

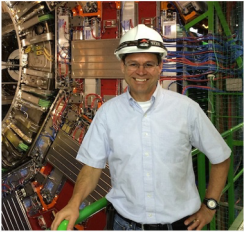
A Muon-Ion Collider at BNL

The future QCD frontier and path to a new energy frontier of $\mu^+\mu^-$ colliders

[arXiv:2107.02073](https://arxiv.org/abs/2107.02073)

Darin Acosta, Wei Li (Rice University)

Who we are



Darin Acosta: Particle Physicist on CMS (Higgs, Standard Model physics and BSM searches etc.), funded by US DOE-HEP; Previously on CDF at the Tevatron, and on ZEUS at HERA ([ep collider](#))



Wei Li: Nuclear Physicist on CMS (high-energy nuclear collisions, QCD in extreme densities), funded by US DOE-NP; also on STAR (and previously PHOBOS) at RHIC (AA collider) and emerging collaborations at EIC ([ep/eA collider](#))

There are many examples of successful synergies between HEP and NP in CMS in physics measurements, detector design, operations and upgrades
In chatting about the future of each other's fields, we recognize further opportunities to collaborate...

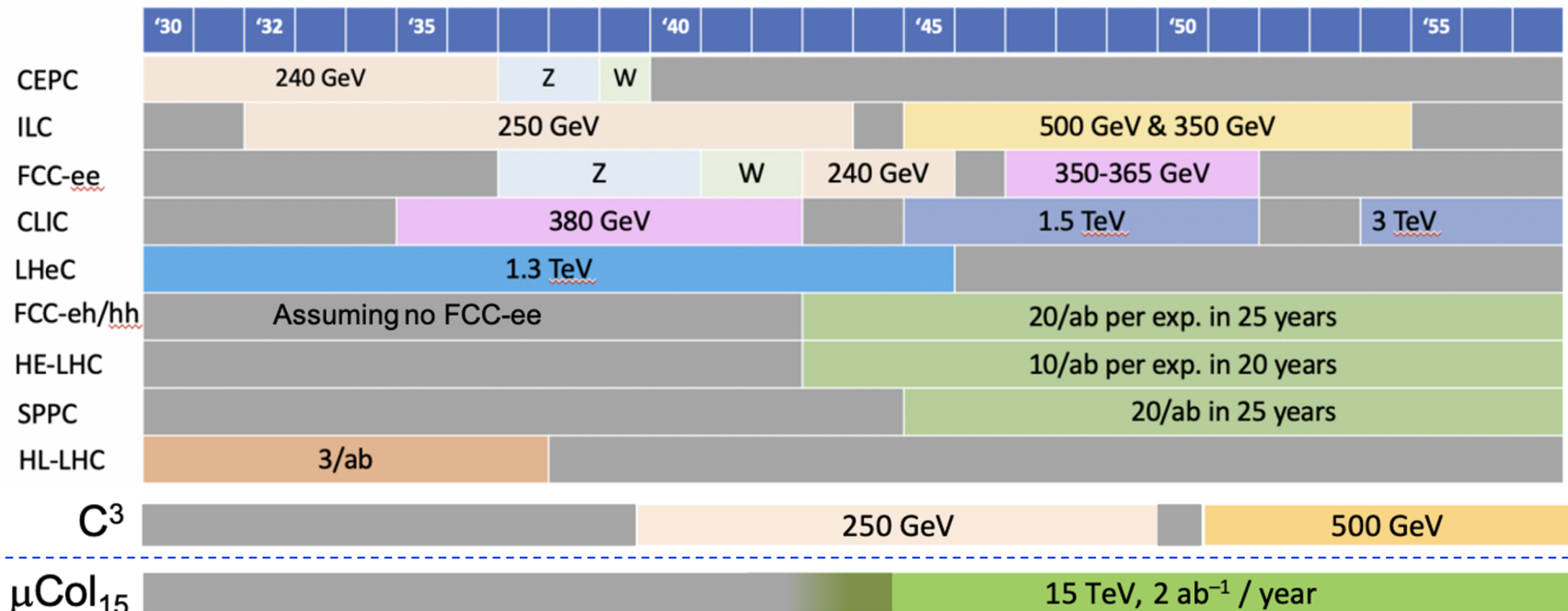
n.b. However neither of us is an accelerator expert...

Future of High Energy Physics Energy Frontier



- Many options for Higgs factories and energy frontier machines
- What would be an optimal and realistic path forward?

S. Dasu



Growing interests in muon colliders!

An Energy Frontier Muon Collider

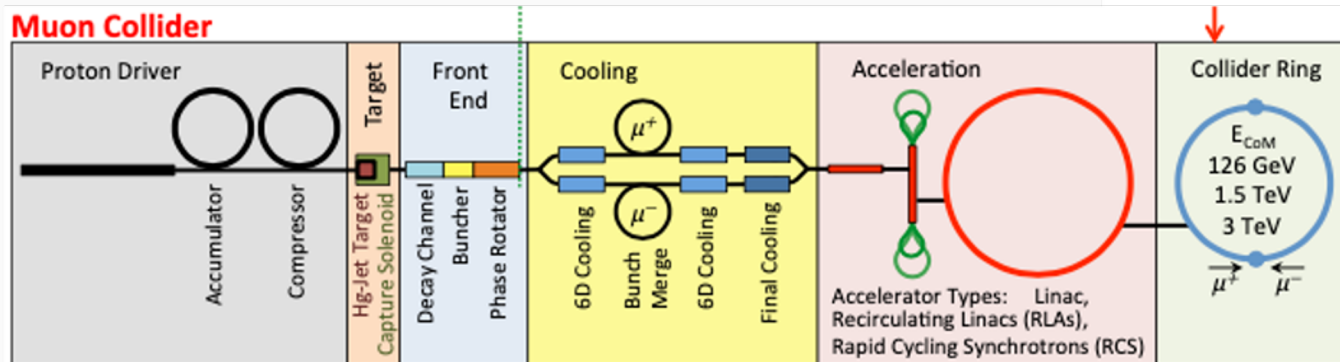
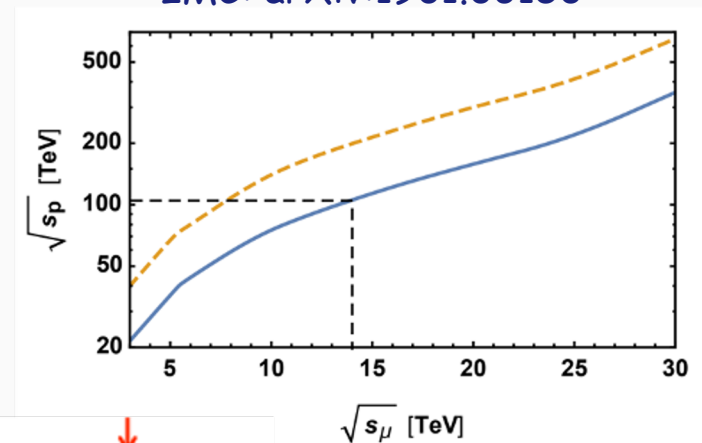


A more compact and innovative facility to incorporate the advantages of a high precision lepton collider and an energy frontier machine

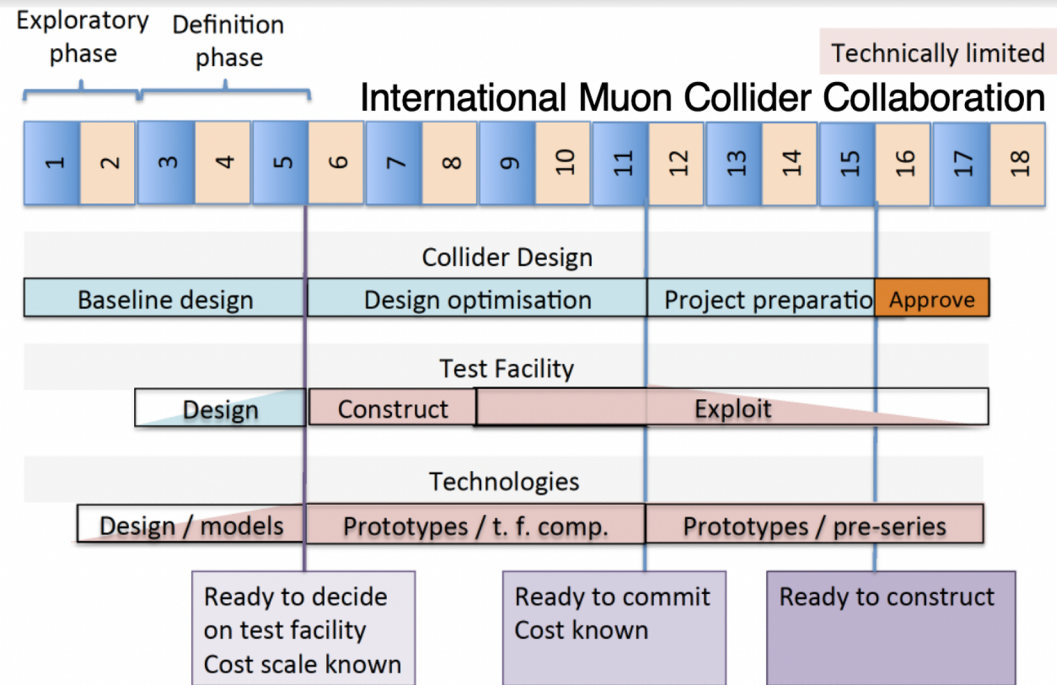
IMC: [arXiv:1901.06150](https://arxiv.org/abs/1901.06150)

An O(10) TeV muon collider has the equivalent mass reach to an O(100) TeV proton collider

But much R&D still to do...



Potential timeline of muon colliders



Physics potential along the way

D. Schulte

Ultimate Beam Limits, April 6, 2021

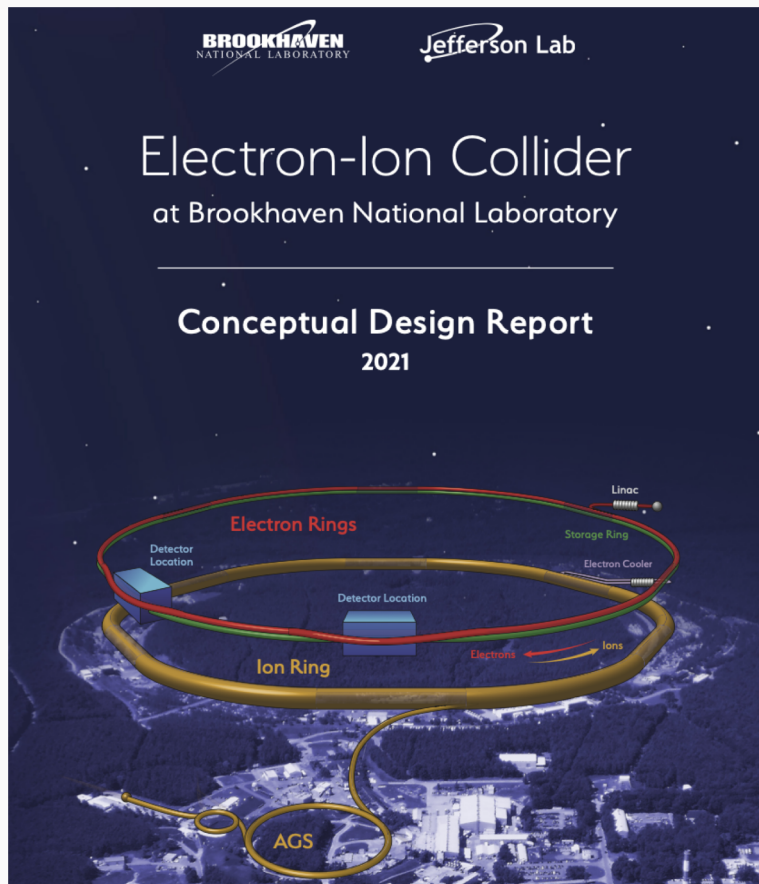
arXiv:1901.06150

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A vigorous and ambitious R&D program is needed to assess the feasibility of a tens-of-TeV's muon collider. Therefore it is important to investigate the physics potential of smaller-scale machines that might be built along the way as technology demonstrators. Starting from medium energy, the first option to be considered is a muon collider operating around the top production threshold (~ 400 GeV). This

A demonstrator with compelling science is needed before going to O(10+) TeV

The Electron-Ion Collider (EIC)



[EIC Conceptual Design Report](#) just released and project approved. Detector designs due this year.

Salient points:

- Hadron beam energy up to 275 GeV (increase from RHIC)
- Electron beam energy up to 18 GeV
- $\sqrt{s} = 20 - 140$ GeV
- Luminosity $10^{33} - 10^{34}$ Hz/cm²
- Polarized electron, proton and ion beams (any)
- Design supports 2 detectors, only one in project scope

Physics goals:

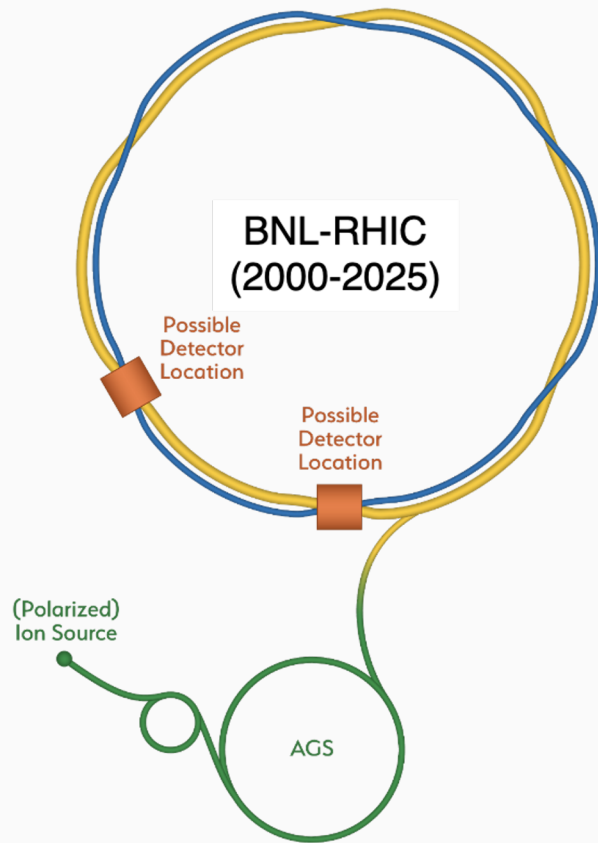
- ep and eN deep inelastic scattering
- Nucleon spin structure
- Gluon saturation scale (Q_s)

Electron-Ion Collider at BNL

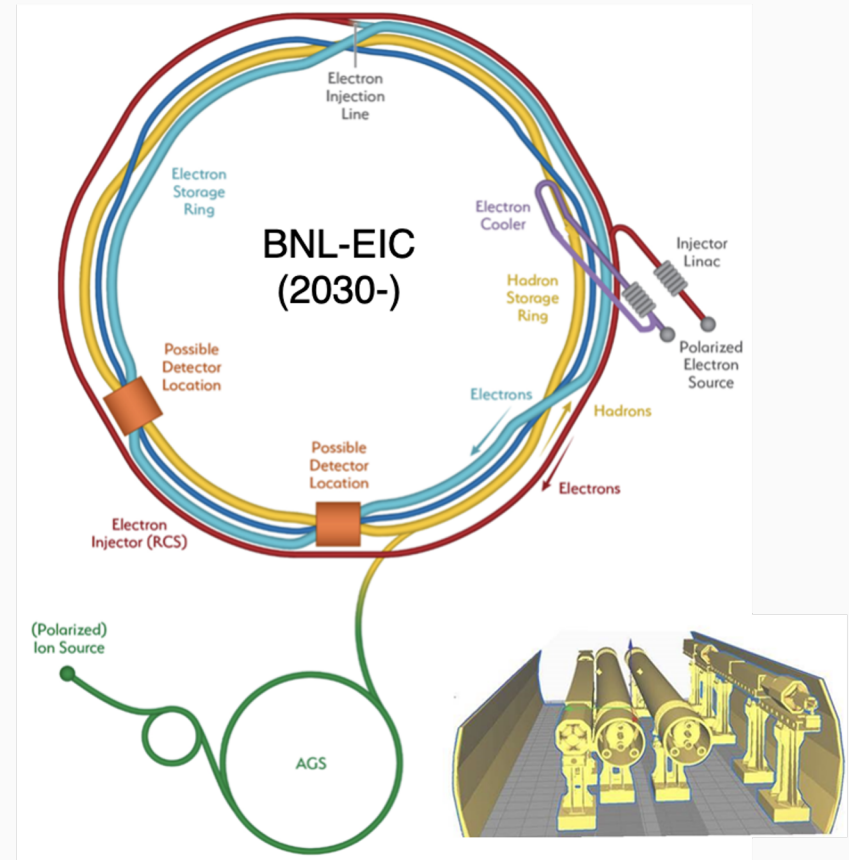


RHIC: pp, pA, AA up to 500 GeV

EIC: ep, eA up to 140 GeV



upgrade
➔



Electron-Ion Collider at BNL



One of hadron storage rings is re-used.

EIC: ep, eA up to 140 GeV

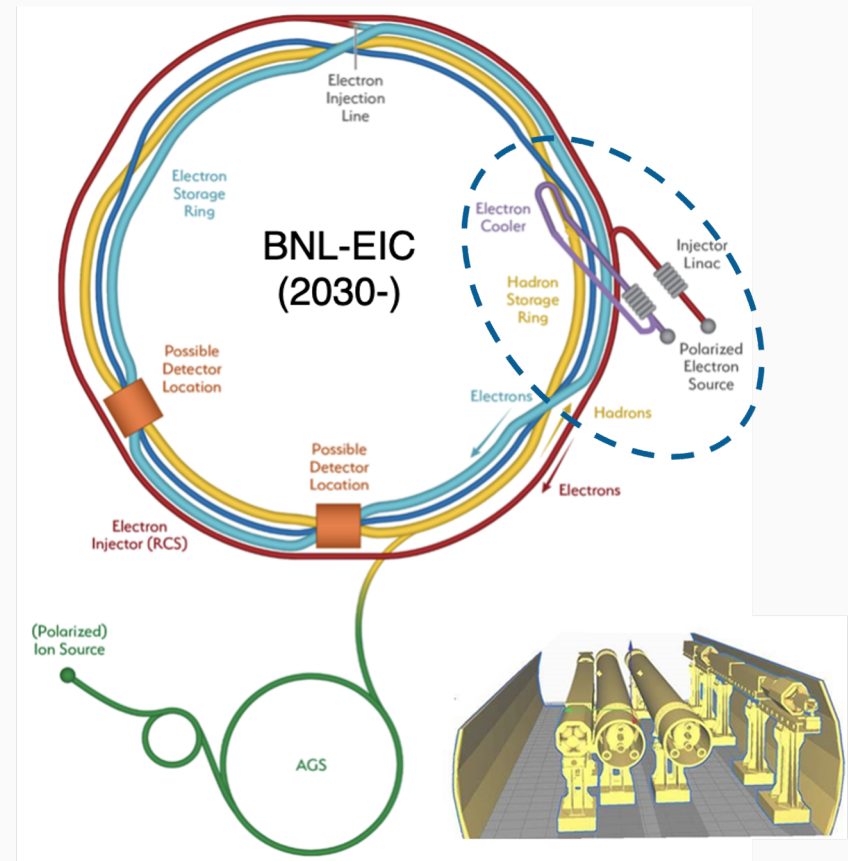
RHIC infrastructure (existing tunnel) is re-used as much as possible.

Additions to RHIC:

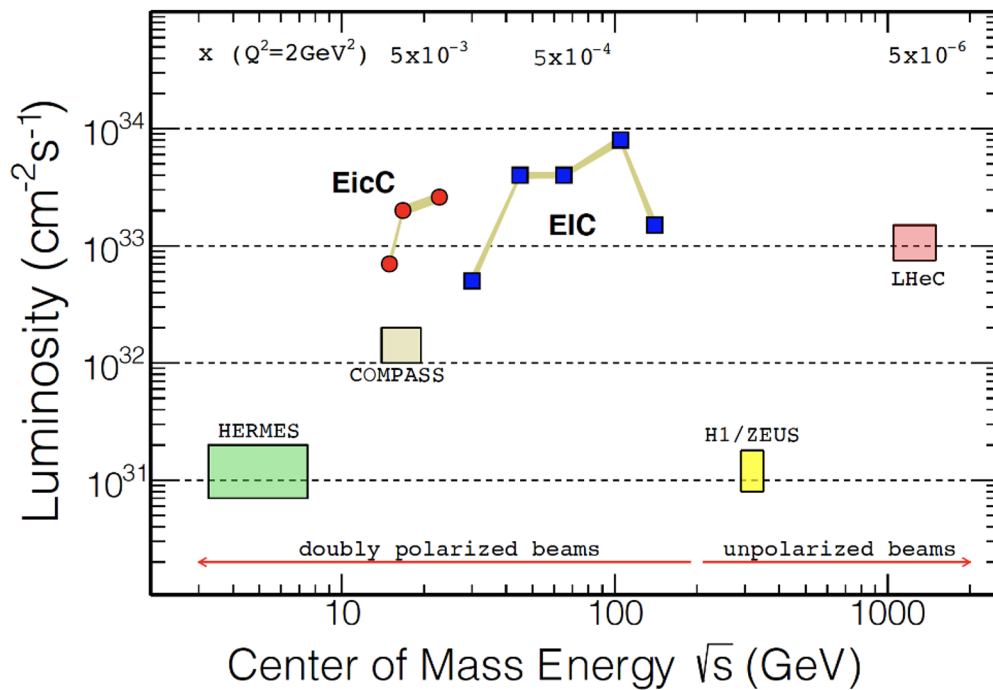
- Polarized electron source
- LINAC
- Rapid-cycling synchrotron (RCS) in the RHIC tunnel.
- A new electron storage ring in the RHIC tunnel.

Cost: \$1.6-2.6B (DOE-NP).

- U.S. accounting, including detectors



Lumi vs. \sqrt{s} at lepton-hadron colliders



HERA at DESY – high energy but low luminosity, unpolarized or singly polarized (*)

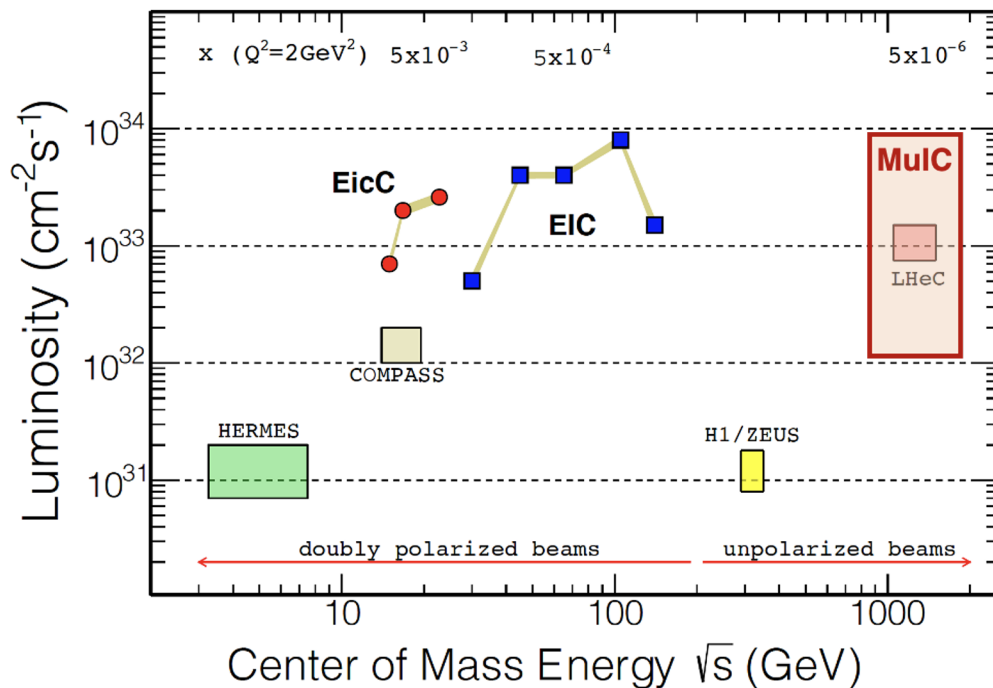
EIC at BNL – lowish energy but high luminosity, doubly polarized, ions

What's after EIC?

- LHeC (arXiv:2007.14491)?

(*) HERA-II did achieve longitudinally polarized electron beams

DIS at lepton-hadron colliders



HERA at DESY – high energy but low luminosity, unpolarized

EIC at BNL – lowish energy but high luminosity, doubly polarized, ions

What's after EIC?

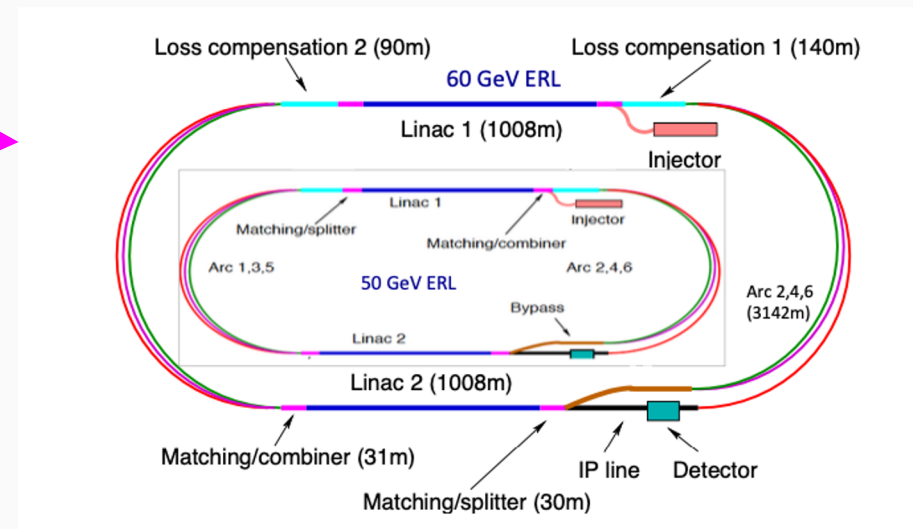
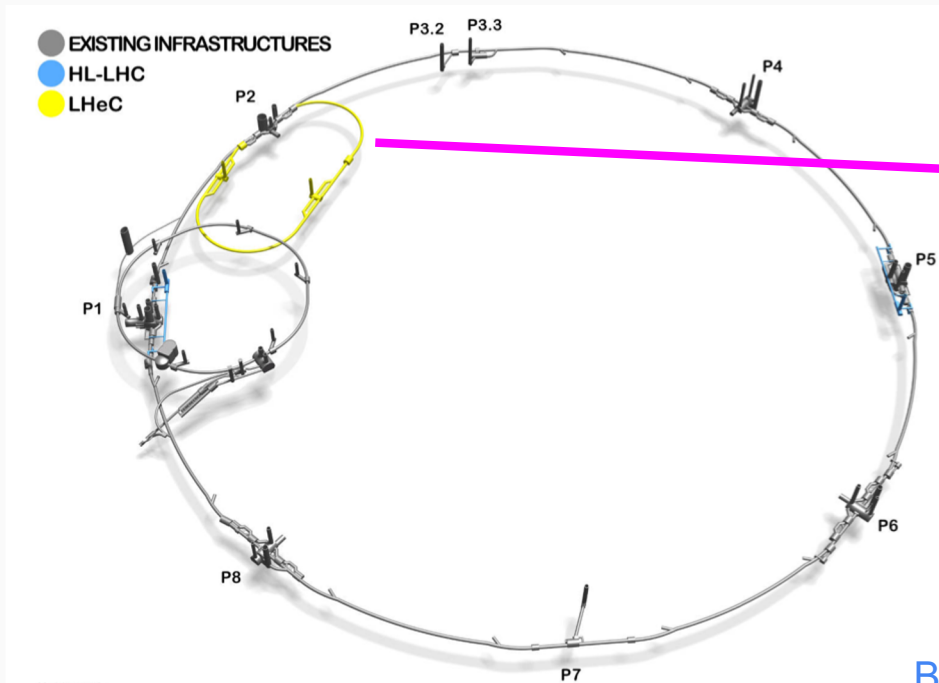
- LHeC ([arXiv:2007.14491](https://arxiv.org/abs/2007.14491))?
- **Muon-Ion Collider at BNL!**
(esp. with polarized muons)

One Approach: the Large Hadron Electron Collider



- **LHeC: 50 – 60 GeV e⁻ on 7 TeV p** ($\sqrt{s} = 1.2\text{--}1.3\text{ TeV}$)
 - Two oppositely directed linacs and 3 arcs
 - Two design options: 50 GeV (smaller) vs. 60 GeV (larger, more expensive)

LHeC: [arXiv:2007.14491](https://arxiv.org/abs/2007.14491)



But how realistic is this option for the HL-LHC timescale?

A Muon-Ion Collider: Who Ordered That?



Probe a **new energy scale** and nucleon momentum fraction in Deep Inelastic Scattering using a relatively compact machine

- $\sqrt{s} \sim 1 \text{ TeV}$
 - Q^2 up to 10^6 GeV^2
 - x as low as 10^{-6}
- } **An order of magnitude beyond the HERA ep collider**

Build a science case for a TeV muon storage ring as a demonstrator toward a multi-TeV $\mu^+\mu^-$ collider

- QCD and hadron/nucleon structure in new regimes
- Higgs, Top, BSM

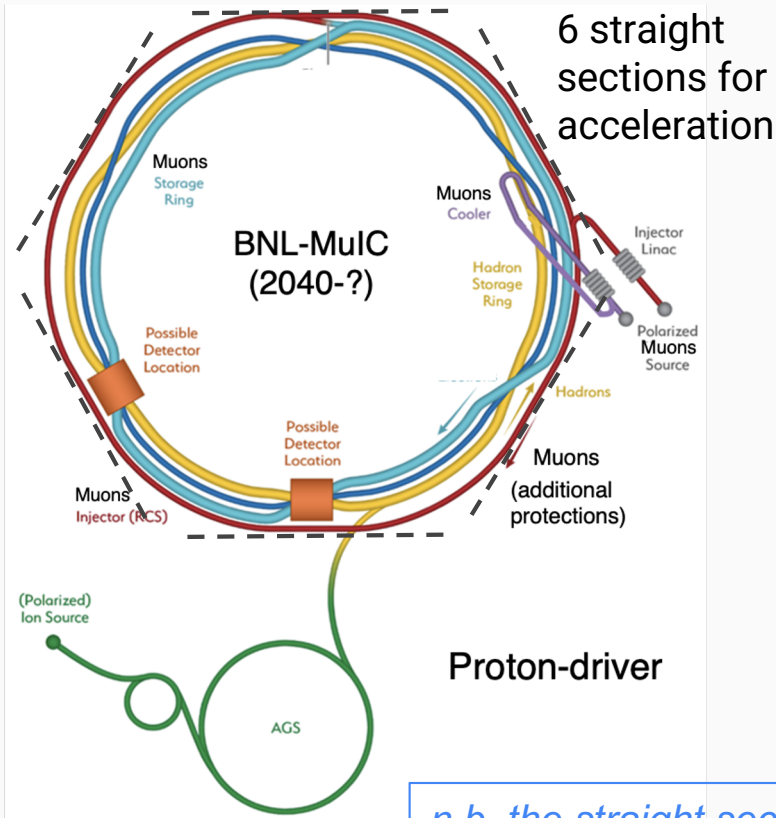
Facilitate the **collaboration of the nuclear and particle physics communities** around an innovative and forward-looking machine

Re-use existing facilities at BNL (MuIC as an upgrade to the EIC)

Muon-Ion Collider at BNL



replace e by μ beam



Bending radius of RHIC tunnel: $r = 290\text{m}$

Achievable muon beam energy: $0.3Br$

Parameter	1 (aggressive)	2 (realistic)	3 (conservative)
Muon energy (TeV)	1.39	0.96	0.73
Muon bending magnets (T)	16 (FCC)	11 (HL-LHC)	8.4 (LHC)
Muon bending radius (m)		290	
Proton (Au) energy (TeV)		0.275 (0.11/nucleon)	
CoM energy (TeV)	1.24 (0.78)	1.03 (0.65)	0.9 (0.57)

7-8X increase over top EIC energy

If $E_p \rightarrow 0.96\text{ TeV}$, $\sqrt{s} \rightarrow 1.9\text{ TeV}$

n.b. the straight sections would provide collimated beams of neutrinos as well

Muon-Ion Collider at BNL



Luminosity estimate:

$$f_c^\mu = f_{\text{rep}} * N_c$$

$$\mathcal{L}_{\mu p} = \frac{N^\mu N^p}{4\pi \max[\sigma_x^\mu, \sigma_x^p] \max[\sigma_y^\mu, \sigma_y^p]} \min[f_c^\mu, f_c^p] H_{hg}$$

arXiv:1905.05564

Parameter	Muon	Proton
Energy (TeV)	0.96	0.275
CoM energy (TeV)	1.03	
Bunch intensity (10 ¹¹)	20	3
Norm. emittance, ε _{x,y} (μm)	25	0.2
β* _{x,y} @IP (cm)	1	5
Trans. RMS beam size, σ _{x,y} (μm)	5.2	5.8
Muon repetition rate, f _{rep} (Hz)	15	
Cycles/Collisions per muon bunch, N _c	3279 (~300B)	
L _{μp} (10 ³³ cm ⁻² s ⁻¹)	7	

Muon beam (MAP):

[arXiv:1901.06150](https://arxiv.org/abs/1901.06150)

Table 1: Main parameters of the proton driver muon facilities

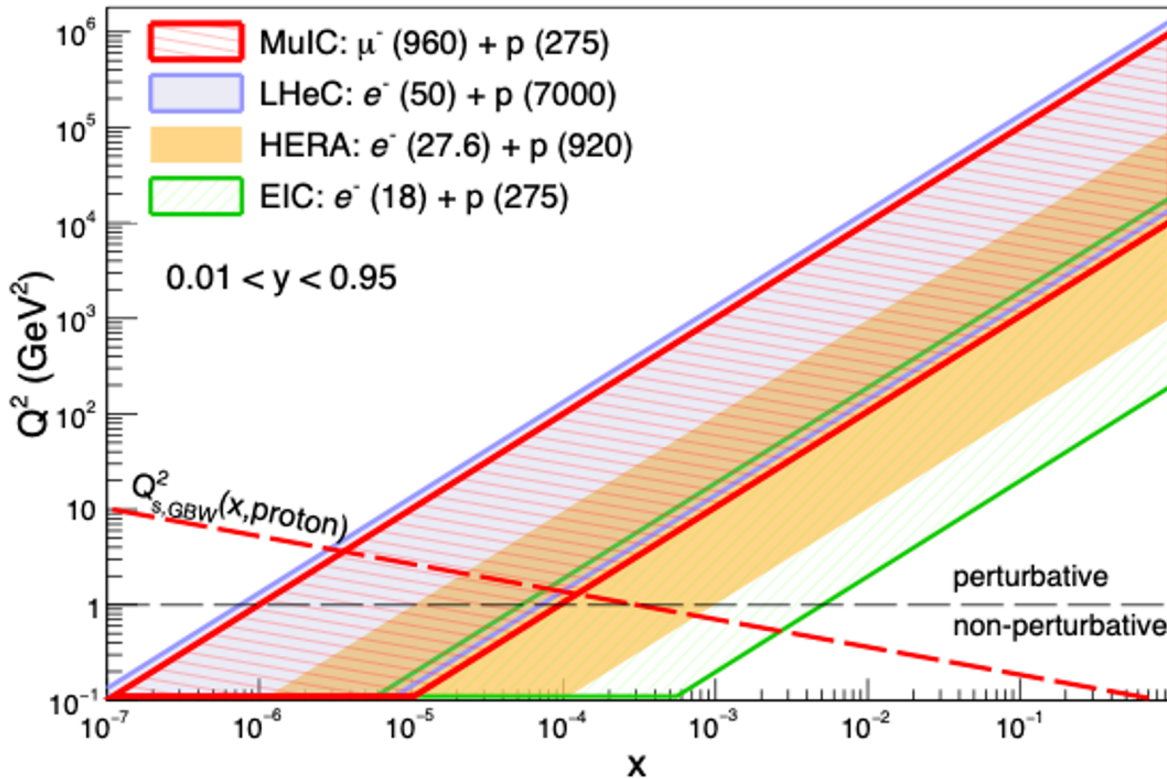
Parameter	Units	Higgs	↓	Multi-TeV	
CoM Energy	TeV	0.126	1.5	3.0	6.0
Avg. Luminosity	10 ³⁴ cm ⁻² s ⁻¹	0.008	1.25	4.4	12
Beam Energy Spread	%	0.004	0.1	0.1	0.1
Higgs Production/10 ⁷ sec		13'500	37'500	200'000	820'000
Circumference	km	0.3	2.5	4.5	6
No. of IP's		1	2	2	2
Repetition Rate	Hz	15	15	12	6
β* _{x,y}	cm	1.7	1	0.5	0.25
No. muons/bunch	10 ¹²	4	2	2	2
Norm. Trans. Emittance, ε _{TN}	μm-rad	200	25	25	25
Norm. Long. Emittance, ε _{LN}	μm-rad	1.5	70	70	70
Bunch Length, σ _S	cm	6.3	1	0.5	0.2
Proton Driver Power	MW	4	4	4	1.6
Wall Plug Power	MW	200	216	230	270

Polarized proton beam from eRHIC/EIC

[arXiv:1409.1633](https://arxiv.org/abs/1409.1633)

And the more experimental interaction points, the better before the muons decay...

Q²-x Reach Comparison: e(μ)-p Scattering



Well beyond the coverage of the EIC and HERA

Similar coverage to the proposed Large Hadron Electron Collider **LHeC** [1]

Polarized beams

Potential to see gluon saturation [2] in the proton

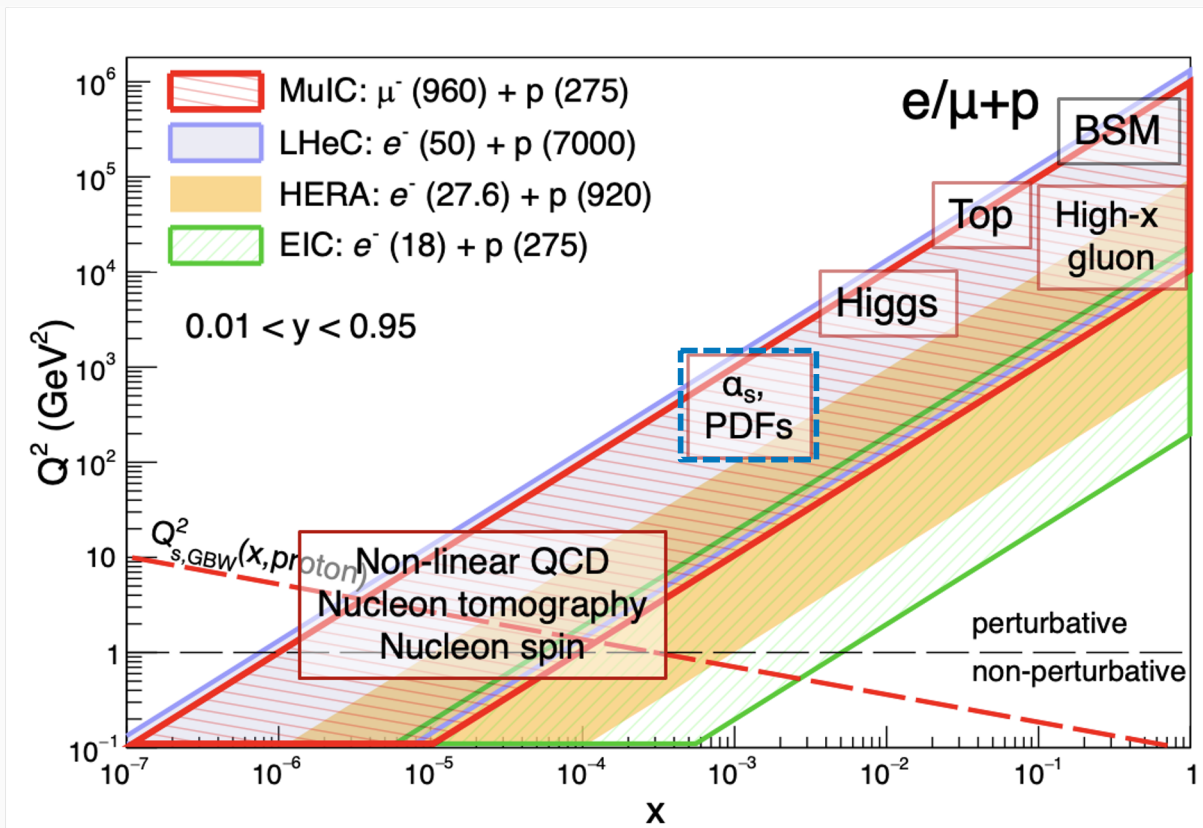
[1] LHeC: [arXiv:2007.14491](https://arxiv.org/abs/2007.14491)

[2] GBW model: [Phys. Rev. D 59, 014017 \(1998\)](https://arxiv.org/abs/hep-ph/9801140)

MuIC: $\mu(960)+p(275)$, $y_{cm} = -0.63$ vs. LHeC: $e(50)+p(7000)$, $y_{cm} = 2.47$

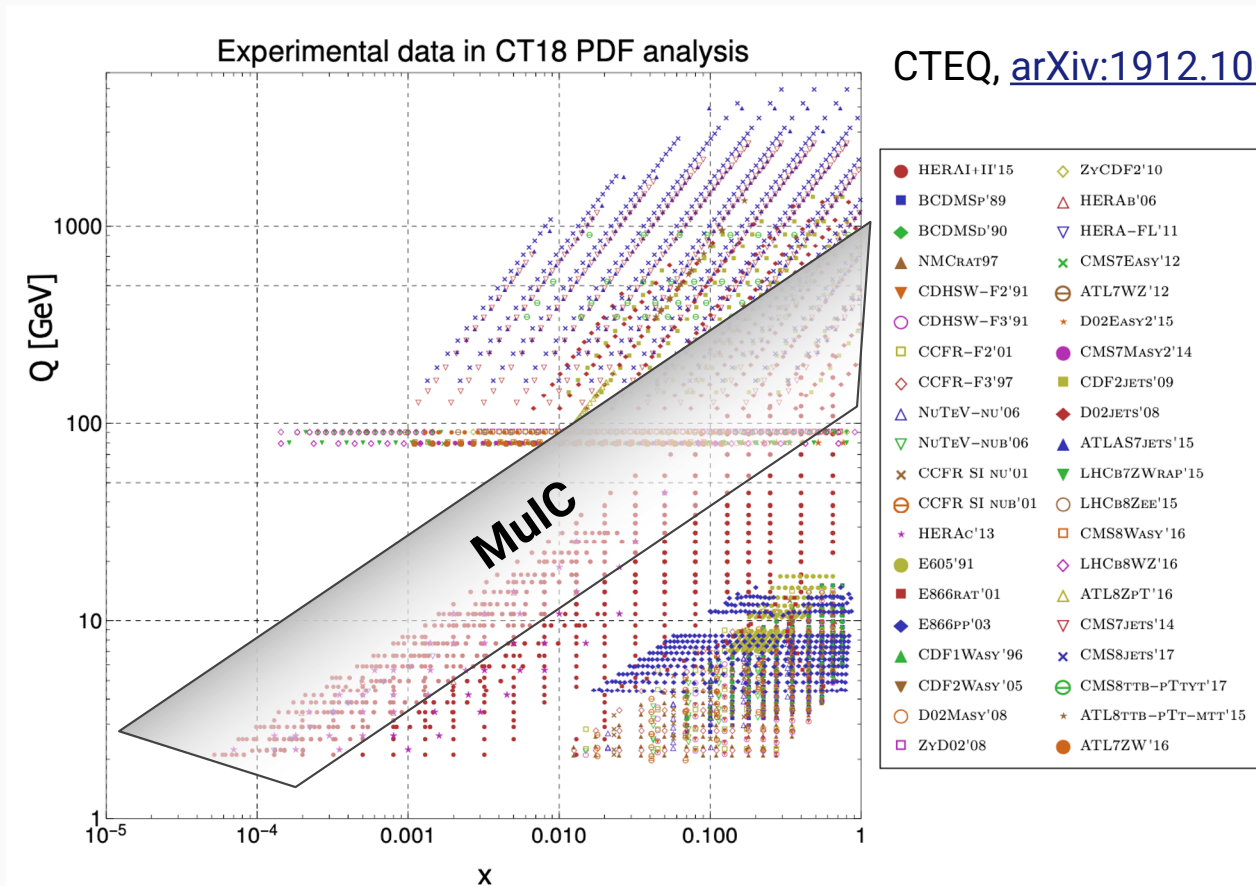
Similar \sqrt{s} but very different final-state kinematics

Science potential at the MuIC



Rich physics in NP and HEP!

Science potential at the MuIC: PDF Measurements

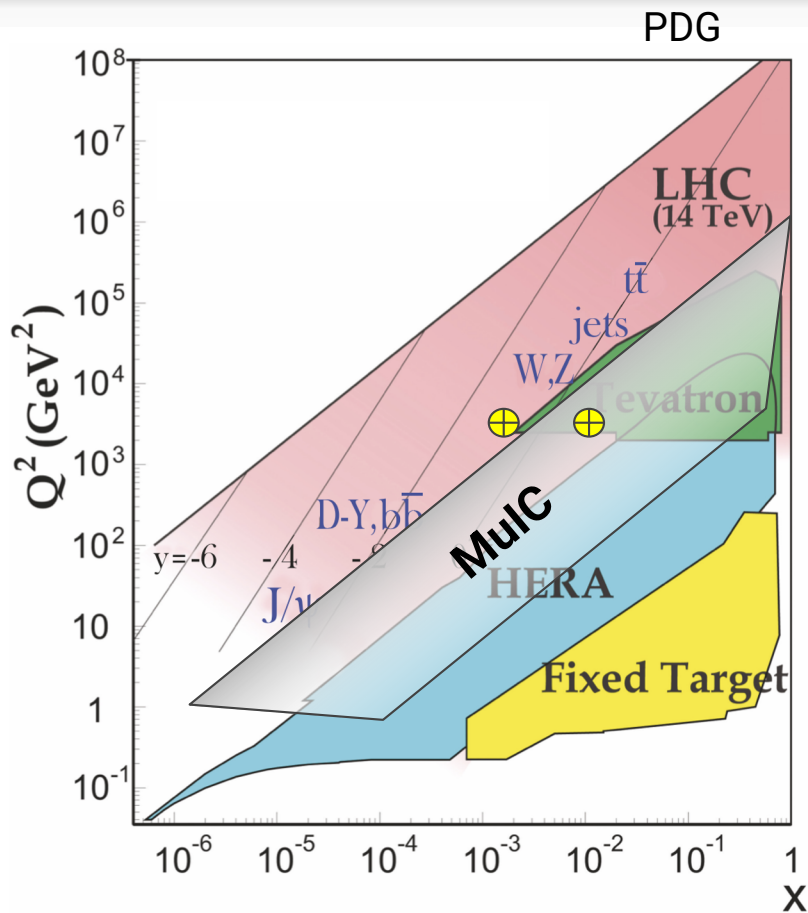


← Data used for global CTEQ fits

The MuIC would definitely probe new territory

With polarization can explore spin-dependent structure functions as well

PDF Measurement is Complementary to Hadron Colliders



LHC data can be used to extract parton densities from Drell-Yan, W, jet, and top production measurements, but:

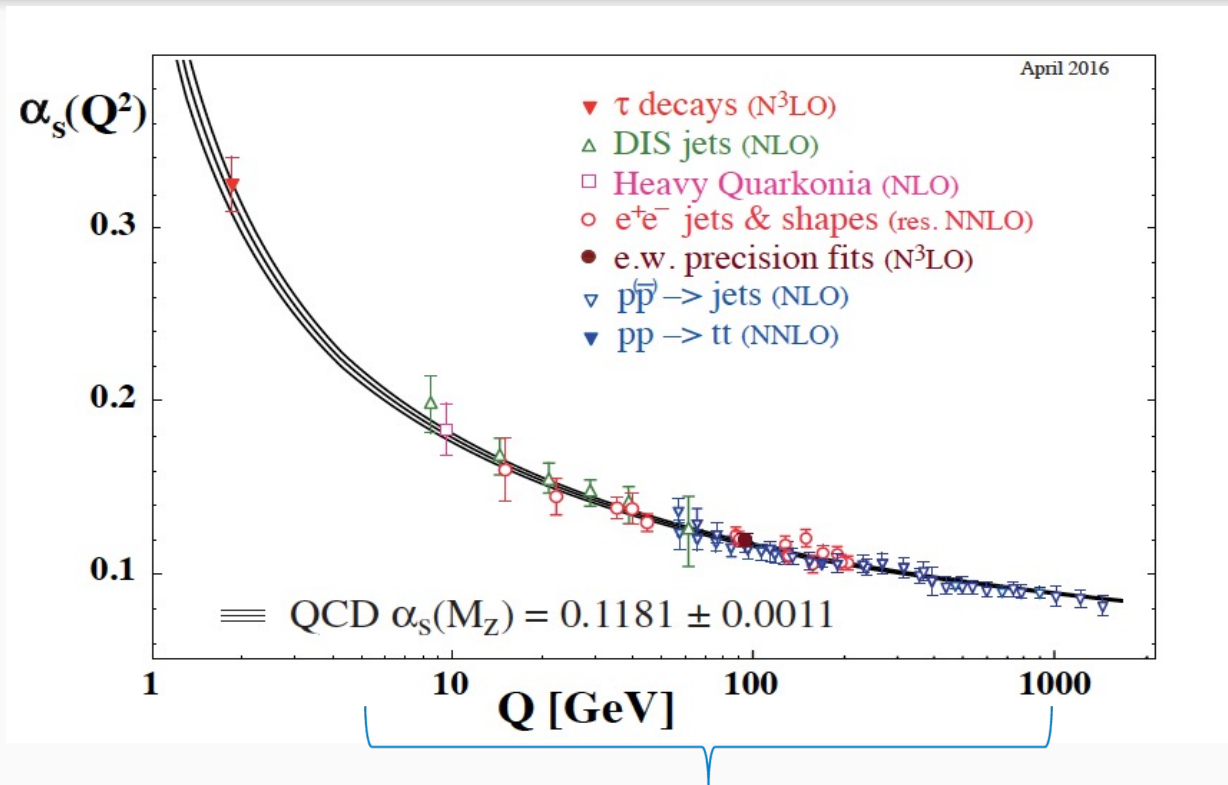
- It's a bit circular when also trying to measure those cross sections...
- Convolved with QCD effects and quark flavor

DIS measurements can more cleanly decouple quark flavor and QCD effects

The MuIC also can directly probe parton densities at the scale for Higgs production at the (HL)LHC, and for a future 100 TeV FCChh should one be built

- Less reliant on fit extrapolation → smaller uncertainties on cross sections ($< \sim 1\%$)
- Useful (and necessary?) input for an FCChh program
 - As HERA was for the LHC

QCD and the Running of α_s

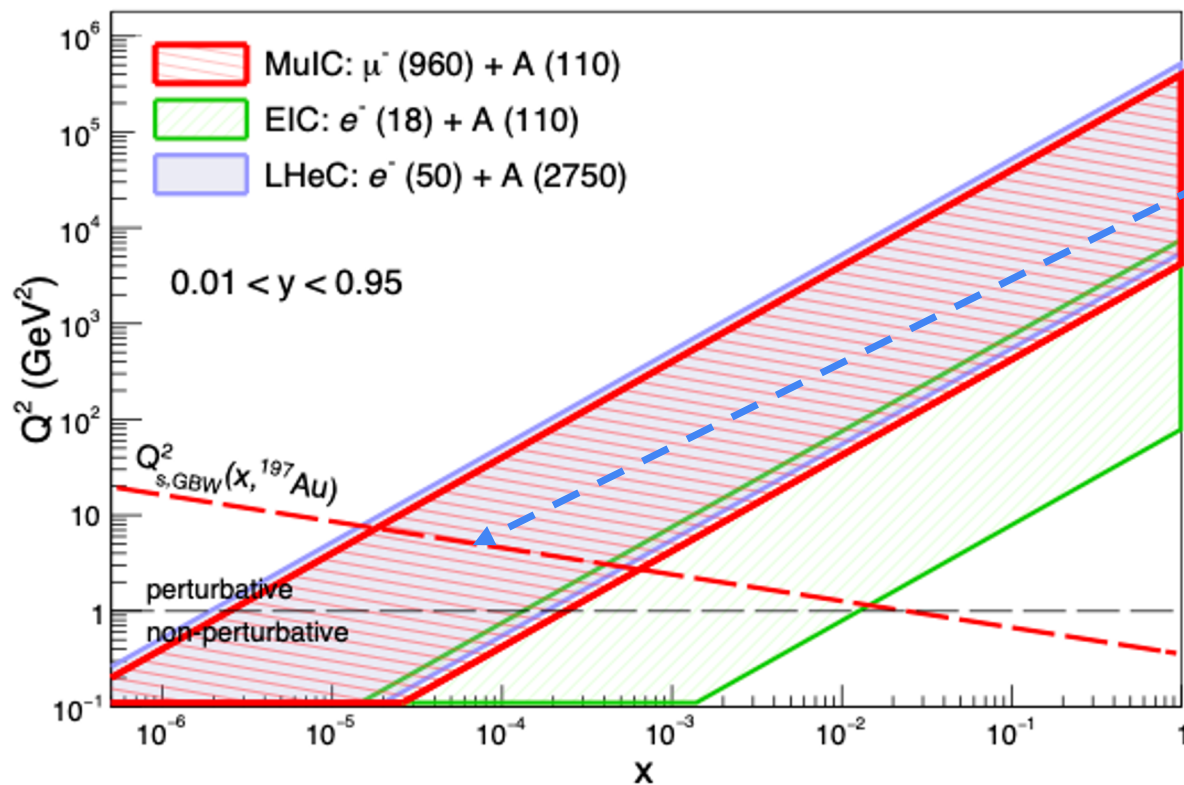


- Measurements can span an even broader range to measure $\alpha_s(Q^2)$ in a **single experiment**
 - Both from QCD evolution fits to structure function data, and from DIS multijet rate measurements
 - Removes some inter-experiment systematics

Q²-x Reach Comparison: e(μ)-A Scattering



Can explore well the predicted saturation regime [1] in ions



Saturation scale:

$$Q_s^2(A) = A^{1/3} Q_s^2(p)$$

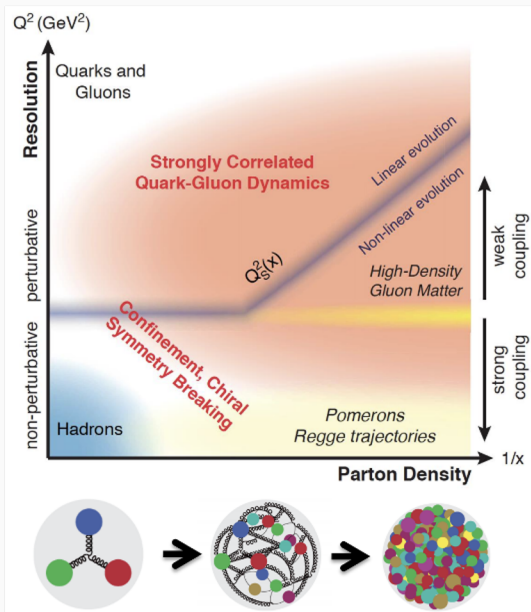
Also the MuIC can scan a wide range of ion species

[1] GBW model: [Phys. Rev. D 59, 014017 \(1998\)](#)

Nuclear Physics at the MuIC

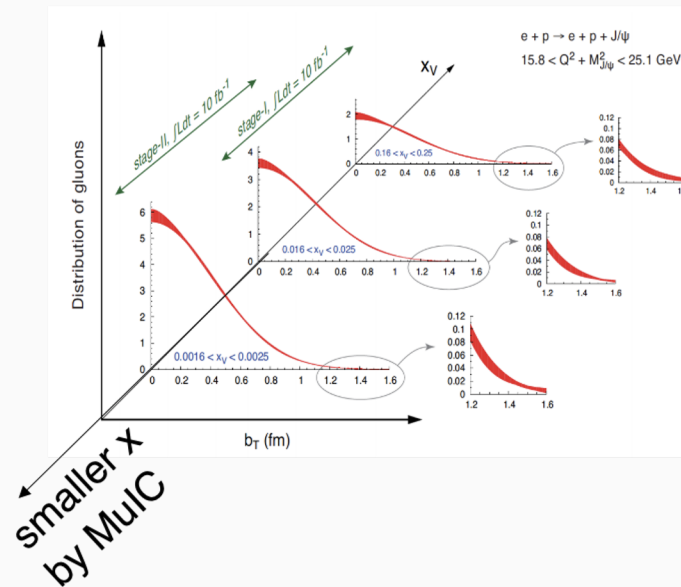


Gluon saturation



What's the property of high-density gluon matter

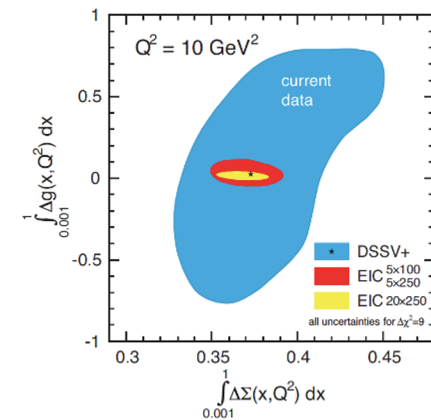
3D Nucleon structure



Nucleon spin puzzle

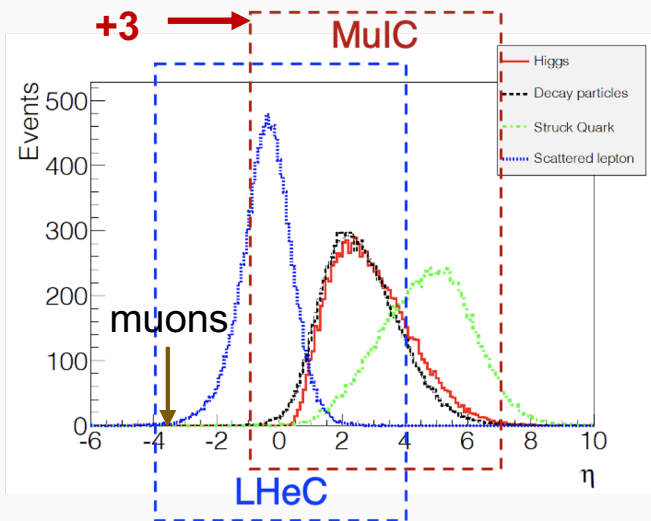
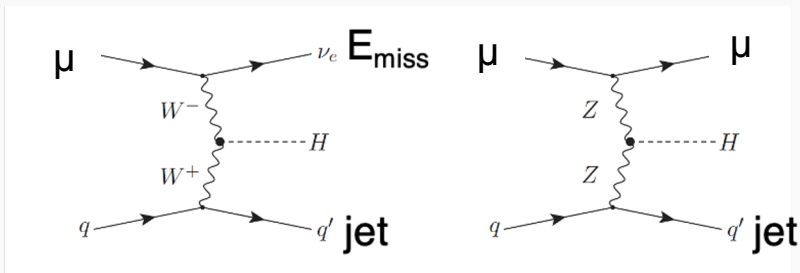
“Helicity sum rule”

$$\frac{1}{2} \hbar = \underbrace{\frac{1}{2} \Delta \Sigma}_{\text{quark contribution}} + \underbrace{\Delta G}_{\text{gluon contribution}} + \underbrace{\sum_q L_q^z + L_g^z}_{\text{orbital angular momentum}}$$



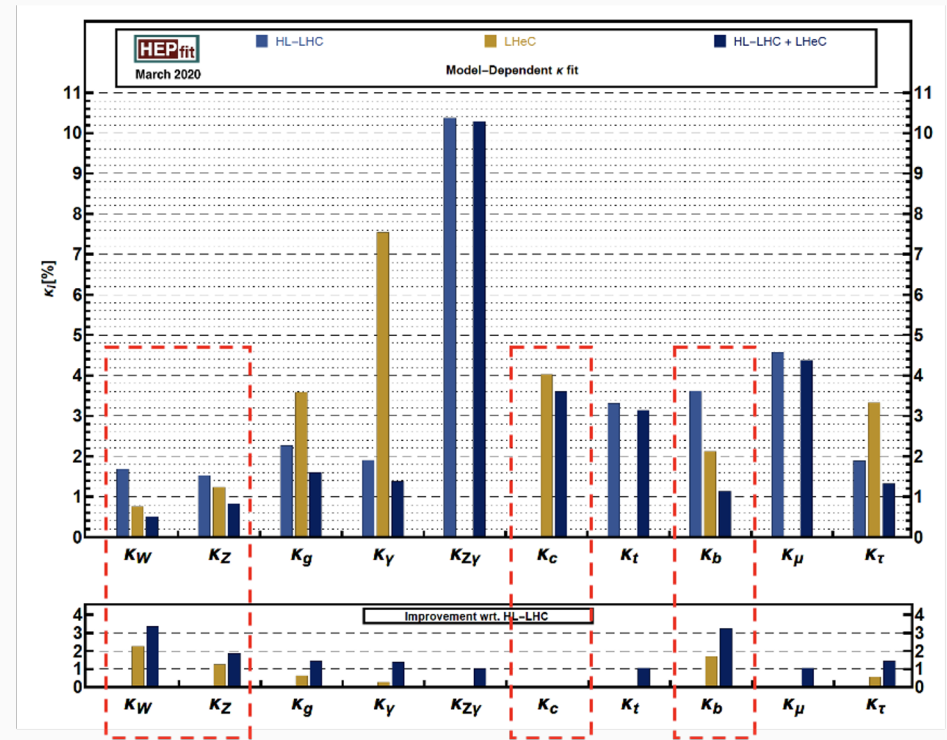
MuIC to reach $x \sim 10^{-5}$

Higgs at the MuIC



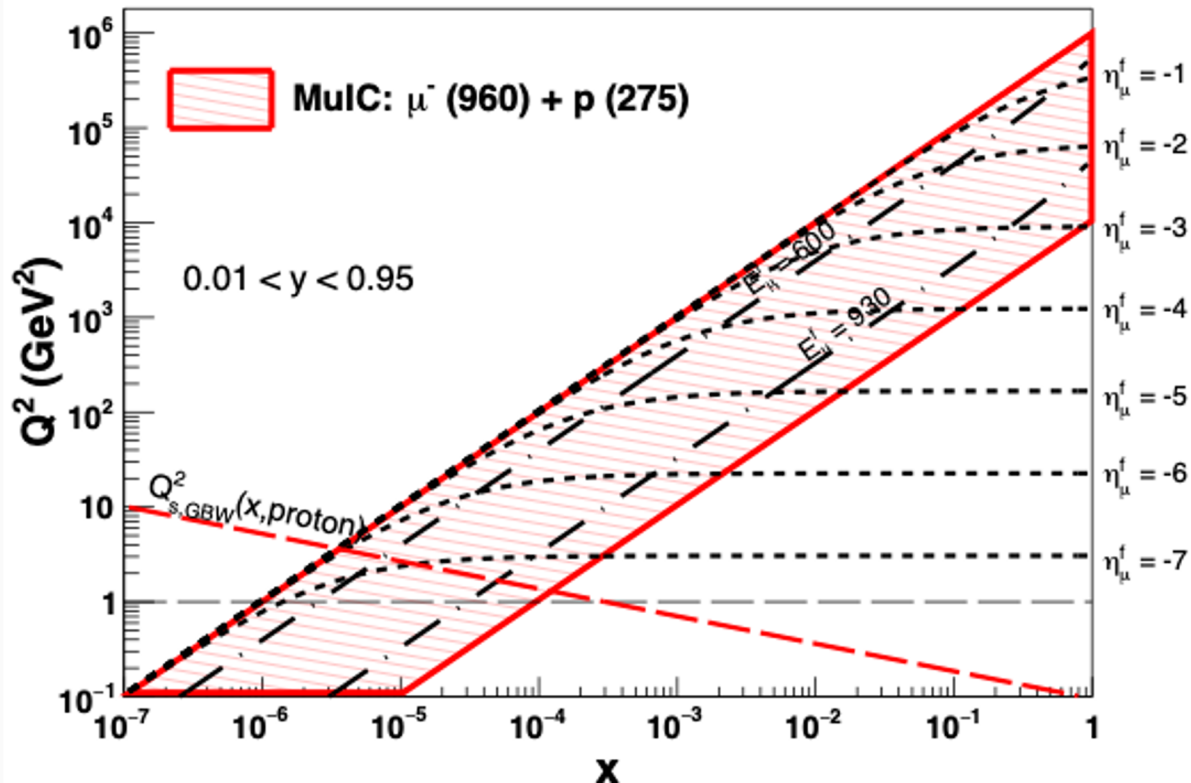
At MuIC, kinematics for Higgs are more central, but scattered muon is very forward.

Uncertainties of Higgs couplings



LHeC outperforms HL-LHC with $L_{\text{int}} = 1/\text{ab}$ in $\kappa_W, \kappa_Z, \kappa_b, \kappa_c$ Second generation!

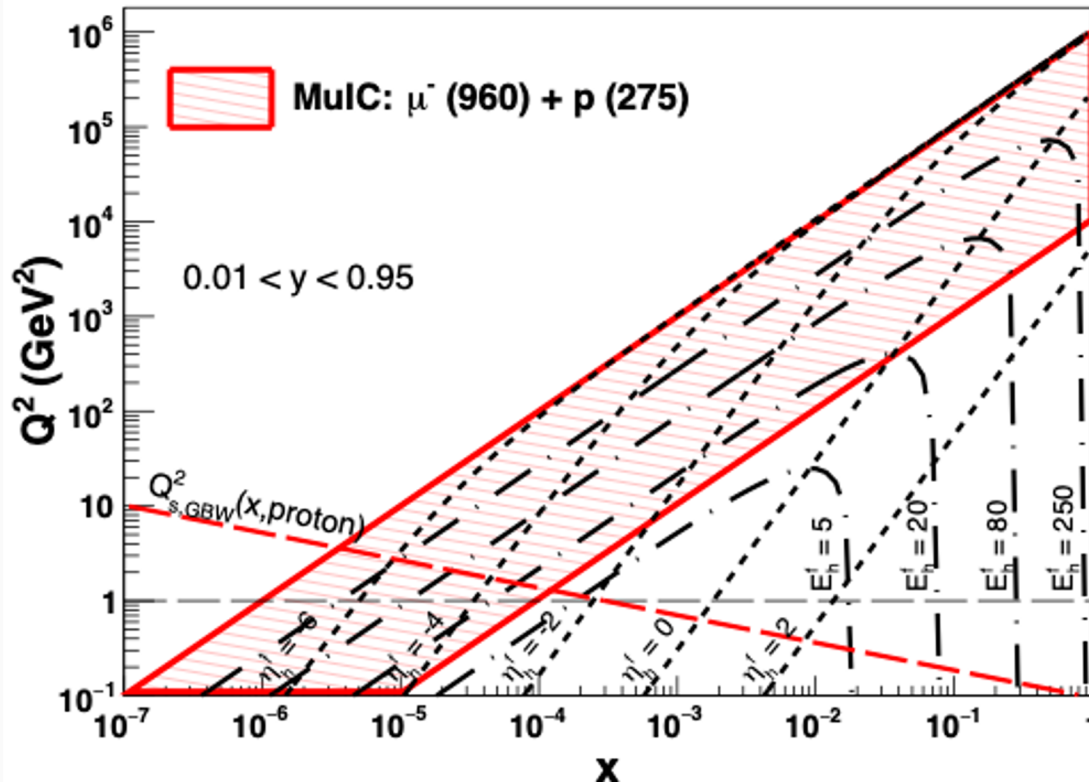
Scattered Lepton Kinematics - MuIC



- Scattered muon momentum essentially defines y (decreases with y increasing)
 - Typically > 500 GeV
- Scattering angle is in very backward (lepton) direction
 - $-7 < \eta < -5$ at low Q^2

Distinct experimental challenges in tagging very forward muons to address. (but hundreds of GeV muons will penetrate through anything, i.e. shielding)

Scattered Hadron Kinematics - MuIC



- Scattered energy of hadron system essentially defines y (increases with y)
 - Typically 20 – 500 GeV
 - LHeC: < 50 GeV
- Scattering angle is in backward (lepton) direction, less so than muon except at low x
 - Jet kinematics more central ($-4 < \eta < 2$)

Detector requirements and design

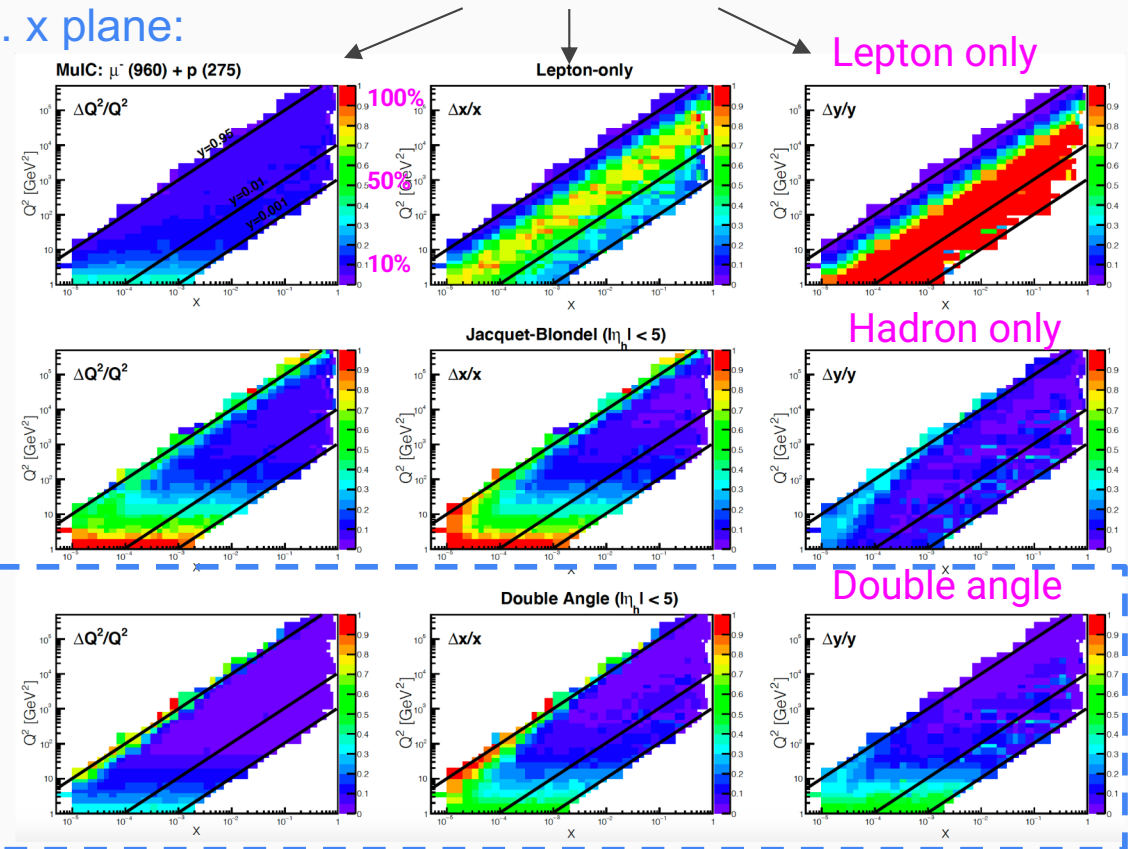


Resolutions of reconstructed Q^2 , x and y with 3 methods

Q^2 vs. x plane:

Simple assumptions of detector resolutions to smear particles from PYTHIA 8

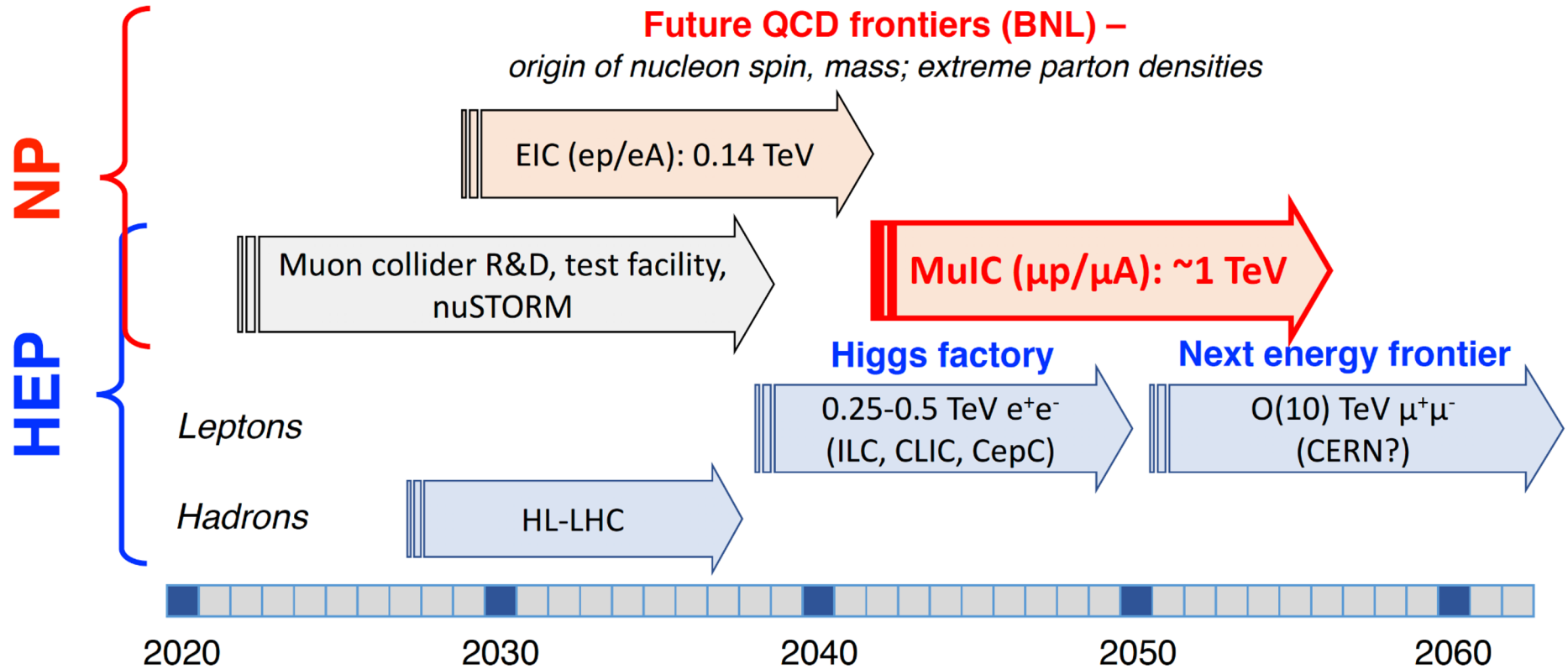
Particle	Detector	Resolution	
		$\frac{\sigma(p)}{p}$ or $\frac{\sigma(E)}{E}$	$\sigma(\eta, \varphi)$
(Forward) Muons	e.g., MPGD	$0.01\% p \oplus 1\%$	0.2×10^{-3}
Charged particles ($\pi^\pm, K^\pm, p/\bar{p}, e^\pm$)	Tracker + PID	$0.1\% p \oplus 1\%$	$\left(\frac{2}{p} \oplus 0.2\right) \times 10^{-3}$
Photons	EM Calorimeter	$\frac{10\%}{\sqrt{E}} \oplus 2\%$	$\frac{0.087}{\sqrt{12}}$
Neutral hadrons (n, K_L^0)	Hadronic Calorimeter	$\frac{50\%}{\sqrt{E}} \oplus 10\%$	$\frac{0.087}{\sqrt{12}}$



- Muons: 10% at 1 TeV, $\eta > -7$
- Hadrons: $|\eta| < 5$

Acosta, Li Future work: detailed simulations to fully demonstrate the experimental feasibility

Path forward (in our view)

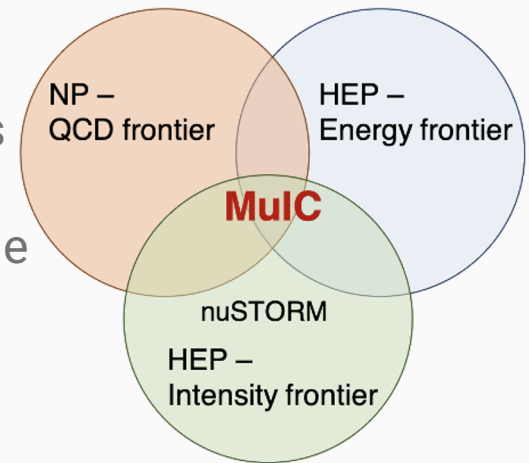


A possible roadmap to future muon colliders in NP and HEP

Summary of Key Merits of MuIC Concept



- Compelling science case with synergies across NP and HEP energy and intensity (e.g, [nuSTORM](#)) frontiers
 - Nucleon structure, QCD, EWK, Higgs, BSM?
- Serves as a demonstrator or staging option to establish the muon collider technology toward the ultimate $O(10+)$ TeV $\mu^+\mu^-$ (CERN?)
 - And if instead there will be an FCC-hh, perhaps the only chance for relevant PDF measurements in advance of that program
- Affordable as an “upgrade” to the EIC by re-using the existing facility, infrastructure, accelerator expertise.
- A unique muon collider sited in the US with a clear design goal by joint efforts of the HEP and NP communities, and even attracting worldwide interests
 - [More realistic than a completely new facility in the US?](#)



Next steps



- Propose MuIC at BNL as one of future muon collider options in US to the Snowmass2021 planning exercise, and also propose the idea to the NP community in the upcoming long-range planning process in 2022
- With the MuIC concept, bolster the case to establish a dedicated R&D program on muon collider technology in US, involving HEP and NP in collaboration with the International Muon Collider Collaboration
- Engage BNL to consider MuIC as a future option of the lab, to start conceiving a possible design and potentially establish test facilities.
 - **Discuss with accelerator design experts on feasibility of muon acceleration at BNL facility**
- **Engage broader theoretical and experimental communities to explore the physics potential and to address detector design requirements/challenges (workshops, collaborations, and working groups)**