

# HL-LHC and $e^+e^-$ inputs to global fits

EF03 Heavy flavor and top

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Based on [arXiv:1907.10619](https://arxiv.org/abs/1907.10619), [arXiv:2006.14631](https://arxiv.org/abs/2006.14631) and [arXiv:2107.13917](https://arxiv.org/abs/2107.13917)

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# Introduction

- As the top quark was not produced in LEP its EW sector could not be precisely measured until now
- The LHC data allows, finally, for precise measurements of this sector
- Here we present results of a global fit to top-quark EW couplings
- We used the most recent available data from the LHC (ATLAS and CMS), and also from LEP and Tevatron
- We include the QCD corrections at NLO on most of the observables used
- The fits have been performed using HEPfit [\[1910.14012\]](#)
- Estimations on the improvement of the measurements are presented for the HL-LHC
- Estimation for the relevant observables for this fit in a future  $e^+e^-$  colliders are shown
- Prospects for our limits in the HL-LHC and a future  $e^+e^-$  colliders are obtained

# Theoretical Framework

- We use an EFT description to parametrise deviations from the SM

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda^2} \sum_i C_i O_i + \mathcal{O}(\Lambda^{-4})$$

- The Wilson coefficients can be interpreted in terms of NP mediators
- We include  $\Lambda^{-2}$  terms from the interference between the SM and D6
- We also include  $\Lambda^{-4}$  operators arising from squaring the D6
- The effects of D8 operators, contributing to the same  $\Lambda^{-4}$  order, are omitted

$$\sigma = \sigma_{\text{SM}} + \underbrace{\frac{1}{\Lambda^2} \sum C_i O_i}_{\text{SM} \times \text{D6}} + \underbrace{\left( \frac{1}{\Lambda^2} \sum C_i O_i \right) \left( \frac{1}{\Lambda^2} \sum C_j O_j \right)}_{\text{D6} \times \text{D6}} + \underbrace{O(1/\Lambda^4)}_{\text{SM} \times \text{D8}}$$

- We only consider the EW two-fermion operators and ignore the imaginary parts
- The four-fermion operators are ignored

# EW top-quark EFT Basis

Left and right-handed couplings of the t- and b-quark to the Z

$$\begin{aligned}
 O_{\varphi Q}^3 &\equiv \frac{1}{2} (\bar{q} \tau^I \gamma^\mu q) (\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi) \\
 O_{\varphi Q}^1 &\equiv \frac{1}{2} (\bar{q} \gamma^\mu q) (\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) \\
 O_{\varphi u} &\equiv \frac{1}{2} (\bar{u} \gamma^\mu u) (\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) \\
 O_{\varphi d} &\equiv \frac{1}{2} (\bar{d} \gamma^\mu d) (\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)
 \end{aligned}$$

EW dipole operators

$$\begin{aligned}
 O_{uW} &\equiv (\bar{q} \tau^I \sigma^{\mu\nu} u) (\varepsilon \varphi^* W_{\mu\nu}^I) \\
 O_{dW} &\equiv (\bar{q} \tau^I \sigma^{\mu\nu} d) (\varphi W_{\mu\nu}^I) \\
 O_{uB} &\equiv (\bar{q} \sigma^{\mu\nu} u) (\varepsilon \varphi^* B_{\mu\nu}) \\
 O_{dB} &\equiv (\bar{q} \sigma^{\mu\nu} d) (\varphi B_{\mu\nu})
 \end{aligned}$$

Chromo magnetic dipole operators

$$\begin{aligned}
 O_{uG} &\equiv (\bar{q} \sigma^{\mu\nu} T^A u) (\varepsilon \varphi^* G_{\mu\nu}^A) \\
 O_{dG} &\equiv (\bar{q} \sigma^{\mu\nu} T^A d) (\varphi G_{\mu\nu}^A)
 \end{aligned}$$

Top/Bottom yukawa

$$\begin{aligned}
 O_{u\varphi} &\equiv (\bar{q} u) (\varepsilon \varphi^* \varphi^\dagger) \\
 O_{d\varphi} &\equiv (\bar{q} d) (\varphi \varphi^\dagger)
 \end{aligned}$$

Charged current interaction

$$O_{\varphi ud} \equiv \frac{1}{2} (\bar{u} \gamma^\mu d) (\varphi^T \varepsilon i D_\mu \varphi)$$

- Rotation of Warsaw basis following [\[1802.07237\]](#) (LHC Top WG)

$$O_{\varphi Q}^1 \rightarrow O_{\varphi Q}^- = O_{\varphi Q}^1 - O_{\varphi Q}^3; \quad O_{xB} \rightarrow O_{xZ} = -\sin \theta_W O_{xB} + \cos \theta_W O_{xW}$$

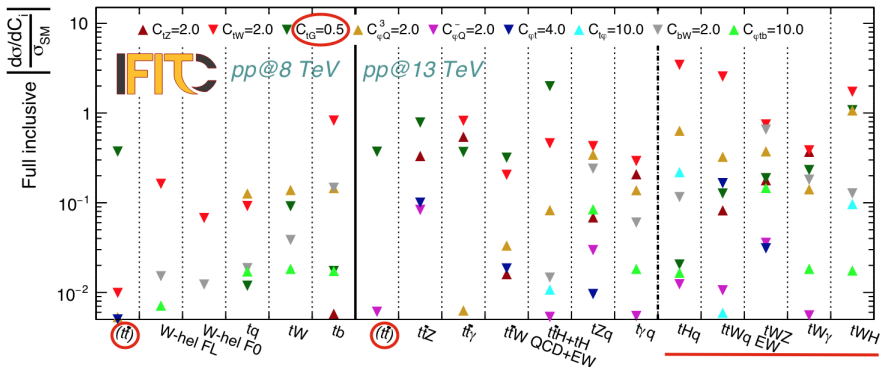
## Methods & Data

- Dependence of the observables calculated at NLO in QCD with the Monte Carlo generator MG5\_aMC@NLO [JHEP 07 (2014) 079]
- SMEFT@NLO [arXiv:2008.11743] UFO model was used except for  $C_{bW}$ ,  $C_{\phi tb}$ ,  $C_{bZ}$  and  $C_{\phi b}$  where the TEFT\_EW [JHEP 05 (2016) 052] UFO model was used
- The fit is performed as a Bayesian statistical analysis of the model using the open source HEPfit [1910.14012]

Process	Observable	$\sqrt{s}$	$\int \mathcal{L}$	Experiment
$pp \rightarrow t\bar{t}H$	cross section	13 TeV	$140 \text{ fb}^{-1}$	ATLAS
$pp \rightarrow t\bar{t}W$	cross section	13 TeV	$36 \text{ fb}^{-1}$	CMS
$pp \rightarrow t\bar{t}Z$	(differential) x-sec.	13 TeV	$140 \text{ fb}^{-1}$	ATLAS
$pp \rightarrow t\bar{t}\gamma$	(differential) x-sec.	13 TeV	$140 \text{ fb}^{-1}$	ATLAS
$pp \rightarrow tZq$	cross section	13 TeV	$140 \text{ fb}^{-1}$	CMS
$pp \rightarrow t\gamma q$	cross section	13 TeV	$36 \text{ fb}^{-1}$	CMS
$pp \rightarrow tb$ (s-ch)	cross section	8 TeV	$20 \text{ fb}^{-1}$	ATLAS+CMS
$pp \rightarrow tW$	cross section	8 TeV	$20 \text{ fb}^{-1}$	ATLAS+CMS
$pp \rightarrow tq$ (t-ch)	cross section	8 TeV	$20 \text{ fb}^{-1}$	ATLAS+CMS
$t \rightarrow W^+ b$	$F_0, F_L$	8 TeV	$20 \text{ fb}^{-1}$	ATLAS+CMS
$p\bar{p} \rightarrow t\bar{b}$ (s-ch)	cross section	1.96 TeV	$9.7 \text{ fb}^{-1}$	Tevatron
$e^- e^+ \rightarrow b\bar{b}$	$R_b, A_{FBLR}^{bb}$	$\sim 91 \text{ GeV}$	$202.1 \text{ pb}^{-1}$	LEP

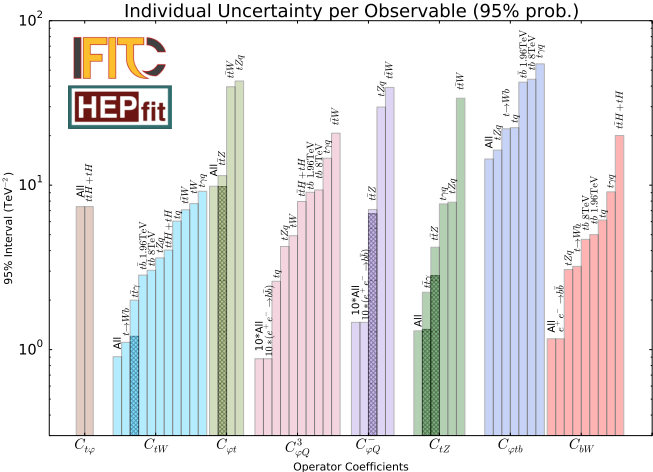
# Sensitivity

- The observables and coefficients in red are not included
- The  $pp \rightarrow t\bar{t}$  process is omitted in the fit in order to be consistent as it is used to reduce the dependence of  $pp \rightarrow t\bar{t}X$  on Wilson coefficients that have not been included.

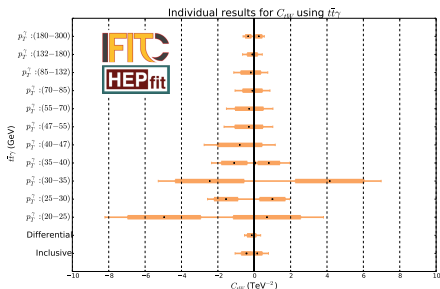
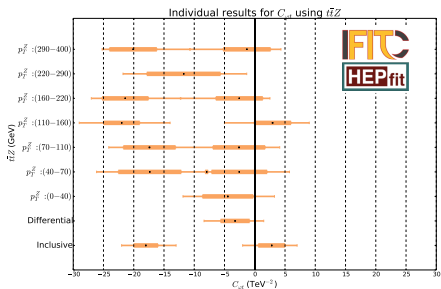
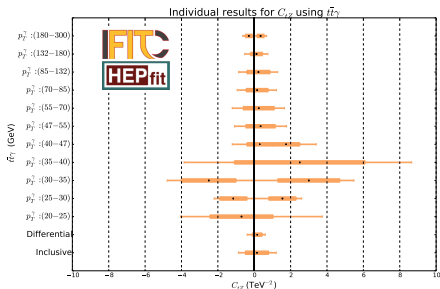
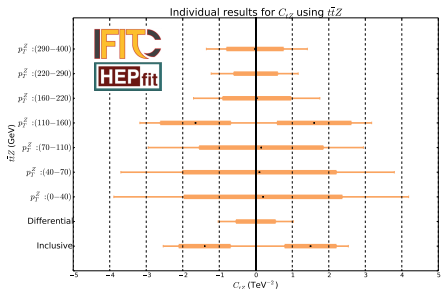


# Results - Sensitivity Individual Constraints

- Good interplay between the parameters and chosen observables
- The differential cross sections (darker regions) provide the best constraints for some observables



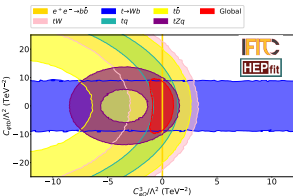
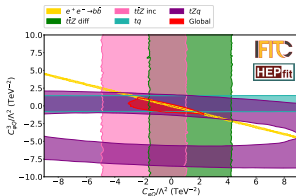
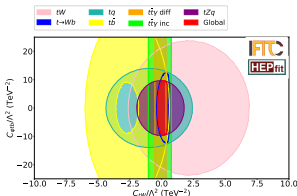
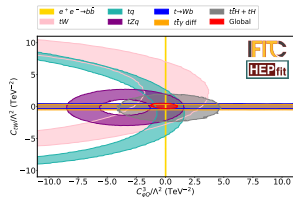
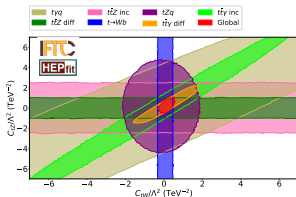
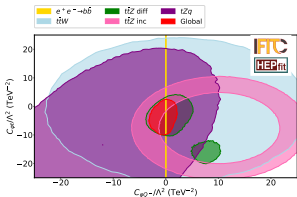
# Results - Differential Cross Section Effect





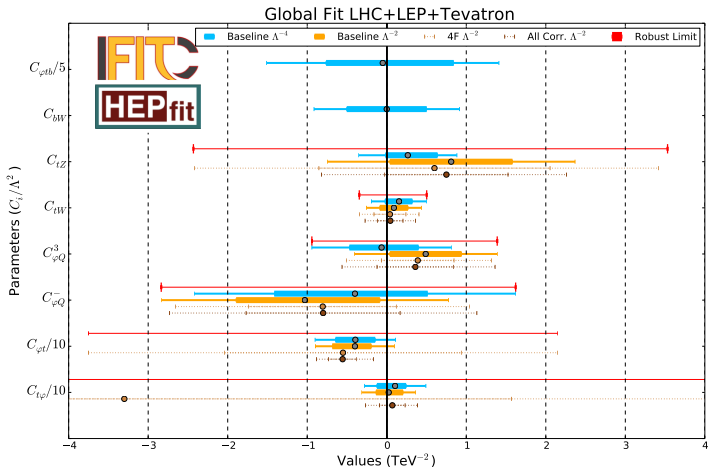
# Results - Complementarity between Observables

- Very good complementarity between the observables
- The global fit marginalised limit is quite close to the intersection of individual fits → The data set is diverse enough to avoid the existence of blind directions



# Results - Global Fit

- The constraints of the linear (only  $\Lambda^{-2}$  terms) global fit are similar to those of the quadratic ( $\Lambda^{-2} + \Lambda^{-4}$  terms) global fit for most cases
- Estimation of the impact of correlations between the observables and the extension of our basis with 7 four-fermion operators and  $C_{tG}$
- **Robust Limit:** Envelope found from combining all the results



## Results - Conclusions

- All the results are compatible with the SM with a 95% probability
- We find a reduction of the uncertainty of all the parameters of around a factor two with respect to our previous work [JHEP12(2019)098]
- Adding important correlations between the observables does not dramatically change the results, but increasing the basis has an effect
- LEP measurements provide tight bounds on several operators as the left-handed coupling  $C_{\varphi Q}^-$  and  $C_{\varphi Q}^{(3)}$
- The limits are quite robust even when we only consider linear terms, except for  $C_{bW}$ ,  $C_{\varphi tb}$  and  $C_{tZ}$
- The addition of the differential cross sections of  $pp \rightarrow t\bar{t}Z$  and  $pp \rightarrow t\bar{t}\gamma$  have an important effect on  $C_{tZ}$  and  $C_{\varphi t}$
- We find the most stringent bound on top EW couplings from an EFT including all relevant 2-fermions degrees of freedom (see [JHEP 04 (2019) 100], [JHEP 02 (2020) 131], [CMS-PAS-TOP-19-001])

# Future Colliders - Prospects for Measurements at HL-LHC

Theoretical Uncertainties  $\longrightarrow$  scale with  $1/2$

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Experimental Uncertainties  $\left\{ \begin{array}{l} \text{Modelling} \longrightarrow \text{scale with } 1/2 \\ \text{Systematic} \longrightarrow \text{scale with } 1/\sqrt{\mathcal{L}} \\ \text{Statistical} \longrightarrow \text{scale with } 1/\sqrt{\mathcal{L}} \end{array} \right.$

# Future Colliders - Prospects for Measurements at HL-LHC

## Inclusive cross sections and helicities

Process	Measured (fb)	SM (fb)	LHC Unc.					HL-LHC Unc.				
			theo.	exp.				theo.	exp.			
				stat.	sys.	mod.	tot.		stat.	sys.	mod.	tot.
$pp \rightarrow t\bar{t}H + tHq$	640	664.3	41.7	90	40	70.7	121.2	20.9	19.4	8.6	35.4	41.3
$pp \rightarrow t\bar{t}Z$	990	810.9	85.8	51.5	48.9	67.3	97.8	42.9	11.1	10.6	33.6	37.0
$pp \rightarrow t\bar{t}\gamma$	39.6	38.5	1.76	0.8	1.25	2.16	2.62	0.88	0.17	0.27	1.08	1.13
$pp \rightarrow tZq$	111	102	3.5	13.0	6.1	6.2	15.7	1.75	2.09	0.98	3.1	3.87
$pp \rightarrow t\gamma q$	115.7	81	4	17.1	21.1	21.1	34.4	2	1.9	2.3	10.6	11.0
$pp \rightarrow t\bar{t}W + EW$	770	647.5	76.1	120	59.6	73.0	152.6	38.1	13.1	6.5	36.5	39.4
$pp \rightarrow t\bar{b}$ (s-ch)	4900	5610	220	784	936	790	1454	110	35	42	395	399
$pp \rightarrow tW$	23100	22370	1570	1086	2000	2773	3587	785	49	89	1386	1390
$pp \rightarrow tq$ (t-ch)	87700	84200	250	1140	3128	4766	5810	125	51	140	2383	2390
$F_0$	0.693	0.687	0.005	0.009	0.006	0.009	0.014	0.003	0.0004	0.0003	0.004	0.004
$F_L$	0.315	0.311	0.005	0.006	0.003	0.008	0.011	0.003	0.0003	0.0002	0.004	0.004

**Table:** The data shown is the inclusive cross-section written in fb for all the channels except, obviously, for the  $W$  Helicities ( $F_0$  and  $F_L$ ).

# Future Colliders - Prospects for Measurements at HL-LHC

$pp \rightarrow t\bar{t}Z$  differential cross section

$pp \rightarrow t\bar{t}Z$	Measured ( $\text{fb} \cdot \text{GeV}^{-1}$ )	SM ( $\text{fb} \cdot \text{GeV}^{-1}$ )	LHC Unc.				HL-LHC Unc.					
			theo.	exp.			theo.	exp.				
				stat.	sys.	mod.		tot.	stat.	sys.	mod.	tot.
$p_T^Z : (0-40)$	1.47	2.21	0.263	0.53	0.23	0.21	0.615	0.132	0.114	0.050	0.105	0.163
$p_T^Z : (40-70)$	4.32	4.59	0.543	0.94	0.60	0.51	1.223	0.272	0.203	0.130	0.253	0.349
$p_T^Z : (70-110)$	4.24	4.60	0.555	0.75	0.54	0.36	0.993	0.278	0.162	0.117	0.182	0.270
$p_T^Z : (110-160)$	4.4	3.45	0.429	0.55	0.43	0.39	0.800	0.215	0.118	0.093	0.197	0.248
$p_T^Z : (160-220)$	1.75	2.05	0.261	0.31	0.15	0.13	0.371	0.131	0.067	0.033	0.066	0.100
$p_T^Z : (220-290)$	0.58	1.03	0.130	0.16	0.047	0.034	0.174	0.065	0.035	0.010	0.017	0.041
$p_T^Z : (290-400)$	0.56	0.59	0.071	0.11	0.055	0.057	0.132	0.036	0.023	0.012	0.029	0.038

**Table:** We show the unfolded bin contents for the absolute parton-level differential cross-section measurement.

# Future Colliders - Prospects for Measurements at HL-LHC

$pp \rightarrow t\bar{t}\gamma$  differential cross section

$pp \rightarrow t\bar{t}\gamma$	Measured ( $\text{fb} \cdot \text{GeV}^{-1}$ )	SM ( $\text{fb} \cdot \text{GeV}^{-1}$ )	LHC Unc.					HL-LHC Unc.				
			theo.	exp.				theo.	exp.			
				stat.	sys.	mod.	tot.		stat.	sys.	mod.	tot.
$p_T^{\gamma} : (20-25)$	1.782	1.670	0.066	0.116	0.168	0.108	0.231	0.033	0.025	0.036	0.054	0.070
$p_T^{\gamma} : (25-30)$	1.328	1.183	0.040	0.089	0.052	0.092	0.138	0.020	0.019	0.011	0.046	0.051
$p_T^{\gamma} : (30-35)$	0.966	0.8663	0.0302	0.072	0.026	0.060	0.097	0.0151	0.016	0.0056	0.030	0.0342
$p_T^{\gamma} : (35-40)$	0.705	0.6616	0.0205	0.058	0.015	0.042	0.0733	0.0103	0.0125	0.0032	0.021	0.0248
$p_T^{\gamma} : (40-47)$	0.474	0.4790	0.0160	0.04	0.0096	0.048	0.0629	0.0080	0.0086	0.0021	0.024	0.0254
$p_T^{\gamma} : (47-55)$	0.333	0.3464	0.0094	0.031	0.0067	0.017	0.0360	0.0047	0.0067	0.0014	0.0085	0.0109
$p_T^{\gamma} : (55-70)$	0.221	0.2188	0.0056	0.019	0.0038	0.0081	0.0210	0.0028	0.0041	0.00082	0.0041	0.0058
$p_T^{\gamma} : (70-85)$	0.122	0.1286	0.0031	0.014	0.0026	0.0069	0.0158	0.0016	0.0030	0.00056	0.0035	0.0046
$p_T^{\gamma} : (85-132)$	0.060	0.06037	0.0017	0.005	0.0014	0.0068	0.0086	0.00084	0.0011	0.00029	0.0034	0.0036
$p_T^{\gamma} : (132-180)$	0.020	0.02373	0.00077	0.003	0.00044	0.00080	0.00314	0.00039	0.00065	0.000095	0.00040	0.00077
$p_T^{\gamma} : (180-300)$	0.009	0.00790	0.00028	0.00045	0.000085	0.0014	0.00144	0.00014	0.000097	0.000018	0.00068	0.00069

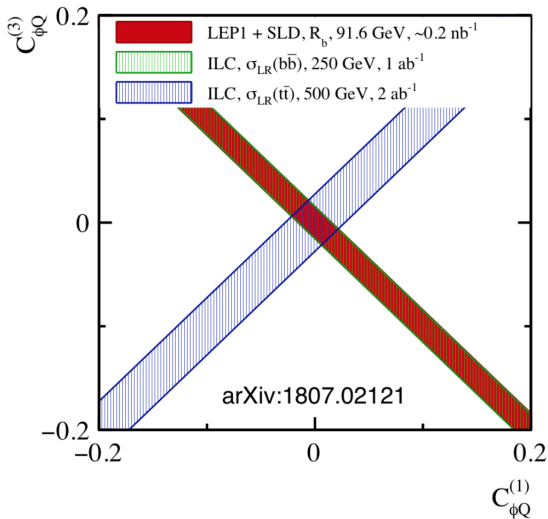
**Table:** We show the unfolded bin contents for the absolute parton-level differential cross-section measurement.

# Future Colliders - Complementarity on $e^+e^-$ Colliders

Good complementarity between  $b\bar{b}$  (LEP) and  $t\bar{t}$  (future  $e^+e^-$  collider) if we reach  $\sqrt{s} > 2m_t$

$$\delta g_L^t = -(C_{\phi Q}^1 - C_{\phi Q}^3)m_t^2/\Lambda^2$$

$$\delta g_L^b = -(C_{\phi Q}^1 + C_{\phi Q}^3)m_t^2/\Lambda^2$$





# Future Colliders - Prospects for Measurements at $e^+e^-$ Linear Collider

Process	Observable	$\sqrt{s}$	$\int \mathcal{L}$	Experiment
$e^+e^- \rightarrow b\bar{b}$	(+80%, -30%) x-section, $A_{FB}^{bb}$	250 GeV	2 ab <sup>-1</sup>	ILC250
	(-80%, +30%) x-section, $A_{FB}^{bb}$	250 GeV	2 ab <sup>-1</sup>	ILC250
	(+80%, -30%) x-section, $A_{FB}^{bb}$	500 GeV	4 ab <sup>-1</sup>	ILC500
	(-80%, +30%) x-section, $A_{FB}^{bb}$	500 GeV	4 ab <sup>-1</sup>	ILC500
	(+80%, -30%) x-section, $A_{FB}^{bb}$	1000 GeV	8 ab <sup>-1</sup>	ILC1000
	(-80%, +30%) x-section, $A_{FB}^{bb}$	1000 GeV	8 ab <sup>-1</sup>	ILC1000
$e^+e^- \rightarrow t\bar{t}$	optimal observables	500 GeV	4 ab <sup>-1</sup>	ILC500
$e^+e^- \rightarrow t\bar{t}$	optimal observables	1000 GeV	8 ab <sup>-1</sup>	ILC1000

Optimal Observables: minimise the determinant of the covariance matrix  
[\[1807.02121\]](#)

$$\frac{d\sigma}{d\Phi} = \frac{d\sigma_{SM}}{d\Phi} + \sum_i C_i \frac{d\sigma_i}{d\Phi}, \quad \bar{O}_i = \varepsilon \mathcal{L} \int d\Phi \left( \frac{d\sigma_i}{d\Phi} / \frac{d\sigma_{SM}}{d\Phi} \right) \frac{d\sigma}{d\Phi}$$

# Future Colliders - Prospects for Measurements at $e^+e^-$

## Linear Collider: ILC250

S. Bilokin, A. Irlles, R. Pöschl and F. Richard, *in preparation*

$e^+e^- \rightarrow b\bar{b}$ :

	Uncertainty	Correlation			
		LR x-section	LR $A_{FB}^{bb}$	RL x-section	RL $A_{FB}^{bb}$
LR x-section	5 fb	1	0.35	0.92	0.88
LR $A_{FB}^{bb}$	0.165	0.35	1	0.38	0.50
RL x-section	1.8 fb	0.92	0.38	1	0.97
RL $A_{FB}^{bb}$	0.214	0.88	0.50	0.97	1

# Future Colliders - Prospects for Measurements at $e^+e^-$

## Linear Collider: ILC500

$$\underline{e^+e^- \rightarrow b\bar{b}}:$$

S. Bilokin, et al.	Uncertainty
LR x-section	1.34 fb
LR $A_{FB}^{bb}$	0.19
RL x-section	0.74 fb
RL $A_{FB}^{bb}$	0.34

$$\underline{e^+e^- \rightarrow t\bar{t}}:$$

[1807.02121]	Uncertainty	Correlation			
		$C_{\varphi t}$	$C_{\varphi Q}^-$	$C_{tW}$	$C_{tB}$
$C_{\varphi t}$	0.011	1	0.82	0.94	-0.91
$C_{\varphi Q}^-$	0.011	0.82	1	0.94	-0.93
$C_{tW}$	0.022	0.94	0.94	1	-0.97
$C_{tB}$	0.0076	-0.91	-0.93	-0.97	1

# Future Colliders - Prospects for Measurements at $e^+e^-$

## Linear Collider: ILC1000

$$e^+e^- \rightarrow b\bar{b}:$$

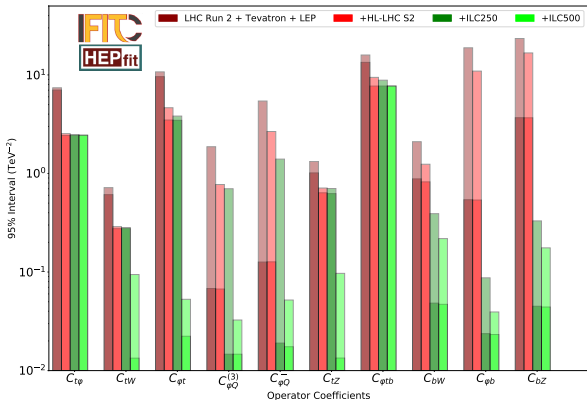
S. Bilokin, et al.	Uncertainty
LR x-section	0.74 fb
LR $A_{FB}^{bb}$	0.42
RL x-section	0.40 fb
RL $A_{FB}^{bb}$	0.78

$$e^+e^- \rightarrow t\bar{t}:$$

[1807.02121]	Uncertainty	Correlation							
		$C_{et}$	$C_{eQ}$	$C_{It}$	$C_{IQ}^-$	$C_{\varphi Q}^-$	$C_{\varphi t}$	$C_{tW}$	$C_{tB}$
$C_{et}$	0.00053	1	-0.053	0	0	0	0	0	0
$C_{eQ}$	0.00053	-0.053	1	0	0	0	0	0	0
$C_{It}$	0.0005	0	0	1	-0.18	0	0	0	0
$C_{IQ}^-$	0.0005	0	0	-0.18	1	0	0	0	0
$C_{\varphi Q}^-$	0.087	0	0	0	0	1	0.31	0	0
$C_{\varphi t}$	0.087	0	0	0	0	0.31	1	0	0
$C_{tW}$	0.00905	0	0	0	0	0	0	1	-0.85
$C_{tB}$	0.0052	0	0	0	0	0	0	-0.85	1

# Future Colliders - Prospects for EW Top-Quark Couplings

- Results from [JHEP12(2019)098] show the extraordinary impact of adding the data from a  $e^+e^-$  collider working at 500 GeV  $\rightarrow$  It is crucial to go  $\sqrt{s} > 2m_t$
- The LHC Run 2 data here refers to the data available in mid 2019, with the current data the errors are reduced around a factor two



# Future Colliders - Prospects for EW Top-Quark Couplings + $e^+e^- Q \bar{Q}$

Only constrained with data at two  $\sqrt{s} > 2m_t$ :

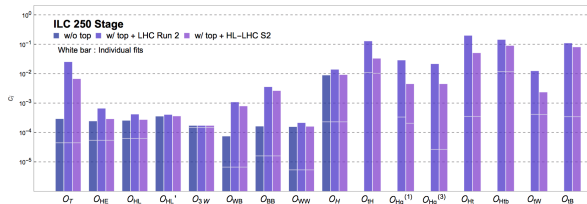
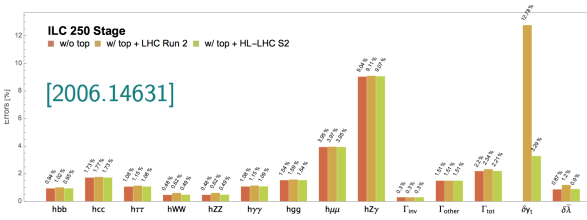
$$\begin{aligned}
 O_{lQ}^1 &\equiv \frac{1}{2} \bar{Q} \gamma_\mu Q \bar{l} \gamma^\mu l \\
 O_{lQ}^3 &\equiv \frac{1}{2} \bar{q} \tau^I \gamma_\mu q \bar{l} \tau^I \gamma^\mu l \\
 O_{lt} &\equiv \frac{1}{2} \bar{t} \gamma_\mu t \bar{l} \gamma^\mu l \\
 O_{lb} &\equiv \frac{1}{2} \bar{b} \gamma_\mu b \bar{l} \gamma^\mu l \\
 O_{eQ} &\equiv \frac{1}{2} \bar{Q} \gamma_\mu Q \bar{e} \gamma^\mu e \\
 O_{et} &\equiv \frac{1}{2} \bar{t} \gamma_\mu t \bar{e} \gamma^\mu e \\
 O_{eb} &\equiv \frac{1}{2} \bar{b} \gamma_\mu b \bar{e} \gamma^\mu e
 \end{aligned}$$

	10-parameter fit ILC250 + ILC500	17-parameter fit + ILC1000
$C_{\phi t}/\Lambda^2$	0.037	0.021
$C_{\phi Q}^3/\Lambda^2$	0.020	0.017
$C_{\phi Q}^-/\Lambda^2$	0.036	0.021
$C_{tW}/\Lambda^2$	0.071	0.030
$C_{tZ}/\Lambda^2$	0.074	0.032
$C_{t\phi}/\Lambda^2$	1.735	1.735
$C_{\phi b}/\Lambda^2$	0.030	0.047
$C_{bW}/\Lambda^2$	0.204	0.478
$C_{bZ}/\Lambda^2$	0.163	0.438
$C_{\phi tb}/\Lambda^2$	3.90	3.67
$C_{eu}/\Lambda^2$	—	0.0021
$C_{ed}/\Lambda^2$	—	0.0032
$C_{eq}/\Lambda^2$	—	0.0019
$C_{lu}/\Lambda^2$	—	0.0020
$C_{ld}/\Lambda^2$	—	0.0100
$C_{lq}^-/\Lambda^2$	—	0.0020
$C_{lq}^+/\Lambda^2$	—	0.0039

# Future Colliders - Prospects for Top-Quark+Higgs Sector

For current limits on this sector look at [\[2012.02779\]](#) and [\[1910.03606\]](#)

- The determination of the Higgs boson couplings at ILC250 is degraded by the additional top-quark operators
- We can recover the original bounds by the inclusion of precise measurements of top-quark EW couplings at the LHC
- The physical Higgs couplings are relatively robust, as the top mass is larger than the energy scale of EW processes
- If the ILC reaches 500 GeV it will provide very precise constraints on the top operators



## Summary

- Current data allows for constraining the top-quark EW considering only  $\Lambda^{-2}$  terms
- $\Lambda^{-4}$  terms are specially relevant for  $C_{bW}$  and  $C_{\phi tb}$  whose  $\Lambda^{-2}$  dependence vanishes in the limit  $m_b \rightarrow 0$
- The correlation between observables does not seem to have a dramatic impact in the final result
- Including additional operators has an important effect on some (but not all) of the limits
- In the HL-LHC the theoretical and modelling uncertainties are dominant  $\rightarrow$  hinders the improvement on the limits
- To improve the limits in some order of magnitudes it is crucial to build a  $e^+e^-$  collider working at  $\sqrt{s} > 2m_t$
- An  $e^+e^-$  collider working at two different energies above  $2m_t$  is needed to constrain  $e^+e^- Q \bar{Q}$
- For a precise fit on the combined sector of the top plus the Higgs it could be enough with the data of a  $e^+e^-$  collider working at  $\sqrt{s} = 250$  GeV given the expected precision that the LHC could achieve for the top-quark EW couplings



Thank you!

## Back up

Numerical values for the Wilson Coefficients

$C/\Lambda^2$ (TeV <sup>-2</sup> )	Linear+Quadratic (95% probability intervals)		
	Individual	Global-Baseline	Global-Robust
$C_{t\phi}$	[-3.05, 4.05]	[-2.82, 4.92]	[-121.82, 62.82]
$C_{\phi Q}^-$	[-0.038, 0.079]	[-2.42, 1.62]	[-2.84, 1.62]
$C_{\phi Q}^3$	[-0.019, 0.040]	[-0.94, 0.81]	[-0.94, 1.39]
$C_{\phi t}$	[-8.6, 1.5]	[-9.01, 1.11]	[-37.50, 21.50]
$C_{tW}$	[-0.28, 0.32]	[-0.19, 0.50]	[-0.35, 0.50]
$C_{tZ}$	[-0.39, 0.57]	[-0.35, 0.88]	[-2.43, 3.53]
$C_{\phi tb}$	[-6.61, 6.71]	[-7.55, 7.05]	–
$C_{bW}$	[-0.47, 0.47]	[-0.91, 0.91]	–

**Table:** Allowed ranges of the Wilson coefficients with a probability of 95% expressed in TeV<sup>-2</sup> including linear and quadratic terms. We show, from left to right, the results of three fits: individual, global baseline and global robust. The robust result accounts for the effects of the correlations between the observables, the inclusion of further operators and the theoretical uncertainties on the parameterisations.

## Back up

### Numerical values for the Wilson Coefficients

$C/\Lambda^2$ ( $\text{TeV}^{-2}$ )	Linear (95% probability intervals)	
	Individual	Global-Baseline
$C_{t\varphi}$	[-3.17, 3.47]	[-3.13, 3.63]
$C_{\varphi Q}^-$	[-0.038, 0.079]	[-2.84, 0.78]
$C_{\varphi Q}^3$	[-0.019, 0.040]	[-0.41, 1.39]
$C_{\varphi t}$	[-6.6, 1.8]	[-8.96, 0.96]
$C_{tW}$	[-0.30, 0.38]	[-0.26, 0.44]
$C_{tZ}$	[-0.82, 2.21]	[-0.75, 2.37]

**Table:** Allowed ranges of the Wilson coefficients with a probability of 95% expressed in  $\text{TeV}^{-2}$  including only linear terms. We show, from left to right, the results of three fits: individual, global baseline and global robust. The robust result accounts for the effects of the correlations between the observables, the inclusion of further operators and the theoretical uncertainties on the parameterisations.

# Back up

## 4-fermion operators

$C_{qq}^{1(ijkl)}$	$(\bar{q}_i \gamma^\mu q_j)(\bar{q}_k \gamma_\mu q_l)$	$C_{qq}^{3(ijkl)}$	$(\bar{q}_i \tau^l \gamma^\mu q_j)(\bar{q}_k \tau^l \gamma_\mu q_l)$
$C_{uu}^{(ijkl)}$	$(\bar{u}_i \gamma^\mu u_j)(\bar{u}_k \gamma_\mu u_l)$	$C_{ud}^{8(ijkl)}$	$(\bar{u}_i \gamma^\mu T^A u_j)(\bar{d}_k \gamma_\mu T^A d_l)$
$C_{qu}^{8(ijkl)}$	$(\bar{q}_i \gamma^\mu T^A q_j)(\bar{u}_k \gamma_\mu T^A u_l)$	$C_{qd}^{8(ijkl)}$	$(\bar{q}_i \gamma^\mu T^A q_j)(\bar{d}_k \gamma_\mu T^A d_l)$
$C_{tu}^8$	$\sum_{i=1,2} 2 C_{uu}^{(i33i)}$	$C_{td}^8$	$\sum_{i=1,2,3} C_{ud}^{8(33ii)}$
$C_{Qu}^8$	$\sum_{i=1,2} C_{qu}^{8(33ii)}$	$C_{Qq}^{1,8}$	$\sum_{i=1,2} C_{qq}^{1(i33i)} + 3 C_{qq}^{3(i33i)}$
$C_{Qd}^8$	$\sum_{i=1,2,3} C_{qd}^{8(33ii)}$	$C_{Qq}^{3,8}$	$\sum_{i=1,2} C_{qq}^{1(i33i)} - C_{qq}^{3(i33i)}$
—	—	$C_{tq}^8$	$\sum_{i=1,2} C_{uq}^{8(ii33)}$

# Back up

Dependencies [1910.03606] :

parameter	$t\bar{t}$	single $t$	$tW$	$tZ$	$t$ decay	$t\bar{t}Z$	$t\bar{t}W$
$C_{Qq}^{1,8}$	$\Lambda^{-2}$	–	–	–	–	$\Lambda^{-2}$	$\Lambda^{-2}$
$C_{Qq}^{3,8}$	$\Lambda^{-2}$	$\Lambda^{-4} [\Lambda^{-2}]$	–	$\Lambda^{-4} [\Lambda^{-2}]$	$\Lambda^{-4} [\Lambda^{-2}]$	$\Lambda^{-2}$	$\Lambda^{-2}$
$C_{tu}^8, C_{td}^8$	$\Lambda^{-2}$	–	–	–	–	$\Lambda^{-2}$	–
$C_{Qq}^{1,1}$	$\Lambda^{-4} [\Lambda^{-2}]$	–	–	–	–	$\Lambda^{-4} [\Lambda^{-2}]$	$\Lambda^{-4} [\Lambda^{-2}]$
$C_{Qq}^{3,1}$	$\Lambda^{-4} [\Lambda^{-2}]$	$\Lambda^{-2}$	–	$\Lambda^{-2}$	$\Lambda^{-2}$	$\Lambda^{-4} [\Lambda^{-2}]$	$\Lambda^{-4} [\Lambda^{-2}]$
$C_{tu}^1, C_{td}^1$	$\Lambda^{-4} [\Lambda^{-2}]$	–	–	–	–	$\Lambda^{-4} [\Lambda^{-2}]$	–
$C_{Qu}^8, C_{Qd}^8$	$\Lambda^{-2}$	–	–	–	–	$\Lambda^{-2}$	–
$C_{tq}^8$	$\Lambda^{-2}$	–	–	–	–	$\Lambda^{-2}$	$\Lambda^{-2}$
$C_{Qu}^1, C_{Qd}^1$	$\Lambda^{-4} [\Lambda^{-2}]$	–	–	–	–	$\Lambda^{-4} [\Lambda^{-2}]$	–
$C_{tq}^1$	$\Lambda^{-4} [\Lambda^{-2}]$	–	–	–	–	$\Lambda^{-4} [\Lambda^{-2}]$	$\Lambda^{-4} [\Lambda^{-2}]$
$C_{\phi Q}^-$	–	–	–	$\Lambda^{-2}$	–	$\Lambda^{-2}$	–
$C_{\phi Q}^3$	–	$\Lambda^{-2}$	$\Lambda^{-2}$	$\Lambda^{-2}$	$\Lambda^{-2}$	–	–
$C_{\phi t}$	–	–	–	$\Lambda^{-2}$	–	$\Lambda^{-2}$	–
$C_{\phi tb}$	–	$\Lambda^{-4}$	$\Lambda^{-4}$	$\Lambda^{-4}$	$\Lambda^{-4}$	–	–
$C_{tZ}$	–	–	–	$\Lambda^{-2}$	–	$\Lambda^{-2}$	–
$C_{tW}$	–	$\Lambda^{-2}$	$\Lambda^{-2}$	$\Lambda^{-2}$	$\Lambda^{-2}$	–	–
$C_{bW}$	–	$\Lambda^{-4}$	$\Lambda^{-4}$	$\Lambda^{-4}$	$\Lambda^{-4}$	–	–
$C_{tG}$	$\Lambda^{-2}$	$[\Lambda^{-2}]$	$\Lambda^{-2}$	–	$[\Lambda^{-2}]$	$\Lambda^{-2}$	$\Lambda^{-2}$

**Table 1.** Wilson coefficients in our analysis and their contributions to top-quark observables via SM-interference ( $\Lambda^{-2}$ ) and via dimension-6 squared terms only ( $\Lambda^{-4}$ ). A square bracket indicates that the Wilson coefficient contributes via SM-interference at NLO QCD. All quark masses except  $m_t$  are assumed to be zero. ‘Single  $t$ ’ stands for  $s$ - and  $t$ -channel electroweak top production.