



Neutrino interactions in FLUKA: NUNDIS

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Neutrinos in FLUKA

- Generators of neutrino-nucleon interactions:
 - QuasiElastic Acta Phys.Polon. B40 (2009) 2491-2505
 - Resonance CERN-Proceedings-2010-001 pp.387-394.
 - DIS
- Embedded in FLUKA nuclear models for Initial State and Final State effects
- Only for Argon: absorption of few-MeV (solar) neutrinos on whole nucleus
- Elastic scattering on electrons - to be refreshed
- Products of the neutrino interactions can be directly transported in the detector (or other) materials
- Used for all ICARUS simulations/publications

Web Site: <http://www.fluka.org>

Quasi Elastic and Resonant

QE

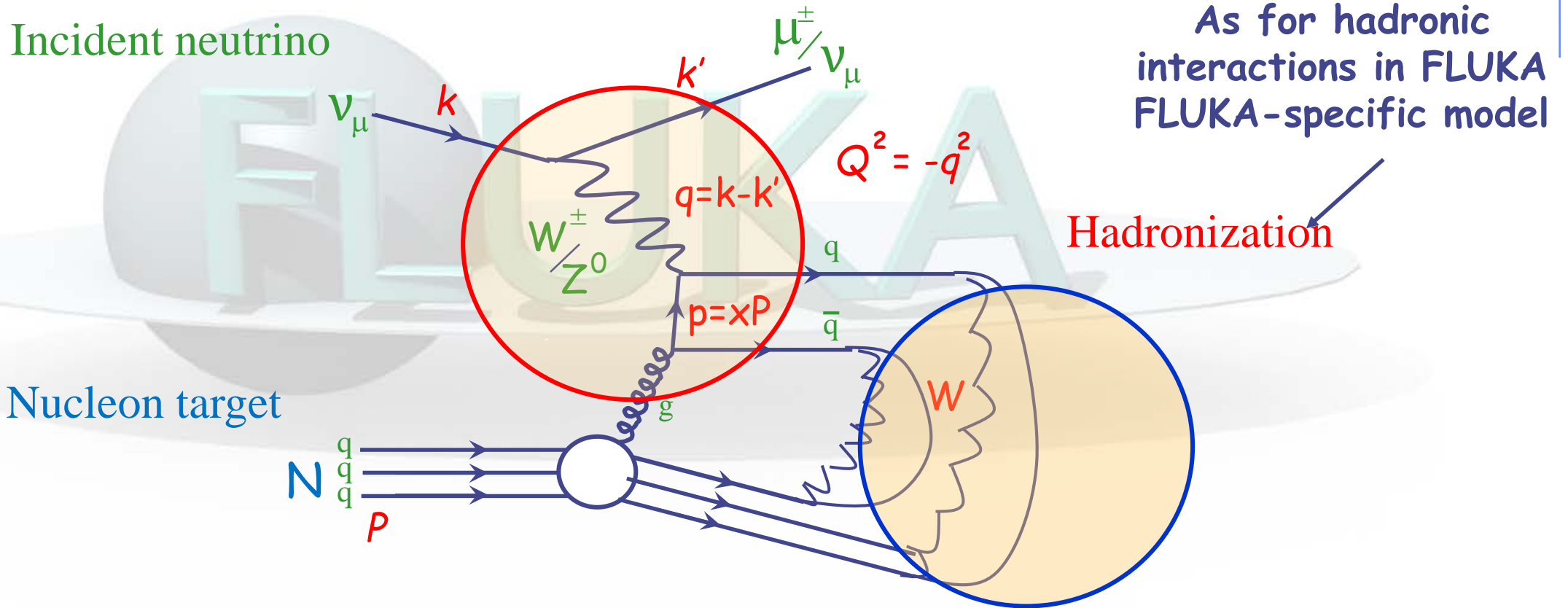
- Following Llewellyn Smith formulation
- $M_A = 1.03$, $M_V = 0.84$
- Lepton masses accounted for

Resonance production

- From Rein-Sehgal formulation
- Keep only Δ production
- No non-resonant background term, assuming that the non-resonant contribution comes from NunDIS
- **TRANSITION** from RES to DIS: linear decrease of both σ as a function of W

DIS (NUNDIS)

FLUKA hadronization and nuclear interactions work well independently of primary interaction vertex



Sample x and Q^2 from double differential cross sections

$$\frac{d^2\sigma}{dx dQ^2} = \frac{d^2\sigma}{dx dy} \cdot \frac{dy}{dQ^2} = \frac{d^2\sigma}{dx dy} \cdot \frac{1}{2ME_\nu x}$$

$$\frac{d^2\sigma}{dx dy} = \frac{G_F^2 M E_\nu}{\pi(1 + Q^2/M_{W/Z}^2)^2} \sum_{i=1}^5 A_i(x, y, E_\nu) F_i(Q^2, x)$$

Structure functions $F_i(Q^2, x)$

$$F_2^{\nu p}(Q^2, x) = 2x[d + \bar{u} + s + \bar{c}]$$

$$xF_3^{\nu p}(Q^2, x) = 2x[d - \bar{u} + s - \bar{c}]$$

Callan-Gross relation: $F_1 = \frac{F_2}{2x}$

To be updated to

$$2xF_1(Q^2, x) = F_2(Q^2, x) \frac{1 + 4M^2 x^2 / Q^2}{1 + R(Q^2, x)}$$

Albright-Jarlskog relations:

$$F_4 = 0,$$

$$F_5 = \frac{F_2}{x}.$$

$$A_1 = y \left(xy + \frac{m_\ell^2}{2ME_\nu} \right)$$

$$A_2 = 1 - y \left(1 + \frac{Mx}{2E_\nu} \right) - \frac{m_\ell^2}{4E_\nu^2}$$

$$A_3 = \pm y \left[x \left(1 - \frac{y}{2} \right) - \frac{m_\ell^2}{4ME_\nu} \right]$$

$$A_4 = \frac{m_\ell^2}{2ME_\nu} \left(y + \frac{m_\ell^2}{2ME_\nu x} \right)$$

$$A_5 = -\frac{m_\ell^2}{ME_\nu}$$

Quark dependence $q_i(Q^2, x)$ determined from Parton Distribution Functions (PDFs)

GRV94	Glück et al., Z. Phys. C67 (1995) 433.
GRV98	Glück et al., Eur. Phys. J. C5 (1998) 461.
BBS	Bourelly et al., Eur. Phys. J. C23 (2003) 487.
CTEQ	J. High Energy Phys. 0207 (2002) 012.
MRST	arXiv:hep-ph/0211080.
Alekhin	Phys. Rev. D68 (2003) 014002.
...	...

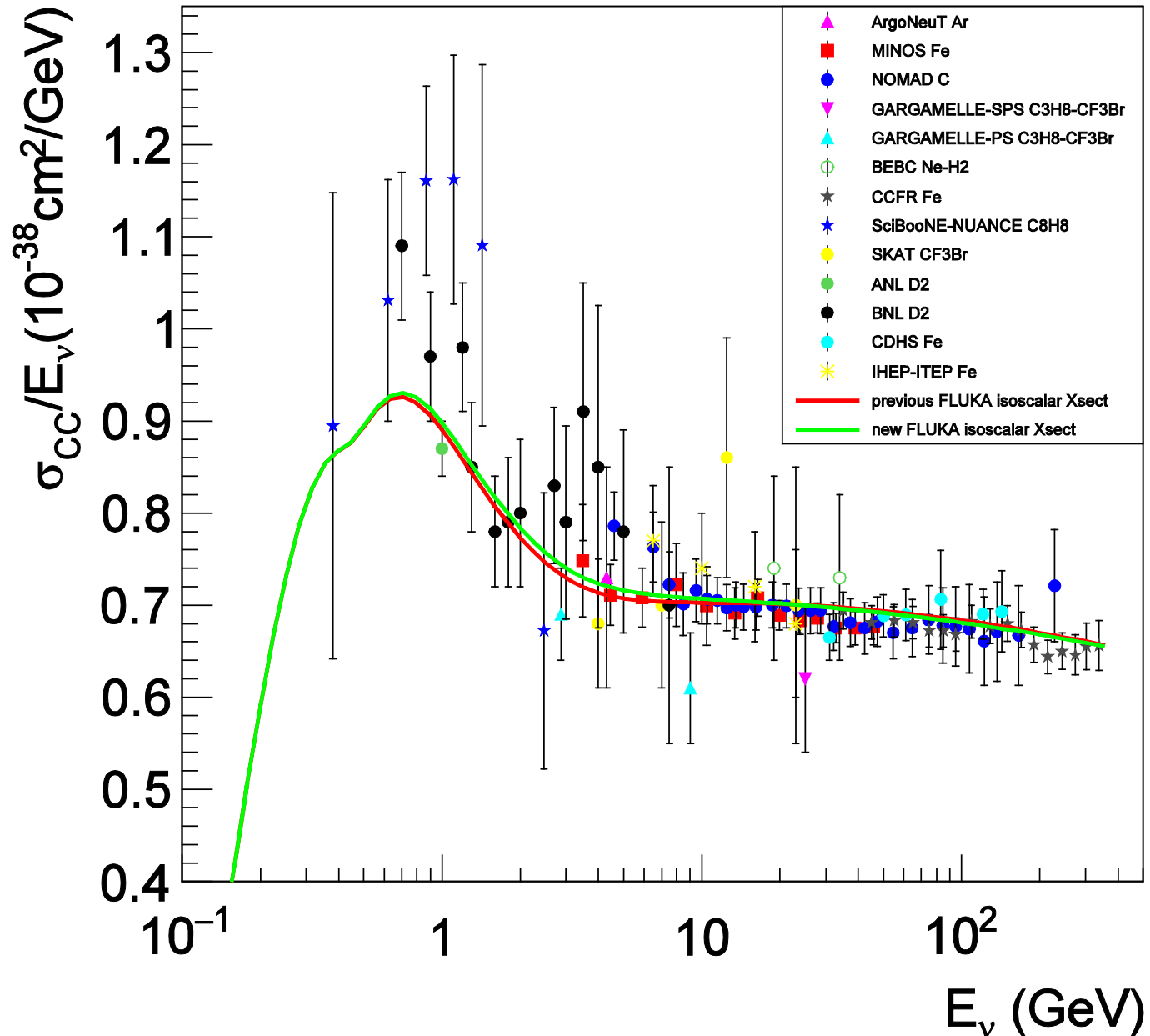
NUNDIS WORKS WITH THESE PDFs

DEFAULT OPTION

In the NLO (DIS) version
M. Glück, E. Reya and A. Vogt, Eur. Phys. J. C5 (1998) 461
With extrapolation to $Q^2=0$ as in
M. Bertini et al. 1996

Comparison with data on total cross section

Isoscalar
 ν_μ - Nucleon total
CC cross section
Fluka (lines) with
two pdf options
Vs
Experimental data



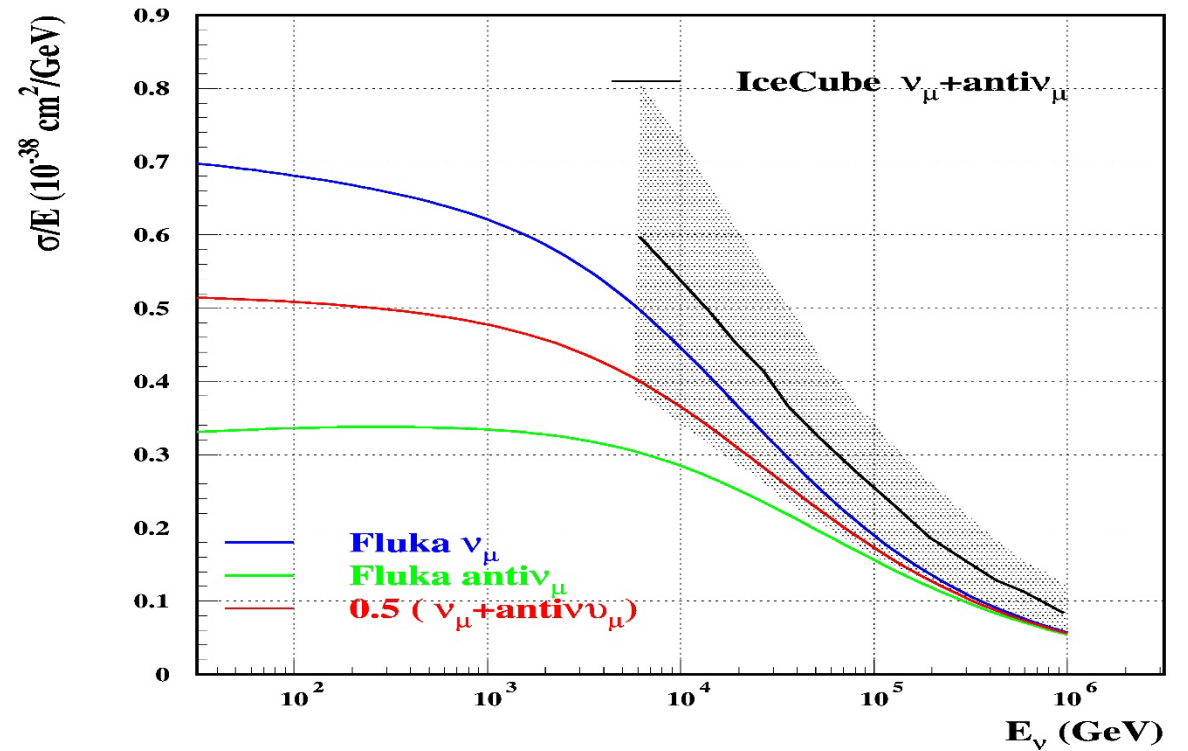
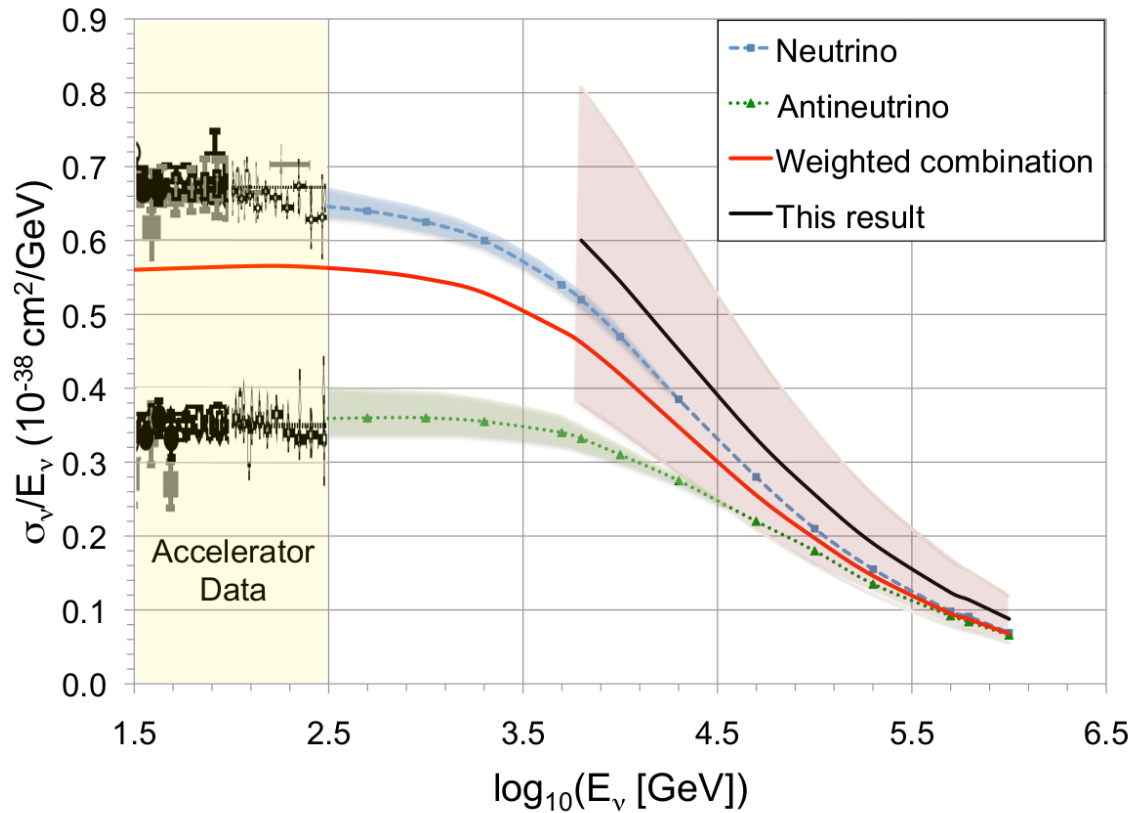
At higher energies

IceCube cross section data, Muon neutrino and antineutrino ,
"weighted combination" ?

[arXiv:1711.08119](https://arxiv.org/abs/1711.08119) , *Nature* 51,596 (2017)

Blue and green: "standard model predictions"

FLUKA results



Hadronization

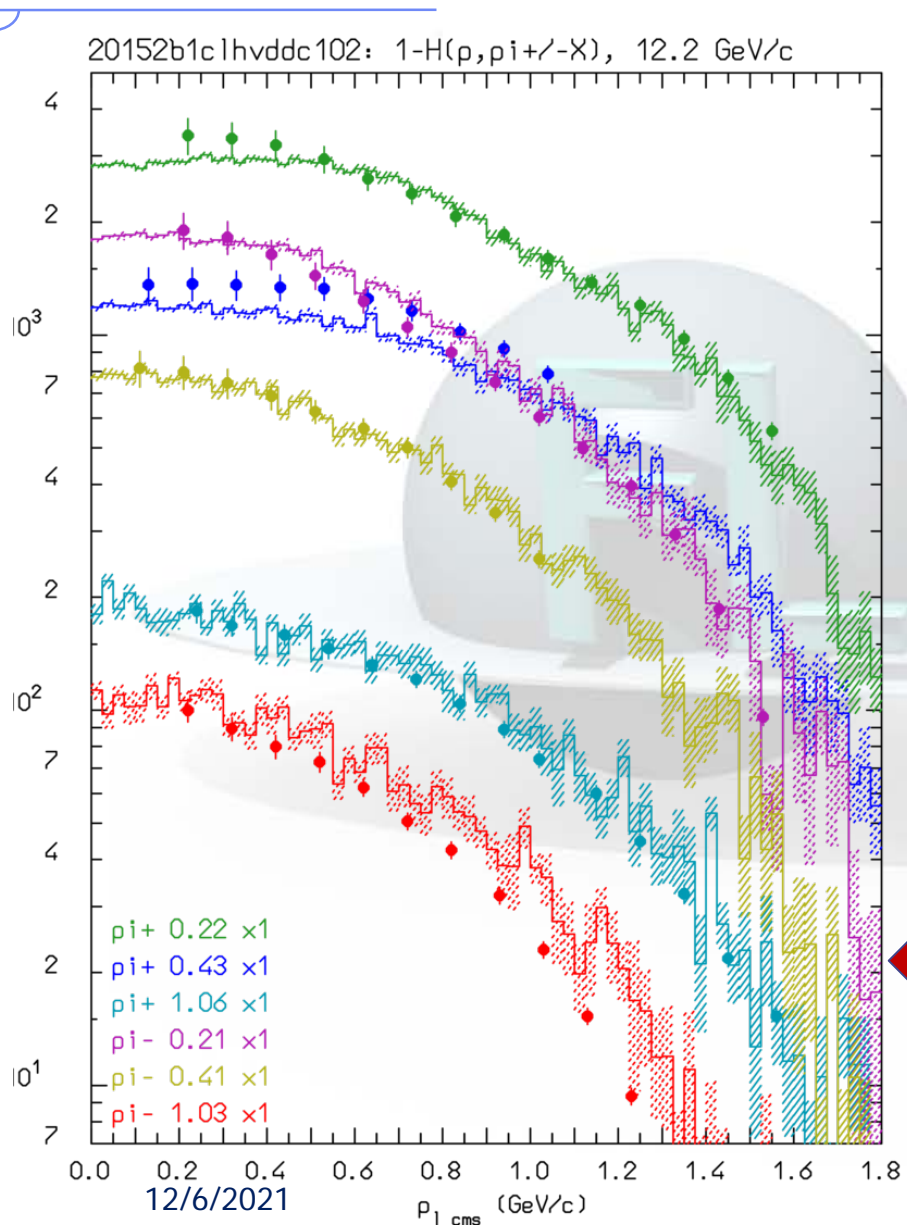
Implementation FLUKA-native
(evolution of old BAMJET)

- Assumes chain universality
- Fragmentation functions from hard processes and $e+e^-$ scattering
- Transverse momentum from uncertainty considerations
- Mass effects at low energies (change fragmentation function to account for the need to create real hadrons)
- Chains generated at very low energy \rightarrow create single resonances
- Chains generated at low energy \rightarrow “phase space explosion” constrained in p_T , including baryons, mesons, resonances.

The same functions and parameters for all reactions and energies

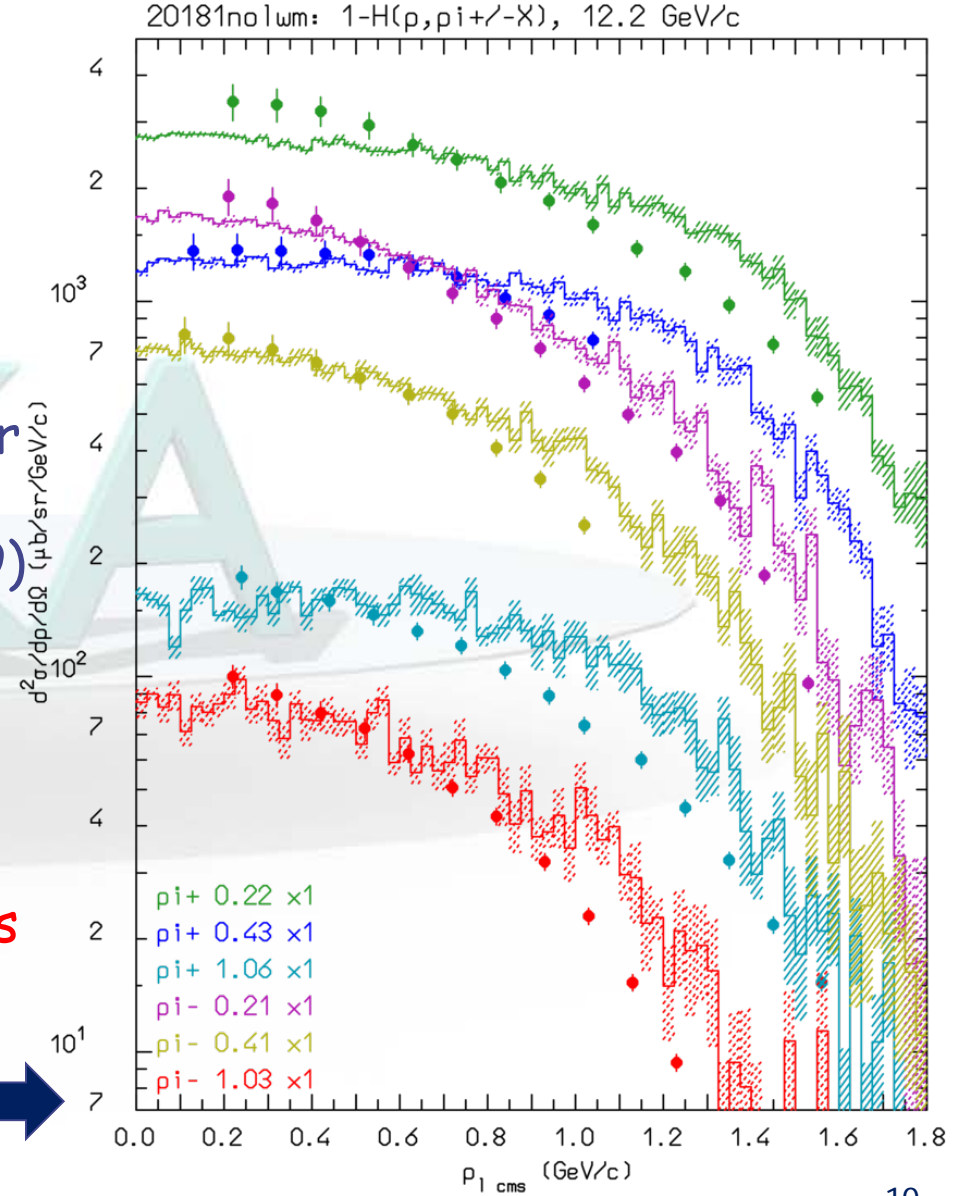
- Chains from ν DIS :
 - One quark-diquark chain if interaction on valence quark
 - One quark-diquark plus one q - q bar chain if int on sea quark

Effect of low \sqrt{s} chain treatment (see later for ν)



Left: with low mass
phase space
hadronization

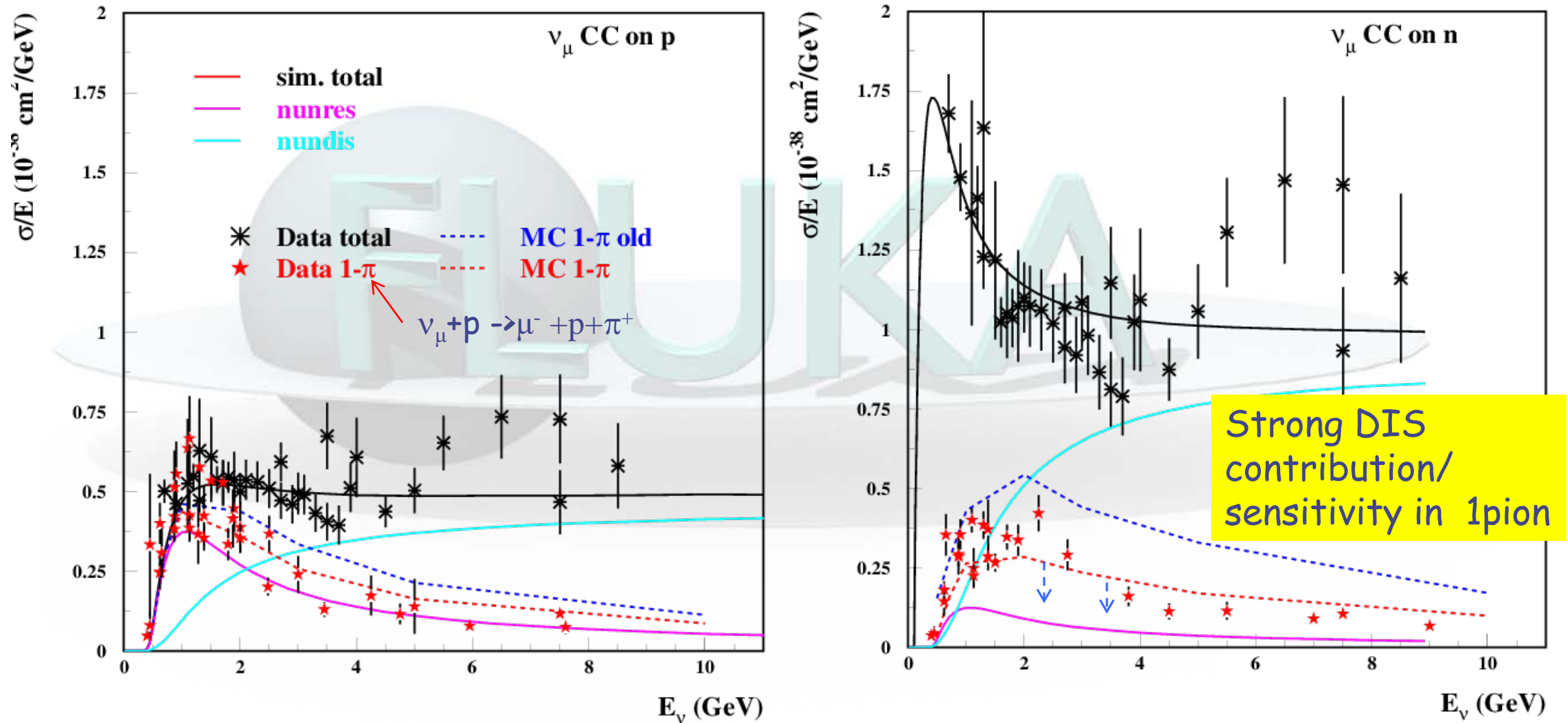
Right: without



Single pion production

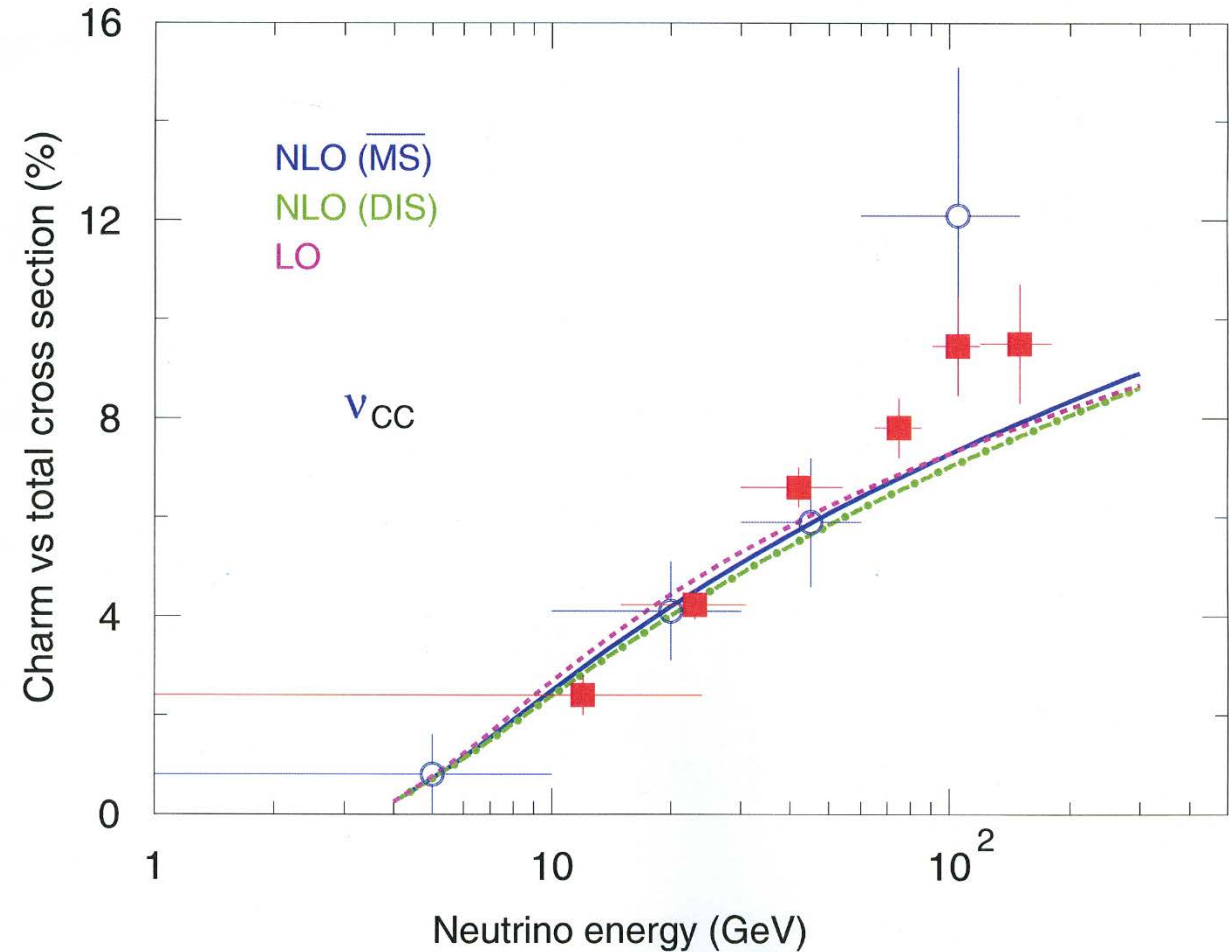
NDS 120, 211 (2014)

New *low-mass chain treatment of fragmentation* → improvements in the **RES-DIS** transition

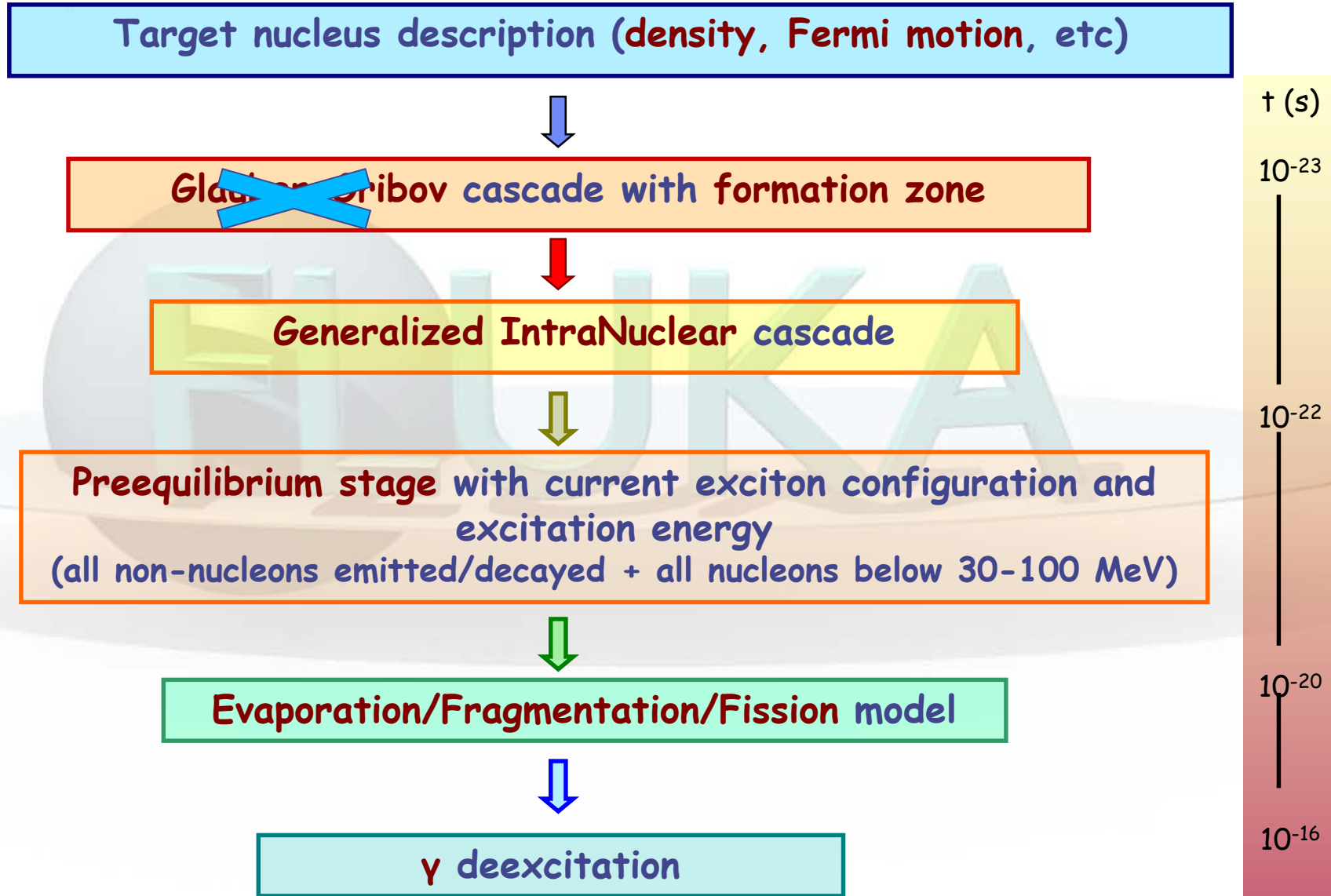


Charm production in neutrino interactions

- Ratio of the charm to total cross sections
- Results of NUNDIS simulation with $M_c = 1.35$ GeV (curves) and experimental data: E531 (open circles) and CHORUS-2011 (filled squares).



Nuclear interactions in FLUKA: the PEANUT model



Nucleon Fermi Motion in FLUKA

- Fermi gas model: Nucleons = Non-interacting Constrained Fermions

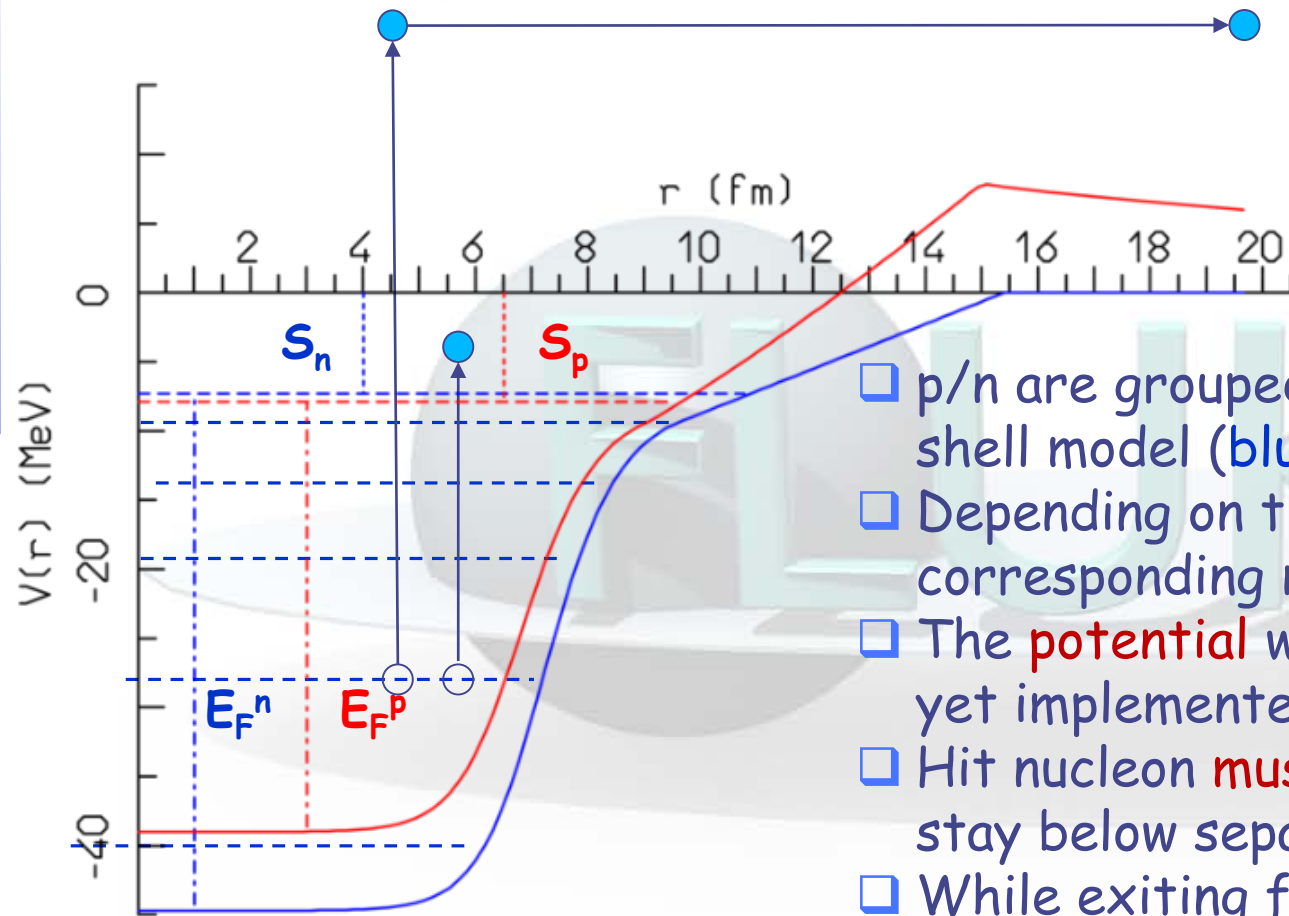
Momentum distribution

$$\propto \frac{dN}{dk} = \frac{|k|^2}{2\pi^2}$$

for k up to a (local) Fermi momentum $k_F(r)$ given by $k_F(r) = [3\pi^2 \rho_N(r)]^{1/3}$

- Momentum smearing according to uncertainty principle assuming a position uncertainty = $\sqrt{2}$ fm
- Nuclear density given by symmetrized Woods-Saxon for $A > 16$ and by a harmonic oscillator shell model for light isotopes
- Proton and neutron densities are different
- Nucleons are bound in the nuclear well

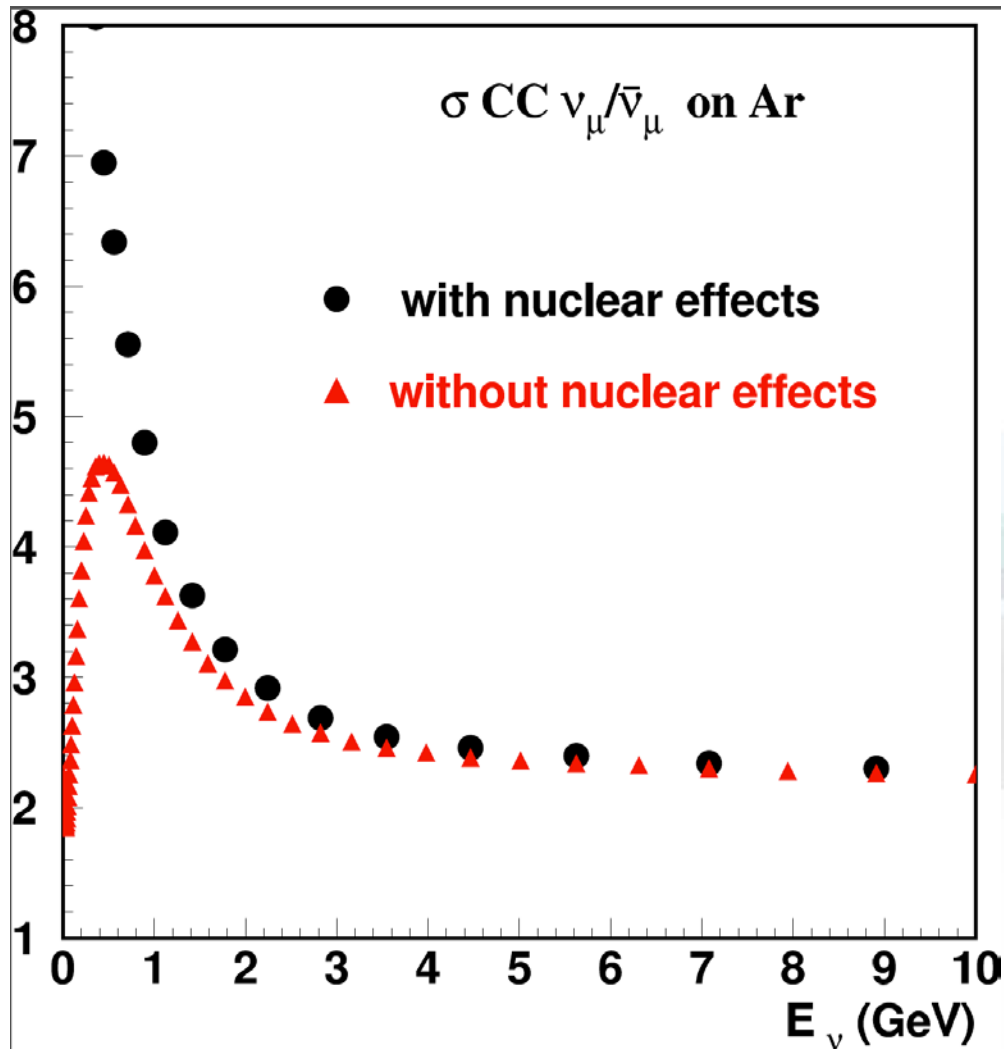
Nucleon levels inside the nuclear potential: schematic drawing



- Blue: neutron
- Red: proton

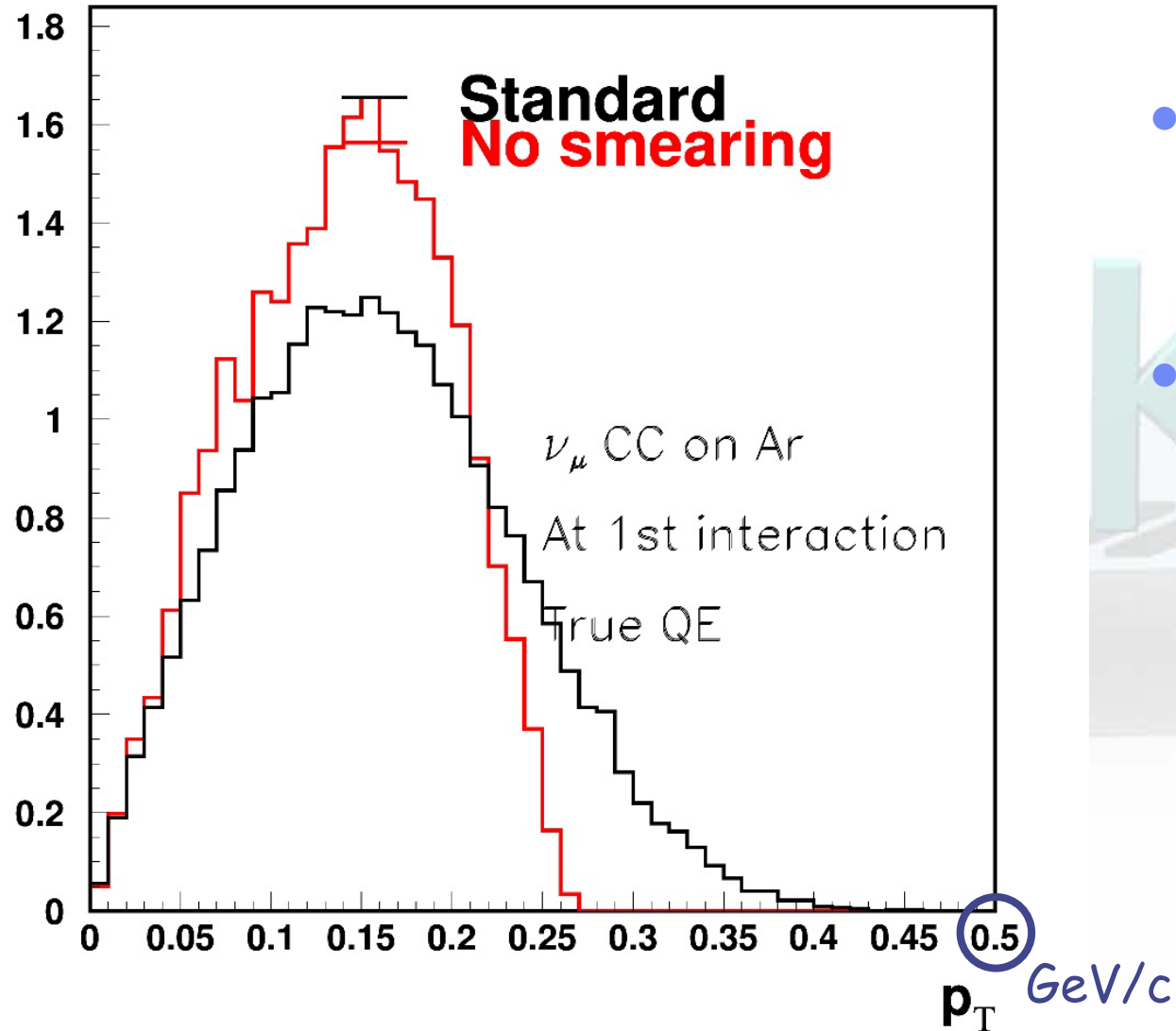
- ❑ p/n are grouped on energy levels spaced according to the shell model (blue lines, shown for neutrons)
- ❑ Depending on the level, the maximum radius for the corresponding nucleon is less or equal to the nuclear radius
- ❑ The **potential** well depth **depends on the nucleon energy** (not yet implemented for neutrino and electron interactions)
- ❑ Hit nucleon **must go above Fermi level** (Pauli blocking), can stay below separation energy.
- ❑ While exiting from the nucleus, the nucleon moves in the nuclear potential, changing kinetic energy and direction
- ❑ The **residual nucleus** is often left in an **excited state** → **particle emission**
- ❑ Changing A or Z → Q value

Pauli + Q value example



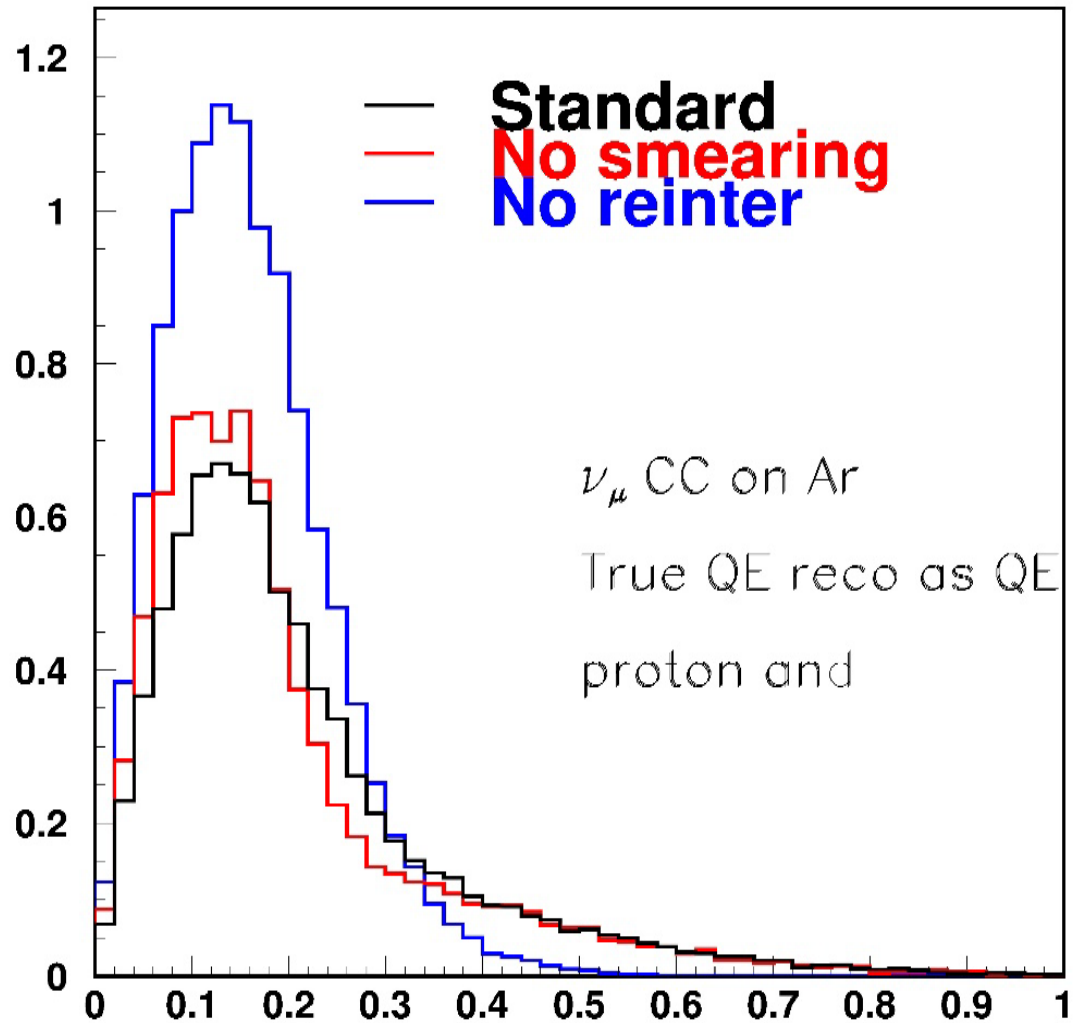
- ν_{μ} CC interactions on Ar : ratio of neutrino/antineutrino cross section vs neutrino energy
- Antineutrino: lower $q^2 \rightarrow$ more sensitivity to Pauli blocking and reaction Q value (few-MeV more unfavorable in case of anti-nu)

Momentum smearing on Fermi: example

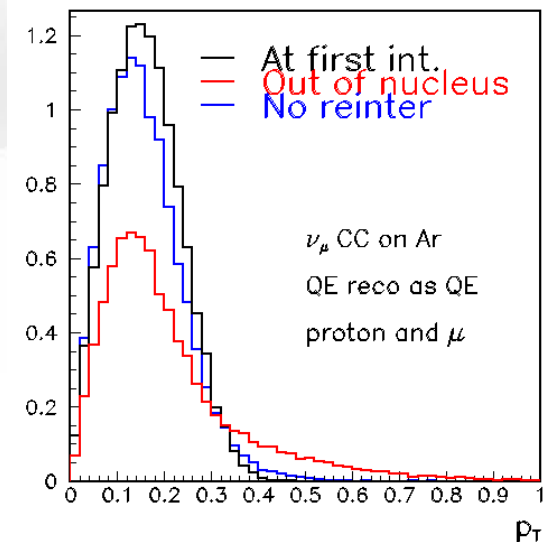


- ν_μ CC interactions on Ar. Neutrino energy spectrum as in DUNE ($\sim 3\text{GeV}$)
- Plot: **total transverse momentum** (proton + muon) from QE interactions **at the primary interaction**, before ANY final state effect.
- With (black) and without fermi momentum smearing

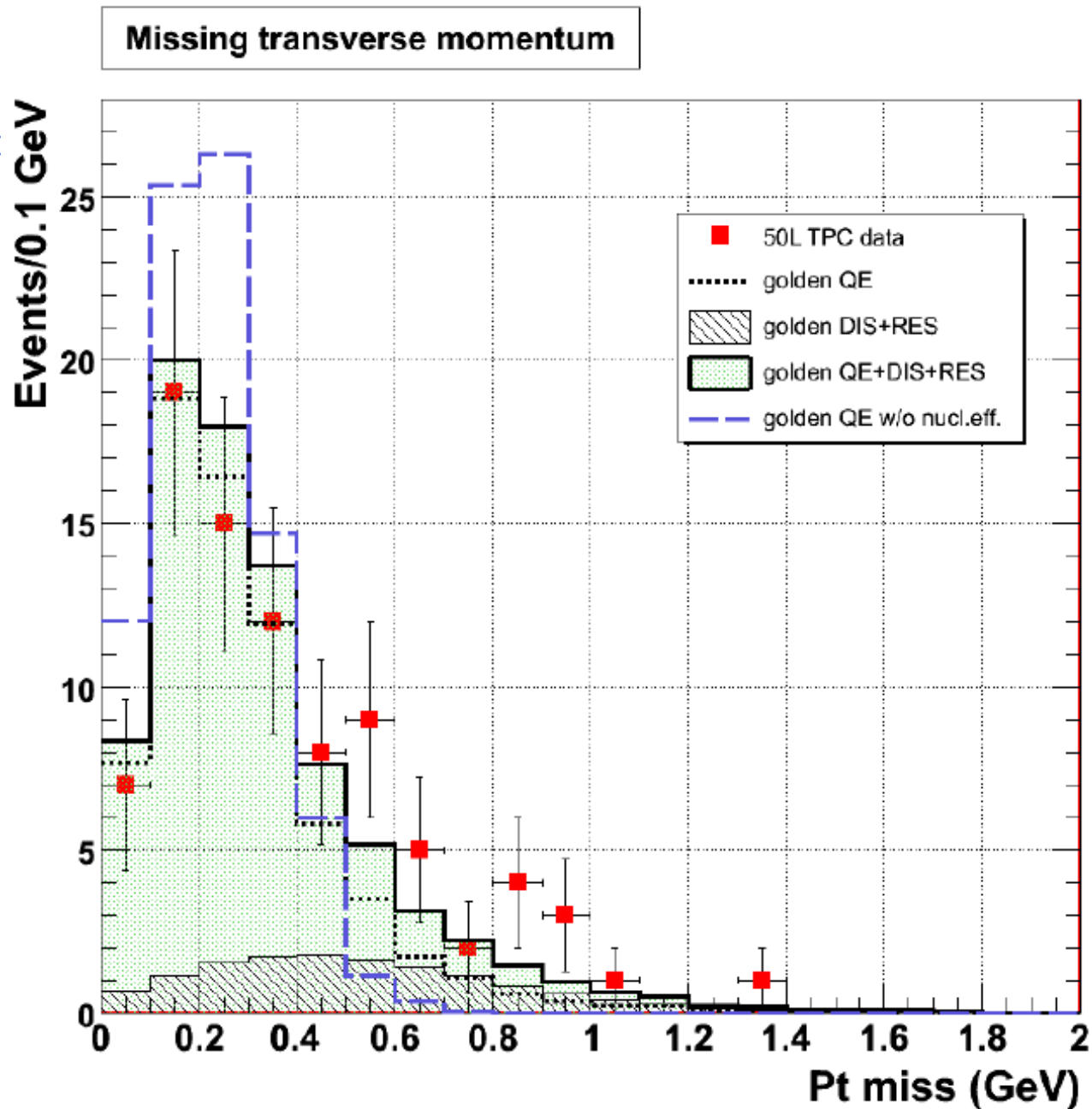
Fermi momentum: smeared by FSI



- ν_μ CC interactions on Ar. Neutrino energy spectrum as in DUNE ($\sim 3\text{GeV}$)
- Plot: total transverse momentum (proton + muon)
- QE interactions reconstructed as QE interactions (1p, 1 μ , no thresholds) outside the nucleus.
- With and without smearing, with and without reinteractions (effects of the nuclear binding/potential are always in)



The 50L LAr TPC in the WANF neutrino beam



- Broad band spectrum, $\langle E \rangle = 24.3 \text{ GeV}$
- from 400 QE - golden fraction 16%
- background - additional 20%

finally expected

$80 \pm 9(\text{stat.}) \pm 13(\text{syst.})$ (syst. \rightarrow mainly QE fraction and beam simul)

to be compared with **86** events observed

Very good consistency with expectations

a special FSI : Formation zone

Naively: "materialization" time (originally proposed by Stodolski).

Qualitative estimate:

In the frame where $p_{\parallel} = 0$

$$\bar{t} = \Delta t \approx \frac{\hbar}{E_T} = \frac{\hbar}{\sqrt{p_T^2 + M^2}}$$

Particle proper time

$$\tau = \frac{M}{E_T} \bar{t} = \frac{\hbar M}{p_T^2 + M^2}$$

Note: in the particle frame, not lab

Going to the nucleus system

$$\Delta x_{for} \equiv \beta c \cdot t_{lab} \approx \frac{p_{lab}}{E_T} \bar{t} \approx \frac{p_{lab}}{M} \tau = k_{for} \frac{\hbar p_{lab}}{p_T^2 + M^2}$$

Condition for possible reinteraction inside a nucleus:

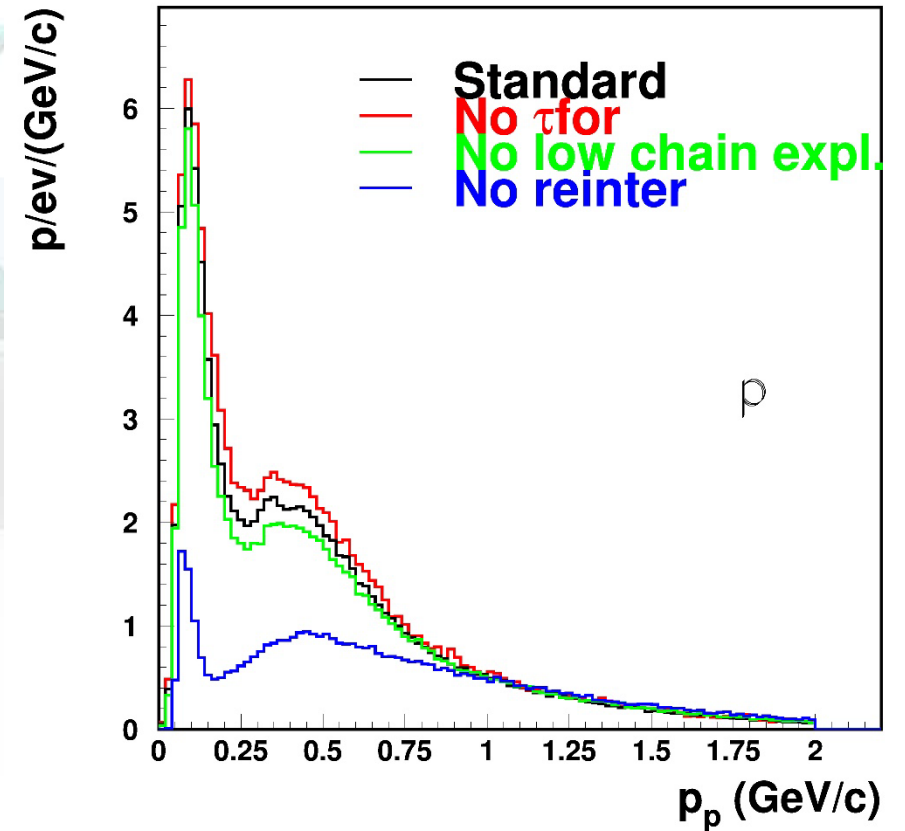
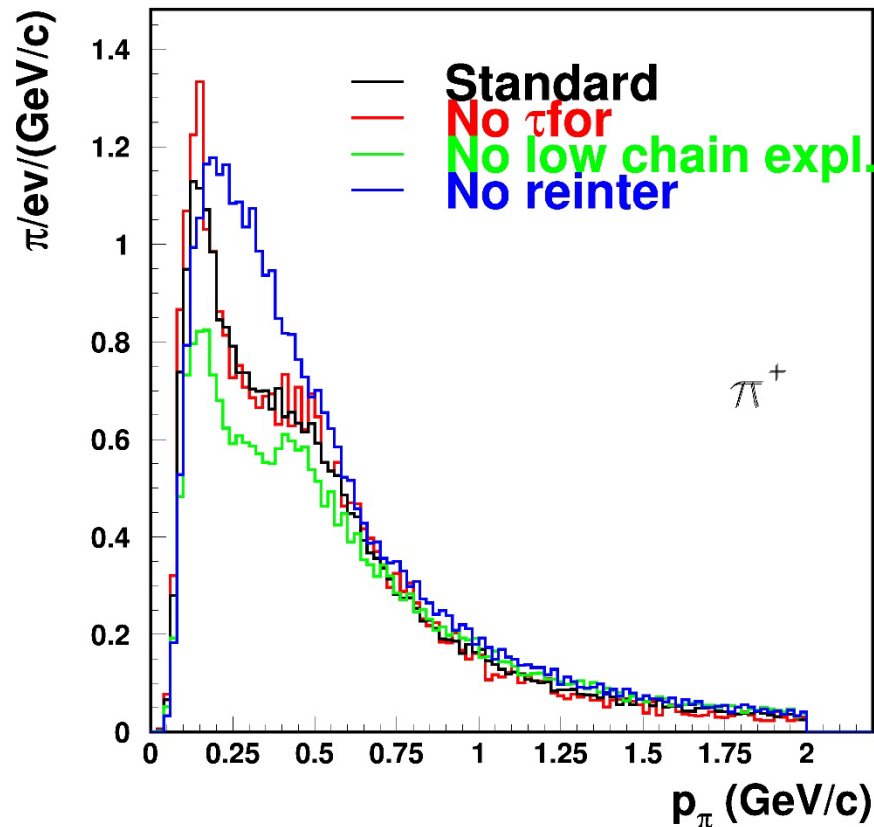
$$\Delta x_{for} \leq R_A \approx r_0 A^{\frac{1}{3}}$$

Decrease of the reinteraction probability, ~proportional to particle momentum

Applied also to DIS neutrino interactions and, in an analogue way, to QE neutrino interactions

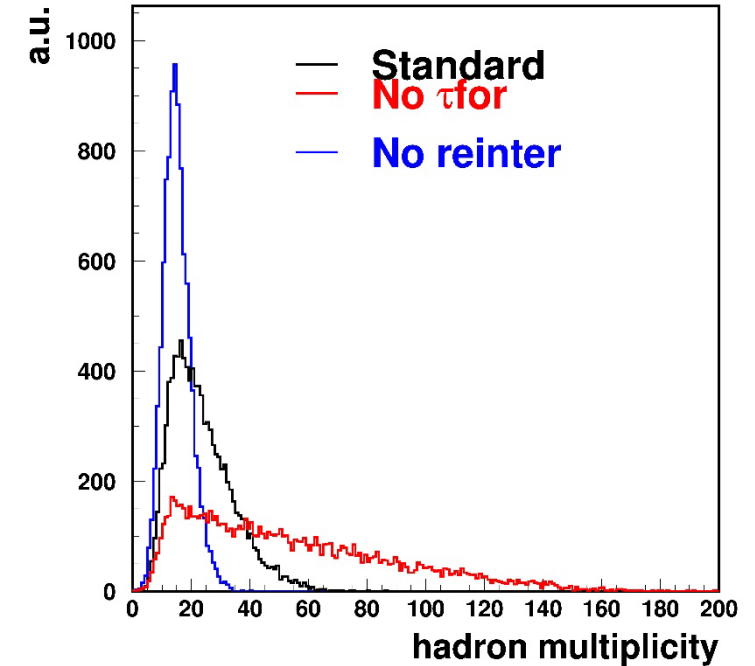
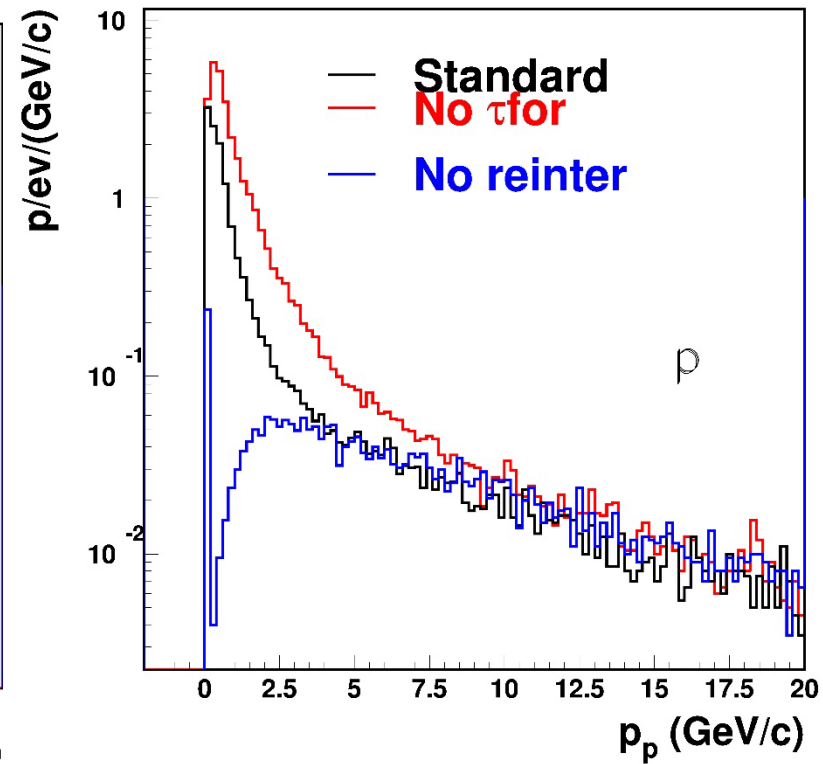
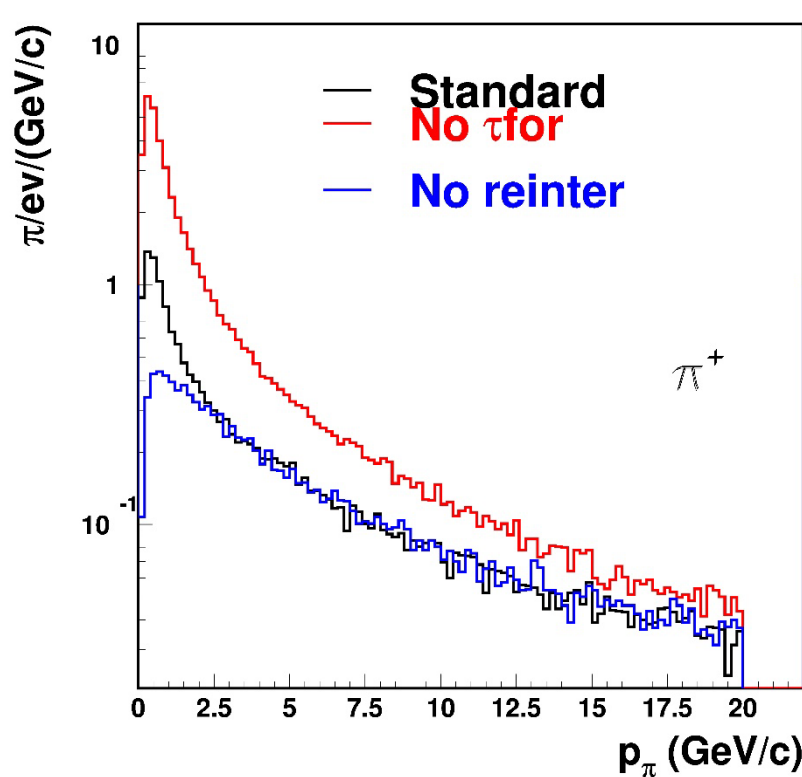
Effect of Formation zone etc.

- DUNE spectrum, numu-CC on Ar. Pion (left) and proton (right) momentum spectra in various conditions, cut at 2 GeV/c.
- Note the effect of DIS treatment on pions, of reinteractions on both..in opposite way
- Formation zone has a small effect at these energies

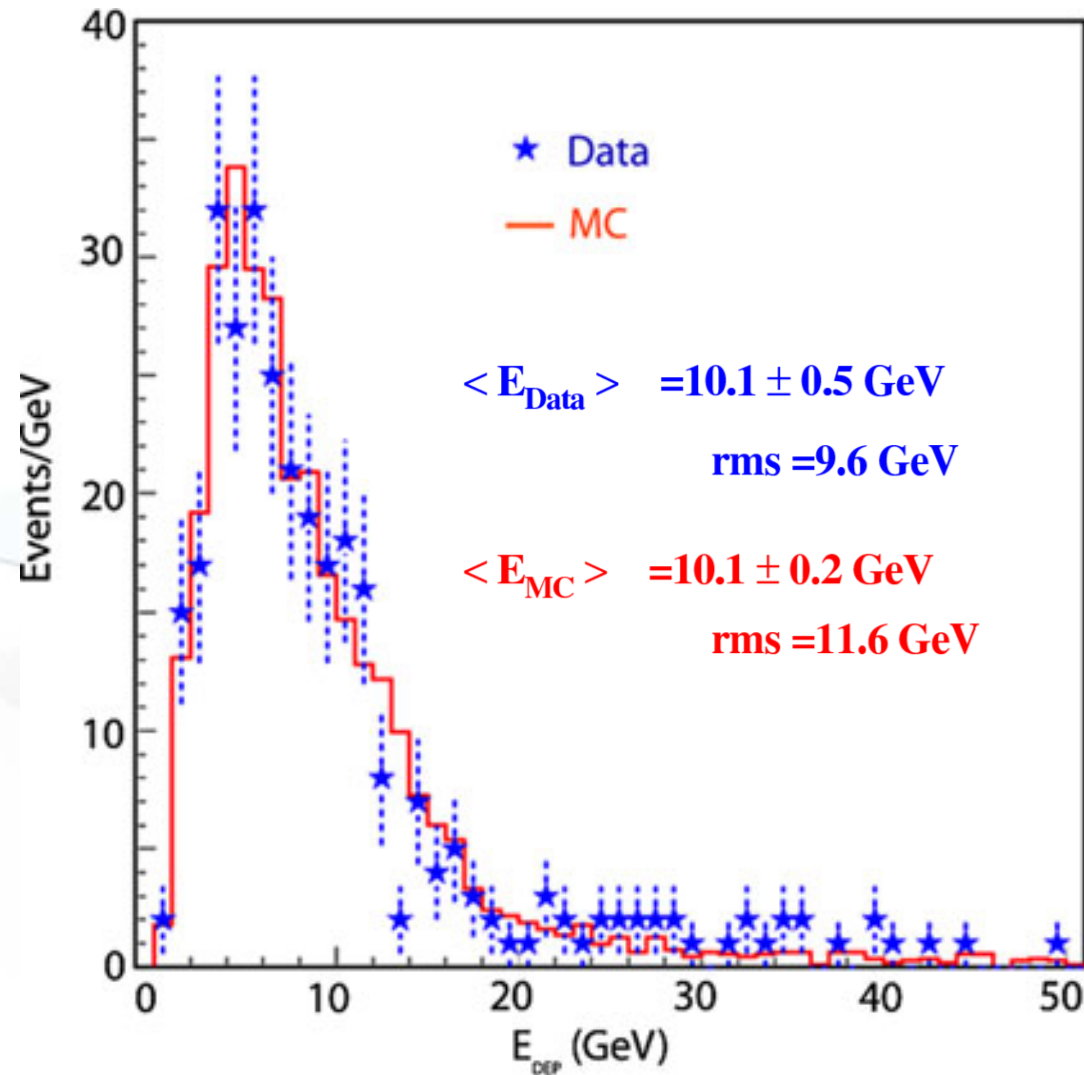


Effect of Formation zone etc., 1TeV

- 1TeV neutrinos, numu-CC on Ar, spectra cut at 20 GeV/c
- Here the formation zone has a huge effect



CNGS data

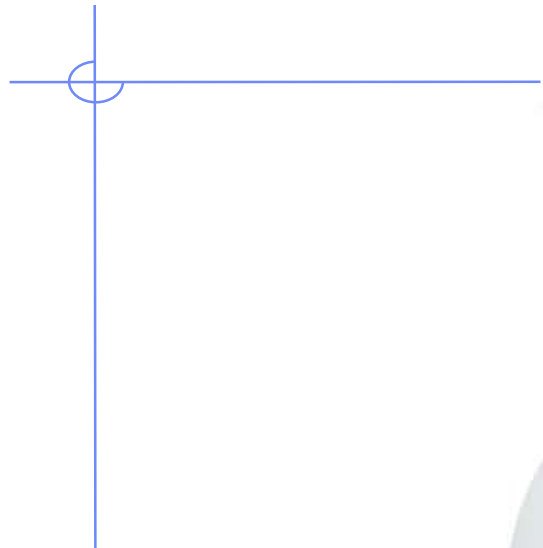


Distribution of total deposited energy in the T600 detector
CNGS numuCC events (~20 GeV E_{ν} peak)

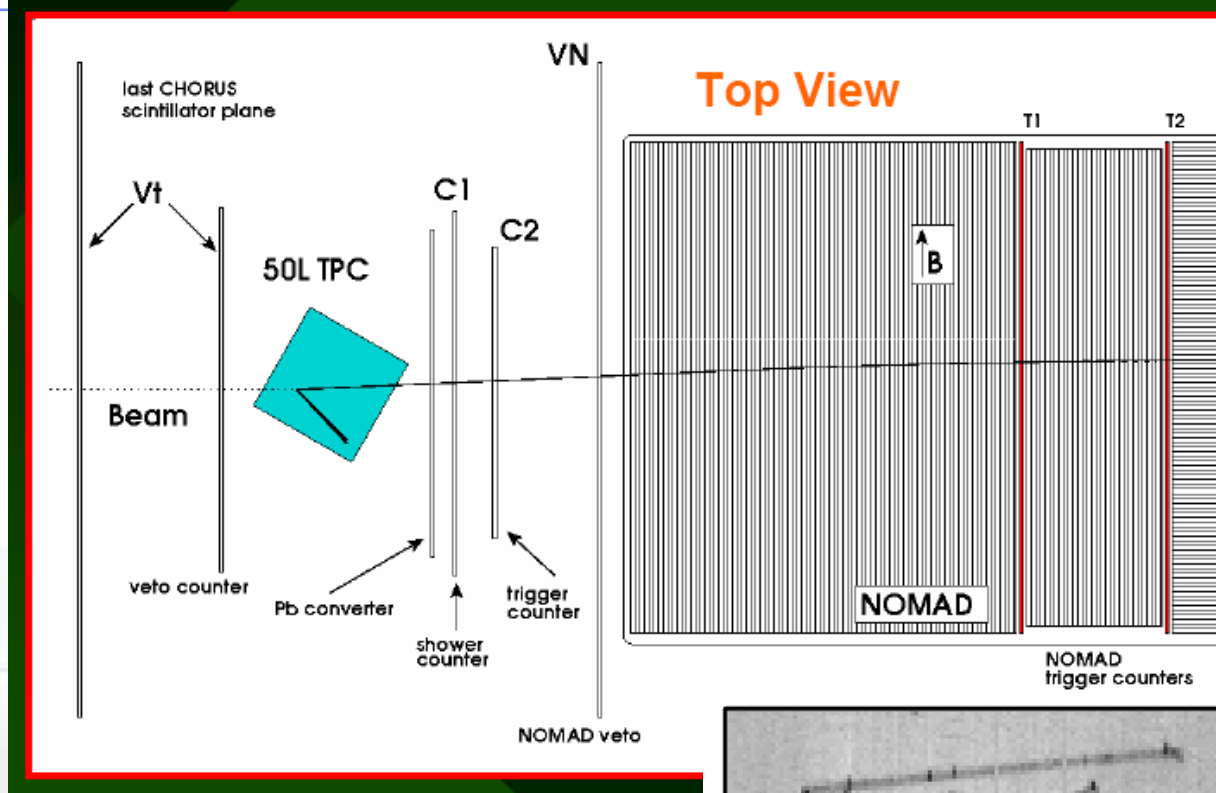
Same reconstruction in MC and Data
Neutrino fluxes from FLUKA cngs simulations

Absolute agreement on neutrino rate within 6%

Eur. Phys. J. C (2013) 73:2345
Phys. Lett. B (2014)



The 50L LAr TPC in the WANF neutrino beam(1997)

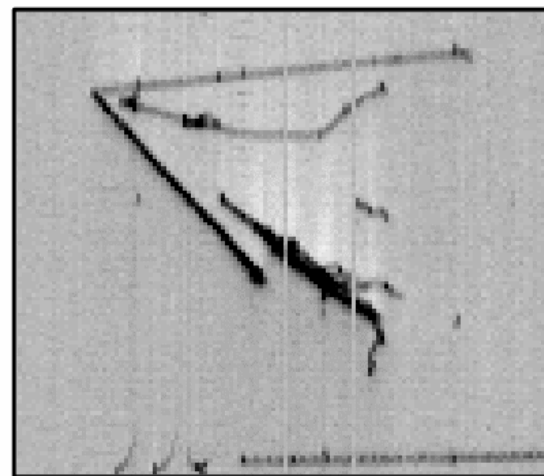


Trigger and μ
reconstruction: NOMAD

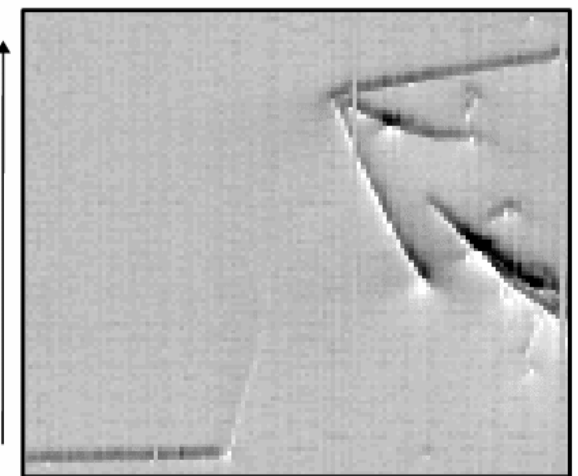
Event selection: "GOLDEN sample"
= 1 μ and 1 proton $>40\text{MeV}$ fully contained

Phys.Rev. D74 (2006) 112001

12/6/2021

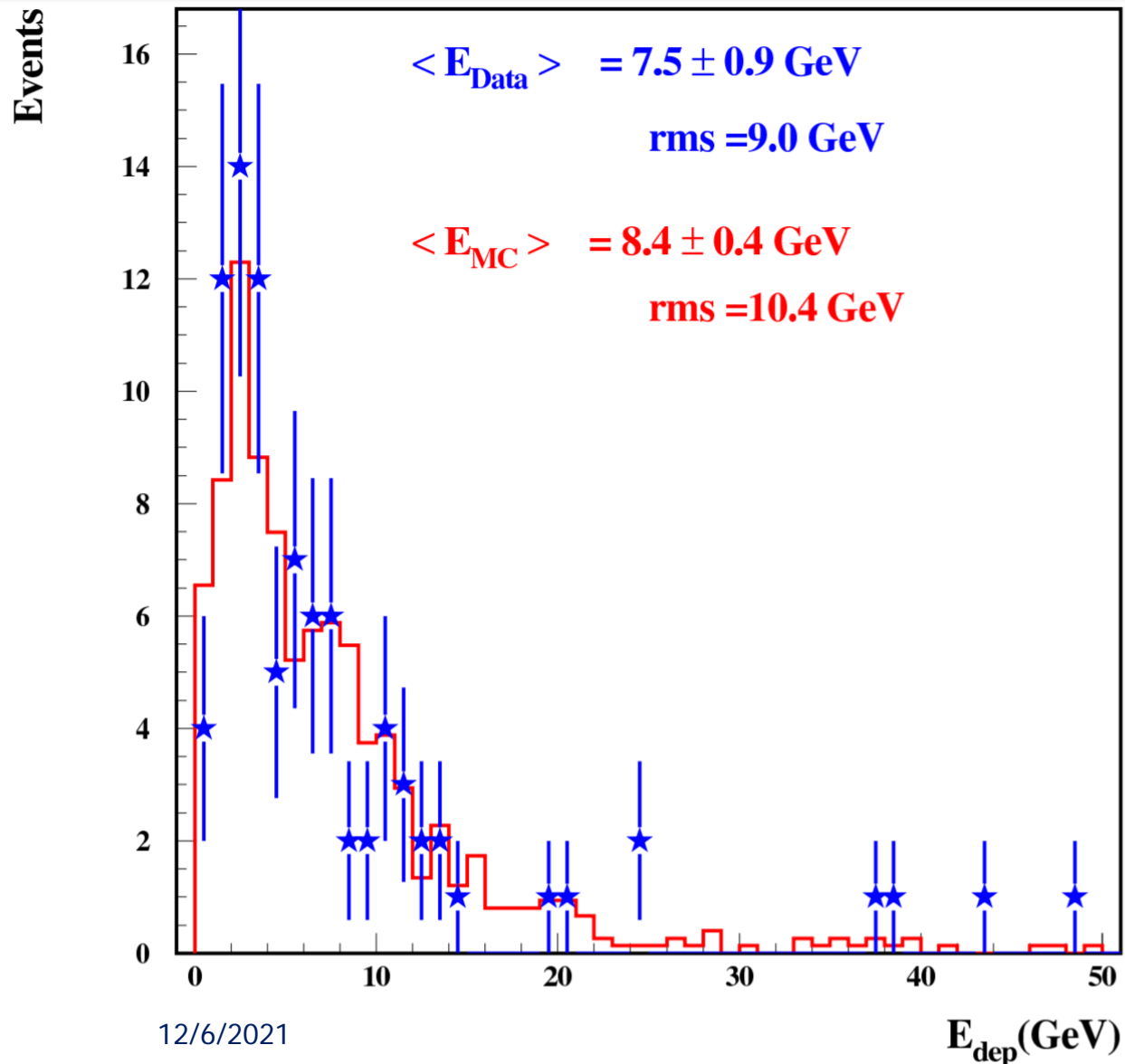


Collection wires. (128 wires: 32 cm.)



Induction wires. (128 wires: 32 cm.)

CNGS data



Distribution of total deposited energy in the T600 detector
CNGS nuNC

Same reconstruction in MC and Data
Neutrino fluxes from FLUKA cngs simulations

Only events with $E_{\text{dep}} > 500$ MeV

Nuclear cascade in lowenergy nuclear breakup

Alexei Larionov

Institut für Theoretische Physik, Universität Gießen, D-35392 Gießen, Germany

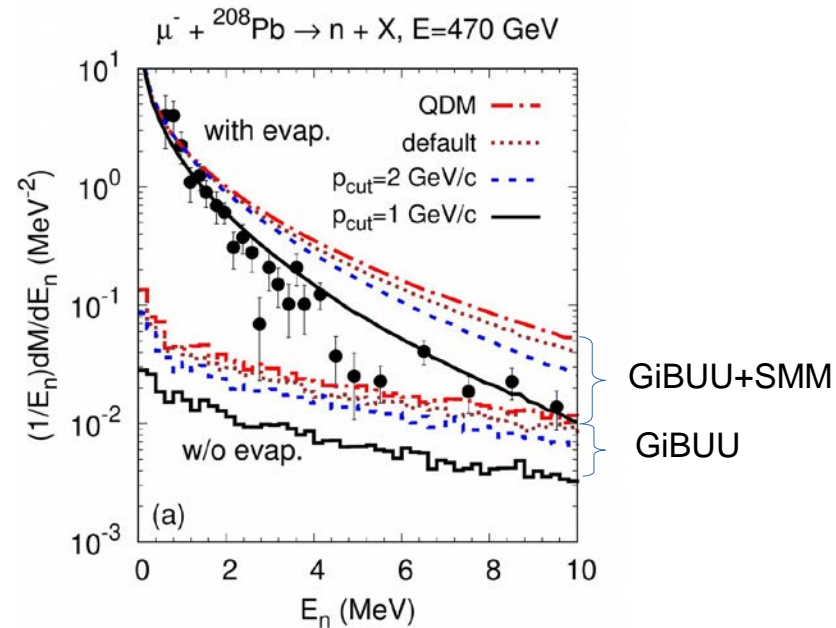
In collaboration with

Mark Strikman

Pennsylvania State University, University Park, PA 16802, USA

CFNS Adhoc Workshop: Target Fragmentation Physics with EIC, 28-30.09.2020

The neutron spectrum contains both the preequilibrium part (cascade particles) and the equilibrium part from the decay of the excited residual nucleus.



E665 data from
M.R. Adams et al.,
PRL 74, 5198 (1995)

Cuts:
 $\nu > 20$ GeV,
 $Q^2 > 0.8$ GeV².

- almost all neutrons below 1 MeV are statistically evaporated;
- sensitivity to the model of hadron formation for $E_n > 5$ MeV;
- E665 data for lead target can be only described with very strong restriction on the FSI of hadrons ($p_{cut} = 1$ GeV/c) in agreement with earlier calculations
M. Strikman, M.G. Tverskoy, M.B. Zhalov, PLB 459, 37 (1999)

NUNDIS 2015: kinematics

- Considered kinematical limits for the *PDF* available from GRV94, GRV98, and BBS analyses.

Variable	Required	GRV94		GRV98		BBS	
		Default	Tested	Default	Tested	Default	Tested
E_{min} (GeV)	—	0.050					
E_{max} (GeV)	$\geq 10^4$	$70 \cdot 10^3$			10^5		
Q_{min}^2 (GeV ²)	$\leq 5.5 \cdot 10^{-12}$	0.4	0.4	0.8	0.8	2	0.8
Q_{max}^2 (GeV ²)	$\geq 1.9 \cdot 10^4$	10^6	10^9	10^6	10^9	10^4	$2 \cdot 10^4$
x_{min}	$\leq 1.4 \cdot 10^{-11}$	10^{-5}	10^{-30}	10^{-9}	10^{-30}	10^{-4}	10^{-30}
x_{max}	1	0.99999	0.99999	1	1	1	1

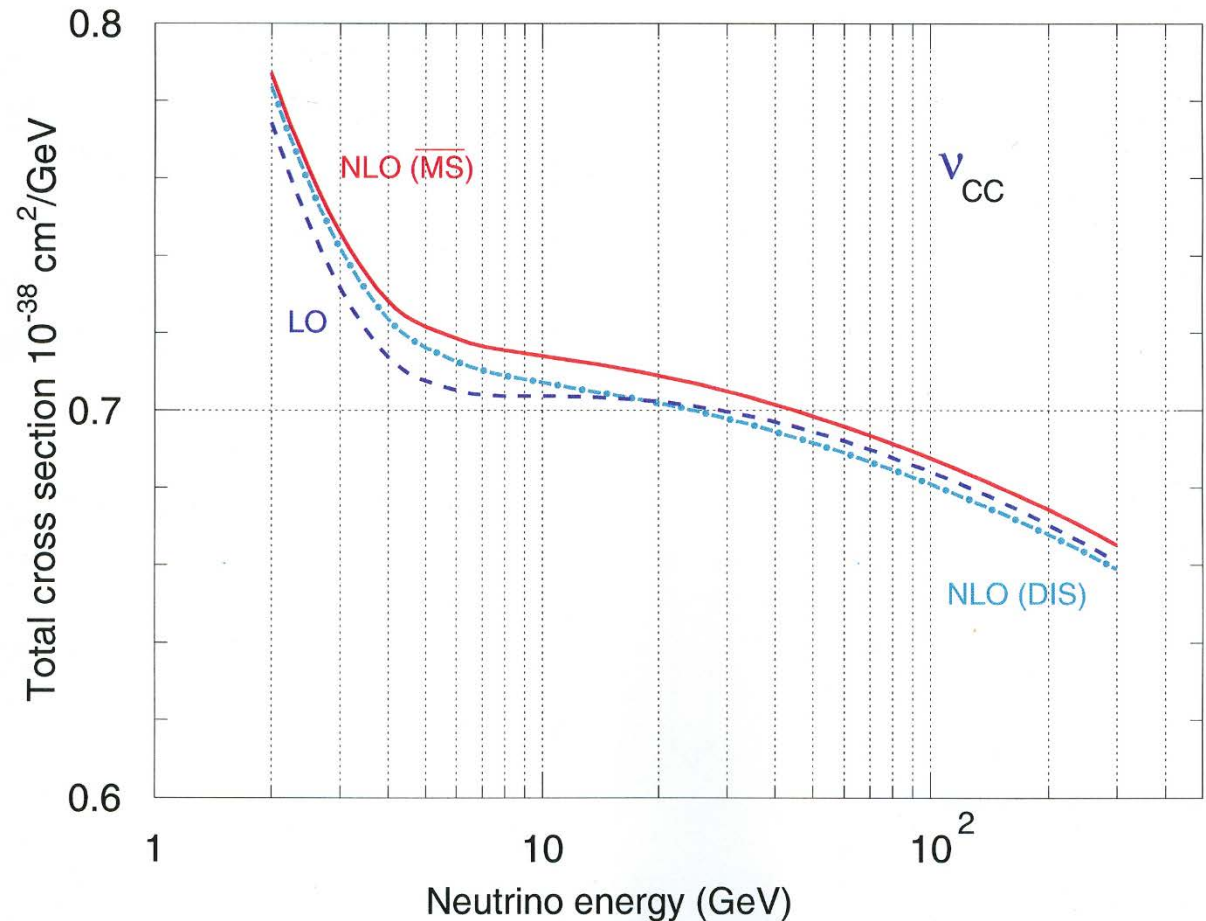
More on pdfs

Three versions of pdf from the GRV98 analysis are included as options for evaluating nucleon structure functions

1. Leading order analyses (LO)
2. Next to leading order analyses (NLO $\overline{\text{MS}}$)
3. Next to leading order analyses (NLO DIS)

An interesting feature of the GRV98 analysis is a low threshold for the transferred, 4-momentum, $Q^2 = 0.8 \text{ GeV}^2$

NLO (DIS) is chosen as a default option



Nucleon correlation function:

Correlation function: it can be computed within the Fermi-gas model

Due to the anti-symmetrization of the fermion's wave function, given a nucleon in a position \vec{r} in a nucleus with density ρ_0 , the probability of finding another like nucleon in a position \vec{r}' is decreased for small values of the distance $d = |\vec{r} - \vec{r}'|$ by a factor


$$g(x) = 1 - \frac{1}{2} \left[\frac{3}{x^2} \left(\frac{\sin x}{x} - \cos x \right) \right]^2$$

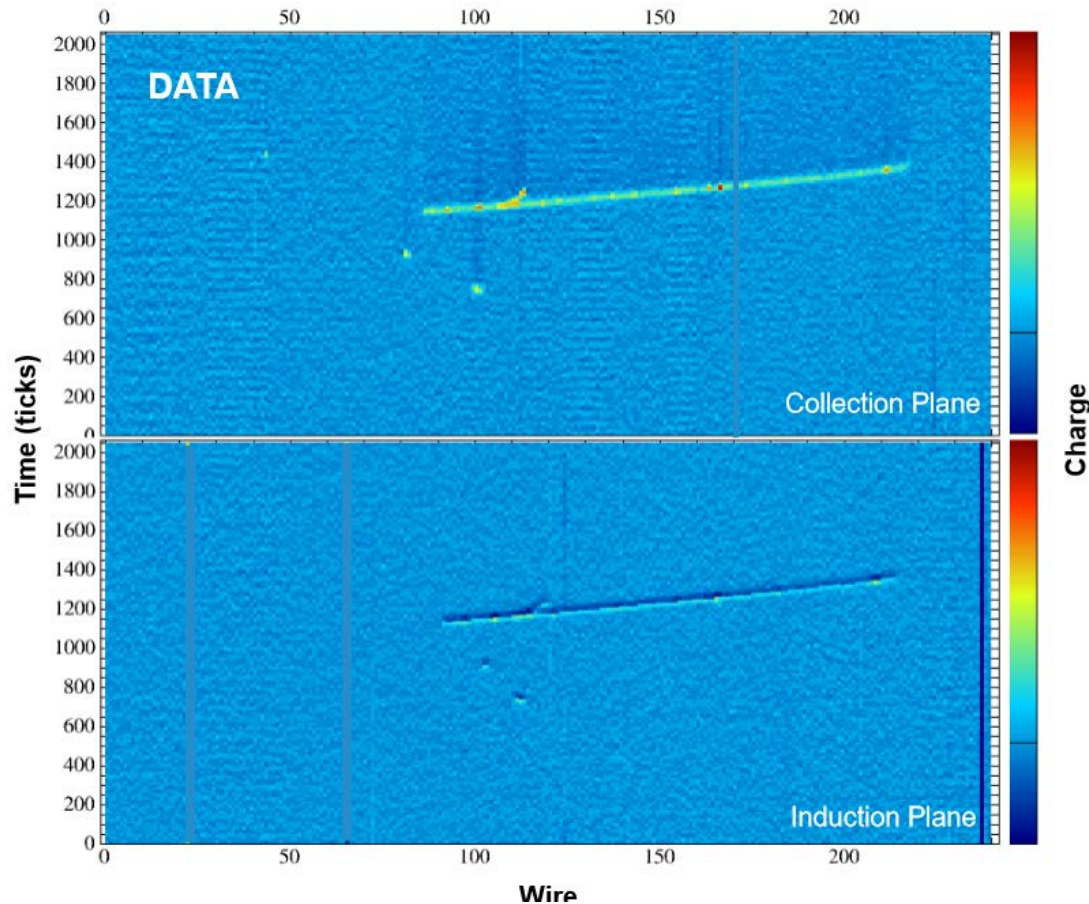
where $x = K_F \cdot d$, and the factor 1/2 in front of the parenthesis accounts for the two possible spin orientations.

Nucleon hard core effects are also taken into account, forbidding to "find" a nucleon of the same or different type at less than 1-1.5 fm distance. This check is applied at every possible re-interaction, checking against all nucleons already involved in previous interactions

First Demonstration of LArTPC MeV-Scale Physics in ArgoNeuT

Ivan Lepetic *APS_April2018*

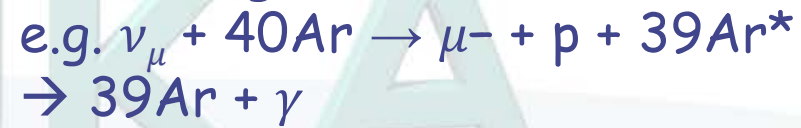
 ILLINOIS INSTITUTE OF TECHNOLOGY
For the ArgoNeuT Collaboration



12/6/2021

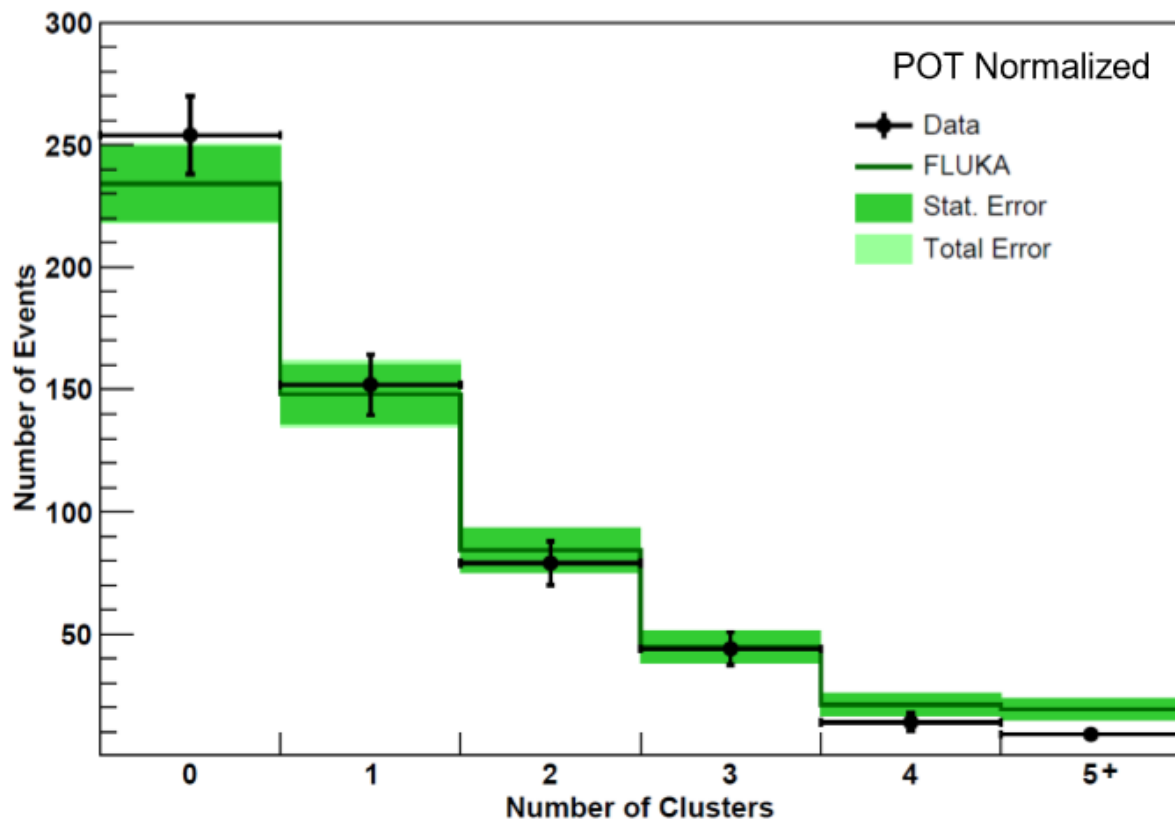
Low-energy gammas produced by neutrino-nucleus interactions in ArgoNeuT

Photons from **neutrino-produced nuclear de-excitation** and inelastic neutron scattering -



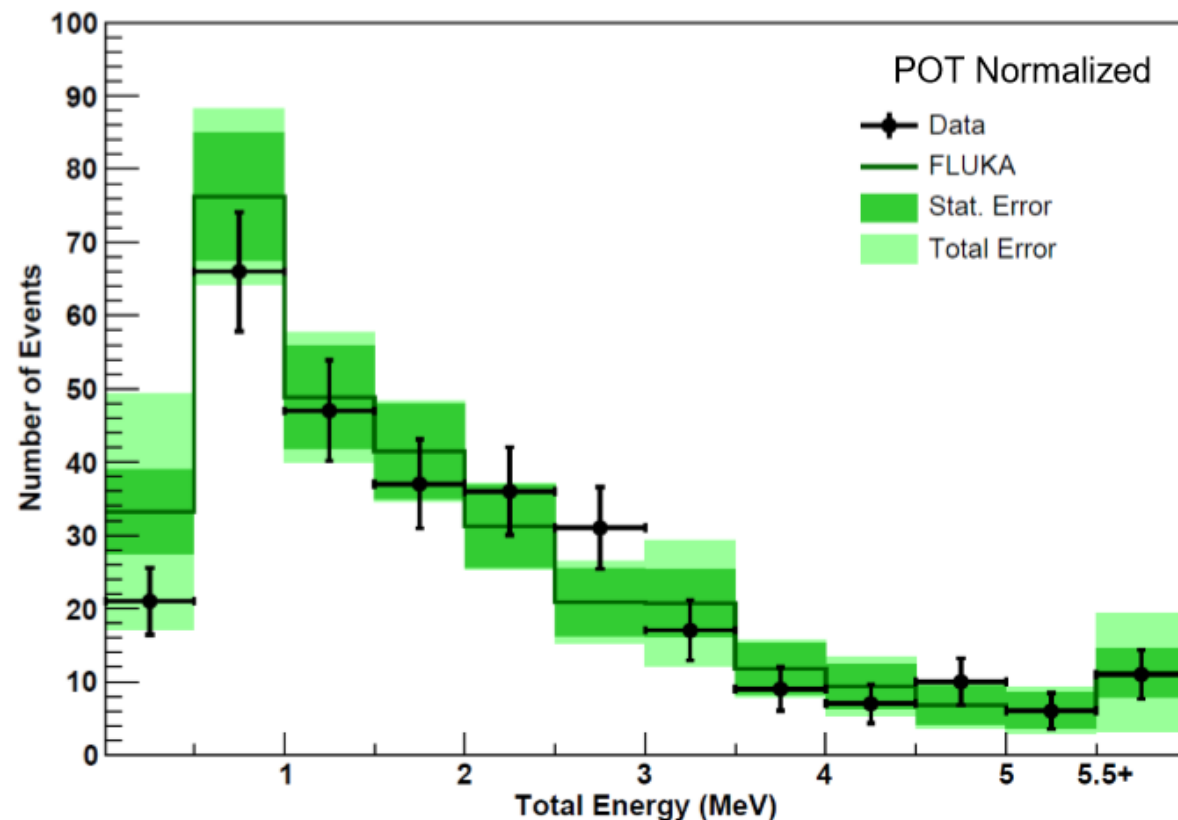
Data and FLUKA

Number of Clusters in an Event



$\chi^2/\text{ndf} = 9.62/6$. p-value = 0.14

Total Reconstructed Energy in an Event



$\chi^2/\text{ndf} = 7.74/12$. p-value = 0.81

Agreement is far worse if either de-excitation or neutron produced gammas are removed.

Effect of formation zone on residuals

Experimental and computed residual nuclei mass distribution

Ag(p,x)X at 300 GeV (top)

Au(p,x)X at 800 GeV (bottom)

Data from:

Phys. Rev. C19 2388 (1979) and

Nucl. Phys. A543, 703 (1992)

(The heavy fragment evaporation model is key for FLUKA predictions for $A < 30$)

Ag **with** and **without** form.zone:

$\langle \pi \rangle = 21.1$, $\langle E_\pi \rangle = 7.3$ GeV

$\langle \pi \rangle = 49.7$, $\langle E_\pi \rangle = 3.4$ GeV

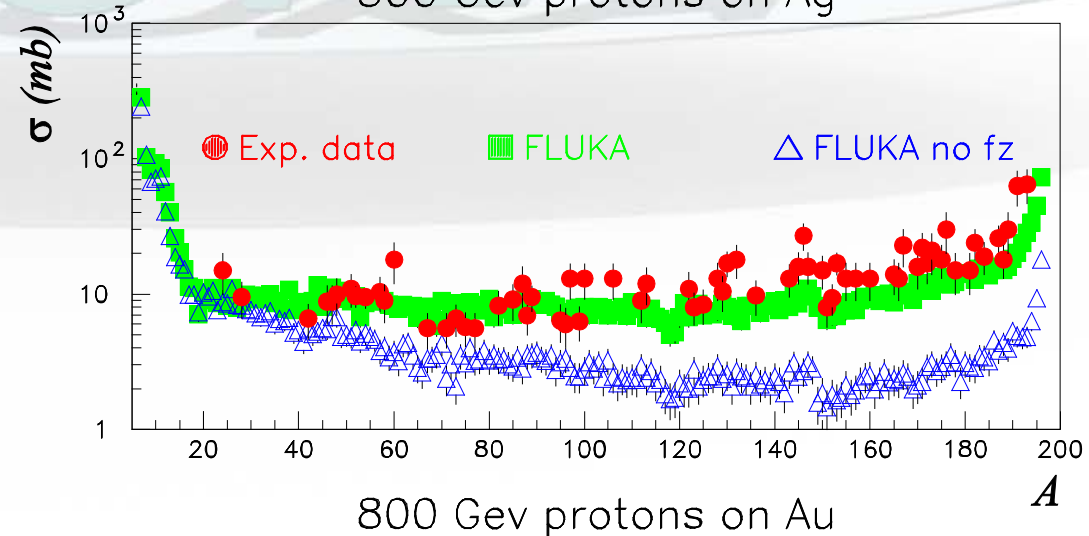
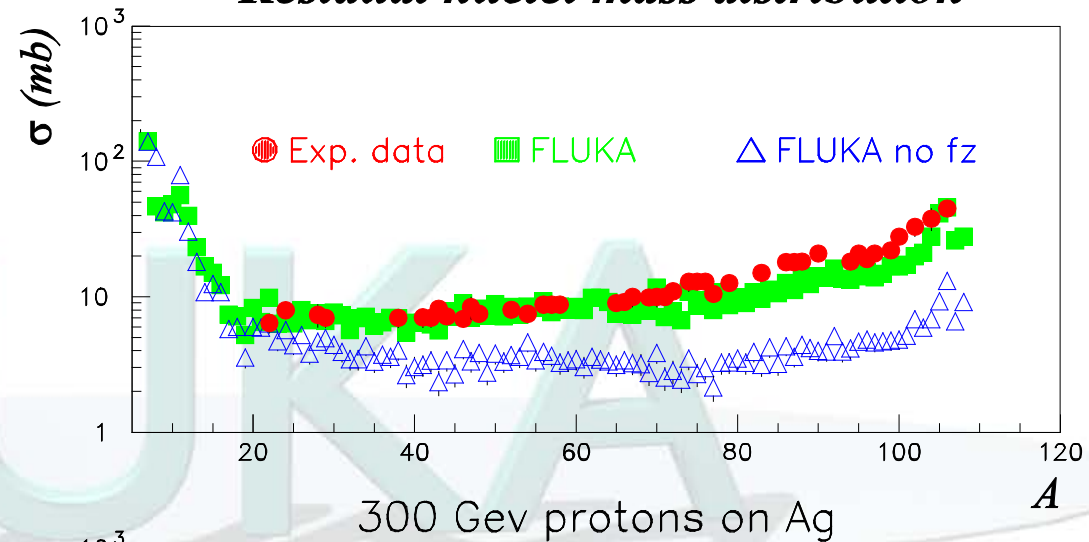
Au **with** and **without** form.zone:

$\langle \pi \rangle = 30.1$, $\langle E_\pi \rangle = 12.5$ GeV

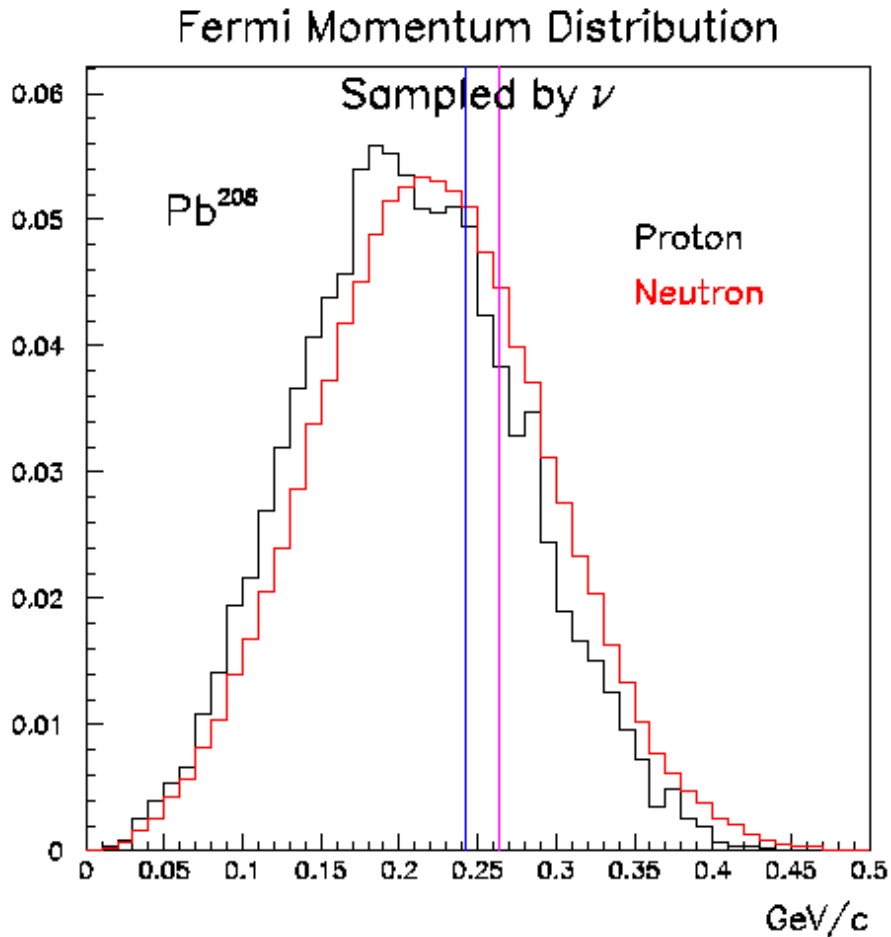
$\langle \pi \rangle = 96.0$, $\langle E_\pi \rangle = 4.6$ GeV

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Residual nuclei mass distribution



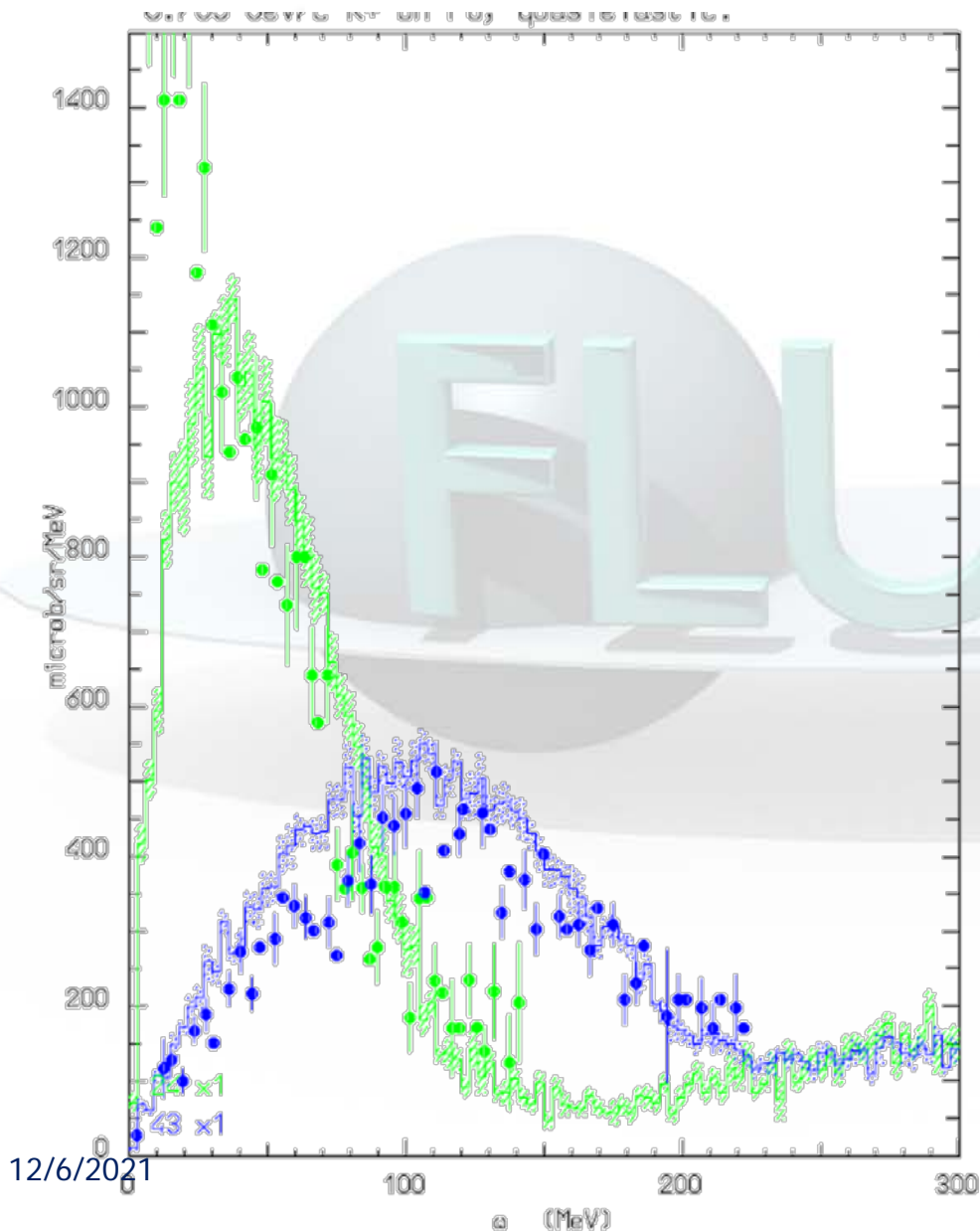
Example of Fermi distribution



Fermi momentum distribution as "seen" by interacting neutrinos on lead.

Vertical lines: maximum Fermi momentum according to un-smearred distribution

Positive kaons as a probe of Fermi motion



K^+ and K^0

- No low mass $S=1$ baryons
 - weak K^+N interaction
 - Only elastic and charge exchange up to ≈ 800 MeV/c

$K^+ Pb \rightarrow K^+ Pb$ 705 MeV/c

Residual excitation spectrum

With K^+ at 24° (green)

at 43° (blue)

Histogram : FLUKA

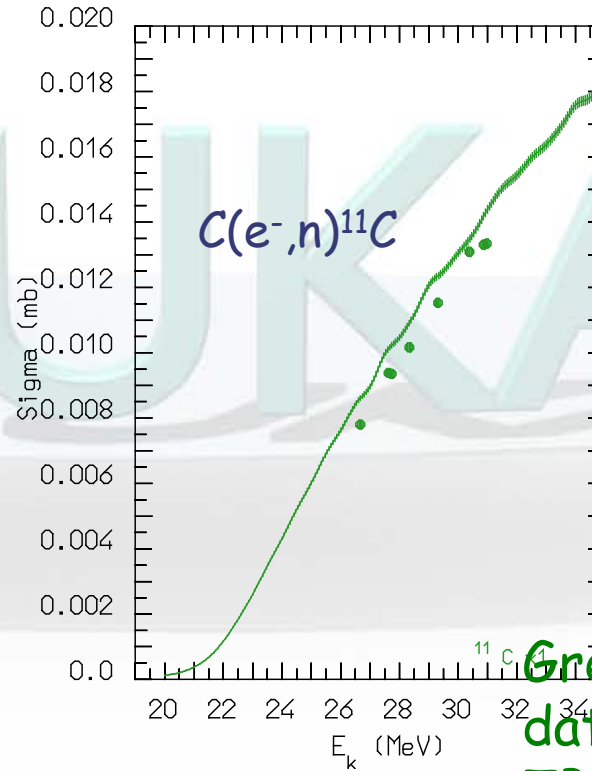
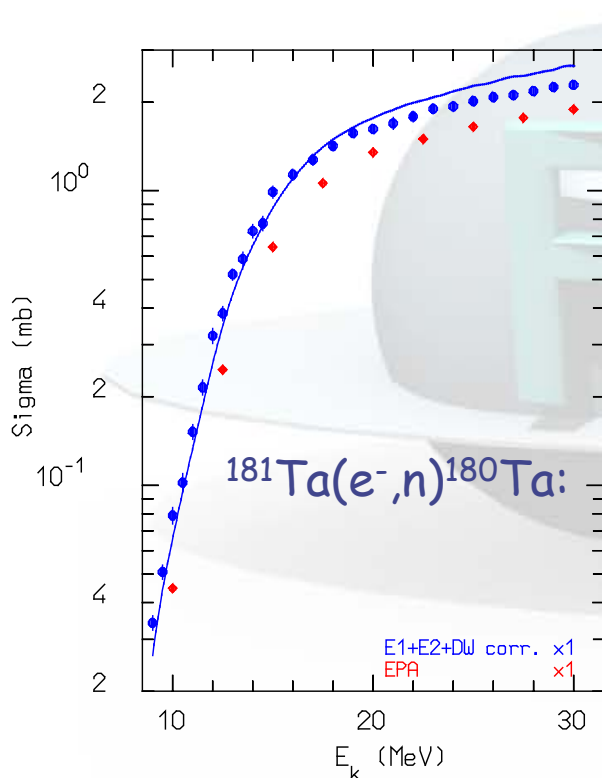
Dots : data (Phys. Rev. C51,669 (1995))

On free nucleon: recoil at 43 MeV or 117 MeV

0-deg tail is elastic on nucleus, not included in sim

Electron scattering

- Quasi-Elastic on nucleon (+ all nuclear)
- Inelastic via virtual photon exchange, recently improved (E1+E2)

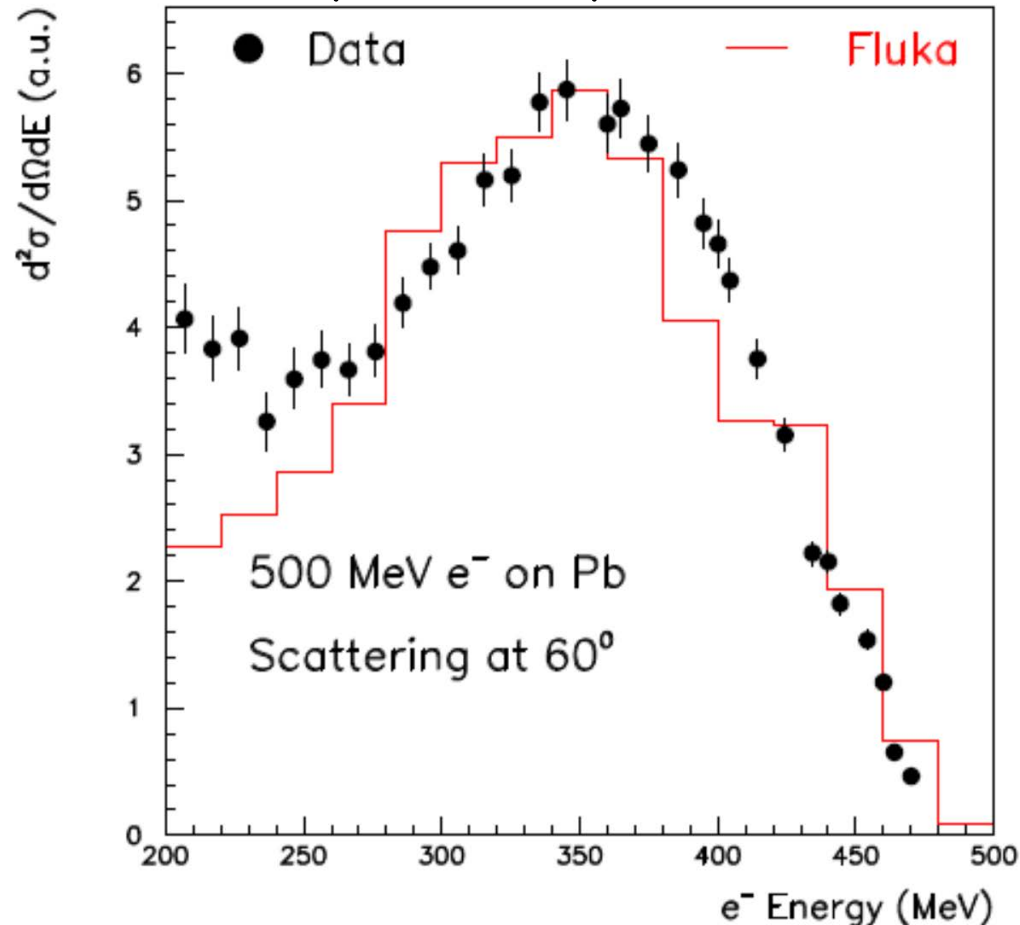


First checks with electrons

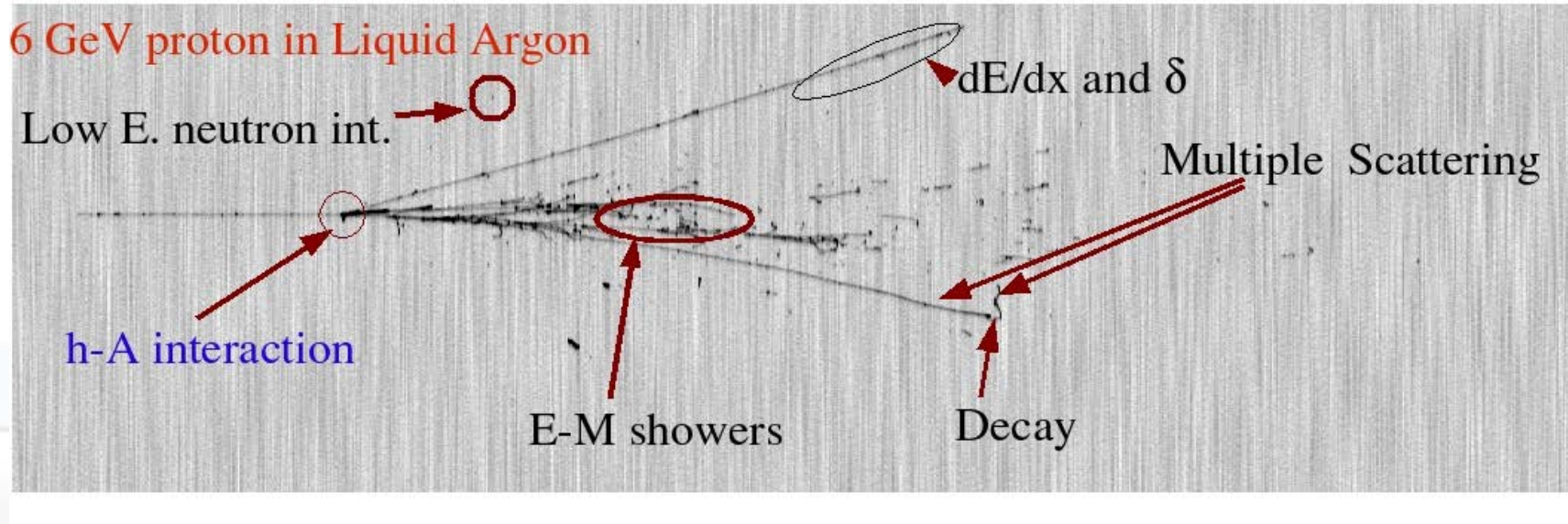
- **Quasi-Elastic scattering** of electrons on Lead, outgoing electron spectrum at 60°
- Inelastic tail not included in simulation
- To be improved with the inclusion of **energy-dependent nuclear well**, as already there for nucleon-induced reactions
- **Much more tests needed**

Data:

R.R. Whitney et al., Phys Rev C9,2230 (1974)



FLUKA : a multi-purpose Monte Carlo code



Web Site: <http://www.fluka.org>

Extrapolation from $Q^2 = 1.0 \text{ GeV}^2$ to $Q^2 = 0$

Solid lines: M. Bertini et al. 1996 (Default in NUNDIS)

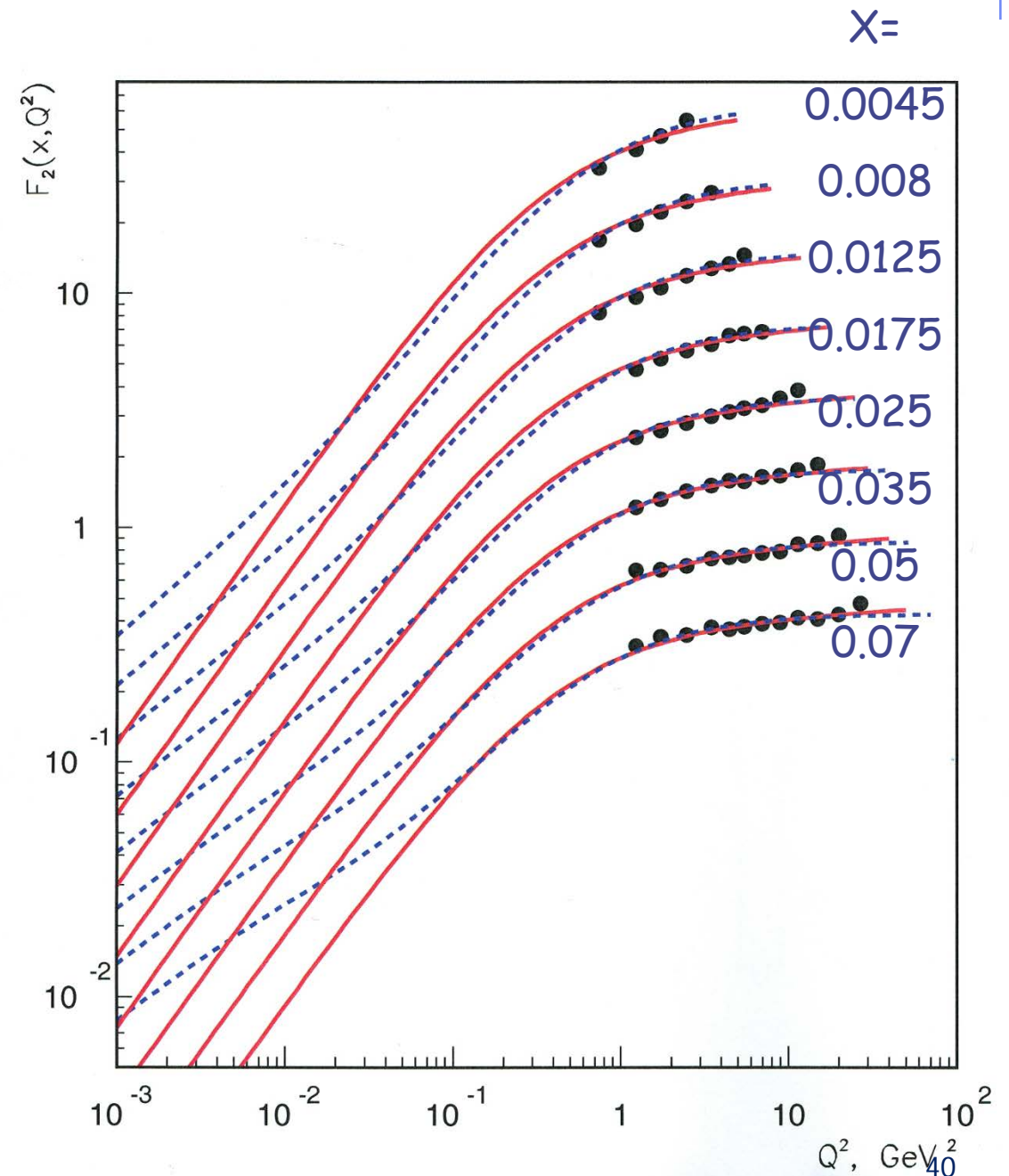
$$F_2(x, Q^2) = A \left[1 + \epsilon \ln(Q^2(1/x - 1) + M^2) \right] \ln(1 + Q^2/(Q^2 + a^2)) .$$

Dashed lines: Donnachie-Landshoff 1994

$$F_2(x, Q^2) \sim Ax^{-0.0808} \left(\frac{Q^2}{Q^2 + a} \right)^{1.0808} + Bx^{0.4525} \left(\frac{Q^2}{Q^2 + b} \right)^{0.5475}$$

data points from NMC Collab., M. Arneodo et al., Nucl. Phys. B 483 (1997) 3-43
Data/cuves scaled for clarity, factors from 1 to 128

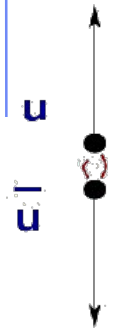
12/6/2021



The "hadronization" of chains

An example:

Low mass chain: just 2-3 meson/(anti)baryon resonances

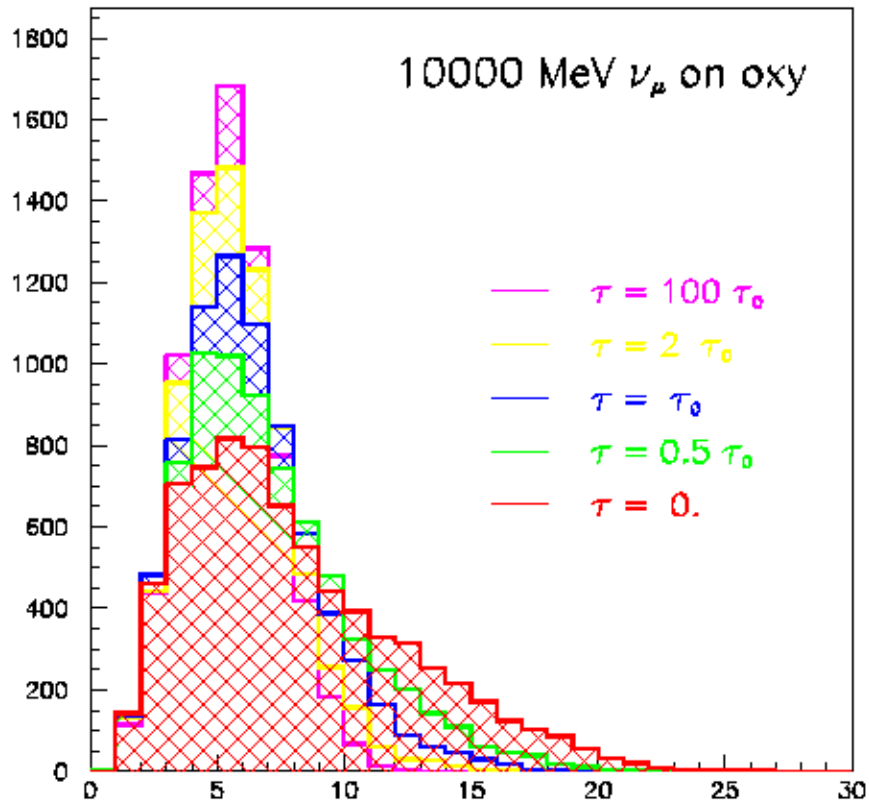


- $u\bar{d}$
- $d\bar{u}$
- $\bar{u}u\bar{d}$
- udd
- $u\bar{s}$
- $s\bar{d}$
- $u\bar{d}$
- $q\bar{q}$
- $q\bar{q}$
- $-$
- \dots
- $d\bar{u}$

Implementation FLUKA-native (evolution of old BAMJET)

Effect of formation zone, neutrino int.

Total hadron multiplicity



Charged hadron spectra

