

ProtoDUNE-SP Neutral Pion Reconstruction

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DUNE-UK Project Meeting

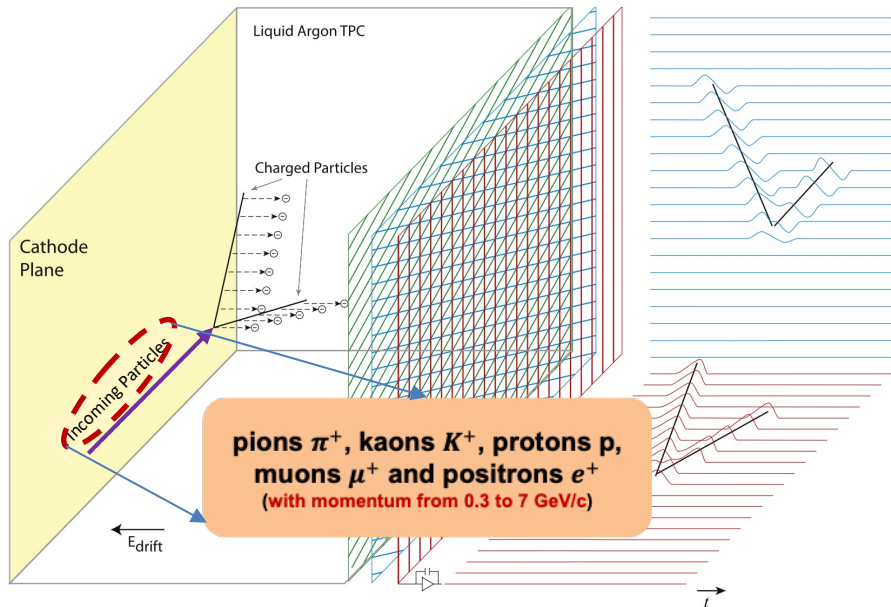
2022 Jan. 17

ProtoDUNE-Single Phase

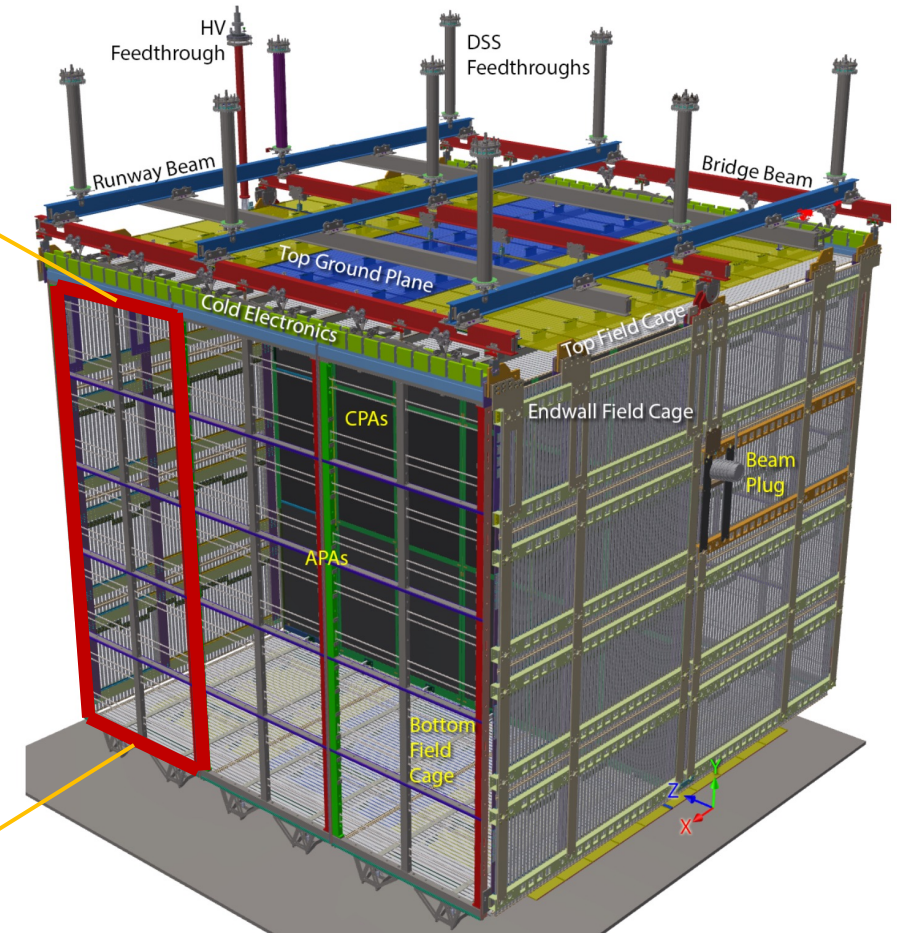
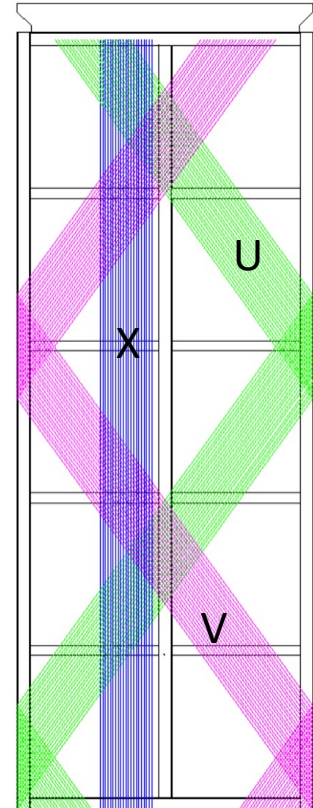
The protoDUNE single-phase apparatus is one of the two large scale prototypes of the far detector module of DUNE.

❖ Several goals:

- Cryostat design validation (electronics, high voltage, LAr purity)
- Data acquisition and storage
- Detector performance characterisation
- Event reconstruction and analysis



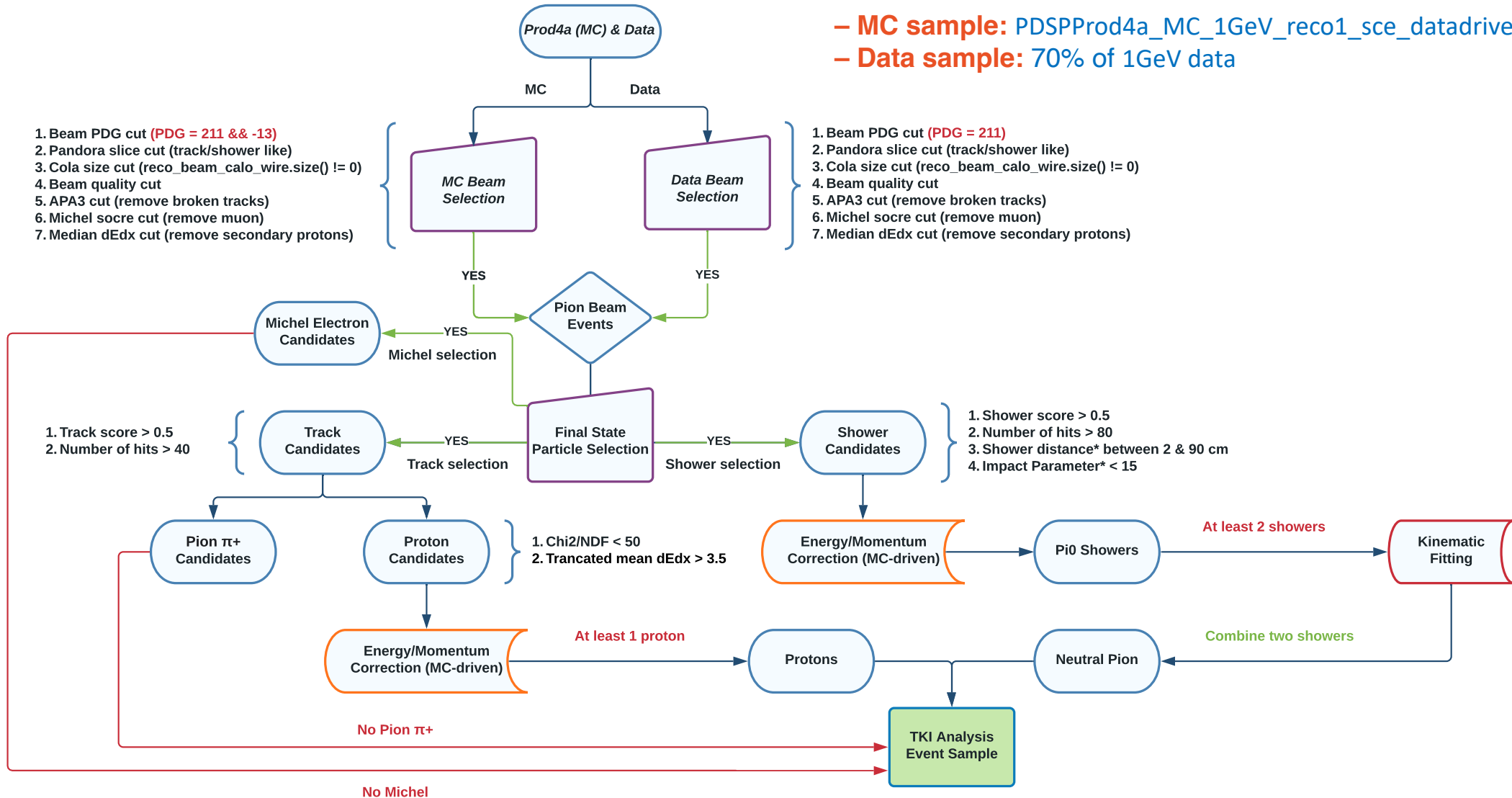
ProtoDUNE-SP APA



Analysis Flowchart

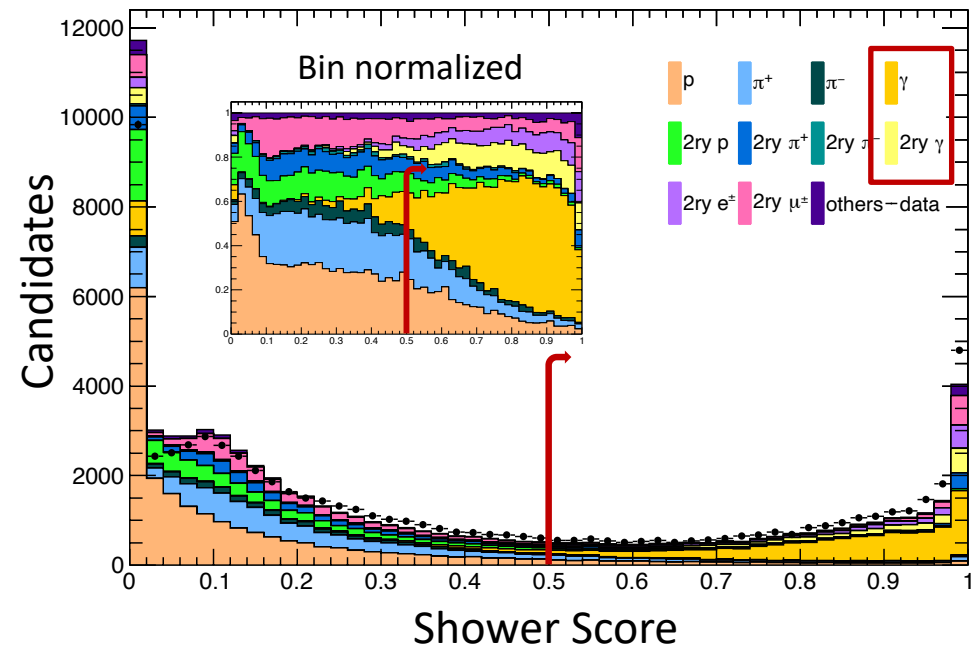
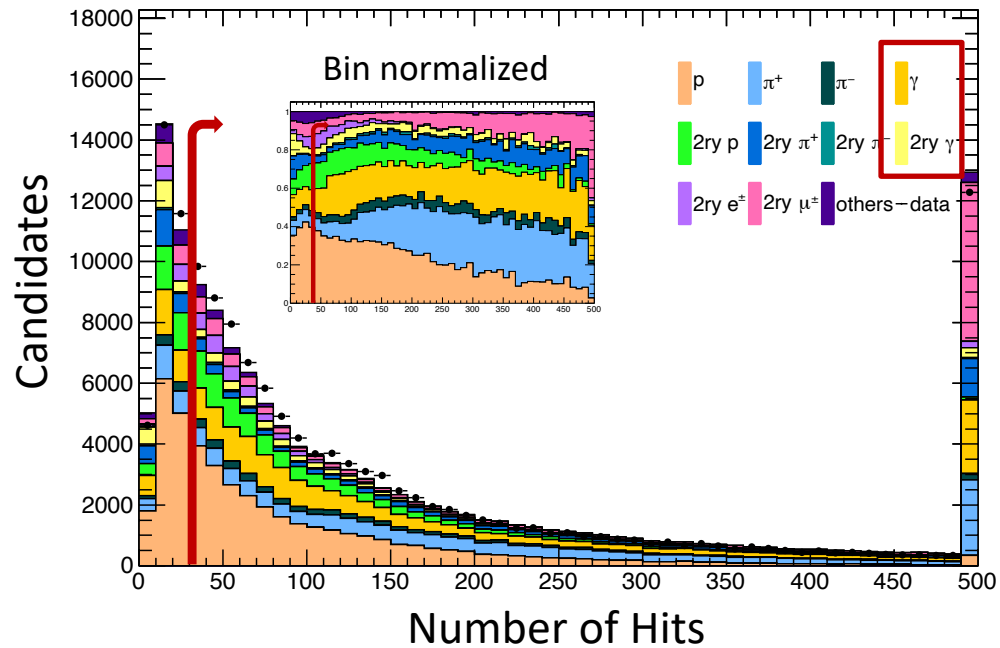


- MC sample: PDSPProd4a_MC_1GeV_reco1_sce_datadriven_v1_00 - 09
- Data sample: 70% of 1GeV data



Shower Selection & Reconstruction

Shower Selection

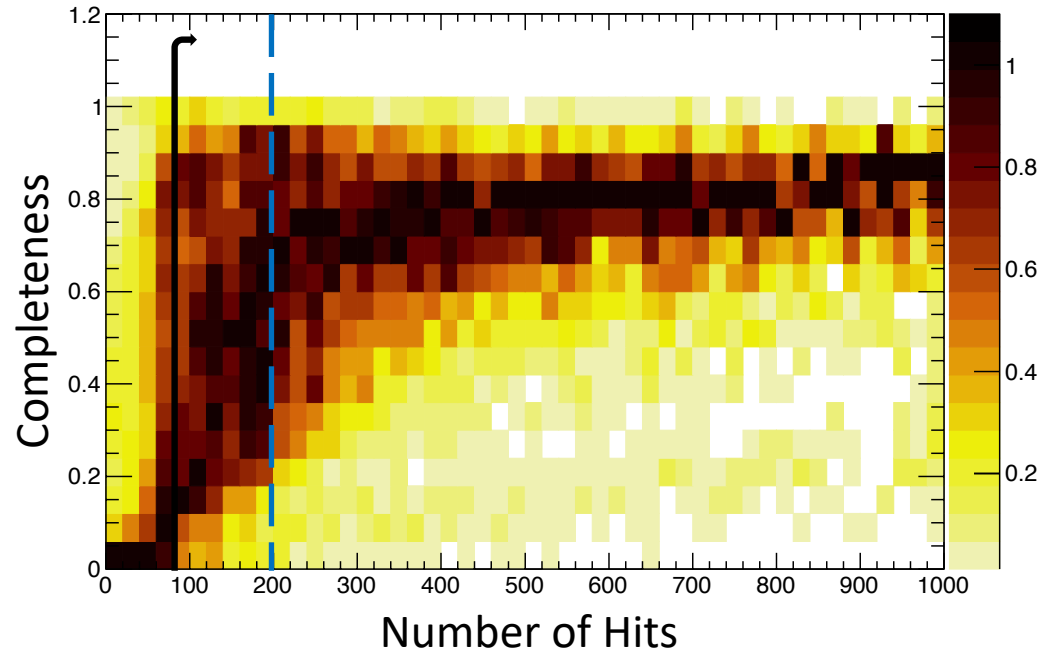


- ❖ **Shower score** can be used to select shower like particles.
- ❖ Most protons and pions have shower score less than 0.5

- ❖ Rec. particles are counted as a **shower** if :
 1. Number of hits > 80
 2. Shower Score > 0.5

Why $n\text{Hits} > 80$ (Shower Selection)

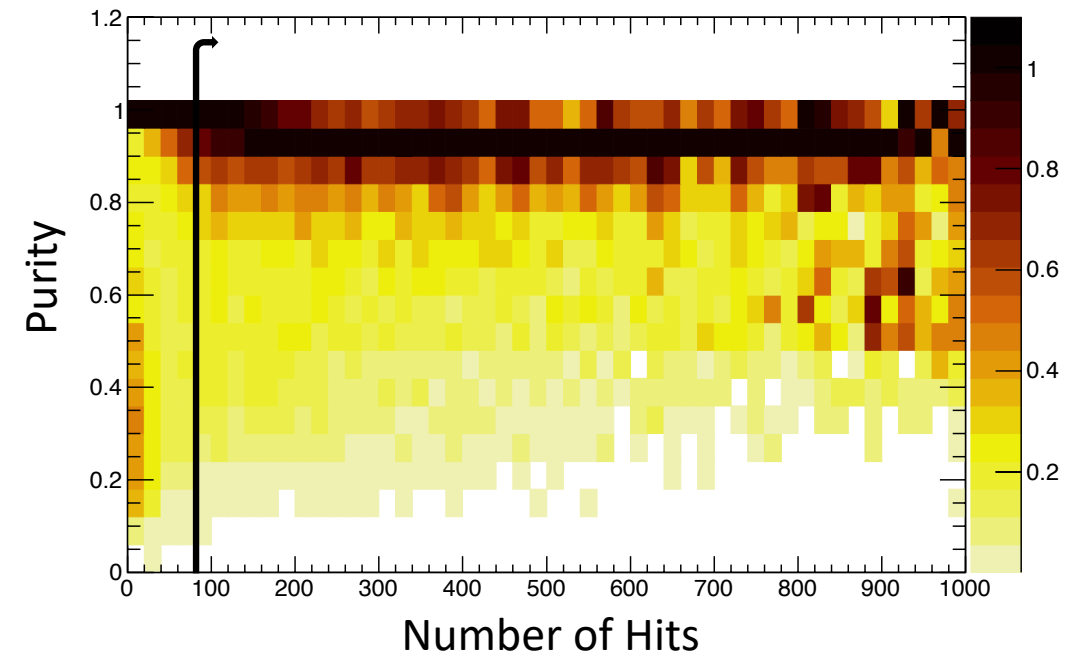
Column normalized



- ❖ The max. completeness is about **0.8**.
- ❖ Best cut would be $n\text{Hits} > 200$, but will reduce the sample size dramatically.
- ❖ We can see that the rec. showers are not completed, **20%** of hits are missing.

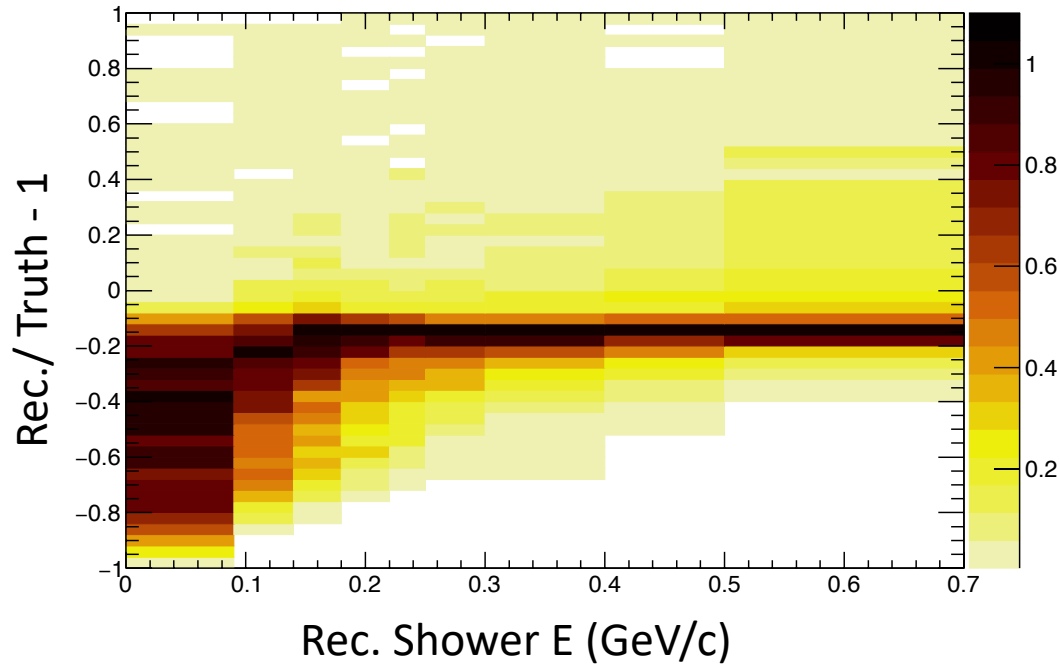
- ❖ This is the Completeness VS $n\text{Hits}$ after select particle with **shower score** > 0.5
- ❖ Select $n\text{Hits} > 80$ will reject those very low completeness rec. particle.

Column normalized

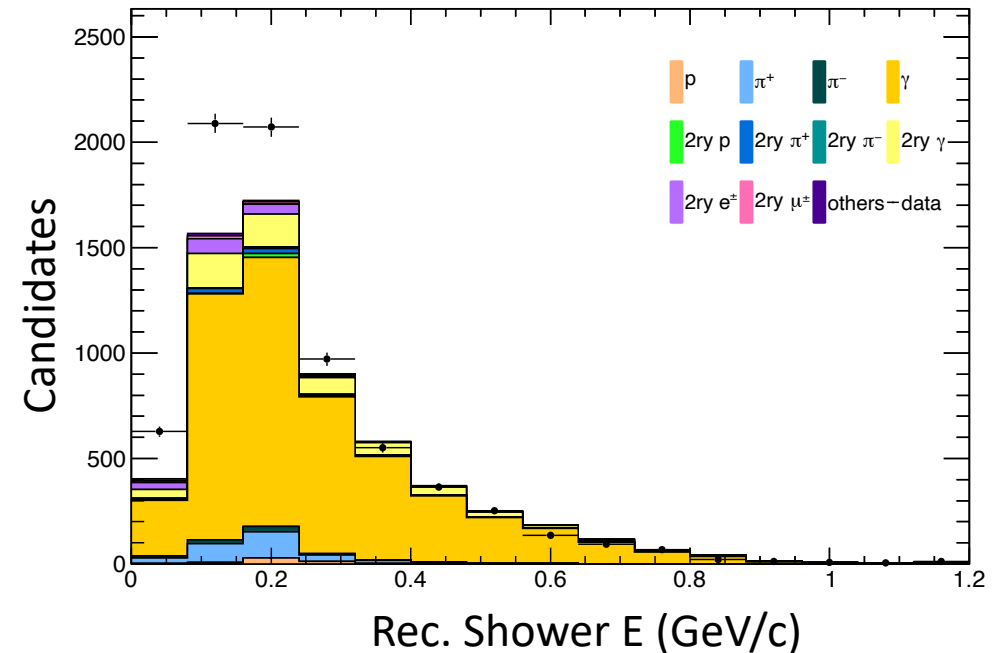


Shower Energy Reconstruction

Column normalized



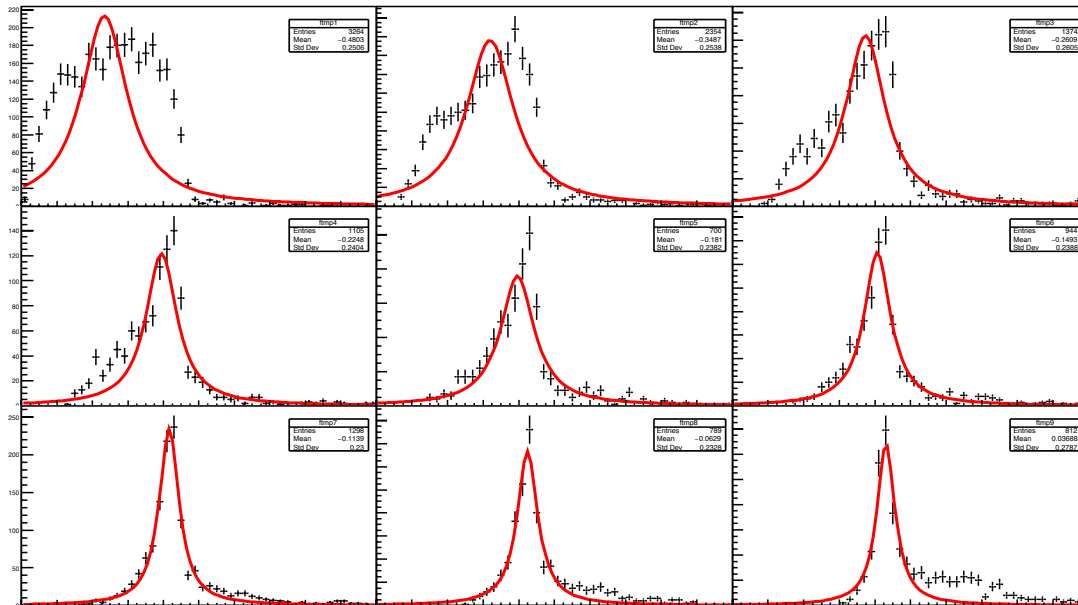
- ❖ A very large rec. bias is found in shower energy (- 15%) in 0.2 – 0.7 GeV.
- ❖ Lower energy region has even larger bias.



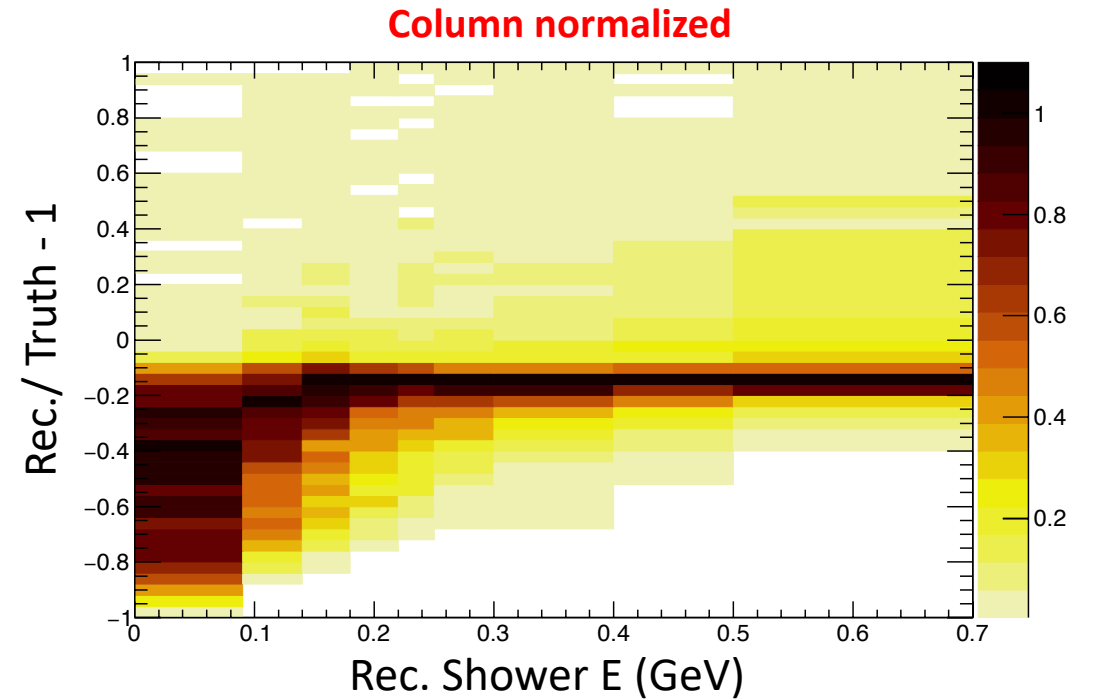
- ❖ We have a MC-data discrepancy for energy below 0.2 GeV.
- ❖ Can apply the energy correction

Shower Energy Correction

- ❖ A MC-driven method can be used to correct the bias in the reconstruction.



Rec./Truth - 1

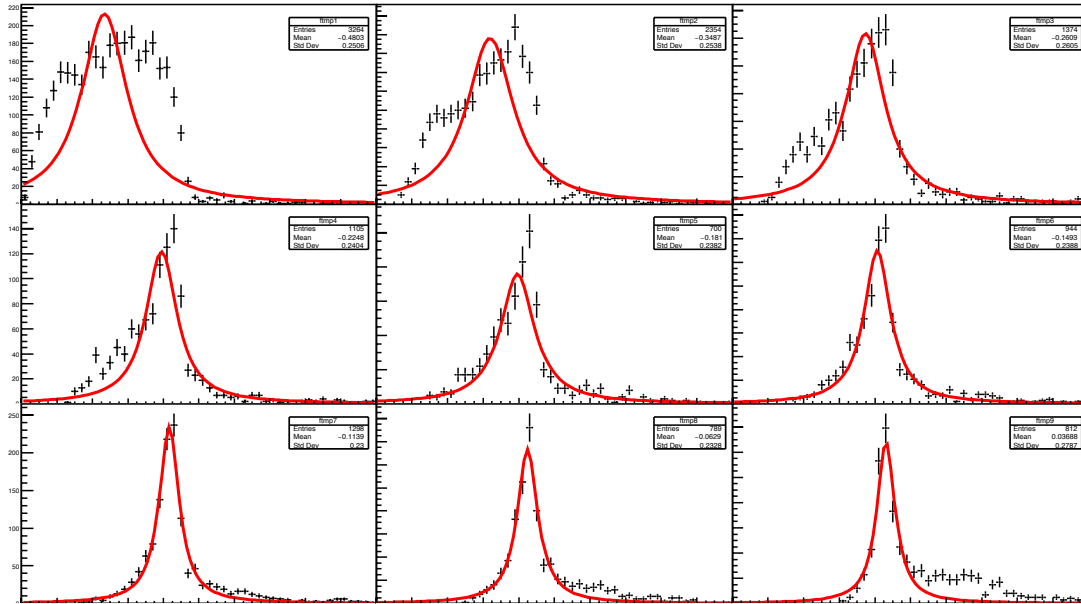


0.0-0.7 GeV in 9 unequal bins

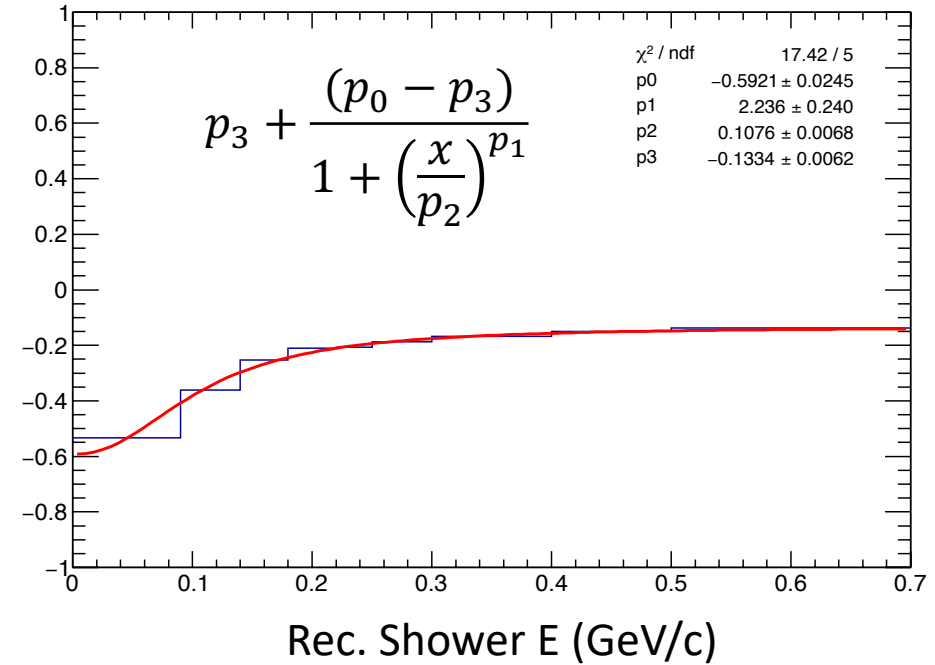
- ❖ For the energy < 0.18 GeV, the fractional bias distribution cannot be fitted by a Cauchy function
- ❖ Still have very poor resolution in low energy region

Shower Energy Correction

- ❖ A MC-driven method can be used to correct the bias in the reconstruction.



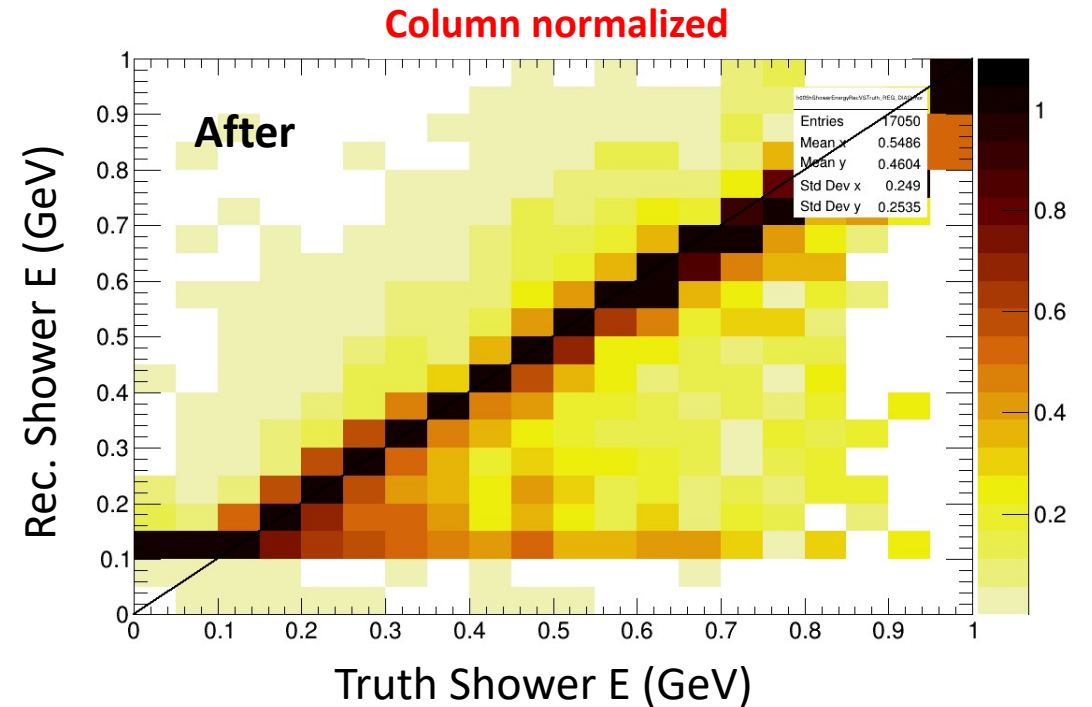
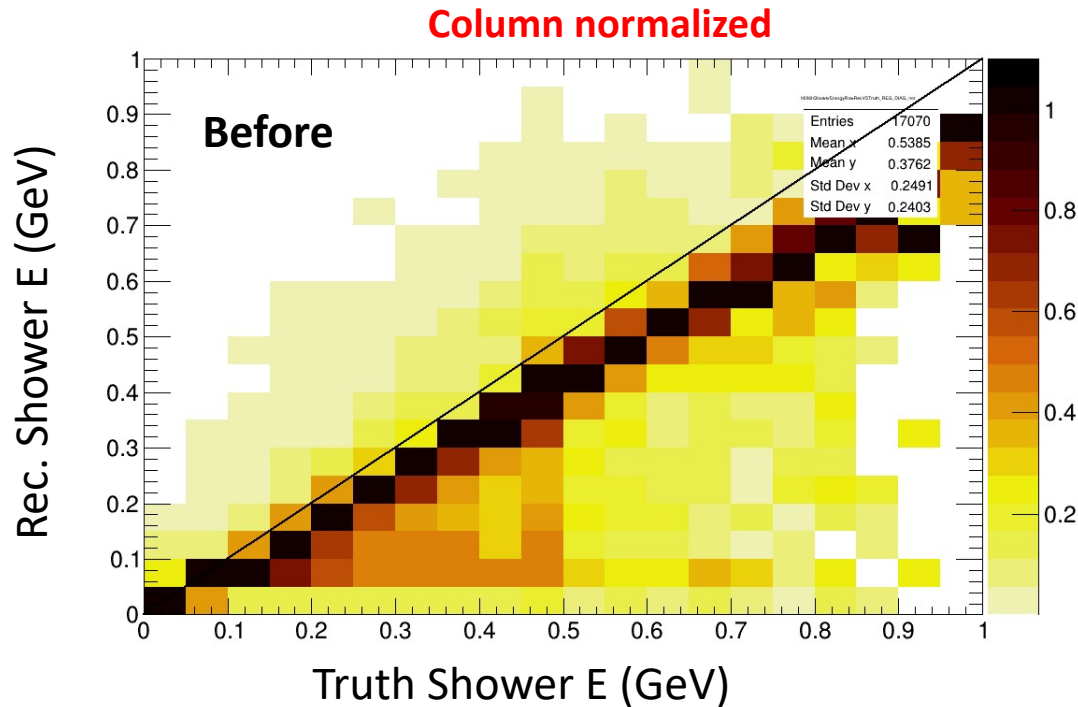
Rec./Truth -1



0.0-0.7 GeV in 9 unequal bins

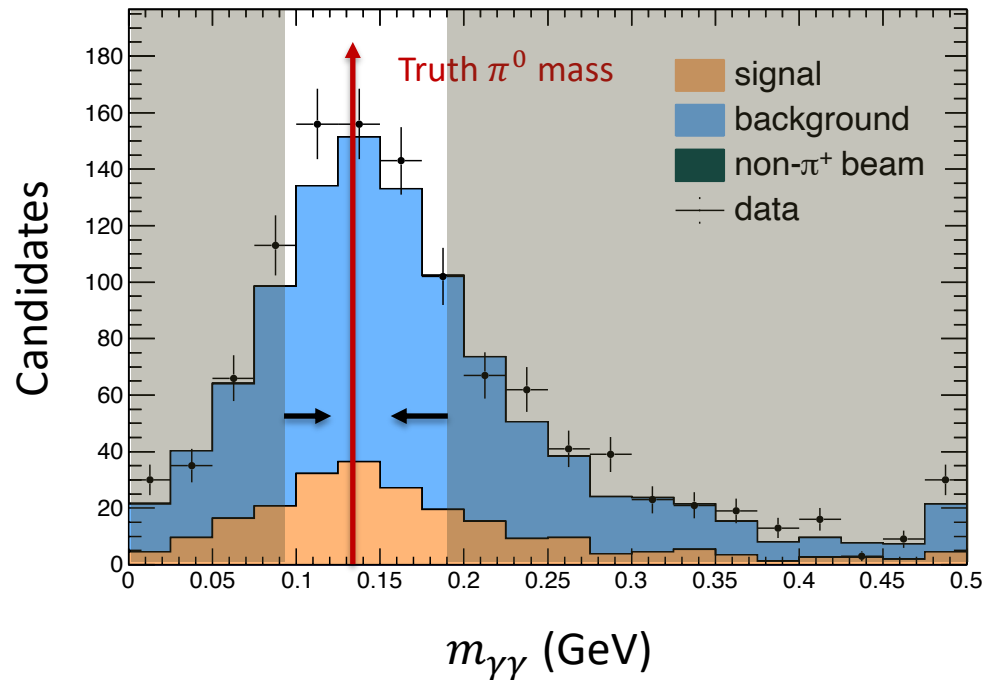
- ❖ For the energy < 0.18 GeV, the fractional bias distribution cannot be fitted by a Cauchy function
- ❖ Still have very poor resolution in low energy region

Before/After Energy Correction



- ❖ After applying the energy correction for showers, the bias in the shower reconstruction is reduced.
- ❖ Correction function works well.

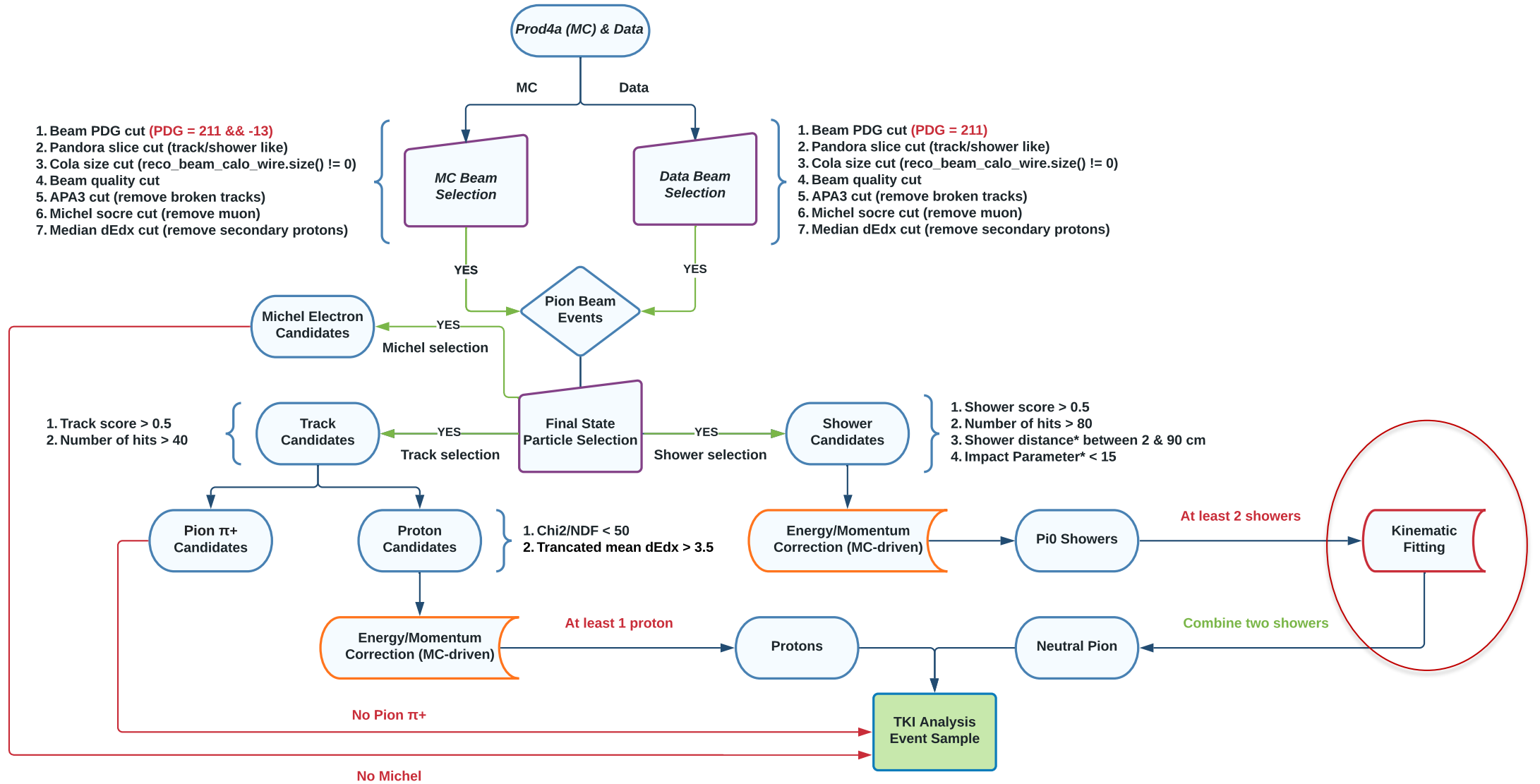
Reconstructed Neutral Pion



- The two photon invariant mass looks great after the energy correction.
- The spread in the mass distribution is quite large in signal
- Apply the kinematic fitting to further improve the shower energy or opening angles
- KF is used to improve the rec. π^0 momentum and energy

*See back-up slides (page 27) for signal definition

Analysis Flowchart



π^0 Kinematic Fitting

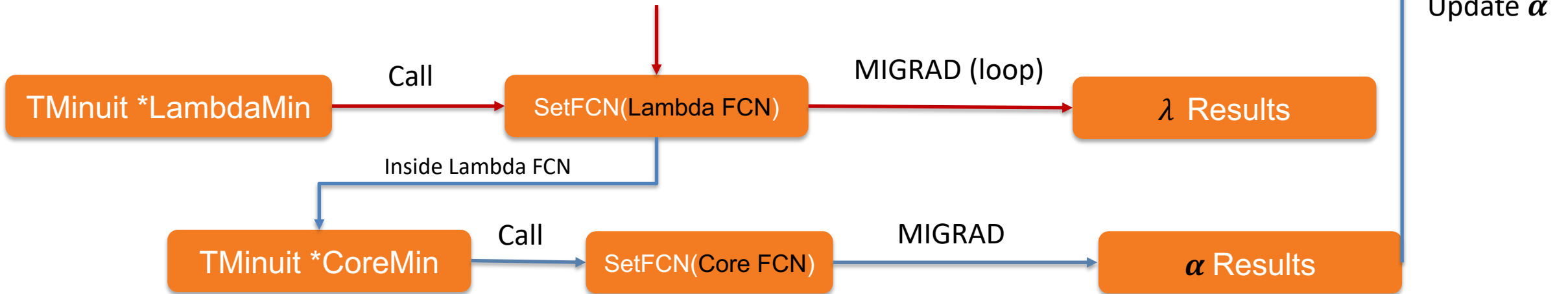
TMinuit Double Minimisation

$$\diamond m_{\gamma\gamma}^2 = 2E_1E_2(1 - \cos(\theta))$$

- We could use two TMinuit object to achieve the minimisation.
- We are using the “MIGRAD” algorithm.

Variables in red are varying in the process

$$\chi^2 = \lambda * \{2 * E_1E_2[1 - \cos(\theta)] - m_{\gamma\gamma}^2\} + (\alpha - \alpha_0)V_{\alpha_0}^{-1}(\alpha - \alpha_0)$$



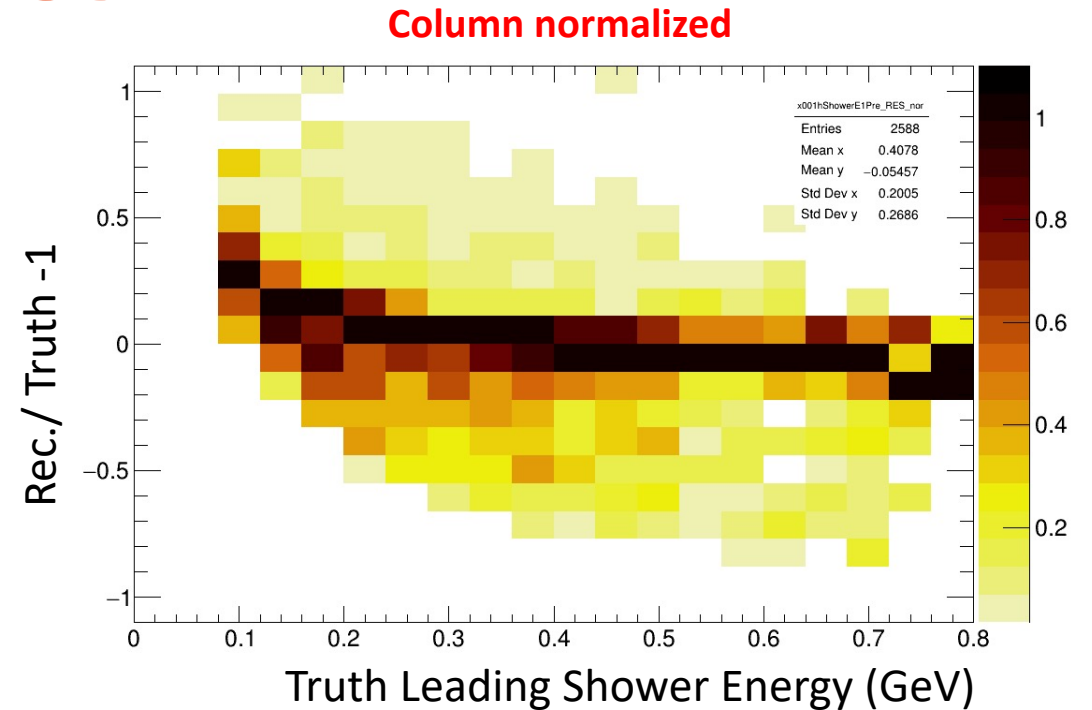
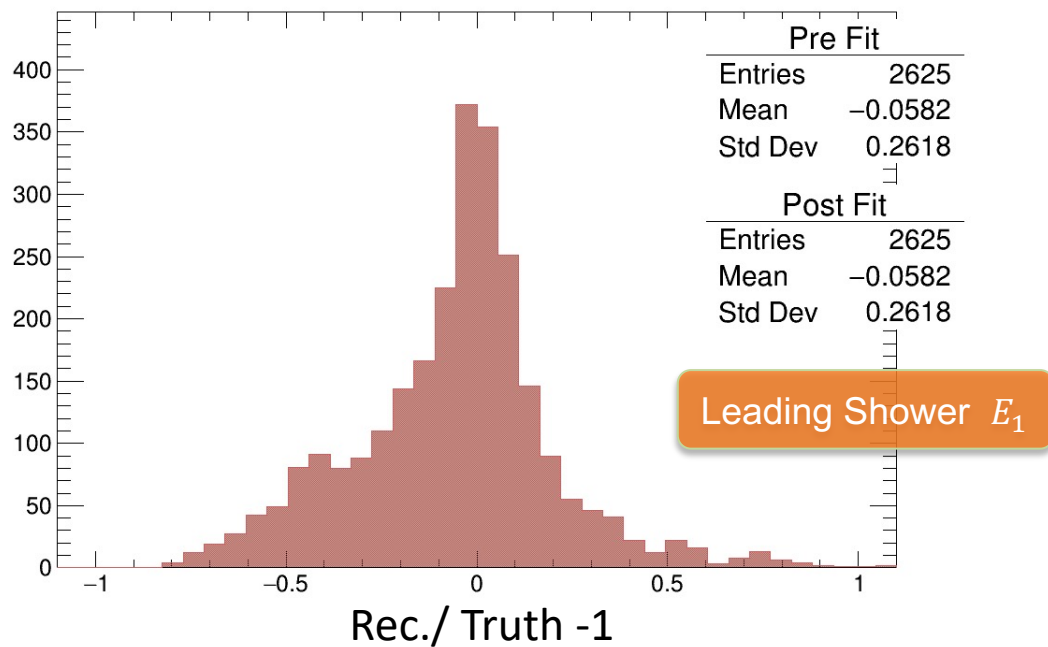
$$\chi^2 = \lambda * \{2 * E_1E_2[1 - \cos(\theta)] - m_{\gamma\gamma}^2\} + (\alpha - \alpha_0)V_{\alpha_0}^{-1}(\alpha - \alpha_0)$$

α : a vector of optimized variables

α_0 : a vector of the expected value of the measurements

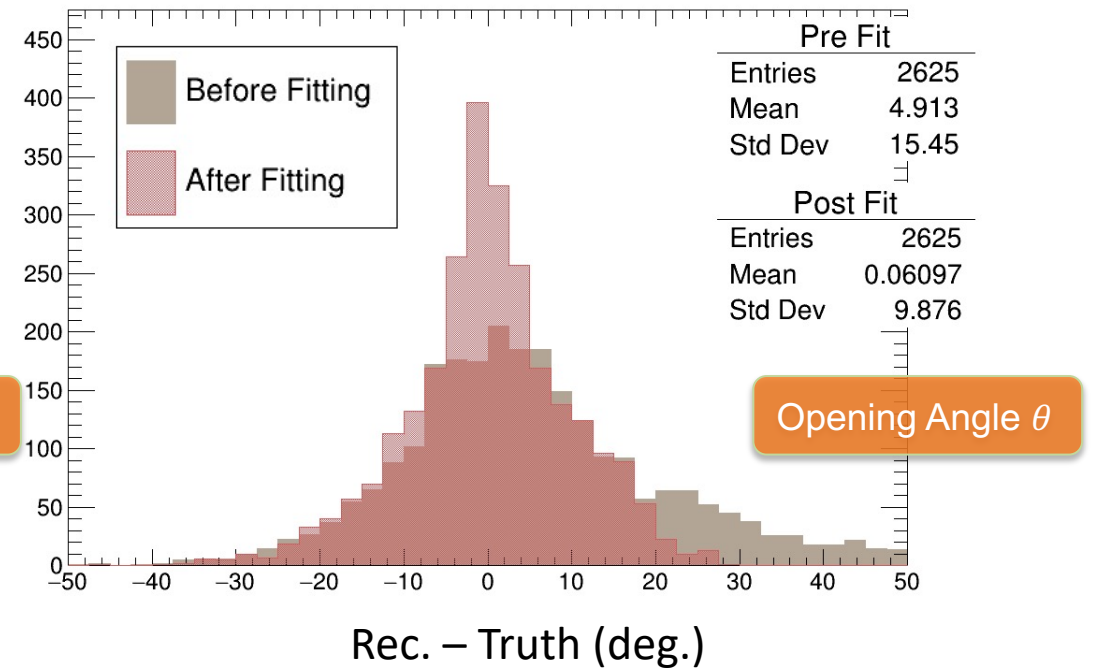
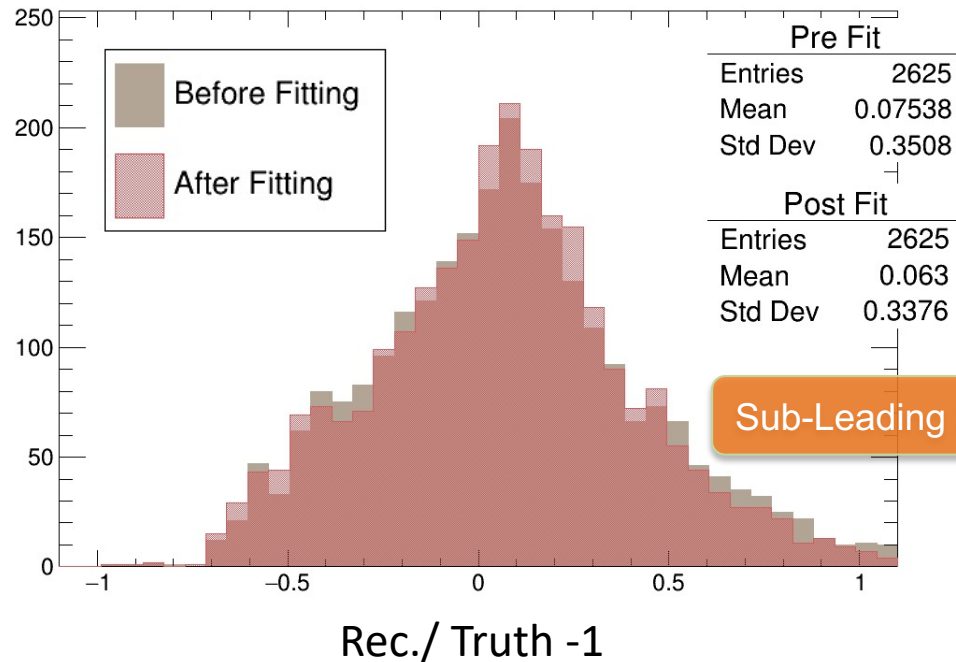
$$\alpha: [E_1, E_2, \theta]$$

Leading Shower Energy



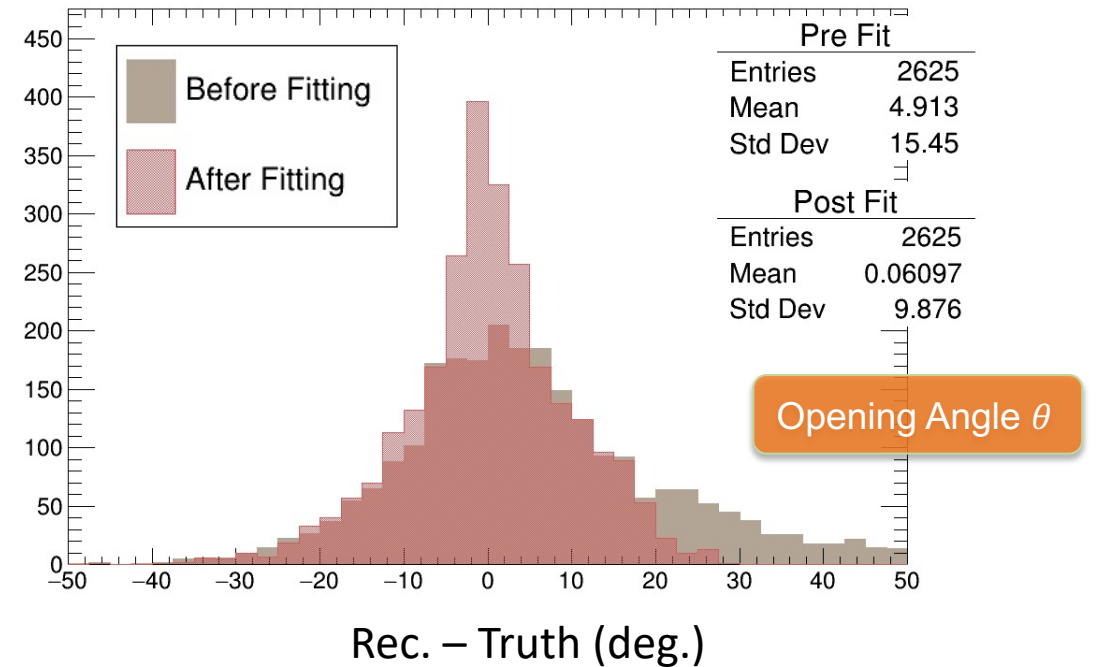
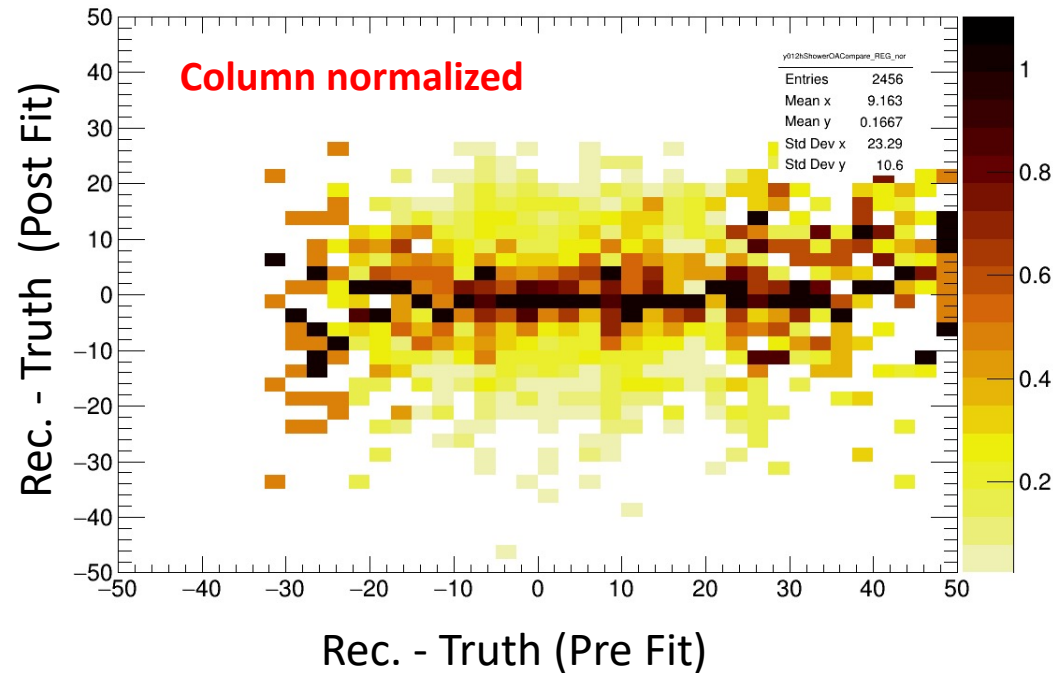
- ❖ The reconstructed leading shower energy is pretty good.
- ❖ Fix it in the process of kinematic fitting

Kinematic Fitting Results



- ❖ After the kinematic fitting, the opening angle between two shower vectors is improved a lot.
- ❖ Reconstruct π^0 using leading shower E and opening angle

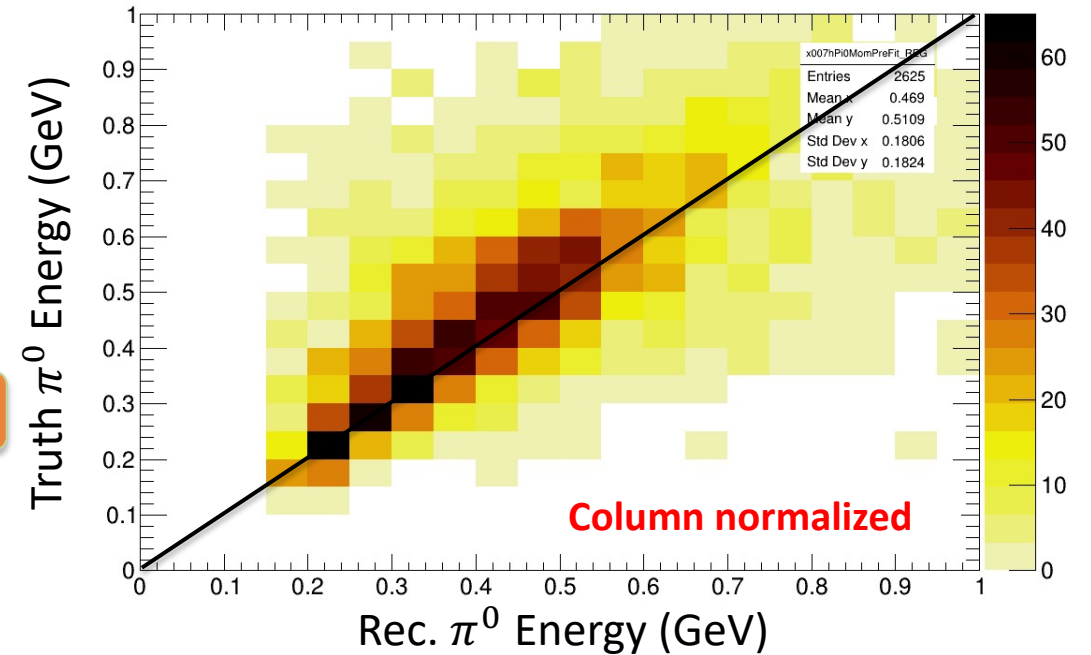
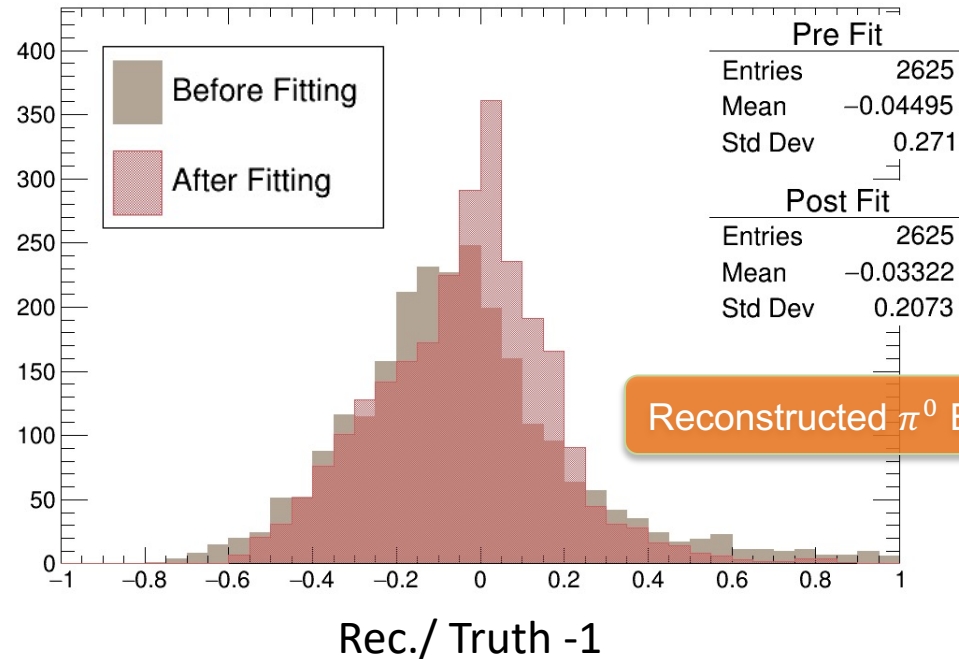
Kinematic Fitting Results



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- ❖ Reconstruct π^0 using leading shower E and opening angle

Reconstructed π^0 Energy

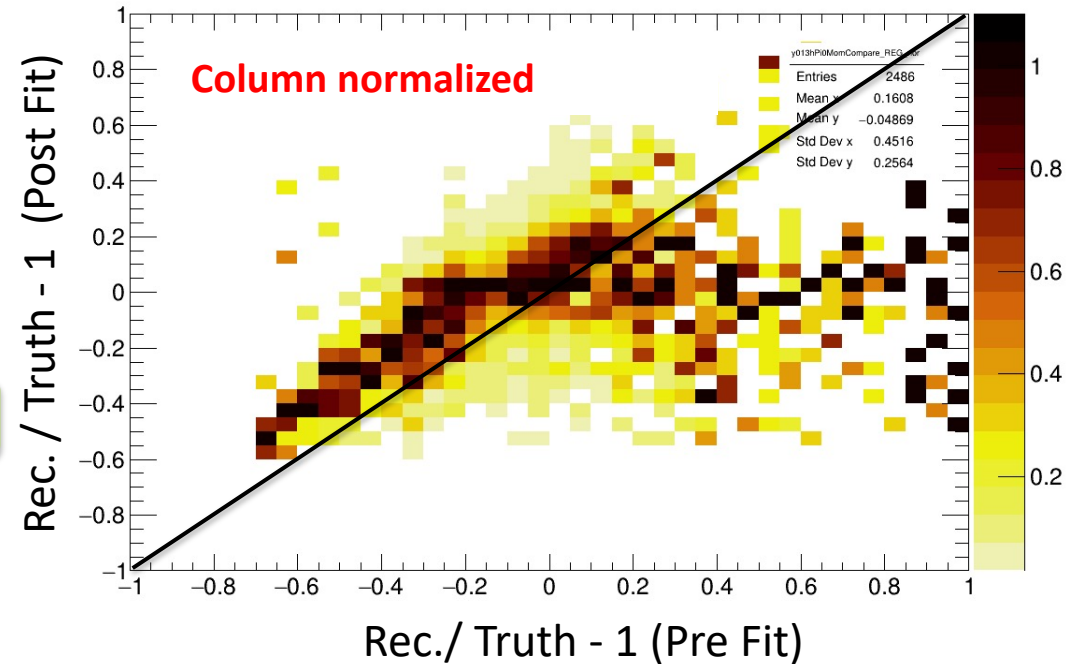
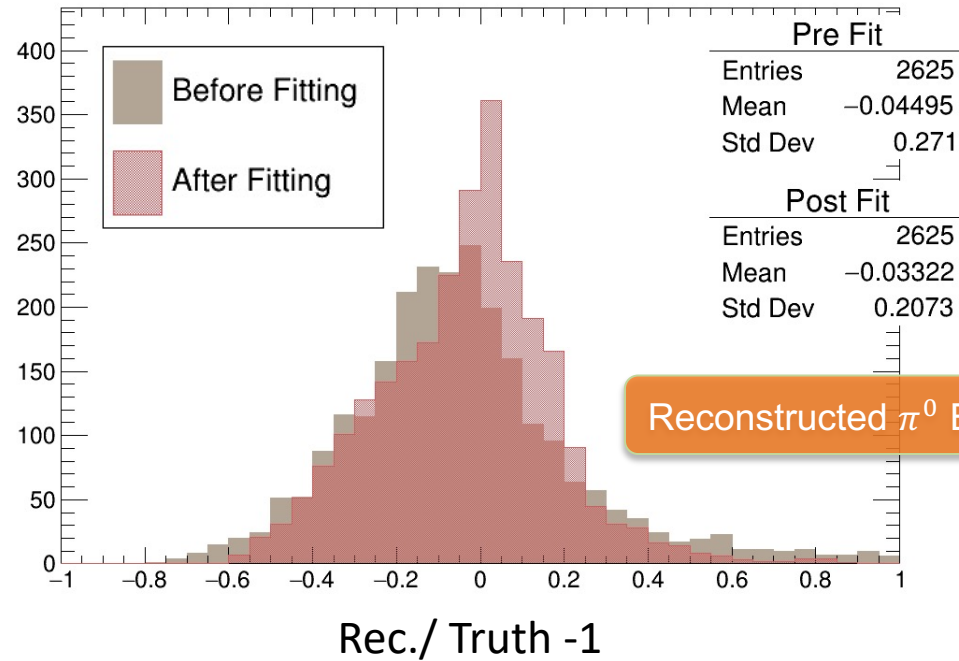
$$E_\pi = E_1 + \frac{m_{\pi^0}^2}{2E_1(1 - \cos\theta)}$$



- ❖ The reconstructed π^0 energy looks pretty good after the fitting
- ❖ The spread of the distribution is reduced and we have a sharper peak around 0.

Reconstructed π^0 Energy

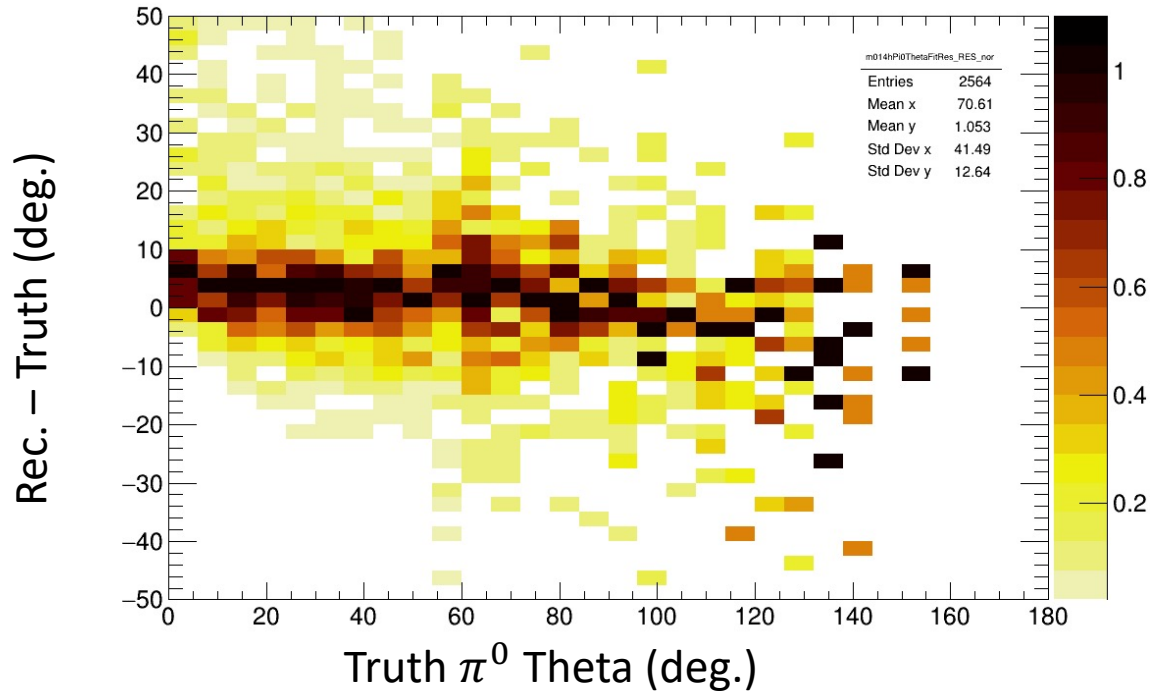
$$E_\pi = E_1 + \frac{m_{\pi^0}^2}{2E_1(1 - \cos\theta)}$$



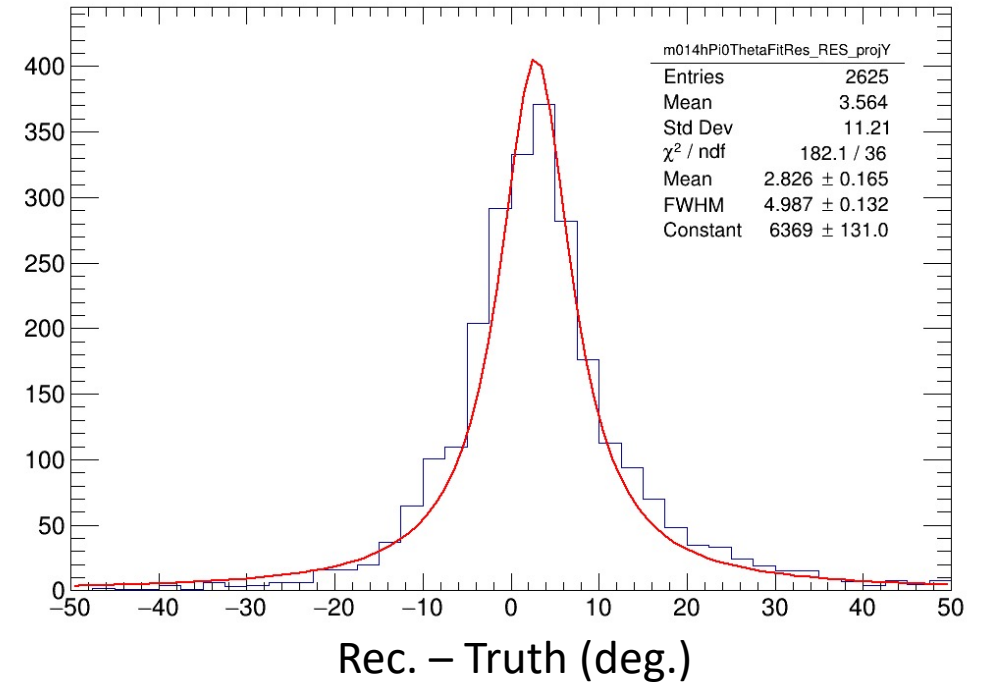
- ❖ The reconstructed π^0 energy looks pretty good after the fitting
- ❖ The spread of the distribution is reduced and we have a sharper peak around 0.

Rec. π^0 Theta θ (Detector coordinates)

Column normalized



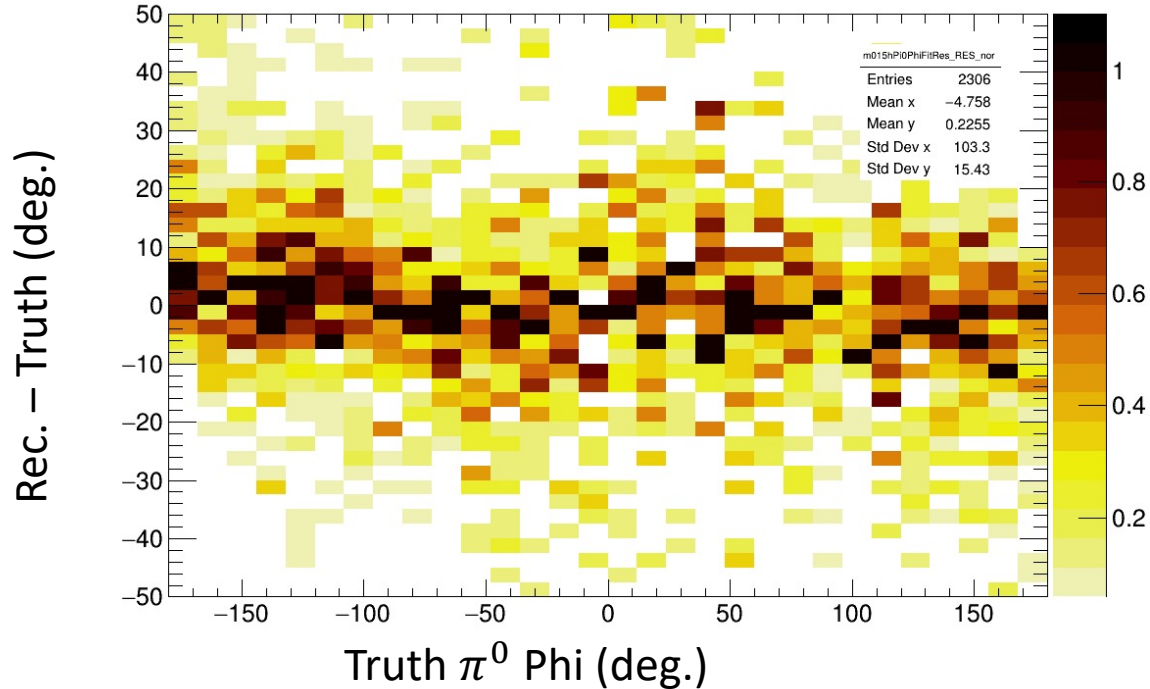
Y Projection



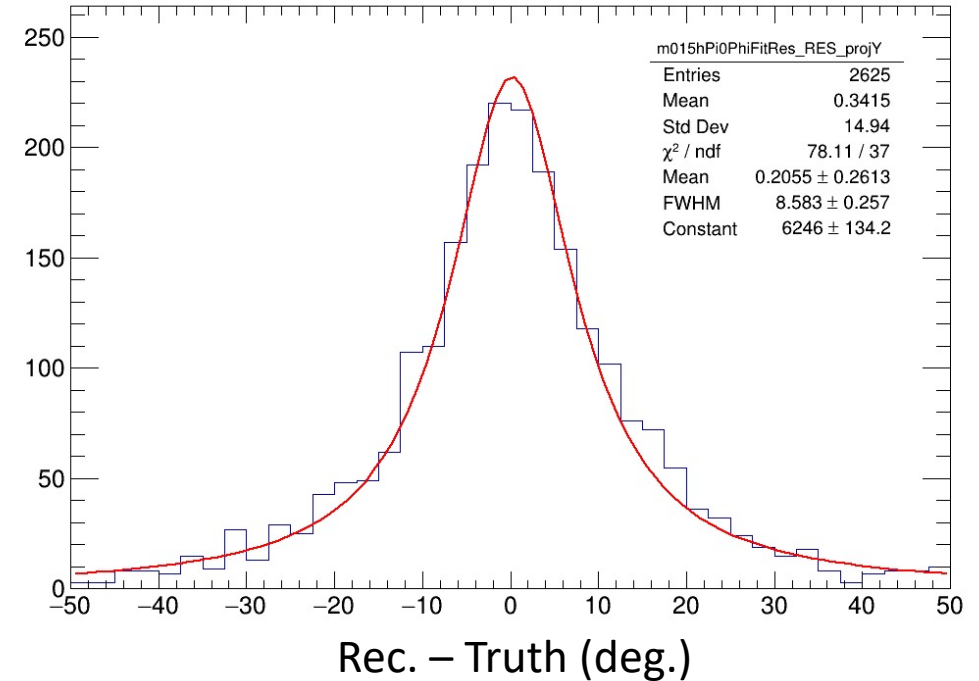
- ❖ The reconstructed π^0 theta θ (detector coordinates) has a $\sim 3^\circ$ bias
- ❖ Need to think about how to use the improved opening angle values to corrected the π^0 momentum vector (i.e. it's direction)

Rec. π^0 Phi ϕ (Detector coordinates)

Column normalized



Y Projection



- ❖ The reconstructed π^0 phi ϕ (detector coordinates) has a $< 1^\circ$ bias
- ❖ Need to think about how to use the improved opening angle values to corrected the π^0 momentum vector (i.e. it's direction)

Summary and Outlook

- ❖ A MC based energy correction is applied for reconstructed shower candidates.
- ❖ π^0 mass reconstruction was improved after selecting good shower candidates and applying the energy correction.
- ❖ The opening angle between two shower vectors was improved by the kinematic fitting
- ❖ π^0 energy reconstruction was also improved if we calculating it using E_1 and θ .
- ❖ Can correct the rec. π^0 momentum vector from the improved opening angle θ
- ❖ Plan to apply all the presented procedures for all energy beams and make inclusive π^0 measurement ($\pi^+ + \text{Ar} \rightarrow \pi^0 + X$)

Thank you for your attention !

Back-up

MC Selections Efficiency

| Cuts | All | Selected | Fraction | Total Fraction |
|---------------------------------|--------|------------|----------|----------------|
| Pion Beam Selection | | | | |
| Beam PDG | 358929 | 205219 | 57.2% | 57.2% |
| Pandora Beam Type | 205219 | 174724 | 85.1% | 48.7% |
| Calo Size | 174724 | 171519 | 98.2% | 47.8% |
| Beam Quality | 171519 | 123403 | 71.9% | 34.3% |
| APA 3 | 123403 | 100303 | 81.3% | 28.0% |
| Michel Score | 100303 | 98272 | 98.0% | 27.4% |
| Mean dEdx | 98272 | 93871 | 95.5% | 26.1% |
| Event Topology Selection | | | | |
| Protons (≥ 1) | 93871 | 28712 | 30.6% | 8.00% |
| Showers (≥ 2) | 28712 | 947 | 3.3% | 0.26% |
| No Pion π^+ | 947 | 770 | 81.3% | 0.21% |
| No Michel electron | 770 | 710 | 92.2% | 0.20% |

Data Selections Efficiency

| Cuts | All | Selected | Fraction | Total Fraction |
|---------------------------------|---------|------------|----------|----------------|
| Pion Beam Selection | | | | |
| Beam PDG | 1192336 | 164415 | 13.8% | 13.8% |
| Pandora Beam Type | 164415 | 123906 | 75.4% | 10.4% |
| Calo Size | 123906 | 120507 | 97.3% | 10.1% |
| Beam Quality | 120507 | 82984 | 68.9% | 6.96% |
| APA 3 | 82984 | 63209 | 76.2% | 5.30% |
| Michel Score | 63209 | 61606 | 97.5% | 5.17% |
| Mean dEdx | 61606 | 57941 | 94.1% | 4.86% |
| Event Topology Selection | | | | |
| Protons (≥ 1) | 57941 | 16211 | 28.0% | 1.36% |
| Showers (≥ 2) | 16211 | 680 | 4.2% | 0.06% |
| No Pion π^+ | 680 | 563 | 82.8% | 0.05% |
| No Michel electron | 563 | 516 | 91.7% | 0.04% |

Truth Signal Definition

- Phase space cuts on protons and pions:

1. Leading proton momentum 0.45 - 1 GeV/c
2. Sub-leading proton momentum < 0.45 GeV/c
3. No cuts on pions

0.45 GeV/c is the reconstruction threshold, 1 GeV/c is limit where momentum by range is reliable

- Beam type and Event topology cuts:

1. Incoming π^+ beam
2. At least one proton
3. At least one π^0
4. No π^+
5. No background particles (π^- and kaons, doesn't care about neutrons and nucleus)

π^0 Decay Kinematics

- Invariant mass of two photons:

$$\diamond m_{\gamma\gamma}^2 = 2E_1E_2(1 - \cos(\theta))$$

- Minimizing (Full CVM):

$$\diamond \chi^2 = \lambda * \{2 * E_1E_2[1 - \cos(\theta)] - m_{\gamma\gamma}^2\} + (\alpha - \alpha_0)V_{\alpha_0}^{-1}(\alpha - \alpha_0)$$

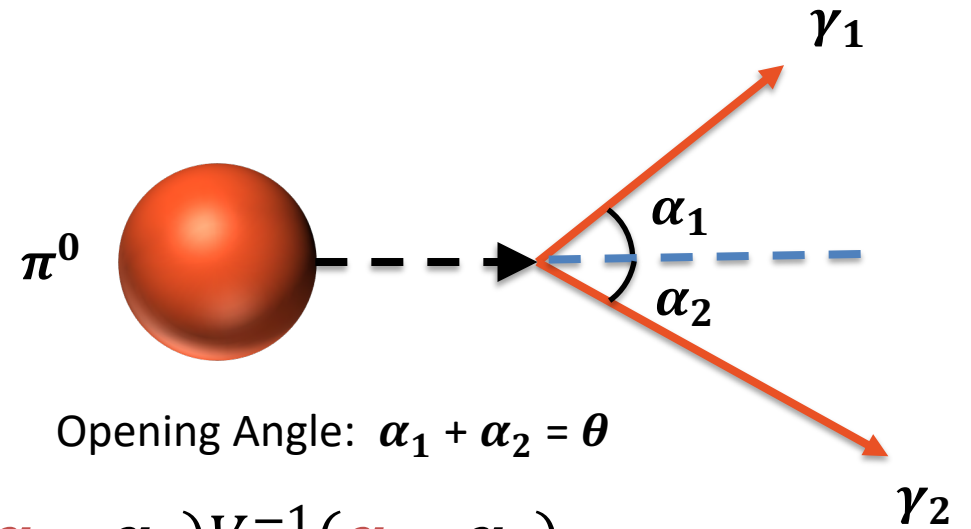
$$\diamond \text{where } \alpha = (E_1 \quad E_2 \quad \theta)$$

$$\diamond V_{\alpha_0}^{-1} \text{ is the inverse of the full CVM matrix}$$

- More familiar form (diagonal only CVM)

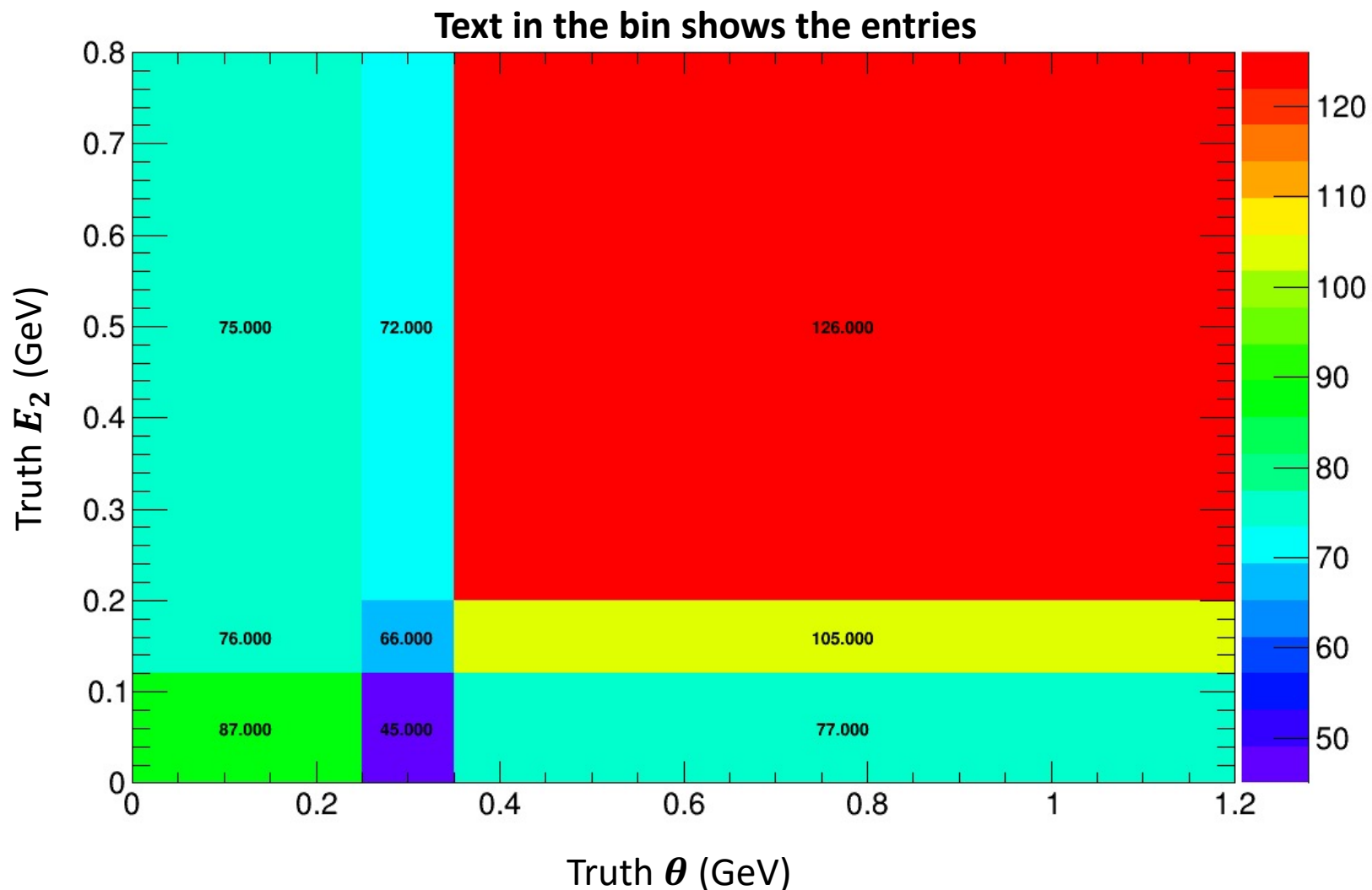
$$\diamond \chi^2 = \lambda * \{2 * E_1E_2[1 - \cos(\theta)] - m_{\gamma\gamma}^2\} + \sum_i (\alpha_i - \alpha_{0_i})^2 / \sigma_i^2$$

$$\diamond \text{we set the off diagonal elements to be 0}$$



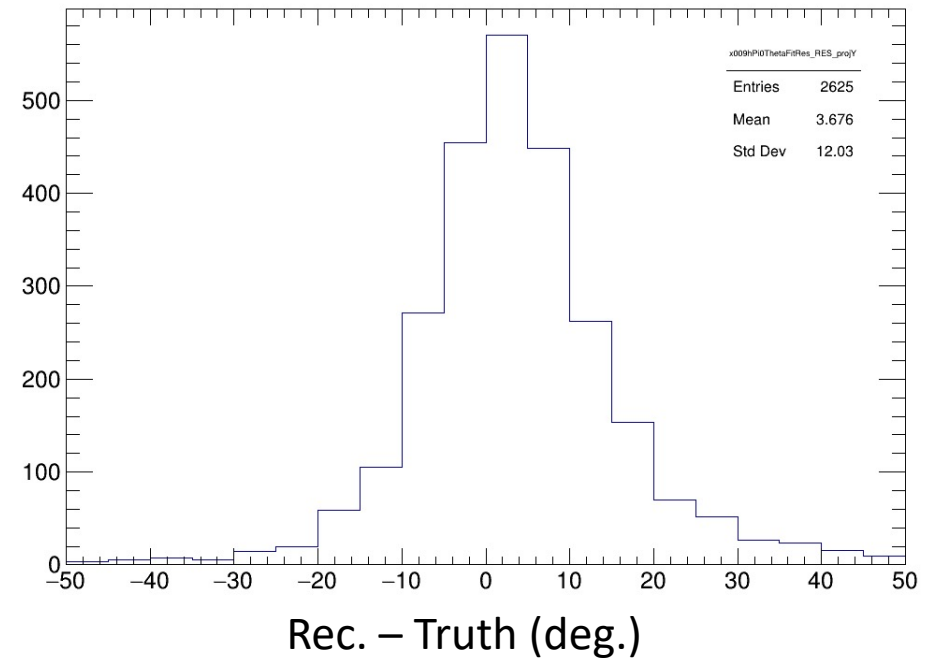
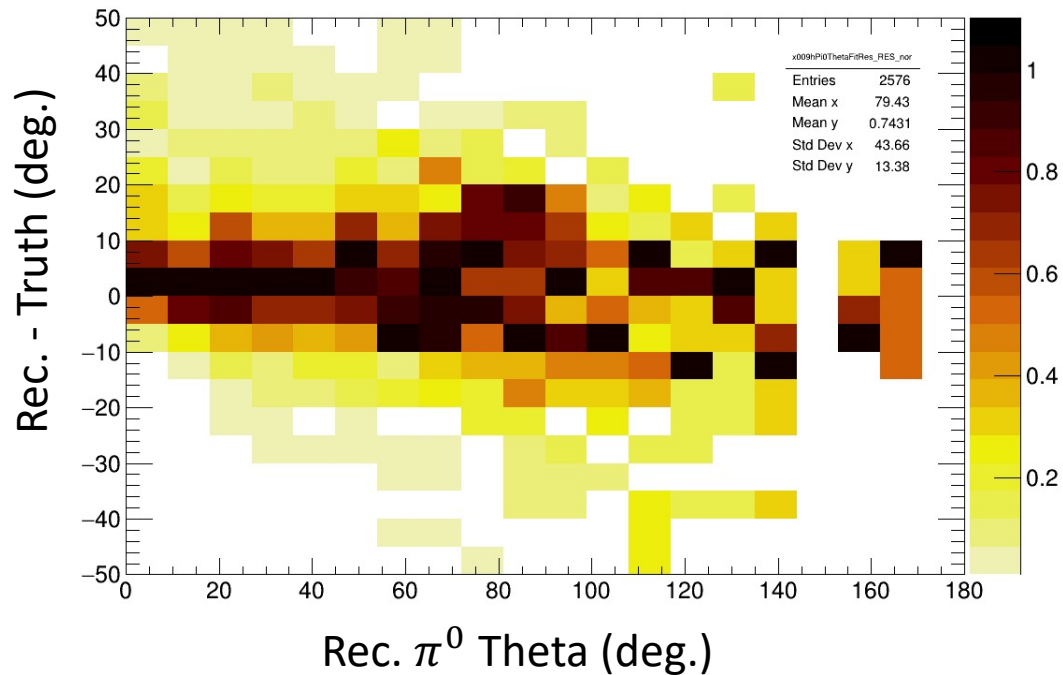
$$\alpha: [E_1, E_2, \theta]$$

Covariance Matrix



- Need to make sure the entries in each bin are similar.
- Each bin will have a set of rec. quantities and a set of truth quantities.
- The **expected value** of the measurements is the **mean** value of the truth distribution in that bin.
- For each bin, one can calculate the CVM.

Reconstructed π^0 Theta



- ❖ The reconstructed π^0 theta (relative to the beam) has a 3 - 4° bias
- ❖ Need to think about how to use the improved opening angle values to corrected the π^0 momentum vector (i.e. it's direction)