

# R Measurements and QCD Studies at future super $\tau$ - $c$ factory

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RF3 session: Fundamental Physics in Small Experiments  
Snowmass Rare Processes and Precision Frontier meeting

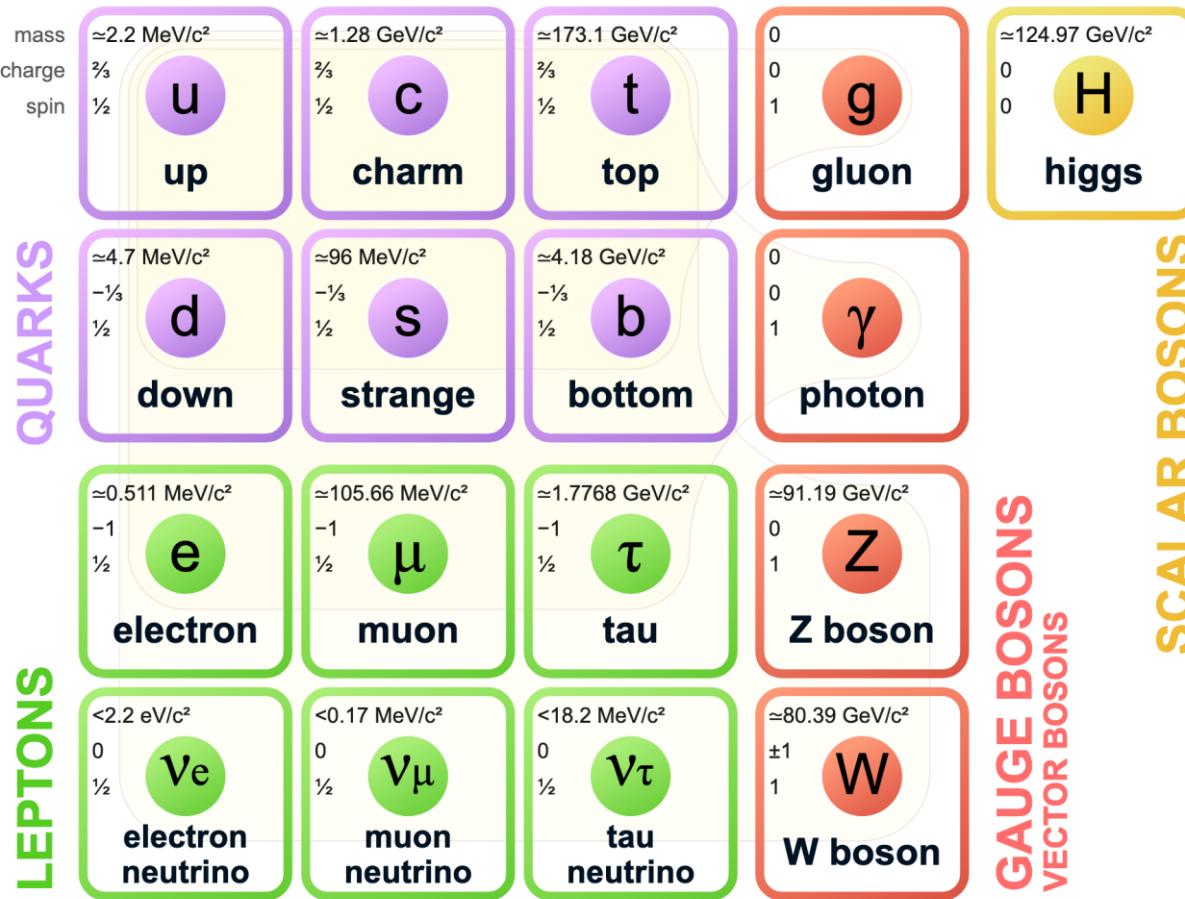
May 16-19, 2022, Cincinnati, OH, USA

# Outline

- Introduction
- R measurements at BESIII
- QCD studies at BESIII
  - Meson cross sections
  - Baryon form factors
- Summary

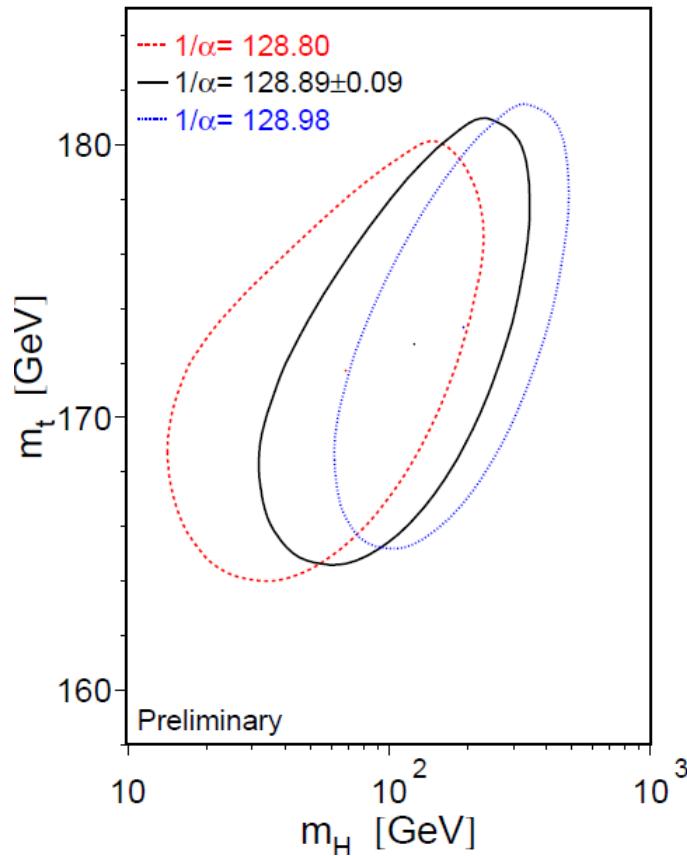
# Standard Model

- Successful, but many parameters;
- Precision test needed!

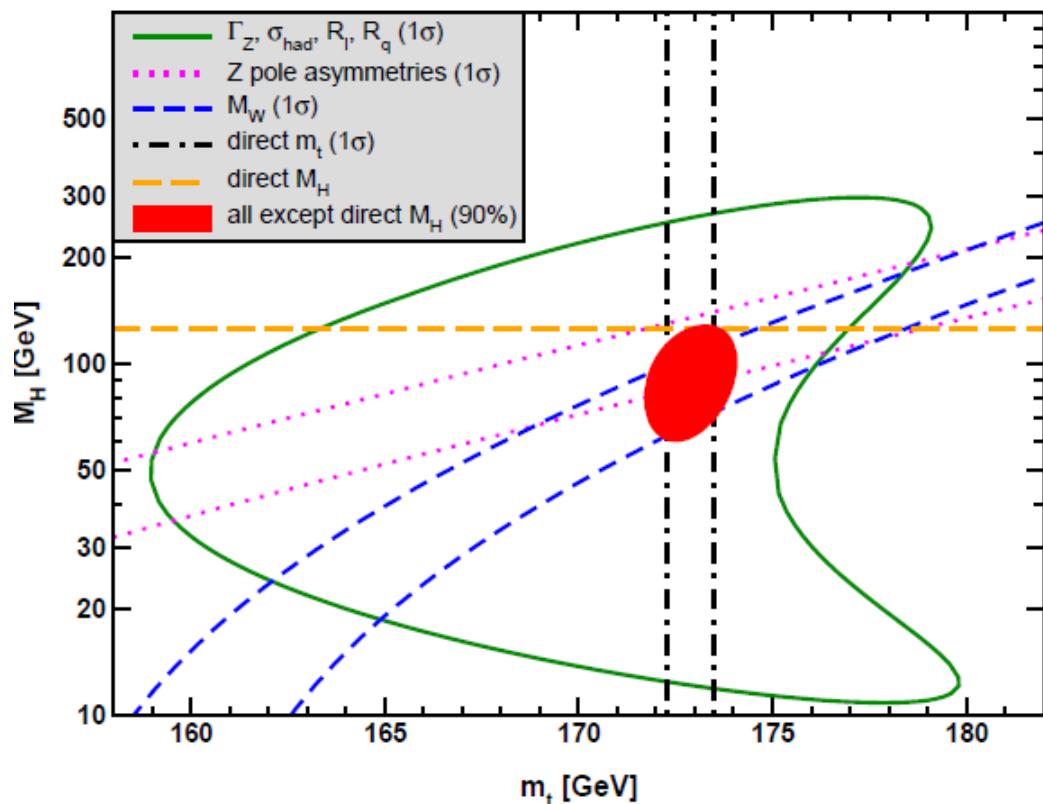


# $m_H$ , $m_t$ and $\alpha$ in SM fit

EW Group 1997

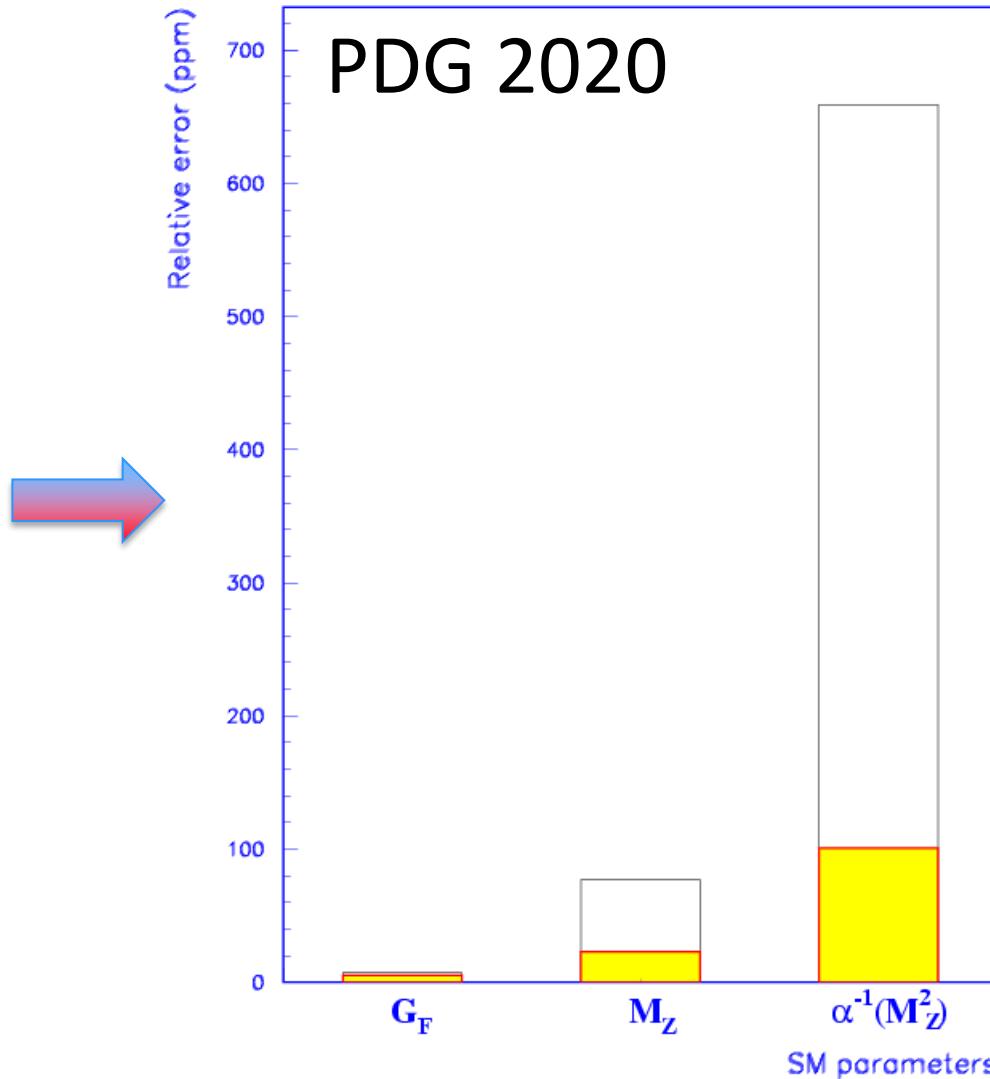
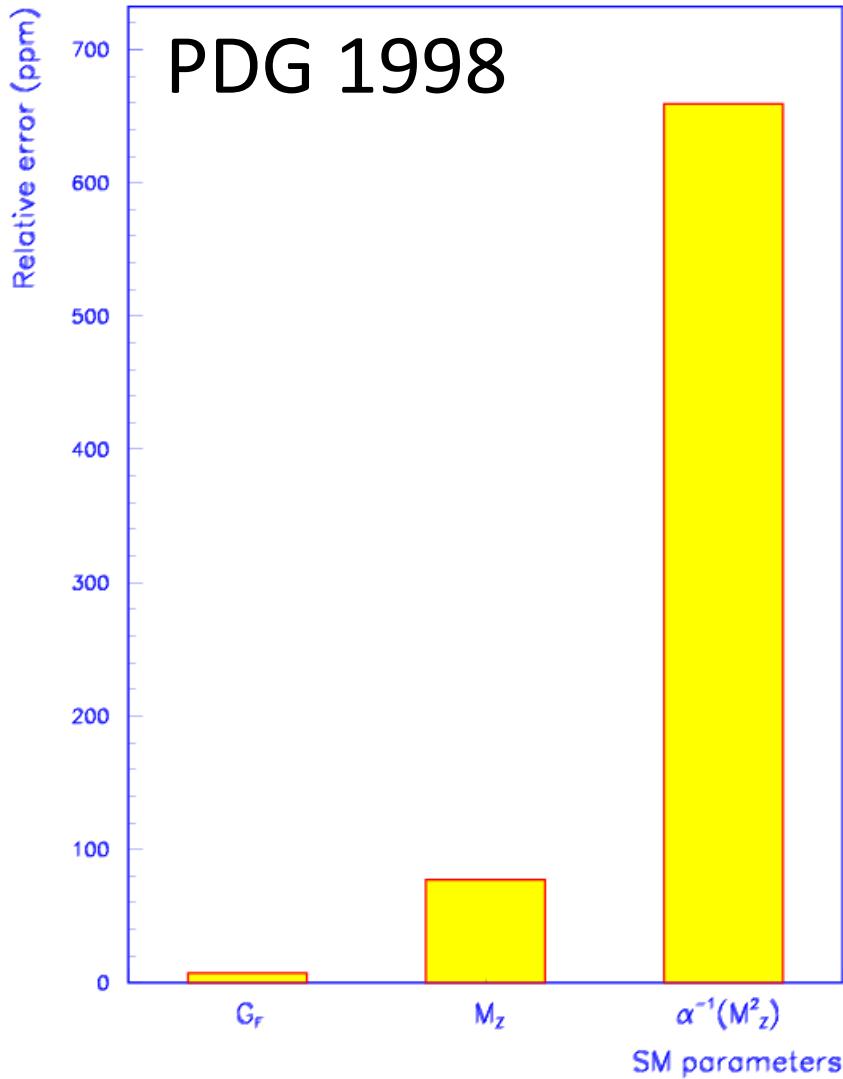


PDG 2022



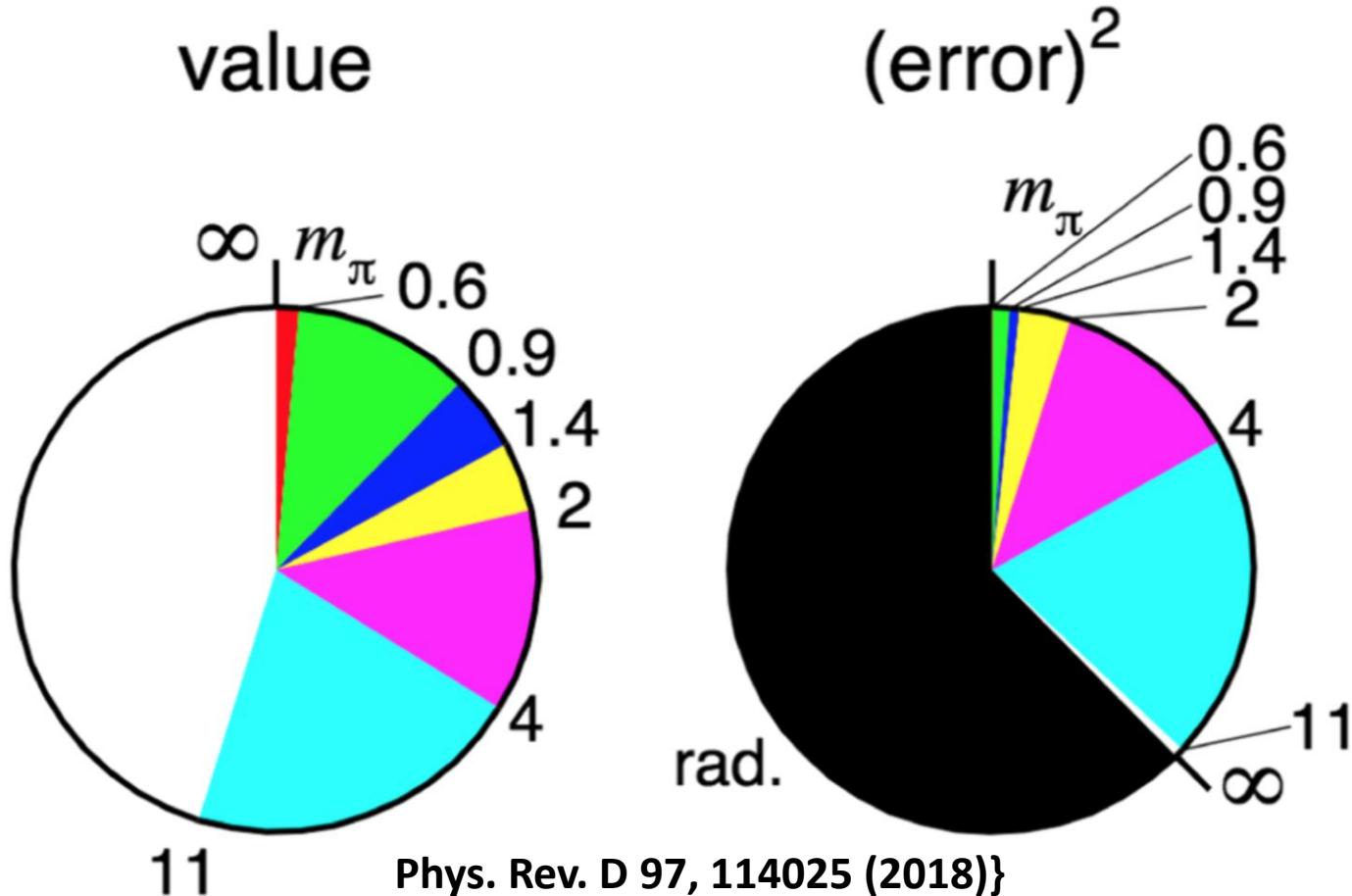
Improvement due to better precision of  $\alpha$ , ...

# Uncertainties of SM parameters



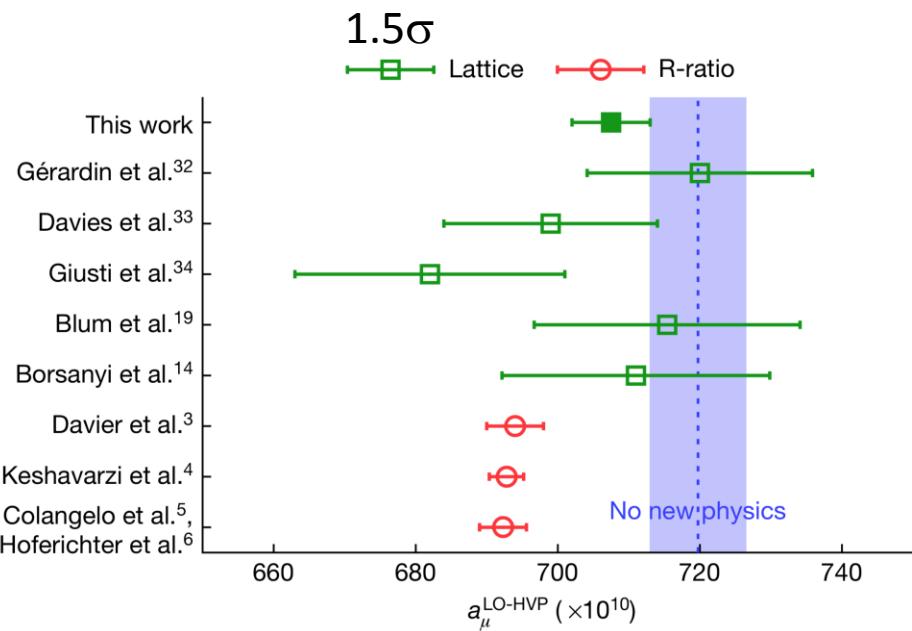
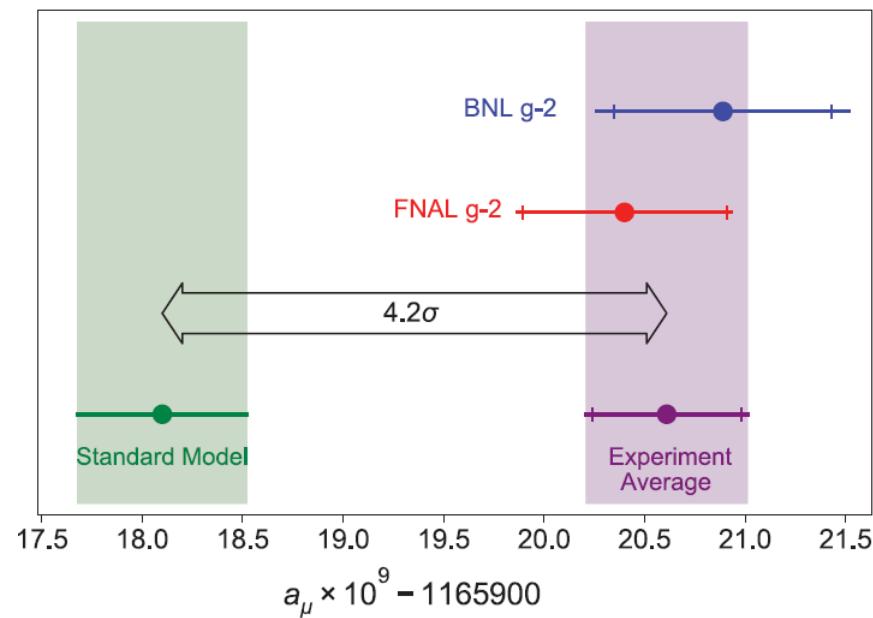
# $\Delta\alpha(M_Z^2)$

- $\Delta\alpha(s) = \Delta\alpha(s)_{\text{lepton}} + \Delta\alpha(s)_{\text{top}} + \Delta\alpha^{(5)}_{\text{had}}(s);$
- Dominant:  $\Delta\alpha_{\text{had}}^{(5)}(s) = -\frac{\alpha s}{3\pi} \operatorname{Re} \int_{E_{\text{th}}}^{\infty} ds' \frac{R(s')}{s'(s' - s - i\varepsilon)}$



$$a_\mu \equiv (g_\mu - 2)/2$$

- $4.2\sigma$  discrepancy?



Phys. Rev. Lett. 126, 141801 (2021)

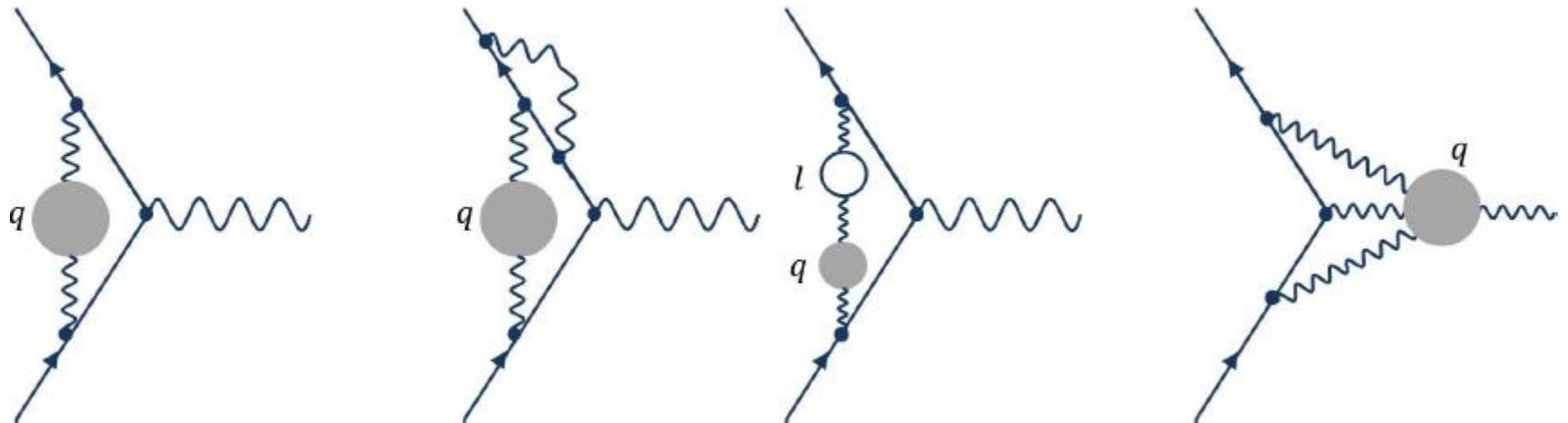
Nature 593, 51 (2021)

$a_\mu^{\text{LO-HVP}}$  (R-ratio)  
 $a_\mu^{\text{LO-HVP}}$  (lattice)

$6931 \pm 40$   
 $7075 \pm 55$

$$a_\mu \equiv (g_\mu - 2)/2$$

$$a_\ell^{\text{SM}} = a_\ell^{\text{QED}} \checkmark + a_\ell^{\text{Weak}} \checkmark + a_\ell^{\text{had}} \times$$



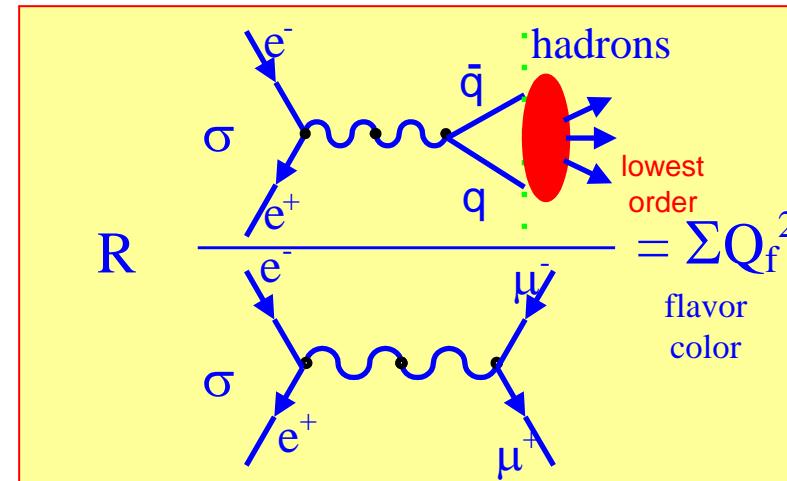
$$a_\ell^{\text{had}} = a_\ell^{\text{LO-HVP}} + a_\ell^{\text{NLO-HVP}} + a_\ell^{\text{HLbL}}$$

$$a_\mu^{\text{LO-HVP}} = \left( \frac{\alpha m_\mu}{3\pi} \right)^2 \int_{4m_\pi^2}^\infty ds \frac{R(s)K(s)}{s^2}$$

- R in low energy matters more!

# Definition of R:

- At lowest order



- At higher order

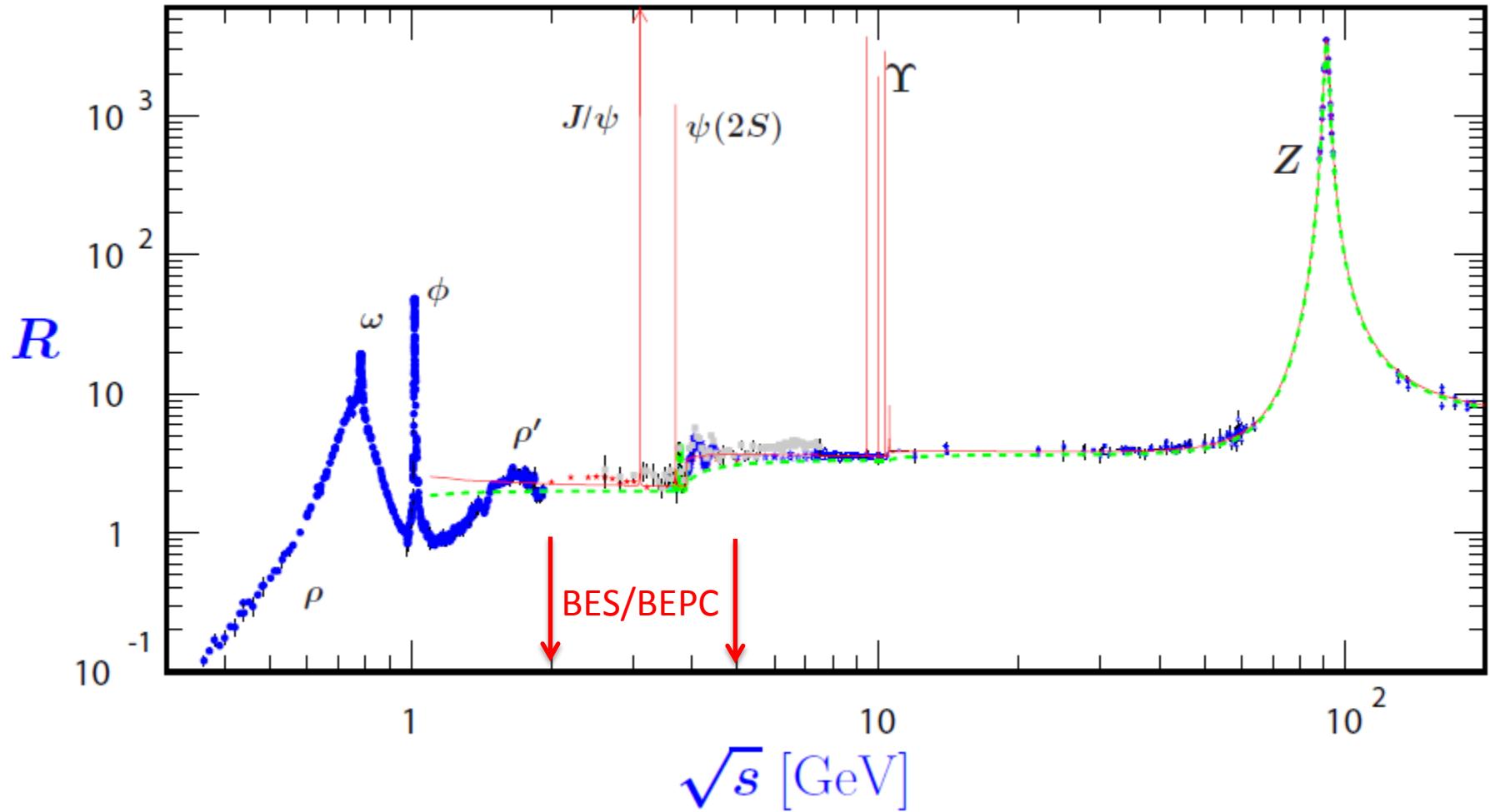
$$R = 3 K_{QCD} \sum_q Q_q^2,$$

$$K_{QCD} = 1 + \frac{\alpha_s(\mu^2)}{\pi} + \sum_{n \geq 2} C_n \left( \frac{s}{\mu^2} \right) \left( \frac{\alpha_s(\mu^2)}{\pi} \right)^n$$

Number of quark colors

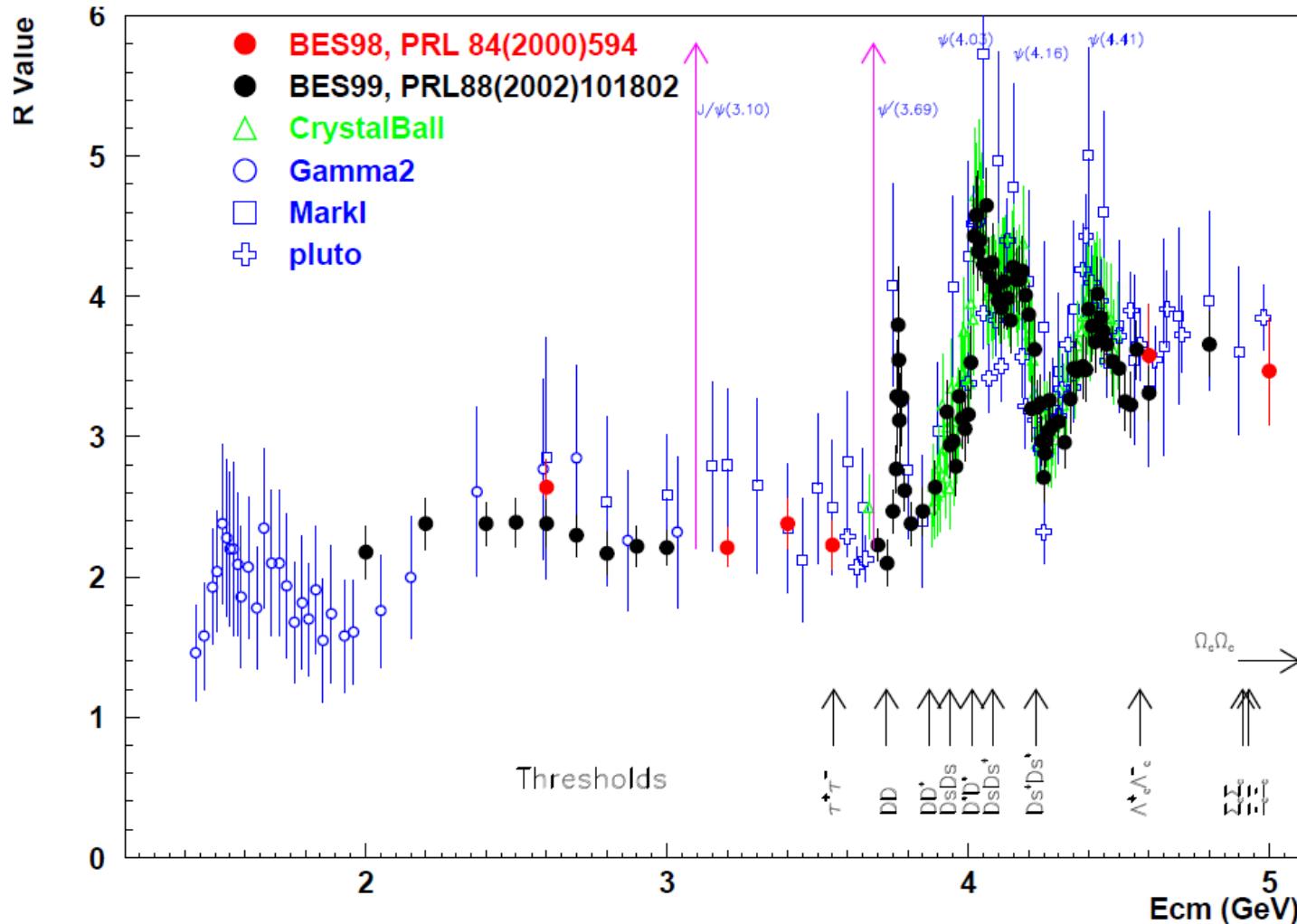
- R is one of the **most fundamental** quantities in particle physics that directly reflect the flavor and color of quarks.
- **Directly test** quark model & QCD, and **discover** new particles.

# R: from threshold to Z

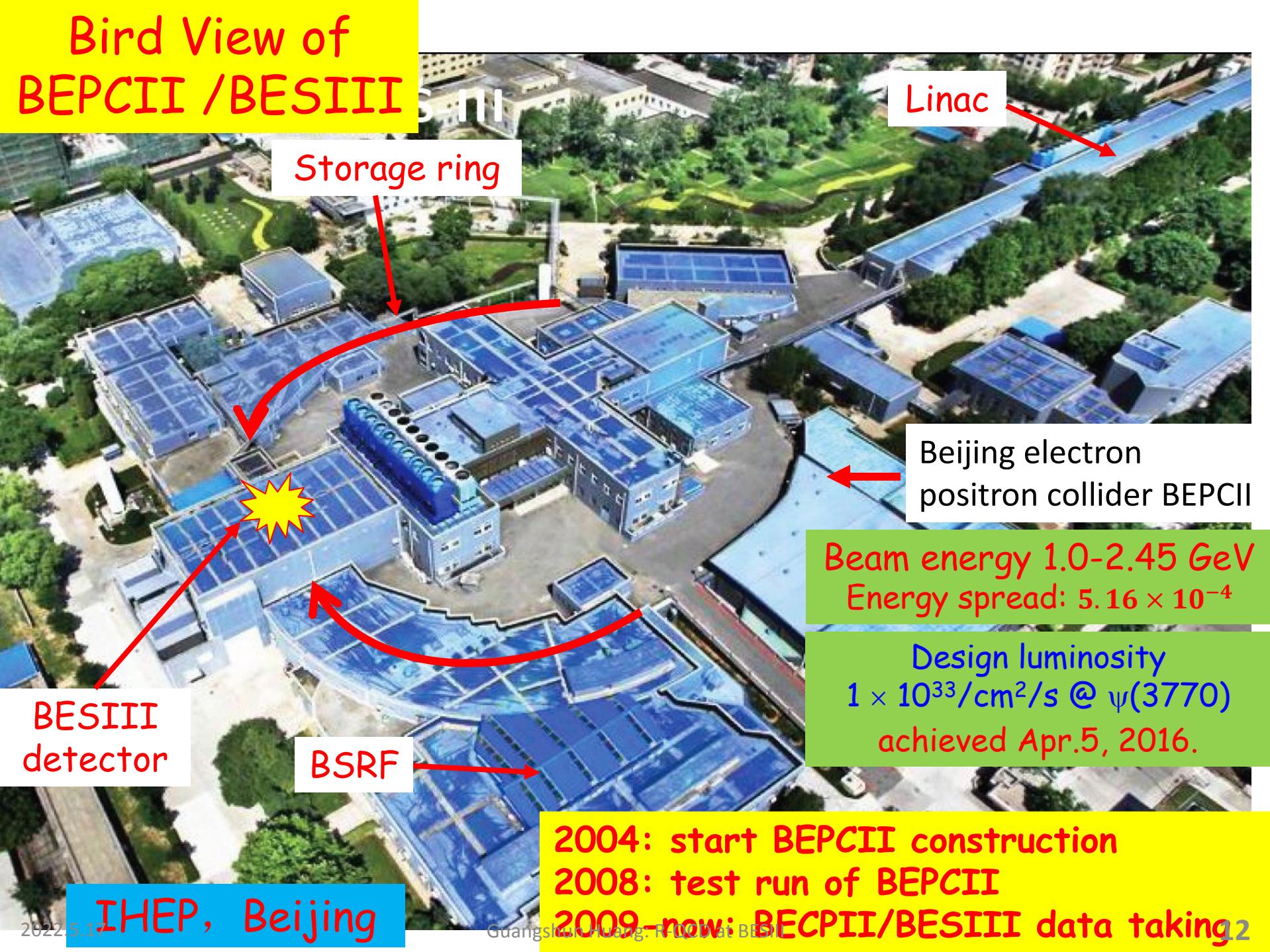


# R Scans at BESII

- 6 + 85 energy points, total  $\sim 5 \text{ pb}^{-1}$  data, average uncertainty 6.6% in [2 – 5] GeV.



# Bird View of BEPCII /BESIII



# The BESIII Detector

Drift Chamber (MDC)

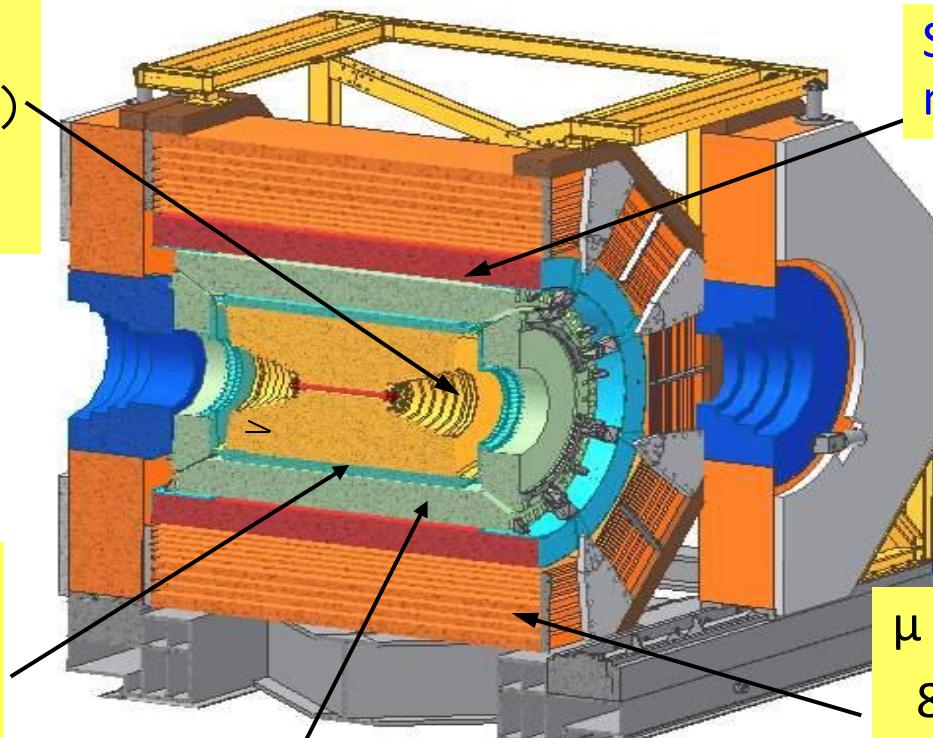
$$\sigma p/p (\%) = 0.5\% (1 \text{ GeV})$$

$$\sigma_{dE/dx} (\%) = 6\%$$

Super-conducting magnet (1.0 Tesla)

Time of Flight (TOF)

$$\begin{aligned}\sigma_T: & 90 \text{ ps for Barrel;} \\ & 110 \text{ ps} \rightarrow 65 \text{ ps} \\ & \text{for Endcaps}\end{aligned}$$



$\mu$  Counter

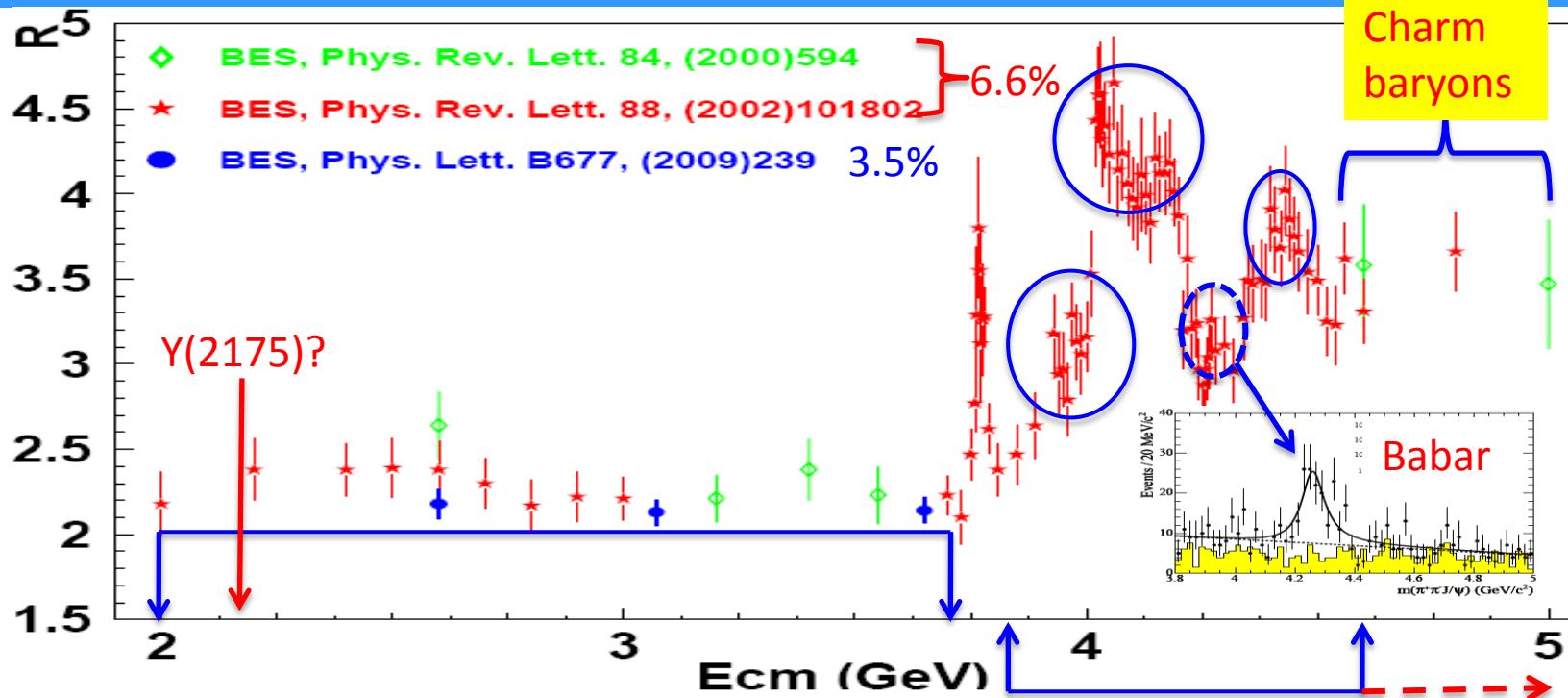
8 - 9 layers RPC

$$\delta R = 1.4 \text{ cm} \sim 1.7 \text{ cm}$$

EMC:  $\sigma E/\sqrt{E} (\%) = 2.5 \% (1 \text{ GeV})$

(CsI)  $\sigma_{z,\phi} (\text{cm}) = 0.5 - 0.7 \text{ cm}/\sqrt{E}$

# R-QCD Strategy at BESIII (original plan)



- **Phase I:** pre-study,  
Machine study at 2.0, 2.5 and 4.2(4.6) GeV, MC tuning, ...
  - **Phase II:** scan continuum region,  
15 points in 2.0–3.6 GeV, step 100 MeV,  $100k+$  hadrons < 3 GeV.
  - **Phase III:** scan resonance region,  
~100 points in 3.8–4.6 GeV,  $100k$  events, step 2, 5, 10, 20 MeV.  
( $10^8$  hadrons at 4040, 4160, 4415 for radiative decay search?)
- to extend?

# Measurement of R Values

$$R = \frac{1}{\sigma_{\mu^+\mu^-}} \cdot \frac{N_{had} - N_{bg}}{L \cdot \varepsilon_{had} \cdot (1 + \delta)}$$

$N_{had}$ : observed hadronic events

$N_{bg}$ : background events

L: integrated luminosity

$\varepsilon_{had}$ : detection efficiency for  $N_{had}$

$\delta$ : radiative correction factor

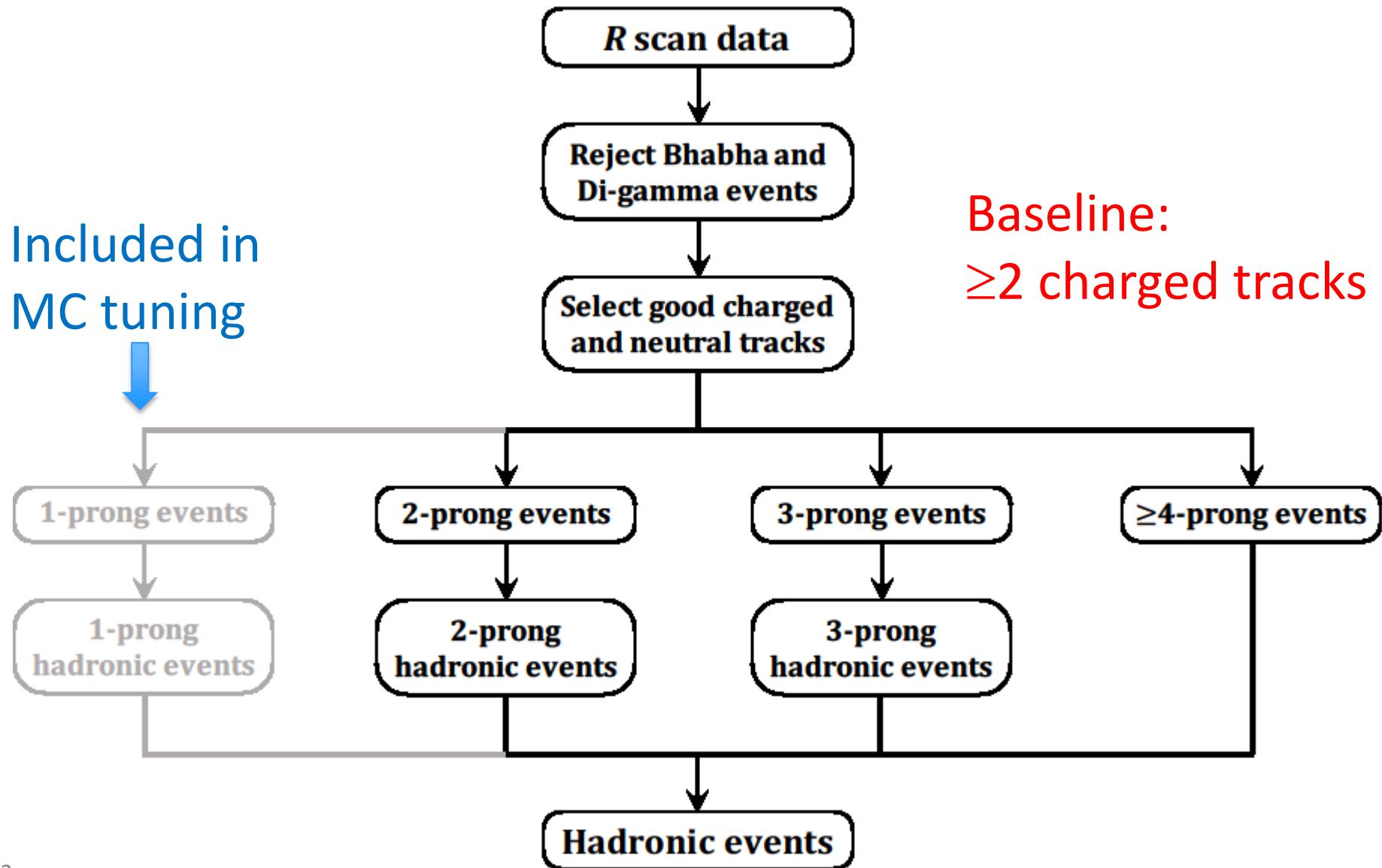
$\sigma_{\mu\mu}$ : can be precisely calculated(QED). Measurement of R  
is to measure the total  $\sigma(e^+e^- \rightarrow \text{hadrons})$

Except for controlling each item to the precision requested,  
stable long term machine and detector performance is crucial.

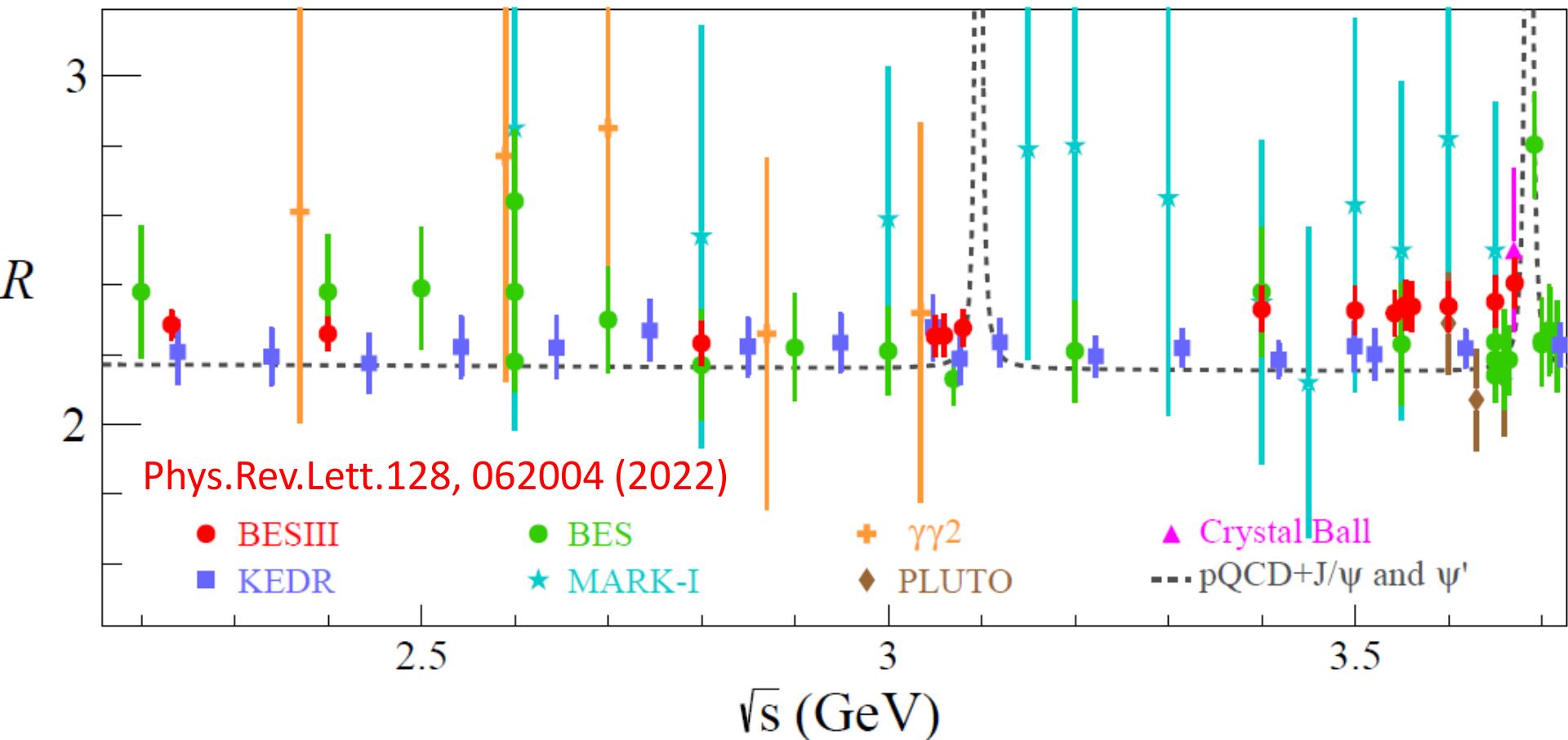
# Strategy of hadron selection

Included in  
MC tuning

Baseline:  
 $\geq 2$  charged tracks



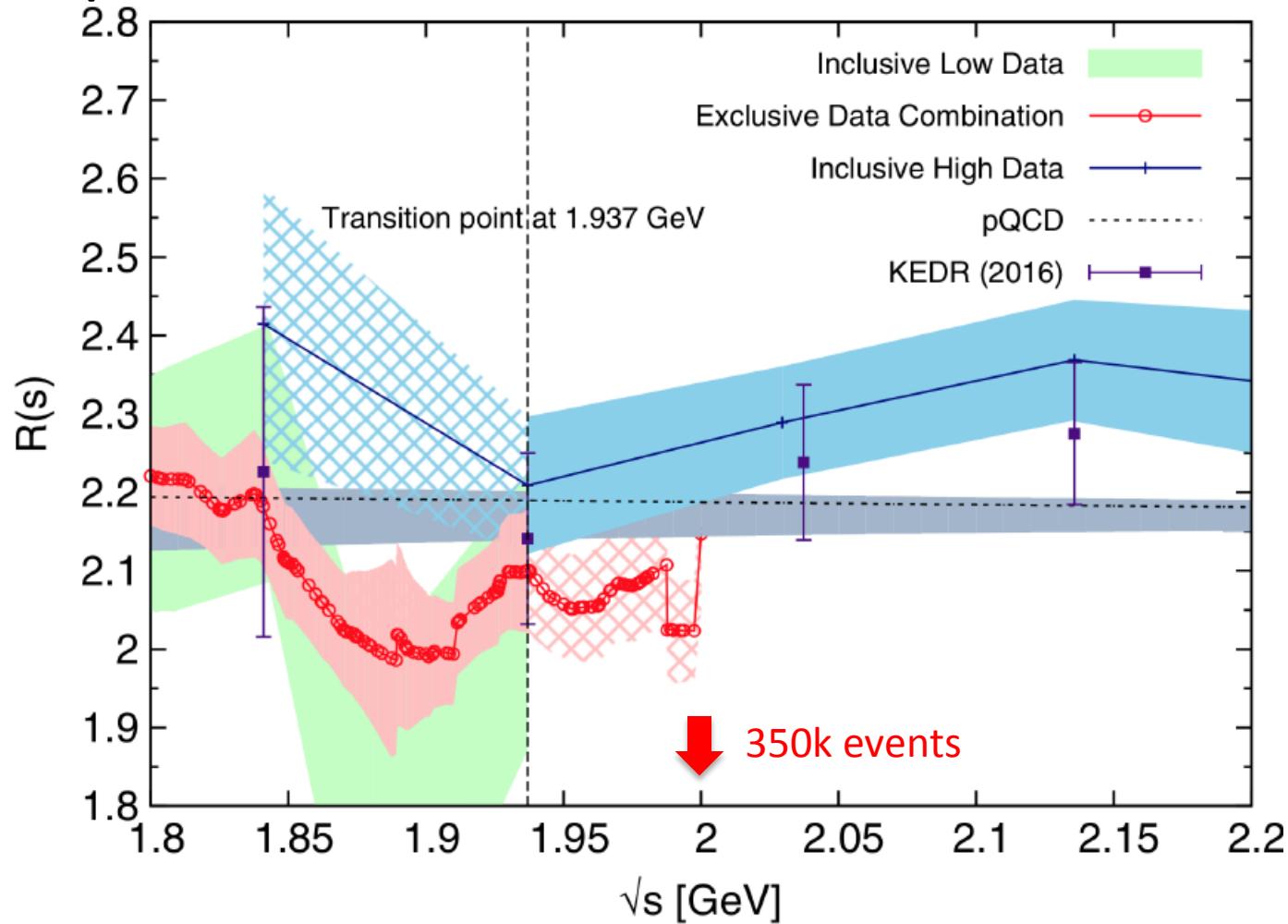
# R value in [2.2324, 3.671] GeV



- Precision better than 3%;
- Larger than pQCD by  $2.7\sigma$  in [3.4, 3.7] GeV.

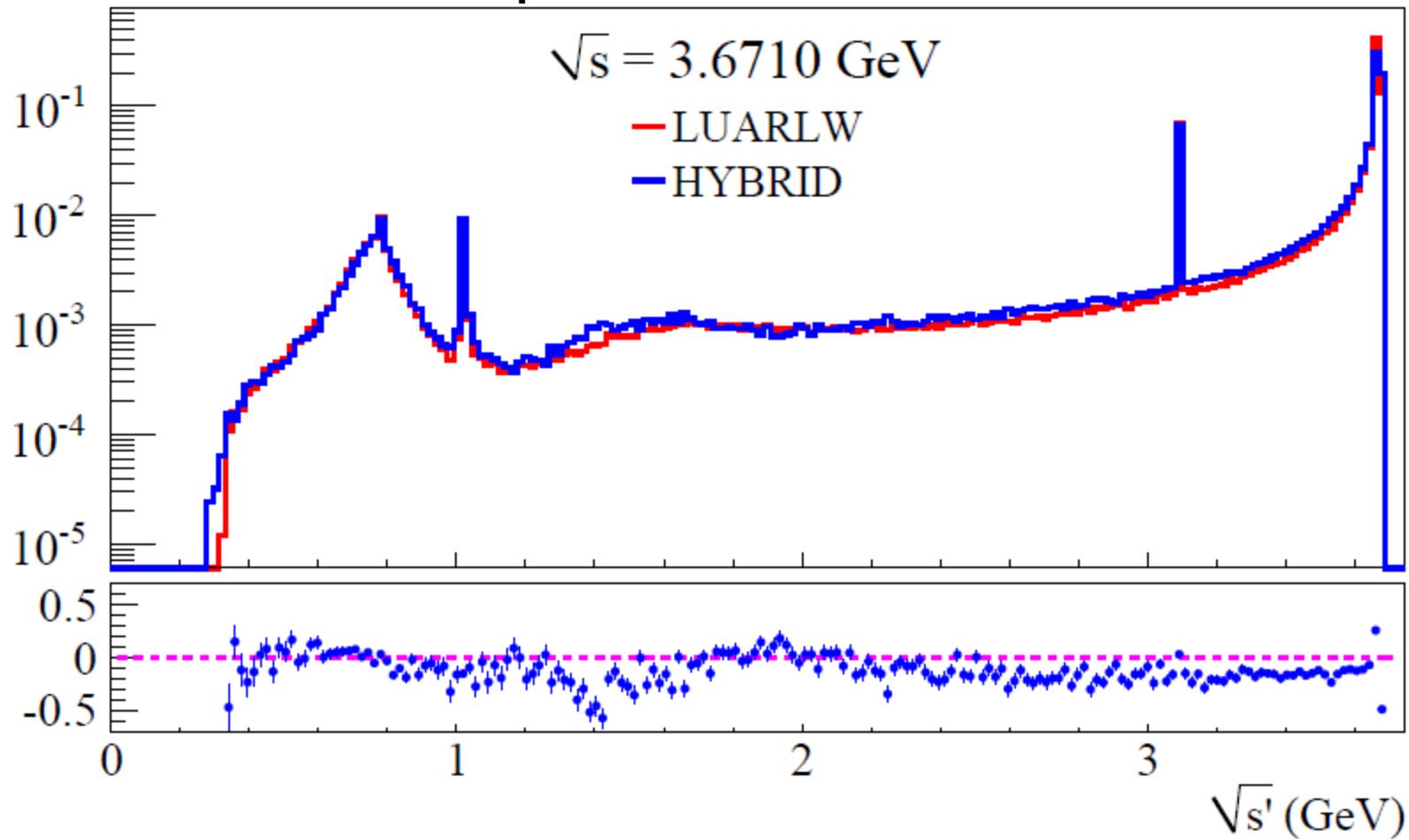
# R: ongoing studies and prospects

- R value in the full energy range [2.0, 4.6] GeV;
- Comprehensive measurement at 2.0 GeV:



# R: ongoing studies and prospects

- R via ISR technique down to  $\pi^+\pi^-$  threshold!



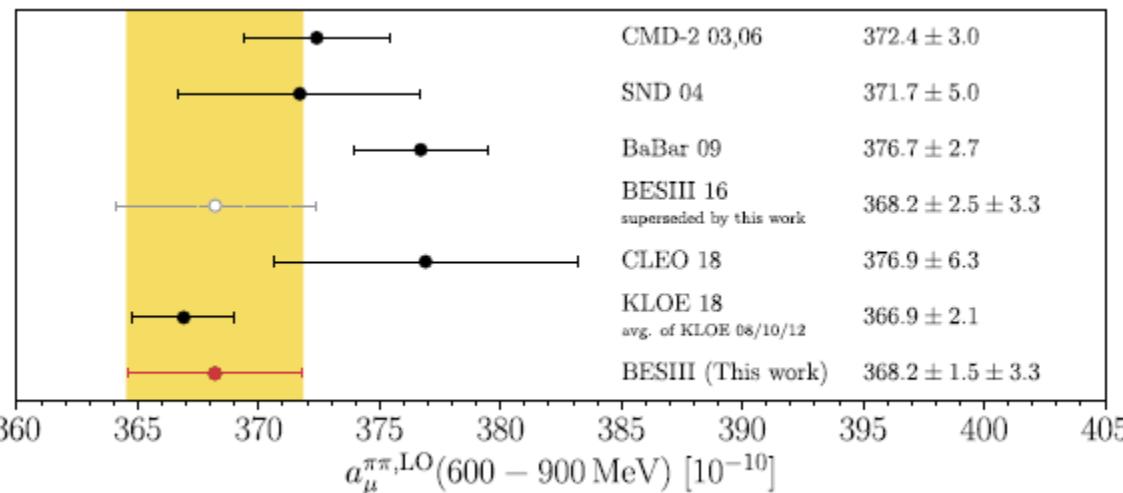
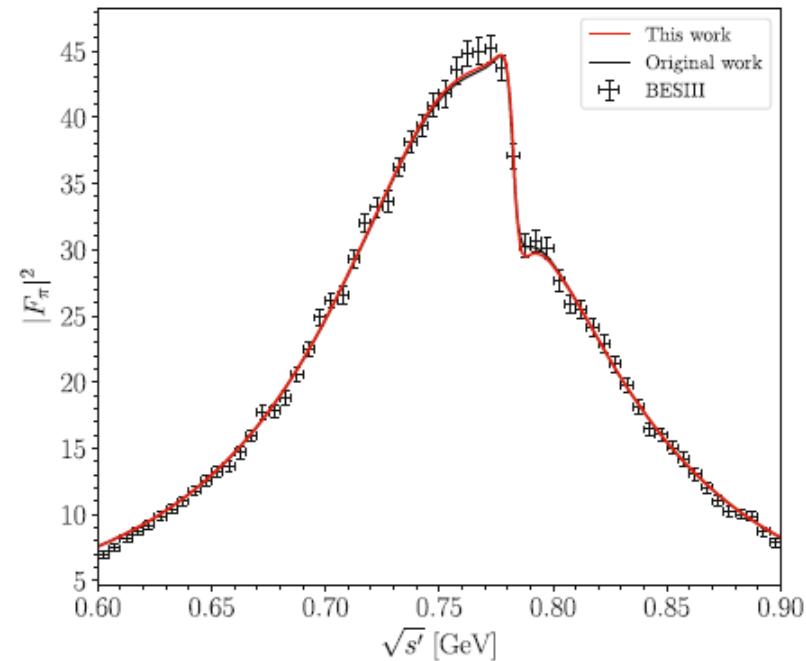
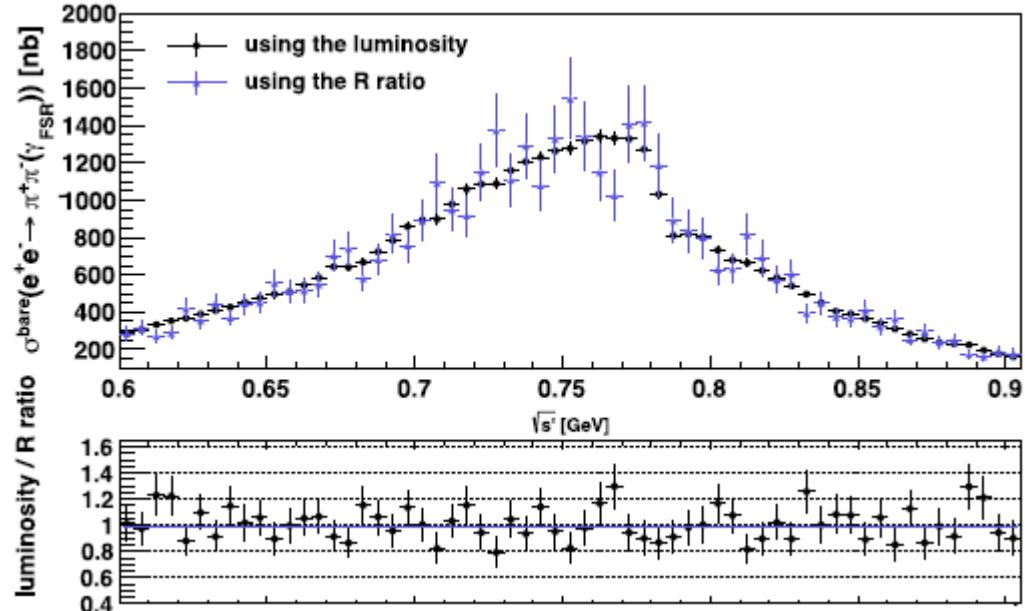
- To take data in [1.8, 2.0] GeV.

# Meson cross section & form factor

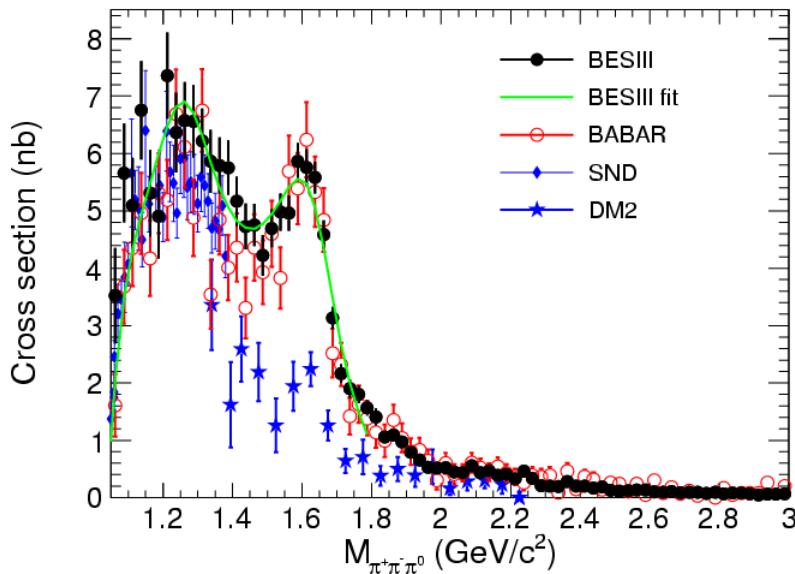
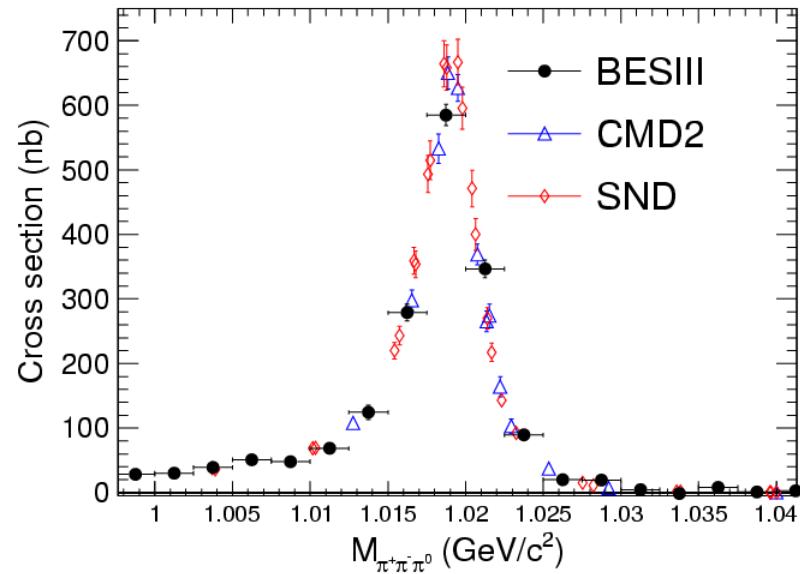
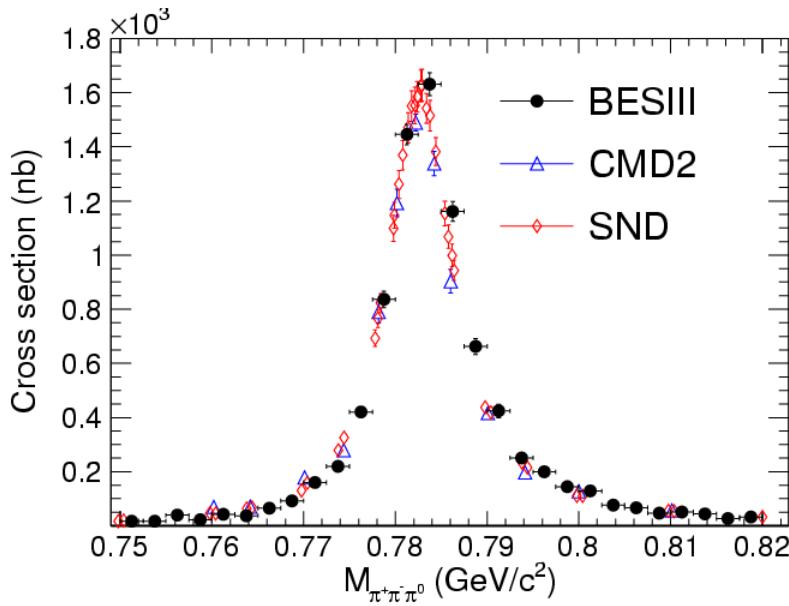
- Energy scan data in [2.0 - 3.08] GeV;
- With high-statistics data at higher energies, Initial State Radiation (ISR) technique allows access below 2.0 GeV;
- Lot of channels studied:  $e^+e^- \rightarrow \pi^+\pi^-$ ,  $\pi^+\pi^-\pi^0$ ,  $\omega\pi^0/\eta$ ,  $\eta'\pi^+\pi^-$ ,  $\omega\pi^+\pi^-$ ,  $\omega\pi^0\pi^0$ ,  $\gamma\eta$ ,  $\omega\eta'$ ,  $K^+K^-$ ,  $K_SK_L$ ,  $2(K^+K^-)$ ,  $\phi\pi^+\pi^-$ ,  $\phi\pi^0$ ,  $\phi\eta/\eta'$ ,  $\omega K^+K^-$ , ...

# ISR $e^+e^- \rightarrow \pi^+\pi^-$

- PLB 753, 629 (2016); Erratum: 812, 135982 (2021).
- New effort to go  $> 1\text{GeV}$ .



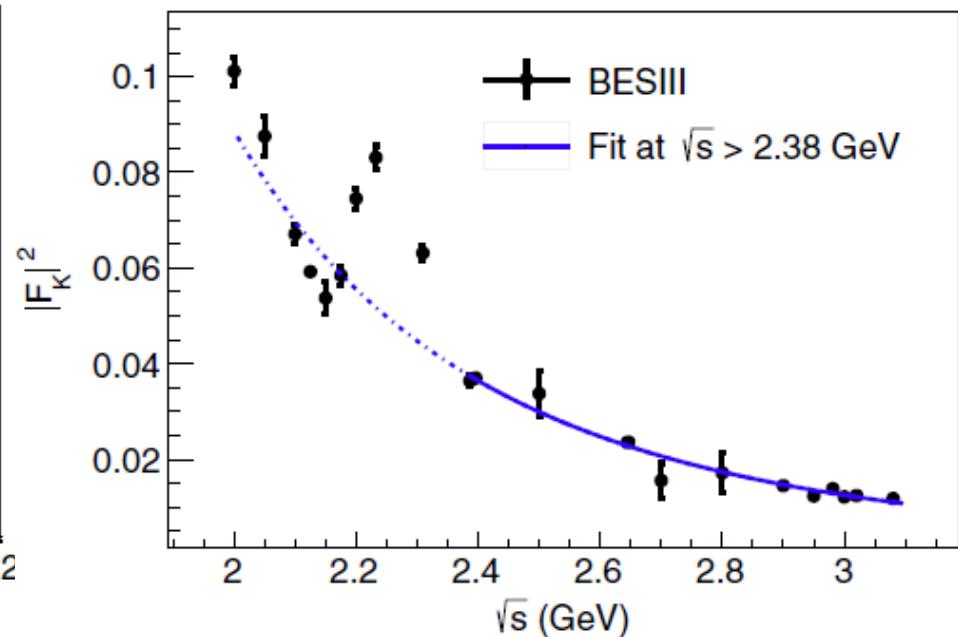
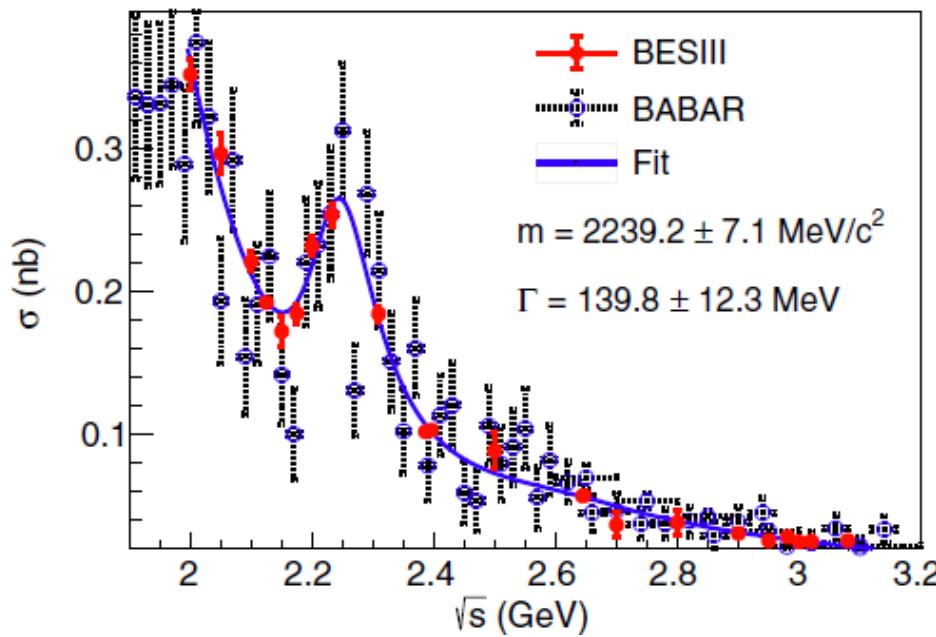
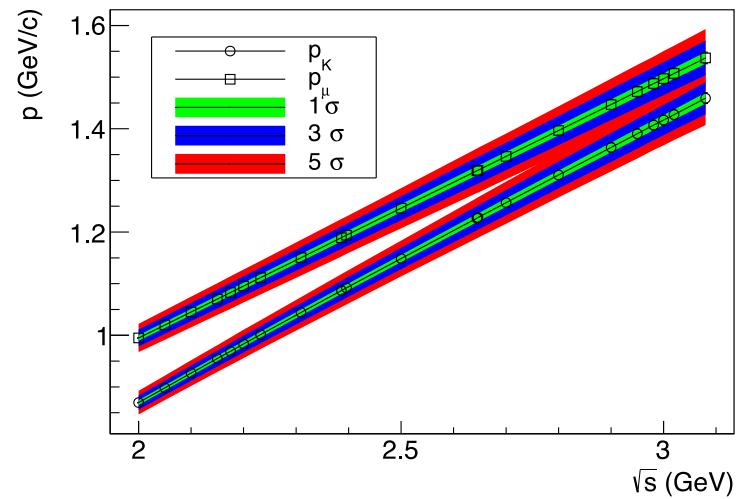
# ISR $e^+e^- \rightarrow \pi^+\pi^-\pi^0$



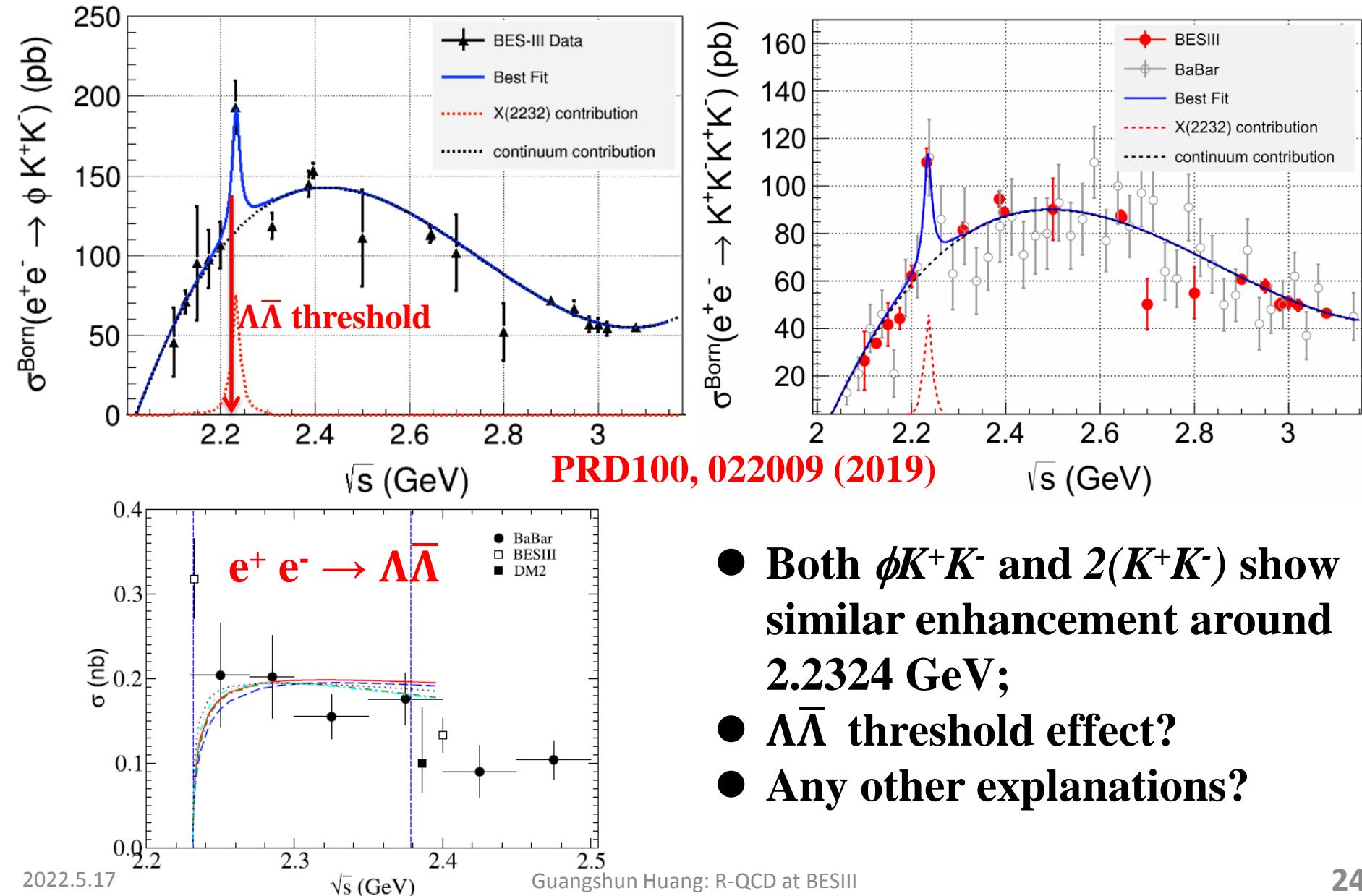
- Tagged & untagged analyses;
- 0.7 ~ 3.0 GeV, 1<sup>st</sup> result from a single experiment;
- arXiv:1912.11208.

# Scan $e^+e^- \rightarrow K^+K^-$

- Signal & background well separated;
- Much better precision than BaBar;
- Shape of FF agrees with pQCD  $1/s$ ;
- Unknown structure at 2.23 GeV;
- Phys. Rev. D 99, 032001 (2019).

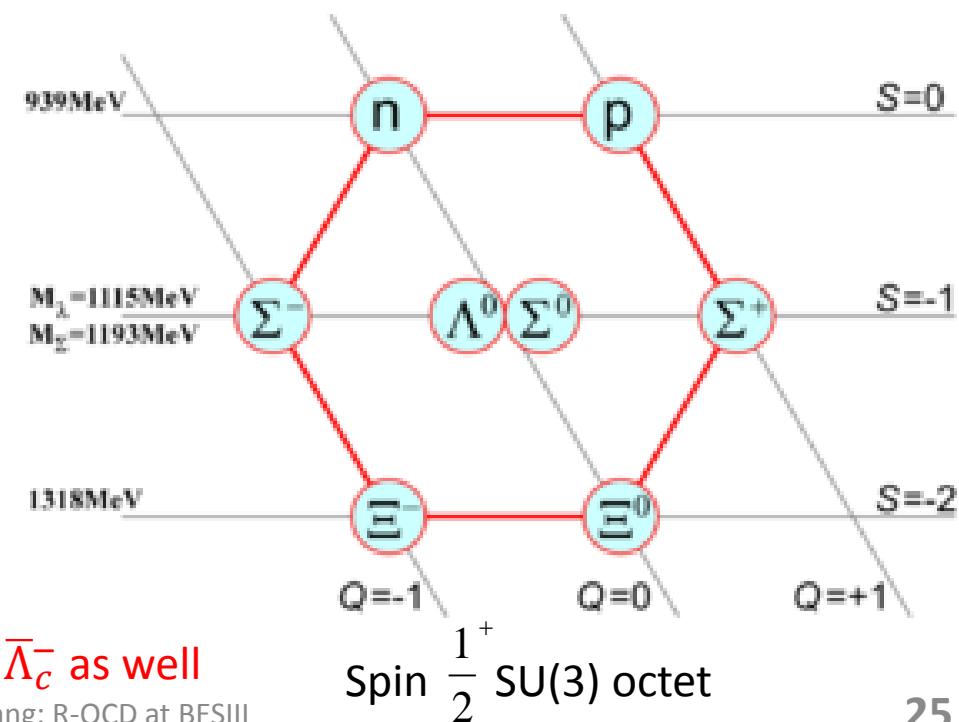
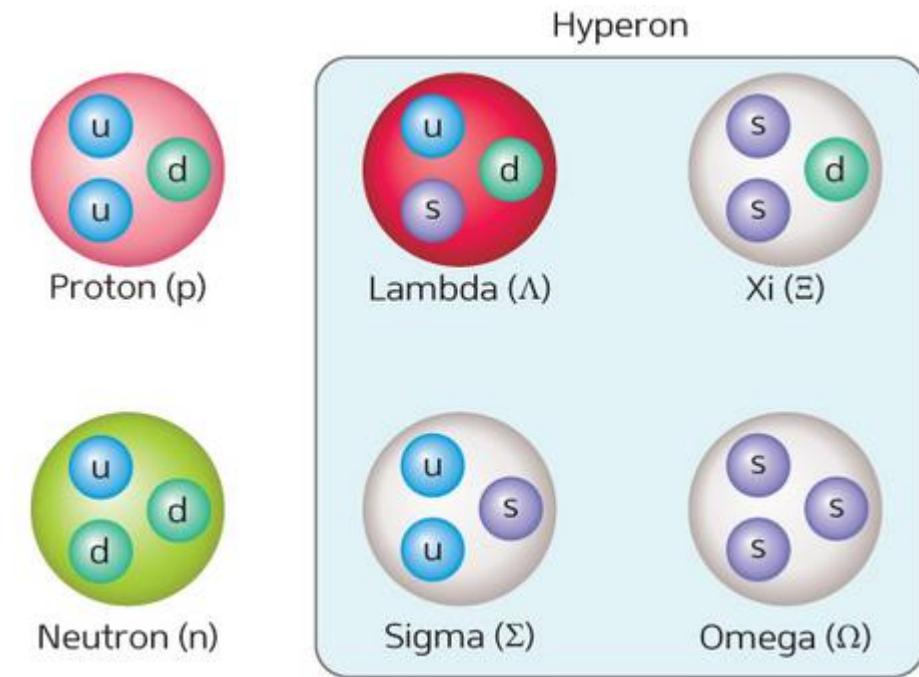


# Scan $e^+ e^- \rightarrow 2(K^+ K^-)$



# Baryon form factor

- $p\bar{p}$ : PRD 91, 112004 (2015); PRL 124, 042001 (2020);
- $n\bar{n}$ : Nature Physics 17, 1200 (2021);
- $\Lambda\bar{\Lambda}$ : Phys. Rev. D 97, 032013 (2018);
- $\Sigma^+\bar{\Sigma}^-/\Sigma^-\bar{\Sigma}^+$ : Phys. Lett. B814, 136110 (2021);
- $\Sigma^0\bar{\Sigma}^0$ : Phys. Lett. B (accepted);
- $\Xi^-\bar{\Xi}^+$ : Phys. Rev. D103, 012005 (2021);
- $\Xi^0\bar{\Xi}^0$ : Phys. Lett. B820, 136557 (2021). →  $\frac{1}{2}^+$  octet all covered!

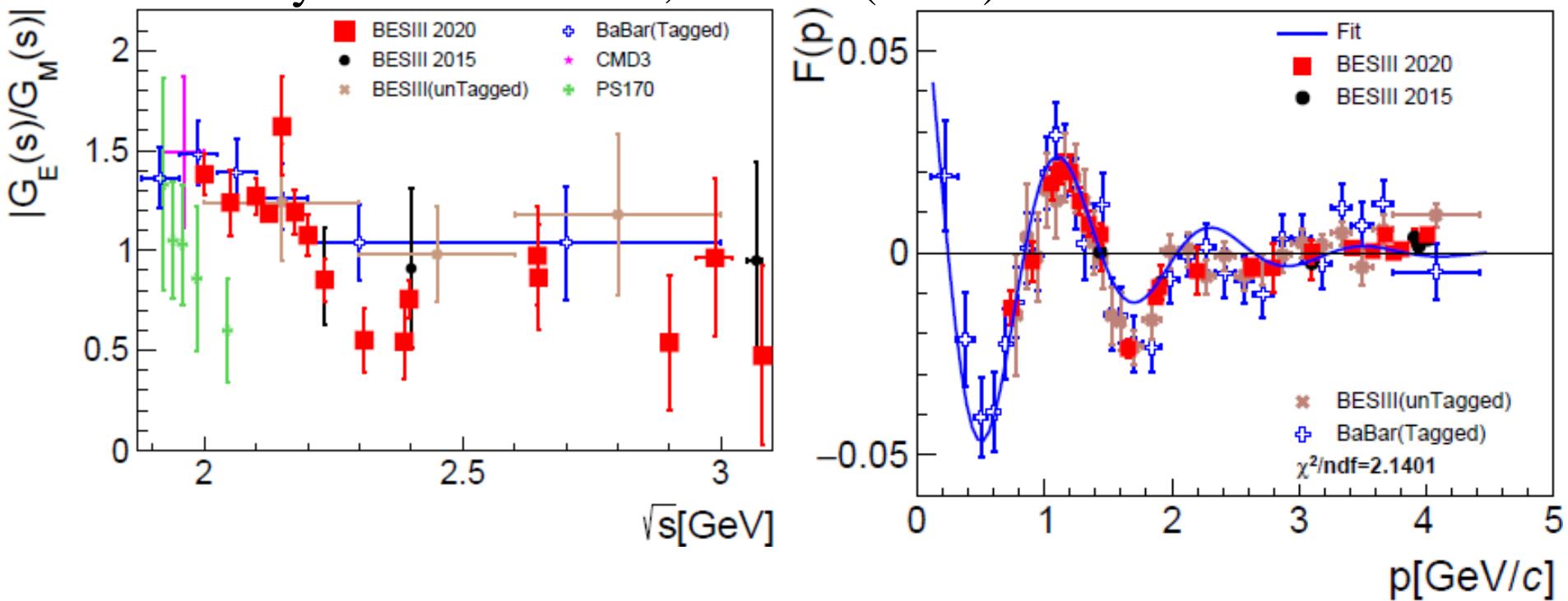


# Proton form factors

- Oscillation seen in the effective form factor

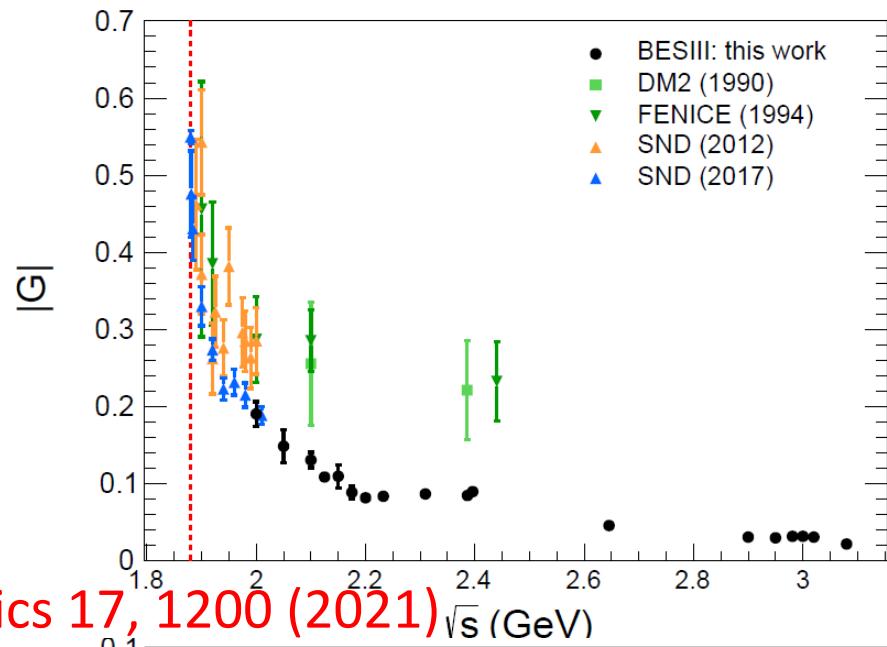
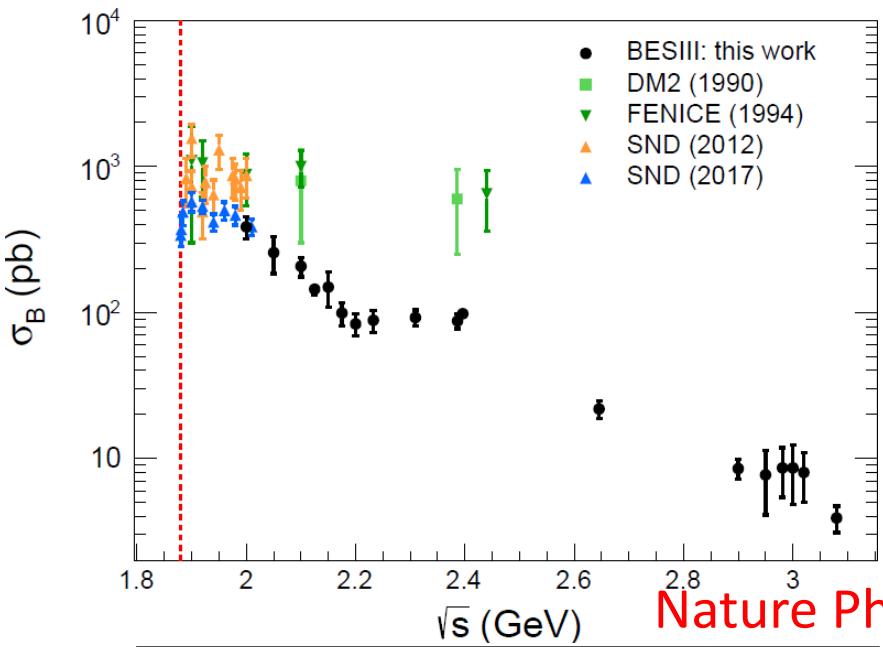
$$F^{osc}(p) = |G_{eff}| - F^0 \quad (F^0: \text{regular shape})$$

Phys. Rev. Lett. 124, 042001 (2020)

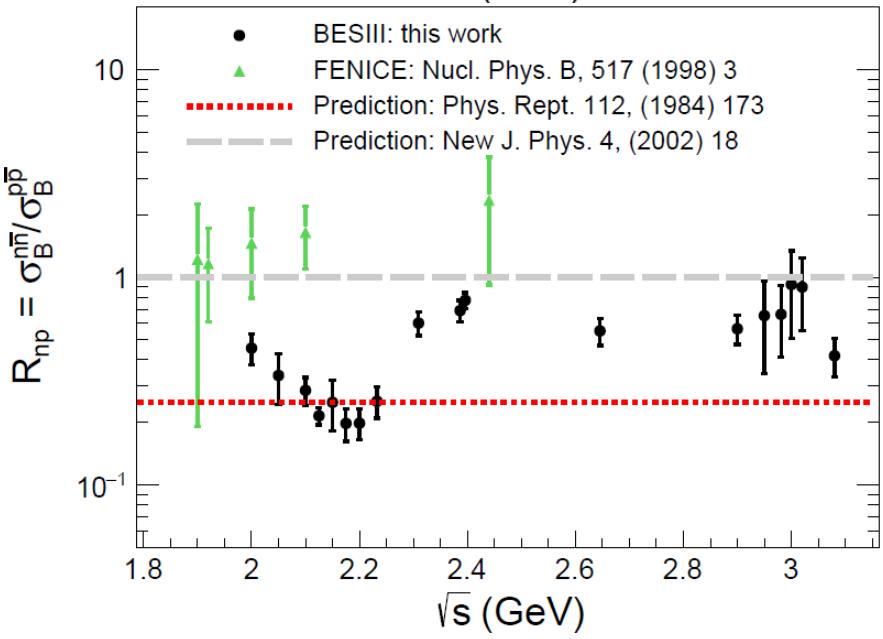


$p$  is the 3-momentum of proton in the frame of anti-proton. Re-scattering effect?

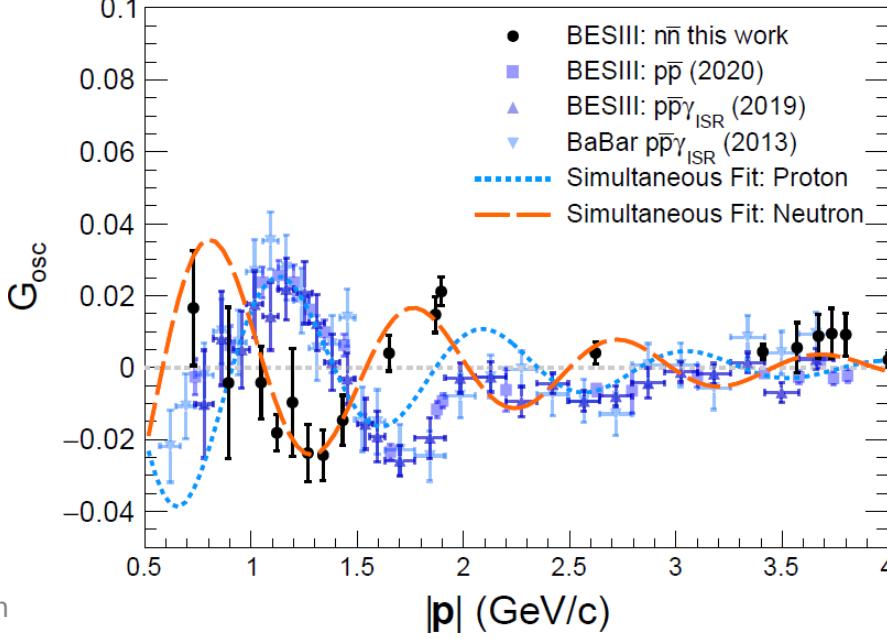
# Neutron form factors



Nature Physics 17, 1200 (2021)  $\sqrt{s}$  (GeV)



Huan



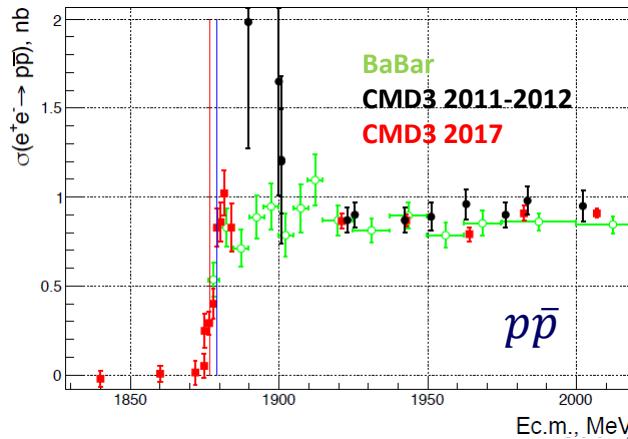
# Baryon-pair production near threshold

$\bar{p}p$	$\bar{\Lambda}\Lambda$	$\bar{\Sigma}^-\Sigma^+$	$\bar{\Sigma}^0\Sigma^0$	$\bar{\Sigma}^-\Sigma^+$	$\bar{\Xi}^0\Xi^0$	$\bar{\Xi}^+\Xi^-$	$\bar{\Omega}^+\Omega^-$	$\bar{\Lambda}_c^-\Lambda_c^+$
$\downarrow$	$\downarrow$	$\downarrow$	$\downarrow$	$\downarrow$	$\downarrow$	$\downarrow$	$\downarrow$	$\downarrow$
$p\pi^-$	$p\pi^0$	$\Lambda\gamma$	$n\pi$	$\Lambda\pi^0$	$\Lambda\pi$	$\Lambda\pi$	$\Lambda K$	$\Lambda\pi$
64%	52%	$\approx 100\%$	$\approx 100\%$	$\approx 100\%$	$\approx 100\%$	$\approx 100\%$	68%	$\approx 1\%$

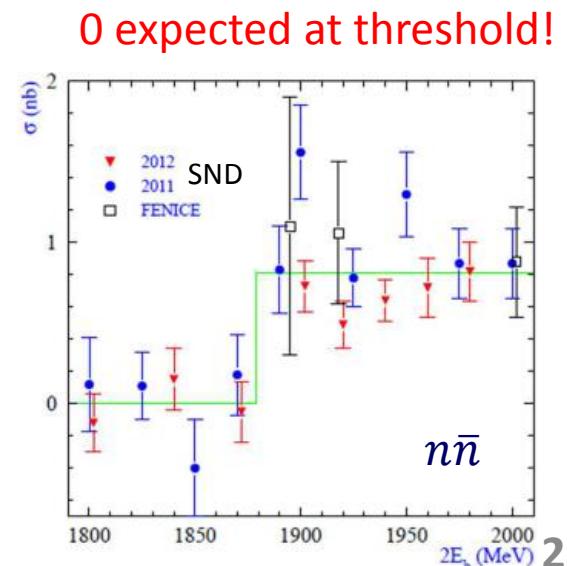
$e^+e^- \rightarrow \gamma^* \rightarrow B\bar{B}$  production cross section:

$$\sigma_{B\bar{B}}(m) = \frac{4\pi\alpha^2 C\beta}{3m^2} [|G_M(m)|^2 + \frac{1}{2\tau} |G_E(m)|^2]$$

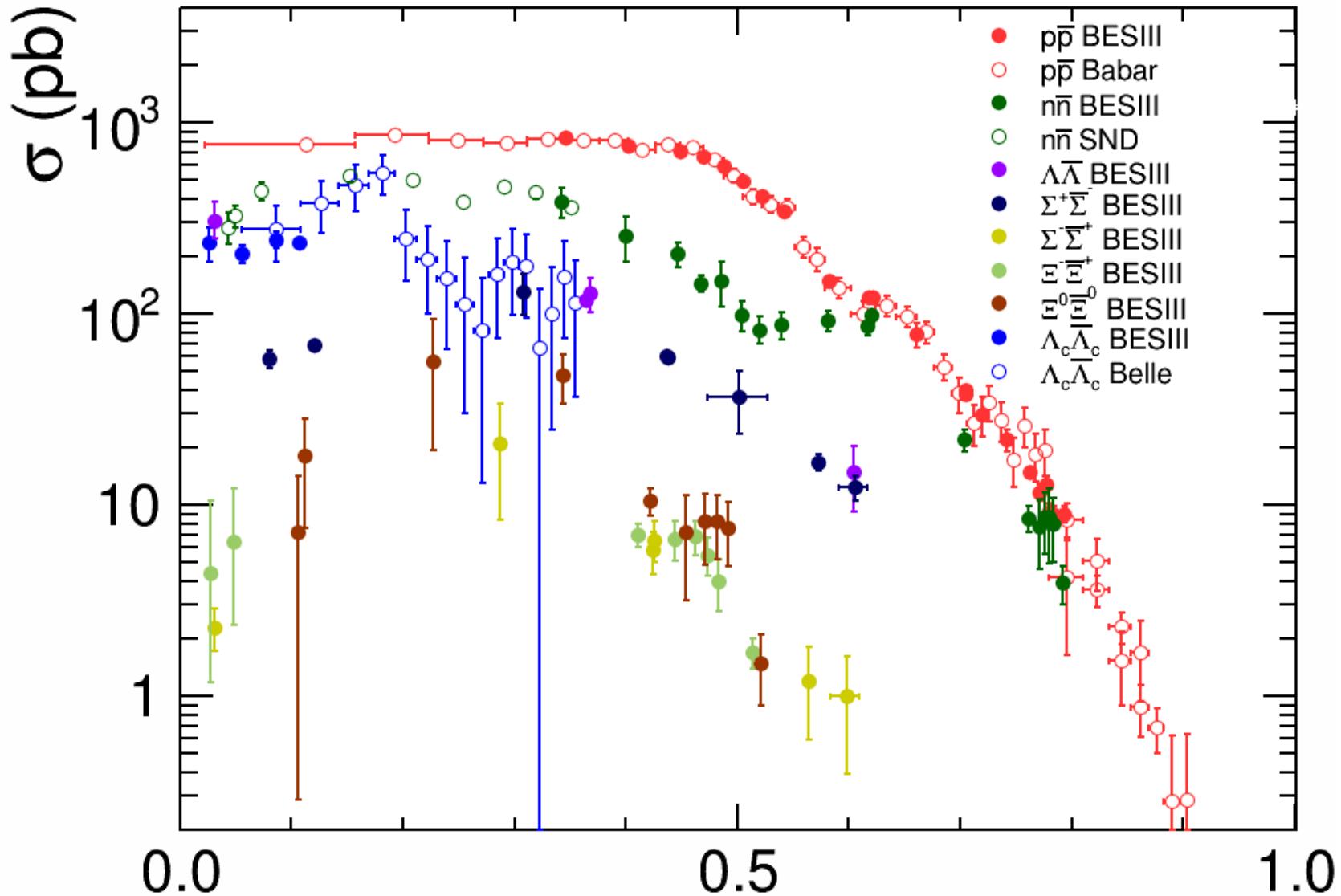
$$\text{Coulomb factor } C = \begin{cases} \frac{\pi\alpha}{\beta} \frac{1}{1-\exp(-\frac{\pi\alpha}{\beta})}, & \text{for charged } B\bar{B} \\ 1, & \text{for neutral } B\bar{B} \end{cases}$$



$p\bar{p}$ 、 $n\bar{n}$  should be different, but poor precision for latter.  
How about other baryon-pairs?



# Baryon-pair production in a glance



National Science Review 8, nwab187 (2021)

$$\beta = \sqrt{1 - 4M_B^2/s}$$

# Summary

- High-quality data for R-QCD at BESIII in 2.0–4.6 GeV:  $1.5 \text{ fb}^{-1}$
- BESIII First R values with uncertainties  $<3\%$  at 14 energies in [2.2324, 3.671] GeV published;
- Meson cross sections measured for precision test;
- Form factors measured and threshold production behavior studied for various baryons;
- Prospects at a future super  $\tau$ -c factory:
  - Inclusive R:  $\sim 2\%$  (generator model, radiative correction);
  - Exclusive measurements down to meson production threshold;
  - Insight into structure of hadrons.