)$	C_{LL}^{NP}	$C_9 = -C_{10}$	$R_K \simeq R_{K^*} < 1$

- motivates new direct searches

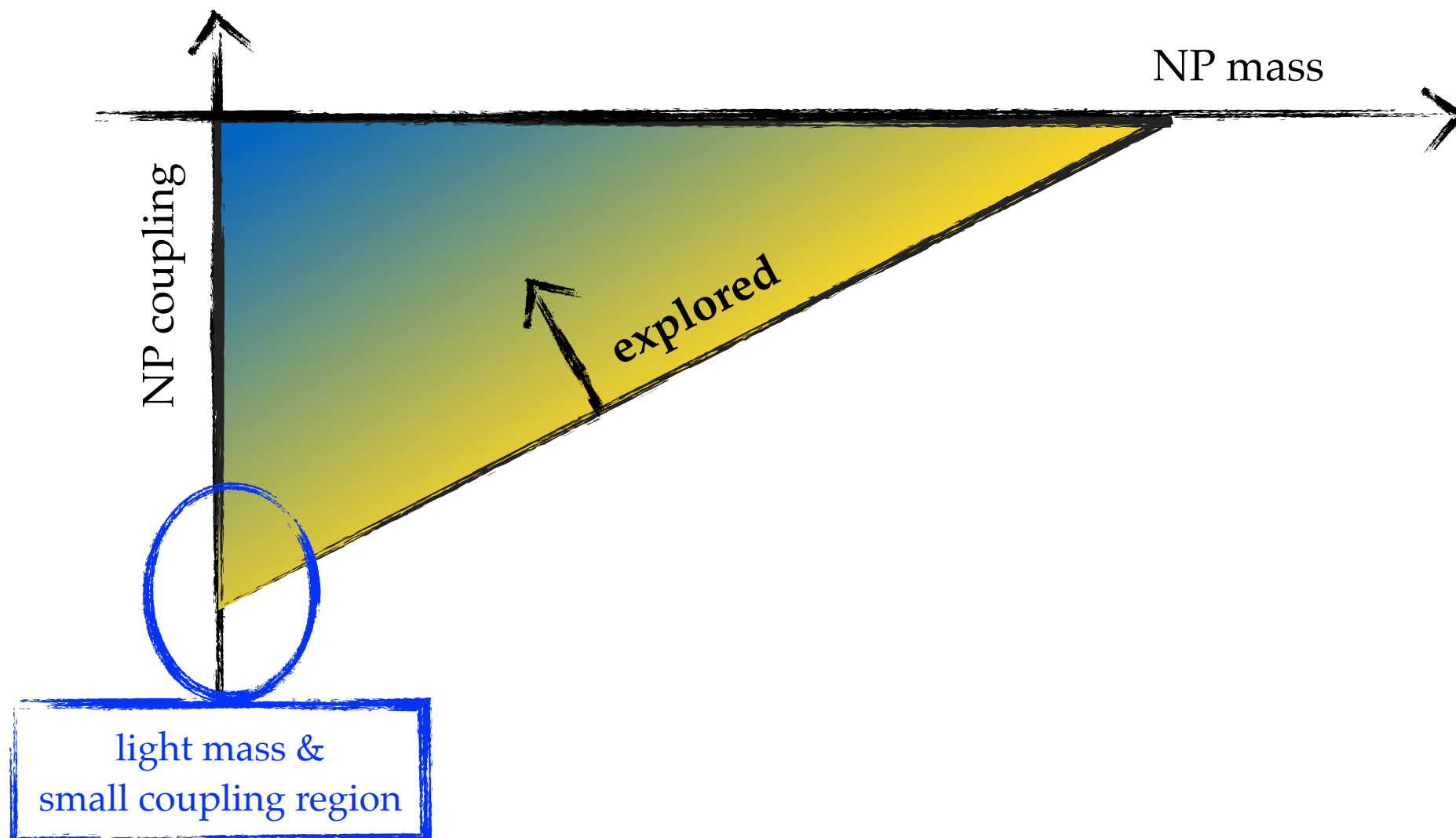
THE CASE FOR LIGHT NEW PHYSICS SEARCHES

- explored only part of the NP parameter space
- light particles: a window to high UV dynamics



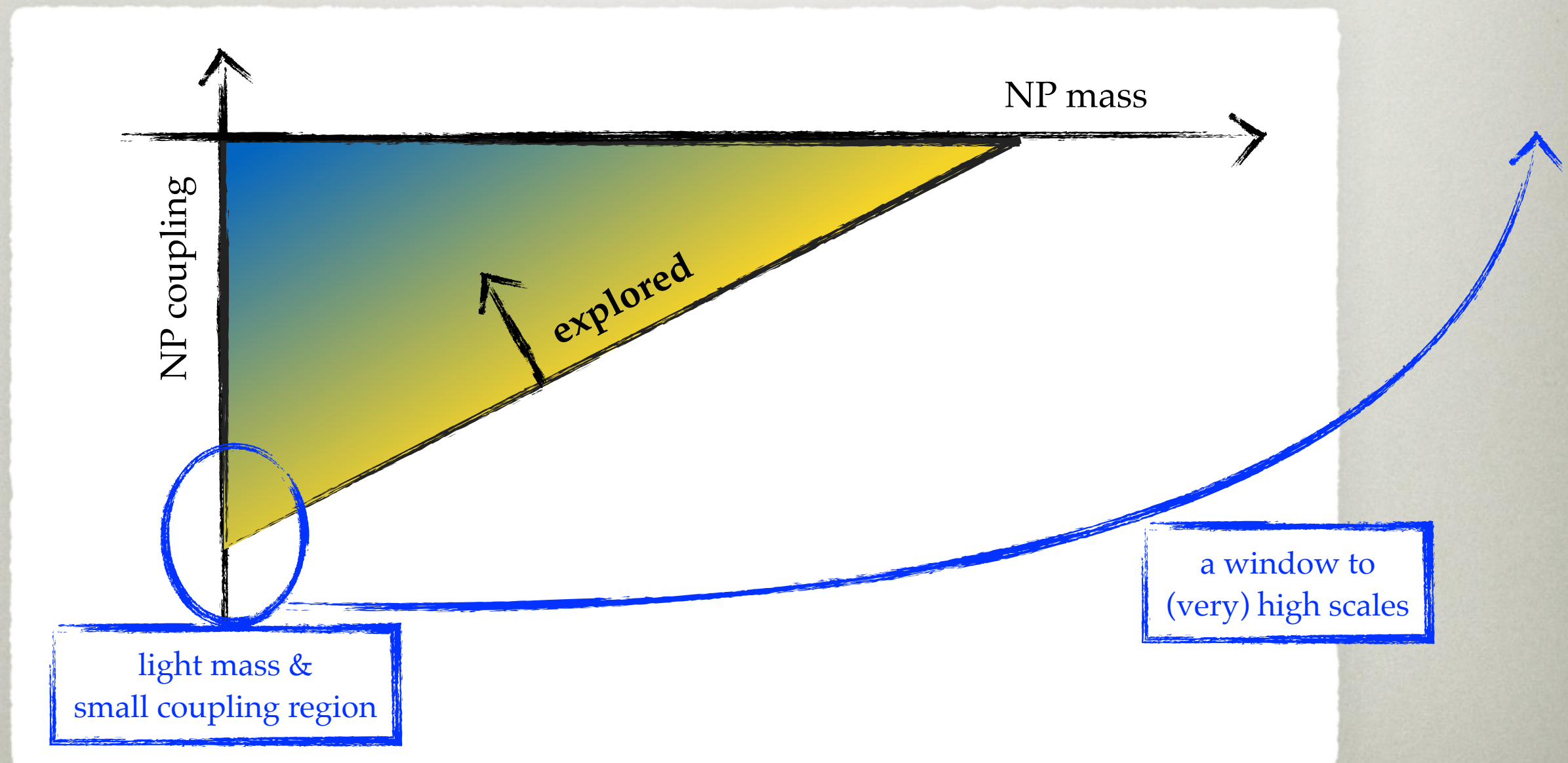
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LIGHT NEW PARTICLES

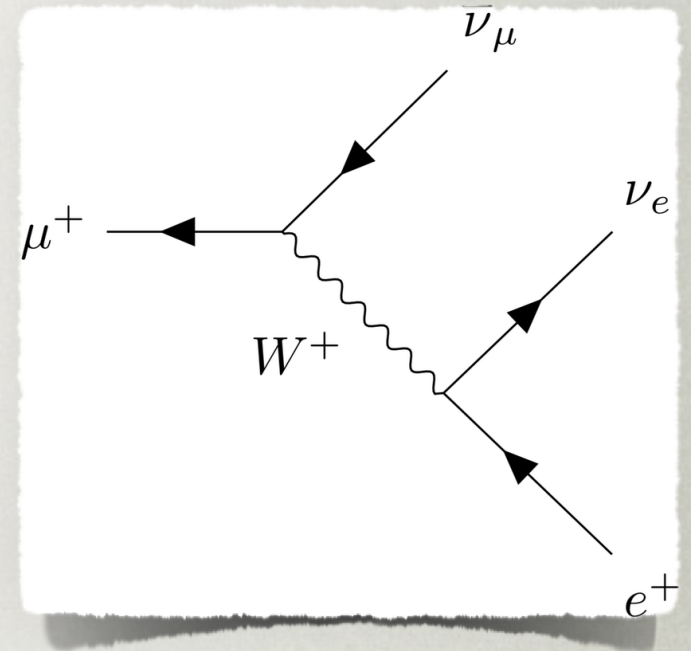
- how generic are light new particles?
- any spontaneously broken global symmetry
 - \Rightarrow massless Nambu-Goldstone boson

PORTALS

Portal	Interactions
Dark Photon, A'_μ	$-\epsilon F'_{\mu\nu} B^{\mu\nu}$
Dark Higgs, S	$(\mu S + \lambda S^2) H^\dagger H$
Heavy Neutral Lepton, N	$y_N L H N$
Axion-like pseudo scalar, a	$a F \tilde{F} / f_a, a G \tilde{G} / f_a, (\bar{\psi} \gamma^\mu \gamma_5 \psi) \partial_\mu a / f_a$

LIGHT NEW PHYSICS \Rightarrow PROBE OF HIGH SCALES

- rare decays into a light state, X , e.g.,
 $K \rightarrow \pi X$ or $\mu \rightarrow e X$,
 - exquisite probes of UV physics
- parametric gains compared to probing NP through dim-6 ops.
 - SM decay width power suppressed: $\Gamma_M \propto m_M^5/m_W^4$
- if through dim 5 op. suppressed by $1/f_a$
 - $\Rightarrow Br(\mu \rightarrow e \varphi) \propto (m_W^2/f_a m_\mu)^2$
 - similar for dim 4
- no such $1/m_\mu$ or $1/m_K$ enhancement for dim. 6 couplings
 - $Br(\mu \rightarrow 3e) \propto (m_W/\Lambda)^4$



UPSHOT

- searching for $K \rightarrow \pi X, \mu \rightarrow e X, \tau \rightarrow \mu X$
decays expect to reach very high UV
scales

EXAMPLE: FLAVOR VIOLATING QCD AXION

Martin Camalich, Pospelov, Vuong, Ziegler, JZ, 2002.04623

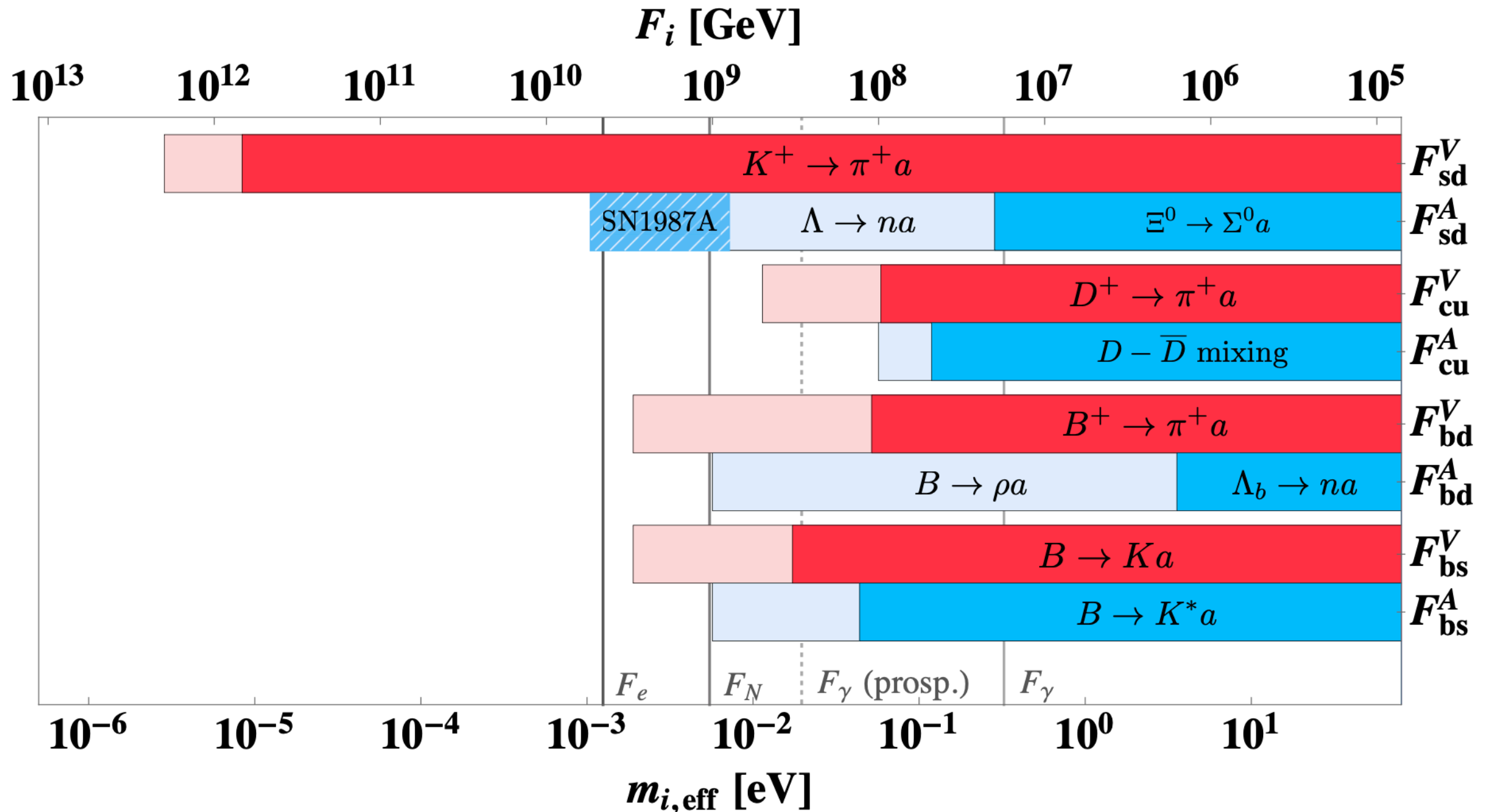
- QCD axion with FV couplings to quarks
 - solves the strong CP problem
 - can be a cold DM candidate
 - effectively massless in FV transitions
- general analysis, allowing for FV couplings as well
 - first focus on quark FV transitions

$$\mathcal{L}_{\text{eff}} = \frac{\alpha_s}{8\pi} \frac{a}{f_a} G\tilde{G} + \frac{E}{N} \frac{\alpha_{\text{em}}}{8\pi} \frac{a}{f_a} F\tilde{F} + \frac{\partial_\mu a}{2f_a} \bar{f}_i \gamma^\mu (C_{f_i f_j}^V + C_{f_i f_j}^A \gamma_5) f_j$$

$$F_{f_i f_j}^{V,A} \equiv \frac{2f_a}{C_{f_i f_j}^{V,A}}$$

THE STRONGEST FV CONSTRAINTS

Martin Camalich, Pospelov, Vuong, Ziegler, JZ, 2002.04623



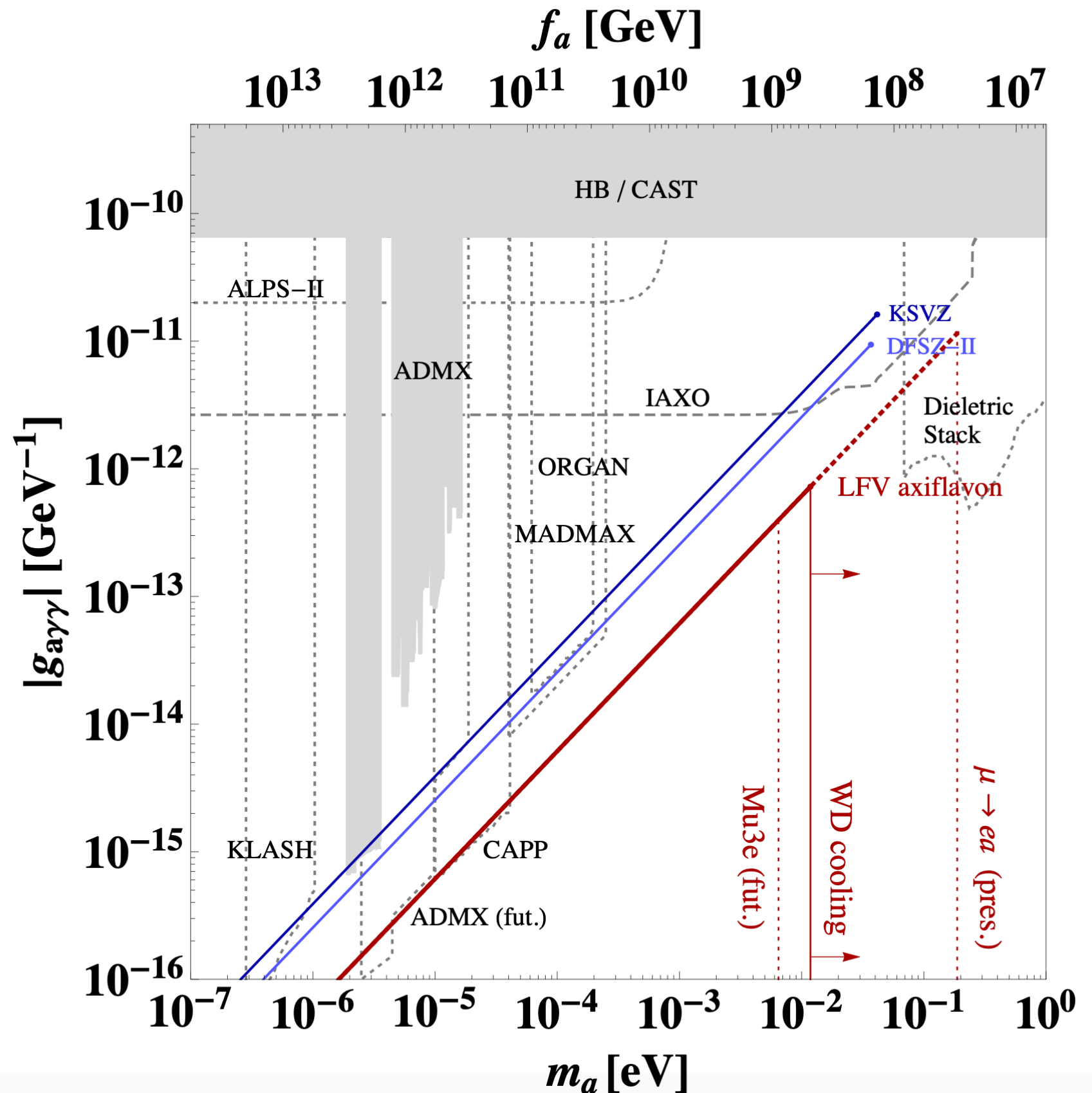
LFV AXIFLAVON

Calibbi, Redigolo, Ziegler, JZ, 2006.04795

see also, Linster, Ziegler, 1805.07341

- the PQ symmetry is part of $SU(2)_F \times U(1)_F$ flavor group
 - all FV couplings need to go through 3rd generation
 - for leptons 1-2 and 1-3 mixings are larger (in LH sector to reproduce PMNS matrix)
- \Rightarrow unlike minimal axiflavor, $K \rightarrow \pi a$ suppr.
 - the observation mode is $\mu \rightarrow ea$

- the PQ flavor g
- all FV gener
- for lep (in LF
- \Rightarrow unlik
- the ok



THEORY CROSS-FEED

- tools that were developed for flavor physics find use in other areas
 - SCET first developed for predictions in rare B decays
 - now part of standard theory tool-kit for collider physics / pQCD
 - calculation of indirect DM signal in photon lines
 - HQET and NRQED / NRQCD originate in B physics / precision frontier physics
 - DM relic abundance calculations
 - J/ψ production in pp collisions
 - WIMP direct detection scattering rates
 - influenced higher loop perturbative calculations in other areas
 - Laporta algorithm, application of IBP to more cases, loop computations with massive particles in initial / final state

CONCLUSIONS

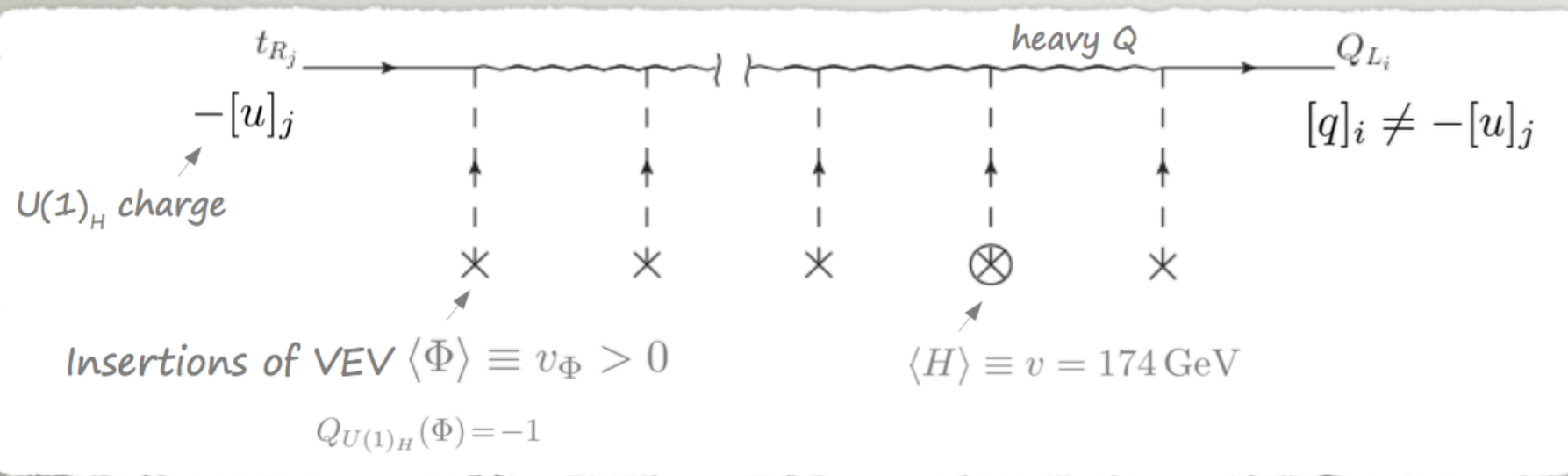
- we are entering a new era of precision measurements: Belle 2, LHCb, muon experiments, dark sector searches,
- theory is an integral part of this effort

BACKUP SLIDES

AXIFLAVON

- flavor symmetries that explain Yukawa hierarchies have a QCD anomaly
 - example FN models of flavor

Froggatt, Nielsen, NPB 147, 277 (1979),...



$$\mathcal{L}_{eff} \sim \left(\frac{\phi}{\Lambda_F} \right)^{x_{ij}} h \bar{q}_i u_j$$

$$\epsilon \equiv \frac{\phi}{\Lambda_F}$$

- axiflavor mechanism: identify PQ symmetry with FN $U(1)_H$
 - the phase of the flavon is the QCD axion = axiflavor

$$\Phi = \frac{f + \phi(x)}{\sqrt{2}} e^{i a(x)/f}$$

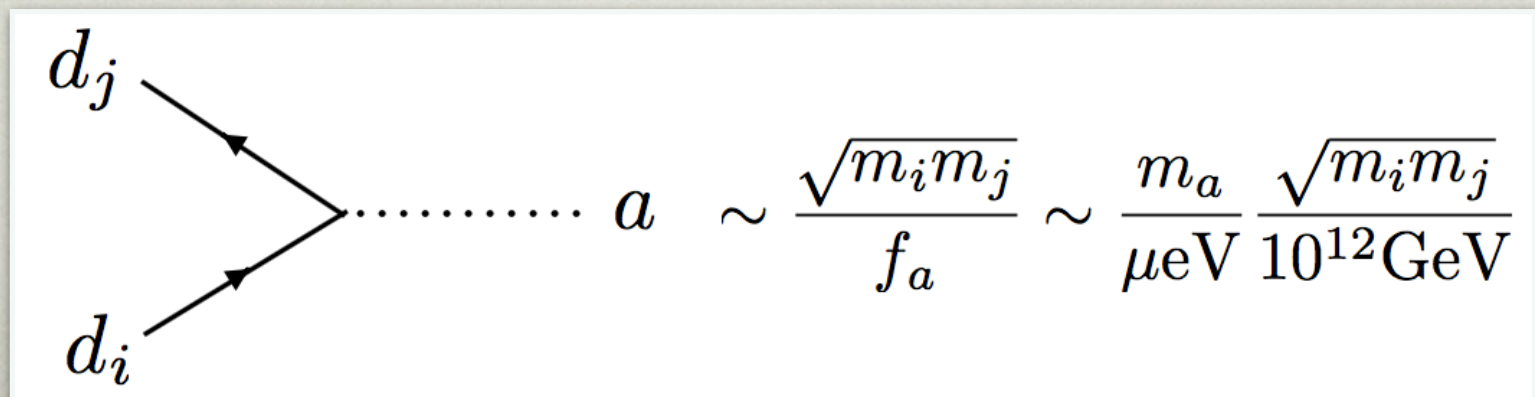
Wilczek, PRL 49, 1549 (1982)

Calibbi, Goertz, Redigolo, Ziegler, JZ, 1612.08040

Ema, Hamaguchi, Moroi, Nakayama, 1612.05492

SEARCHING FOR AXIONS/ AXIFLAVONS

- axion searches use
 - couplings to photons (haloscopes, helioscopes,...)
 - couplings to gluons (CASPEr)
 - flavor diagonal couplings to electrons, nucleons (astrophysical bounds)
- axiflavor
 - in addition flavor violating couplings to fermions
 - in the minimal FN axiflavor model



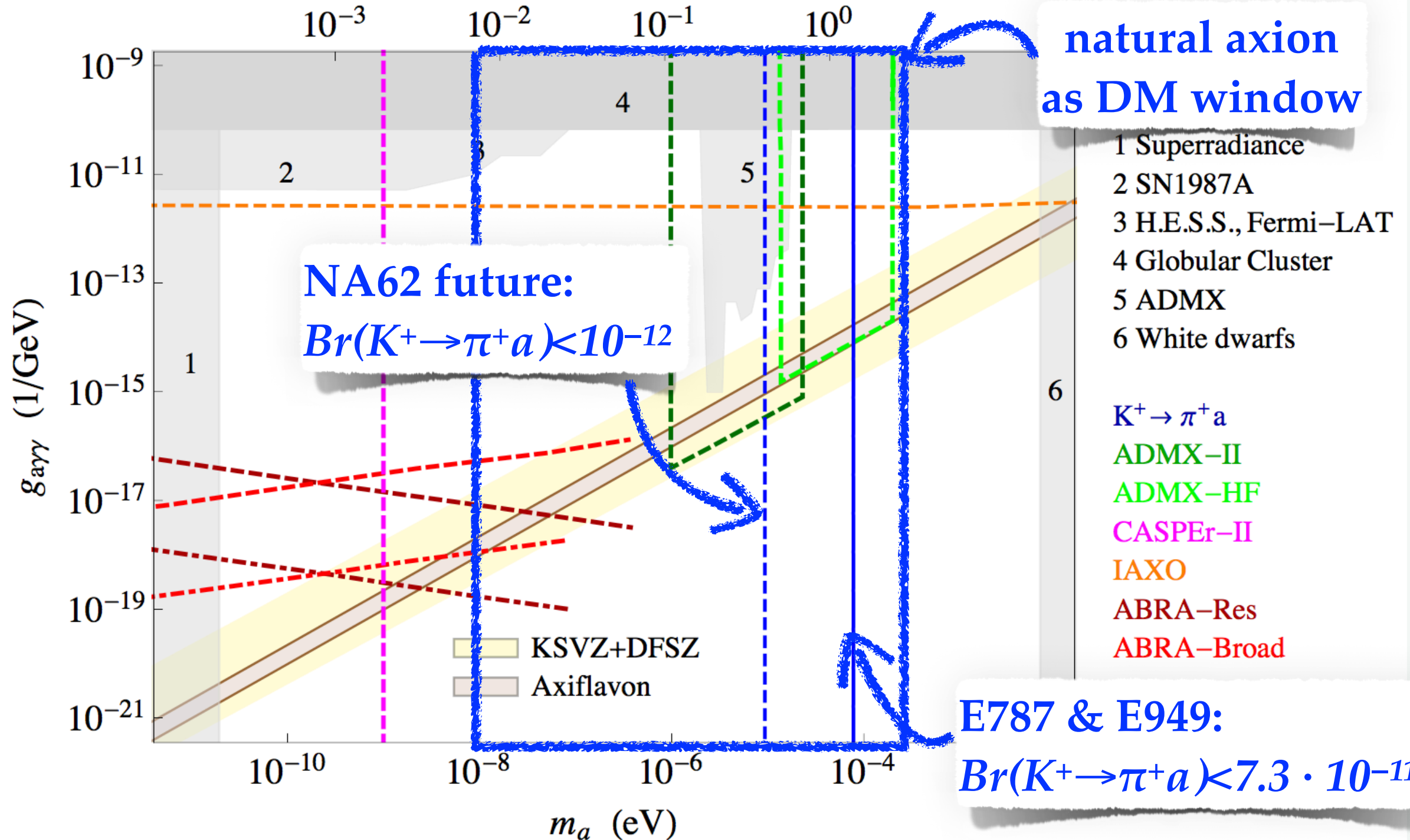
$$a \sim \frac{\sqrt{m_i m_j}}{f_a} \sim \frac{m_a}{\mu\text{eV}} \frac{\sqrt{m_i m_j}}{10^{12}\text{GeV}}$$

SEARCHING FOR AXIONS/ AXIFLAVONS

minimal axiflapon

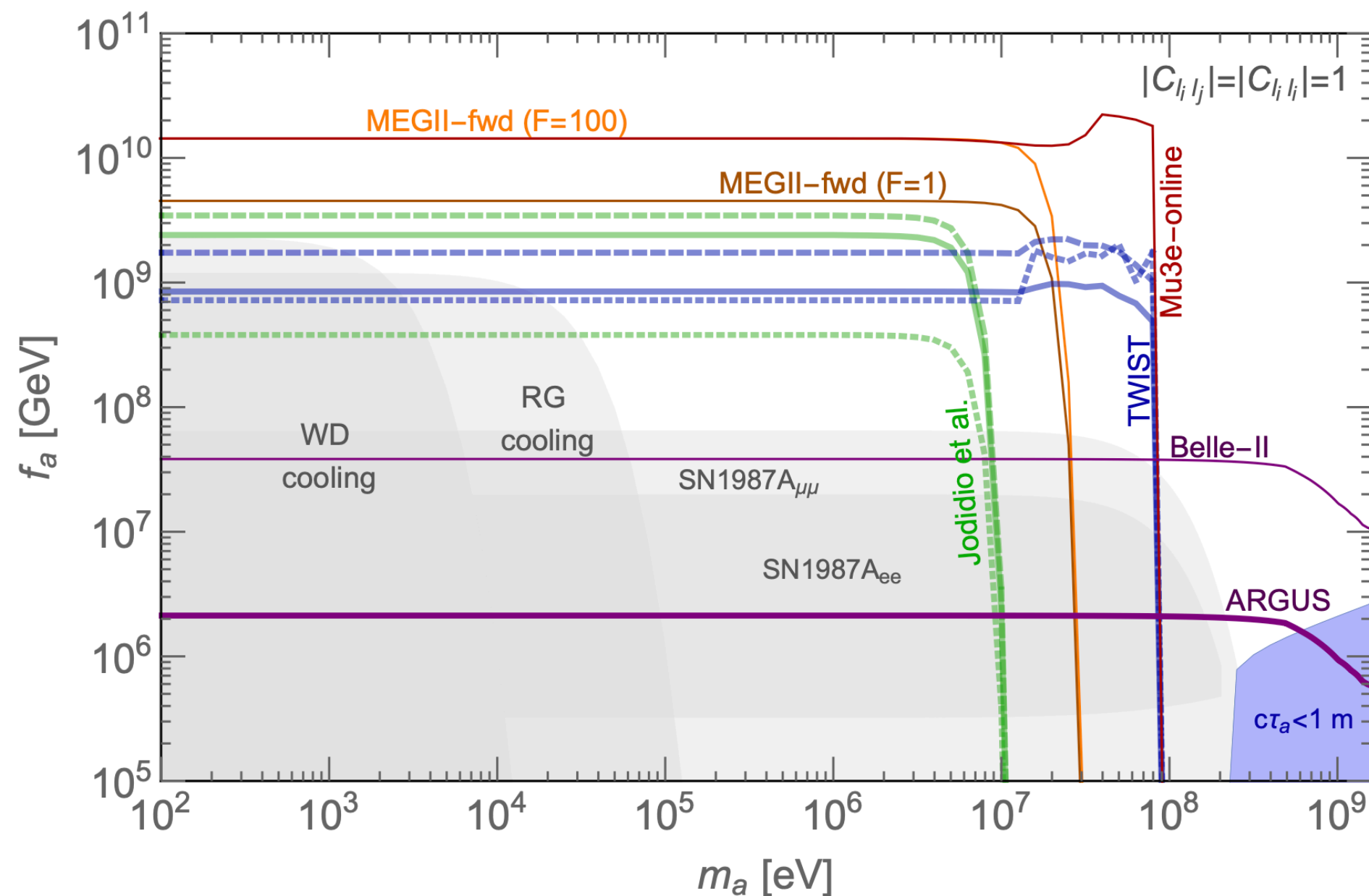
Calibbi, Goertz, Redigolo, Ziegler, JZ, 1612.08040

natural axion
as DM window

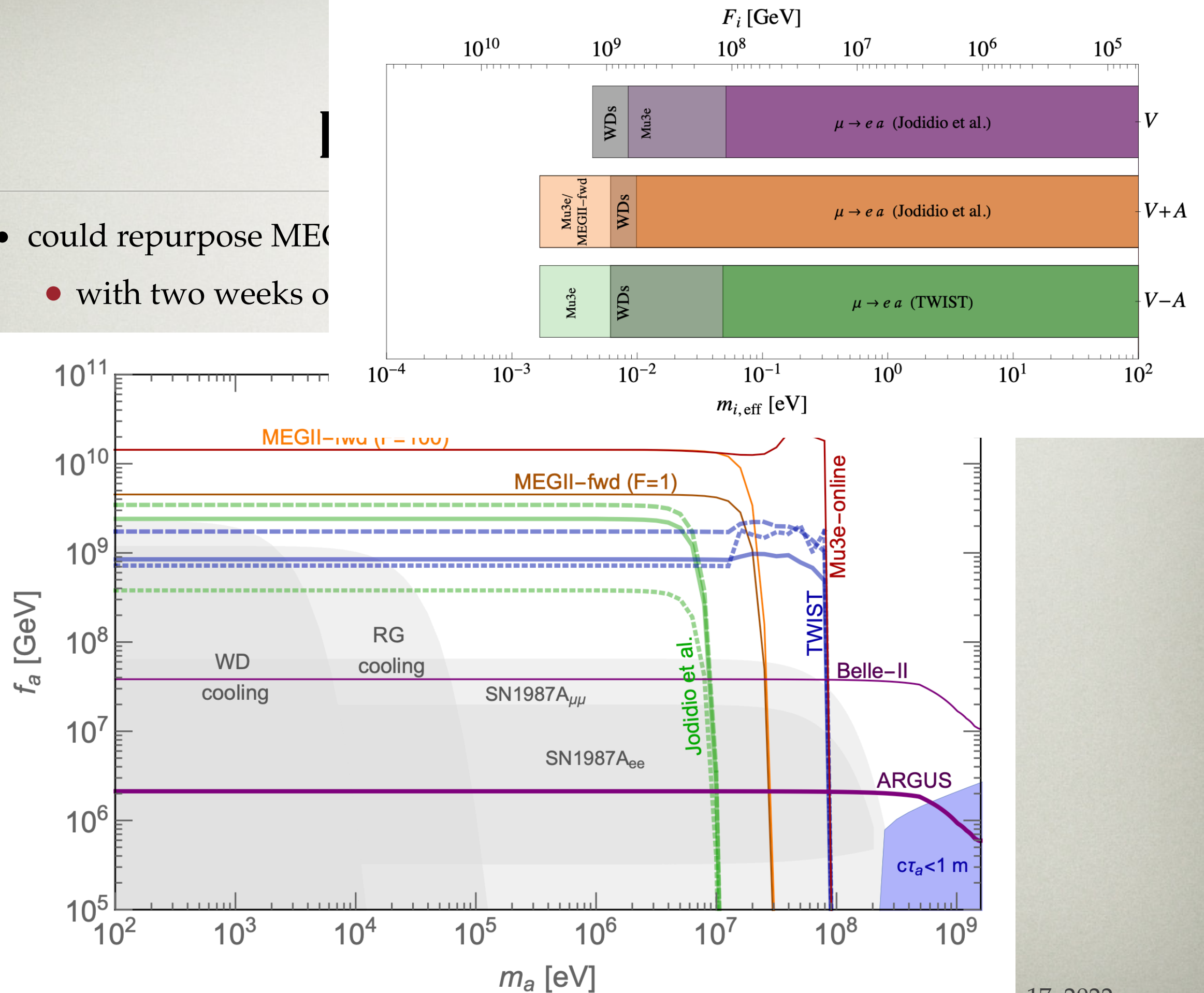


MEGII-FWD

- could repurpose MEG II (\rightarrow MEGII-fwd) Calibbi, Redigolo, Ziegler, JZ, 2006.04795
- with two weeks of running already very stringent constraints possible



- could repurpose MEG II
- with two weeks of



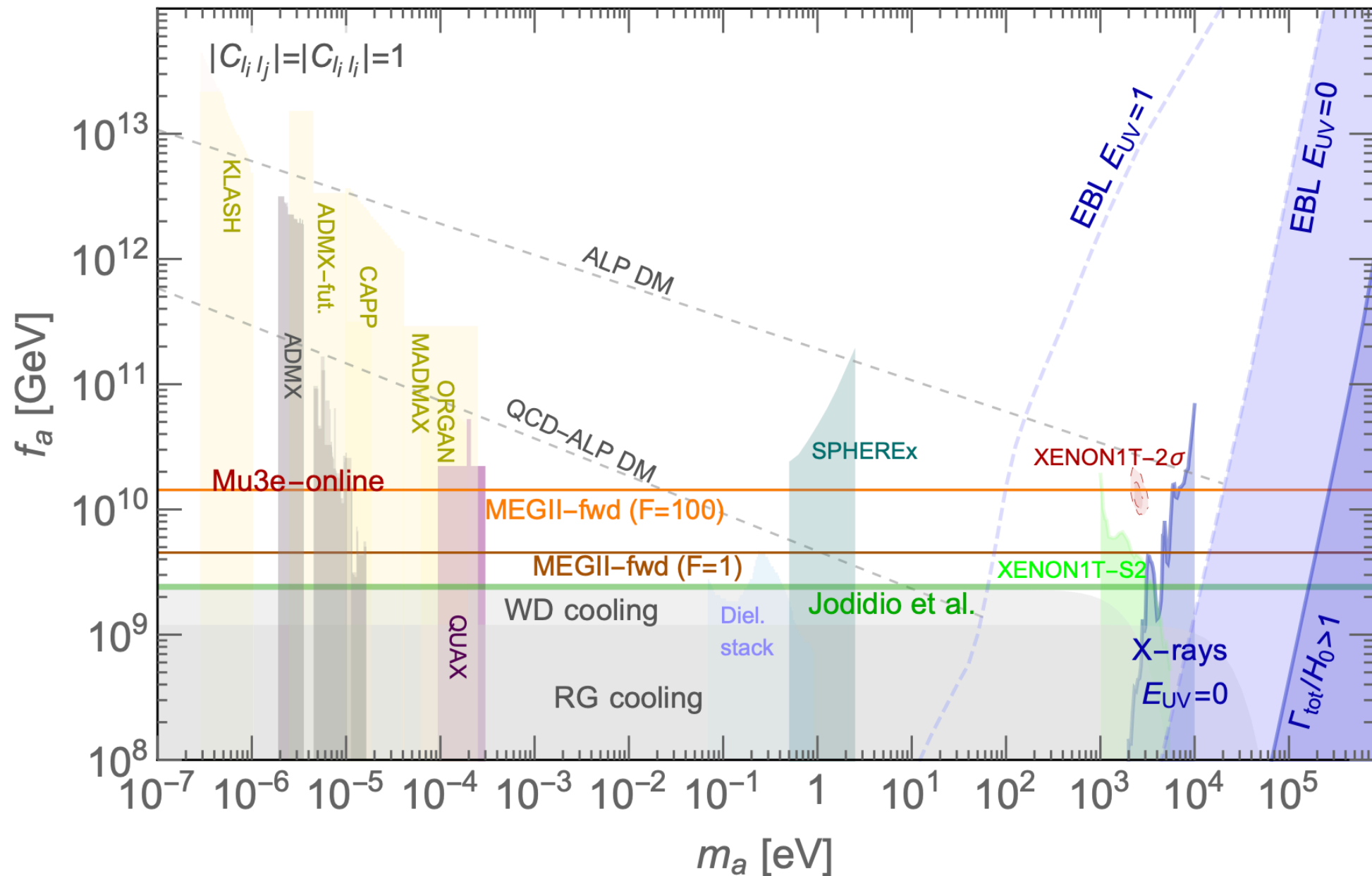
LFV ALP DARK MATTER

- 0-th order condition for ALP to be a DM: be stable on Hubble time
- assume $a \rightarrow \gamma\gamma$ dominates

$$\frac{H_0}{\Gamma_{\text{tot}}} = H_0\tau_a > 1, \quad \text{where} \quad H_0\tau_a \simeq 5.4 \left(\frac{1}{E_{\text{eff}}^2} \right)^2 \left(\frac{10 \text{ keV}}{m_a} \right)^3 \left(\frac{f_a}{10^{10} \text{ GeV}} \right)^2.$$

- if ALP is observed in a LFV process $\Rightarrow m_a \lesssim 10 \text{ keV}$
 - LFV experiments most sensitive for some m_a
 - need other experiments to confirm it is DM

$$\frac{H_0}{\Gamma_{\text{tot}}} =$$

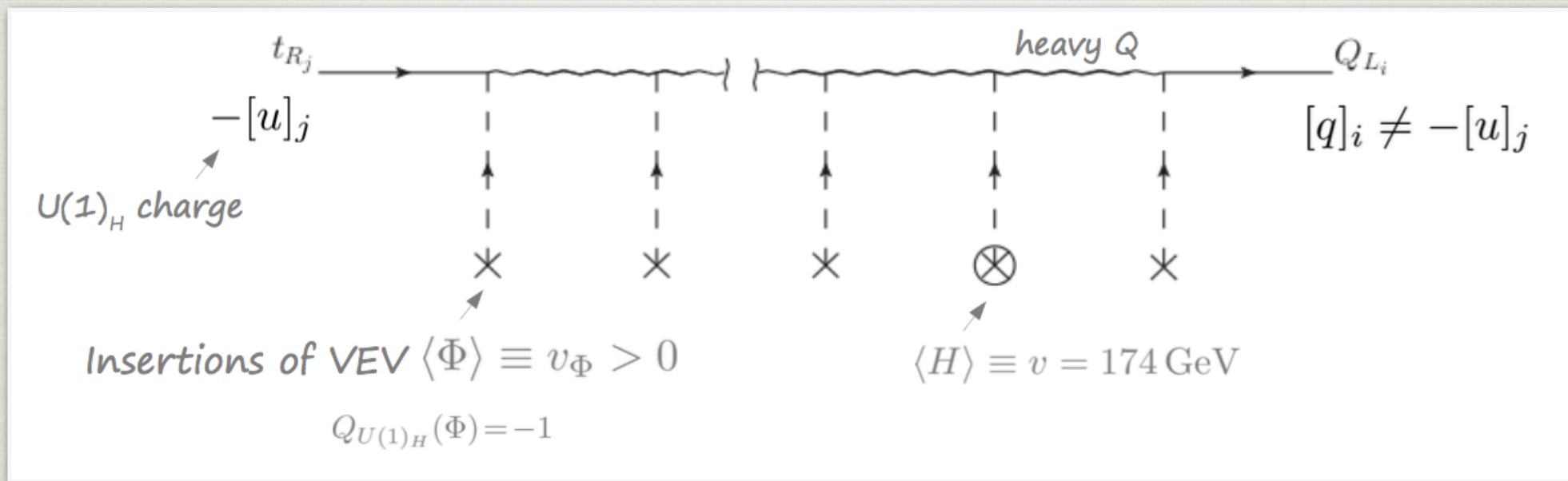


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LIGHT NEW PHYSICS \Rightarrow PROBE OF HIGH SCALES

- rare decays into a light state, X , e.g., $K \rightarrow \pi X$ or $\mu \rightarrow eX$,
 - exquisite probes of UV physics
- parametric gains compared to probing NP through dim-6 ops
 - the reason: SM decay widths are power suppressed
 $\Gamma_\ell \propto m_\ell^5/m_W^4$
- if light NP couples through dim 4 op with mixing angle θ
 - $\Rightarrow \Gamma(K \rightarrow \pi\varphi) \propto \theta^2 m_K \Rightarrow Br(K \rightarrow \pi\varphi) \propto \theta^2 (m_W/m_K)^4$
- if through dim 5 op. suppressed by $1/f_a$
 - $\Rightarrow Br(\mu \rightarrow e\varphi) \propto (m_W^2/f_a m_\mu)^2$
- no such $1/m_\mu$ or $1/m_K$ enhancement for dimension 6 couplings
 - $Br(\mu \rightarrow 3e) \propto (m_W/\Lambda)^4$

ANOMALY FREE FN MODELS



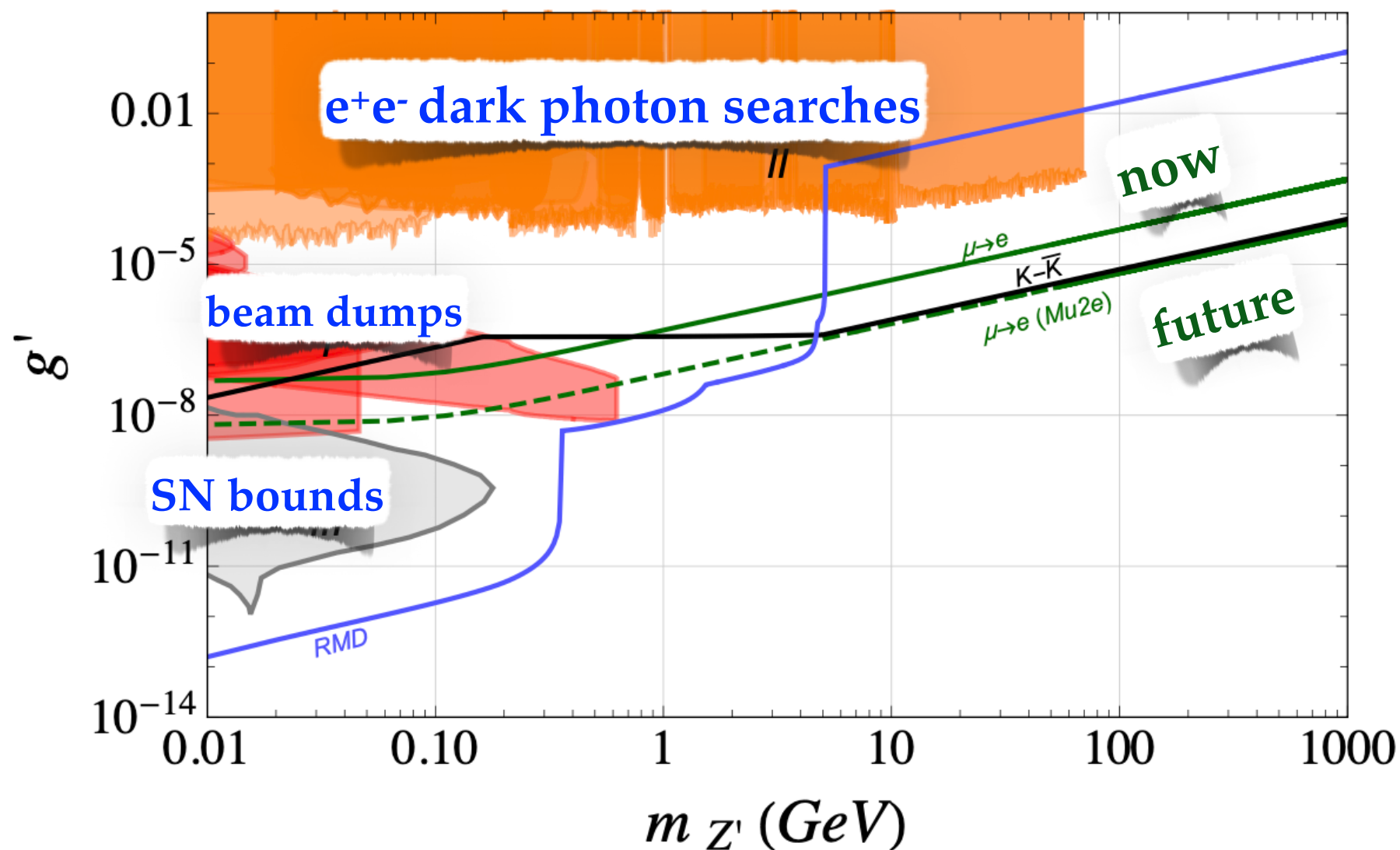
- inverted FN mechanism \Rightarrow non-anomalous $U(1)_{\text{FN}}$
 - vector-like fermions all charged under $U(1)_{\text{FN}}$ (no anomaly)
 - chiral fields not charged under $U(1)_{\text{FN}}$ (in the middle of the chain)
 - a concrete realization of the "clockwork" mechanism
- $U(1)_{\text{FN}}$ can be gauged

EXPERIMENTAL SEARCHES

- how to observe experimentally?
- search in FCNCs
 - $K - \bar{K}, B - \bar{B}$ mixing, etc.
 - exchanges of flavons, heavy vector-like fermions, flavorful Z' s
 - for $\mathcal{O}(1)$ couplings masses $\gtrsim 10^7$ GeV
- for small $U(1)_{\text{FN}}$ gauge couplings Z' can be light
 - can also search for it directly: beam dumps, e^+e^- colliders, astrophysics

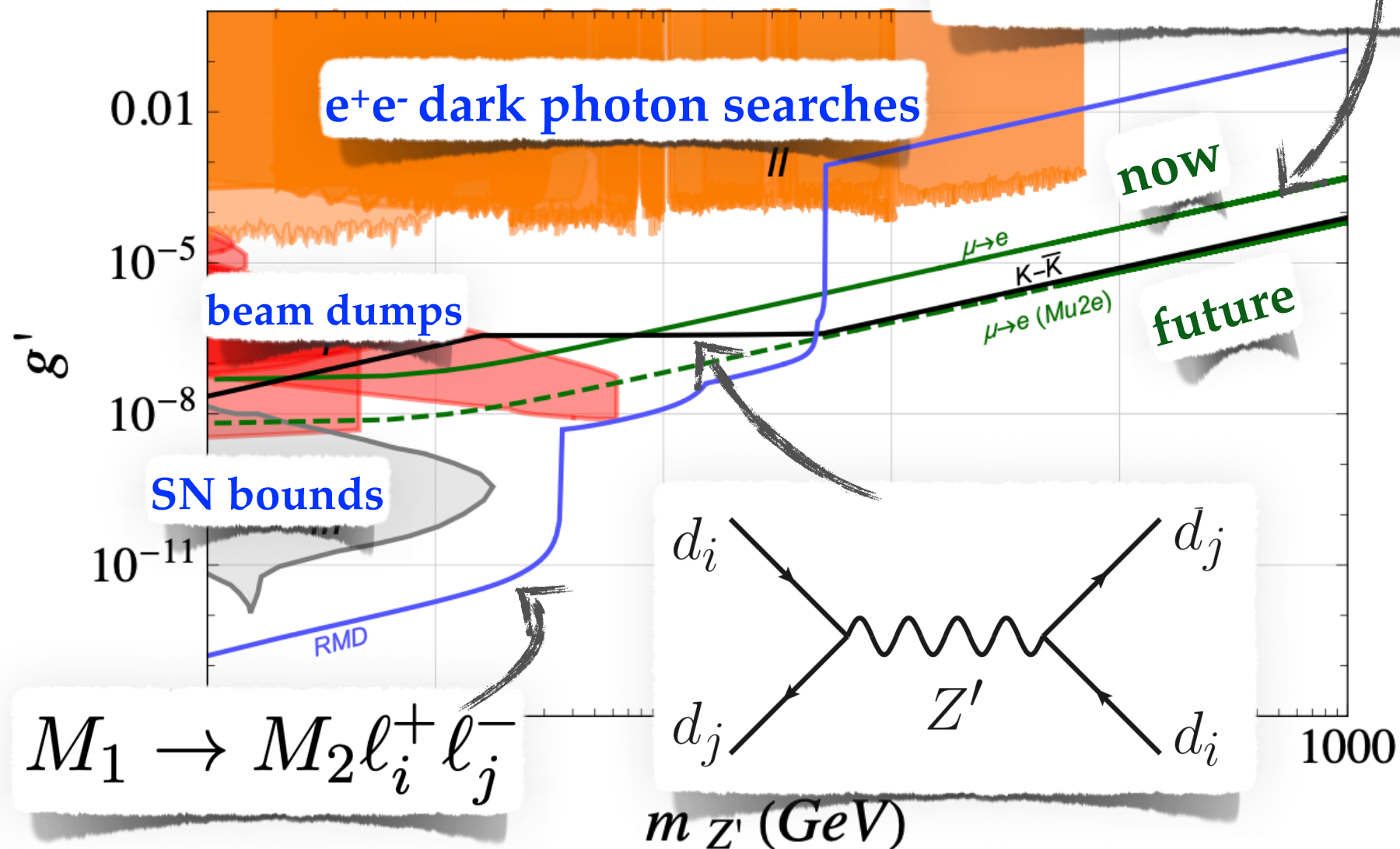
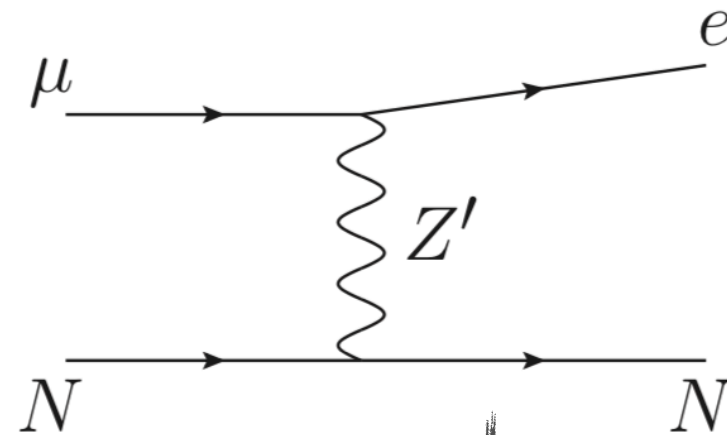
FLAVORFUL Z'

- for $U(1)_{FN}$ benchmark, assuming anarchic neutrino mass from Weinber op.



FLAVORFUL Z'

- for $U(1)_{FN}$ benchmark, as
anarchic neutrino mass



LFV QCD AXION

- DFSZ-like model: 2HDM+S: $X_S = 1, X_{H_2} = 2 + X_{H_1}$
- flavor universal $U(1)_{PQ}$ charges in quark sector, non-universal in leptonic

Yukawa coupl. to H_1

$$y_e = \begin{pmatrix} 0 & x & x \\ x & 0 & 0 \\ x & 0 & 0 \end{pmatrix},$$

Yukawa coupl. to H_2

$$y'_e = \begin{pmatrix} 0 & 0 & 0 \\ 0 & x & x \\ 0 & x & x \end{pmatrix}$$

\Rightarrow gives lepton FV coupl.s of axion

$$y_u = \begin{pmatrix} x & x & x \\ x & x & x \\ x & x & x \end{pmatrix},$$

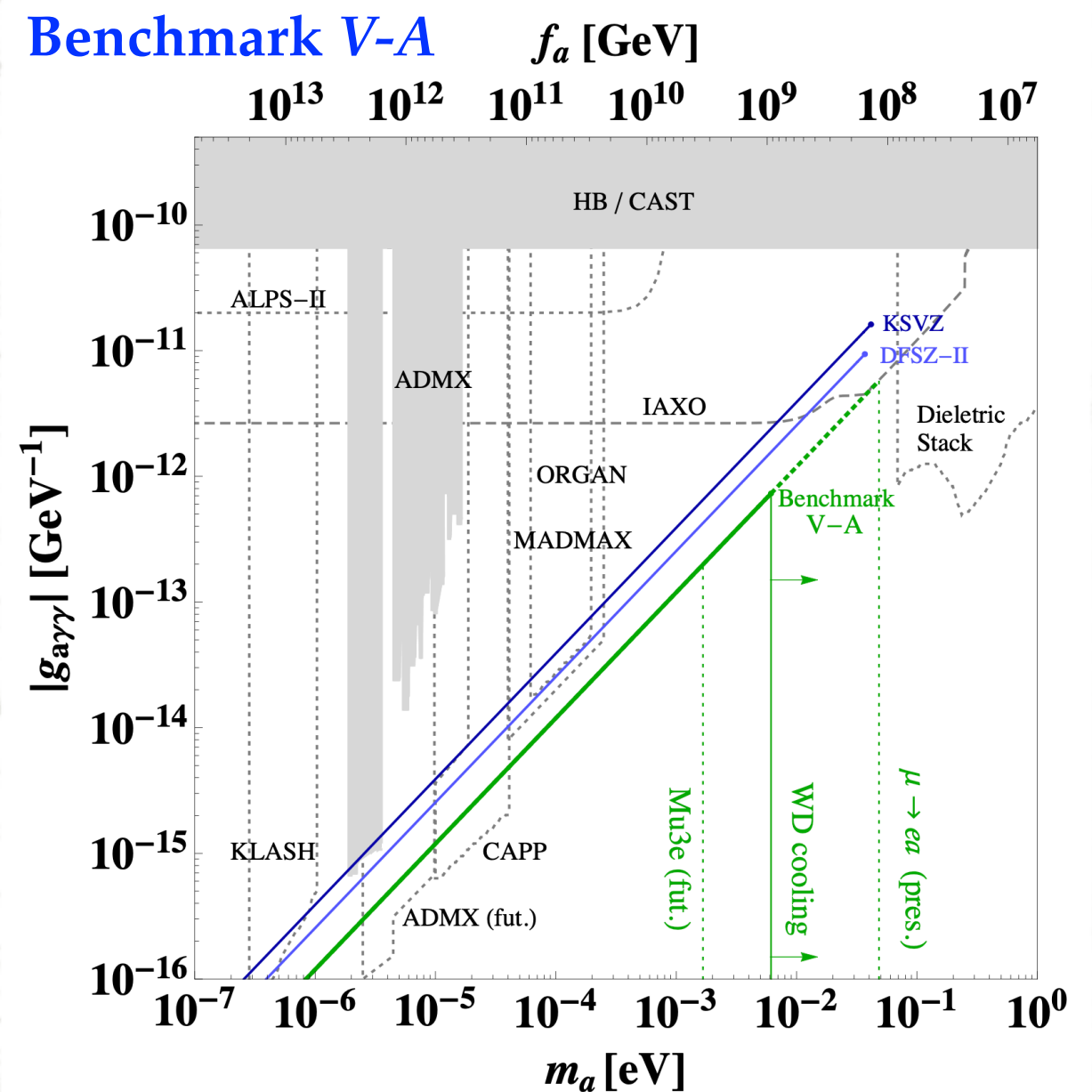
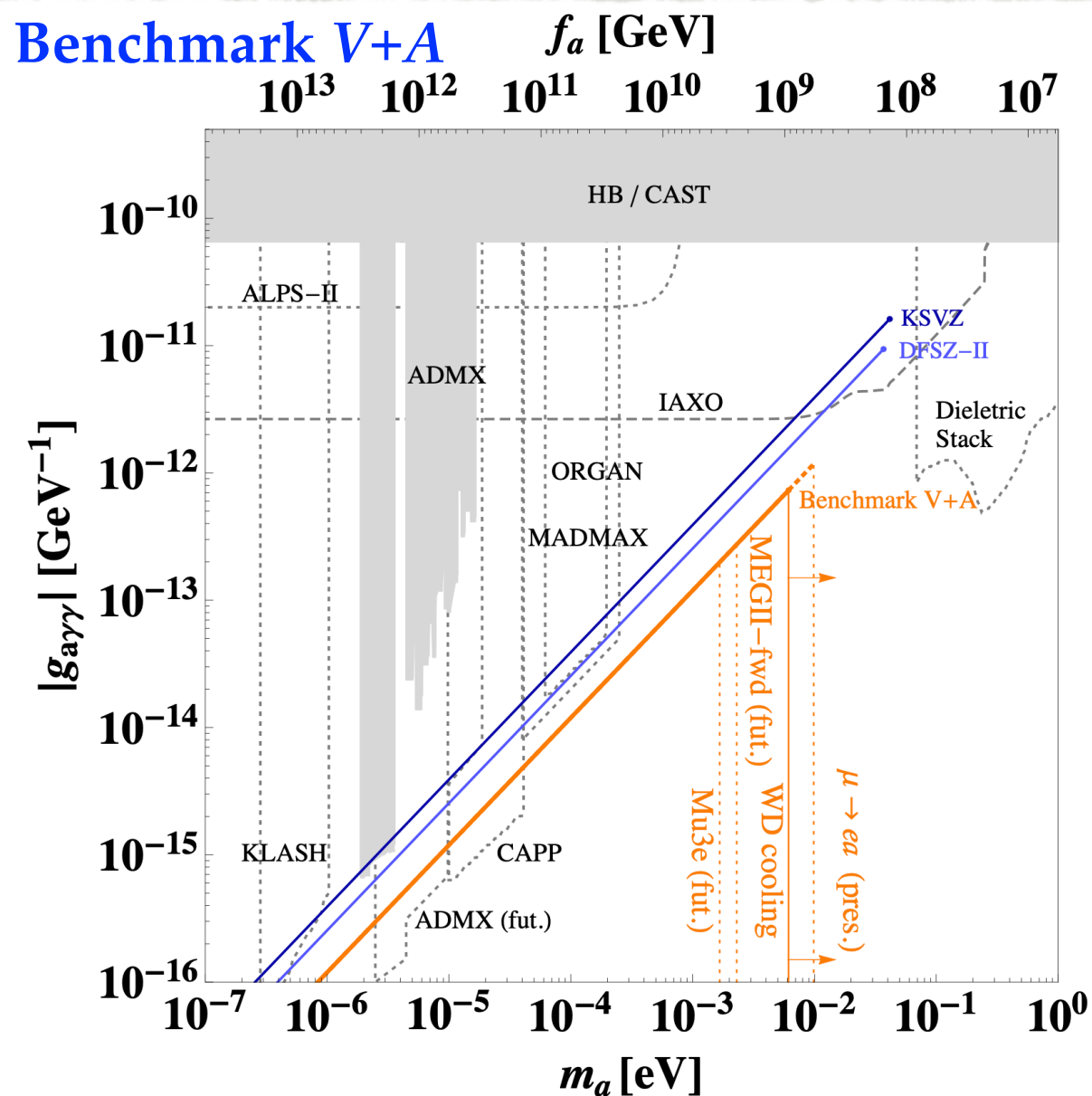
$$y_d = \begin{pmatrix} x & x & x \\ x & x & x \\ x & x & x \end{pmatrix}$$

\Rightarrow axion-quark couplings flavor diagonal

- hierarchy of entries external input

LFV QCD AXION

- two benchmarks, assume just 1-2 mixing



LEPTONIC FAMILON

- separate Froggatt-Nielsen U(1) for quarks and leptons
- leptonic f_a scale assumed lighter \Rightarrow these couplings dominate

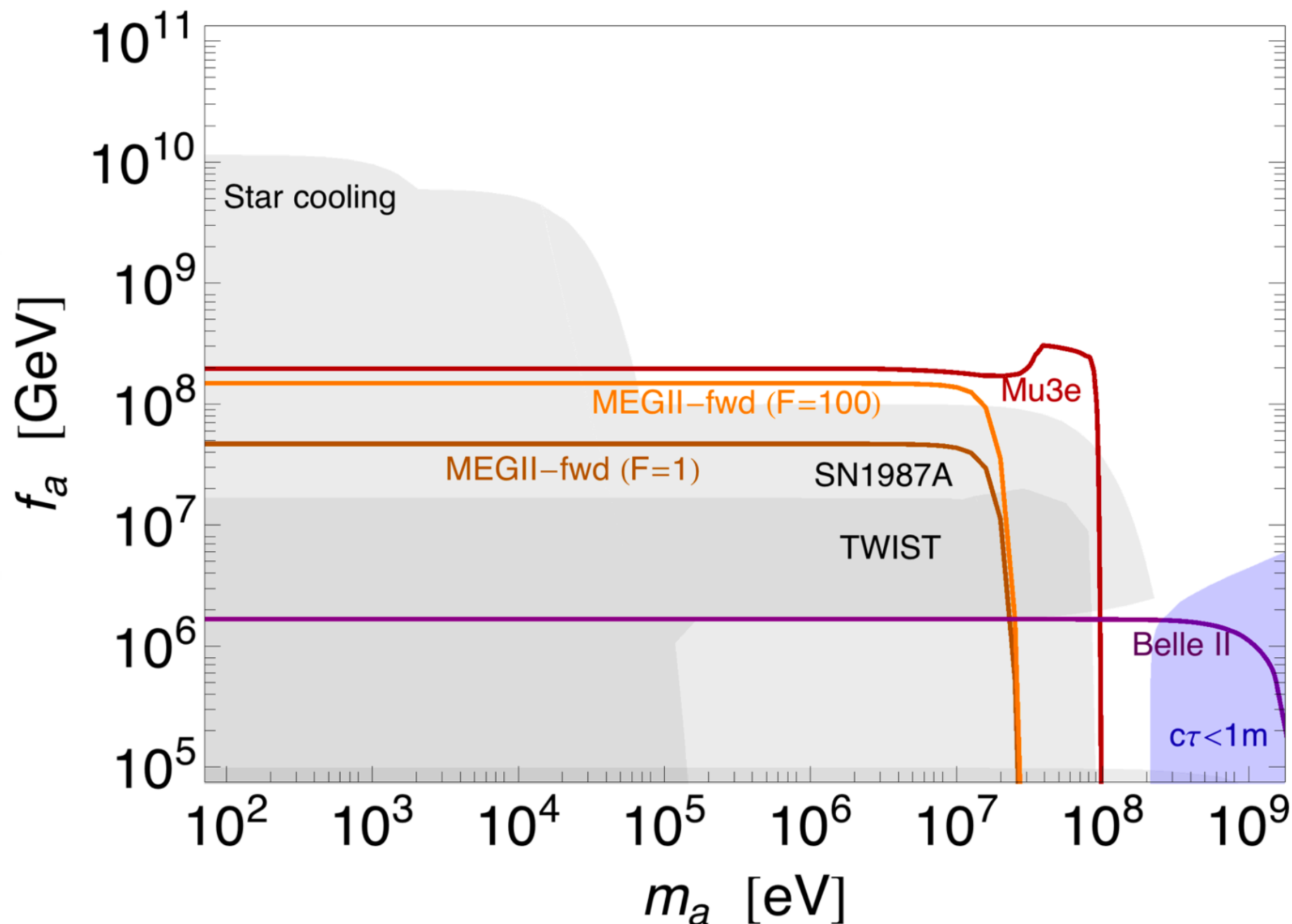
$$([L]_1, [L]_2, [L]_3) = (L, L, L), \quad [\text{Pure Anarchy}] . \quad \Rightarrow \text{RH ALP}$$

- two benchmark charge assignments

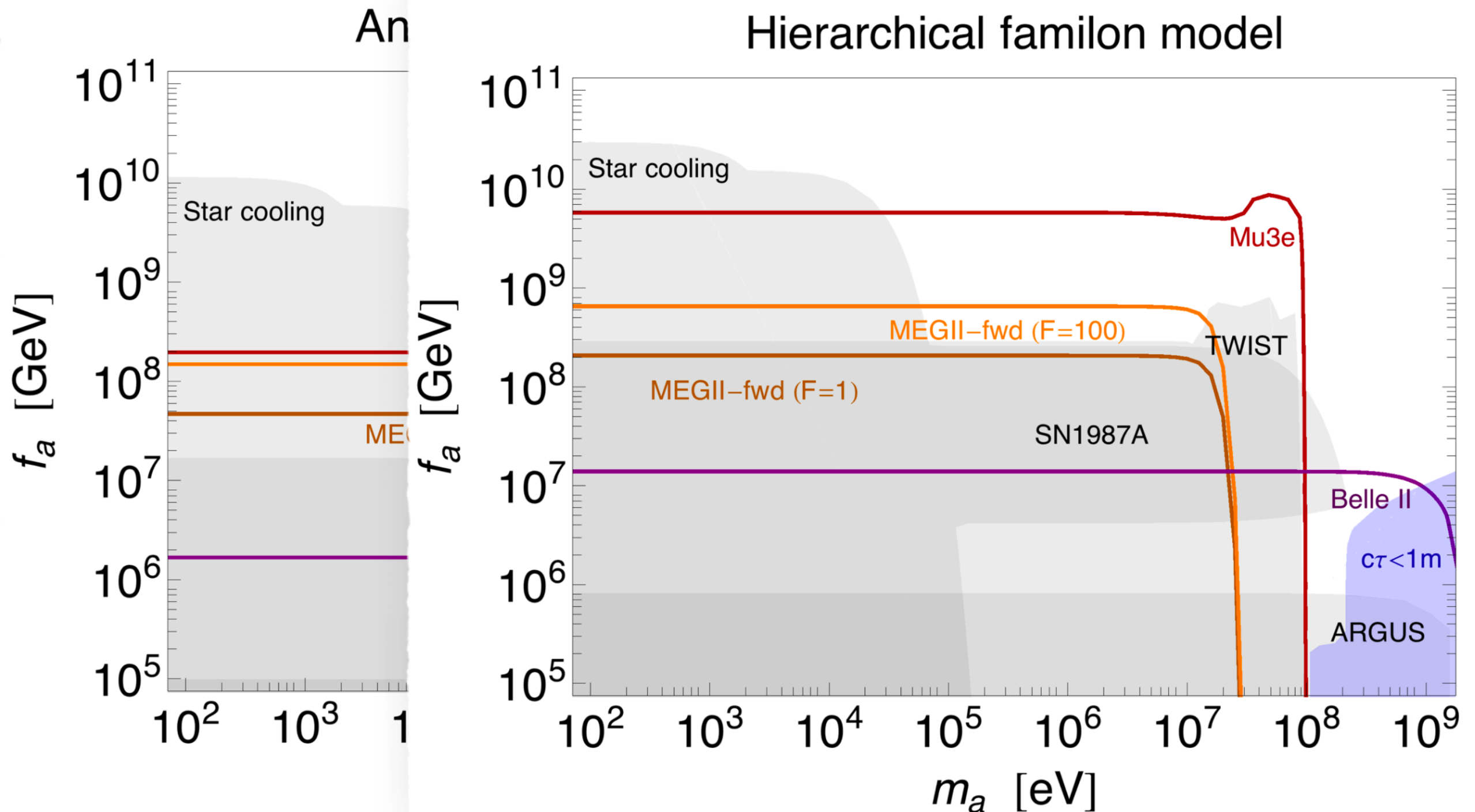
$$([L]_1, [L]_2, [L]_3) = (L + 2, L + 1, L), \quad [\text{Hierarchy}] . \quad \Rightarrow \text{LH and RH couplings}$$

LEPTONIC FAMILON

Anarchical familon model

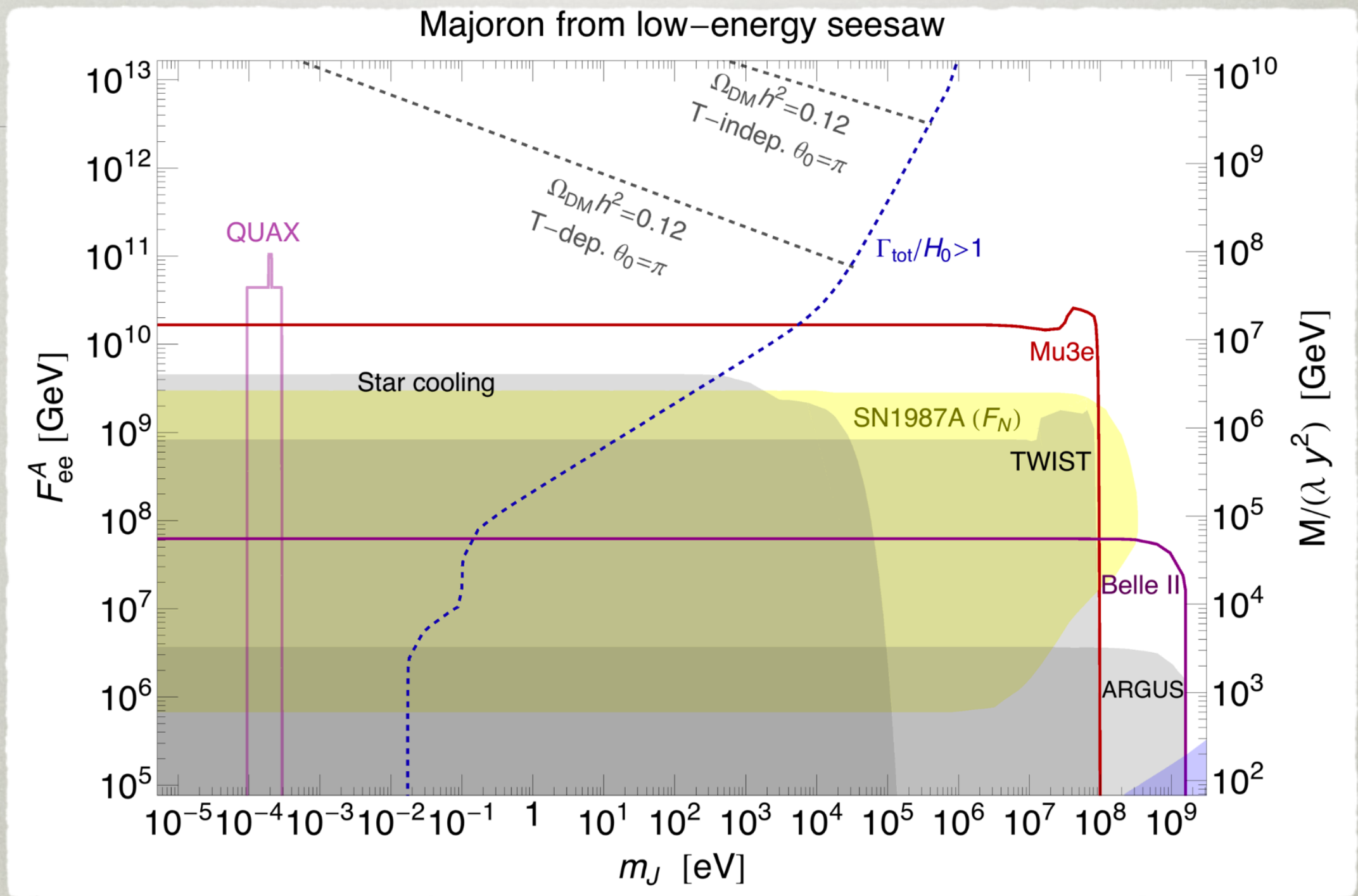


LEPTONIC FAMILON



MAJORON

- majoron- PNGB due to spontaneous breaking of the lepton number
- neutrino masses $m_\nu \propto y_\nu y_\nu^T v^2 / m_N$
- majoron couplings, $C_{ij} \propto y_\nu y_\nu^\dagger$
- if m_ν suppressed by global U(1)
 - \Rightarrow majoron observable
 - "low energy see-saw"

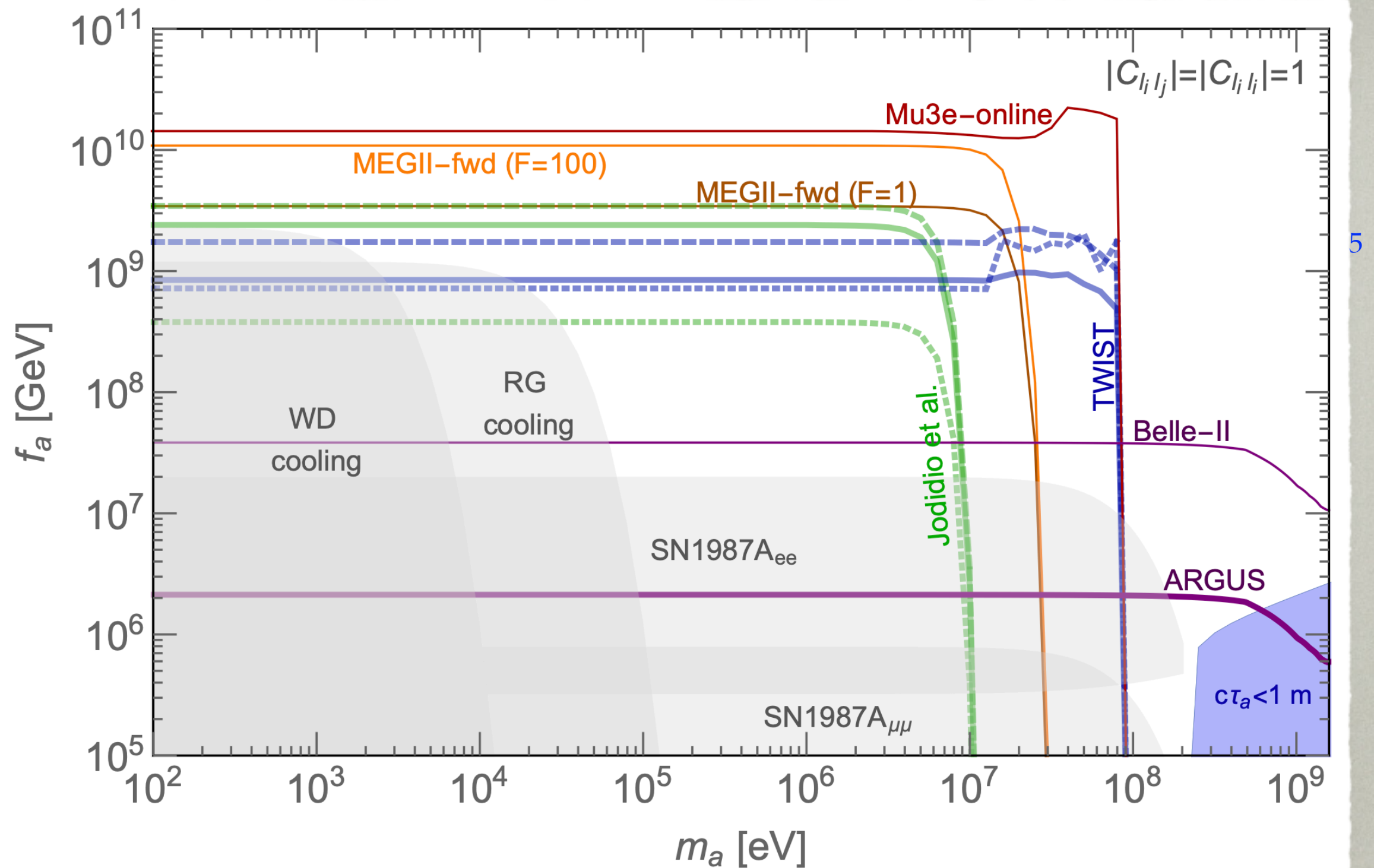


● "low energy see-saw"

ASTROPHYSICS BOUNDS

Raffelt, Weiss , [hep-ph/9410205](#)

- bounds on massless ALP-electron from red giants and white-dwarf cooling well known
 - due to $e^- + N \rightarrow e^- + N + a$
 - rescaled to nonzero ALP masses
- above $m_a \gtrsim 0.1$ MeV SN bounds become important
- also bounds on couplings to muons, but less severe



- also bounds on couplings to muons, but less severe

CONNECTION TO BARYOGENESIS

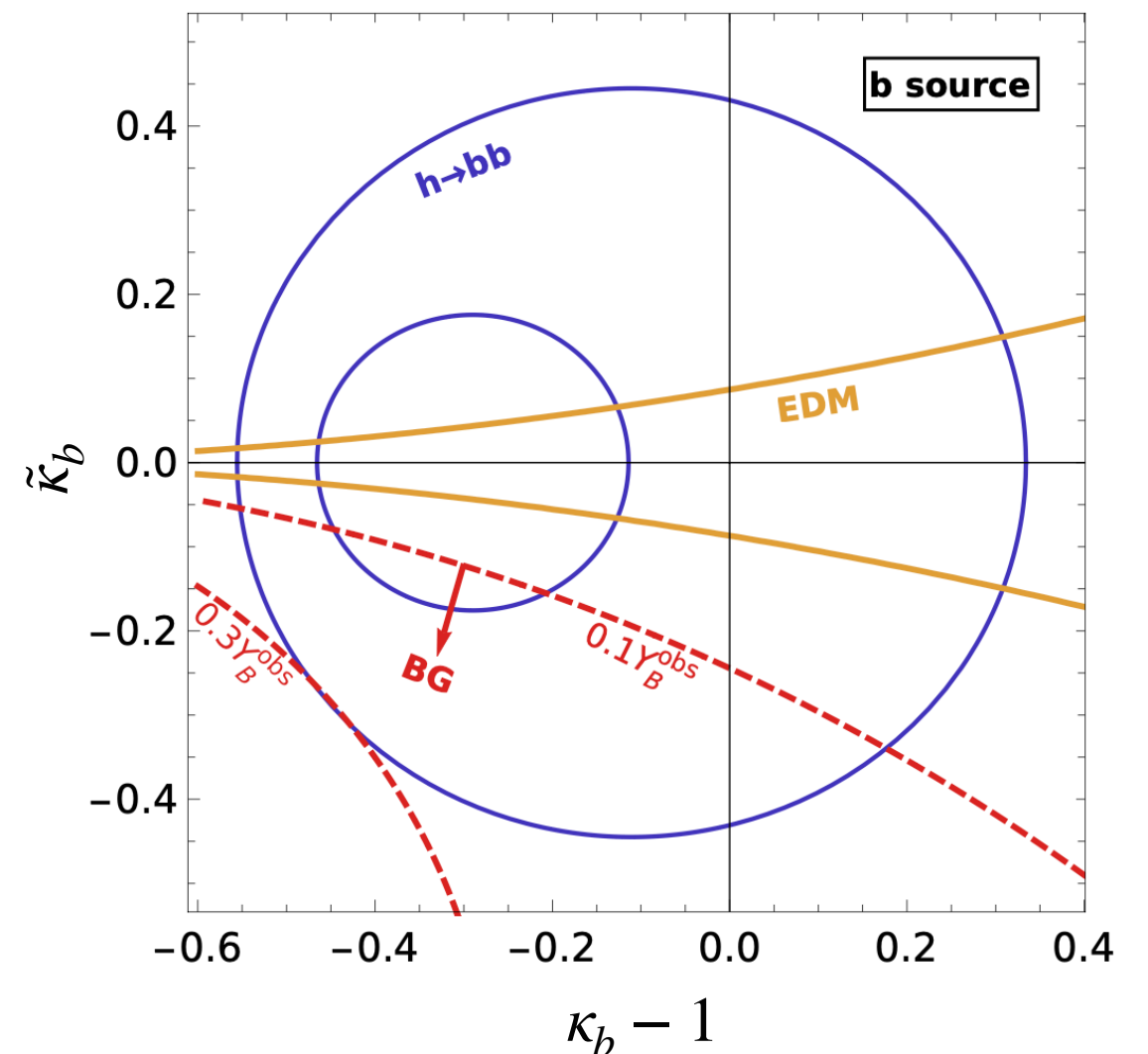
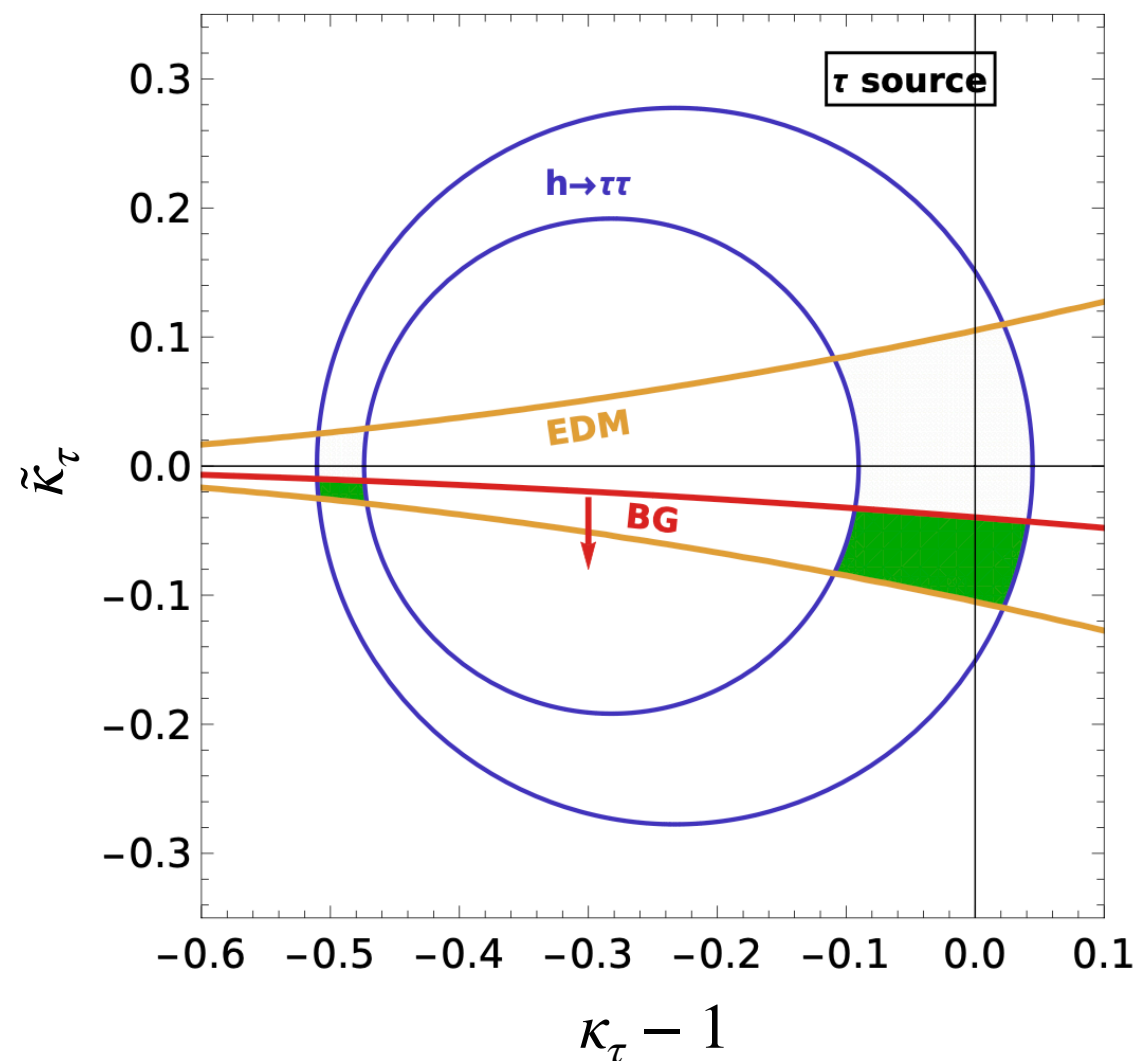
Fuchs, Losada, Nir, Viernik, 1911.08495, 2003.00099

- if EW baryogenesis assumed to be dominated by dim 6 Yukawas
 - \Rightarrow lower limit on CPV Yukawas, κ_f
- additional assumptions:
 - there are additional d.o.f.s that give strongly first-order EWPT
 - these do not change SM fermion interact. in the bubble wall
 - no other (relevant) sources of CPV
- tau $\tilde{\kappa}_\tau \neq 0$ can explain EWBG, but not top or bottom
 - reduced wash-out since no strong sphalerons for tau lepton
 - large lepton diffusion coeffs. lead to efficient diffusion of baryon asymmetry into the broken phase
 - overcompensate the smaller τ -Yukawa coupling

CONNECTION TO BARYOGENESIS

Fuchs, Losada, Nir, Viernik, 2003.00099

- $\tilde{\kappa}_\tau \sim 0.01 - 0.1$ required for successful EWBG
- corresponds to $\Lambda/\sqrt{\lambda'_{\tau\tau}} \lesssim 18 \text{ TeV} \sqrt{0.01/\tilde{\kappa}_\tau}$



2HDM EXAMPLE: SEQUESTERED MASS GENERATION

- two Higgs doublets, neutral compts: $\phi, \phi',$ vevs v, v'
 - ϕ couples to 3rd family, ϕ' to all three

$$\tan \beta = v/v'$$

$$M^l = \begin{pmatrix} \text{X} & \text{X} & \text{X} \\ \text{X} & \text{X} & \text{X} \\ \text{X} & \text{X} & \text{X} \end{pmatrix}$$

Diagram illustrating the mass matrix M^l structure. The matrix is a 3x3 grid. The top two rows and columns are marked with red 'X's, indicating contributions from ϕ' . The bottom row and column are marked with blue 'X's, indicating contributions from ϕ and ϕ' . Arrows point from the labels ϕ' and ϕ and ϕ' to the corresponding entries in the matrix.

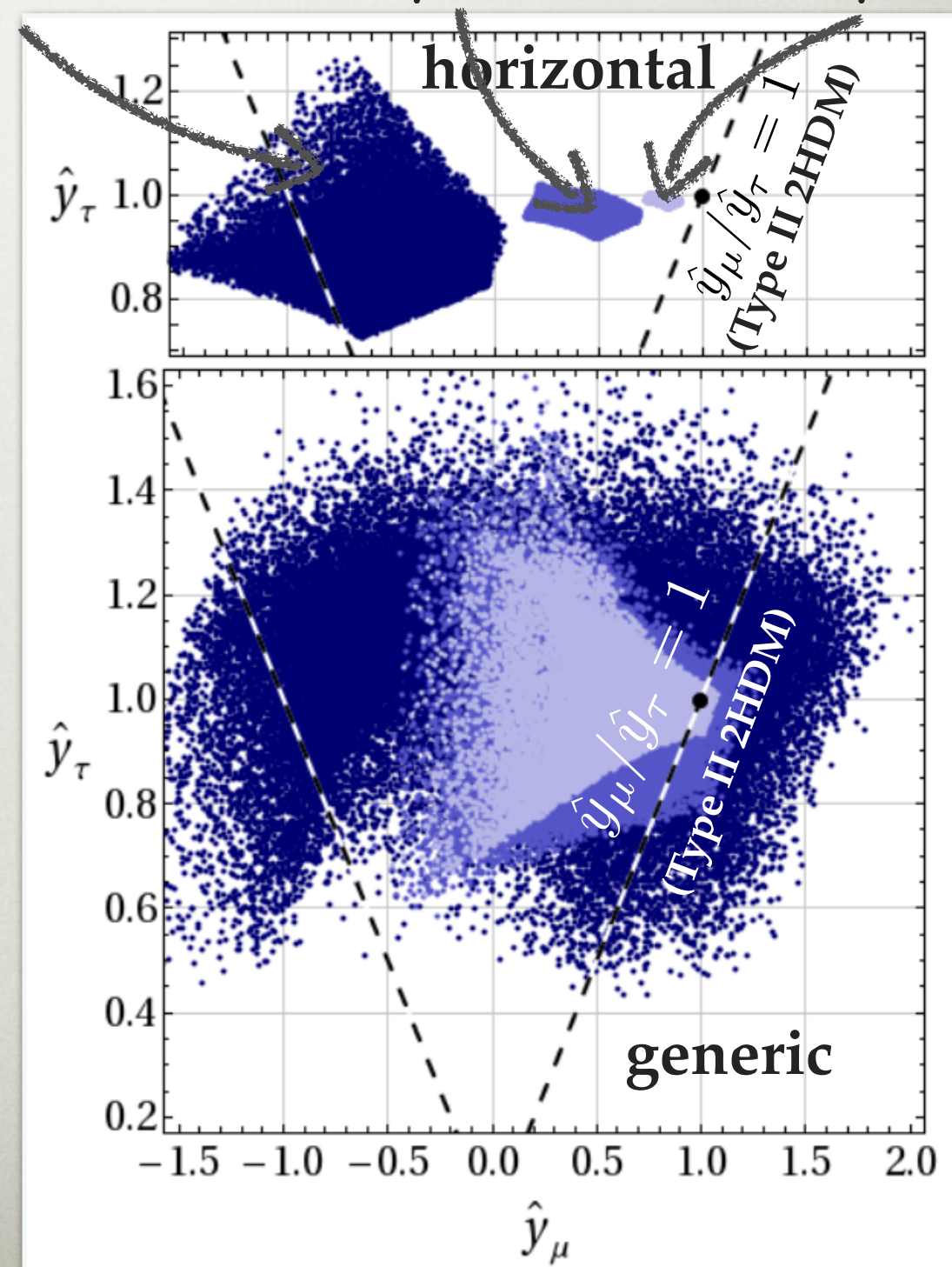
- a hierarchy of vevs $v \gg v'$ can explain $m_\tau \gg m_\mu$
- consider two flavor structures for ϕ' contribs. to M^l
 - “horizontal”: only off-diagonal entries nonzero
 - “generic”: all m_{ij}' nonzero

DIAGONAL YUKAWAS

CMS: $Br(h \rightarrow \tau\mu) < 0.15\%$

$Br(h \rightarrow \tau\mu) = 0.84\%$ $Br(h \rightarrow \tau\mu) = 0.28\%$ $Br(h \rightarrow \tau\mu) = 0.08\%$

- scanning over mass matrix entries and imposing:
 - that m_μ, m_τ are eigenvalues
 - the heavy Higgs xsec bounds
- ratios $\kappa_\mu < 1$ and $\kappa_\mu/\kappa_\tau < 1$ favored
- sizeable flavor violating $Br(h \rightarrow \tau\mu)$

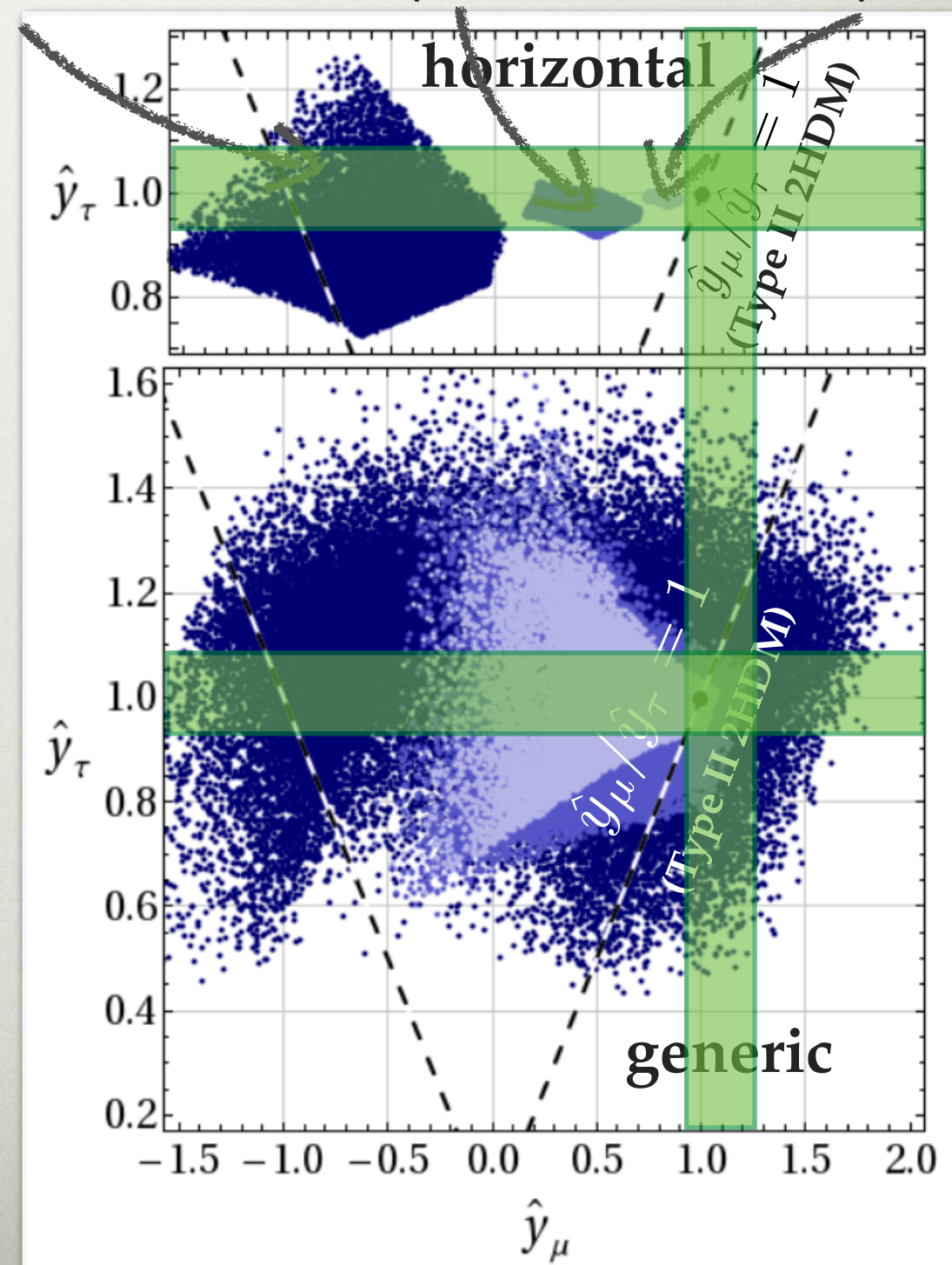


DIAGONAL YUKAWAS

CMS: $Br(h \rightarrow \tau\mu) < 0.15\%$

$Br(h \rightarrow \tau\mu) = 0.84\%$ $Br(h \rightarrow \tau\mu) = 0.28\%$ $Br(h \rightarrow \tau\mu) = 0.08\%$

- scanning over mass matrix entries and imposing:
 - that m_μ, m_τ are eigenvalues
 - the heavy Higgs xsec bounds
- ratios $\kappa_\mu < 1$ and $\kappa_\mu/\kappa_\tau < 1$ favored
- sizeable flavor violating $Br(h \rightarrow \tau\mu)$



MAGNETIC AND ELECTRIC DIPOLE MOMENTS

- two flavor diagonal dimension 5 operators

$$\mathcal{L}_{\text{eff}} \supset -\frac{ea_\ell}{4m_\ell} (\bar{\ell}\sigma^{\mu\nu}\ell) F_{\mu\nu} - \frac{d_\ell}{2} (\bar{\ell}\sigma^{\mu\nu}i\gamma_5\ell) F_{\mu\nu}$$

- anomalous magnetic moment $(g - 2)_\ell = 2a_\ell$
 - CP conserving
 - SM value nonzero
- electric dipole moment d_ℓ
 - CP violating
 - SM value highly suppressed

POSSIBLE DEVIATION

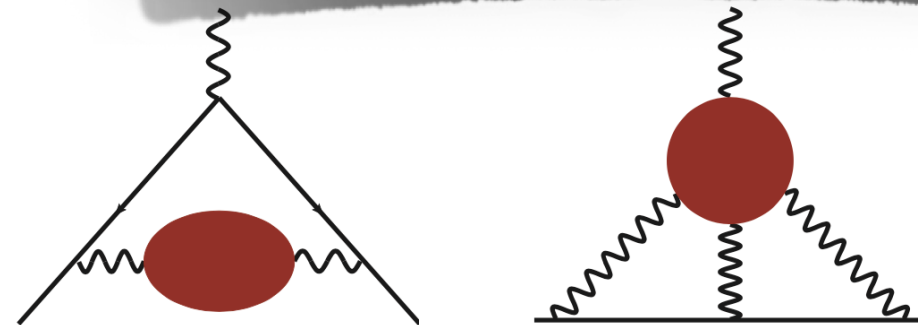
IN $(g - 2)_\mu$

- the value of $(g - 2)_\mu$ from g-2 coll.

$$a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 251(59) \times 10^{-10}$$

- the SM theory error dominated by hadronic uncert.

$$a_\mu^{\text{SM}} = 116591810(43) \times 10^{-10}$$



QED

Electroweak

HVP (e^+e^- , LO + NLO + NNLO)

HLbL (phenomenology + lattice + NLO)

Total SM Value

116 584 718.931(104)

153.6(1.0)

6845(40)

92(18)

116 591 810(43)

IF NEW PHYSICS...

- $(g - 2)_\mu$ showing 4.2σ deviation from the SM
 - in SMEFT from dim6 operator

$$\mathcal{L} \supset -\frac{\sqrt{2}e v}{(4\pi\Lambda_{ij})^2} \bar{\ell}_L^i \sigma^{\mu\nu} \ell_R^j F_{\mu\nu} + \text{h.c.} ,$$

$$(g - 2)_\mu \Rightarrow \Lambda_{22} \sim 15 \text{ TeV}$$

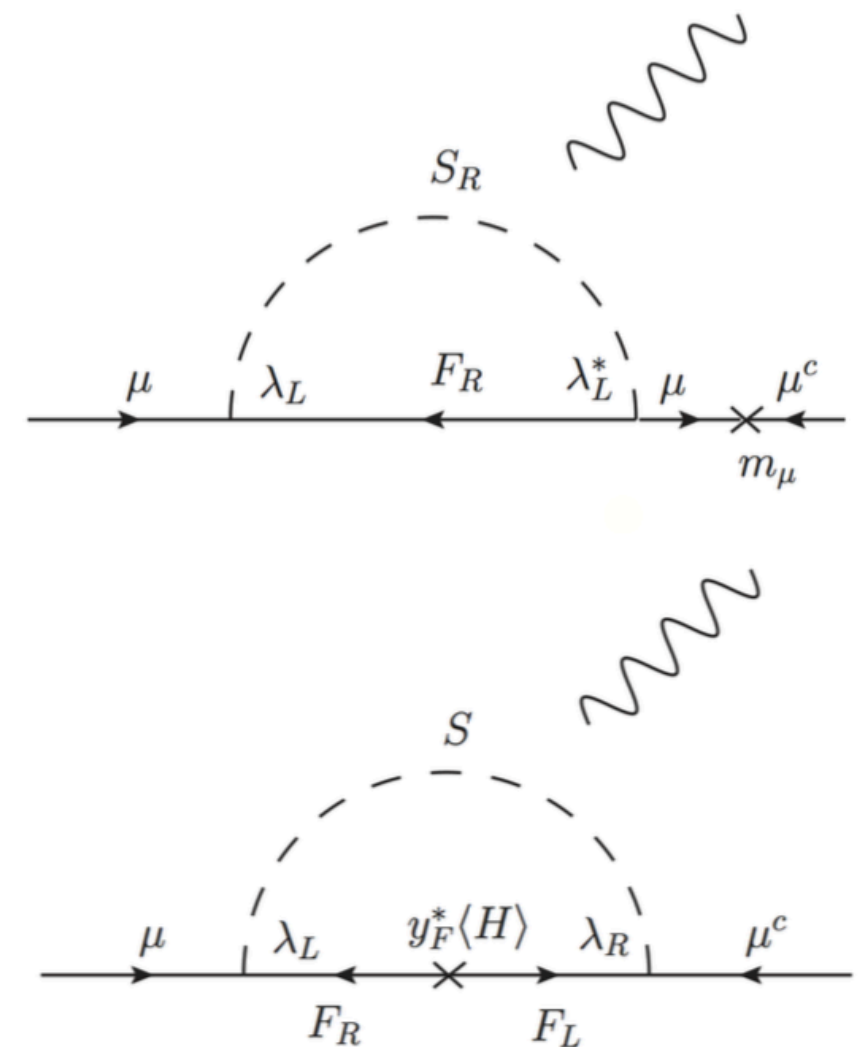
- note: any flavor violation needs to be highly suppressed $\mu \rightarrow e\gamma \Rightarrow \Lambda_{21} \gtrsim 3500 \text{ TeV}$ [Greljo, Stangl, Thomsen, 2103.13991](#)
- a possible (natural) solution - a symmetry
 - a phenomenologically viable example: $L_\mu - L_\tau$

$(g - 2)_\mu$ NEW PHYSICS MODELS

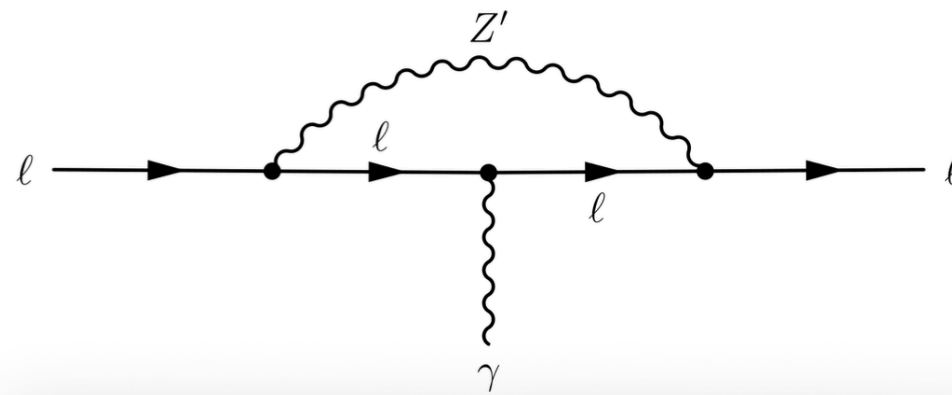
$$a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 251(59) \times 10^{-10}$$

- NP models of two types
- chirality flip on SM fermion leg
 - NP need to be light,
example: Z' from $L_\mu - L_\tau$
- chirality flip can be on the NP fermion leg
 - NP can be much heavier
 - example: minimal models with DM

$$\frac{e}{8\pi^2} (\bar{\mu} \sigma^{\mu\nu} \mu) F_{\mu\nu}$$



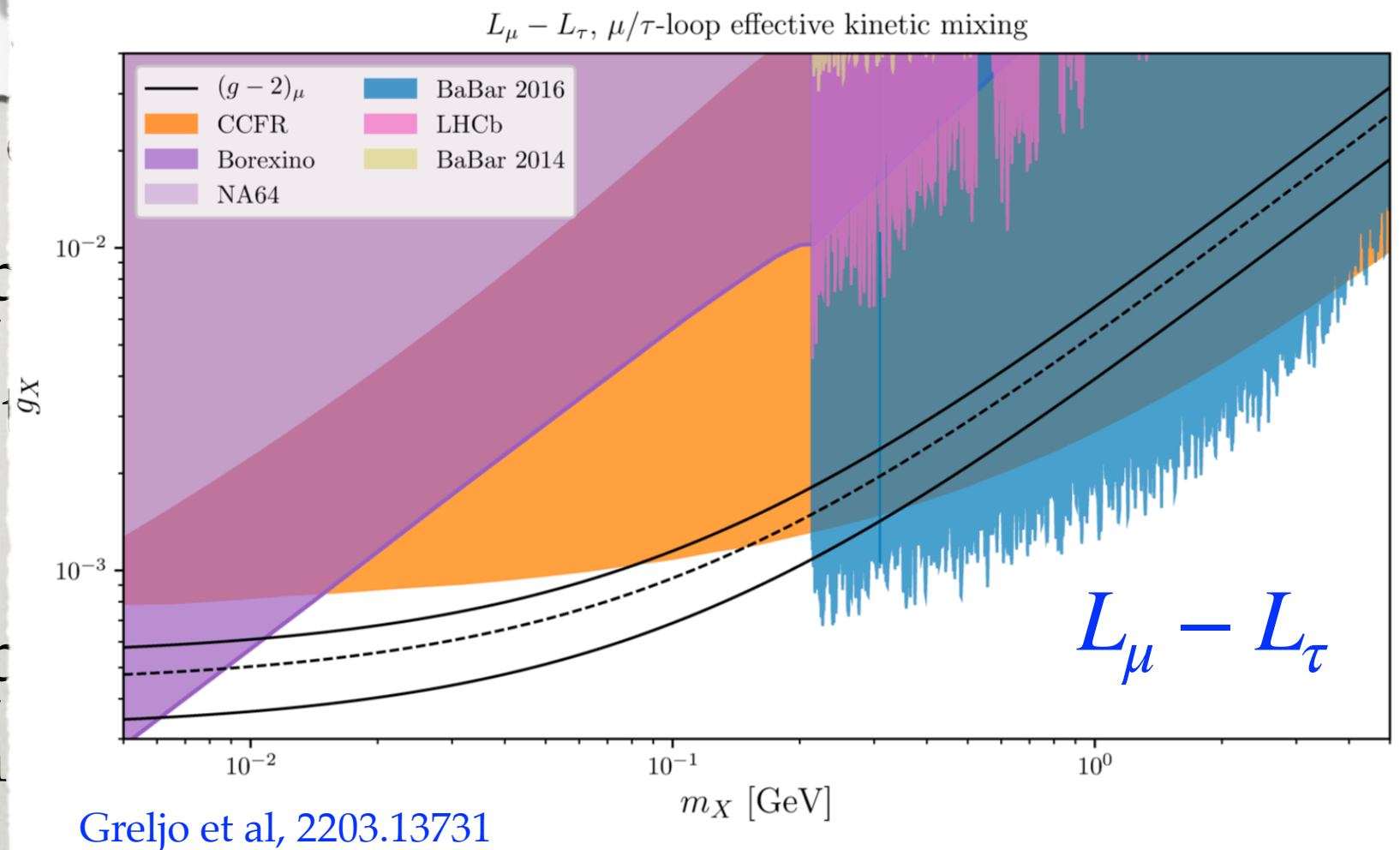
$$(g - 2)_\mu$$



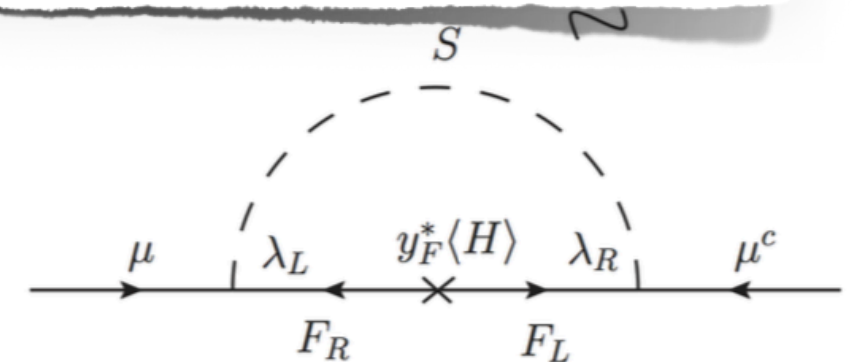
MODELS

$$a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 251$$

- NP models
- chirality flip
 - NP need example:
- chirality flip NP fermion



- NP can be much heavier
- example: minimal models with DM

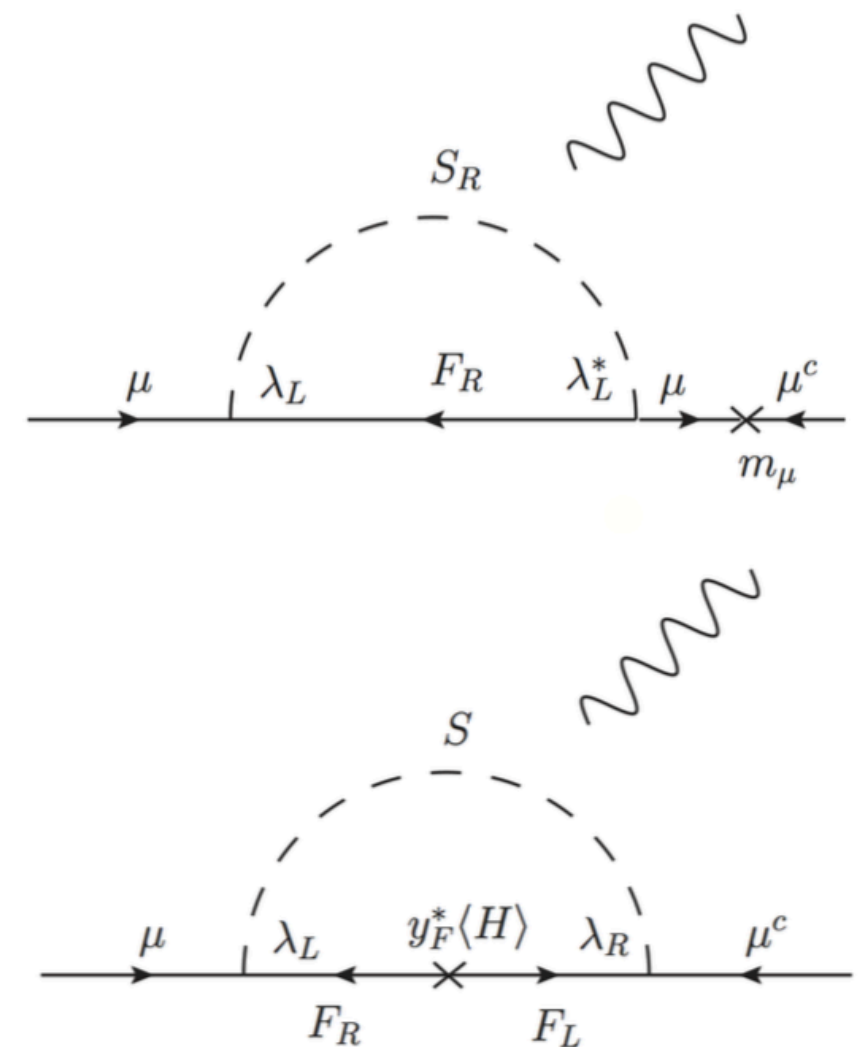


$(g - 2)_\mu$ NEW PHYSICS MODELS

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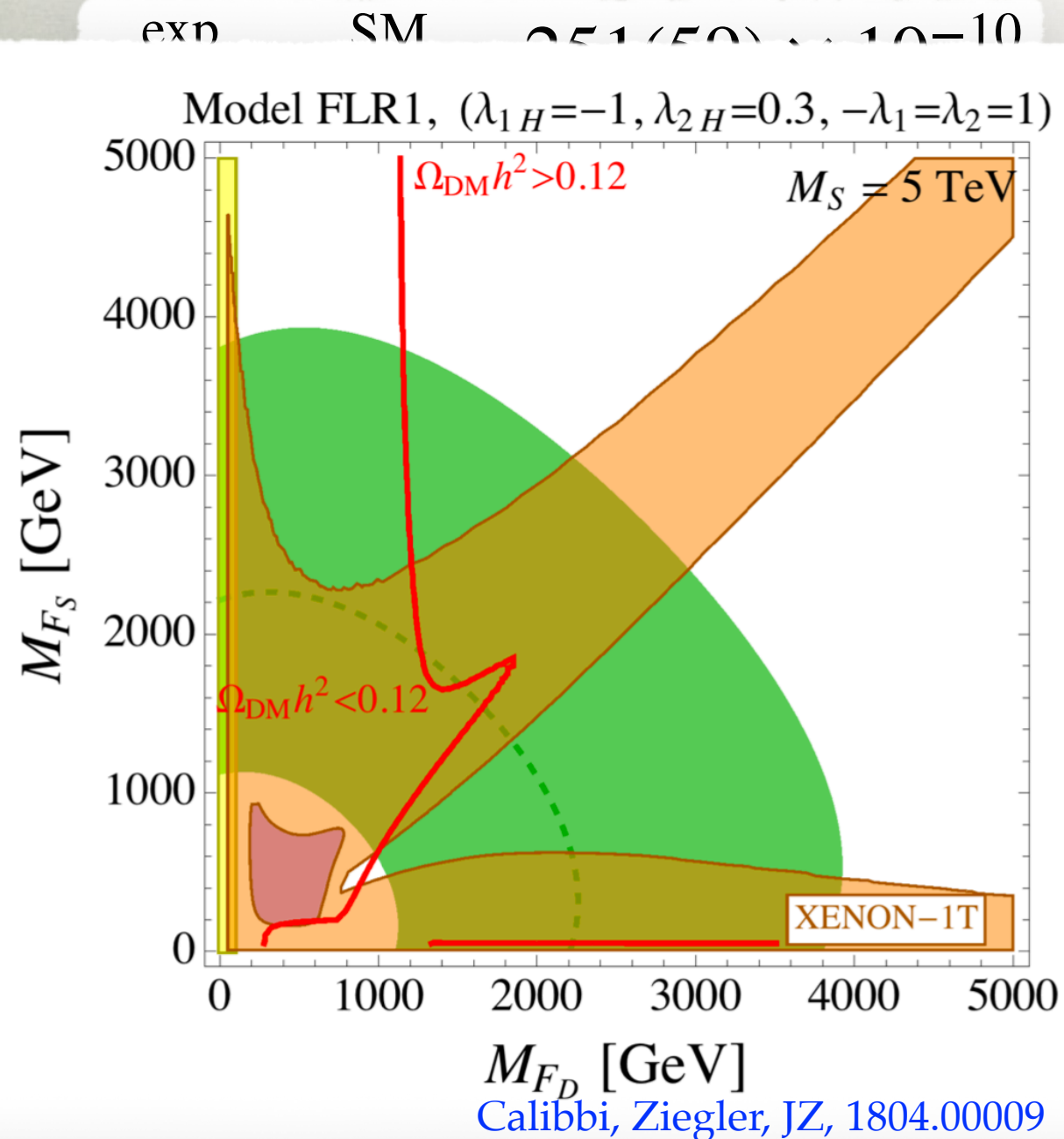
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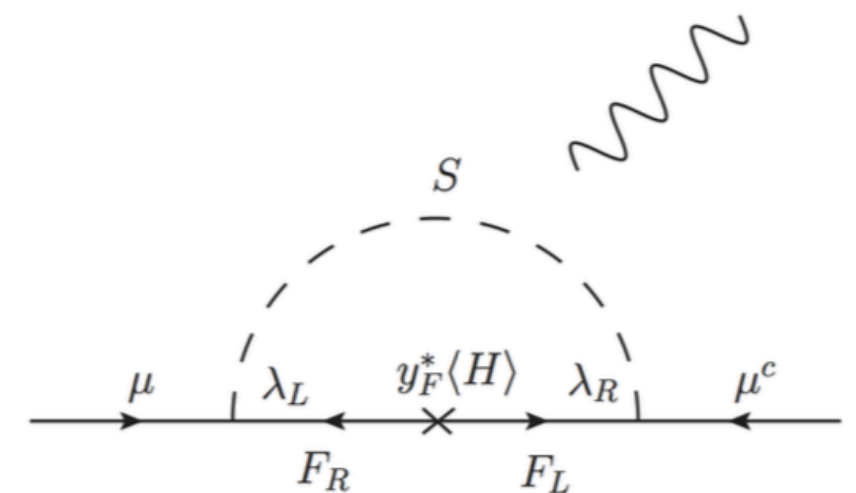
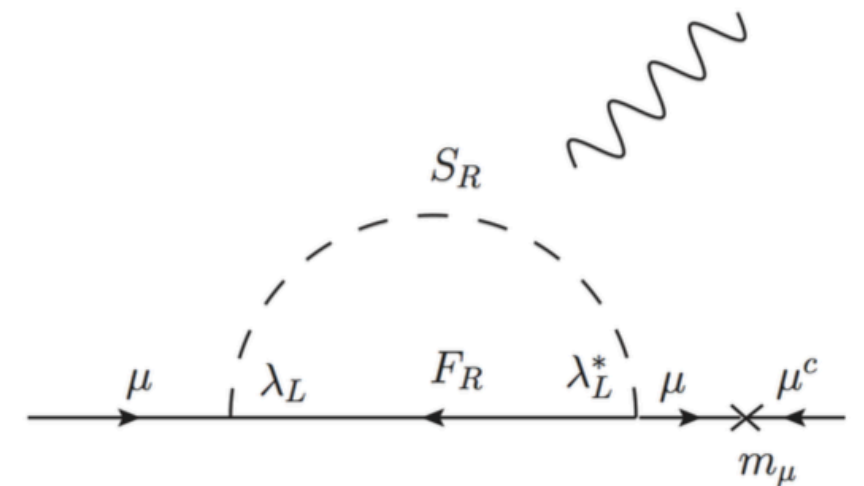
ion leg

L_τ

e

er

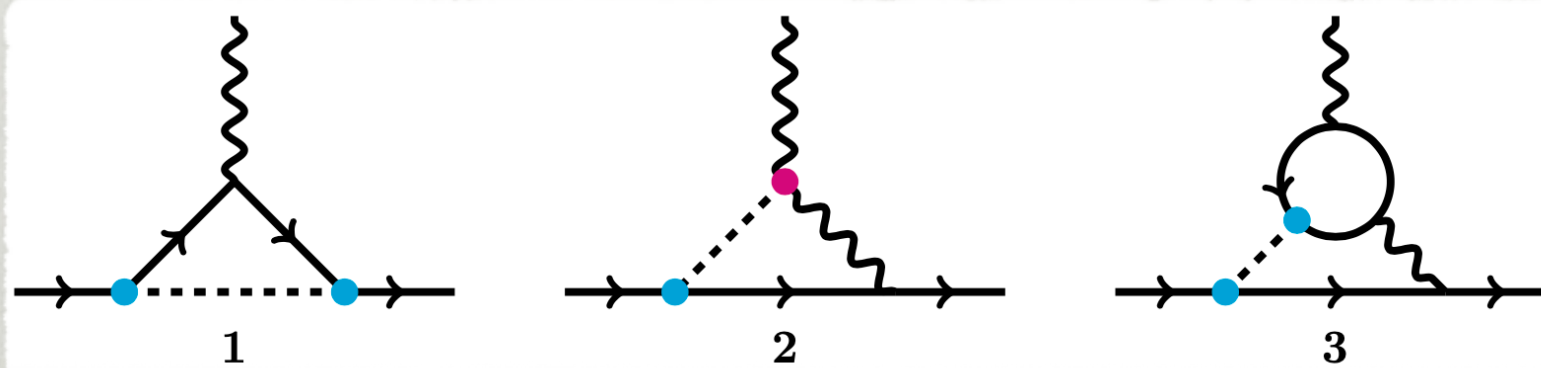
odels



$$F_S \equiv F_R \sim 1_0, \quad F_D \equiv F_L \sim 2_{-1/2}, \quad F_D^c \equiv F_L^c \sim 2_{1/2}^*, \quad S \equiv S_R \sim 2_{1/2},$$

FLAVOR DIAGONAL ALP?

- ALP coupling to muons gives wrong sign contrib. to Δa_μ

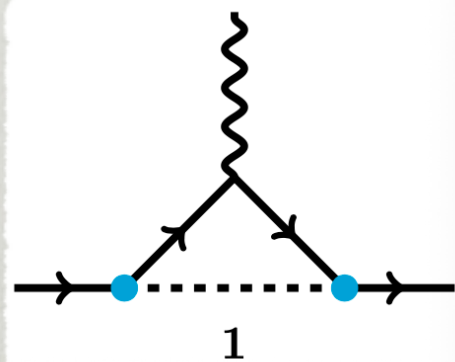


$$\Delta a_\mu^{(1)} \propto -\frac{c_{\mu\mu}^2}{16\pi^2}, \quad \Delta a_\mu^{(2)} \propto -\frac{c_{\mu\mu}c_{\gamma\gamma}\alpha}{16\pi^3}, \quad \Delta a_\mu^{(3)} \propto -\frac{c_{\mu\mu}c_{ii}\alpha}{16\pi^3},$$

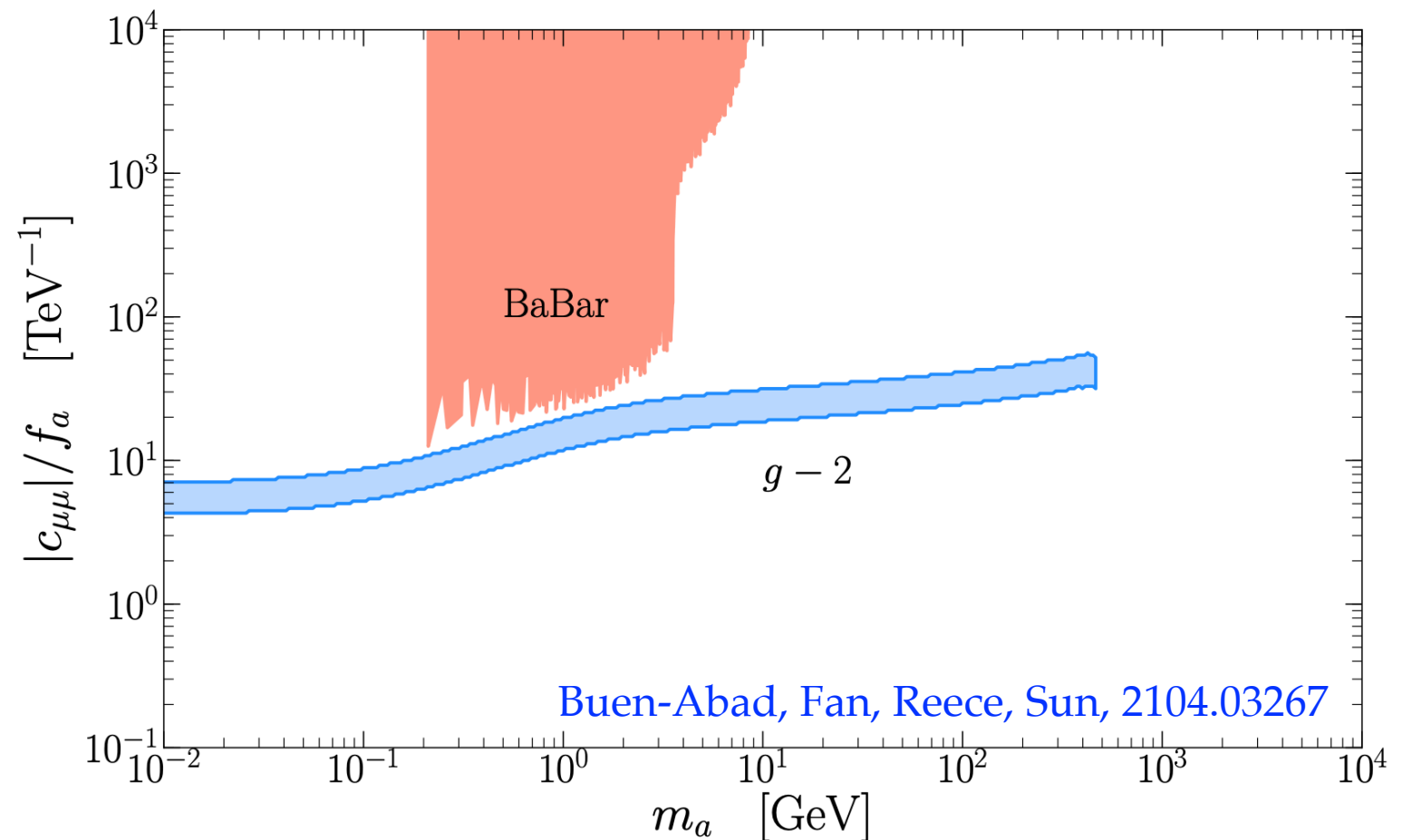
- need to compensate with $aF\tilde{F}$ coupling at 1-loop, and with 2-loop contris
- the scale required to explain Δa_μ anomaly low, $f_a \sim 100$ GeV
- difficult model building
- note: at the same order, $1/f_a^2$, expect other contris. to a_μ from UV

FLAVOR

- ALP coupling to muon



$$\Delta a_\mu^{(1)} \propto -\frac{c_{\mu\mu}^2}{16\pi^2},$$

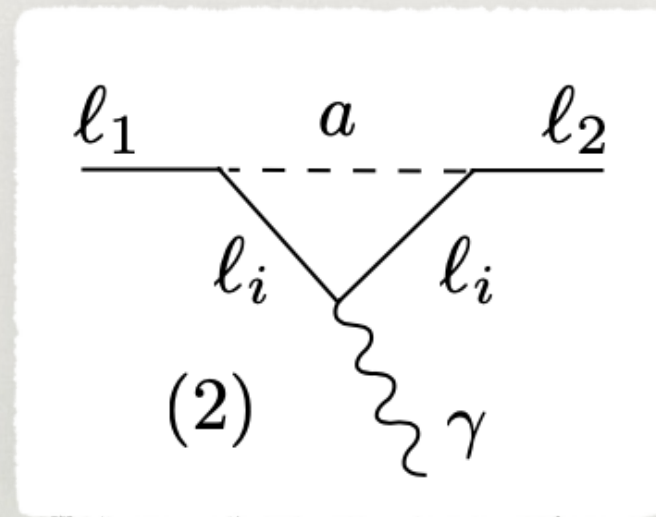


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FLAVOR VIOLATING ALP

FOR $(g - 2)_\mu$

- FV coupling $c_{e\mu}^A$ gives the right sign of Δa_μ for $m_a > m_\mu$

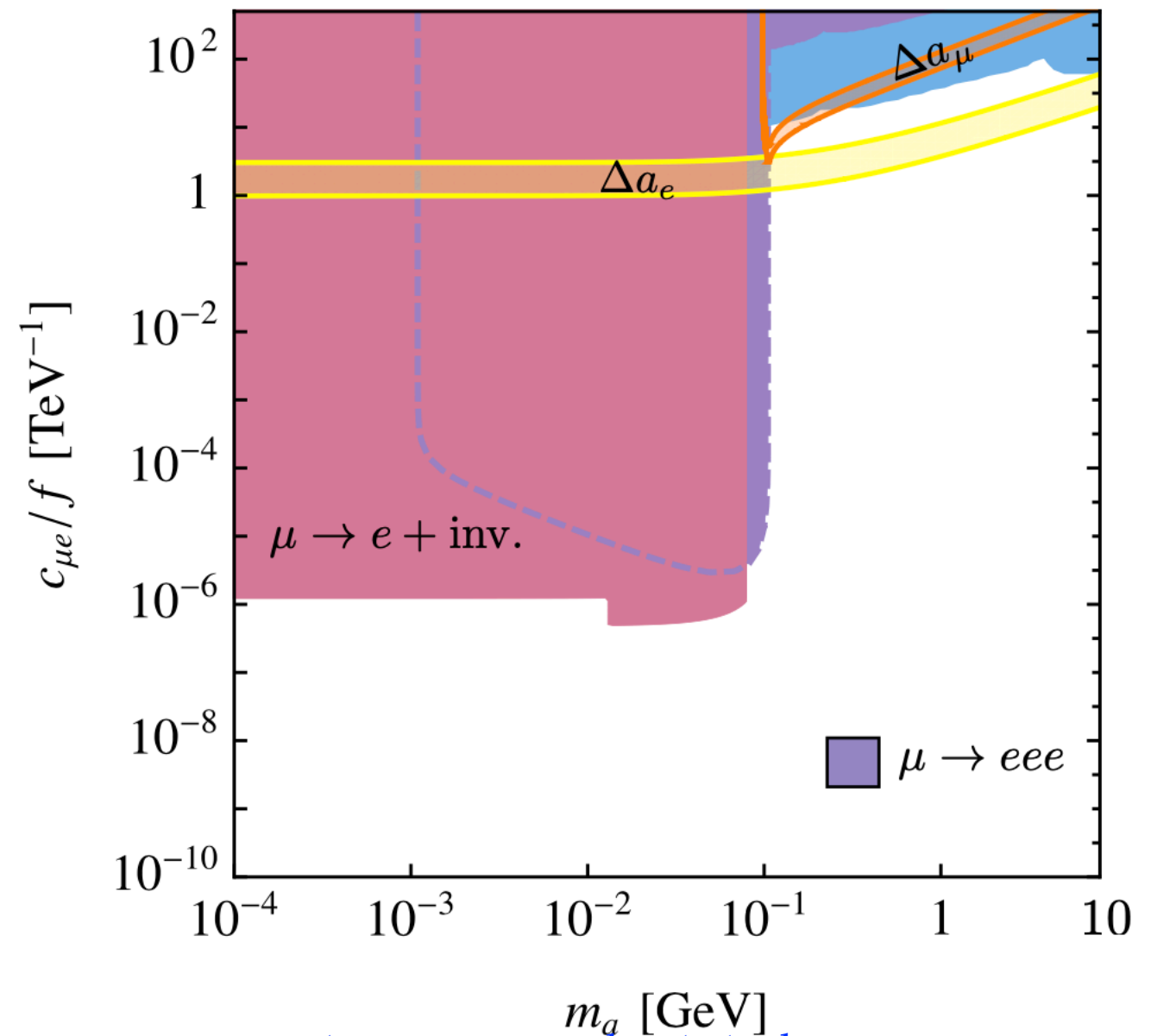
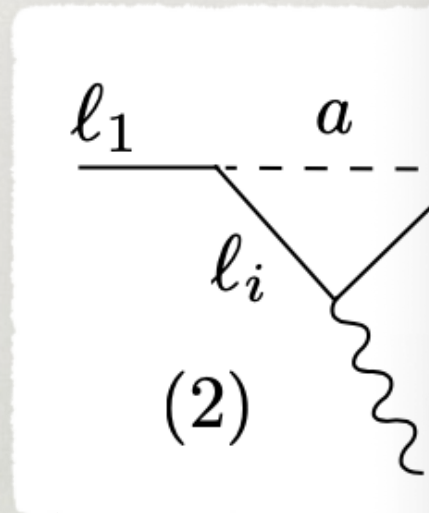


- same model building challenge: low f_a
- a possible way out: couple μ off-diagonally to heavy vector-like fermions E_i, L_i
 - chirality flip from internal E_i, L_i line \Rightarrow higher $f_a \gtrsim 1 \text{ TeV}$

Brdar, Jana, Kubo, Lindner, 2104.03282

FLAVOR VIO FOR

- FV coupling $c_{e\mu}^A$ give
 $m_a > m_\mu$



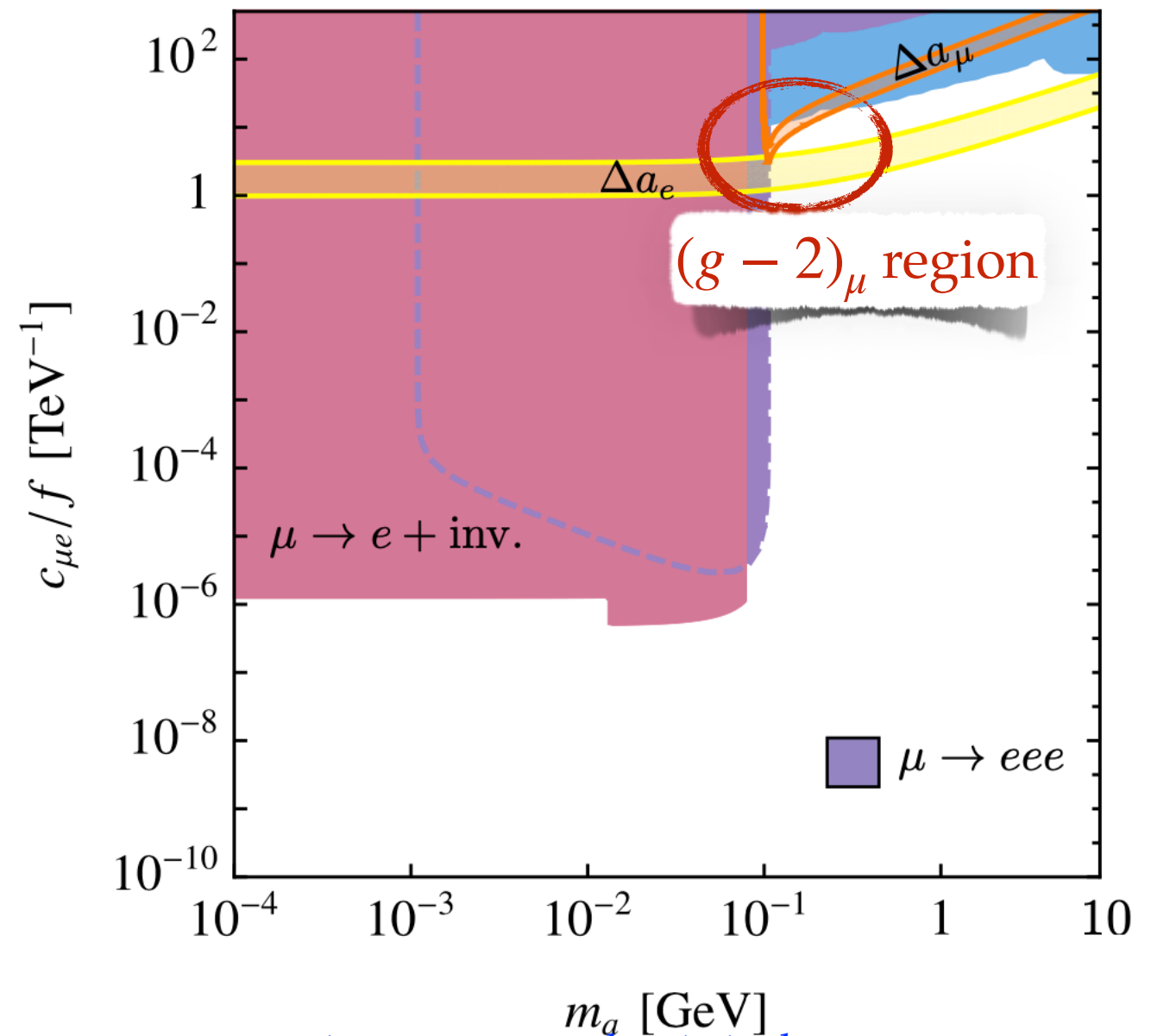
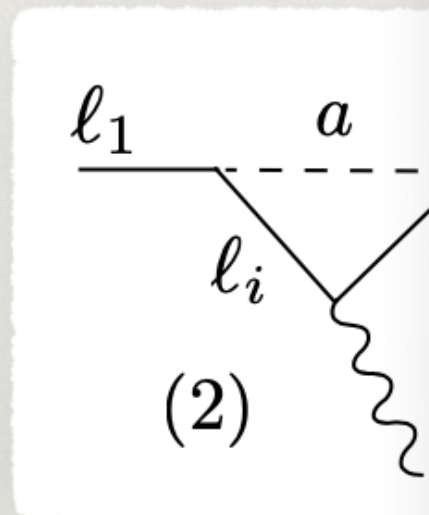
Bauer, Neubert, Renner, Schnubel, Thamm, 1908.00008

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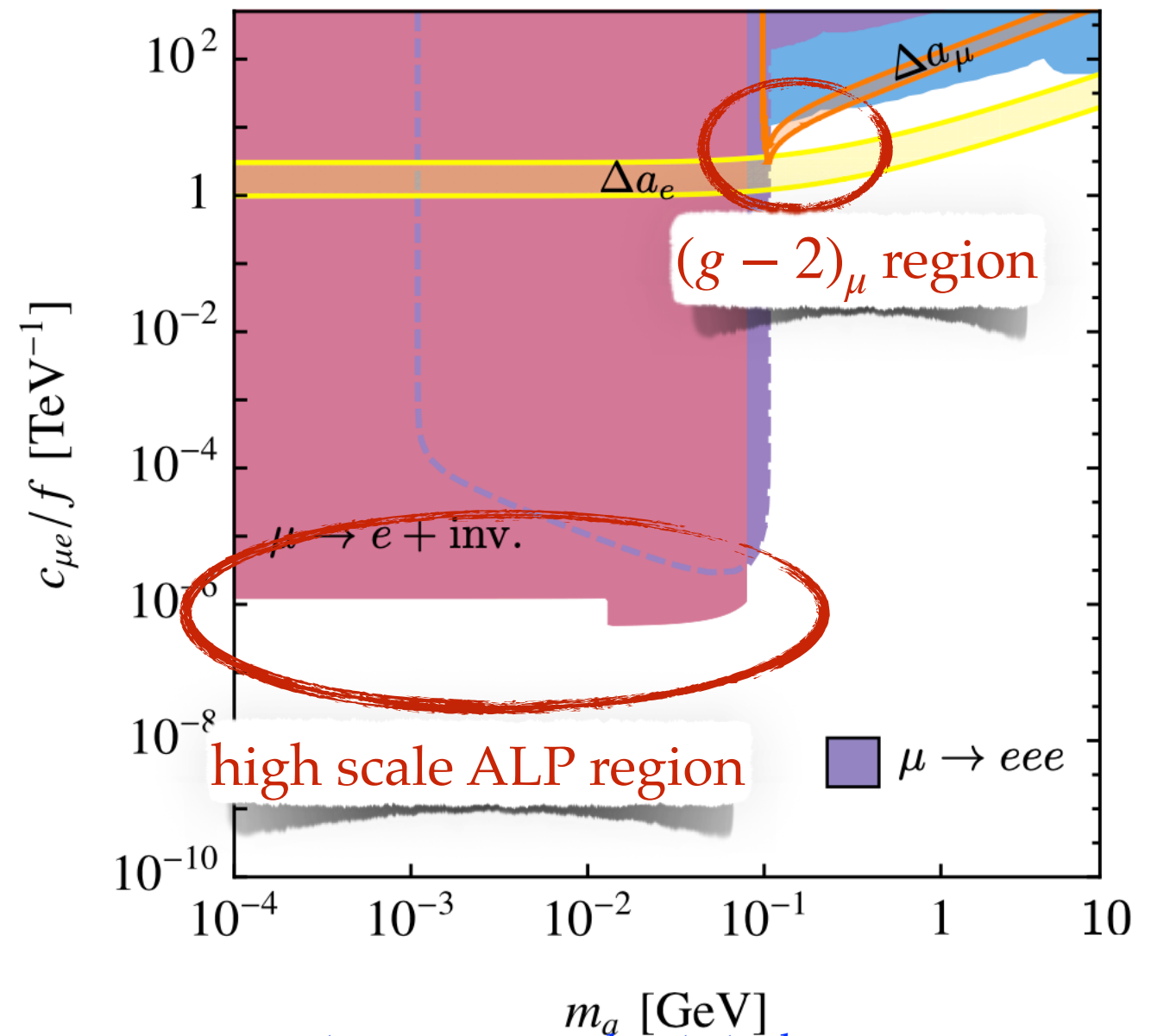
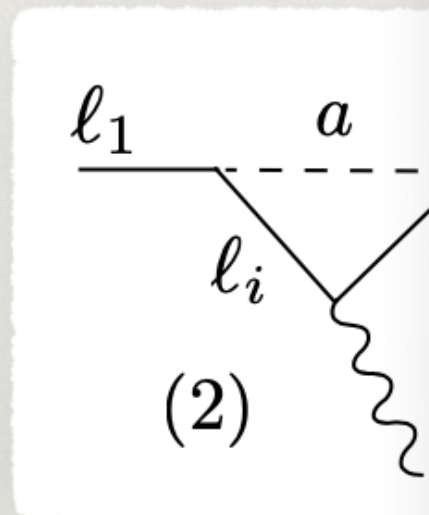
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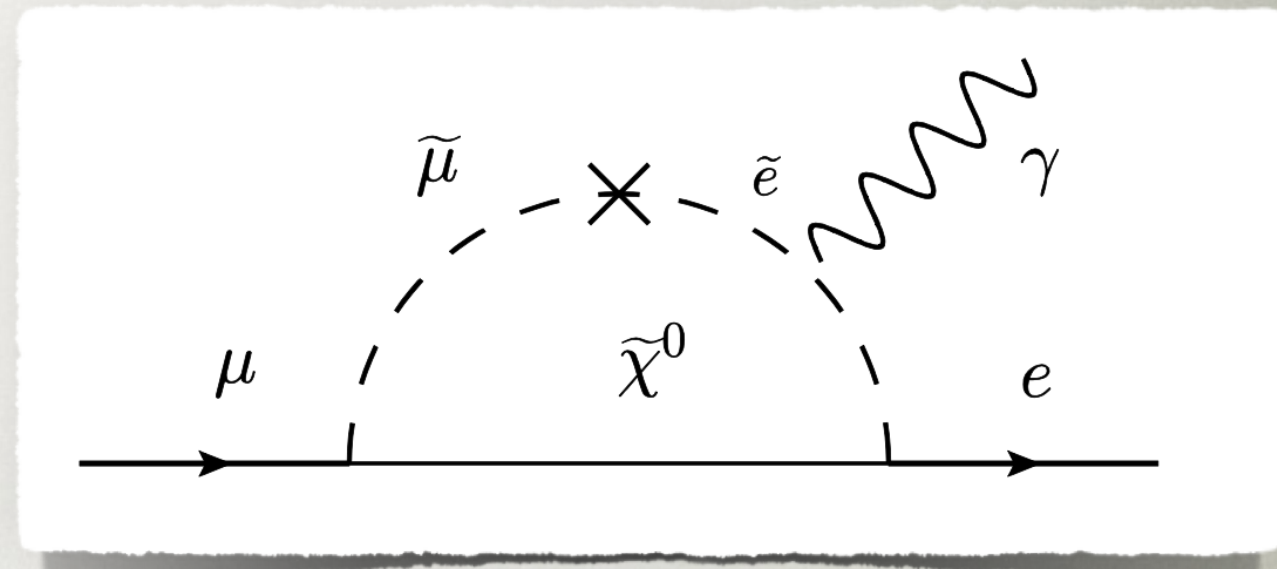
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Brdar, Jana, Kubo, Lindner, 2104.03282

SUPERSYMMETRIC SEE-SAW

- the dominant LFV contribution comes from dipole operators ("photon penguin")



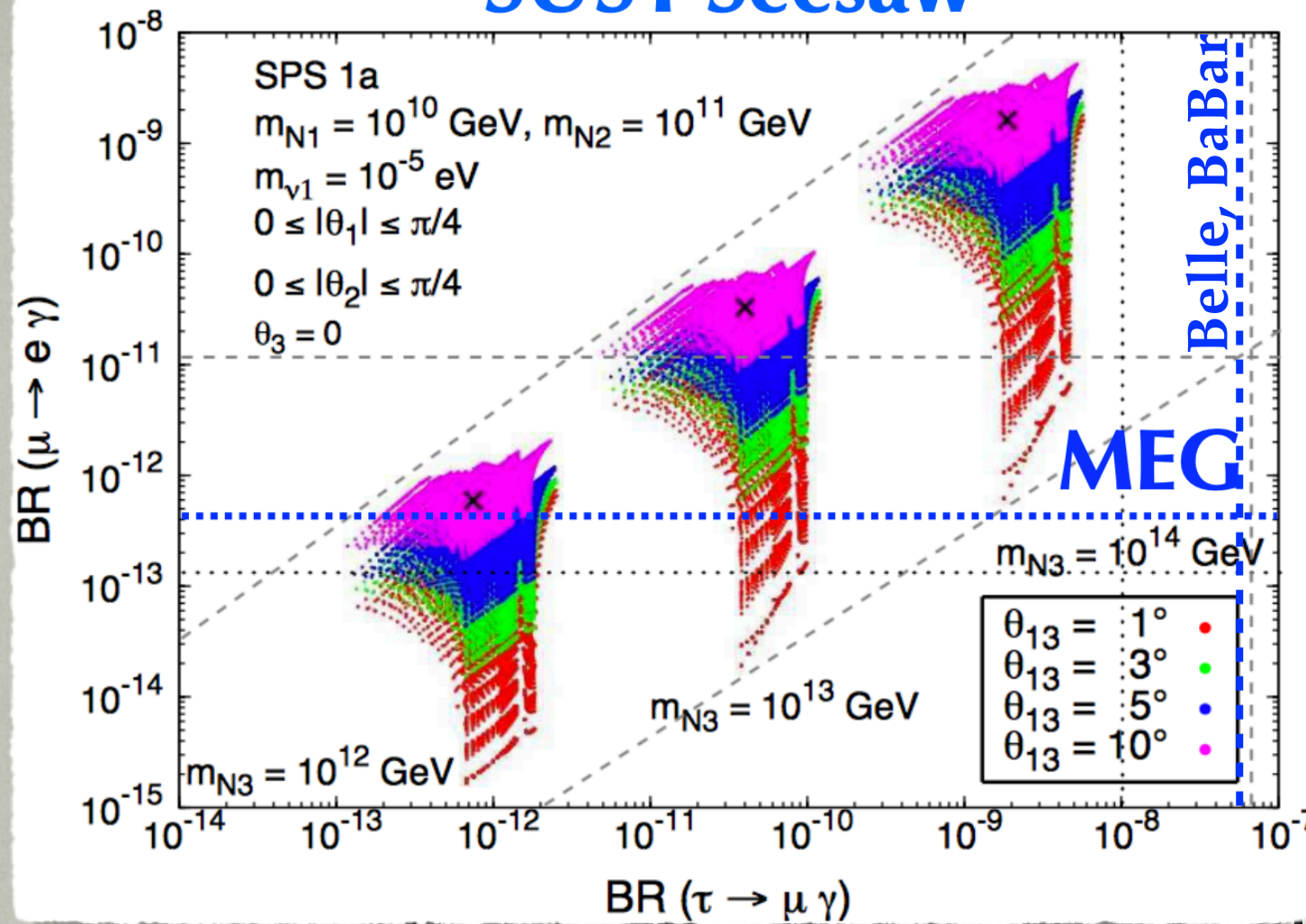
- the $\ell_j \rightarrow 3\ell_i$ are thus given by

[Antusch et al., hep-ph/0607263](#)

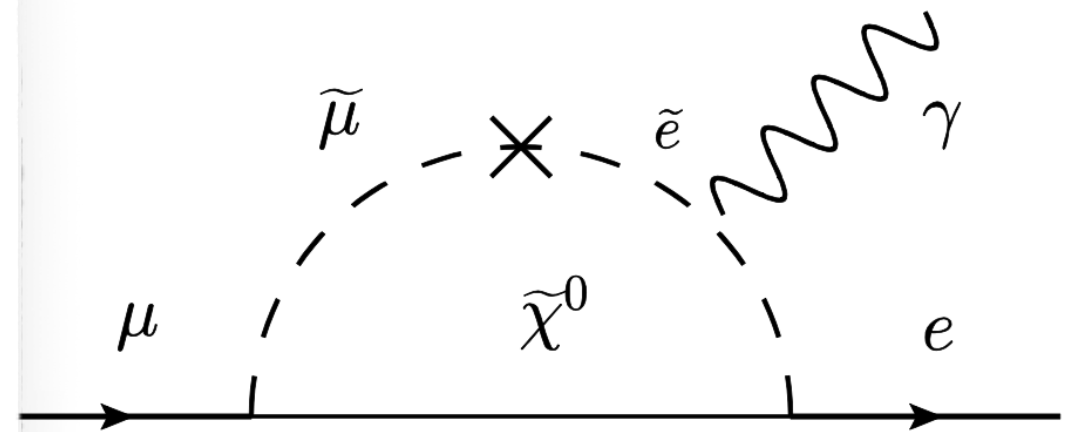
$$\text{BR}(\ell_j \rightarrow 3\ell_i) = \frac{\alpha}{3\pi} \left(\log \frac{m_{\ell_j}^2}{m_{\ell_i}^2} - \frac{11}{4} \right) \times \text{BR}(\ell_j \rightarrow \ell_i \gamma),$$

- because of restricted flavor structure there is also a relation between $\mu \rightarrow e\gamma$ and $\tau \rightarrow \mu\gamma$

SUSY-Seesaw



METRIC
W



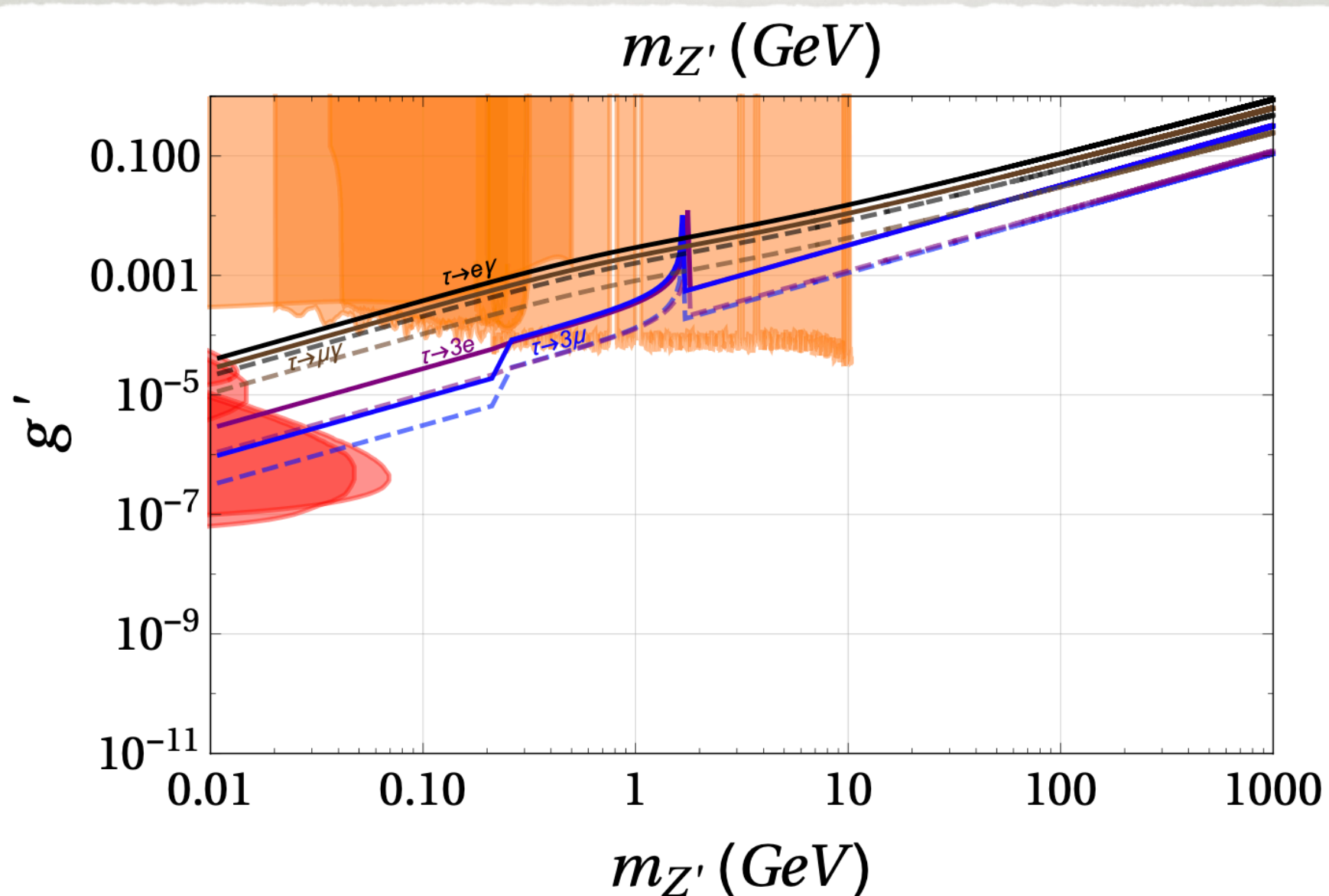
Antusch et al., hep-ph/0607263

$$\text{BR}(l_j \rightarrow 3l_i) = \frac{\alpha}{3\pi} \left(\log \frac{m_{l_j}^2}{m_{l_i}^2} - \frac{11}{4} \right) \times \text{BR}(l_j \rightarrow l_i \gamma),$$

- because of restricted flavor structure there is also a relation between $\mu \rightarrow e \gamma$ and $\tau \rightarrow \mu \gamma$

TAU DECAYS

- in this model tau decays less sensitive as discovery tool
- but essential to be measured in order to confirm the model

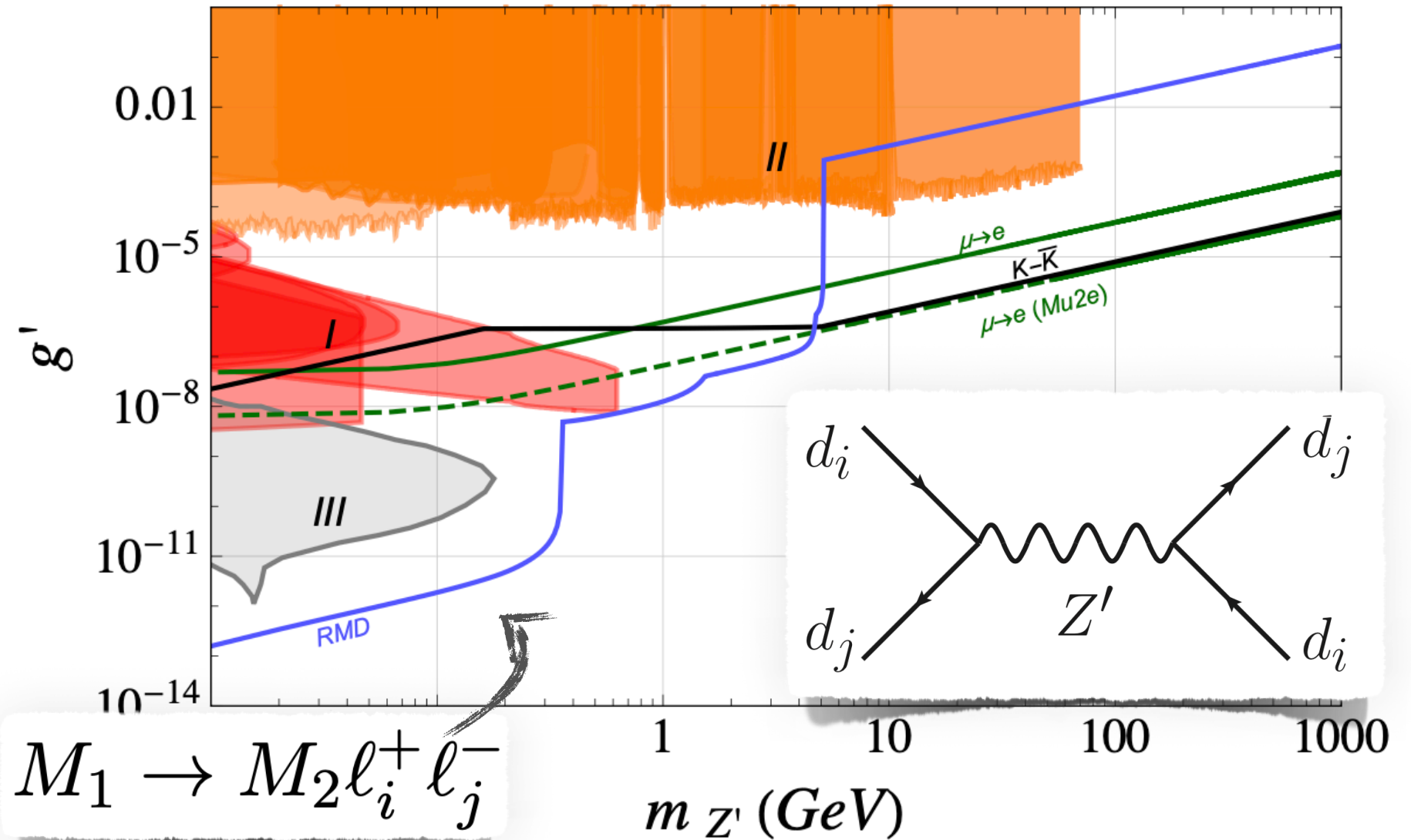


RARE MESON DECAYS

- so far a focus on LFV transitions with μ, τ in the initial state
- another possibility, use meson decays
 - $K^+ \rightarrow \pi^+ \mu^+ e^-, B^+ \rightarrow K^+ \mu^+ e^-, \dots$
- an example already shown is Z' in $U(1)_{\text{FN}}$
 - if tree-level mediator off-shell \Rightarrow meson mixing or LFV FCNCs more constrained
 - for on-shell Z' on the other hand $M_i \rightarrow M_j Z'$ gives the leading constraints
 - note: Z' may decay through flavor conserving mode, so searches such as $B \rightarrow K \mu^+ \mu^-$ also relevant

RA

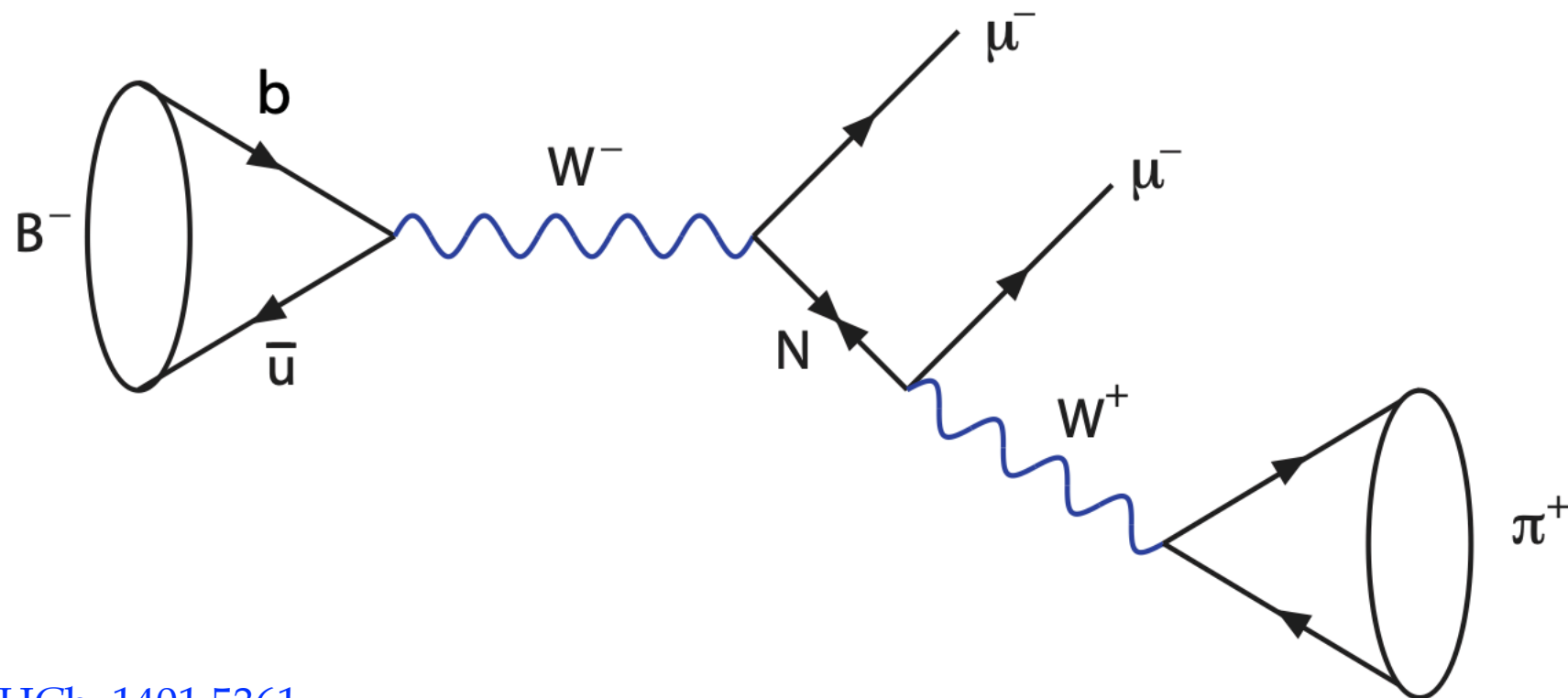
- so far a f
- another p
- $K^+ \rightarrow$
- an exam
- if tree-FCNCs more constrained



- for on-shell Z' on the other hand $M_i \rightarrow M_j Z'$ gives the leading constraints
- note: Z' may decay through flavor conserving mode, so searches such as $B \rightarrow K \mu^+ \mu^-$ also relevant

MAJORANA NEUTRINOS

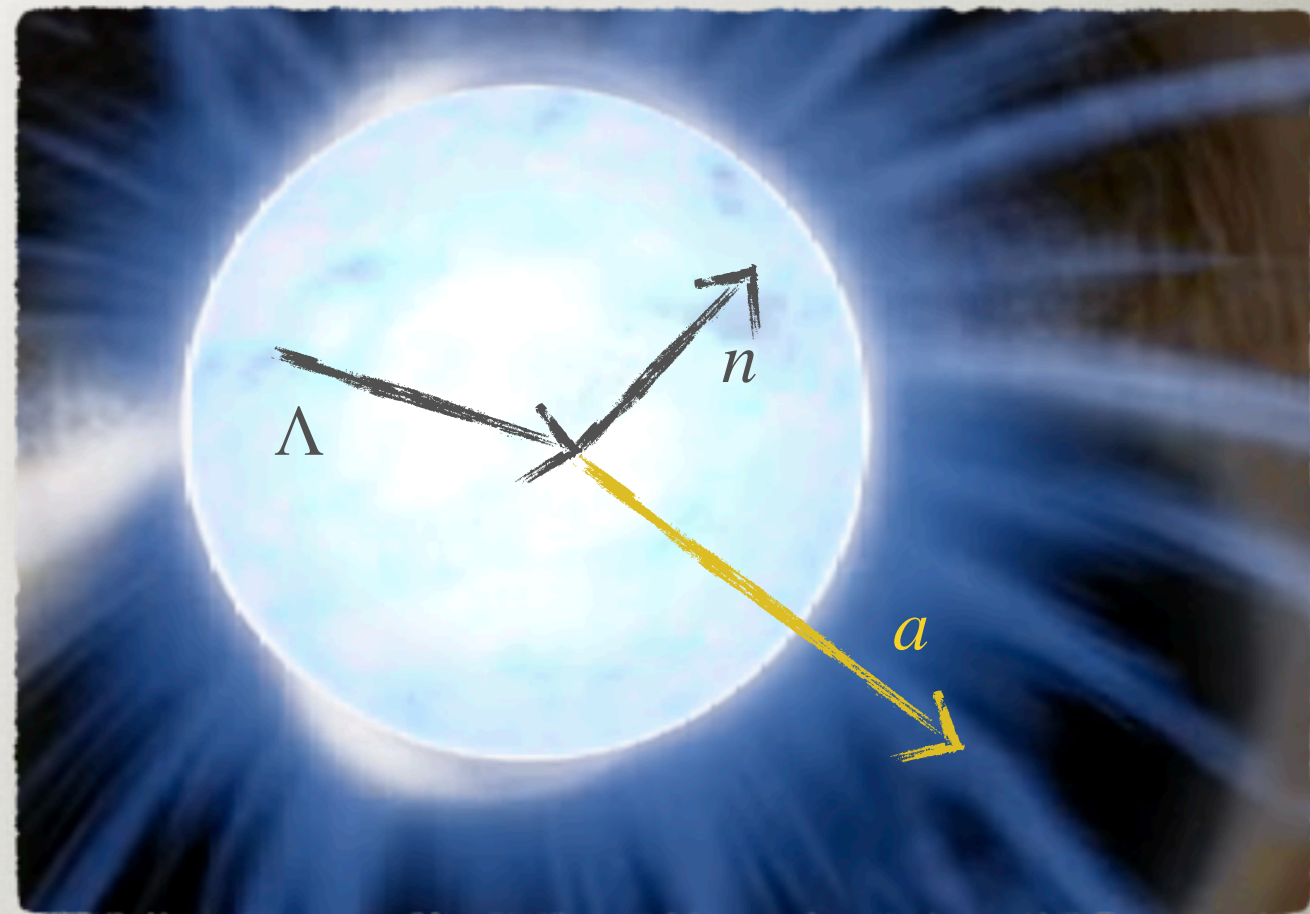
- if neutrinos Majorana fermions then lepton number violating decays possible
- leptons can be of same flavor, $B^- \rightarrow \pi^+ \mu^- \mu^-$, or different flavor, $B^- \rightarrow \pi^+ \mu^- e^-$, $B^- \rightarrow \pi^+ \mu^- \tau^-$, ...



[LHCb, 1401.5361](#)

SUPERNOVA BOUNDS

- in neutron star Λ , n , p , e are in equilibrium
- $\Lambda \rightarrow na$ decays can cool the proto-neutron star
- Λ , n have the same Fermi energy \Rightarrow at $T=0$ Pauli blocking forbids $\Lambda \rightarrow na$ decays
- at finite temperature volume emission rate (in NR limit)



$$Q \simeq n_n (m_\Lambda - m_n) \Gamma(\Lambda \rightarrow na) e^{-\frac{m_\Lambda - m_n}{T}},$$

see also Camalich et al, 2012.11632

- assuming this is below neutrino emission rate 1sec after the collapse of SN1987A
 - bounds on $|F_{sd}^A|$ and $|F_{sd}^V|$ in the range $10^9 - 10^{10}$ GeV