Snowmass Rare and Precision Measurements Frontier Spring Meeting Cincinnati, May 16-19 2022

Lepton Number Violation and Neutrinoless Double Beta Decay

Vincenzo Cirigliano Institute for Nuclear Theory University of Washington

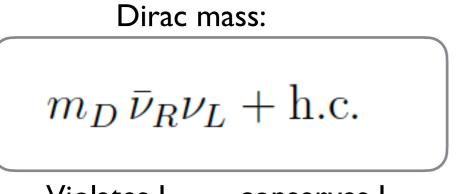
Outline

- Introduction
 - Lepton number violation: $0\nu\beta\beta$ and other probes
 - Effective Field Theory framework for $0\nu\beta\beta$
- Survey of $0\nu\beta\beta$ reach in classes of LNV models
 - High scale seesaw (dim 5)
 - TeV-scale LNV (dim 7, 9,)
 - Low-scale LNV (`light' V_R, ...)
 - Unraveling the mechanism?
- Outlook

For a comprehensive discussion see the 'theory-oriented' WP 2203. 21169

Why Lepton Number Violation?

- L is an accidental symmetry of the SM (up to anomalies which induce $\Delta B = \Delta L = 3$, highly suppressed): unique window on BSM dynamics
- Connected with big questions: unification, origin of matter-antimatter asymmetry, origin of neutrino mass



Violates $L_{e,\mu,\tau}$, conserves L

Majorana mass:

$$\frac{1}{2}m_M \nu_L^T C \nu_L + \text{h.c.}$$

Violates $L_{e,\mu,\tau}$ and L ($\Delta L=2$)

Why Lepton Number Violation?

- L is an accidental symmetry of the SM (up to anomalies which induce $\Delta B = \Delta L = 3$, highly suppressed): unique window on BSM dynamics
- Connected with big questions: unification, origin of matter-antimatter asymmetry, origin of neutrino mass

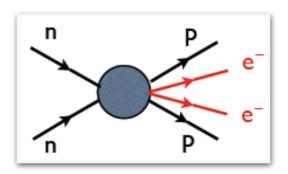
$$\mathcal{L}_{\nu \mathrm{SM}} = \mathcal{L}_{\mathrm{SM}} + \mathcal{L}_{\nu - \mathrm{mass}} + \dots$$

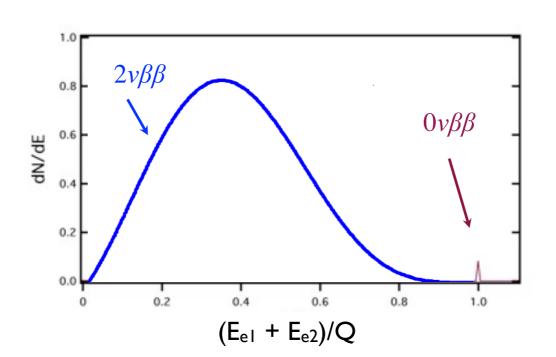
- Key question: is Lepton Number a good symmetry of the new dynamics?
- Smallness of V mass and chiral nature of the weak interactions implies that *neutrino-less* processes are the best probes of $\Delta L=2$ interactions

• Neutrinoless double beta decay

 $(N,Z) \to (N-2,Z+2) + e^- + e^-$

$$T_{1/2} > \# \, 10^{25} \mathrm{yr}$$





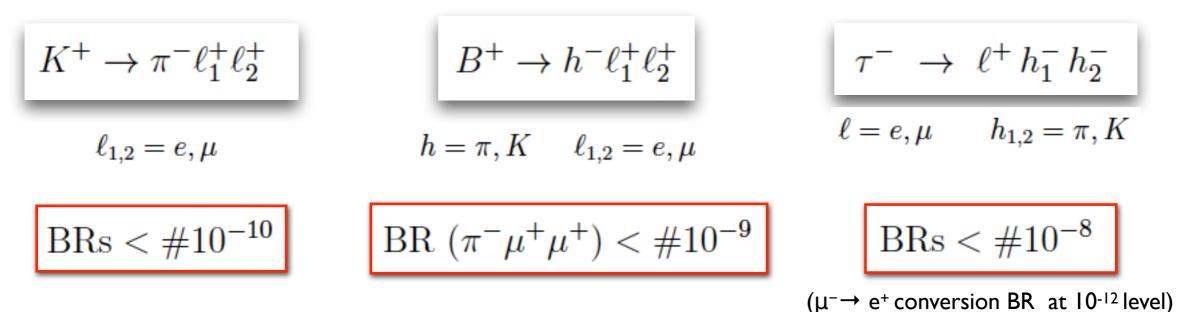
Observable in certain even-even nuclei for which single beta decay is energetically forbidden

• Neutrinoless double beta decay

$$(N,Z) \to (N-2,Z+2) + e^- + e^-$$

$$T_{1/2} > \# 10^{25} \mathrm{yr}$$

• Decays of mesons or charged leptons



• Neutrinoless double beta decay

$$(N,Z) \to (N-2,Z+2) + e^- + e^-$$

$$T_{1/2} > \# \, 10^{25} \mathrm{yr}$$

• Decays of mesons or charged leptons

$$\begin{split} K^{+} &\to \pi^{-} \ell_{1}^{+} \ell_{2}^{+} \\ \ell_{1,2} &= e, \mu \\ BRs &< \# 10^{-10} \\ \end{split} \qquad \begin{aligned} B^{+} &\to h^{-} \ell_{1}^{+} \ell_{2}^{+} \\ h &= \pi, K \quad \ell_{1,2} &= e, \mu \\ BRs &= \pi, K \quad \ell_{1,2} &= e, \mu \\ \end{array} \qquad \begin{aligned} \tau^{-} &\to \ell^{+} h_{1}^{-} h_{2}^{-} \\ \ell &= e, \mu \qquad h_{1,2} &= \pi, K \\ BRs &\leq \# 10^{-8} \\ \end{aligned}$$

 $(\mu^- \rightarrow e^+ \text{ conversion BR} \text{ at } 10^{-12} \text{ level})$

Collider processes, e.g. same sign di-lepton production at LHC

$$pp \rightarrow \ell\ell + 2 \text{ jets} \qquad \ell = e, \mu, \tau$$

• Neutrinoless double beta decay

$$(N,Z) \rightarrow (N-2,Z+2) + e^- + e^ T_{1/2} > \# 10^{25} \text{yr}$$

- 0vββ provides in many scenarios the strongest sensitivity to `ee' LNV couplings ("Avogadro's number wins", P. Vogel)
- Other processes can be competitive for `ee' couplings in certain scenarios and probe flavorful LNV couplings beyond `ee', inaccessible in $0\nu\beta\beta$

Given our ignorance of the mechanism and scale of LNV

Ļ

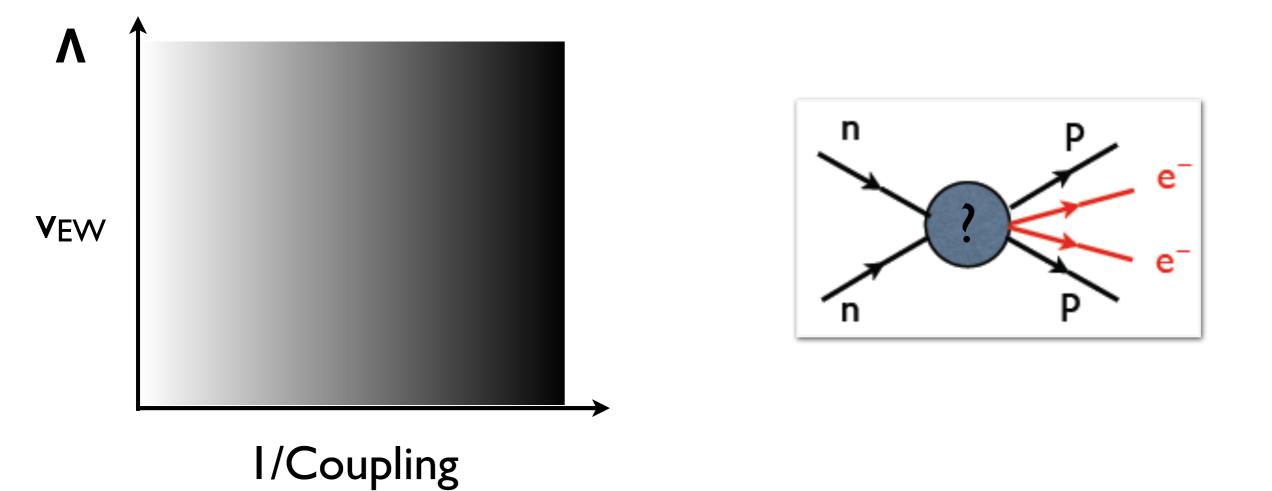
Pursuing many probes is essential. While LNV discovery may come from 0vββ, all probes will be essential to reconstruct LNV origin. This requires an ambitious theoretical program [WP 2203. 21169]

$$pp \rightarrow \ell\ell + 2 \text{ jets}$$

$$\ell = e, \mu, \tau$$

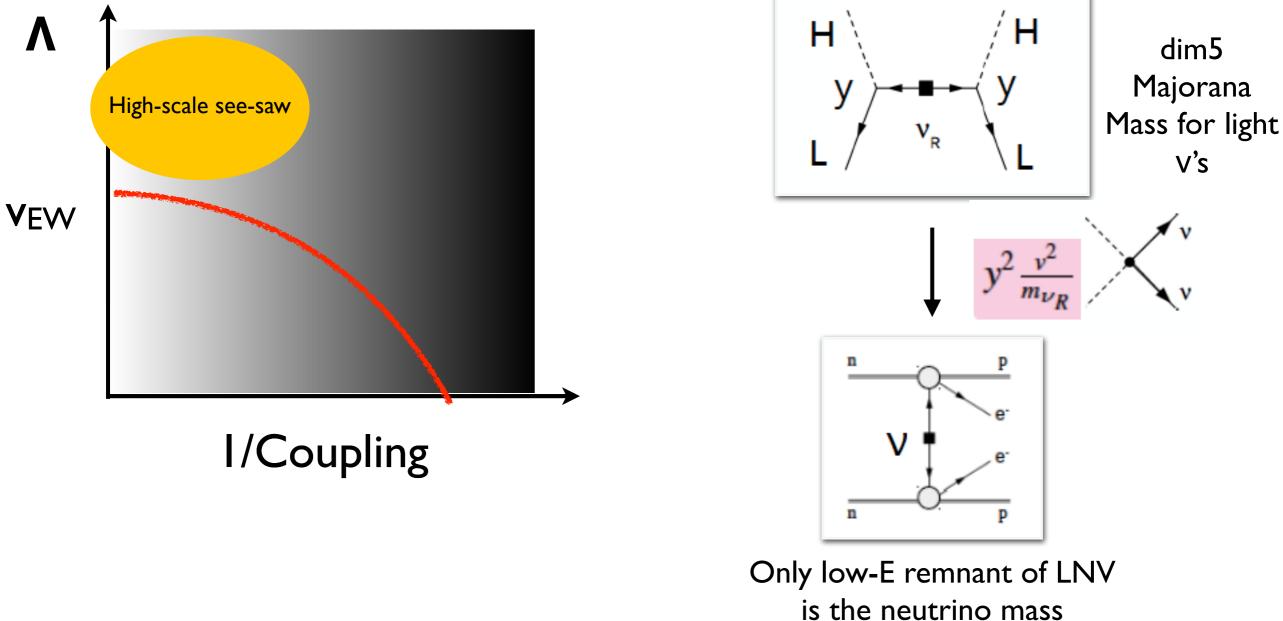
$0\nu\beta\beta$ physics reach

• Ton-scale $0\nu\beta\beta$ searches (T_{1/2} > 10^{27-28} yr) will probe at unprecedented levels LNV from a broad range of mechanisms



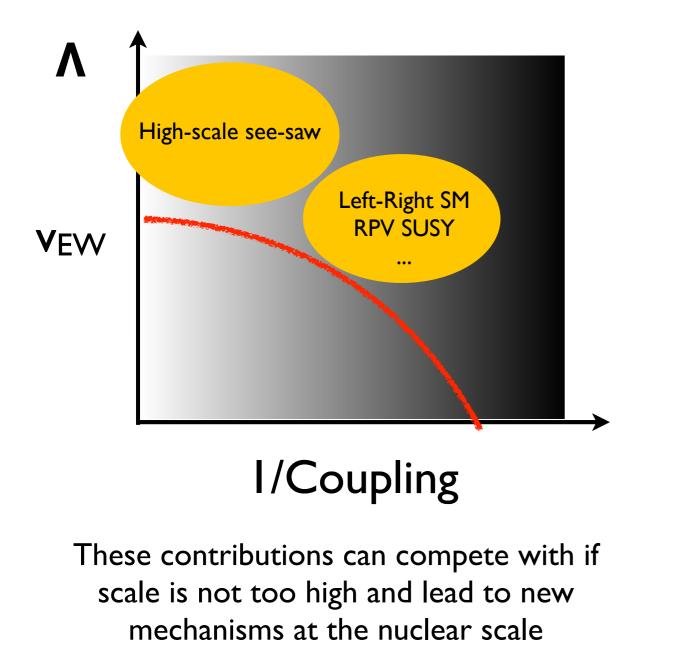
$0\nu\beta\beta$ physics reach

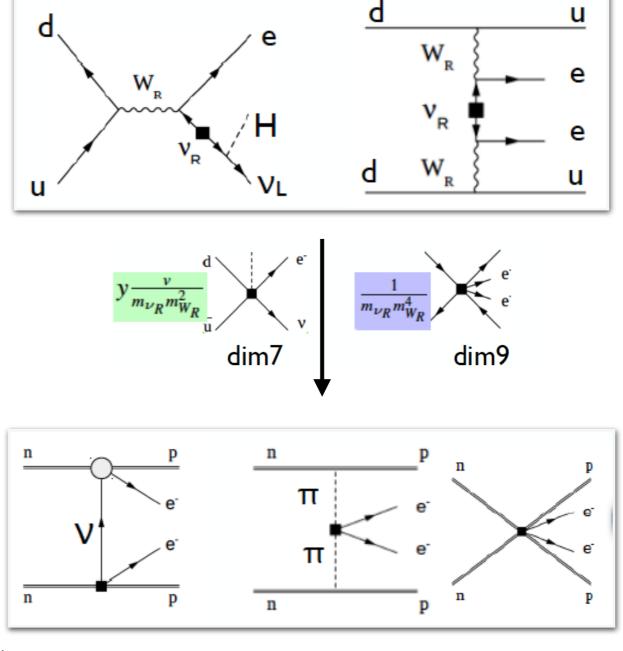
• Ton-scale $0\nu\beta\beta$ searches (T_{1/2} > 10^{27-28} yr) will probe at unprecedented levels LNV from a broad range of mechanisms



$0v\beta\beta$ physics reach

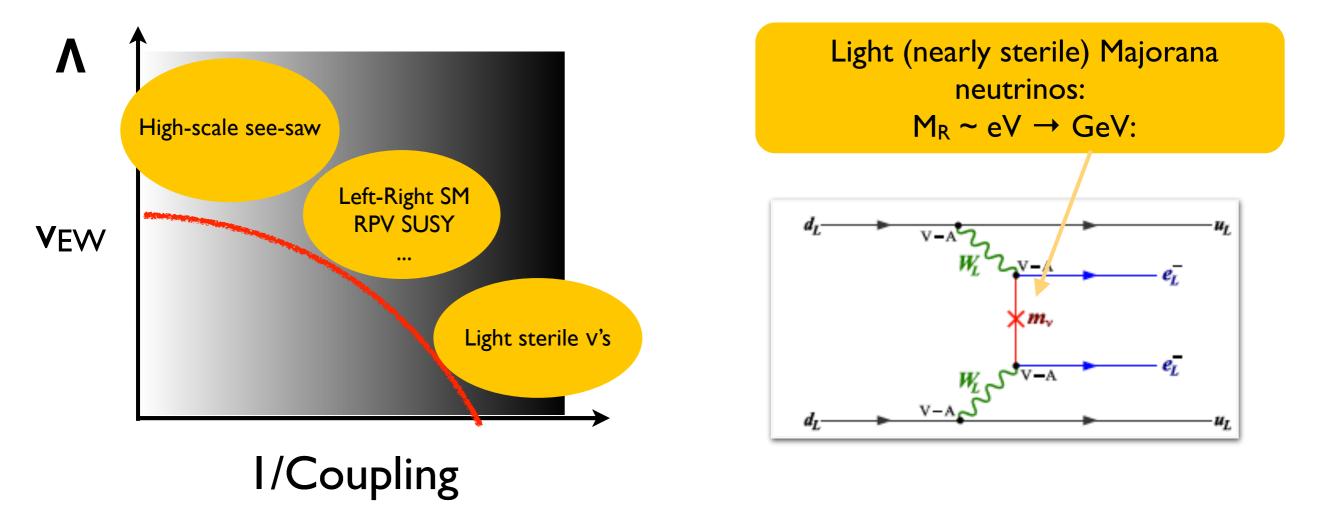
• Ton-scale $0\nu\beta\beta$ searches (T_{1/2} > 10^{27-28} yr) will probe at unprecedented levels LNV from a broad range of mechanisms





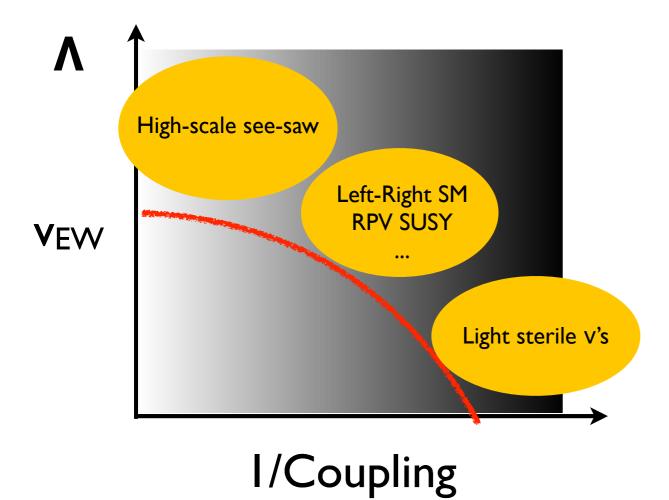
$0\nu\beta\beta$ physics reach

• Ton-scale $0\nu\beta\beta$ searches $(T_{1/2} > 10^{27-28} \text{ yr})$ will probe at unprecedented levels LNV from a broad range of mechanisms



$0\nu\beta\beta$ physics reach

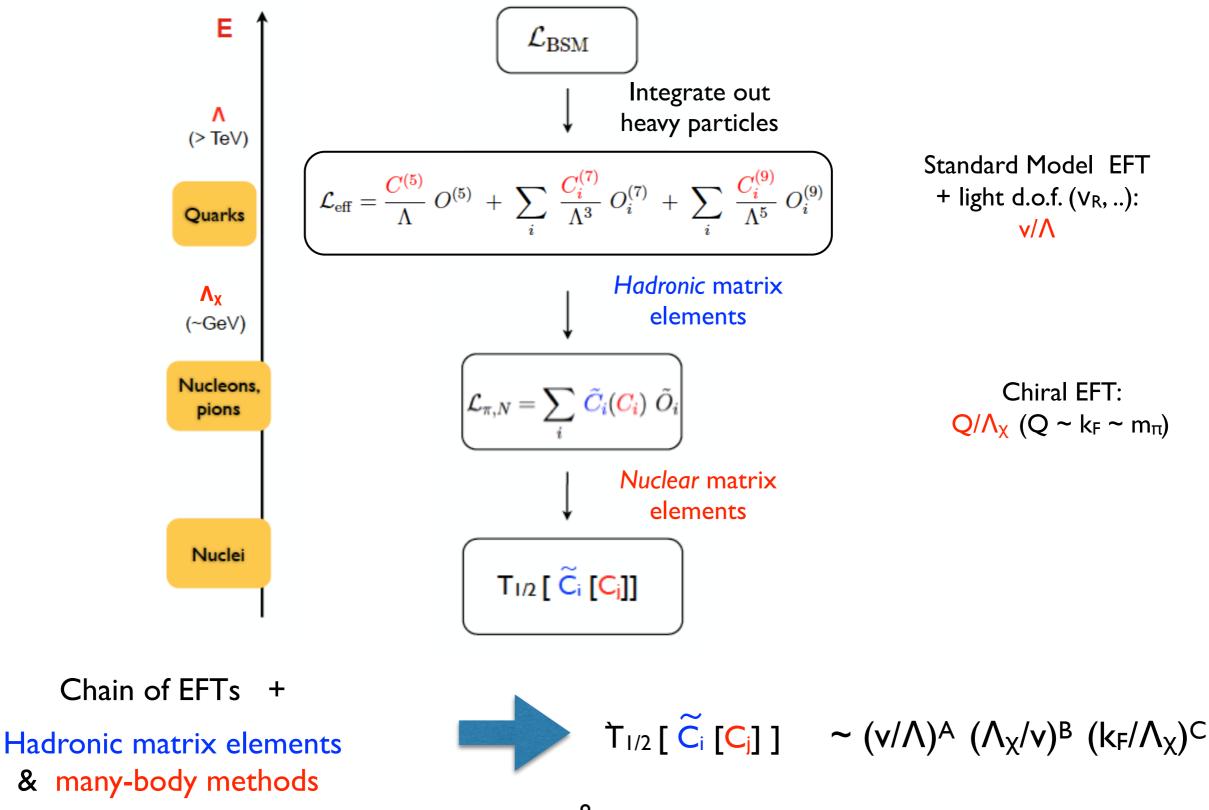
• Ton-scale $0\nu\beta\beta$ searches $(T_{1/2} > 10^{27-28} \text{ yr})$ will probe at unprecedented levels LNV from a broad range of mechanisms



0vββ's impact and relation to other probes of LNV is best analyzed through a tower of EFTs that connect LNV scale Λ to nuclear scales, with controllable uncertainties

See VC-Dekens-deVries-Graesser-Mereghetti 1806.02780 and references therein

EFT framework



Main themes

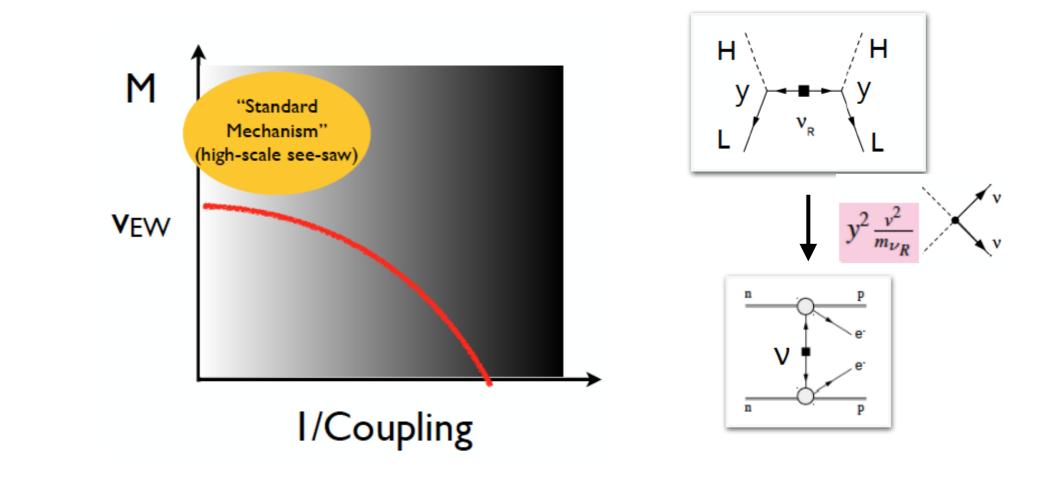
WP 2203. 21169

- Model building and phenomenology:
 - Investigate correlated signals of TeV (and lower) scale LNV across multiple phenomena and experiments, from cosmology to colliders to nuclei
- The "hadronic threshold":
 - Somewhat overlooked in the past. EFT methods have revealed that this is relevant even for light V exchange mechanism
 - Requires two-nucleon matrix elements from LQCD: decadal program
- Nuclear matrix elements:
 - Shift from phenomenological approaches to nuclear "ab-initio" methods, with EFT-based nucleon interactions rooted in QCD.
 - First results for ⁴⁸Ca decay. Ambitious & challenging program ahead

In the rest of this talk

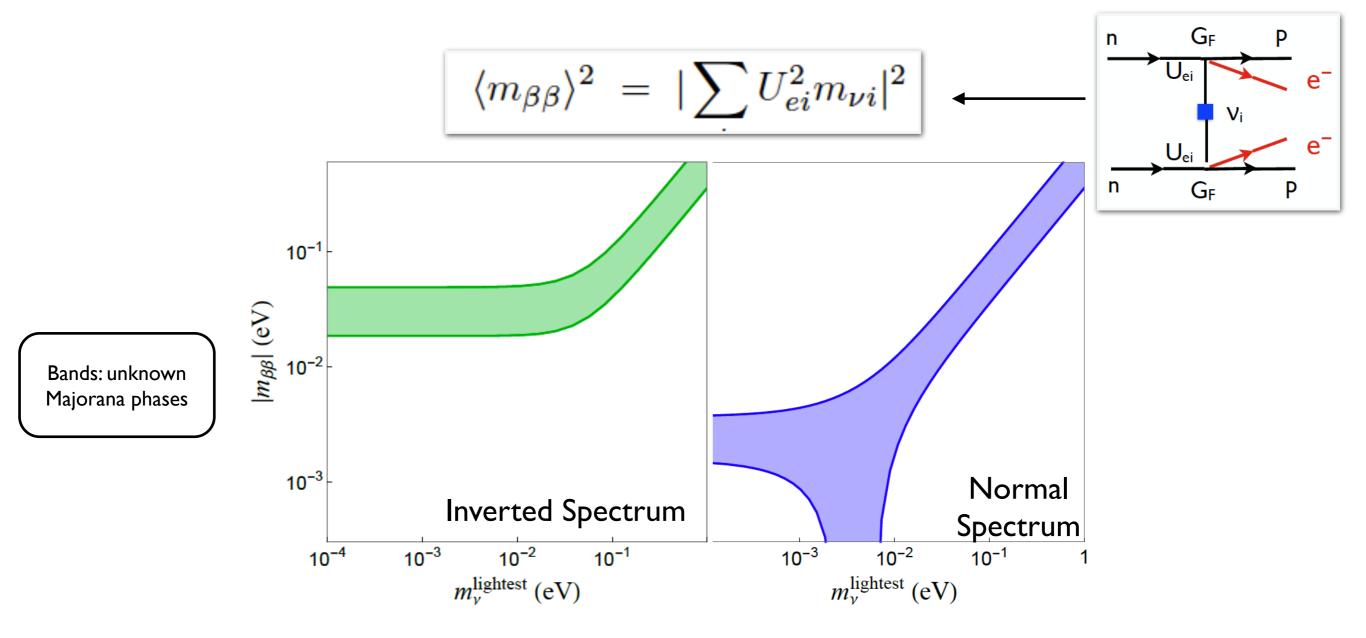
- Survey classes of models by LNV scale (op. dimension), highlighting:
 - phenomenological interest
 - theoretical developments and challenges (EFT, hadronic / nuclear matrix elements, ...)

High-scale seesaw (LNV at dim-5)



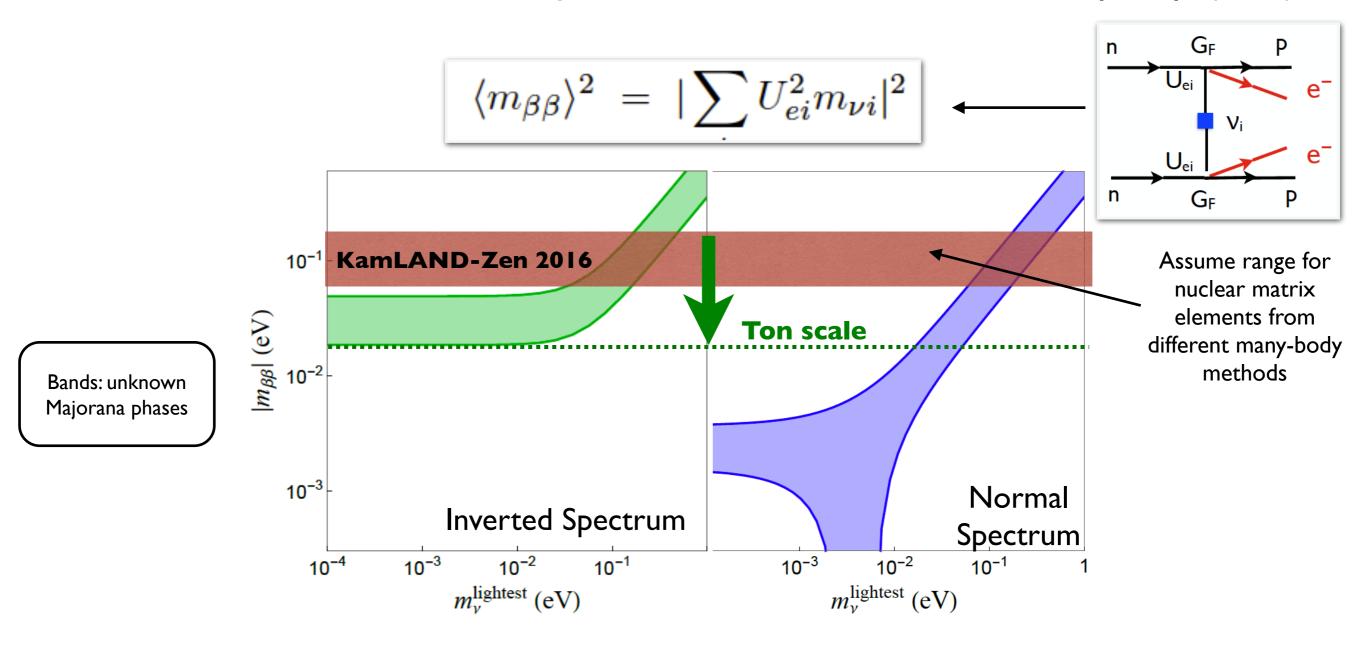
Discovery potential / target

• In this case $0\nu\beta\beta$ is a direct probe of ν Majorana mass: $\Gamma \propto |M_{0\nu}|^2 (m_{\beta\beta})^2$



Discovery potential / target

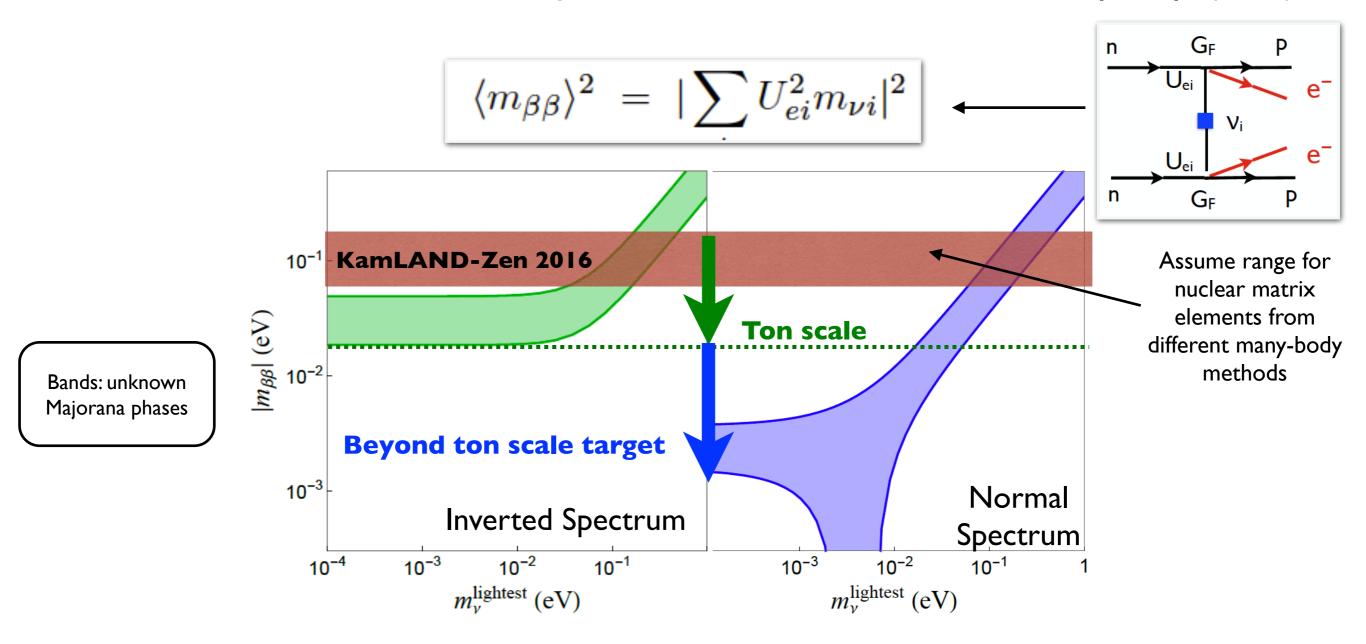
• In this case $0\nu\beta\beta$ is a direct probe of ν Majorana mass: $\Gamma \propto |M_{0\nu}|^2 (m_{\beta\beta})^2$



Assuming current range for matrix elements, discovery @ ton-scale *possible* for inverted spectrum or m_{lightest} > 50 meV

Discovery potential / target

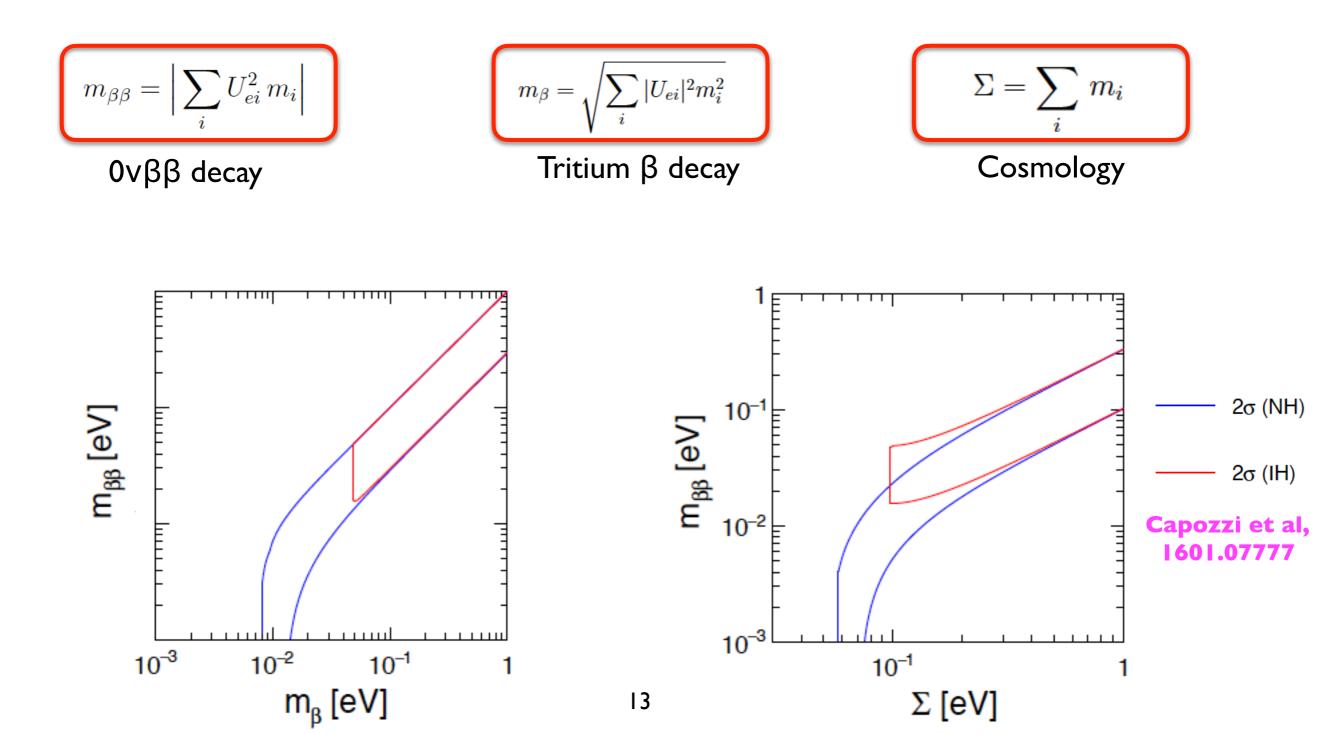
• In this case $0\nu\beta\beta$ is a direct probe of ν Majorana mass: $\Gamma \propto |M_{0\nu}|^2 (m_{\beta\beta})^2$



Natural (but challenging!) beyond ton-scale target seems $m_{\beta\beta} \sim meV$

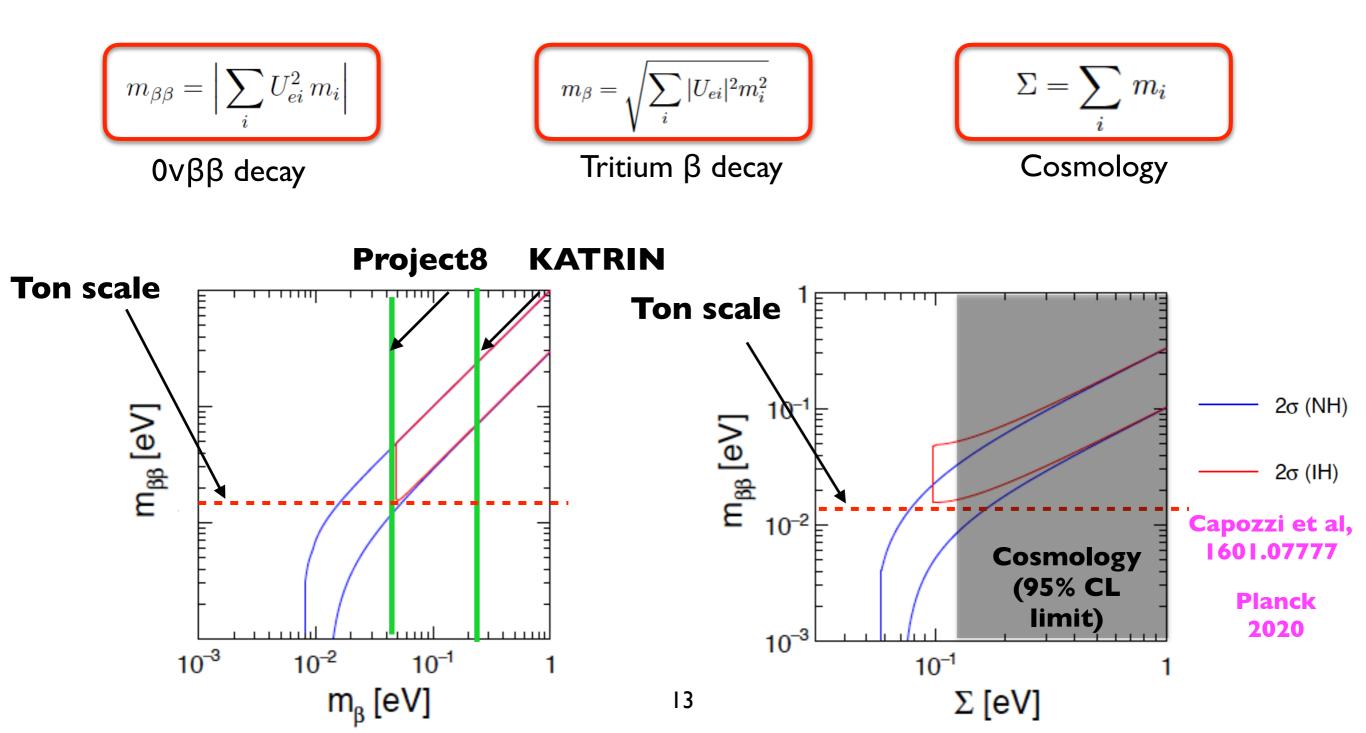
Diagnosing power

• High scale seesaw implies falsifiable correlation with other V mass probes. Future data can unravel new LNV sources or physics beyond " Λ CDM + m_v"



Diagnosing power

• High scale seesaw implies falsifiable correlation with other V mass probes. Future data can unravel new LNV sources or physics beyond " Λ CDM + m_v"



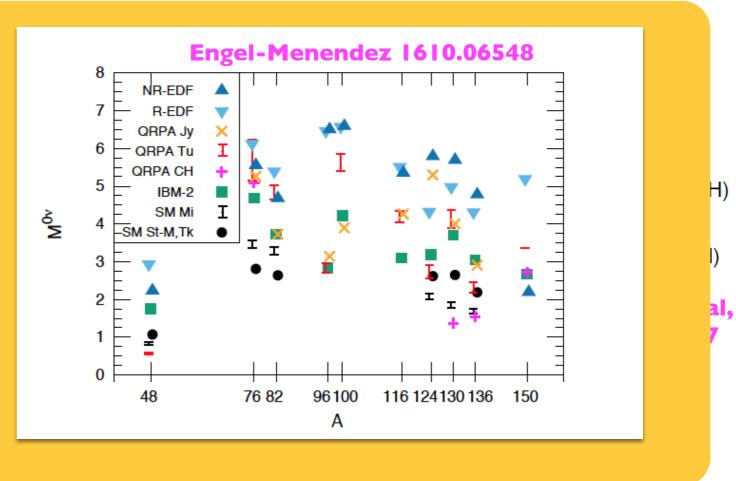
Diagnosing power

High scale seesaw implies falsifiable correlation with other v mass probes.
Future data can unravel new LNV sources or physics beyond "ΛCDM + m_v"

$$\begin{aligned} m_{\beta\beta} &= \left| \sum_{i} U_{ei}^2 m_i \right| \\ \mathbf{0} \mathbf{v} \mathbf{\beta} \mathbf{\beta} \text{ decay} \end{aligned} \qquad \begin{aligned} m_{\beta} &= \sqrt{\sum_{i} |U_{ei}|^2 m_i^2} \\ \mathbf{Tritium} \mathbf{\beta} \text{ decay} \end{aligned} \qquad \begin{aligned} \Sigma &= \sum_{i} m_i \\ \mathbf{Cosmology} \end{aligned}$$

But these important quantitative connections require knowing nuclear matrix elements and their uncertainties!

Τα

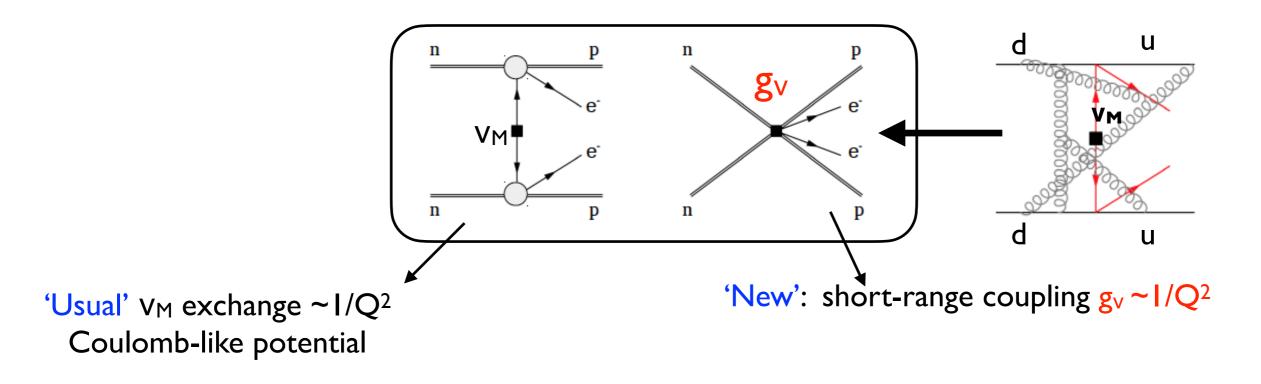


7 [ev]

New insights from EFT

VC, W. Dekens, E. Mereghetti, A. Walker-Loud, 1710.01729 VC, W. Dekens, J. de Vries, M. Graesser, E. Mereghetti, S. Pastore, U. van Kolck 1802.10097

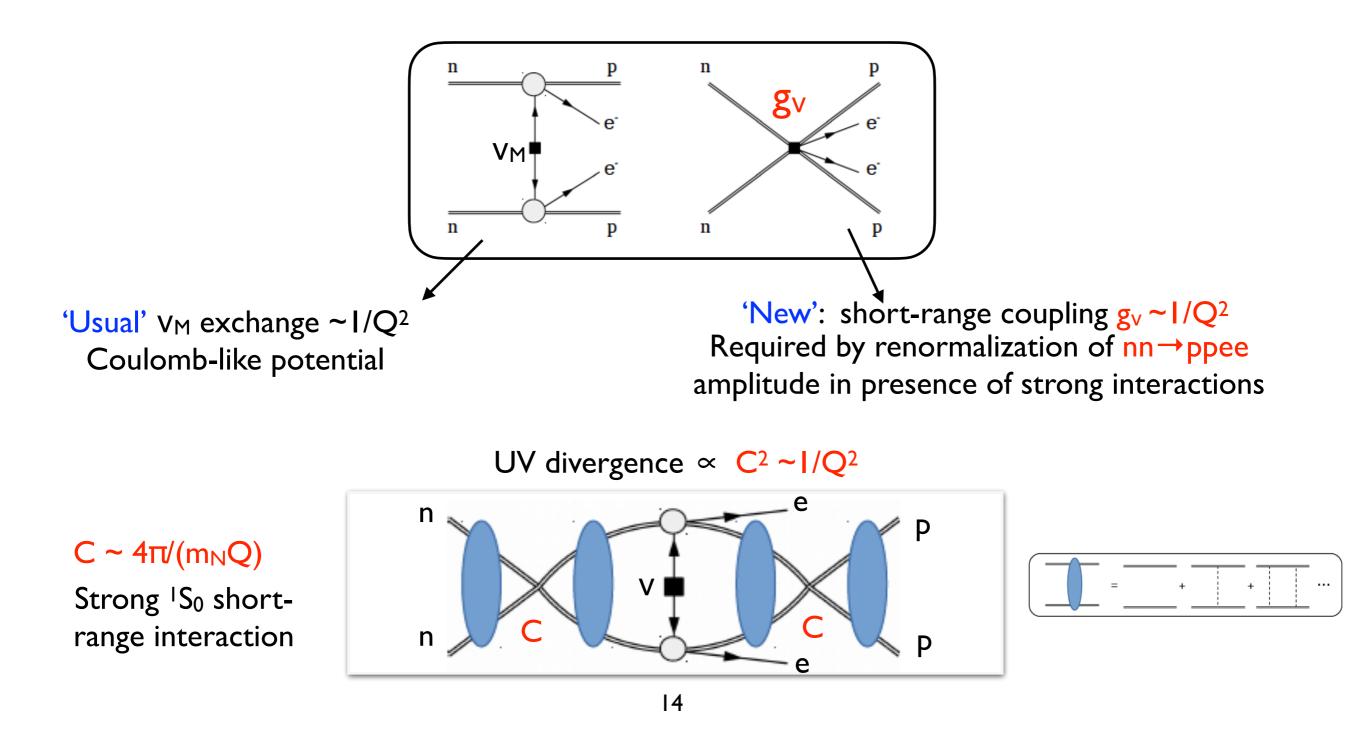
• Transition operator to leading order in Q/Λ_{χ} (Q~k_F~m_T, Λ_{χ} ~GeV)



New insights from EFT

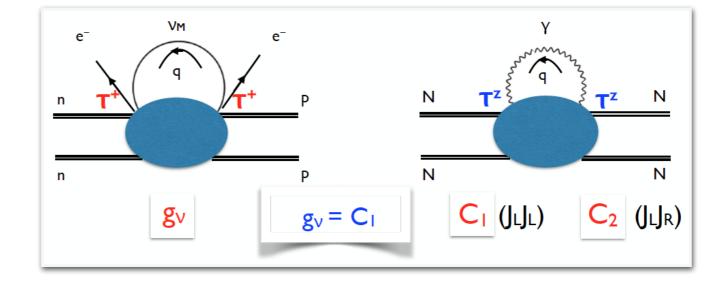
VC, W. Dekens, E. Mereghetti, A. Walker-Loud, 1710.01729 VC, W. Dekens, J. de Vries, M. Graesser, E. Mereghetti, S. Pastore, U. van Kolck 1802.10097

• Transition operator to leading order in Q/Λ_{χ} (Q~k_F~m_T, Λ_{χ} ~GeV)



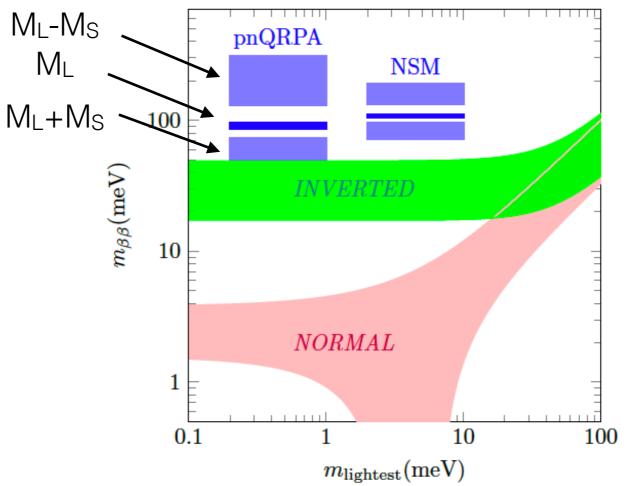
Impact on nuclear matrix elements

 Chiral+isospin symmetry relates g_v to one of two I=2 e.m. couplings (hard γ's & v's)



- NN data $(a_{nn}+a_{pp}-2a_{np})$ determine C_1+C_2 , confirming LO scaling
- Assuming $g_v \sim (C_1 + C_2)/2$ $\rightarrow O(1)$ impact on m.e. and $m_{\beta\beta}$ extraction

Jokiniemi-Soriano-Menendez, 2107.13354



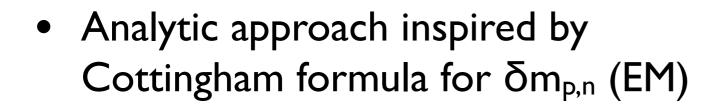
Towards determining gv

- Large-N_C arguments point to $g_v \sim (C_1 + C_2)/2$
- Lattice QCD
 - $\pi^- \rightarrow \pi^+ e^- e^-$ precisely known
 - Formalism for NN developed

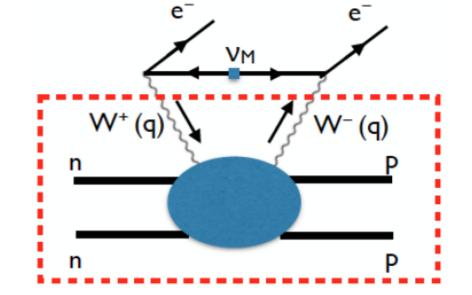
Richardson, Shindler, Pastore, Springer, 2102.02814

Tuo et al. 1909.13525; Detmold, Murphy 2004.07404

Davoudi, Kadam, 2012.02083 Feng, Jin, Wang, Zhang, 2005.01956



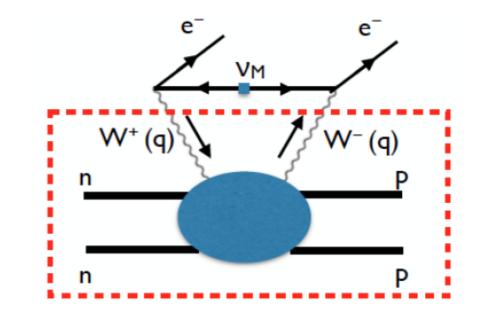
VC, Dekens, deVries, Hoferichter, Mereghetti, 2012.11602, 2102.03371



Towards determining gv

- Dispersive approach provides $C_{1,2}$ and can be validated by data: $C_1+C_2 \Rightarrow (a_{nn}+a_{pp})/2 - a_{np} = 15.5(4.5)$ fm versus 10.4(2) fm (exp)
- Ab initio (IMSRG) calculation of ${}^{48}Ca \rightarrow {}^{48}Ti$ with dispersive $g_v = C_1$ \Rightarrow contact term enhances nuclear matrix element by $(43\pm7)\%$
- Lattice QCD results expected in the next few years

 Analytic approach inspired by Cottingham formula for δm_{p,n} (EM)

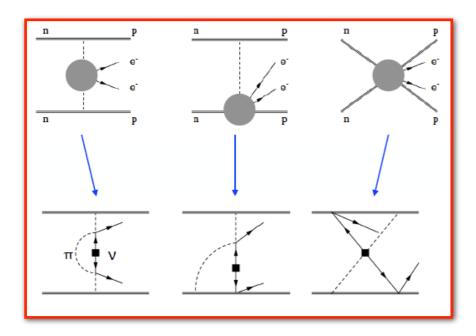


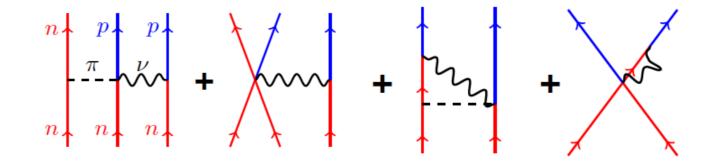
VC, Dekens, deVries, Hoferichter, Mereghetti, 2012.11602, 2102.03371

What about higher orders?

- N2LO
 - πN loops + new contact VC, W. Dekens, E. Mereghetti, A. Walker-Loud, 1710.01729
 - 2-body x 1-body current (and a new contact) Wang-Engel-Yao 1805.10276
 - Neglecting contact terms, calculations in light and heavy nuclei find O(10%) corrections: encouraging!

S. Pastore, J. Carlson, V.C., W. Dekens, E. Mereghetti, R. Wiringa 1710.05026 J. Engel, private communication





What about higher orders?

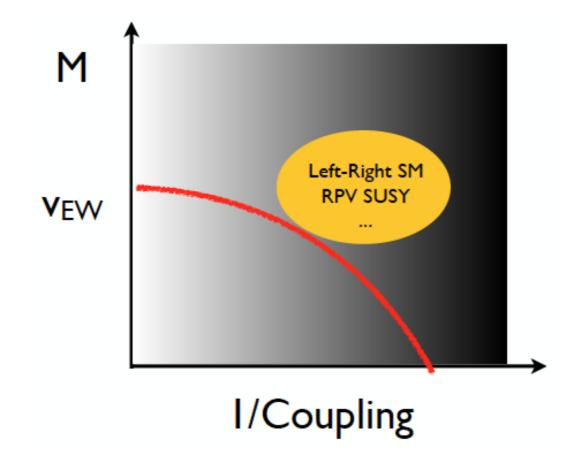
- N2LO
 - πN loops + new contact VC, W. Dekens, E. Mereghetti, A. Walker-Loud, 1710.01729
 - 2-body x 1-body current (and a new contact) Wang-Engel-Yao 1805.10276
 - Neglecting contact terms, calculations in light and heavy nuclei find O(10%) corrections: encouraging!

S. Pastore, J. Carlson, V.C., W. Dekens, E. Mereghetti, R. Wiringa 1710.05026 J. Engel, private communication



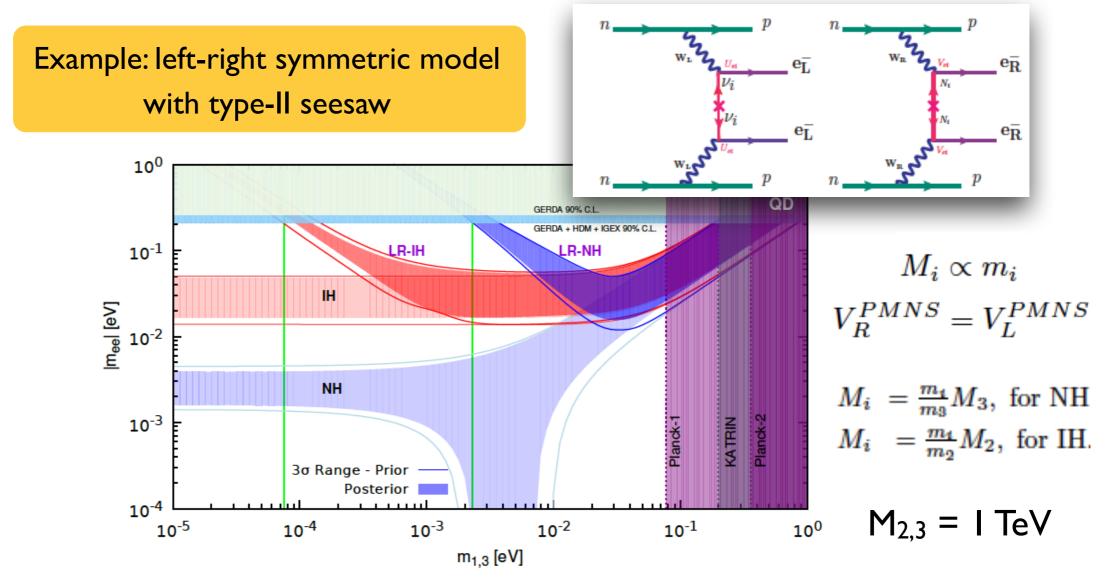
Full analysis beyond leading order requires again matching to Lattice QCD and dedicated many body calculations — decadal goal

0vββ from multi-TeV scale dynamics (dim-7, 9, ...operators)



• Induce contributions to $0\nu\beta\beta$ not directly related to the exchange of light neutrinos, within reach of current experiments

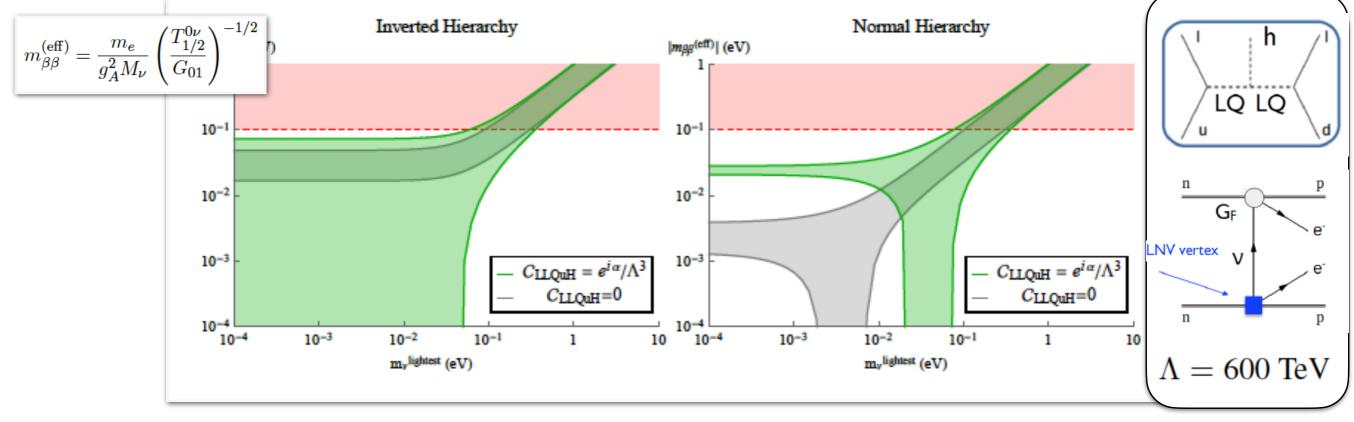
• Induce contributions to $0V\beta\beta$ not directly related to the exchange of light neutrinos, within reach of current experiments



Tello-Nemevesek-Nesti-Senjanovic-Vissani 1011.3522 Ge-Lindner-Patra 1508.07286. **

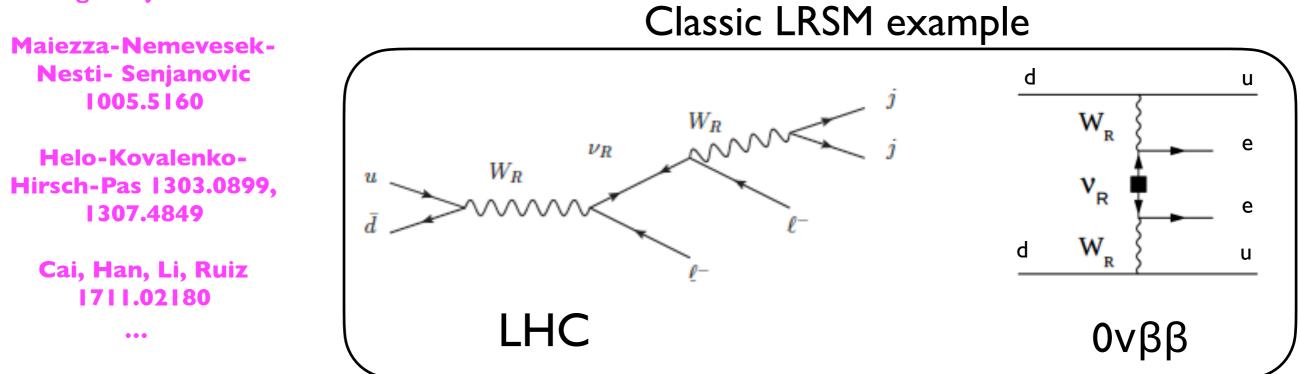
• Induce contributions to $0\nu\beta\beta$ not directly related to the exchange of light neutrinos, within reach of current experiments

New contributions can add incoherently or interfere with $m_{\beta\beta}$, significantly affecting the interpretation of experimental results



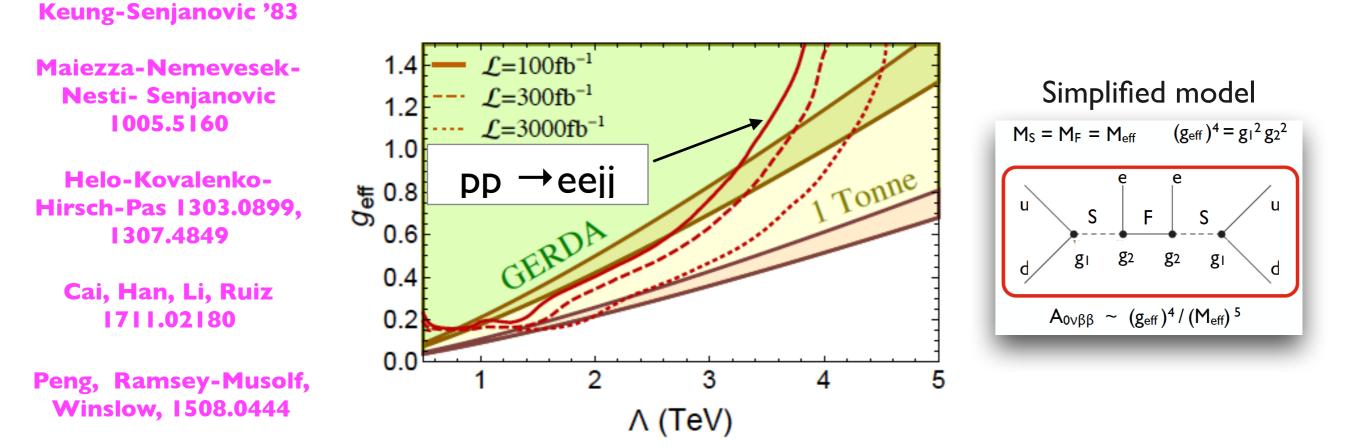
VC, W. Dekens, J. de Vries, M. Graesser, E. Mereghetti, 1708.09390

- Induce contributions to $0\nu\beta\beta$ not directly related to the exchange of light neutrinos, within reach of current experiments
- May lead to correlated (or precursor!) signal at LHC: $pp \rightarrow ee jj$



Keung-Senjanovic '83

- Induce contributions to $0\nu\beta\beta$ not directly related to the exchange of light neutrinos, within reach of current experiments
- May lead to correlated (or precursor!) signal at LHC: $pp \rightarrow ee jj$

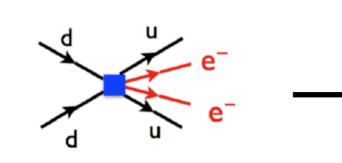


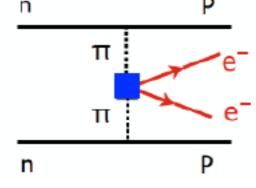
20

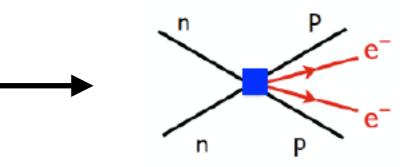
...

Hadronic theory developments

• Chiral EFT & Lattice QCD







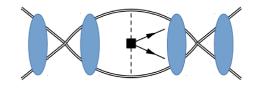
In Weinberg's counting, pion contribution dominates

Prezeau, Ramsey-Musolf,

Vogel hep-ph/0303205

ππ matrix element known from LQCD at <10%

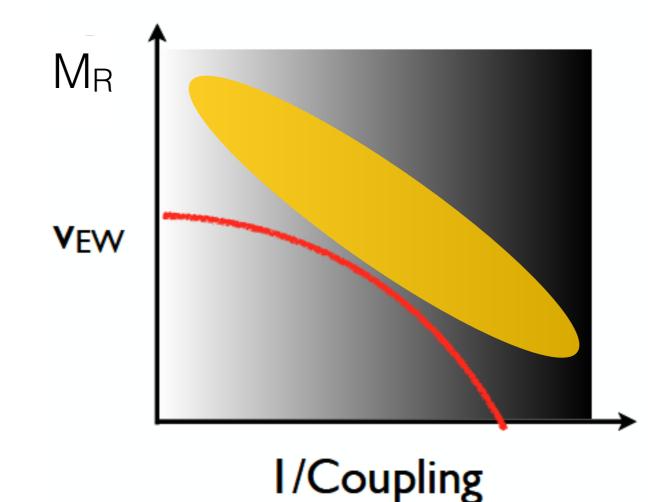
Nicholson et al (CalLat), 1805.02634 Renromalization requires a contact at the same order!



V.C, W. Dekens, J. de Vries, M. Graesser, E. Mereghetti [1806.02780]

• Several unknown LO NN contact couplings. Opportunity for LQCD

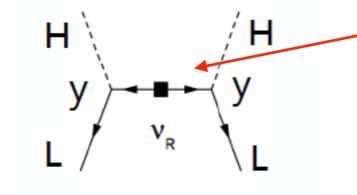
$0\nu\beta\beta$ and sterile neutrinos

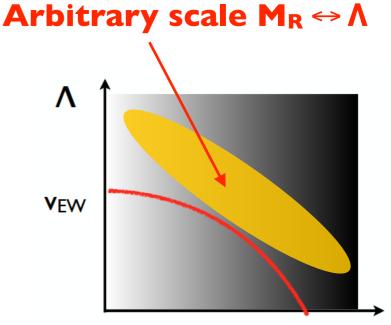


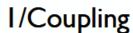
Akhmedov. Rubakov, Smirnov hep-ph/9803255

Canetti, Drewes, Shaposhnikov I 204.3902

...







- Attractive class of "minimal" models
 - V_R can give rise to light neutrino masses
 - V_R can provide a dark matter candidate
 - V_R can generate the baryon asymmetry through leptogenesis
- In general $m_{\beta\beta} \neq (m_{\beta\beta})_{active}$, with strong dependence on V_R spectrum
- Can be probed at colliders, beam dump, semileptonic decays, EWPO, ...

EFT developments and challenges

• vSMEFT + chiral EFT analysis

Dekens et al. 2002.07182

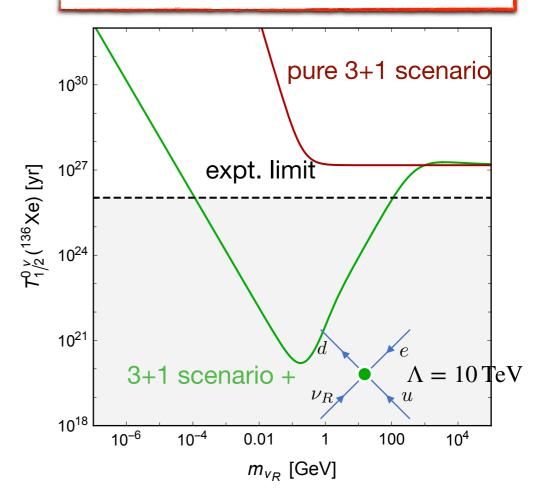


- V_R's interaction beyond Yukawa can have large impact
- Challenges:
 - New LECs in hadronic EFT
 - Dependence of m.e. and LECs on V_R mass

deGouvea et al hep-ph/0608147 Faessler et al, 1408.6077 Dekens et al. 2002.07182

...

O(100%) uncertainties not shown



Plot courtesy of Wouter Dekens

Unraveling $0v\beta\beta$ mechanisms?

Graf, Lindner, Scholer 2204.10845

• 32 operators below weak scale @ dim=3, 6, 7, 9 contribute to $0\nu\beta\beta$

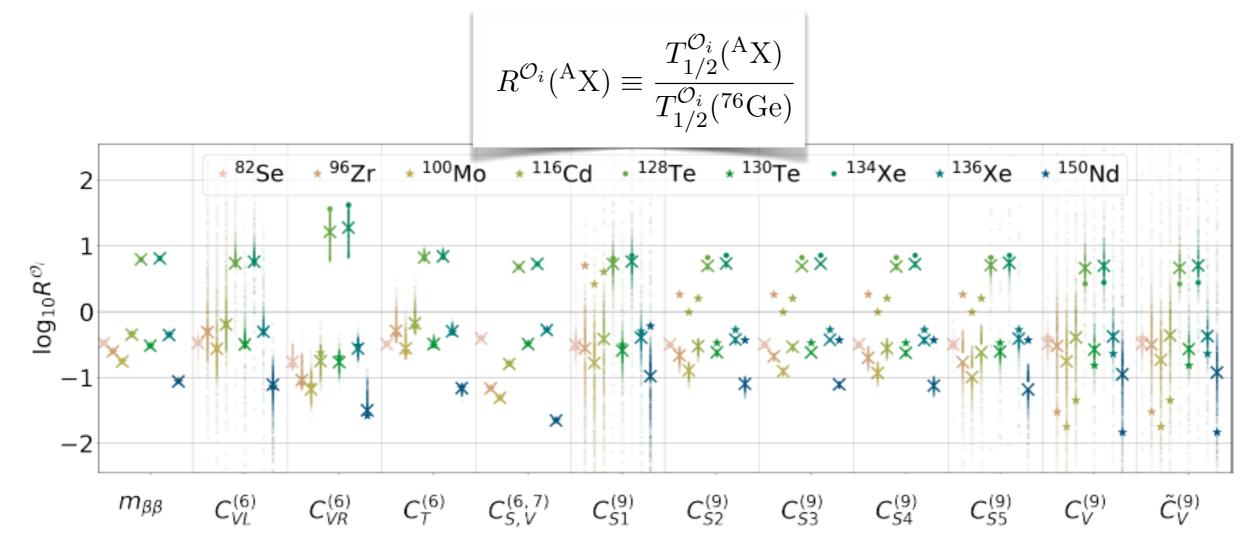
- Can they be distinguished by
 - I. Isotope-dependence of the decay rates?
 - 3. Phase space observable? (single electron spectra, relative angle of outgoing electrons)

Despite degeneracies, useful diagnosing tools 'within' $0\nu\beta\beta$

Isotope dependence

Graf, Lindner, Scholer 2204.10845

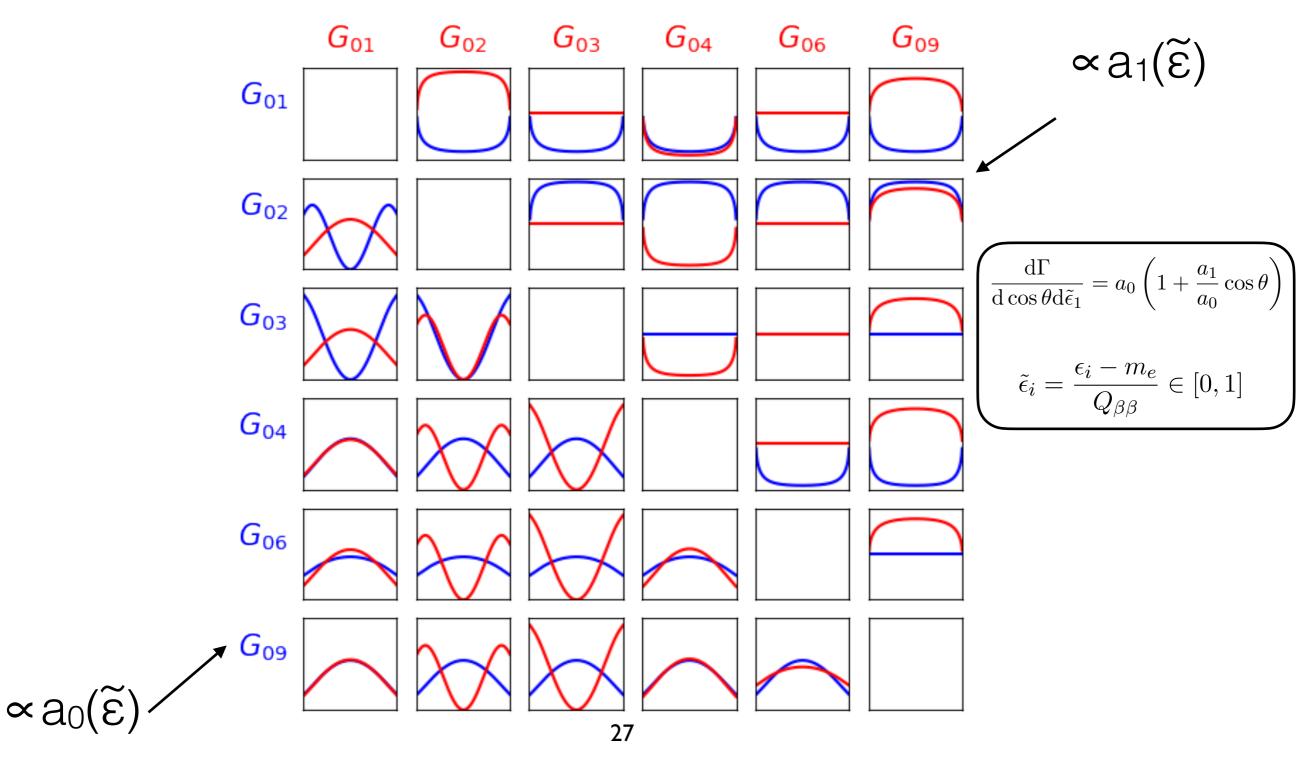
- Only 12 groups of operators can be distinguished by taking ratios of decay rates
- Quite sensitive to LECs (varied around reference values denoted by larger markers)
- Distinguishing classes of operators will require combined theoretical uncertainty of $\sim 10\%$, due to LEC + NME (here only IBM used)



Phase space observables

Graf, Lindner, Scholer 2204.10845

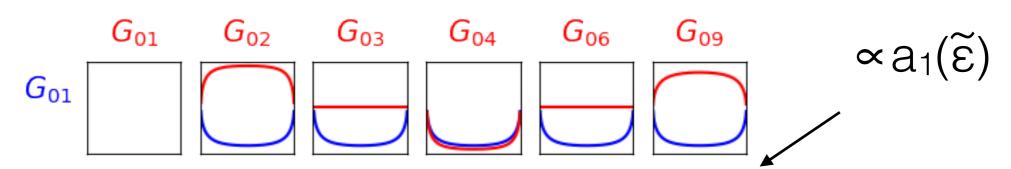
• Six phase space structures G_{0k} , after including interference terms



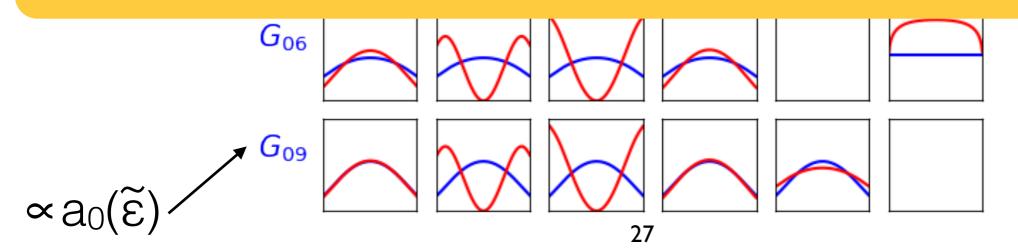
Phase space observables

Graf, Lindner, Scholer 2204.10845

- Six phase space structures G_{0k} , after including interference terms



- Despite degeneracies, useful diagnosing tools 'within' $0\nu\beta\beta$
- This analysis reiterates two important points:
 - Need much improved matrix elements, with O(10%) uncertainty
 - Unraveling the mechanism of LNV will also require other probes (cosmology, collider, ...)



LNV & $0\nu\beta\beta$ outlook

- Ton-scale $0\nu\beta\beta$ searches have great discovery potential we simply don't know the origin of m_v and the scale Λ associated with LNV
- Model diagnosing: what is the underlying source of LNV?
 - Within $0v\beta\beta$: rate variation with isotope; single electron spectra and electron's angle distribution
 - 0vββ + other probes: oscillations, direct m_v measurements, cosmology, meson & lepton decays, LNV @ colliders, LFV, ...
- Exciting prospects thanks to synergy of model building, cosmology, collider physics, EFT, lattice QCD, and nuclear structure + (of course) experiment!